

# Accurate equivalent-network modelling of GaAs/AlAs based resonant tunnelling diode with symmetric thin barrier and spacer layers

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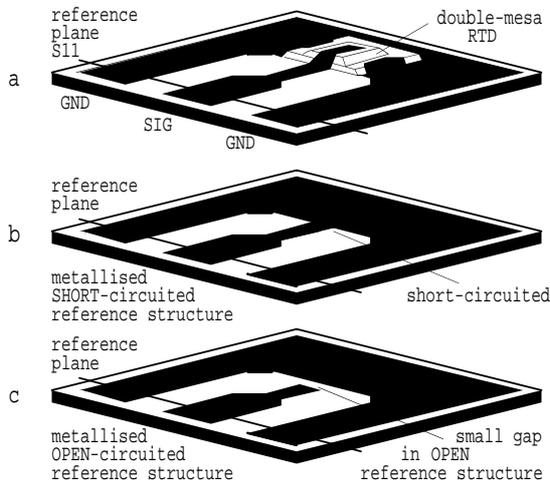


Fig. 2. (a) Planar RTD with coplanar probe access. (b) SHORT-reference structure ( $Z_d = 0$ ) (c) OPEN-reference structure ( $Z_d \Rightarrow \infty$ )

### Equivalent-network models

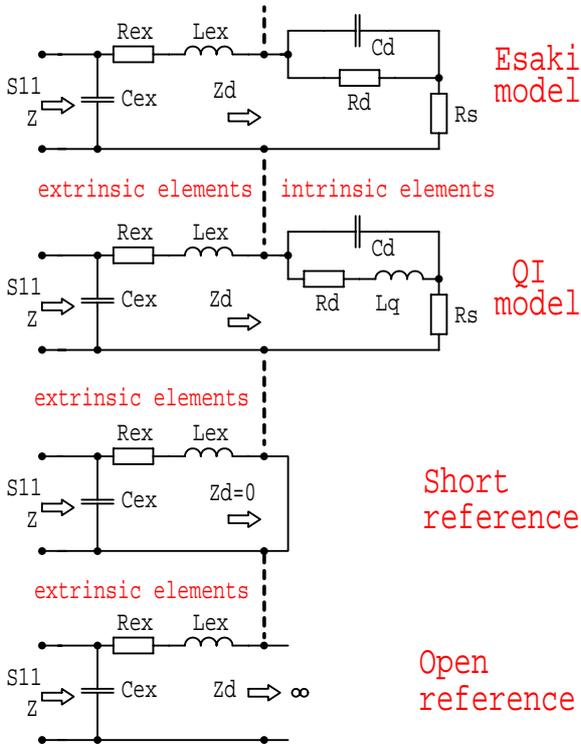


Fig. 3. Equivalent-circuit models of extrinsic RTD, consisting of interconnection elements  $C_{ex}$ ,  $R_{ex}$ ,  $L_{ex}$  (pads-to-mesa), and intrinsic RTD equivalent-circuits: Esaki-model and Quantum Inductance (QI)-model. Also shown are the SHORT and OPEN reference structures.

choice of the device area ( $20 \mu\text{m}^2$ ; to make  $R_d + R_s + R_{ex}$  more negative than  $-50 \Omega$  at the steepest slope in the NDR region, which gives a finite  $S_{11}$ ) and a specially designed bias circuit, the stability condition was met in our experiments.

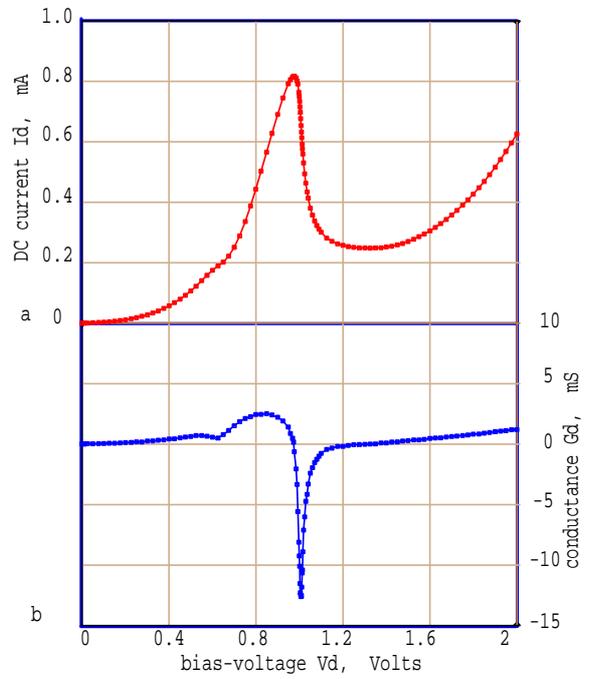


Fig. 4. (a) DC I-V curve of extrinsic RTD, measured at  $21^\circ\text{C}$  (on-wafer reference plane). (b) Differential conductance  $G_d$  [mS].

