

Spin-dependent emission from arrays of planar chiral nanoantennas due to lattice and localized plasmon resonances

Citation for published version (APA):

Cotrufo, M., Osorio, C. I., & Koenderink, A. F. (2016). Spin-dependent emission from arrays of planar chiral nanoantennas due to lattice and localized plasmon resonances. *ACS Nano*, *10*(3), 3389–3397.
<https://doi.org/10.1021/acsnano.5b07231>

DOI:

[10.1021/acsnano.5b07231](https://doi.org/10.1021/acsnano.5b07231)

Document status and date:

Published: 08/02/2016

Document Version:

Accepted manuscript including changes made at the peer-review stage

Please check the document version of this publication:

- A submitted manuscript is the version of the article upon submission and before peer-review. There can be important differences between the submitted version and the official published version of record. People interested in the research are advised to contact the author for the final version of the publication, or visit the DOI to the publisher's website.
- The final author version and the galley proof are versions of the publication after peer review.
- The final published version features the final layout of the paper including the volume, issue and page numbers.

[Link to publication](#)

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal.

If the publication is distributed under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license above, please follow below link for the End User Agreement:

www.tue.nl/taverne

Take down policy

If you believe that this document breaches copyright please contact us at:

openaccess@tue.nl

providing details and we will investigate your claim.

Spin-Dependent Emission from Arrays of Planar Chiral Nanoantennas Due to Lattice and Localized Plasmon Resonances

1 Michele Cotrufo,^{*,†,‡} Clara I. Osorio,[‡] and A. Femius Koenderink[‡]

COBRA Research Institute, Eindhoven University of Technology, 5600 MB Eindhoven, The Netherlands, and Center for Nanophotonics, FOM Institute AMOLF, Science Park 104, 1098 XG Amsterdam, The Netherlands

E-mail: m.cotrufo@tue.nl

2 **Abstract**

3 Chiral plasmonic nanoantennas manifest a strong asymmetric response to circularly
4 polarized light. Particularly, the geometric handedness of a plasmonic structure can
5 alter the circular polarization state of light emitted from nearby sources, leading to
6 a spin-dependent emission direction. In past experiments, these effects have been at-
7 tributed entirely to the localized plasmonic resonances of single antennas. In this work
8 we demonstrate that, when chiral nanoparticles are arranged in diffractive arrays, lat-
9 tice resonances play a primary role in determining the spin-dependent emission of light.
10 We fabricate 2D diffractive arrays of planar chiral metallic nanoparticles embedded in a
11 light-emitting dye-doped slab. By measuring the polarized photoluminescence enhance-
12 ment we show that the geometric chirality of the array's unit cell induces a preferential

*To whom correspondence should be addressed

[†]COBRA Research Institute, Eindhoven University of Technology, 5600 MB Eindhoven, The Netherlands

[‡]Center for Nanophotonics, FOM Institute AMOLF, Science Park 104, 1098 XG Amsterdam, The Netherlands

1 circular polarization, and that both the localized surface plasmon resonance and the
2 delocalized hybrid plasmonic-photonic mode contribute to this phenomenon. By fur-
3 ther mapping the angle-resolved degree of circular polarization, we demonstrate that
4 strong chiral dissymmetries are mainly localized at the narrow emission directions of
5 the surface lattice resonances. We validate these results against a coupled dipoles model
6 calculation, which correctly reproduces the main features. Our findings demonstrate
7 that, in diffractive arrays, lattice resonances play a primary role into the light spin-orbit
8 effect, introducing a highly non-trivial behavior in the angular spectra.

9 **Keywords**

10 localized plasmon resonances, surface lattice resonances, k-space polarimetry, chirality, plas-
11 monic nanoantennas, spin-orbit

12 Plasmonic nanoantennas can control, manipulate and redirect emission of light by provid-
13 ing an interface between plane waves in the far-field and localized emitters in the near-field.¹
14 While intrinsically based on the material resonance of free electrons, shape and aspect ratio
15 of these nanoantennas can be used to tune antenna performance in terms of resonance fre-
16 quency, near-field enhancement and spontaneous emission decay rate enhancement.² More-
17 over, antenna shape can impart preferential polarization on the emission of nearby emitters.²
18 Indeed, localized surface plasmon resonances (LSPRs) supported by anisotropic structures
19 such as nanorods, bowtie antennas, patch antennas or split rings, can strongly favor particu-
20 lar electric field components.^{3,4} Therefore, light polarization plays a key-role in the behavior
21 of nano-antennas.

22 Strong polarization responses are not exclusive to linear polarization: plasmonic anten-
23 nas can be highly selective with respect to the helicity of light if they possess a geometric
24 chirality.⁵ Chiral objects cannot be superimposed onto their mirror image by mere rotations
25 and translations, and interact differently with right-handed (RCP) and left-handed (LCP)
26 circularly polarized light (CPL). For chiral molecular matter this interaction is usually de-

1 scribed in terms of far-field quantities like optical activity (OA) which describes the rotation
2 of incident linear polarization, or circular dichroism (CD) which accounts for preferential
3 absorption of right or left-handed circular polarized light. Several experimental and the-
4 oretical studies have shown that planar chiral structures such as gammadians⁶ or spirals⁷
5 and 3D chiral structures like helices^{8,9} can exhibit large optical activity and circular dichro-
6 ism,¹⁰⁻¹⁴ and can enhance the weak circular dichroism signals obtained from biological chiral
7 molecules.^{5,15} Chiral nanostructures can also alter the far-field polarization state of fluo-
8 rescent sources positioned in their near-field. Split-ring resonators, for example, have been
9 shown to provide spin control¹⁶ of photons emitted from II-VI semiconductor quantum dots.
10 In a recent experiment by Meinzer *et al.*¹⁷ it was shown that a planar chiral arrangement
11 of two silver nanorods embedded in a slab of achiral emitters gives rise to a substantial
12 asymmetry in the intensity of LCP and RCP light emitted normal to the sample. In this
13 experiment the handedness of emission is inherited from the handed nature of the localized
14 plasmonic resonances of the antennas.

15 In this work we investigate periodic arrays of planar chiral antennas interacting with
16 achiral emitters, and show that diffractive resonances play a dominant role in determining
17 the spin-dependent directional emission. Plasmonic antennas arrays with pitches comparable
18 to the wavelength are known to exhibit hybrid plasmonic-photonic modes with very narrow
19 line-widths¹⁸ known as surface lattice resonances (SLRs).¹⁹ These modes arise from radia-
20 tive coupling between LSPRs and waves diffracted into the plane of the array. For simple
21 antenna shapes, like rods, this hybrid resonance has been shown to strongly improve the
22 photoluminescence properties of nearby emitters²⁰ and, in particular, to drastically mod-
23 ify their angular emission pattern.²¹ While Meinzer *et al.*,¹⁷ and Kruk *et al.*¹⁶ attributed
24 chiral emission properties to the physics of single antennas, their structures were actually
25 arranged in arrays, triggering the question how surface lattice resonances impact handedness
26 in emission.

1 We report k-space polarimetry measurements^{22,23} that quantify how asymmetries in circu-
 2 larly polarized light emission are distributed over angle, as mapped across the backaperture
 3 of a microscope objective. We demonstrate that the SLR introduces much larger CPL-
 4 asymmetries at selected angles than observed in experiments that only consider emission
 5 normal to the array.¹⁷ Our experimental results are validated against a coupled-dipole model.

