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A Process Specification Formalism based on static COLD

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Abstract

PSF/C is a formal specification language, based on COLD, a wide spectrum specification language developed at Philips Research, Eindhoven. In PSF/C, we can specify concurrent communicating processes. The process syntax and semantics is based on the algebraic concurrency language ACP.

Key Words & Phrases:
concurrent languages, formal description techniques, specification languages, wide spectrum language, COLD, process algebra, ACP, abstract data types, semantics.

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F.1.2.	(Modes of Computation)	Parallelism
F.3.2.	(Semantics of Programming Languages)	Algebraic approaches to semantics, Operational semantics

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1 INTRODUCTION

PSF/C is an *experiment* in language design. It is not meant as a finished language that would justify the substantial efforts of writing its necessary tools. PSF/C is a language in which we can specify concurrent communicating processes. Moreover, we have ample facilities to specify data types. These data types can occur as parameters of actions and processes. Also, we have a modular structure: data types and processes are defined in modules. Modules can be parameterized by other modules, and parts of the signature can be exported or hidden. The starting point for construction of PSF/C has been the wide spectrum language COLD, developed at Philips Research, Eindhoven. From COLD, we get data type specifications, parameterization and the modular structure with imports and exports. On top of that, we specify processes and their interaction in the spirit of the concurrency theory ACP of [BK84].

The design objectives have been:

- to combine ACP and the *static part* of COLD in one language where the concrete syntax is borrowed from COLD;
- to combine processes and data in a similar fashion as is done in PSF/ASF of [MV88], where data are used as parameters of actions and process names;
- to obtain a semantic description of the language by means of a translation to COLD;
- to generate a parser for the syntax by means of the SDF system of the GIPE project (see [BHK89]).

2 THE COLD-S LANGUAGE

In this section we will present COLD-S, which is obtained by dropping all dynamic features from the language COLD-K (this language is called COLD-A in RENARDEL DE LAVALETTE [RdL89]; we want to reserve the postfix A for another purpose). The language COLD-K has been developed in the framework of ESPRIT project 432, METEOR (see FEIJS, JONKERS, KOYMANS & RENARDEL DE LAVALETTE [FJKR87]). COLD-K has been designed to be a so-called wide spectrum language in which it should be possible to capture the whole spectrum of software development. The language supports *transformational* design, in which implementations are constructed from specifications by replacing, step by step, all parts of the specification by equivalents that show more and more aspects of an executable language.

Like COLD-K, COLD-S is defined by means of a translation of its grammatical constructs to the constructs of a three layered formal language. The top layer of this kernel is a special version of lambda calculus, which is called $\lambda\pi$, and is used for modelling parameterization. Expressions in this lambda calculus contain terms from a special many-sorted algebra, called CA, which is used for modelling modularization constructs. This algebra constitutes the middle layer. The constants used in the terms of this algebra are presentations of logical theories. The logical language used at the bottom level is based on a special infinitary logic, called MPL_ω. Every construct in a COLD specification corresponds with an expression in the kernel of formal languages with a well-defined semantics. COLD specifications are translated by means of attribute grammars to the kernel.

In some instances, we want to restrict COLD-K in another way, by taking the *algebraic* subset COLD-A. We obtain COLD-A by restricting all axioms in the language to the format of *conditional equations*, and restricting all functions to *total* functions. Obviously, COLD-SA will be the static algebraic part of COLD-K.

2.1 SOME REMARKS ON THE LANGUAGE

Like COLD-K, the language COLD-S consists of a number of hierarchically ordered sublanguages. This hierarchy is illustrated by the following picture:

$$\begin{tikzcd}
\text{Design Language} \arrow[d] \\
\text{Scheme Language} \arrow[d] \\
\text{Class Language} \arrow[d] \\
\text{Definition Language} \arrow[d] \\
\text{Assertion Language}
\end{tikzcd}$$

In the following sections we will explain each language in some more detail.

2.1.1 The Assertion Language

In the assertion language we can write terms and assertions. The assertions in COLD-K or COLD-S are exactly the formulae of MPL, the underlying many-sorted predicate logic. In the case of COLD-A we only allow (universally quantified) conditional equations.

2.1.2 The Definition Language

In the definition language we come across the items that are defined in the COLD-S language, viz.: sorts, predicates and functions. A definition can be seen in two ways: a declarative and a definitional way. The declarative part introduces the name of an item and possibly its type, while the definitional part defines the meaning of the item introduced. Not all definitions show both aspects. Sort definitions only have a declarative aspect, while axioms are purely definitional. Predicates and functions are both declarative and definitional, their meaning is defined directly, by a defining term or an assertion, or indirectly, by an inductive definition or an axiom. Inductively defined predicates and functions are defined as the smallest predicate or function satisfying the inductive definition.

2.1.3 The Class Language

The class language is used to group a list of definitions into a modular structure which is called *class* in COLD-S. The *signature* of a class is the collection of sorts, functions and predicates that are defined in that particular class.

2.1.4 The Scheme Language

All operations that have to do with the modularization and parameterization of specifications are dealt with in the scheme language.

These operations are a.o. :

- renaming of objects in a class
- import of classes
- export of objects from a class
- parameterization of a class
- application of a class to another one

2.1.5 The Design Language

The design language is used to handle specifications at the highest level. At this level the so-called components, which will finally be used to specify the complete *system*, are specified. A component can be either a specification, in which case it is called a *specified* component, or a specification together with an implementation written in COLD-S, in which case it is called an *implemented* component. Specified components are used when the implementation of a component cannot be described in COLD-S, because it is a piece of hardware or an existing program in some kind of programming language.

2.2 THE GRAMMAR

The definition of the context free grammar of COLD-S is given using a certain BNF-grammar augmented with the following extra rules:

{X}	denotes zero or more occurrences of X (a list of X's)
[X]	denotes zero or one occurrences of X (an optional X)
{ X '@' }	denotes zero or more occurrences of X, with the symbol @ acting as delimiter.

Then, the grammar of COLD-S is defined as follows:

```
<design> ::= DESIGN {<component> ';'} SYSTEM {<scheme> ','}

<component> ::= COMP <scheme-var> : <scheme> [:= <scheme>]
   |  LET <scheme-var> := <scheme>

<scheme> ::= <class>
   |  RENAME <renaming> IN <scheme>
   |  IMPORT <scheme> INTO <scheme>
   |  EXPORT <signature> FROM <scheme>
   |  LAMBDA <scheme-var> : <scheme> OF <scheme>
   |  APPLY <scheme> TO <scheme>
   |  LET <scheme-var> := <scheme> ; <scheme>
   |  <scheme-var>

<renaming> ::= {<namepair> ','}
   |  <renaming> $ <renaming>

<namepair> ::= <sort-name> TO <sort-name>
   |  <predicate-name> TO <predicate-name>
   |  <function-name> TO <function-name>

<signature> ::= {<item> ','}
   |  <renaming> @ <signature>
   |  <signature> + <signature>
   |  <item> ^ <signature>
   |  SIG <scheme>

<item> ::= SORT <sort-name>
   |  PRED <predicate-name> : domain
   |  FUNC <function-name> : domain -> <sort-name>

<class> ::= CLASS {<definition>} END

<definition> ::= SORT <sortname>
   |  PRED <predicate-name> : domain <predicate body>
```

```
    |  FUNC <function-name> : domain -> <sort-name> <function body>
    |  AXIOM <assertion>

<predicate body> ::= [IND <assertion>]
    |  [PAR <varsort list>] DEF <assertion>

<function body> ::= [IND <assertion>]
    |  [PAR <varsort list>] DEF <term>

<assertion> ::= TRUE
    |  FALSE
    |  <term>!
    |  <term> = <term>
    |  <predicate-name> <term list>
    |  NOT <assertion>
    |  <assertion> ; <assertion>
    |  <assertion> AND <assertion>
    |  <assertion> OR <assertion>
    |  <assertion> => <assertion>
    |  <assertion> <=> <assertion>
    |  FORALL <varsort list> <assertion>
    |  EXISTS <varsort list> <assertion>
    |  LET {<assignment> ','} ; <assertion>
    |  ( <assertion> )

<term> ::= <object-var>
    |  <function-name> <term list>
    |  THAT <varsort> <assertion>
    |  LET {<assignment> ','} ; <term>
    |  ( <term> )

<term list> ::= {<term> ','}
    | ( <term list> )

<domain> ::=  {<sort-name> '#'}

<varsort list> ::= {<varsort> ','}

<varsort> ::= <object-var> : <sort-name>

<assignment> ::= <object-var> := <term>

<scheme-var> ::= <identifier>

<sort-name> ::= <identifier>

<predicate-name> ::= <identifier>

<function-name> ::= <identifier>

<object-var> ::= <identifier>
```

3 PSF/C

The concrete syntax of PSF/C is almost identical to the concrete syntax of COLD, with the exception of the additional language constructs we need to represent atomic actions, processes etc. To indicate we restrict ourselves to the static part of COLD, COLD-S, we write PSF/C. Similarly, for PSF/CA we use the static algebraic part of COLD, COLD-SA.

3.1 CHARACTER SET

A PSF/C specification uses the same ASCII character set as COLD, viz. :

```
   ! " # $ % & ' ( ) * + , - . / 0 1 2 3 4 5 6 7 8 9 :
; < = > ? @ A B C D E F G H I J K L M N O P Q R S T U
V W X Y Z [ \ ] ^ _ ` a b c d e f g h i j k l m n o p
q r s t u v w x y z { | } ~
```

3.2 TOKENS

In parsing a PSF/C specification a series of tokens is recognized. Each token is a sequence of ASCII characters and tokens are separated by spaces, tabs and new lines. In cases of ambiguity the longest token that can be recognized is preferred. There are three kinds of tokens, viz. identifiers, keywords and comments. We will discuss these in turn in the following sections.

3.2.1 Identifiers

Identifiers in PSF/C are arbitrary non-empty strings consisting of letters, digits and the following four characters:

" ' / _

excluding those strings which are keywords. Two characters that can be part of a COLD identifier are excluded namely the dot '.' and the backslash '\'. The dot has become a keyword, representing sequential composition and the backslash is reserved to be used as a special character that a program translating PSF/C into COLD-K can use to distinguish user defined identifiers from identifiers generated by the translator.

3.2.2 Keywords

The following strings are PSF/C keywords:

!	<=>	DELTA	IMPORT
#	=	DESIGN	IN
$	=>	EPSILON	IND
&	@	ENCAPS	INTO
(	^	END	LAMBDA
)	ACTION	EXISTS	LET
+	AND	EXPORT	MERGE
,	APPLY	FALSE	NOT
->	AXIOM	FORALL	OF
.	CLASS	FROM	OR
:	COMM	FUNC	PAR
:=	COMP	GCMD	PRED
;	DEF	HIDE	PRETAU

PROCESS	SORT	THAT	|
RENAME	SPEC	TO	||
SET	SUM	TRUE	
SIG	SYSTEM	WITH	

3.2.3 Comments

There are two possible ways to create a comment. The first is to use the comment brackets: '{' and '}', which turn the enclosed text into a comment. Comment brackets cannot be nested and the enclosed text may not contain a '}'.

Example:

{ This is a comment }

The second way to create comment is by using the sign the '%', which turns the rest of the line into a comment.

Example:

% This is comment

Comments may be inserted between any two tokens and have no meaning in terms of the abstract syntax.

