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RESEARCH ARTICLE

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Electromagnetic modeling and design of a novel class of complementary split-ring resonators

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Abstract

This research study reports the assessment of complementary split ring resonators based on Gielis transformation as basic elements for the design of high-performance microwave components in printed technology. From the electromagnetic simulation of said structures, suitable equivalent circuit models are extracted and analyzed. Physical prototypes are fabricated and tested for design validation. The obtained results confirm that the adoption of supershaped geometries enables the synthesis of very compact scalable microwave filters.

KEYWORDS

complementary split-ring resonator, equivalent circuit, Gielis formula, metamaterials, microwave filter

1 | INTRODUCTION

Split ring resonators (SRRs) have been originally proposed as metamaterial structures featuring double negative medium properties,^{1–3} whereas their complementary variant complementary split ring resonators (CSRRs) are typically utilized as negative-permittivity components in planar left-handed structures for synthesis of artificial transmission lines and complex microwave passive components such as multiband impedance inverters.^{4,5} In particular, the use of SRRs and CSRRs as basic resonant units in planar microwave filters has gained a progressively growing interest thanks to their electrically small size when compared to conventional resonators, this enabling the realization of semilumped filtering structures with high performance and controllable characteristics.^{6–11}

Canonical circular or square geometries are commonly adopted for the design of the considered class of resonators. More recently, Sierpinsky fractal geometries have been proposed for the realization of miniaturized CSRRs still with a square-like form factor.¹² It is to be noticed that squares and circles may be

regarded as special cases of the Gielis equation,¹³ so the question arises whether higher-order supershaped geometries could provide benefits or additional degrees of freedom in the synthesis of highly compact planar microwave filters. The goal of this study is therefore to analyze the performance of bandpass CSRR filters whose geometry is based on Gielis formula.

The article is organized as follows. A detailed description of the geometry of the considered CSRR unit cells, as well as of the equivalent circuit models used to investigate the relevant electromagnetic properties is given in section 2. Measurement results are presented and discussed in section 3. Finally, the concluding remarks and outline of future work are summarized in section 4.

2 | SUPERSHAPED CSRR

2.1 | Geometrical foundation of the design

Gielis formula is a generalization of Lamé equation that can be used to describe a wide variety of complex shapes found

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in Nature. Its general expression is reported in Ref. 13. In this study, we are making use of the following particular case:

$$\rho = r_m(\varphi) = \frac{1}{2} \lim_{n \to +\infty} \left(\left| \cos \frac{m\varphi}{4} \right|^n + \left| \sin \frac{m\varphi}{4} \right|^n \right)^{-\frac{1}{n}}$$
$$= \frac{1}{2} \min\left\{ \left| \sec \frac{m\varphi}{4} \right|, \left| \csc \frac{m\varphi}{4} \right| \right\}, \tag{1}$$

with ρ and φ denoting the usual polar coordinates defined with respect to a background Cartesian reference frame Oxy, and where *m* is a positive integer parameter which defines the number of pseudovertices featured by the general closed curve C_m described by (1).

It is known from the basic theory of differential geometry that the length and area of C_m are given, respectively, by:

$$\ell_m = \int_0^{2\pi} \sqrt{r_m^2(\varphi) + \left[\frac{dr_m(\varphi)}{d\varphi}\right]^2} d\varphi, \qquad (2)$$

$$A_m = \frac{1}{2} \int_0^{2\pi} r_m^2(\varphi) d\varphi.$$
(3)

By making use of (2) and (3), it can be found out, after simple algebra, that the considered class of supershaped curves is characterized by unitary area $A_m = 1$ for m > 0, whereas the length can be computed as:



FIGURE 1 Supershaped closed curves C_m (A) and relevant length ℓ_m and area A_m (B) for different values of the Gielis order *m*



FIGURE 2 Topology (A) and physical prototypes (B) of supershaped complementary split ring resonators-based stop-band filters realized in microstrip technology

$$\ell_m = \sqrt{8 + \frac{m^2}{2}} + 4\left[F\left(\frac{\pi}{4} \left| 1 - \frac{m^2}{16}\right) - E\left(\frac{\pi}{4} \left| 1 - \frac{m^2}{16}\right)\right], \quad (4)$$

with $F(\cdot | \cdot)$ and $E(\cdot | \cdot)$ being the elliptic integral of the first and second kind, respectively. It is apparent from (4) that ℓ_m increases asymptotically with linear law, namely $\ell_m \propto (\sqrt{2}-1) m$ as $m \to +\infty$ (see Figure 1).

2.2 | Physical implementation

The microwave filters investigated in this study consist of a microstrip transmission line loaded with a supershaped CSRR of general Gielis order m etched in the relevant ground plane, as shown in Figure 2A.

