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Odd and Even Numbered Ferric Wheels

Daniel J. Cutler, Angelos B. Canaj, Mukesh K. Singh, Gary S. Nichol, David Gracia, Hiroyuki Nojiri,* Marco Evangelisti,* Jürgen Schnack,* and Euan K. Brechin*

The structurally related odd and even numbered wheels $[Fe^{III}_{11}Zn^{II}_{4}(tea)_{10}(teaH)_{1}(OMe)Cl_{8}]$ (1) and $[Fe^{III}_{12}Zn^{II}_{4}(tea)_{12}Cl_{8}]$ (2) can be synthesized under ambient conditions by reacting Fe^{III} and Zn^{II} salts with triethanolamine (teaH₃), the change in nuclearity being dictated by the solvents employed. An antiferromagnetic exchange between nearest neighbors, J = -10.0 cm⁻¹ for 1 and J = -12.0 cm⁻¹ for 2, leads to a frustrated S = 1/2 ground state in the former and an S = 0 ground state in the latter.

1. Introduction

Understanding the magnetic properties of antiferromagnetic (AF) transition metal wheels,^[1] whose behavior depends on both size (length) and topology is key to future application in, for example, quantum information processing^[2] and the study of exotic frustration effects.^[3] Even-numbered homometallic, homovalent AF wheels, which are commonplace and exist in a breadth of nuclearities,^[4] are characterized by a diamagnetic spin ground state. Studies of these species have revealed interesting quantum phenomena, including coherent tunneling of the Néel vector,^[5] spin-multiplet mixing effects,^[6] magnetic level repulsions, and symmetry-related anomalies.^[7] There are fewer

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examples of antiferromagnetic homometallic, heterovalent species, but here the different valences (spins) on neighboring ions can be exploited to stabilize unusual spin ground states. An example is the $[Mn^{III}_{6}Mn^{II}_{6}]$ (6 x *s* = 2, 6 x *s* = 5/2) wheel built with *N*-methyldiethanolamine which has an *S* = 7 ground state.^[8]

Odd-numbered AF wheels present the chance to examine spin frustration effects, perhaps more commonly associated with spin glasses and solid-state materials

conforming to the kagome and pyrochlore structures.^[9] Frustration – here understood as competing interactions – in molecular species^[3] can lead to enhanced ground-state degeneracy, low-lying singlet states, noncollinear ground states, unusual magnetization plateaus and jumps, and attractive magnetocaloric properties.^[10] Odd-numbered wheels with N > 3 (where N = number of metal ions), however, remain remarkably rare. A search of the Cambridge Structural Database reveals these are limited to $[Cu_{5}^{II}]_{,}^{(11]}$ [V^{IV}₇],^[12] [Ti^{IV}₉] and [Ti₈M^{III}],^[13] [Cr^{III}₈M^{III}]^[14] and [Cr^{III}₉].^[15] Herein, we report the synthesis and characterization of the first odd-numbered Fe^{III} wheel, [Fe^{III}₁₁Zn^{II}₄(tea)₁₀(teaH)₁(OMe)Cl₈] (1), and its related evenmembered analog, [Fe^{III}₁₂Zn^{II}₄(tea)₁₂Cl₈] (2), where H₃tea is triethanolamine.

2. Results and Discussion

Reaction of FeCl₃ and Zn(ClO₄)₂·6H₂O with H₃tea in a basic MeOH/MeCN solution (see the SI for full experimental details) leads to the formation of 1 after 3 days (Figure 1). 1 crystallizes in the monoclinic space group $P2_1/n$ (Table S1, Figure S1), with the asymmetric unit comprising the whole cluster. The [Fe^{III}11] metallic skeleton is somewhat S-shaped rather than planar (Figure S2, Tables S2-S4, Supporting Information), with all neighboring Fe ions bridged by two O-atoms from two tea ligands, [Fe-(μ -O_{tea})₂-Fe]. The only exception to this is between Fe6-Fe7 where one of the triethanolamine arms is protonated/nonbonded and replaced in the bridging unit by the sole μ -OMe ligand (Fe6-O19-Fe7) in the cluster, [Fe-(μ -O_{tea})(μ -OMe)-Fe]. This moiety is therefore responsible for the asymmetry of the wheel, with the magnetic core of the molecule being $[Fe_{11}(\mu - O_{tea})_{21}(\mu - OMe)_1]$. The triethanolamine ligands are of three types (Figure S3, Supporting Information). Seven are μ_4 -bridging ([Fe₃Zn]) with two O-atoms bridging two Fe ions, and one O-atom bridging between Fe–Zn. Three are μ_3 -bridging ([Fe₃]) with two O-atoms bridging two Fe ions, and one O-atom being terminally bonded. The remaining ligand is μ_3 -bridging ([Fe₂Zn]) with one O-atom bridging two Fe ions, one bridging