3.3 GRAMMAR

The PSF/C grammar is given in the following section. In fact it is an extension of the COLD-S grammar presented in section 2.

```
<design> ::= DESIGN {<component> ';'} SYSTEM {<scheme> ','}

<component> ::= COMP <scheme-var> : <scheme> [:= <scheme>]
    |  LET <scheme-var> := <scheme>

<scheme> ::= <class>
    |  RENAME <renaming> IN <scheme>
    |  IMPORT <scheme> INTO <scheme>
    |  EXPORT <signature> FROM <scheme>
    |  LAMBDA <scheme-var> : <scheme> OF <scheme>
    |  APPLY <scheme> TO <scheme>
    |  LET <scheme-var> := <scheme> ; <scheme>
    |  <scheme-var>

<renaming> ::= {<namepair> ','}
    |  <renaming> $ <renaming>

<namepair> ::= <sort-name> TO <sort-name>
    |  <predicate-name> TO <predicate-name>
    |  <function-name> TO <function-name>
    |  <action-name> TO <action-name>
    |  <process-name> TO <process-name>
    |  <set-name> TO <set-name>

<signature> ::= {<item> ','}
    |  <renaming> @ <signature>
    |  <signature> + <signature>
    |  <item> ^ <signature>
    |  SIG <scheme>
```

```
<item> ::= SORT <sort-name>
    |  PRED <predicate-name> : domain
    |  FUNC <function-name> : domain -> <sort-name>
    |  ACTION <action-name>  : domain
    |  PROCESS <process-name>  : domain
    |  SET <set-name>

<class> ::= CLASS {<definition>} END

<definition> ::= SORT <sortname>
    |  PRED <predicate-name> : domain <predicate body>
    |  FUNC <function-name> : domain -> <sort-name> <function body>
    |  AXIOM <assertion>
    |  ACTION <action-name> : domain
    |  PROCESS <process-name> : domain  <process body>
    |  SET <set-name> <set body>
    |  COMM <comm assertion>
    |  SPEC <spec body>

<predicate body> ::= [IND <assertion>]
    |  [PAR <varsort list>] DEF <assertion>

<function body> ::= [IND <assertion>]
    |  [PAR <varsort list>] DEF <term>

<process body> ::= [[PAR <varsort list>] DEF <process expr>]

<set body> ::= [IND <assertion>]

<assertion> ::= TRUE
    |  FALSE
    |  <term>!
    |  <term> = <term>
    |  <predicate-name> <term list>
    |  <set-name> <action term list>
    |  NOT <assertion>
    |  <assertion> ; <assertion>
    |  <assertion> AND <assertion>
    |  <assertion> OR <assertion>
    |  <assertion> => <assertion>
    |  <assertion> <=> <assertion>
    |  FORALL <varsort list> <assertion>
    |  EXISTS <varsort list> <assertion>
    |  LET {<assignment> ','} ; <assertion>
    |  ( <assertion> )

<comm assertion> ::= <action term> | <action term> = <action term>
    |  <comm assertion> ; <comm assertion>
    |  FORALL <varsort list> <comm assertion>
    |  ( <comm assertion> )

<spec assertion> ::= <process-name> <term list> = <process expr>
    |  <spec assertion> ; <spec assertion>
    |  FORALL <varsort list> <spec assertion>
    |  ( <spec assertion> )
```

```
<term> ::= <object-var>
    |  <function-name> <term list>
    |  THAT <varsort> <assertion>
    |  LET {<assignment> ','} ; <term>
    |  ( <term> )

<action term list> ::= {<action term> ','}
    |  ( <action term list> )

<action term> ::= <action-name> <term list>
    |  ( <action term> )

<term list> ::= {<term> ','}
    | ( <term list> )

<process expr> ::= PRETAU
    |  DELTA
    |  EPSILON
    |  <process-name> <term list>
    |  <process expr> . <process expr>
    |  <process expr> + <process expr>
    |  <process expr> | | <process expr>
    |  GCMD <ass-process expr>
    |  SUM <varsort list> <process expr>
    |  MERGE <varsort list> <process expr>
    |  ENCAPS  <set-process expr>
    |  HIDE <set-process expr>
    |  ( <process expr> )

<set-process expr> ::= <set expr> , <process expr>
    |  (<set-process expr>)

<ass-process expr> ::= <assertion>, <process expr>
    |  (<ass-process expr>)

<set expr> ::= <set-name>
    |  <set expr> + <set expr>
    |  <set expr> & <set expr>
    |  <set expr> ^ <set expr>
    |  ( <set expr> )

<domain> ::=  {<sort-name> '#'}

<varsort list> ::= {<varsort> ','}

<varsort> ::= <object-var> : <sort-name>

<assignment> ::= <object-var> := <term>

<scheme-var> ::= <identifier>

<sort-name> ::= <identifier>

<predicate-name> ::= <identifier>

<function-name> ::= <identifier>
```

<action-name> ::= <identifier>

<process-name> ::= <identifier>

<set-name> ::= <identifier>

<object-var> ::= <identifier>

3.4 SDF DEFINITION

Next, we give a definition of PSF/C in the Syntax Definition Formalism of HEERING & KLINT [HK89].

SDF stands for: 'Syntax Definition Formalism'. It is a language to specify the lexical syntax, context-free syntax and abstract syntax of programming languages in a formal way and can be seen as an alternative to LEX [Joh79] and YACC [LS79]. It is possible to generate a lexical scanner and some parse tables from such an SDF-definition [Rek87]. These parse tables together with a universal parser form a parser for the specified language. It is also possible to generate a so-called syntax directed editor from a description of the layout and the parse tables. This whole system is being implemented in LISP as part of ESPRIT Project 348: GIPE (Generation of Interactive Programming Environments).

3.4.1 SDF Syntax

An SDF definition consists of two parts: a *lexical syntax* and a *context-free syntax*. In both parts we deal with the notions *sort* and *function* that correspond, respectively, to non-terminals and to production rules as used in BNF grammars [AU77].

This is an adaptation of an example of an SDF definition taken from [HK86].

```
module example
begin

   lexical  syntax

     sorts
        digit, letter, int, id, id-tail, comment-char

     layout
        white-space, comment

     functions
        [a-z]                    -> letter
        [0-9]                    -> digit
        digit+                   -> int
        [a-z0-9]                 -> id-tail
        letter id-tail*          -> id
        [ \n\t\f\r]              -> white-space
        ~[{}]                    -> comment-char
        "{" comment-char* "}"    -> comment


   context-free  syntax

     sorts
        expr

     priorities
        "+" < "*"
        functions
          expr "+" expr        -> expr    {par, left-assoc}
          expr "*" expr        -> expr    {par, left-assoc}
          id                   -> expr

  end example
```

We will point out some of the SDF constructions that appear in this example. The *sorts* and *layout* declarations, in the lexical syntax section, introduce the lexical sorts while their *functions* declarations specify what kind of strings can be constructed over these sorts. Elements of the context-free syntax may be interspersed with strings belonging to the layout sorts. The latter will be skipped by the lexical analyzer generated from the SDF definition. The function declaration may be composed of other lexical sorts, (negated) character classes, terminals and list expressions. In the lexical syntax section two kinds of list expressions are allowed:

S*	zero or more occurrences of sort *S*
S+	one or more occurrences of sort *S*

In the function declaration of the context-free syntax section lexical sorts may be used as terminals of the grammar, though terminals may also be introduced directly, like "+" and "*" in the example. Moreover two more list expressions are allowed:

{S t}*	zero or more occurrences of sort *S*, separated by the terminal *t*.
{S t}+	one or more occurrences of sort *S*, separated by the terminal *t*.

The *priorities* declaration is used to define the relative priority between functions. When unambiguous, the function may be abbreviated by its keyword skeleton. The associativity of functions may be declared by means of the attributes: *assoc*, *left-assoc* and *right-assoc* while the attribute *par* can be added to the function declaration to state that the function may be surrounded by parentheses in order to change its priority.

3.4.2 PSF/C in SDF

```
module PSF/C
begin

  lexical syntax

    sorts
      id-char,identifier,
      comment-1-char, comment-2-char

    layout
      white-space, comment

    functions
      [0-9a-zA-Z"'/_]                                  -> id-char
      id-char+                                         -> identifier

      [ \n\t\r]                                        -> white-space

      ~ [\n]                                           -> comment-1-char
      ~ [}]                                            -> comment-2-char
      "%" comment-1-char* "\n"                         -> comment
    "{" comment-2-char* "}"                        -> comment

context-free syntax

  sorts
    design, component, scheme, renaming, namepair, signature,
    item, class, definition, predicate-body, function-body,
    process-body, set-body, assertion, comm-assertion,
    spec-assertion, term, action-term, term-list,
    process-expr, set-process-expr, ass-process-expr, set-expr,
    domain, varsort-list, varsort, assignment, scheme-var,
    sort-name, predicate-name, function-name, action-name,
    process-name, set-name, object-var


  functions

    "DESIGN" {component ";"}* "SYSTEM" {scheme ","}*    -> design

    "COMP" scheme-var ":" scheme ":=" scheme            -> component
    "COMP" scheme-var ":" scheme                        -> component
    "LET" scheme-var ":=" scheme                        -> component

    class                                               -> scheme
    "RENAME" renaming "IN" scheme                       -> scheme
    "IMPORT" scheme "INTO" scheme                       -> scheme
    "EXPORT" signature "FROM" scheme                    -> scheme
    "LAMBDA" scheme-var ":" scheme "OF" scheme          -> scheme
    "APPLY" scheme "TO" scheme                          -> scheme
    "LET" scheme-var ":=" scheme ";" scheme             -> scheme
    scheme-var                                          -> scheme

    {namepair ","}*                                     -> renaming
    renaming "$" renaming                               -> renaming {left-assoc}

    item "TO" identifier                                -> namepair

    {item ","}*                                         -> signature
    renaming "@" signature                              -> signature
    signature "+" signature                             -> signature {left-assoc}
    item "^" signature                                  -> signature
    "SIG" scheme                                        -> signature

    "SORT" sort-name                                    -> item
    "PRED" predicate-name ":" domain                    -> item
    "FUNC" function-name ":" domain "->" sort-name      -> item
    "ACTION" action-name  ":" domain                    -> item
    "PROCESS" process-name  ":" domain                  -> item
    "SET" set-name                                      -> item

    "CLASS" definition* "END"                           -> class

    "SORT" sort-name                                    -> definition
    "PRED" predicate-name ":" domain predicate-body     -> definition
    "FUNC" function-name ":" domain "->"
                                  sort-name function-body  -> definition
    "AXIOM" assertion                                   -> definition
    "ACTION" action-name ":" domain                     -> definition
    "PROCESS" process-name ":" domain  process-body     -> definition
    "SET" set-name set-body                             -> definition
    "COMM" comm-assertion                               -> definition
    "SPEC" spec-assertion                               -> definition

    "IND" assertion                                     -> predicate-body
    "PAR" varsort-list "DEF" assertion                  -> predicate-body
```

```
"DEF" assertion                                      -> predicate-body
                                                     -> predicate-body

"IND" assertion                                      -> function-body
"PAR" varsort-list "DEF" term                        -> function-body
"DEF" term                                           -> function-body
                                                     -> function-body

"PAR" varsort-list "DEF" process-expr                -> process-body
"DEF" process-expr                                   -> process-body
                                                     -> process-body

"IND" assertion                                      -> set-body
                                                     -> set-body

"TRUE"                                               -> assertion
"FALSE"                                              -> assertion
term "!"                                             -> assertion
term "=" term                                        -> assertion
predicate-name term-list                             -> assertion
set-name "[" action-term "]"                         -> assertion
"NOT" assertion                                      -> assertion
assertion ";" assertion                              -> assertion {left-assoc}
assertion "AND" assertion                            -> assertion {left-assoc}
assertion "OR" assertion                             -> assertion {left-assoc}
assertion "=>" assertion                             -> assertion {left-assoc}
assertion "<=>" assertion                            -> assertion {left-assoc}
"FORALL" varsort-list assertion                      -> assertion
"EXISTS" varsort-list assertion                      -> assertion
"LET" {assignment ","}* ";" assertion                -> assertion
"(" assertion ")"                                    -> assertion {bracket}

action-term "|" action-term "=" action-term          -> comm-assertion
comm-assertion ";" comm-assertion                    -> comm-assertion {left-assoc
"FORALL" varsort-list comm-assertion                 -> comm-assertion
"(" comm-assertion ")"                               -> comm-assertion {bracket}

process-name term-list "=" process-expr              -> spec-assertion
spec-assertion ";" spec-assertion                    -> spec-assertion {left-assoc
"FORALL" varsort-list spec-assertion                 -> spec-assertion
"(" spec-assertion ")"                               -> spec-assertion {bracket}

object-var                                           -> term
function-name term-list                              -> term
"THAT" varsort assertion                             -> term
"LET" {assignment ","}* ";" term                     -> term

action-name term-list                                -> action-term

"(" {term ","}+ ")"                                  -> term-list {bracket}
                                                     -> term-list

action-term                                          -> process-expr
"PRETAU"                                             -> process-expr
"DELTA"                                              -> process-expr
"EPSILON"                                            -> process-expr
process-name term-list                               -> process-expr
process-expr "." process-expr                        -> process-expr
process-expr "+" process-expr                        -> process-expr
process-expr "||" process-expr                       -> process-expr
"GCMD" ass-process-expr                              -> process-expr
"SUM" sum-merge-arg                                  -> process-expr
"MERGE" sum-merge-arg                                -> process-expr
"ENCAPS"  set-process-expr                           -> process-expr
"HIDE" set-process-expr                              -> process-expr
```

```
        "(" process-expr ")"                           -> process-expr

        varsort-list "(" process-expr ")"              -> sum-merge-arg

        "(" assertion "," process-expr ")"             -> ass-process-expr

        "(" set-expr "," process-expr ")"              -> set-process-expr

        set-name                                       -> set-expr
        set-expr "+" set-expr                          -> set-expr
        set-expr "&" set-expr                          -> set-expr
        set-expr "^" set-expr                          -> set-expr
        "(" set-expr ")"                               -> set-expr

        {sort-name "#"}*                               -> domain

        {varsort ","}*                                 -> varsort-list

        object-var ":" sort-name                       -> varsort

        object-var ":=" term                           -> assignment

        identifier                                     -> scheme-var
        identifier                                     -> sort-name
        identifier                                     -> predicate-name
        identifier                                     -> function-name
        identifier                                     -> action-name
        identifier                                     -> process-name
        identifier                                     -> set-name
        identifier                                     -> object-var

    end PSF/C
```

