

1 Progressive pulse dynamics in a mode-locked 2 fiber laser

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11 **Abstract:** Triple different operation regimes like passive Q-switched (PQS), Q-switched
12 mode-locking (QSML) and continuous-wave mode-locking (CWML) are experimentally
13 observed as progressive pulse dynamics in a mode-locked fiber laser, which is constructed
14 with several-meters of cascaded small-core erbium/bismuth co-doped fiber (EBCF) to
15 engineer the cavity loss modulation. The pulse fission evolution from PQS to QSML to
16 CWML operation is flexibly achieved through pump power variation as the only control
17 parameter at fixed polarization orientation. Output characteristics in all triple operation
18 regimes are studied in detail and particularly the pulse transitional process between PQS and
19 QSML is reported experimentally for the first time, to the best of our knowledge. The laser
20 pulse formation criteria for different operation regimes are also theoretically analyzed. The
21 obtained results and analysis disclose the complete pulses evolution process from PQS to
22 QSML to CWML operation, which contribute to further understanding of the complex
23 nonlinear dynamics and laser pulse formation mechanism in a passively mode-locked fiber
24 laser.

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27 1. Introduction

28 Mode-locked fiber lasers have attracted much attention due to their high-power density,
29 ultrashort interaction time, and flexible pulse modulation, which are widely applied in micro-
30 processing [1], biomedical diagnosis [2], molecular spectroscopy [3], optical communication
31 [4], and data storage [5], etc. In fiber lasers, a saturable absorber (SA) is included in the
32 resonant cavity to establish mode-locking operation. Based on their material property, the
33 SAs can be categorized into either natural SA materials or effect of saturable absorption
34 created through nonlinear optical devices. For physical SAs, low-dimensional materials are
35 extensively utilized in mode-locked fiber lasers. However, the low-dimensional materials may
36 suffer irreversible damage cause of higher-power laser operation for prolonged time, resulting
37 in increased loss or even failure to achieve the mode-locking operation. Commonly used
38 optical devices to create saturable absorption effect are nonlinear optical loop mirror or
39 amplification loop mirror (NOLM/NALM) [6-8], nonlinear multimode interference (NMI)
40 [9,10], and nonlinear polarization rotation effect (NPR) [11-12]. In NOLM/NALM based
41 fiber lasers, the nonlinear phase shift difference is accumulated by the two optical signals
42 propagated in opposite directions [6]. Nevertheless, in these type of fiber lasers, the threshold
43 power level to self-start mode-locking operation is relatively high, and some additional
44 actions are to be followed to trigger the mode-locking operation. NMI mode-locking makes
45 use of the interference between various modes with different nonlinear phase shifts in a
46 multimode fiber [9]. In NMI based fiber lasers, modulation depth can be controlled by

47 changing the length of the multimode fiber, which is practically inconvenient. NPR mode-
48 locking is based on the variation of polarization state related to the intensity of the optical
49 signal in the cavity, and in which, saturable absorption is achieved by polarizers [12]. Due to
50 the intrinsic advantages of simple structure, high modulation depth, short response time, and
51 low component cost, NPR technique is widely investigated and applied in various fields.

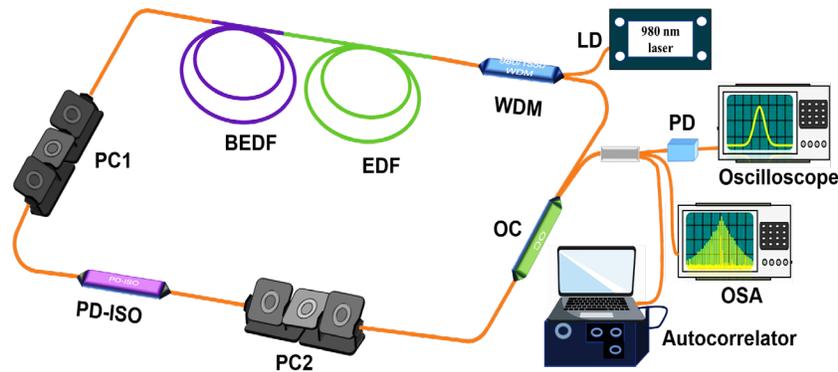
52 For fiber lasers can be divided into three different pulse operation regimes: passive Q-
53 switched (PQS), Q-switched mode-locking (QSML), and continuous-wave mode-locking
54 (CWML). PQS operation is an outcome of the cavity Q-factor modulation by reiteratively
55 emptying and replenishing the stored cavity energy, while CWML operation results from a
56 fixed phase relation between numerous oscillating longitudinal modes in the cavity. QSML is
57 a special type of operation in which the laser pulses consist of mode-locked pulses on and
58 above a Q-switched envelope. To date, the aforementioned PQS [13,14], QSML [15,16], and
59 CWML [7-12] operations are successfully demonstrated in mode-locked fiber lasers. As a
60 vigorous method to achieve Q-switched or mode-locked operation, various low-dimensional
61 SA materials are utilized as modulating devices to generate the laser pulses. Common
62 materials are graphene [17,18], semiconductor saturable absorption mirrors (SESAMs)
63 [19,20], carbon nanotubes (CNTs) [21,22], transition metal dichalcogenides (TMDs) [23,24],
64 topological insulators (TIs) [25], black phosphorus (BP) [26], Mxenes [27], Xenes [28],
65 phosphorene [29,30], ferromagnetic insulators (FIs) [31,32], silicene [33,34], and tellurene
66 [35]. Mid-Infrared PQS and mode-locked fiber lasers at 2-3 μm wavelength range were
67 demonstrated by incorporating CNT/SESAM/Selenide-nanoflowers SAs in the cavity [14,36,
68 37]. Also, Q-switched, mode-locked, or continuous-wave (CW) operation was experimentally
69 demonstrated in an Yb-doped double-clad NPR mode-locked fiber laser [38], but the output
70 results were not explicit, and the different operation regimes could not be flexibly switched
71 with a fixed polarization state. Multimode PQS and spatiotemporal mode-locked operation
72 were observed in a multimode fiber laser through specific spatial coupling and half-wave
73 plate (HWP) / quarter-wave plate (QWP) polarizers setup [39]. However, majority of the
74 research investigations focuses on the output pulse characteristics in various operating
75 regimes or synthesizing of new materials for SAs. Seldom research works are conducted in
76 mode-locked fiber lasers to investigate the feasibility for progressive pulse evolution
77 dynamics from PQS to QSML to CWML state, and thorough analysis of the related temporal
78 and spectral transition characteristics between different operation regimes.

