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# Automated Error Correction of Business Process Models 

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#### Abstract

As order dependencies between process tasks can get complex, it is easy to make mistakes in process model design, especially behavioral ones such as deadlocks. Notions such as soundness formalize behavioral errors and tools exist that can identify such errors. However these tools do not provide assistance with the correction of the process models. Error correction can be very challenging as the intentions of the process modeler are not known and there may be many ways in which an error can be corrected. We present a novel technique for automatic error correction in process models based on simulated annealing. Via this technique a number of process model alternatives are identified that resolve one or more errors in the original model. The technique is implemented and validated on a sample of industrial process models. The tests show that at least one sound solution can be found for each input model within a reasonable response time.


## 1 Introduction and Background

Business process models document organizational procedures and as such are often invaluable to both business and IT stakeholders. They are used to communicate and agree on requirements among business analysts, or used by solution architects and developers as a blueprint for process automation [15]. In all cases, it is of utmost importance that these models are correct. Incorrect process models can lead to ambiguities and misinterpretations, and may not be directly automated [16]. There are different types of errors. A process model can violate simple syntactical requirements (e.g. some nodes are disconnected or used improperly), or suffer from behavioral anomalies (e.g. deadlocks or incorrect completion). Behavioral errors only arise when process models are executed and thus they are typically much more difficult to spot. For these reasons, they are quite common in practice. For example, a recent analysis of more than 1,350 industrial process models reports that $54 \%$ of these models are unsound [6].

Formal correctness notions such as soundness [1] define behavioral anomalies for process models, and advanced process modeling tools implement verification methods based on these notions to automatically detect these anomalies in process models [6|16]. Process modelers can take advantage of the information provided by these verification
features to fix design flaws. However, generally it is up to the user to understand the (often very technical) output produced by these tools and to figure out how to fix these errors. Correcting behavioral errors in process models is not trivial: apparently independent errors can have a common cause and correcting one error may introduce new errors in other parts of the model. This problem is amplified by the inherent complexity of process models, which tends to grow as organizations reach higher levels of Business Process Management (BPM) maturity [12].

This paper presents a novel technique called Petri Nets Simulated Annealing (PNSA) for automatically fixing unsound process models. The core of this technique is a heuristic optimization algorithm based on dominance-based Multi-Objective Simulated Annealing (MOSA) [14|13]. Given an unsound process model and the output of its soundness check, at each run, the algorithm generates a small set of solutions (i.e. alternative models) similar to the original model but potentially containing fewer or no behavioral errors, until a maximum number of desired solutions is found or a given timeframe elapses. These solutions are produced by applying a number of perturbations (i.e. small changes) on the current solution, which in turn is derived from the original model. The similarity of a solution to the original model is determined by its structural similarity and (to remain efficient) by an approximation of its behavioral similarity to the original model. Since the intentions of the process modeler are not known and there are usually many ways in which an error can be corrected, the algorithm returns a small set of non-redundant solutions (i.e. no solution is worse than any of the others). The differences between these solutions and the original model can then be presented to a process modeler as suggestions to rectify the behavioral errors in the original model. This technique is implemented in a prototype tool and validated on a sample of industrial process models. The results indicate that multiple errors can be fixed in a short time and at least one sound solution was found for each model.

The problem of automatically correcting errors has already been explored for software bug fixing (see e.g. [2]). Given a program, a set of positive tests and at least one failed test proving evidence for a bug, these algorithms produce a patch that fixes the error in question, provided that this error is localized. In the BPM field, [3] describes a technique for automatically fixing certain types of data anomalies that can occur in process models, while [10] presents an approach to compute the edit operations required to correct a faulty service in order to interact in a choreography without deadlocks. However, to the best of our knowledge, the problem of automatically fixing unsound process models has not been addressed yet.

In this paper, we represent process models as Workflow nets-a class of Petri nets that has been extensively applied to the formal verification of business process models [16]. In addition, mappings exist between process modeling languages used in practice (e.g. EPCs, BPMN, BPEL) and Petri nets [11]. This provides a basis to extend the results of this paper to concrete process modeling notations.

Based on the above, the rest of this paper is organized as follows: Sec. 2 provides the basic definitions of Workflow nets and soundness. Sec. 3 defines the problem in question, while Sec. 4 describes the PNSA technique in detail. The evaluation of the proposed technique is treated in Sec. [5before Sec. 6concludes the paper.

## 2 Preliminaries

Petri nets are graphs composed of two types of nodes, namely transitions and places, connected by directed arcs. Transitions represent tasks while places are used for routing purposes. Labels are assigned to transitions to indicate the business action they perform, i.e. the observable behavior. A special label $\tau$ is used to represent invisible actions, i.e. actions that are only used for routing purposes and do not represent any task from a business perspective.

Definition 1 (Labeled Petri net). A labeled Petri net is a tuple $N=(P, T, F, L, \ell)$ where $P$ and $T(P \cap T=\emptyset)$ are finite sets of places, resp., transitions, $F \subseteq(P \times$ $T) \cup(T \times P)$ is a flow relation, $L$ is a finite set of labels representing business actions, $\tau \notin L$ is a label representing an invisible action, and $\ell: T \rightarrow L \cup\{\tau\}$ is a labeling function which assigns a label to each transition. For $n \in P \cup T$, we use $\bullet n$ and $n \bullet$ to denote the set of inputs to $n$ (preset) and the set of outputs of $n$ (postset).

We are interested in Petri nets with a unique source place and a unique sink place, and such that all other nodes are on a directed path between the input and the output places. A Petri net satisfying these conditions represents a process model and is known as a Workflow net [1].

Definition 2 (Workflow net). Let $N=(P, T, F, L, \ell)$ be a labeled Petri net and $F^{*}$ be the reflexive transitive closure of $F . N$ is a Workflow net (WF-net) if and only if (iff):

- there exists exactly one input place, i.e. $\exists!_{p_{I} \in P} \bullet p_{I}=\varnothing$, and
- there exists exactly one output place, i.e. $\exists!_{p_{O} \in P} p_{O} \bullet=\varnothing$, and
- each node is on a directed path from the input to the output place, i.e. $\forall_{n \in P \cup T}\left(\left(p_{I}, n\right) \in F^{*} \wedge\left(n, p_{O}\right) \in F^{*}\right)$.

Fig. 1 shows four example Petri nets, where actions are depicted within transitions, e.g. $\ell\left(t_{1}\right)=a$. All these nets have single start and end places, and any transition lies on a path from the start to the end place. Hence all these nets are WF-nets.

Behavioral correctness of a WF-net is defined w.r.t. the states that a process instance can be in during its execution. A state of a WF-net is captured by the marking of its places with tokens. In a given state, each place is either empty or it contains one or more tokens (i.e. it is marked). A transition is enabled in a given marking if all the places in the transition's preset are marked. Once enabled, the transition can fire (i.e. can be executed) by removing a token from each place in the preset and putting a token into each subsequent place of the transition's postset. This leads to a new state.