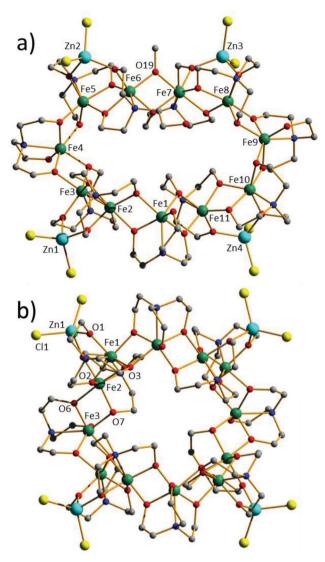


Figure 1. Molecular structures of complexes a) 1 and b) 2. Color code: Fe = green, Zn = pale blue, O = red, N = dark blue, C = grey, Cl = yellow. H atoms omitted.

between Fe and Zn, and the third being nonbonded. The Fe-O-Fe angles fall within the range $\approx 101.6-107.7^{\circ}$. The Fe ions are all six-coordinate and in distorted octahedral geometries, while the Zn ions are four-coordinate and tetrahedral – the remaining two coordination sites on each Zn ion being occupied by Cl ions.

The nonbonded HO-arm of the Htea ligand is oriented towards and above the cavity of the wheel and is H-bonded to an H₂O molecule of crystallization (O(H)···O, ≈ 2.74 Å) which also has a close contact to a µ-bridging O-atom from a tea ligand on the inner rim of the wheel (O(H)···O, ≈ 3.04 Å). The monodentate O(tea) arms are also H-bonded to H₂O molecules of crystallization (O(H)···O, ≈ 2.83 Å). The latter form a near linear chain of five H₂O molecules which also H-bond to the terminal Cl atoms (O(H)···Cl, ≈ 3.4 Å). The Cl atoms in turn are also H-bonded to CH₂(tea) moieties on neighboring clusters (Cl···(H)C, ≈ 3.4 Å) and the latter to other CH₂(tea) moieties (C(H)···(H)C, ≈ 3.5 Å). www.advancedscience.com

The result is a rather complicated network of H-bonded clusters in the extended structure (Figure S4, Supporting Information).

Repetition of the synthetic procedure that produces 1, but in DMF/MeCN affords 2 after 4 days (Figure 1). 2 crystallizes in the tetragonal space group $I4_1/a$ (see the SI for full details; Table S1, Figure S5, Supporting Information). Compound 2 is to some extent a symmetric analog of 1, with the twelve tea ligands now of just two types: one μ_3 -bridging ligand ([Fe₃]) followed by two μ_4 bridging ligands ([Fe₃Zn]) as the wheel is circumnavigated. The result is that the metallic skeleton becomes bowl- or U-shaped rather than S-shaped, with the magnetic core of the molecule being $[Fe_{12}(\mu-O_{tea})_{22}]$ (Figure S6, Tables S5–S6, Supporting Information). In the extended structure of 2 wheels pack in a headto-tail fashion along the *c*-axis of the cell with a square of H₂O molecules (O…O, \approx 2.86 Å) sitting between the wheels mediating H-bonding interactions to the O-arms of the tea ligands (O···O, \approx 2.63 Å). The result is the formation of tubular arrays of wheels down the *c*-axis. In the *ab* plane closest intermolecular interactions are mediated between the Cl atoms and tea ligands (C(H)…Cl, \approx 3.6 Å) resulting in a regular square grid of wheels. Overall, this leads to the aesthetically pleasing packing structure shown in Figure S7, Supporting Information.

The direct current (dc) molar magnetic susceptibilities, χ , of polycrystalline samples of 1–2 were measured in an applied magnetic field, *B*, of 0.1 T, over the 2–300 K temperature, *T*, range. Magnetization (*M*) data was measured in the 2–10 K and 0.5-9.0 T, temperature and field ranges, respectively. The results are plotted in **Figure 2** (and Figure S8, Supporting Information) in the form of the χT product versus *T* and *M* versus *B* (insets of Figure 2). The susceptibility data for 1 and 2 are similar, showing relatively strong AF exchange interactions between nearest neighbors with χT decreasing rapidly with decreasing temperature and reaching values of 0.40 and 0.05 cm³ K mol⁻¹ at *T* = 2.0 K for 1 and 2, respectively.

The variable-temperature-variable-field magnetization data differ significantly between the two compounds. For 1 at T = 2 K, M rises rapidly with increasing field, before saturating at a value of $M = 1.1 \mu_{\rm B}$. At higher temperatures, M rises in a more linear fashion with increasing B. At T = 2-3 K the magnetization data for 2 remains close to zero, before increasing more rapidly for fields above ≈ 4 T. The maximum value at T = 2 K and B = 9.0 T is just 0.88 $\mu_{\rm B}$. With increasing temperature (4-10 K) M increases in a more linear fashion with increasing field.

