

# Improving the efficiency of deep convolutional networks

***Citation for published version (APA):***

Peemen, M. C. J. (2017). *Improving the efficiency of deep convolutional networks*. [Phd Thesis 1 (Research TU/e / Graduation TU/e), Electrical Engineering]. Technische Universiteit Eindhoven.

***Document status and date:***

Published: 12/10/2017

***Document Version:***

Publisher's PDF, also known as Version of Record (includes final page, issue and volume numbers)

***Please check the document version of this publication:***

- A submitted manuscript is the version of the article upon submission and before peer-review. There can be important differences between the submitted version and the official published version of record. People interested in the research are advised to contact the author for the final version of the publication, or visit the DOI to the publisher's website.
- The final author version and the galley proof are versions of the publication after peer review.
- The final published version features the final layout of the paper including the volume, issue and page numbers.

[Link to publication](#)

***General rights***

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal.

If the publication is distributed under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license above, please follow below link for the End User Agreement:

[www.tue.nl/taverne](http://www.tue.nl/taverne)

***Take down policy***

If you believe that this document breaches copyright please contact us at:

[openaccess@tue.nl](mailto:openaccess@tue.nl)

providing details and we will investigate your claim.

# IMPROVING THE EFFICIENCY OF DEEP CONVOLUTIONAL NETWORKS

**PROEFSCHRIFT**

ter verkrijging van de graad van doctor  
aan de Technische Universiteit Eindhoven, op gezag van de  
rector magnificus prof.dr.ir. F.P.T Baaijens, voor een  
commissie aangewezen door het College voor  
Promoties, in het openbaar te verdedigen  
op donderdag 12 oktober 2017 om 16:00 uur

door

**Maurice Cornelis Johannes Peemen**

geboren te Rijsbergen

Dit proefschrift is goedgekeurd door de promotoren en de samenstelling van de promotiecommissie is als volgt:

voorzitter: prof.dr.ir. A.B. Smolders  
promotor: prof.dr. H. Corporaal  
copromotor: dr.ir. B. Mesman  
leden: dr. C.G.M. Snoek (University of Amsterdam)  
prof.dr. L. Benini (ETH Zürich)  
prof.dr.ir. P.H.N. de With  
prof.dr.ir. C.H. van Berkel  
adviseur: dr. O. Temam (Google Mountain View)

*Het onderzoek dat in dit proefschrift wordt beschreven is uitgevoerd in overeenstemming met de TU/e Gedragscode Wetenschapsbeoefening.*

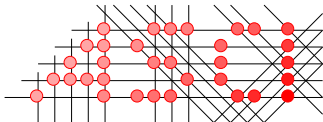
# **IMPROVING THE EFFICIENCY OF DEEP CONVOLUTIONAL NETWORKS**

**Maurice Peemen**

Doctorate committee:

prof.dr. H. Corporaal	TU Eindhoven, <i>promotor</i>
dr.ir. B. Mesman	TU Eindhoven, <i>copromotor</i>
prof.dr.ir. A.B. Smolders	TU Eindhoven, <i>chairman</i>
dr. C.G.M. Snoek	University of Amsterdam
prof.dr.ir. L. Benini	ETH Zürich
dr. O. Temam	Google Mountain View
prof.dr.ir C.H. van Berkel	TU Eindhoven
prof.dr.ir. P.H.N. de With	TU Eindhoven

This work was supported by the Ministry of Economic Affairs of the Netherlands as part of the EVA project PID-07121.



Advanced School for Computing and Imaging

This work was carried out in the ASCI graduate school.  
ASCI dissertation series number 375

© Maurice Peemen 2017. All rights are reserved. Reproduction in whole or in part is prohibited without the written consent of the copyright owner.

Computer chip cover image is illustrative/courtesy of wall.alphacoders.com

Printed by Ipskamp printing – The Netherlands

A catalogue record is available from the Eindhoven University of Technology Library. ISBN: 978-90-386-4361-8

# SUMMARY

## IMPROVING THE EFFICIENCY OF DEEP CONVOLUTIONAL NETWORKS

Throughout the past decade, *Deep Learning* and *Convolutional Networks* (ConvNets) have dramatically improved the state-of-the-art in object detection, speech recognition, and many other pattern recognition domains. These breakthroughs are achieved by stacking simple modules that for each network-level transform the input into a more abstract representation (e.g. from pixels to edges, to corners, and to faces). These modules are trained to amplify aspects that are important for the classification, and suppress irrelevant variations.

The recent success of these deep learning models motivates researchers to further improve their accuracy by increasing model size and depth. Consequently the computational and data transfer workloads have grown tremendously. For beating accuracy records using huge compute clusters this is not yet a big issue; e.g. the introduction of GP-GPU computing improved the raw compute power of these server systems tremendously. However, for consumer applications in the mobile or wearable domain these impressive ConvNets are not used. Their execution requires far too much compute power and energy. For example, running a relatively shallow ConvNet for Speed Sign detection on a popular embedded platform (containing an ARM Cortex-A9) results in a HD frame rate of 0.43 fps; this is far below acceptable performance. The introduction of a multi-core increases performance, however in the optimistic scenario of linear scaling 47 cores are required to achieve 20 fps. The power consumption of this ARM core is almost 1 Watt; for 20 fps this scales to 47 Watt, which would deplete your battery in minutes, even worse are the thermal effects that are comparable to those of a hot light bulb.

To address above issues, this thesis investigates methodologies that substantially improve the energy-efficiency of deep convolutional networks. First a high-level algorithm modification is proposed that significantly reduces the computational burden while maintaining the superior accuracy of the algorithm. This technique combines the large workload of *Convolutional* and *Subsample* layers

into more efficient *Feature Extraction* layers. Real benchmarks show a 65-83% computational reduction, without reducing accuracy.

Second, this thesis addresses the huge data transfer requirements by advanced code transformations. *Inter-tile* reuse optimization is proposed to reduce external data movement up to 52% compared to the best case using traditional tiling.

Third, to further improve the energy efficiency of the embedded compute platform this thesis proposes the *Neuro Vector Engine* (NVE) template; a new ultra-low power accelerator framework for ConvNets. Comparison of an NVE instantiation versus an SIMD optimized ARM Cortex-A9 shows a performance increase of 20 times, but more importantly is the energy reduction of 100 times.

Finally, this thesis addresses the programming efficiency of dedicated accelerators. We present *CONVE* an *optimizing VLIW compiler* that makes the NVE the first ConvNet accelerator with full VLIW compiler support. In several cases this compiler beats the manual expert programmer. The above contributions of this thesis significantly improve the efficiency and programmability of deep Convolutional Networks; it thereby enables their applicability to the mobile and wearable use cases.

# CONTENTS

<b>1. Introduction</b>	<b>1</b>
1.1 Neural networks for classification .....	3
1.1.1 Modeling a neuron.....	3
1.1.2 Pattern classification .....	6
1.1.3 Multilayer perceptron's .....	7
1.1.4 Generalization issues .....	9
1.2 Deep networks for computer vision .....	10
1.2.1 Building prior information in neural net architectures .....	11
1.2.2 Feature hierarchies .....	13
1.3 Trends in deep neural network development .....	14
1.3.1 Model capacity .....	15
1.3.2 Computational work.....	17
1.3.3 Memory transfers .....	21
1.3.4 Platform programmability .....	23
1.4 Problem statement .....	24
1.5 Contributions.....	25
1.6 Thesis outline.....	26
<b>2. Deep Convolutional Networks</b>	<b>27</b>
2.1 Introduction.....	27
2.2 Challenges of visual data processing.....	28
2.3 Parameter sharing .....	30
2.3.1 Convolution layers .....	32
2.3.2 Pooling layers .....	33
2.3.3 Neuron layers .....	34
2.3.4 Normalization layers .....	34
2.4 Constructing a convolutional network .....	35
2.4.1 Coding neuron layers.....	36
2.5 Deeper networks .....	37
2.6 Conclusions.....	38
<b>3. Benchmark Applications</b>	<b>40</b>
3.1 Introduction.....	40
3.2 Object detection with a convolutional net .....	41



3.2.1	Patch classification .....	42
3.2.2	Frame based detection .....	43
3.3	Dataset construction.....	45
3.4	Training a convolutional net for machine vision.....	46
3.4.1	Preprocessing of training data.....	47
3.4.2	Training loop and recipe .....	47
3.4.3	Network design .....	48
3.4.4	Iterative bootstrapping.....	50
3.5	Throughput evaluation.....	51
3.6	Related work .....	53
3.6.1	Region based convolutional networks.....	53
3.6.2	Single shot detectors.....	54
3.7	Conclusions and discussion .....	55
<b>4.</b>	<b>Algorithmic Optimizations</b> .....	<b>57</b>
4.1	Introduction.....	57
4.2	Feature extraction layers .....	58
4.2.1	Convolution layers .....	59
4.2.2	Pooling layers .....	59
4.3	Algorithm optimization.....	60
4.3.1	Merge convolution and pooling .....	60
4.3.2	Training with error back-propagation.....	62
4.4	Evaluate recognition performance .....	65
4.5	Experimental mapping .....	66
4.6	Related work .....	68
4.7	Conclusion .....	69
<b>5.</b>	<b>Inter-Tile Reuse Optimization</b> .....	<b>71</b>
5.1	Introduction.....	71
5.2	Related work .....	74
5.3	Motivation: scheduling for data locality .....	75
5.4	Modelling the scheduling space .....	76
5.4.1	Modelling intra-tile reuse .....	77
5.4.2	Adding inter-tile reuse to the model .....	77
5.5	Scheduling space exploration .....	80
5.6	Implementation demonstrator .....	82
5.7	Evaluation methodology.....	84
5.7.1	Benchmark applications.....	84
5.7.2	Platform and tools .....	86
5.8	Experimental results .....	86
5.8.1	Data transfer volume for inter-tile schedules .....	86
5.8.2	Quality of results.....	88
5.8.3	Energy consumption.....	91
5.9	Conclusions.....	93

<b>6. NVE: a Flexible Accelerator</b>	<b>94</b>
6.1 Introduction.....	94
6.2 Related work .....	96
6.3 Sources of inefficiency in general purpose CPUs.....	99
6.4 The Neuro Vector Engine (NVE) architecture .....	101
6.4.1 Vector data path.....	101
6.4.2 Memory system .....	103
6.4.3 Control and programming .....	105
6.5 Experimental evaluation.....	106
6.5.1 Benchmark setup .....	107
6.5.2 Accelerator characteristics.....	108
6.5.3 Comparison against other ASIC accelerators.....	111
6.6 NVE instantiation and customization.....	112
6.6.1 Limitations and future directions .....	115
6.7 Conclusions.....	116
<b>7. Accelerator Code Generation</b>	<b>117</b>
7.1 Introduction.....	117
7.2 Background and related work.....	119
7.3 ConvNets in a domain specific language .....	121
7.4 Automatic code generation flow.....	122
7.4.1 Task graph construction.....	123
7.4.2 Instruction scheduling .....	125
7.4.3 Scratchpad memory allocation.....	129
7.4.4 Generalization towards VLIW architecture .....	130
7.5 Advanced code optimizations.....	131
7.5.1 Coefficient layout optimizations .....	131
7.5.2 Modulo scheduling .....	131
7.5.3 Feature map combining .....	132
7.6 Experimental evaluation.....	134
7.6.1 Experimental setup .....	134
7.6.2 Performance metrics.....	135
7.6.3 Performance analysis.....	135
7.7 Conclusions.....	137
<b>8. Conclusions and Future Work</b>	<b>139</b>
8.1 Conclusions.....	139
8.2 Future work.....	141
Refereed papers covered in this thesis .....	156
Other (co-)authored papers .....	157
<b>Acknowledgements</b>	<b>158</b>
<b>About the author</b>	<b>160</b>



# INTRODUCTION

Nowadays digital technology is interwoven into many aspects of our daily lives. For example, think of the omnipresence of personal devices such as smartphones, tablet computers, digital cameras, and televisions that guide our decisions and instantly connect us to the internet. From another perspective estimate your daily usage of services such as e-mail, online encyclopedias, on-line shopping, and digital music. More and more we are accessing services through our smartphones; this is reflected by the number of mobile smartphone subscriptions that globally grew by 18% in 2016 to reach 3.9 billion<sup>1</sup>. This trend will extend from *smartphone* to *smart devices*, a class of wearable companion devices that integrates digital services deeply into our daily life. Figure 1.1 depicts a few examples devices such as, smartwatches, smart glasses [140], and in the extreme a smart ring.

The new challenge is to make these so called “smart devices” really smart. Checking e-mail or posting photos on social media are just the first features. The real smart features use integrated sensors like cameras to identify objects in images. Or with a microphone instead of a camera that directly transcribes speech into text. Such features are already successfully used in data-centers (providing *cloud* services for Google and Facebook) to handle image search queries. Currently, these tasks are solved by *Machine Learning* techniques that extract and recognize patterns from huge loads of raw data. Increasingly, these recognition applications make use of a class of techniques called *Deep Learning*.

Probably you have heard or read about deep learning; it is a lot in the news since big companies like Google, Facebook, and Microsoft are acquiring startups with expertise in this field. In the last few years, deep learning made major advances e.g., it has beaten many records in image recognition [79,30,49], and speech recognition [66,127]. Most striking is the fact that in some cases these techniques achieved *superhuman* (better than human) accuracy in solving difficult pattern recognition problems [30,25]. A well know example is the deep

---

<sup>1</sup> Source: *Ericsson Mobility Report Nov 2016*.



**Figure 1.1:** Examples of wearable companion devices: (left) “I’m Watch” the smartwatch that displays email and SMS services of Android devices. (center) “Google Glass” an optical head-mounted display that is worn as a pair of eyeglasses. (right) “MOTA” smartRing links up to your smartphone and notifies you of incoming texts, emails and social alerts.

learning based program named AlphaGo that has recently beaten the best human players at the board game Go [136]. These breakthroughs are achieved by improvements in the learning algorithms that enabled researchers to increase classification model size (more parameters). Consequently they successfully exploit the availability of more example training data, which improves the accuracy and robustness. This search for models that improve upon the state-of-the-art has increased model complexity tremendously.

For deep learning the classification models are often based upon Artificial Neural Networks (ANNs). These networks contain simple decision nodes, so called neurons that are organized in layers [61]. The early ANNs till the 1980s had very shallow architectures, one or two layers of neurons [123,130]. However, today's competition winning deep learners have 20 to 152 layers of neurons [142,62]. To push the accuracy further researchers even use ensembles of models, each specialized at an aspect of the classification problem [138]. Combined these ensembles can boost the final accuracy at the cost of an increased model complexity.

A negative side effect of the large model complexity is a huge amount of computational work required to perform a recognition task. This workload involves many computational operations like multiplications and additions to compute the classification result. In addition, a huge amount of data movement is required to feed the inputs of these computational operations e.g. the parameters or coefficients of the model, the input images and many intermediate representations. The commonality between computations and data movement is that both operations consume energy. Applications that require a lot of those operations in a short period of time, e.g. to classify object in a real-time video stream, are power hungry. This is one of the key reasons that deep learning solutions run often as a cloud service in the data-centers, where massive compute performance is available.

Mobile devices like our tablets, smartphones, and “always on” wearable companions are designed to be energy-efficient. We expect a battery lifetime that spans one or even several days. To achieve such battery lifetimes the available resources of the embedded compute platform are heavily constrained. Developing applications that use the new possibilities of deep learning on your mobile device is not straightforward. However, the rich collection of integrated sensors

in mobile and wearable devices make them the best target for state-of-the-art classifier applications. To bridge the compute energy gap between deep learning algorithm requirements and the capabilities of modern embedded platforms the energy efficiency must be improved. The goal of this thesis is therefore to substantially improve the efficiency of *deep convolutional networks*. These convolutional nets are specialized in visual data processing and recently very popular in machine learning. This chapter will introduce Neural networks (Section 1.1), and explain their evolution into Deep Convolutional Networks (Section 1.2). Next, the trends in Deep Learning research are outlined (Section 1.3), and the problem statement is discussed in detail (Section 1.4). Finally, the main contributions and chapter outline are presented in Section 1.5 and Section 1.6 respectively.

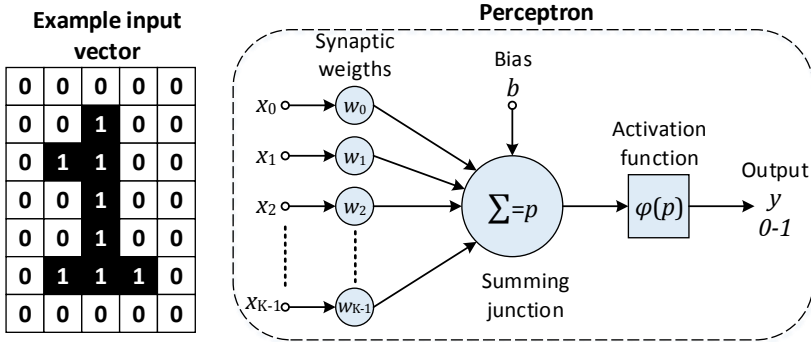
## 1.1 Neural networks for classification

Most work on *artificial neural networks* has been motivated by the observation that the human brain computes in an entirely different way than digital computers do. Instead of performing complex tasks sequentially, the brain solves complex problems in a *distributed* and *highly parallel* approach with simple unreliable operations performed by units known as *neurons*. Although its processing is very different the brain is very successful, and reliable in processing complex tasks. Consider for example *vision*, the brain can process the visual information of the environment around us in a split second. It extracts the context of a scene, warns you for threatening situations, and directly remembers the faces of the people involved. This task requires distinguishing foreground from background, recognizing objects presented in a wide range of orientations, and accurately interpreting spatial cues. The human brain performs such tasks with great ease and compared to modern compute platforms it requires a very modest power budget.

This section will introduce the basic processing elements of neural networks, their interconnections, and their ability to classify patterns. These aspects are addressed without focusing on their capability to learn by adapting their parameters. Training is one of the key features of neural nets, which will be further discussed in Chapter 3 and 4.

### 1.1.1 Modeling a neuron

The fundamental processing elements in neural networks are their *neurons*. The block diagram in Figure 1.2 illustrates the model of a neuron. It forms the basic element for a large family of neural networks that is studied in the further chapters of this thesis. A simple form of this model is already developed in 1943 by the pioneering work of *McCulloch* and *Pitts* [94]. There are basically three elements in this neuron model:



**Figure 1.2:** A basic nonlinear model of a neuron with an example input pattern.

1. A set of connecting input links  $x_j$  or *synapses*, each characterized by a *weight* or *strength*  $w_j$ . The weights model the *synaptic efficiency* of biological connections, unlike the synapses in the human brain the weights of an artificial neuron cover a range that includes negative as well as positive values.
2. A *summing junction* or *adder* for summing the input signals, weighted by the respective synaptic strengths.
3. An *activation function* for limiting the range of the output signal to some finite value. In addition, this function can add non-linear behavior to neural networks.

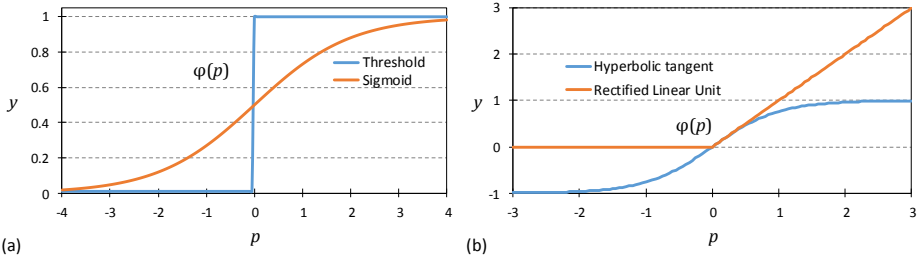
The artificial neuron of Figure 1.2 also includes a *bias* value, denoted by  $b$ . Depending on whether the bias is positive or negative it can increase or lower the net input of the *activation function*. The neuron model can be mathematically described by using a simple pair of equations:

$$p_i = b_i + \sum_{j=0}^{K-1} w_{ij} x_j \quad (1.1)$$

$$y_i = \varphi(p_i) \quad (1.2)$$

The neuron potential  $p_i$  is computed by the weighted sum of the inputs  $x_j$ ;  $w_{i0}$ ,  $w_{i1}$ , ...,  $w_{iK-1}$ , are the respective synaptic weights of neuron  $i$ . The *activation potential* has an external offset bias  $b_i$ . Note that the bias also could be encoded as one of the weights, e.g.  $w_{i0} = b_i$ , and  $x_0 = 1$ . The activation function  $\varphi()$  transforms the neuron potential into an output value. Different activation functions are discussed below.

Assume that the artificial neuron model is used as digit detector e.g., for the number one as displayed on the left side of Figure 1.2. In this scenario the potential should be high if the number one is applied, for all other patterns it should be low. This is achieved when inputs connected to black pixels have positive weights (*excitatory inputs*) and other positions negative weights (*inhibitory inputs*). This ensures that for digits with a significant amount of overlap, e.g. the



**Figure 1.3:** Different neuron activation functions  $\varphi(p)$ : (a) Threshold or Heaviside function as used in the *McCulloch-Pitts model*; Sigmoid or Logistic function as used in the *Perceptron model*; (b) Hyperbolic tangent function, which belongs to the family of Sigmoid functions although it spans from -1 to 1; Rectified Linear Unit (ReLU) or ramp function that recently gained a lot of interest in the field of deep learning.

number two, the inhibitory inputs mitigate the overlapping positions resulting in a reduced potential.

### Types of activation functions

The activation function  $\varphi(p)$  defines the output of a neuron in function of the neuron potential  $p$ . At least three different types of activation functions can be defined:

1. *Threshold*. This function results in the value 1 if the neuron potential is non-negative, and 0 otherwise. Figure 1.3(a) displays the *all or nothing* behavior of the threshold function. It is the activation function of the *McCulloch-Pitts model* [94]. Mathematically defined as:

$$\varphi(p) = \begin{cases} 0, & p < 0 \\ 1, & p \geq 0 \end{cases} \quad (1.3)$$

2. *Sigmoid*. This function is defined as a strictly increasing function that combines linear and non-linear saturating behavior. A very popular sigmoid is the *logistic function* illustrated in Figure 1.3(a). It represents the activation rate of a neuron which assumes a continuous value between 0 and 1. Mathematically the logistic function is defined as:

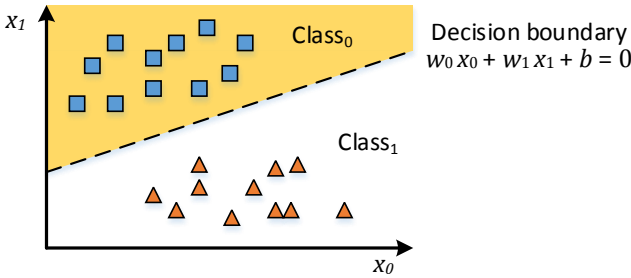
$$\varphi(p) = \frac{1}{1 + \exp(-p)} \quad (1.4)$$

Sometimes it is desirable to extend the range of the activation function from -1 to +1. In this case the *hyperbolic tangent function* is often used, as depicted in Figure 1.3(b) and defined by:

$$\varphi(p) = \tanh(p) = \frac{2}{1 + \exp(-p)} - 1 \quad (1.5)$$

Apart from vertical scaling and offset, these functions are exactly the same. Note that sigmoid functions are differentiable, which is important for training.





**Figure 1.4:** Illustration of a two-class, two-dimensional pattern-classification problem. In this example a pair of linearly separable patterns (a straight line can decide).

3. *Rectifier*. A neuron model that employs a rectifier function is also called a *Rectified Linear Unit* (ReLU). This function is, as of 2015 the most popular activation function for deep neural networks, it performs very well for deeper networks [79]. Figure 1.3(b) shows the ReLU activation function that is defined as:

$$\varphi(p) = \max(0, p) \quad (1.6)$$

A ReLU is not fully differentiable,  $p$  below and on 0 have slope 0, above gives 1.

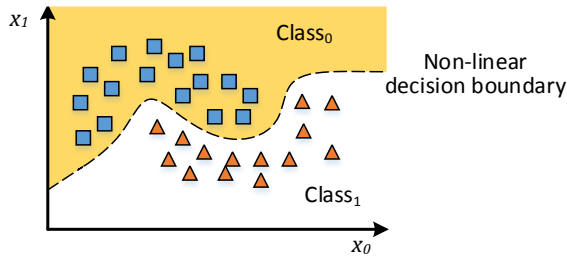
### 1.1.2 Pattern classification

Often a neural network is used to classify patterns. More specifically a single neuron classifies the set of stimuli  $x_0, x_1, \dots, x_{K-1}$ , into one of two classes. To develop some insight into the behavior of a pattern classifier let us reduce the input dimensionality is reduced to  $x_0$  and  $x_1$ , as illustrated in Figure 1.4. A simple classifier such as the *Perceptron model* introduced by Rosenblatt in 1958 [123] could solve these problems. A perceptron is basically a neuron based on the McCulloch-Pitts [94] model, but with a learning algorithm. The perceptron has two decision regions separated by a *hyperplane*, which is defined by:

$$b + \sum_{j=0}^{K-1} w_j x_j = 0 \quad (1.7)$$

The *decision boundary* is illustrated in Figure 1.4 as a straight line. Each point  $(x_0, x_1)$  lying above the decision line is assigned to Class<sub>0</sub>, and each point below the boundary is assigned to Class<sub>1</sub>. The coefficients of a perceptron can be updated according to an error-correction rule. Updates are repetitively performed in so called training iterations to find a good intersection, i.e. the squares are separated from the triangles.

A perceptron can find a good intersection of the two classes when these are *linearly separable*. This means that pattern groups to be classified are sufficiently separated such that a linear line can decide correctly. However, if pattern groups move close to each other the problem becomes *non-linearly separable*, as depicted in Figure 1.5. Classification problems that are not linearly separable are



**Figure 1.5:** Illustration of a two-dimensional pair of non-linearly separable patterns.

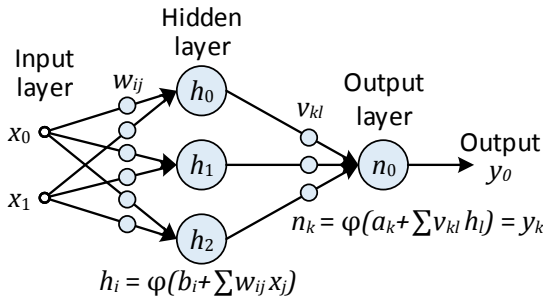
beyond the capability of a single neuron or perceptron. This is a severe limitation of the perceptron model that prevents it from making more complex classifications; e.g., it cannot even solve a binary parity problem like a simple XOR function. This made that artificial neurons fell in despair from the 1960s till the mid-1980s.

In finalizing the introduction of artificial neurons or the perceptron we conclude that the model is an elegant approach to classify linearly separable patterns. However for more complicated patterns like non-linearly separable ones this model is too restricted. Although these limitations perceptron's have proven to be very useful for the development of machine learning. In fact they are nowadays still used as internal building block for the successful deep learning techniques. The next section will show how to extend the learning and classification capabilities of perceptron's.

### 1.1.3 Multilayer perceptron's

To be able to classify more difficult not linearly separable problems a two-step approach is required. Firstly, the input signals should be transformed into a new *representation* into so called *features*. This new representation should separate the classes further apart from each other, which makes it easier to separate the classes. Secondly, a new classifier should use the new representation as input to solve the classification problem. An analogy of this two-step approach is to compare it to how you read a sentence. You do not care about each individual character. Firstly, these characters are classified into words. Secondly, you parse the words into a sentence with his own meaning. If you would lose the ability to recognize words, it would become much more difficult to understand the content of a sentence.

Learning representations is exactly what a *multilayer perceptron* performs. As depicted in Figure 1.6, the multilayer network has a *hidden layer* (neuron  $h_0$ ,  $h_1$ ,  $h_2$ ) between input and output. The hidden neurons act as feature detectors; they perform a non-linear transformation on the inputs. During the learning process these hidden neurons discover the features that characterize the training data. The formation of this extra feature space distinguishes the multilayer perceptron from a single perceptron. The illustrated multilayer perceptron in Figure 1.6 reveals that the network is a directed graph, where each layer is *fully connected* to



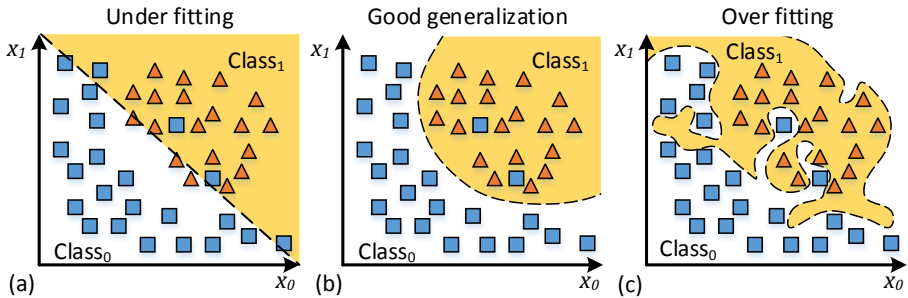
**Figure 1.6:** Architectural graph of a multilayer perceptron with one hidden layer.

the next layer. We can generalize the network description beyond two layers towards any network depth. Therefore the equations in Figure 1.6 change into the more general equation (1.8). The neurons in layer  $y_i^{(l)}$  have a weight matrix  $w_{ij}^{(l)}$  that fully connects them to all neurons (or inputs) of a preceding layer  $y_j^{(l-1)}$ . This is mathematically described as:

$$y_i^{(l)} = \varphi \left( b_i^l + \sum_j w_{ij}^{(l)} y_j^{(l-1)} \right) \quad (1.8)$$

If a neuron is in the first hidden layer (i.e.,  $y_i^{(1)}$ ) the inputs are  $y_j^{(0)} = x_j$ . Note that the operations between layers can be written as matrix vector multiplications, followed by a non-linearity. Without non-linearity we keep only the remaining weighted sum operation, which is linear. Due to the associative property the layers can be collapsed into a single layer. With simple linear algebra any number of layers can be reduced to a single perceptron layer. It is the non-linear activation function that prevents this merge and opens the extra feature space.

The multilayer approach usually substantially increase the number of model parameters. Each layer has a weight matrix that fully connects input and output, which is much larger compared to the perceptron model. For example, perceptron models have around 10 to 400 free parameters. However, the famous *NETtalk* multilayer perceptron (1987) for English speech to phonemes translation had 18,629 model parameters [130]. *NETtalk* has 203 inputs, 80 hidden neurons and 23 output neurons. The number of neurons is not that large, but full-connectivity between layers makes that there are many model parameters. We can conclude that the introduction of multi-layer perceptron's increased the number of free model parameters substantially. As a result, the learning and classification capabilities are improved considerably.



**Figure 1.7:** Examples of classifier decision spaces and generalization: (a) Under fitting, a linear classifier cannot distinguish the two classes correctly, it has not enough parameters; (b) A small multilayer perceptron. Not all training samples are classified correctly. However, it shows good generalization, most new samples are expected to be classified correctly; (c) Over fitting, classifier is too complex. It fits “noise” in the training data. All training samples are classified correctly, but new samples will probably introduce errors.

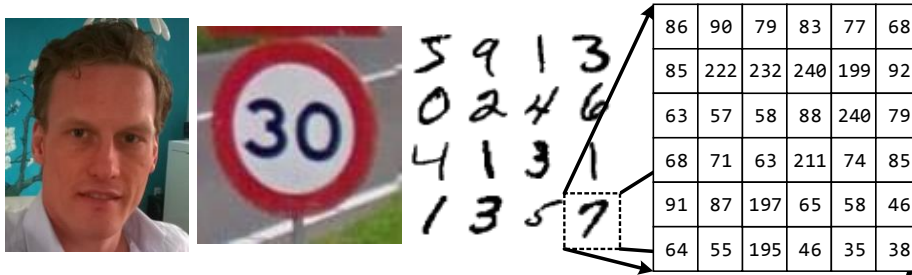
### 1.1.4 Generalization issues

One of the key properties of (multilayer) perceptron’s is the ability to train them with a labelled dataset. This is called *Supervised Learning* or learning with a teacher. It requires a set of input examples with corresponding output labels. The learning algorithm iterates over these samples and corrects the errors on the outputs by adjusting the weights in the network. An efficient algorithm for training is *error-backpropagation*. It adjusts the weights by using the gradient information of errors. Computing the error gradients is done efficiently by propagating back the errors through the networks. Chapter 2 presents more details regarding this learning process.

Since the mid-1980s the back-propagation algorithm caused revived interest into artificial neural networks [125]. Many researchers were using neural networks for pattern classification problems; non-linearly separable problems seemed no problem for multilayer perceptron’s. They used many training examples and hoped that the designed neural net would *generalize* well. A network generalizes well if the input-output mapping is correct or nearly correct for test data that is not used for training the network. Generalization represents how the network would perform in a real-world environment where it is continually exposed to new data.

A neural network that is designed to generalize well will produce a correct input-output mapping even when input samples are slightly different from the ones used for training. Generalization is mainly influenced by three factors:

1. The size of the training set and how representative it is for the problem.
2. The architecture of the neural network, or training method (regularization methods can reduce overfitting).
3. The complexity of the problem at hand.



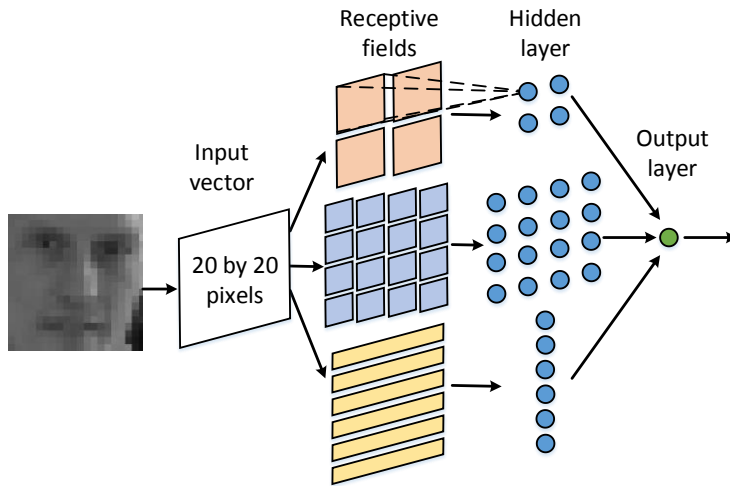
**Figure 1.8:** Examples of visual object recognition tasks: Detecting a familiar face; reading a speed sign; Interpret hand written characters. Easy tasks for humans, however for a computer it is an array of pixel values. It results in a high-dimensional input vector. Would you recognize the number 7 in the example matrix on the right hand side?

Figure 1.7 illustrates how these three aspects influence generalization. *Under fitting* is depicted in Figure 1.7(a), the classifier is too simplistic (too rigid), it cannot capture salient patterns in the data. Although it makes errors on the training data, for the common case it will not perform much worse on new test data. The distribution of triangles suggest that new triangles probably will appear in the top right (yellow) part of the decision space. Although the model suffers from under fitting, we conclude that it generalizes reasonably. Figure 1.7(b) illustrates a classifier that has a good fit on the data. Not all samples in the training set are classified correctly, but it is likely that the two errors are outliers that will not appear again. *Over fitting* is demonstrated in Figure 1.7(c), the classifier is too complex (too flexible). It clearly fits on the “noise” in the training data. All training patterns are classified correctly, but this includes patterns that will not reappear. If this complex classifier is used in a real-world environment with new samples it will probably make many errors.

Especially for *shallow* networks with many parameters, it is difficult obtain a good generalization. So called shallow networks have one or few, but large hidden layers. To find single transformations of the inputs into classifications by using many parameters is difficult. With less parameters the network is forced to make abstractions of the problem, which often helps generalization. The generalization issues show that more difficult problems are not automatically solved by increasing the number of neurons in the hidden layer. Simply increasing the number of neurons (adding model complexity) is not directly the solution to solve more difficult problems.

## 1.2 Deep networks for computer vision

One of the more complex pattern classification problems is visual object recognition. Tasks that humans solve relatively simply can be very challenging for algorithms. Think of detecting a familiar face, reading road signs, or interpretation of hand written characters. Figure 1.8, illustrates that such images are constructed by pixels with a corresponding intensity value. In a digital system these

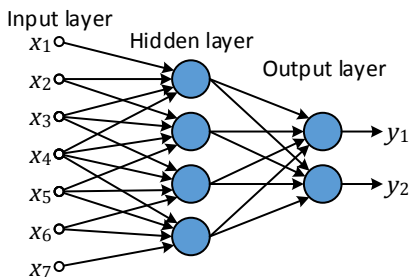


**Figure 1.9:** Example of Rowley's constrained multilayer perceptron. *Prior knowledge* is embedded in the network e.g., receptive fields specialized at detecting eyes, or mouth shapes. Weight freedom is limited to enforce important features and prevent overfitting.

images are arrays of pixel intensity values. It is quite hard for us humans to extract the number 7 from the array by only looking at the numeric values in the array. Especially if you take into account that all pixel values will change when external light conditions alter. This subsection briefly discuss the techniques used to improve neural net architectures to perform well on visual data. Enforcing architecture constraints as shown in Section 1.2.1 is a successful technique to improve generalization for image recognition tasks. These architectural constraints resulted in networks that stack feature hierarchies, see 1.2.2. It is the basis of the successful *Convolutional Networks* (ConvNets). More information on this topic will be given in Chapter 2.

### 1.2.1 Building prior information in neural net architectures

When a neural network is used as face detector it should learn to separate a face from background. E.g., an input patch of 20x20 pixels can be used as input (input retina), which should be classified as face or background. The high dimensionality of the input vector (400 input values) makes it very challenging to train a multilayer perceptron correctly with a good generalization. A very successful approach to cope with the difficulties of high dimensional input data is: Incorporate *prior knowledge* about the problem into the model parameters. This reduces the flexibility of the classifier (prevent over fitting). In addition, it forces the remaining parameters to learn only useful correlations in the training data.



**Figure 1.10:** Illustration of weight sharing combined with receptive fields. All four hidden neurons share the same set of weights for their four synaptic inputs.

## Receptive fields

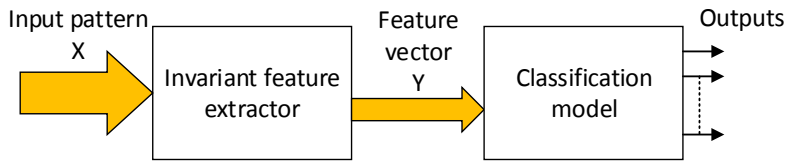
Figure 1.9 depicts a good example of a network architecture that reduces connectivity and incorporates prior knowledge for face detection [124]. Instead of fully connecting the high dimensional input to all neurons in the hidden layer; the hidden layer has three types of specialized *receptive fields*. Receptive fields are input regions that are connected to a neuron, e.g. the red  $10 \times 10$  input boxes in Figure 1.9 show a limitation on the connected inputs. Each of these types is chosen to enforce hidden neurons to detect local features that are important for face detection. In particular, square shaped receptive fields might detect features such as individual eyes, the nose, or corners of the mouth. Stripe shaped receptive fields can detect mouths or a pair of eyes. The constrained network architecture reduces the number of free model parameters to 1,453 compared to 10,427 for a fully connected hidden layer. At the time of introduction (1998) this constrained network architecture significantly improved upon the state-of-the-art for face detection.

## Weight sharing

A second additional measure that is used to build prior information into neural networks is *weight-sharing*. Weight sharing constrains the parameter freedom by enforcing the same weights for multiple neurons. This is better demonstrated by the partially connected network depicted in Figure 1.10. The top four inputs belong to the receptive field of hidden neuron 1, and so on for the other hidden neurons in the network. To satisfy the weight-sharing constraint, the same set of synaptic weights is used for each neuron in the hidden layer of the network. The potential of neuron  $i$  is mathematically expressed as:

$$p_i = b + \sum_{k=0}^{K-1} x_{i+k} w_k \quad (1.9)$$

The weights  $w_k$  are used on shifted input positions similar to a *convolutional sum*. Compared to receptive fields, weight sharing reduces the number of free



**Figure 1.11:** Block diagram of a classical two step object recognition system.

parameters even further. The hidden layer is forced to learn only the most important local features. An additional side effect of sharing with a convolutional sum is *translation/position invariance*. The concept of weight sharing with receptive fields can be easily extended to 2d input images. Especially for vision tasks position invariance of features can be important. Think of edge detection algorithms, it does not matter where the edges occur to classify them as edges. Local position invariant features like edges are important clues for the classification of an object. In ConvNets a combination of both reducing connectivity/receptive fields and weight sharing is used. Chapter 2 will elaborate more on this topic and give a detailed motivation why local features are important for vision tasks.

### 1.2.2 Feature hierarchies

One of the problems with two layer perceptron networks is that the hidden neurons interact with each other globally. For complicated problems this interaction makes it difficult to improve the classifier for certain input patterns without worsening it for others. With multiple hidden layers, the process of learning the best features becomes more manageable. Classical model based image recognition pipelines apply the same partition of classification into several stacked steps. These models separate a recognition task into *feature extraction* and *classification*, as illustrated by Figure 1.11.

1. *Feature extraction* can involve multiple successive steps such as pre-processing and extraction of features. This step makes it easier to classify the data, and increases the likelihood of correct classification by removal of irrelevant variations. For example, illumination normalization, and translating to edges or gradients which are not much affected by the illumination. Examples of advanced model based feature extractors are: SIFT [91]; SURF [4]; and HOG [38].

2. *Classification* is performed on the feature vector that is carefully designed to reduce the amount of data, and amplify only important aspects of the recognition task. The classification task can be performed by a simple classifier model, e.g., a Perceptron, k-Nearest Neighbour (k-NN), or a Support Vector Machine (SVM).

The very successful idea of solving classification problems in a hierarchical approach is also applied to neural networks. These can also exploit the property that many signals in nature are composed of hierarchies, in which higher-level features are obtained by composing lower-level ones. In images, local combinations of edges form motifs that are arranged into parts, and parts form objects.



In speech and text similar hierarchies can be observed: from sounds to phones, phonemes, syllables, words and sentences. These hierarchical part-whole relationships apply to almost every object recognition task.

Section 1.2.1 shows how *prior information* is embedded into a network architecture. By stacking layers crafted to detect features from the corresponding hierarchical level, one obtains a classifier that is much easier to train, and has greatly improved generalization properties. Each hidden layer can perform a non-linear transformation of the previous layer, so a *deep network* (multiple hidden layers) can compute more complex features of the input. In the case of vision tasks deeper networks learn part-whole decompositions as described above. For instance, the first layer groups pixels together to detect edges. A second layer might group together the edges to detect longer contours. Even deeper layers can group together these contours and detect parts of objects. Learning such deep feature hierarchies by training many stacked layers is what the term *Deep Learning* refers to.

### 1.3 Trends in deep neural network development

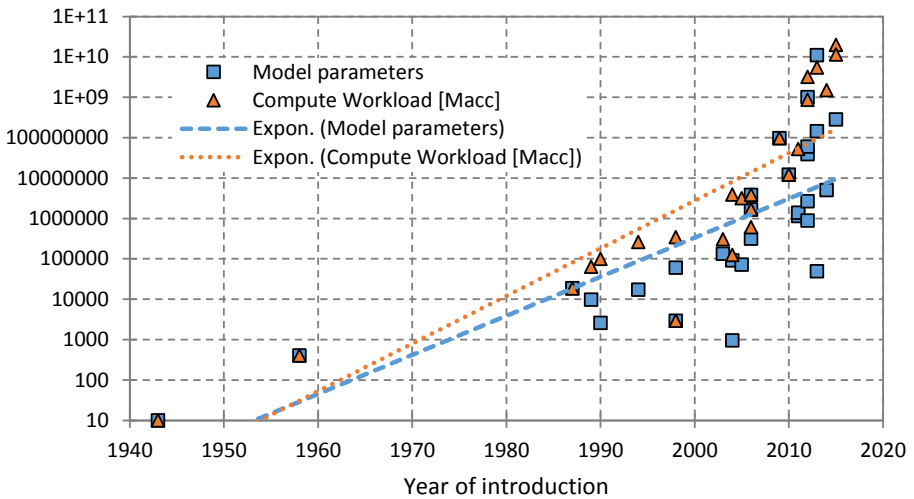
The depth increase of classifiers by stacking many layers is a key differentiator from the earlier shallow models. It resulted in remarkable improvements in classifier accuracy. For example, new deep networks are breaking records in image recognition [79,30,49], and speech recognition [66,127]. In addition, they are very successful in other domains e.g. drug discovery, as demonstrated by the winning entry in the Kaggle<sup>2</sup> competition to predict useful drug candidates for pharma company Merck [93]. Nowadays on many tasks deep networks achieve near-human accuracy levels e.g., Face detection [143]. In extreme cases these deep nets deliver superhuman accuracy, as demonstrated by [25,63].

The recently introduced machine learning models that challenge human accuracy levels have a long history. From the simple models of the 1940s they evolved into the powerful classifiers of today. This evolution is not only reflected by their accuracy scores or the difficulty of the problems they solve. The detection scores are a result of many model parameters and huge amounts of training data used to tune these parameters. This section takes a closer look at the historical trends in deep neural network development. Throughout this section, a set of 30 popular neural network publications is used as historical data<sup>3</sup>, each representative for the state-of-the-art at their year of publication.

---

<sup>2</sup> The Merck Molecular Activity Challenge on [www.kaggle.com](http://www.kaggle.com)

<sup>3</sup> Neural network articles used for trend analysis: [13,24-31,51,59,63,64,74,77-82,88,111,112,114,115,121,122,127,128,132]



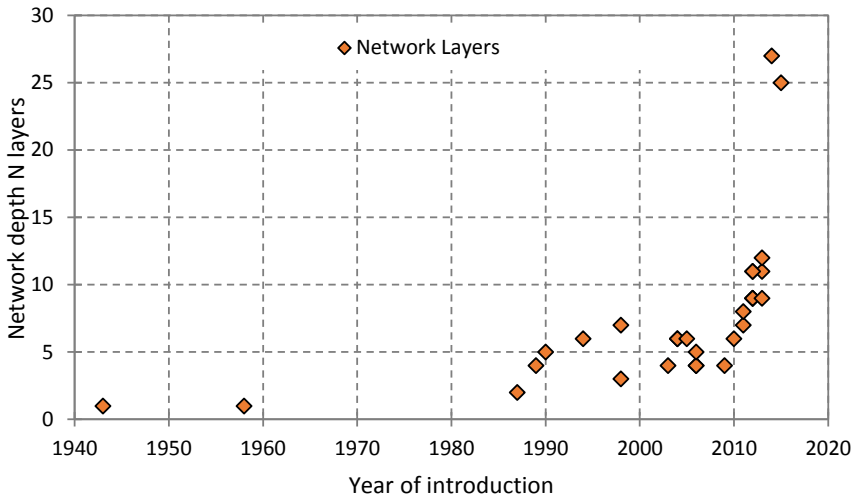
**Figure 1.12:** Historical data on 30 neural networks<sup>3</sup> showing the explosive scaling for the number of model parameters, and involved computational workload. Multiply Accumulate (Macc) are the used measure for computational workload.

### 1.3.1 Model capacity

In Figure 1.12, the model size of classifier networks published during the last 70 years is illustrated. Model size is given as the number of trainable model parameters, i.e. the number of weights. In addition, the computational workload defined as the number of Multiply Accumulate operations required for a single classification is plotted. This data shows an important observation:

Both model size and computational workload have grown immensely over time, especially since 2008 there was an acceleration of the already impressive growth rate. The model growth is reflected by an increasing complexity of the classification tasks solved by neural networks. The old perceptron's of the 1950s learned linearly separable patterns like simple lines and planes [123]. However competition winners of today's ImageNet summarize the content of a million images, they recognize 1000 different classes of complex objects such as hammers, or bikes, ants, etcetera [126]. The huge complexity of these tasks is represented by the data set size, which has grown tremendously. To absorb this enormous amount of training data the number of model parameters in neural networks exploded. The dotted exponential trend lines in Figure 1.12 reveal the immense growth of model parameters and computational work. Let's have a closer look at the breakthroughs that enabled the exponential growth rate in model capacity.

The first single layer networks of the 1940s to 1950s had up to 400 model parameters. During the 1980s the error back-propagation algorithm helped to



**Figure 1.13:** Depth increase of neural networks over the last 70 years on a linear scale. Note that recently introduced residual networks have a depth of 152 layers [58] and beyond.

train larger multi-layer networks like NETtalk with 18.000 parameters [130]. Around 2000 techniques as receptive fields and weight sharing evaluated into the *Convolutional Networks* of Yann LeCun [84]. The Convolutional nets pushed the number of model parameters over 90.000 while maintaining excellent generalization [85]. In addition, Convolutional Nets increased the depth of classifier models from two layer models to 4-7 layers. Figure 1.13, illustrates the network depth increase caused by the introduction of Convolutional Networks. From 2006 onwards weight regularization techniques enabled regular non weight sharing networks to scale in depth to 4-7 layers [67,68]. These nets, so called *Deep Belief Networks* (DBN), increased the model size to almost 4 million parameters.