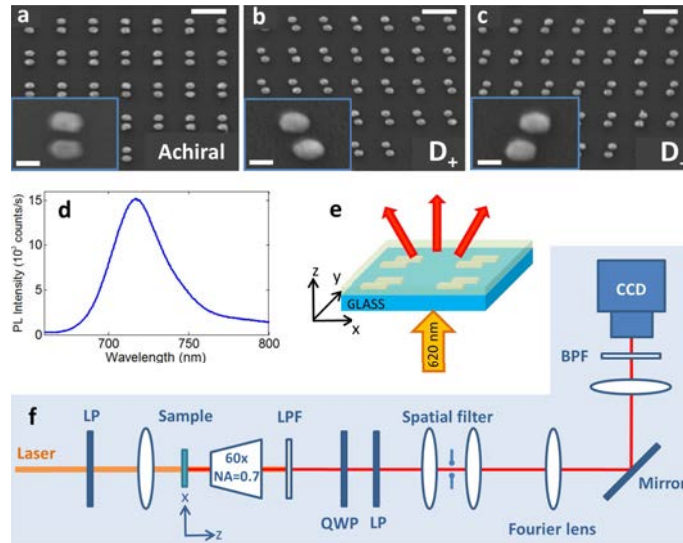


Figure 1: (a-c) SEM micrographs of the arrays of (a) achiral, (b) D_+ and (c) D_- structures. The pitch of the array is 480 nm. The scalebars of the main pictures are 500 nm. The inset of each figure shows a zoom on the correspondice unit cell. The scalebar is 100 nm. (d) Fluorescence emission from the dye Rh800 collected from a region far from the plasmonic structures. (e) Schematic of the sample, the experiment configuration for the k-space polarimetry measurements, and the reference frame. (f) Schematic of the setup. The laser light ($\lambda = 620$ nm) is focused on the sample from the glass side and the luminescence is collected on the other side through a 60x objective. After filtering out the laser with a long pass filter (LPF) and selecting the desired state of polarization with the quarter wave plate (QWP) and the linear polarizer (LP), the beam is spatially filtered with a $400 \mu\text{m}$ diameter pinhole. A flippable Fourier lens allows to image on the CCD either the plane of the sample or the back focal plane of the objective. A band pass filter (BPF) in front of the camera allows to acquire monochromatic Fourier images.

6 Sample design, optimization and characterization

7 In this work we study periodic arrays of chiral and achiral dimer antennas fabricated on
 8 a glass substrate and embedded in a thin dye-doped polymer layer. We emphasize that,

1 apart from the small refractive index contrast introduced by the substrate, the structures
2 considered in this work are not 3D chiral, but they possess a planar chirality. Previous
3 works have shown²⁴ that planar chiral structures feature strong asymmetric response for
4 the transmission of CPL, because the handedness is reversed when they are observed from
5 opposite sides.

6 The achiral dimers consist of two identical silver rod antennas shifted along their short
7 dimension (fig. 1a). The planar chiral structures were obtained by further shifting the rods
8 along their long dimension to obtain a relative displacement equal to half their length (*i.e.*
9 60 nm in the geometry we adopted, see below). According to the direction of the shift we
10 label the dimers D_+ and D_- , as shown in the inset of figs. 1(b-c). This unit cell is based on
11 the design by Meinzer *et al.*¹⁷ Fig. 1e illustrates schematically the geometry of the sample,
12 the chosen reference frame and the excitation-collection configuration used for the k-space
13 polarimetry measurements discussed below.

14 The geometry of the sample (rods length and array pitch) was optimized using FDTD
15 simulations (with a commercial solver²⁵) to ensure that both the LSPR and the SLR wave-
16 length fall in the emission band of the dye used in this experiment, *i.e.* $\lambda \approx 700 - 780 \text{ nm}$
17 (see fig. 1d). We notice that further optimizations (*e.g.* the gap between the rods) could
18 lead to larger values of the chiral dissymmetry, but this would go behind the scope of the
19 present work. We calculated normal-incidence transmittance spectra of the sample for dif-
20 ferent nanorod lengths, array pitches and impinging polarizations. Figs. 2(a-b) shows the
21 different behaviors for light linearly polarized along (panel a) and perpendicular to (panel b)
22 the dimer rods. The transmittance of an x-polarized beam (fig. 2a) shows a broad minimum,
23 whose spectral position strongly depends on nanorod length. This feature is identified as the
24 dipolar LSPR of the dimer plasmonic antenna. For polarization rotated by 90° , a much nar-
25 rower transmission minimum appears with a spectral position strongly affected by the lattice
26 period (fig. 2b), but independent of the nanorod length (see Supplementary Information).
27 Moreover, the dip's wavelength lies close to the Rayleigh anomaly condition,¹⁸ indicated by

1 the dashed-dotted blue line in fig. 2b and given by $\lambda = n_{glass} \cdot p$, where n_{glass} is the substrate
2 refractive index and p is the lattice pitch. These characteristics are typical signatures of the
3 SLR.¹⁸ Based on these simulations, and on the emission band of the dye used (see fig. 1d)
4 we set the single rod dimensions to 120 nm \times 70 nm \times 30 nm and the array pitch to $p =$
5 480 nm in our experiments. The vertical shift between the rod centers is 130 nm and, in
6 simulations and experiments, the rods are embedded in a 65 nm thick SU8 polymer layer
7 hosting the dye Rh800.

8 Having chosen a promising geometry, we evaluated the average of the square modulus of
9 the electric field in the dye-doped polymer layer for different impinging beam polarizations.
10 Due to the reciprocity theorem, this calculation gives a prediction for the far-field polarized
11 luminescence enhancement of the dye (averaged over all possible positions in the polymer
12 slab) expected for emission normal to the sample plane. Fig. 2c shows the calculated
13 photoluminescence enhancement (PLE) for an array of D_+ structures. The predicted x-
14 polarized luminescence enhancement shows a broad feature whose position and linewidth
15 agree well with the x-polarized LSPR. The y-polarized signal is instead characterized by
16 a narrow peak, due to the SLR. When considering the right and left handed circularly
17 polarized components of the luminescence enhancement, a clear difference between the two
18 signals is visible for both the LSPR and the SLR. In other words, the simulations predict
19 a helicity-dependent photoluminescence enhancement for observation normal to the sample,
20 in agreement with previous observations.¹⁷

21 Fig 3a shows measured transmittance spectra of the sample under white light illumina-
22 tion for different impinging polarizations and different chirality of the plasmonic structures.
23 The transmittance of an x-polarized (dashed lines) and y-polarized (solid lines) excitation
24 beam shows the signature of the LSPR and SLR, respectively, in good agreement with the
25 calculations (figs. 2(a-b)). The transmittance curves for the achiral and chiral structures
26 are, even for a linearly polarized input, slightly different: the SLR minimum from an array of
27 chiral structures is blue-shifted by about 10 nm with respect to an array of achiral antennas.