The magnetic susceptibility data can be accurately simulated using an isotropic spin-Hamiltonian $\hat{H} = -2 \sum_{i} J_{j} \hat{\vec{s}}_{i} \cdot \hat{\vec{s}}_{j+1}$ with

a coupling scheme that assumes (as a reasonable simplification) just one independent exchange interaction between nearest neighbors, $J = -10.0 \text{ cm}^{-1}$ for 1 and $J = -12.0 \text{ cm}^{-1}$ for 2, with g = 2.0 in both cases (Figure 2, red lines). The susceptibility data is also approximated well with the DFT calculated *J* values (see below), though the magnetization data is not (Figure S8, Supporting Information, blue lines). DFT suggests that *J* values vary in some range for nearest neighbor exchange interactions. Likely this leads to an incorrect approximation of ground and low-lying excited states. The ground state for 1 is an $S = \frac{1}{2}$ state, [10b] and for 2 is S = 0 as can be clearly seen in **Figure 3**. All calculations have been performed by means of the finite-temperature Lanczos method. [16] www.advancedsciencenews.com

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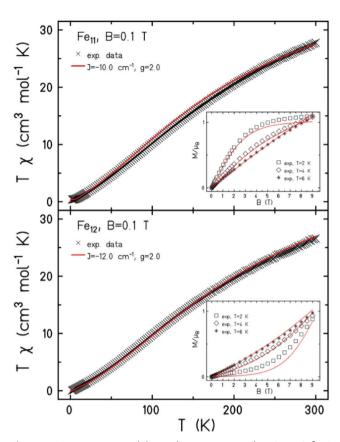


Figure 2. Magnetic susceptibility and magnetization data (insets) for **1** (top) and **2** (bottom). The solid red lines are simulations of the experimental data with $J = -10.0 \text{ cm}^{-1}$ and $J = -12.0 \text{ cm}^{-1}$, respectively, with g = 2.0. See the main text for details and Figure S8, Supporting Information, for larger versions of the insets.

The relatively large magnitude of *J* results in sizeable level spacings between the lowest Zeeman levels (Figure 3), with the sequence of levels being as expected for odd and even spin rings.^[10b,17,18] The large gap size explains the (very) small magnetization values, even in fields of up to 9 T.

At fields of up to 32.5 T at T = 0.4 K the magnetization data for 1 and 2 reveal a series of step-like level crossings (solid and dashed black lines in Figure 4, Figure S8, Supporting Information). For 2 these are relatively well resolved for $B \approx 7.5$ T (S = $0\rightarrow 1$), 17.5 T ($S = 1\rightarrow 2$), and 27.5 T ($S = 2\rightarrow 3$). For 1 there appear to be two broader, less well-resolved steps centered around $B \approx$ 18 T ($S = 3/2 \rightarrow 5/2$) and 23 T ($S = 5/2 \rightarrow 7/2$), the $S = 1/2 \rightarrow 3/2$ step being smeared out. The remarkable difference between the two sets of data reflects the high and low symmetry of molecules with even and odd numbered metal ions, respectively. Specifically, for an odd-numbered ring with lower symmetry, the local anisotropy (single ion and exchange anisotropy) is not canceled out, inducing mixing between energy levels and the broadening of magnetization steps. The steps are remarkably well simulated using the same model employed to fit the low-field susceptibility and magnetization data, particularly for 2, albeit slightly shifted in *M* and *B*. We attribute the small differences to a) the simplicity of the (one-J) model, b) possible anisotropic contributions to the Hamiltonian relevant at very low temperatures, c) the fact that the

high-field measurement uses a pulsed field and thus may show dynamic effects such as slow equilibration and discontinuities.

This same model explains the differences observed in the heat capacity (*C*) of the two compounds (**Figure 5**). For **1** the main feature of the zero-applied-field *C* is a broad Schottky anomaly centered at \approx 8 K, while **2** has a more prominent Schottky anomaly at \approx 3.5 K. Both features are quantitatively accounted for by the large energy gap existing between the two lowest multiplets for each respective compound (Figure 3).

