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Bottom-quark effects in Higgs production at intermediate transverse momentum

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ABSTRACT: We provide a precise description of the Higgs boson transverse momentum distribution including top and bottom quark contributions, that is valid for transverse momenta in the range $m_b \leq p_{\perp} \leq m_t$, where m_b and m_t are the bottom and top quark masses. This description is based on a combination of fixed next-to-leading order (NLO) results with next-to-next-to-leading logarithmic (NNLL) transverse momentum resummation. We show that ambiguities in the resummation procedure for the *b*-quark loops are of the same order as the related fixed-order uncertainties. We conclude that the current uncertainty in the top-bottom interference contribution to the Higgs transverse momentum spectrum is $\mathcal{O}(20\%)$.

KEYWORDS: NLO Computations, QCD Phenomenology

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1 Introduction

Understanding the Higgs particle observed at the LHC requires studies of its properties that include quantum numbers and couplings to gauge and matter fields. Current experimental results have relatively small $\mathcal{O}(10\% - 20\%)$ uncertainties in Higgs couplings to electroweak gauge bosons and larger $\mathcal{O}(100\%)$ uncertainties in Higgs Yukawa couplings, especially for light quarks [1]. However, it is quite conceivable that physics beyond the Standard Model manifests itself in smaller, few percent, contributions to Higgs couplings. Thus, facilitating further improvements in extracting Higgs couplings to gauge bosons and helping constrain Yukawa couplings are very important issues in contemporary Higgs physics.

Both of these issues can, at least partially, be addressed by improving the description of Higgs boson production in gluon fusion. Indeed, since $gg \to H$ is the main production mechanism of Higgs bosons at the LHC, a refined understanding of this process in QCD perturbation theory will lead to an improved understanding of fiducial cross sections and, eventually, will allow for a better extraction of various Higgs couplings constants from e.g. Higgs decays to bosonic final states.

Although the contributions of bottom and charm loops to the ggH coupling and direct production of a Higgs boson in quark fusion $q\bar{q} \rightarrow H$, $q \in \{c, b\}$ are small in the Standard Model, if the Yukawa couplings differ from their Standard Model values, these light-quark effects in Higgs production become much more important. In fact, it was pointed out [2, 3] that studies of kinematic distributions of Higgs bosons produced in hadron collisions may lead to interesting constraints on light quark Yukawa couplings, especially at the highluminosity LHC. A particularly important and highly non-trivial kinematic distribution is the Higgs boson transverse momentum spectrum. At the LHC, Higgs bosons are produced with very different transverse momenta, from very small to very large; the p_{\perp} distribution peaks at $p_{\perp} \approx 15$ GeV. Depending on the value of the Higgs transverse momentum, the p_{\perp} distribution is sensitive to different physics, from multiple emissions of soft gluons at small p_{\perp} to top quark mass effects at the tail of the spectrum. The difficulty in describing the Higgs transverse momentum distribution as a whole is related to this point.

Higgs production in gluon fusion receives contributions from top and light-quark loops. Since Yukawa couplings are proportional to quark masses, top quark loops play the dominant role. For values of the transverse momenta $p_{\perp} \lesssim m_t$, top loops can be treated in the $m_t \to \infty$ approximation. This leads to enormous technical simplifications since, essentially, it allows us to "remove" one loop from the computations that involve the ggH vertex. As the result, the $m_t \to \infty$ approximation allowed for the computation of next-to-next-tonext-to-leading order (N³LO) QCD corrections to the inclusive cross section and basic kinematic distributions [4–6], as well as next-to-next-to-leading order (NNLO) QCD corrections to the production of Higgs bosons in association with one jet [7–11]. It is also quite straightforward to compute the $\mathcal{O}(1/m_t)$ corrections to the $m_t \to \infty$ approximation; they are available for the total cross section [12–14] and for the Higgs p_{\perp} distribution [15–17]. NLO QCD corrections including the top-quark dependence in the full Standard Model have become available recently either via a high-energy expansion [18, 19] or a direct numerical calculation [20] of the relevant two-loop virtual amplitudes.

When small transverse momenta $p_{\perp} \ll m_H$ are considered, radiative corrections to Higgs production become enhanced by large logarithms $\ln m_H/p_{\perp}$. It is possible to resum these logarithms in case of Higgs production in gluon fusion if the ggH coupling is pointlike, which is the case in the $m_t \to \infty$ approximation. Such resummations were performed with ever increasing accuracy through the years [21–24]. The necessary ingredients to compute the next-to-next-to-leading logarithmic (N³LL) corrections, apart from the four-loop cusp anomalous dimension, were obtained in refs. [25–28]. This allowed for a description of the Higgs boson p_{\perp} spectrum at N³LL+NNLO [29].¹

Resummed computations are usually extrapolated from small transverse momenta, where they are valid, to large momenta, where they are matched to fixed-order computations. As we explained in the previous paragraphs, the accuracy of both resummed and fixed-order computations has been constantly increasing; as a result, the $m_t \to \infty$ top-loop mediated contribution to the Higgs transverse momentum distribution is currently known with a precision of about 10 - 15 percent for all values of the Higgs p_{\perp} [7–11, 29].

Having reached this level of understanding in the $m_t \to \infty$ limit, it is essential to ask if additional small effects, that could have been neglected previously, need to be accounted for at the present level of accuracy and, if so, if they are sufficiently well understood. Examples of such contributions are corrections to the ggH interaction vertex due to light quarks and electroweak corrections to the Higgs transverse momentum distribution. Both of these effects appear at the one-loop level; light-quark contributions change the Higgs

¹The numerical impact of the four-loop cusp anomalous dimension is expected to be small [30].

boson transverse momentum distribution by about -5%. For moderate values of transverse momenta, electroweak contributions to the Higgs p_{\perp} spectrum are smaller [31] and we neglect them in what follows.

Since QCD corrections in $gg \to H$ are known to be large for the top quark contribution, it becomes important to understand if a similar enhancement exists for light quark contributions as well. Unfortunately, such computations require two-loop calculations with massive internal particles that are currently hardly feasible. An alternative possibility is to compute the corresponding two-loop amplitudes in the approximation where all kinematic variables and the mass of the Higgs boson are considered large relative to the quark mass m_q . In this case, one computes a two-loop amplitude as an expansion in m_q^2/m_H^2 , m_q^2/s , m_q^2/p_{\perp}^2 . In this approximation, the relevant amplitudes have been computed in refs. [32, 33]. For b-quark loops, such an expansion is valid for transverse momenta larger than $\mathcal{O}(10-20)$ GeV since corrections to the approximate result for two-loop amplitudes scale like $(m_b/p_{\perp})^2 \sim 0.2$ for $p_{\perp} = 10$ GeV.

Light-quark contributions develop a peculiar double-logarithmic dependence on the light quark masses $\ln^2(m_H/m_q), \ln^2(p_\perp/m_q)$. Such dependences originate from soft quark exchanges in the loops that facilitate the ggH couplings. For the processes $gg \rightarrow H + g, qg \rightarrow Hq$ and $q\bar{q} \rightarrow H + g$ these terms are sensitive to gluons emitted from both "inside" and "outside" the loops at finite transverse momentum, i.e. to the structure-dependent radiation.

Light-quark contributions to Higgs production in gluon fusion make the resummation of the transverse-momentum distribution difficult [34, 35]. Indeed, since both top and bottom quark loops contribute to the ggH coupling and since these loops are characterized by very different intrinsic scales for the structure-dependent radiation (m_b and m_t), it appears that one will have to treat them differently. However, this is not possible since the dominant contribution is given by the interference of the two amplitudes. In addition, since it is not understood how to resum the potentially large logarithms $\log(p_{\perp}/m_b)$ that appear in the light-quark loops, it becomes impossible to treat all the different contributions to the Higgs p_{\perp} spectrum on the same footing. The best thing that one can do is to employ a variety of prescriptions for combining light quark contributions with small- p_{\perp} resummations and to study how the resulting uncertainty in predictions compares with other sources of theoretical error.

The goal of this paper is to study the Higgs p_{\perp} spectrum including top and bottomquark contributions at next-to-leading order combined with next-to-next-to-leading logarithmic transverse momentum resummation (NLO+NNLL). A similar study at leading order combined with next-to-leading logarithmic resummation (LO+NLL) was performed in ref. [34].² To this end, we include the recently computed NLO QCD corrections to light-quark contributions to Higgs production in gluon fusion [32, 33, 36]. We find that the uncertainty in our matched NLO+NNLL result for the top-bottom interference contribution to the Higgs transverse momentum distribution in the region 10 GeV $\leq p_{\perp} \leq 100$ GeV

²Note that this was referred to as NLO+NLL in this reference, while we always use the formal accuracy of the differential distribution for the fixed order. In the notation of ref. [34] our result would be NNLO+NNLL.

is dominated by ambiguities in the perturbative description of light-quark loops rather than by uncertainties in the resummation itself. In particular, we do not find large uncertainties related to the choice of the resummation scale for the *b*-quark loops.

The paper is organized as follows. In section 2 we briefly review the structure of small- p_{\perp} resummation for the case of point-like interactions, and elucidate its main assumptions and limitations. We also study light-quark contributions, discuss why in this case the resummation is challenging and describe a possible pragmatic solution to this problem. In section 3, we explain the implementation of the resummation procedure for the *b*-quark contribution and study its ambiguities, and we present our main results for the Higgs transverse momentum distribution. We conclude in section 4. Some useful formulas and derivations are collected in the appendix.

2 Resummation of the Higgs transverse momentum distribution

2.1 The standard point-like case

We would like to describe the transverse momentum distribution of Higgs bosons produced in hadron collisions. This is non trivial and requires a combination of fixed order and resummed perturbative calculations. Indeed, depending on the value of the Higgs boson transverse momentum, we can distinguish two regions. For large values of transverse momenta $p_{\perp} \sim m_H$, one can compute $d\sigma/dp_{\perp}$ in a perturbative expansion in α_s following standard rules of perturbative Quantum Field Theory. For small values of the transverse momentum $p_{\perp} \ll m_H$, the situation is different since emerging large logarithms $\ln(p_{\perp}/m_H) \gg 1$ may compensate the smallness of the strong coupling constant, $\alpha_s \ln^2(p_{\perp}/m_H) \sim 1$, and spoil a conventional perturbative expansion. To deal with this case, one resums the logarithmically enhanced terms to all orders in the coupling constant, and develops a perturbative expansion on top of the resummed result.

Since, eventually, we need to describe the Higgs boson p_{\perp} distribution for all values of transverse momenta, the two distinct approaches — resummation and fixed order computations — have to be combined. This is done by smoothly interpolating between results derived at small and large p_{\perp} . The region where the transition happens is characterized by a quantity that we refer to as the resummation scale Q. This scale has the following physical meaning: for $p_{\perp} \lesssim Q$, the transverse momentum distribution is mostly described by the resummed result, while for $p_{\perp} \gtrsim Q$ it is mostly described by the fixed order computation.