Around 2008 the availability *Graphics Processing Units* (GPUs) for general purpose computing improved the computational abilities of machine learning scientists. The use of GPUs resulted in huge networks; e.g., DBNs with 100 million parameters are successfully trained [118]. In addition to GPUs, the introduction of huge data sets in 2012 like the 1 million images of the ImageNet competition in 2012 [126] pushed the state-of-the-art Convolutional Networks to 60 million parameters divided over 11 layers [79]. This 60 million parameter network named “AlexNet” won the competition by a large margin over other approaches. Due to the success of AlexNet many research groups now contribute to the development of large classifier models. Nowadays the largest Convolutional Nets such as VGG have 280 million parameters [138]. In the extreme, huge DBNs with 11 billion parameters are trained by GPU clusters [32]. These examples

demonstrate the tremendous growth in classifier model size over time, and it is not expected that this growth will stop any soon.

### 1.3.2 Computational work

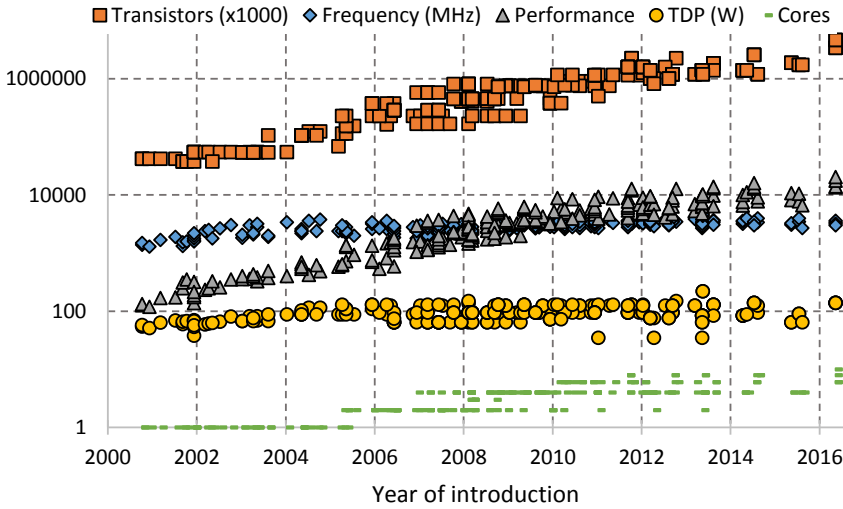
The computational requirements of deep neural nets have grown even faster than the number of model parameters. This claim is supported by the exponential trend lines in Figure 1.12. For the early neural networks computational workload scaled with the number of trainable model parameters. For example, each layer of neurons was fully connected, it required as many multiply accumulate operations as the number of weights in the network. However, the introduction of weight sharing since 1990 made that weights are reused for multiple compute operations. As a result, the number of compute operations grew even faster than the number of model parameters.

#### The role of computing platforms

To train increasingly larger nets with the impressive pace as presented in Figure 1.12 the machine learning community is driven by huge developments in computing platforms. Very important are the developments that enabled transistor scaling; e.g. Moore's Law [96] is a fundamental driver of computing over the past 40 years. In more detail, chip manufacturing facilities have been able to develop every 18 months new technology generations that double the number of transistors on a single chip. However, more transistors does not give any benefits by itself. It is the computer architecture industry that utilizes these transistors in new microprocessor designs. Computer architecture (in particular the ISA, Instruction Set Architecture of a processor) provides the abstractions that make these transistors accessible to compilers, programming languages, application developers, and machine learners.

Computer architecture harvested the exponentially increasing number of transistors to deliver an almost similar rate of performance improvement for microprocessors. The huge performance increase helped machine learners to build and train large neural networks. Nevertheless there are fundamental challenges associated with the development of new process technologies and integrating an exponential increasing number of transistors on a chip. One of the main challenges when doubling the number of transistors is powering them without melting the chip. During the last 15 years power consumption has become a huge problem in the field of computer architecture.

To quantify the power problem and look into possible directions for the coming decade we analyzed recent trends for desktop grade microprocessors. In this study data from 218 Intel and AMD processors is used by combining data from Intel's ARK database [72], which is extended with information from Wikipedia [149,148]. In addition, the relative computational throughput is added, which is measured by the PassMark processor benchmark software [139].



**Figure 1.14:** Historical data on Intel and AMD microprocessors showing the scaling of a chip’s transistors, clock frequency, compute performance, power dissipation, and core count. Performance is measured by the PassMark processor benchmark software [129].

## Challenges in transistor scaling

To illustrate the current technology scaling trends our data is presented in Figure 1.14. It shows five properties of the evaluated processors in our database: 1) number of transistors, 2) nominal clock frequency, 3) relative computational throughput, 4) maximal power dissipation or *thermal design power* (TDP), and 5) the number of cores. From Figure 1.14 we clearly observe that the number of transistors on a chip is still exponentially increasing, while the chip power remained almost constant. It is remarkable that we can drive chips with exponentially more transistors using the same amount of power.

Over successive technology nodes the power dissipation per transistor decreases by the same rate as their area shrinks. Therefore, a new technology can double the number of transistors without increasing the power consumption of the chip. This effect is known as Dennard scaling [42] and can be explained by the dynamic power dissipation relation that transistors follow:

$$P_{\text{dyn}} = \alpha C_{\text{eff}} f_{\text{clk}} V^2 \quad (1.10)$$

Here  $\alpha$  is the activity (switching factor, between 0 and 1),  $f_{\text{clk}}$  the frequency at which the transistor operates, and  $V$  is the supply voltage of the transistor. The circuit has an effective capacitance of  $C_{\text{eff}}$ . Due to scaling the capacitance  $C_{\text{eff}}$  and the transistor operating voltage  $V$  are reduced with a factor  $S$  (e.g. from 130 nm to 90 nm the scale factor is 1.4). Given equation (1.10) scaling reduces the power dissipation per transistor by  $S^3$ . However, a new technology node has a factor  $S^2$  higher transistors density ( $S$  in both dimensions), and by increasing

$f_{\text{clk}}$  by a factor  $S$  the chip power remains constant. Note that the potential performance of the new technology went up by a factor  $S^3$  (faster and more transistors).

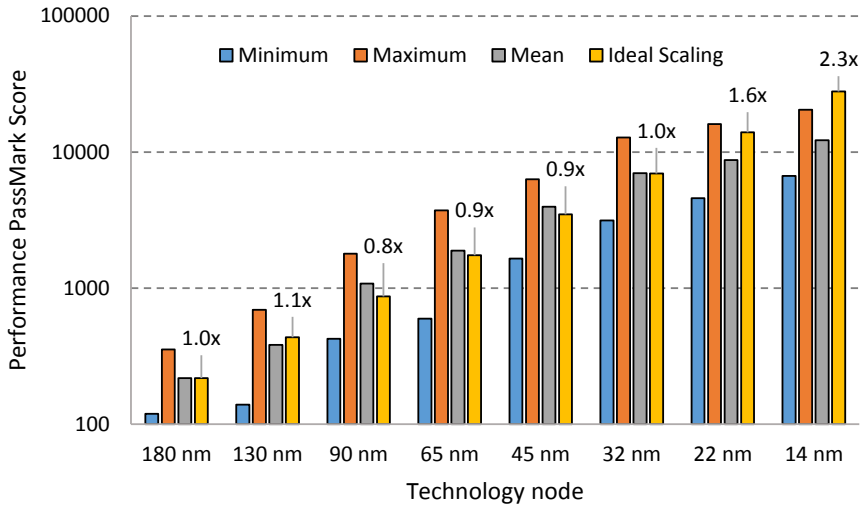
The bad news is that since 2005, at the 90 nm node, the rate of supply voltage scaling dramatically slowed down due to limits in threshold voltage scaling. As a result Dennard scaling stopped from that point onwards [42]. The number of transistors on a chip continued to grow with the historical rate, while the power per transistor is not decreasing at the same rate. This quickly results in power dissipation issues, especially since 100 Watt per chip/die is about the limit if no excessive cooling is applied. For embedded devices these limits are even lower e.g., 10 Watt for Tablets, 1 Watt for Smartphones, and 0.1 Watt for wearables.

### Computer architecture challenges

The first step to prevent excessive power consumption is to stop increasing the clock frequency  $f_{\text{clk}}$ . Figure 1.14 shows that since 2005 clock frequency stopped increasing and it leveled around 3.5 GHz. To maintain improvements in computational throughput and utilize the extra transistors of new technology nodes multicore architectures are introduced. Instead of more complex and faster single-cores, multiple simpler and lower frequency cores are integrated on a die. By exploiting parallelism in the applications multicore processors try to overcome the trends in transistor level scaling [134].

If we study equation (1.10) more closely we observe a factor  $S^2$  power increase because Dennard scaling stopped. Not increasing the clock frequency reduces this problem to a factor  $S$  power increase. This reveals another challenge for the near future; it might not be possible to turn on and utilize all the transistors that scaling provides due to *power limitations*. In addition, it is often very difficult to exploit enough application parallelism to *utilize* all cores in a multicore architecture. This second utilization problem automatically reduces the number of transistors that are turned on. Both problems make that in current technology nodes a growing portion of transistors is underutilized. A popular term for these chip portions that are underutilized is '*dark silicon*'.

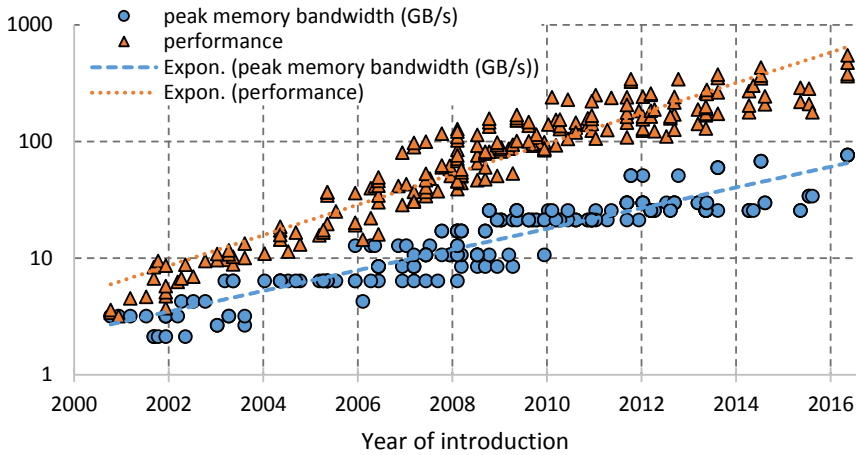
The implications of this growing portion of dark silicon pose great challenges for computer architecture. As a result it will become more difficult to increase computational performance over time. A recent exhaustive and comprehensive quantitative study by Esmaeilzadeh et al. [48] estimated the impact of dark silicon on the performance of processors. Under optimistic assumptions they predict that performance will increase by 7.9x over a period of ten years, resulting in a 23-fold gap w.r.t. the historic doubled performance per generation. If their predictions are correct the microprocessor performance increase per generation will dramatically slow down. As a result, this process will slow down developments in the application domains that benefit from the historic performance increase. Among these applications the huge and deep neural networks will face this problem. However, the work of Esmaeilzadeh et al. is a prediction, with our new dataset we can quantify the accuracy of their prediction.



**Figure 1.15:** PassMark performance of processors summarized per technology node versus ideal scaling or performance doubling per technology node.

The dark silicon performance prediction of Esmailzadeh et al. [48] covers 10 years from the 45nm node in 2008 to the 8nm node in 2018. Our dataset spans the 180nm node in 2000 till the 14nm node in 2016. Therefore, the gap between historic performance doubling for every node and the real world implications of power constraints must be visible in our data. To visualize this trend the PassMark performance of processors is summarized per technology node. Figure 1.15 presents these statistics as a minimum, maximum, and mean performance versus ideal performance scaling of the mean (doubling every generation). Technology generations up to 32 nm in 2010 were able to achieve the target of doubling performance per generation. The relative performance difference with the mean is plotted as a factor above the ideal scaling bar. However, since the 32 nm node in 2010 new generations were unable to keep up with the ideal target. As of today, the difference is already 2.3 x. Note that this is a substantial gap; it is more than the performance doubling of one technology generation. Still it is not as dramatic as Esmailzadeh et al. predicted. For instance in the unlikely scenario that there will be no performance increase for the coming two technology nodes the gap would be 9.1 x, which is less than the predicted 23-fold gap.

Although the performance gap is not as large as Esmailzadeh et al. predicted also we conclude that there is a large compute performance problem that most likely will not be solved by technology scaling. Studying literature and analysis of our recent data reveals that this compute performance problem is real and non-negligible. The causes of this problem seem to be chip power, and core underutilization due to limited application parallelism. Since deep neural networks contain massive amounts of parallelism the key challenge is power. Especially, since the class of always on embedded devices is very interesting. Currently deep neural nets run mostly on lab PCs equipped with power hungry



**Figure 1.16:** Historical data on Intel and AMD processors showing the peak DRAM bandwidth versus microprocessor performance scaling.

GPUs. When the target platform changes from these 100 Watt desktop processors to 0.1 Watt always on embedded devices it is evident that power dissipation and compute performance is the key challenge.

### 1.3.3 Memory transfers

In the previous section we analyzed computational workload. We looked into the computations requirements for large scale deep neural nets, and studied trends in compute platforms and transistor scaling that for a long time provided an exceptional performance increases. In this section we address a more specific part that is involved in the computational work, namely memory transfers.

In the computer architecture community it is well-known that memory bandwidth is a *bottleneck* that often limits application performance. Over time communication throughput of *dynamic memory technology* (DRAM) does not improve with the same rate as microprocessor performance [151,10]. Figure 1.16 illustrates that this trend is also visible in our microprocessor dataset. The relative PassMark performance score contains an offset such that it starts at the bandwidth level of the first Pentium 4 processors. This illustration clearly shows the difference in the two exponential trend lines. In addition to the memory bottleneck the datasets for applications continues to grow. This same trend is observed for deep neural network applications (see Section 1.3.1). For example, an image stream of images must be processed and therefore the huge set of model parameters must be transferred into the microprocessor. Without enough communication bandwidth this processing becomes memory bandwidth limited.

The positive part of this story is that most applications contain data-reuse, i.e. the same data element is often used for multiple compute operations. This motivates specialized memory hierarchies that exploit locality, e.g. small fast caches on-die that utilize reuse, and large high-density off-chip DRAM to hold



Operation	Energy	Relative cost
Alu op	1.0 pJ-4.0 pJ	1 x
Register file read	1.0 pJ	1 x
Read from SRAM	5 pJ	5 x
L1 Cache 32kB	20 pJ	20 x
Move 10 mm across chip	26 pJ-44 pJ	25 x
Send off-chip	200 pJ-800 pJ	200 x
Send to DRAM	200 pJ-800 pJ	200 x
Send over LTE	50 $\mu$ J-600 $\mu$ J	50,000,000 x

**Table 1.1:** Energy cost of different operations on 32-bit values in a 45 nm technology. Note that communication is significantly more expensive than computation, and its cost increases proportional with the distance [116].

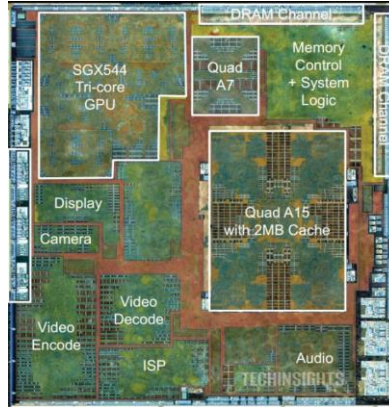
the huge datasets of modern applications. Given an application with enough data reuse these sophisticated memory hierarchies can reduce off-chip communication substantially.

### Energy of data movement

In addition to the memory bandwidth problems there is another communication bottleneck that limits performance. Again this bottleneck is power related, indeed data movement consumes a lot of power. Especially since transistors scaled down and improved their energy efficiency. However, on-chip wires, off-chip transceiver pins, and off-chip memory interface lanes do not scale well. As a result the energy cost of moving data within a chip and over a network can easily dominate the cost of computation, and therefore limit the gains from shrinking transistors.

Nowadays, loading data into a small local SRAM cache is several times more expensive compared to performing an arithmetic operation. Moving data 10 millimeters across a chip is an order of magnitude more expensive w.r.t. the arithmetic operation. Finally, moving data to off-chip RAM is almost three orders of magnitude more expensive than computing the value. Table 1.1 outlines the quantitative energy costs for different kind of data movements. The numbers depend on technology parameters, such as technology node, operating voltage and frequency, etc., but the general trend will be the same:

- Communication is very expensive.
- Computation is much cheaper than memory access.
- Memory access cost depend on the capacity (register file vs DRAM).
- Due to technology scaling the relative cost difference of computation versus data movement will further increase.



**Figure 1.17:** Die photo of Samsung’s Exynos Octa SoC. It contains a big and a small ARM quad core CPU, a GPU, and multiple accelerators for video, audio, and image processing.

### 1.3.4 Platform programmability

In the previous sections we studied the trends in transistor scaling and discussed the growing problem of data movement. Both trends show that future platforms are very much power limited, and it seems that faster systems are only possible if their energy efficiency can be improved. This also holds for the ultra-low power scenario where energy efficiency is key.

It is well known that these sources of inefficiency are often caused by the flexibility of general-purpose processors. Hameed et al. [58] demonstrate that a dedicated accelerator can be 500 times more energy-efficient than a general purpose multiprocessor. The main differences are in the customized local memory data structures and the programming model. Both significantly reduce the application flexibility, and they improve energy efficiency. This extreme example of energy-efficiency improvement motivates a shift to more heterogeneous compute platforms. In the domain of Smartphones we clearly see this trend, e.g. platforms like Samsung’s Exynos filled multiple dedicated accelerator cores (see Figure 1.17) are no exception. This results in heterogeneous systems with large cores to provide compute power when necessary, and small efficient cores for normal mode.

Although specialized cores can improve energy-efficiency they pose a major challenge for programmers. Currently, there are already significant programmability issues with normal multicore processors and GPUs. On a set of throughput computing benchmarks it is shown that natively written C/C++ code that is parallelism unaware is on average 24x (up to 53x) slower than the best-optimized code on a recent 6-core Intel Core i7 [129]. Note that this is for a general purpose processor that is designed to be flexible. In a heterogeneous context this slowdown is much bigger. Getting the best multicore performance requires the use of concepts such as parallel threads and vector instructions. In addition, making

effective use of the memory hierarchy requires is very challenging code transformations.

Due to the dark silicon energy problems future heterogeneous platforms will have multiple cores and accelerators, each with their ISA (Instruction Set Architecture, x86 or ARM), different type of parallelism (threads, vectors), a shared or their own memory space, a custom memory hierarchy. This will result in an even more challenging programming environment where much more programming effort will be required to optimize applications. We conclude that the increased complexity of heterogeneous platforms in the near future will increase the performance gap between native and optimized code.

## 1.4 Problem statement

In the previous sections the trends in deep neural network development were discussed. It seems that the size (in number of model parameters) is key for their recent success in many application domains. Continuing the existing exponential trend of larger and deeper networks will likely result in even more advanced applications, and record breaking accuracy on complicated classification problems. Pushing the deep neural network processing forward is one interesting direction. However, the usage of existing and future deep learning technologies in our daily life could be a game changer. It would give our personal companion devices the intelligence to help us with many complicated decisions.

The problematic part that prevents us from running deep neural nets on the class of embedded or always on portable devices is their huge computational workload. The embedded platforms of today simply do not have the processing capabilities to run such applications in real-time. For example, running a relatively shallow ConvNet for Speed Sign detection on a popular embedded platform (containing an ARM cortex-A9) results in a frame rate of 0.43 fps, which is far below acceptable. After studying the trends in microprocessor development we can conclude that it is not likely that the large performance gap will be closed any soon by new and more powerful embedded platforms.

As of today almost all compute platforms are power constrained, from the large super computers to the wearable system domain. The computational trends that are outlined in the previous section reveal that there are multiple problems that will slow down progress in compute performance for the coming years. Important issues are:

- The failure of Dennard scaling since 2005, disabled a large part of the energy-efficiency advantage of new and smaller transistor technology generations [42];
- The memory bottleneck and the increasing portion of energy that's consumed by data movement in current compute platforms;
- The huge programmability issues that become even worse since computer architects try to cope with the energy problem by moving towards more specialized heterogeneous architectures.

For the application domain of deep neural networks the current compute problems can stop or at least slow down further embedded use of deep learning. Even more problematic is the fact that these compute problems reduce the applicability of this state-of-the-art technology. To make that step from benchmarks towards real products and life changing solutions substantial improvements are required.

The goal of this thesis is to substantially improve the *efficiency* of deep convolutional networks. This improvement should enable the final technological step that moves the applicability of deep convolutional networks from offline only (cloud based) scenarios to the real-time portable and even wearable use-cases.

Efficiency is defined by three quantitative properties:

1. The number of compute operations that are required (Compute);
2. The number of necessary external memory transfers (Data Movement);
3. The amount of utilization that a normal programmer achieves when mapping different network workloads (Flexibility).

In the end all three efficiency properties influence the *energy-efficiency*.

## 1.5 Contributions

This thesis focusses on addressing the efficiency problems when running Deep Neural Network applications. In this work the problems are addressed on multiple fronts that span opportunities on the algorithmic side all the way down to the platform side. Our efforts to improve efficiency are published in [103,108,104,102,109,107]. Although the main focus is on Deep Convolutional Networks it is important to realize that many of the contributions are applicable to other applications, in particular the image processing and vision applications. The main contributions of this these can be summarized as:

1. An algorithmic modification to the feature extraction layers of Convolutional Networks. The modification *merges* the convolution and sub-sampling layers of these networks [103]. This layer merging reduces the computational and data transfer workloads of Convolutional Networks.
2. A new method for data locality optimization named *inter-tile reuse optimization* [104]. This method is developed to exploit the knowledge that for many accelerators workloads with a static schedule the future data content is known. This is directly applicable to Convolutional networks and increases the amount of utilized data reuse by a significant amount upon the state-of-the-art.
3. The Neuro Vector Engine (NVE) a flexible and programmable accelerator architecture for Convolutional Networks [109]. This is an ultra-low power accelerator that is designed for flexibility such that many different Convolutional Network workloads run close to full utilization.
4. An optimizing compiler framework for the NVE accelerator template. From abstract and simple network specification the compiler generates

close to optimal code (fully utilizing the NVE data path). Important to note is that the NVE is the first Deep Learning accelerator with an optimizing VLIW compiler [107]. This directly increases the applicability and ease of use in future SoC's.

This work shows that optimizations in multiple domains can drastically improve the energy-efficiency of deep convolutional networks. This is demonstrated by using the first two contributions for mapping on the NVE design. Combined the presented contributions address the challenges posed in our problem statement. As a result these contributions enables future mobile and wearable platforms to run Convolutional Network applications.

## 1.6 Thesis outline

After this motivational introduction chapter this thesis will continue with explaining background of deep convolutional networks in Chapter 2. This chapter provides the necessary background information to understand the later contributions.

In Chapter 3 our two baseline applications are defined. These are two different convolutional networks that will be used throughout the thesis: 1) Speed Sign Detection and Classification [105]; 2) A face detection network based upon [53]. Both applications are trained and their conversion to a video processing application is discussed. For both applications we will give the naïve C based mapping results.

Our main contributions are presented in the Chapters 4 to 7. In Chapter 4 we start with the merging of feature extraction layers [103]. We show theoretical gains of this optimization and we evaluate and verify these gains with a CPU and a GPU mapping. Chapter 5 describes our inter-tile reuse optimization methodology [104]. We evaluate the effectiveness of inter-tile reuse optimization on various accelerator workloads, to show the broad applicability of our technique. Our evaluation metrics are external memory transfers, FPGA resource costs and FPGA execution time, all based upon accelerator architecture templates that can be used with high-level synthesis tools [108]. Chapter 6 introduces the template for the Neuro Vector Engine (NVE) [109]. Our optimizing VLIW compiler [107] is presented and evaluated in Chapter 7.

Finally, in Chapter 8 we conclude the thesis and summarize possible directions for future work. This thesis does not contain a separate related work chapter. The relevant related work is discussed per chapter.

# CHAPTER **2.**

## DEEP CONVOLUTIONAL NETWORKS

*During the last decade Deep Convolutional Networks (ConvNets) have rigorously changed the domains of computer vision and pattern recognition. Many of these results are achieved because these nets are able to combine domain knowledge of the problem and machine learning from huge amounts of data. In this background chapter the different concepts and their motivations for the structure of ConvNets are discussed. This shows the differences and similarities with classical neural networks. ConvNets benefit from simple operators that are applied many times on input to build feature hierarchies. Different layer types such as convolution or pooling layers are discussed with their motivations. By stacking these layer module deep classification machines are constructed that can give impressive classification result.*

---

### 2.1 Introduction

As illustrated in the previous chapter, neural networks were used successfully for simple pattern recognition problems. Later, researchers realized that these algorithms and networks were too simplistic to solve more complicated and real-world pattern recognition problems. Section 1.1 concludes with the generalization issues of so called ‘shallow’ neural network models. Adding more free parameters to a two layers neural network does not solve this issue, but it makes the generalization problem even worse.

In Section 1.2 we briefly touched the topic of deep networks that stack many layers to improve the classification accuracy and prevent overfitting. We have shown that it is not only the depth of these nets but especially the structural constraints that make that these deeper nets are so successful. Building prior information in neural networks is key to achieve a good generalization. Techniques such as *receptive fields* and *weight sharing* are the basis for modern deep

Convolutional Networks (ConvNets). It enabled the construction of complicated feature extraction hierarchies that gave a tremendous boost to machine vision.

This background chapter should give the reader a clear understanding of the structure in ConvNets. Outlining how neural networks evolved into these deep classification machines? That information is required to understand the later optimization Chapters 4, 5, 6, and 7. In these later chapters we propose methods to reduce the increasing network complexity. This to ensure that these powerful classifier models can be implemented on resources constrained mobile devices. Which should give intelligent features to or next generation of companion devices. The task of training deep convolutional networks is covered in Chapter 3, where we develop our benchmark applications. The details of gradient propagation for learning is covered in more detail in Chapter 4, where this matter is needed to evaluate our layer merging operations.

In this chapter an introduction into visual data processing is given in Section 2.2. In Section 2.3 we cover the motivations that resulted into convolution operations to process visual data. From the need for parameter reduction by convolutions we go over the different types of layers in a ConvNet. The methods to construct powerful classifiers out of the different layer modules are discussed in Section 2.4. In Section 2.5, recent advances are discussed that enabled the use of even deeper networks resulting in a depth of 152 layers. Section 2.6 end this chapter with a summary and conclusions from this ConvNet background chapter.

## 2.2 Challenges of visual data processing

In Chapter 1.2 we briefly discussed the intriguing challenges of visual object recognition. Humans solve it without much effort, but for computer algorithms it is a very challenging task. In this section we discuss the properties of visual data and analyze how visual data is different from feature vectors. With feature vectors we refer to a set of features like the ones used to classify a person's health, e.g., "age", "nationality", "weight", "length", "blood pressure", "respiratory rate", "heart rate", "oxygen saturation", and "gender".

One of the first observations that sets visual data apart from feature vectors is the huge dimensionality. As illustrated by Figure 2.1, a road scene image for speed sign recognition easily contains 2.76 Million input variables. This involves three channels RGB of a 720p HD video frame. If this problem is reduced to single sign detection the frame size could be reduced to a 32 x 32 pixel grayscale patch; see Figure 2.2. Still the patch contains 1,024 input variables. A simple two-layer neural network with 1,024 hidden neurons and one output neuron has 1 Million parameters. This is a huge number of network parameters, especially compared with networks that classify on feature vectors. For example the health classification network has an input vector of 9 values. With 9 hidden neurons and one output neuron the network has 100 parameters. This is a difference of four orders of magnitude compared with a simple speed sign detector. It clearly illustrates the huge dimensionality challenges involved in visual images.



**Figure 2.1:** A 720 x 1,280 RGB road scene image for speed sign recognition has a huge input dimensionality of 2.76 Million input variables.

On the other hand visual data mainly contains inputs that are locally correlated. If we shift an image by a few pixels the image contents is still very similar. However, the input vector changed a lot. This effect is demonstrated in Figure 2.2 where changes like shift, scaling, or rotation do not change the local correlation between variables. In all cases a speed sign has large regions of white pixels. This is very different for feature based vector representations. Table 2.1 demonstrates that an element shift in the health classification vector would result in a vector that does not make any sense, i.e. there is no local correlation between elements.

Age	Nation- ality	Weight	Length	Blood pressure	Resp. rate	Heart rate	Gender
33	Dutch	80	1.88	120	13	60	Male
Male	33	Dutch	80	1.88	120	13	60

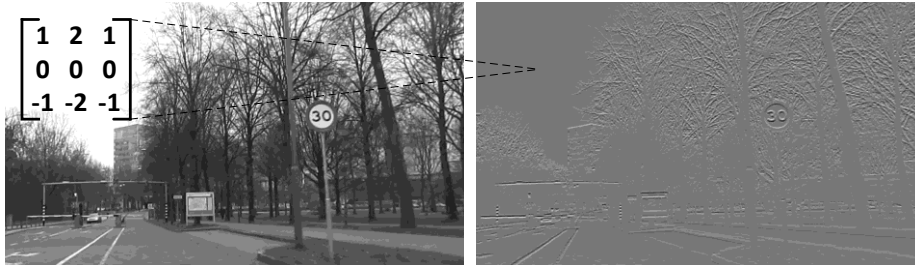
**Table 2.1:** A small shift in the feature vector of the health classification problem would result in a very strange input vector. However, for images a one element offset is very common.

We conclude that image data is very high dimensional, which poses challenges such as overfitting on the data. Furthermore, we conclude that the individual elements of image data can be very different after a subtle change in the image. For example a shift or illumination change will often modify all individual elements. Therefore image data requires a different approach. It requires a focus on the local correlations. Absolute pixel values alone do not describe the information in an image, it are the local patterns that best describe the image content.



**Figure 2.2:** Visual data has a huge dimensionality even a grayscale 32x32 pixel speed sign image consists of 1,024 variables. Small visual changes like a shift, scale, or rotate have a big impact on all variables. However, there is local structure between variables that remains similar after a visual change. For example the regions of neighbouring white pixels do exist in all versions of the speed sign images.





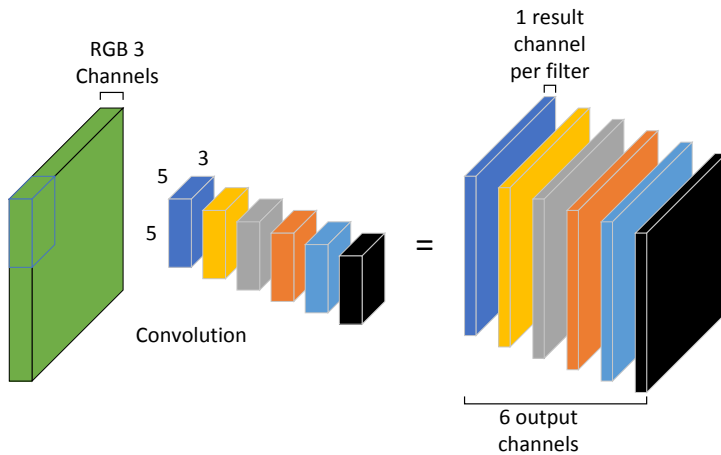
**Figure 2.3:** Classical Sobel filter operation on a road scene for local gradient or edge detection. Observe the strong and distinctive gradients in the region of the speed sign.

## 2.3 Parameter sharing

In the previous section we observed that image data differs from standard feature vectors. Most information in images is encoded in local correlations instead of absolute values. For example the well-known “Sobel” filter operator can be used to detect local edge gradient features. As illustrated in Figure 2.3, such filters can highlight the local correlations of edge patterns. There are many more local filter operations with different orientations that are often used as preprocessing steps in classical model based image classification.

In Chapter 1.2.2 we discussed the basic concepts of two step classification models for image data. Figure 1.1.1 illustrates a feature extraction step followed by a classifier. In a naïve classifier model feature extraction could be performed by the Sobel operator followed by thresholding to recognize edge features. The edge features are used by a classification model to recognize speed signs. Although this could work with a good classifier we do not know if edge features are optimal for this task. Much better would be an approach that learns the filter coefficients from the classification data. In this trainable scenario the filter operation is optimized for the task at hand.

Figure 2.1 reveals that the visual input could be even 3D instead of only 2D. The RGB 3D color channel inputs have their own local correlation. For some applications this extra dimension is very important, therefore the filter parameters should be 3D as well. This could even be extended to  $k$  dimension; e.g. think of *hyperspectral* data [23]. On the other hand, more than one filter operation could be required. For instance the Sobel kernel in Figure 2.3 does not highlight horizontal gradients, e.g. the pole holding the speed sign is not well extracted. Performing a second filter operation with a transposed Sobel kernel would extract the pole. The number of different kernel operations define a new dimension in the number of output maps. Figure 2.4 depicts the multi filter scenario where different filter operations are used to extract local correlations in the images, i.e. features.



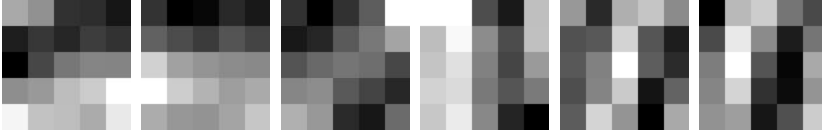
**Figure 2.4:** Multiple filter operations applied to an RGB input patch. Filter operations are performed by convolution with a set of filter coefficients. These coefficients are tuned to extract the important local correlations in the image data, e.g. gradient detection for different orientations.

Detecting local correlations can be parameter efficient. For example, the 6 extraction filters in Figure 2.4 require only 450 parameters. If we apply this operation on 3 color channels of  $32 \times 32$  pixel speed signs it would result in 6 output maps of  $28 \times 28$  values. The reduced number of output resolution is caused since the filter is applied only to the valid part of the image.

A fully connected neural network with the same number of outputs would require a massive amount of parameters. In this case  $28 \times 28 \times 6$  hidden neurons, each having  $32 \times 32 \times 3$  inputs (fully connected), resulting into 14.5 million parameters. In chapter 1.2.1 the concept of receptive fields for neurons was explained. Using a  $5 \times 5 \times 3$  receptive fields for each hidden layer neuron the parameter set is reduced to 353 thousand parameters. Both neural net implementations use way too many parameters for the speed sign classification problem. It would give two major problems:

1. The model would suffer from overfitting on the problem. Using many training examples and regularization techniques [69] could help reducing the overfitting.
2. The computational workload involved when evaluating such a model is huge.

For image data it seems that weight sharing by using convolutions is much more efficient compared to fully connected layers; even receptive fields use too many parameters to be efficient.



**Figure 2.5:** Weight visualizations of the first layer containing 6 filters in a trained Convolutional Network for speed sign recognition. See Chapter 3 for more details on the full network that is used as a speed sign recognition application.

### 2.3.1 Convolution layers

The previous section demonstrated that convolution operations are very powerful operators to detect local correlations in images. Convolutions can be modeled as neurons that exploit weight sharing, in essence convolution and weight sharing result in the same operation. Equation (2.1) gives the expression to compute fully connected neurons on a 2D image grid. Here  $M$  and  $N$  give the input image dimensions. The parameter sharing into convolution operations is given in Equation (2.2).

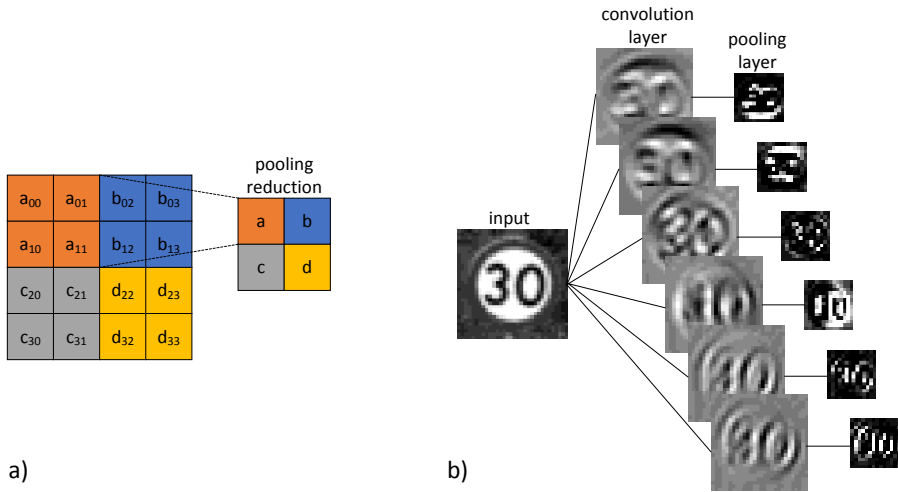
$$p_{m,n} = b_{m,n} + \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} x_{k,l} w_{m,n,k,l} \quad (2.1)$$

$$p_{m,n} = b + \sum_{k=0}^{K-1} \sum_{l=0}^{K-1} x_{m+k,n+l} w_{k,l} \quad (2.2)$$

In Equation (2.2) we observe that the full image dot product (summing over all elements in  $M$  and  $N$ ) is reduced to a local patch (summing in two dimensions with a small size  $K$ ). Furthermore, coefficient parameters, such as bias  $b$ , and weight kernel  $w_{k,l}$  are shared for every output neuron  $p_{m,n}$ . The input image ( $x$ ) of a convolution layer has two dimensions. However, often multiple input images, color channels, or feature maps can be used as input. In this scenario equation (2.2) is used. Each neuron matrix  $p_{m,n}$  corresponds to one output channel as shown in Figure 2.4.

$$p_{m,n} = b + \sum_{q \in Q} \sum_{k,l=0}^{K-1} x_{q,m+k,n+l} w_{q,k,l} \quad (2.3)$$

One could use multiple output channels where each channel specializes at extracting a different feature. Think of two orientations of the Sobel filter that specialize at gradients in x or y direction. Figure 2.5 depicts the coefficients of the first layer of trained Convolutional Network. Also here we observe that the coefficients specialize at local correlations such as gradient patterns with an orientation. The result of applying the convolution kernels to a speed sign patch



**Figure 2.6:** a) Pooling operation aggregates multiple values into a single value. b) First layers of the speed sign recognition net illustrating data reduction and feature selection by pooling.

is given in Figure 2.6b. The descriptive local gradients are highlighted in the 6 feature maps.

### 2.3.2 Pooling layers

Convolution layers often use multiple kernels to extract different features. The example illustrated by Figure 2.4 generates 6 feature maps of  $28 \times 28$  neurons resulting in 4704 values. The three channel  $32 \times 32$  pixel input consisted of 3072 values, so the convolution layer significantly increased the amount of data. For efficient classification only descriptive features are required, so probably not all features are required.

Pooling layers are used to aggregate multiple feature values into a single value, see Figure 2.6a. This reduces the resolution in feature maps, but it should preserve important features. Figure 2.6b illustrates the data reduction achieved by a pooling layer. Another desirable effect of feature pooling is invariance to small transformations. A feature grid that shifts a position will still propagate into the pooling result.

In general there are two popular pooling strategies:

- 1) *Average pooling* is very similar to the operation in a convolution layer. The main difference is that a single weight is used instead of a kernel. Furthermore, a stride is used to achieve the data reduction. Equation (2.4) gives the operation for average pooling. A scale coefficient  $w$  and a bias  $b$  are the trainable values in this layer.

$$p_{m,n} = b + w \sum_{k,l=0}^{S-1} x_{mS+k,nS+l} \quad (2.4)$$

2) *Max pooling* selects the local maximum from a window by using the  $\max()$  operator as given in equation (2.5). Max pooling does not involve any trainable parameter. It differs from average pooling that has a weight and bias.

$$p_{m,n} = \max_{0 \leq k < S, 0 \leq l < S} (x_{mS+k,nS+l}) \quad (2.5)$$

Both pooling functions use a scale factor  $S$  as a reduction parameter. This parameter defines the distance between neighboring windows. In the presented examples the pooling windows do not overlap, but pooling with overlap is also a valid option.

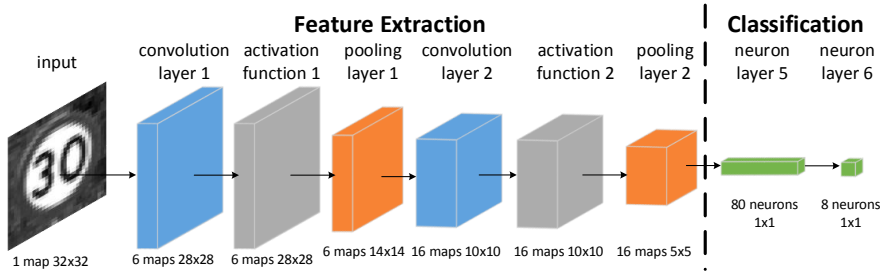
### 2.3.3 Neuron layers

For completeness we give the definition of classical neuron layers. There is no parameter sharing in neuron layers, every neuron has his own set of weights. The neuron layer operation on an image was given in Equation (2.1). Similar as for convolution layers the neuron layer operation can be extended to multiple input feature maps. Note that not all neuron layers are fully connected to all input feature maps. To keep all notations the same one could define a neuron layer with convolution operations. These convolutions have only a single output point so it is not a shifting window over the image, but a single position. In case the input of a neuron layer is a neuron layer we could use a  $1 \times 1$  kernel for convolution. Further details regarding neuron layers is given in chapter 1.

### 2.3.4 Normalization layers

Some networks use fixed normalization structures in a few layers. These normalizations enforce group behavior like sparsity or they normalize the mean and variance in a feature map. *Local response normalization* is one of these normalization structures. It implements competition between neurons at the same location, but in different feature maps. Popular competition winning networks like the ImageNet winner from 2012 use local response normalization to improve the generalization [79]. Local response normalization is performed by the operation in equation (2.6). The input activities  $x_{q,mn}$  for neighboring feature map positions  $q$  are used to normalize each neuron output  $p_{r,m,n}$ . The constants  $k, n, \alpha$ , and  $\beta$  are hyper-parameters that must be tuned carefully.

$$p_{r,m,n} = x_{r,m,n} / \left( k + \alpha \sum_{q=\max(0,r-n/2)}^{\min(N-1,r+n/2)} (x_{q,m,n})^2 \right)^\beta \quad (2.6)$$



**Figure 2.7:** Convolutional network architecture for speed sign recognition. Stacking several convolution, activation, and pooling combinations to obtain a feature vector. Continue processing with a few neuron layers to converge to a classification label.

Recently, *Batch Normalization* [73] is introduced which replaced local response normalization. Batch normalization improves the training process of a network by adding normalization layers that normalize small sets of training examples (mini-batches).

We mention these two normalization layer types for completeness. Although some of our proposed optimization methods are applicable to both techniques we do not further evaluate them in this thesis.

## 2.4 Constructing a convolutional network

In the previous section we demonstrated that local correlations in image data can be extracted by convolution layers. In addition to feature extraction a pooling operation can be used to select only important features. However, these two operations alone do not make a classifier. For this we should stack layer operations together and compute towards a classification label. Each of the presented layer types can be used as compute modules that perform a transformation on the intermediate data.

For instance, classification of a grayscale speed sign patch could use multiple convolutional layers. Each convolutional layer can use a non-linear activation function. In chapter 1 we discussed several activation functions. After each activation function a pooling step with or without another activation can be used to reduce the data. After a few cascades of this convolution, activation, and pooling structure the image is converted into a feature vector. Depending on the size of the input patch and the different kernel parameters this can be few cascades or many, like 5 or even more. Figure 2.7 depicts a ConvNet that reduces the 32x32 grayscale patch to a 16x5x5 value feature vector. In this case a relatively small patch is converted. When the classified objects are larger often much deeper networks are used. For example, the VGG [138] ImageNet 2014 submission uses 16 convolution and 5 pooling layers to convert 224x224 patches into a feature vector of 512x7x7. The convolution layers use small 3x3 kernels that can still describe left/right, up/down, or center gradients. The inputs of convolution layers

are padded such that the output/input size is similar. Only max pooling layers reduce the input/output size by a factor 2.

The cascade of convolution and pooling layers results in a descriptive feature vector that will be used for classification. It contains all important input information summarized in a concise format. To classify this feature vector into a classification label score one or a few neuron layers can be used. For example, the speed sign network in Figure 2.7 uses two neuron layers. The first one is a fully connected layer to encode the feature vector into 80 neurons. The second neuron layers transforms the 80 neurons into 8 class labels with a certain probability. Example classes are Background, 30 km/h, 50 km/h, 60 km/h, etc.

### 2.4.1 Coding neuron layers

The feed forward layer operations in a ConvNet can be implemented as series of deeply nested loops. The loops perform convolution operations between weight kernels and input feature maps as shown in code Listing 2.1. The loop nest for other layer functions, such as pooling (Listing 2.2) or classification (Listing 2.3), are very similar to the convolution implementation. These layer implementations show that many data elements are repetitively used to compute network outputs; as a result excessive amounts of data movement is required.

```
for(o=0; o<No; o++){ //output feature map
  for(m=0; m<Nm; m++){ //row in feature map
    for(n=0; n<Nn; n++){ //column in feature map
      acc=Bias[o];
      for(i=0; i<Ni; i++) //input feature map
        for(k=0; k<Nk; k++) //row in convolution kernel
          for(l=0; l<Nl; l++) //column in convolution kernel
            acc += In[i][m+k][n+l] * Weight[o][i][k][l];
      Out[o][m][n]=activationf(acc);
    }
  }
}
```

Listing 2.1: Loop-nest representing a convolution layer

```
for(o=0; o<No; o++){ //output feature map
  for(m=0; m<Nm; m++){ //row in feature map
    for(n=0; n<Nn; n++){ //column in feature map
      acc=Bias[o];
      for(k=0; k<Nk; k++) //row in pooling kernel
        for(l=0; l<Nl; l++) //column in pooling kernel
          //subsampling version
          acc+=In[o][Sm*m+k][Sn*n+l]*Weight[o];
          //max pooling version
          acc=max(acc, In[o][Sm*m+k][Sn*n+l]);
      Out[o][m][n]=sigmoid(acc);
    }
  }
}
```

Listing 2.2: Loop-nest representing two different types of pooling layers. Average pooling or subsampling, and max pooling. Note that the loop nest should contain only one of them at the same time.

```

for(o=0; o<No; o++){ //output feature map
  for(m=0; m<Nm; m++){ //row in feature map
    for(n=0; n<Nn; n++){ //column in feature map
      acc=Bias[o];
      for(i=0; i<Ni; i++) //input feature map
        acc+=in[i][m][n]*weight[o][i];
      out[o][m][n]=sigmoid(acc);
    }}
}

```

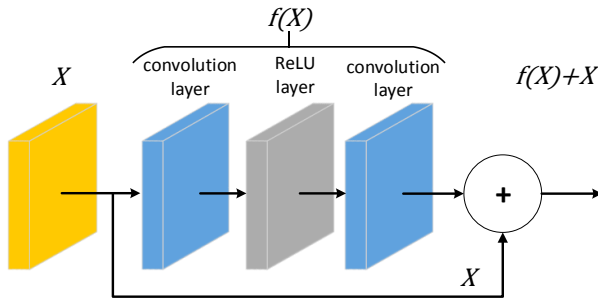
Listing 2.3: Loop-nest representing a neuron based classification layer.

## 2.5 Deeper networks

The early multilayer perceptron's often used two layers, one hidden layer and one output layer. These 'shallow' classifiers did not generalize well when trained on raw pixel values. Often these classifiers required good feature extractors that reduce the high dimensional pixel space into feature representations. The introduction of Convolutional Networks [84] provided a framework where feature extraction could be combined with classification in a single end-to-end trainable model. By enforcing structural constraints into the first layers of a network these ConvNets were able to use 5 to 8 layers of non-linear transformations efficiently. Each layer extracts a set of features starting with simple gradients towards more complicated shapes that are built on top of preceding layer features. Due to a larger number of layers these nets can implement complicated functions of its inputs.

Training a network with a depth beyond 8 layers is rather challenging. This is mainly caused by the gradient based training algorithms. Error gradients are used to update coefficients to a new state that performs better on the cost function. In chapter 3 we provide more information on error gradient based optimization procedures. For now error gradients are defined as  $\frac{\partial E}{\partial w}$ , where  $E$  is a loss function on the produced labels by the network in function of  $W$  holding the network weights. The gradients are efficiently computed by the chain rule that requires propagation from network output back to the inputs. Propagating the error gradients from the output cost function back towards the input layers is the difficult part. Sigmoid or hyperbolic tangent activation functions have the problem that they decrease error gradients. The introduction of Rectified Linear Units (ReLUs) improved the training of deep networks a lot [56]. Examples are the networks from 2012 to 2014 that won the ImageNet competition [79,138]. These nets benefit from efficient gradient propagation. The ReLU activation is described by  $\max(0, x)$ , where  $x$  is the input signal. Since ReLUs do not decrease gradients it enables training of much deeper networks. In addition, the ReLU activation gives sparsity to the neuron feature encodings in the network due to the zero part. For example, VGG [138] uses ReLU activations and demonstrates up to 21 layers with a total of 280 Million parameters. Such very deep nets stack many feature representations resulting in very advanced classifiers.





**Figure 2.8:** A schematic overview of a Residual learning building block. Multiple blocks can be cascaded, and each block can have a varying depth for network  $f(X)$ .