4 Semantics

4.1 Introduction

The semantics of the COLD-K language can be found in [FJKR87]. These semantics will be used as a base to define the semantics of PSF/C. All constructs in PSF/C that are already part of COLD-K have the same meaning as their counterparts in COLD-K. New constructs, i.e. all constructs dealing with process behaviour, are indirectly defined using the COLD-K semantics. This is done by giving a translation from PSF/C into COLD-K.

The intention is to give a semantics to the process definition part that resembles the algebraic semantics normally attached to process algebra (see e.g. BERGSTRA & KLOP [BK84, BK86b]). In order to be able to understand the formal translation, we will give an overview of the usual algebraic semantics for process algebra expressions.

4.2 ACP

We start from a given set A of atomic actions. Atomic actions are the simplest kind of processes, indivisible, and usually considered as having no duration. Complex processes can be constructed from simpler ones by applying several predefined functions and operators. Each atomic action is a constant in the set Action. The set Action is embedded in the set of processes, named Process.

On A, we have given a partial binary function γ, the *communication function*. γ must be commutative and associative, i.e.

$\gamma(a,b) = \gamma(b,a)$

$\gamma(a,\gamma(b,c)) = \gamma(\gamma(a,b),c)$

(when defined) for all $a,b,c \in A$. If $\gamma(a,b) = c$, we say a and b *communicate*, and the result of their communication is c. If $\gamma(a,b)$ is undefined, we say that a and b do not communicate. A and γ can be considered as *parameters* of the theory: in each application we will have to specify what atomic actions we have, and how they communicate. In PSF/C, we write $\gamma(a,b) = c$ as $a \mid b = c$.

On the domain of processes we define an equivalence relation by making a number of identifications between processes. These identifications follow from a set of axioms. For all processes x and y e.g. we consider the processes x+y and y+x to be identical. The intuition behind the identifications will be explained next.

The first two compositional operators we consider are $\cdot$, denoting sequential composition, and + for alternative composition. If x and y are two processes, then $x \cdot y$ is the process that starts the execution of y after the completion of x, and x+y is the process that chooses either x or y and executes the chosen process (not the other one). Each time a choice is made, we choose from a set of alternatives. We do not specify whether a choice is made by the process itself, or by the environment. Axioms A1-5 in table 1 below give the laws that + and $\cdot$ obey. We leave out $\cdot$ and brackets as in regular algebra, so xy + z means $(x \cdot y) + z$. $\cdot$ will always bind stronger than other operators, and + will always bind weaker.

On intuitive grounds $x(y + z)$ and $xy + xz$ present different mechanisms (the moment of choice is different), and therefore, an axiom $x(y + z) = xy + xz$ is not included.

We have a special constant δ denoting deadlock, the acknowledgement of a process that it cannot do anything any more, the absence of any alternative. Axioms A6-7 give the laws for δ. We also have a special constant t that is used for *pre-abstraction* (see the following section). t or δ are not in the given set A, but are in the set of constants Action. Thus, γ is not defined for constants t, δ, which means that t or δ do not communicate.

Next, we have the parallel composition operator $\|$, called merge. The merge of processes x and y will interleave the actions of x and y, except for the communication actions. In $x \| y$, we can either do a step from x, or a step from y, or x and y both synchronously perform an action, which together make up a new action, the communication action. This trichotomy is expressed in axiom CM1. Here, we use two auxiliary operators $\mathbin{|\!\!\lfloor}$ (left-merge) and $|$ (communication merge). Thus, $x \mathbin{|\!\!\lfloor} y$ is $x \| y$, but with the restriction that the first step comes from x, and $x \mid y$ is $x \| y$ with a communication step as the first step. Axioms CM2-9 and CF1-2 give the laws for $\mathbin{|\!\!\lfloor}$ and $|$. The laws CF1-2, that say that on atomic actions $|$ coincides with γ, differ slightly from laws C1-3 in BERGSTRA & KLOP [BK84]. Finally, we have in table 1 the encapsulation operator ∂_H. Here H is a set of atomic actions ($H \subseteq A$), and ∂_H blocks those actions, renames them into δ. The operator ∂_H can be used to encapsulate a process, i.e. to block communications with the environment. Since $t \notin A$, always $\partial_H(t) = t$.

$x+y=y+x$	A1
$(x+y)+z=x+(y+z)$	A2
$x+x=x$	A3
$(x+y)z=xz+yz$	A4
$(xy)z=x(yz)$	A5
$x+\delta=x$	A6
$\delta x=\delta$	A7
$a\mid b=\gamma(a,b)$ if $\gamma(a,b)$ is defined	CF1
$a\mid b=\delta$ otherwise	CF2
$x\Vert y=x⌊\!⌊y+y⌊\!⌊x+x\mid y$	CM1
$a⌊\!⌊x=ax$	CM2
$ax⌊\!⌊y=a(x\Vert y)$	CM3
$(x+y)⌊\!⌊z=x⌊\!⌊z+y⌊\!⌊z$	CM4
$a\mid bx=(a\mid b)x$	CM5
$ax\mid b=(a\mid b)x$	CM6
$ax\mid by=(a\mid b)(x\Vert y)$	CM7
$(x+y)\mid z=x\mid z+y\mid z$	CM8
$x\mid(y+z)=x\mid y+x\mid z$	CM9
$\partial_H(a)=a$ if $a\notin H$	D1
$\partial_H(a)=\delta$ if $a\in H$	D2
$\partial_H(x+y)=\partial_H(x)+\partial_H(y)$	D3
$\partial_H(xy)=\partial_H(x)\cdot\partial_H(y)$	D4

Table 1. ACP.

In this table, $a,b \in$ Action $(= A\cup\{t,\delta\})$, $H \subseteq A$, and x,y,z are arbitrary processes. In addition to the axioms of ACP, we often use the following axioms of **Standard Concurrency**.

$x\Vert\delta=x\delta=\delta\Vert x$	SC1
$(x\Vert y)\Vert z=x\Vert(y\Vert z)$	SC2
$x\Vert y=y\Vert x$	SC3

Table 2. Standard Concurrency.

4.3 PRE-ABSTRACTION

In system *verification*, it is essential that we can abstract from the internal actions of a system, in order to prove that the external behaviour is as specified beforehand. Here, we are defining a *specification* language, and we do not want to deal with silent steps, and a suitable set of axioms for such steps. Thus, we are dealing with *concrete* process algebra (process algebra without silent steps. A first (important) step in dealing with internal actions can however be made in concrete process algebra, and this is that we can give all internal actions the same name. We use the constant t for this purpose. The unary operator t_I will rename all atomic actions from the set I into t. We call the operator t_I *pre-abstraction* and we sometimes call the constant t *pre-tau*. These notions were introduced in BAETEN & BERGSTRA [BB88]. The axioms for t_I are presented in table 3.

$t_I(a) = a \quad \text{if } a \notin I$	PT1
$t_I(a) = t \quad \text{if } a \in I$	PT2
$t_I(x + y) = t_I(x) + t_I(y)$	PT3
$t_I(xy) = t_I(x) \cdot t_I(y)$	PT4

Table 3. Pre-abstraction.

4.4 EMPTY PROCESS

In the formulation of the generalized merge later on, it is very useful to have a special constant ε standing for the empty process. Also, this constant is useful when defining an operational semantics. On the other hand, the empty process does not stand for a concrete action, and the axiomatizations for it are less standardized as for other concepts. Since we follow a modularized set-up, the constant ε can be removed (together with the generalized merge construct) in situations where it is not wanted. We give the additional axioms needed in table 4. We follow essentially the axiomatization of VRANCKEN [Vr86].

$\varepsilon \cdot x = x$	A8
$x \cdot \varepsilon = x$	A9
$\varepsilon \mathbin{\|\!\_} \varepsilon = \varepsilon$	EM1
$\varepsilon \mathbin{\|\!\_} ax = \delta$	EM2
$\varepsilon \mathbin{\|\!\_} (x + y) = \varepsilon \mathbin{\|\!\_} x + \varepsilon \mathbin{\|\!\_} y$	EM3
$\varepsilon \mid x = x \mid \varepsilon = \delta$	EM4,5
$\partial_H(\varepsilon) = \varepsilon$	ED
$t_I(\varepsilon) = \varepsilon$	EPT
$\varepsilon \parallel x = x$	SC4

Table 4. Empty process.