79 In this paper, we propose a cascaded gain-fiber mode-locked laser, and experimentally
80 report the progressive evolution of laser pulses from PQS to QSML to CWML state that is
81 simply achieved through pump power variation as the only control parameter at fixed
82 polarization orientation. The temporal and spectral transition processes from PQS to QSML
83 to CWML operation are recorded and reconstructed, and the laser output properties are
84 analyzed in detail for all three operation regimes. The progressive pulse splitting process from
85 PQS to QSML operation is experimentally demonstrated for the first time, and the built-in
86 loss modulation resulting from the combined effects of the cascaded small-core
87 erbium/bismuth co-doped fiber (EBCF) and the polarization controllers in the cavity is
88 studied. Experimental results and analyses reported in this work can contribute to further
89 comprehending the nonlinear dynamics of passively mode-locked fiber laser.

90 2. Experimental setup

91 To study the output performance of pulse laser at various operation regimes, a ring mode-
92 locked fiber laser is constructed as shown in Fig. 1. A 980 nm laser diode (LD) with a
93 maximum pump power of 600 mW is launched into the fiber cavity through a 980/1550 nm
94 wavelength-division-multiplexer (WDM). A 2 m long erbium-doped fiber (EDF) and an 8 m
95 long bismuth-EDF (BEDF) with a core diameter of 4 μm are cascaded as gain media. A
96 polarization-dependent isolator (PD-ISO) is placed between the two polarization controllers
97 (PCs) to ensure unidirectional operation and serves as a polarizer in the laser cavity. PC1 and

98 PC2 are used to control the polarization state of the light signal in the cavity, that acts as a SA
 99 effect creating device together with the PD-ISO to achieve the mode-locking operation. When
 100 the light signal propagates in the cavity, both the orthogonal polarization components will
 101 accumulate the nonlinear phase shift that are dependent on the light intensity due to the
 102 nonlinear Kerr effect. Adjusting the polarization devices gets the head and tail ends of the
 103 pulse with lower intensity attenuated to temporally narrow down the pulse width. This
 104 narrowing of the pulse continues until gain-loss balance is established, and thus the mode-
 105 locked pulses are produced in the cavity. The total length of the cavity is about 14.1 m, which
 106 is consists of 10 m long gain fiber (EDF and BEDF) and about 4.1 m long standard single-
 107 mode fiber (SMF). Due to core diameter mismatch between BEDF and SMF, fused biconical
 108 taper technique was adopted to minimize the splicing loss, and the coupling efficiency was
 109 about 84.23%. Laser pulse-train is extracted from the cavity through a fiber output coupler
 110 (OC) with 10% ratio. The temporal pulse sequence and output spectrum are measured using a
 111 real-time scanning oscilloscope (MSO64, Tektronix) and a spectrum analyzer (AQ6370D)
 112 with a resolution of 0.02 nm, respectively. A radio frequency (RF) signal analyzer (FSV-40)
 113 with a bandwidth of 10 Hz-40 GHz is used to monitor the repetition rate of the laser output.
 114 The autocorrelation trace of the mode-locked pulse is analyzed by a an autocorrelator, and the
 115 average output power is measured by a power meter (S470C, Thorlabs) with a wavelength
 116 range of 250 nm-10.6 μm .