Definition 3 (Marking notation). Let $N=(P, T, F, L, \ell)$ be a WF-net. Then $M$ : $P \rightarrow \mathbb{N}$ is a marking and $\mathcal{Q}$ is the set of all markings. Moreover:

- for any two markings $M, M^{\prime} \in \mathcal{Q}, M \geq M^{\prime}$ iff $\forall_{p \in P} M(p) \geq M^{\prime}(p)$,
- for any two markings $M, M^{\prime} \in \mathcal{Q}, M>M^{\prime}$ iff $M \geq M^{\prime}$ and $M \neq M^{\prime}$.
- $\mathbb{M}(N)$ as the set of all markings of $N$,
- $M_{I}^{N}$ as the initial marking of $N$ with one token in place $p_{I}$, i.e. $M_{I}^{N}=\left[p_{I}\right]$,
- $M_{O}^{N}$ as the final marking of $N$ with one token in place po, i.e. $M_{O}^{N}=\left[p_{O}\right]$,


Fig. 1. Four example WF-nets

- for any transition $t \in T$ and any marking $M \in \mathbb{M}(N)$, $t$ is enabled at $M$, denoted as $M[t\rangle$, iff $\forall_{p \in \bullet t} M(p) \geq 1$. Marking $M^{\prime}$ is reached from $M$ by firing $t$ and $M^{\prime}=M-\bullet t+t \bullet$,
- for any two markings $M, M^{\prime} \in \mathbb{M}(N), M^{\prime}$ is reachable from $M$ in $N$, denoted as $M^{\prime} \in N[M\rangle$, iff there exists a firing sequence $\sigma=t_{1} \cdot t_{2} \ldots t_{n}(n \geq 0)$ leading from $M$ to $M^{\prime}$, and we write $M \xrightarrow{\sigma}{ }_{N} M^{\prime}$.
- $\operatorname{Tr}(N)=\left\{\sigma \in T^{*}: \exists_{M \in \mathbb{M}(N)} M_{I} \stackrel{\sigma}{\rightarrow}_{N} M\right\}$ is its set of traces, i.e. firing sequences that start from the initial marking,
$-\operatorname{CTr}(N)=\left\{\sigma \in T^{*}: M_{I} \xrightarrow{\sigma}_{N} M_{O}\right\}$ is its set of correct traces, i.e. traces that lead to the final marking,
- $\hat{\ell}: T^{*} \rightarrow L^{*}$ returns the string of its visible actions, where

$$
\hat{\ell}(\sigma)=\left\{\begin{array}{l}
\epsilon \text { if } \sigma=\epsilon(\text { the empty string }), \\
\ell(t) \cdot \hat{\ell}\left(\sigma^{\prime}\right), \text { if } \sigma=t \cdot \sigma^{\prime} \text { and } \ell(t) \neq \tau \\
\hat{\ell}\left(\sigma^{\prime}\right), \text { if } \sigma=t \cdot \sigma^{\prime} \text { and } \ell(t)=\tau
\end{array}\right.
$$

In the remainder, we omit $N$ as superscript or subscript when it is clear from the context. All the nets in Fig. 1 are marked with their initial marking, i.e. they have one token in their input place depicted as a dot inside the place.

The execution of a process instance starts with the initial marking and should then progress through transition firings until a proper completion state. This intuition is captured by three requirements [1]. First, every process instance should always have an option to complete. If a WF-net satisfies this requirement, it will never run into deadlocks or livelocks. Second, every process instance should eventually reach the final marking, i.e. the state in which there is one token in the output place, and no tokens are left behind in any other place, since this would signal that there is still work to be done. Third, for every transition, there should be at least one correct trace that includes at least one firing of this transition. A WF-net fulfilling these requirements is sound [1].

Definition 4 (Sound WF-net). Let $N=(P, T, F)$ be a WF-net and $M_{I}, M_{O}$ be the initial and end markings. $N$ is sound iff:

- option to complete: for every marking $M$ reachable from $M_{I}$, there exists a firing sequence leading from $M$ to $M^{\prime} \geq M_{O}$, i.e. $\forall_{M \in N\left[M_{I}\right\rangle} \exists_{M^{\prime} \in N[M\rangle} M^{\prime} \geq M_{O}$, and
- proper completion: the marking $M_{O}$ is the only marking reachable from $M_{I}$ with one token in place $p_{O}$, i.e. $\forall_{M \in N\left[M_{I}\right\rangle} M \geq M_{O} \Rightarrow M=M_{O}$, and
- no dead transitions: every transition can be reached by the initial marking, i.e. $\forall_{t \in T} \exists_{M \in N\left[M_{I}\right\rangle} M[t\rangle$.

A behavioral error is a violation of one of the three soundness properties. For example, the first WF-net in Fig. 1 is not sound: it can only complete successfully if transition $t_{5}$ fires only once before $t_{3}$ fires. In fact, if $t_{3}$ fires before $t_{5}, t_{7}$ will deadlock in marking [ $p_{7}$ ] waiting for a token in $p_{8}$ which will never arrive (no option to complete error). Also, if $t_{5}$ fires more than once before $t_{3}$, it will put more than one token in $p_{8}$ and when $t_{3}$ and $t_{7}$ fire, the net will complete with the marking $\left[p_{O}+k p_{8}\right]$ with $k>0$ (no proper completion error). Nets (b) and (c) also suffer from behavioral problems. (b) has no proper completion in markings $\left[p_{O}+p_{5}+p_{8}\right]$ and $\left[p_{O}+p_{6}+k p_{8}\right]$ with $k \geq 0$, while (c) has a deadlock in $\left[p_{7}\right]$ and a dead transition $t_{7}$. Net (d) is sound. In the next section we focus on the problem of automatically fixing unsound process models.

## 3 Automatic Process Model Correction

We name the problem of automatically fixing process model errors as the Automatic Process Model Correction (APMC) problem. Intuitively, given an unsound WF-net $N$ and the output of its verification method, we want to find a set of remedial suggestions, each one presented as a minimal set of changes, that transforms $N$ into a sufficiently similar WF-net $N^{\prime}$ with fewer or no behavioral errors. Since there are usually different ways to solve a behavioral error in an unsound model, we should return different alternative solutions $N^{\prime}$, such that none of these solutions is strictly worse than the others. However since the set of solutions can be potentially large, we should limit it to a maximum number of solutions and a maximum timeframe that the user is willing to wait to find such solutions. The user can then evaluate the solutions found to see if some of these are consistent with their initial intentions, and apply the changes accordingly.

A solution should be sufficiently similar to the original model in order to preserve the modeler's intentions. Otherwise we could obtain a sound variant simply by reducing the original model to a trivial sequence of actions. The notion of process model similarity can be approached from a structural and from a behavioral perspective [5]. From a structural perspective, we should create models whose structure is similar to that of the original model, i.e. we should minimize the changes that we apply to the original model in terms of insertion and deletion of nodes and arcs, and control the type of these changes. From a behavioral perspective, we should preserve the observable behavior of a process model as far as possible, and meantime, try to reduce the number of behavioral errors without introducing new ones. Finally, a solution should not be inferior to the others in terms of number and type of errors being fixed. For example, the final set of solutions should not contain a model that fixes one error if there also exists another model in the same set that fixes that error and a second error.

Structural similarity alone does not guarantee behavioral similarity. Also, two different process structures can have same observable behavior, thus a solution that is
structurally-different to the original model may actually suffer from the same behavioral errors. While behavioral similarity may be sufficient to characterize a solution, a solution that is behaviorally-similar to the original model but structurally very different may not be recognized as a good solution by the user. Moreover, structural similarity enhances confidence about not introducing new errors, and limits the search space. For these reasons, we consider both structural and behavioral similarities in our study. In the following section, we formalize these notions.

## 4 Petri Nets Simulated Annealing

A well-established measure for structural similarity of process models is based on graph-edit distance [4]. A challenge in this technique is finding the best mapping between the nodes of the two graphs to compare, which can be computationally expensive. However we avoid this problem because we measure the graph edit distance by computing the costs of the operations that we perform to change the original model into a given solution. Unfortunately, behavioral similarity cannot be computed efficiently. As an example, the Transition Adjacency Relation technique [17] requires the exploration of the entire state-space of the two models to determine their behavioral similarity. This would be unfeasible in our case, as we would need to check the state-space of each proposed solution against that of the original model, and we do build a high number of candidate solutions. Thus, we opt for an approximation of behavioral similarity based on two components. First, we introduce a notion of behavioral distance to measure the ability of a solution to simulate a finite set of correct traces of the original model. Second, we introduce a notion of badness to measure how many errors of the original model are still present in the solution, and how many new errors have been introduced.