In order to discuss these concepts more precisely, we consider the all-order resummation in a toy model, where we work at leading-logarithmic (LL) accuracy. To this end, we consider the cumulative distribution

$$\Sigma(p_{\perp}) = \int_0^{p_{\perp}} \mathrm{d}p'_{\perp} \, \frac{\mathrm{d}\sigma}{\mathrm{d}p'_{\perp}}.$$
(2.1)

At low p_{\perp} , we resum the logarithms of $\ln p_{\perp}/m_H$ and write

$$\Sigma(p_{\perp}) = \Sigma^{\text{resum}}(p_{\perp}), \quad p_{\perp} \ll m_H.$$
(2.2)

In this region, the distribution is dominated by the emission of soft and collinear partons. In the LL approximation it is sufficient to consider the most singular contribution to the QCD matrix elements, where all final-state partons are soft and strongly ordered in angle. In this limit, the squared matrix element for the emission of n extra partons $gg \to H + n$ is given by the product of the matrix element for $gg \to H$ times n independent eikonal factors. More specifically, at LL the partonic p_{\perp} distribution

$$\frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}p_{\perp}} = [dp_H] \left(\prod_{i=1}^n [dk_i] \right) |\mathcal{M}(p_1 + p_2 \to H + n)|^2 \\ \times \delta^{(4)} \left(p_1 + p_2 - p_H - \sum_{i=1}^n k_i \right) \delta \left(p_{\perp} - |\sum_{i=1}^n \vec{k}_{\perp i}| \right)$$
(2.3)

can be simplified as

$$\frac{d\hat{\sigma}}{dp_{\perp}} \simeq [dp_H] |\mathcal{M}(p_1 + p_2 \to H)|^2 \delta^{(4)}(p_1 + p_2 - p_H) \\ \times \frac{1}{n!} \prod_{i=1}^n [dk_i] |M_{\text{soft}}(k_i)|^2 \delta\left(p_{\perp} - |\sum_{i=1}^n \vec{k}_{\perp i}|\right),$$
(2.4)

where $[dk_i]$, $[dp_H]$ are the phase space volumes of the *i*-th parton k_i and the Higgs boson, and M_{soft} is the matrix element of the single-emission eikonal current. Note that the *reduced* matrix element $\mathcal{M}(p_1 + p_2 \to H)$ is evaluated at zero transverse momentum.³

Starting from eq. (2.4) it is possible to show (for details see appendix A) that the resummed cross section takes the form

$$\Sigma^{\text{resum}}(p_{\perp}) = \sigma_0 e^{-\int [dk] |M_{\text{soft}}(k)|^2} \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=1}^n \int [dk_i] |M_{\text{soft}}(k_i)|^2 \Theta\left(p_{\perp} - |\sum_{i=1}^n \vec{k}_{\perp i}|\right), \quad (2.5)$$

where σ_0 is the Born cross section for $gg \to H$. The overall exponential factor contains the all-order effects of soft-collinear virtual gluons which are encoded in the leading divergence of the gluon form factor $\mathcal{M}(p_1 + p_2 \to H)$.⁴ The distribution in the small p_{\perp} region is governed by two competing mechanisms. In the strict limit $p_{\perp} \to 0$, the dominant contribution comes from emissions with finite transverse momentum $p_{\perp} \ll k_{\perp i} \ll m_H$ that mutually cancel in the transverse plane. This collective effect gives rise to a power suppressed scaling [37]

$$\Sigma(p_{\perp}) \sim \mathcal{O}(p_{\perp}^2). \tag{2.6}$$

As p_{\perp} increases, but still remains small compared to m_H , the distribution is described by kinematic configurations with $p_{\perp} \sim k_{\perp i} \ll m_H$. As discussed in appendix A.1, in this region the cumulative distribution features an exponential suppression of the form

$$\Sigma(p_{\perp}) \sim \sigma_0 \exp\left\{-\bar{\alpha}\ln^2\frac{m_H}{p_{\perp}}\right\},$$
(2.7)

where $\bar{\alpha} = 2C_A \alpha_s / \pi$.

³This is valid at all logarithmic orders.

 $^{^{4}}$ Clearly, all integrals in eq. (2.5) are divergent in the soft and collinear limits, and require regularization. However, the final result eq. (2.5) does not depend on the regularization procedure.

At larger transverse momenta $(p_{\perp} \sim m_H)$ the approximation that led to eq. (2.5) is not justified anymore. Therefore, in this region one has to smoothly switch from the resummed prediction to the fixed-order one, where the effect of the hard radiation is treated correctly. This can be done for example using the following matching formula

$$\Sigma(p_{\perp}) = \Sigma^{\text{resum}}(p_{\perp}) + \left(\Sigma^{\text{f.o.}}(p_{\perp}) - \mathcal{T}^{\text{f.o.}}\left[\Sigma^{\text{resum}}(p_{\perp})\right]\right), \qquad (2.8)$$

where we indicate with $\mathcal{T}^{\text{f.o.}}[f]$ the fixed-order expansion of f. At small p_{\perp} the difference between the fixed-order result and the Taylor expansion of the resummed result is free of logarithmically-enhanced terms

$$\lim_{p_{\perp} \to 0} \left(\Sigma^{\text{f.o.}}(p_{\perp}) - \mathcal{T}^{\text{f.o.}}[\Sigma^{\text{resum}}(p_{\perp})] \right) = \text{const.}$$
(2.9)

This allows one to extend the fixed-order description to $p_{\perp} \rightarrow 0$ and, at the same time, ensures that all terms that contain large logarithms at low p_{\perp} are resummed.

The precise way to switch from the resummation to the fixed-order description is ambiguous. One source of ambiguity comes from choosing a particular form for the matched cross section (in our example, eq. (2.8), we chose to combine the resummed and fixed-order predictions additively). A second source of ambiguity is connected with the scale at which the transition from resummed to fixed-order result takes place. Although all of these effects are formally of higher-order both in the resummation and fixed-order counting, their numerical impact can be non-negligible. We consider the latter issue in what follows, while leaving a discussion of the choice of the matching scheme to the next section.

In order to switch off resummation effects at large p_{\perp} , one can modify the resummed cross section by including controlled power-suppressed corrections. One possible way to do this is to modify the resummed logarithms in eq. (2.7) as follows⁵

$$L \equiv \ln \frac{m_H}{p_\perp} = \ln \frac{m_H}{Q} + \ln \frac{Q}{p_\perp}, \qquad (2.10)$$

where Q is an arbitrary scale of order m_H . Moreover, we write

$$\ln \frac{Q}{p_{\perp}} \to \frac{1}{p} \ln \left(\left(\frac{Q}{p_{\perp}} \right)^p + 1 \right) \equiv \tilde{L}, \qquad (2.11)$$

where p is a positive number. The motivation for the transformations described above is as follows:

• First, we split the resummed logarithm L into the sum of a small logarithm $\ln(m_H/Q)$ (with $Q \sim m_H$) and a large logarithm $\ln(Q/p_{\perp})$. This operation allows us to introduce a generic scale Q which then appears in the resummed result. We can now expand L around $\ln(Q/p_{\perp})$, retaining all terms with the desired logarithmic accuracy. Effectively, this implies that $\ln(m_H/Q)$ is treated perturbatively at fixed order.

⁵A more correct prescription is to modify the logarithms $\ln(m_H/k_{\perp 1})$ where $k_{\perp 1}$ is the transverse momentum of the hardest emitted gluon. This technicality is avoided here for the sake of clarity, and it will be discussed in appendix A.

In our LL example, for $p_{\perp} \sim k_{\perp i} \ll m_H$, this means

$$\Sigma^{\text{resum}}(p_{\perp}) \sim e^{-\bar{\alpha}L^2} = \exp\left\{-\bar{\alpha}\left[\ln^2\frac{Q}{p_{\perp}} + 2\ln\frac{Q}{p_{\perp}}\ln\frac{m_H}{Q} + \ln^2\frac{m_H}{Q}\right]\right\}$$
$$= \exp\left\{-\bar{\alpha}\ln^2\frac{Q}{p_{\perp}} + \mathcal{O}\left(\alpha_s L\right)\right\}\left(1 - \bar{\alpha}\ln^2\frac{m_H}{Q} + \mathcal{O}(\alpha_s^2)\right)$$
$$\simeq \exp\left\{-\bar{\alpha}\ln^2\frac{Q}{p_{\perp}}\right\},$$
(2.12)

where all terms beyond LL were neglected. This prescription is convenient because the Q-dependence is always of higher-logarithmic order and, therefore, a Q-variation probes the size of subleading logarithms that are not considered in the resummation.

• Second, we modify the logarithm $\ln(Q/p_{\perp})$ by including power-suppressed terms that force \tilde{L} to vanish at large p_{\perp} . These modifications do not affect the small- p_{\perp} limit. Indeed, it follows from eq. (2.11) that

$$\tilde{L} \sim \ln \frac{Q}{p_{\perp}}, \text{ for } p_{\perp} \ll Q; \qquad \tilde{L} \sim \frac{1}{p} \left(\frac{Q}{p_{\perp}}\right)^{p}, \text{ for } p_{\perp} \gg Q.$$
(2.13)

As a consequence, the resummation scale Q and the scaling parameter p must be chosen in such a way that the high- p_{\perp} scaling of the resummed component (and its fixed-order expansion) does not modify the scaling of the fixed-order prediction. This means that p and Q are to be chosen in such a way that the resummed component vanishes more quickly than the fixed-order result for $p_{\perp} \gtrsim Q$.

The above discussion shows that Q is indeed the scale at which the transition between resummed and fixed-order results occurs. Similarly to the renormalization and factorization scales, its choice is ambiguous, although certain conditions should be satisfied. Indeed, it is clear that (a) Q should not be too different from m_H , to ensure that $\ln Q/m_H$ are not large and (b) it should approximately correspond to the scale at which the soft and collinear approximations to the matrix element and kinematics break down. In practice, one can choose Q by comparing the exact result $\Sigma^{\text{f.o.}}$ with the expansion of the resummed result $\mathcal{T}^{\text{f.o.}}[\Sigma^{\text{resum}}]$, and set Q to the p_{\perp} scale at which the two start to significantly deviate from each other. This is illustrated in figure 1, which shows the difference between the LO differential p_{\perp} spectrum and the expansion of the resummed result at the same order. Specifically, we plot

$$\left| \left(\frac{d\sigma^{\rm LO}}{dp_{\perp}} - \mathcal{T}^{\rm LO} \left[\frac{d\sigma^{\rm resum}}{dp_{\perp}} \right] \right) \middle/ \frac{d\sigma^{\rm LO}}{dp_{\perp}} \right|.$$
(2.14)

We observe that when only the top contribution is included (solid, red curve), the logarithmic terms account for about half of the fixed-order result at scales $p_{\perp} \sim 50-60$ GeV. This suggests that the resummation scale should be of this order. We conventionally choose $Q = m_H/2$ as a central value. As far as the choice of the parameter p is concerned, we have to ensure that at large p_{\perp} the resummed component vanishes faster than the fixed order. Considering the asymptotic scaling in eq. (2.13), we choose p = 4 which guarantees that the differential distribution vanishes as fast as $1/p_1^5$ for $p_{\perp} \gtrsim Q$. In principle, any value



Figure 1. Differences between leading-order distributions and their logarithmic contributions, normalized to the leading-order results. The three curves show the case for top quark (solid/red), top and bottom quarks (dotted/blue), and top-bottom interference (dot-dashed/green). See text for details.

of p greater than 3 will equally do, since p only determines how fast the resummation is turned off above the scale Q. We have indeed checked that by varying p by one unit around p = 4 the results do not change significantly.

The same figure shows results for the full spectrum where both top and bottom loops are included (dotted, blue curve), and results for top-bottom interference (dot-dashed, green curve).⁶ In this case the situation changes considerably, and this will be the subject of the next section.