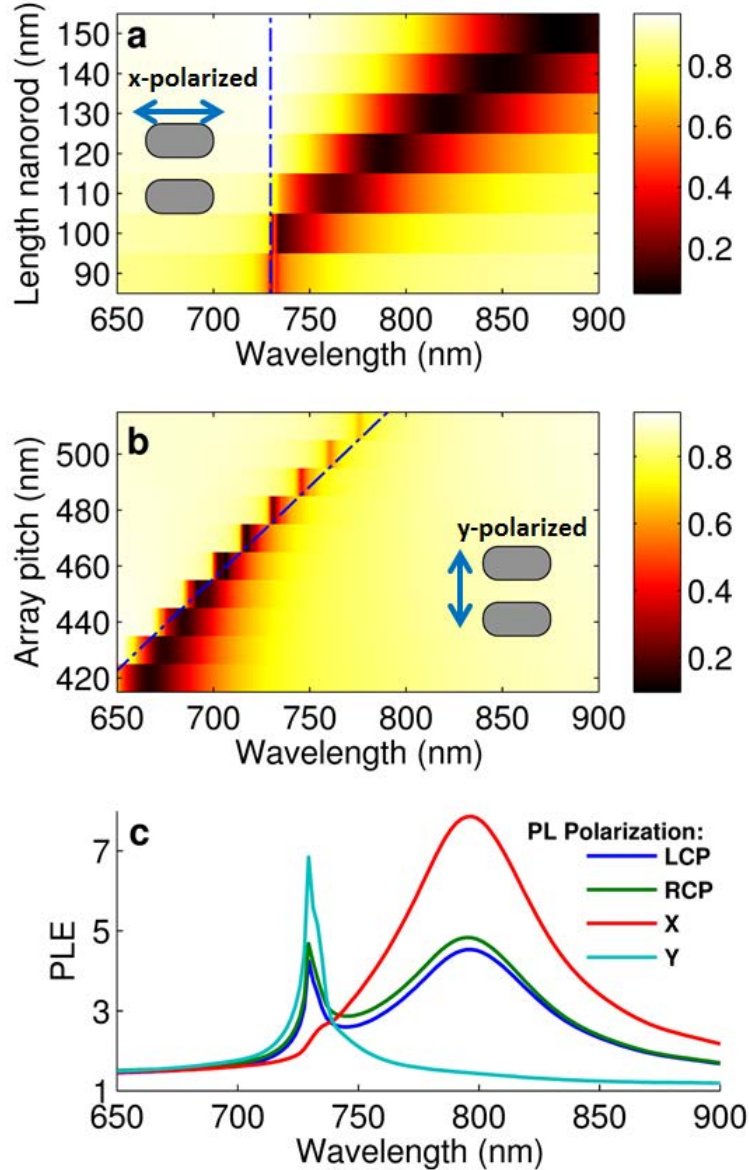


Figure 2: Numerical optimization of the sample geometry. (a) Calculated x-polarized transmittance of an array of achiral structures for different lengths L of the rods and for an array pitch of $p = 480$ nm. The vertical dashed-dotted line shows the position of the Rayleigh's anomaly. (b) Calculated y-polarized transmittance of an array of achiral structures for different array pitches p and for a rod length of 120 nm. The dashed-dotted line shows the dispersion relation of the Rayleigh's anomaly. (c) Calculated luminescence enhancement for a D_+ structure with $L = 120$ nm and $p = 480$ nm, for different luminescence polarizations.

- 1 For the LSPR the shift has approximately the same absolute value, but is opposite in sign.
- 2 We attribute this spectral shift to the different near-field interactions between the two silver
- 3 rods, caused by the different geometry of the achiral and chiral structures.

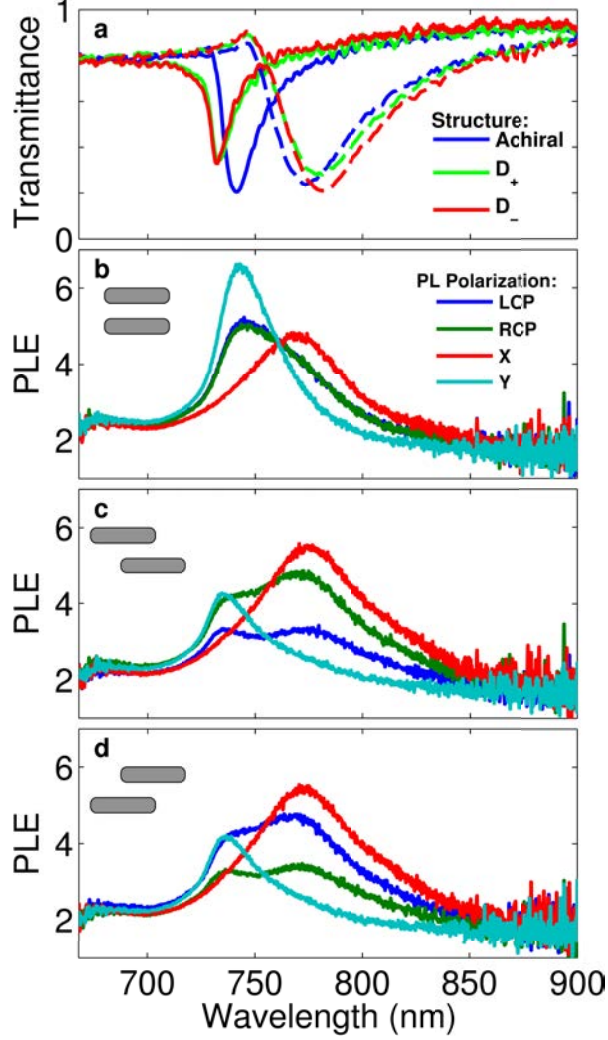


Figure 3: (a) Transmittance spectra of the sample for y- (solid lines) and x-polarized (dashed lines) white light illumination and for different chirality of the array's unit cell, as indicated in the legend. (b)-(d) Polarized photoluminescence enhancement (PLE) for different collection polarizations and for (b) achiral, (c) D_+ and (d) D_- structures. The geometry of the unit cell is shown in the inset of each plot. The PLE is dominated by the LSPR (SLR) for the x-polarized (y-polarized) collection. The LCP and RCP components of the PLE are equal for the achiral structure. A D_+ structure, instead, shows a different PLE for the two circular polarizations; the effect is mirrored for the case of the D_- structure. In these measurements the sample is excited from the polymer side and the signal is collected from the glass side.

1 Results and discussion

2 Chiral photoluminescence enhancement from SRL and LSPR

3 We start by studying how the LSPR and SLR modify the emission spectra of the dye,
 4 measuring in a low-NA geometry similar to the configuration used by Meinzer *et al.*¹⁷ In these

1 measurements, the sample is pumped from the polymer side and the luminescence is collected
2 from the glass side. To calculate the polarized photoluminescence enhancement (PLE), we
3 measured the LCP, RCP, x- and y-polarized components of the photoluminescence. Each
4 measurement was normalized to a reference measurements (with the same polarization)
5 taken from a region of the sample without structures. Figure 3(b-d) shows the results for
6 the achiral, D_+ and D_- structures. For the array of achiral structures, the polarized PLE
7 shows two distinct features for the X (red line) and Y (cyan line) polarizations, (fig. 3b).
8 The wavelengths and linewidths of these features agree very well with the transmittance
9 measurements for the corresponding excitation polarizations. Therefore, we interpret these
10 enhancements as the result of the interaction between the emitters and the LSPR and SLR
11 of the particles array. Circularly polarized PLEs show no difference between LCP and RCP
12 light for the achiral structures (blue and green curves in fig. 3b) .

13 In contrast to the achiral structures, the chiral structures show a clear difference between
14 the LCP and RCP polarized photoluminescence enhancement. In the wavelength range
15 spanned by the SLR and the LSPR, an asymmetry of about 20% is observed between the
16 two circular polarizations. This difference is mirrored when inverting the geometric chirality
17 of the structure (cf. fig. 3c and 3d). In addition to confirming the effect of the LSPR,
18 already reported by Meinzer *et al.*,¹⁷, we demonstrate here that also the emission from
19 the SLR shows a pronounced asymmetry in the circular polarization of the light emitted.
20 While the measured values of the PLE are in good agreement with the calculations (fig. 2c)
21 for the LSPR, the measurements show a broadening and a weakening of the signal due to
22 the SLR. This effect can be attributed to both fabrication imperfections and to the finite
23 angular acceptance of our setup. As the emission from the SLR strongly changes in angle
24 with wavelength,²¹ the sharp peak calculated for emission normal to the sample (fig. 2c) is
25 broadened by angular integration over our set up NA.

26 Even far from any plasmonic resonances, the measured polarized photoluminescence en-
27 hancement has a value of about 2. According to the FDTD calculations (*i.e.*, at fixed source

1 strength), the PLE is expected to be about 1.5 at a wavelength of 650 nm (see fig. 2c)
 2 when ignoring the pump field enhancement. Numerically evaluating the enhancement of the
 3 electric field at the laser wavelength excitation ($\lambda = 620$ nm), we found a spatially averaged
 4 value of 1.4 which leads to an overall expected PLE of about 2.1 (given by the product of
 5 the excitation and emission enhancement), in a good agreement with the measurements.

6 **K-space polarimetry measurements on planar chiral plasmonic an-** 7 **tennas**

8 We now discuss the polarized angular-emission of the sample measured with the k-space
 9 polarimetry setup shown in fig. 1f and described in more detail in the Methods section.
 10 As shown in previous works,^{16,22,23} by combining a Fourier microscope and a polarimeter
 11 we can measure the Stokes parameters (which describe the full polarization state of the
 12 emitted light, see Methods section) for each point of the back focal plane of the objective,
 13 *i.e.* $S_i = S_i(k_x, k_y)$. Furthermore, by using different narrow band-pass filters in front of
 14 the detector we can measure the Stokes parameters as a function of the emission frequency
 15 within the emission band of our dye. Therefore, we characterize the light emitted by a source
 16 in terms of *momentum, energy and polarization*.