Recently, researchers successfully trained substantially deeper networks. To propagate the subtle details of a classification problem through more than 20 layers a different approach was required. Instead of learning transformations from  $x$  to  $f(x)$  they learn only the deltas on  $x$  and reuse the original  $x$  to perform the transformation. This is achieved by using *Residual blocks* that learn the function  $h(x) = f(x) + x$ . Figure 2.8 shows the structure of residual blocks. Learning only the differences from the input signals of layers enables a huge network depth of 152 layers [63].

This extreme depth has further improved the network complexity. Maybe not directly in the number of free parameters. Some of the deeper nets have fewer trainable parameters. However data movement and data dependencies between results make the computational requirements more challenging. In addition, the parallelism in these deeper networks has become more complicated. Data dependencies over layers make that it is more difficult to exploit all parallelism.

## 2.6 Conclusions

This chapter has discussed the current developments in the field of deep learning that resulted in more powerful networks. By understanding the structure in your data it became possible to embed this knowledge into the classifier architecture. This resulted into parameter sharing by means of convolution layers. Or in the extreme case learning only the deltas upon the input format to increase network depth. All these techniques enabled the use of larger networks, larger in number of free parameters, and deeper in number of layers. As a result the computational challenges when implementing such a network have become much more difficult.

In Chapter 1 we demonstrated that the complexity growth of ConvNets was historically accelerated by the developments in computing platforms. However, a similar pace in compute performance increase for the coming years is not expected. Power limitations are nowadays slowing down the performance growth for each new technology generation. Therefore the remainder of this thesis will

focus on efficiency improvements. We will research and apply high-level algorithm modifications and low-level data movement strategies that exploit data reuse. Furthermore this thesis will show a custom accelerator architecture including advanced optimizing compilers to simplify the mapping.

# CHAPTER **3.**

## BENCHMARK APPLICATIONS

*In the next chapters several methods will be introduced to improve the effectiveness of Deep Convolutional Networks. We need benchmark applications to quantify these improvements. Compute workload models may help to increase the understanding of trade-offs that are made. In addition, real applications on different platforms are used to verify our models. In this chapter we introduce two real-world vision applications for the purpose of benchmarking. A Speed sign recognition application for autonomous driving purposes, and a face detection application for surveillance. For both applications we explain the data collection and training procedure to obtain an accurate and robust ConvNet. Additionally, the conversion from a patch classification network to a video detection application is outlined. Finally we evaluate the performance of our applications on a CPU and a massively parallel GPU platform.*

*Parts of this chapter are based on work presented in the 8<sup>th</sup> International Automotive Congress 2011 [103]*

---

### 3.1 Introduction

This thesis proposes multiple contributions that improve the efficiency of deep convolutional networks, so it also requires evaluation. Each contribution can be evaluated by a performance or efficiency model. For example such a model could evaluate the achieved workload reduction. A good model can increase our understanding of the trade-offs that arise when applying optimizations. On the other hand, these models and optimizations should be verified with real data or in our case real-world applications. This ensures that the performance models are correct and it further increases the understanding of the problem. In some cases a real experiment will show unexpected side effects that are very valuable. This holds especially for the machine learning domain where many side effects can occur, e.g. properties such as overtraining and bad generalization can give

deceiving results. Similar effects could occur in computer architecture, e.g. an optimization that reduces the number of compute operations could give an undesired effect due to an increase of data movements .

Many of the published ConvNet implementations focus on the detection network itself. A real machine vision application embeds such a network to solve a detection or recognition problem. Be aware that the overall application often changes the characteristics and the important tradeoffs in the ConvNet. The main focus of this thesis is improving the efficiency of deep learning based applications, so we need real applications to evaluate the efficiency. Therefore, this chapter will introduce two machine vision applications based upon ConvNets:

1. Speed Sign Detection and Recognition for Autonomous Driving
2. Face Detection for Surveillance

Both applications are relatively small compared to the state-of-the-art in deep neural networks. However, we demonstrate that a real-time embedded mapping of such small ConvNet based vision applications is far from feasible on today's platforms.

Most literature does not explain how a ConvNet is used in a detection application. To clarify the differences this chapter will first outline the process of application development for ConvNets in Section 3.2. The guidelines for collecting training data is discussed in Section 3.3. Next this data is used for training, so we describe our training strategy for the applications in Section 3.4. The baseline throughput on different platforms is evaluated in Section 3.5. In Section 3.6 we discuss the state-of-the-art vision applications for detection and localization as related work. This chapter ends with conclusions and discussion in Section 3.7.

## 3.2 Object detection with a convolutional net

In Chapter 1 we outlined the spectacular results that recent deep convolutional networks (ConvNets) achieve on object classification tasks. In Chapter 2 we moved on and described these networks in more detail. We showed how a ConvNet classifies a  $32 \times 32$  pixel input patch into high level concepts like the digit 3 or 8. By using global training of the network parameters it is able to detect faces, recognize speed signs, or pedestrians. Although classification from a patch of pixel values is impressive it does not make a full application yet.

In this section we discuss the conversion of a patch classification ConvNet to a full-fledged recognition application that processes a video stream. Such applications have extra requirements such as scale invariance; furthermore they can exploit temporal knowledge about the object to improve accuracy.

Our first application performs speed sign detection and recognition for autonomous driving based upon [105]. An in-car camera captures a video stream that is processed on-the-fly to detect and recognize speed signs. As visualized in Figure 3.1 these signs occur on different positions in a frame and they differ in scale depending on the distance to the object. The second application performs face detection for surveillance based upon a ConvNet developed by [53]. As



**Figure 3.1:** Speed sign detection and recognition by an in car camera. Speed signs occur on different locations and with various scales depending on their distance.

shown in Figure 3.2, the application can process video frames captured at a busy crossroad to count people. Note that faces occur at different positions and with different scales.

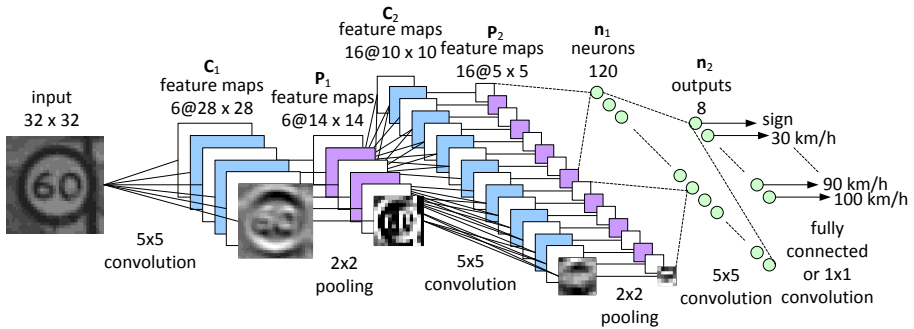
### 3.2.1 Patch classification

The core part of both applications is a ConvNet trained to classify a patch of neighboring pixel values. Depending on the difficulty of the classification problem the network could be large or small. For speed sign recognition we use a network based upon LeNet-5 that was originally developed to classify hand written digits [84]. The configuration of our speed sign classification network is depicted in Figure 3.3. The motivation for this starting point is the high similarity between the task of digit and speed sign recognition. Firstly, hand written digits are visualized in  $32 \times 32$  pixel patches which is a practical size to display speed signs. Reducing the patch size makes it difficult to differentiate between a 30 and 80 km/h sign. Increasing the patch size does not add much useful detail to a sign. Secondly, LeNet-5 has 10 different output classes, digit 0-9. For speed sign detection we define 8 classes (background, 30, 50, 60, 70, 80, 90, and 100 km/h).

As illustrated in Figure 3.4, the face detection network of Garcia et al. [53] is of similar depth as LeNet-5. However, the face detection network is relatively



**Figure 3.2:** Face detection demonstrated on a movie video still from “The Matrix” (1999).



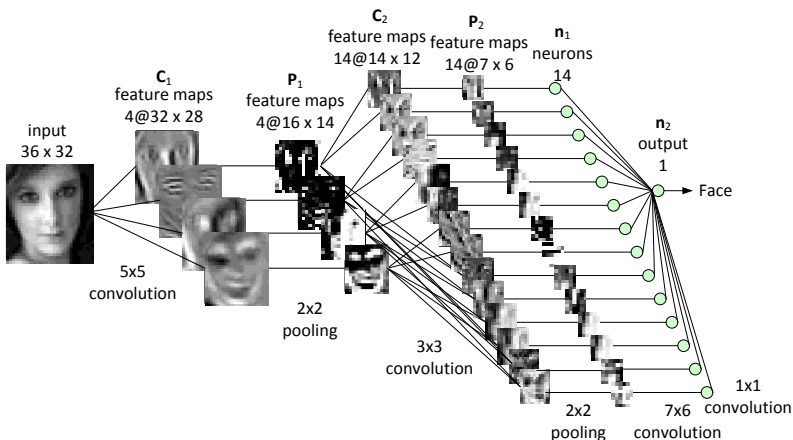
**Figure 3.3:** Dense ConvNet architecture for speed sign recognition.

sparse; the model has only 947 trainable parameters. Compared to the 50,356 parameters used for speed sign recognition the face detection model is very small. This difference is explained by the complexity of the task. Face detection is a two class problem (background, and face), so the reduced number of model parameters makes sense.

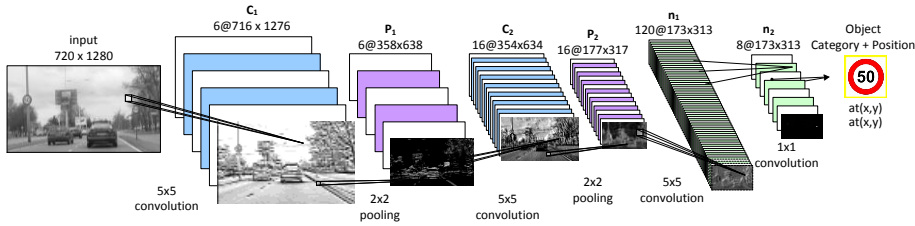
### 3.2.2 Frame based detection

A patch classifier is not directly useful as video application. Often the classifier is used as sliding window to test for an object at each location and scale in a video frame [147,39]. A naive sliding window search strategy quickly becomes computationally expensive, especially if high resolution frames are used. Therefore advanced search algorithms are developed that search by a smart schedule at the cost of increased control complexity [35]. Many of the complex search patterns introduce data dependencies that reduce the available parallelism.

ConvNets can use an interesting alternative approach to search a full frame. The convolution operator can be performed on any patch size, so the patch is



**Figure 3.4:** Sparse ConvNet architecture for face detection.

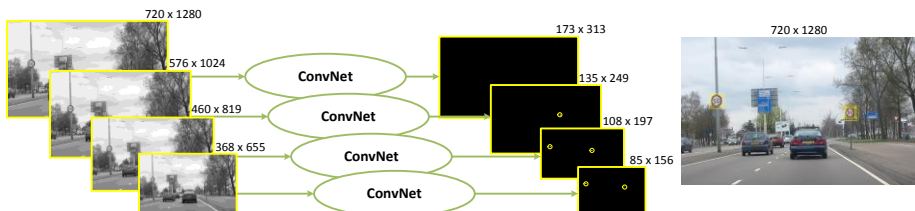


**Figure 3.5:** Speed sign recognition ConvNet modified to process 720p HD video frames.

replaced by a video frame. Figure 3.5 illustrates the result of extending a patch to a full frame where all feature maps scale accordingly. Note that this reduces the workload, since the overhead of processing overlapping sliding windows is automatically eliminated. In addition, the large amount of parallelism in each layer can be easily exploited since there are no window based data dependencies. As depicted in Figure 3.5 a map of classification scores is obtained where each position corresponds to a patch in the input frame.

Often patch detectors are trained with limited scale invariance, so objects are only detected at the scale available in the training set. Scale invariance can be further extended by converting frames to an image pyramid as demonstrated in Figure 3.6. The ConvNet is applied at all scales and the detections are mapped back to patches in the original frame. Finally, the ConvNet output of multiple frames can be combined to increase classifier robustness. For example, when a sign occurs at a certain position it should be detected at similar positions in the succeeding frames. These assumptions can help in the removal of false detections. Advanced usage of such assumptions as outlined in section 3.6 is beyond the scope of this thesis since it is a post-processing step.

Frame based detection applications require substantially more computational work compared to a patch detector. For example, the patch detectors for face and speed sign detection require 126,378 and 322,544 MACC operations respectively. For face detection on a single 720p HD frame the workload increases by 1,355 times to 0.171 GMACC. For speed sign recognition the increase is even larger; workload increases by 9,662 times resulting in 3.117 GMACC. The huge number of operations makes frame based detection applications much more challenging as a benchmark. In Section 3.4.3 on network design and Section 3.5 on throughput evaluation we will discuss more details of workload distribution in these frame based detection applications.



**Figure 3.6:** Image pyramid implementation of a ConvNet for multiscale speed sign recognition.



Figure 3.7: Example images from the collected traffic sign dataset.

### 3.3 Dataset construction

A very important element in the development of robust and accurate ConvNet applications is the dataset used for training. Each layer relies on patterns in the data, e.g., to extract the best features that increase class separation for robust classification. As a result, the dataset should be representative for the classification problem, e.g. for face detection normal faces must be included but also faces with a moustache or sunglasses. This is not specific for ConvNets, other works have shown that large datasets with a good variety of examples result in classifiers with excellent generalization and accuracy [99]. In this section dataset collection for our benchmark applications is outlined. We mainly show the procedure for our speed sign recognition network; to reduce redundancy we summarize only the differences for face recognition. Note that most of these techniques can be found in other works, so we discuss them for sake of reproducibility of our experiments.

Construction of the dataset for speed sign recognition is done by gathering real-world examples. One part is collected by using the Google image search engine for speed signs in the Netherlands. The other part consist of images that are obtained with Google Street View. In addition, the training set is increased with a representative data set that was published [98]. Finally the used data set contained 713 images of speed signs, which are cropped to show the full sign with a small background border. A subset of the training images is depicted in Figure 3.7. Training with these real-world examples creates invariance for natural variations such as, light conditions, small scale differences, and perspective.

Traffic sign images alone are not sufficient to train a classifier; additionally good set of background images is required. This background training class prevents false detections and is therefore very important. Example images from our background class are shown in Figure 3.8. One part of our background class contains random image patches that are collected from road scene images. A second part contains traffic sign images that look very similar to the speed sign classes.



Figure 3.8: Example images from the speed sign background class.



Class	Output label	# Patterns		
		Training	Testing	Total
Background	0 0000000	2489	415	2904
30 km/h max	1 1000000	77	13	90
50 km/h max	1 0100000	120	20	140
60 km/h max	1 0010000	62	10	72
70 km/h max	1 0001000	129	21	150
80 km/h max	1 0000100	75	13	88
90 km/h max	1 0000010	79	13	92
100 km/h max	1 0000001	69	12	81
		3100	517	3617

**Table 3.1:** Dataset configuration with the desired output coding for each different class.

To test the generalization of the classifier a small part (1/7) of the training set is excluded and later used for testing. An overview of the dataset organization is depicted in Table 3.1. Collecting a speed sign dataset of this size is time consuming but necessary to obtain a robust benchmark application. To our knowledge little effort is done to publicize real-world speed sign image databases. Also the fact that speed signs differ from country to country makes it valuable to publicize our dataset<sup>1</sup>. Additionally our public data set increases the reproducibility of the experiments described in this thesis.

The face detector is trained with the popular and public available Labeled Faces in the Wild (LFW) dataset [71]. The set of 13,458 face images from the web is split into 9,992 training and 3,466 testing images. All images contain alignment and scale coordinates such that it can be automatically cropped to match the ConvNet patch.

### 3.4 Training a convolutional net for machine vision

In Chapter 2 we introduced the well know error back-propagation algorithm [125]. This algorithm combined with Stochastic Gradient Descent (SGD), is often used for large-scale learning problems due its high computational efficiency [11]. SGD computes the error gradient for each network parameter and performs small updates in the negative direction of the error to converge to a minimum error. The usage of SGD on a large training set often involves a long script with many problem specific settings to obtain a well-trained network. In this section we outline the procedure that is used for training of our benchmark applications. As in the previous section we mainly discuss the speed sign recognition application. The differences with face detection are summarized at the end.

<sup>1</sup> Our speed sign dataset is publicly available at <http://parse.ele.tue.nl/research/speedsign/>

### 3.4.1 Preprocessing of training data

Before the training procedure is started the data set is prepared. Since both applications use a single input patch the datasets are converted to grey scale images. Although color gives extra information we did not use it because color representations are not very consistent between day and night conditions.

Inspired by the good results for handwritten digit recognition in [137] we artificially increase our data set by applying small modifications to each training sample. Adding such small deformations results in better invariance to the applied distortion, which improves the robustness of the detector. The following distortions are used to expand the training set:

- Light intensity scaling with clipping by a factor [0.8 0.9 1.0 1.1 1.2].
- Shift in x and y position [-2 -1 0 +1 +2] pixel positions.
- Scaling of the images [0.93 1 1.05], the resulting patch is cropped or padded to the original size.
- Face detection patches are flipped over the x axis.

The deformations are performed by a function,  $\hat{\mathbf{x}} \leftarrow g(\mathbf{x})$  that converts patches.

### 3.4.2 Training loop and recipe

For training a custom MatLab implementation of SGD is used. It is well known that SGD performs very well on large-scale learning problems [5,12]. Problems for which the computing time is the bottleneck are considered large-scale learning. Usually these algorithms are time bound due to the very large number of training iterations. In addition, to being effective SGD is relatively simple which improves the reproducibility our benchmarks.

Although SGD is relatively simple there are many variants and modifications of the algorithm. Additionally, SGD requires multiple *hyper-parameters* such as, learning rate  $\eta$ , and epoch size. The training methodology that is used for our benchmarks is outlined in the pseudo description given in Algorithm 3.1. Local gradients diverge over network parameters when computing back from the network output to the input. Therefore each layer has a dedicated learning rate  $\eta_l$  such that layers further from the output use a larger update this equalizes the learning speed over all layers.

The first step in training is parameter initialization. For our benchmarks all coefficients are initialized to small random values taken from the interval  $\theta \in \left(-\frac{1}{8}, \frac{1}{8}\right)$ . Advanced training methods sometimes use unsupervised pre-training to initialize the network parameters [47]. However, the introduction of Rectified Linear Units ReLU replaced the need for pre-training in deep networks. We do not discuss pre-training since advanced training methods are beyond the scope of this thesis. After parameter initialization the training loop is entered; every iteration performs one epoch of training succeeded by a test loop to measure generalization. Generalization score  $E_{\text{gen}}$  and a predefined number of epochs is used as stopping criteria. During training a sample is deformed as outlined in

**ALGORITHM 3.1:** Custom Stochastic Gradient Descent for ConvNets

---

**Input:** weight  $\mathbf{W}$  and bias  $\mathbf{b}$  coefficients as network parameters  $\theta$

**Input:** training set  $\{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(N)}\}$  with corresponding labels  $\{\mathbf{d}^{(1)}, \dots, \mathbf{d}^{(N)}\}$

**Input:** test set  $\{\mathbf{x}^{(N+1)}, \dots, \mathbf{x}^{(N+M)}\}$  with corresponding labels  $\{\mathbf{d}^{(N+1)}, \dots, \mathbf{d}^{(N+M)}\}$

**Input:** per layer learning rates  $\eta_1, \eta_2, \dots, \eta_L$

**Output:** Trained weights  $\mathbf{W}$  and bias  $\mathbf{b}$  coefficients  $\theta$

- 1 **while** stopping criterion not met **do**
- 2     **for**  $i = 1$  **to** epochsize **do**
- 3         Take random sample  $\mathbf{x}^{(j)}$  and corresponding label  $\mathbf{d}^{(j)}$  from training set
- 4         Apply deformation on sample:  $\hat{\mathbf{x}} \leftarrow g(\mathbf{x}^{(j)})$
- 5         Forward propagate through network:  $\mathbf{y}^{(j)} \leftarrow f(\theta; \hat{\mathbf{x}})$
- 6         Threshold error:  $\hat{\mathbf{y}}^{(j)} \leftarrow h(\mathbf{d}^{(j)}; \mathbf{y}^{(j)})$
- 7         **if**  $E_{\text{CE}}(\hat{\mathbf{y}}^{(j)}; \mathbf{d}^{(j)}) > 0$  **then**
- 8             Compute error gradient estimates:  $\tilde{\mathbf{g}}_{\theta} \leftarrow \frac{\partial E_{\text{CE}}}{\partial \theta}$
- 9             Apply per layer coefficient updates:  $\theta \leftarrow \theta - \eta_i \tilde{\mathbf{g}}_{\theta}$
- 10         Reset generalization score  $E_{\text{gen}} \leftarrow 0$
- 11         **for all** test set samples  $\mathbf{x}^{(i)}$  **do**
- 12             Forward propagate through network:  $\mathbf{y}^{(i)} \leftarrow f(\theta; \mathbf{x}^{(i)})$
- 13             Compute generalization score:  $E_{\text{gen}} \leftarrow E_{\text{gen}} + E_{\text{CE}}(\mathbf{y}^{(i)}; \mathbf{d}^{(i)})$

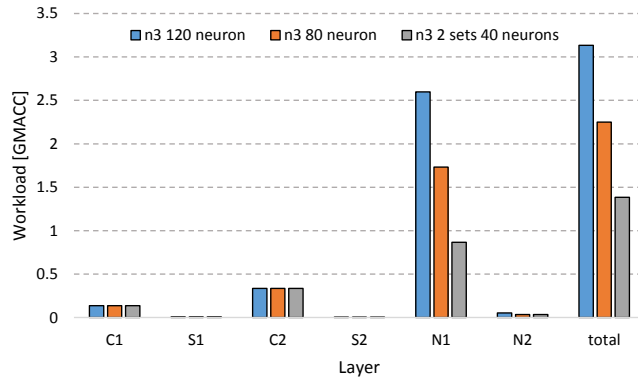
---

Section 3.4.1 and propagated through the network. The function  $h()$  compares the network output and the label  $\mathbf{d}^{(j)}$ , when per element differences are within 10% element  $y_k^{(j)}$  is set to label  $d_k^{(j)}$ . This rule removes unnecessary parameter updates and has two advantages: 1) reduces computational workload since a network quickly classifies a portion of the training data correctly; 2) The unnecessary updates could break learned patterns that were learned earlier. The remaining parameter updates are based upon plain SGD by applying the delta rule. The cross-entropy (CE) error-function [65] is used for gradient computation since multiple sources show that CE performs often very well for pattern recognition problems [78].

Our benchmark training does not use others use techniques to improve convergence speed such as *momentum* [115] or *Nesterov's accelerated gradients* [141]. Again, these more advanced methods increase the number of parameters and require dedicated tuning to result in a speedup of convergence time.

### 3.4.3 Network design

In the previous section the implementation of the used learning algorithm is discussed. In this section we explain how learning is used to obtain a good performing network for our benchmark applications. In Section 3.2.1 the patch detection network for speed sign recognition is given. This ConvNet is based upon the LeNet-5 configuration for hand written digit recognition. Only the output layer is modified to be able to separate background from speed signs and perform classification.



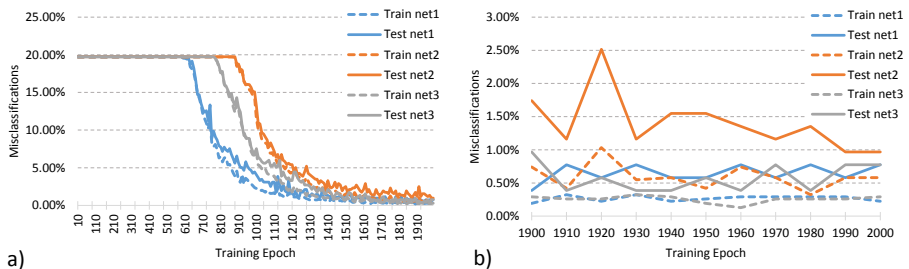
**Figure 3.9:** Workload distribution over layers of the speed sign detection application.

In Section 3.2.2 is shown that the video detection application requires 3.117 GMACC operations to evaluate a single 720p video frame, which is a lot. A more detailed analysis reveals that 83% of the workload is required in the first neuron layer  $n_1$ . Since the overall workload is dominated by layer  $n_1$ , it makes sense to investigate if it really needs this huge number of parameters. To reduce the computational workload three different configurations of layer  $n_1$  are evaluated:

1. The original LeNet-5 with 120 neurons in layer  $n_1$  is trained as a reference.
2. Layer  $n_1$  is reduced to 80 fully connected neurons.
3.  $n_1$  contains 40 neurons that are connected to feature map 1 to 8 and another 40 to feature map 9 to 16.

Figure 3.9 shows a detailed workload breakdown for the three ConvNet configurations.

The training progress for the three network configurations is illustrated in Figure 3.10. A magnification of the results during the last 100 epochs shows that network 1 and 3 give the best generalization accuracy. It seems that the 80 neurons of network configuration 2 have a somewhat reduced accuracy on the test set. However, by enforcing specific connections in configuration number 3 the generalization performance improves. A reason for the improved performance



**Figure 3.10:** Per training epoch classification score for speed sign network configuration 1-3. a) Gives the accuracy over 2000 training epochs. b) Highlights the final accuracy.

bootstrap iteration	false detections @ 0.5	selection threshold	detections selected	Training set size
1	12595	0.9	361	3461
2	232	0.8	18	3479
3	419	0.7	85	3564
4	18	0.6	7	3571
5	103	0.5	103	3674
6	3	0.4	15	3689
7	1	0.3	19	

**Table 3.2:** Overview of the rejection score after each bootstrapping iteration.

could be that dedicated connections enforce features to occur at restricted parts in the network. Fully connected layers have too much freedom to guide features.

The parameter reduction in layer  $n_1$  reduced the single frame workload to 1.384 GMACCs while demonstrating similar generalization performance. Although the workload in layer  $n_1$  is reduced it still represents 63% of the total workload. For benchmarking purposes in the later chapters layer  $n_1$  is kept in this dense configuration, likely the number of parameters could be further reduced.

The face detection network based upon the work of Garcia [53] is with 947 parameters is very sparse. The computational workload of 0.171 GMACCs per frame shows that the network is clearly developed with frame based detection in mind. For this thesis the face detector is not further altered, the relatively low number of parameters makes it an excellent sparse example for further benchmarking versus the dense speed sign recognition network.

### 3.4.4 Iterative bootstrapping

During the first real-world tests with our trained ConvNet benchmark applications a large number of false detections are measured. The main reason for the large amount of false detections is that the background class has almost infinite variety of patterns, which is impossible to include in the training set. To efficiently train the application to suppress background patterns an iterative bootstrapping procedure similar to the one in [53] is used. The basic idea behind the algorithm is to add only patterns to the training set which resulted in false detections. This forces the network to learn from his previous errors.

To automate the bootstrapping procedure 292 road scene images without speed signs are collected. First the recognition algorithm is executed on the new dataset with a high detection threshold. This step selects detections with a confidence value above 0.9. The resulting patterns are image patches for which the classifier is very sensitive. These examples are added to the training set and training is continued for 200 epochs. Next these steps are repeated with a decreased acceptance threshold. After 6 bootstrapping iterations is concluded that the number of false detections above a threshold of 0.5 is acceptable. The results of the individual bootstrap iterations are outlined in Table 3.2.

The network obtained after bootstrapping scores very well on the test set that was used for training in Section 3.4. For the 517 test images only one misclassification is measured. Effectively the percentage of misclassifications is reduced from 0.77% after training, to 0.19% with bootstrapping. We conclude that for our applications bootstrapping improved the recognition accuracy by a significant amount.

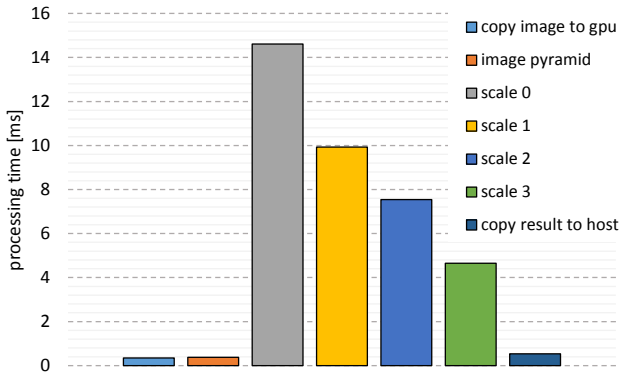
For the face detection task a similar bootstrapping procedure is used. Face detection bootstrapping iteratively gathered false detection samples from detection threshold [0.9 0.8 0.7 0.6 0.5 0.4]. This significantly reduced the number of false detections in frames, but the overall detection accuracy is similar. This indicates that the face detection network is under fitting on the dataset i.e., with the limited number of parameters there is no further improvement achieved by applying more data. For the dense speed sign detection network a further improvement in accuracy was achieved by performing the bootstrapping procedure.

## 3.5 Throughput evaluation

In the previous sections we outlined the development of two ConvNet based vision applications. The final step in this development is the mapping to a computational platform. The goal of such a mapping is to obtain a real-time detection system. For this purpose a consumer grade Nvidia GTX 460 GPU is selected as example of a high throughput compute platform. With 336 CUDA cores this GPU can exploit the huge amount of parallelism in ConvNet applications. In addition, this graphics card has a memory bandwidth 115 GB/sec to deliver the massive data transfer requirements of such applications. Of course the Thermal Design Power (TDP) of 160 Watts reveals that this is not a mobile or embedded platform. The GPU mapping is illustrative to show the computational challenges in these applications. Note that our benchmark applications are rather small compared to the huge nets in recent publications.

One of the application processing steps is the construction of an image pyramid. This step scales the input image with bilinear filtering using steps of 1.25 to increase scale invariance such that large signs close to the camera are detected. A GPU can perform bilinear filtering very efficient by using dedicated texture units. The bilinear filtering example from the CUDA programming guide [101] is used to implemented the image pyramid task.

The next step is processing of the ConvNet layers. First the implementation is optimized to increase data locality by loop interchange and tiling. For each layer different thread block configurations are compared to obtain a high CUDA core utilization and good data locality. Additionally, GPU specific optimizations described in the CUDA programming guide [101] are applied. For example, memory accesses to images are grouped such that transfers are coalesced, which maximizes external memory bandwidth. Kernel coefficients are kept locally on



**Figure 3.11:** Processing time of various tasks in a speed sign detection application on an Nvidia GTX 460 GPU platform.

chip by storing them in the fast constant memory. A final optimization is mapping the sigmoid activation functions to the fast GPU special function units.

The execution times of the different steps in the algorithm are illustrated in Figure 3.11. The total processing time for a four scale detection on a 1280x720 HD video frame is 38 ms, which results in a practical frame rate of 26 fps. As expected, the total execution time is dominated by the processing of ConvNet layers. A detailed breakdown of the single scale execution time given in Table 3.3. For comparison a C based naïve floating point CPU mapping on a 2.67 GHz Intel Core-i5 580M processor is given. As expected with a throughput difference of 80 times the CPU mapping performs much slower than the GPU. This results in a CPU execution time of 2.83 seconds for the four scale application and effectively a frame rate 0.35 fps.

These results again demonstrate that ConvNet applications have a huge efficiency problem. Only a power hungry GPU mapping delivers the required throughput at a huge energy cost. A mobile CPU with a 35 Watt TDP delivers an unacceptable performance 0.35 fps. This CPU mapping is far from optimal, one could divide the workload over two cores, and use the SIMD data path to improve performance. A theoretical linear speedup of 8 times would result in a disappointing throughput of 2.8 fps, and the 35 Watt dissipation is far beyond the practical power budget of a mobile or wearable device. Our aim at the mobile 1 Watt or wearable 0.1 Watt at a frame rate of 20 fps seems very challenging.

For face the detection application the workload is much smaller and therefore a GPU mapping would perform at a very high framerate. In the later chapters mappings of the face detection network are included. Especially for a low power ARM-A9 core this workload becomes interesting to take into account.

Platform	$C_1$	$S_1$	$C_2$	$S_2$	$N_1$	$N_2$	Total
GPU	1.19 ms	0.40 ms	4.83 ms	0.30 ms	6.34 ms	1.55 ms	14.6 ms
CPU	86 ms	23 ms	451 ms	17 ms	559 ms	46 ms	1182 ms

**Table 3.3:** Overview of processing time for the single scale speed sign detection ConvNet on an Nvidia GTX 460 GPU versus a mobile CPU 580M Intel Core-i5.

## 3.6 Related work

This section will focus on other real-world vision applications that use a ConvNet for object detection and localization. Recently the computer vision community embraced ConvNets which is improving the state-of-the-art. It would have been great to use one of the recently proposed vision pipelines as a benchmark application. However, the mapping effort of these new applications would involve a substantial amount of work. We will see in this section that the main compute workload in these applications is not any different from our smaller benchmarks.

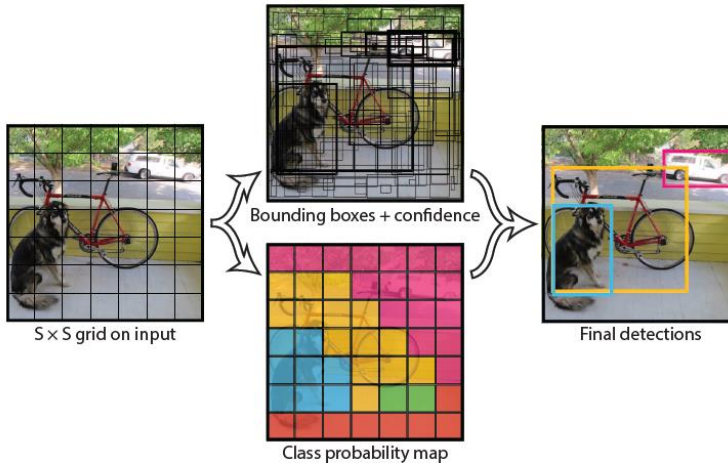
### 3.6.1 Region based convolutional networks

Our benchmark applications are designed for scenarios with were one type of object is localized in a frame. For example, the face detector generalizes such that many different types of faces (with glasses, facial hair, skin color, etc.) are detected. The speed sign recognizer detects a relatively small set of signs that all look very similar. Recently introduced vision applications have increased the complexity of detection and localization scenarios substantially. A very influential paper (cited over 3400 times) on the use of ConvNets for object detection is the work on *Region based ConvNets* [55]. The region based ConvNets split the recognition task into a region proposal step and a classification step. Instead of searching the whole frame a *selective search* method [144] is used to obtain boxes or so called region proposals are selected based on texture, color, and intensity of neighboring pixels. These region proposals are suggestions for objects that are passed to a powerful classifier such as one of the ImageNet winners [79,142,138,62]. For each region proposal the following steps are performed:

1. Warp the content to a size fitted for the ConvNet patch size.
2. Compute the ConvNet layers up to the last classification layer.
3. Use a SVM classifier to identify the object.
4. Use a bounding box regressor to refine the proposal region.

The region based ConvNets successfully apply a large ConvNet as feature extractor in a classical compute vision pipeline. Although the approach works really well, it is computationally very demanding. About 2000 regions are generated per image that each require a forward pass through a large network. Furthermore, the training is demanding since three models are trained: A ConvNet to generate image features; the classifier that predicts the class, the regression model to refine the bounding boxes. To overcome the computational issues *Fast Region ConvNets* are introduced [54]. Instead of generating region proposals from the image, the feature map activations in a ConvNet layer are warped as proposals. The huge advantage is that the feedforward run is performed only once per image. The network input patch size is stretched to match the image size, which is far more efficient than evaluating all those proposal patches. In essence this approach is similar to our benchmarks where we also scale the network to use the full frame. However in this work they use the ConvNet features





**Figure 3.12:** The output of a single shot detector like the YOLO model. The image is represented as an  $S \times S$  grid, each cell is encoded as a vector that contains class probabilities and the confidence for different bounding boxes. Image source: [86].

on which they perform Region of Interest (RoI) pooling. These features are warped into the proposal box that is the classification layer input. The final part of the model uses the RoI feature vector to perform classification with a SoftMax layer and a regressor for the bounding box refinement. The huge advantage is that this structure results in a single network model.

Fast region ConvNets provide a 25 times speedup over the original algorithm, but there is still a performance bottleneck. In a follow-up work so called *Faster Region Proposal ConvNets* [122] are introduced. These remove the selective search step. A new region proposal network is inserted after the last convolutional layer. It uses the raw feature maps to decide if there is an objects and propose a box location. From that point onwards the same pipeline is used as for the fast region ConvNets. The faster region proposal ConvNets have increased throughput by 10 times over the fast region proposal networks. As a result this work is able to test images in about 0.2 seconds per frame. Note that this is a GPU accelerated throughput of 5 fps, performed by an NVIDIA Tesla K45 that consumes about 235 Watt of power under load conditions. Unless the huge efficiency improvements that are recently demonstrated it seems that region proposal ConvNets are computationally still way too demanding for real-time applications on embedded devices. However, we should mention here that region proposal ConvNets are more accurate and much more general purpose in classification compared to our benchmarks.

### 3.6.2 Single shot detectors

A more efficient approach to object detection are the recently introduced *Single Shot Detectors*. These perform object detection as a single regression problem, directly from pixels to bounding box coordinates and class probabilities. A key

system that adopts this approach is named *You Only Look Once* (YOLO) [121]. They train a single network to segment an image into a low resolution grid, see Figure 3.12. Each cell in the grid contains a vector with the probability to be one of the 20 object classes, and two bounding boxes definitions ( $x_{pos}$ ,  $y_{pos}$ , width, height, confidence). To filter out the final box positions a Non-Maxima Suppression algorithm is used as a post-processing step. The base YOLO model requires input images of 448x448 pixels and performs the detections in real-time at 45 frames per second. This is almost a 10 times increase compared to the *Faster Region Proposal ConvNets*. Note that the YOLO model uses less object classes and it is constrained in the box positioning and sizing accuracy. The 45 fps throughput is achieved on a NVIDIA Titan X GPU that consumes about 250 Watts of power under load.

Very recently, the concepts of the single shot YOLO approach are further improved as described in the *Single Shot MultiBox Detector* (SSD) work [89]. To improve the detection accuracy SSD uses feature maps of different scales, and they explicitly separate predictions by aspect ratio. For training they use advanced data augmentation techniques, like *hard negative mining* which is essentially similar to iterative bootstrapping see section 3.4.4. The sampling of training examples is performed under special conditions to improve detection accuracy, e.g. object boxes with less overlap or the wrong aspect ratios. The SSD on a 300x300 pixel image is with 46 fps slightly faster than the 448x448 pixel YOLO approach. Both use a NVIDIA Titan X GPU. The main improvement of the SSD is the substantially better accuracy which is on-par with the much slower region proposal methods.

The compute workload in Single Shot Detector is very similar to the workload in our benchmark applications. The techniques proposed in this thesis can bring further efficiency improvements to enable the use of ConvNet based object detection on power constrained embedded devices. This to replace the 250Watt power hungry GPU by a low power ( $\leq 1$  Watt) embedded device.

## 3.7 Conclusions and discussion

In this chapter we demonstrate how a ConvNet based vision application is developed. We have shown the large computational differences between a single patch classification ConvNet and a multiscale video detection application that embeds a ConvNet. Furthermore, the importance of training data collection is emphasized. A good training and validation set is essential in the development of vision applications that performs well in a real-world environment. Additionally, the dataset should be used in a network training procedure to obtain a set of network parameters that solves the recognition problem. Training a ConvNet is a very demanding task, but often this is a one-time effort that can be done in a lab. Although this thesis focuses on inference and not on the training task, we

show that during training the network structure should be adapted to substantially improve the efficiency for the inference workload. For example our speed sign detection workload can be reduced by a factor 2.3 without loss of quality.

Our application development efforts resulted in two ConvNet applications that are used through the next chapters of this thesis. One is a *Speed Sign Detection* application for driver assistance or autonomous driving. The other application performs *Face Detection* for surveillance. Both video applications are very representative examples of deep learning based machine vision applications that will be deployed in the very near future as replacements of classical model based object recognition systems. The more advanced state-of-the-art detection and localization works often use a different training approach, but except for the post processing the inference mode is very similar to our benchmark networks. At this point we conclude that for a wide range of ConvNet structures our applications are quite representative. The face detection workload is a very sparse example where the speed sign network contains a quite dense workload.

By mapping the Speed Sign detection ConvNet to an NVidia Graphics Processing Unit (GPU) we demonstrated that our workload is very suitable for parallel compute platforms. Furthermore this mapping demonstrates that real-time detection tasks by ConvNet based vision applications is possible. However the 160 Watt power consumption for this GPU is far above the mobile energy budget. Another mapping to a mobile CPU shows a disappointing 0.35 fps throughput, and also this platform consumes a factor 35 more power than allowed. These mapping reveal the huge compute efficiency problem in ConvNet application workloads.

To harvest the huge advantages of deep learning based applications for our mobile devices the efficiency problems must be solved. The remainder of this thesis will focus on reducing the workload and improving the compute efficiency of these applications. If we could bring the deep learning techniques to our embedded platforms it will open a whole domain of new application opportunities. Firstly, the deep learning base applications have shown to outperform classical approaches in classification quality, for some problems superhuman performance is demonstrated. Secondly, application features can be added by a simple coefficient file update. Or our applications can automatically learn from errors made in a real-wold environment. These possibilities will greatly improve the quality of the next generation of machine vision applications.

# CHAPTER **4.**

## ALGORITHMIC OPTIMIZATIONS

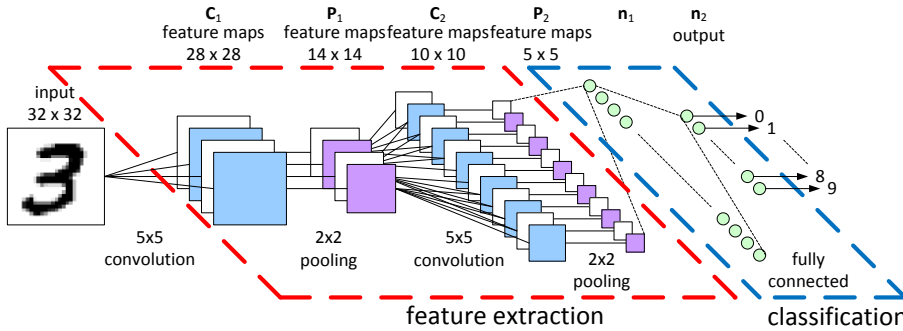
*The huge computational requirements of Convolutional Networks (ConvNets) often reduce their applicability to offline detection tasks. To ease these requirements we propose a high-level algorithmic modification applicable to the first layers of a ConvNet. These first layers are responsible for feature extraction by alternating Convolution and Pooling layers. This first part is often very complicated with multiple layers that often contain over 100,000 interconnected computational nodes. The proposed modification reduces computational complexity; real benchmarks show 65 - 83% reduction, with equal recognition accuracy. Often such modifications can introduce severe implications to the available parallelism. Therefore, the modified CNN algorithm is implemented and evaluated on a GPU platform to demonstrate the suitability of the proposed modification for massively parallel platforms. Our benchmark implementation achieves a speedup of 2.5 times w.r.t. the original algorithm.*

*This chapter is based on work presented in ACIVS 2011 [103]*

---

### 4.1 Introduction

Although Deep Convolutional Networks (ConvNets) achieve the best accuracy on many vision or classification tasks they are rarely used in mobile or embedded applications. In the earlier chapters we motivated that the huge computational challenges in (ConvNets) often prevent their usage in embedded systems. Often there exist a less accurate, but computationally cheaper algorithm. In these scenarios a classical model based solution is often used that trades functionality, accuracy, and robustness to obtain a simpler algorithm. Our main goal is to improve the efficiency of ConvNets, such that this class of algorithms with all their desirable properties can be used in mobile applications. In this first optimization chapter we focus on reducing the computational complexity without sacrificing on accuracy or quality.



**Figure 4.1:** An example CNN architecture used for a handwritten digit recognition task.

ConvNets have many levels of possible improvements e.g., Algorithmic, Tiling and Memory, Platform Architecture, and Technology. Here we focus on algorithmic changes, these are more abstract and can have a huge impact on the performance. A successful example is the 3-D RS motion estimator [41] that improved the expensive full-search block matchers into smart efficient recursive matchers. This algorithmic optimization is very radical and almost a different algorithm. However, in essence it still matches the surrounding blocks to find a best candidate for the motion vector.

In our work a modified feature extraction stage for ConvNets is proposed that reduces the computational workload and the number of data transfers. Figure 4.1 illustrates the feature extraction part that we optimize. Note that our optimization does not apply to the classification stage. The optimization can be directly applied on a trained networks. However, it is also possible to train a ConvNet structure with this modification, so we derived the required training rules. The network accuracy after training is evaluated with two real world benchmarks. To verify the theoretical performance claims, an Intel CPU and an NVIDIA CUDA-enabled Graphics Processing Unit (GPU) mapping is performed to demonstrate the achieved performance improvement.

The remainder of this chapter is organized as follows. Section 4.2 contains a recap of the ConvNet model to explain the proposed optimization. Then section 4.3 describes the algorithmic optimization and new training rules are derived. Next, section 4.4 evaluates the recognition accuracy of the optimization. Section 4.5 describes our mapping of the feature extractors and the speedup of our modification is evaluated. Related work and Conclusion are presented in Section 4.6 and 4.7 respectively.

## 4.2 Feature extraction layers

To explain the proposed algorithmic modifications, we provide a short recap the feature extraction part of a ConvNet. More details on the algorithm are discussed in Chapter 2.

Although ConvNets have different configurations with many or a few layers they often have a similar structure to the network depicted in Figure 4.1. Their first layers function as trainable feature extractor, and the second part implements a classifier. These first layers have constraints like receptive fields and weight sharing to extract position invariant features from two-dimensional shapes. Many networks contain two different successive layer types to extract these features: *Convolution Layers*, and *Pooling Layers*.

### 4.2.1 Convolution layers

In Figure 4.1 layers  $C_1$  and  $C_2$  are convolution layers. They take inputs from a local receptive field, and all neighboring neurons share the same set of weights. Basically it is a similar operation as a convolution by a small weight kernel. The 2d or 3d operation in a convolution layer that generates a single feature map is defined as:

$$c[m, n] = \varphi(p) = \varphi \left( b + \sum_{q \in Q} \sum_{k, l=0}^{K-1} w_q[k, l] x_q[m + k, n + l] \right) \quad (4.1)$$

Here  $b$  is the bias,  $w$  the shared weight kernel, and  $x$  is an input feature map that is transformed into output feature map  $c$ . The outer sum over  $q$  is optional, in layer  $C_2$  it is used to sum the contributions of multiple input feature maps. Different activation function  $\varphi$  can be used, in chapter 1 we discussed several options.

### 4.2.2 Pooling layers

As depicted in Figure 4.1 most convolution layers are succeeded by a pooling layer ( $P_1$  and  $P_2$ ) to reduce the number of detected features. There are two popular pooling functions that reduce the number of features.

1) *Subsampling* summarizes a window of features by local averaging with a trainable coefficient and a bias offset. The subsampling operation is defined as:

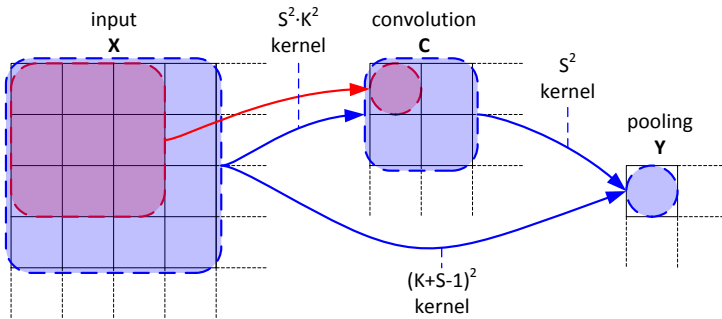
$$y[m, n] = \varphi(p) = \varphi \left( a + v \sum_{k, l=0}^{S-1} x[mS + k, nS + l] \right) \quad (4.2)$$

Here  $v$  and  $a$  are trainable parameter for scaling and bias offset respectively.

2) *Max pooling*, selects the local maximum from a window.

$$y[m, n] = \varphi(p) = \varphi \left( \max_{0 \leq k < S, 0 \leq l < S} (x[mS + k, nS + l]) \right) \quad (4.3)$$

Both function use scale factor  $S$  as reduction parameter. These reduction parameters define the distance between neighboring windows. Note that a window can have overlap.



**Figure 4.2:** Dependency analysis for a 2d-convolution kernel of size  $K = 3$  and pooling layer where  $S = 2$ . The dependencies from the input to convolution layer are given in red these results are consumed by the pooling layer. The merged solution directly consumes the inputs to generate the pooling result.

### 4.3 Algorithm optimization

In the previous section the feature extraction layers of a ConvNet are outlined. Depending on the network configuration these first layers will be responsible for a significant up to a large portion of the computational workload. The optimization proposed in this section focuses on reducing the workload in these first layers by merging the operation of convolution and pooling into a single operation. Depending on the network configuration there are two scenarios when our optimization is applied be applied:

- 1) A trained ConvNet can be directly converted into an optimized net if there is a linear function from the convolution layer inputs to the pooling layer. For example, conversion is possible when the convolution layer does not use an activation function and the pooling function performs subsampling.
- 2) A ConvNet must be retrained after conversion to the optimized network. This is necessary when a non-linear activation function is used in the convolution layer, or when the subsampling layer uses max-pooling.