An array of  $S_{11}$ -data was collected in the 0 to +2 V range of the I-V curve (mesa top is +V), where  $S_{11}$  of the extrinsic RTD was measured at 75 bias points and from 0.05 - 40.05 GHz (401 points), after network analyser calibration with on-wafer standards. Fig. 5 shows some of these  $S_{11}$ 's in a compressed Smith chart, amongst them  $S_{11}$  in the smallest-NDR point ( $V_d = 1.0060\text{V}$ ;  $|S_{11}| \sim 3.9$ ). The prober-chuck temperature was  $21^\circ\text{C}$ .

### III. ESAKI AND MODIFIED ESAKI MODELS

Note that in a substantial range of NDR-region bias-voltages, the  $S_{11}$  curves show an inflection point, a feature that cannot be modeled by the Esaki equivalent-circuit with three, frequency-independent intrinsic elements (Fig. 3). Optimisation of these intrinsic parameters to carefully match the measured  $S_{11}$ -data (at each bias point), leads to the conclusion that the Esaki-model needs an extra degree of freedom to fit the measured  $S_{11}$  data array in the NDR region sufficiently accurate. Fig. 6a displays the real and imaginary parts of the intrinsic impedance  $Z_d$  at  $V_d = 1.0060\text{V}$  (largest negative  $G_d$ ), and Fig. 6b shows the dynamic conductance  $G_d$  and capacitance  $C_d$ , when these elements are taken frequency-dependent (in accordance with [4]) to match the measured  $S_{11}$ . The mathematical equations that describe  $G_d$  and  $C_d$  as a function of frequency in the modified Esaki-model are also bias-dependent, which complicates CAD use.

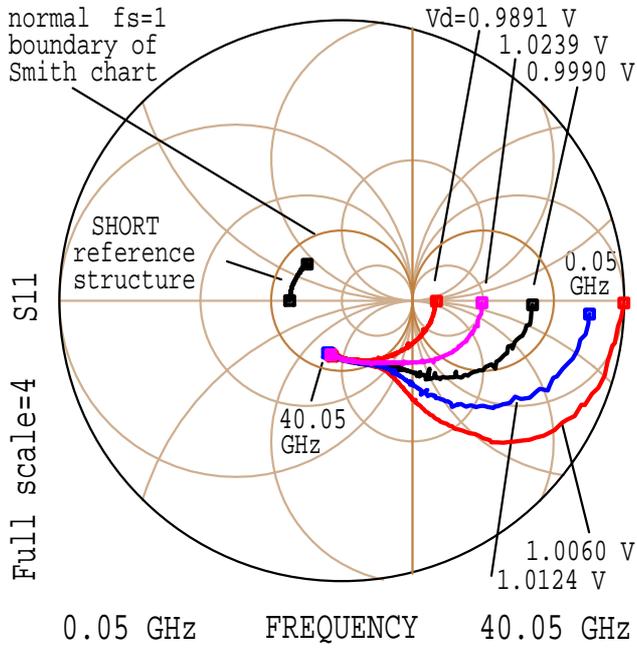


Fig. 5. Measured  $S_{11}$  of SHORT-reference ( $Z_d = 0$ ) and measured  $S_{11}$  of extrinsic RTD at several bias-voltages  $V_d$ , plotted in a compressed Smith chart (full scale=4.0).  $T_{\text{chuck}}=21^\circ\text{C}$ .

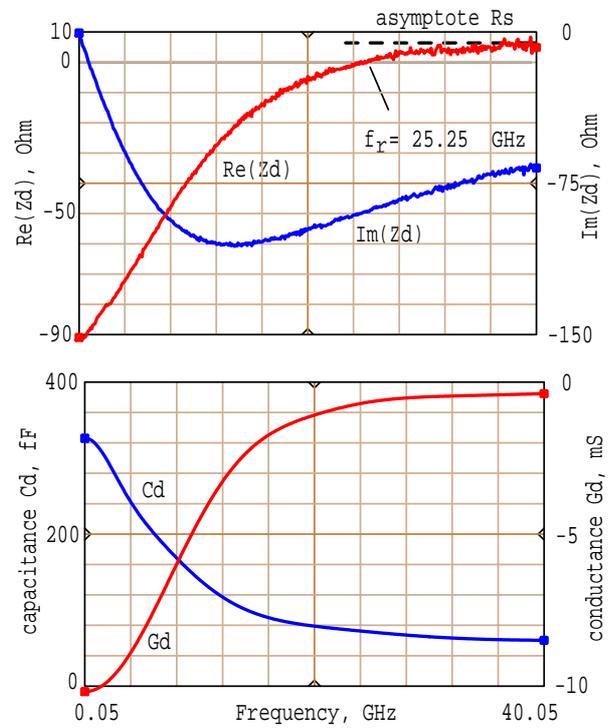


Fig. 6. (a) Real and imaginary parts of measured intrinsic RTD impedance  $Z_d$ , at steepest slope of NDR region (1.0060V). (b) Frequency-dependence of optimized dynamic elements  $C_d$  and  $G_d$  of modified Esaki-model (1.0060V).