In the light of this, the APMC problem becomes a multi-objective optimization problem which can be solved by trying to simultaneously minimize three objective functions: the structural distance, the behavioral distance and the badness of a solution w.r.t. the original model. At each iteration of our algorithm, we search candidate solutions with lower structural distance, behavioral distance and badness w.r.t. previous solutions. We compute the behavioral distance and the badness over a sample set of traces of the original model, which we select at each iteration. If we find a solution that increases these objective functions, we discard it. Otherwise we maintain the solution so that it can be tested with further sample traces in subsequent iterations. The more tests a solution passes, the more the confidence increases that this is a good solution. The procedure concludes when a maximum number of non-redundant solutions with high confidence is reached (i.e. each solution is not worse than any of the others), or a given timeframe elapses. In the following subsections, we formalize the ingredients of this technique and describe its algorithm in detail.

### 4.1 Structural Distance

Each candidate solution is obtained by applying a minimal sequence of edit operations, i.e. an edit sequence, in order to insert or remove a single arc or node. Inserting or removing one arc is a single atomic operation and does not violate the properties of a WF-net, i.e. the solution will always be a WF-net. Inserting a node implies adding
the node itself and one incoming and one outgoing arc to connect this new node to the rest of the net (a total of three edit operations are needed). Deleting a node implies removing the node itself and all its incoming and outgoing arcs, and can only be done if the elements in the node's preset and postset remain on a path from $p_{I}$ to $p_{O}$ after removing the node. This requires at least three edit operations.

Given that each edit sequence is minimal, i.e. it corresponds to the insertion or removal of one arc or node only, more complex perturbations on the original model can be obtained by applying multiple edit sequences through a number of intermediate solutions. Coming back to the example in Fig. [1] nets (b)-(d) are all solutions of (a) which can be obtained via one or more edit sequences. For example, net (b) can be obtained directly from (a) with one edit sequence consisting of one edit operation (removal of arc $p_{5}-t_{3}$ ), while net (c) can be obtained with two edit sequences consisting of four edit operations in total (addition of arc $p_{8}-t_{6}$ and removal of place $p_{6}$ with its two arcs).

While it is safe to add or remove places and arcs, we need special considerations for transitions. Since the modeler's intentions are not known, we assume that a business action was introduced with a specific business purpose, so its associated transition should not be removed from the model. On the other hand, an invisible action (i.e. a $\tau$ transition) is only used for routing purposes, so we assume it can be safely removed or inserted. Thus, we only allow insertion and removal of $\tau$ transitions.

The cost of each type of edit operation can be controlled by the user. For example, one may rate removal operations as more expensive than addition operations, based on the assumption that it is less likely that modelers would introduce something erroneous than that they forgot to introduce something essential. Similarly, one may rate operations on transitions as more expensive than operations on places, and the latter as more expensive than operations on arcs.

The structural distance between two WF-nets is obtained by the total cost of the edit sequence between the two nets.

Definition 5 (Structural distance). Let $N$ and $N^{\prime}$ be two $W F$-nets, $E$ the set of all edit operations, $e\left(N, N^{\prime}\right)=\left\langle e_{i} \in E\right\rangle_{i=1}^{k}$ the edit sequence between $N$ and $N^{\prime}$, and $c: E \rightarrow \mathbb{R}$ a function that assigns a cost to each edit operation. The structural distance $\lambda: \mathcal{N} \times \mathcal{N} \rightarrow \mathbb{R}$ between $N$ and $N^{\prime}$ is $\lambda\left(N, N^{\prime}\right)=\sum_{i=1}^{k} c\left(e_{i}\right)$.

Let us assume a cost of 1 for each type of edit operation. Then the structural distance between nets (b) and (a) is 1, between (c) and (a) is 4 and between (d) and (a) is 5.

### 4.2 Behavioral Distance

Given a sample set of traces $R$ from the original model $N$, we compute the behavioral distance of a solution $N^{\prime}$ from $N$ as its ability to simulate the correct traces in $R$, i.e. those traces that start from marking $M_{I}$ and complete in $M_{O}$. Hence, this function can only be used if the original model has at least one correct trace.

A model $N^{\prime}$ can simulate a trace $\sigma$ if its string of visible actions $\hat{\ell}(\sigma)$ can be replayed in $N^{\prime}$. For example, given the trace $\sigma_{1}=t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{3} \cdot t_{7}$ of net (a) in Fig. 1 we want to check whether $\hat{\ell}\left(\sigma_{1}\right)=$ a.b.c.d.c.e.f can be replayed in a solution of (a). Precisely, we want to know to what extent $\hat{\ell}\left(\sigma_{1}\right)$ can be simulated by its best simulation
trace, i.e. by the longest prefix of $\hat{\ell}\left(\sigma_{1}\right)$ that can be replayed in $N^{\prime}$. For example, net (b) can fully simulate $\sigma_{1}$ while (c) cannot simulate action $f$ because $t_{7}$ is dead in (c). The extent of a simulation is called simulation ratio and is given by $\frac{\left|\hat{\ell}\left(\sigma^{\prime}\right)\right|}{|\hat{\ell}(\sigma)|}$ where $\sigma^{\prime}$ is the best simulation of $\sigma$ in a given solution. The simulation ratio of $\sigma_{1}$ in net (b) is 1 while in (c) it is $\frac{6}{7} \approx 0.86$.

We limit the number of silent actions that can be used to simulate a trace via a parameter $m$ for efficiency reasons. In fact, the higher $m$ is, the more the solution model needs to be explored to see if a given trace can be simulated (and each silent action may open new paths to explore).

Definition 6 (Trace simulation, Best simulation). Let $N$ and $N^{\prime}$ be two WF-nets and $\sigma \in \operatorname{Tr}(N)$ be a trace of $N$. Then $\operatorname{Sim}\left(N, N^{\prime}, \sigma, m\right)=\left\{\sigma^{\prime} \in \operatorname{Tr}\left(N^{\prime}\right): \mid\{t \in\right.$ $\left.\alpha(\sigma): l(t)=\tau\} \mid \leq m \wedge \hat{\ell}\left(\sigma^{\prime}\right) \in \operatorname{Pref}(\hat{\ell}(\sigma))\right\}$ is the set of traces that can simulate $\sigma$ in $N^{\prime}$ with at most $m$ silent actions, where $\alpha(\sigma)$ returns the alphabet of $\sigma$ and $\operatorname{Pref}(s)$ returns the set of all prefixes of string s. We say that $\sigma^{\prime}$ is a best simulation of $\sigma$ in $N^{\prime}$ with at most $m$ silent actions, denoted as $\operatorname{sim}_{b}\left(N, N^{\prime}, \sigma, m\right)$, iff $\sigma^{\prime} \in$ $\operatorname{Sim}\left(N, N^{\prime}, \sigma, m\right)$ and $\left|\hat{\ell}\left(\sigma^{\prime}\right)\right|=\max _{\theta \in \operatorname{Sim}\left(N, N^{\prime}, \sigma, m\right)}|\hat{\ell}(\theta)|$. Let $\sigma^{\prime}=\operatorname{sim}_{b}\left(N, N^{\prime}, \sigma, m\right)$ such that $M_{I}{\xrightarrow{\sigma^{\prime}}}_{N^{\prime}} M$. Then $M_{e}^{\sigma^{\prime}}=M$ is the final marking of $\sigma^{\prime}$ and $\mathbb{M}^{\sigma^{\prime}}=\{M \in$ $\left.\mathbb{M}\left(N^{\prime}\right): \exists_{\theta \in \operatorname{Pref}\left(\sigma^{\prime}\right)} M_{I} \xrightarrow{\theta}_{N^{\prime}} M\right\}$ is the set of all markings traversed by $\sigma^{\prime}$.