2.2 Issues with *b* quarks

The "standard" approach to resummation described in section 2.1 becomes problematic in case of the Higgs boson production in hadron collisions [34, 35, 38–41]. The difficulty is related to the fact that the ggH vertex is not point-like but, rather, is induced by a quark loop. The presence of the quark loop implies the existence of structure-dependent radiation with peculiar properties and has important consequences for the resummation. The key to the following discussion is the appreciation of the fact that the structure-dependent radiation is suppressed if p_{\perp} is smaller than the mass of the quark but it becomes important otherwise. For p_{\perp} larger than the quark mass, the soft and collinear approximations that provide the foundation for small p_{\perp} resummation become unreliable, as they focus on emissions off external lines and systematically neglect structure-dependent effects. In this section we elaborate on this issue.

We consider Higgs boson production in gluon fusion mediated by a quark loop. We denote the mass of the quark by m_q and consider two cases $m_q \gg m_H$ and $m_q \ll m_H$. In the first case, the structure dependence enters at $p_{\perp} \gtrsim m_q \gg m_H$, so that emissions off the external lines dominate for transverse momenta up to the Higgs mass and even higher. Therefore, if we restrict ourselves to values of p_{\perp} that are comparable to m_H , the situation

⁶We ignore the bottom squared contribution, which is completely negligible in the Standard Model.

is no different from point-like interaction, and there are no issues in the resummation procedure described in the previous section. In the Standard Model, this is indeed what happens with the top loop contribution to the Higgs boson transverse momentum spectrum.

The second case, $m_q \ll m_H$ is very different. Indeed, in this case there are three distinct regions $p_{\perp} \lesssim m_q$, $m_q \lesssim p_{\perp} \lesssim m_H$ and $m_H \lesssim p_{\perp}$. In the first region $p_{\perp} \lesssim m_q$, the transverse momenta of the Higgs boson and the recoiling partons are typically small enough not to resolve the structure of the loop and the extra radiation factorizes. For the bottom-quark contribution ($m_q \sim 5 \,\text{GeV}$) the effect of additional QCD radiation is strongly suppressed in this region by all-order effects, so that its impact on the total cross section is small.⁷ Note, however, that in this region there are large logarithmic contributions of the type $\ln^2 m_H/m_b$, whose resummation is not fully understood even at the lowest perturbative order [42, 43].

In the second region $m_q \lesssim p_{\perp} \lesssim m_H$ the structure-dependent radiation becomes essential and the ggH vertex does not factorize. In addition to the usual logarithms $\ln m_H/p_{\perp}$, the radiation gives rise to logarithms $\ln p_{\perp}/m_q$ and $\ln m_H/m_q$, whose origin and potential resummation are not well understood.⁸

The reason why the small- p_{\perp} resummation is problematic in this region is the following. Emissions off internal lines can become as important as emissions off external lines, and together they probe the loop structure of the ggH vertex. It follows that approximating the small p_{\perp} region with an on-shell ggH form factor is not justified. In particular, while form factor effects in the top-quark case only introduce (p_{\perp}/m_H) -suppressed corrections, in this case they both introduce a new logarithmic structure $(\ln p_{\perp}/m_q \text{ and } \ln m_H/m_q)$ and suppress radiation with $p_{\perp} \gtrsim m_q$. In other words, while in the top case, described in section 2.1, at finite p_{\perp} , the coefficients of the logarithms differ from the resummed result by p_{\perp} -suppressed terms, in the *b*-quark case, this difference contains new logarithmic terms $\ln p_{\perp}/m_b$ and $\ln m_H/m_b$ in the region $m_b \lesssim p_{\perp} \lesssim m_H$.

As a consequence, the collinear approximation should not be expected to work far away from the *b*-quark threshold. To quantify this effect, we go back to figure 1. We see that, while for the top-only case (solid, red line) the collinear approximation to the leading order accounts for half of the result at about $p_{\perp} \sim 50 - 60$ GeV, for the top-bottom interference this scale is reduced to about 30 GeV. When top and bottom contributions are considered together, this effect is less dramatic since in the SM the interference accounts for about $\sim 5\%$ of the full result. This can be seen in the dotted blue curve of figure 1.

Because of the above issues, it is clear that constructing a reasonable description of the *b*-quark contribution to the Higgs transverse momentum distribution is problematic. Since, as we already stressed, in this case the resummation of potentially large logarithms is not entirely understood, the best we can do is to use different ways to interpolate between regions of small and large transverse momenta and check to what extent the different results are compatible.

As already stated, the Higgs boson production in the Standard Model is dominated by the top quark loop; the bottom loop provides a very small contribution that is lifted up to

⁷This region is also very sensitive to non-perturbative effects.

⁸For some recent studies, see e.g. refs. [42–44].

 $\mathcal{O}(-5\%)$ by its interference with the top amplitude. Because of this, a $\mathcal{O}(20-30\%)$ control on the top-bottom interference is sufficient to control the Higgs transverse momentum spectrum at the few percent level. With this in mind, we now study in more detail the different ways to treat the bottom contribution.

One option is to apply eq. (2.8) with the resummation scale set to $Q \sim m_b$ [34]. This choice is equivalent to employing fixed-order description for all values of transverse momenta. Indeed, for 1 GeV $\leq p_{\perp} \leq Q \sim m_b$, the resummed logarithms $\ln(Q/p_{\perp})$ never become large and for $p_{\perp} \geq Q$ the fixed-order result is adopted anyhow. Since a typical error made within this approach is provided by uncalculated higher order terms, if we use a NLO computation for the interference, we make an error of order⁹ $[\alpha_s/(2\pi)]^2 \ln^4(m_H/m_b)$ and $[\alpha_s/(2\pi)]^2 \ln^4(p_{\perp}/m_H)$ which both evaluate to 15-20 percent, for $p_{\perp} \sim m_b \sim 5$ GeV.

The previous option amounts to neglecting the resummation for the top-bottom interference and to using the fixed-order result for all transverse momenta; the other extreme alternative consists of extending the resummation beyond its established domain of validity. We can do this by using the same resummation scale, $Q \sim m_H/2$, both for the top and the top-bottom interference contributions [35, 38]. In this case, at low p_{\perp} we introduce logarithms $\ln p_{\perp}/Q$ in the interference through the resummation prescription which are not guaranteed to be correct and, by doing that, we effectively introduce errors that are similar to those discussed above. At higher p_{\perp} the impact of these logarithms becomes smaller since at $p_{\perp} \sim Q$ the resummation effects smoothly turn off and we recover the fixed order prediction. Hence, when we under- or over-resum logarithms we expect comparable $\mathcal{O}(20\%)$ theoretical errors on the interference contribution to the Higgs p_{\perp} spectrum. An important question is whether these different sources of uncertainties pull the predictions apart or they remain compatible with each other.

Before concluding this section, we mention that within the *additive* matching scheme of eq. (2.8) the resummation term, which is proportional to the lowest-order form factor at zero transverse momentum, is added to the fixed order result. As we mentioned earlier, the form factor effects lead to a dependence of the leading order amplitude on p_{\perp} , that is not captured in this approach. To account for this, we also consider a *multiplicative* matching scheme, which can be schematically defined as¹⁰

$$\Sigma(p_{\perp}) = \Sigma^{\text{resum}}(p_{\perp}) \, \mathcal{T}^{\text{f.o.}}\left[\frac{\Sigma^{\text{f.o.}}(p_{\perp})}{\Sigma^{\text{resum}}(p_{\perp})}\right].$$
(2.15)

Similarly to eq. (2.8), eq. (2.15) smoothly interpolates between a low $p_{\perp} \ll Q$ region, where resummation dominates, to a large $p_{\perp} \gg Q$ region, where the result is obtained from a fixed order calculation. Clearly, the fixed order accuracy is preserved in the $p_{\perp} \rightarrow 0$ limit. The main difference with eq. (2.8) is that now the higher order terms induced by the resummation in the transition region are weighted with the fixed (lower) order result at *finite* transverse momentum. This should at least partially capture the p_{\perp} dependence of the exact higher order amplitude, and lead to a more realistic description of the physics. Because

⁹Note that these estimates refer to the top-bottom *interference* contribution. As we said, the term proportional to y_b^2 is negligible in the Standard Model.

¹⁰The actual implementation of this procedure requires extra care, as described in appendix A.3.

of this, we choose the multiplicative matching scheme eq. (2.15) as our default matching scheme. Nevertheless, matching ambiguities are by construction of higher-order nature and, therefore, any matching prescription is formally equally valid. Differences between matching prescriptions can be used to estimate the uncertainty in the transition region.

3 Results

3.1 Inclusion of bottom-quark loops and matching uncertainties

In this section we describe the practical and technical implementation of the top-bottom interference in the resummation and matching, and the uncertainty associated with it. As we described in section 2.2, the rigorous resummation in the presence of the bottom-quark loop is currently impossible. To remedy this problem, we adopt different approaches to include this contribution in the matched result. We use the arbitrariness in the choice of the resummation scale associated with the top-bottom interference and in the choice of the matching scheme to assess the inherent ambiguity of the resummation procedures.

We start by discussing the resummation scale. We treat separately the contribution of the top-squared amplitude and the top-bottom interference.¹¹ In particular, we associate two different resummation scales with the top and the interference contributions, and we use the following notation to denote the various cumulative distributions

$$\Sigma_{t+b}(p_{\perp}, Q_t, Q_b) \to \text{top and bottom, including the interference;}$$
 (3.1)

$$\Sigma_t(p_\perp, Q_t) \to \text{only top.}$$
 (3.2)

As explained in section 2.1, for the top-only contribution we set the resummation scale to $Q_t = m_H/2$. For the interference, instead, we use the following prescriptions to quantify the associated uncertainty (see section 2.2):

• We choose $Q_b \sim m_b$, effectively switching off the resummation for the interference at scales of the order of the bottom mass. As it was initially suggested in ref. [34], we choose $Q_b = 2m_b$ as our central scale. This is achieved by computing

$$\Sigma_{t+b}(p_{\perp}, m_H/2, 2m_b) = \Sigma_t(p_{\perp}, m_H/2) + \Sigma_{t+b}(p_{\perp}, 2m_b, 2m_b) - \Sigma_t(p_{\perp}, 2m_b).$$
(3.3)

This implies that in the region of transverse momenta that we are interested in, the interference is described only at fixed order and no resummation for this contribution is performed.

• We consider the opposite situation in which we rely on the collinear approximation also for $m_b \ll p_{\perp}$, and simply treat the new logarithmic terms that appear above this scale as a regular remainder that can be described at fixed order. As a consequence, the resummation for the interference contribution is switched off, as in the top-only case, at scales of order 60 GeV. We choose $Q_t = Q_b = m_H/2$ as our central scale, for simplicity.

¹¹For our numerical results, we also include the bottom squared contribution, which is however negligible in the Standard Model.

In both approaches, logarithms of the ratio p_{\perp}/m_b are not resummed. Although in the region $m_b \ll p_{\perp} \ll m_H$ these logarithmic terms can be potentially large and therefore should be included to all orders, recent studies seem to suggest that an accurate prediction of these terms is achieved by considering the first few terms in the fixed-order perturbative expansion [42, 43].