#### 4.3.1 Merge convolution and pooling

The merge operation of convolution and pooling layers can be derived from dependency analysis. Figure 4.2 illustrates the data dependencies between both layers; it also shows how a single operation could bypass the convolution result. In the scenario of direct merging a new operator is obtained by substitution of the convolution operation (4.1) into the subsample expression (4.2). This substitution of operations is outlined in equation (4.4). The new enlarged kernel  $\tilde{w}$  is constructed from all coefficients that are multiplied by each input  $x$ . The new bias  $\tilde{b}$  is the convolution layer bias  $b$  multiplied by  $v$  and summed with the subsample bias  $a$ .

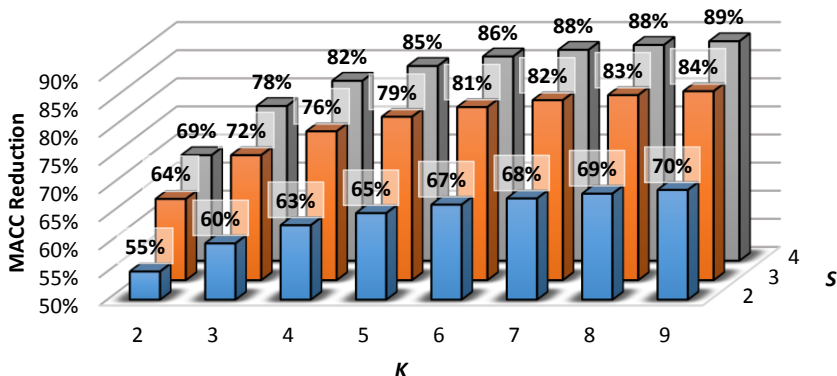
feature extractor	kernel weights	MACC operations
separated	$K^2$	$S^2(K^2 + 1)$
merged	$(K + S - 1)^2$	$(K + S - 1)^2$

**Table 4.1:** Comparison of the required kernel coefficients and operations for neurons in an original versus merged feature extraction layers. The improvement varies per layer configuration (different kernel size  $K$  and subsample factor  $S$ ).

$$\begin{aligned}
y[m, n] &= \varphi_p \left( a + v \sum_{i,j=0}^{S-1} c[mS + i, nS + j] \right) \\
&= \varphi_p \left( a + v \sum_{i,j}^{S-1} \varphi_c \left( b + \sum_{k,l=0}^{K-1} w[k, l] x[mS + i + k, nS + j + l] \right) \right) \\
&= \tilde{\varphi} \left( \tilde{b} + \sum_{k,l=0}^{K+S-2} \tilde{w}[k, l] x[mS + k, nS + l] \right)
\end{aligned} \tag{4.4}$$

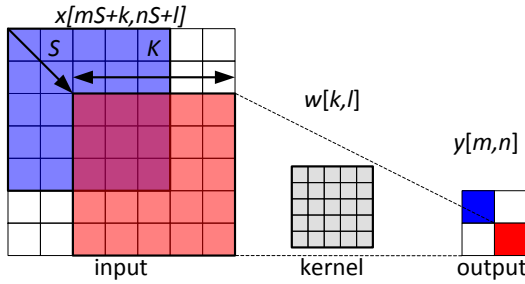
From Figure 4.2 and equation (4.4) it is visible that merging a linear convolution and subsample layer result in a significant reduction of MACC operations while retaining functional correctness. In addition, there are less memory transfers since there is no intermediate storage of convolution results. The reduction of MACC operations depends on the  $K$  and  $S$  parameters of the original network, their relation is given in Table 4.1. Large  $K$  and  $S$  sizes experience a more workload reduction as indicated in Figure 4.3. Inspection of Table 4.1 indicates that there is also negative effect of merging; it increases the relatively small number of the kernel coefficients.

Important to underline is that new coefficients for  $\tilde{w}$  and  $\tilde{b}$  cannot be derived when the convolution layer uses a non-linear activation function. This is not a severe problem, since the network can be retrained by an adapted learning algorithm. Since the weight space of the merged network has increased it could find



**Figure 4.3:** Influence of kernel size  $K$  and subsample size  $S$  on the compute workload reduction due to feature map merging.





**Figure 4.4:** Feed-forward computation through merged Feature Extraction Layers (FELs)

even better solutions. The recognition accuracy after retraining is further evaluated in Section 4.4.

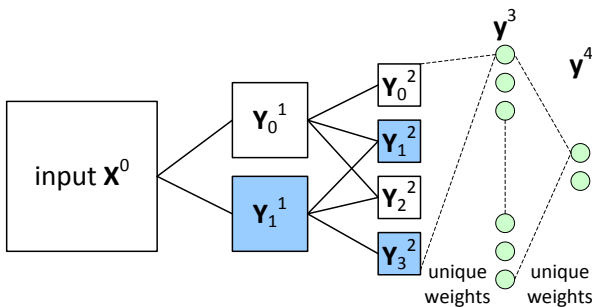
The remaining part of this chapter uses the new merged layers; named as Feature Extraction Layers (FELs). For completeness the new expression is given:

$$y[m, n] = \varphi \left( b + \sum_{q \in Q} \sum_{k, l=0}^{K-1} w_q[k, l] x_q[mS + k, nS + l] \right) \quad (4.5)$$

Here  $y$  is the new feature map result (former pooling), and  $x$  is the input as detailed in Figure 4.4. Note that a new value  $K$  is used to define the merged window size. Figure 4.5 shows the new merged network where convolution and pooling layers are replaced.

### 4.3.2 Training with error back-propagation

In the previous section we have seen that for some networks the new coefficients cannot be derived. In this section we will outline the retaining procedure. The learning algorithm is based upon stochastic gradient descent (SGD), also known as the on-line mode of error back-propagation [125]. The training algorithm is described in detail, because merged FELs substantially change the published training algorithms for ConvNets [84].



**Figure 4.5:** Merged network overview; separate convolution and pooling layers are replaced by FELs.

In chapter 2 the Stochastic Gradient Descent (SGD) algorithm is introduced. Here we explain the modifications that are necessary to apply SGD on ConvNets with merged FELs. The basic idea does not change; again partial derivatives of the error in function of the weights are computed for a given input pattern. These derivatives are used to reduce the error by small weight updates in the negative direction of the derivative. For clarity this procedure is split in three parts; feed-forward processing, partial derivative computation, and weight updates. During the outline of the algorithm we use the notation given in Figure 4.4 to describe signals in different layers.

### Feed-forward processing

Before training all coefficients are initialized to a small random value. First a pattern from the training set is processed in feed-forward by the merged ConvNet, using equation (4.5) for the FELs and a regular multi-layer perceptron (1.8) for the classification part. Next, the network outputs are compared with the desired output in an error-function. In this case we used the cross-entropy error function [64] as given in equation (4.6). Here  $N$  is the set output neurons,  $d_n$  the target labels, and  $y_n$  the output neuron values.

$$E_{\text{CE}} = - \sum_{\forall n \in N} d_n \log(y_n) + (1 - d_n) \log(1 - y_n) \quad (4.6)$$

### Compute partial derivatives

The previous expressions use  $x$  for layer inputs and  $y$  for outputs. The back propagation of derivatives over layers requires more variables, so we use  $y^\lambda$  to specify from which relative layer we obtain inputs. We start computing local gradients from the output of the network towards the input. This is done by applying the chain rule on the cross-entropy error function, which results in:

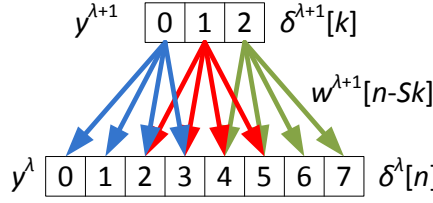
$$\begin{aligned} \frac{\partial E_{\text{CE}}}{\partial w_n^\lambda[k]} &= \frac{\partial E_{\text{CE}}}{\partial y_n^\lambda} \frac{\partial y_n^\lambda}{\partial p_n^\lambda} \frac{\partial p_n^\lambda}{\partial w_n^\lambda[k]} \\ &= \frac{y_n^\lambda - d_n}{y_n^\lambda(1 - y_n^\lambda)} \varphi'(p_n^\lambda) y_k^{\lambda-1} \\ &= (y_n^\lambda - d_n) y_k^{\lambda-1} \\ &= \delta_n^\lambda y_k^{\lambda-1} \end{aligned} \quad (4.7)$$

Important for the simplification is:

$$\varphi'(x) = \varphi(x)(1 - \varphi(x)) = y_n(1 - y_n) \quad (4.8)$$

$$\delta = \frac{\partial E_{\text{CE}}}{\partial y} \frac{\partial y}{\partial p} \quad (4.9)$$

Efficient computation of partial derivatives for the non-output neuron layers can be done by reusing the local gradients  $\delta$  of the output layer.



**Figure 4.6:** Gradient back-propagation through one dimensional feature extraction layers. This example uses layer parameters  $K = 4$  and  $S = 2$ .

$$\begin{aligned}
 \frac{\partial E_{\text{CE}}}{\partial w_n^{\lambda-1}[k]} &= \sum_{i \in D} \frac{\partial E_{\text{CE}}}{\partial y_i^\lambda} \frac{\partial y_i^\lambda}{\partial p_i^\lambda} \frac{\partial p_i^\lambda}{\partial y_n^{\lambda-1}} \frac{\partial y_n^{\lambda-1}}{\partial p_n^{\lambda-1}} \frac{\partial p_n^{\lambda-1}}{\partial w_n^{\lambda-1}[k]} \\
 &= \sum_{i \in D} \delta_i^\lambda w_i^\lambda[n] y_n^{\lambda-1} (1 - y_n^{\lambda-1}) y_k^{\lambda-2} \\
 &= \delta_n^{\lambda-1} y_k^{\lambda-2}
 \end{aligned} \tag{4.10}$$

The set  $D$  contains all neurons of the succeeding layer that are connected to neuron  $y_n^{\lambda-1}$  or  $y_n^3$  in Figure 4.4. In case of a fully connected layer all output neurons are connected. Equation (4.10) can be used recursively to compute the partial derivatives for multiple neuron layers.

The computation of local gradients for the weight kernels in the feature extraction layers is done in two steps. First, the local gradients of the neurons are computed by back-propagating from the succeeding layer (one closer to the output). Second, the local gradients are used to compute the gradients of the weight kernels. For the first step there are two scenarios: 1) *the feature extraction layer is connected to a neuron layer* (e.g.  $y^2$  in Figure 4.4). Computation of local gradients is done by:

$$\delta^\lambda[m, n] = \sum_{i \in D} \delta_i^{\lambda+1} w_i^{\lambda+1}[m, n] \varphi'(p^\lambda[m, n]) \tag{4.11}$$

Note that the expression is very similar to equation (4.10). However, in the other scenario the expression will change a lot: 2) *the succeeding layer is a FEL* (e.g.  $y^1$  in Figure 4.4). In this case only a select set of neurons of the succeeded FEL is connected, so we should only propagate the gradients of connected neurons as shown in Figure 4.6. Since, the connection pattern depends on the current neuron indices the summing of gradients restricts to a range of connected neurons:

$$\delta^\lambda[m, n] = \sum_{q \in Q} \sum_{k=K_{\min}}^{K_{\max}} \sum_{l=L_{\min}}^{L_{\max}} \delta_q^{\lambda+1}[k, l] w_q^{\lambda+1}[m - Sk, n - Sl] \varphi'(p^\lambda[m, n]) \tag{4.12}$$

where,

$$K_{\max} = \left\lfloor \frac{m}{S} \right\rfloor, \quad K_{\min} = \left\lfloor \frac{m - K + S}{S} \right\rfloor, \quad L_{\max} = \left\lfloor \frac{n}{S} \right\rfloor, \quad L_{\min} = \left\lfloor \frac{n - K + S}{S} \right\rfloor.$$

Border effects restrict  $K_{\max}$ ,  $K_{\min}$ ,  $L_{\max}$ , and  $L_{\min}$  to the featuremap indices.

In the second step, the local neuron gradients are used to compute the gradients of FEL coefficients. Since, the bias is connected to all feature map neurons we obtain its gradient by summing over the local gradients:

$$\frac{\partial E_{CE}}{\partial b} = \sum_{\substack{0 \leq m < M \\ 0 \leq n < N}} \delta[m, n] \quad (4.13)$$

The gradients for the kernel coefficients are obtained by:

$$\frac{\partial E_{CE}}{\partial w^\lambda[k, l]} = \sum_{\substack{0 \leq m < M \\ 0 \leq n < N}} \delta^\lambda[m, n] y^{\lambda-1}[mS + k, nS + l] \quad (4.14)$$

### Update network coefficients

The standard delta rule for SGD is used for updating to keep training simple and reproducible with  $\eta$  as single tuning parameter. This well-known coefficient update function uses the computed gradients to push the weights to a better solution.

$$W_{\text{new}} = W_{\text{old}} - \eta \frac{\partial E_{CE}}{\partial W_{\text{old}}} \quad (4.15)$$

In the update function (4.15)  $W$  refers to all weights  $w$  and bias  $b$  values in the network.

## 4.4 Evaluate recognition performance

In the previous section we introduced merging of convolution and pooling layers to reduce computational workload. If a ConvNet uses max-pooling or the convolution layer has a non-linear activation function the network must be retained to obtain a new coefficient set. In this section we evaluate the recognition accuracy after merging and retraining. Obviously, in case direct computation of the weights is possible there is no difference in accuracy.

To evaluate the recognition performance we use two well-known data sets with known network configurations, which increases reproducibility. The first evaluation is done on the MNIST handwritten digit dataset [84]. MNIST consists of 70,000 samples, each containing a 28x28 pixel digit as shown in Figure 4.7a. We use the LeNet-5 ConvNet to compare separated versus merged accuracy [84]. The second dataset is the small-NORB object classification dataset [85]. NORB consist of 48,600 stereoscopic image pairs, each 96x96 pixels as shown in Figure 4.7b. This set contains 50 different objects from different angles, distributed over 5 classes. For evaluation we use the LeNet-7 network, which is substantially larger compared to LeNet5. For training we used our MATLAB implementation of both networks and our implementation of the SGD training algorithm. As in the benchmark papers we used the original dataset division: MNIST 60,000 for



Figure 4.7: Subset of the visual patterns, used for accuracy evaluation.

training and 10,000 for testing; NORB 24,300 for training and 24,300 for testing. Table 4.2 contains the results that demonstrate the performance of our FELs that merge convolution and subsample layers. Firstly we observe that merging does not negatively influence the network's ability to generalize. For MNIST merging improves the final accuracy and for NORB merging performs on par with separated convolution and subsampling. Note that our implementations perform a bit better compared to the presented results in [84] and [85]. This shows that our training implementation results in a realistic and good operating point. The small improvement can be caused by small differences in the training algorithm. As predicted in section 4.3 the computational workload reduction in the feature extraction stage is substantial at the cost of extra weights.

## 4.5 Experimental mapping

The workload reduction presented in Table 4.2 of Section 4.4 is based upon the feature extraction layers of a small network that is used for training. However, in real applications the small input patch is often scaled to a 720p HD video frame. This scaling of the network increases the total workload, but it changes also the workload division. In addition, a workload reduction does not always result in a similar amount of speedup. Often there are other issues that influence

Benchmark	Misclassification	MACC ops.	FEL Coefficient
MNIST LeNet-5 [84]	0.82%	281,784	1,716
separated	0.78%	281,784	1,716
merged	0.71%	91,912	2,398
reduction	8.97%	65%	-40%
NORB LeNet-7 [85]	6.6%	3,815,016	3,852
separated	6.0%	3,815,016	3,852
merged	6.0%	632,552	6,944
reduction	0%	83%	-80%

Table 4.2: Evaluation of merged feature extraction layers for MNIST and NORB dataset.

the speedup e.g., the memory behavior (cache misses), or the utilized parallelism. To quantify the real speedup we mapped our speed sign recognition application with merged FELs to a CPU and a GPU. These mapping results are compared to the results we presented in Chapter 3 to obtain a quantitative measure of speedup.

First a single core C implementation is developed for a 2.66 GHz Intel Core-i5 M580 processor. This mapping is optimized for data locality by loop interchanges. The code is compiled with MS Visual Studio 2010 where the compiler flags are set to optimize for execution speed.

Secondly, a massively parallel implementation is developed for an NVIDIA GTX460 GPU platform. Feature extraction layers contain a lot of parallelism, so a good speedup is expected. For fair comparison of the feature extraction layers we tuned the code to utilize the GPU thread parallelism and to improve data locality (loop interchanges and tiling). In addition, GPU specific optimizations described in the CUDA programming guide [101] are applied. For example, memory accesses to the images and feature-maps are grouped to enforce fast coalesced memory accesses. The kernel coefficients are stored in fast constant memory. As final optimization the non-linear sigmoid activation function is evaluated fast using the special function units on the GPU. To enable this last optimization specific intrinsics from the programming guide are used:

```
__fdividef(1,1+__expf(-x));
```

The execution times for the CPU and GPU mappings are presented in Table 4.3. The speed sign application uses window size  $K = 5$  and subsample factor  $S = 2$ , so according to Figure 4.3 there should be a workload reduction of 65%. This workload reduction is very much in line with the 2.84 times speedup that is demonstrated on the CPU platform. For the sequential case we demonstrated an effective speedup similar to the workload reduction. However for the parallel platform this is not entirely true. Although the speedup of 2.48 times is considered as quite good, it is 13% less than the theoretical improvement. A parallel mapping of merged layers has more complicated access patterns and it utilizes less data reuse; both make that the theoretical speedup is not achieved. Still it is important to underline that our merged feature extractors improve the real GPU implementation by 2.48 times, which is a substantial speedup.

configuration	CPU	GPU	speedup
separate conv. & sub.	577 ms	6.72 ms	86 x
merged FELs	203 ms	2.71 ms	75 x
<b>speedup</b>	2.84 x	2.48 x	

**Table 4.3:** Speed sign recognition application execution time comparison of separated versus merged feature extraction stage.

## 4.6 Related work

Improving the throughput of ConvNets is not a new field of research. In the last decade many works proposed dedicated hardware implementations and accelerators for ConvNets [16,51]. These implementations often reduce execution time by the use of hand crafted systolic implementations of the convolution operation, which heavily reduces the flexibility. For example, a  $3 \times 3$  convolution performed by a systolic  $10 \times 10$  array results in a utilization of only 9% of the multipliers.

Improving the throughput by algorithmic optimization is often much more flexible and it can be applied to multiple platforms. For example, a related acceleration approach was presented in [137], where the authors give a reduced type of ConvNet. Instead of averaging with subsampling by using equation (4.2) they only compute one of the convolution results in an  $S^2$  window. Similar to our approach this reduces computational complexity, however the number of network parameters is not increased. The paper does not report on any quality loss, but this could occur if one only reduces the number of operations. Furthermore, the work in [137] differs because there is no analysis published that shows how kernel size  $K$  and pooling factor  $S$  influence the reduction of computational complexity. Finally, there are no performance measurements on parallel platforms such as a GPU.

Nowadays it is evident that the excessive workload of ConvNets poses huge challenges for computing platforms. As a result multiple recent works on algorithmic optimization are published. For example, the well-known Strassen algorithm for efficient matrix multiplication is used to reduce the multiplication workload in ConvNets [36]. To enable this optimization series of input images is buffered (a batch). This creates an opportunity to rewrite a ConvNet as a Convolutional Matrix Multiplication for which many optimized mappings exist from the linear algebra domain. Although the theoretical workload reduction of 65% is substantial, the average measured runtime reduction of 17% is minimal. The main cause of this gap is because the technique trades multiplications for additions. This tradeoff could also result in more memory accesses due to the partial results that must be computed, and they must buffer a series of input frames. Instead of mobile accelerators, datacenters could be an excellent domain to apply the Convolutional Matrix Multiplication. However, their technique is not evaluated on a parallel platform, so for parallel scalability further research is required.

A similar but more refined optimization uses Winograd's algorithm for minimal filtering [81]. Their minimal filtering is able to reduce the multiplications without creating excessive overhead. CPU mappings demonstrate a 2.58 times speedup, and GPU mappings give a 2.26x speedup compared to direct implementation. This complicated technique is highly tuned for  $3 \times 3$  filter sizes, which give a very efficient Winograd transform. For larger kernel sizes such as  $5 \times 5$  the

transform costs increase quickly and will overwhelm any savings in the number of multiplications.

Another high-level optimization approach performs convolutions in the frequency domain [145]. In frequency domain convolutions are point wise multiplications and therefore much cheaper compared to spatial domain. However, for small convolution kernels and small batch sizes the transformation costs destroy the savings in the number of multiplications. A combination of the Winograd and Frequency transform would probably give very competitive results.

A closely related work [75] also exploits the redundancies in representations that occur in ConvNet layers. They approximate the 2d convolution filters as combinations of a rank-1 filter basis (separable filters). Direct training a network on their rank-1 filter banks does not give good results. As a result, their approach requires an additional optimization on a trained network to find the optimal filter approximations. They report 2.4 times speedup without loss of accuracy. Their method also allows more accuracy loss e.g., at 1% accuracy loss they show 4x speedup.

Very recent work demonstrated that the weights in a deep ConvNet can be reduced to 1 bit (representing +1, or -1) with a scale factor  $\alpha$  per kernel [120]. In essence this convolution approximation is similar to the rank-1 filters of [75] but theirs is reduced even further. This so called Binary Weight Network must be trained with a custom implementation of SGD, and is able to achieve on-par performance with AlexNet [79]. However, on other large networks [142] a relatively large accuracy penalty of 5-10% is reported. The authors of [120] reduce the precision further by XNOR networks that additionally enforces the inputs of convolutions to 1 bit values (+1, or -1). XNOR nets use a trained scale matrix  $\beta_{i,j}$  for all outputs, and the  $\alpha$  scale per weight kernel. The XNOR approximates convolutions with less parameters than the Binary Weight Network. As a result, the accuracy penalty on AlexNet [79] is 5-10%, and for GoogLeNet [142] it does not converge anymore. Both Binary Weight Networks and XNOR exploit the parameter redundancy in ConvNets to the extreme. As a result both substantially reduce the memory footprint. Although throughput measurements for real network are not given we do expect a significant speedup due to this approximation.

## 4.7 Conclusion

In this chapter a high-level algorithm modification is proposed to reduce the computational workload of the trainable feature extractors in a ConvNet. We demonstrated that the learning abilities of the modified algorithm did not decrease; this is verified with real-world benchmarks. Our benchmarks show that the proposed modifications result in a MACC operation reduction of 65-83% for the required number of MACC operations in feature extraction layers.

To measure the actual application speedup due to workload reduction; our road sign classification application from Chapter 3 is used. This application is



mapped to a CPU and GPU platform. The speedup on CPU is a factor 2.7 where GPU implementation gains a factor 2.5, compared to the original convolution and subsample feature extractor. These speedups demonstrate that our modification is suitable for parallel implementation.

The modifications proposed in this chapter reduce the huge performance gap between the requirements of current ConvNets and the capabilities of today's embedded platforms. Although the factor 2.5-2.7 is not enough to close the performance gap it is a significant improvement that can be combined with other optimizations. In the next chapters we continue with different optimizations that use incorporate this layer merging technique.

# INTER-TILE REUSE OPTIMIZATION

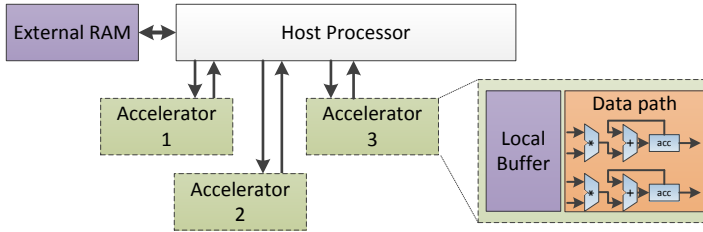
*Dedicated hardware acceleration of Convolutional Networks (ConvNets) can give a huge efficiency improvement over general purpose CPUs. A complex scaling problem that remains is the data transfer bottleneck. To scale-up performance accelerators require huge amounts of data, and often they are limited by interconnect resources. In addition, the energy spend by the accelerator is dominated by the transfer of data, either in the form of memory references or data movement over the interconnect. In this chapter we drastically reduce accelerator communication by exploration of computation reordering and local scratchpad memory usage. Consequently, we present a new analytical methodology to optimize nested loops for inter-tile data reuse with loop transformations like interchange and tiling. We focus on embedded accelerators that can be used in a multi-accelerator System on Chip (SoC), so performance, area, and energy are key in this exploration. 1) We demonstrate that our methodology reduces external memory communication up to 2.1 times compared to the best case of intra-tile optimization. This is done on our Speed Sign ConvNet and two common embedded image/video processing workloads (demosaicing and block matching). 2) We demonstrate that our small accelerators (1-3% FPGA resources) can boost a simple Microblaze soft-core to the performance level of a high-end Intel-i7 processor.*

*This chapter is based on work presented in ICCD 2013 [108] and DATE 2015 [104]*

---

## 5.1 Introduction

For many algorithms the compute efficiency is improved orders of magnitude by using specialized hardware accelerators instead of general purpose processor cores [58]. Designers of embedded compute platforms embrace customization



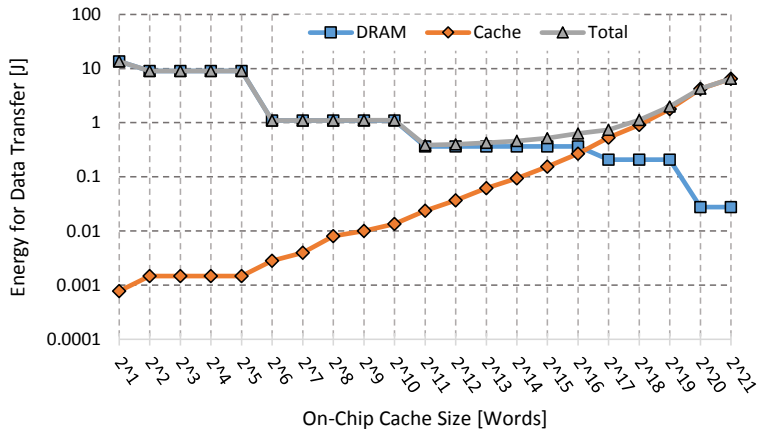
**Figure 5.1:** A host processor with multiple accelerator to achieve high compute efficiency by heterogeneity. Data transfer is reduced by local buffers that exploit data reuse.

to realize the best possible performance within a low power envelope [114]. This trend has successfully brought complex tasks e.g., HD video playback to Smartphones, and in the extreme to wearable devices such as Smartwatches or Glasses. For this class of dedicated accelerators the compute primitives are customized for the compute workload. If we for example, consider FPGAs there is plenty of hardware for parallel compute units.

By specializing the compute operators a more complex scaling problem is introduced. Providing these parallel compute units with the required high-speed data streams is a major challenge. This is particularly difficult if the system is equipped with multiple parallel accelerator cores, see Figure 5.1. Especially in the computer vision and image processing domain the data transfer requirements are challenging, since high resolution frames or images that must be processed do not fit in on-chip memories. Therefore, frames are stored in external memory which has limited transfer throughput, and requires much more energy per access compared to on-chip memories. As a result most compute platforms spend the majority of energy consumption on data movement and computation is almost for free.

Deep Convolutional Network (ConvNet) applications have this similar data transfer problem. There is sufficient parallelism to execute hundreds of operations in parallel. However supplying the data streams is very challenging and it dissipates a lot of energy. For example, our speed sign detection application from Chapter 3 requires 3.5 billion memory accesses in a single layer. Without an on-chip buffers all accesses will communicate through slow and costly external memory. These involved data elements are often required several times for the computation, so there is reuse of data elements. Therefore, elements can be temporarily stored into on-chip caches or buffers such that a huge number of external transfers can be overcome by efficient local reuse of data. Varying the on-chip memory size is in essence trading chip area versus external memory bandwidth. E.g. 4 MB on-chip memory can already reduce the external accesses in a dense speed sign detection layer from 3.5 billion to 5.4 million, which is a substantial reduction of external communication.

We estimated the data transfer energy for varying on-chip memory sizes with a memory tracing tool [6], additionally we performed energy estimation for external [17] and on-chip [97] accesses. From the result, as depicted in Figure 5.2,



**Figure 5.2:** Data transfer energy for external DRAM and On-Chip cache accesses.

we conclude that increasing accelerator utilization with a lot of external memory bandwidth is bad for energy. This huge external bandwidth scenario is used by GPU platforms, and it explains why GPUs consume a lot of power. Although on-chip memories can help increase accelerator utilization, along with the size, the energy consumption per access also increases. In other words, large on-chip memories do not solve the energy problem. The large cache scenario is used by general purpose CPUs, and also this causes efficiency problems.

Careful analysis of Figure 5.2 reveals that the sweet spot for energy efficiency lies somewhere in the middle i.e., small local buffers reduce external accesses and don't add a large energy penalty. In this chapter we propose a methodology to maximize data reuse in small local buffers. It is well-known that advanced code transformations such as interchange and tiling can increase data locality. However, obtaining the best set of transformations is often intractable due to the huge design space. We propose combinations of tiling and interchange that result into efficient *tile-strips*. In contrast to others, our method optimizes the *inter-tile* reuse which open more reuse opportunities, and is perfectly suited for accelerator controlled local memories. We make the following new contributions:

- Development of analytical data transfer models that take inter-tile reuse into account. (Section 5.4)
- Pruning of the search space to enable quick design space exploration for the best schedules, given a buffer size. (Section 5.5)
- Demonstrator by using our technique to equip a simple processor with high performance accelerators. (Section 5.6)
- Evaluation on ConvNet workload and two other common embedded applications, and show that huge speedups can be achieved with a modest amount of buffer size. (Section 5.7 and 5.8)

First we present related work in Section 5.2. Next continue with a motivating example in of iteration reordering in Section 5.3. After the main contributions this chapter will end with conclusions in Section 5.9.

## 5.2 Related work

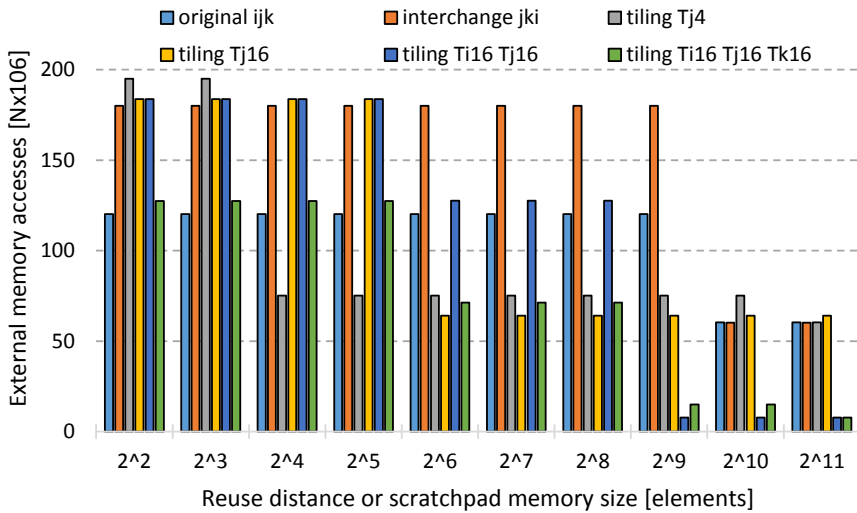
The scheduling of loop iterations for data locality is studied for decades for decades [150]. A milestone in this field is the Data Transfer and Storage Exploration (DTSE) methodology [14]. For embedded processors DTSE uses loop fusion and interchange to improve access regularity and locality. More recent works rely on a Polyhedral description [8] of the loop iterations on which automatic transformations are applied that enhance performance. State-of-the-art approaches for x86 CPU code that are used in production compilers are, Pluto [9], and POCC [111]. These works select transformations for communication-minimized parallelization and locality, in some sense this looks very similar to *inter-tile* data reuse optimization. However, their approach is opposite to ours we maximize communication between tiles, and convert that into reuse. Their approach is similar to *intra-tile* reuse optimization i.e., maximize reuse within a tile and minimize communication over tiles, which is good for parallelization and locality. In Section 6 (intra-tile opt.), we compare with such scheduling approaches and show significant data transfer reductions.

Exploiting data overlap of successive tiles is introduced only very recently [1], here it is used after optimization to remove redundant transfers. In Section 6 we compare to this strategy (inter-tile reuse) and show that it is important to include inter-tile reuse into the tile size selection process. Their follow-up work [40] parameterizes the tile size selection, so time consuming empirical search methods with the system in the loop can be used to find good parameter configurations.

The tile size selection problem is not solved, with analytical bounds and empirical search methods it is possible to find good performing tile parameters for CPU caches [133]. This work is extended with multi-level caches, conflict misses, and vectorization [95]. We focus on low-power accelerators that rely on more area and power efficient scratchpad memories. For compile-time known access patterns [74] shows that efficient data placement for reuse is more efficient than cache, but in contrast to us they consider the iteration order fixed.

The Halide compiler [117] also focuses on static image processing and computer vision applications, but for x86 and GPUs. In their work Interval Analysis is used for optimization with a stochastic auto tuner that takes up to 2 days to converge to good solutions. In [90] the data reuse optimization problem for FPGA hardware is solved by efficient geometric programming. To use geometric programming a simplified data reuse model is used. In contrast to our method, important properties such as overlap between successive tiles is neglected.

Recently a new tool is developed that optimizes HLS input descriptions for parallelism and locality [112]. This method uses the polyhedral framework for



**Figure 5.3:** Data transfer histogram for the matrix multiplication kernel given in Listing 5.1. Loop transformations such as interchange and tiling have a huge impact on the external data transfer.

transformations and uses a HLS tool such as Vivado HLS (former AutoESL) to estimate the quality of result. The downside of this approach is its long iteration time; e.g. testing 100 design points can take up to five hours. Secondly, the polyhedral framework generates x86 optimized code with complicated loop bounds resulting in many extra divisions, and min/max operations. In [156] the authors remove some of the x86 artefacts in the generated output code with a HLS friendly code generator, but the fundamental problem of complex bounds remains.

### 5.3 Motivation: scheduling for data locality

For hardware controlled local memories, such as caches, the reuse distance [44] is a good metric to predict if a value can be reused given a certain cache size. Reuse distance is defined as: *the number of distinctive data elements accessed between two consecutive uses of the same element*. A modification in the iteration order of a loop nest can change the reuse distance of the enclosed array accesses. Hence, data transfer requirements can be changed by reordering loop nest iterations. Important transformations that are used for this purpose are *loop interchange* and *tiling*.

The effect of transformations is demonstrated on an educational example of matrix multiplication, the corresponding loop nest is given in Listing 5.1 For simplicity the result matrix  $\mathbf{C}$  is already initialized to zero, and the sizes of loop bounds is set to:  $\mathbf{Bi}=500$ ,  $\mathbf{Bj}=400$ , and  $\mathbf{Bk}=300$ . The inner loop iterates over  $\mathbf{k}$ , so

each iteration one element of **C** is reused. After **Bk** iterations a row of **A** is reused. We used *Suggestions for Locality Optimizations* (SLO) [6], a reuse profiling tool, to visualize the remaining data transfers. Remaining transfers are defined as the total number of memory accesses minus the reuses of data elements. Figure 5.3 shows these remaining transfers for different local buffer sizes. With a very small buffer ( $2^2$  elements) only accesses to **C** are reused, the elements of **A** are reused when the buffer increases to  $2^{10}$  elements.

```
for(i=0; i<Bi; i++){
  for(j=0; j<Bj; j++){
    for(k=0; k<Bk; k++){
      C[i][j] += A[i][k] * B[k][j];
    } } }
```

**Listing 5.1:** Nested loop code description of a matrix multiplication kernel as a running example.

By loop interchange, loop **i** can be positioned as inner loop, so reuse of **B** is exploited. However, Figure 5.3 shows that an interchange does not improve but worsens the total amount of data reuse, since it removed the reuse in array **A** and **C**. One could better perform tiling of loop **j** with factor  $T_j=4$ , as a result the reuse distance of **A** is reduced to  $2^4$  entries. Tiling can also be performed in other directions and with different factors. Listing~2 demonstrates tiling in all three dimensions. Further experiments with different tile factors on multiple loops, reveal that obtaining the best configuration for a buffer size is a very intricate problem. Even worse is the huge difference in data transfers for different configurations, i.e. the design space is very chaotic. For example, loop tiling with  $T_i=16$  and  $T_j=16$  gives excellent results for a buffer size of  $2^9$ , but for  $2^8$  it is one of the worst schedules. If the designer could find the best schedules a huge reduction in the number of communications could be achieved, at the cost of a modest amount of buffer area.

```
for(ii=0; ii<Bi; ii+=Ti){
  for(jj=0; jj<Bj; jj+=Tj){
    for(kk=0; kk<Bk; kk+=Tk){
      for(i=ii; i<ii+Ti; i++){
        for(j=jj; j<jj+Tj; j++){
          for(k=kk; k<kk+Tk; k++){
            C[i][j] += A[i][k] * B[k][j];
          } } } } } }
```

**Listing 5.2:** Loop tiling to transfer parts of loop **i**, **j**, and **k** to the inner loop.

## 5.4 Modelling the scheduling space

To obtain the best tiling and interchange transformations for a loop nest we formulate an optimization problem. This starts with the derivation of a cost function that represents the number of external transfers. In addition, a bounding function is used to limit the required buffer size.

### 5.4.1 Modelling intra-tile reuse

For the cost function we assume that a loop nest is split into two parts; an inner part (zero or more loops) for execution on the accelerator, and an outer part that runs on a host processor. The outer part facilitates the data transfer between the external memory and the accelerator. The inner part uses this data to perform computations, which results in partial or finished output results that are transferred back to the host. *Our cost function represents the number of transfers to and from accelerator.* For the loop nest in Listing 5.2 the cost function is given below:

$$N_{\text{tiles}}(\text{datatransfer}/\text{tile}) = \left\lceil \frac{B_i}{T_i} \right\rceil \left\lceil \frac{B_j}{T_j} \right\rceil \left\lceil \frac{B_k}{T_k} \right\rceil (2T_i T_j + T_i T_k + T_k T_j) \quad (5.1)$$

The first part of equation (5.1) models the *number of tiles* by dividing the domain of each loop by the corresponding tile factor. By ceiling the number of tiles the required padding values for tile factors that are no divisor of the bound are automatically taken into account. This ensures that our cost function favors tile factors that result in minimal padding of tiles, since padding values are counted as extra transfers. Alternatively, we could implement another check on the inner loop containing an expensive MIN/MAX operator to handle the border tiles differently. In this case no padding is required at the cost of more complex tile operator control. General purpose x86 optimization frameworks like Pluto [9] and POCC [111] use the later strategy since. However, we use padding of tiles since it results in more regular accelerator code, which is good for throughput and energy.

The second part of equation (5.1) represents the *data transfers per tile*. Depending on the loop body it contains multiple terms that count the unique array references for reading/writing that depends on the tile size. The term  $2T_i T_j$  models reads and writes to array **C**. Array **A** is only read in code Listing 5.2, so the communication volume is modeled by  $T_i T_k$ . Accesses to array **B** are very similar to array **A**, only the loop iterators that access elements are different  $T_k T_j$ .

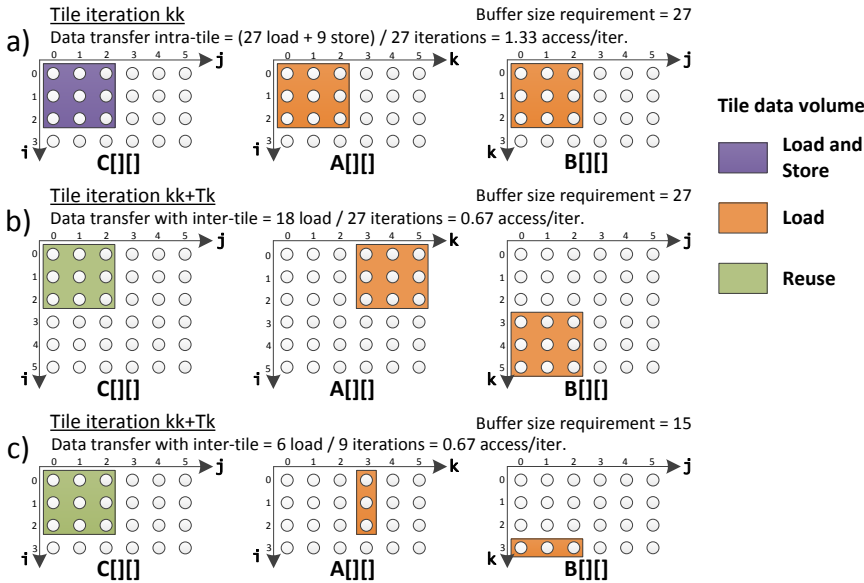
Tile factors should fit in a local buffer, otherwise the reuse cannot be utilized. Valid tile factors are obtained by using a buffer requirement model as a constraint. The buffer requirement is modeled as the number of distinct array elements accessed in an inner tile. For Listing 5.2 this results in expression (5.2). The selected tile factors with their array indices select the data volume of the inner tile.

$$T_i T_j + T_i T_k + T_k T_j \leq [\text{Buffer size}] \quad (5.2)$$

### 5.4.2 Adding inter-tile reuse to the model

For simple accelerators that overwrite all buffer content after processing a tile, the *intra-tile* reuse model described in Section 5.4.1 is correct. However, much





**Figure 5.4:** Data access pattern for matrix multiplication based on code Listing 5.2. a) Demonstrates the data transfer for *intra-tile* reuse in which all accessed elements must be transferred. b) Demonstrates the  $2\times$  data transfer reduction when *inter-tile* reuse is exploited. All elements of  $C$  can be reused over successive tiles, which saves a load and a store communication. c) Reducing the tile size in the dimension of loop  $k$  results in equal communication with a smaller buffer capacity constraint.

more reuse can be utilized if the *inter-tile* reuse is taken into account. For *inter-tile* we should exploit knowledge about the contents of the next tile. This increases complexity, since the first tile (prolog) of a series must perform initialization. The successive tiles (steady-state) should only load new data content and store this over old unnecessary data, exploiting the data overlap. Furthermore, dependencies are created between successive tiles that reduce inter-tile parallelism. Nevertheless, inter-tile reuse can substantially reduce data transfer, which is a key issue affecting the performance of many applications.

Figure 5.4a depicts an example that visualizes data transfer for matrix multiplication. Optimizing for intra-tile reuse with a buffer size constraint of 32 elements result in tile factors  $T_i=3$ ,  $T_j=3$ ,  $T_k=3$ . Without *inter-tile* reuse the host would send 27 values ( $3\times 3$  patch of  $A$ ,  $B$ , and  $C$ ), and receive 9 values ( $3\times 3$  patch of  $C$ ) for every tile. However, if data overlap of successive tiles is exploited, only 18 values ( $3\times 3$  patch of  $A$  and  $B$ ) are transferred in the steady-state tiles. As depicted in Figure 5.4b the data of  $C$  can be reused. Hence, data transfer for all steady-state tiles is reduced by a factor two.

The cost function of Section 5.4.1 does not take *inter-tile* reuse into account, so tile factors and loop interchanges are suboptimal regarding data transfer. The key observation that opens opportunities to find even better schedules is that tiling of the inner control loop does not influence *inter-tile* reuse. For example,

if  $T_k=1$  as in Figure 5.4c the number of accesses per compute iteration does not change, but the memory footprint reduces. As a result, not tiling the inner control loop opens opportunities in other dimensions to increase reuse. To include the effects of *inter-tile* reuse our transfer model in expression (5.1) can be used. However, the full range of the inner control loop should be modeled as a single tile or a *tile strip*. In a tile strip the transfers of the prolog, steady-state, and epilog are all included. Equation (5.3) shows the updated tile strip data transfer model with  $\mathbf{k}\mathbf{k}$  as inner control loop. Note that for each inner control loop (e.g.,  $\mathbf{i}\mathbf{i}$ ,  $\mathbf{j}\mathbf{j}$ , and  $\mathbf{k}\mathbf{k}$ ) there is a different tile strip model.

$$\begin{aligned} N_{\text{tiles}}(\text{datatransfer}/\text{tile}) &= \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor \left\lfloor \frac{B_k}{B_k} \right\rfloor (2T_i T_j + T_i B_k + B_k T_j) \\ &= \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor (2T_i T_j + T_i B_k + B_k T_j) \end{aligned} \quad (5.3)$$

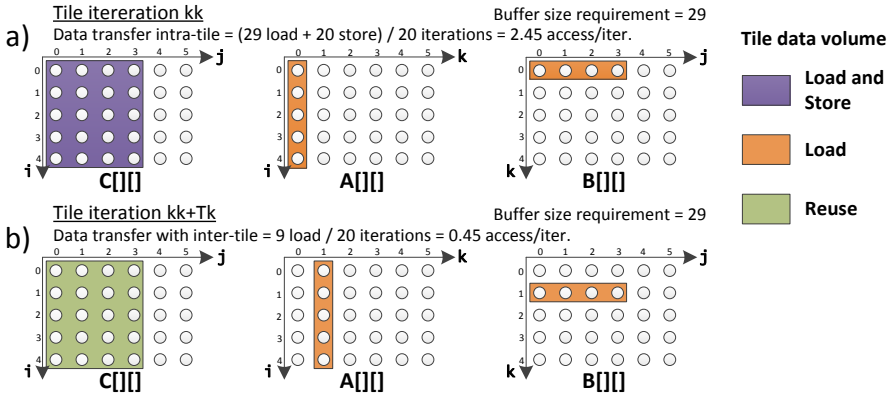
Equation (5.3) can be derived from the *intra-tile* data transfer expression (5.1) by subtracting the *inter-tile* reuses in a strip. *Inter-tile* reuses of  $\mathbf{C}$  occur between the first load and the final store in a sequence of small tiles of control loop  $\mathbf{k}\mathbf{k}$ . As a result, the reuses should be subtracted as demonstrated in expression (5.4).

$$\begin{aligned} &\left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor \left\lfloor \frac{B_k}{T_k} \right\rfloor (2T_i T_j + T_i T_k + T_k T_j) - \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor \left( \left\lfloor \frac{B_k}{T_k} \right\rfloor - 1 \right) 2T_i T_j \\ &= \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor \left\lfloor \frac{B_k}{T_k} \right\rfloor (T_i T_k + T_k T_j) + \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor 2T_i T_j \\ &= \left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_j}{T_j} \right\rfloor \left( 2T_i T_j + \left\lfloor \frac{B_k}{T_k} \right\rfloor T_i T_k + \left\lfloor \frac{B_k}{T_k} \right\rfloor T_k T_j \right) \end{aligned} \quad (5.4)$$

When  $B_k$  is a multiple of  $T_k$  equation (5.4) is can be simplified into (5.3), which shows that the size of  $T_k$  does not influence the communication volume. However, to create space in the buffer size constraint of equation (5.2)  $T_k$  should be minimized, so  $T_i$ , and  $T_j$  can be maximized. In other words, one dimension of the loop nest gets all reuse for free.

A different inner control loop for the *tile strip* influences the amount of data overlap between successive tiles. In the example of Listing 5.2 the inner control loop is  $\mathbf{k}\mathbf{k}$ . Hence,  $\mathbf{C}[\mathbf{i}][\mathbf{j}]$  is reused and the send and receive transfers for array  $\mathbf{C}$  are minimized. By loop interchange  $\mathbf{j}\mathbf{j}$  becomes the inner control loop, and instead send transfers for array  $\mathbf{A}$  are minimized. The corresponding model is given in equation (5.5). For complete evaluation of the solution space each possible inner control direction is modeled separately.

$$\left\lfloor \frac{B_i}{T_i} \right\rfloor \left\lfloor \frac{B_k}{T_k} \right\rfloor (2T_i B_j + T_i T_k + T_k B_j) \quad (5.5)$$

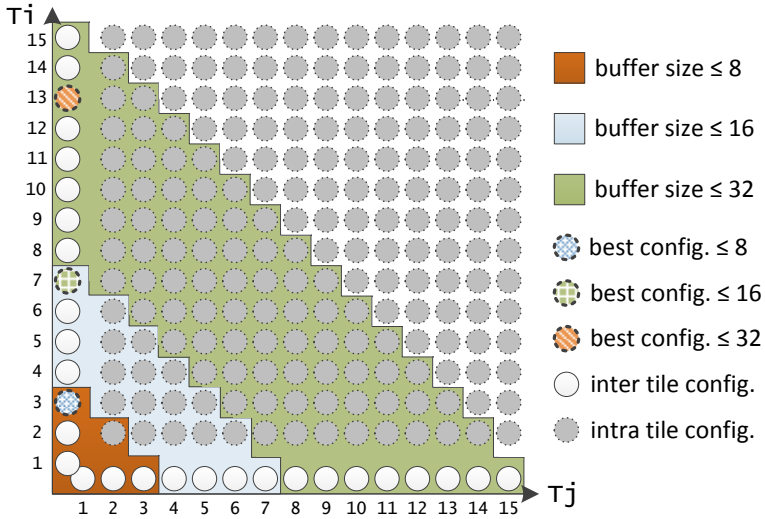


**Figure 5.5:** Inter-tile optimized data access patterns for matrix multiply. a) The data communication volume of intra-tile is larger compared to the schedules of Figure 5.4a. b) Communication volume for inter-tile reuse is less than in Figure 5.4b. With a buffer size constraint of 32 elements inter-tile reuse optimization with tile factor  $T_k=1$  utilizes the most data reuse.