17 For this measurement, the sample was excited from the glass side and photoluminescence
 18 was collected from the polymer side. For the achiral structures, figs. 4(a-f) show the change
 19 of the intensity distribution in the back focal plane (*i.e.* S_0 , total intensity) as the emission
 20 wavelength varies from 700 nm to 750 nm in steps of 10 nm. All the plots are normalized to
 21 their maximum, which is typically of the order of 10^3 counts. The emission patterns show
 22 narrow circular features whose position strongly depends on emission wavelength. These
 23 emission patterns are characteristic of the SLR²¹ and result from the diffractive coupling of
 24 the LSPR of the single antennas. Each circle corresponds to a single frequency cut through
 25 the dispersion relation $\omega(\mathbf{k}_{\parallel})$ of the SLR, which is repeated at every reciprocal lattice point
 26 $\mathbf{G}_{m,n} = (m, n)\frac{2\pi}{d}$. Each point of a circle represents a wave vector \mathbf{k}_{\parallel} (allowed for that

1 particular frequency) with origin on the corresponding $\mathbf{G}_{m,n}$ point. To verify the role of
 2 the SLR, we fitted the radius of curvature of the observed feature, while keeping the center
 3 of the circle fixed at the corresponding reciprocal lattice vector, as shown in fig. 4f. The
 4 results of this fitting procedure are shown in Fig. 4g. A linear fit of the data gives a value
 5 of $n = 1.52 \pm 0.01$ for the effective refractive index of the SLR. This value is identical to the
 6 nominal value of the refractive index of the supporting glass substrate, confirming that the
 7 SLR is due to diffractive coupling to glass.²⁶

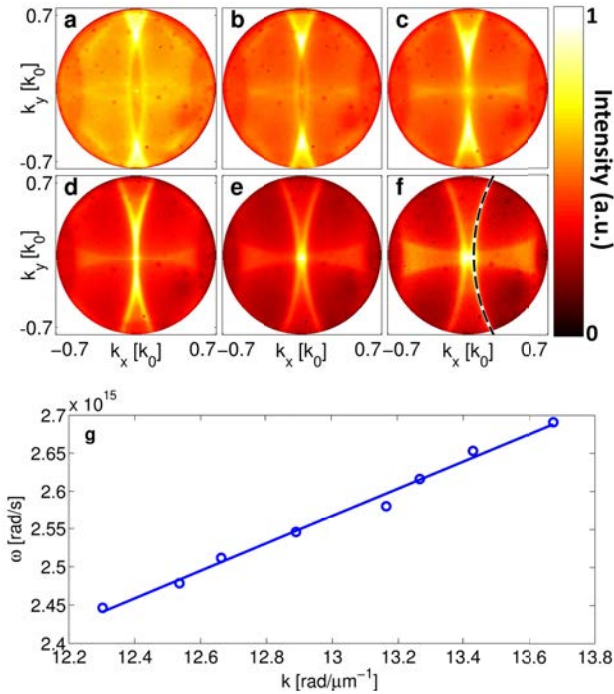


Figure 4: (a)-(f) Angular distribution of the total emitted intensity (*i.e.* the Stokes parameter S_0) from the array of achiral structures, for different emission wavelengths: (a) $\lambda = 700$ nm, (b) $\lambda = 710$ nm, (c) $\lambda = 720$ nm, (d) $\lambda = 730$ nm, (e) $\lambda = 740$ nm, (f) $\lambda = 750$ nm. All the plots are normalized to their respective maximum value. The vertical and horizontal axes indicate the values of the in-plane coordinates of the wave-vector, normalized to the absolute value of the corresponding free-space wave-vector. The maximum value of 0.7 corresponds to the NA of our objective. The dashed circular segment in (f) shows an example of the fits used to calculate the dispersion curve. (g) Result of the fitting procedure for all the measured wavelengths in the range 700 – 770 nm. The solid line is a linear fit to the data, which gives a value of $n = 1.52 \pm 0.01$ for the effective refractive index.

8 The angular positions of the different features shown in each of the figs. 4(a-f) indicate
 9 a clear symmetry in k -space, as expected since the array is square. However, a strong

1 asymmetry in the intensity is observed: the vertical features (*i.e.* the circular segments
2 located in the area $k_x \simeq 0$) are much brighter than the horizontal ones. This effect can
3 be attributed to the anisotropy of the unit cell, which leads to a mainly x-polarized dipole
1 moment for the dimer antennas. As the radiation pattern of an electric dipole is maximum
2 at the directions perpendicular to its axis,²⁷ a stronger emission in the yz plane is expected,
3 as confirmed by our measurements. For $\lambda = 740 \text{ nm}$ (fig. 4e) all the circles intersect each
4 other at $(k_x, k_y) \simeq 0$. This corresponds to a strong emission into the direction orthogonal
5 to the sample plane and coincides with the second order Bragg diffraction condition for the
6 SLR. Indeed, in the normal-incidence transmittance measurements and in the low-NA PLE
7 measurements the signal related to the SLR appears at $\lambda \simeq 740 \text{ nm}$.

8 The sample emission is due to an ensemble of many incoherent and randomly located
9 sources, and therefore light emitted by different molecules do not interfere. Nevertheless,
10 the patterns observed in figs. 4(a-f) show a clear spatial coherence in the angular spectra.
11 Indeed, as explained by Langguth *et al.*,²⁸ summing over the emission of incoherent sources,
12 randomly distributed in a periodic array, still leads to a spatial coherence of emission. The
13 angular spectra of the emission from the ensemble is identical to that of a single source
14 located in particular position, apart for the smoothing of some intensity variations that
15 occur solely at the crossings of the observed circles.²⁸

16 After having characterized the angle-resolved intensity distribution of emission, we ana-
17 lyze the angular dependence of the polarization properties, in particular the degree of circular
18 polarization (DCP, as defined by equation 2c in the Methods section). Fig. 5(a-e) shows
19 the DCP for five emission wavelengths (700, 720, 740, 760 and 770 nm) for the case of the
20 achiral antennas. According to the definition of DCP a positive (negative) DCP denotes
21 emission directions for which the RCP (LCP) component of light is more enhanced. Inter-
22 estingly, even for the achiral geometry, pronounced asymmetries between RCP and LCP (up
23 to a maximum value of $DCP \simeq 0.7$) are observed for certain emission angles. The greatest
24 (absolute) values of the DCP are localized along narrow areas which correspond to the SLR

25 emission features. Since in absence of scatterers the emission is unpolarized for all angles in
 26 the objective NA, the induced polarization is due to the LSPR and to the SLR, that is ap-
 27 parent as the set of sharp features. Somewhat similar effects, *i.e.*, handed optical responses
 1 for non-handed structures upon asymmetric observation conditions, were already reported
 2 in both scattering²⁹⁻³¹ and PLE¹⁶ experiments, and they have been sometimes referred to as
 3 *extrinsic chirality*^{29,30} and pseudochirality.³² They are due to the fact that even for an achiral
 4 structure, the overall experimental configuration, including the oblique collection direction
 5 and the structure, is geometrically chiral. For achiral structures the DCP is antisymmetric
 6 for reflections across the lines $k_x = 0$ and $k_y = 0$. In other words, each emission direction with
 7 a preferential circular polarization is compensated by another (specular) direction for which
 8 the circular polarization is reversed. Overall, the *integrated* chirality of the light emitted in
 9 the z-positive half-space is zero, even though emission into particular directions is preferen-
 10 tially handed. When considering the chiral structures, the DCP shows striking differences.
 11 In the center and right columns of fig. 5 we report the DCP for the D_+ (center column)
 12 and the D_- (right column) structures, for the same wavelength selection. The color-plots
 13 show a clear breaking of symmetry between RCP and LCP emission, meaning that the DCP
 14 averaged over the back aperture now shows a net bias towards a particular handedness. This
 15 handedness is inverted when the geometric chirality is inverted. Let us focus, *e.g.*, on the
 16 case $\lambda = 720$ nm (figs. 5[b,g,n]). The D_+ structures (panel g) redirect the LCP light (*i.e.*
 17 blue color) to the same directions as the achiral structures (panel b) but no circular polarized
 18 light is present (*i.e.* $DCP = 0$, white color) at angles into which the achiral structure directs
 19 RCP light. The D_- antennas (panel n) behave in exactly the opposite way: they emit RCP
 20 light at the same angles as the achiral structure, but the corresponding degree of LCP at
 21 the specular emission angles is absent.

