

1 A novel approach for construction of radiocarbon-based chronologies
2 for speleothems

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22

23 **Abstract**

24 **Robust chronologies are crucial for the correct interpretation of climate**
25 **proxy records and for detailed reconstructions of palaeoclimate.**
26 **Stalagmites have garnered strong interest as recorders of past climate in**
27 **part due to their amenability to U-series dating. However, many**
28 **stalagmites are not dateable using this technique due to low ²³⁸U and/or**
29 **high detrital Th concentrations (e.g., many tropical cave systems (Adkins et**
30 **al., 2013)), and occasionally these issues affect stalagmites across wide**
31 **geographical regions (e.g., large parts of Australia (Green et al. 2013))**
32 **complicating the use of stalagmites in these areas. Radiocarbon (¹⁴C) offers**
33 **an alternative method of dating stalagmites, but issues associated with the**
34 **'dead carbon fraction' (DCF) have historically hindered this approach.**
35 **Here, a novel ¹⁴C-based method for dating stalagmites is presented and**
36 **discussed. The technique calculates a best-fit growth rate between a time-**
37 **series of stalagmite ¹⁴C data and known atmospheric ¹⁴C variability. The**
38 **new method produces excellent results for stalagmites that satisfy four**
39 **requirements: *i*) the absence of long-term secular variability in DCF (i.e.,**

40 stalagmite DCF varies around a mean value with no long-term trend), *ii*)
41 stalagmite growth rate does not vary significantly (the technique identifies
42 stalagmites with substantial growth rate variability), *iii*) the stalagmite
43 record is long enough that measurable ^{14}C decay has occurred, and *iv*) one
44 'anchor' point exists where the calendar age is known. The model produces
45 good results for a previously U-Th dated stalagmite from Heshang Cave,
46 China, and is then applied to an undated stalagmite from southern Poland.
47 The new method will not replace high-precision U-Th measurements,
48 because the precision of the technique is difficult to quantify. However, it
49 provides a means for dating certain stalagmites undateable by
50 conventional U-Th methods and for refining coarse U-Th chronologies.

51

52 1. Introduction

53 Stalagmites are becoming increasingly important climate archives, and have
54 yielded numerous iconic records of past terrestrial climate (e.g., Cheng et al.,
55 2009; Wang et al., 2001; Fairchild et al., 2006). Generally, stalagmites are
56 amenable to very precise absolute dating using the U-Th method (Cheng et al.,
57 2013; Dorale et al., 2007). The distinctly different behavior of U and Th in drip
58 waters means that stalagmite carbonate theoretically contains almost no ^{230}Th
59 when deposited, and that subsequent ^{230}Th accumulation results purely from
60 radioactive decay of ^{238}U and ^{234}U , allowing precise determination of carbonate
61 precipitation age (van Calsteren and Thomas, 2006). Additionally, the
62 development of powerful analytical techniques, initially Thermal Ionisation Mass
63 Spectrometry (TIMS) (Edwards et al., 1987; Li et al., 1989) and subsequently
64 Multi-Collector Inductively Coupled Plasma Mass Spectrometry (MC-ICPMS)
65 (Hoffmann et al., 2007), have greatly improved chronological precision.
66 However, stalagmites either with high detrital Th (not derived from in situ
67 radioactive decay) or with extremely low uranium concentrations have proven
68 problematic, and are occasionally not dateable using this approach (González-
69 Lemos et al., 2015; Urban et al., 2015). Young stalagmites (< 300 years), where
70 the U-Th method has its largest uncertainties, are most susceptible to these
71 issues (Hodge et al., 2011; Matthey et al., 2008).

72

73 The first method proposed to develop chronologies for stalagmite-based climate
74 records was ^{14}C dating (Broecker et al., 1960; Hendy and Wilson, 1968), due to
75 its already widespread application to other terrestrial archives such as tree rings
76 and lake sediments (e.g., Reimer et al., 2013; Street and Grove, 1979; Suess,
77 1980) and in groundwater research (Wigley, 1975). However, ^{14}C in
78 groundwater and consequently stalagmite carbonate reflects contemporaneous
79 atmospheric ^{14}C combined with variable amounts of ^{14}C -depleted carbon from
80 the soil and host rock. This reservoir effect, termed the “dead carbon fraction”
81 (DCF, used hereafter in this text), or “dead carbon proportion” (dcp, DCP), if not
82 properly constrained, results in stalagmite ages that are too old (Genty and
83 Massault, 1999; Genty et al., 2001; Holmgren et al., 1994). Formally, DCF is
84 expressed as:

$$85 \quad DCF = 1 - \left(\frac{a^{14}\text{C}_{stal.init.}}{a^{14}\text{C}_{atm.init.}} \right) \quad (1)$$

86 where $a^{14}\text{C}_{stal.init.}$ and $a^{14}\text{C}_{atm.init.}$ represent stalagmite and atmosphere ^{14}C activity
87 (respectively) at the time of carbonate deposition. Potentially unquantifiable
88 DCF variability, combined with contemporaneous analytical advances involving
89 the U-Th method, resulted in the dismissal of ^{14}C -dating of stalagmites as a viable
90 approach (Gascoyne, 1992; Genty et al., 2001). The issues with absolute ^{14}C
91 dating of stalagmites revolve around accurate quantification of DCF. Solving this
92 problem would thus open the door to the application of the technique to
93 speleothems. Over the past two decades, numerous studies have attempted to
94 identify mechanisms governing DCF and its variability, largely with the aim of
95 using DCF as tracer for hydrological and carbon cycle processes (Fohlmeister et
96 al., 2011, 2010; Genty and Massault, 1999; Genty et al., 2001; Griffiths et al.,
97 2012; Noronha et al., 2014). This past research strongly suggests that host rock
98 dissolution processes and the degree of open- versus closed-system behavior
99 within the karst (Fohlmeister et al., 2010; Griffiths et al., 2012; Noronha et al.,
100 2014), as well as contributions from soil organic matter (Oster et al., 2010;
101 Scholz et al., 2012), exert primary control on DCF variability. All these processes
102 are dependent on hydrological conditions, and consequently several recent
103 papers have proposed that changes in DCF reflect past hydroclimate variability

104 (Griffiths et al., 2012; Noronha et al., 2014; Oster et al., 2010). Additionally, the
105 location of the atmospheric 'bomb spike' (resulting from widespread nuclear
106 testing in the 1950s and 1960s) within stalagmite stratigraphy represents a
107 potentially useful chronological tool. For example, Matthey et al. (2008) and
108 Hodge et al. (2011) used the bomb spike imprint to date stalagmites by inverse
109 modelling of their ^{14}C uptake, providing a method for development of robust
110 chronologies for very recent deposits (~1950-present) where U-Th techniques
111 are less precise. Hua et al. (2012) constructed additional chronologies for two of
112 the stalagmites used by Hodge et al. (2011) using the ^{14}C bomb spike combined
113 with high-resolution $\delta^{18}\text{O}$ and $\delta^{13}\text{C}$ measurements. Another approach is
114 illustrated in González-Lemos et al. (2015), who used $\delta^{13}\text{C}$ values to define
115 periods of similar DCF, assuming a comparable hydrological influence on both
116 parameters. These studies have applied ^{14}C dating to stalagmites using very
117 different approaches to constrain DCF, illustrating the potential applicability of
118 the technique to stalagmites. For most samples, U-Th dating produces the best
119 dates, but for samples not amenable to U-Th dating, the ^{14}C method provides an
120 alternate chronological tool. Additionally, high precision ^{14}C dating typically
121 requires only 8-10 mg powdered sample, compared to up to several 100 mg for U-
122 Th, which is advantageous in many situations.