With *inter-tile* data reuse models it is possible to obtain schedules that require less accelerator communication. In Figure 5.5a the best schedule for matrix multiplication with a buffer size constraint of 32 elements is visualized. The inner control loop is  $kk$ , and the tile factors are  $T_i=5$ ,  $T_j=4$ , and  $T_k=1$ . Similar to Figure 5.4a it outlines the communication requirement for only *intra-tile* reuse. As expected, considering *intra-tile* reuse the new schedule performs much worse. However, if we compare the data transfer requirement with *inter-tile* reuse a reduction of 1.48 times per compute iteration is achieved over the schedule of Figure 5.4c. As demonstrated by this matrix multiplication example, the effects of *inter-tile* reuse must be taken into account when optimizing the iteration order. If not, a sub-optimal solution will be obtained.

## 5.5 Scheduling space exploration

When considering valid transformations such as loop interchange and tiling on deep nested loops the scheduling space can be huge, as shown in Section 5.3. We use the models proposed in Section 5.4 to obtain the best schedules, and this will take only seconds instead of hours or days as reported by other search methods [112,117]. This target is achieved by using analytical models that can be evaluated quickly. Additionally, *inter-tile* reuse optimization prunes the search space by evaluating *tile strips* instead of all combinations of tile factors. Our scheduling approach is outlined by a simple 1D-convolution kernel, see Listing 5.3. This code example demonstrates the modeling of convolution access patterns as required for array reference  $X[\mathbf{i}+\mathbf{j}]$ . Basically convolutional nets have the same inner operator where  $X[\mathbf{i}+\mathbf{j}]$  is an input featuremap,  $H[\mathbf{j}]$  the weights, and  $\text{Out}[\mathbf{i}]$  the



**Figure 5.6:** Design space for tiling configurations on the convolution code in Listing 5.3. Each axis represents a possible tile factor as parameter. For inter-tile reuse optimization one of the tile factors is fixed to one, which prunes the space. Two options remain  $T_i=1$  or  $T_j=1$  the other free parameter is optimized. The best configuration given a buffer size, is not always located on the border as shown for a buffer constraint of 32 elements.

neuron results. Extending this example to the 2-d access patterns in a ConvNet is straightforward. The loop bounds in the example nesting are  $B_i=50$  and  $B_j=100$ .

```

for(i=0; i<Bi; i++){
  for(j=0; j<Bj; j++){
    Out[i] += X[i+j] * H[j];
  }
}

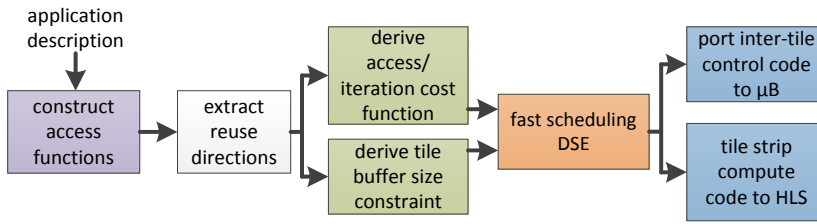
```

**Listing 5.3:** Nested loop code example for 1d-convolution.

For *intra-tile* optimization different tiling factors should be explored e.g., combinations of  $T_i$  for loop  $i$ , and  $T_j$  for loop  $j$  that fit the constraints. The search space for this problem is depicted in Figure 5.6. However, for *inter-tile* optimization the search space is much smaller. One loop e.g.  $i$  is selected as inner control loop and for the other loop  $j$ , tile sizes are evaluated. In addition, this is evaluated for the other option with  $j$  as control loop. Effectively one dimension of the search space is removed. The corresponding cost functions are given in equation (5.6), and the buffer size constraint is given in equation (5.7).

$$\text{Cost} = \begin{cases} \left\lceil \frac{B_i}{T_i} \right\rceil (2T_i + (T_i + B_j - 1) + B_j), & T_j = 1 \\ \left\lceil \frac{B_j}{T_j} \right\rceil (2B_i + (B_i + T_j - 1) + T_j), & T_i = 1 \end{cases} \quad (5.6)$$

$$T_i + (T_i + T_j - 1) + T_j \leq [\text{Buffer size}] \quad (5.7)$$



**Figure 5.7:** Design space exploration flow for inter-tile optimized accelerator development.

The search for the best configuration is performed by a bounded search through the valid solution space. Since the buffer size requirement function is monotonic, the bounds on the valid solution space can be efficiently set with the guarantee that optimal solutions are obtained. This search method is visualized in Figure 5.6. Important to note is the short search time that is required to obtain the best schedules for very deep nested loops. On a standard laptop the search space for an 8-level deep loop nest for motion estimation is explored in 4.2 seconds, with a buffer size constraint of 1024 elements.

## 5.6 Implementation demonstrator

An optimized schedule should be converted to host processor code and an HLS accelerator description according to the steps outlined in Figure 5.7. The required conversions are described by our educational matrix multiplication example for a buffer size constraint of 32 entries. The optimal schedule derived from Listing 5.2 and inter-tile reuse optimization has tiling parameters  $T_i=5$ ,  $T_j=4$ , and the inner control loop is  $kk$ . The resulting data access pattern is depicted in Figure 5.5b.

The host processor code executes the outer control loops, and performs data transfer of tiles between host and accelerator, see Figure 5.8 for a graphical illustration of the communication. Basically, the outer control loops of Listing 5.2 are used. Furthermore, the prolog and epilog parts are inserted, which transfer input data and output results, respectively. Finally, the inner control loop is inserted, which transfers the steady-state data chunks. In Listing 5.4, a description of the host code is given. Note that the Send and Receive functions facilitate FIFO based communication. For the connection between the host and accelerator we use the Fast Simplex Links (FSLs) from Xilinx.

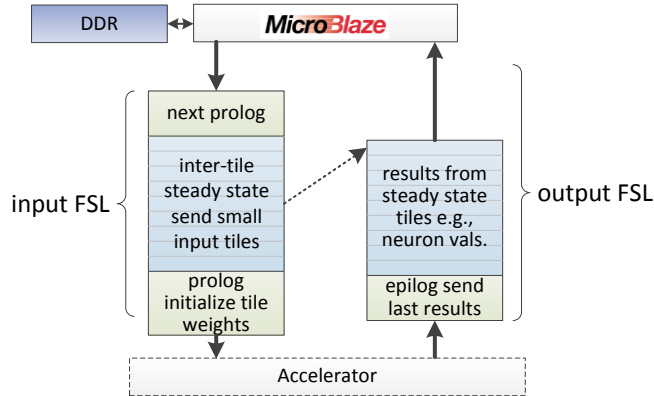


Figure 5.8: Schematic overview of the pipelined communication stream to an accelerator.

```

for(ii=0; ii<Bi; ii+=Ti){
  for(jj=0; jj<Bj; jj+=Tj){
    //prolog part nothing to send
    for(k=0; k<Bk; k++){ //steady state
      Send(A[ii:ii+Ti-1][k]);
      Send(B[k][jj:jj+Tj-1]);
    }
    //epilog part receive results
    Receive(C[ii:ii+Ti-1][jj:jj+Tj-1]);
  } }

```

Listing 5.4: Host processor code that corresponds to the matrix multiply example in Listing 5.2. This code performs data transfer by executing the outer control loops.

The accelerator code performs the content of the tiles, which is the main compute workload. It has no notion of the position in the program; it just repeats execution of streams with overlapping tiles. Furthermore, it describes the load/store policy in the local buffers. The prolog and epilog parts are specified, and in addition the steady state inner control loop is inserted. This last part contains a data transfer and a compute part. If required, the compute part can be parallelized by adding HLS specific pragmas for pipelining or unrolling [154]. Listing 5.5 shows the accelerator code:

```

Init(C[0:Ti-1][0:Tj-1]); //prolog
for (k=0; k<Bk; k++){ //steady state
  Receive(A[0:Ti-1]);
  Receive(B[0:Tj-1]);
  for(i=0; i<Ti; i++){
    for(j=0; j<Tj; j++){
      C[i][j]+=A[i]*B[j];
    } } }
Send(C[0:Ti-1][0:Tj-1]); //epilog return results

```

Listing 5.5: Accelerator code, which computes on incoming data by executing inner loops of the matrix multiply example

## 5.7 Evaluation methodology

To evaluate the effectiveness of inter-tile reuse optimization for dedicated accelerators, we study a representative set of real-world applications. Our study will first look at the number of data transfers for different memory sizes. For this our analytical modeling framework is used to compute the number of external accelerator communications.

To analyze the effect of communication reduction real mappings of the applications are done. Firstly on fixed platforms to set a baseline execution time score. Secondly, these mappings are performed for dedicated accelerators connected to an embedded MicroBlaze core to demonstrate the impressive performance of inter-tile optimized accelerators.

### 5.7.1 Benchmark applications

Our first focus is the workload in Convolutional Networks (ConvNets). However, the inter-tile optimization method is much broader applicable, so we include a few applications from the image and video processing domain with extensive data transfer requirements. As outlined these applications should contain loops nests that can be written as static affine loops, and these should represent the major compute workload. A short overview of the applications is given below and in addition their sources are made available on the web<sup>5</sup>.

#### Convolutional network

ConvNets should be used for state-of-the-art object detection and recognition, e.g. face detection in photo cameras [53], and speed sign recognition in portable navigation devices [105]. To comply with the restricting power budgets in embedded devices fixed function accelerators are an interesting target that could give enough compute throughput. In our evaluation we use the dense speed sign recognition application that's introduced in Chapter 3. More specifically, we use the optimized version with merged feature extraction layers, see Chapter 4. For our benchmarks the application used on a 720p HD video stream.

#### Demosaicing

Camera processing pipelines typically require a demosaicing step, since the red, green, and blue (RGB) channels of the sensor are laid out in a Bayer [3] pattern. A demosaicing algorithm interpolates the two missing color values, at each pixel position. However, interpolation is difficult because the color channels have an inadequate sampling resolution, which causes color artifacts. We use a 5x5 position adaptive interpolation kernel based upon the Malvar-He-Cutler [92]

---

<sup>5</sup> Benchmark sources can be downloaded from: <http://parse.ele.tue.nl/research/locality/>

method. Furthermore, an 8 Mpixel input image is used for realistic data transfer figures.

```

for (y=0; y<By; y++){
  for (x=0; x<Bx; x++){
    for (c=0; c<Bc; c++){
      for (k=0; k<Bk; k++){
        for (l=0; l<Bl; l++){
          Out [y][x][c] += In[y+k][x+l] * W[y&1][x&1][c][k][l];
        } } } } }

```

**Listing 5.6:** Pseudo description of the Malvar method for demosaicing.

### Motion estimation

An important step in video coding is Motion Estimation; since it significantly improves compression, though substantially increasing complexity. In modern coding standards, such as H.264, the Integer Motion Estimation (IME) step represents 78% of the compute workload, and 78% of the memory accesses [19]. We use a full-search block matching kernel with a window of  $32 \times 32$  that searches in a previous and future reference frame for the best matching block, using the Sum of Absolute Differences (SAD) cost function. Furthermore, there are four HD 720p frames between two reference frames that must be encoded by motion vectors. As outlined in Listing 5.7 the algorithm can be described by a very deep loop nest, with reuse opportunities in all dimensions.

```

for (f=0; f<Bf; f++){ // encoded frame nr.
  for (by=0; by< Bby; by++){ // macro block
    for (bx=0; bx< Bbx; bx++){
      min = 65535;
      for (r=0; r<Br; r++){ // reference frame
        for (sy=0; sy< Bsy; sy++){ // search window
          for (sx=0; sx< Bsx; sx++){
            diff = 0;
            for (y=0; y<By; y++){ // block difference
              for (x=0; x<Bx; x++){
                diff += abs(in[f][by,y][bx,x] -
                           ref[r][by,sy,y][bx,sx,x]);
              } }
            if (diff<min){ // update best match
              min = diff;
              vec = (ref<<15)|((sy<<8)|sx);
            } } } }
            idx[f][by][bx] = vec;
          } } }

```

**Listing 5.7:** Pseudo description of Integer Motion Estimation (IME) for a video coding application.



### 5.7.2 Platform and tools

As a baseline reference for evaluation fixed-point implementations of the applications are mapped to three different platforms:

- Intel Core-i7 960 CPU at 3.2GHz
- Arm-A9 CPU at 667MHz, Xilinx Zynq SoC
- MicroBlaze soft core configured for performance, at 200MHz

In addition, our methodology is used to develop hardware accelerators that increase the performance of the MicroBlaze host processor. The designs are synthesized for the Xilinx ML605 board, which has one Virtex-6 FPGA (xc6vlx240t-iffg1156). For development we use the Xilinx Vivado 2012.3 tools, including Vivado HLS (AutoESL), which is used to create accelerators. The clock frequency of our FPGA designs is set to 200 MHz.

## 5.8 Experimental results

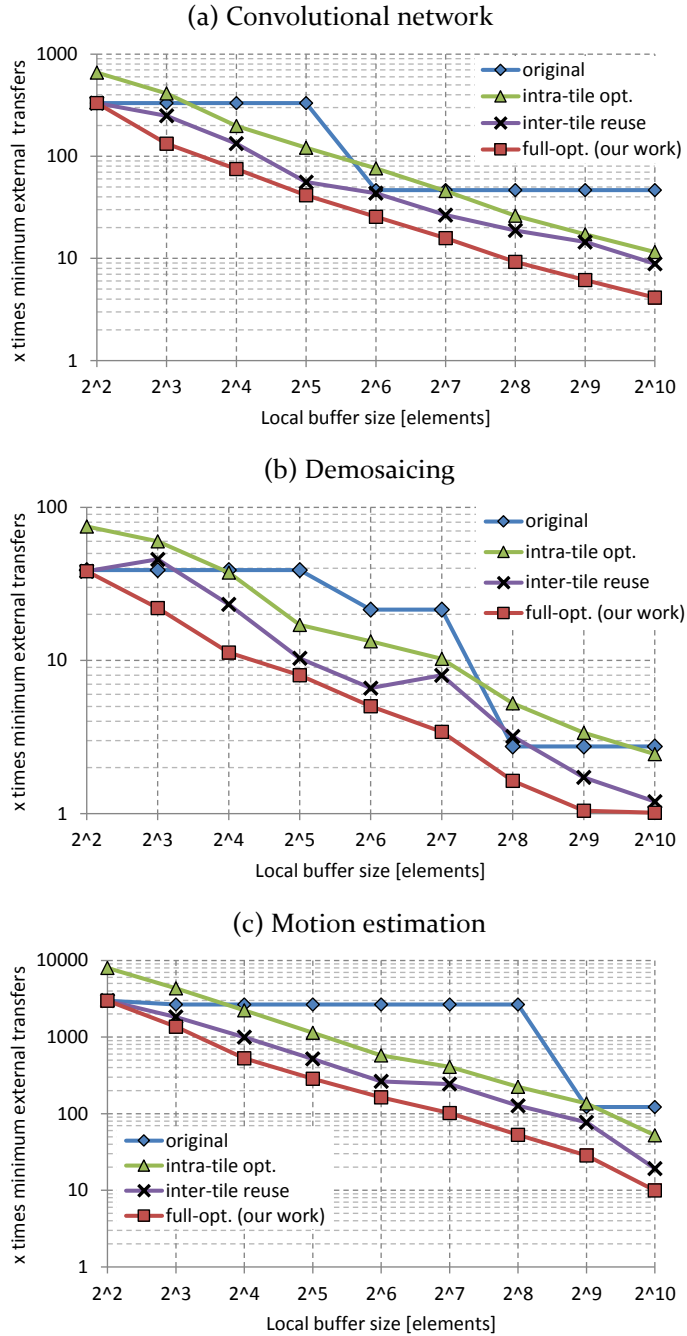
To quantify the effectiveness of inter-tile reuse optimization the number of data transfers for the three benchmark applications computed. For each application the cost functions and buffer size requirements are derived. With these descriptions the scheduling space exploration is performed for different buffer size constraints, as outlined in Section 5.5.

### 5.8.1 Data transfer volume for inter-tile schedules

Figure 5.9 shows the data transfer requirements for the original iteration ordering versus three other optimization strategies. Data transfer is specified as a factor with respect to the theoretical minimum, i.e. communicating each input and final output only once. This can always be achieved with an infinite buffer size. The communication volume is plotted for the required buffer size, which preferably is as small as possible.

Intra-tile optimization shows the result for accelerators that reset all buffer contents after each tile, which is outlined in section 5.4.1. This optimization target does not enforce any ordering between tiles which is good for parallelism; as a result it sometimes gives worse results compared to the original iteration order. If we exploit the available inter-tile reuse for schedules optimized for intra-tile reuse the communication volume is significantly reduced. Finally, the schedule dimensions are optimized for inter-tile reuse, which for all benchmarks results in the smallest communication volume.

Important to note, are the huge data transfer reductions. E.g. in the motion estimation benchmark the best schedule can reduce data transfer up to 50x compared to the original. Furthermore, we demonstrate that a relatively small local buffer of 1024 elements can substantially reduce data transfer. For motion estimation and object recognition the remaining number of transfers is within one order of magnitude of the minimum. However, for demosaicing the minimum is



**Figure 5.9:** External data transfers versus accelerator buffer size. The original loop ordering is compared with: intra-tile schedules; intra-tile schedules where inter-tile reuse is utilized; and full optimization where inter-tile schedule dimensions are optimized.

already reached with a buffer of 512 elements. A designer should stop increasing buffer size after this point, because the amount of data transfer stays constant and it only increases the area footprint.

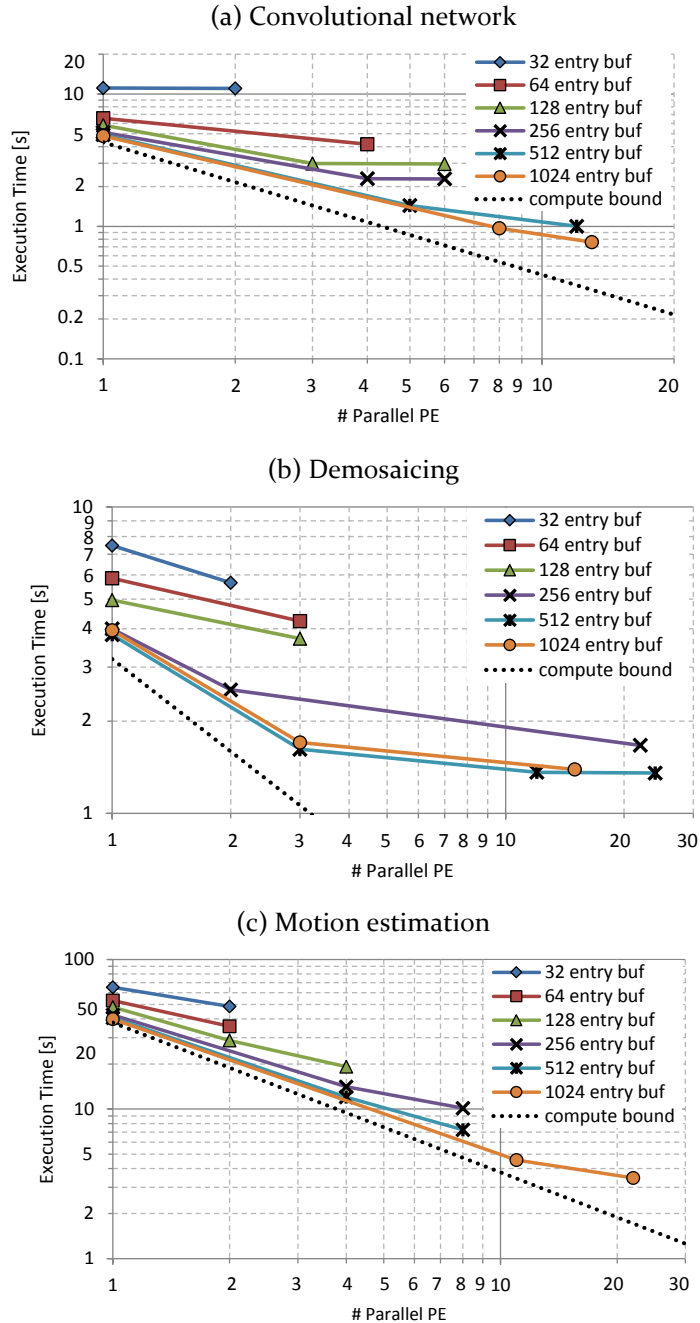
### 5.8.2 Quality of results

As demonstrated, there is a trade-off between buffer size and communication requirements for hardware accelerators. In addition, the amount of compute resources influence the communication requirements. For HLS descriptions this is achieved by unrolling parts of algorithm code. As a result, the data path is replicated to utilize available parallelism, which requires more data to feed the extra compute resources. Figure 5.10 presents execution time measurements for different accelerator configurations. Accelerators with a small buffer (e.g. 32 elements like a register file) are bandwidth limited, so throughput will not scale with extra compute resources.

The quality of implemented accelerator schedules is evaluated by comparing execution time with resource usage. For FPGAs, resource usage is defined as:  $MAX(\%DSPs, \%BRAMs, \%LUTs, \%flip-flops)$ . In Figure 5.11 the execution time versus resource usage is visualized by plotting the design points of figure Figure 5.10. In addition, the area-delay product is used to define the efficiency of different implementations. For each benchmark the best area-delay product is extrapolated and plotted as a dotted line in the comparison.

The results for the ConvNet and Demosaicing application behave intuitive. Designs that are balanced score close to the dotted line, while designs severely limited by either compute or buffer resources occur further from this line. As predicted in Figure 5.9 for Demosaicing increasing the buffer size beyond 512 entries does not improve the design any further. However, for Motion Estimation a few results behave counter intuitive, e.g. increasing parallelism in small data buffer designs can reduce the resource usage. Vivado HLS is a production tool, and therefore a small change in the input description can trigger different optimizations. Due to unrolling with a factor two the number of required LUTs in the 32 and 64 entry designs are reduced, which reduces overall resource usage and the area delay product.

Finally, the best accelerators are compared with other platforms, as shown in Table 5.1. These accelerators do not have a dedicated DMA controller, which severely constraints the available communication bandwidth. However our inter-tile accelerators can increase the original MicroBlaze performance by 16 to 82 times, at the cost of a very small increase of overall resource usage. Hence simple embedded processors can perform on par with a high-end general purpose processor. Dedicated DMA can be added, but it will only shift the result of Figure 5.11.



**Figure 5.10:** Execution time scaling for different buffer size optimized accelerators. Parallelism is increased by unrolling in the HLS compute code. The dotted line represents the ideal execution time assuming no data transfer time. As Figure 5.9 predicted, demosaicing exploits all available reuse with a 512 entry buffer.

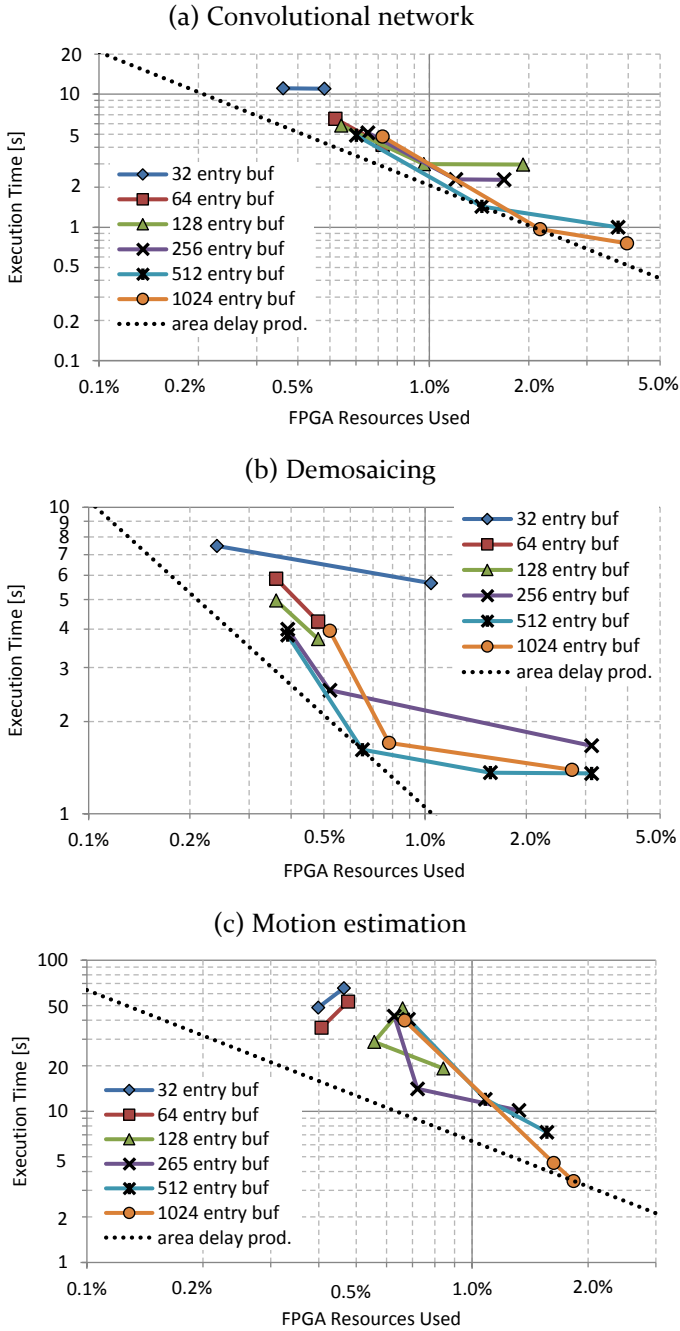


Figure 5.11: FPGA resource utilization for accelerator mappings with an inter-tile iteration order. The best area delay product is selected as most efficient solution and extrapolated by the dotted line.

Platform	Demosaic [s]	Block Match [s]	ConvNet [s]
Intel-i7	0.54	8.12	0.63
Arm-A9	5.75	72.32	5.92
MicroBlaze	22.10	283.96	19.05
Accelerator	1.36	3.45	0.75

**Table 5.1:** Execution time comparison for multiple platforms.

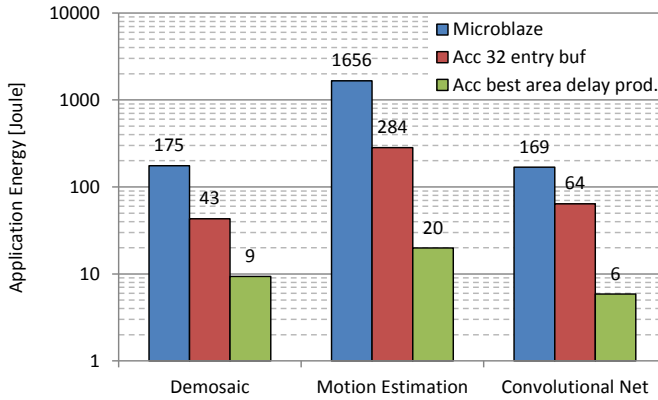
### 5.8.3 Energy consumption

In the previous section throughput and resource utilization are evaluated. Another key parameter for embedded systems is energy efficiency. Energy consumption is evaluated by FPGA bit toggling simulations for the real applications. To measure bit toggling during application runtime the Xilinx ISIM simulator is used. This simulator performs a behavioural simulation of the MicroBlaze core including connected peripherals like the Memory Interface Controller (MIC), or dedicated accelerators. Due to the excessive simulation time of such large systems only 1 ms of the real workload (the initialization part is not recorded) is recorded in a Switching Activity Interchange Format (SAIF) file.

The Xilinx XPower tools combine the SAIF file with the placed and routed design to estimate the FPGA power usage. For a complete power figure we included the activity of the external DDR3 memory module. This is performed by recording the output of the Xilinx soft-core memory controller, and feed the memory command sequence to a DDR3 memory energy estimator [17].

The estimated system power consumption during 1 ms of effective workload is extrapolated to the run time of each complete application. Figure 5.12 presents the energy consumption to run each complete application for the different mappings. These figures demonstrate that even the very small accelerators with 32 buffer entries can substantially improve energy efficiency, factors of 2.5 up to 5.8 better efficiency are shown. However, if data transfer is reduced aggressively by using the best area delay product mappings energy efficiency increases by 18 to 82 times compared to the MicroBlaze mapping.

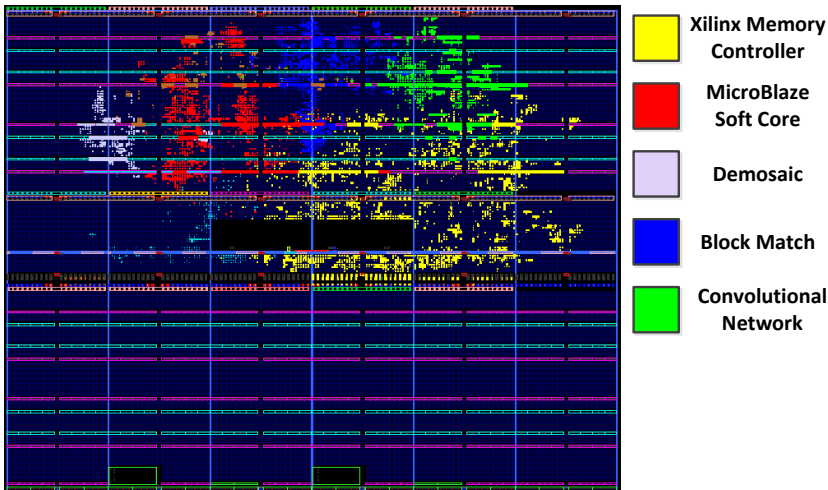
The huge energy efficiency improvement is mainly caused by execution time reduction, since dynamic power usage changes only by a small amount. The exact power figures are outlined in Table 5.2, which reveals that the major portion of power consumption is static. This is mainly due to large design area used for the Memory Interface Controller and the MicroBlaze core, see Figure 5.13. These results indicate that the addition of the relatively small accelerators does not increase power usage significantly. In addition, though the use of efficient data reuse in local buffers the data movement does not increase. The relatively small accelerators and optimized data reuse schedules do not increase power usage, but they reduce execution time tremendously which gives a boost to energy efficiency. Although energy efficiency improved a lot, the energy per effective operation is still 1 to 7 nJ depending on the application data reuse. For smartphone or wearable scenarios this is a good step forward, but not enough. These use cases require one or two orders of magnitude efficiency improvement.



**Figure 5.12:** Full application energy consumption for three mappings: MicroBlaze only; Accelerator with 32 buffer entries; And the accelerator with the best area delay product.

Application	Mapping	Dynamic	Static	DDR <sub>3</sub>	Total Power	Joule/op.
Demosaic	MB	2438 mW	3092 mW	310 mW	5841 mW	138 nj/op
	acc 32	2420 mW	3092 mW	312 mW	5823 mW	34 nj/op
	acc 512	2427 mW	3092 mW	317 mW	5836 mW	7 nj/op
Motion Est.	MB	2426 mW	3092 mW	313 mW	5832 mW	109 nj/op
	acc 32	2395 mW	3091 mW	311 mW	5797 mW	19 nj/op
	acc 1024	2439 mW	3092 mW	311 mW	5843 mW	1 nj/op
ConvNet	MB	2413 mW	3092 mW	310 mW	5841 mW	98 nj/op
	acc 32	2417 mW	3092 mW	313 mW	5822 mW	37 nj/op
	acc 1024	2445 mW	3093 mW	317 mW	5854 mW	3 nj/op

**Table 5.2:** Platform power usage and energy efficiency overview.



**Figure 5.13:** FPGA mapping of the SoC, a MicroBlaze core equipped with the three best area delay product accelerators. The three accelerators occupy only 7.4% of the available FPGA resources. The resources in red and yellow are used for the MicroBlaze and the DDR memory controller respectively; combined these consume 9.8% of FPGA resources.

## 5.9 Conclusions

In this Chapter we presented our new inter-tile reuse optimization strategy for nested loop accelerators. This optimization strategy searches the best combination of loop interchange and tiling with optimal tile sizes. We demonstrated that maximizing efficiency for local buffers in FPGA based accelerators gives a substantial performance improvement. These improvements are enabled by efficiently exploiting local buffering with data access optimizations for nested loops. Our optimizations manage to limit buffering requirements while achieving a significant reduction of external data transfer. The main improvement is achieved by optimizing for inter-tile reuse. Although the design space can be huge and chaotic for deeply nested loops, we show that the best configuration of transformations can be found with a model-based approach. Our focus on inter-tile reuse effectively prunes the search space of configurations, and limits the effort of exploration to mere seconds. The fruits of our optimizations are verified with the Xilinx Vivado HLS tools, and we observe a significant reduction in the effort of designing efficient dedicated accelerators. With our approach the number of required design iterations is minimized, by directly computing the best candidates before time consuming synthesis. As a result, the mapping process of static image or video processing applications to dedicated hardware accelerators is much better manageable.



# CHAPTER 6.

## NVE: A FLEXIBLE ACCELERATOR

*As outlined in the earlier chapters Convolutional Networks (ConvNets) enable record breaking classification performance for many daily tasks. However the associated demands on computation and data transfer prohibit straightforward adoption by energy constrained wearable consumer platforms. The computational burden can be overcome by dedicated hardware accelerators, but it is the sheer amount of data transfer, and level of utilization that largely determines the energy-efficiency of such implementations. This chapter presents the Neuro Vector Engine (NVE) a SIMD accelerator template for ConvNet based vision applications, targeting the consumer market, in particular the ultra-low power wearable devices. The NVE is very flexible due to the use of a VLIW ISA, which comes at the cost of instruction fetch overhead. We demonstrate that this overhead is insignificant when the flexibility enables advanced data locality optimizations from the previous chapters. In addition, our flexibility ensures an excellent hardware utilization for different ConvNet vision applications. By co-optimizing accelerator architecture and applying the inter-tile reuse optimization methodology, 30 Gops is achieved within a power envelope of 54 mW and only 0.26 mm<sup>2</sup> silicon footprint in TSMC 40 nm technology. These performance numbers enable high-end visual object recognition by portable and even wearable devices.*

*This chapter is based on work presented at DATE 2016 [109].*

---

### 6.1 Introduction

Although Convolutional Networks (ConvNets) achieve superior results for machine vision, they lack an attribute crucial for mobile and wearable applications, and that is energy-efficiency. The rather large computational workload and data intensity has motivated optimized implementations on CPUs [18], GPUs [28] and FPGAs [108,155]. All these implementations do not fit the very constrained (less

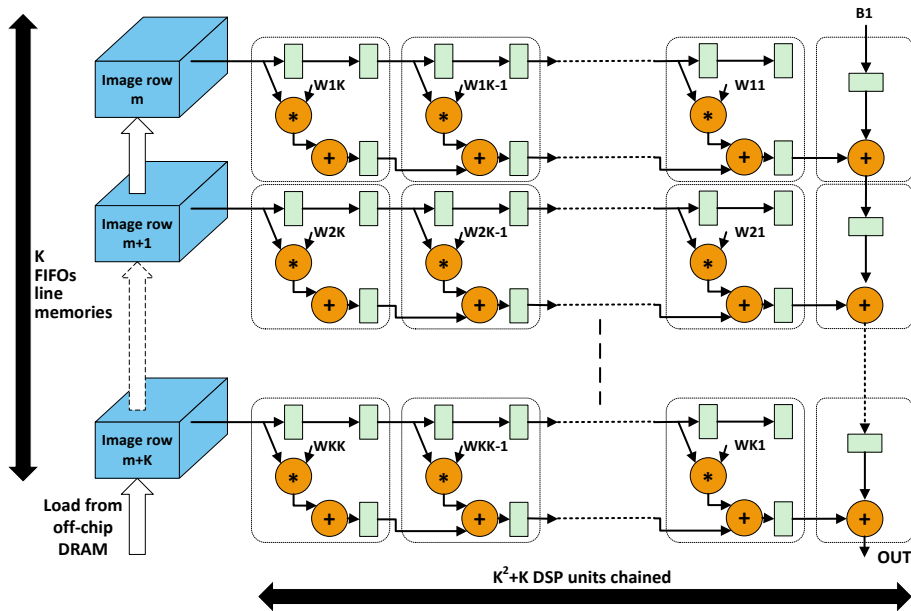
than 1 Watt) mobile power budget. In Chapter 5 we demonstrated with dedicated FPGA accelerators that it is very challenging to reach the sub 1 Watt target while achieving sufficient compute performance. Although FPGAs have the flexibility to reprogram the data path their operators simply consume too much energy compared to their ASIC counterparts. On the other hand, instruction based CPUs or GPUs spend way too much energy on non-compute related control structures, e.g. instruction fetch, decode, pipeline management, program sequencing, etc.

The computer architecture community is well aware of the trend towards heterogeneous computing where architecture specialization is used to achieve high performance at low energy [58]. A few research groups use the customization paradigm to design highly specialized hardware accelerators that could enable excellent machine vision for mobile devices [16,50,20]. The main challenge in accelerator design is to reconcile architecture specialization and flexibility. Especially, the right level of flexibility is key for the energy-efficiency of an accelerator. ConvNets have many parameters such as the layers, feature maps, and kernels, which are different for every task. Hence the architecture should support different parameters efficiently, and on the other hand data storage structures should be tuned to the data-flow and data-locality requirements. Earlier works focused on this last aspect by focusing on efficiently implementing the compute primitives. However, by adding more flexibility we demonstrate an additional efficiency improvement that is counter intuitive, but crucial for real-world ConvNet vision applications.

In this chapter we present the Neuro Vector Engine (NVE), an ultra-efficient accelerator template for ConvNet based vision applications. The design builds on efficient SIMD operations that focus on data reuse opportunities by employing a local scratchpad buffer. The VLIW ISA enables a very high utilization; real-world benchmarks demonstrate an excellent silicon area efficiency (performance/area = 115 Gops/mm<sup>2</sup>). In addition, the VLIW ISA enables advanced data locality optimizations that increase energy efficiency tremendously (performance/power = 559 Gops/W). Our main contributions are:

- A new ultra-low power accelerator template for ConvNets.
- The first extremely flexible ConvNet accelerator with full VLIW compiler support.
- Extensive evaluation of the architectural design involving data movement analysis due to the inter-tile data locality optimization.
- Detailed comparison with a low-power ARM-A9 core and an embedded NVIDIA TK1 GPU.

First, Section 6.2 gives an overview of related work. Next in Section 6.3 the inefficiencies of general purpose CPUs are analyzed. In Section 6.4 these inefficiencies are addressed by the NVE architecture. Section 6.5 presents an in depth evaluation of the NVE architecture. Section 6.6 will evaluate different instances of the template and will discuss limitations and future work. The chapter is finalized with conclusions in Section 6.7.



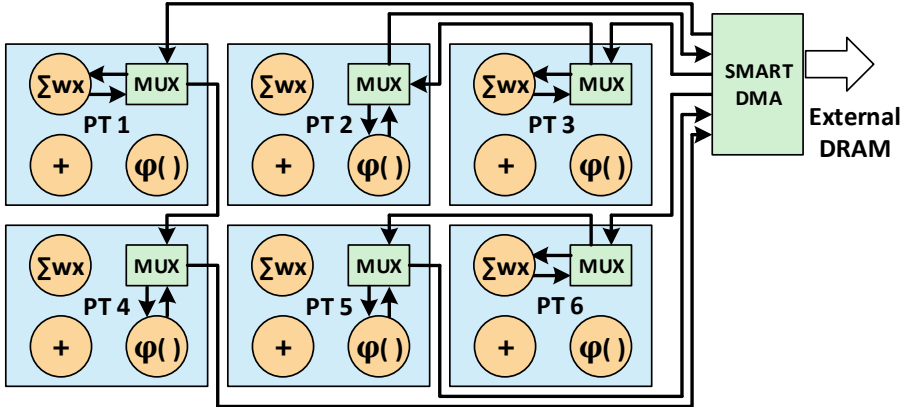
**Figure 6.1:** Architecture of a systolic 2d convolution operation [119]. The systolic structure has a peak throughput of one  $K \times K$  dot product per cycle. For  $K=7$  this results in 49 MACC operations per cycle. For a single 2d convolution all data reuse is exploited.

## 6.2 Related work

The energy constraints on mobile and embedded devices, forces researchers to find solutions that improve efficiency. In this search others have proposed custom accelerator architectures of ConvNets for FPGA or ASIC. In this section we will investigate popular architectures that are proposed in the literature. We will show that most of the work is too specific, i.e. when different networks must be supported the efficiency drops substantially.

Many works focus on a computational operator that implements the filtering part in a ConvNet. Filtering represents 90% of the computational workload, so it is an important part. A systolic implementation seems a natural fit since these structures are very efficient at filtering. Two popular works propose the use of a systolic implementation of a 2D convolution operation [16,50]. Figure 6.1 illustrates the architectural concept of a systolic array for 2D convolution. In this structure the weight coefficient registers  $w_{11}$ - $w_{kk}$  are programmed by a host processor. Next, image lines are streamed in and the outputs are streamed out for a complete output image. No instructions are required only input and output streams and almost all resources are dedicated to the computation.

Although systolic implementations are computationally efficient they have limited flexibility. For example, running the benchmark networks from Chap-

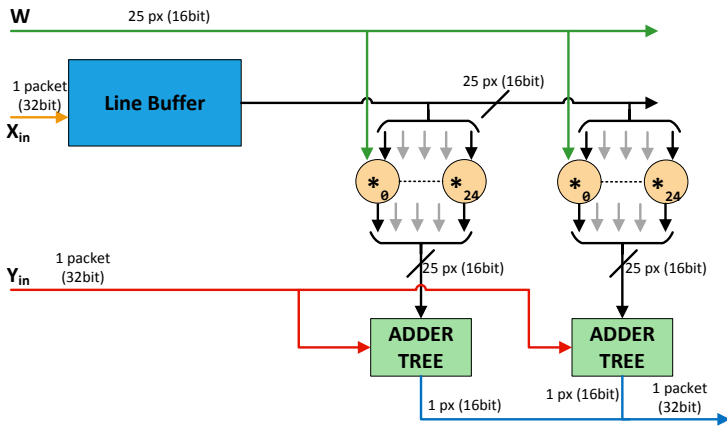


**Figure 6.2:** The tiled organisation of NeuFlow [48] based accelerator core. Processing Tiles (PT) can be configured to implement a dataflow for ConvNet workloads. In this example three feature maps are computed.

ter 3 on this systolic architecture would involve many load/store streams for feature maps. The fixed structure does not exploit data reuse over feature maps. As a result, accelerator architectures that employ systolic convolution structures resort to complex arbitration logic to share input streams, e.g. in [16] they use energy hungry multi-channel memory controllers to meet the huge memory bandwidth requirements.

The NeuFlow [50] processor in Figure 6.2 uses systolic arrays organized in processing tiles (PTs) to create a dataflow processor. This creates the flexibility to reuse incoming data streams. However, for many ConvNet configurations processing tiles will be underutilized, e.g. in the illustrated configuration three of the systolic arrays PT(2, 4, and 6) are disabled. Secondly, a systolic array has limited flexibility to cope with varying convolution kernel sizes. A  $7 \times 7$  array can be used to compute  $3 \times 3$  convolutions, but only 18% of the MACC units are utilized in this scenario. We conclude that systolic convolution structures are extremely efficient but do not offer enough flexibility to execute different ConvNet workloads with a good utilization. As a result, for nets with different parameter settings NeuFlow is inefficient, i.e. low silicon and energy efficiency.

A more flexible but similar accelerator is presented in [37] where Hardware Convolution Engines (HWCE) implement a dedicated dot product operation. Figure 6.3 illustrates the data path architecture consisting of line buffers, an array of multipliers, and an adder tree. The HWCEs have programmable control logic and a dedicated weight loader mechanism to quickly change weight sets. This enables the HWCE to perform larger convolutions e.g.  $11 \times 11$  by reloading multiple  $5 \times 5$  convolution windows. This reloading will give a performance penalty but for networks with varying layer workloads this flexibility can improve utilization. The line buffer ensures single feature map locality, but data reuse over feature maps must be solved externally. Pooling and activation function operations are not supported. This results in extra memory transfers to execute



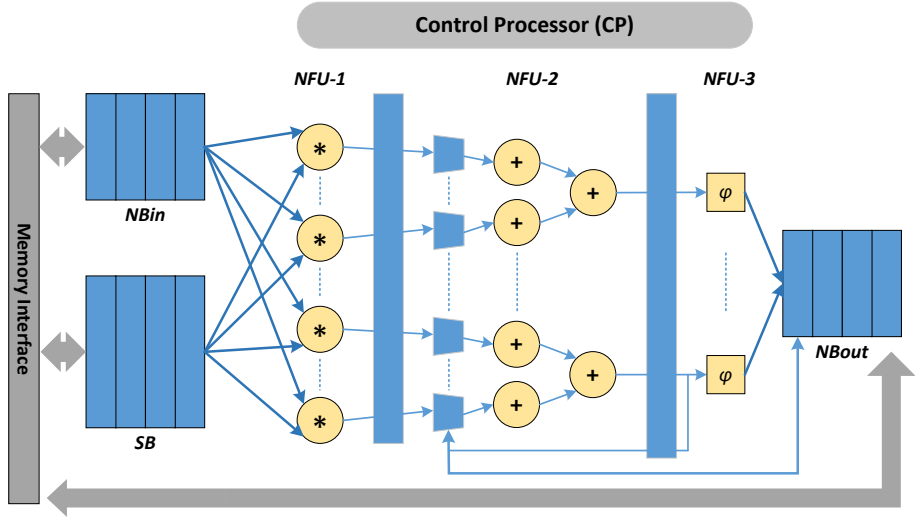
**Figure 6.3:** Hardware Convolution Engine (HWCE) unit, used as accelerator for ConvNets in [36].

these steps in software. The HWCEs are integrated in a multi-core RISC cluster, so moving the missing parts to software is possible but it reduces energy efficiency.

Another important work is DianNao [20], a high-throughput standalone pipelined accelerator core. Similar to the other accelerators DianNao implements a dot product operator, see the pipelined datapath in Figure 6.4. The implemented dot product operator is more configurable compared to other works. The first stage is a multiplier stage, followed by a reduction stage that configures adder trees or implements max pooling operators. The last stage performs activation function interpolation. Multiple multipliers are used to exploit the parallelism over many input feature maps. The rationale is that convolution windows have  $5 \times 5$  sizes where the number of input maps in large networks can run into hundreds. Utilizing parallelism only over input feature maps and not over window operations makes that the input vector is 1d instead of 2d. By repeating the 1d operation for multiple input window positions a convolution window is constructed.

Compared to earlier works DianNao focusses much more on data locality in the reuse buffers. They use separate buffers for synaptic weights (SB), input maps (NBin) and output maps (NBout). These buffers hold vectors with the data elements. The vectors do not exploit reuse over different convolution kernel positions, so unique weights are send out into the data path causing many loads from the SB memory. DianNao focusses on very large networks with many feature maps. However, the face detection workload from Chapter 3 reveals that vision applications can have ConvNets with only few input feature maps per layer. This severely limits the parallelism that can be used by the DianNao accelerator resulting in underutilization.

All these architectures implement a dedicated dot product operator, some in a streaming pipeline others as a configurable operator. For all these accelerators we observe significant flexibility issues. If the network operators are tuned to the



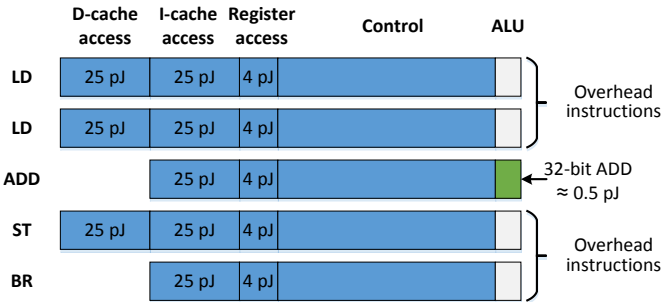
**Figure 6.4:** The pipelined data path of the DianNao accelerator core [19]. Separate memories load vectors for

accelerator data path a good efficiency level can be achieved. However a ConvNet with different parameters results in a substantial reduction of efficiency. The goal of the Neuro Vector Engine is to deliver a constant and high efficiency level on different ConvNets. To achieve a more constant and high efficiency level more control flexibility is necessary. This is a challenging goal, because often this control flexibility results in a reduced efficiency.

### 6.3 Sources of inefficiency in general purpose CPUs

In the previous section we showed the utilization problem for very dedicated accelerator cores. When multiple networks with varying parameters are used the efficiency often drops substantially. To increase accelerator flexibility we study the properties of general purpose CPUs but we try to minimize their excessive inefficiency's.