The behavioral distance of a solution w.r.t. a set of traces $R$ is the inverse of the cumulative simulation ratio of all the best simulation traces, normalized to the number of correct traces in $R$.

Definition 7 (Behavioral distance to $\mathbf{N}$ w.r.t. $\mathbf{R}$ and m). Let $N$ be a WF-net such that its set of correct traces $\operatorname{CTr}(N) \neq \varnothing$ and let $N^{\prime}$ be another $W F-n e t$. The behavioral distance $\delta: \mathcal{N} \times \mathcal{N} \times 2^{\operatorname{Tr}(N)} \times \mathbb{N} \rightarrow[0,1]$ of $N^{\prime}$ to $N$ w.r.t. a representative set of traces $R$ of $N$ and a simulation parameter $m$ is $\delta\left(N, N^{\prime}, R, m\right)=$ $1-\frac{\sum_{\sigma \in R \cap C \operatorname{Tr}(N)} \psi\left(N, N^{\prime}, \sigma, m\right)}{|R \cap \operatorname{CTr}(N)|}$, where the simulation ratio $\psi\left(N, N^{\prime}, \sigma, m\right)=$ $\left\{\begin{array}{l}\frac{\left|\hat{\ell}\left(\sigma^{\prime}\right)\right|}{|\hat{\ell}(\sigma)|} \text { such that } \sigma^{\prime}=\operatorname{sim}_{b}\left(N, N^{\prime}, \sigma, m\right) \\ 0 \text { otherwise }\end{array}\right.$

With reference to Fig. 1 let us consider $R_{1}=\left\{\left(t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{3} \cdot t_{7}\right),\left(t_{1} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4}\right.\right.$. $\left.\left.t_{2} \cdot t_{3} \cdot t_{7}\right),\left(t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{3}\right),\left(t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{3} \cdot t_{7}\right)\right\}$ where the first two traces are correct. The behavioral distance of nets (b) and (d) to (a) over the correct traces in $R_{1}$ is 0 since all such traces in $R_{1}$ can be fully simulated in (b) and (d), while the behavioral distance of (c) to (a) is $1-\frac{0.86+0.86}{2}=0.14$ (using at most $m=5$ silent actions).

### 4.3 Badness

Broadly speaking a model is behaviorally better than another if it contains less behavioral errors, but not all errors are equal and errors of the same type can have a different severity. For example, a no option to complete may prevent an entire process fragment
from being executed, which is far worse than having a single dead transition in a model. Thus, we need a function to rank errors based on their gravity. More precisely, given a sample set of traces $R$, we want to find out if and to what extent each of these traces leads to an error. In the WF-net context, a trace is proof of no option to complete if it produces a marking $M$ such that $M \neq M_{O}$ and no transition can be enabled in $M$. A trace is proof of improper completion if it produces a marking $M$ such that $M>M_{O}$, i.e. there are other marked places besides $p_{O}$. These conditions can be efficiently checked on a trace. Unfortunately it is not possible to provide evidence for a dead transition unless the whole state space is explored, which we cannot afford to do when generating solutions (exploring the entire state space is notoriously an exponential problem). However, given a trace, we can still provide a "warning" for a potentially-dead transition, i.e. a transition that is partially enabled in the last marking of that trace, due to some places in its preset not being marked (where the maximum number of admissible missing places is a parameter $d$ ).

Definition 8 (Potentially-dead transition). Given a WF-net $N$, a marking $M \in$ $\mathbb{M}(N)$ and a transition $t \in T$, $t$ is potentially-dead in marking $M$, i.e. pdt $(N, M, t, d)$ iff it holds that $0<|\{p \in \bullet t \mid M(p)=0\}| \leq d$ and $\exists_{p \in \bullet t} M(p)>0$, where $0<d<|\bullet t|$ denotes the maximum number of admissible missing places.

We can now provide the classification of erroneous traces.
Definition 9 (Erroneous trace classification). Let $N$ be a WF-net, $\sigma \in \operatorname{Tr}(N)$ be one of its traces $\left(M_{I} \xrightarrow{\sigma} M\right.$ ), and $d$ be a parameter indicating the maximum number of admissible missing places. Then $\sigma$ has:

1. a no option to complete error iff $M \neq M_{O}$ and $\nexists_{t \in T} M[t\rangle$
2. an improper completion error iff $M>M_{O}$
3. a potentially-dead transition, iff $\exists_{t \in T} p d t(N, M, t, d)$.

We denote the set of all erroneous traces for a net $N$ as $\mathrm{E} \operatorname{Tr}(N)$. While no option to complete and improper completion are mutually exclusive errors in a trace, a trace that suffers from either of these problems can also have a potentially-dead transition.

For each $\sigma$ in $R$ of $N$, the badness is a function measuring the severity of each error for a best simulation $\sigma^{\prime}$ of $\sigma$ in $N^{\prime}$ (if $N \equiv N^{\prime}$, the best simulation of $\sigma$ is the trace itself). For example, if $\sigma$ has an improper completion error while its best simulation $\sigma^{\prime}$ in $N^{\prime}$ does not have this error, the badness of $\sigma^{\prime}$ will be lower than that of $\sigma$ ( 0 if no errors are found for that trace). Thus, while for the behavioral distance we are only interested in simulating correct traces, when computing the badness we need to make sure $R$ contains both correct and erroneous traces of $N$. Correct traces in $N$ will have a badness of 0 and can be tested against their simulations in $N^{\prime}$ to see if a new error has been introduced (the badness of the simulation trace will be greater than 0 ); erroneous traces in $N$ will have a badness $>0$ and can be tested against their simulations to see if the errors have diminished or disappeared (the badness of the simulation trace will be lower than that of the original trace).

The badness, denoted as $\beta$, consists of three components each measuring the severity of one error type: $\beta_{n}$ for no option to complete, $\beta_{i}$ for improper completion and $\beta_{d}$ for potentially-dead transitions. Given a trace $\sigma$ of $N, \beta_{n}$ measures the probability of
ending up in a deadlock while executing one of its best simulations $\sigma^{\prime}$ in $N^{\prime}$. This is done by counting the number of enabled transitions that are not fired at each state traversed by $\sigma^{\prime}$ : each such a transition provides an option to diverge from the route of $\sigma$, thus potentially avoiding the final deadlock. So the more such options there are while executing $\sigma^{\prime}$, the lower the probability is of ending up in the deadlock in question, and the less onerous this error is. $\beta_{n}$ is also proportional to the complexity of $\sigma^{\prime}$, which is estimated by counting the number of different transitions in $\sigma^{\prime}$ over the total number of transitions in $N^{\prime}$. The intuition is that an error appearing in a more complex trace is worse than the same error appearing in a simple trace. Thus, if the badness of a complex trace is higher than that of a simpler trace featuring the same error, we will prioritize the fixing of the complex trace as opposed to fixing the simple one, with the hope that as a side-effect of fixing the complex trace, other erroneous traces may be fixed. $\beta_{i}$ measures the probability of ending up in an improper completion state while executing $\sigma^{\prime}$. This is done by counting the number of places that are marked when $\sigma^{\prime}$ marks $p_{O}$, over the total number of places that are marked while executing $\sigma^{\prime} . \beta_{i}$ is also proportional to the complexity of $\sigma^{\prime}$. Finally, $\beta_{d}$ returns the probability of having dead transitions in the last state of $\sigma^{\prime}$. This is done by counting how many places are not marked over the size of the preset of each transition that $i$ ) is potentially-dead in the last state of $\sigma^{\prime}$ and ii) is not fired in any best simulation of any trace in $R$. Indeed, even if a transition satisfies the potentially-dead condition, we know for sure that it is not dead if it can be fired in a best simulation of a trace in $R$. This measure is counteracted by the complexity of the trace, under the assumption that the more transitions are fired by $\sigma^{\prime}$, the less likely it is that the potentially-dead transitions in the last state of $\sigma^{\prime}$ need to be fired.