123

124 Here we present a new method for the construction of accurate stalagmite
125 chronologies using ^{14}C . The method determines the mean stalagmite growth rate
126 by comparing a long stalagmite ^{14}C time-series to atmospheric ^{14}C over the same
127 time interval. The technique is not yet applicable to all stalagmites, but highlights
128 promising aspects of stalagmite ^{14}C records that could be refined to fit a wide
129 variety of samples.

130

131 2. Sample description

132 Stalagmite NIED08-05 was collected in 2008 from Niedźwiedzia Cave in Kletno,
133 Poland (Fig. 1). The cave has been a closed system since the Early Holocene, with
134 access to the surface only through ponors (Don, 1989; Pflitsch and Piasecki,
135 2003). However, the presence of cave bear skulls and entire skeletons in the cave
136 indicate that there must always have been a relatively large opening to the

137 outside world (Bieronski et al., 2009). The first 200 m of cave passage were
138 discovered in 1966 during marble mining followed by an additional ~2 km in
139 1982.

140 The cave's isolation from the outside atmosphere would have minimized
141 external influences, and encouraged slow calcite growth. NIED08-05 grew in the
142 upper level of Niedźwiedzia Cave, approximately 10 meters below the surface
143 (Fig. 1), where air temperature is very stable (<1.0°C variation around the multi-
144 annual average), and relative humidity (RH) is almost 100% (Piasecki and
145 Sawinski, 2009). The mean annual temperature within the cave is 6°C, reflecting
146 the mean annual outside temperature. To ensure active stalagmite growth, the
147 drip feeding NIED08-05 was monitored for ~three months (04 April - 20 June
148 2008) using a Stalagmate drip counter. After removal from the cave, NIED08-05
149 was sectioned along its growth axis and polished at Durham University. The
150 stalagmite is 12.5 cm long and composed of very dense, coarse crystalline calcite
151 (Fig. 2a). No regular visible laminae exist, except for a few white microcrystalline
152 layers that may reflect growth hiatuses. Very low concentrations of ²³⁸U (mean
153 concentrations = ~14 ppb) prevented high-precision U-Th dating, as typical
154 dating errors over the Holocene were between 190 and 4065 years, with
155 numerous stratigraphic inversions. Because the stalagmite was otherwise an
156 excellent sample (free from detrital contamination, appropriate crystal
157 morphology, from a region with few long palaeoclimate records), it was decided
158 to date the sample using ¹⁴C.

159

160 3. Analytical methods

161 3.1. ¹⁴C measurements

162 Samples for high-precision graphite ¹⁴C analysis were drilled at 5 mm resolution
163 along the growth axis using a semi-automatic high precision drill (Sherline 5400
164 Deluxe) at ETH Zurich. To minimise potential contamination, all the equipment
165 and the stalagmite were cleaned with methanol and dried using compressed air
166 prior to sampling, and the top 0.1 mm of stalagmite surface powder was
167 discarded. Aliquots of ~8 mg of carbonate powder were dissolved in 1 ml of 85%
168 H₃PO₄. Fast carbonate dissolution and a complete conversion to CO₂ were
169 ensured by heating the sample vials to 85°C for one hour. Graphitisation was

170 performed using an Automatic Graphitization Equipment (AGE) system (Wacker
171 et al., 2010) via iron-catalysed hydrogen reduction of the CO₂. The resultant
172 graphite was transferred to aluminum targets for determination of ¹⁴C activities
173 (a¹⁴C) using a Mini radioCarbon Dating System (MICADAS) accelerator mass
174 spectrometer (AMS) (Synal et al., 2007) at the Laboratory for Ion Beam Physics
175 (LIP) at ETH Zurich. In addition, detailed sampling and ¹⁴C analysis was
176 undertaken to detect the atmospheric ¹⁴C bomb spike imprint. For this, the top
177 1mm of NIED08-05 was milled at an extremely high resolution (100µm per
178 sample) over four different tracks. Approximately 0.8 mg of carbonate were
179 dissolved in 85% H₃PO₄, and the CO₂ produced was measured directly on the
180 MICADAS using a Gas Ion Source (GIS) system (Ruff et al., 2007), again at LIP. A
181 series of laboratory standards (Oxalic acid II, IAEA C1 and C2, and a modern
182 coral standard) were used to ensure high precision: Oxalic acid II was measured
183 to a precision of better than 2‰ for graphite and 10‰ for GIS analyses. In
184 addition, ¹⁴C-dead stalagmite material (stalagmite material from NE India, MAW-
185 1: ~170 kyr, based on U-Th dates) was used as a procedural blank during all
186 measurement runs.

187

188 3.2 Stable isotope and trace element analysis

189 260 samples for stable isotope analysis were milled continuously along the
190 growth axis, using a Proxxon micromill at Durham University. The samples were
191 transferred to glass Exetainer vials and flushed with He to remove outside air
192 before acid digestion using 103% H₃PO₄. The measurement was conducted on a
193 Thermo-Finnigan MAT253 Isotope Ratio Mass Spectrometer at Durham
194 University, and uncertainties were assessed from standards NBS-18, NBS-19,
195 LSVEC and an in-house standard. External analytical uncertainties for both δ¹³C
196 and δ¹⁸O are 0.1‰ and presented relative to the Vienna Pee Dee Belemnite (V-
197 PDB).

198

199 A high-resolution profile of major trace elements over the top ca. 105 mm of
200 NIED08-05 was produced using a prototype RESolution M-50 excimer (193 nm)
201 laser-ablation system with a two-volume laser-ablation cell coupled to an Agilent
202 7500ce/cs quadrupole ICPMS at Royal Holloway University, London. Müller et al.

203 (2009) describe in detail the analytical configuration and initial performance
204 metrics. The profile was measured using a 140 by 10 μ m rectangular laser slit, a
205 15Hz repetition rate of a 90mJ laser spot, and a 10 μ m s⁻¹ scan speed. Samples
206 were bracketed by analyses of NIST 612, NIST 610 and MACS3 standards for
207 quantification. Data reduction was performed using the Lolite software package
208 using NIST 610/612 standards for external standardization (Paton et al., 2011).
209 Calcium-43 was measured throughout the sample runs as an internal standard.