22 From the Fourier images in fig. 4 and fig. 5 we conclude that when reporting a PLE
 23 measurement, such as the one by Meinzer¹⁷ and the ones reported in fig. 3(b-d), it is firstly
 24 important to report the lens opening angle (NA=0.12 in Fig. 3(b-d)), and secondly, that

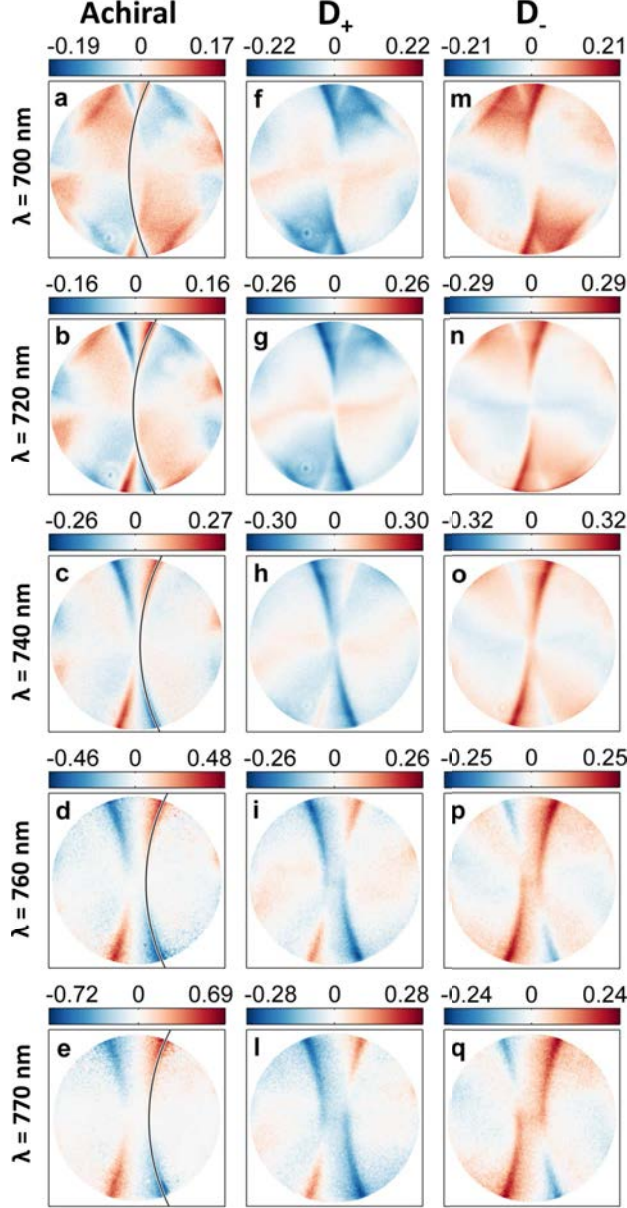


Figure 5: Angle-resolved DCP of the emission from the achiral and chiral structures. The horizontal and vertical axes for each plot are the same as fig. 4(a-f). Each row of the panel corresponds to fixed emission wavelength, ranging from 700 nm (top row) to 770 nm (bottom row), as indicated in the label. For each row the three plots correspond, from left to right, to the emission from the achiral, D_+ and D_- structures. The colorbar of each plot is indicated on top of it. The black lines in the panels (a-e) indicate the SLR emission pattern obtained from the fit of fig.4(a-f).

25 angular integration tends to obscure handed effects. Indeed, as the PLE features strongly
 26 change in angle with wavelength, in a high-NA collection optics scenario where one integrates
 27 over (rather than resolves) angle, no marked PLE features would stand out. The handed PLE

1 asymmetry reported in Figure 4 and by Meinzer *et al.*¹⁷ for a cone of angles integrated around
2 the normal direction are hence only very modest compared to the actual angle-resolved PLE
3 asymmetries.

4 Finally, as the dye used in this experiment is achiral, and the structures that we study are
5 planar, one does not expect net circular polarization when integrating over all solid angles.
6 For the achiral structure, a global vanishing of preferential emission helicity is already evident
7 from the anti-symmetry of the DCP. The planar chiral structures, instead, redirect light with
8 a preferential circular polarization to the $z > 0$ semi-space. In other words, the system formed
9 by the dye and the antennas behaves like an apparent chiral emitter into one half space. As
10 already pointed out by other authors,¹⁷ this asymmetry towards one semi-space (*i.e.* $z > 0$),
11 is compensated by an opposite asymmetry in the other semi-space. This interpretation is
12 confirmed by comparing fig. 5 with the measurements shown in fig. 3(b-d). These show
13 an opposite helicity preference consistent with the fact that light is collected from opposing
14 sample sides. As a *caveat* we do note that the air/glass interface itself introduces a further
15 symmetry breaking, whereby the above reasoning does not hold above $\text{NA} = 1$ (not reported
16 in our data).

17 **Comparison to a theoretical model**

18 We now compare the results of our experiment with the prediction of a coupled dipole
19 model,²⁷ which is described in details in the Methods section. Each antenna is modeled by
20 an electric dipole located in its center and characterized by an electric polarizability tensor.
21 For a certain external excitation of the system, we calculate the dipole moment acquired by
22 each dipole and, from it, we compute the far-field electromagnetic field. In this way, the
23 polarized angular emission of the sample can be reconstructed and the information about
24 the, *e.g.*, DCP, can be retrieved. Fig. 6 shows the results of this procedure for the same set
25 of unit cell chirality and wavelengths used in fig. 5. The calculations reproduce quite well
26 the main results observed in the experiment, *i.e.* a strongly handed response especially near

1 the SLR features, whose handedness is greatly affected by the geometric chirality of the unit
2 cell. Also the symmetries, indicating null net handedness for the achiral unit cell, and net
3 handed emission otherwise, are clearly reproduced. Discrepancies from the measured DCP
4 are also evident, in particular in the regions with $k_x \simeq 0.7$ and $k_y \simeq 0$, where the DCP has
5 opposite signs (compare fig. 5a and fig. 6a) and/or remarkably different values (cfr., *e.g.*,
6 fig. 5e and fig. 6e). We attribute these discrepancies to the inherent limitation of the dipole
7 model that inaccurately estimates rod-rod coupling for closely spaced rods. At close spacing,
8 hybridization physics requires to take into account the real shape of the fabricated structures.
9 A first pointer that the DCP is indeed highly geometry dependent is given already by the
10 dipole model: as the amplitudes of the RCP and LCP light depend on a coherent sum of
11 scattered E_x and E_y fields, varying the amplitude and phase of the polarizability tensor
12 components α_{xx} and α_{yy} , quite strongly influences the far-field polarization state. While
13 from a modelling point of view this poses a challenge, from a measurement point of view this
14 underlines that k-space polarimetry can sensitively discriminate between proposed models.