Definition 10 (Badness w.r.t. R, m and d). Let $N, N^{\prime}$ be two $W F$-nets, $R$ a set of traces of $N, m$ the simulation parameter and $d$ the maximum number of admissible missing places. Let also $V=\bigcup_{\sigma \in R} \alpha\left(\operatorname{sim}_{b}\left(N, N^{\prime}, \sigma, m\right)\right)$ be the set of all transitions of $N^{\prime}$ fired in a best simulation of a trace in $R$. The badness of $N^{\prime}$ w.r.t. $R, m$ and $d$ is $\beta: \mathcal{N} \times \mathcal{N} \times 2^{\operatorname{Tr}(N)} \times \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{R}$ :

$$
\beta\left(N, N^{\prime}, R, m, d\right)=\sum_{\sigma \in R}\left(w_{n} \beta_{n}\left(N, N^{\prime}, \sigma, m\right)+w_{i} \beta_{i}\left(N, N^{\prime}, \sigma, m\right)+w_{q} \beta_{d}\left(N, N^{\prime}, \sigma, m, d\right)\right)
$$

where $w_{n}, w_{i}$ and $w_{q}$ are the weights of each error type. For each $\sigma \in R$, given $\sigma^{\prime}=\operatorname{sim}_{b}\left(N, N^{\prime}, \sigma, m\right)$ with set of traversed markings $\mathbb{M}^{\sigma^{\prime}}$ and final marking $M_{e}^{\sigma^{\prime}}$ we define. 1

$$
\begin{aligned}
& \beta_{n}\left(N, N^{\prime}, \sigma, m\right)=\frac{\left|\alpha\left(\sigma^{\prime}\right)\right|}{\left|T^{\prime}\right|} \cdot \frac{\left[M_{e}^{\sigma^{\prime}}\left(p_{O}\right)=0 \wedge \nexists_{t \in T} M_{e}^{\sigma^{\prime}}[t\rangle\right]}{1+\left(\sum_{M \in \mathbb{M}^{\sigma^{\prime}}, t \in T^{\prime}}[M[t\rangle]\right)-\left|\sigma^{\prime}\right|} \\
& \beta_{i}\left(N, N^{\prime}, \sigma, m\right)=\frac{\left|\alpha\left(\sigma^{\prime}\right)\right|}{\left|T^{\prime}\right|} \cdot \frac{\left[M_{e}^{\sigma^{\prime}}\left(p_{O}\right)>0\right] \sum_{p \in P^{\prime} \backslash\left\{p_{O}\right\}}\left[M_{e}^{\sigma^{\prime}}(p)>0\right]}{\sum_{M \in \mathbb{M}^{\sigma^{\prime}}, p \in P^{\prime} \backslash\left\{p_{O}\right\}}[M(p)>0]} \\
& \beta_{d}\left(N, N^{\prime}, \sigma, m, d\right)=\frac{1}{\left|\alpha\left(\sigma^{\prime}\right)\right|} \cdot \sum_{t \in T^{\prime} \backslash V, p d t\left(N^{\prime}, M_{e}^{\sigma^{\prime}}, t, d\right)} \frac{\left\{\left|p \in \bullet t: M_{e}^{\sigma^{\prime}}(p)=0\right|\right\}}{|\bullet t|}
\end{aligned}
$$

[^0]Let us consider again set $R_{1}$ used in Sec. 4.2 for net (a) and let us assume $m=5, d=2$ and $w_{n}=w_{i}=w_{q}=1$. We recall that net (a) has a deadlock in state $\left[p_{7}\right]$. This can be obtained by firing $\sigma_{3}=t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{3} \in R_{1}$ producing a badness of 0.29 . This error is corrected in net (b). In fact the best simulation of $\sigma_{3}$ in (b) completes in state $\left[p_{5}+p_{7}\right]$ which enables $t_{5}$. Its badness is thus 0 (there are no potentially-dead transitions in this state with $d=2$ ). So (b) improves (a) w.r.t. $\sigma_{3}$. On the other hand, since the deadlock still remains in (c), the badness for $\sigma_{3}$ in (c) is 0.41 . This badness is higher than that of (a) since $t_{7}$ can never be executed in (c). So (c) worsens (a) w.r.t. $\sigma_{3}$.

The no proper completion of (a) in $\left[p_{O}+p_{8}\right]$, obtained e.g. by firing $\sigma_{4}=$ $t_{1} \cdot t_{2} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{5} \cdot t_{6} \cdot t_{4} \cdot t_{3} \cdot t_{7}$ with badness 0.12 , is best simulated in (b) by a trace completing in $\left[p_{O}+p_{5}+p_{8}\right]$. Since this state marks two places besides $p_{O}$ instead of one, it induces a badness of 0.17 which is worse than that of $\sigma_{4}$. So (b) worsens (a) w.r.t. $\sigma_{4}$. For net (c), $\sigma_{4}$ can be best simulated with a trace completing in state $\left[p_{7}\right]$ with a badness of 0.28 . In fact, while there is no improper completion error (the trace does not even mark $p_{O}$ ), there is still a deadlock in $\left[p_{7}\right]$ and $t_{7}$ is dead. So (c) also worsens (a) w.r.t. $\sigma_{4}$. Since (d) is sound, its badness for the above traces is 0 .

Finally, both (b) and (c) worsen (a) w.r.t. $\sigma_{1}$ and $\sigma_{2}$ (the correct traces of $R_{1}$ shown in Sec.4.2], as they introduce new improper completion, resp., no option to complete errors. The overall badness of (a), (b), (c) and (d) w.r.t. $R_{1}$ is $0.41,0.53,1.19$ and 0 .

### 4.4 Dominance-Based Simulated Annealing

Given an erroneous model $N \in \mathcal{N}$, the goal of the PNSA technique is to produce a good set of solutions $\mathcal{S} \subseteq \mathcal{N}$ such that each model $N_{i} \in \mathcal{S}$ is similar to $N$ but contains fewer or no errors. $\mathcal{S}$ can be considered good if i) its members are good solutions according to the three objective functions (structural distance, behavioral distance and badness); ii) they are non-redundant, i.e. no member is better than the others; and iii) all have high confidence, i.e. they have been tested against a given number of sets $R$.

In order to find good solutions while avoiding redundancy in the final solution set, we need to be able to compare two solutions. To do so, we use the values of their objective functions. First, we need to group these functions into a unique objective function w.r.t. a set $R$. Since a solution can be tested against multiple sets $R$, we also need a notion of average unique objective function over the various $R$.

Definition 11 (Unique objective function). Let $N, N^{\prime}$ be two WF-nets. Assuming $N$ and the simulation parameter $m$ are fixed, we define the following objective functions w.r.t. a set of traces $R$ of $N: f_{1}\left(N^{\prime}, R\right)=\lambda\left(N, N^{\prime}\right), f_{2}\left(N^{\prime}, R\right)=\delta\left(N, N^{\prime}, R, m\right)$ and $f_{3}\left(N^{\prime}, R\right)=\beta\left(N, N^{\prime}, R, m\right)$. These functions are grouped into a unique objective function $\bar{f}: \mathcal{N} \times 2^{\operatorname{Tr}(N)} \rightarrow \mathbb{R}^{3}$ such that for each $N^{\prime}$ and $R, \bar{f}\left(N^{\prime}, R\right)$ identifies the triple $\left(\lambda\left(N, N^{\prime}\right), \delta\left(N, N^{\prime}, R, m\right), \beta\left(N, N^{\prime}, R, m\right)\right)$. Given $i$ sets $R_{k}$ with $1 \leq$ $k \leq i$, we compute the average unique objective function $\bar{f}_{\text {avg }}\left(\left\{\bar{f}^{k}\left(N^{\prime}, R_{k}\right)\right\}_{k=1}^{i}\right)=$ $\left(a v g_{1 \leq k \leq i}\left(f_{1}\left(N^{\prime}, R_{k}\right)\right), a v g_{1 \leq k \leq i}\left(f_{2}\left(N^{\prime}, R_{k}\right)\right), \operatorname{avg} g_{1 \leq k \leq i}\left(f_{3}\left(N^{\prime}, R_{k}\right)\right)\right)$.