210

211 4. Results

212 4.1. ¹⁴C measurements: chronology and bomb spike identification

213 Twenty-five high-precision graphite ¹⁴C ages, ranging from 1,139 \pm 27 years at 5
214 mm from the top to 8,909 \pm 38 years at the base (122 mm from the top), were all
215 in stratigraphic order within measurement uncertainty, apart from a small
216 reversal at 102 mm depth (Fig. 2a, Table 1). The ¹⁴C data suggest the NIED08-05
217 growth spans much of the Holocene, in agreement with the initial assumption
218 based on the very imprecise U-Th ages. Very regularly increasing ¹⁴C ages with
219 depth suggest generally constant stalagmite growth. However, an abrupt 1,700-
220 year shift occurs between 47 and 52 mm from top coinciding with a thin white
221 microcrystalline layer, strongly suggesting the presence of a growth hiatus (Fig.
222 2a). Similar microcrystalline layers elsewhere in the stalagmite suggest that
223 other hiatuses exist, but because the ¹⁴C ages do not indicate growth interruption
224 at these times these possible (probably very brief) hiatuses were not considered
225 in the final chronology. The very high resolution GIS measurements along the top
226 1 mm of NIED08-05 show considerably increased ¹⁴C activity in the uppermost
227 0.4 mm in three out of four replicate tracks, confirming the presence of the bomb
228 spike (Fig. 2b, Suppl. Table 1). The different manifestations of the atmospheric
229 ¹⁴C bomb spike in the four traverses is attributable to strong signal attenuation
230 in the karst (max. a¹⁴C = 0.96 fraction modern (fM) compared with 1.98 fM in the
231 atmosphere in 1963; Hua et al., 2013), to sampling bias due to the transect
232 position relative to stalagmite curvature, and to the remarkably high-resolution
233 nature of these ¹⁴C analyses. All samples were larger than the threshold where
234 significant blank contributions occur that could influence the reliability of the
235 results (see section **Error! Reference source not found.**). To our knowledge,

236 these are the first high-resolution ^{14}C measurements performed on replicate
237 tracks in a stalagmite.

238 Replicate blank measurements on milled aliquots of the ^{14}C -dead stalagmite
239 MAW-1 ensure that no contamination from modern atmospheric ^{14}C during
240 carbonate drilling, as encountered by previous studies (Hoffmann et al., 2010;
241 Southon et al., 2012), occurred.

242

243 4.2. Stable isotope and trace element analysis

244 Overall, in NIED08-05 $\delta^{13}\text{C}$ remains very stationary with only a minor longer-
245 term trend (mean = -7.48‰ , $\sigma = 1.17$, Suppl. Fig. 1). Conversely, Mg
246 concentrations are quite variable throughout the stalagmite (mean Mg/Ca ratio \times
247 1000 = 2.56, $\sigma = 0.85$). Several large excursions exist within the Mg dataset, with
248 gradual increases in Mg/Ca followed by more abrupt decreases (e.g. at 10 mm,
249 44 mm and 51.5 mm from top) possibly reflecting karst hydrology processes
250 and/or growth hiatuses (Suppl. Fig. 1).

251

252 5. Chronology development

253 The technique described herein does not utilise ^{14}C ages as discrete dates, but
254 instead focusses on the topology of the long-term $a^{14}\text{C}$ -depth relationship.
255 Regularly decreasing $a^{14}\text{C}$ with depth from the sample top strongly suggests that
256 only small stalagmite growth rate and DCF changes occurred, and that
257 exponentially decreasing $a^{14}\text{C}$ is only due to radioactive decay. In this case, the
258 best-fit line describing the ^{14}C data should reflect the stalagmite's long-term
259 average growth rate, and a simple chronology can be built by anchoring the
260 growth rate to a point of known age (such as collection date, or the bomb spike).
261 Similar approaches are used in other fields of geochronology, for example in
262 ^{210}Pb dating of sediments over the last 100 years (Appleby & Oldfield, 1978;
263 Baskaran et al., 2014) or in ^{230}Th excess dating of deep sea sediments (Francois
264 et al., 1990). However, whereas those methods generally assume that
265 radionuclide incorporation rate is essentially constant over time, this is not the
266 case with ^{14}C due to past variations in atmospheric $a^{14}\text{C}$ (e.g., Reimer et al.,
267 2013).

268

269 The model presented here identifies stalagmites with ‘stationary’ growth rates
270 over long time intervals (i.e., samples with growth rates that vary around a long-
271 term mean value). Stationarity in DCF implies that no secular changes in both the
272 soil organic matter age and the host rock dissolution systems (open vs. closed)
273 occurred. Secular changes in DCF define long-term trends resulting from large
274 fluctuations in climate (e.g. deglaciations (Rudzka et al., 2011)) or changes in the
275 cave’s carbon cycle (e.g. build-up of soils (Genty et al., 2001; Scholz et al., 2012)).
276 These trends in DCF are detectable using through other geochemical proxies,
277 such as $\delta^{13}\text{C}$ and Mg/Ca, as demonstrated by many previous studies (e.g. Scholz
278 et al., 2012, Genty et al., 2001, Rudzka et al., 2011). Such long-term changes in
279 DCF would preclude a stalagmite to be suitable for the method presented here.
280 Small DCF variations around a long-term mean value, however, are permissible.

281

282 Assuming that the stationarity condition is met, the model builds an age-depth
283 relationship accounting for both variable DCF and atmospheric ^{14}C . There are
284 two principal steps to the process: *i*) the chronology is anchored to an
285 independent point of known age and *ii*) an iterative, MATLAB-based process
286 adjusts modelled stalagmite growth rate by considering past atmospheric ^{14}C
287 variability. If DCF remains stationary on long timescales, short-term (seasonal or
288 longer term) DCF fluctuations around a mean value do not affect the calculations.
289 This is not dissimilar to U-Th dating, which only produces ages for a few select
290 depths and infers the ages of other depths (and consequently growth rates)
291 using best-fit equations.

292

293 5.1. Model setup

294 The model is based on the radioactive decay equation, expressed by:

295

$$296 \quad A/A_0 = e^{-\lambda t} \quad (2)$$

297 where A is the ^{14}C activity measured in the stalagmite, A_0 is the initial stalagmite
298 ^{14}C activity, and λ is the ^{14}C decay constant ($1/8267 \text{ yr}^{-1}$). Carbonate deposition
299 age (t) is unknown and is expressed as:

300

301 $t = d/R$ (3)

302 where d is the depth from the stalagmite top and R is the growth rate.

303 Converting equation 2 to its linear form with respect to t yields:

304

305 $\ln(A/A_0) = -\lambda t$ (1)

306 and if

307

308 $\ln(A/A_0) = -\lambda * d/R$ (2)

309 the slope is proportional to $1/R$.

310

311 Variable atmospheric ^{14}C and karst carbon transfer dynamics (i.e., DCF)
312 complicate quantifying A_0 . A point of known age anchors the entire chronology
313 taking into account DCF, and thus atmospheric $a^{14}\text{C}$ entirely drives A_0 .