15 Conclusions

16 We investigated the angular distribution of helicity-dependent photoluminescence enhance-
17 ment from arrays of planar chiral plasmonic nanostructures embedded in a light-emitting dye
18 layer. Despite the achiral nature of the emitters, this system presents a distinct dissymmetry
19 in the far-field emission between the RCP and LCP light, which is controlled by the geomet-
20 rical handedness of the array unit cell. While previous works experimentally investigated
21 this effect by sampling photoluminescence orthogonal to the plane of the array (*i.e.* $k \simeq 0$),
22 in this work we found a remarkable and non-trivial distribution of the DCP into the far-field,
23 characterized by angularly narrow areas of high values of the DCP. The angular position of
24 these strong chiral dissymmetries coincide with surface lattice resonances, thus highlighting
25 the important role of diffractive coupling in the light spin-orbit effect. Our findings demon-

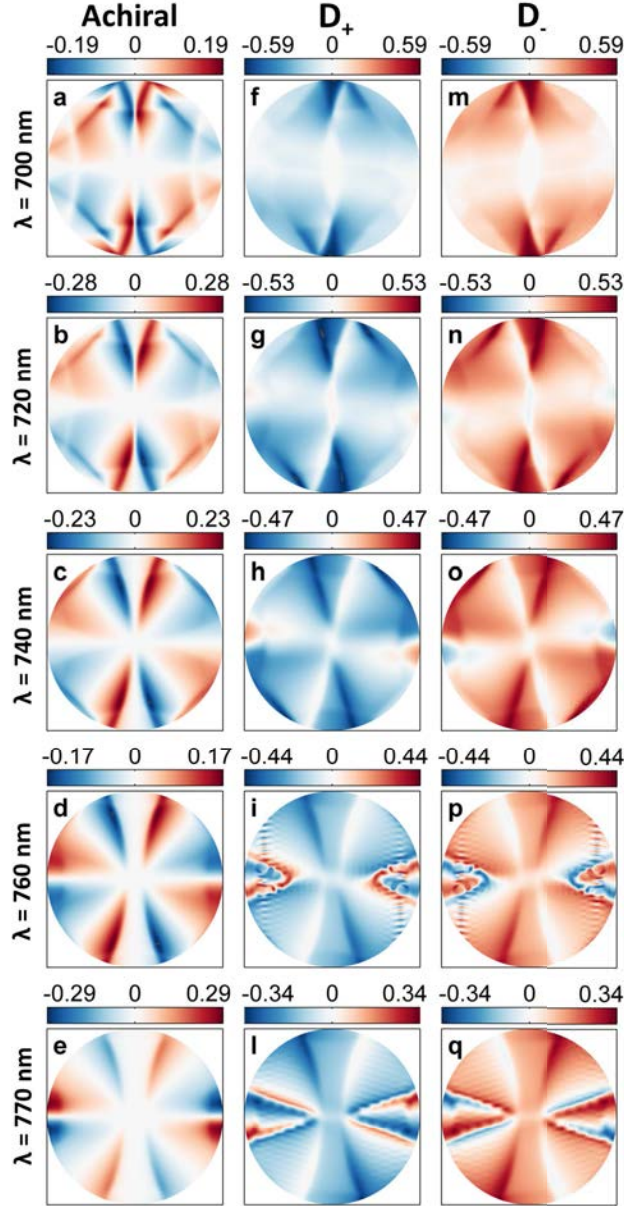


Figure 6: Simulated angle-resolved DCP of the emission from the achiral and chiral structures. The horizontal and vertical axes for each plot are the same as fig. 4(a-f). Each row of the panel corresponds to fixed emission wavelength, ranging from 700 nm (top row) to 770 nm (bottom row), as indicated in the label. For each row the three plots correspond, from left to right, to the emission from the achiral, D_+ and D_- structures. The colorbar of each plot is indicated on top of it.

- 1 strate how an array of planar chiral nanostructures can efficiently redirect light from achiral
- 2 emitters into different narrow directions with distinct circular polarization states. Moreover,
- 3 these results demonstrate that, when studying the spin-orbit effect in a periodic array of

1 plasmonic nanostructures, k-space measurements are an essential tool, since sampling only
2 the $k \simeq 0$ portion of the angular spectra can not reveal the intricate angle-dependent effects.

3 **Methods**

4 **Sample Fabrication**

5 The sample was fabricated by spin-coating a positive resist (PMMA 950 A4) on a $24 \times 24 \times 0.7$
6 mm glass coverslide (Menzel) which was first cleaned with a $H_2O : H_2O_2 : NH_4OH$
7 base piranha solution. Square arrays of antennas, with a side of about $300 \mu\text{m}$, were de-
8 fined through electron beam lithography (30 keV, RAITH150-TWO) with a typical dose of
9 $400 \mu\text{C}/\text{cm}^2$. After development with a MIBK:IPA=1:3 solution, we thermally evaporated 2
10 nm of chromium followed by 30 nm of silver at an evaporation rate of $0.5 - 1 \text{ \AA}/\text{s}$. Lift-off was
11 performed by keeping the sample in acetone vapour overnight and subsequently immersing
12 it in liquid acetone for one hour.

13 In order to deposit a dye-doped layer on top of the fabricated plasmonic structures, a 10
14 mM solution of cyclopentanone and Rhodamine 800 (Rh800) was mixed with the photoresist
15 SU8 (Microchem SU8-2005) in 1:1 ratio. To decrease its viscosity and obtain thinner layers,
16 we further diluted 2 ml of this solution with 8 ml of cyclopentanone. The resulting solution
17 was spun on the sample at a speed of 4000 rpm for 45 s resulting in a layer thickness of about
18 65 nm. The sample was finally baked for 2 minutes at 95° to evaporate the cyclopentanone.
19 The dye Rh800 has its absorption maximum at about 680 nm and its emission maximum at
20 about 720 nm, as shown in fig.1d.

21 **Setup for k-space polarimetry**

22 Figure 1f shows the setup used to perform the k-space polarimetry measurements. A linearly
23 polarized super-continuum laser (Fianium), filtered with an acousto-optical tunable filter
24 (AOTF, Crystal Technologies) and a band-pass filter (620-10 nm), is focused on the sample

1 by an achromatic lens. The power of the laser, measured before the lens, is about 16 μ W.
2 The fluorescence is collected from the other side of the sample with a 60x objective (NA=0.7,
3 Nikon CFI Plan Fluor) and separated from the excitation light by a 650 nm long pass filter
4 (LPF). The desired state of polarization is selected by a polarimeter, composed of a quarter
5 wave plate (QWP) and a linear polarizer (LP). A subsequent spatial filter, composed of a
6 1:1 telescope ($f_{telescope} = 50$ mm) and a 400 μ m pinhole, ensures that only the signal coming
7 from an area of about 25 μ m on the sample is collected, so that the array edges for our finite
8 sample fields do not affect the measurement. The Fourier (or Bertrand) lens ($f_{Fourier} = 200$
9 mm) is mounted on a flippable stage, allowing to image either the real space or the back
10 focal plane of the objective. Finally, a tube lens ($f_{tube} = 200$ mm) focuses the light on a
11 silicon CCD camera (Photometrics CoolSnap EZ). The exposure time of the camera was 60
12 s for all the measurements. A set of narrow (FWHM=10 nm) band pass filters (in the range
13 700-790 nm) has been used in front of the camera to acquire quasi-monochromatic images.

14 In this configuration, the signal collected by the camera is directly proportional to the
15 intensity of the polarization state selected by the polarimeter. In more complex systems,
16 in which other optical components are present between the sample and the polarizer, the
17 polarization state of light is transformed according to the Mueller matrix of each element.
18 This matrix can be calculated from preliminary calibration measurements,^{22,23} and therefore
19 used to correct for the polarization conversion effects due to each optical element.

20 **Setup for low-NA transmission and PLE**

21 In order to both benchmark our results against those of Meinzer *et al.*¹⁷ and to show the
22 role of the SLR, we measured the photoluminescence enhancement (PLE) and transmittance
23 (fig.3) in a low-NA normal-incidence configuration . We used a simplified version of the setup
24 described in fig. 1f, in which the collection objective is replaced by a low-NA achromatic lens
25 (NA=0.12) and the Fourier lens is removed, as shown in fig. 7(a-b). Instead of imaging the
26 emission on the camera CCD, it is focused on a fiber and directed to the entrance slit of a

1 spectrometer. For the transmittance measurements (fig. 7b) we illuminated the sample with
 2 linearly polarized white light from a fiber-coupled halogen lamp without any polarization
 analysis on the transmitted light (*i.e.* the polarimeter is removed).