To further support the relative sign and magnitude of the coupling constants above, and given that the single *J* model serves as a general/qualitative model to understand the gross features, we have performed DFT calculations (see the SI for computational details) on model complexes derived from 1 and 2 (Figures S9 and 10, Tables S7–S8, Supporting Information). All computed exchange interactions are antiferromagnetic in nature. For 1 the eleven independent coupling constants fall in the range $-3.5 < J < -12.8 \text{ cm}^{-1}$ (Figure S11, Supporting Information). For 2 the three independent coupling constants fall in the range $-7.1 < J < -12.7 \text{ cm}^{-1}$ (Figure S12). The narrower range of *J* values for 2 is consistent with the structural similarity of nearest neighbor bridging.^[19] DFT computed spin densities suggest a strong spin-delocalization mechanism for the magnetic exchange interaction in both cases, with the spin on Fe^{III} centers ranging between

40 E-E₀ (cm⁻¹) 30 20 10 0 40 Fe₁₂ E-E₀ (cm⁻¹) 30 20 10 0 2 0 1 3 4 5 6 7 8 9 B (T)

Figure 3. Low-lying Zeeman energy diagram. For 1 (top) $M = \pm 1/2$ black lines, $M = \pm 3/2$ red lines, and $M = \pm 5/2$ blue lines. For 2 (bottom) M = 0 black lines, $M = \pm 1$ red lines, and $M = \pm 2$ blue lines. For 1 the levels are degenerate; the degeneracy – typically 2 – is given in Refs. [10b,16].

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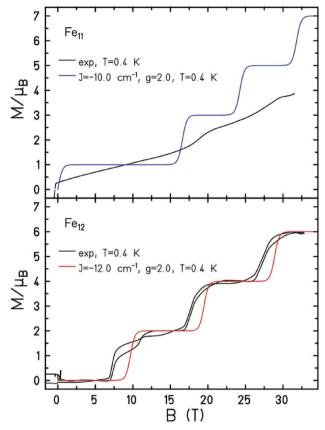


Figure 4. High-field magnetization data (solid black lines for B > 0 and B < 0 T) were collected for 1 (top) and 2 (bottom) in fields up to 32.5 T. The solid blue and red lines are simulations of the experimental data with $J = -10 \text{ cm}^{-1}$ (1), -12.0 cm^{-1} (2) at T = 0.4 K.

4.128 and 4.187 for **1** (Figure S13, Supporting Information) and 4.014–4.165 for **2** (Figure S14, Supporting Information). Both the experimentally and computationally derived *J* values agree with previous magneto-structural correlations developed for O-bridged Fe^{III} complexes in which the magnitude of *J* is dictated by the Fe—O–Fe angle and Fe–O distance.^[19]

3. Conclusion

In summary, we have synthesized and characterized two structurally related wheels of Fe^{III}, specifically the odd numbered [Fe₁₁] and the even numbered [Fe₁₂]. The former is the first example of an odd numbered Fe wheel. Synthetically, the formation of one over the other can be controlled via the choice of solvent, a mixture of MeCN and MeOH for the former, and a mixture of MeCN and DMF for the latter. The asymmetry in 1 originates from the presence of a protonated/nonbonded arm in one triethanolamine ligand which is replaced in the bridging unit by methoxide anion. Magnetic susceptibility, magnetization, and heat capacity measurements reveal relatively strong antiferromagnetic exchange between nearest neighbors, J = -10.0 cm⁻¹ for 1 and J = -12.0cm⁻¹ for 2. This leads to a frustrated S = 1/2 ground state in the former and an S = 0 ground state in the latter, with the relatively large value of *J* resulting in sizeable level spacings between the

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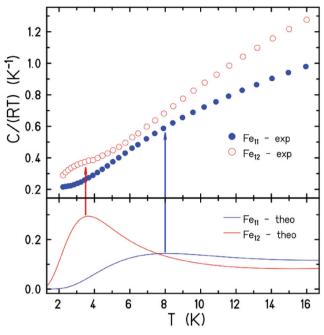


Figure 5. Experimental heat capacity data for 1 and 2 at zero-applied field (top), depicted as C/(RT), where *R* is the molar gas constant. The solid blue and red lines in the bottom panel are simulations with $J = -10 \text{ cm}^{-1}$ (1), -12.0 cm^{-1} (2). The arrows highlight the Schottky anomalies. The increase of the experimental data with temperature must be ascribed to the ordinary lattice contribution, which is not considered by the simulations.

lowest Zeeman levels. High-field magnetization data collected up to \approx 32.5 T reveals a series of step-like level crossings for both compounds.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Author Contributions

D.J.C. and A.B.C. contributed equally to this work. D.J.C. and A.B.C. performed the synthesis, collected and analyzed PXRD data, and collected the magnetometry data. G.S.N. collected and solved single crystal XRD data. M.K.S. carried out the theoretical analyses. D.J.C. and H.N. measured the high-field magnetization data. M.E. measured and analyzed the heat capacity data. J.S. fitted the magnetic data. E.K.B. conceived the idea. All authors contributed to writing and editing the manuscript. SCIENCE NEWS _____

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

 $\mathsf{Fe}^{\mathsf{III}},$ even numbered wheel, odd numbered wheel, magnetism, spin frustration

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