314

315 5.2. Anchor point selection and identifying the best-fit decay curve

316 The model requires a point of known age to account for DCF, and therefore the
317 ‘anchor point’ needs to be defined before starting the modelling procedure. For
318 stalagmites that were growing when collected, the collection date is suitable.
319 Other possibilities are the beginning of the bomb spike rise (i.e., the first
320 indication of bomb ^{14}C in the atmosphere, 1955 AD), or a robust U-Th
321 measurement, if available. In the first step, the model computes a best fit through
322 all $a^{14}\text{C}$ measurements in the dataset, defining an initial growth rate (Fig. 3a). A_0
323 is kept at 1 for this step (i.e., constant atmospheric ^{14}C). The anchor point
324 permits calculation of each sample’s calendar age via the growth rate. Because A_0
325 = 1, this initial age-depth relationship requires further refinement. In the second
326 iteration, atmospheric ^{14}C values from the IntCal13 calibration curve (Reimer et
327 al., 2013), corresponding to the calculated sample ages, are assigned as new A_0
328 values and a new, slightly different growth rate is calculated. Atmospheric ^{14}C
329 values from the IntCal13 are smoothed prior to the fitting procedure using a
330 moving average (window size 5) to mimic the effect of soil organic matter and
331 vegetation on the soil CO_2 (Fohlmeister et al., 2011). The stalagmite ages are then

332 re-adjusted accordingly, with a static anchor point (i.e., unchanged from iteration
333 1). The procedure is repeated until convergence is reached and growth rate
334 changes become insignificant ($<0.0001\text{mm yr}^{-1}$). This condition is typically
335 reached after four to six iterations of the fitting procedure (Fig. 3).

336

337 5.3. Hiatus integration in the model

338 Constraining and delimiting the duration and exact timing of hiatuses is critical
339 for developing accurate chronologies. The probable lack of an anchor point
340 below hiatuses complicates applying the model described here, as is the case in
341 NIED08-05 for the growth interval older than the depositional hiatus ('pre-
342 hiatus'). A modified version of the method can develop the pre-hiatus
343 chronology, although only qualitatively.

344

345 For stalagmites with a depositional hiatus, the model initially constrains the
346 post-hiatus interval as in section 5.2., permitting the calculation of mean DCF for
347 that interval. Assuming stationary DCF over the entire stalagmite, this mean DCF
348 and its standard deviation are applied to all ^{14}C ages from the pre-hiatus interval.
349 The DCF corrected ^{14}C ages are then calibrated to calendar years using a
350 procedure similar to commonly available calibration tools, but built into the
351 MATLAB modelling procedure. Correcting and calibrating all pre-hiatus ages
352 prevents over- or under-estimation of the stalagmite age due to a single offset
353 age (from a possible extreme DCF value), and is therefore more robust than
354 treating only one individual (i.e., the first) pre-hiatus age. The calibration of the
355 DCF corrected ^{14}C ages provides a probability density distribution in time for
356 each ^{14}C age. The best growth rate (Fig. 3b, red line) through the probability
357 densities of all ages is determined by using the following procedure: *i)* the
358 youngest pre-hiatus age acts as a preliminary anchor point, and the constant
359 growth rate line is positioned through that point (Fig. 3b, red line); *ii)* The
360 growth rate line is then shifted gradually through time, intersecting each point of
361 the calibrated age probability distribution at a certain point (Fig. 3b); *iii)* The
362 probabilities of the intersection points are added and quantify the constant
363 growth rate line's fit to the entire data (Fig. 3c). *iv)* Shifting the line of constant
364 growth through the calibrated ^{14}C ages establishes a new probability function for

365 the placement of this line. The best placement is determined using the weighted
366 mean of the probability distribution, which again ensures that the model is not
367 biased by single offset ages (Fig. 3c).

368

369 5.4. Uncertainties and error estimation

370 The model considers different sources of error, including: A) Estimated growth
371 rate error, related to the goodness of the fit through the measured ^{14}C data; B)
372 Measurement error regarding the depth from stalagmite top (i.e. uncertainty
373 introduced from the sampling); C) Error on the calculated mean DCF, defined by
374 its standard deviation, and D) Uncertainty from the calibration, given by the
375 probability density distribution of the calibrated ^{14}C ages.

376

377 For the simple case of an age model without any hiatus, the resulting uncertainty
378 depends only on errors of type A and B. The chronological uncertainty is
379 calculated using common error propagation, and increases with distance from
380 the anchor point, due to uncertainty in the growth rate estimate (uncertainty in
381 the slope determined during the fitting procedure). In this case, the model's
382 chronological error is small, and depends on how well the anchor point is
383 constrained. If a hiatus is present, the chronological uncertainty for the lower
384 part is assessed differently, and the uncertainty is governed largely by type C and
385 D errors, whereas other errors are trivial and not considered. Because the age
386 model's pre-hiatus interval is not based on a single anchor point, but rather all
387 ^{14}C ages act as anchor points, the uncertainty is defined by the new probability
388 function for the placement of the constant growth rate line (Fig. 3c). This results
389 in much larger errors than for the case with no hiatus.

390

391 6. Model testing and application

392 6.1. Stalagmite HS4 (Heshang Cave)

393 The model was tested using a previously published stalagmite ^{14}C dataset from
394 Heshang Cave (China) (Noronha et al., 2014). Stalagmite HS4 is 250 cm tall and
395 was dated using U-Th techniques, which suggest continuous growth with an
396 almost constant growth rate over the past ~8,000 years (Hu et al., 2008). DCF is
397 stationary but varied between 7 and 14% (Noronha et al., 2014); therefore the

398 sample is ideal for testing the reliability of the ^{14}C chronology development
399 technique presented here.

400

401 The exponential decay function was transformed to a linear relationship to
402 simplify data visualization and handling. Removing the linear trend from the
403 natural logarithm of the $a^{14}\text{C}$ ($\ln(a^{14}\text{C})$) data reveals that the top three ^{14}C ages
404 in HS4 are anomalous (defined as ages more than 1σ away from the dataset's
405 mean (Suppl. Fig. 2)), possibly due to a shift in growth rate or DCF. If a growth
406 rate shift occurred, and an anchor point were chosen in the anomalous interval,
407 an offset in the age-depth model may result. To avoid chronological bias, the
408 anchor was therefore set to the first ^{14}C data point beyond the anomalous top
409 interval (the fourth ^{14}C point from the top overall) (Suppl. Fig. 2), rather than at
410 the first data point from the top of the ^{14}C dataset. Growth rate convergence was
411 reached after four iterations, and comparison between modelled and actual
412 growth rate (derived from U-Th dating) show excellent agreement (modelled ^{14}C
413 growth rate = $0.0262 \pm 0.00047 \text{ cm yr}^{-1}$; U-Th growth rate = $0.0259 \text{ cm yr}^{-1}$). The
414 model's chronological error is between ± 1 and ± 155 years (Fig. 4). In
415 comparison, if the first data point from the top of the ^{14}C dataset is used as
416 anchor point, the modelled ages are overestimated throughout most of the
417 chronology. Consequently DCF is underestimated on average by 3% (max.
418 underestimation = 6%), although the chronological precision is unchanged (Fig.
419 4). A shortcoming of the model is therefore its dependency on the choice of
420 anchor point; even with prolonged, nearly constant growth rate, the anchor point
421 determines chronological accuracy. A detailed analysis of the raw ^{14}C data profile
422 can help evaluating the suitability of any chosen anchor point, and assessment of
423 whether that point is representative of average DCF throughout the stalagmite.