Considering our example set $R_{1}$, the values of the unique objective functions for nets (ad) are: $(0,0,0.41),(1,0,0.53),(4,0.14,1.19)$ and $(5,0,0)$. The (average) unique objective function can be used to compare two solutions via the notion of dominance. A solution
$N_{1}$ dominates a solution $N_{2}$ iff $N_{1}$ is better than $N_{2}$ in at least one objective function and equivalent in the remaining ones.

Definition 12 (Dominance). Given a set of traces $R$, a solution $N_{1}$ dominates a different solution $N_{2}$ w.r.t. $R$, i.e. $N_{1} \prec_{R} N_{2}$, iff $\bar{f}\left(N_{1}, R\right) \leq \bar{f}\left(N_{2}, R\right)$ and there exists a $1 \leq j \leq 3$ such that $f_{j}\left(N_{1}, R\right)<f_{j}\left(N_{2}, R\right)$. If $N_{1}$ does not dominate $N_{2}$, we write $N_{1} \nprec_{R} N_{2}$. When we have multiple sets $R$, we compute the average dominance by comparing the average unique objective functions of two solutions, and denote this relation with $\prec_{\text {avg }}$.

The dominance relation establishes a partial order and two solutions $N_{1}$ and $N_{2}$ are $m u$ tually non-dominating iff neither dominates the other. In our example, net (a) dominates both (b) and (c), (b) dominates (c), while (d) is mutually non-dominating with all other nets: (d) has higher structural distance than (a-c) although its behavioral similarity and badness are lower than those of the other nets.

A Pareto-set is the set of all mutually non-dominating solutions w.r.t. the average unique objective functions of the solutions, i.e. a set of non-redundant solutions.

Definition 13 (Pareto-set). Two solutions $N_{1}, N_{2} \in \mathcal{N}$ are mutually non-dominating w.r.t. a set of traces $R$ iff $N_{1} \nprec_{R} N_{2}$ and $N_{2} \nprec_{R} N_{1}$. Similarly, $N_{1}$ and $N_{2}$ are mutually non-dominating on average w.r.t. a number of sets of traces, iff $N_{1} \nprec_{\text {avg }} N_{2}$ and $N_{2} \nprec$ avg $N_{1}$. A Pareto-set is a set $\mathcal{S} \subseteq \mathcal{N}$ such that for all solutions $N_{1}, N_{2} \in \mathcal{S}$, $N_{1} \nprec_{\text {avg }} N_{2}$ and $N_{2} \nprec$ avg $N_{1}$.

A Pareto-optimum is a solution that is not dominated by any other solution. The set of Pareto-optima is called the Pareto-front.

Definition 14 (Pareto-optimum, Pareto-front). A Pareto-optimum $N_{1} \in \mathcal{N}$ is a solution for which no $N_{2} \in \mathcal{N}$ exists such that $N_{2} \prec_{\text {avg }} N_{1}$. A Pareto-front $\mathcal{G}$ is the set of all Pareto-optima.

Our PNSA technique is an adaptation of dominance-based MOSA [13]14] to the problem of automatically fixing errors in process models. Dominance-based MOSA is a robust technique for solving multi-objective optimization problems. At the core of the MOSA technique is an optimization procedure called simulated annealing [9]. The term "simulated annealing" derives from the "annealing" process used in metallurgy: the idea is to heat and then slowly cool down a metal so that its atoms reach a low-energy, crystalline state. At high temperatures atoms are free to move around. However, as the temperature lowers down, their movements are increasingly limited due to the high-energy cost of movement. By analogy with this physical process, each step of the annealing procedure replaces the current solution by a random "nearby" solution with a probability that depends both on the difference between the corresponding objective values and a global parameter Temp (the temperature), that is decreased during the process. The dependency is such that the current solution changes almost randomly when Temp is high, but increasingly less as Temp goes to zero. Allowing "uphill" moves potentially saves the method from getting stuck at local optima, which is the main drawback of greedy algorithms. The goal is thus to move towards the Pareto-front while encouraging the diversification of the candidate solutions. It has been shown that simulated annealing
can be more effective than exhaustive enumeration when the goal is to find an acceptably good solution in a fixed amount of time, rather than the best possible solution [9]. Our technique differs from the classic dominance-based MOSA by the presence of approximate objective functions (behavioral distance and badness), and by the notion of confidence, which is used to compensate for this approximation by testing each solution against multiple sample traces.

In order to escape from local optima, and in-line with dominance-based MOSA, we do not simply compare two solutions based on their dominance relation. This in fact would exclude a candidate solution $N_{2}$ that based on the current set of sample traces $R$ is dominated by the current solution $N_{1}$ even if globally $N_{2}$ may be better than $N_{1}$. Rather, we use a notion of energy. The energy of a solution measures the portion of the front that dominates that solution. Thus, the lower the energy of a solution is, the better the solution is. Unfortunately, the true Pareto-front $\mathcal{G}$ is unavailable during an optimization procedure. To obviate this problem, the energy function is computed based on a finite approximation of the Pareto-front $G \subseteq \mathcal{N}$, called estimated Paretofront. $G$ is built incrementally based on the Pareto-set $\mathcal{S}$ under construction. Thus, $G$ is initially empty and incrementally populated with new values as long as new mutually non-dominating solutions are added to $\mathcal{S}$ during the annealing procedure.

Definition 15 (Energy). Let $R$ be a set of traces and $G \subseteq \mathcal{N}$ be a finite estimation of the Pareto-front $\mathcal{G}$. The energy of a $W F$-net $N^{\prime}$ w.r.t. $R$ and $G$ is $E\left(N^{\prime}, R, G\right)=\mid\left\{N^{\prime \prime} \in\right.$ $\left.G: N^{\prime \prime} \prec_{R} N^{\prime}\right\} \mid$.

Having defined the notion of energy, we can use this to compare two solutions in the annealing procedure. A candidate solution $N_{2}$ is accepted in place of the current solution $N_{1}$ on the basis of their energy difference $\Delta_{E}$ w.r.t. $R$ and an estimated Pareto-front, i.e. the difference in the number of solutions in the estimated Pareto-front that dominate $N_{1}$ and $N_{2}$ w.r.t. $R$.