4.5 GUARDED COMMAND

We want to extend the axiom system ACP with generalized sum and generalized merge constructs. In order to do this, it is very useful to introduce the **guarded command** construct first. If ϕ is an assertion in MPL, and p is a process expression, we write

$$\phi :\rightarrow p$$

for the process that is p if ϕ holds. If ϕ does not hold, we get deadlock. It is easy to write down the axioms for the guarded command. See table 5.

$\phi :\rightarrow p = p$	if ϕ	GC1
$\phi :\rightarrow p = \delta$	if NOT ϕ	GC2

Table 5. Guarded Command.

From these axioms, we can derive some very useful corollaries. We list a few:

$\phi :\rightarrow (\psi :\rightarrow p) = (\phi \text{ AND } \psi) :\rightarrow p$

$(x=t) :\rightarrow p = (x=t) :\rightarrow p[x:=t]$.

Example: we can define the *if...then...else* construction by:

$\textit{if } \phi \textit{ then } p \textit{ else } q = \phi :\rightarrow p + \text{NOT}\phi :\rightarrow q$.

4.6 GENERALIZED SUM AND MERGE

In order to give some motivation for what is to follow, we discuss an example first. Consider a one-place buffer with one input port and two output ports, called O and E. Atomic actions are parameterized by natural numbers, elements of the data sort N. We have the actions in(n), outO(n) and outE(n) for each $n \in N$. The buffer will output all odd numbers received at port O, all even numbers at port E. A recursive equation for this buffer can be given as follows:

$$\text{Buf} = \sum_{\substack{n \in N \\ n \text{ odd}}} \text{in}(n) \cdot \text{outO}(n) + \sum_{\substack{n \in N \\ n \text{ even}}} \text{in}(n) \cdot \text{outE}(n).$$

Now the advantage of the guarded command introduced in 6.4 is, that we can rewrite this as follows:

$$\text{Buf} = \sum_{n \in N} (n \text{ odd}) :\rightarrow \text{in}(n) \cdot \text{outO}(n) + \sum_{n \in N} (n \text{ even}) :\rightarrow \text{in}(n) \cdot \text{outE}(n).$$

This makes that we need to describe the generalised sum and merge constructs with only two arguments: first, a list of variables with sort names, and second a process expression. If $\underline{x}$ is a list of variables, and $\underline{D}$ a list of sort names of same length, then we write $\underline{x} \in \underline{D}$ to denote that a variable in list $\underline{x}$ is an element of the corresponding sort name in list $\underline{D}$. Then, the form of the sum and merge constructs is as follows:

$$\sum_{\underline{x} \in \underline{D}} p \qquad \Big\|_{\underline{x} \in \underline{D}} p,$$

where variables from $\underline{x}$ may occur in p. Axioms for these constructs are non-trivial, but giving axioms is facilitated by using the guarded command of the previous section. We give the sum axioms in table 6.

$\sum_{\underline{x} \in \underline{D}} p = \sum_{\underline{x} \in \underline{D}} \phi :\rightarrow p + \sum_{\underline{x} \in \underline{D}} \text{NOT}\phi :\rightarrow p$		SUBSUM
$\sum_{\underline{x} \in \underline{D}} (\underline{x}=\underline{t}) :\rightarrow p = p[\underline{x}:=\underline{t}]$	if no $\underline{x}$ occurs free in $\underline{t}$	SINGSUM

Table 6. Generalized sum.

Actually, in the translation to COLD-K, to be presented in section 6.7, we will use a different axiomatization of generalized sum, one that is easier to code in COLD.

The axioms in table 5 are sufficient to prove that each *finite* sum behaves as repeated applications of alternative composition (in fact, only assertions of the form $\underline{x}{:=}\underline{t}$ are needed). We give an example: suppose we have the booleans B with constants TRUE and FALSE. Then:

$$\sum_{x \in B} p(x) = \sum_{x \in B} (x{=}\mathrm{TRUE}) :\rightarrow p(x) + \sum_{x \in B} (x{=}\mathrm{FALSE}) :\rightarrow p(x) \qquad \text{(by SUBSUM)}$$

$$= p(\mathrm{TRUE}) + p(\mathrm{FALSE}) \qquad \text{(by SINGSUM).}$$

A useful additional axiom is the following axiom, which we can call FLATSUM:

$$\sum_{\underline{x} \in \underline{D}} p = p \qquad \text{if no } \underline{x} \text{ occurs free in } p$$

In order to deal with *infinite* sums, we need two additional axioms: ACTSUM, that says that any action performed by a sum construct must be an action of one of its summands, and the axiom of extensionality EXT, that says that a process is determined by its summands. These axioms are presented in table 7.

$\sum_{\underline{x} \in \underline{D}} p = \sum_{\underline{x} \in \underline{D}} p + \varepsilon \Rightarrow \exists \underline{x} \in \underline{D}\, (p = p + \varepsilon)$	ACTSUM 1
$\sum_{\underline{x} \in \underline{D}} p = \sum_{\underline{x} \in \underline{D}} p + a \cdot r \Rightarrow \exists \underline{x} \in \underline{D}\, (p = p + a \cdot r)$ no $\underline{x}$ free in r	ACTSUM 2
$\forall a \in A\, (p = p + \varepsilon \Leftrightarrow q = q + \varepsilon)$ AND $\forall a \in A\, \forall r\, (p = p + ar \Leftrightarrow q = q + ar) \Rightarrow p = q$	EXT

Table 7. Infinite sums, extensionality.

The axioms for finite merge are similar to the axioms in table 6. We give them in table 8. Notice that we can derive that each empty sum is equal to δ, which is good since δ is the neutral element of addition. The neutral element for merge, however, is not δ but ε. This is why we cannot use the guarded command construction directly, as for sum, but the *if...then...else...* construction defined in 6.5.

In order to deal with infinite merges, we can have an axiom similar to ACTSUM in table 6. We prefer, however, not to do this, since some people advocate the viewpoint that infinite merges do not occur "in reality". In this viewpoint, each infinite merge will equal CHAOS. Our theory here will not make a choice one way or the other.

$\mathop{\Vert}_{\underline{x} \in \underline{D}} p = \mathop{\Vert}_{\underline{x} \in \underline{D}} (\mathit{if}\ \phi\ \mathit{then}\ p\ \mathit{else}\ \varepsilon) \mathbin{\Vert} \mathop{\Vert}_{\underline{x} \in \underline{D}} (\mathit{if}\ \mathrm{NOT}\phi\ \mathit{then}\ p\ \mathit{else}\ \varepsilon))$	SUBMERGE
$\mathop{\Vert}_{\underline{x} \in \underline{D}} \mathit{if}\ (\underline{x}{=}\underline{t})\ \mathit{then}\ p\ \mathit{else}\ \varepsilon = p[\underline{x}{:=}\underline{t}]$ if no $\underline{x}$ occurs free in $\underline{t}$	SINGMERGE

Table 8. Generalized merge.

4.7 TRANSLATION TO COLD-K

Now we give a possible translation of the constructs of PSF/C into COLD-K. We present one of the possible translations.

The translation will introduce a number of new names. By using the backslash '\' in the sort names and constant names (see 5.2.1), we can ensure that these names are fresh, i.e. that they do not occur in a PSF/C specification. The translation of a PSF/C specification into COLD-K is described by the following, informally presented rules.

4.7.1 Basic class

To every specification we add a class, in which all basic sorts and functions are defined. In this class we define the two sorts \Process and \Action. We have three pre-defined actions: \delta, which stands for deadlock, \eps, which stands for the empty process, and \pretau, which is the action t of pre-abstraction. The injection function i enables us to see every action as a (simple) process. The three functions alt, seq and par are used to define alternative, sequential and parallel composition of two processes.

```
LET \BASIC :=

CLASS
   SORT \Process
   SORT \Action
   FUNC \delta : -> \Action
   FUNC \eps : -> \Process
   FUNC \pretau : -> \Action
   FUNC comm: \Action # \Action -> \Action
   FUNC i : \Action -> \Process
   FUNC alt : \Process # \Process -> \Process
   FUNC seq : \Process # \Process -> \Process
   FUNC par : \Process # \Process -> \Process
END;

LET \BASIC2 :=

IMPORT Booleans INTO
CLASS
   SORT \Actionset
   FUNC is-in : \Action # \Actionset -> Bool
   AXIOM FORALL S:\Actionset, T:\Actionset (
     (FORALL a:\Action (is-in(a,S) = is-in(a,T))) <=> (S=T) )
   FUNC union : \Actionset # \Actionset -> \Actionset
   FUNC intersection : \Actionset # \Actionset -> \Actionset
   FUNC difference : \Actionset # \Actionset -> \Actionset
   AXIOM FORALL S:\Actionset, T:\Actionset, a:\Action (
     is-in(a,union(S,T)) <=> is-in(a,S) OR is-in(a,T);
     is-in(a,intersection(S,T)) <=> is-in(a,S) AND is-in(a,T);
     is-in(a,difference(S,T)) <=> is-in(a,S) AND NOT is-in(a,T) )
   FUNC encaps : \Actionset # \Process -> \Process
   FUNC hide : \Actionset # \Process -> \Process
   PRED summand : \Process # \Process
   AXIOM FORALL x:\Process, y:\Process (
     summand(x,y) <=> y = alt(y,x) )
   PRED defined : \Process
   IND  defined(\eps) AND
     FORALL a:\Action, x:\Process (
     NOT (a=\delta) => (defined(i(a)) AND defined(seq(i(a),x)));
     (defined(x) OR defined(y)) => defined(alt(x,y)) )
   AXIOM FORALL x:\Process (
     NOT(defined(x)) => (x = \delta) )
END;
```

4.7.2 Translation

We will now walk through the grammar of section 5.3 in order to define a translation for all constructs which where not already part of COLD-S.

<namepair>

Since <action-name>, <process-name> and <set-name> in the sequel are all translated into instances of <function-name>, and since all objects involved are identifiers, these sections remain unchanged after the translation.

<item>

- `ACTION <action-name> : domain` is translated into
  FUNC <action-name> : domain -> \Action.
- PROCESS <process-name> : domain is translated into
  FUNC <process-name> : domain -> \Process.
- SET <set-name> is translated into
  FUNC <set-name>-> \Actionset.
  PRED <set-name>: \Action

<definition>

- ACTION <action-name> : domain is translated into
  FUNC <action-name> : domain -> \Action.
- PROCESS <process-name> : domain <process-body> is translated into
  FUNC <process-name> : domain -> \Process <process-body>.
- SET <set-name> <set-body> is translated into
  `PRED <set-name>: \Action <set-body>.`

In order to define the encapsulation and hide functions, we need to define a function of type \Actionset with the same name and meaning as the predicate. This meaning is defined by the function is-in.

```
FUNC <set-name>-> \Actionset
AXIOM FORALL a:\Action (
   is-in(a,<set-name>) = true <=> <set-name>(a);
   is-in(a,<set-name>) = false <=> NOT <set-name>(a) )
```

- `COMM <comm-assertion>` is translated into
  `AXIOM <comm-assertion>`
- `SPEC <spec-body>` is translated into
  `AXIOM <spec-body>`

<comm assertion>

- `<action term> | <action term> = <action term>` is translated into
  AXIOM comm (<action term>, <action term>) = <action term>

<process expr>

•PRETAU into
 i(\pretau)

•DELTA into
 i(\delta)

•EPSILON into
 \eps

•<process expr> . <process expr> into
 seq(<process expr>, <process expr>)

•<process expr> + <process expr> into
 alt(<process expr>, <process expr>)

•<process expr> || <process expr> into
 par(<process expr>, <process expr>)

•GCMD <assertion> <process expr> needs a more complex translation. Each time the guarded command construction occurs, we have to declare a new process name (since we cannot have an assertion occur as the argument of a function). Thus, we have a new process name

gcmd\ext.