As far as the resummation is concerned, the result will be nearly identical to the $m_q \to \infty$ one.¹² The only difference is that now the Born squared amplitude and the hard-virtual correction will contain the full dependence on the top and bottom masses. In particular, no modification of the p_{\perp} -dependent radiation pattern is introduced. Technically, we implement the LO and the NLO amplitudes for $gg \to H$ with full mass dependence following ref. [45].

We now study numerically the difference between the two prescriptions for the bottom resummation scale. We start by introducing the setup that we adopt for our predictions. We consider proton collisions at the 13 TeV LHC. The Higgs boson mass is taken to be $m_H = 125$ GeV and the top and bottom pole masses¹³ are set to $m_t = 173.2$ GeV and $m_b = 4.75$ GeV, respectively. We work within a fixed flavor-number scheme ($n_F = 5$) and use the PDF4LHC15_nnlo set of parton distribution functions [46] interfaced through LHAPDF6 [47]. We use the value of the strong coupling constant α_s provided by the PDF set. As central values for the renormalization and factorization scales we take

$$\mu_R = \mu_F = M_T/2$$
, with $M_T = \sqrt{m_H^2 + p_\perp^2}$. (3.4)

In order to estimate the perturbative uncertainties for each prediction, we perform a 7-point variation of the factorization (μ_F) and renormalization (μ_R) scales around the central value by a factor of two. Moreover, we vary Q_t and Q_b by a factor of two around their respective central values, keeping fixed $\mu_R = \mu_F = M_T/2$. The final uncertainty band is obtained as the envelope of all above variations. As a default, we adopt the multiplicative scheme discussed in section 2.2 and described in detail in appendix A.3.

The fixed-order NLO results for the top-bottom interference are based on the calculation presented in [36], which in turn comprises the two-loop amplitudes for $gg \to Hg$, $q\bar{q} \to Hg$ and $qg \to Hq$ derived in [32, 33] together with corresponding loop-squared real radiation amplitudes as provided by OPENLOOPS [48, 49] combined with COLLIER [50]. For the Monte Carlo integration and subtraction the POWHEG-BOX-RES is used [51, 52].

We now discuss the dependence on the choice of the resummation scale associated with the bottom contribution. We start by comparing results for the top-bottom interference for two values of the resummation scale Q_b . The results are displayed in the left plot in figure 2. The two predictions differ by about 20% for $p_{\perp} \sim 30 \text{ GeV}$, in line with what we expected from the discussion in section 2.2. We note, however, that although the two results are computed for very different choices of the resummation scales, they are still compatible (although marginally for $p_{\perp} \gtrsim 25 \text{ GeV}$) within their respective uncertainties. Only for $p_{\perp} \gtrsim 50 \text{ GeV}$ the two results differ significantly, since the interference obtained

¹²HEFT in the following.

 $^{^{13}\}mathrm{We}$ work in the on-shell renormalization scheme as a default.



Figure 2. Comparison between two resummation-scale prescriptions for top-bottom interference (left) and full (right) distributions. See text for details.

with $Q_b = 2 m_b$ vanishes faster than the one obtained with $Q_b = m_H/2$. However, in this region the contribution of the interference to the physical spectrum is completely negligible. Each of the two results has a relative uncertainty of about 15% for $p_{\perp} \lesssim 40 \text{ GeV}$. The variations of the resummation scales around their central value, and the variation of μ_R and μ_F have a similar impact on the final band.

The right plot of figure 2 shows an analogous comparison for the transverse momentum distribution that includes both top and bottom contributions. Since the interference only accounts for about 5% of the full result, we find that the two resummation prescriptions for the top-bottom interference are indistinguishable within the uncertainties of the top contribution. Indeed, in this case the uncertainty band is dominated by the μ_R and μ_F variation of the top contribution, which amounts to about 10 - 15% for $p_{\perp} \lesssim 40$ GeV, while the resummation-scale uncertainty amounts to about 5% in this region. Note however that the top-only contribution has been computed one order higher, both in fixed-order QCD [7–11] and in the resummation framework [29]. In this paper, we focus on the *b*-quark effects and hence do not include these results but, as a matter of principle, they can be used to further reduce the uncertainty on the top contribution.

We now investigate the second source of resummation ambiguity, namely the choice of the matching scheme. As discussed in section 2.2, besides our default multiplicative scheme we also consider an additive scheme. Both schemes are precisely defined in appendix A.3. We remind the reader that, as far as the top-bottom interference is concerned, the main qualitative difference between the two approaches is that within the *additive* matching scheme, the resummation contribution is proportional to the $gg \to H$ form factor at zero transverse momentum whereas in the *multiplicative* matching scheme it is weighted by the form factor $g^*g^* \to H$ at finite transverse momentum. In order to study this source of ambiguity more precisely, we consider the additive matching scheme, with two different scales ($Q_b = m_H/2$ and $Q_b = 2m_b$), and compare the results to the multiplicative scheme.

Since in the additive scheme the resummed contribution does not include form-factor effects, we expect sizable differences between results obtained with $Q_b = m_H/2$ and



Figure 3. Comparison between the additive scheme with $Q_t = m_H/2$, $Q_b = 2m_b$ (left plot) or $Q_t = Q_b = m_H/2$ (right plot), and the default multiplicative scheme with $Q_t = Q_b = m_H/2$.

 $Q_b = 2m_b$. We recall that this is not the case in the multiplicative scheme (see figure 2) where form-factors effects are automatically accounted for. We then show, in figure 3, the comparison between the top-bottom interference in the default multiplicative scheme with $Q_b = m_H/2$ and the additive scheme with $Q_b = 2m_b$ (left plot) and $Q_b = m_H/2$ (right plot). We observe that the difference between the two schemes is larger when the additive scheme with $Q_b = m_H/2$ is used. Nevertheless, we find that also in this case, the difference between the two schemes for the interference does not exceed ~ 20% in the bulk of the distribution. Again, the full transverse momentum distribution, shown in the left plot of figure 4, is only mildly affected by this ambiguity.

Finally, in the right plot of figure 4, we show the ratio of the full distribution computed using the default multiplicative scheme, to the corresponding HEFT result. The default result, i.e. multiplicative matching scheme with $Q_t = Q_b = m_H/2$, is in good agreement with the NLO prediction. For comparison, we also report the other extreme solution obtained with the multiplicative scheme with $Q_t = m_H/2$, $Q_b = 2m_b$. We observe that this choice is in good agreement with both the fixed order and the default matched solution.

In summary, we find that a conservative approach towards the inclusion of bottom-mass effects in the matched prediction for the Higgs- p_{\perp} spectrum leads to a ~ 20% ambiguity on the top-bottom interference in the region $m_b \lesssim p_{\perp}$. Since the interference provides a rather small contribution to the Higgs transverse momentum distribution, this ambiguity translates into a few-percent uncertainty in the Higgs p_{\perp} spectrum.

In what follows, we will use the result obtained with the multiplicative matching scheme with $Q_t = Q_b = m_H/2$ as our central value. To estimate uncertainties, we will consider the envelope of scale variations and the result obtained either by using the multiplicative or the additive scheme with $Q_t = m_H/2$, $Q_b = 2m_b$. In addition to these source of uncertainty, an additional ambiguity arises from the choice of the renormalization scheme for the quark masses. This will be discussed in the next section.



Figure 4. Left plot: comparison for the full distribution between the additive scheme with $Q_t = Q_b = m_H/2$, and the default multiplicative scheme with $Q_t = Q_b = m_H/2$. Right plot: ratio of the full distribution with different accuracies to the HEFT prediction based on the same accuracy. In the right plot all matched results are obtained within the multiplicative matching scheme.



Figure 5. The top-bottom interference contribution for the fixed order (left) and the matched (right) distributions, for different choices of the mass-renormalization scheme. See text for details.

3.2 Mass-scheme uncertainty and final results

In this section, we present our final results for the NNLL+NLO matched distributions. We use as default the multiplicative matching scheme with resummation scales $Q_t = Q_b = m_H/2$. We renormalize the bottom-quark mass in the on-shell scheme. To estimate the uncertainty we change the details of the resummation and matching as explained in the previous section. In addition, we consider a different renormalization scheme for the bottom quark mass to estimate the related uncertainty. To this end, we employ the $\overline{\text{MS}}$ renormalization scheme. We take the mass renormalization scale to be 100 GeV, and use $m_b = m_b^{\overline{\text{MS}}}(100 \text{ GeV}) = 3.07 \text{ GeV}$ as an input parameter.¹⁴

In figure 5 we display the results for the top-bottom interference contribution. The fixed order result is presented in the left plot. We show the uncertainty band for the on-shell

¹⁴We calculated this value using the program RunDec [53, 54] with the input value $m_b^{\overline{\text{MS}}}(m_b^{\overline{\text{MS}}}) = 4.2 \text{ GeV}.$



Figure 6. The full top plus bottom distribution for the fixed order (left) and the matched (right) results, for different choices of the mass renormalization scheme. See text for details.

mass-renormalization scheme and the central value for the $\overline{\text{MS}}$ scheme. The uncertainty band is calculated from a 7-point scale variation. We see that the scheme ambiguity is larger than the scale variation, as already observed in ref. [36]. The right plot shows our results for the matched distributions with the two different mass schemes. The difference between the two bottom-mass schemes is similar to the fixed order case, but since now the matched prediction has a smaller uncertainty, the separation between the two results is more significant. As follows from figure 5, the top-bottom interference contribution has an ambiguity of about 15-20% down to $p_{\perp} \sim 10$ GeV. In order to improve on this, one would need a NNLO calculation for the top-bottom interference, which is currently out of reach.

The analogous plots for the full distribution that includes both top and bottom amplitudes are shown in figure 6, for the fixed order (left) and resummed (right) results. Unlike for the top-bottom interference contribution, in this case the difference between the two results for the bottom-mass schemes are much smaller, at the level of a few percent. This is because the top-bottom interference contributes to just $\mathcal{O}(-5\%)$ of the full spectrum.¹⁵

Our best current predictions for the top-bottom interference and full p_{\perp} spectrum including all the relevant uncertainties are shown in figure 7. As discussed earlier, the uncertainty bands are obtained as an envelope of:

- a 7-point renormalization and factorization scale variation;
- resummation scale variation $Q_t = Q_b \in \{m_H/4, m_H/2, m_H\}$ for $\mu_R = \mu_F = M_T/2$;
- multiplicative matching scheme with $Q_t = m_H/2$, $Q_b = 2m_b$ for $\mu_R = \mu_F = M_T/2$;
- additive matching scheme with $Q_t = m_H/2$, $Q_b = 2m_b$ for $\mu_R = \mu_F = M_T/2$.

In addition, if the default matched result but in the $\overline{\text{MS}}$ renormalization scheme for the bottom-quark mass is outside the uncertainty band estimated as described above, we extend

¹⁵Although the bottom-mass scheme ambiguity has a very moderate impact on the SM Higgs p_{\perp} spectrum, this effect might be more significant for specific BSM scenarios. A dedicated study of such scenarios is necessary in order to assess the theory uncertainties precisely.



Figure 7. The distributions for the top-bottom interference contribution (left) and the full NNLL matched result (right), using the multiplicative scheme with resummation scale $Q_b = Q_t = m_h/2$ as central values. See text for details.

the uncertainty band to accommodate the mass scheme ambiguity. In fact, as shown in figure 5, the latter ambiguity is the major source of uncertainty for the top-bottom interference for transverse momenta below 30 GeV.