It is well known in the domain of computer architecture that general-purpose processors spend most energy on instruction control. This definitely holds for advanced out-of-order superscalar designs that consume a lot of energy in the instruction reorder part. The energy consumption of a much simpler RISC processors is also dominated by instruction overheads such as instruction fetch, decode, pipeline management, program sequencing, etc. This energy consumption distribution is extensively studied in [113,58]. Figure 6.5 illustrates the energy distribution for a simple RISC (45 nm @ 0.9V technology) ADD instruction, which consumes about 70 pJ of energy. A load/store type of instruction would use the data cache and increases instruction energy to 95 pJ. The energy dissipa-



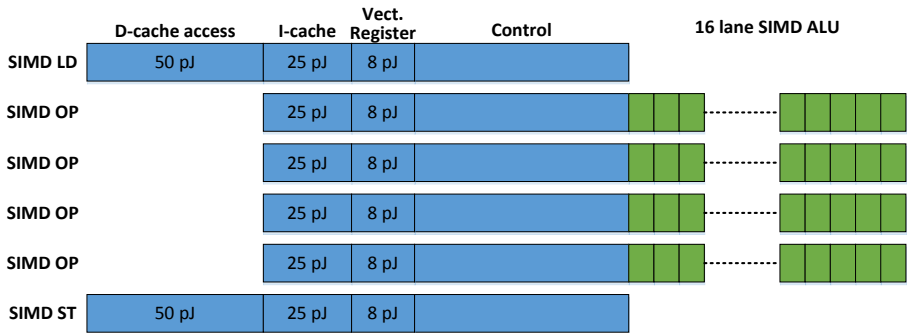
**Figure 6.5:** Instruction energy breakdown for a typical addition loop executed by a 45 nm RISC core at 0.9V [54,107]. Note the very small portion of energy spend on the actual addition. This is an example of the large inefficiencies in general purpose CPUs.

tion in a functional unit to add two 32-bit numbers is only 0.5 pJ. This huge difference in energy consumption demonstrates that the useful fraction of energy in an ADD operation is only  $\frac{1}{140}$ . In practice it is even worse, because such operations are often done in loops that require overhead instructions for loads and branching. Overhead instructions further reduce the useful energy fraction to  $\frac{1}{850}$ . This example clarifies why custom accelerators can be 100 times more efficient than general purpose CPUs, they simply don't need all those instructions.

To use the flexibility of instruction programmed accelerators, but with a much better energy efficiency the overhead should be drastically reduced.

1. Many useful operations should be performed per instruction. This can be achieved by the Single Instruction Multiple Data (SIMD) paradigm. E.g., a 16 element vector ADD could increase the amount of useful work per instruction from  $\frac{1}{140}$  to  $\frac{1}{10}$ , see Figure 6.6.
2. The ratio of useful instructions should be high, so overhead instructions should be minimized. This involves minimizing the number of load/store operations (locality), and replacing them by more efficient vector load/stores. An instruction pattern as depicted in Figure 6.6 improves the loop efficiency from  $\frac{1}{850}$  to  $\frac{1}{18}$ . Note that control instructions like the branch are replaced by a hardware loop counter.

Switching to vector instructions and increasing register level data reuse improves the energy efficiency almost by 50 times. This does not result in the same efficiency levels as presented by dedicated accelerators, but it will give a much higher degree of flexibility. In addition, other optimizations like loop transformations, fixed point precision exploration, should be applied to further increase the efficiency. Motivated by this example of processor architecture modifications towards a flexible and efficient accelerator we developed the Neuro Vector Engine (NVE). An accelerator template based upon energy efficient processors. The NVE is positioned between the design points of high efficiency custom accelerators and general purpose processors. This to combine the best of both worlds, high efficiency, good utilization and a high degree of flexibility.



**Figure 6.6:** Instruction energy breakdown for a simple SIMD processor. Vector loads and register accesses consume more energy than scalar ones. However, reduction of overhead instructions and a substantial increase of useful work improves efficiency by 50 times compared to the scalar version.

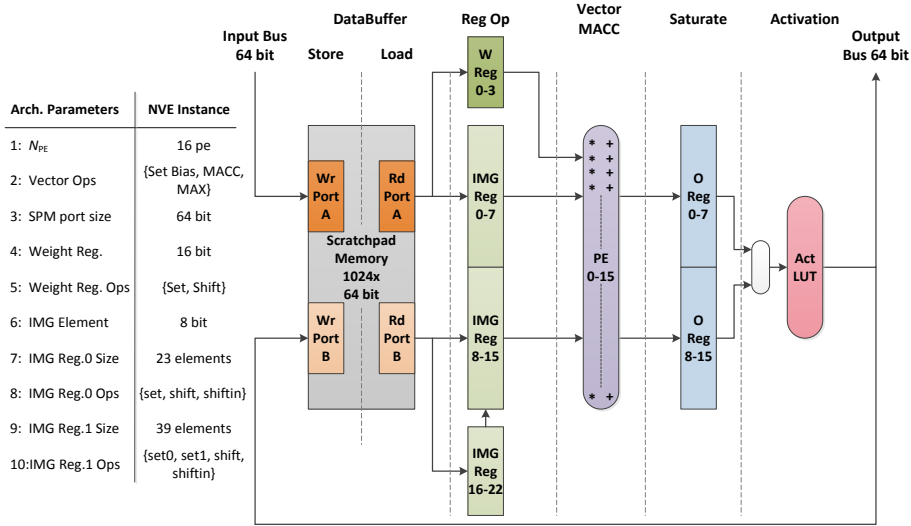
## 6.4 The Neuro Vector Engine (NVE) architecture

In this section our flexible NVE accelerator template is outlined. As the name suggests all operations are done on vectors to achieve a good efficiency. A balance between efficiency and flexibility is created with a VLIW based processor template that is equipped with vector operations tuned for ConvNets. Figure 6.7 illustrates the 6 issue slot VLIW template. A VLIW organization gives flexibility to program the accelerator for different ConvNet workloads. Secondly this template supports the advanced access patterns required for inter-tile data reuse optimization, see Chapter 5. Here we focus on a single instance of the template, but custom modifications can be easily performed. We will comment on possible modifications at the end of this section.

### 6.4.1 Vector data path

Often systolic or dedicated convolution operators are used in custom accelerators (see Section 6.2). The NVE uses a different and more flexible iterative operation for the computation of convolutions. The main compute operation is a vector Multiply Accumulate (MACC), i.e.  $\vec{y} \leftarrow \vec{y} + \vec{x} \times w$ . It modifies an array of accumulator values  $\vec{y}$  where each value represents a neighbouring neuron. By sequentially repeating this operation over all inputs of a 2D or 3D convolution window the reduction operation is performed. For varying kernel sizes a MACC resource is well utilized. Other accelerators use dedicated adder trees for the reduction [20,37] which has the disadvantage that reconfiguring for other kernel sizes is costly. The usage of accumulation registers in the NVE makes it relatively simple to implement other operations like the MAX operation used in max pooling layers.



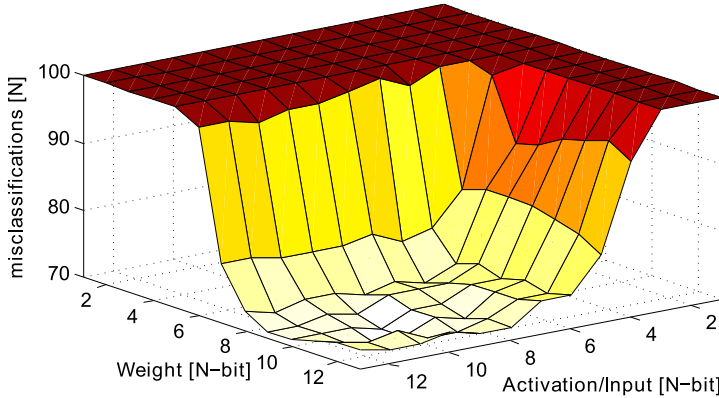


**Figure 6.7:** Pipelined accelerator datapath with 6 connected issue slots: Store Scratchpad; Load Scratchpad; Register Reorder; Vector MACC; Saturate; Activation. The vector operations of issue slots are selected by VLIW instructions. The right hand table outlines the parameters of this NVE instance. Modifications like a single port scratchpad are possible.

The locality optimized tile strips from Chapter 5 map straightforward to an array of MACC units. First a series of neighboring neurons in a feature map are initialized to a bias value, which is implemented by setting the accumulation registers. Secondly, the PE array performs a series of MACC operations that corresponds with the kernel size. Finally when all connected inputs are accumulated the result is output to the activation function lookup tables. The MACC vector operations are similar to a series of iterations for loop iterator  $m$  or  $n$ , as shown in Listing 2.1 of Chapter 2. The *Vector MACC* unit is positioned in the middle of the data path, as shown in Figure 6.7 in purple. To achieve a high clock frequency a three stage pipelined MACC design is used.

### Arithmetic precision

Instead of floating point data representation the more simple but energy efficient fixed point data types are used. It is well known that neural networks do not require the range and precision of a 32-bit floating point type [70]. To obtain the minimum precision we explored the accuracy requirements of a ConvNet trained for the MNIST digit recognition task [84]. We trained the well-known Lenet-5 configuration on 60,000 images using floating point precision and evaluated the accuracy on 10,000 separate test images. The floating-point baseline has an error rate of 70 misclassifications (0.7%), which is in line with [84]. We used the MatLab fixed-point toolbox to reduce the fixed-point accuracy in the network, the results are illustrated in Figure 6.8. We conclude that ConvNets require only 8-bit fractional precision, which is in line with earlier studies on



**Figure 6.8:** ConvNet fixed point accuracy exploration for varying fractional precision.

classical neural nets. Table I, gives the exact configuration of the data types that are used in the NVE accelerator design. The MACC PE array has a 16-bit (weight) and 8-bit (neuron) input that are used by a truncated multiplication. The accumulation register is extended to 9 integer bits with a hardware check to prevent overflow. Before activation function lookup the accumulation value is saturated to the 10-bit potential format given in Table 6.1. The *Activation Function* is implemented at the end of the pipeline with a look-up memory of 1024 entries of 8-bit, see Figure 6.7. As a result it is possible to implement any activation function efficiently by reloading the activation LUT.

## 6.4.2 Memory system

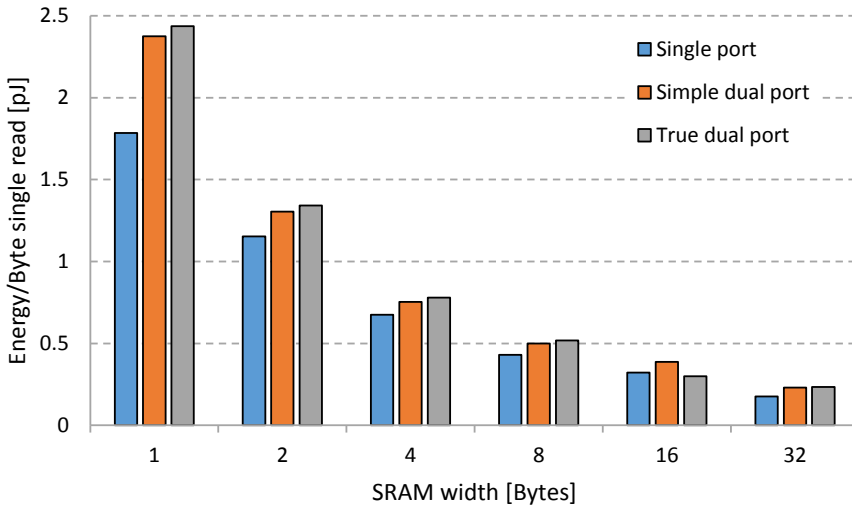
To exploit the inter-tile reuse opportunities that are proposed in Chapter 5 a programmable and flexible memory system is implemented. There is no need for expensive caches, because the access functions in ConvNets are static and predictable. Hence, we use an efficient scratch pad memory and vector reorder registers to exploit data reuse. Separating the accessing of values over two different data structures gives a huge complexity reduction. A 2D register file or scratch pad with reordering functionalities would be complex. Therefore 1D reordering is performed in L<sub>0</sub> (registers), and the orthogonal 1D reordering by reloading in L<sub>1</sub> (scratchpad).

### Lo: Vector reorder registers

To feed the vector MACC unit with weight coefficients and input values dedicated vector reorder registers are used. These registers are located in the *Reg Op*

Data type	Word size	Fixed point format
Weights	16 bit	<i>SIIIIIII.FFFFFFFF</i>
In/Act	8 bit	<i>.FFFFFFF</i>
Potential	10 bit	<i>SIII.FFFFF</i>

**Table 6.1:** Fixed-point data word configurations for the NVE instantiation.



**Figure 6.9:** CACTI 8 KB SRAM read energy exploration at 40 nm technology. The energy overhead when reading from a dual ported memory is marginal for vectors.

stage in Figure 6.7. They are designed to exploit data reuse at the level of neighbouring neurons by performing several reorder and broadcast operations. For example, the code listings in section 2.3 show that all layer types share weights in the direction of loop  $n$  and  $m$ . As a result, a *broadcast register* is implemented that sends out one of the vector weights to all PE. The reuse over neighbouring input values is exploited by a flexible 1D shift register. It supports filter kernels of any size since a dedicated *shift in* register is used. To ensure a high utilization of the *Vector MACC* unit the *shift in* register can reload a vector on the fly without stall cycles.

## L1 Local scratchpad memory

Vector registers are loaded from a local scratchpad memory that is placed in the first two issue slots. The scratchpad adds orthogonal dimensions of data reuse, this to simulate the working of a 2D or 3D shift register. For energy-efficient access to the scratchpad weights and inputs are stored as 64-bit vectors. This is motivated by simulations using CACTI [97] on an 8kB SRAM in 40nm technology. Figure 6.9 demonstrates that a vector access per byte (e.g. from 64-bit) is far more energy-efficient compared to short loads (e.g. from 8-bit). Furthermore, dual-ported memory can be used because it gives much more flexibility at the cost of an energy overhead of only 17%<sup>6</sup>. The flexibility of dual-ported memory is important in the NVE template, because multiple data streams access scratchpad concurrently. For example, new data is stored into the scratchpad, and concurrently multiple register reads occur. When memory ports are shared the data

<sup>6</sup> For dual-ported SRAM the energy penalty is relatively small, but area increases a factor two.

Cycle	MEM A	MEM B	WREG	IREG	VMACC	WB Sgm
1	st [s(i+2) word0]		shift	set r0,r1	macc rw,ri	
2	ld [b w0 w1 -]		shift	set r2 shift	macc rw,ri	
3	ld [s(i+0) word0]	ld [s(i+0) word1]	shift	shift	macc rw,ri	
4	st [s(i+2) word1]	ld [s(i+0) word2]	set [b w0 w1 -]		macc rw,ri	
5	ld [w2 w3 w4 -]		shift	set r0,r1	set rw	
6	ld [s(i+1) word0]	ld [s(i+1) word1]	shift	set r2 shift	macc rw,ri	
7	st [s(i+2) word2]	ld [s(i+1) word2]	set [w2 w3 w4 -]	shift	macc rw,ri	
8	ld [w5 w6 w7 w8]		shift	set r0,r1	macc rw,ri	act [s(i-1) word0]
9	ld [s(i+2) word0]	ld [s(i+2) word1]	shift	set r2 shift	macc rw,ri	act [s(i-1) word1]
10		ld [s(i+2) word2]	set [w5 w6 w7 w8]	shift	macc rw,ri	

**Figure 6.10:** VLIW assembly description of a steady-state program for 3x3 convolution in a feature map. Note that control is distributed over the different NVE issue-slots. Image load/stores of the scratchpad use modulo addressing over steady-state iterations to maximize the storage efficiency (i.e. old data is immediately overwritten by new).

path should stall more often, which reduces hardware utilization. One could use multiple separate memories e.g., for weights, inputs, and temporal results. However it is very difficult to effectively utilize the capacity and throughput of these memories. Each layer has different requirement w.r.t. the ratio of weights and inputs, so with a single shared flexible buffer we can utilize buffer capacity and throughput over different workloads.

### 6.4.3 Control and programming

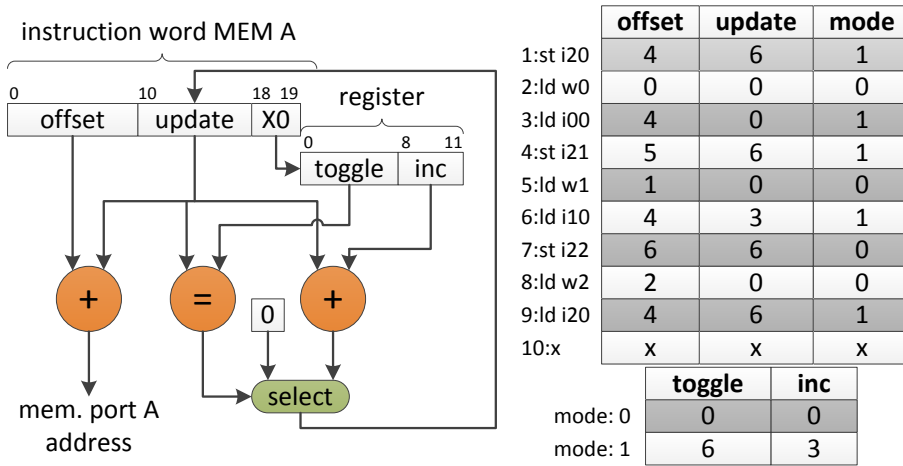
The NVE architecture exist of 6 successive *issue slots*; each performs a different functionality. The control of issue slots is distributed over one Very Long Instruction Word (VLIW). Using instructions improves flexibility substantially at the cost of instruction fetch overhead. Each issue slot is very specific so the instruction width can be small (54-bit). To minimize the overhead we use three techniques:

1. An energy-efficient on-chip loop buffer that holds 512 instructions.
2. Modulo software pipelining [80] to efficiently fold instructions together.
3. Modulo address generators to remove many instructions.

In addition, all issue slot operations of the NVE are performed on vectors, which increases the amount of useful work per instruction, see Section 6.3.

### Software pipelining

A high data path utilization with a small code size is achieved by software pipelining operations of successive issue slots. The basic idea is to translate the repetitive operations in a *tile strip* to a *steady-state* description. Many iterations of the *steady-state* are repeated to execute a complete *tile strip*, which improves instruction reuse. As an educational example the steady-state program of 16 concurrent rows of 3x3 convolution is given in Figure 6.10. Note that our techniques push a lot of work from each instruction. Each steady-state (10 instructions) process 16 dot products (144 MACC operations) this excludes, load/stores, vector



**Figure 6.11:** (left) Architecture of based modulo address generator. (right) Instruction memory contents for the 3x3 convolution example.

reorder operations, and activations. Before the steady-state begins prolog code initializes weight vectors and first image vectors in the local scratchpad.

### Modulo address generators

For efficient execution of tile-strips input columns in the scratchpad are replaced by a modulo addressing scheme. Combined with the 1D shift register the addressing effectively simulates a 2D or even 3D shift register. To provide the load/store addresses with a modulo replacement scheme dedicated address generators are developed. Figure 6.11 illustrates an address generator, both memory ports have a dedicated generator. Address generators use a part of the instruction word i.e., an offset memory, an update counter, and a pattern mode. The separate mode register implements different patterns e.g., weights are loaded from the same position, so the increment is zero over each steady-state interval. However, image vectors are over written with a step size increment and a toggle value to jump back to the first value. As shown in Figure 6.11, the address generator updates instruction address field for the next steady-state iteration. Address generators reduce the number of required instructions resulting in a compressed and efficient program.

## 6.5 Experimental evaluation

To evaluate the NVE accelerator architecture and the inter-tile reuse transformation techniques we used a set of tools and applications. The settings of our setup are further outlined in this section.

<b>Face Detection [53]</b>	$N_o$	$N_i$	$N_m$	$N_n$	$N_k$	$N_l$	$S$
Layer 1	4	1	638	358	6	6	2
Layer 2	14	2	317	177	4	4	2
Layer 3	14	1	312	172	6	6	1
Layer 4	1	14	312	172	1	1	1
<b>Speed Sign [105]</b>	$N_o$	$N_i$	$N_m$	$N_n$	$N_k$	$N_l$	$S$
Layer 1	6	1	638	358	6	6	2
Layer 2	16	3	317	177	6	6	2
Layer 3	80	40	313	173	5	5	1
Layer 4	8	80	312	172	1	1	1

**Table 6.2:** Convolutional Network application parameters.

### 6.5.1 Benchmark setup

To NVE architecture is evaluated with the two Convolutional Network recognition applications introduced in Chapter 3. These applications are the Face detection network [53], and Speed sign detection [105]. In addition, the educational example of  $3 \times 3$  convolution is used for evaluation. All applications run on a HD720p video stream and for best performance we use the optimized implementations with merged convolution and subsample layers as described in Chapter 4. The two real-world applications contain a mix of different layers with varying kernel sizes, dense and sparse connectivity, as detailed in Table 6.2.

### Baseline commercial platform mappings

As baseline to compare the NVE an ARM Cortex-A9 core is selected. Due to its good energy efficiency and performance it is a popular embedded platform in many Smartphones. In addition, we compare with an Nvidia Embedded GPU the Jetson TK1 with 192 Cuda cores [100]. The NVE is positioned as flexible IP core for the next generation of smart compute platforms, so the ARM A9 and Nvidia TK1 are direct competitors.

For fair comparison it is important that both ConvNet vision applications are optimized. For the ARM-A9, we used all compiler optimizations of GCC 4.7, which made the C implementation of speed sign detection 13.4x faster with an energy efficiency increase of 13.3x. In addition, usage of SIMD NEON intrinsics resulted in an extra speedup of 2.7x with an energy efficiency increase of 1.8x.

For the TK1 mapping we used a CUDA optimized mapping, e.g., we use the constant memory for coefficients, exploit tiling and memory access coalescing. For the ARM core we use a GEM5 [7] and McPAT [88] simulator setup. The model assumes a 4-issue superscalar core with 800MHz clock, 32kB instruction and 64kB data cache with an associativity of 2, and a line size of 64 bytes. McPAT is configured for low power operating mode in 40nm technology. The Jetson TK1 measurements are done on the NVidia development board.

Module	Area [mm <sup>2</sup> ]	(%)	Power [mW]	(%)
Accelerator	0.259		54.1	
Logic	0.076	(29%)	43.3	(80%)
Scratchpad	0.112	(43%)	5.9	(11%)
Act. LUT	0.045	(17%)	1.5	(3%)
Instr. Buf.	0.026	(10%)	3.4	(6%)

**Table 6.3:** Breakdown of synthesized area and power during simulation at 40 nm.

## NVE instantiation

For evaluation of the NVE architecture a 16 MACC PE data path with all control is designed in VHDL. The required memories in the design are configured as follows:

- 8 kB dual-port scratchpad with 64-bit entries
- 8 activation function LUT memories of 1 kB each
- a 54-bit wide 512 entry instruction buffer

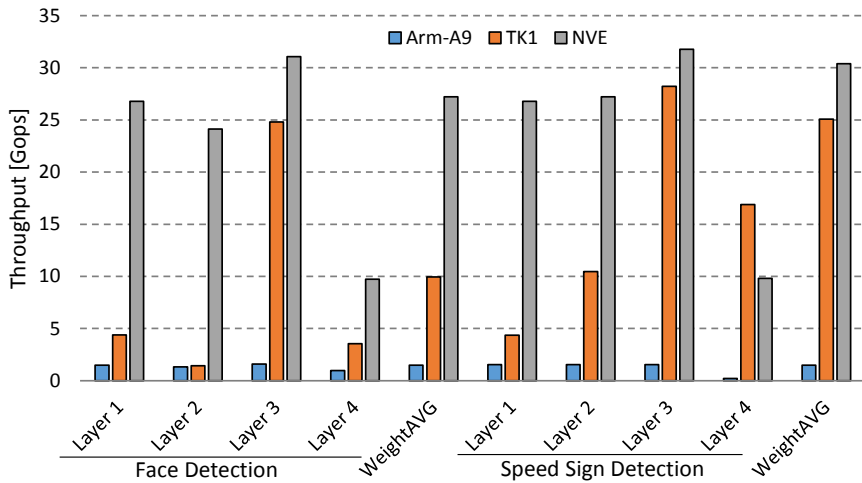
Although we target ASIC technology the functional correctness of the design is verified by FPGA mapping. For estimation of ASIC properties the design is synthesized with Cadence Encounter RTL Compiler from a 40 nm TSMC low power library. The SRAM memories are simulated with CACTI [97] for a similar 40nm low power library. The target clock frequency of 1 GHz is achieved by pipelining of the stages in the data path. It is important to enable retiming, since it reduced area by 32% and power consumption by 41%.

For accelerator mapping an optimizing compiler [107] is used. This compiler reads a JSON ConvNet descriptions that is automatically converted into optimized software pipelined VLIW programs. These programs are automatically converted into VHDL test benches that are simulated on the post-synthesis result for energy estimation. An extensive review of this compiler is given in Chapter 7.

### 6.5.2 Accelerator characteristics

The total area footprint of the accelerator is 0.26 mm<sup>2</sup>, which makes it a very small design, e.g., the McPAT ARM core requires 14 mm<sup>2</sup>. The area breakdown of the different components in the synthesized accelerator is given in Table 6.3. From the results is observed that (71%) of the area is spend on the on-chip SRAM. Given the fact that the complete architecture aims at minimizing external communication by reusing data or instructions in local buffers this is in line with our expectation.

The power results are obtained by post-synthesis simulation of tile strips from the vision applications implemented as steady-state programs similar to the 3x3 convolution code in Figure 6.10. Table 6.3 presents the average power breakdown of the simulations. The major energy portion is consumed by the



**Figure 6.12:** Throughput comparison ARM-A9, NVidia Jetson TK1, and NVE. The NVE shows very constant throughput level compared to the commercial platforms.

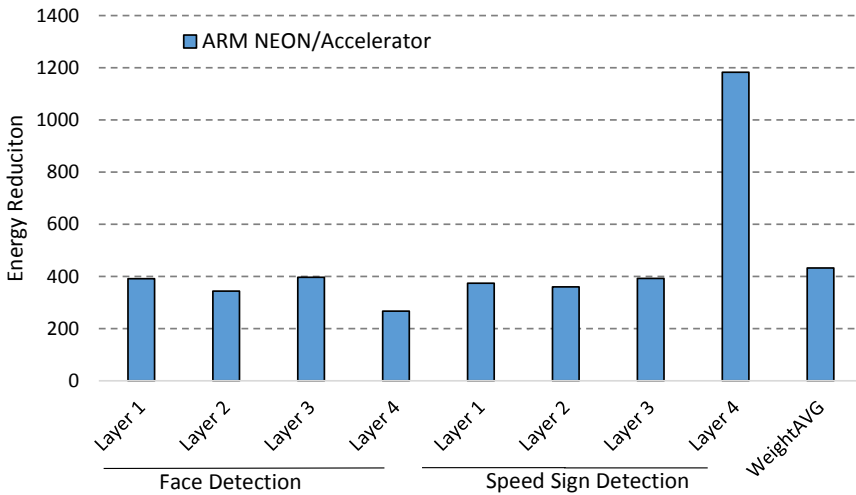
logic (80%), which contains the multipliers, adders, registers, instruction decoder, etc. The on-chip memory is responsible for only a small amount of power. The main reason is the relatively small number of accesses to the memories due to data reuse in the special purpose registers, which significantly reduces the memory pressure. For example in layer 1 of the speed sign application there are 1.66 scratchpad accesses per cycle on average. However, every cycle also 16 MACC operations are performed. This large ratio explains the difference between logic power and on-chip memory accesses. Note that the instruction buffer consumes only 6% of the total power budget. Given the substantial flexibility improvement the 6% energy penalty of the instruction fetch system is defensible.

## Throughput

With a full utilization of the vector MACC stage the accelerator theoretically performs 32 fixed point operations/cycle. Additionally, the activation function array can perform 8 activation function lookups in parallel. Combined a peak performance of 40 GOp/s can be reached at 1 GHz operation. For real-world ConvNet applications the performance number is less e.g., time is required to load instructions, execute the prolog part, or stall cycles due to conflicts. The mapping of the speed sign detection ConvNet layers demonstrated a weighted average of 30.2 GOp/s. Due to the higher degree of register locality convolution layers without subsampling perform best in the range of 32 GOp/s. On the other hand, output layers with  $1 \times 1$  convolutions have no register locality, so these have a lower performance of 10 GOp/s.

The throughput comparison between ARM-A9, NVIDIA TK1 and the NVE is given in Figure 6.12. The NVE shows a speedup of 20x compared to the ARM,





**Figure 6.13:** Energy consumption reduction NVE vs NEON optimized ARM-A9.

surprisingly the NVE is also able to beat the TK1 by a factor 1.2-2.6 depending on the application. Note that the flexible NVE achieves a very constant utilization over the different layers, only the classifier layers with substantially less data reuse perform worse.

## Energy

The energy consumption of the ARM core versus the NVE is compared in Figure 6.13, which shows a very similar trend. On average the accelerator reduces energy consumption by 430x, which is a lot considering we compare with an embedded ARM core that uses energy efficient SIMD operations. With a power requirement of 54 mW, a compute efficiency of  $\frac{30.2 \text{ Gop/s}}{54 \text{ mW}} = 559 \text{ GOps/Watt}$  is achieved. As a result the average energy per fixed point operation is 1.8 pJ, which is very competitive for 40nm technology. From this observation we conclude that the accelerator does not sacrifice compute efficiency as a tradeoff for the increased flexibility.

The NVIDIA TK1 consumes 6.9 Watt of power [100] this is substantially more than the NVE with 54mW. This is expected because the TK1 is a far more generic platform designed for Tablets with a larger energy budget. In the energy simulations the external data transfer is not taken into account. When we add the energy spend by DMA and external memory requests, the majority of the energy budget is on memory transfers. This is not caused by a bad data-reuse strategy, but the energy consumed by the NVE is reduced to a very low level, which was the main goal of this work.

### 6.5.3 Comparison against other ASIC accelerators

Researchers and computer architects nowadays recognize that the major improvements in cost-energy-performance should come from domain specific hardware. This trend caused the introduction of many very new dedicated ASIC accelerators for ConvNet workloads. In Table 6.4 a number of ASIC based ConvNet accelerators is compared to our default NVE configuration. We tried to obtain all accelerator characteristics, such as clock frequencies, technology node, and core voltages. Our proposed NVE accelerator has with only 16 MACC units less computational resources than the other comparison targets. For example, in the extreme there is a Tensor Processing Unit (TPU) [77] with 64k Multiply and Add units. The smallest accelerators are represented by Origami [15] and ShiDianNao [46], with 196 and 64 multipliers respectively.

The listed accelerators employ different techniques for parallelizing computations. The NVE and ShiDianNao perform convolution in time and thereby maps computational resources to different output neurons. This makes utilization of the MACC units invariant to convolution window size. The other accelerators such as DianNao and Origami, perform convolutions in space, so mapping computational resources to different pixels on the receptive fields of a neuron. Mapping convolutions in space makes the computational efficiency dependent on window size and negatively impacts utilization when the network parameters do not match the hardware.

The accelerator presented in [132] avoids most multiplications by performing lookups in a Q-table that contains pre-computed multiplication results. It uses a custom instruction set based controller that configures finite state machines on lower lever convolution cores. The chip presented in [43] contains multiple

Accelerator	mW	V	Tech.	MHz	Gops	Gops/ W	On-Chip Mem.	Con- trol	mm <sup>2</sup>	Gops/mm <sup>2</sup>
NeuFlow [110]	600	1.0	45 SOI	400	294	490	75 kB	Data- flow	12.5	23.5
Origami [15]	93	0.8	umc 65	189	55	803	43 kB	Config	1.31	42
NVE [109]	54	-	TSMC 40	1000	30	559	20 kB	VLIW	0.26	115
DianNao [20]	485	-	TSMC 65	980	452	931	44 kB	FSM	3.02	149.7
ShiDianNao [46]	320	-	TSMC 65	1000	128*	400	288 kB	FSM	4.86	26.3
Desoli et al. [43]	51	0.58	28 FD- SOI	200	78	1277	6 MB	Config	34	2.29
Shin et al. [132]	35	0.77	65 1P8M	50	73	2100**	290 kB	FSM	16	4.5
TPU [77]	40,000	-	28 nm	700	46,000	1150	28 MB	CISC	<331	>139

\* Only gives theoretical peak performance, as opposed to actual measurements on a real network.

\*\* Q-table lookup of precomputed multiplication results.

**Table 6.4:** Dedicated ASIC accelerator overview for ConvNets.

DSP cores for general vision processing, a big on-chip memory, and a co-processor subsystem with multiple convolution accelerators. The paper only lists power consumption for the co-processor, excluding on-chip memory. Control of the accelerator is handled through a set of configuration registers that configure a stream switch, allowing the reuse of data streams (similar to [16,110]).

The Tensor Processing Unit (TPU) [77] is a huge accelerator designed for server applications. The reported performance and power consumption are several orders of magnitude larger compared to the other designs, but still it is very efficient and makes good use of data reuse in the large on-chip memory. The control of a TPU is handled by complex high-level instructions that take multiple cycles to complete.

A computational throughput comparison of the accelerators shows that the NVE achieves 30 Gops, which is a relatively low throughput. Note that the throughput numbers in Table 6.4 are the measured numbers that are given in the papers. The only exception is ShiDianNao [46] that only reports peak performance. Due to the large architectural differences it would be very interesting to simulate our real-world vision benchmarks on these architectures. Big accelerators such as a TPU are only well utilized if the workload fits their architecture. For instance the 256x256 Multiply Add array of a TPU would be completely underutilized when we map the Speed sign or Face detection workload. Underutilization effects would also occur for DianNao and Origami, because they use fixed convolution window sizes. Underutilization would substantially reduce the efficiency numbers of the other accelerator that are given in Table 6.4.

The NVE can perform layer merging technique as proposed in Chapter 4. For networks that support merging this results in a higher effective throughput. Our benchmark results in Figure 6.12 demonstrate that the NVE achieves a high utilization degree for different layers and convolution window configurations. One of the reasons is the VLIW based control model that also enables the use of optimizing compilers. Important to note is that the NVE is by far the smallest design and upon the three best designs regarding power consumption. These aspects make the NVE an excellent addition for ultra-low power systems on chip.

## 6.6 NVE instantiation and customization

During the evaluation a very flexible NVE instance is used. However the NVE is an accelerator template i.e., it is possible to modify the architecture at design time to specialize for different workloads. In this section an overview of some important configurations is given and the consequences of these modifications are discussed.

As demonstrated in Section 6.5.2 the largest component in silicon area (43%) is the local scratchpad memory. On the total energy budget the scratchpad consumes (11%). Different buffer configurations could reduce silicon area or energy consumption. For a quick exploration we evaluate 3 alternative memory configurations:

1. Single port scratchpad, one load/store port 64-bit.
2. Simple dual port scratchpad, one load and one store port 64-bit.
3. Single port scratchpad, one load/store port 128-bit.

These configurations are compared against true dual port memory configuration (two load/store ports 64-bit wide) that maximizes flexibility. The  $3 \times 3$  convolution example from Figure 6.10 is used to evaluate the properties. The new schedules are given in Figure 6.14, Figure 6.15, and Figure 6.16.

The single port 64-bit wide memory (see Figure 6.14) has a clear memory bandwidth problem. The memory port is fully utilized and the vector MACC stage is stalling quite often. On the other hand, this single 64-bit ported memory has a significantly smaller silicon footprint, see Table 6.6. At the cost of a throughput reduction the NVE instantiation would shrink to  $0.194 \text{ mm}^2$ , which is the smallest design. Because it is a single port design one of the AGUs can be removed, which reduces the power consumption. Table 6.5 shows that the single port memory consumes less power than others, but the energy efficiency is reduced due to the low utilization of the vector MACC stage.

A simple dual port configuration increases memory bandwidth. Although loads and stores can be performed concurrently the schedule in Figure 6.15 reveals that the load bandwidth is a performance bottleneck. Table 6.5 shows that the simple dual port memory is relatively large and has a lower energy efficiency. A further increase of scratchpad bandwidth is achieved by using a 128-bit wide single port memory. This configuration uses less silicon area w.r.t. the true dual port memory, and it offers similar data load bandwidth at a small flexibility penalty. According to Figure 6.9 single port loads of 128-bit require less energy per byte than any of the other configuration. However, the wide memory port loads require more unnecessary data since the shift-in vector always contains 16 values that are fully utilized for convolutions with kernel windows of 16 elements. From the schedule in Figure 6.16 we conclude that throughput can be similar to the true dual ported configuration. However, the external input port should send more data into the accelerator due to the vector size inefficiency. The overview Table 6.5 shows that there is an energy efficiency advantage for the wide vector memory, over all other configurations. If we would take external memory energy into account this gain over the other configurations could be removed.

Cycle	MEM port A	Weight REG	Image REG	VMACC	VACT
1	st [s(i+2) word0]	shift	set r1		
2	st [s(i+2) word1]	shift	set r2 shift	macc rw,ri	
3	st [s(i+2) word2]			macc rw,ri	
4	ld [b w0 w1 -]			macc rw,ri	
5	ld [s(i+0) word0]				
6	ld [s(i+0) word1]	set [b w0 w1 -]			
7	ld [s(i+0) word2]		set r0	set rw	
8	ld [w2 w3 w4 -]	shift	set r1		
9	ld [s(i+1) word0]	shift	set r2 shift	macc rw,ri	
10	ld [s(i+1) word1]	set [w2 w3 w4 -]	shift	macc rw,ri	act [s(i-1) word0]
11	ld [s(i+1) word2]		set r0	macc rw,ri	act [s(i-1) word1]
12	ld [w5 w6 w7 w8]	shift	set r1		
13	ld [s(i+2) word0]	shift	set r2 shift	macc rw,ri	
14	ld [s(i+2) word1]	set [w5 w6 w7 w8]	shift	macc rw,ri	
15	ld [s(i+2) word2]		set r0	macc rw,ri	

**Figure 6.14:** Assembly schedule for a single port 64-bit wide scratchpad. Note that the VMACC stage is underutilized due to a bandwidth bottleneck with the scratchpad.

Cycle	MEM port A	MEM port B	Weight REG	Image REG	VMACC	VACT
1	st [s(i+2) word0]	ld [b w0 w1 w2]	shift	set r2 shift	macc rw,ri	
2	st [s(i+2) word1]	ld [s(i+0) word0]	shift	shift	macc rw,ri	
3	st [s(i+2) word2]	ld [s(i+0) word1]	set [b w0 w1 -]		macc rw,ri	
4		ld [s(i+0) word2]		set r0	set rw	
5		ld [w3 w4 w5 -]	shift	set r1		
6		ld [s(i+1) word0]	shift	set r2 shift	macc rw,ri	
7		ld [s(i+1) word1]	set [w2 w3 w4 -]	shift	macc rw,ri	act [s(i-1) word0]
8		ld [s(i+1) word2]		set r0	macc rw,ri	act [s(i-1) word1]
9		ld [w6 w7 w8 -]	shift	set r1		
10		ld [s(i+2) word0]	shift	set r2 shift	macc rw,ri	
11		ld [s(i+2) word1]	set [w5 w6 w7 w8]	shift	macc rw,ri	
12		ld [s(i+2) word2]		set r0	macc rw,ri	
13			shift	set r1		

**Figure 6.15:** Assembly schedule for a simple dual port 64-bit wide scratchpad. The dedicated load port is still a performance bottleneck for the VMACC issue slot.

Cycle	MEM port A	MEM port B	Weight REG	Image REG	VMACC	VACT
1	st [s(i+2) word0]		shift	set r0	macc rw,ri	
2		ld [b w0 - w4]	shift	set r1, shift	macc rw,ri	
3		ld [s(i+0) word0]	shift	shift	macc rw,ri	
4		ld [s(i+0) word1]	set [b w0 - w4]		macc rw,ri	
5	st [s(i+2) word1]		shift	set r0	set rw	
6		ld [s(i+1) word0]	shift	set r1, shift	macc rw,ri	
7		ld [s(i+1) word1]	shift	shift	macc rw,ri	
8		ld [w6 w7 w8 -]	shift	set r0	macc rw,ri	act [s(i-1) word0]
9		ld [s(i+2) word0]	shift	set r1, shift	macc rw,ri	act [s(i-1) word1]
10		ld [s(i+2) word1]	set [w5 w6 w7 w8]	shift	macc rw,ri	

**Figure 6.16:** Assembly schedule for a single port 128-bit wide scratchpad. The VMAC issue slot can be fully utilized since there is enough memory bandwidth to the scratchpad.

Scratchpad config.	Area [mm <sup>2</sup> ]	(%)	Power [mW]	(%)
single port 64 bit	0.047	24%	3.445	6.7%
simple dual port 64 bit	0.088	37%	4.397	8.6%
single port 128 bit	0.070	32%	5.147	9.6%
true dual port 64 bit	0.112	43%	5.926	10.9%

**Table 6.6:** Area and power consumption overview for different scratchpad configurations. All memories sizes are configured to have 8 Kbyte.

### 6.6.1 Limitations and future directions

As show by the short scratchpad memory exploration different trade-offs are possible in NVE configurations. Depending on the application set one could select the perfect NVE instantiation at design time. A similar exploration could be done for the size of the vector MACC array. The 16 processing elements that are selected for this chapter are very well utilized for different workloads. Due to aggressive pipelining a clock speed of 1 Ghz is achieved that gives 32 Gop/s peak convolution performance. For some applications this is not enough, and one could evaluate larger vector arrays of 32, 64, or 128 MACC units. Note that the utilization of the vector MACC units will quickly decrease due to border effects. The NVE template really focusses at the ultra-low power domain below 100mW which will limits the wide vector scalability. Probably a multi-processor configuration of NVE instances would give more flexibility and better scaling.

The current true dual ported implementation with 16 PEs achieves 13 fps real-time performance on the speed sign detection application. Wide vector implementations or multi NVE accelerator configurations can certainly further improve on this performance. In addition, further work on the DMA engines is required. The NVE benefits a lot from streaming data that is well prepared for the architecture, e.g. packed coefficient vectors, or columns of feature map data. In [153] we developed a custom shuffling unit that can reorder and send the data vectors efficiently to the NVE accelerator. These Reordering Units are placed between the memory interface controller and the NVE FIFO streams, as depicted in Figure 6.17. With larger memory structures these Reorder Engines could be used to exploit more data reuse over successive tile strips.

Scratchpad Config.	Throughput	Area NVE	Power	Gop/Watt	pJ/Op
single port 64 bit	21.3 Gop/s	0.194 mm <sup>2</sup>	45.3 mW	470	2.12
simple dual port 64 bit	24.5 Gop/s	0.235 mm <sup>2</sup>	50.6 mW	484	2.06
single port 128 bit	31.9 Gop/s	0.217 mm <sup>2</sup>	51.4 mW	621	1.61
true dual port 64 bit	31.9 Gop/s	0.259 mm <sup>2</sup>	54.1 mW	589	1.70

**Table 6.5:** NVE benchmark characteristics for the different scratchpad memory configurations while running the 3x3 convolution application.

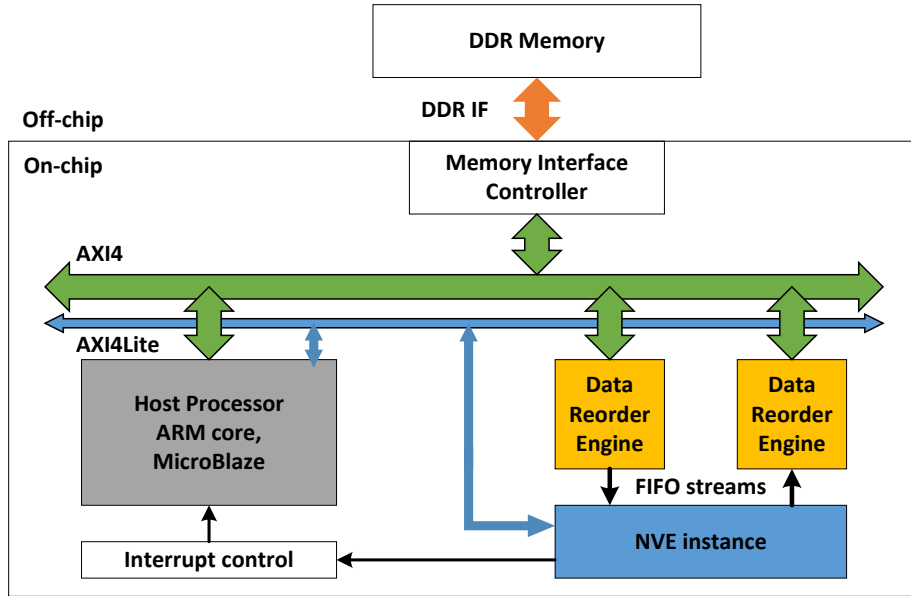


Figure 6.17: Inter connection overview for a SoC equipped with an NVE instance.

## 6.7 Conclusions

Customized hardware acceleration for visual object classification has significantly improved the computational efficiency of Convolutional Networks (ConvNets). The current works are very specialized, which is often suboptimal for varying network configurations. We have presented a new SIMD architecture template for hardware-acceleration, the Neuro Vector Engine (NVE). In addition we demonstrated mapping and optimizations for inter-tile reuse to exploit the data locality optimizations from Chapter 5.

A VLIW-type of controller allows for sufficient flexibility to encode many ConvNet based machine vision applications. Synthesis on a low power 40 nm CMOS technology library resulted in a pipelined circuit that operates at 1 GHz, yielding an effective performance of 30.2 GOP/s on real benchmarks (20x faster w.r.t. a SIMD optimized ARM-A9). Considering the power budget of only 54 mW, this accelerator is suitable for embedment in the next-generation mobile devices and bring smart features like real-time visual object classification and speech recognition to our cherished portable companions.

# ACCELERATOR CODE GENERATION

*This chapter presents a compiler flow to map Deep Convolutional Networks (ConvNets) to highly specialized VLIW accelerator cores targeting the ultra-low power embedded market. Earlier works focused on energy efficient accelerators for this class of algorithms, but none of them provides a complete and practical programming model or a compiler. Due to the large parameter set of ConvNets it is important that the user can abstract from the accelerator architecture and does not have to rely on an error prone and ad-hoc assembly programming model. By using automatic advanced code optimization techniques such as data layout modification, modulo scheduling for software pipelining, and schedule combining for locality, we demonstrate that our compiler can produce highly optimized accelerator code. We evaluated our compiler on complex real-world vision applications with different network layer configurations. The average throughput of our compiler mapped applications is on-par with manual mappings by architecture experts that required multiple days of tuning. By combining multiple task schedules in ConvNet layers our compiler is able to reduce data transfers which is important for energy. More importantly our compiler solution reduces the huge manual workload to efficiently map ConvNets to energy-efficient accelerator cores for the next-generation of mobile and wearable devices.*

*This chapter is based on work presented at SCOPES 2015 [107].*

---

## 7.1 Introduction

In Chapter 4, 5, and 6 we have shown that Convolutional Networks (ConvNets) have multiple computational challenges. Firstly, the computational workload in the number of operations is very high, which is addressed in Chapter 4 by convolution and subsample merging. Secondly, the required data movement is a



performance bottleneck and it consumes a lot of energy. The inter-tile reuse optimization strategy from Chapter 5 reduces off-chip data transport a lot. Finally, we addressed the inefficiencies in general purpose computer architectures and existing accelerators in Chapter 6 by presenting the Neuro Vector Engine (NVE), a VLIW based accelerator that relies on vector operations.

Our community is well aware of the fact that architecture specialization is often required to achieve the best performance at low energy [113]. Other research groups also exploited the customization paradigm to design highly specialized, and thus highly efficient cores that enable excellent machine vision for mobile devices [16,50,20,37,46]. These cores achieve most of their efficiency gains by tuning data storage structures to the dataflow and data-locality requirements of the algorithm. The main challenge in accelerator design is to improve efficiency by architecture specialization, but maintain the flexibility. Especially, this flexibility is key for adoption of a new core. ConvNets have many parameters such as the number and type of layers, feature maps, and kernels, which are different for every task. Hence the architecture should support different parameter combinations efficiently and it should have a programming model. A programming model can be an Instruction Set Architecture (ISA), or a configurable state machine. The NVE architecture is designed to be flexible in multiple ways: 1. A NVE is customizable such that it can be tuned at design time to match the user needs; 2. It achieves high data path utilization for many ConvNet workloads, so it is workload flexible; 3. It has the flexibility of being fully programmable; by loading an instruction sequence it can execute a different ConvNet.

Most earlier works focus on efficiently implementing compute primitives, but none provides a flexible architecture template. Additionally, these published architectures do not have a practical programming model or a compiler. They voluntarily ignore programming for simplicity [16], or they refer to an ad-hoc and therefore impractical assembly program [20,37], or a restrictive state machine [46]. Only the Neuflow work [50] has a compiler model, but for this instance the architecture is very dedicated to a single network operator size.

In this chapter we present CONVE: a COmpiler for Neuro Vector Engines. To the best of our knowledge this is the first ConvNet compiler for a flexible accelerator template such as, the Neuro Vector Engine [109] see Chapter 6. The automatic CONVE flow replaces the complicated and error prone task of manual assembly writing by a network specification in our Design Specific Language (DSL). This DSL is compiled into optimized VLIW assembly programs. This increases another degree of efficiency which is *the mapping efficiency*, i.e. the time and energy required to obtain an efficient mapping. Often the quality of generated code is far lower than manually tuned code. However the performance on our compiled benchmark applications is slightly better than code optimized for days by architecture experts. The main contributions of this chapter are:

- Building a flexible VLIW compilation flow from a high level .json network description to assembly output.