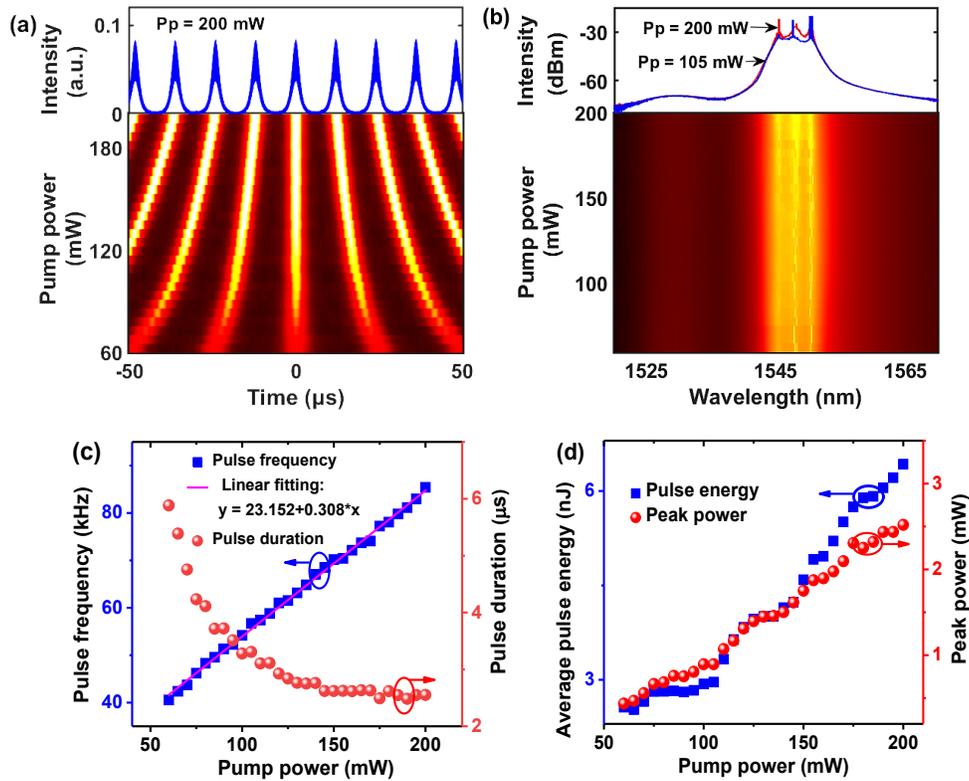
117
 118 Fig. 1. Experimental setup of the cascaded gain-fiber mode-locked laser. PD: photodiode; OSA:
 119 optical spectrum analyzer.

120 3. Experimental results and discussion

121 3.1 PQS operation

122 To initiate a stable PQS operation, the cavity energy needs to be accumulated to a certain
 123 value by increasing the pump power and then the cavity loss is sharply reduced by fine
 124 adjustments of the PCs. PQS operation of the fiber laser is easily achieved by increasing the
 125 pump power to 60 mW. As a single laser operation regime, the PQS state can sustain at pump
 126 power ranging from 60 to 200 mW. Figure 2(a) depicts the pulse evolution of the PQS laser
 127 output for gradual increase of the pump power in steps of 5 mW. Note that the time interval
 128 between adjacent pulses nonlinearly decreases with increase of the pump power, that
 129 indicates the increase of pulse repetition rate in accordance to pump power increase (typical
 130 feature of PQS operation). In contrast to the previously reported results for the SA-materials-
 131 based fiber lasers [35,37], in this experiment the pulse intensity is gradually enhanced as the
 132 pump power is increased, which is shown as the bright intensity color in Fig. 2(a).
 133 Oscilloscope trace of the pulse-train at 200 mW pump power is shown as blue curve in Fig.
 134 2(a). The profile of the pulse-train is quite uniform without any disturbances or noises
 135 indicated that the PQS mode of operation of this laser is highly stable.

136 Fig. 2(b) shows the evolution of output spectra against various pump power. Spectral
 137 profiles are almost similar at different pump power levels, but several peaks appear at
 138 fluctuating wavelength locations in the spectrum. In the upper part of Fig. 2(b) the blue and
 139 red curves are the output spectra at the pump powers of 105 mW and 120 mW, respectively.
 140 The central wavelength of these spectra coincides and located at 1548.06 nm with a 3-dB
 141 bandwidth of 5.81 nm. Three distinct peaks contributed by the CW components are observed
 142 in the spectrum, and their locations and/or intensities are controllable through the PC
 143 orientation maneuver. Figure 2(c) exhibits the pulse repetition rate (blue) and pulse duration
 144 (red) versus the pump power levels for a fixed intracavity polarization. The pulse repetition
 145 rate linearly rises from 40.54 to 85.42 kHz with a slope of ~ 3.08 kHz/10 mW, when the pump
 146 power is increased from 60 to 200 mW. On the other hand, the pulse duration evolution
 147 showed an inversely proportional characteristics with the pump power levels and reduced
 148 from 5.88 to 2.55 μ s. This can be attributed to the rapid accumulation of intracavity energy at
 149 a higher pump power that can swiftly accomplish the transition process between energy
 150 emptying and replenishing, which eventually results in a higher repetition rate and shorter
 151 duration PQS pulse formation. The average pulse energy and peak power as a function of
 152 pump power is shown in Fig. 2(d). The maximum pulse energy of 6.47 nJ is obtained at the
 153 pump power of 200 mW, corresponding to a peak power of 2.51 mW.



154

155

156 Fig. 2. Output characteristics of PQS pulse laser with pump power ranging from 60 to 200
 157 mW: (a) Evolution of temporal pulses train; (b) Corresponding evolution of output spectra; (c),
 158 (d) Pulse repetition rate, pulse duration, average pulse energy and peak power with the pump
 159 power increase.