Definition 16 (Energy difference). Let $N_{1}, N_{2}$ be two WF-nets, $R$ be a set of traces and $G$ be the finite estimation of $\mathcal{G}$. Given the set $\tilde{G}=G \cup\left\{N_{1}, N_{2}\right\}$, the energy difference between $N_{1}$ and $N_{2}$ w.r.t. $R$ and $G$ is $\Delta_{E}\left(N_{2}, N_{1}, R, G\right)=$ $\frac{E\left(N_{2}, R, \tilde{G}\right)-E\left(N_{1}, R, \tilde{G}\right)}{|\tilde{G}|}$.
A candidate solution $N_{2}$ that is dominated by one or more members of the current estimated Pareto-front, may still be accepted with a probability equal to $\min \left(1, \exp \left(-\Delta_{E}\left(N_{2}, N_{1}, R, G\right) / \operatorname{Temp}(i)\right)\right)$ where $\operatorname{Temp}(i)$ is a monotonically decreasing function indicating the temperature for the iteration $i$ of the annealing procedure. In Def. 16, the inclusion of $N_{1}$ and $N_{2}$ in set $\tilde{G}$ yields a negative $\Delta_{E}$ if $N_{2} \prec_{R} N_{1}$. This ensures that candidate solutions that move the estimated front towards the true front are always accepted. The division by $|\tilde{G}|$ also ensures that $\Delta_{E}$ is always less than 1 , and provides some robustness against fluctuations in the number of solutions in $G$. A further benefit of $\Delta_{E}$ is that, while fostering convergence to the front, it also fosters its wide coverage. For example, let us assume we only have two objective functions $f_{1}$ and $f_{2}$. Fig. 2 depicts the objective values of two solutions, $N_{1}$ and $N_{2}$ (represented as empty circles) in relation to the values of the Pareto-front and its estimation $G . N_{1}$ and
$N_{2}$ are mutually non-dominating ( $N_{1}$ is better than $N_{2}$ along $f_{2}$ but $N_{2}$ is better along $f_{1}$ ). However $N_{1}$ is dominated by fewer elements of $G$ than $N_{2}$ ( 2 instead of 4). Thus, $N_{1}$ has lower energy and would be more likely accepted in place of $N_{1}$.

Let us assume an estimated Pareto-front of $\{(0,0,0.41),(5,0.12,0.23),(9,0,0),(11,0,0.71)\} \quad$ for our working example. Accordingly, net (b) has a lower energy than (c) so it has a higher probability of being accepted than (c). In turn, despite (d) is mutually non-dominating with both (b) and (c), it has a lower energy than these two nets, so it has a higher probability of being accepted in place of them.

At each iteration $i$ of the annealing procedure we test the solutions for a random set of traces $R_{i}$ of the original model.


Fig. 2. Two solutions $N_{1}$ and $N_{2}$ and their energy If at any iteration a candidate solution $N_{2}$ has the same energy as the current one $N_{1}, N_{2}$ has probability of 1 of being chosen ( $\Delta_{E}=0$ ). However, we prefer to keep the current solution since this has also been tested against some other sets $R_{j<i}$. This is captured by the notion of confidence of a solution, which indicates how many annealing iterations a solution has survived through. The more iterations a solution survives through, the more the confidence increases that this is a good solution.

We now have all ingredients to present the PNSA algorithm. The PNSA algorithm consists of multiple runs of the annealing procedure so as to incrementally construct a Pareto-set formed by mutually non-dominated solutions on average, with the same high confidence. At each run the produced solutions are exploited to feed the estimated Pareto-front, which in turn is used to compare solutions based on their energy difference. The PNSA algorithm terminates when a given timeframe $t f$ elapses or a maximum number of final solutions $s$ is found, and returns the Pareto-set. The algorithm also requires as input the original model $N$, a finite representation of its traces $\operatorname{Tr}(N)$ and of its erroneous traces $\overline{\mathrm{E} \operatorname{Tr}}(N)$, the desired confidence $c$ of a solution, the maximum number of iterations $o$ for each run of the annealing procedure, a temperature $\operatorname{Temp}(i)$ decreasing at each iteration $i$, the maximum size $k$ of each set $R_{i}$, and the parameters used for behavioral distance and badness (see Sec. 4.2 and 4.3).

The annealing procedure invoked at each run of the PNSA algorithm requires as input the Pareto-set $\mathcal{S}$ of the current solutions (initially empty), and uses it to create the estimated Pareto-front $G$. Then, at each iteration the procedure creates a perturbation of a solution randomly drawn from $\mathcal{S} \cup\{N\}$, and compares their energy difference w.r.t. a random set of traces $R_{i}$ of $N$ and $G$. Based on the resulting probability, one of the two solutions is added to a priority list of current solutions $L S$ ordered by decreasing confidence. The procedure terminates when the maximum number of iterations $o$ is reached or when the first member of $L S$ has confidence $c$, and produces as output the first element of $L S$ if this has confidence equal to $c$. This solution is added to $\mathcal{S}$ for the next run of the PNSA algorithm if it is non dominated on average by any element currently in $\mathcal{S}$. If so, the elements of $\mathcal{S}$ that are dominated on average by the solution being added are removed to ensure that all elements of $\mathcal{S}$ are always mutually non-dominated on average. The average dominance is computed by keeping for each solution $N^{\prime}$ an archive $A_{N^{\prime}}$ storing the values of the unique objective functions of $N^{\prime}$ for all sets $R_{i}$ used for testing $N^{\prime}$. The steps of the PNSA algorithm are:

1. Initialize the estimated Pareto-front $G$ with the Pareto-set $\mathcal{S}$ and empty the solution list $A$ (in the initial run, $\mathcal{S}=\varnothing$ ).
2. Randomly draw a solution $N_{1}$ from $\mathcal{S} \cup\{N\}$ and set $N_{1}$ as the current solution (in the initial run, $N_{1} \equiv N$ ).
3. Generate a random perturbation $N_{2} \in \mathcal{N}$ of $N_{1}$ via a minimum sequence of edit operations.
4. Randomly draw a set $R_{i} \subseteq \overline{\operatorname{Tr}}(N)$ of size $k$ such that $\left|\overline{\mathrm{ETr}}(N) \cap R_{i}\right|=k / 2$ if $|\overline{\operatorname{ETr}}(N)|>$ $k / 2$ or $\overline{\mathrm{ETr}}(N) \subset R_{i}$ if $|\overline{\mathrm{ETr}}(N)| \leq k / 2$.
5. Compute the unique objective functions of $N_{1}$ and $N_{2}$ w.r.t. $R_{i}$ and add their values to the respective archives $A_{N_{1}}$ and $A_{N_{2}}$.
6. Compute the energy difference $\Delta_{E}\left(N_{2}, N_{1}, R_{i}, G\right)$ between $N_{2}$ and $N_{1}$ using the estimated Pareto-front $G$.
7. If $\Delta_{E}\left(N_{2}, N_{1}, R_{i}, G\right) \neq 0$ replace the current solution $N_{1}$ with $N_{2}$ with a probability equal to $\min \left(1, \exp \left(-\Delta_{E}\left(N_{2}, N_{1}, R_{i}, G\right) / \operatorname{Temp}(i)\right)\right)$. Otherwise discard $N_{2}$ and increase the confidence of $N_{1}$ by 1 .
8. If $N_{2}$ is accepted in place of $N_{1}$, set $N_{2}$ as the current solution with confidence 1 , and add $N_{2}$ to $L S$.
9. Repeat from Step 3 while the confidence of the current solution is less than $c$ and the maximum number of iterations $o$ is not reached.
10. Add the current solution to $L S$. If the first element of $L S$, $l s_{1}$, has confidence at least $c$, compute its average unique objective function $\bar{f}_{\text {avg }}\left(l s_{1}, A_{l s_{1}}\right)$ based on its archive $A_{l s_{1}}$. Add $l s_{1}$ to $\mathcal{S}$ if $l s_{1}$ is not dominated on average by any element of $\mathcal{S}$, and remove all elements of $\mathcal{S}$ that are dominated on average by $l s_{1}$.
11. Repeat from Step 1 until the timeframe $t f$ elapses or $|\mathcal{S}|=s$.

The complexity of each annealing iteration is dominated by Steps 3, 5 and 6 (the rest is achieved in constant time). Step 3 computes a perturbation, which is linear on the size of the WF-net to be changed (the net is explored depth-first to check if a node can be removed; node/arc insertion and arc removal are achieved in constant time). Step 5 entails the computation of the objective functions. Computing the structural similarity is linear on the number of edit operations used in the perturbation, which in turn is bounded by the size of the WF-net. For the behavioral similarity and badness we use a depth-first search on the WF-net, which is linear on the product of i) the sum of the lengths of the traces in $R$ to be simulated, ii) the maximum number of silent actions we can use to simulate a trace, and iii) the size of the WF-net. Step 6 entails the computation of the energy difference, which is done in logarithmic time on the size of the estimated Pareto-front [13]. So each annealing iteration can be executed efficiently.