The top-bottom interference is shown in the left plot of figure 7. The qualitative features of the fixed-order result are unchanged by the resummation, which however has a noticeable effect on the shape of the distribution. Our final result has an uncertainty of about ~ 20%, and is compatible with the fixed-order one. In the right plot of figure 7 we present the results for the full spectrum. At large values of the Higgs $p_{\perp} \gtrsim 30$ GeV the fixed order result is contained in the error band of the resummed result. However at smaller values, $p_{\perp} \lesssim 30$ GeV we observe a marked difference between the two results. The error for the full matched result is close to 10% for $p_{\perp} \lesssim 30$ GeV and close to ~ 20% at larger p_{\perp} . We stress however that the uncertainty on the dominant top contribution can be further reduced by employing the results of refs. [7–11, 29, 55].

4 Conclusions

In this paper we performed a detailed study of the Higgs transverse momentum distribution, focusing on the region of intermediate values of transverse momenta, $m_b \lesssim p_{\perp} \lesssim m_H$. Indeed, a precise theoretical control of the Higgs p_{\perp} distribution in this region is essential to test the Higgs sector of the Standard Model. In particular, it provides a rare opportunity to probe the Yukawa couplings of light quarks, which are currently poorly constrained. In fact, although the main contribution to the Higgs production cross section is due to the coupling of the Higgs to top quarks, the coupling to bottom quarks has a non-negligible impact on the total cross section through its interference with the top, decreasing the cross section by about $\mathcal{O}(5\%)$.

The theoretical description of the Higgs p_{\perp} distribution for $m_b \lesssim p_{\perp} \lesssim m_H$ in QCD is particularly challenging since, once the contribution of bottom quarks is included, the perturbative cross section for small p_{\perp} suffers from the presence of potentially large logarithms $\ln (p_{\perp}/m_b)$, $\ln (m_H/m_b)$, which can spoil the convergence of the perturbative expansion. The physical origin of these large logarithms is not yet fully understood, and their all-order resummation remains currently out of reach.

Given these conceptual limitations, we provided our best theoretical description of the Higgs p_{\perp} distribution at NNLL+NLO QCD for moderate values of the transverse momentum, including dependence on the bottom mass. An important part of our study was a proper assessment of the theory uncertainty of our results. The NLO result for the topbottom interference suffers from scale uncertainties, which amount to around 15%. On top of this, a non-negligible source of uncertainty is provided by the renormalization scheme ambiguity for the bottom-quark mass, which we estimated by varying from the on-shell to the $\overline{\text{MS}}$ scheme. This amounts to an uncertainty of up to 20% and it dominates the error budget of our prediction for the top-bottom interference at small values of the Higgs p_{\perp} . Together with the uncertainties associated with the fixed order calculation, we also performed a detailed study of the ones associated with the resummation procedure in the presence of bottom quarks. In order to estimate these ambiguities for the top-bottom interference, we matched the fixed order NLO predictions with the NNLL resummed crosssection using two different schemes, an additive and a multiplicative one, and two very different choices of the resummation scale, $Q_b = 2m_b$ and $Q_b = m_H/2$. This leads to an uncertainty between 15 - 20% on the top-bottom interference contribution to the p_{\perp} spectrum. Since the interference amounts to about 5% of the full p_{\perp} spectrum, we conclude that unknown higher order b-quark mass effects can modify the Higgs transverse momentum distribution by few percent. All ambiguities associated with the resummation in the presence of bottom quarks produce consistent results within the NNLL+NLO uncertainty band, which is however driven by uncertainties in the (NLO) top quark contribution. The latter is currently known to higher $N^3LL+NNLO$ accuracy [7–11, 29, 55]. It would be interesting to combine these results with the ones presented in this article. We leave this for future investigations.

In conclusion, we presented a description of the Higgs p_{\perp} spectrum at NNLL+NLO QCD including both top and bottom quark contributions. We found that the uncertainty on the top-bottom interference is $\mathcal{O}(20\%)$ in the region of interest $m_b \leq p_{\perp} \leq m_H$. Given the intrinsic ambiguities from scale dependence and, in particular, from the choice of the bottom-mass renormalization scheme and matching scheme, any improvement in this description will inevitably require the computation of the NNLO QCD corrections to the bottom-quark contribution to $gg \to H$ and $gg \to H + jet$.

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A Resummation and matching: details

In this appendix we briefly derive the resummation formula in the toy model described in the main text, report the final NNLL formulas that we eventually used in our results and describe in details the matching procedure we employ. We follow the approach of refs. [29, 55], and we refer the reader to these publications for the details.

A.1 The LL case

We consider the p_{\perp} distribution of a Higgs boson in $pp \to H$ in the $p_{\perp} \to 0$ limit, at leading-logarithmic accuracy. In this approximation, one must only control the leading singularity of the *n*-emissions matrix element at all perturbative orders. This is done by approximating the process with an ensemble of independent soft-collinear gluons emitted off the two incoming legs.

To set up the notation we introduce two reference light-like momenta along the beam direction that will serve to parametrize the radiation 16

$$\tilde{p}_1 = \frac{m_H}{2}(1,0,0,1), \qquad \tilde{p}_2 = \frac{m_H}{2}(1,0,0,-1).$$
(A.1)

We now consider a real emission k_1 collinear to \tilde{p}_1 that can be expressed as

$$k_1 = \left(1 - z_1^{(\ell_1)}\right) \tilde{p}_1 + \left(1 - z_1^{(\ell_2)}\right) \tilde{p}_2 + \kappa_{\perp 1} , \qquad (A.2)$$

where $\kappa_{\perp 1}$ is a space-like four-vector, orthogonal to both \tilde{p}_1 and \tilde{p}_2 such that $\kappa_{\perp 1}^2 = -k_{\perp 1}^2$. Note that since k_1 is massless

$$k_{\perp 1}^2 = \left(1 - z_1^{(\ell_1)}\right) \left(1 - z_1^{(\ell_2)}\right) m_H^2 = \frac{2(\tilde{p}_1 \cdot k_1) 2(\tilde{p}_2 \cdot k_1)}{2(\tilde{p}_1 \cdot \tilde{p}_2)} \,.$$

Moreover, if k_1 is collinear to \tilde{p}_1 one has (from $(1 - z_1^{(\ell_1)}) > (1 - z_1^{(\ell_2)})$)

$$z_1^{(\ell_1)} < 1 - \frac{k_{\perp 1}}{m_H}.\tag{A.3}$$

An analogous limit on $z_1^{(\ell_2)}$ as in eq. (A.3) holds when k_1 is collinear to \tilde{p}_2 . Subsequent emissions off leg ℓ_1 can be parametrized analogously to eq. (A.2), replacing the reference momentum \tilde{p}_1 with

$$\tilde{p}_1 \to \left(\prod_{\substack{i=1\\\ell_i=\ell_1}}^k z_i^{(\ell_i)}\right) \tilde{p}_1 \simeq \tilde{p}_1,\tag{A.4}$$

¹⁶We remind the reader that we are working in the soft approximation. As a consequence the kinematics is much simplified.

where the product runs over all emissions off leg ℓ_1 that occur prior to the emission we are parametrizing, and we used the fact that in the soft limit $z_i^{(\ell_i)} \simeq 1$. A similar parametrization holds for emissions off leg ℓ_2 .

The transverse recoil of the radiation is absorbed entirely by the Higgs boson that acquires a transverse momentum

$$p_{\perp} = |\sum_{i} \vec{k}_{\perp i}|. \tag{A.5}$$

In order to predict the $p_{\perp} \rightarrow 0$ limit, we need to sum emissions at all orders in the strong coupling. With LL accuracy, the squared amplitude for n emissions can be approximated by a product of n independent splitting kernels, as the soft correlation between emissions starts contributing at NLL order. The physical picture corresponding to this approximation is given by a set of independent emissions off legs ℓ_1 and ℓ_2 . In this approximation, the differential partonic distribution can be written as

$$\frac{\mathrm{d}\hat{\sigma}}{\mathrm{d}p_{\perp}} \simeq [dp_H] |\mathcal{M}(\tilde{p}_1 + \tilde{p}_2 \to H)|^2 \delta^{(4)}(\tilde{p}_1 + \tilde{p}_2 - p_H) \\ \times \frac{1}{n!} \prod_{i=1}^n [dk_i] |M_{\mathrm{soft}}(k_i)|^2 \delta\left(p_{\perp} - |\sum_i \vec{k}_{\perp i}|\right), \tag{A.6}$$

where the eikonal squared amplitude for a single emission reads

$$[dk]|M_{\text{soft}}(k)|^{2} = \sum_{\ell=1,2} 2C_{A} \frac{\alpha_{s}(k_{\perp})}{\pi} \frac{dk_{\perp}}{k_{\perp}} \frac{dz^{(\ell)}}{1 - z^{(\ell)}} \Theta\left((1 - z^{(\ell)}) - k_{\perp}/m_{H}\right) \frac{d\phi}{2\pi}.$$
 (A.7)

In eq. (A.7), the coupling is evaluated at k_{\perp} to account for the leading-logarithmic contribution of the gluon branching into either a pair of soft quarks or gluons, see e.g. [56] for a detailed explanation.

The resummation is naturally performed at the level of the cumulative distribution, defined as

$$\Sigma(p_{\perp}) = \int_0^{p_{\perp}} dp'_{\perp} \frac{d\sigma}{dp'_{\perp}}.$$
 (A.8)

Indeed while the differential spectrum involves plus distributions in p_{\perp} , $\Sigma(p_{\perp})$ is a regular function. From eq. (A.6), it follows that the cumulative distribution with LL accuracy can be written as

$$\Sigma(p_{\perp}) \simeq [f_g(\mu_F) \otimes f_g(\mu_F)] (m_H^2/s) \times \int d\hat{\sigma} \Theta\left(p_{\perp} - |\sum_i \vec{k}_{\perp i}|\right), \tag{A.9}$$

where $f_g(\mu_F)$ is the gluon parton density evaluated at the factorization scale μ_F , and the convolution is defined as usual

$$[f \otimes g](x) \equiv \int_0^1 \mathrm{d}y \,\mathrm{d}z \,\delta(x - yz)f(y)g(z). \tag{A.10}$$

Since p_{\perp} only constrains the transverse momentum of the emissions, we can perform the integrals over the $z_i^{(\ell_i)}$ components inclusively. It is therefore convenient to introduce the functions

$$R'_{1}(p_{\perp}) = \int [dk] |M_{\text{soft}}(k)|^{2} (2\pi) \delta(\phi - \bar{\phi}) p_{\perp} \delta(p_{\perp} - k_{\perp}) \Theta(z^{(2)} - z^{(1)}),$$

$$R'_{2}(p_{\perp}) = \int [dk] |M_{\text{soft}}(k)|^{2} (2\pi) \delta(\phi - \bar{\phi}) p_{\perp} \delta(p_{\perp} - k_{\perp}) \Theta(z^{(1)} - z^{(2)}).$$
(A.11)

This notation allows us to parametrize the real-emission matrix element and phase space as

$$[dk_i]|M_{\text{soft}}(k_i)|^2 = \frac{dk_{\perp i}}{k_{\perp i}} \frac{d\phi_i}{2\pi} \sum_{\ell_i=1,2} R'_{\ell_i}(k_{\perp i}) = \frac{d\zeta_i}{\zeta_i} \frac{d\phi_i}{2\pi} \sum_{\ell_i=1,2} R'_{\ell_i}(\zeta_i k_{\perp 1}) , \qquad (A.12)$$

where we defined $\zeta_i = k_{\perp i}/k_{\perp 1}$.