160 3.2 QSML operation and transition process between PQS and QSML

161 When the pump power is more than 200 mW, the PQS pulse becomes unstable and the cavity

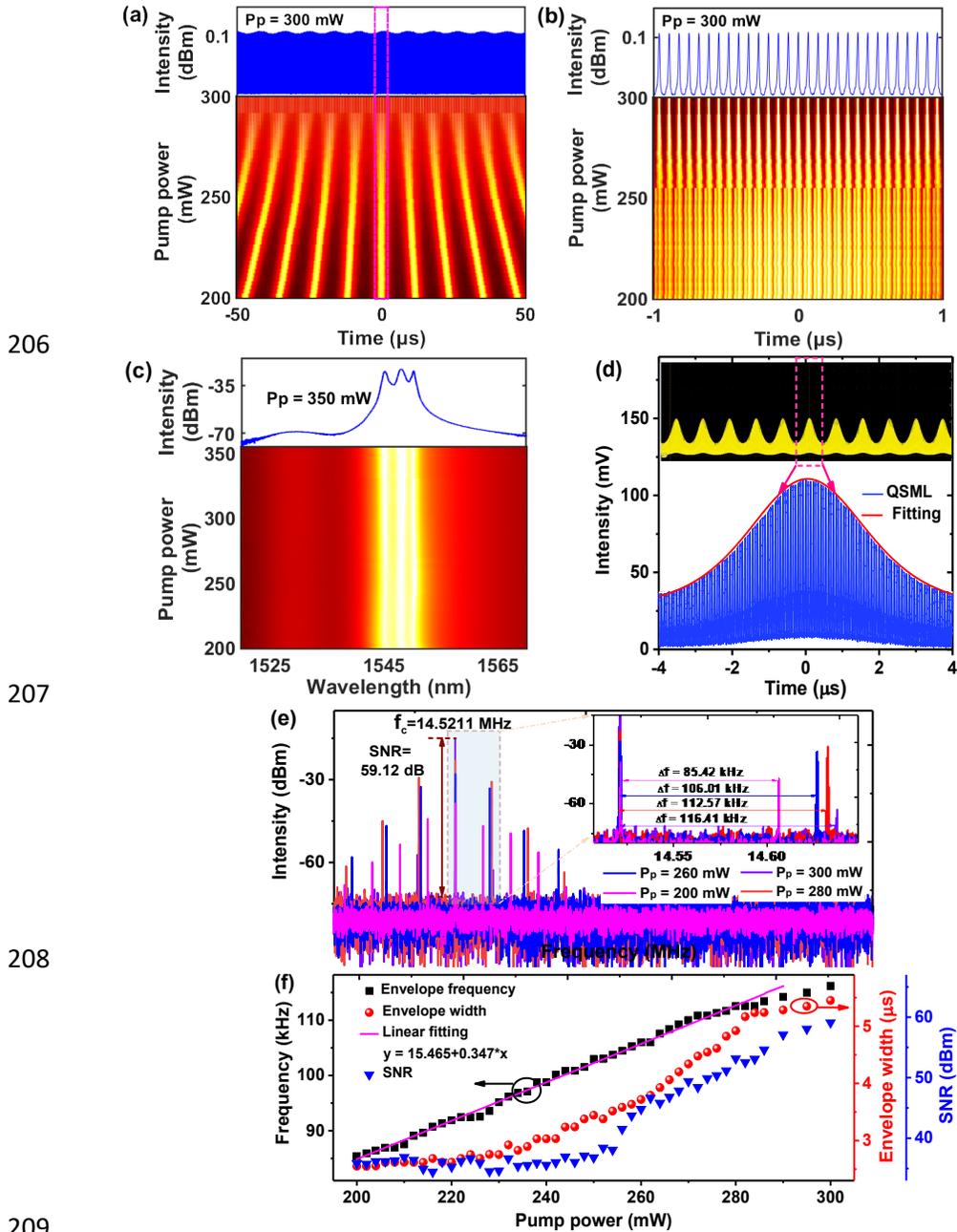
162 dynamics enters the Q-switched mode-locking (QSML) operation, where the pulses gradually
 163 split and the temporal profile of the pulse train is modulated by a periodic Q-switched pulse
 164 envelope. Figure 3(a) shows the pulse evolution of QSML laser operation for the pump power
 165 ranging from 200 to 300 mW. Time interval between adjacent Q-switched pulse envelopes
 166 decreases with increase of pump power, implying the generation of high repetition rate Q-
 167 switched pulse envelope as the pump power is increased. Unlike the pulse characteristics in
 168 the PQS state, the Q-switched pulse envelope intensity is not enhanced as the pump power is
 169 increased, and rather the external pump energy is transferred to the mode-locked pulses in
 170 QSML operation. Figure 3(b) displays the zoomed-in view of the pulse evolution of QSML
 171 laser for a time range of 2 μ s, corresponding to the red-dashed region in Fig. 3(a). Stable
 172 mode-locked pulse is gradually formed through a complex evolution process, and the explicit
 173 process and formation mechanism are analyzed further in detail later with the results reported
 174 in Fig. 4. The spectral evolution of the QSML operation is exhibited in Fig. 3(c), whose
 175 central wavelength is located at 1548.11 nm with a 3-dB bandwidth of 5.88 nm. The spectral
 176 bandwidth and central wavelength have no obvious change for pump power variations,
 177 indicating that the QSML operation has excellent long-term stability.