Here ext is a counter that is increased each time a guarded command occurs in the specification. We define gcmd\ext by adding the following definition:

```
FUNC gcmd\ext: \Process -> \Process
AXIOM FORALL p: \Process (<assertion> => gcmd\ext(p) = p).
```

By the definedness condition in the class \BASIC2, gcmd\ext(p) will become i(\delta) when the assertion does not hold, which is as required.

Thus the GCMD expression is translated into gcmd\ext(<process expr>).

•`SUM <varsort list>  <process expr>` is translated as follows:

First determine all free variables in <process expr> that not are in <varsort list>. Denote these variables by <free var list>. Then define a function sum\ext, with these free variables as arguments. <free varsort list> is derived from <free var list> by adding appropriate type information. This type information is denoted by <free sort list>.

```
FUNC sum\ext : <free sort list> -> \Process
AXIOM FORALL <free varsort list>, <varsort list>  (
   summand(<process expr>, sum\ext(<free var list>) )
```

This axiom states that all instances of the argument of the sum construct are a summand of the total process.

```
AXIOM FORALL a:\Action, p:\Process, <free varsort list> (
   summand(seq(i(a),p), sum\ext(<free var list>) ) =>
      EXISTS <varsort list>
         summand(seq(i(a),p), <process expr>  )
AXIOM FORALL <free varsort list>
   summand(\eps, sum\ext(<free var list>) ) =>
      EXISTS <varsort list>
         summand(\eps, <process expr>)
```

These two axioms state that all summands of the total expression can be obtained as summands of the instances of the sum argument.

So the sum construction is translated into sum\ext(<free var list>)

•`MERGE <varsort list> <process expr>` is translated as follows:
First determine all free variables in <process expr> that not are in <varsort list>. Denote these variables by <free var list>. Then define a function merge1\ext, with these free variables as arguments.

```
FUNC merge1\ext: <free sort list> -> \Process
```

The axioms for merge are harder to formulate. We need an additional function that keeps track of all elements that are already used to split off a sub-merge. These elements are collected in a set.

```
FUNC merge2\ext: <free sort list> # Set\ext -> \Process
AXIOM FORALL <free varsort list> (
  merge1\ext(free var list>) = merge2\ext(<free var list>, empty);
  FORALL <var sort list>, set : Set\ext (
     NOT is_in(<var list>, set)  =>
     merge2\ext(<free var list>, set)
        = par(merge2\ext(<free var list>, add(<var list>,set)), <process expr> );
  FORALL set : Set\ext (
     (FORALL <var sort list> is_in(<var list>, set) )  =>
           merge2\ext(<free var list>, set) = \eps))
```

In order to define the set concept we need the following definitions:

```
SORT Set\ext
FUNC empty -> Set\ext
FUNC add: <sort list> # Set\ext -> Set\ext
PRED is_in: <sort list> # Set\ext
IND  FORALL <var sort list>, set : Set\ext (
        NOT is_in(<var list>, empty);
        FORALL <var sort list>'  is_in(<var list>, add(<var list>', set) =
                         " <var list> = <var list>' "  OR  is_in(<var list>, set)
```

Here we use the meta-notation " <var list> = <var list>' " to indicate the COLD expression that both lists are componentwise equal. The notation <var sort list>' stands for a new list of variable names and sorts, compatible with the list <var sort list>

•`ENCAPS <set-process expr>` into
encaps (<set expr>, <process expr>)

•`HIDE <set-process expr>` into
hide (<set expr>, <process expr>)

<set expr>

•<set expr> + <set expr> into
union<set expr>, <set expr>)

•<set expr> & <set expr> into

intersection<set expr>, <set expr>)

<set expr> ^ <set expr> into

difference<set expr>, <set expr>)

Algebraic laws

Finally we add the class containing the algebraic laws.

```
LET laws :=
EXPORT
   SORT \Process,
   SORT \Action,
   FUNC \delta : -> \Action,
   FUNC \pretau : -> \Action,
   FUNC comm : \Action # \Action -> \Action,
   FUNC i : \Action -> Process,
   FUNC alt : \Process # \Process -> \Process,
   FUNC seq : \Process # \Process -> \Process,
   FUNC par : \Process # \Process -> \Process,
   SORT \Actionset,
   FUNC union : \Actionset # \Actionset -> \Actionset,
   FUNC intersection : \Actionset # \Actionset -> \Actionset,
   FUNC difference : \Actionset # \Actionset -> \Actionset,
   FUNC encaps : \Actionset # \Process -> \Process,
   FUNC hide : \Actionset # \Process -> \Process,
   PRED summand : \Process # \Process,
   PRED defined : \Process

FROM
IMPORT \BASIC INTO
IMPORT \BASIC2 INTO
CLASS
   AXIOM FORALL x:\Process, y:\Process, z:\Process (        {BPA}
      alt(x,y) = alt(y,x);
      alt(alt(x,y),z) = alt(x,alt(y,z));
      alt(x,x) = x;
      seq(alt(x,y),z) = alt(seq(x,z),seq(y,z));
      seq(seq(x,y),z) = seq(x,seq(y,z)) )
   AXIOM FORALL x:\Process (                          {DELTA}
      alt(x,i(\delta)) = x;
      seq(i(\delta),x) = i(\delta))
   AXIOM FORALL H:\Actionset, a:\Action, x:\Process, y:\Process (   {ENCAPS}
      NOT(H(a)) => encaps(H,i(a)) = a;
      H(a) => encaps(H,i(a)) = i(\delta);
      encaps(H,alt(x,y)) = alt(encaps(H,x),encaps(H,y));
      encaps(H,seq(x,y)) = seq(encaps(H,x),encaps(H,y)) )
FUNC comm: \Process # \Process -> \Process
AXIOM FORALL a:\Action, b:\Action, c:\Action (
      comm(i(a),i(b)) = i(comm(a,b));
      comm(a,b) = comm(b,a);
      comm(comm(a,b),c) = comm(a,comm(b,c));
      comm(\delta,a) = \delta
      comm(\pretau,a) = \delta  )
   FUNC leftmerge : \Process # \Process -> \Process
   AXIOM FORALL a:\Action, b:\Action, x:\Process, y:\Process, z:\Process (  {ACP}
      par(x,y) = alt(alt(leftmerge(x,y),leftmerge(y,x)),comm(x,y));
      leftmerge(i(a),x) = seq(i(a),x);
      leftmerge(seq(i(a),x),y) = seq(i(a),par(x,y));
      leftmerge(alt(x,y),z) = alt(leftmerge(x,z),leftmerge(y,z));
      comm(seq(i(a),x),i(b)) = seq(comm(i(a),i(b)),x);
      comm(i(a),seq(i(b),x)) = seq(comm(i(a),i(b)),x);
      comm(seq(i(a),x),seq(i(b),y)) = seq(comm(i(a),i(b)),par(x,y));
      comm(alt(x,y),z) = alt(comm(x,z),comm(y,z));
      comm(x,alt(y,z)) = alt(comm(x,y),comm(x,z)) )
```

```
    AXIOM FORALL H:\Actionset, a:\Action, x:\Process, y:\Process (   {HIDE}
       ((a = \delta) OR NOT(H(a)))  =>  hide(H,i(a)) = i(a);
       ((NOT a=\delta) AND H(a))  =>  hide(H,i(a)) = i(\pretau);
       hide(H,alt(x,y)) = alt(hide(H,x),hide(H,y));
       hide(H,seq(x,y)) = seq(hide(H,x),hide(H,y)) )
    AXIOM x:\Process, y:\Process, z:\Process (       {SC}
       par(x,i(\delta)) = seq(x,i(\delta));
       par(i(\delta),x) = seq(x,i(\delta));
       par(x,par(y,z)) = par(par(x,y),z);
       par(x,y) = par(y,x)
    AXIOM x:\Process, y:\Process, a:\Action, H:\Actionset (        {EPS}
       seq(\eps,x) = x;
       seq(x,\eps) = x;
       leftmerge(\eps,\eps) = \eps;
       leftmerge(\eps,seq(i(a),x)) = i(\delta);
       leftmerge(\eps,alt(x,y)) = alt(leftmerge(\eps,x),leftmerge(\eps,y);
       comm(\eps,x) = i(\delta);
       comm(x,\eps) = i(\delta);
       encaps(H,\eps) = \eps;
       hide(H,\eps) = \eps;
       par(\eps,x) = x )
END;
```

Example

The translation presented in the previous sections will be demonstrated with an example. Consider the simple PSF/C specification:

```
DESIGN
   NONE
SYSTEM

LET SPEC1 :=

CLASS
   SORT D
   FUNC d1: -> D
   FUNC d2: -> D
   ACTION s : D
   PROCESS send
      DEF PRETAU.s(d1) + PRETAU.s(d2)
END;

LET SPEC2 :=
IMPORT SPEC1 INTO
CLASS
   ACTION r : D
   ACTION c : D
   PROCESS read
   PROCESS system
   SET H
      IND FORALL d:D
         H(r(d));
         H(s(d)))
   COMM FORALL d:D (
      r(d) | s(d) = c(d))

   SPEC
      system = ENCAPS(H, send || read);
      read = SUM( d:D, r(d))
END;
SPEC2
```

```
DESIGN
   NONE
SYSTEM
LET BASIC := ...

LET SPEC1 :=

IMPORT BASIC INTO
CLASS
   SORT D
   FUNC d1: -> D
   FUNC d2: -> D
   FUNC s : D -> \Action
   FUNC send : -> \Process
      DEF alt(seq(i(\pretau),i(s(d1)), seq(i(\pretau),i(s(d2)))
END;

LET SPEC2 :=
IMPORT BASIC INTO
IMPORT SPEC1 INTO
CLASS
   FUNC r : D -> \Action
   FUNC c : D -> \Action
   FUNC read -> \Process
   FUNC system -> \Process
   PRED H : \Action
      IND FORALL d:D
         H(r(d));
         H(s(d)))
   FUNC H -> \Actionset
   AXIOM FORALL a: \Action (
      is-in(a,H) = true <=> H(a);
      is-in(a,H) = false <=> NOT H(a) )
   AXIOM FORALL d:D (
      comm(r(d),s(d)) = c(d))

   AXIOM
      system = encaps(H, par(send,read));
      read = sum\1
   FUNC sum\1 : -> \Process
   AXIOM FORALL d:D ( summand(i(r(d)), sum\1))
   AXIOM FORALL a:\Action, p:\Process (
      summand(seq(i(a),p), sum\1) =>
         EXISTS d:D
            summand(seq(i(a),p), i(r(d))   )
   AXIOM
      summand(\eps, sum\1 ) =>
         EXISTS d:D
            summand(\eps, i(r(d)))
END;
SPEC2
```

5 Examples

In this section we give some examples of a specification in PSF/C, which illustrate the use of simple data types, process definitions and the concept of parameterization. The examples deal with vending machines, a landing control system for an airport and the alternating bit protocol.

5.1 A VENDING MACHINE

5.1.1 The Problem

In this first example, adapted from MAUW & VELTINK [MV89], we want to specify a vending machine that sells tea and coffee. In fact this is a very simple machine, for it only accepts two kinds of coins, 10c coins and 25c coins, it does not give any change and there are no buttons to choose between coffee or tea. The choice is determined by whichever coin is inserted.