We now discuss the purely virtual corrections, which are encoded in the gluon form factor $|\mathcal{M}(\tilde{p}_1 + \tilde{p}_2 \to H)|^2$. We write it as

$$|\mathcal{M}(\tilde{p}_1 + \tilde{p}_2 \to H)|^2 = \mathcal{H}(m_H)|\mathcal{M}_B(\tilde{p}_1 + \tilde{p}_2 \to H)|^2, \tag{A.13}$$

where the function \mathcal{H} contains all the IRC singularities and the constant finite corrections of the form factor, and \mathcal{M}_B denotes the Born amplitude. Since we are working with LL accuracy, we are only interested in the leading singular term of \mathcal{H} at all orders (while neglecting all finite terms) which can be written as

$$\mathcal{H}(m_H) \simeq \exp\left\{-\int [dk] |M_{\text{soft}}(k)|^2\right\}.$$
 (A.14)

Note that the integral in eq. (A.14) is divergent and is to be considered as regularized. In order to cancel the IRC divergences of the real emissions (A.6) against the ones in the virtual corrections (A.14) at all orders, we introduce a small slicing parameter $\epsilon > 0$ such that all emissions with a transverse momentum $k_{\perp i}$ smaller than $\epsilon k_{\perp 1}$ can be ignored in the computation of the observable p_{\perp} , in the limit $\epsilon \to 0$. The real emissions with $k_{\perp i} < \epsilon k_{\perp 1}$, hereby denoted as *unresolved*, can be directly combined with the virtual corrections at all orders. Their combination gives rise to an exponential suppression factor of the type

$$\mathcal{H}(m_H) \sum_{m}^{\infty} \frac{1}{m!} \prod_{i=1}^{m} \left[\int \frac{dk_{\perp i}}{k_{\perp i}} \frac{d\phi_i}{2\pi} \sum_{\ell_i=1,2} R'_{\ell_i} \left(k_{\perp i} \right) \Theta \left(\epsilon k_{\perp 1} - k_{\perp i} \right) \right]$$
$$= \exp\left\{ -\int \frac{dk_{\perp}}{k_{\perp}} \frac{d\phi}{2\pi} \sum_{\ell=1,2} R'_{\ell} \left(k_{\perp} \right) \Theta \left(k_{\perp} - \epsilon k_{\perp 1} \right) \right\} \equiv e^{-R(\epsilon k_{\perp 1})}.$$
(A.15)

On the other end, emissions with $k_{\perp i} > \epsilon k_{\perp 1}$, that we denote as *resolved*, are constrained by the observable's measurement function and therefore cannot be integrated over inclusively. The resummed LL cross section thus reads

$$\Sigma(p_{\perp}) \simeq \sigma_B \int \frac{dk_{\perp 1}}{k_{\perp 1}} \frac{d\phi_1}{2\pi} e^{-R(\epsilon k_{\perp 1})} \sum_{\ell_1 = 1,2} R'_{\ell_1} (k_{\perp 1}) \\ \times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^1 \frac{d\zeta_i}{\zeta_i} \frac{d\phi_i}{2\pi} \sum_{\ell_i = 1,2} R'_{\ell_i} (\zeta_i k_{\perp 1}) \Theta\left(p_{\perp} - |\sum_i \vec{k}_{\perp i}|\right), \quad (A.16)$$

where σ_B is the Born cross section. The above formula, in the limit $\epsilon \to 0$ exactly reproduces the LL corrections to the p_{\perp} distribution, see ref. [29] for a formal proof. Eq (A.16) can be further simplified by observing that in the resolved radiation one always has $\zeta_i \sim 1$, since configurations in which $\zeta_i \ll 1$ are automatically canceled against the exponential Sudakov factor $e^{-R(\epsilon k_{\perp 1})}$. Therefore, one can expand the functions $R'(\zeta_i k_{\perp 1})$ in powers of $\ln(1/\zeta_i)$ as

$$R'_{\ell_i}\left(\zeta_i k_{\perp 1}\right) = R'_{\ell_i}\left(k_{\perp 1}\right) + R''_{\ell_i}\left(k_{\perp 1}\right) \ln \frac{1}{\zeta_i} + \dots, \qquad (A.17)$$

and retain terms that contribute at a given logarithmic order. In particular, at LL, only the first term in this expansion contributes, and higher-order terms matter at higher logarithmic orders (see refs. [29] for details).

Similarly, we can consistently expand out the ϵ dependence of the exponential Sudakov as

$$e^{-R(\epsilon k_{\perp 1})} = e^{-R(k_{\perp 1})} e^{-R'(k_{\perp 1}) \ln \frac{1}{\epsilon} + \dots},$$
(A.18)

where the ϵ dependence manifestly cancels against the one in the resolved contribution, and we defined

$$R'(k_{\perp 1}) \equiv \sum_{\ell_1=1,2} R'_{\ell_1}(k_{\perp 1}).$$
(A.19)

Therefore, with LL accuracy, eq. (A.16) becomes

$$\Sigma(p_{\perp}) \simeq \sigma_B \int \frac{dk_{\perp 1}}{k_{\perp 1}} \frac{d\phi_1}{2\pi} e^{-R(k_{\perp 1})} \epsilon^{R'(k_{\perp 1})} \sum_{\ell_1 = 1,2} R'_{\ell_1} (k_{\perp 1}) \times \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^1 \frac{d\zeta_i}{\zeta_i} \frac{d\phi_i}{2\pi} \sum_{\ell_i = 1,2} R'_{\ell_i} (k_{\perp 1}) \Theta\left(p_{\perp} - |\sum_i \vec{k}_{\perp i}|\right).$$
(A.20)

Equation (A.20) is suitable for a numerical implementation, as explained in ref. [29] in detail. The dependence on ϵ is at most power suppressed (i.e. $\mathcal{O}(\epsilon p_{\perp})$) and it vanishes in the limit $\epsilon \to 0$. This limit can therefore be taken safely numerically, and the result is absolutely stable for very small values of ϵ .¹⁷

We now introduce the resummation scale Q as a possible way to switch off the resummation at large transverse momentum. This is defined with a procedure similar to the one discussed in the text. We first break the logarithm as follows

$$L \equiv \ln \frac{m_H}{k_{\perp 1}} = \ln \frac{m_H}{Q} + \ln \frac{Q}{k_{\perp 1}}.$$
 (A.21)

The above operation will allow us (as explained shortly) to have an additional handle (namely the scale Q) to estimate the size of subleading logarithmic terms. Moreover, we also slightly modify the phase space available for the radiation, by introducing powersuppressed contributions that ensure that at large p_{\perp} the resummation effects completely

¹⁷In our implementation we use $\epsilon = e^{-20}$, although any value below $\epsilon = e^{-6}$ does not lead to any appreciable differences.

vanish. This can be done, as a first step, by modifying the resummed logarithms as follows

$$\ln \frac{Q}{k_{\perp 1}} \to \frac{1}{p} \ln \left(\frac{Q^p}{k_{\perp 1}^p} + 1 \right) \equiv \tilde{L}, \tag{A.22}$$

where p is a positive real parameter which is chosen such that the resummed differential distribution vanishes as $1/p_{\perp}^{p+1}$ at large p_{\perp} . The above prescription essentially amounts to the following

1. First, we split the resummed logarithm L into the sum of a small logarithm $\ln(m_H/Q)$ (with $Q \sim m_H$) and a large one $\ln(Q/k_{\perp 1})$. This operation allows one to introduce a generic scale Q which appears in the resummed logarithms. One can now expand L about $\ln(Q/k_{\perp 1})$, retaining all terms with the desired logarithmic accuracy. Effectively, this implies that $\ln(m_H/Q)$ is treated perturbatively at fixed order. Moreover, we replace $\ln(Q/k_{\perp 1})$ by the modified logarithm \tilde{L} . In our LL example this means

 $R(k_{\perp 1}) \to \tilde{R}(k_{\perp 1}) + \mathcal{O}(\ln m_H/Q); \qquad R(k_{\perp 1}) \to \tilde{R}'(k_{\perp 1}) + \mathcal{O}(\ln m_H/Q), \quad (A.23)$

where \tilde{R} and \tilde{R}' are functions of the modified logarithm \tilde{L} only.

2. eq. (A.22) comes together with the following prefactor \mathcal{J} in eq. (A.20)

$$\mathcal{J}(k_{\perp 1}) = \left(\frac{Q}{k_{\perp 1}}\right)^p \left(1 + \left(\frac{Q}{k_{\perp 1}}\right)^p\right)^{-1}.$$
 (A.24)

This corresponds to the Jacobian for the transformation (A.22), and ensures the absence of fractional (although power suppressed) α_s powers in the final distribution [29]. This factor, once again, leaves the small $k_{\perp 1}$ region untouched, and only modifies the large p_{\perp} region by power-suppressed effects. This is effectively mapping the limit $k_{\perp 1} \rightarrow Q$ onto $k_{\perp 1} \rightarrow \infty$. Although this procedure seems a simple change of variables, we stress that the observable's measurement function (i.e. the Θ function in eq. (A.20)) is not affected by this prescription. As a consequence, the final result will depend on the parameter p through power-suppressed terms.

The difference between the above prescription and what was introduced in the text is that the argument of the (modified) logarithms is now $k_{\perp 1}$ instead of p_{\perp} . This prescription is technically more correct, since in the small $k_{\perp 1}$ region, which governs the $p_{\perp} \rightarrow 0$ limit, the modified logarithms leave eq. (A.20) untouched. Conversely, at large $k_{\perp 1}$, where one has $k_{\perp 1} \sim p_{\perp}$, the above prescription reduces to what was defined in the text, i.e. the modified logarithms of $k_{\perp 1}$ in this region are formally equivalent to modified logarithms in p_{\perp} . To see this, we observe that when $k_{\perp 1} \gg Q$ the function $R'(k_{\perp 1}) \ll 1$. Therefore, the probability of having any emission after the first one in eq. (A.20) is strongly suppressed. As a consequence, at large $k_{\perp 1}$, the only relevant event is the one that involves a single emission k_1 , for which the cross section reads

$$\Sigma(p_{\perp}) \sim \sigma_B \int \frac{dk_{\perp 1}}{k_{\perp 1}} \frac{d\phi_1}{2\pi} \mathcal{J}(k_{\perp 1}) e^{-\tilde{R}(k_{\perp 1})} \sum_{\ell_1 = 1,2} \tilde{R}'_{\ell_1}(k_{\perp 1}) \Theta\left(p_{\perp} - |\vec{k}_{\perp 1}|\right) = e^{-\tilde{R}(p_{\perp})}.$$
(A.25)

It is easy to see that, if eq. (A.25) were evaluated without the factor \mathcal{J} , it would lead to additional power-suppressed terms with fractional power of the coupling, which are clearly spurious.