178 Zoomed-in view of single Q-switched pulse envelope at a pump power of 280 mW is
 179 presented in Fig. 3(d) in blue color, and a screenshot of the pulse sequence over a time range
 180 of 100 μ s is in yellow color. Mode-locked pulse train is modulated by a Q-switching pulse
 181 envelope, and the pulse interval is about 68.9 ns that corresponds to the cavity roundtrip time.
 182 The Q-switched pulse envelope is curve fitted by follow function [40]:

$$183 \quad P(t) = \frac{a}{[\exp(1.76 \times t / t_1) + \exp(-1.76 \times t / t_2)]^2} \quad (1)$$

184 where a is the scaling factor, the estimated $t_1=3.87 \mu$ s and $t_2=3.70 \mu$ s represent the rise-time
 185 and fall-time of the Q-switched pulse envelope respectively, and the full width at half
 186 maximum (FWHM) of the Q-switched pulse envelope is calculated as $\tau = (t_1+t_2)/2$. In Fig.
 187 3(d), red curve fits well with the Q-switched pulse envelope, the repetition rate of the Q-
 188 switched pulse envelope is ~ 112.57 kHz, and the FWHM of the pulse envelope is $\sim 3.79 \mu$ s.

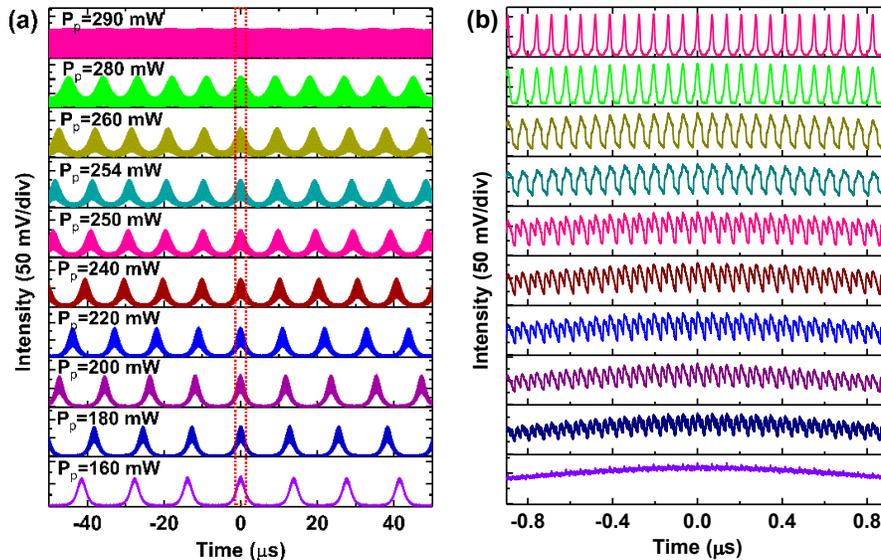
189 To further investigate the QSML operation, the radio-frequency (RF) spectral distributions
 190 are studied for various pump powers and the results are depicted in Fig. 3(e). A central
 191 frequency peak accompanied by a series of sideband frequency components are observed, and
 192 the frequency of central peak located at about 14.52 MHz (coincides with the fundamental
 193 repetition rate of the mode-locked pulse) with a signal-to-noise ratio (SNR) of 59.12 dB. For
 194 a fixed pump power, note the uniform frequency interval between adjacent sideband
 195 components, which corresponds to the repetition rate of the Q-switched pulse envelope [43].
 196 As noticed in the zoomed-in view of the dashed region in Fig. 3(e), the frequency offset
 197 between the adjacent side frequency components shifts farther away from the central
 198 frequency while the pump power is increased, and the explicit frequency offsets are measured
 199 as 85.42, 106.01, 112.57, and 116.41 kHz for the pump powers of 200, 260, 280 and 300 mW,
 200 respectively. Fig. 3(f) shows the variations of the pulse envelope repetition rate, the FWHM
 201 of the pulse envelope, and the SNR of the central frequency as a function of the pump power.
 202 As the pump power increased from 200 to 300 mW, the pulse envelope repetition rate linearly
 203 increased from 85.42 to 116.41 kHz with a slope of 3.47 kHz/10 mW, the FWHM of the
 204 pulse envelope is gradually broadened from 2.55 to 5.24 μ s nonlinearly, and the SNR of
 205 central frequency is improved from 35.84 to 57.11 dB.



210 Fig. 3. Properties of QSML pulse laser at different pump powers: (a) Evolution of temporal
 211 pulses train, and (b) enlarged view of the dashed region; (c) Evolution of output spectra; (d)
 212 Details of a single pulse envelope at the pump power of 280 mW; (e) RF spectra at different
 213 pump powers, and the illustration is the enlarged view of the dashed region; (e) Variations of
 214 the pulse envelope repetition rate, FWHM of the pulse envelope and SNR of central frequency
 215 versus pump power.