The considered structure is realized on dielectric laminate having relative permittivity $\varepsilon_r = 3.78$, and loss tangent tan $\delta = 0.025$, the thickness of the metal layers being



FIGURE 3 Stop-band frequency f_z and peak insertion loss IL_{max} of supershaped complementary split ring resonators-based filters as a function of the Gielis parameter m and the geometrical parameters s, d, g as shown in Figure 2

 $t = 35 \,\mu\text{m}$. The two concentric ring slots forming the CSRR unit are separated by distance s, and are characterized by width d and gap g. Conversely, the microstrip line printed on the circuit substrate features a width w = 1.835 mm, which is selected in such a way as to achieve a nearly 50 Ω characteristic impedance.

The design and full-wave analysis of the complete assembly has been carried out by making use of the commercially available electromagnetic solver CST Microwave Studio.¹⁴ In this way, the characteristics of the structure in

terms of stop-band frequency f_z and peak insertion loss $(IL_{\text{max}} = -20 \log |S_{21}(f_z)|)$ have been evaluated as a function of the geometrical parameters s, d, g, and m.

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From the visual inspection of Figure 3, it is apparent that f_z is decreasing as s, d, g become smaller, and the Gielis order m increases. Conversely, under the same conditions, $IL_{\rm max}$ tends to decrease. It is worth noting here that the general supershaped CSRR as described by (1) degenerates in the conventional circular and square one for $m \rightarrow 0$ and m = 4, respectively.

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FIGURE 4 Lumped-element equivalent circuit models of a complementary split ring resonators-loaded microstrip line (see Figure 2) as proposed by Baena et al. (A) and Li et al. (B)

Following the design stage, several physical demonstrators of the considered filtering structures (see Figure 2A), with s = d = g = 0.75 mm and *m* ranging from 5 to 10, have been fabricated. As it can be noticed in Figure 2B, SMA adapters are soldered at both ports of the device, and adopted as connector interface to external coaxial cables for *S*-parameter measurements.

2.3 | Equivalent circuit models

Thanks to the small electrical size of CSRRs at the resonance ($\sim \lambda/10$), the considered structures can be conveniently described by means of suitable lumped-element equivalent circuits. Several models have been proposed in the scientific literature. In this respect, Baena et al. proposed the circuit topology shown in Figure 4A,⁶ where the CSRR unit is modeled as a parallel resonant tank with inductance L_c and capacitance C_c and, therefore, characterized by resonant frequency:



FIGURE 5 Insertion loss of a microstrip transmission line loaded with a supershaped complementary split ring resonators of Gielis order $m \in [5, 10]$

TABLE 1 Equivalent circuit parameters of supershaped complementary split ring resonators as a function of the relevant Gielis order m (C_x in pF, L_x in nH)

m	L	С	L_c	C_c	L_1	<i>C</i> ₁	<i>C</i> ₂
5	3.85	0.95	5.59	0.27	8.31	0.83	-2.51
6	3.54	1.06	5.62	0.22	7.98	0.90	-2.51
7	4.18	0.91	6.38	0.28	9.44	0.80	-2.51
8	4.33	0.87	6.70	0.30	10.28	0.76	-2.53
9	4.45	0.89	6.98	0.31	10.35	0.81	-2.63
10	4.37	0.86	7.92	0.27	11.58	0.78	-2.59

$$f_0 = \frac{1}{2\pi\sqrt{L_c C_c}}.$$
(5)

In said schematic, the capacitance C models the coupling between the CSRR and the microstrip line which, in turn, is characterized by inductance L. It is worth mentioning that the inductance L_c is mainly dependent on the length ℓ_m of the CSRR embedded in the design, whereas the capacitance C is largely affected by the relevant area which, for the proposed class of structures, is an invariant.

At frequency f_0 , the shunt admittance is zero and, therefore, the impedance measured at the any port of the network is set by the host line inductance *L* which, in turn, can be readily estimated by using well-known computer-aided design (CAD) formulas available in the scientific literature. Conversely, the transmission-zero frequency of the filter, at which the condition $S_{21} = 0$ holds true, is readily found to be:

$$f_z = \frac{1}{2\pi\sqrt{L_c(C+C_c)}}.$$
(6)

Finally, upon denoting the series and shunt impedances of the equivalent T-network of the structure as Z_1 and Z_2 , respectively, one can verify, after simple mathematical manipulations, that:

$$Z_1(f_{\pi/2}) + Z_2(f_{\pi/2}) = 0, \tag{7}$$

with $f_{\pi/2}$ being the frequency where the phase of the transmission coefficient S_{21} is equal to zero. By combining (5) and (6) with (7), the parameters of the circuit model in Figure 4A can be extracted from the numerically simulated *S*-parameter data.

Li et al. proposed, for the considered structure, the alternative equivalent circuit topology shown in Figure 4B,⁷ that consists of a series *LC* resonator (L_1 , C_1) with a capacitance C_2 connected in parallel, as well as two sections of 50 Ω transmission lines having length *l* at both sides. This model is characterized by a higher degree of accuracy over a broader frequency band of operation, though it relies on a negative-value parameter as outlined hereinafter.