A.2 Final formulas for NNLL resummation

Beyond LL, eq. (A.20) is corrected to account for the description of the real-emission matrix element and phase space in less singular configurations, as well as higher perturbative corrections. To NNLL order it can be expressed as [29]

$$\Sigma(p_{\perp}) = \int \frac{dk_{\perp 1}}{k_{\perp 1}} \frac{d\phi_{1}}{2\pi} \mathcal{J}(k_{\perp 1}) \left[\epsilon^{\tilde{R}'(k_{\perp 1})} \sum_{n=0}^{\infty} \frac{1}{n!} \prod_{i=2}^{n+1} \int_{\epsilon}^{1} \frac{d\zeta_{i}}{\zeta_{i}} \frac{d\phi_{i}}{2\pi} \sum_{\ell_{1}=1,2} \tilde{R}'_{\ell_{1}}(k_{\perp 1}) \right] \\ \times \left\{ \frac{d}{d\tilde{L}} \left[-e^{-\tilde{R}(k_{\perp 1})} \mathcal{L}(k_{\perp 1}) \right] \Theta \left(p_{\perp} - \left| \sum_{i=1}^{n+1} \vec{k}_{\perp i} \right| \right) + e^{-\tilde{R}(k_{\perp 1})} \tilde{R}'(k_{\perp 1}) \right. \\ \left. \times \int_{\epsilon}^{1} \frac{d\zeta_{s}}{\zeta_{s}} \frac{d\phi_{s}}{2\pi} \left[\sum_{\ell_{i}=1,2} \left(\delta \tilde{R}'_{\ell_{i}}(k_{\perp 1}) + \tilde{R}''_{\ell_{i}}(k_{\perp 1}) \ln \frac{k_{\perp 1}}{k_{\perp s}} \right) \hat{\mathcal{L}}(k_{\perp 1}) - \frac{d\hat{\mathcal{L}}(k_{\perp 1})}{d\tilde{L}} \right] \\ \left. \times \left[\Theta \left(p_{\perp} - \left| \sum_{i=1}^{n+2} \vec{k}_{\perp i} \right| \right) - \Theta \left(p_{\perp} - \left| \sum_{\substack{i=1\\i\neq s}}^{n+2} \vec{k}_{\perp i} \right| \right) \right] \right\},$$
(A.26)

where $\zeta_i = k_{\perp i}/k_{\perp 1}$. In this formula, the Sudakov radiator $\tilde{R}(k_{\perp 1})$ is corrected with respect to its LL expression by higher-order corrections of both soft and collinear origin. The same comment applies to the function \tilde{R}'_{ℓ_i} which we decided to split into the old \tilde{R}' (derivative of the LL radiator defined above), plus a correction that contains all subleading effects, therefore replacing \tilde{R}' with

$$\tilde{R}'_{\ell_i} \to \tilde{R}'_{\ell_i} + \delta \tilde{R}'_{\ell_i}.$$
 (A.27)

The correction due to $\delta \tilde{R}'_{\ell_i}$ is only relevant to NNLL order for one of the resolved emissions. This *special* emission is denoted by the subscript *s* in eq. (A.26). After expanding to first order the corresponding term proportional to $\delta \tilde{R}'_{\ell_i}$ arising from the initial $\epsilon^{\tilde{R}'}$ factor, one ends up with the second term in the curly bracket in eq. (A.26), see ref. [29] for a full derivation. The same manipulations apply to the \tilde{R}'' correction coming from the expansion (A.17) discussed above.

Moreover, we introduced the following generalized luminosity coefficient

$$\mathcal{L}(k_{\perp 1}) = |\mathcal{M}_B|^2 \sum_{i,j} \int dx_1 dx_2 \int_{x_1}^1 \frac{dz_1}{z_1} \int_{x_2}^1 \frac{dz_2}{z_2} f_i \left(\mu_F e^{-\tilde{L}}, \frac{x_1}{z_1}\right) f_j \left(\mu_F e^{-\tilde{L}}, \frac{x_2}{z_2}\right) \\ \times \delta(x_1 x_2 s - m_H^2) \left[\delta_{gi} \delta_{gj} \delta(1 - z_1) \delta(1 - z_2) \left(1 + \frac{\alpha_s(\mu_R)}{2\pi} \tilde{H}^{(1)} \left(\mu_R, \frac{Q}{m_H}\right) \right) \right. \\ \left. + \frac{\alpha_s(\mu_R)}{2\pi} \frac{1}{1 - 2\alpha_s(\mu_R) \beta_0 \tilde{L}} \left(\tilde{C}_{gi}^{(1)} \left(z_1, \mu_F, \frac{Q}{m_H} \right) \delta(1 - z_2) \delta_{gj} + \{z_1 \leftrightarrow z_2; i \leftrightarrow j\} \right) \right],$$
(A.28)

and its NLL approximation

$$\hat{\mathcal{L}}(k_{\perp 1}) = |\mathcal{M}_B|^2 \int dx_1 dx_2 f_g \Big(\mu_F e^{-\tilde{L}}, x_1 \Big) f_g \Big(\mu_F e^{-\tilde{L}}, x_2 \Big) \,\delta(x_1 x_2 s - m_H^2). \tag{A.29}$$

We now report all the various ingredients entering the above formulas. The $\mathcal{O}(\alpha_s)$ correction to the collinear coefficient functions reads

$$\tilde{C}_{gi}^{(1)}\left(z,\mu_F,\frac{Q}{m_H}\right) = -P_{ij}^{(0),\epsilon}(z) - \delta_{ij}\delta(1-z)C_A\frac{\pi^2}{12} + P_{ij}^{(0)}(z)\ln\frac{Q^2}{\mu_F^2}$$
(A.30)

where $P_{ij}^{(0)}$ are the LO Altarelli-Parisi splitting functions

$$P_{qq}^{(0)}(z) = C_F \left[\frac{1+z^2}{(1-z)_+} + \frac{3}{2}\delta(1-z) \right],$$

$$P_{qg}^{(0)}(z) = T_R \left[z^2 + (1-z)^2 \right],$$

$$P_{gq}^{(0)}(z) = C_F \frac{1+(1-z)^2}{z},$$

$$P_{gg}^{(0)}(z) = 2C_A \left[\frac{z}{(1-z)_+} + \frac{1-z}{z} + z(1-z) \right] + 2\pi\beta_0\delta(1-z),$$
 (A.31a)

with $\beta_0 = (11C_A - 2n_f)/(12\pi)$ and $P_{ij}^{(0),\epsilon}(z)$ are given by

$$P_{qq}^{(0),\epsilon}(z) = -C_F(1-z),$$
 (A.32a)

$$P_{gq}^{(0),\epsilon}(z) = -C_F z$$
, (A.32b)

$$P_{qg}^{(0),\epsilon}(z) = -2T_R z(1-z), \qquad (A.32c)$$

$$P_{gg}^{(0),\epsilon}(z) = 0.$$
 (A.32d)

The function $\tilde{H}^{(1)}\left(\mu_R, \frac{Q}{m_H}\right)$ is defined as

$$\tilde{H}^{(1)}\left(\mu_R, \frac{Q}{m_H}\right) = H^{(1)} - \left(B^{(1)} + \frac{A^{(1)}}{2}\ln\frac{m_H^2}{Q^2}\right)\ln\frac{m_H^2}{Q^2} + 4\pi\beta_0\ln\frac{\mu_R^2}{m_H^2}, \quad (A.33)$$

where $H^{(1)}$ denotes the finite one-loop virtual correction to the $gg \to H$ process and $A^{(i)}, B^{(i)}$ are reported below. For the top contribution in the $m_t \to \infty$ approximation, $H^{(1)}$ reads

$$H^{(1)} = C_A \left(5 + \frac{7}{6} \pi^2 \right) - 3C_F = 11 + \frac{7}{2} \pi^2 \,. \tag{A.34}$$

The result including full quark mass dependence has been computed analytically in refs. [45, 57, 58].¹⁸

We expand the Sudakov radiator as

$$\tilde{R} = \tilde{L}g_1(\lambda) + g_2(\lambda) + \frac{\alpha_s(m_H)}{\pi}g_3(\lambda), \qquad (A.35)$$

 $^{^{18}}$ In our implementation we take both the Born amplitude and the virtual corrections from ref. [45].

where

$$\lambda = \alpha_s(\mu_R)\beta_0 \tilde{L}.\tag{A.36}$$

We introduce

$$x_Q = \frac{Q}{m_H},\tag{A.37}$$

and write

$$g_{1}(\lambda) = \frac{A^{(1)}}{\pi\beta_{0}} \frac{2\lambda + \ln(1-2\lambda)}{2\lambda},$$

$$g_{2}(\lambda) = \frac{1}{2\pi\beta_{0}} \ln(1-2\lambda) \left(A^{(1)} \ln \frac{1}{x_{Q}^{2}} + B^{(1)} \right) - \frac{A^{(2)}}{4\pi^{2}\beta_{0}^{2}} \frac{2\lambda + (1-2\lambda)\ln(1-2\lambda)}{1-2\lambda}$$

$$+ A^{(1)} \left(-\frac{\beta_{1}}{4\pi\beta_{0}^{3}} \frac{\ln(1-2\lambda)((2\lambda-1)\ln(1-2\lambda)-2) - 4\lambda}{1-2\lambda} - \frac{1}{2\pi\beta_{0}} \frac{(2\lambda(1-\ln(1-2\lambda)) + \ln(1-2\lambda))}{1-2\lambda} \ln \frac{\mu_{R}^{2}}{x_{Q}^{2}m_{H}^{2}} \right),$$
(A.38)
(A.39)

$$g_{3}(\lambda) = \left(A^{(1)}\ln\frac{1}{x_{Q}^{2}} + B^{(1)}\right) \left(-\frac{\lambda}{1-2\lambda}\ln\frac{\mu_{R}^{2}}{x_{Q}^{2}m_{H}^{2}} + \frac{\beta_{1}}{2\beta_{0}^{2}}\frac{2\lambda + \ln(1-2\lambda)}{1-2\lambda}\right) - \frac{1}{2\pi\beta_{0}}\frac{\lambda}{1-2\lambda} \left(A^{(2)}\ln\frac{1}{x_{Q}^{2}} + B^{(2)}\right) - \frac{A^{(3)}}{4\pi^{2}\beta_{0}^{2}}\frac{\lambda^{2}}{(1-2\lambda)^{2}} + A^{(2)}\left(\frac{\beta_{1}}{4\pi\beta_{0}^{3}}\frac{2\lambda(3\lambda-1) + (4\lambda-1)\ln(1-2\lambda)}{(1-2\lambda)^{2}} - \frac{1}{\pi\beta_{0}}\frac{\lambda^{2}}{(1-2\lambda)^{2}}\ln\frac{\mu_{R}^{2}}{x_{Q}^{2}m_{H}^{2}}\right) + A^{(1)}\left(\frac{\lambda\left(\beta_{0}\beta_{2}(1-3\lambda) + \beta_{1}^{2}\lambda\right)}{\beta_{0}^{4}(1-2\lambda)^{2}} + \frac{(1-2\lambda)\ln(1-2\lambda)\left(\beta_{0}\beta_{2}(1-2\lambda) + 2\beta_{1}^{2}\lambda\right)}{2\beta_{0}^{4}(1-2\lambda)^{2}} + \frac{\beta_{1}^{2}}{4\beta_{0}^{4}}\frac{(1-4\lambda)\ln^{2}(1-2\lambda)}{(1-2\lambda)^{2}} - \frac{\lambda^{2}}{(1-2\lambda)^{2}}\ln^{2}\frac{\mu_{R}^{2}}{x_{Q}^{2}m_{H}^{2}} - \frac{\beta_{1}}{2\beta_{0}^{2}}\frac{(2\lambda(1-2\lambda) + (1-4\lambda)\ln(1-2\lambda))}{(1-2\lambda)^{2}}\ln\frac{\mu_{R}^{2}}{x_{Q}^{2}m_{H}^{2}}\right).$$
(A.40)