216 To explore the pulse evolution process from PQS to QSML operation, by maintaining the
 217 PC orientation fixed, we recorded oscilloscope traces of the output laser pulse train for
 218 various pump powers, and the results are exhibited in Fig. 4(a). Figure 4(b) is the zoomed-in
 219 view of the pulse trains between -0.9 and 0.9 μ s, which corresponds to the dashed region in

220 Fig. 4(a). PQS pulse starts to break up when the pump power is 180 mW, weak multiple
 221 peaks are formed in Q-switched pulse envelope, and the pulse intensity becomes unstable.
 222 These dynamics got aggravated as the pump power is further increased, and the modulation
 223 depth increased. A double-humped type pulse can be observed in Fig. 4(b), and this type of
 224 laser pulse is sustained for the pump power ranging from 180 to 250 mW. When the pump
 225 power is increased up to 254 mW, the double-humped peaks begin to merge together into
 226 single peak laser pulse, and a stable uniform mode-locked pulse is eventually generated for a
 227 pump power of 280 mW. The switching between PQS and QSML operation can be attributed
 228 to the built-in loss modulation of the cavity [42-44]. In our experiment, the loss modulation
 229 mainly resulted from the combined effects of the PCs and the cascaded small-core EBCF. The
 230 several meters small-core EBCF introduces an additive birefringence in the cavity for
 231 intensity-dependent phase delay, the laser pulses at different pump powers will undergo
 232 different phase delays during intracavity round-trips, which provides the required appropriate
 233 conditions to initiate and sustain a stable QSML operation. In addition, a nonlinear phase
 234 change is feasibly generated when the laser pulse propagates in EBCF with a 4 μm core
 235 diameter, which is beneficial for the formation of intensity-dependent loss modulation in the
 236 cavity [42]. If the small-core EBCF is removed from the cavity, the aforementioned evolution
 237 process between PQS and QSML state could not be achieved only with the adjustments of the
 238 PCs orientation.



239 Fig. 4. The pulse evolution process from PQS to QSML state along with the pump power
 240 increase: (a) The recorded oscilloscope traces of the pulse train at different pump powers; (b)
 241 the zoomed-in view of the pulse train in a time range of 1.8 μs .
 242

243 3.3 CWML operation

244 Mode-locking operation is a combined effect of dispersion, nonlinearity, gain, and loss in the
 245 cavity. The pump power should be high enough to provide sufficient gain and nonlinearity in
 246 the cavity, the weak longitudinal modes are attenuated by the nonlinear saturable absorption
 247 effect, while the longitudinal modes with a certain intensity are to be superimposed in-phase,
 248 resulting in the mode-locking operation. With a fixed PC orientation, the CWML operation is
 249 easily achieved for a pump power of 290 mW. Figure 5 (a) depicts the recorded oscilloscope
 250 traces of the pulse trains at 290, 310, 330, and 350 mW pump power over a time range of 100
 251 μs , and the temporal profiles of the pulse trains are maintained with high stability. To show

252 the intensity fluctuation of mode-locked pulse train, the zoomed-in view of the dashed region
 253 in Fig. 5(a) is shown in blue as the oscilloscope traces. Weak intensity modulation still exists
 254 in the CWML pulse train, and the time interval between adjacent pulse envelopes decreases
 255 slightly from ~ 8.72 to ~ 8.17 μs for rise in the pump power from 290 to 330 mW, and cease to
 256 appear for a pump power of 350 mW. The corresponding RF spectra are exhibited in Fig. 5(b)
 257 with a resolution bandwidth (RBW) of 100 Hz and a span of 1.4 MHz. The measured SNRs
 258 are 43.25, 48.51, 51.82, and 60.15 dB, indicating that the mode-locking can stably operate in
 259 the pump power ranging from 290 to 350 mW. The sideband frequency components are
 260 observed in the RF spectra, with frequency offsets of 114.61, 118.91, and 122.41 kHz which
 261 corresponds to the time intervals between adjacent pulse envelopes in Fig. 5(a). No sidebands
 262 indicate the disappearance of intensity modulation in the pulse train, which is ascertained by
 263 the pulse oscilloscope traces at 350 mW pump power. Figure 5(c) depicts the output spectra
 264 produced by the CWML laser for various pump powers. The central wavelength is 1547.95
 265 nm with a 3-dB spectral bandwidth of 5.83 nm. It is evident that three wavelength peaks
 266 located at 1545.08, 1547.95, and 1550.13 nm are distinct in the spectrum which is caused by
 267 the intracavity birefringence-induced spectral filtering effect. The measured intensity
 268 autocorrelation trace is shown in Fig. 5(d), and the pulse durations are about 436.81,
 269 387.24, and 382.46 fs, and the time-bandwidth products (TBP) are estimated to be 0.22, 0.21,
 270 0.19, and 0.19, which are nearly the transform-limited soliton pulses.