Element values against bias  $V_b$  :

- 7a Conductance  $G_d$
- 7b Capacitance  $C_d$
- 7c Resistance  $R_s$
- 7d Inductance  $L_q$
- 7e Time constant  $\tau$
- 7f Cutoff frequency  $F_r$

Fig.7d-f on 0.5-1.5 V scale for improved visibility

Dotted line in all figures is DC current  $I_d$  1 mA full scale.

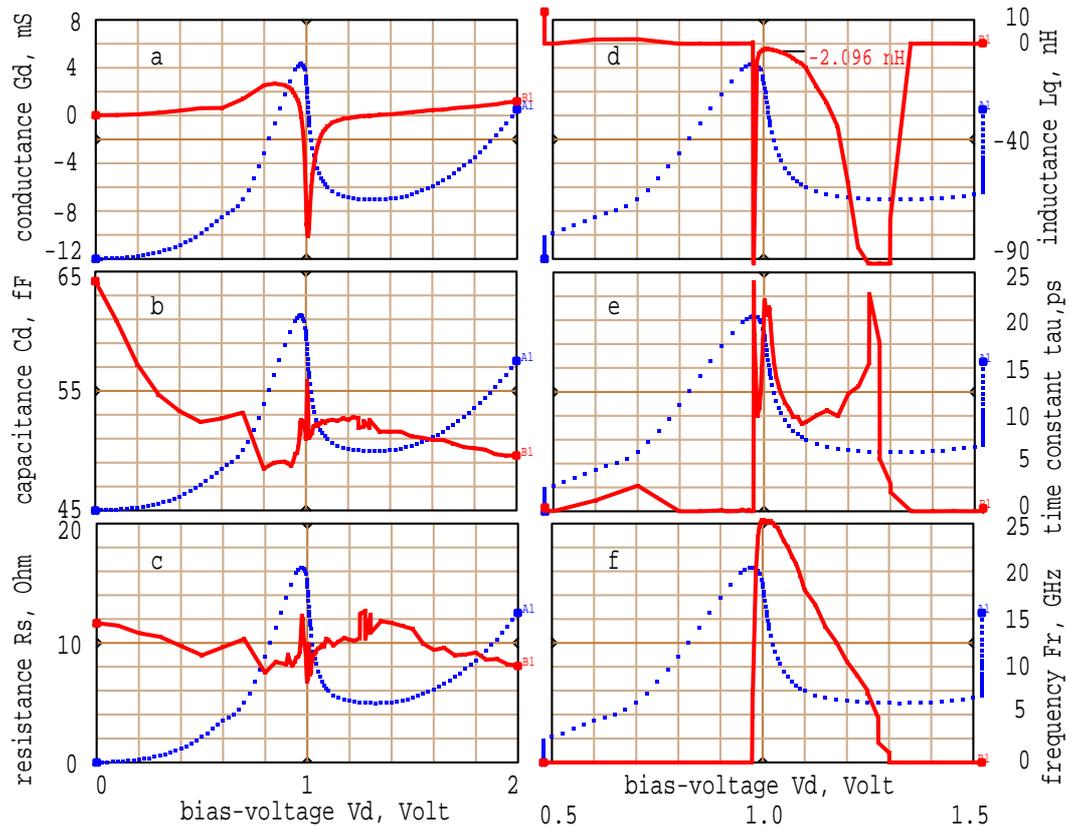


Fig. 7. Optimized intrinsic RTD elements Quantum Inductance (QI) model. Dynamic elements against bias-voltage, 75 points.

#### IV. QUANTUM INDUCTANCE MODEL

The same measured small-signal  $S_{11}$  datasets can be described 'perfectly' by the Quantum Inductance circuit model (Fig. 3) over the full bias-voltage (0-2 V) and frequency ranges (0.05-40.05 GHz) with four, frequency-independent intrinsic elements (Fig. 7a-d). The measurement of  $S_{11}$  on the stable RTD throughout the entire NDR region without hiatus, results in the correct determination of a time constant  $\tau$ , here defined as  $\tau = L_q/R_d (= L_q \cdot G_d)$  which, according to several authors [1,2], should be an indication of the quasibound-state lifetime in the quantum well. The display of this parameter  $\tau$  (Fig. 7e) and of  $L_q$  continuously over the whole undistorted NDR region is a novelty. Near the point where  $G_d$  has zero conductance (at the peak and valley voltages), the values of  $\tau$  are less reliable.  $\tau$  is not defined where  $G_d = 0$ . The peak value of  $\tau$  corresponds with the negative  $G_d$ -peak (same bias). The calculated quasibound ground-state lifetime  $\tau_1$  given in [5] of  $\sim 50$  ps for an AlAs barrier thickness of 2.547 nm and  $\sim 18$  ps for 2.264 nm (a decrease of 1 monolayer), compares well with the time constant  $\tau = 22$  ps measured. Fig. 7f shows the resistive cut-off frequency  $f_r$  against bias-voltage of the intrinsic RTD. In the passive regions of the I-V curve, the QI-model reduces to the Esaki-model, since the element-optimisation process finds there low values of  $L_q$ . For CAD purposes, a very good RTD intrinsic impedance description in the entire bias/frequency space (0-2V; 0.05-40.05 GHz) is obtained with four frequency-independent intrinsic elements, scalable with device area.

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