424

425 6.2. NIED08-05 (Niedźwiedzia Cave)

426 The procedure was applied to develop a chronology for stalagmite NIED08-05
427 from Niedźwiedzia Cave, which lacks a robust U-Th chronology. Dating with U-
428 Th was attempted and roughly confirms growth during most of the Holocene
429 (present – 9000 yr BP). However, very large errors and numerous stratigraphic

430 inversions, related to low ^{230}Th and unknown initial $^{230}\text{Th}/^{232}\text{Th}$ ratios, prevent
431 the construction of a reliable U-Th chronology for this stalagmite.

432

433 A continuous $\delta^{14}\text{C}$ decrease with increasing depth suggests that DCF and growth
434 rate were stationary. Very stable $\delta^{13}\text{C}$ values (i.e., only a minor long-term trend)
435 support this interpretation (Suppl. Fig. 1). However, the $\delta^{14}\text{C}$ values suggest that
436 a hiatus exists and that growth rate is slightly different before and after the
437 hiatus. The pre- and post-hiatus intervals were therefore considered separately,
438 and two different growth models were constructed.

439

440 The younger (post-hiatus) interval was anchored to 2008 AD (the year of
441 collection). The choice of the anchor point is justified by active dripping of the
442 feeding stalactite and by the presence of the bomb spike in the top 0.4 mm of the
443 stalagmite, both strongly suggesting recent growth. Additionally, the top \ln
444 ($\delta^{14}\text{C}$) value lies within the dataset's 1σ boundary, suggesting no growth rate
445 anomalies (as was the case for HS4, Suppl. Fig. 2). The model reached
446 convergence after four iterations, yielding a calculated mean growth rate of
447 $0.0132 \pm 0.0012 \text{ mm yr}^{-1}$ and a growth interval from $3,833 \pm 330 \text{ yr BP}$ until
448 2008 AD (Fig. 5). The mean modelled DCF for the post-hiatus interval is 10%
449 ($\pm 4\%$), similar to the DCF calculated from the bomb spike ($\sim 14\%$).

450

451 No independent anchor points exist below the hiatus and the chronology for pre-
452 hiatus growth was developed using the methodology outlined in section 5.3.
453 After three iterations, the model reached convergence, resulting in a mean
454 growth rate of $0.0227 \pm 0.00054 \text{ mm yr}^{-1}$ over this lower interval. The modelled
455 ages suggest that stalagmite NIED08-05 began growing at $7,961 \pm 1,354 \text{ yr BP}$
456 and continued until $4,876 \pm 1,354 \text{ yr BP}$, at which point growth stopped for
457 $\sim 1,000$ years (Fig. 5). However, because of the large dating uncertainty in this
458 interval, these ages should be considered as only qualitative.

459

460 Because ^{14}C sample powders were obtained at a resolution (every 5 mm) that
461 prevents pinpointing the location of the hiatus, the high resolution LA-ICPMS Mg
462 concentration profile was used to locate its exact depth. At 51.5 mm depth, a

463 gradual increase to very high Mg values within the two ^{14}C samples bracketing
464 the hiatus and coinciding with its probable petrographic expression occurs. This
465 is followed by a very abrupt return to lower values (Suppl. Fig. 1), strongly
466 suggesting that the hiatus is located at 51.5 mm depth. This feature probably
467 reflects decreased rainfall and elevated Mg concentrations derived from high
468 prior calcite precipitation (PCP) or bedrock dissolution (Sherwin & Baldini,
469 2011; Stoll et al., 2012), followed by abrupt growth cessation. Once drip water
470 flow resumed and/or the drip water was again supersaturated with respect to
471 calcite, stalagmite growth re-initiated and calcite Mg concentrations abruptly
472 returned to lower values. Therefore, the exact location of the hiatus was placed
473 at the transition between the highest Mg/Ca point and the return to the baseline.
474 We are aware of the fact that other prominent excursions in Mg/Ca, as well as
475 petrographic layers, exist throughout the record, which could indicate the
476 presence of more growth hiatuses. However, the fact that these excursions are
477 not accompanied by substantial shifts in ^{14}C suggests that these potential
478 hiatuses (if present) were very short lived, and do not have a significant impact
479 on the final chronology.

480

481 7. Evaluation of the age model

482 The procedure presented here provides accurate ^{14}C -based chronologies for
483 some stalagmites where U-Th dating is not possible. Stalagmites amenable to this
484 dating method are characterised by: *i*) stationary DCF without long-term secular
485 variability, *ii*) stationary growth rate, *iii*) measurable ^{14}C decay, *iv*) the presence
486 of an 'anchor point' (an independent age estimate) determined by other means,
487 *iii*) growth during the last $\sim 50\text{ka}$ (the current ^{14}C detection limit). The model
488 provides a mean growth rate for a stalagmite by finding the best fit through all
489 available ^{14}C ages, so small-scale growth rate variability is not resolvable. Two
490 problems arise from this: first, stalagmites that experienced substantial growth
491 rate shifts will have larger chronological uncertainty, potentially impeding the
492 convergence of the iterative process, especially in the case of young stalagmites
493 (i.e., where little ^{14}C -decay has occurred). However, a sufficiently high-resolution
494 ^{14}C dataset could detect and model a growth rate change if the shift was large
495 enough and occurred over a long time period. To test this, we produced a

496 synthetic dataset of a 192 mm long stalagmite where a substantial growth rate
497 change occurs at 77.5 mm depth (0.0613 to 0.0133 mm yr⁻¹) and DCF varies
498 between 12 and 16%. The ln (a¹⁴C)-depth relationship highlights the growth rate
499 change in the synthetic dataset (Fig. 6), illustrating that pronounced growth rate
500 changes are detectable using raw ¹⁴C data, and that, conversely, the model can
501 confirm stationary growth rates (e.g., as in NIED08-05). Future refinements to
502 the model could be made to fit the sections individually.

503

504 Additionally, and probably more importantly, the anchor point used in the model
505 ultimately affects chronological accuracy. If the anchor point lies in an interval
506 where the growth rate deviates considerably from its mean value, the resulting
507 chronology will over- or under-estimate actual ages. Anchor selection and
508 evaluation of the ¹⁴C data is therefore crucial. As shown for stalagmite HS4,
509 apparently small deviations of ln (a¹⁴C) data can result in substantial offset of the
510 final chronology, if not considered. Careful evaluation of potential anchor points
511 with respect to their representativity of the entire dataset prior to the modelling
512 procedure is therefore essential (Suppl. Fig. 2), and can help identify the best
513 possible option in cases where multiple anchor points are available.

514

515 The ¹⁴C data also highlight longer growth hiatuses, which complicate
516 chronological development for older (pre-hiatus) intervals and introduce very
517 large uncertainties. In the case of NIED08-05, mean pre-hiatus uncertainty is ±
518 1,354 years, essentially providing no chronological control except for a
519 qualitative indication of the general growth interval (i.e., the early Holocene).
520 Therefore, although the technique produces accurate chronologies for stalagmite
521 growth periods with independent anchor points, intervals below hiatuses are
522 currently problematic, and cannot be resolved quantitatively without an
523 additional independent anchor point (e.g. one accurate U-Th age). Other
524 geochemical information (e.g., Mg or δ¹³C) might provide useful constraints on
525 DCF independent of an anchor point, greatly reducing dating uncertainties below
526 hiatuses.