5.1.2 The Implementation

In our example we have used just one class, called VENDING_MACHINE_AND_USERS, to specify the vending machine. Firstly, we define all atomic actions that occur in the specification. The atomic actions fall apart into three categories. These categories are the actions of the vending machine, the action of the customer and the actions that are the result of a communication between the customer and the vending machine. In the COMM section we define all possible pairs of actions that can communicate with each other and we specify what the resulting action will be. This implicitly implies that all communications that are not listed here are prohibited. Next we define a set of atomic actions called H. This set contains all atomic actions that are performed by either the machine or the customer. Its use will show up later on. After having defined the atomic actions and the communication function we are able to specify the processes. The first process is called VMCT and represents the vending machine. Initially it offers the choice of a insert_10c or a insert_25c action, after which it continues to serve tea or coffee. After having served a drink VMCT returns to its initial state. The two next processes define a customer who wants tea and a customer who wants coffee. The last process defines the combination of the three previously defined processes. The vending machine is operating in parallel with the customers, in this example it serves a Tea_User followed by a Coffee_User, in that specific order. The ENCAPS operator forbids the atomic actions listed in H to occur on their own and such forces communication.

5.1.3 The Specification

```
DESIGN
  NONE
SYSTEM

%
% Name : VENDING_MACHINE_AND_USERS
% Date : 14/11/88
%
% Description :
%
% A very simple vending machine with two users.

LET VENDING_MACHINE_AND_USERS :=


CLASS
  ACTION insert_10c       :
  ACTION accept_10c       :
  ACTION 10c_paid         :
  ACTION insert_25c       :
  ACTION accept_25c       :
  ACTION 25c_paid         :
  ACTION serve_tea        :
  ACTION take_tea         :
  ACTION tea_delivered    :
    ACTION serve_coffee     :
    ACTION take_coffee      :
    ACTION coffee_delivered :

  COMM
    insert_10c    | accept_10c   = 10c_paid;
    insert_25c    | accept_25c   = 25c_paid;
    serve_tea     | take_tea     = tea_delivered;
    serve_coffee  | take_coffee  = coffee_delivered

  SET  H
    IND
      H(insert_10c);
      H(accept_10c);
      H(insert_25c);
      H(accept_25c);
      H(serve_coffee);
      H(take_coffee);
      H(serve_tea);
      H(take_tea)

    PROCESS VMCT :
    DEF ((accept_10c . serve_tea) +
         (accept_25c . serve_coffee)) . VMCT;

    PROCESS Tea_User :
    DEF insert_10c . take_tea;

    PROCESS Coffee_User :
    DEF insert_25c . take_coffee;

    PROCESS System :
    DEF ENCAPS(H, VMCT || ( Tea_User . Coffee_User ))

  END;

  VENDING_MACHINE_AND_USERS
```

5.2 A LANDING CONTROL SYSTEM

5.2.1 The Problem

In the next example, adapted from MAUW & VELTINK [MV88], we specify a hypothetical landing control system for an airport. It is designed to handle the landing of a number of airplanes on a number of landing strips. Since the actual names of the airplanes and the strips can be considered as conditions local to some specific airport, we specify a control system which is parameterized with these items. The system consists of a number of parallel operating subsystems, first of which is the *Distribution* process. The other processes, the *Strip_Controllers*, all have the same behaviour. Each of them has control over exactly one landing strip.

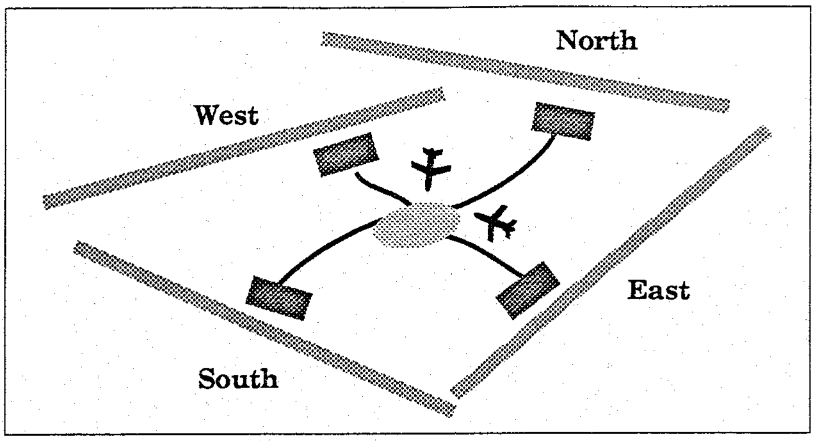

figure 1. Timbuktu Airport.

5.2.2 The Implementation

The class *Landing_Control* is parameterized by the class *Airport*. This class consists of the two sorts *Strips*, containing the names of the landing strips, and *Plane_Ids*, containing the id's of all planes potentially willing to land. The *Landing_Control* exports the atomic action *receive-req-to-land*, which enables the system to communicate with arriving airplanes, and the process *Control*, which is the name of the overall process being specified. Internal to this class are a number of atomic actions. The atoms *read, send* and *communicate* are used to model the communication between the process *Distribution* and each of the *Strip_Controllers*. The *Strips* argument determines which *Strip_Controller* is involved, and the *Plane_Ids* argument indicates the plane that should be landed. As is indicated in the communications section, placing the atoms *send* and *read* in parallel yields the atom *communicate*. The set *H*, containing the *read* and *send* actions will be used to encapsulate unsuccessful communication. This happens when the *read* and *send* actions do not have a partner to communicate with. The other atomic actions, *land* and *disembark*, are not intended to take part in a communication.

Apart from the *Control* process we define three processes. The process *Distribution* receives a request to land from some plane and sends its id to one of the *Strip_Controllers*, which is willing to communicate with the *Distribution*. After that, the *Distribution* process starts all over again. The process *Strip_Control* is indexed with the name of some *Strip*. In fact it defines a new process for each *Strip*. It starts by receiving a message from the *Distribution* to handle a plane with a given id. After handling this plane, as defined by the process *Handle*, the *Strip_Controller* starts all over and is again able to receive a plane-id. The process *Handle* serves as a sub-process of the process *Strip_Control*. The second argument determines the plane and the first one determines the *Strip* the plane must land on. This process stops after landing and disembarking the plane.

Finally the overall process *Control* is defined as the concurrent operation of the *Distribution* and all *Strip_Controllers*. The encapsulation operator removes unsuccessful communications.

5.2.3 The Specification

```
DESIGN
  NONE
SYSTEM

%
```

```
% Name : AIRPORT
% Date : 11/11/88
%
% Description :
%
% Local airport conditions, to be supplied to the Landing_Control

LET AIRPORT :=

CLASS
  SORT Strips
  SORT Plane_Ids
END;

%
% Name : Landing_Control
% Date : 11/11/88
%
% Description :
%
% A generic landing control system for an airport.

LET LANDING_CONTROL :=

LAMBDA X:AIRPORT OF

EXPORT
  SORT Plane_Ids,
  ACTION receive_req_to_land : Plane_Ids,
  PROCESS Control :
FROM

IMPORT X INTO

CLASS
  ACTION receive_req_to_land : Plane_Ids
  ACTION read                : Strips # Plane_Ids
  ACTION send                : Strips # Plane_Ids
  ACTION communicate         : Strips # Plane_Ids
  ACTION land                : Strips # Plane_Ids
  ACTION disembark           : Plane_Ids

COMM FORALL s:Strips, id:Plane_Ids
    (send(s,id) | read(s,id)  = communicate(s,id))

SET  H
  IND FORALL s:Strips, id:Plane_Ids (
    H(read(s,id));
    H(send(s,id)) )

  PROCESS Distribution :
  DEF SUM id:Plane_Ids (receive_req_to_land(id) .
                         SUM s:Strips (send(s,id))
                        ) . Distribution

  PROCESS Strip_Control : Strips
  PAR s:Strips
  DEF SUM id:Plane_Ids (read(s,id) . Handle(s,id)
                         ) . Strip_Control(s)

  PROCESS Handle : Strips # Plane_Ids
  PAR s:Strips, id:Plane_Ids
  DEF land(s,id) . disembark(id)

  PROCESS Control :
    DEF ENCAPS(H, Distribution ||
                   MERGE s:Strips (Strip_Control(s))) )

  END;
```

This specification can be used as a generic specification for *Landing_Controllers*. A *Landing_Control* at for instance *Timbuktu-Airport* can be constructed by binding a class which defines the landing strips and the planes that potentially land at *Timbuktu-Airport* to the parameter of *Landing_Control*.

```
%
% Name : TIMBUKTU_AIRPORT
% Date : 11/11/88
%
% Description :
%
% Airport conditions local to Timbuktu-airport

LET TIMBUKTU_AIRPORT :=

CLASS
  SORT Timbuktu_Strips
  SORT Timbuktu_Plane_Ids
  FUNC North : -> Timbuktu_Strips
  FUNC East  : -> Timbuktu_Strips
  FUNC South : -> Timbuktu_Strips
  FUNC West  : -> Timbuktu_Strips
  FUNC KL204 : -> Timbuktu_Plane_Ids
  FUNC SQ001 : -> Timbuktu_Plane_Ids
  FUNC JL403 : -> Timbuktu_Plane_Ids
  FUNC PA666 : -> Timbuktu_Plane_Ids
  FUNC HA345 : -> Timbuktu_Plane_Ids

END;


%
% Name : TIMBUKTU_LANDING_CONTROL
% Date : 11/11/88
%
% Description :
%
% The landing control system at Timbuktu-airport

LET TIMBUKTU_LANDING_CONTROL:=


APPLY
  RENAME
    SORT Strips    TO Timbuktu_Strips,
    SORT Plane_Ids TO Timbuktu_Plane_Ids
  IN LANDING_CONTROL
TO TIMBUKTU_AIRPORT;

TIMBUKTU_LANDING_CONTROL
```

5.3 ALTERNATING BIT PROTOCOL

5.3.1 The Problem

One of the most famous communication protocols is the Alternating Bit Protocol (ABP). It has been used many times to serve as a test case for a new specification formalism. Our specification emanates from the ABP specification in ACP as described in BERGSTRA & KLOP [BK86a,BK86b].

We can represent the Alternating Bit Protocol with a picture as follows:

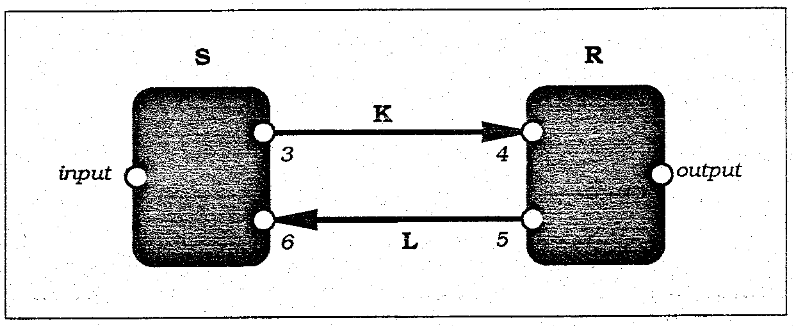

figure 2 Graphical representation of the Alternating Bit Protocol.

It consists of four components:

- *S* : The sender.
- *R* : The receiver.
- *K* : A channel connecting the sender and the receiver.
- *L* : A channel connecting the receiver and the sender.

The goal of the Alternating Bit Protocol is to transport data items from a certain set *D* from the input port to the output port. In the next paragraphs we will give a description of each component.