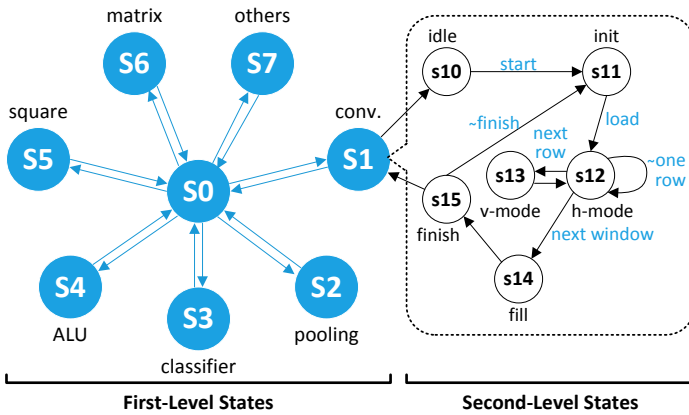
- A new bottom-up list scheduling approach that can be adapted for different accelerator instantiations.
- New optimization steps:
  - Data layout modification to resolve resource conflicts;
  - Automatic modulo software pipelining to increase utilization;
  - Schedule combining to maximize performance and increase data locality.
- An in-depth evaluation against manual written assembly code that's written by architecture experts by using real-world ConvNet vision applications.

This chapter is organized as follows: Section 7.2 gives an overview of related work in the field of compilers for accelerators and ConvNets. Section 7.3 introduces our Domain Specific Language (DSL) to specify network configurations for CONVE. Section 7.4 presents the CONVE code generation flow, and Section 7.5 discusses the advanced code optimization steps. In Section 7.6 we present an in-depth evaluation of the compiler results. Finally, Section 7.7 ends this chapter with conclusions.

## 7.2 Background and related work

Dedicated application accelerators are commonly used to process the dedicated workloads of different application domains. For example, our smartphones, digital (video) cameras, and tablets all capture and process high-resolution images or video with a power constrained compute platform. Performing the complicated real-time processing tasks on high rate pixel streams require fixed function accelerators. Often these accelerators have limited flexibility, so no support for different coding standards or data processing steps. Much more flexibility is achieved with software defined solutions, such as a Digital Signal Processor (DSP), and Image Signal Processor (ISP), or techniques to enable Software Defined Radios. In these cases programmable solutions are used which are more flexible and able to perform multiple tasks (better silicon efficiency). In addition, flexible cores can implement new functionalities or support new standards with a simple firmware update.

The NVE is a similar flexible signal processor specialized at ConvNet workloads. The NVE template uses concepts from Very Long Instruction Word (VLIW) [52] based processors. The VLIW approach is popular among commercial DSPs e.g., the Tensilica Xtensa [57], or Silicon Hive [135] processor, or the more recent Qualcomm Hexagon [33] DSP; all are used in high end smartphones. A VLIW puts the complex scheduling responsibility for instruction level parallelism into a compiler and thereby avoids costly and power-hungry dynamic-scheduling hardware. By moving the complicated scheduling to a compiler the processor can be rather simple while it is able to achieve high performance. However, compiling efficient code for a general purpose VLIW core is challeng-



**Figure 7.1:** Hierarchical control finite state machine of the ShiDianNao accelerator.

ing. The compilation challenges make that it is difficult to map applications efficiently; as a result the programmer has to optimize his code manually or accept a bad hardware utilization. In conclusion, VLIW cores require a good optimizing compiler, otherwise the programmer must spend a tremendous effort in mapping applications.

The CONVE compiler focusses on ConvNets, so the input programs have a regular structure. By narrowing the group of target applications compilation and optimization becomes more specific. As a result, more effort is spend in compilation routines that produce code that achieve close to peak performance on the NVE template without manual tuning.

Next to the general purpose VLIW base accelerator DSP cores there are many fixed function cores focussing on ConvNets. However most of them are less flexible compared to the NVE template. These works mainly focus on the convolution operations, but programmability or efficient code generation are out of the scope or simply neglected. Some exceptions do exist, for instance the NeuFlow [50] dataflow architecture which uses a software API called LuaFlow. Their flow converts descriptions, using Torch [34] into dataflow programs. In Torch ConvNets are specified layer-by-layer, each with parameters such as kernel size, subsample factor, number of inputs, and number of outputs for each layer. However, Torch lacks the freedom to assign a custom feature map connectivity. Only several connection types are allowed, e.g. fully connected, one-to-one, or random. For our vision benchmarks this would be too restrictive and forcing us to make many extra connections with coefficient values set to zero. In addition, the operators are specified as systolic array streams, which are underutilized if multiple varying kernel sizes are used.

Another recent fixed function accelerator program flow is used in the ShiDianNao [46] work. ConvNets are described as a Hierarchical Finite State Machine (FSM), see Figure 7.1. Two hierarchical FSM levels are used where the first describes the high-level flow through the network and the second controls low-

level details, e.g., the operation patterns of convolution or pooling. This approach replaces the use of instructions by FSM parameters, but these are less flexible and limited by the number of FSM states. For the FSM there is no high-level language, so programmers must create their own low-level FSM parameters to express each new network. Note that while the ShiDianNao accelerator has worked out an energy efficient control mechanism other key works still neglect this very important part. For example, the very recent and detailed Eyeriss publications [22,21] do not discuss their control architecture or input code generation. These papers present an in-depth study on data movement patterns and compute workload. For some reason the control architecture is left out and also input code generation is not covered. We argue that control and input code are key parts to improve the efficiency of an accelerator core. Therefore we discuss the details of building an application specific compiler. Firstly, the challenge that must be overcome is to generate code that achieves high accelerator utilization. Secondly, the mapping process needs to be simplified for applications on accelerators or improving the programmer's productivity, which is also an efficiency.

## 7.3 ConvNets in a domain specific language

As shown in the previous section many related ConvNet accelerators do not discuss their method of programming network parameters into their design. On the opposite there are also general purpose accelerator cores that use the C language with advanced compilers. These cores often struggle with the wide range of input programs for which always valid machine code should be generated. The CONVE framework takes a more abstract approach by relying on a Domain Specific Language (DSL) for ConvNets.

Our DSL is based upon the network description format for the popular software library Caffe [76]. Caffe is used to train Deep ConvNets with consumer hardware like GPUs. It brings the complicated training algorithms that are used for Deep Learning to the mass public. Their input description is based on `.json`, an open-standard format that uses human-readable text to define data objects. By default their language assumes full connectivity between feature maps, but the connectivity can be split with "group" parameters. These "group" parameters do not support the specification of custom layer-to-layer connectivity, which is important for workload reduction. Therefore we modified the CONVE input language such that users are able to express custom networks with sparse feature map connectivity. Furthermore, our CONVE input format is restrictive to ConvNet workloads such that unsupported program flows are prevented. This makes it much simpler to generate correct code from our DSL input.

Caffe trained networks can be easily mapped to our platform, since both description languages are very similar. The main difference is the flexibility to use connectivity patterns that are supported by the NVE. These sparse maps are key for efficient processing, since it substantially reduces the workload. Listing 7.1 gives an example description for the first and second layer of the face detection

```

{
  "name": "Face Detector",
  "layers": [{
    "output": {"size": [638,358], "act": "sigm",
    "map": [
      [0,1,2,3]
    ]
  },
  "kernel": {"size": [6,6], "pool": {"size": [2,2], "type": "avg"}}
}, {
  "output": {"size": [317,177], "act": "sigm",
  "map": [
    [0,1,8,11,13],
    [2,3,8,9,12],
    [4,5,9,10,11],
    [6,7,10,12,13]
  ]
},
  "kernel": {"size": [4,4], "pool": {"size": [2,2], "type": "avg"}}
}]
}

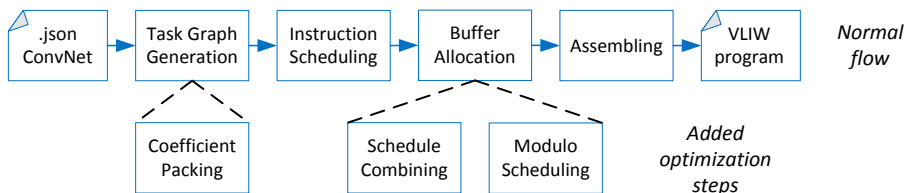
```

**Listing 7.1:** JSON Convolutional network description of first and second layer of the face detection benchmark workload.

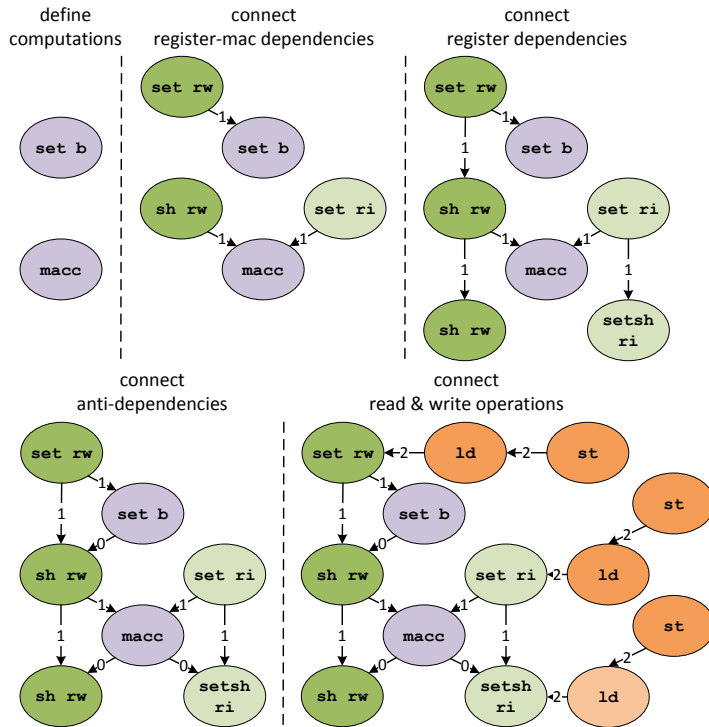
benchmark. First an application (**name**) is specified and then the network (**layers**). Each layer has a descriptor which lists parameters such as output size (**output.size**), activation function (**output.act**), output mapping (**output.map**), kernel size (**kernel.size**), pooling size (**kernel.pool.size**), and pooling kernel type (**kernel.pool.type**).

## 7.4 Automatic code generation flow

This section presents our automatic code generation flow in detail. As illustrated by Figure 7.2 the flow starts with a high-level ConvNet input description (Section 7.3). This description is converted into a separate task graph for each output feature map (Section 7.4.1). The taskgraph can be optimized by coefficient repackaging (Section 7.5.1) The instruction scheduling step constructs a schedule for every graph (Section 7.4.2). Further optimization steps are performed: e.g. modulo scheduling to increase utilization (Section 7.5.2); and combine feature map schedules to improve locality (Section 7.5.3). Physical buffer space is assigned for



**Figure 7.2:** The CONVE automatic NVE code generation flow.



**Figure 7.3:** Direct Acyclic Graph (DAG) construction for computation of an output feature map.

the schedules (Section 7.4.3), and finally these are converted into executable binaries for the VLIW instruction memory.

### 7.4.1 Task graph construction

The first step of the VLIW code generation is to represent the network layers as task graph or a Direct Acyclic Graph (DAG). These graphs are constructed by tracing back through the computation sequence for neuron outputs. This is performed by our graph constructor that creates a DAG from the `.json` input description. The graph is constructed by applying the structure rules of a ConvNet. The details of construction are discussed by an educational example of a  $3 \times 3$  filter application.

Convolution outputs of  $3 \times 3$  kernels require 9 MACC and one `set bias` initialization. In addition, these operations require coefficients, e.g., one bias, and 9 weight values that are broadcasted to the MACC vector unit, recall Figure 6.7. The weight register loads a word of four 16-bit coefficients (full capacity). The first entry is broadcasted directly after the load and the others by shift operations. As a result, three weight register set, and 7 shift operations are instantiated. The corresponding image data must be loaded in the image registers.

Depending on the number of MACCs, pooling stride, and kernel shape a sequence of image register operations is selected. For  $3 \times 3$  convolution the sequence is: `set`, `set shift`, and `shift` which is repeated for each column. The `register set` operations require loads from the scratchpad memory e.g., for weights three loads from port A. A `register set` on the image register requires two loads (port A and B) to fill position 0-15. The image register `set` and `shift` operation require a single load from port B, which fills the shift-in register. The small example requires 9 scratchpad loads for image data per group of 16 neurons. In case of a pooling factor a different set of image registers is used that require four loads to fill the larger image vector.

Operations in a task graph or Direct Acyclic Graph (DAG) must be connected with their dependencies, e.g., a `set bias` occurs before the first MACC operation so a dependence is connected, see Figure 7.3 (top-left). MACC operations require data from registers, so dependence arrows from register operations are connected (topmiddle). Successive `register shift` operations are connected, since they depend on the previous value (top-right); Anti-dependencies from MACCs to the registers are added as depicted in Figure 7.3 (bottom-left). These anti-dependencies ensure that the weights and pixels are not overwritten before the associated MACC operation takes place. Finally, dependencies between `register set` operations and scratchpad load operations are connected (bottom-right). A load has a dependency to a preceding store operations. All dependencies have a distance parameter representing the minimum latency between adjacent vertices. A simplified task graph construction pseudo description is given in Algorithm 8.1.

---

**ALGORITHM 8.1:** Direct Acyclic Graph (DAG) construction for an output feature map
 

---

```

input: kernel size  $k_x$  and  $k_y$ , subsample  $p_x$  and  $p_y$ , number of inputs  $p$ 
output: graph  $G(v, e)$ 
1 graph  $G$ ;
2 vertex  $v$ ;
3  $v \leftarrow$  set bias; //initialize neurons
4 insert_vertex( $v, G$ );
5 for  $i < k_x * k_y$  do
6    $v \leftarrow$  MACC; //process neuron inputs
7   insert_vertex( $v, G$ );
8 end
9 create dependencies between set bias and first MACC vertices in  $G$ ;
10 for  $i < 2$  do
11    $v \leftarrow$  activation; //two acts per vector for this NVE instance
12   insert_vertex( $v, G$ );
13   insert_dep( $v_{\text{setbias}}, v, G$ );
14 end
15 for  $i < n * k_x * k_y$  do
16   if  $i \% k_y = 0$  then
17      $v \leftarrow$  set ri; //each  $k_y$  a set register
18   else if  $i \% k_y = 1$  then
19      $v \leftarrow$  set shift ri; //load the shift-in register

```

---

---

```

20  else if then
21       $v \leftarrow \text{shift ri};$            //shift the image registers
22       $\text{insert\_vertex}(v, G);$ 
23  end
24  create dependencies between set ri and following shift ri vertices in  $G$ ;
25  create dependencies between shift ri and following shift ri vertices in  $G$ ;
26  create dependencies between MACC and adjacent ri vertices in  $G$ ;
27  create dependencies between ri operations with adjacent MACC in  $G$ ;
28   $\text{PackCoefficients}();$            //see section 7.5.1
29  foreach set ri/rw in  $G$  do
30       $v \leftarrow \text{ld ri/rw};$            //load operation from local scratchpad
31       $\text{insert\_vertex}(v, G)$ 
32       $v \leftarrow \text{st ri/rw};$            //store operation into local scratchpad
33       $\text{insert\_vertex}(v, G);$ 
34  end
35  foreach ld ri/rw in  $G$  do
36       $\text{insert\_dep}(v_{\text{ld}}, v_{\text{set}}, G);$  //connect load and set registers
37  end
38  foreach st ri/rw in  $G$  do
39       $\text{insert\_dep}(v_{\text{st}}, v_{\text{ld}}, G);$  //connect store and load operations
40  end

```

---

### 7.4.2 Instruction scheduling

A task graph alone cannot be executed by our accelerator. It is an intermediate representation for the operations with their dependency constraints. This graph must be converted into operations that are timed in the VLIW slots. Algorithm 8.2 describes our custom list scheduling procedure that works bottom up through the graph. At the bottom there exist a single root where at top multiple start vertices should be evaluated. Breadth First Search (BFS) is used to visit and schedule vertices with a complexity of  $O(V + E)$ . For example, BFS starts by adding the bottom vertex ( $x$ ) of task graph ( $G$ ) to a queue ( $Q$ ) then all parents of ( $x$ ) are visited one-by-one. During a visit, a time slot ( $t$ ) is assigned to the visited parent vertices ( $w$ ), these time slots are based on the time slots of child vertices ( $v$ ) and distance ( $d$ ).

In Figure 7.4 the scheduling procedure is demonstrated on the  $3 \times 3$  filter example. First, time slot 0 is assigned to the bottom vertex. By applying BFS time slots are assigned bottom-up to the parent nodes based upon the dependence distances. The required resources are claimed, however in some cases these are already occupied which causes a delay slot in the schedule. For example, a bit further in the graph a MACC operation is assigned to slot (-5). The connected parent nodes (see dashed nodes in Figure 7.4) require a set weight (**set rw**) and a set image register (**set ri**) operation. The scratchpad memory port constraints allow only one of the two set register operations at a time. As a result, the first visited (**set rw**) is assigned to slot -6. In the set register resource table slot -6 is claimed, see Figure 7.5. When the other parent node is visited a conflict



occurs, because the set register resource at slot -6 is already claimed and therefore the `set ri` is scheduled at -7.

---

**ALGORITHM 8.2:** Instruction Scheduling
 

---

```

input: graph  $G(v, e)$ , bottom vertex  $x$ 
output: VLIW schedule for graph  $G(v, e)$ 
1  create queue  $Q$ ;
2  create table  $T$ ;
3   $t_x \leftarrow 0$ ;           //assigned time slot
4   $s_x \leftarrow \text{visited}$ ;   //scheduled operations
5  insert  $x$  to  $Q$ ;
6  while  $Q$  is not empty do;
7     $v \leftarrow$  first element in  $Q$ ;
8    foreach edges  $e$  from  $w$  to  $v$  in  $G$  do
9      if  $i_w \neq \text{st}$  and  $i_w \neq \text{act}$  then
10     if  $s_w \neq \text{visited}$  then
11        $t_w \leftarrow t_v - d_e$ ; //compute new time slot
12        $s_w \leftarrow \text{visited}$ ;
13       if  $i_w = \text{set reg}$  then
14         while  $t_w$  exist in table  $T$  do
15            $t_w \leftarrow t_w - 1$ ; //resource occupied shift slot up
16         end
17         insert  $t_w$  into  $T$ ;
18       end
19     else
20        $t \leftarrow t_v - d_e$ ; //check if different path distance is valid
21       if  $t < t_w$  then
22          $t_w \leftarrow t$ ;
23       end
24     end
25   end
26 end
27 end

```

---

A challenging example is `ix1` convolution (an output neuron layer) as illustrated in Figure 7.6. There is no data reuse in a kernel window which requires the image register to load every cycle. When scheduling bottom-up through the graph the scheduler quickly runs into conflicts. For example, after the `MACC` in slot -2 it schedules a `set rw` at -3, a resource conflict enforces the `(set ri)` to be delayed to -4. The instruction table in Figure 7.7 reveals that many stalls will be inserted.

Note that the instruction scheduling procedure ignores all stores into the scratchpad memory and the activation function lookups. Activation operations are inserted in an As Soon As Possible (ASAP) time slot selection after scheduling. To hide the 3 cycle latency of the `MACC` stage activations from the previous iteration ( $s(i-1)$ ) are scheduled in the current iteration, otherwise the complete schedule would become much longer, see Figure 7.8. Store operations are divided in two parts: 1) The initialization part or prolog of the program. Here the required coefficients are stored and the first pixels are placed before starting the

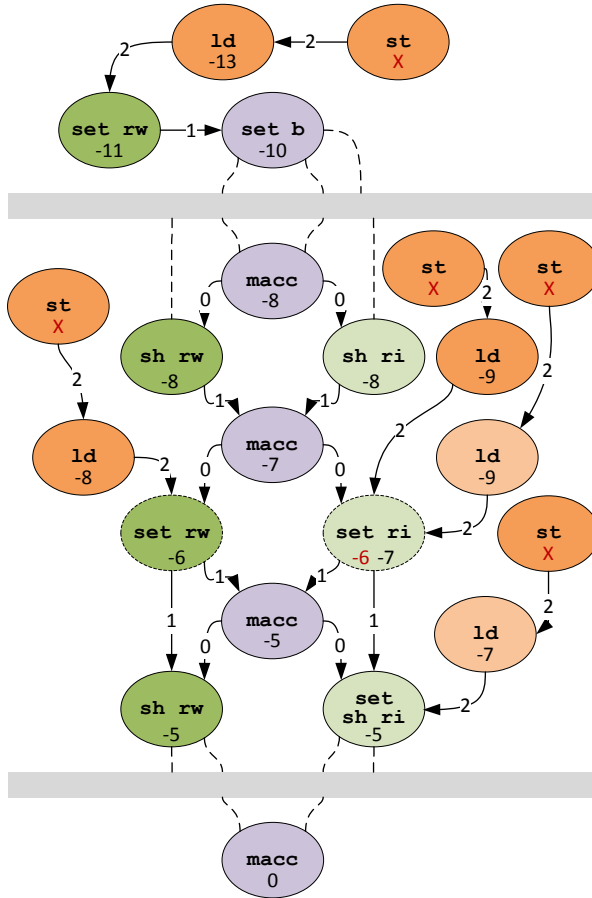


Figure 7.4: Assigning time slots to a 3x3 convolution task graph.

second part; 2) The repetitive part or steady-state, where only the new pixels for each tile are stored. For inter-tile strips only the few new columns of pixels from the new tile are stored, the overlapping ones from the previous tile are kept. The new pixel write operations in the steady-state are inserted in an As Late As Possible (ALAP) scheme. This ensures that the write operation can fill the scheduling gaps in the local scratchpad buffer.

Set REG	Cycle	MEM A	MEM B	WREG	IREG	VMACC	VACT
	-8	ld [w3 w4 w5 w6]		shift	shift	macc rw,ri	
-7	-7		ld [s[+1] word2]		set r0,r1	macc rw,ri	
-6	-6			set [w3 w4 w5 w6]		nop	
-5	-5			shift	set r2 shift	macc rw,ri	

Figure 7.5: Partial VLIW instruction schedule of the 3x3 convolution example.

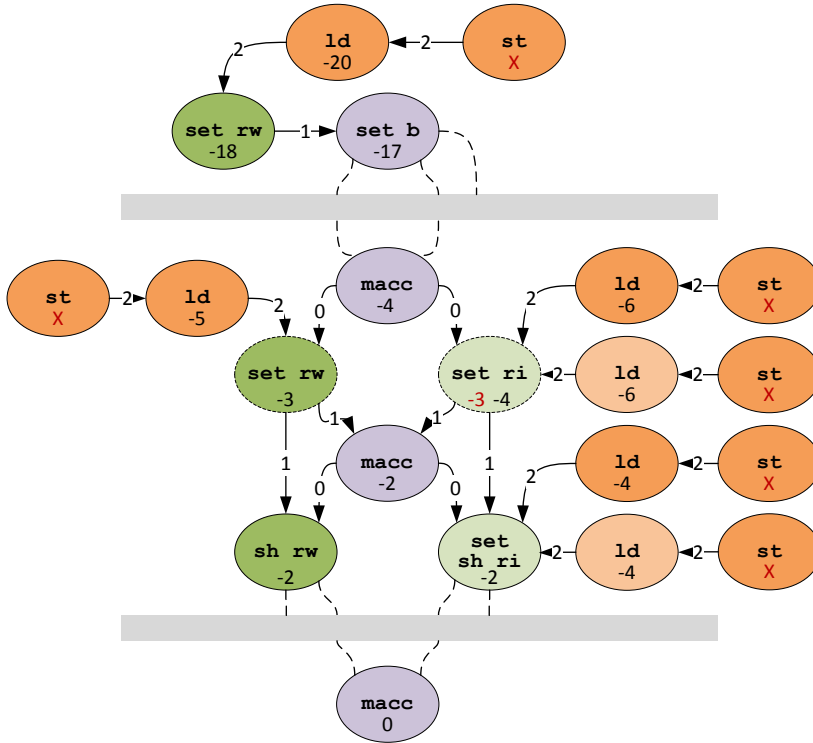


Figure 7.6: Assigning time slots to a 1x1 convolution schedule for an output layer.

Set REG	Cycle	MEM A	MEM B	WREG	IREG	VMACC	VACT
-5	-5	ld [w11 w12 w13 -]					
-4	-4	ld [s(i+0) word0]	ld [s(i+0) word1]		set r0,r1	macc rw,ri	
-3	-3			set [w3 w4 w5 w6]		nop	
-2	-2			shift	set r0,r1	macc rw,ri	

Figure 7.7: Partial schedule of 1x1 convolution on 14 input feature maps.

Cycle	MEM A	MEM B	WREG	IREG	VMACC	VACT
1	ld [b w0 w1 w2]					
2	ld [s(i+0) word0]	ld [s(i+0) word1]				
3		ld [s(i+0) word2]	set [b w0 w1 w2]			
4	st [s(i+2) word0]		shift	set r0,r1	set rw	
5	ld [s(i+1) word0]	ld [s(i+1) word1]	shift	set r2 shift	macc rw,ri	
6	ld [w3 w4 w5 w6]		shift	shift	macc rw,ri	
7	st [s(i+2) word1]	ld [s(i+1) word2]		set r0,r1	macc rw,ri	act [s(i-1) word0]
8	st [s(i+2) word2]		set [w3 w4 w5 w6]			act [s(i-1) word1]
9	ld [s(i+2) word0]	ld [s(i+2) word1]	shift	set r2 shift	macc rw,ri	
10	ld [w7 w8 -]	ld [s(i+2) word2]	shift	shift	macc rw,ri	
11			shift	set r0,r1	macc rw,ri	
12			set [w7 w8 -]	set r2 shift	macc rw,ri	
13			shift	shift	macc rw,ri	
14					macc rw,ri	

Figure 7.8: Finished instruction schedule for 3x3 convolution with store operations assigned to the free memory port A slots.

### 7.4.3 Scratchpad memory allocation

The last step in completing an accelerator program is assigning scratchpad memory locations to the load/store operations in the instruction schedule. Due to our dedicated Address Generation Units (AGUs) each address consist three fields: *offset*; *update*; and *mode* field. Along with *toggle* and *increment* register settings, the address field can produce *modulo* addressing patterns. Allocation starts at address 0 for the prologue part, since the prologue is executed only once all the addressing is static, so the offset field is assigned to contain the address and the other parameters are set to 0 to prevent updates.

In the steady-state part the pixel store and load operations are assigned with *modulo* addressing. This is done by assigning a base address pointing to the first pixels in the buffer which are used by this instruction. To perform modulo addressing an automatic increment value is set, which is defined by the subsample stride parameter. In addition, a toggle value is used to trigger the jump back after the last value in the kernel sequence is loaded. Coefficient load operations again use static addressing, because their location does not change. The scratchpad memory operation assignment is outlined in Algorithm 8.3.

---

#### ALGORITHM 8.3: Buffer Allocation

---

**input:** schedule  $X$ , consists of prologue  $X_p$ , and steady-state  $X_s$   
**output:** allocated schedule  $X$ , toggle and increment register settings

```

1  addr ← 0;
2  base ← 0;                               //start point of feature map values
3  foreach memory operation  $v$  in  $X_p$  do
4     $v.offset$  ← addr;
5    if  $v$  is first feature map operation then
6      base ← addr;                         //set feature map start point
7    end
8    addr++;
9     $v.update$  ← 0;                        //no update value for prologue
10    $v.mode$  ← 0;                          //static address mode 0
11  end
12  if base = 0 then
13    base ← addr;                          //no prolog feature map values
14  end
15  foreach store operation  $v$  in  $X_s$  do
16     $v.offset$  ← base;                     //start store sequence
17     $v.update$  ← addr - base;             //iteration jump
18     $v.mode$  ← 1;
19    addr++;
20  end
21  toggle ←  $N$  kernel loads;              //img register loads in kernel iteration
22  inc ← pooling step;                    //img register load offset between tiles
23  addr ← 0;
24  foreach load operation  $v$  in  $X_s$  do
25    if load coefficients then
26       $v.offset$  ← addr;                 //coefficients are static

```

---

---

```

27     v.update ← 0;           //no updating of addresses
28     v.mode ← 0;
29     addr++;
30     end
31 end
32 addr ← 0;
33 foreach load operation v in Xs do
34     if load feature map then
35         v.offset ← base;     //start load sequence
36         v.update ← addr;
37         v.mode ← 1;
38         addr++;
39     end
40 end

```

---

#### 7.4.4 Generalization towards VLIW architecture

The CONVE compiler framework is designed with flexibility in mind. In case the instantiation of an NVE core changes (see parameters in Figure 6.7) small modifications to the task graph construction procedure are required. These techniques are well-known from VLIW processor design e.g. Tensilica Xtensa [57] or the Silicon Hive [135] tools. For example, when instructions are added or removed the operators in the task graph should be changed accordingly based upon the new set of operations. Additionally, the dependencies among vertices can change based upon modifications in the processing pipeline. Instruction scheduling is adapted mainly in the resource conflict resolution scheme. For example, the use of a single port scratchpad memory changes the resource allocation table.

The memory address allocation is rather specific due to the use of AGUs. In case the AGUs are removed addresses would be static which removes the huge advantages of inter-tile reuse patterns. Note that dedicated Caches could largely solve these issues at the cost of an area and energy penalty. Finally the translation of a new instruction scheme into executable binaries is straight forward but it must comply with the VLIW slots of the architecture.

From this point onwards different architecture variants can be explored. Consider a case where the NVE instance has more scratchpad memory ports, e.g. a dedicated port assigned to each set register operation this to remove conflict nop operations. Another example would be doubling the size of the vector MACC unit, which will result in more image register operations in case the vector memory size of 8 byte is kept. All these alternatives could be explored in future work to find good *performance/area/energy* configurations.

## 7.5 Advanced code optimizations

Compiling high-level program descriptions into correct assembly programs is essential for any accelerator. Without such tools mapping of complicated tasks would become almost impossible. Another aspect is the code quality, ideally it performs similar to a manual mapping. However, often an automatic compiler path generates low-quality code, reducing the energy and performance advantages of dedicated architectures like the NVE. In this section we focus on advanced code optimizations to generate code that performs on-par with an expert programmer.

Careful analysis of manual (Figure 6.10) and default compiler (Figure 7.8) generated schedules reveals that the later one reduces throughput by 1.4 times. Generated instruction schedules contain more NOP gaps due to resource conflicts and idle time between steady-state iterations. Furthermore, there is no data locality optimization for shared inputs over output feature maps. The following optimizations sections will improve performance by addressing these three missing optimization steps.

### 7.5.1 Coefficient layout optimizations

Register load port sharing is one of the architecture constraints that sometimes inserts NOP gaps since the `set register` of a weight and image register cannot execute in the same cycle. The default compiler resolves such resource conflicts by delaying one of the operations, which causes a NOP in the VMACC slot. This is illustrated in the task graph of Figure 7.4 and the instruction schedule of Figure 7.5. An expert programmer resolves such conflicts by off-line altering coefficient layout of scratchpad vectors. As a result, a weight set and shift operation can be interchanged which often avoids the conflict and the inserted NOP. Our compiler uses a similar coefficient packing procedure in the task graph generation step that reduces the number of weights in a vector before a conflict occurs. This procedure imitates the manual optimization strategy. Note that this procedure does not always solve the conflicts, sometimes the upper load port is over-utilized. For example, in the  $1\times 1$  convolution benchmark there is no image register reuse and therefore every cycle a set register operation is requested. Without insertion of stalls there are simply no free slots to load the weight register (see Figure 7.6 and Figure 7.7). In these cases our compiler accepts the penalty and packs the weight vectors with the maximum number of weights.

### 7.5.2 Modulo scheduling

Modulo scheduling is implemented by measuring the *Resource Minimum Initiation Interval* (ResMII), which is defined by the issue slot that requires the longest sequence of execution cycles. The ResMII is used to wrap the schedule and con-

Cycle	MEM A	MEM B	WREG	IREG	VMACC	VACT
1	st [s(i+2) word0]		shift	set r0,r1	macc rw,ri	
2	ld [b w0 w1 - ]		shift	set r2 shift	macc rw,ri	
3	ld [s(i+0) word0]	ld [s(i+0) word1]	shift	shift	macc rw,ri	
4	st [s(i+2) word1]	ld [s(i+0) word2]	set [b w0 w1 - ]		macc rw,ri	
5	ld [w2 w3 w4 - ]		shift	set r0,r1	set rw	
6	ld [s(i+1) word0]	ld [s(i+1) word1]	shift	set r2 shift	macc rw,ri	
7	st [s(i+2) word2]	ld [s(i+1) word2]	set [w2 w3 w4 - ]	shift	macc rw,ri	
8	ld [w5 w6 w7 w8]		shift	set r0,r1	macc rw,ri	act [s(i-1) word0]
9	ld [s(i+2) word0]	ld [s(i+2) word1]	shift	set r2 shift	macc rw,ri	act [s(i-1) word1]
10		ld [s(i+2) word2]	set [w5 w6 w7 w8]	shift	macc rw,ri	

**Figure 7.9:** The resulting schedule after modulo rescheduling. Instructions in red belong to a previous iteration.

tinue scheduling at modulo ResMII positions i.e.,  $t_{\text{new}} = t_{\text{old}} \bmod(\text{ResMII})$ . Figure 7.9 demonstrates the beneficial effect of modulo scheduling, which is applied directly after instruction scheduling. Resource under-utilization problems at the start and end of a schedule are removed and maximum utilization of the VMACC unit is achieved.

### 7.5.3 Feature map combining

ConvNet layers often have feature maps that share input maps e.g., see layer 2 in our benchmark workloads Figure 3.3 and Figure 3.4 in Chapter 3. Reusing input maps in the scratchpad improves locality, however due to the sparse nature of feature map connections it is challenging to find the best combination that maximize locality for a fixed capacity constraint.

Consider two feature maps  $I_0 = [0,1,2,3]$  and  $I_1 = [1,2,3,4]$  where the array defines connected input maps. These maps share three inputs that can be reused when the schedules are combined. Using the maximum intersection does not guarantee an optimal reuse solution. Suppose, three input sets  $I_0 = [0,1,2,3]$ ,  $I_1 = [1,2,3,4]$ , and  $I_2 = [1,3,5]$ , and  $I_3 = [0,2,4]$  are given. The possible combinations are:

- Combining  $I_0 - I_1$  that share three maps.
- All combinations where  $I_0$  or  $I_1$  is combined with either  $I_2$  or  $I_3$  share two maps.
- Combining  $I_2 - I_3$  that do not share any map.

A greedy approach combines the largest intersection and therefore it starts with  $I_0I_1$  to share three maps. It could happen that no further combining is possible, because the data buffer is full or the instruction buffer cannot hold larger programs. The other combination would be  $I_2I_3$  which have no reuse. A full-search method would have combined  $I_0I_4$  and  $I_1I_3$ , both reuse two feature maps. As a result the full-search would reuse 4 maps where the greedy solution reuses 3 maps.

In practice it is very challenging to take all constraints into account. Programs must fit into the instruction buffer, and the data buffer has a capacity constraint. Full-search always gives the best result at the cost of excessive search

time for large layers. As a trade-off we implemented greedy feature map combining. For many layers our greedy scheduling finds a solution close to the optimum and is already much better than not combining at all.

Algorithm 8.4 lists our combining procedure, where  $L$  holds individual schedules and  $R$  a list of combined programs. First, it searches for the program with the largest number of input featuremaps. The selected featuremap is combined with another map that gives: 1) Minimizes the difference  $\alpha$  of input maps; 2) Obtain the largest intersection  $\beta$ . This repeats until the scratchpad buffer or the instruction buffer is filled and the program  $f$  can be stored as a valid schedule. Next, the procedure repeats for the remaining featuremaps until all maps are stored. Featuremap combining is performed before modulo scheduling, since the modulo operation merges a program across iterations, which makes it difficult to insert another featuremap. Combining featuremaps and afterwards performing modulo scheduling is much simpler and gives benefit of both optimizations. Note that modulo scheduling is tested after every new combination to validate the instruction memory capacity constraint.

---

**ALGORITHM 8.4:** Feature Map Fusion
 

---

```

input: list of individual feature map schedules  $L$ 
output: list of combined schedules  $R$ .
  1  $f \leftarrow$  first schedule in  $L$ ;
  2 foreach schedule  $v$  in list  $L$  do
  3   if  $s_v > s_f$  then
  4      $f \leftarrow v$ ;
  5   end
  6 end
  7 remove  $f$  from  $L$ ;
  8  $g \leftarrow f$ ; //take featuremap with the most input maps
  9 while  $L$  is not empty do
 10    $\alpha \leftarrow \infty$ ; //non overlapping input featuremaps
 11    $\beta \leftarrow 0$ ; //overlapping input featuremaps
 12   foreach schedule  $v$  in list  $L$  do
 13     if  $|I_f \Delta I_v| < \alpha$  then; //symmetric difference should be small
 14        $\alpha \leftarrow |I_f \Delta I_v|$ ; //featuremaps without reuse are minimized
 15        $\beta \leftarrow |I_f \cap I_v|$ ;
 16        $c \leftarrow v$ ;
 17     else if  $|I_f \Delta I_v| = \alpha$ 
 18       if  $|I_f \cap I_v| > \beta$  then //more reuse is preferred
 19          $\alpha \leftarrow |I_f \Delta I_v|$ ;
 20          $\beta \leftarrow |I_f \cap I_v|$ ;
 21          $c \leftarrow v$ ;
 22     end
 23   end
 24   end
 25    $g \leftarrow$  combination of  $g$  and  $c$ ;
 26    $h \leftarrow g$ ;
 27   modulo scheduling  $h$ ;
  
```

---



---

```

28  if  $s_h > \text{INSTRUCTION\_BUFFER\_SIZE}$  then
29      modulo scheduling  $f$ ; //revert previous solution and add to list
30      insert  $f$  to  $R$ ;
31       $f \leftarrow$  first schedule in  $L$ ;
32      foreach schedule  $v$  in list  $L$  do
33          if  $s_v > s_f$  then
34               $f \leftarrow v$ ;
35          end
36      end
37      remove  $f$  from  $L$ ;
38       $g \leftarrow f$ ;           //select featuremap with the most input maps
39      else
40           $f \leftarrow g$ ;       //continue combining with the current set
41          remove  $c$  from  $L$ ;
42      end
43 end

```

---

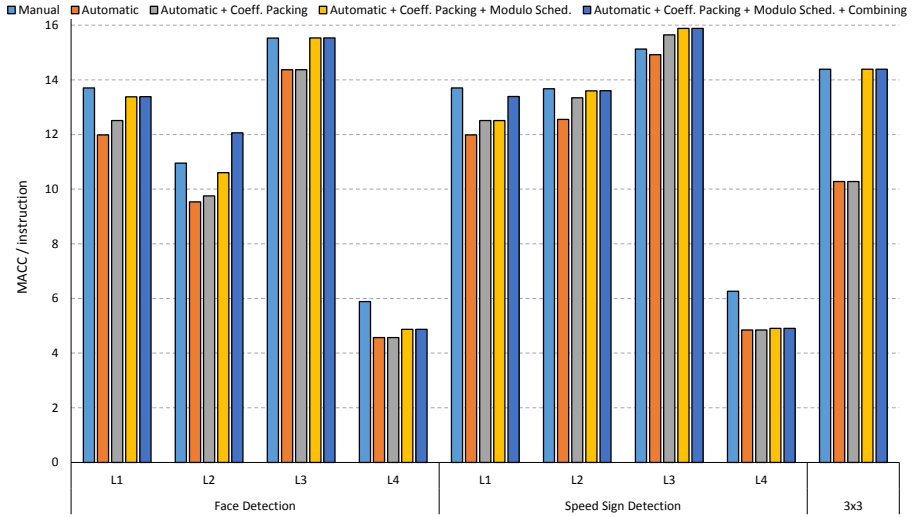
## 7.6 Experimental evaluation

To understand the performance of the NVE an ARM-based processor is used as a baseline reference platform. An ARM Cortex A9 is chosen since it is used in many mobile devices and represents the performance of currently available embedded computing solution in the market. This ARM platform is compared with an instance of the NVE template to measure the differences in performance. Firstly both platforms are discussed in detail.

### 7.6.1 Experimental setup

The general purpose ARM architecture has many variants for a wide range of embedded applications. In this experiment the ARM Cortex-A9 is used as a baseline. The core has a 64-bit wide NEON SIMD coprocessor that enables acceleration by exploiting sub word parallelism. The NEON coprocessor can perform up to four 16-bit operations or eight 8-bit operations per cycle. The NEON optimized code can either be generated by the compiler or manually written using NEON intrinsic or assembly code.

The NVE instance is implemented on the Zynq SoC which uses an ARM Cortex-A9 as host processor. The interconnects use the AXI standard interfaces for interconnection with the FPGA part. Our setup uses the AXI-Lite interfaces for setting control registers and high bandwidth AXI-Stream interface for data communication. These data streams consist of instructions, coefficients, and pixels or neuron values. The AXI-Stream interfaces are connected to dedicated Direct Memory Access (DMA) devices with scatter-gather transfer modes. The scatter-gather mechanism provides a sequence of individual transfers without the need of new commands by using a sequence of Buffer Descriptor (BD). The BDs are arranged as a linked-list and each of them contains information of a new transfer



**Figure 7.10:** HW utilization comparison of manually written programs versus multiple performance settings of the automatically generated programs.

such as starting address, size, and pointer to the next BD. The ARM core places the BDs in memory after which it initiates the execution sequence. Then the DMAs automatically fill the instruction memory, and continue with pixel processing. Our code correctness is verified by executing generated programs for our face detection and speed sign detection workloads (see Chapter 3).

## 7.6.2 Performance metrics

Our definition of code quality is the number of computations (effective MACCs) per VLIW instruction. This represents only effective workload, but note that there are many load/store ops., and data reorder ops. that are neglected by this definition. Low quality code has a low MACC unit utilization due to NOP slots in the pipeline or loop overhead (additional prolog/epilog code to start and finish a loop). Additionally, the amount of external data transfer is important. Firstly, it can stall the pipeline if DMAs cannot keep up with the accelerator, and secondly it is often bad for energy consumption.

## 7.6.3 Performance analysis

CONVE generated code quality is evaluated by comparison against manual coding by architecture experts. These experts spent days to write and optimize a complete ConvNet assembly program which is generated in a few seconds by our compiler. Figure 7.10 summarizes the performance on our benchmarks for different optimization flows. For example, the first graph gives the performance of manual mapping, compared to the second (CONVE without optimization) the

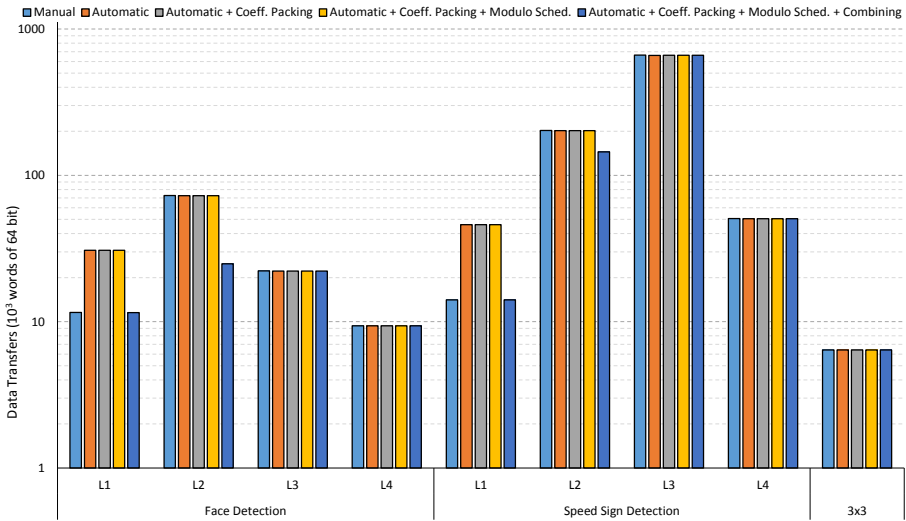
manual mapping achieves a 7 up to 28% better MACC unit utilization. This indicates that the default CONVE flow is already quite competitive to a fine-tuned manual mapping.

The set of bars on the left hand side shows performance on the educational example of a  $3 \times 3$  convolution. Both steady-state schedules with 10 instructions manual and 14 automatic is relatively short, therefore the relative performance difference is large. In a dense workload like layer 3 of our speed sign application the difference is relatively small. Both steady-state schedules contain over 200 instructions. This example shows that workloads will behave different and it is not always obvious why code under-performs. For very long schedules the effect of missing modulo scheduling is relatively small, since the borders of a schedule represent a minor portion. On the other hand, for short schedules like in our  $3 \times 3$  convolution this effect is very dominant.

The first optimization performs resource conflict resolving through *coefficient layout optimization*, which reduces the number of NOP slots. On average coefficient repacking improves performance by 2%. For layer 3 of the speed sign detection workload the schedule compresses enough to beat the manual expert. This is an example where the schedule was too complicated for our manual expert programmer, hence he could not find all optimizations. For some short schedules like  $3 \times 3$  convolution the removal of NOP slots does not reduce the schedule length, which is due to the necessary stores in the scratchpad memory.

The second optimization reduces under-utilization between iterations of the schedule by modulo scheduling. Modulo scheduling on average gives an additional performance improvement of 7%. With modulo scheduling most benchmark layers perform very close to the manual implementation. For the very dense ConvNet layers like layer 3 the performance is very important since they represent the major part of application workload. It is clear that for these dense layers the performance is close to the accelerator peak performance of 16 MACCs per instruction. For the other layers the performance lacks behind, which is often caused due to communication bandwidth limitations on the local scratchpad ports. Layer 1 and 2 of both applications contain a  $2 \times 2$  pooling which increases the data volume for 16 parallel convolution results. In layer 4 there is even less register reuse due to  $1 \times 1$  convolution operations. Both configurations stress the scratchpad memory bandwidth.

The final optimization under evaluation is featuremap combining which increases data locality. For some layers the number of scratchpad store operations are reduced which gives a performance increase, see Figure 7.10. More important is the data communication reduction with external memory. Figure 7.11, reveals that featuremap combining is sometimes needed to perform on-par with the manual experts. Due to our efficient inter-tile execution patterns data-reuse in convolution windows and over input featuremaps is already very well utilized. Mostly the sparsely connected layers such as layer 1 and 2 benefit from this optimization. Note the large communication reductions on the logarithmic scale. In very dense layers the instruction loop buffer with only 512 entries prevents



**Figure 7.11:** Data transfer comparison of manually written programs versus different configurations of automatically generated programs.

combining feature maps. To enable combining for these layers a larger instruction buffer and a larger scratchpad memory are required.

Combining all optimizations improves MACC unit utilization up to 16.5%. However for some layers like output layer 4 of the benchmarks CONVE generated schedules perform 20% worse than the manual code. In this case the manual programmer uses half vectors (8 MACC operations), which is not yet available in CONVE. For the evaluated NVE instance the half vectors reduce load pressure from scratchpad port A. Remember that layer 4 is only a small portion of the total workload. The performance of the complete benchmark applications (all layers) is better for the CONVE generated code. In conclusion for very specific workloads (layer 4) the manual programmer is the better one, but for large complicated workloads CONVE performs better, see layer 3. In addition, our featuremap combining step improves data locality at the cost of more complicated schedules. A manual programmer faces a huge challenge when he has to implement such combinations. It is simply difficult to overlook the huge set of schedule combinations and match those with the many platform constraints.

## 7.7 Conclusions

Dedicated hardware accelerators for Convolutional Networks (ConvNets) have substantially improved the computational efficiency of this challenging algorithm. One of the remaining bottlenecks for broad usage of such accelerators is the large complexity involved when programming such accelerators. For many of the proposed accelerators this problem is simply ignored, as a result these

accelerators are often not used in embedded platforms due to their huge mapping complexity.

We demonstrated with our new COmpiler for Neuro Vector Engines (CONVE) that optimized accelerator code for VLIW based vector accelerators can be generated from high-level .JSON ConvNet descriptions. This technique is very generic and straight forward such that it can be applied to different instances of the NVE template. By using advanced code optimization with Modulo Scheduling and data layout optimization CONVE generates codes that achieves hardware utilization levels on-par with code manually optimized by architecture experts. Due to techniques like inter-tile optimization and feature-map combining our generated code has better data locality, which reduces the challenging data transfer requirements.

The introduction of the CONVE flow enables users to abstract from the NVE accelerator architecture and only specify a ConvNet and choose an instance of the NVE Template. This abstraction reduces the programming workload for ConvNet vision application development from days to minutes. The removal of this last productivity bottleneck enables the adoption of ConvNets in the next-generation mobile and wearable devices. This step will bring 'intelligent' features like real-time machine vision and speech translation to our portable companions.