527

528 As high precision ^{14}C analysis requires much smaller sample sizes than U-Th
529 (especially for young samples), a combination of high-resolution ^{14}C
530 measurements and low-resolution U-Th measurements could provide a powerful
531 tool to develop precise chronologies that have the advantage of high
532 spatiotemporal resolution. This would allow determination of multiple anchor
533 points for the procedure, providing more robust chronologies. Although U-Th
534 remains the method of choice for high-precision dating of stalagmites, such a
535 combined method could provide a powerful additional tool for dating Holocene
536 stalagmites.

537

538 8. Refining the model: the potential for independent DCF estimation

539 Several studies illustrate that vegetation, soil, and hydrological conditions
540 modulate DCF (Genty et al., 2001; Griffiths et al., 2012; Noronha et al., 2014;
541 Oster et al., 2010; Rudzka et al., 2011; Rudzka-Phillips et al., 2013). Griffiths et al.
542 (2012) found strong similarities between DCF and both Mg/Ca and $\delta^{13}\text{C}$ values in
543 an Indonesian stalagmite from Liang Luar cave. Mg/Ca and $\delta^{13}\text{C}$ reflect karst
544 hydrological conditions and general hydroclimate (Johnson et al. 2006; Partin et
545 al. 2013; Stoll et al. 2012; Ridley et al. 2015), with drier conditions favouring
546 higher $\delta^{13}\text{C}$ and Mg/Ca values because of lower soil bioproductivity, increased
547 bedrock dissolution, enhanced degassing, and PCP (Johnson et al. 2006; Griffiths
548 et al. 2012; Tremaine & Froelich 2013). For Liang Luar cave and several other
549 sites, low recharge during dry periods promotes open system conditions (i.e.,
550 where water is in contact with an unlimited reservoir of soil CO_2) within the
551 karst, allowing drip water dissolved inorganic carbon (DIC) to re-equilibrate
552 with soil CO_2 and consequently lowering DCF. Conversely, closed system
553 conditions associated with wetter periods promote higher DCF due to
554 'waterlogging' of the karst leading to reduced exchange between drip water and
555 soil air (Fohlmeister et al., 2010; Griffiths et al., 2012).

556

557 Published Mg/Ca and $\delta^{13}\text{C}$ data from individual stalagmites often co-vary,
558 implying hydrological control on both parameters (Fig. 7). Independent DCF
559 estimation is theoretically possible on such stalagmites, due to the link between
560 Mg/Ca, $\delta^{13}\text{C}$, and DCF. Data from stalagmite HS4 (Heshang cave, China) (Hu et al.,

561 2008; Liu et al., 2013; Noronha et al., 2014) were used to investigate this
562 possibility. Because the original $\delta^{13}\text{C}$, Mg/Ca, and DCF were all sampled
563 individually and at different depths, the datasets were resampled and smoothed
564 to bring all parameters on the same timescale and reduce sampling bias. $\delta^{13}\text{C}$ and
565 Mg/Ca are significantly correlated ($r^2=0.68$), and smoothing markedly improves
566 the correlation ($r^2=0.91$, $p<0.001$). DCF and $\delta^{13}\text{C}$ are weakly correlated ($r^2=0.13$
567 for the original data; $r^2=0.29$, $p<0.001$, for smoothed data), and similarly DCF and
568 Mg/Ca ($r^2=0.21$, for the original data; $r^2=0.37$, $p<0.001$, for smoothed data).
569 Higher (lower) DCF values correspond to lower (higher) Mg/Ca and $\delta^{13}\text{C}$ values
570 (Fig. 8). However, other factors such as contributions from the soil/vegetation
571 system must drive a significant portion of the signal, impacting both $\delta^{13}\text{C}$ and
572 DCF (Fohlmeister et al., 2011; Oster et al., 2010).

573

574 Considering only karst processes, the distance of a coupled Mg/Ca- $\delta^{13}\text{C}$
575 measurement from the point of initial DIC (before the start of limestone
576 dissolution) should reflect DCF (Fig. 8). When applied to the HS4 dataset, this
577 approach estimates DCF moderately well, although the amplitude of variation in
578 the modelled results is much lower than measured, due to the smoothing of the
579 $\delta^{13}\text{C}$ and Mg/Ca datasets (Suppl. Fig. 3). However, DCF varies considerably
580 depending on cave and climatic settings (Genty et al. 1999), so that DCF from a
581 single stalagmite (e.g., HS4) cannot be used to calibrate samples from other
582 locations. Available published data suggest that very different and sample-
583 specific relationships between DCF and $\delta^{13}\text{C}$ exist, and no clear pattern related to
584 climate or cave settings is apparent (Suppl. Fig. 4). However, many of the
585 available datasets are limited in size, and the relationships presented are not
586 statistically significant.

587

588 These results illustrate that constraining DCF via Mg/Ca, and $\delta^{13}\text{C}$ data is
589 potentially attainable, but the underlying processes and the interdependencies
590 between parameters remains elusive. The lack of available data at sufficiently
591 high resolution and in many cases sampling bias, such as not measuring all
592 proxies on the same aliquot of powder, contribute to the uncertainty. Although

593 the paucity of robust datasets precludes reaching any firm conclusions with
594 respect to these observations, our work and previous studies on DCF and soil-
595 cave carbon transfer (e.g. Genty et al., 2001; Rudzka et al., 2011; Rudzka-Phillips
596 et al., 2013) suggest that climate does influence DCF. Tropical sites where
597 temperature is high throughout the year but rainfall is very seasonal (e.g., Liang
598 Luar cave) might produce different DCF responses than temperate sites where
599 both rainfall and temperature may vary seasonally (e.g., Niedźwiedzia cave). It is
600 likely that specific climate conditions at a cave site result in a continuum of
601 systems between tropical and temperate end members, resulting in different
602 DCF- $\delta^{13}\text{C}$ relationships.

603

604 9. Correcting the chronology for DCF variations

605 Our model estimates DCF, which can help adjust the final chronology for subtle
606 offsets from the constant growth trend. The residual DCF (i.e., the deviation of
607 each calculated DCF data point from the mean DCF) is used to calculate the
608 correction in years for each data point (using the modeled ages). These
609 corrections are applied to the modelled chronology, resulting in an “DCF
610 corrected” chronology that is compatible with existing chronology development
611 software (e.g., COPRA (Breitenbach et al., 2012), StalAge (Scholz and Hoffmann,
612 2011)). Dating uncertainty is comprised by the modelling uncertainty plus the
613 DCF estimation error. Applying this correction to the modelled HS4 chronology
614 reproduces long-term trends apparent in the U-Th based chronology (Fig. 9a and
615 b). The correction does introduce some age reversals, particularly in the older
616 and highly resolved intervals of HS4; the chronology was therefore
617 downsampled to remove inversions prior to COPRA treatment.