The expressions of $\tilde{R}', \, \delta \tilde{R}'$, and \tilde{R}'' used in eq. (A.26) are defined as

$$\tilde{R}' = -\frac{d}{d\tilde{L}} \left(\tilde{L}g_1(\lambda) \right), \quad \delta \tilde{R}' = -\frac{dg_2(\lambda)}{d\tilde{L}}, \quad \tilde{R}'' = \frac{d\tilde{R}'}{d\tilde{L}}.$$
(A.41)

The β function coefficients read

$$\beta_{0} = \frac{11C_{A} - 2n_{f}}{12\pi},$$

$$\beta_{1} = \frac{17C_{A}^{2} - 5C_{A}n_{f} - 3C_{F}n_{f}}{24\pi^{2}},$$

$$\beta_{2} = \frac{2857C_{A}^{3} + (54C_{F}^{2} - 615C_{F}C_{A} - 1415C_{A}^{2})n_{f} + (66C_{F} + 79C_{A})n_{f}^{2}}{3456\pi^{3}}.$$
(A.42)

Finally, we have

(1)

$$\begin{aligned} A^{(1)} &= 2C_A, \\ A^{(2)} &= \left(\frac{67}{9} - \frac{\pi^2}{3}\right) C_A^2 - \frac{10}{9} C_A n_f, \\ A^{(3)} &= \left(-22\zeta_3 - \frac{67\pi^2}{27} + \frac{11\pi^4}{90} + \frac{15503}{324}\right) C_A^3 + \left(\frac{10\pi^2}{27} - \frac{2051}{162}\right) C_A^2 n_f \\ &+ \left(4\zeta_3 - \frac{55}{12}\right) C_A C_F n_f + \frac{50}{81} C_A n_f^2, \\ B^{(1)} &= -\frac{11}{3} C_A + \frac{2}{3} n_f, \\ B^{(2)} &= \left(\frac{11\zeta_2}{6} - 6\zeta_3 - \frac{16}{3}\right) C_A^2 + \left(\frac{4}{3} - \frac{\zeta_2}{3}\right) C_A n_f + C_A C_F. \end{aligned}$$
(A.44)

A.3 Matching to fixed order

In this section we discuss the matching of the resummed and the fixed-order results. We work at the level of the cumulative distribution Σ , that at NNLO reads

$$\Sigma^{\text{NNLO}}(p_{\perp}) = \sigma_{\text{tot}}^{\text{NNLO}} - \int_{p_{\perp}}^{\infty} \mathrm{d}p_{\perp}' \left[\frac{\mathrm{d}\sigma}{\mathrm{d}p_{\perp}}\right]^{\text{NLO}}.$$
 (A.45)

We stress that in the main text we only show results for the differential p_{\perp} distribution, therefore we label them as NLO. This corresponds to what we label as NNLO at the integrated level in this appendix. Since the total $gg \rightarrow H$ cross section is not known in the full SM beyond NLO, we approximate the NNLO correction to $\sigma_{\text{tot}}^{\text{NNLO}}$ by multiplying the exact NLO result by the NNLO/NLO K factor as computed in the $m_t \rightarrow \infty, m_b \rightarrow 0$ limit. We stress, however, that at the level of the differential distributions we are interested in, this approximation is formally a N³LL effect, and it is beyond the accuracy considered in our study.

In order to assess the uncertainty associated with the matching procedure, we consider here two different matching schemes. The first scheme we introduce is the common additive scheme discussed in the main text defined as

$$\Sigma_{\text{add}}(p_{\perp}) = \Sigma^{\text{NNLL}}(p_{\perp}) + \Sigma^{\text{NNLO}}(p_{\perp}) - \mathcal{T}^{\text{NNLO}}\left[\Sigma^{\text{NNLL}}(p_{\perp})\right].$$
(A.46)

Since the $\mathcal{O}(\alpha_s^2)$ (relative to the Born) collinear coefficient functions and virtual corrections are unknown in the full SM, in the additive scheme we approximate them by multiplying the HEFT ones by the exact Born squared amplitude.

The second scheme we consider belongs to the class of multiplicative schemes. In the text, we schematically defined it as

$$\Sigma_{\text{mult}}(p_{\perp}) = \Sigma^{\text{NNLL}}(p_{\perp}) \ \mathcal{T}^{\text{NNLO}}\left[\frac{\Sigma^{\text{NNLO}}(p_{\perp})}{\Sigma^{\text{NNLL}}(p_{\perp})}\right].$$
(A.47)

We recall that we indicate with $\mathcal{T}^{\text{NNLO}}[f]$ the fixed-order expansion of f to NNLO. The two schemes (A.46), (A.47) are equivalent at the perturbative order we are working at, as

they only differ by N³LO and N³LL terms. The main difference between the two schemes is that, in the multiplicative approach, unlike in the additive one, higher-order corrections are damped by the resummation factor Σ^{NNLL} at low p_{\perp} . One advantage of the multiplicative solution is that the NNLO constant terms, of formal accuracy N³LL, are automatically extracted from the fixed order in the procedure. Furthermore, as we explained in the text, in this case higher order effects introduced by the resummation follow the same scaling in p_{\perp} of the fixed-order result, which at least partially mimics higher order form-factor effects.

However, there is a drawback in using eq. (A.47) as is. Indeed, Σ^{NNLL} does not tend to one for $p_{\perp} \gg Q$, but rather to the luminosity factor defined in eq. (A.28) evaluated at $\tilde{L} = 0$. Therefore, the fixed-order result Σ^{NNLO} at large p_{\perp} receives a relative spurious correction of order α_s^3

$$\Sigma_{\text{mult}}(p_{\perp}) \sim \Sigma^{\text{NNLO}}(p_{\perp}) \left(1 + \mathcal{O}(\alpha_s^3)\right).$$
 (A.48)

Despite being formally of higher order, these effects can be moderately sizable in processes with large K factors such as Higgs production. There are different possible solutions to this problem. In ref. [29] the resummed factor (and the relative expansion) was modified by introducing a damping factor as

$$\Sigma^{\text{NNLL}} \to (\Sigma^{\text{NNLL}})^Z,$$
 (A.49)

where Z is a p_{\perp} -dependent exponent that effectively acts as a smoothened Θ function that tends to zero at large p_{\perp} . This solution, however, introduces new parameters that control the scaling of the damping factor Z (see section 4.2 of ref. [29] for details). In this article we adopt a simpler solution, which avoids the introduction of extra parameters in the matching scheme. We therefore define the multiplicative matching scheme by normalizing the resummed prefactor to its asymptotic value for at $\tilde{L} \to 0$. This is simply given by

$$\Sigma_{\text{asym.}}^{\text{NNLL}} = \lim_{\tilde{L} \to 0} \mathcal{L}(k_{\perp 1}).$$
(A.50)

We obtain

$$\Sigma_{\text{mult}}(p_{\perp}) = \frac{\Sigma^{\text{NNLL}}(p_{\perp})}{\Sigma_{\text{asym.}}^{\text{NNLL}}} \mathcal{T}^{\text{NNLO}}\left[\Sigma_{\text{asym.}}^{\text{NNLL}} \frac{\Sigma^{\text{NNLO}}(p_{\perp})}{\Sigma^{\text{NNLL}}(p_{\perp})}\right],\tag{A.51}$$

where

$$\Sigma^{\text{NNLL}}(p_{\perp}) \xrightarrow[p_{\perp} \gg Q]{} \Sigma^{\text{NNLL}}_{\text{asym.}}.$$
 (A.52)

This ensures that in the $p_{\perp} \gg Q$ limit eq. (A.51) reproduces by construction the fixed-order result, and no large spurious, higher-order, corrections arise in this region. The detailed matching formulas for the two schemes considered in our analysis are reported below.

We start by introducing a convenient notation for the perturbative expansion of the various ingredients. We define

$$\sigma_{\rm tot}^{\rm NNLO} = \sum_{i=0}^{2} \sigma^{(i)}, \qquad \Sigma^{\rm NNLO}(p_{\perp}) = \sigma^{(0)} + \sum_{i=1}^{2} \Sigma^{(i)}(p_{\perp}), \qquad (A.53)$$

where

$$\Sigma^{(i)}(p_{\perp}) = \sigma^{(i)} + \bar{\Sigma}^{(i)}(p_{\perp}), \qquad \bar{\Sigma}^{(i)}(p_{\perp}) \equiv -\int_{p_{\perp}}^{\infty} \mathrm{d}p'_{\perp} \frac{\mathrm{d}\Sigma^{(i)}(p'_{\perp})}{\mathrm{d}p'_{\perp}}.$$
 (A.54)

Moreover, we denote the perturbative expansion of the resummed cross section Σ^{NNLL} as

$$\mathcal{T}^{\text{NNLO}}\left[\Sigma^{\text{NNLL}}(p_{\perp})\right] = \sigma^{(0)} + \sum_{i=1}^{2} \Sigma^{(i)}_{\text{NNLL}}(p_{\perp}).$$
(A.55)

With this notation, the additive scheme of eq. (A.46) becomes (for simplicity we drop the explicit dependence on p_{\perp} in the following)

$$\Sigma_{\text{add}} = \Sigma^{\text{NNLL}} + \left\{ \sigma^{(1)} + \bar{\Sigma}^{(1)} - \Sigma^{(1)}_{\text{NNLL}} \right\} + \left\{ \sigma^{(2)} + \bar{\Sigma}^{(2)} - \Sigma^{(2)}_{\text{NNLL}} \right\},$$
(A.56)

where the three terms in curly brackets denote the NLO, NNLO and N³LO contributions to the matching, respectively.

For the multiplicative scheme we need to introduce the perturbative expansion of the asymptotic value $\Sigma_{\text{asym.}}^{\text{NNLL}}$, defined in eq. (A.50). We write

$$\Sigma_{\text{asym.}}^{\text{NNLL}} = \sigma^{(0)} + \Sigma_{\text{asym.}}^{(1)}.$$
 (A.57)

With this notation the matching formula (A.51) reads

$$\Sigma_{\text{mult}}(p_{\perp}) = \frac{\Sigma_{\text{asym.}}^{\text{NNLL}}}{\Sigma_{\text{asym.}}^{\text{NNLL}}} \left[\sigma^{(0)} + \left\{ \sigma^{(1)} + \bar{\Sigma}^{(1)} + \Sigma_{\text{asym.}}^{(1)} - \Sigma_{\text{NNLL}}^{(1)} \right\} + \left\{ \sigma^{(2)} + \bar{\Sigma}^{(2)} - \Sigma_{\text{NNLL}}^{(2)} + \frac{\Sigma_{\text{asym.}}^{(1)}}{\sigma^{(0)}} (\sigma^{(1)} + \bar{\Sigma}^{(1)}) + \frac{(\Sigma_{\text{NNLL}}^{(1)})^2}{\sigma^{(0)}} - \frac{\Sigma_{\text{NNLL}}^{(1)}}{\sigma^{(0)}} (\sigma^{(1)} + \bar{\Sigma}^{(1)} + \Sigma_{\text{asym.}}^{(1)}) \right\} \right],$$
(A.58)

where, as above, we grouped the terms entering at NLO, and NNLO within curly brackets.

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