5.3.1.1 The Sender

First, component *S* reads a message at the input port. This message is extended with a *control boolean* to form a so-called *frame* and this frame is sent along channel *K* (3). The sending of the frame proceeds until component *S* receives an acknowledgement of a successful transmission at channel *L* (6). After a successful transmission component *S* flips the control boolean and starts all over again.

5.3.1.2 Communication Channel *K*

Component *K* transmits frames from the sender (3) to the receiver (4). There are two situations that can occur when sending information along channel *K*.

- The frame is properly transmitted.
- The frame is corrupted during the transmission.

We assume channel *K* to be *fair*, i.e, it will not produce an infinite stream of corrupted data.

5.3.1.3 The Receiver

The receiver *R* reads a frame from channel *K* (4). We assume that *R* is able to tell, e.g. by performing a *checksum control*, whether or not the frame has been corrupted. When the frame is correct *R* checks the control boolean in the frame. If this control boolean matches the internal control boolean of *K*, the message in the frame is sent to the output port, *K* flips its internal boolean and starts waiting for the next frame to arrive. In all other cases *R* sends the complement of its own control boolean along channel *L* (5) and waits for the retransmission of the frame.

5.3.1.4 Communication Channel *L*

Component *L* is used to transmit *receive acknowledgements* from the receiver (5) to the sender (6). Like channel *K*, channel *L* is able to corrupt data. We will assume that the sender *S* can tell whether an acknowledgement has been corrupted. We assume that channel *L* is fair too.

5.3.2 The Implementation

The specification of the Alternating Bit Protocol starts of with a some classes from the COLD IGLOO (Incremental Generic Library Of Objects). These classes are ITEM, ITEM1, ITEM2, BOOL_SPEC and TUP2_SPEC. The first three classes specify a class with a single free sort. Further on in this specification these classes are used as a parameter restriction. The booleans are specified in BOOL_SPEC, and TUP2_SPEC defines tuples of data types.

Next come the classes that are specific for this application. At first we have to model the frames that are sent along channel K. This is achieved in FRAME_SPEC by binding the second parameter of TUP2_SPEC to the booleans, leaving the first parameter untouched. Next we want to specify the unreliable channels of the protocol. Because channels K and L are fairly similar we want to exploit this fact, and so we give a specification of a channel, that is parameterized by the data item that is transported along it, in UC_SPEC. There are three atomic actions involved with the definition of an unreliable channel: a read and a send action, both parameterized by a certain data type, and an error action indicating malfunctioning of the channel.

The sender S and the receiver R are specified in SENDER_SPEC and RECEIVER_SPEC respectively. Both are still parameterized by the data type that is to be transmitted by the system and both make use of the BOOL_SPEC and the FRAME_SPEC so these two classes have to be imported.

Now that we have defined the separate objects of the system, we have to glue them together. This is done in the class ABP_SPEC. The specification of the sender and the receiver are imported and the unreliable channel is imported twice, even. During the import some renamings on the items of the classes are performed along with some bindings. In this way it is possible to create two different channels viz.: one which is bound to frames to model K, and one which is bound to the booleans to model L. Note that this class is still parameterized by the data item to be transmitted, so that we now have an universal specification of the Alternating Bit Protocol supplying one process: ABP, an input action: read_item and an output action: send_item.

The last thing we have to do is to supply two objects, one at either side of the ABP process, one of which supplies the data items, RANDOM_SPEC, and one of which reads all data items, DRAIN_SPEC. In this example we want to transmit bits along the system so we define BIT by renamings on BOOL_SPEC, and finally we tie together the RANDOM_SPEC, ABP_SPEC and DRAIN_SPEC and instantiate the parameter with BIT in the final class called: ABP_SYSTEM_SPEC.

5.3.3 The Specification

```
DESIGN
  NONE
SYSTEM

%
% Name : ITEM
% Date : 15/03/88
%
% Description :
%
% This specifies a class with a single free sort.

LET ITEM :=

CLASS
  SORT Item  FREE
END;



%
% Name : ITEM1
% Date : 15/03/88
%
% Description :
%
% This specifies a class with a single free sort.

LET ITEM1 :=

CLASS
  SORT Item1  FREE
END;



%
% Name : ITEM2
% Date : 15/03/88
%
% Description :
%
% This specifies a class with a single free sort.

LET ITEM2 :=

CLASS
  SORT Item2  FREE
END;



%
% Name : BOOL_SPEC
% Date : 09/03/88
%
% Description :
%
% This is a specification of the data type of booleans with
% inductive definitions for the non-constructor operations.
% The inductive definitions are in a compact style.
```

```
LET BOOL_SPEC :=

EXPORT

  SORT Bool,
  FUNC true  :                -> Bool,
  FUNC false :                -> Bool,
  FUNC not   : Bool           -> Bool,
  FUNC and   : Bool # Bool -> Bool,
  FUNC or    : Bool # Bool -> Bool,
  FUNC imp   : Bool # Bool -> Bool,
  FUNC eqv   : Bool # Bool -> Bool,
  FUNC xor   : Bool # Bool -> Bool

FROM
CLASS

  SORT Bool
  FUNC true  :-> Bool
  FUNC false :-> Bool

  AXIOM
  {BOOL1} true!;
  {BOOL2} false!;
  {BOOL3} NOT true = false

  PRED is_gen : Bool
  IND is_gen(true);
      is_gen(false)

  AXIOM FORALL b:Bool
  {BOOL4} is_gen(b)

  FUNC not: Bool -> Bool
  IND  not(true) = false;
       not(false) = true

  FUNC and: Bool # Bool -> Bool
  IND FORALL b:Bool
      ( and(false,b) = false;
        and(true,b) = b  )

  FUNC or: Bool # Bool -> Bool
  IND FORALL b:Bool
      ( or(false,b) = b;
        or(true,b) = true  )

  FUNC imp: Bool # Bool -> Bool
  IND FORALL b:Bool
      ( imp(false,b) = true;
        imp(true,b) = b  )

  FUNC eqv: Bool # Bool -> Bool
  IND FORALL b:Bool, c:Bool
      ( b = c        => eqv(b,c) = true;
        NOT  b = c   => eqv(b,c) = false )

  FUNC xor: Bool # Bool -> Bool
  IND FORALL b:Bool, c:Bool
      ( b = c        => xor(b,c) = false;
        NOT  b = c   => xor(b,c) = true )

END;
```

```
%
% Name : TUP2_SPEC
% Date : 10/03/88
%
% Description :
%
% This is an axiomatic specification of the 2-tuple data type
% with inductive definitions for the non-constructor operations.

LET TUP2_SPEC :=

LAMBDA X:ITEM1 OF
LAMBDA Y:ITEM2 OF
EXPORT

  SORT Tup,
  SORT Item1,
  SORT Item2,
  FUNC tup   : Item1 # Item2 -> Tup,
  FUNC proj1 : Tup           -> Item1,
  FUNC proj2 : Tup           -> Item2

FROM
IMPORT X INTO
IMPORT Y INTO

CLASS
  SORT Tup   DEP Item1, Item2
  FUNC tup : Item1 # Item2 -> Tup

  AXIOM FORALL i1:Item1, j1:Item1, i2:Item2, j2:Item2 (
  {TUP1} tup(i1,i2)!;
  {TUP2} tup(i1,i2) = tup(j1,j2) => i1 = j1 AND i2 = j2 )

  PRED is_gen: Tup
  IND FORALL i1:Item1, i2:Item2 (
        is_gen(tup(i1,i2)) )

  AXIOM FORALL t:Tup
  {TUP3} is_gen(t)

  FUNC proj1: Tup -> Item1
  IND FORALL i1:Item1, i2:Item2 (
        proj1(tup(i1,i2)) = i1 )

  FUNC proj2: Tup -> Item2
  IND FORALL i1:Item1, i2:Item2 (
        proj2(tup(i1,i2)) = i2 )

END;


%
% Name : FRAME_SPEC
% Date : 20/10/88
%
% Description :
%
% This is a specification of a frame consisting of the item
% that is used in the Alternating Bit Protocol and a boolean.

LET FRAME_SPEC :=
    LAMBDA X:ITEM OF
      APPLY
        RENAME
     SORT Item1 TO Item
        IN
     APPLY
       RENAME
         SORT Item2 TO Bool,
         SORT Tup   TO Frame,
         FUNC tup : Item1 # Item2 -> Tup  TO frame
       IN TUP2_SPEC
          TO X
      TO BOOL_SPEC;


%
% Name : UC_SPEC
% Date : 19/08/88
%
% Description :
%
% This is a specification of an unreliable channel that
% either transports one item from its input to its output,
% or generates some kind of error stating malfunctioning

LET UC_SPEC :=

LAMBDA X:ITEM OF

EXPORT
  SORT Item,
  PROCESS UC: ,
  ACTION read: Item ,
  ACTION send: Item ,
  ACTION error:
FROM

IMPORT X INTO

CLASS
  ACTION read: Item
  ACTION send: Item
  ACTION error:

  PROCESS UC:
  DEF SUM d:Item (read(d)  . UC(d));

  PROCESS UC: Item
  PAR d:Item
  DEF (skip . send(d) + skip . error) . UC

END;



%
% Name : SENDER_SPEC
% Date : 19/08/88
%
% Description :
%
% This is a specification of the sender of the
% Alternating Bit Protocol.
```

```
LET SENDER_SPEC :=

LAMBDA X:ITEM OF

EXPORT
  SORT Frame,
  SORT Item,
  SORT Bool,
  PROCESS S : ,
  ACTION read_item: Item ,
  ACTION send_frame: Frame ,
  ACTION read_ack: Bool ,
  ACTION read_ack_error:
FROM

IMPORT X INTO
IMPORT BOOL_SPEC INTO
IMPORT APPLY FRAME_SPEC TO X INTO

CLASS
  ACTION read_item: Item
  ACTION send_frame: Frame
  ACTION read_ack: Bool
  ACTION read_ack_error:

  PROCESS S :
  DEF RM(false)

  PROCESS RM : Bool
  PAR b:Bool
  DEF SUM d:Item (read(d) . SF(d,b))

  PROCESS SF : Item # Bool
  PAR d:Item, b:Bool
  DEF send_frame(frame(d,b)) . RA(d,b)

  PROCESS RA : Item # Bool
  PAR d:Item, b:Bool
  DEF (read_ack(not(b)) + receive_error) . SF(d,b)
     + read_ack(b) . RM(not(b))

END;



%
% Name : RECEIVER_SPEC
% Date : 20/08/88
%
% Description :
%
% This is a specification of the receiver of the
% Alternating Bit Protocol.

LET RECEIVER_SPEC :=

LAMBDA X:ITEM OF

EXPORT
  SORT Frame,
  SORT Item,
  SORT Bool,
  PROCESS R : ,
    ACTION send_item: Item ,
    ACTION read_frame: Frame ,
    ACTION send_ack: Bool ,
    ACTION read_frame_error:
  FROM

  IMPORT X INTO
  IMPORT BOOL_SPEC INTO
  IMPORT APPLY FRAME_SPEC TO X INTO

  CLASS
    ACTION send_item: Item
    ACTION read_frame: Frame
    ACTION send_ack: Bool
    ACTION read_frame_error:

    PROCESS R :
    DEF RF(false);

    PROCESS RF : Bool
    PAR b:Bool
    DEF (SUM d:Item (read_frame(d,not(b))) + receive_error)
           . SA(not(b))
         + SUM d:Item (read_frame(d,b) . SM(d,b))

    PROCESS SA : Bool
    DEF send_ack(b) . RF(not(b))

    PROCESS SM : Item # Bool
    PAR d:Item, b:Bool
    DEF send_item(d) . SA(b)

  END;


  %
  % Name : ABP_SPEC
  % Date : 25/10/88
  %
  % Description :
  %
  % This is a specification of the Alternating Bit Protocol, which
  % combines all previously defined classes into one system

  LET ABP_SPEC :=

  LAMBDA X:ITEM OF

  EXPORT

    SORT Item,
    PROCESS ABP : ,
    ACTION read_item : Item ,
    ACTION send_item : Item

  FROM

  IMPORT BOOL_SPEC INTO
  IMPORT X INTO

  IMPORT
    APPLY
      RENAME
        PROCESS S :  TO SENDER
      IN SENDER_SPEC
  TO X
INTO

IMPORT
  APPLY
    RENAME
      PROCESS R :  TO RECEIVER
    IN RECEIVER_SPEC
  TO X
INTO

IMPORT
  APPLY
    RENAME
      SORT Item TO Frame,
      PROCESS UC :  TO FRAME_CHANNEL,
      ACTION read : Item  TO read_frame_item,
      ACTION send : Item  TO send_frame_item,
      ACTION error :  TO send_frame_error
    IN UC_SPEC
  TO
    APPLY FRAME_SPEC TO X
INTO

IMPORT
  APPLY
    RENAME
      SORT Item TO Bool,
      PROCESS UC :  TO ACK_CHANNEL,
      ACTION read : Item  TO read_ack_item,
      ACTION send : Item  TO send_ack_item,
      ACTION error :  TO send_ack_error
    IN UC_SPEC
  TO BOOL_SPEC
INTO


CLASS

  ACTION frame_error :
  ACTION ack_error :
  ACTION ack_enters_channel : Bool
  ACTION ack_leaves_channel : Bool
  ACTION frame_enters_channel : Frame
  ACTION frame_leaves_channel : Frame

COMM
  send_frame_error | read_frame_error  = frame_error;
  send_ack_error   | read_ack_error    = ack_error

COMM FORALL b:Bool (
  send_ack(b)      | read_ack_item(b)  = ack_enters_channel(b);
  send_ack_item(b) | read_ack(b)       = ack_leaves_channel(b) )

COMM FORALL f:Frame (
  send_frame(f)      | read_frame_item(f)  = frame_enters_channel(f);
  send_frame_item(f) | read_frame(f)       = frame_leaves_channel(f) )

SET  H
  IND FORALL d:Item, b:Bool, f:Frame (
    H(send_frame_error);
    H(read_frame_error);
    H(send_ack_error);
    H(read_ack_error);
    H(read_item(d));
    H(send_item(d));
    H(send_ack(b));
    H(read_ack(b));
    H(read_ack_item(b));
    H(send_ack_item(b));
    H(send_frame(f));
    H(read_frame(f));
    H(read_frame_item(f));
    H(send_frame_item(f)) )

  PROCESS ABP :
  DEF ENCAPS(H, SENDER || RECEIVER || ACK_CHANNEL || FRAME_CHANNEL)

END;


%
% Name : RANDOM_SPEC
% Date : 25/10/88
%
% Description :
%
% This is a specification of a process that produces a random stream
% of items of the specified sort

LET RANDOM_SPEC :=

LAMBDA X:ITEM OF
EXPORT

  SORT Item,
  PROCESS RANDOM : ,
  ACTION output : Item

FROM

IMPORT X INTO

CLASS

  ACTION output : Item
  PROCESS RANDOM :
  PAR d:Item
  DEF SUM d:Item (SKIP . output(d)) . RANDOM )

END;

%
% Name : DRAIN_SPEC
% Date : 25/10/88
%
% Description :
%
% This is a specification of a process discarding all elements
% of a certain sort

LET DRAIN_SPEC :=

LAMBDA X:ITEM OF
EXPORT

  SORT Item,
  PROCESS DRAIN : ,
  ACTION input : Item
```

```
FROM

IMPORT X INTO

CLASS

  ACTION input : Item
  PROCESS DRAIN :
  PAR d:Item
  DEF SUM d:Item (input(d))  . DRAIN )

END;


%
% Name : BIT
% Date : 25/10/88
%
% Description :
%
% This is a specification of the class of binary digits, which
% is constructed by renamings and restrictions on the booleans

LET BIT :=

EXPORT
  SORT Bit
FROM

RENAME
  SORT Bool TO Bit,
  FUNC true : -> Bool TO 1,
  FUNC false : -> Bool TO 0
IN

BOOL_SPEC;




%
% Name : ABP_SYSTEM_SPEC
% Date : 14/11/88
%
% Description :
%
% Here the total system is created by instantiating the parameterized
% specifications with bits as data items and linking them together by
% defining communications between the subsystems.
%

LET ABP_SYSTEM_SPEC :=

EXPORT
  PROCESS ABP_SYSTEM :
FROM

IMPORT APPLY ABP_SPEC TO BIT INTO
IMPORT APPLY DRAIN_SPEC TO BIT INTO
IMPORT APPLY RANDOM_SPEC TO BIT INTO

CLASS
  ACTION item_read : Item
  ACTION item_sent : Item
```

```
COMM FORALL d:Item (
  output(d)     | read_item(d)   = item_read(d);
  send_item(d)  | input(d)       = item_sent(d) )

SET  H
  IND FORALL d:Item (
    H(output(d));
    H(input(d));
    H(read_item(d));
    H(send_item(d)) )

  PROCESS ABP_SYSTEM :
  DEF ENCAPS(H, RANDOM || ABP || DRAIN)

END;

ABP_SYSTEM_SPEC
```