Three independent equations are needed for the synthesis of the circuit in Figure 4B. The first one is given by the resonant condition of the whole shunt branch of the equivalent T-network that reflects in the zero of the input reflection



FIGURE 6 Magnitude of the scattering parameters of the supershaped complementary split ring resonator of order m = 9 as simulated numerically, measured on a physical prototype, and evaluated by using the equivalent circuits in Figure 4

coefficient S_{11} at frequency f_1 . The second equation is related to the resonance condition of the series *LC* tank (L_1 , C_1), that corresponds to the zero of the transmission coefficient S_{21} at frequency f_2 . The third condition is derived by enforcing the 3 dB insertion loss level at frequency f_3 . In this way, one can verify that⁷:

$$C_2 = \frac{Y_0 f_2^2 - f_3^2}{\pi f_3 f_1^2 - f_3^2},\tag{8}$$

$$C_1 = \left[\left(\frac{f_1}{f_2} \right)^2 - 1 \right] C_1, \tag{9}$$

$$L_1 = \frac{1}{\left(2\pi f_2\right)^2 C_1},\tag{10}$$

where Y_0 is the characteristic admittance of the input lines. It is apparent from (10) that the C_2 is negative as $f_1 < f_3 < f_2$. Finally, the length *l* of the microstrip line sections embedded in the series branches of the equivalent circuit is determined by fitting the phase of the scattering parameters.

As it appears in Figure 4, the considered equivalent circuit networks do not account for loss mechanisms occurring in the corresponding physical structure. However, this nonideality can be easily addressed by integrating resistive elements in the resonant *LC* tanks included in both models.

3 | NUMERICAL RESULTS AND MEASUREMENTS

Following the procedure described in section 2, equivalent circuit models of the considered supershaped CSRR filters have been extracted starting from the numerical simulation data. The circuit parameters are given in Table 1 as a

TABLE 2 Transmission-zero frequency of supershaped complementary split ring resonators as a function of the relevant Gielis order m (f_z in GHz)

т	5	6	7	8	9	10
f_z (EM simulation)	1.918	1.877	1.827	1.798	1.738	1.679
f_z (measurements)	1.910	1.850	1.820	1.780	1.740	1.690

function of the Gielis order *m*. It is worth noting that, in Baena's model, the inductance L_c increases with the length of the CSRR, whereas the capacitance C_c is nearly constant with a slow variation around the average value of about 0.275 *pF*. As for Li's model, one can notice that the equivalent capacitance C_2 is negative, though that can be easily offset by using the same approach suggested in Ref. 7

Figure 5 shows the simulated and measured insertion loss versus frequency of the designed structures for different values of the order m. As it appears from Table 2, the transmission-zero frequency f_z of the considered class of CSRRs decreases, with a nearly linear progression, as m becomes larger. A good agreement between numerical and experimental results can be noticed in Figure 5 and Table 2. However, from the visual inspection of Figure 5, it is apparent that a deviation occurs in terms of simulated and measured insertion-loss bandwidth, this being attributable to a mismatch between the actual loss tangent featured by the dielectric laminate used for the manufacturing of the filter prototypes (see Figure 2B) and the nominal value adopted in the numerically based electromagnetic model of the various structures.

As an example, Figure 6 shows the frequency-domain behavior of the magnitude of the coupling coefficient $|S_{21}|$ and input reflection coefficient $|S_{11}|$ of the supershaped CSRR of order m = 9, as simulated with *CST Microwave Studio*, measured on physical prototypes, and evaluated using the equivalent circuits shown in Figure 4. The agreement between numerical and experimental results is pretty good, minor discrepancies in return loss being attributed to tolerances in the fabrication process and parasitic effects associated with the microstrip-line-connector transition which is responsible for an unwanted impedance deviation.

As for the equivalent circuits, both proposed models can predict the stop-band behavior of supershaped CSRRs with a reasonable accuracy, though Li's equivalent circuit shows a better agreement with simulated data across a broader range of frequencies, this being beneficial for a more effective design process of microwave systems by means of CAD software applications. This is however achieved at the expense of a higher complexity level associated with the integration of microstrip line sections and, possibly, a negative capacitor (see Table 1) in the network. Conversely, Baena's circuit provides a useful physical insight in terms of the equivalent intrinsic inductance and capacitance of CSRRs.

4 | CONCLUSIONS

A new class of supershaped CSRR filters has been presented, and the relevant circuital behavior studied extensively. It has been demonstrated that the transmission-zero frequency of the considered structures can be easily tuned by properly selecting their Gielis order, while keeping other characteristics nearly unchanged. Novel designs based on the periodic or

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aperiodic clustering of supershaped CSRRs are being investigated to synthesize high-performance filter structures.

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