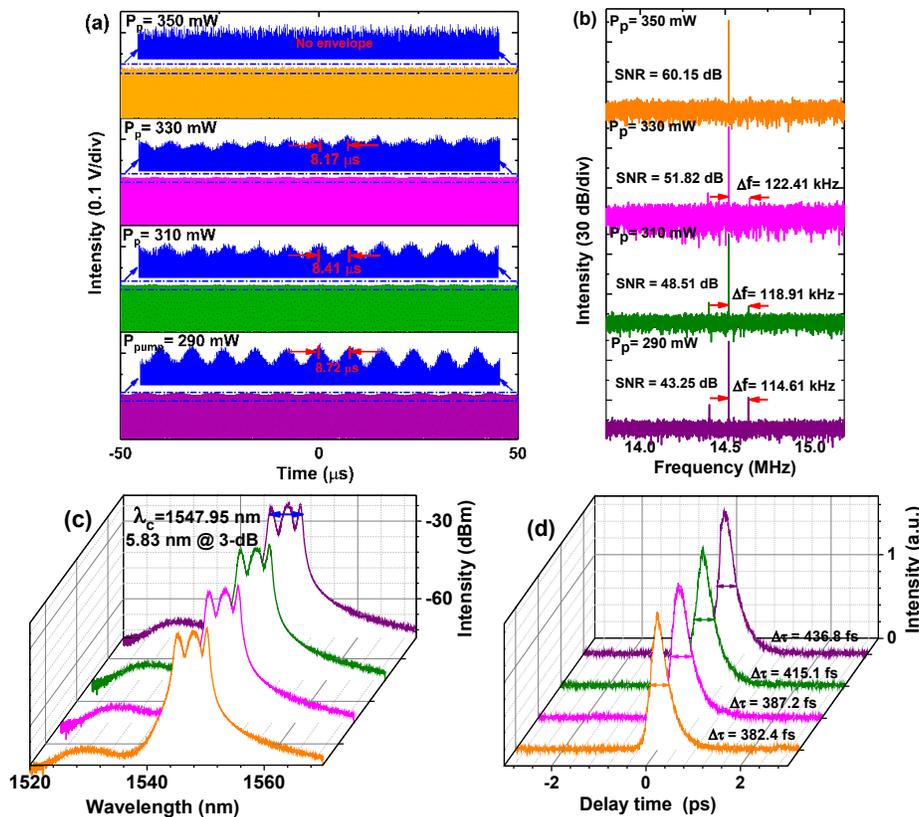


Fig. 5. Properties of CWML pulse laser with pump power ranging from 290 to 350 mW: (a) Temporal pulses train at different pump powers; (b) RF spectra, (c) Mode-locked spectra at different pump powers; (d) Corresponding autocorrelation traces of laser pulses.

277 **4. Discussion**

278 Pulsed fiber laser operation in different regimes such as PQS, QSML, and CWML is
 279 dependent on several cavity parameters for instance gain saturation power, gain relaxation
 280 time, modulation depth, and saturation power of SA etc. [14-37]. Inclusion of several-meters
 281 of small-core EBCF to enhance the built-in loss modulation in the cavity, made our proposed
 282 fiber laser dynamics to progressively evolve the lasing signal from PQS to QSML to CWML
 283 operation by simply varying the pump power for a fixed cavity polarization. The length of
 284 EBCF and/or polarization orientation are found to be additional control features for the laser
 285 state operation (similar to diode-pumped solid-state lasers [40]). In the experiment, when the
 286 pump power is increased up to 60 mW, the SA reaches saturation, and a high transmittance
 287 triggers the PQS pulse generation. Intracavity criterion to generate PQS pulses is [45,46]:

288
$$\left| \frac{dq}{dI} \right| I > \frac{\tau_R}{\tau_{stim}} \approx r \frac{\tau_R}{\tau_L} \quad (2)$$

289 where q is the intracavity loss introduced by SA during each roundtrip. I is the pulse intensity.
 290 τ_R is the cavity roundtrip time. τ_L is the upper-level lifetime of the gain fiber and
 291 $r = 1 + P / P_{sat}$ is the pump parameter. P and P_{sat} are the laser power and the gain saturation
 292 power. From inequality (2) we find that if the gain saturation cannot swiftly respond within
 293 the loss reduction per roundtrip time, the cavity gain gets higher than the loss, and hence the
 294 laser intensity will increase rapidly, resulting in the generation of PQS pulses. Also, longer
 295 upper-level lifetime of the erbium-doped fiber (~ 10 ms) in the laser cavity [47] is favorable
 296 for the PQS pulse formation.

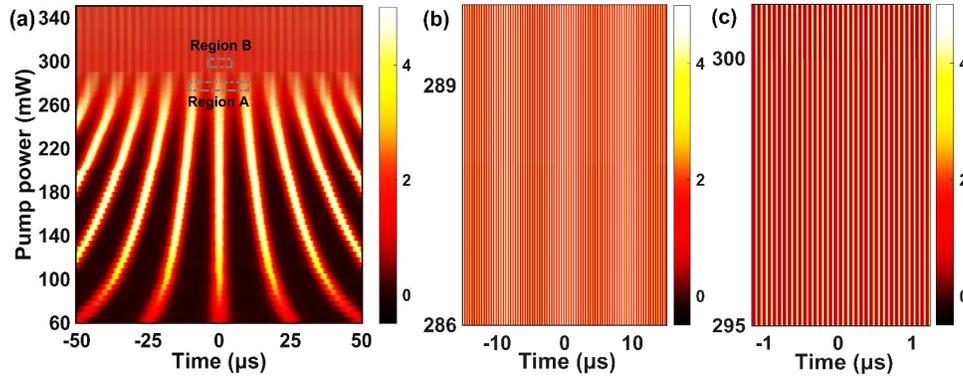
297 The QSML state can be regarded as a phenomenon of the amplitude modulation of mode-
 298 locked pulse caused by the instability of Q-switching. For numerous applications requiring
 299 uniform pulse energy and repetition rate, instability in Q-switching to be eliminated. When
 300 the pump power is increased to 180 mW, the PQS pulse envelope starts to break up, and
 301 stable QSML is gradually established for 300 mW pump power through a series of pulse
 302 evolution. The CWML formation criterion far from QSML is expressed as [48]:

303
$$\left| \frac{dq}{dE_P} \right| E_P < r \frac{\tau_R}{\tau_L} = \frac{\tau_R}{\tau_L} + \frac{E_P}{E_{sat}} \quad (3)$$

304 where E_{sat} is the gain saturation energy. Compared with inequality (2), the laser intensity I is
 305 replaced by the pulse energy E_P in inequality (3), since the gain saturation of SA is caused by
 306 the mode-locked pulse energy, rather than the average power of pulses [46]. When the
 307 intracavity gain saturation rate is faster than that of the SA, the gain saturation will inhibit the
 308 continuous enhancement of the Q-switched pulses. At the same time, if the resonator satisfies
 309 the mode-locking condition, then the laser can operate in the CWML state. When the
 310 intracavity pulse energy is higher than a certain value caused while increasing the pump
 311 power, the pulse laser will cease operating in QSML state and switch to operate in CWML
 312 state.

313 The recorded progressive temporal evolution of laser operation from PQS to QSML to
 314 CWML is exhibited in Fig. 6(a). When the pump power is increased from 60 mW to 200 mW,
 315 the laser stably operates in PQS state with the pulse repetition rate and peak power get
 316 increased as with the pump power. When the pump power increased beyond 200 mW, the
 317 PQS pulse becomes unstable and gradually evolve into QSML state. Figure 6(b) exhibits an
 318 enlarged QSML pulse evolution for a time range of 30 μ s (corresponding to the region A in
 319 Fig. 6(a)), in which both Q-switched pulse envelope and mode-locked pulses are observed.
 320 With further increase in the pump power, the laser is switched from QSML state to CWML
 321 state, and a mode-locked pulse evolution in CWML state for a time range of 2.4 μ s

322 (corresponding to the region B in Fig. 6(a)) is shown in Fig. 6(c). Here, the cavity operates in
 323 a robust mode-locked state without any intensity fluctuations. Different from the reported
 324 results in fiber lasers based on low-dimensional SA materials [14-37], the PQS, QSML, and
 325 CWML operation states can be flexibly switched simply by varying the pump power for a
 326 fixed polarization, and each state operates sturdily. This versatile switchable mode-locked
 327 fiber laser can be used as a seed pulse laser for subsequent power amplification, then further
 328 studying the luxuriant nonlinear interactions of laser pulses in highly nonlinear materials,
 329 such as photonic crystal fibers, nonlinear optical waveguide, and hollow-core fibers.



330

331 Fig. 6. (a) Progressive temporal evolution of pulse laser from PQS to QSML to CWML state;
 332 (b), (c) Zoomed-in pulse evolution in QSML (Region A) and CWML (Region B) operation
 333 states.

334 5. Conclusion

335 In conclusion, we have experimentally investigated the progressive pulse dynamics in a
 336 cascaded gain-fiber mode-locked laser. Due to the intracavity loss modulation resulting from
 337 the combined effects of the cascaded small-core EBCF and the polarization controllers, the
 338 pulse evolutions from PQS to QSML to CWML state are demonstrated and studied in detail
 339 by simply varying the pump power. The small-core EBCF introduces an additional
 340 birefringence effect in the cavity for the intensity-dependent phase delay, which provides the
 341 necessary conditions to initiate and sustain different operation regimes at suitable pump
 342 powers, especially the pulse transitional process between PQS and QSML is experimentally
 343 reported for the first time. For PQS state, the repetition rate increases from 40.54 to 85.42
 344 kHz, the pulse duration decreases from 24.66 to 5.88 μs with the increment of the pump
 345 power from 60 to 200 mW. For QSML state, the repetition rate of the Q-switched pulse
 346 envelope can be linearly tuned from 85.42 to 113.45 kHz with a slope of 3.47 kHz/10 mW,
 347 and the FWHM of the Q-switched pulse envelope is gradually increased from 2.55 to 5.24 μs.
 348 For CWML state, the center wavelength is 1547.95 nm with a 3-dB bandwidth of 5.83 nm.
 349 The fundamental repetition rate is 14.52 MHz with a SNR of >60 dB, which indicates high
 350 stability of the generated mode-locked pulses. This research work opens up a novel way of
 351 manipulating the operating regimes of mode-locked fiber laser and provides an innovative
 352 method to progressively realize the various laser operations from PQS to QSML to CWML
 353 state. Moreover, it exposes an effective and realistic technical route to study the complex
 354 nonlinear dynamic process in a passively mode-locked fiber laser.

355 **Funding.** National Natural Science Foundation of China (62275060).

356 **Disclosures.** The authors declare no conflicts of interest.

357
358

Data availability. Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

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References

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