# CONCLUSIONS AND FUTURE WORK

*This chapter concludes the thesis. It is subdivided in two main sections. The first summarizes the conclusions of the individual chapters and reflects how these address the issues identified in the problem statement of Chapter 1. The second section presents some open issues that still remain to be solved, as well as, ideas that are not fully worked out and remain as future work.*

## 8.1 Conclusions

*Deep Learning and Convolutional Networks (ConvNets) have become increasingly popular as pattern recognition methods to solve complicated problems in many different domains. These machine learning techniques have set many new accuracy records and have shown super human performance on various tasks. However, for consumer applications in the mobile or wearable domain these impressive classifier models are not often used. The huge number of model parameters and the challenging compute workload make it difficult to use these nets on an ultra-low power platform. The general purpose CPUs and GPUs do not fit the power requirements and embedded processors do not deliver the required performance. The use of these techniques in embedded platforms is key to develop save autonomous driving solutions. Or it should give drones the intelligence to automatically navigate and deliver packages that are ordered remotely. In continuously operating or so called “always on” wearable companion devices, it could help us in daily tasks. For these reasons industry and academia have started to investigate different techniques to improve the energy efficiency of ConvNets. This has led to various results on high-level optimizations, dedicated function accelerators, and compilation frameworks for deployment.*

The problem statement (Chapter 1.4) defines the number of required compute operations as one of the key quantitative properties that influences the energy efficiency. Chapter 4 of this thesis addresses the huge computational

workload in ConvNets by an algorithmic transformation that merges Convolution and Averaging Pooling layers. Our technique can be used on trained networks with average pooling layers without sacrificing accuracy. On the other hand it can also be used to train new nets with merged layers, which enables approximation and replacement of nets having max pooling layers. Real benchmark applications demonstrate 65% to 83% workload reduction, without reducing accuracy. The impact of MACC workload reduction on compute performance is measured with a CPU and GPU platform mapping. Compared to the original convolution and subsample part the CPU mapping is 2.7 times faster where the GPU mapping improves 2.5 times. An efficiency improvement of 2.5-2.7 times is a first step towards mapping on power constrained platforms. The important part is that this optimization can be combined with other optimizations to achieve a much more aggressive efficiency improvement.

Another important other efficiency problems is data movement. The thesis problem statement defines the number of external memory transfers as a quantitative metric for data movement efficiency. Nowadays, data movement is responsible for a large portion of the consumed energy in compute platforms. Inter-tile data reuse optimization is a new tiling or blocking technique that considerably improves data reuse in nested loop accelerators. Before this work accelerators could exploit the data overlap between successive tiles, but not automatically shape the tiles to maximize this overlap. With real benchmarks we show that optimizing the tile shape for inter-tile reuse can further reduce external memory accesses up to 52% compared to an already aggressively optimized schedule. To exploit maximum inter-tile overlap we developed an analytical data reuse model that quickly gives the number of external accesses and the required buffer size to fit this schedule into a local scratchpad. With our model-based search approach we obtain the best schedules in mere seconds. These best schedules are evaluated with real FPGA mappings done by the Xilinx Vivado HLS tools. This resulted in a locality optimized design workflow that eases the mapping of ConvNets to dedicated hardware accelerators.

Dedicated function accelerators in FPGAs are a flexible alternative for CPUs and GPUs. To improve the energy-efficiency even further we propose the Neuro Vector Engine (NVE), a flexible accelerator template for ASIC implementation. The NVE performs extremely efficient SIMD operations on vector words. In addition, it has flexible VLIW-type control such that it can use layer merging and inter-tile reuse optimizations. This combines the optimizations from earlier chapters into an efficient accelerator template. Synthesis of a good performing instance of the template with a 40nm low power TSMC library demonstrated that the NVE is a very small design, requiring only 0.259 mm<sup>2</sup>. On our real world speed sign recognition benchmark and face detection application our 1 Ghz instance achieves 30.2 GOP/s. This is 20 times faster than our NEON optimized mappings on an ARM-A9 Core. In addition, it is benchmarked against CUDA optimized mappings for an NVIDIA TK1 embedded GPU. Depending on the layer configurations the NVE is 1.2 to 2.6 times faster than the GPU. Considering the ultra-low power consumption of NVE (only 54 mW), this is a very impressive

result. Especially the high degree of flexibility makes that our NVE has a high utilization which is important for efficiency. Many other accelerators are too dedicated to the convolution operation. As a result, they require more data movement, or have a low utilization during several stages of the algorithm; both reduce energy efficiency substantially.

This thesis has shown that dedicated accelerators can bridge the energy efficiency gap for ConvNets. However, the programmability of many accelerators can be improved a lot from both an architectural and a compiler perspective. The thesis problem statement defines the utilization level that a normal programmer can achieve when mapping different network workloads as a quantitative metric for flexibility, which again results into efficiency. Our work proposes a flexible VLIW instruction format for the NVE to obtain a very programmable architecture. In addition, the compiler part opens opportunities to improve application portability and designer productivity by abstracting away from target specific assembly languages. Our COmpiler for Neuro Vector Engines (CONVE) addresses the portability and productivity problems. By using an abstract .JSON network description the programmer does not have to think of architectural details. Also the application fine tuning is handled by the CONVE framework. Advanced code optimizations such as, *modulo scheduling*, and *feature map combining* ensure that an expert level of optimization is achieved automatically.

Although this thesis focused on a broad range of techniques to improve the computational efficiency of ConvNets, it is also applicable to a much broader application domain. Other image/video processing pipelines, such as *Motion Estimation* for video coding can benefit from the proposed contributions. Algorithms that require several *Linear Algebra* operations can be made much more efficient with the contributions of this thesis. In Chapter 5 we presented detailed evaluations of the effect of inter-tile reuse optimization for such applications. In addition the NVE is basically a vector processor that can accelerate these and many other workloads for the embedded domain. This also holds for the quickly developing field of Deep Learning. New network architectures that contain for instance residual nodes or recurrent nodes can benefit a lot from the ideas on inter-tile reuse and the NVE with the CONVE framework.

## 8.2 Future work

This thesis is written in a time where *Deep Learning* based algorithms became very popular. Nowadays many research groups are studying the efficiency problems in deep learning. Keeping up with the state-of-the-art was one of the major challenges for this work. This section will discuss limitations of this work with regard to new deep learning techniques. In addition, to a changing field with new contributions we encountered several opportunities for improvement of the various efficiency optimization techniques. Some of these opportunities deserve to be mentioned as possible extensions of the presented work.



*Network compression for further computational workload reduction:* Very recent works on workload reduction have further reduced the computational requirements [60,120]. For instance they perform advanced network pruning techniques that remove unnecessary parts in deep networks. This often reduces the required computational workload, but it makes networks less regular. Our layer merging technique and fixed point accuracy exploration from Chapter 4 had a similar goal. However, our early work from 2011 did not go as far as these new solutions. Still our work is very valuable next to other works. For example the Deep Compression work [60] focuses on reducing the weight set. The huge amount of intermediate neuron data per layer should still be communicated to larger memories. Their work could be further improved by merging layers like we did. This will reduce the intermediate data communication significantly. Another aspect is the regularity of the networks. Our reduction maintains a regular network structure where these newer techniques create very irregular and sparse structures. For these compute workloads it is difficult to achieve a high utilization. Future work into more advanced architectures is necessary to cope efficiently with very irregular compute workloads. Alternatively, we need different network compression techniques that enforce regular network structure to exploit existing computer architecture techniques such, as sub word parallelism by SIMD, and spatial locality by wide cache lines.

*Aggressive data locality optimization by layer fusion and re-computation:* Our work on inter-tile reuse optimization (Chapter 5) is an important technique to improve the data locality for deep ConvNets. However, we did not address the depth of the networks. Inter-tile optimizations are performed on single or a merged layer. New recent works exploit the data reuse over successive layers [2]. The difficulty in fusing layers is the growing set of data dependencies per layer. Before fusing two layers a portion of the first layer must be computed, next this portion is consumed by the second layer. This producer consumer relation and the fact that a larger portion from an early layer is required to compute a small portion of a later layer make it difficult to implement fusion efficiently. Also the work in [2] is challenged with these dependencies. They use sliding window tiles that contain a few fused layers. For these fused tiles a lot of local buffer space is required to meet the inter layer dependencies. We developed an early technique to fuse layers as addition to the inter-tile work. It is quite easy to interleave successive tile strips from succeeding layers. Our new method does even take re-computation of intermediate results into account to reduce the number of dependency constraints. As a result, an additional external traffic reduction of 1.5 to 2 times is demonstrated upon the best schedules of our inter-tile work. This work is presented on the NeuroArch workshop at ISCA 2014 [102]. At the time of writing this thesis we are working out the mathematical details of this improved data locality optimization technique.

*Improving the NVE template:* During our work on the NVE accelerator template we identified opportunities for further improvement. The NVE aims at the ultra-low power embedded SoC domain. Therefore, the energy efficiency is very

high at an effective compute throughput (in multiply and accumulate operations) in the range of 30 Gop/s. A silicon efficiency of 115 Gops/mm<sup>2</sup> and an energy efficiency of 559 Gops/W is demonstrated. Note that in addition to the 30 Gop/s of effective neuron operations a substantial amount of data re-order and address computation is performed by the dedicated function units. Scaling up the effective performance beyond 300 Gop/s is rather difficult. Wider vector processing gives a performance increase but, it reduces the vector MACC unit utilization and thereby the energy efficiency. To increase performance further a multiprocessor configuration should be developed. Since data sharing between processing nodes is key the multiprocessor design should have a flexible communication structure.

*Memory reordering units for the NVE:* The NVE benefits from excellent data locality in the computations due to inter-tile reuse optimization. This works very well if incoming and outgoing data streams are controlled by flexible Direct Memory Access (DMA) controllers. In a report [152] we show the first efforts towards flexible DMA devices. These can offer high bandwidth and flexibility. Further improvements on dedicated DMAs and the memory subsystem are important for accelerator developments.

*More efficient ConvNet operations:* As demonstrated in this thesis the computational workload in a ConvNet is dominated by MACC operations. To improve the efficiency at the operator level we could further improve these MACC operations. In a short study we looked into Carry Save Multiply Accumulates. It requires that the accumulator uses numbers in its carry save format. This significantly reduces the complexity of multiplications and the accumulations. Only after the last accumulation the independent sum and carry part should be combined with a more costly conventional adder. This technique could be further developed and used as a compute element in the NVE template to increase efficiency.

*Compute architecture for irregular ConvNets:* With the introduction of XNOR-net [120] and network compression techniques [60] their workload has become irregular. These new techniques have e.g. introduced the requirement to perform sparse matrix operations efficiently. However, from a compute perspective this opens new challenges for computational efficiency. The work in [59] is one of the first accelerator architectures that focusses on the irregular operations for compressed networks. These new works design advanced circuits to perform network operators very efficiently. However, these irregular workloads require a well-tuned ISA to achieve flexibility and efficiency. Maybe the ISA is even more important since the program control becomes more complicated. In addition, good compilers such as our CONVE framework are key to achieve good hardware utilization on such sparse network accelerators. Future work in these domains are important to further increase ConvNet efficiency.

# BIBLIOGRAPHY

- [1] C. Alias, A. Darte, and A. Plesco, "Optimizing Remote Accesses for Offloaded Kernels: Applications to high-level synthesis for fpga," in *Proceedings of the Conference on Design, Automation and Test in Europe (DATE '13)*, 2013, pp. 575-580.
- [2] M. Alwani, H. Chen, M. Ferdman, and P. Milder, "Fused-Layer CNN accelerators," in *49th Annual IEEE/ACM International Symposium on Microarchitecture (MICRO)*, 2016, pp. 1-12.
- [3] B. Bayer, "Color imaging array," US Patent 3,971,065, 1976.
- [4] H. Bay, T. Tuytelaars, and L. van Gool, "Surf: Speeded up robust features," in *Computer vision - ECCV*, 2006, pp. 404-417.
- [5] Y. Bengio, "Practical recommendations for gradient-based training of deep architectures," in *Neural Networks: Tricks of the Trade*, K.-R. Müller, G. Montavon, and G.B. Orr, Eds.: Springer, 2013, ch. 19.
- [6] K. Beyls and E.H. D'Hollander, "Refactoring for data locality," *Computer*, vol. 42, no. 2, pp. 62-71, 2009.
- [7] N. Binkert et al., "The gem5 simulator," *SIGARCH Computer Architecture News*, vol. 39, no. 2, pp. 1-7, 2011.
- [8] U. Bondhugula et al., "Automatic Transformations for Communication-minimized Parallelization and Locality Optimization in the Polyhedral Model," in *Proceedings of the Joint European Conferences on Theory and Practice of Software 17th International Conference on Compiler Construction*, 2008, pp. 132-146.
- [9] U. Bondhugula, A. Hartono, J. Ramanujam, and P. Sadayappan, "A practical and fully automatic polyhedral program optimization system," in *Proceedings of the 29th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI)*, 2008, pp. 101-113.
- [10] S. Borkar and A.A. Chien, "The future of microprocessors," *Communications of the ACM*, vol. 54, no. 5, pp. 67-77, 2011.
- [11] L. Bottou, "Large-scale machine learning with stochastic gradient descent," in *In Proceedings of COMPSTAT*, 2010, pp. 177-186.

- [12] L. Bottou, "Stochastic gradient descent tricks," in *Neural Networks: Tricks of the Trade.*: Springer, 2012, ch. 18, pp. 421-436.
- [13] L. Bottou et al., "Comparison of classifier methods: a case study in handwritten digit recognition," in *Proceedings of the 12th International Conference on Pattern Recognition and Neural Network*, 1994, pp. 77-82.
- [14] F. Catthoor et al., *Data access and storage management for embedded programmable processors.*: Springer Science & Business Media, 2013.
- [15] L. Cavigelli et al., "Origami: A convolutional network accelerator," in *25th edition of the ACM/IEEE Great Lakes Symposium on VLSI (GLS-VLSI)*, 2015, pp. 199-204.
- [16] Srimat Chakradhar, Murugan Sankaradas, Venkata Jakkula, and Srihari Cadambi, "A dynamically configurable coprocessor for convolutional neural networks," in *Proceedings of the 37th annual international Symposium on Computer Architecture*, 2010.
- [17] K. Chandrasekar, B. Akesson, and K. Goossens, "Improved Power Modeling of DDR SDRAMs," in *Euromicro Conference on Digital System Design (DSD)*, 2011, pp. 99-108.
- [18] K. Chellapilla, S. Puri, and P. Simard, "High performance convolutional neural networks for document processing," in *10th International Workshop on Frontiers in Handwriting Recognition*, 2006.
- [19] T.-C. Chen et al., "Analysis and architecture desing of an hdtv 720p 30 frames/s h264/avc encoder," *IEEE Transactions on Circuits and Systems for Video Technology*, pp. 16:673-688, 2006.
- [20] T. Chen et al., "DianNao: a small-footprint high-throughput accelerator for ubiquitous machine-learning," in *Proceedings of the 19th international conference on Architectural support for programming languages and operating systems*, 2014, pp. 269--284.
- [21] Y. Chen, J. Emer, and V. Sze, "Eyeriss: A Spatial Architecture for Energy-efficient Dataflow for Convolutional Neural Networks," in *Proceedings of the 43rd International Symposium on Computer Architecture (ISCA)*, Seoul, Republic of Korea, 2016, pp. 367-379.
- [22] Y. Chen, T. Krishna, J. Emer, and V. Sze, "Eyeriss: An energy-efficient reconfigurable accelerator for deep convolutional neural networks," in *IEEE International Solid-State Circuits Conference (ISSCC)*, 2016, pp. 262-263.
- [23] Y. Chen, Z. Lin, X. Zhao, G. Wang, and Y. Gu, "Deep Learning-Based Classification of Hyperspectral Data," *IEEE Journal of Slected Topics in Applied Earth Observations and Remote Sensing*, vol. 7, no. 6, pp. 2094-2107, June 2014.
- [24] W. Chen, J.T. Wilson, S. Tyree, K.Q. Weinberger, and Y. Chen, "Compressing neural networks with the hashing trick," in *Proceedings of*

- the 32nd International Conference on Machine Learning*, 2015, pp. 2285-2294.
- [25] D. Cireşan, A. Giusti, L.M. Gambardella, and J. Schmidhuber, "Deep Neural Networks Segment Neuronal Membranes in Electron Microscopy Images," *Advances in Neural Information Processing Systems* 25, pp. 2843-2851, 2012.
- [26] D.C. Cireşan, A. Giusti, L.M. Gambardella, and J. Schmidhuber, "Mitosis detection in breast cancer histology images with deep neural networks," in *Medical Image Computing and Computer-Assisted Intervention-MICCAI*, 2013, pp. 411-418.
- [27] D.C. Cireşan, U. Meier, L.M. Gambardella, and J. Schmidhuber, "Deep, big, simple neural nets for handwritten digit recognition," *Neural Computation*, vol. 22, no. 12, pp. 3207-3220, 2010.
- [28] D.C. Cireşan, U. Meier, J. Masci, J.M. Gambardella, and J. Schmidhuber, "Flexible, high performance convolutional neural networks for image classification," in *IJCAI Proceedings-International Joint Conference on Artificial Intelligence*, 2011, pp. 1237-1242.
- [29] D.C. Cireşan, U. Meier, J. Masci, and J. Schmidhuber, "A committee of neural networks for traffic sign classification," in *IJCNN International Conference on Neural Networks*, 2011, pp. 1918-1921.
- [30] D. Cireşan, U. Meier, J. Masci, and J. Schmidhuber, "Multi-column deep neural network for traffic sign classification," *Neural Networks*, vol. 32, pp. 333-338, 2012.
- [31] D.C. Cireşan, U. Meier, and J. Schmidhuber, "Multi-column deep neural networks for image classification," in *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2012, pp. 3642-3649.
- [32] A. Coates, B. Huval, T. Wang, D.J. Wu, and A.Y. Ng, "Deep learning with COTS HPC systems," in *Proceedings of the 30th international conference on machine learning*, 2013, pp. 1337-1345.
- [33] L. Codrescu et al., "Hexagon DSP: an Architecture Optimized for Mobile Multimedia and Communications," *IEEE Micro*, vol. 34, no. 2, pp. 34-43, March 2014.
- [34] R. Collobert, K. Kavukcuoglu, and C. Farabet, "Torch7: A matlab-like environment for machine learning," in *BigLearn, NIPS Workshop*, 2011.
- [35] F. Comaschi, S. Stuijk, T. Basten, and H. Corporaal, "RASW: a run-time adaptive sliding window to improve viola-jones object detection," in *Proceedings of 7th International Conference on Distributed Smart Cameras ICDSC*, 2013, pp. 1-6.
- [36] J. Cong and B. Xiao, "Minimizing computation in convolutional neural networks," in *International Conference on Artificial Neural Networks*, 2014, pp. 281-290.

- [37] F. Conti and L. Benini, "A Ultra-Low-Energy Convolution Engine for Fast Brain-Inspired Vision in Multicore Clusters," in *Proceedings of the Design, Automation & Test in Europe Conference & Exhibition*, 2015, pp. 683-688.
- [38] N. Dalal and B. Triggs, "Histograms of oriented gradients for human detection," in *IEEE Computer Society Conference on Computer Vision and Pattern Recognition CVPR*, 2005, pp. 886-893.
- [39] N. Dalal and B. Triggs, "Histograms of Oriented Gradients for Human Detection," in *Proceedings of the IEEE Computer Society Conference on Computer Vision and Pattern Recognition CVPR*, 2005, pp. 886-893.
- [40] A. Darte and A. Isoard, "Parametric Tiling with Inter-Tile Data Reuse," in *In 4th International Workshop on Polyhedral Compilation Techniques (IMPACT'14)*, 2014.
- [41] G. De Haan, P.W. Biezen, H. Huijgen, and O.A. Ojo, "True-motion estimation with 3-D recursive search block matching," *IEEE Transactions on Circuits and Systems for Video Technology*, vol. 3, no. 5, pp. 368-379, 1993.
- [42] R.H. Dennard, J. Cai, and A. Kumar, "A perspective on today's scaling challenges and possible future directions," *Solid-State Electronics*, vol. 51, no. 4, pp. 518-525, 2007.
- [43] G. Desoli et al., "A 2.9 Tops/w deep convolutional neural network soc in fd-soi 28nm for intelligent embedded systems," in *IEEE International Solid-State Circuits Conference*, 2017, pp. 238-239.
- [44] C. Ding and Y. Zhong, "Predicting Whole-program Locality Through Reuse Distance Analysis," in *PLDI '03*, 2003, pp. 245-257.
- [45] C. Ding and Y. Zhong, "Reuse Distance Analysis," University of Rochester, 2001.
- [46] Z. Du et al., "ShiDianNao: Shifting vision processing closer to the sensor," in *Proceedings of the 42nd Annual International Symposium on Computer Architecture ISCA*, Portland, Oregon, 2015, pp. 92-104.
- [47] D. Erhan et al., "Why does unsupervised pre-training help deep learning?," *Journal of Machine Learning Research*, pp. 625-660, 2010.
- [48] H. Esmaeilzadeh, E. Blem, R. St. Amant, K Sankaralingam, and D Burger, "Dark Silicon and the End of Multicore Scaling," in *38th Annual International Symposium on Computer Architecture (ISCA)*, 2011, pp. 365-376.
- [49] C. Farabet, C. Couprie, L. Najman, and Y. LeCun, "Learning hierarchical features for scene labeling," *Pattern Analysis and Machine Intelligence, IEEE Transactions on*, vol. 35, pp. 1915-1929, 2013.
- [50] C. Farabet et al., "Neuflow: A runtime reconfigurable dataflow processor for vision," in *IEEE Computer Society Conference on Computer Vision and Pattern Recognition Workshops (CVPRW)*, 2011, pp. 109-116.

- [51] C. Farabet, C. Poulet, J. Han, and Y. LeCun, "An FPGA-based processor for convolutional networks," in *International Conference on Field Programmable Logic and Applications FPL*, 2009, pp. 32-37.
- [52] J.A. Fisher, P. Faraboschi, and C. Young, *Embedded Computing: A VLIW Approach to Architecture, Compilers and Tools.*: Morgan Kaufmann, 2012.
- [53] C Garcia and M Delakis, "Convolutional face finder: a neural architecture for fast and robust face detection," *IEEE Transaction on Pattern Analysis and Machine Intelligence*, vol. 26, pp. 1408-1423, 2004.
- [54] R. Girshick, "Fast R-CNN," in *Proceedings of the IEEE International Conference on Computer Vision (ICCV)*, 2015.
- [55] R. Girshick, J. Donahue, T. Darrell, and J. Malik, "Rich feature hierarchies for accurate object detection and semantic segmentation," in *Proceedings of the IEEE conference on computer vision and pattern recognition*, 2014, pp. 580-587.
- [56] X. Glorot, A. Bordes, and Y. Bengio, "Deep Sparse Rectifier Neural Networks," in *14th International Conference on Artificial Intelligence and Statistics*, 2011, pp. 315-323.
- [57] R.E. Gonzales, "Xtensa: a configurable and extensible processor," in *IEEE Micro*, 2000, pp. 60-70.
- [58] R. Hameed et al., "Understanding sources of inefficiency in general-purpose chips," *ACM SIGARCH Computer Architecture News*, vol. 38, no. 3, pp. 37-47, 2010.
- [59] S. Han et al., "EIE: Efficient Inference Engine on Compressed Deep Neural Networks," in *Proceedings of the 43rd International Symposium on Computer Architecture (ISCA)*, 2016, pp. 243-254.
- [60] S. Han, H. Mao, and W.J. Dally, "Deep Compression: Compressing Deep Neural Networks with Pruning, Trained Quantization and Huffman Coding," in *International Conference on Learning Representations (ICLR)*, 2016.
- [61] S.O. Haykin, *Neural Networks and Learning Machines*, 3rd ed.: Prentice Hall, 2008.
- [62] K. He, X. Zhang, S. Ren, and J. Sun, "Deep Residual Learning for Image Recognition," arXiv preprint arXiv: 1512.03385, 2015.
- [63] K. He, X. Zhang, S. Ren, and J. Sun, "Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification," in *The IEEE International Conference on Computer Vision (ICCV)*, 2015, pp. 1026-1034.
- [64] G.E. Hinton, "Connectionist learning procedures," *Artificial intelligence*, vol. 40, no. 1, pp. 185-234, 1989.
- [65] G.E. Hinton, "Connectionist learning procedures," *Artificial intelligence*, vol. 40, no. 1, pp. 185-234, 1989.

- [66] G. Hinton et al., "Deep Neural Networks for Acoustic Modeling in Speech Recognition: The Shared Views of Four Research Groups," *Signal Processing Magazine, IEEE*, vol. 29, pp. 82-97, 2012.
- [67] G.E. Hinton, S. Osindero, and Y.W. Teh, "A fast learning algorithm for deep belief nets," *Neural computation*, vol. 18, no. 7, pp. 1527-1554, 2006.
- [68] G.E. Hinton and R.R. Salakhutdinov, "Reducing the dimensionality of data with neural networks," *Science*, vol. 313, no. 5786, pp. 504-507, 2006.
- [69] G.E. Hinton, N. Srivastava, A. Krizhevsky, I. Sutskever, and R. Salakhutdinov, "Improving neural networks by preventing co-adaptation of feature detectors," Technical Report, arXiv:1207.0580 2012.
- [70] J.L. Holi and J.N. Hwang, "Finite precision error analysis of neural network hardware implementations," *IEEE Transactions on Computers*, vol. 42, no. 3, pp. 281-290, 1993.
- [71] G. Huang, M. Mattar, H. Lee, and E.G. Learned-Miller, "Learning to align from scratch," *In Advances in Neural Information Processing Systems*, pp. 764-772, 2012.
- [72] Intel. ARK Processor Database. [Online]. <http://ark.intel.com/>
- [73] S. Ioffe and C. Szegedy, "Batch normalization: Accelerating deep network training by reducing internal covariate shift," in *ICML*, 2015.
- [74] I. Issenin, E. Brockmeyer, M. Miranda, and N. Dutt, "DRDU: A Data Reuse Analysis Technique for Efficient Scratch-pad Memory Management," *ACM Trans. Des. Autom. Electron. Syst.*, vol. 12, no. 2, 2007.
- [75] M. Jaderberg, A. Vedaldi, and A. Zisserman, "Speeding up convolutional neural networks with low rank expansions," arXiv preprint, arXiv:1405.3866 2014.
- [76] Y. Jia et al., "Caffe: Convolutional Architecture for Fast Feature Embedding," in *Proceedings of the 22nd ACM International Conference on Multimedia*, Orlando, Florida, USA, 2014, pp. 675-678.
- [77] N.P. Jouppi et al., "In-datacenter performance analysis of a tensor processing unit," in *Proceedings of the 44th Annual International Symposium on Computer Architecture (ISCA)*, 2017, pp. 1-12.
- [78] D. Kline and V. Berardi, "Revisiting squared-error and cross-entropy functions for training neural networks classifiers," *Neural Computing & Applications*, vol. 14, no. 4, pp. 310-318, 2005.
- [79] A. Krizhevsky, S. Ilya, and G.E. Hinton, "ImageNet Classification with Deep Convolutional Neural Networks 25," *Advances in Neural Information Processing Systems*, pp. 1097-1105, 2012.
- [80] M. Lam, "Software pipelining: an effective scheduling technique for VLIW machines," in *Proceedings of the ACM SIGPLAN conference on Programming language design and implementation (PLDI)*, 1988, pp. 318-328.



- [81] A. Lavin and S. Gray, "Fast algorithms for convolutional neural networks," arXiv preprint, preprint arXiv: 1509.09308, 2015.
- [82] Y. LeCun et al., "Backpropagation Applied to Handwritten Zip Code Recognition," *Neural Computation*, vol. 1, no. 4, pp. 541-551, 1989.
- [83] Y. LeCun et al., "Handwritten Digit Recognition with a Back-propagation Network," *Advances in Neural Information Processing Systems NIPS 2*, pp. 396-404, 1990.
- [84] Y. Lecun, L. Bottou, Y. Bengio, and P. Haffner, "Gradient-based learning applied to document recognition," *Proceedings of the IEEE*, vol. 86, no. 11, pp. 2278-2324, Nov 1998.
- [85] Y. LeCun, F.J. Huang, and L. Bottou, "Learning methods for generic object recognition with invaricance to pose and lighting," in *Proceedings of the Computer Society Converncde on Computer Vision and Pattern Recognition CVPR*, 2004, pp. 97-104.
- [86] Y. LeCun, U. Muller, J. Ben, E. Cosatto, and B. Flepp, "Off-road obstacle avoidance through end-to-end learning," *Advances in Neural Information Processing Systems*, pp. 739-746, 2005.
- [87] Q.V. Le et al., "Building high-level features using large scale unsupervised learning," in *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, 2013, pp. 8595-8598.
- [88] S. Li et al., "Mcpat: An integrated power, area, and timing modeling framework for multicore and manycore architectures," in *Proceedings of the 42nd Annual IEEE/ACM International Symposium on Microarchitecture*, 2009, pp. 469-480.
- [89] W. Liu et al., "SSD: Single Shot MultiBox Detector," in *European conference on computer vision (ECCV)*, 2016.
- [90] Q. Liu, G.A. Constantinides, K. Masselos, and P.Y.K. Cheung, "Combining Data Reuse With Data-Level Parallelization for FPGA-Targeted Hardware Compilation: A Geometric Programming Framework," in *IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems*, vol. 28, no. 3, pp. 305-315, 2009.
- [91] D.G. Lowe, "Object recognition from local scale-invariant features," in *Proceedings of the 7th IEEE International Coference on Computer Vision*, 1999, pp. 1150-157.
- [92] R. Malvar, L. He, and R. Cutler, "High-Quality Linear Interpolation for Demosaicing of Bayer-Patterned Color Images," in *IEEE International Conference of Acoustic, Speech and Signal Processing*, 2004.
- [93] J. Ma, R.P. Sheridan, A. Liaw, G.E. Dahl, and V. Svetnik, "Deep Neural Nets as a Method for Quantitative Structure-Activity Relationships," *Journal of Chemical Information and Modeling*, vol. 55, no. 2, pp. 263-274, 2015.

- [94] W.S. McCulloch and W. Pitts, "A logical calculus of the ideas immanent in nervous activity," *Bulletin of Mathematical Biophysics*, vol. 5, pp. 115-133, 1943.
- [95] S. Mehta, G. Beeraka, and P.-C. Yew, "Tile size selection revisited," *ACM Trans. Archit. Code Optim.*, vol. 10, no. 4, pp. 35:1-35:27, 2013.
- [96] G.E. Moore, "Cramming more components onto integrated circuits.," *Electronics*, vol. 38, no. 8, April 1965.
- [97] N. Muralimanohar, R. Balasubramonian, and N. Jouppi, "Optimizing NUCA Organizations and Wiring Alternatives for Large Caches with CACTI 6.0," in *40th Annual IEEE/ACM International Symposium on Microarchitecture (MICRO)*, 2007, pp. 3-14.
- [98] Y.-Y. Nguwi and S.-Y. Cho, "Emergent self-organizing feature map for recognizing road sign images," *Neural Computing and Applications*, vol. 19, no. 4, pp. 601-615, 2010.
- [99] D. Nistér and H. Stewénus, "Scalable recognition with a vocabulary tree," in *IEEE Computer Society Conference on Computer Vision and Pattern Recognition CVPR*, 2006, pp. 2161-2168.
- [100] "NVIDIA Jetson TK1 Development Kit, Bringing GPU accelerated computing to Embedded Systems," Technical Brief 2014.
- [101] Nvidia, "NVIDIA CUDA C Programming Guide 3.2," NVIDIA Corporation, 2010.
- [102] M. Peemen, B. Mesman, and H. Corporaal, "A Data-Reuse Aware Accelerator for Large-Scale Convolutional Networks," in *Workshop on Neuromorphic Architectures (NeuroArch)*, 2014.
- [103] M. Peemen, B. Mesman, and H. Corporaal, "Efficiency Optimization of Trainable Feature Extractors for a Consumer Platform," in *Advanced Concepts for Intelligent Vision Systems*, 2011, pp. 293-304.
- [104] M. Peemen, B. Mesman, and H. Corporaal, "Inter-tile reuse optimization applied to bandwidth constrained embedded accelerators," in *Design Automation and Test in Europe (DATE)*, Grenoble, France, 2015.
- [105] M. Peemen, B. Mesman, and H. Corporaal, "Speed sign detection and recognition by convolutional neural networks," in *8th International Automotive Congress*, Eindhoven, 2011.
- [106] M. Peemen, W. Pramadi, B. Mesman, and H. Corporaal, "VLIW code generation for a convolutional network accelerator," in *In proceedings of the 18th International Workshop on Software and Compilers for Embedded Systems*, 2015, pp. 117-120.
- [107] M. Peemen, W. Pramadi, B. Mesman, and H. Corporaal, "VLIW Code Generation for a Convolutional Network Accelerator," in *Proceedings of the 18th International Workshop on Software and Compilers for Embedded Systems (SCOPES)*, 2015, pp. 117-120.

- [108] M. Peemen, A.A.A. Setio, B. Mesman, and H. Corporaal, "Memory-centric accelerator design for convolutional neural networks," in *Computer Design (ICCD), IEEE 31st International Conference on*, Ashville, 2013.
- [109] M. Peemen et al., "The neuro vector engine: flexibility to improve convolutional net efficiency for wearable vision," in *Design, Automation & Test in Europe Conference & Exhibition (DATE)*, Dresden, 2016, pp. 1604-1609.
- [110] P.H. Pham et al., "Neuflow: Dataflow vision processing system-on-a-chip," in *IEEE 55th International Midwest Symposium on Circuits and Systems*, 2012, pp. 1044-1047.
- [111] L.-N. Pouchet et al., "Loop Transformations: Convexity, Pruning and Optimization," in *Proceedings of the 38th Annual ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages*, 2011, pp. 549-562.
- [112] L.-N. Pouchet, P. Zhang, P. Sadayappan, and J. Cong, "Polyhedral-based Data Reuse Optimization for Configurable Computing," in *Proceedings of the ACM/SIGDA International Symposium on Field Programmable Gate Arrays*, 2013, pp. 29-38.
- [113] W. Qadeer et al., "Convolution Engine: Balancing Efficiency and Flexibility in Specialized Computing," *Communications ACM*, vol. 58, no. 4, pp. 85-93, March 2015.
- [114] W. Qadeer et al., "Convolution Engine: Balancing Efficiency and Flexibility in Specialized Computing," in *Proceedings of the 40th Annual International Symposium on Computer Architecture*, 2013, pp. 24-35.
- [115] N. Qian, "On the momentum term in gradient descent learning algorithms," *Neural Networks*, vol. 12, no. 1, pp. 145-151, 1999.
- [116] J. Ragan-Kelley, *Decoupling algorithms from the organization of computation for high performance image processing.*: Ph.D. Dissertation. Massachusetts Institute of Technology., 2014.
- [117] J. Ragan-Kelley et al., "Halide: a language and compiler for optimizing parallelisms, locality, and recomputation," in *Proceedings of the 34th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI)*, 2013, pp. 519-530.
- [118] R. Raina, A. Madhavan, and A.Y. Ng, "Large-scale Deep Unsupervised Learning Using Graphics Processors," in *Proceedings of the 26th Annual International Conference on Machine Learning*, 2009, pp. 873-880.
- [119] M. Ranzato, C. Poultney, S. Chopra, and Y. LeCun, "Efficient learning of sparse representations with an energy-based model," *Advances in Neural Information Processing Systems 19*, pp. 1137-1144, 2006.
- [120] M. Rastegari, V. Ordonez, J. Redmon, and A. Farhadi, "XNOR-Net: ImageNet Classification Using Binary Convolutional Neural Networks," arXiv preprint, arXiv:1603.05279 2016.

- [121] J. Redmon, S. Divvala, R. Girshick, and A. Farhadi, "You Only Look Once: Unified, Real-Time Object Detection," in *The IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2016.
- [122] S. Ren, K. He, R. Girshick, and J. Sun, "Faster R-CNN: Towards real-time object detection with region proposal networks. ," in *Advances in neural information processing systems.*, 2015.
- [123] F. Rosenblatt, "The Perceptron: A probabilistic model for information storage and organization in the brain," *Psychological Review*, vol. 65, pp. 386-408, 1958.
- [124] H. Rowley, S. Baluja, and T. Kanade, "Neural network-based face detection," *IEEE Transactions on Pattern Analysis and Machine Intelligence*, vol. 20, pp. 22-38, 1998.
- [125] D.E. Rumelhart and J.L. McClelland, *Parallel Distributed Processing: Explorations in the Microstructure of Cognition*, 1st ed. Cambridge, MA: MIT Press, 1986.
- [126] O. Russakovsky et al., "ImageNet Large Scale Visual Recognition Challenge," *International Journal of Computer Vision*, vol. 115, no. 3, pp. 211-252, 2015.
- [127] T.N. Sainath, A.-R. Mohamed, B. Kingsbury, and B. Ramabhadran, "Deep convolutional neural networks for LVCSR," in *Acoustics, Speech and Signal Processing (ICASSP), 2013 IEEE International Conference on*, 2013, pp. 8614-8618.
- [128] M. Sankaradas et al., "A Massively Parallel Coprocessor for Convolutional Neural Networks," in *IEEE International Conferenc on Application -specific Systems, Architectures and Processors*, 2009, pp. 53-60.
- [129] N. Satish et al., "Can Traditional Programming Bridge the Ninja Performance Gap for Parallel Computing Applications?," in *In ISCA 39*, 2011, pp. 440-451.
- [130] T.J. Sejnowski and C.R. Rosenberg, "Parallel networks that learn to pronounce English text," *Complex Systems*, vol. 1, pp. 145-168, 1987.
- [131] P. Sermanet et al., "Overfeat: Integrated recognition, localization and detection using convolutional networks," in *International Conference on Learning Representations (ICLR)*, 2013.
- [132] D. Shin, J. Lee, J. Lee, and H.J. Yoo, "DNPU: an 8.1TOPS/W reconfigurable CNN-RNN processor for general-purpose deep neural networks," in *IEEE International Solid-State Circuits Conference*, 2017, pp. 240-241.
- [133] J. Shirako et al., "Analytical bounds for optimal tile size selection," in *in Proceedings of the 21st International Conference on Compiler Construction*, 2012, pp. 101-121.

- [134] R. Shiveley. (2008) Performance scaling in the multi-core era. [Online]. <http://software.intel.com/en-us/articles/performance-scaling-in-the-multi-core-era>
- [135] Silicon Hive, "Silicon Hive Technology Primer," Phillips Electronics NV, The Netherlands, 2003.
- [136] D. Silver et al., "Mastering the game of Go with deep neural networks and tree search," *Nature*, vol. 529, pp. 484-489, January 2016.
- [137] P.Y. Simard, D. Steinkraus, and J.C. Platt, "Best Practices for Convolutional Neural Networks Applied to Visual Document Analysis," *Proceedings of the Seventh International Conference on Document Analysis and Recognition*, vol. 2, pp. 958-962, 2003.
- [138] K. Simonyan and A. Zisserman, "Very Deep Convolutional Networks for Large-Scale Image Recognition," in *International Conference on Learning Representations (ICLR)*, 2015.
- [139] PassMark Software. CPU Benchmark Charts. [Online]. <http://www.cpubenchmark.net>
- [140] T. Starner, "Project Glass: An Extension of the Self," *Pervasive Computing, IEEE*, vol. 12, pp. 14-16, 2013.
- [141] I. Sutskever, J. Martens, G.E. Dahl, and G.E. Hinton, "On the importance of initialization and momentum in deep learning," in *International Conference on Machine Learning (ICML)*, 2013, pp. 1139-1147.
- [142] C. Szegedy et al., "Going Deeper With Convolutions," in *The IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2015, pp. 1-9.
- [143] Y. Taigman, M. Yang, M. Ranzato, and L. Wolf, "DeepFace: Closing the Gap to Human-Level Performance in Face Verification," in *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2014, pp. 1701-1708.
- [144] J. Uijlings, K. van de Sande, T. Gevers, and A. Smeulders, "Selective search for object recognition," in *IJCV*, 2013.
- [145] N Vasilache, J. Johnson, M. Mathieu, S. Chintala, and Y. LeCun, "Fast convolutional nets with fbfft: A GPU performance evaluation," in *International Conference on Learning Representations*, 2014.
- [146] A. Vasilyev, "CNN optimizations for embedded systems and FFT," Stanford, Thesis 2015.
- [147] P. Viola and M. Jones, "Rapid object detection using a boosted cascade of simple features," in *Proceedings of the IEEE Computer Society Conference on Computer Vision and Pattern Recognition CVPR*, 2001, pp. 511-518.
- [148] Wikipedia. List of AMD Microprocessors. [Online]. [https://en.wikipedia.org/wiki/List\\_of\\_AMD\\_microprocessors/](https://en.wikipedia.org/wiki/List_of_AMD_microprocessors/)

- [149] Wikipedia. List of Intel Microprocessors. [Online]. [http://wikipedia.org/wiki/List\\_of\\_Intel\\_microprocessors/](http://wikipedia.org/wiki/List_of_Intel_microprocessors/)
- [150] M.E. Wolf and M.S. Lam, "A data locality optimizing algorithm," in *Proceedings of the ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI)*, 1991, pp. 30-44.
- [151] W.A. Wulf and S.A. McKee, "Hitting the memory wall: implications of the obvious," *ACM SIGARCH computer architecture news*, vol. 23, no. 1, pp. 20-24, 1995.
- [152] R.Z. Xie, "A flexible memory shuffling unit for image processing accelerators," Eindhoven University of Technology, Msc Thesis 2013.
- [153] R.Z. Xie, M. Peemen, and H. Corporaal, "A flexible memory shuffling unit for image processing accelerators," Eindhoven University of Technology, Master graduation report 2013.
- [154] Xilinx, "Vivado Desing Suite User Guide, High-Level Synthesis," UG902 2014.
- [155] C. Zhang et al., "Optimizing FPGA-based Accelerator Design for Deep Convolutional Neural Networks," in *Proceedings of the ACM/Sigda International Symposium on Field-Programmable Gate Arrays*, 2015, pp. 161-170.
- [156] W. Zuo et al., "Improving Polyhedral Code Generation for High-level Synthesis," in *Proceedings of the Ninth IEEE/ACM/IFIP International Conference on Hardware/Software Codesign and System Synthesis*, 2013, pp. 15:1-15:10.

# LIST OF PUBLICATIONS

## Refereed papers covered in this thesis

- [1] M. Peemen, B. Mesman, and H. Corporaal, "Inter-Tile Reuse Optimization Applied to Bandwidth Constrained Embedded Accelerators," in *DATE: Design Automation and Test in Europe*, pp. 169-174, 2015.
- [2] M. Peemen, A.A.A. Setio, B. Mesman, and H. Corporaal, "Memory-Centric Accelerator Design for Convolutional Neural Networks," in *ICCD: International Conference on Computer Design*, pp. 13-19, IEEE, 2013.
- [3] M. Peemen, B. Mesman, and H. Corporaal, "Efficiency Optimization of Trainable Feature Extractors for a Consumer Platform," in *ACIVS: Advanced Concepts for Intelligent Vision Systems*, pp. 293-304, LNCS, 2011.
- [4] M. Peemen, B. Mesman, and H. Corporaal, "Speed Sign Detection and Recognition by Convolutional Neural Networks," in *International Automotive Congress*, pp. 162-170, 2011.
- [5] M. Peemen, W. Pramadi, B. Mesman, and H. Corporaal, "VLIW Code Generation for a Convolutional Network Accelerator," in *SCOPES: International Workshop on Software and Compilers for Embedded Systems*, 2015.
- [6] M. Peemen, B. Mesman, and H. Corporaal, "A Data-Reuse Aware Accelerator for Large-Scale Convolutional Networks," in *NeuroArch Workshop at ISCA*, 2014.
- [7] M. Peemen, B. Mesman, R. Shi, S. Lal, B. Juurlink and H. Corporaal, "The Neuro Vector Engine: Flexibility to Improve Convolutional Network Efficiency for Wearable Vision," in *DATE: Design Automation and Test in Europe 2016*.

## Other (co-)authored papers

- [8] S. Tabik, M. Peemen, N. Guil, and H. Corporaal, "Demystifying the 16x16 thread-block for stencils on the GPU," *Concurrency and Computation: Practice and Experience, Design Automation and Test in Europe*, 2015.
- [9] S. Tabik, M. Peemen, L.F. Romero, and E. Zapata, "Iterative Multiple 3d-stencil pipeline on GPUs," *International Journal of High Performance Computing Applications*, Under review.
- [10] R. Shi, Z. Xu, Z. Sun, M. Peemen, A. Li, H. Corporaal, and D. Wu, "A Locality Aware Convolutional Neural Networks Accelerator," in *Euromicro DSD: Conference on Digital System Design*, IEEE, 2015.
- [11] T. Geng, L. Waeijen, M. Peemen, H. Corporaal, Y. He, "MacSim: A MAC-Enabled High-Performance Low-Power SIMD architecture" in *Euromicro DSD: Conference on Digital System Design, IEEE, 2016*
- [12] Y. He, M. Peemen, L. Waeijen, E. Diken, M. Fiumara, G. Rauwerda, H. Corporaal, T. Geng, "A configurable SIMD architecture with explicit datapath for intelligent learning," in *International Conference on Embedded Computer Systems: Architectures, Modeling and Simulation (SAMOS)*, IEEE, 2016



# ACKNOWLEDGEMENTS

This thesis is the result after an intense period of hard work that could only be completed with the support of many people around me. A key person in this is my promotor Henk Corporaal who always provided guidance, inspiration, creative ideas, and the encouragement to continue and finish my research. Together with my copromotor Bart Mesman you invited me to join the Electronic Systems (ES) Group and created the opportunity to work on Convolutional Networks, which at that time (2010) was a new and risky topic. I really appreciated the supervision style that encouraged independent work, greatly stimulating creativity. I also thank Ralph Otten, who was my second promotor during my research period in the ES group. It is very sad that Ralph passed away last year, the result of this thesis benefited considerably from his feedback and advice.

I thank Cees Snoek, Luca Benini, Olivier Temam, Kees van Berkel, and Peter de With for being part of my Doctoral Committee, and for their time and effort in reviewing the manuscript. I also like to thank the different industrial collaboration partners that provided several interesting real-world problems, which improved the applicability of my Ph.D. research. For instance the collaboration with TomTom initiated the development of my speed sign detector as part of the SPITS project. The company Assembléon introduced me to challenging recognition problems in the EVA project. With RECORE Systems we worked on wide SIMD architectures for deep learning in the RECA project. I really appreciated these industrial collaborations.

The many collaboration in the ES group also contributed greatly to the work in this thesis. Being a member of the PARsE research team helped to get good feedback on my research ideas and improved my understanding. The synergy between the members and different topics in the team accelerated research by quickly shaping raw ideas into methodologies and experiments. I thank Zhenyu, Yifan, Dongrui, Cedric, Gert-Jan, Shakith, Roel, Erkan, Ang, Luc and Mark for their feedback and advice during the biweekly PARsE meetings. Especially the support from Gert-Jan, who was my office friend during my research period at the TU/e, helped me a lot. I thank him for the practical help on so many topics and the good reviews of my papers. I also thank him for the time that we spent traveling. On conferences like ICCD in Asheville, NC, USA, and the summer school in Fiuggi, Italy, it was always great to have you around.

Many thanks to everyone at the ES group, you all made my work at the TU/e a success. I value the work, support, and care of the group leaders Ralph Otten and Twan Basten, the project manager Jan van Dalen, and the secretaries Marja, Rian, and Margot. I thank Kees Goossens for the experience of being teaching assistant in your system design courses, it was fun and an excellent experience. Also many thanks to the people who joined our (non)scientific discussions at the coffee table: Marc, Sander, Luc, Raymond, Marcel, Martijn, Sven, Andrew, Joost, and all the others.

One of the best experiences of my Ph.D. work are the many Master student projects that I supervised together with Henk. The projects of Roy, Rui Zhou, Peter, Arnoud, Wisnu, and Gaurav contributed to the content in this thesis. It was great to have you on board, your contributions really made this a team effort. I also express my gratitude for the good collaborative work with Siham Tabik from Málaga, Spain. Our work on GPU thread-block scheduling did not directly end up in this thesis, but it did result in efficient GPU mappings for the NVE comparisons.

A big word of thanks goes to the Dutch railway operator “Nederlandse Spoorwegen (NS)”. Every day I commuted from Breda to Eindhoven by train. For some reason this environment had a very creative effect on my thinking. For example, my first data access patterns that resulted into the inter-tile reuse methodology have been created during sketching and thinking while traveling home. On the other hand, I probably also lost a few good ideas while I was freezing on a cold train station and had to wait forever due to train breakdowns.

I thank my family and friends for being supportive, and creating the necessary distraction that was needed for creativity. Dad and mom, you always helped me in any possible way to develop into the person that wrote this thesis. You both showed me that anything is possible with the right mindset, thank you. Finally, this thesis would never have been finished without the support and encouragement of my beautiful wife Marie-Louise. You’ve let me trade quality time for work time, managed tasks at home such that I could focus on research, and kept life in balance. You also gave me our beautiful son Mika that brings joy and new inspiration. This thesis is dedicated to both of you.

*Maurice Peemen  
September 2017*

## ABOUT THE AUTHOR

M.C.J. (Maurice) Peemen was born in Rijsbergen, the Netherlands, on August 26, 1983. He received a B.Eng. degree in Electrical Engineering from Fontys University of applied sciences in 2007. His Bachelor's graduation project was at CNSE in Albany, New York, USA on a EUV lithography mask flatness metrology tool.

In 2010 he obtained his M.Sc. degree in Electrical Engineering with the predicate '*cum laude*' from Eindhoven University of Technology. The focus of his Master's thesis was the mapping of Convolutional Networks to FPGAs. After graduating Maurice worked as a researcher in the Electronic Systems group at Eindhoven University of Technology until 2011, and then started as a Ph.D. student in the same group. His research interests include deep learning, loop transformations, and accelerator architectures.

In 2015 he left the ES group to start as Research Scientist at Thermo Fisher Scientific (formerly FEI Company) to work on high-performance microscopy workflow solutions.