618

619 The model can reliably estimate DCF (Fig. 4c), suggesting that a common process
620 controls both growth rate and DCF, possibly recharge conditions. Growth rate
621 and DCF in stalagmite HS4 appear weakly anti-correlated ($r^2 = 0.14$), and it is
622 possible that elevated rainfall at the Heshang cave site encourages closed-system
623 conditions and increased DCF, while simultaneously reducing the DIC of the
624 percolation water and stalagmite growth rate. We emphasise that although the
625 model appears to yield reasonable DCF estimates, the reasons why DCF is linked

626 to growth rate are unclear. Furthermore, although the DCF correction appears to
627 work for HS4, its applicability to non-monsoonal sites where temperature may
628 play a larger role in DCF determination is unknown. We present a provisional
629 DCF-corrected chronology for NIED08-05, but emphasise that whether the
630 relationship observed in HS4 is transferrable to NIED08-05 is not known.
631 Despite these uncertainties, the DCF corrected NIED08-05 chronology shows
632 only very minor differences to the uncorrected chronology, consistent with the
633 stationary $\delta^{13}\text{C}$ and the stable, slow growth rate of the sample.

634

635 10. Summary and conclusions

636 This study describes a novel approach to develop chronologies for stalagmites
637 using ^{14}C . The model introduced estimates the average growth rate of a
638 stalagmite from ^{14}C ages, taking into account past variations in atmospheric ^{14}C ,
639 and anchors the chronology to a point of known age. The model does not require
640 DCF estimation, which is advantageous considered that DCF remains an
641 enigmatic parameter with respect to its influencing factors. Application of the
642 model on a U-Th dated stalagmite, a synthetic dataset, and a stalagmite without a
643 U-Th chronology, demonstrates that this method produces reliable chronologies
644 provided the sample's long-term growth rate was regular and DCF was
645 stationary. The choice of the anchor point is crucial and ultimately defines
646 chronological accuracy. This currently leads to two main issues:

647

648 • Deviations from the long-term growth rate close to the anchor point will
649 lead to chronological bias, as illustrated in the case of stalagmite HS4.
650 However, measured ^{14}C ages, particularly when highly resolved, can
651 reveal potentially anomalous growth rate shifts, and justify anchor point
652 selection.

653

654 • Depositional hiatuses result in very large chronological uncertainty in the
655 pre-hiatus interval of stalagmite growth, if no independent anchor point
656 exists. The magnitude of the error (>1000 yr) results in virtually no
657 chronological control for those intervals, and provides only qualitative
658 information.

659

660 Future work may overcome these limitations, possibly by coupling the approach
661 described here with other lines of geochemical information (e.g., Mg/Ca and $\delta^{13}\text{C}$
662 data) that may provide independent constrains on DCF. Although still being less
663 precise than dating using the U-Th method, this current model as presented
664 provides chronologies for stalagmites meeting certain criteria, and represents a
665 useful alternative in cases where more established techniques are not applicable,
666 or in combination with U-Th dating.

667

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- 865
- 866 Figure captions:

867 **Figure 1:** Map of Niedźwiedzia Cave and location of the cave in SW Poland (insert). The
868 stalagmite NIED08-05 sampling location is indicated in red.

869

870 **Figure 2:** Results of the ^{14}C analysis on stalagmite NIED08-05. A: ^{14}C ages vs. depth from graphite
871 analysis are shown in black; error bars denote 1σ errors. A scan of the stalagmite is shown on the
872 far right, including indication of the sampling locations for ^{14}C and the location of the hiatus. B:
873 results of high-resolution GIS measurements for ^{14}C across the top 1mm of stalagmite NIED08-
874 05. Four different tracks were milled and analysed (shown in different colors and symbols), the
875 average of all tracks is shown in black. Three of four profiles show a significant increase in ^{14}C
876 in the top 0.5 mm, indicating the presence of bomb carbon and confirming recent growth of
877 NIED08-05.

878 **Figure 3:** Flowchart illustrating the modelling steps in MATLAB for the construction of
879 chronologies using ^{14}C . Small figures show some key steps in the modelling procedure. A)
880 Conceptual figure illustrating the exponential decay pattern in measured ^{14}C data, a prerequisite
881 for the successful construction of an age model. B) Calibration of pre-hiatus ages (when no
882 independent anchor point is available). The growth rate line (red line) is positioned at the
883 youngest of all calibrated ages and then shifted through time until the best fit (i.e. point with
884 highest probability for all ages) is found. 95% confidence intervals from calibration and DCF
885 estimation are shown in light pink. C) While shifting the line through the probabilities, a new
886 probability density distribution is established with respect to the youngest position, which
887 reaches convergence after a few iterations of the model. The weighted mean (red line) of the
888 probability density distribution is determined and used to find the best placement of the growth
889 rate.

890 **Figure 4:** Modelling results for stalagmite HS4 from Heshang Cave, China. A: published age-depth
891 relationship derived from the U-Th age model (black line), with 95% confidence bounds in grey
892 (Hu et al., 2008; Noronha et al., 2014). Blue symbols show the measured, uncorrected and
893 uncalibrated ^{14}C ages (Noronha et al., 2014). The red line indicates the age model derived from
894 ^{14}C using the anchor point at 43 cm from top, with 95% confidence interval (this study). The
895 dashed blue line is the modelled growth rate that would result if the anchor point was placed at
896 the 24.6 cm from top (beginning of the ^{14}C dataset), where the actual growth rate deviates from
897 the long-term mean (and ^{14}C ages are anomalous). This anchor point would result in a less
898 accurate chronology, due to the bias from the ^{14}C ages. B: Expanded view of the top of the HS4
899 age model. The anchor point (fourth ^{14}C age, 43 cm from top) is indicated. C: DCF vs. depth plot.
900 The black line indicates DCF derived from U-Th ages, the red line shows the DCF derived from
901 our model anchored at 43 cm from top, and the blue dashed line is the modelled DCF using the
902 anchor point at 24.6 cm from top.

903

904 **Figure 5:** Chronology developed for stalagmite NIED08-05 from Niedźwiedzia Cave, Poland. Blue
905 symbols show the measured ^{14}C ages (25 from graphite AMS analysis and one additional from
906 GIS analysis averaging all measurements taken at 0.3 mm from top), and the anchor point used
907 (2008 = year of collection). The red line indicates the best fitting growth rate derived from the
908 presented model, with 95% confidence intervals. The depositional hiatus at 51.5 mm depth is
909 marked by the grey dashed line. Very large age uncertainties in the pre-hiatus interval (due to
910 the lack of an independent anchor point), result in this being only a qualitative chronology. It is
911 also apparent that the uncertainty estimates for the pre-hiatus chronology are conservative,
912 since most measured ^{14}C ages are younger than the maximum error. This problem could be
913 solved by applying a stalagmite-specific threshold for the uncertainty, so that the resulting
914 modelled chronology is younger than the measured ^{14}C ages (not shown).

915 **Figure 6:** In ($a^{14}\text{C}$)-depth relationships for stalagmite HS4 (blue diamonds), NIED08-05 (red
916 squares) and a synthetic dataset showing a large and prolonged change in growth rate (grey
917 crosses). The change in growth rate is clearly visible as a change in the slope of the synthetic
918 dataset. This shows that major changes in growth rate can be detected in stalagmites with the
919 procedure described in this study, and corroborates our assumption that NIED08-05 experienced
920 relatively constant growth rates and is a suitable sample for the method described in this study.