## 5 Experimental Results

We implemented the PNSA algorithm in a prototype Java tool (available at Www.apromore.org/tools). This tool imports an unsound WF-net in LoLA format, and builds a finite representation of its state-space using Karp-Miller's acceleration [8]. This is done by exploring as many distinct transitions as possible in the smallest number of states. The result of the soundness check and the user parameters trigger the PNSA algorithm. At each iteration $i$ of the annealing procedure, the tool performs at most $k$ prioritized random walks on the state-space to extract the sample traces of set $R_{i}$. More precisely, for each trace, the state-space is traversed backwards starting from
a final state and by prioritizing those transitions that have been visited the least, until the initial state is reached. Correct traces are extracted starting from $M_{O}$; erroneous traces are extracted starting from a final state that led to an error (available from the soundness check). The output of the tool is a set of solutions in LoLA format, which is limited by the maximum response time or by the maximum number of solutions set by the user.

We used the tool to fix a sample of 152 unsound nets drawn from the BIT process library [6]. This library contains 1,386 BPMN models in five collections (A, B1, B2, B3, C), out of which 744 are unsound. We converted these 744 models into WF-nets and filtered out those models that did not result in lawful WF-nets (e.g. those models that had multiple output places). In particular, we only kept models with up to two output places, and when we found two output places we merged them in a single output place. Since this operation may introduce a lack of synchronization, we discarded models with more than two output places to minimize the impact of such artificial errors. As a result, we obtained 152 models none of which from collection $C$. We set the maximum number of final solutions to 6 , the desired confidence to 100 , the maximum number of iterations for each annealing run to 1,000 , the initial temperature to 144 , the maximum size of each set of sample traces to 50 , and all the parameters for behavioral distance and badness to 1 . After the experiment each solution was checked for soundness. The tests were conducted on a PC with a 3 GHz Intel Dual-Core x64, 3 GB memory, running Microsoft Windows 7 and JVM v1.5. Each test was run 10 times by using the same random seed (to obtain deterministic results) and the execution times were averaged. The results are reported in Table 1

Table 1. Experimental results

| Input models |  |  |  | Solutions |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Collection | $\begin{gathered} \text { No. } \\ \text { models } \end{gathered}$ | Avg/Max nodes | $\begin{gathered} \text { Avg/Max } \\ \text { errors } \end{gathered}$ | Avg/Max nodes | $\begin{gathered} \text { Avg/Max } \\ \text { errors } \end{gathered}$ | Avg Error <br> reduction | $\begin{array}{c}\text { Sound } \\ \text { models }\end{array}$ | Avg/Max str. distance [cost] | $\begin{gathered} \text { Avg/Max Time } \\ {[\mathrm{s}]} \end{gathered}$ |
| BIT A | 48 | 46.54/129 | $2.21 / 5$ | 45.85/129 | 0.74/20 | 73.6\% | 85.7\% | 4.25/39 | 16.52/171.43 |
| BIT B1 | 22 | 29.55/87 | 2.55/6 | 27.18/87 | 1.07/29 | 75.6\% | 82.9\% | 5.02/91 | 8.75/100.45 |
| BIT B2 | 35 | 22.86/117 | 2.54/9 | 21.79/118 | 0.69/9 | 84.9\% | 87.3\% | 3.47/47 | 12.08/217.91 |
| BIT B3 | 47 | 20.38/73 | 2.77/9 | 21.42/118 | 1.26/24 | 72.4\% | 79.6\% | 4.62/61 | 10.85/156.93 |

The error-reduction rate of a solution is the difference between the number of errors in the initial model and the number of errors in the solution, over the number of errors in the initial model. Table 1 shows the average error-reduction rate for all solutions of each collection, which leads to an average error-reduction of $76.6 \%$ over all four collections. This indicates that the algorithm is able to fix the majority of errors in the input models. Moreover, the structural distance of the solutions is very low (4.34 on average using a cost of 1 for each edit operation). Thus, the solutions are very similar to the original model. These solutions are obtained with an average response time of 11 s . Despite the large response time in some outlier cases (218s), most solutions are behaviorally better than their input models ( $83.9 \%$ are sound) and at least one sound solution was found for each input model. Very few cases are worse than the input model (e.g. 29 errors instead of 6 errors in the input model). This is due to the fact that we did not fine-tune the annealing parameters based on the characteristics of each input model (e.g. if the number of annealing iterations is too low w.r.t. the number of errors in the input model, a solution could contain more errors than the input model).

## 6 Conclusion

This paper contributes a technique for automatically fixing behavioral errors in process models. Given an unsound WF-net and the output of its soundness check, we generate a set of alternative nets containing fewer or no behavioral errors, until a given number of desired solutions is found or a timeframe elapses. Each solution is i) sufficiently similar to the original model, ii) non-redundant in terms of fixed errors, and iii) optimal with high-confidence, i.e. it must pass a number of tests. Moreover, there is no restriction on the type of unsound WF-net that can be fixed (e.g. acyclic, non-free choice).

The core of this technique is a heuristic optimization algorithm based on dominancebased MOSA. The choice of this algorithm over other optimization algorithms is mainly motivated by i) the availability of a single individual (the unsound model) rather than a population; ii) the fact that the modeler's intentions are unknown, which determines the fuzziness of the result; and iii) by the need to independently optimize different objectives. Also, an important advantage of MOSA over other optimization algorithms is that while converging to optimal solutions, it encourages the diversification of the candidate solutions. In turn, this allows the algorithm to escape from local optima, i.e. solutions that sub-optimally improve the original model. It has been shown that dominance-based MOSA outperforms other multi-objective genetic algorithms [13]. Our adaptation of MOSA to the problem of fixing unsound process models uses three objective functions to drive the selection of candidate solutions. These functions measure the similarity of a solution to the unsound model and the severity of its errors. Moreover, we embed a notion of confidence to measure the reliability of a solution. This compensates for the approximation of our definitions of behavioral distance and badness, which is due to efficiency reasons. Clearly, more sophisticated metrics could be employed in place of our objective functions, e.g. to identify dead transitions. However one has to strike a trade-off between accuracy and computational cost. Indeed, we compute our objective functions in linear time.

More generally, our work can be seen as a modular framework for improving business process models. In fact one could plug in other objective functions to serve different purposes, such as fixing non-compliance issues or increasing process performances.

We prototyped our technique in a tool and validated it on a sample of industrial process models. While we cannot guarantee that the returned solutions are always sound, we found at least one sound solution for each model used in the tests, and the response times were reasonably short. However, in order to prove the usefulness of this technique, the quality of the proposed changes needs to be empirically evaluated. In future work, we plan to compare our solutions with those produced by a team of modeling experts and use these results to train the algorithm to discard certain types of perturbations.

There are other interesting avenues for future work. First, the randomness of the perturbations could be controlled by exploiting crossover techniques from genetic algorithms [7], so as to obtain a new perturbation by combining correct (sub-)traces from each solution in the current Pareto-set. Second, to accelerate the identification of optimal solutions, the energy resolution could be increased by using attainment surface sampling techniques [13]. This would compensate for the small size of the estimated Pareto-front at the beginning, which yields coarse-grained comparisons of solutions. Finally, the structural features of the unsound model and the result of its soundness check
could be exploited to estimate the annealing parameters (e.g. the number of annealing iterations could depend on the number of errors found in the unsound model).

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[^0]:    ${ }^{1}[x]$ returns 1 if the boolean formula $x$ is true, or 0 otherwise