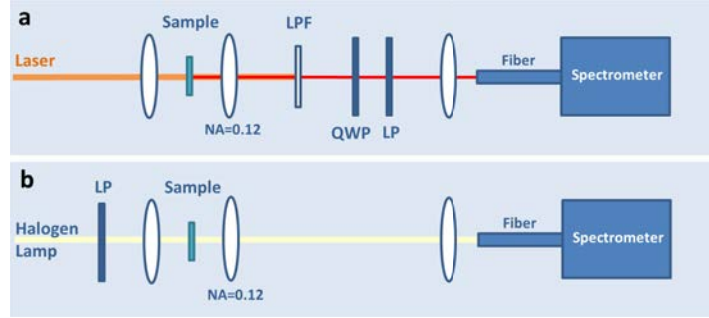


Figure 7: Scheme of the setups used for (a) PLE and (b) transmittance measurements

3

4 Polarimetry principle

Each set of angle-resolved Stokes parameters was retrieved based on six consecutive Fourier images, according to

$$S_0 = I_V + I_H \quad (1a)$$

$$S_1 = I_V - I_H \quad (1b)$$

$$S_2 = I_+ - I_- \quad (1c)$$

$$S_3 = I_R - I_L. \quad (1d)$$

Where I_H , I_V , I_+ and I_- denote the intensities of the linear horizontal, vertical, diagonal and anti-diagonal polarized components of the emission, while I_L and I_R denote the intensities of the LCP and RCP components, respectively. Once the Stokes parameters have been obtained through the measurements of the six intensities mentioned above, all other quantities related to polarization can be calculated. In particular, the degrees of polarization DP, linear

polarization DLP and circular DCP can be derived from the Stokes parameters³³

$$DP = \frac{\sqrt{S_1^2 + S_2^2 + S_3^2}}{S_0}, \quad (2a)$$

$$DLP = \frac{\sqrt{S_1^2 + S_2^2}}{S_0}, \quad (2b)$$

$$DCP = \frac{S_3}{S_0}. \quad (2c)$$

1 These quantities describe the ratio of polarized, linearly polarized, and circularly polarized
 2 light to total emission. For the DCP definition, the absolute value of S_3 is commonly used.
 3 With our definition the DCP is a signed quantity which can vary from -1 (light is completely
 4 LCP) to $+1$ (light is completely RCP).

5 Coupled dipoles model

6 Each antenna is modeled by an electric dipole located in its center and characterized by an
 7 electric polarizability tensor α . If the system is excited by a monochromatic external field
 8 \mathbf{E}_{inc} at frequency ω , the dipole moment \mathbf{p}_i acquired by the i -th dipole reads

$$\mathbf{p}_i = \alpha(\omega)\mathbf{E}_{inc,i} + \alpha(\omega) \sum_{j \neq i} \mu\omega^2 G(\mathbf{r}_i, \mathbf{r}_j, \omega)\mathbf{p}_j \quad (3)$$

9 where $\mathbf{E}_{inc,i}$ denotes the incident field at the position of the i -th dipole, μ is the magnetic
 10 permeability, and $G(\mathbf{r}_i, \mathbf{r}_j, \omega)$ is the Green tensor of the system, which quantifies the prop-
 11 agation of the electromagnetic field from a dipole at position \mathbf{r}_j to position \mathbf{r}_i . The sum is
 12 performed over all N dipoles. The problem can be easily cast in a system of $3N$ algebraic
 13 equations, and solved with numerical methods to obtain the dipole moments $\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_N$.
 14 Once the dipole moments are known, the far-field electromagnetic field can be obtained by
 15 using the appropriate asymptotic far-field Green function G_{FF} ^{27,34}

$$\mathbf{E}_{FarField}(\theta, \phi) = \sum_{i=1}^N \mu\omega^2 G_{FF}(\theta, \phi, \mathbf{r}_i, \omega)\mathbf{p}_i. \quad (4)$$

1 In this way, the polarized angular emission of the sample can be reconstructed and the
2 information about the, *e.g.*, DCP, can be retrieved. Our system is described by a three-layers
3 structure with refractive indexes $n_{glass} = 1.52$, $n_{SU8} = 1.58$ and $n_{air} = 1$. The Green tensors
4 of such stratified structures are calculated numerically starting from analytical formulas.²⁷
5 We simulated arrays with 61×61 unit cells (*i.e.* 7442 single dipoles) and with different
6 chirality of the unit cell. The polarizability tensor of a single rod is calculated by adding
7 two correction terms to the static polarizability^{35,36} of a silver rod, to take in account the
8 depolarization induced by the accumulated surface charges and the radiation damping.³⁶
9 The static polarizability and the depolarization factor depend on the rod dimensions, while
10 the radiation damping depends on the environment in which the dipole is placed (*i.e.* the
11 three-layers stack, in our case). For the permittivity of the silver we assumed a Drude model,
12 $\epsilon(\omega) = 1 - \omega_p^2/(\omega^2 - i\omega\gamma)$, with $\omega_p = 2\pi \cdot 2.321 \cdot 10^{15}$ Hz and $\gamma = 2\pi \cdot 5.513 \cdot 10^{12}$ Hz.

13 In order to simulate the excitation of the nanoantennas by nearby fluorescent emitters
14 we used, as driving field, several dipolar sources with different polarization and in different
15 positions inside the SU8 layer. The far-field electric field is calculated separately for each
16 source. Afterwards, the total far-field polarized intensities are obtained by summing inco-
17 herently the contribution of each source. Finally, the DCP is calculated according to eq. 2c.
18 Moreover, when using eq. 4, a gaussian spatial filter is applied in order to smoothly remove
19 the contribution from dipoles located close to the array's edge.

20 Acknowledgement

21 We thank H. Schokker for assistance with samples fabrication, C. Guo and L. Langguth
22 for providing the scripts for the coupled dipoles model calculations and A. Fiore for fruitful
23 discussions. The work is part of the research programme of the Foundation for Fundamental
24 Research on Matter (FOM), which is financially supported by the Netherlands Organisation
25 for Scientific Research (NWO). The work of C.I.O. and A.F.K. is supported by NanoNextNL,
26 a micro- and nanotechnology consortium of the Government of The Netherlands and 130

1 partners. A.F.K. gratefully acknowledges an NWO-Vidi grant for financial support.

2 **Supporting Information Available**

3 Additional numerical calculation of the sample transmittance, near-field patterns for localized
4 and lattice resonances. This material is available free of charge via the Internet at [http:](http://pubs.acs.org/)
5 [//pubs.acs.org/](http://pubs.acs.org/).

6 **References**

- 7 1. Novotny, L.; van Hulst, N. Antennas for light. *Nature Photon.* **2011**, *5*, 83–90.
- 8 2. Muskens, O.; Giannini, V.; Sanchez-Gil, J.; Gómez Rivas, J. Strong Enhancement of
9 the Radiative Decay Rate of Emitters by Single Plasmonic Nanoantennas. *Nano letters*
10 **2007**, *7*, 2871–2875.
- 11 3. Kinkhabwala, A.; Yu, Z.; Fan, S.; Avlasevich, Y.; Müllen, K.; Moerner, W. Large Single-
12 Molecule Fluorescence Enhancements Produced by a Bowtie Nanoantenna. *Nature Pho-*
13 *tonics* **2009**, *3*, 654–657.
- 14 4. Akselrod, G. M.; Argyropoulos, C.; Hoang, T. B.; Ciraci, C.; Fang, C.; Huang, J.;
15 Smith, D. R.; Mikkelsen, M. H. Probing the Mechanisms of Large Purcell Enhancement
16 in Plasmonic Nanoantennas. *Nature Photonics* **2014**, *8*, 835–840.
- 17 5. Valev, V. K.; Baumberg, J. J.; Sibilía, C.; Verbiest, T. Chirality and Chiroptical Effects
18 in Plasmonic Nanostructures: Fundamentals, Recent progress, and Outlook. *Advanced*
19 *Materials* **2013**, *25*, 2517–2534.
- 20 6. Kuwata-Gonokami, M.; Saito, N.; Ino, Y.; Kauranen, M.; Jefimovs, K.; Vallius, T.; Tu-
21 runen, J.; Svirko, Y. Giant Optical Activity in Quasi-Two-Dimensional Planar Nanos-
22 tructures. *Phys. Rev. Lett.* **2005**, *95*, 227401.