921

922 **Figure 7:** Compilation of Mg/Ca vs. $\delta^{13}\text{C}$ relationship for published stalagmite datasets from
923 different cave systems. Abbreviations indicate the cave system: NIED- stalagmite NIED08-05,
924 Niedźwiedzia cave, Poland, (this study); CC – Stalagmite CC-Bil, Crag cave, Ireland (McDermott et
925 al., 1999); PNC – stalagmite PN95, Pere Noel cave, France (Verheyden et al., 2000); BF – Brown's
926 Folly mine, England (Baldini et al., 2005); BR – flowstone RL-4, Buca della Renella, Italy (Drysdale
927 et al., 2006); HC – stalagmite HS4, Heshang cave, China (Hu et al., 2008; Liu et al., 2013); LLC –
928 stalagmite LR06-B1, Liang Luar cave, Indonesia (Griffiths et al., 2010). The regression lines
929 showing the best fit are shown for each stalagmite, highlighting different Mg/Ca vs. $\delta^{13}\text{C}$
930 relationships depending on dripwater degassing rate, as described by Johnson et al. (2006).

931 **Figure 8:** Relationships between $\delta^{13}\text{C}$, Mg/Ca and DCF in stalagmite HS4 from Heshang cave,
932 China (Hu et al., 2008; Liu et al., 2013; Noronha et al., 2014). DCF decreases with increasing $\delta^{13}\text{C}$
933 and Mg/Ca, and could theoretically be quantified this way.

934

935 **Figure 9:** A) Offset corrected chronology for stalagmite HS4. Measured ^{14}C ages (blue) are
936 compared to the U-Th chronology (black) and to the final corrected ^{14}C -derived chronology (red,
937 uncertainty in pink). B) Detail of the HS4 chronology. C) Offset corrected chronology for
938 stalagmite NIED08-05. Measured ^{14}C ages (blue) and final corrected ^{14}C -derived chronology (red,
939 uncertainty in pink) are shown.

940

941

942 **Suppl. Figure 1:** A) $\delta^{13}\text{C}$ record for stalagmite NIED08-05. The dashed grey line indicates mean
943 $\delta^{13}\text{C}$, the black line is the linear trendline of the dataset. Variation in $\delta^{13}\text{C}$ is relatively small
944 (average: -7.48‰, σ : 1.17), and there is only a negligible long-term trend in the dataset,
945 corroborating the assumption that variations in DCF were small as well. B) High resolution laser
946 ablation Mg/Ca record for NIED08-05. Black dots indicate the position of ^{14}C ages. The dashed
947 grey line shows the location of the hiatus at the local maximum Mg/Ca value. The gradual
948 increase in Mg/Ca, followed by a sharp decrease back to baseline values is interpreted as
949 increasingly dry conditions and enhanced PCP, followed by a growth stop until water started
950 flowing again (with lower Mg/Ca). Therefore, the exact depth of the hiatus in NIED08-05 is
951 placed at 51.5 mm from top.

952

953 **Suppl. Figure 2:** Detrended $\ln(a^{14}\text{C})$ data for stalagmites NIED08-05 and HS4 highlighting the
954 importance of $a^{14}\text{C}$ values representative of the entire dataset at the anchor point. The top panel
955 shows $\ln(a^{14}\text{C})$ values for NIED08-05, including the mean and standard deviation. It is apparent
956 that the top $a^{14}\text{C}$ value lies within the stalagmites 1σ boundary, justifying the choice of the anchor
957 point at the top of the sample. In the lower panel, $\ln(a^{14}\text{C})$ values, their mean and standard
958 deviation for stalagmite HS4 are shown. The top three $\ln(a^{14}\text{C})$ values are anomalous (outside of
959 1σ boundaries) and will therefore result in a chronological bias if used. The fourth $\ln(a^{14}\text{C})$ value,
960 however, is within the 1σ boundaries and can be used. This procedure should always be applied
961 as a quality control for the chronology, and could greatly help in choosing the best anchor point if
962 multiple possible anchors exist.

963

964 **Suppl. Figure 3:** Example of DCF modelling using Mg/Ca vs. $\delta^{13}\text{C}$ from stalagmite HS4, Heshang
965 cave (Hu et al., 2008; Liu et al., 2013; Noronha et al., 2014), and re-applying the relationship on
966 the same stalagmite. DCF calculated from U-Th chronology (blue line) and DCF estimated from
967 the Mg/Ca vs. $\delta^{13}\text{C}$ relationship (red line) are shown. It is apparent that DCF variations can be
968 modelled to a certain extent using this approach; however, the estimated DCF is strongly muted
969 with respect to the actual DCF, due to the smoothing processes prior to the modelling. At present,
970 this approach cannot be widely applied to stalagmites with unknown DCF, as the Mg/Ca vs. $\delta^{13}\text{C}$ -
971 DCF relationship is cave-specific and difficult to quantify for the general case.

972

973 **Suppl. Figure 4:** Compilation of DCF vs. $\delta^{13}\text{C}$ relationships for published datasets from different
974 caves. Positive correlation (red symbols): HC - stalagmite HS4, Heshang cave, China (Hu et al.,
975 2008; Noronha et al., 2014); LGC - stalagmite GAR-01, La Garma cave, Spain (Rudzka et al., 2011);
976 VC - stalagmite Vil-stm1, Villars cave, France (Genty et al. 1999); SOC - stalagmite So-1, Sofular
977 cave, Turkey (Rudzka et al., 2011); Negative correlation (blue symbols): HSLC - stalagmites Han-
978 stm1 and Han-stm5, Han-sur-Lesse cave, Belgium (Genty et al., 1999, 1998); UTC - stalagmites
979 SU-2, SU-96-1, SU-96-7, Uamh-an-Tartair cave, Scotland (Genty et al., 2001); SC - stalagmite Sal-
980 stm1, Salamandre cave, France (Genty et al., 2001); no correlation (green symbols): MC -

981 stalagmite MC3, Moaning cave, California (Oster et al., 2010); LLC - stalagmite LR06-B1, Liang
982 Luar cave, Indonesia (Griffiths et al., 2012); EPC - stalagmite Candela, El Pindal cave, Spain
983 (Rudzka et al., 2011); HUC - stalagmite H-82, Hulu cave, China (Southon et al., 2012). High p-
984 values for most of the correlations indicate their low significance, and therefore most of these
985 relationships should be carefully evaluated. Datasets with more paired DCF- $\delta^{13}\text{C}$ measurements
986 could help improve our understanding of the governing factors for both proxies at specific sites
987 and regionally/globally.

988

989 **Table 1:** Results from the high precision graphite AMS ^{14}C analysis for stalagmite NIED08-05.

990

991 **Suppl. Table 1:** Results from the high-resolution tracks of the top 1 mm of stalagmite NIED08-05.
992 Analyses were conducted using a Gas Ion Source (GIS).

993