6 Extensions

A number of possible extensions of PSF/C come to mind, most of them concerning the addition of extra process composition operators. We mention a few of them.

Instead of having only two simple renaming operators, viz. encapsulation (that renames a set of atomic actions into δ, leaving other actions fixed) and pre-abstraction (renaming into t), we can allow general *renaming operators*, having an operator ρ_f for each function f from A into the set Action. For more details, see BAETEN & BERGSTRA [BB88]. In this paper, also generalized renaming operators can be found, most notably the *state operator*, with which we can keep track of the state of a process during execution. This operator finds applications in the translation of programming languages or specification languages into process algebra.

Another issue is the addition of the silent step τ. This process is necessary for system verification. On the other hand, addition of a silent leads to complicated issues, one of which is the exact formulation of axioms. The concrete language ACP has remained fixed over a number of years, so is fairly well-established, and moreover is amenable to term rewriting analysis. We do have empty steps in this paper, but the empty step can be removed from the language if required.

There are several other operators that can be added to PSF/C and will ease specifications. We can think of the *mode transfer operator*, the *priority operator*, determination of *alphabets*, *process creation* operator, etc.

The semantics of PSF/C can also be given in a different way than was presented here. Notably, it is possible to give an operational semantics with Plotkin-style rules, by defining a COLD predicate *arrow* on \Process # \Action # \Process, with all rule definitions translated into COLD axioms.

7 Comparison of PSF/C with similar languages

The most obvious candidate for comparison is PSF/ASF as it was described in [MV88]. The difference is that the data type specifications are now given in the way of COLD. Moreover the concrete syntax of the process declarations is formatted in the style of COLD. (In the case of PSF/ASF the process declarations were formatted in the style of ASF.) Because we wanted to use the data type specifications from COLD only the static fragment of it has been imported into PSF/C. It is an open question for us how the dynamic part of COLD could be combined with ACP. There seems to be an inherent overlap between the procedures in COLD and the processes of ACP. Due to this overlap an orthogonal language design based on a combination of COLD and ACP seems difficult to obtain.

The reason to consider a combination of ACP with COLD rather than with ASF is threefold:

(i) It is easier to base process declarations on data types specifed with first order formulae than on types that are algebraically specified using initial algebra semantics. Indeed for the precise definition of guardedness for systems of recursion equations negative information (i.e. information about expressions denoting different data) is essential. COLD allows the use of full first order specifications. The induction scheme of COLD also allows the restriction of data algebras to so-called minimal (term generated) algebras. So the expressive power exceeds that of ASF for all practical purposes. Of course there is a price to be paid: automatic specification and implementation of COLD specifications is not an easy matter. It is essentially harder than for the algebraic specifications of ASF

(ii) The major strong point of COLD is its modularisation mechanism. The power of that mechanism is already fully present in the static part. We observed that by simply adopting COLD for data type declaration, and using the same modularisation mechanisms also in the presence of process declarations one obtains a language for which a semantics can be defined in just the same way as for COLD. Indeed the meaning of PSF/C constructs is found by translating these into theories in the infinitary many sorted partial logic (as it was done in [FJKR 87]). For notational reasons this translation is found via an intermediate translation of PSF/C into COLD. We feel that the semantics of modular constructs is better understood this way than in the case of PSF/C. Its should be noted, however, that this mechanism can in principle be used to obtain a semantic description of PSF/ASF as well. That would require a meticulous and unpleasant translation of ASF into COLD however.

(iii) We are interested in the relation (and possible combinations) of COLD and ACP. It seems to be the obvious point of departure to begin with a language definition that combines COLD and ACP in the same way as LOTOS combines Act-one and CCS.

In MORELL MEERFORDT [Mor88], a syntactic combination of CSP and Meta IV, the specification language is proposed and illustrated by examples. The main point is that processes can be parameterized by data structures. A systematic translation into Ada exists for this formalism.

(Differences with PSF/C: (i) bias towards CSP instead of bias towards ACP, (ii) there seems to have been paid be less attention to modularisation, and of course (iii) COLD syntax is replaced by Meta IV. The difference between these formats is minimal for flat specifications (i.e. specifications without explicit modular structure).

No particular semantic model is selected to describe the semantics of the CSP/Meta IV combination. Probably the authors have transition systems in mind.

In ASTESIANO, MASCARI, REGGIO & WIRSING [AMRW85], the formalism SMOLCS for specifying concurrent systems. Differences with PSF/C are the following: (i) SMOLCS is biased towards CCS rather than to ACP, the semantics is presented in terms of transition systems (ii) although SMOLCS uses an algebraic formalism for data type specification (as does PSF/ASF from [MV88]) the semantic intuition is quite different because SMOLCS inherits the orientation towards hierarchical specifications that was proposed by the Munich School.

Although not apparent from the syntax one might say that SMOLCS is closer to LOTOS than to PSF/C.

FOREST is a specification language that has been developed at the Imperial College in London by a team around Tom Maibaum, see GOLDSACK [G88]. The language uses deontic logic to express (potential) system behaviour. The behaviour of agents is formalized in terms of modal action logic. The data are described in terms of a first order language based on the declaration of structured signatures. The semantics of the agents is given in the context of trace theory. The formalism FOREST provides a combination of data type specifications and process (agent) specifications just as PSF/C does. The main difference is that FOREST uses a process logic, whereas PSF/C uses a process algebra. The data type specifications of FOREST seem in fact to be comparable with the possibilities of static COLD as it is used in PSF/C .

8 CONCLUSION

In the construction of the language PSF/C, the design objectives stated in the introduction have been met. A few additional remarks:

- we found that the translation of the process constructions to COLD is cumbersome, and it is our preliminary conclusion that the resulting insights do not justify the effort. An alternative would be to develop a semantics by using structured operational semantics;
- the SDF system suffices to generate simple tools for the language;
- we obtained a COLD oriented language in which certain comparative advantages of COLD over ASF are preserved. Thus, PSF/C has greater expressive power than PSF/ASF, and a more flexible semantic theory;
- the hiding mechanism of COLD (not exporting elements of a signature) is not yet satisfactorily integrated with the process part.

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