- 1 7. Gorodetski, Y.; Shitrit, N.; Bretner, I.; Kleiner, V.; Hasman, E. Observation of Optical
2 Spin Symmetry Breaking in Nanoapertures. *Nano Lett.* **2009**, *9*, 3016–3019.
- 3 8. Kuzyk, A.; Schreiber, R.; Fan, Z.; Pardatscher, G.; Roller, E.-M.; Högele, A.; Sim-
4 mel, F. C.; Govorov, A. O.; Liedl, T. DNA-Based Self-Assembly of Chiral Plasmonic
5 Nanostructures with Tailored Optical Response. *Nature* **2012**, *483*, 311–314.
- 6 9. Song, C.; Blaber, M. G.; Zhao, G.; Zhang, P.; Fry, H. C.; Schatz, G. C.; Rosi, N. L.
7 Tailorable Plasmonic Circular Dichroism Properties of Helical Nanoparticle Superstruc-
8 tures. *Nano Lett.* **2013**, *13*, 3256–3261.
- 9 10. Decker, M.; Ruther, M.; Kriegler, C.; Zhou, J.; Soukoulis, C.; Linden, S.; Wegener, M.
10 Strong Optical Activity from Twisted-Cross Photonic Metamaterials. *Opt. Lett.* **2009**,
11 *34*, 2501–2503.
- 12 11. Gorkunov, M.; Ezhov, A.; Artemov, V.; Rogov, O.; Yudin, S. Extreme Optical Activity
13 and Circular Dichroism of Chiral Metal Hole Arrays. *Appl. Phys. Lett.* **2014**, *104*, 221102.
- 14 12. Eftekhari, F.; Davis, T. J. Strong Chiral Optical Response from Planar Arrays of Sub-
15 wavelength Metallic Structures Supporting Surface Plasmon Resonances. *Phys. Rev. B*
16 **2012**, *86*, 075428.
- 17 13. Fan, Z.; Govorov, A. O. Plasmonic Circular Dichroism of Chiral Metal Nanoparticle
18 Assemblies. *Nano Lett.* **2010**, *10*, 2580–2587.
- 19 14. Schäferling, M.; Dregely, D.; Hentschel, M.; Giessen, H. Tailoring Enhanced Optical
20 Chirality: Design Principles for Chiral Plasmonic Nanostructures. *Phys. Rev. X* **2012**,
21 *2*, 031010.
- 22 15. Hendry, E.; Carpy, T.; Johnston, J.; Popland, M.; Mikhaylovskiy, R. V.; Laphorn, A. J.;
23 Kelly, S. M.; Barron, L. D.; Gadegaard, N.; Kadodwala, M. Ultrasensitive Detection and

- 1 Characterization of Biomolecules Using Superchiral Fields. *Nat. Nanotechnol.* **2010**, *5*,
2 783–787.
- 3 16. Kruk, S. S.; Decker, M.; Staude, I.; Schlecht, S.; Greppmair, M.; Neshev, D. N.;
4 Kivshar, Y. S. Spin-Polarized Photon Emission by Resonant Multipolar Nanoantennas.
5 *ACS Photonics* **2014**, *1*, 1218–1223.
- 6 17. Meinzer, N.; Hendry, E.; Barnes, W. L. Probing the Chiral Nature of Electromagnetic
7 Fields Surrounding Plasmonic Nanostructures. *Phys. Rev. B* **2013**, *88*, 041407.
- 8 18. Vecchi, G.; Giannini, V.; Rivas, J. G. Surface Modes in Plasmonic Crystals Induced by
9 Diffractive Coupling of Nanoantennas. *Phys. Rev. B* **2009**, *80*, 201401.
- 10 19. Rodriguez, S.; Schaafsma, M.; Berrier, A.; Rivas, J. G. Collective Resonances in Plas-
11 monic Crystals: Size Matters. *Physica B: Condensed Matter* **2012**, *407*, 4081–4085.
- 12 20. Lozano, G.; Louwers, D. J.; Rodríguez, S. R.; Murai, S.; Jansen, O. T.; Verschu-
13 uuren, M. A.; Rivas, J. G. Plasmonics for Solid-State Lighting: Enhanced Excitation and
14 Directional Emission of Highly Efficient Light Sources. *Light: Science & Applications*
15 **2013**, *2*, e66.
- 16 21. Lozano, G.; Grzela, G.; Verschuuren, M. A.; Ramezani, M.; Rivas, J. G. Tailor-
17 Made Directional Emission in Nanoimprinted Plasmonic-Based Light-emitting Devices.
18 *Nanoscale* **2014**, *6*, 9223–9229.
- 19 22. Osorio, C. I.; Mohtashami, A.; Koenderink, A. K-space Polarimetry of Bullseye Plasmon
20 Antennas. *Sci. Rep.* **2015**, *5*, 9966 1–7.
- 21 23. Mohtashami, A.; Osorio, C. I.; Koenderink, A. F. Angle-Resolved Polarimetry Measure-
22 ments of Antenna-Mediated Fluorescence. *arXiv preprint arXiv:1506.00140* **2015**,
- 23 24. Fedotov, V.; Mladyonov, P.; Prosvirnin, S.; Rogacheva, A.; Chen, Y.; Zheludev, N.

- 1 Asymmetric Propagation of Electromagnetic Waves through a Planar Chiral Structure.
2 *Phys. Rev. Lett.* **2006**, *97*, 167401.
- 3 25. Lumerical Solutions, Inc. <http://www.lumerical.com/tcad-products/fdtd/>.
- 4 26. Murai, S.; Verschuuren, M.; Lozano, G.; Pirruccio, G.; Rodriguez, S.; Rivas, J. G. Hybrid
5 Plasmonic-Photonic Modes in Diffractive Arrays of Nanoparticles Coupled to Light-
6 Emitting Optical Waveguides. *Optics express* **2013**, *21*, 4250–4262.
- 7 27. Novotny, L.; Hecht, B. *Principles of Nano-Optics*; Cambridge University Press, 2006.
- 8 28. Langguth, L.; Schokker, A.; Guo, K.; Koenderink, A. Plasmonic Phase-Gradient Meta-
9 surface for Spontaneous Emission Control. *Physical Review B* **2015**, *92*, 205401.
- 10 29. Plum, E.; Fedotov, V.; Zheludev, N. Extrinsic Electromagnetic Chirality in Metamate-
11 rials. *Journal of Optics A: Pure and Applied Optics* **2009**, *11*, 074009.
- 12 30. Lu, X.; Wu, J.; Zhu, Q.; Zhao, J.; Wang, Q.; Zhan, L.; Ni, W. Circular Dichroism from
13 Single Plasmonic Nanostructures with Extrinsic Chirality. *Nanoscale* **2014**, *6*, 14244–
14 14253.
- 15 31. Sersic, I.; van de Haar, M. A.; Bernal Arango, F.; Koenderink, A. F. Ubiquity of Optical
16 Activity in Planar Metamaterial Scatterers. *Phys. Rev. Lett.* **2012**, *108*, 223903.
- 17 32. Lindell, I. V.; Sihvola, A. H.; Tretyakov, S. A.; Viitanen, A. J. *Electromagnetic Waves*
18 *in Chiral and Bi-Isotropic Media*; Artech House, Norwood, MA, 1994.
- 19 33. Goldstein, D. H. *Polarized Light*; CRC Press, 2010.
- 20 34. Lukosz, W. Light Emission by Magnetic and Electric Dipoles Close to a Plane Dielectric
21 Interface. III. Radiation Patterns of Dipoles with Arbitrary Orientation. *J. Opt. Soc. Am.*
22 **1979**, *69*, 1495–1503.

- 1 35. Maier, S. A. *Plasmonics: Fundamentals and Applications*; Springer Science & Business
2 Media, 2007.
- 3 36. Hofmann, H. F.; Kosako, T.; Kadoya, Y. Design Parameters for a Nano-Optical Yagi-
4 Uda Antenna. *New Journal of Physics* **2007**, *9*, 217.

1 Graphical TOC Entry

2

