

# Magnetic anisotropy of single Mn acceptors in GaAs in an external magnetic field

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**Magnetic anisotropy of single Mn acceptors in GaAs in an external magnetic field**M. Bozkurt,<sup>1,\*</sup> M. R. Mahani,<sup>2</sup> P. Studer,<sup>3,4</sup> J.-M. Tang,<sup>5</sup> S. R. Schofield,<sup>3,6</sup> N. J. Curson,<sup>3,4</sup> M. E. Flatté,<sup>7</sup> A. Yu. Silov,<sup>1</sup> C. F. Hirjibehedin,<sup>3,6,8</sup> C. M. Canali,<sup>2</sup> and P. M. Koenraad<sup>1</sup><sup>1</sup>*Photonics and Semiconductor Nanophysics, Department of Applied Physics, Eindhoven University of Technology, P.O. Box 513, NL-5600 MB Eindhoven, The Netherlands*<sup>2</sup>*School of Computer Science, Physics and Mathematics, Linnaeus University, 391 82 Kalmar, Sweden*<sup>3</sup>*London Centre for Nanotechnology, University College London (UCL), London, WC1H 0AH, United Kingdom*<sup>4</sup>*Department of Electronic and Electrical Engineering, UCL, London, WC1E 7JE, United Kingdom*<sup>5</sup>*Department of Physics, University of New Hampshire, Durham, New Hampshire 03824-3520, USA*<sup>6</sup>*Department of Physics and Astronomy, UCL, London, WC1E 6BT, United Kingdom*<sup>7</sup>*Department of Physics and Astronomy, University of Iowa, Iowa City, Iowa 52242-1479, USA*<sup>8</sup>*Department of Chemistry, UCL, London, WC1H 0AJ, United Kingdom*

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We investigate the effect of an external magnetic field on the physical properties of the acceptor hole states associated with single Mn acceptors placed near the (110) surface of GaAs. Cross-sectional scanning tunneling microscopy images of the acceptor local density of states (LDOS) show that the strongly anisotropic hole wave function is not significantly affected by a magnetic field up to 6 T. These experimental results are supported by theoretical calculations based on a tight-binding model of Mn acceptors in GaAs. For Mn acceptors on the (110) surface and the subsurfaces immediately underneath, we find that an applied magnetic field modifies significantly the magnetic anisotropy landscape. However, the acceptor hole wave function is strongly localized around the Mn and the LDOS is quite independent of the direction of the Mn magnetic moment. On the other hand, for Mn acceptors placed on deeper layers below the surface, the acceptor hole wave function is more delocalized and the corresponding LDOS is much more sensitive on the direction of the Mn magnetic moment. However, the magnetic anisotropy energy for these magnetic impurities is large (up to 15 meV), and a magnetic field of 10 T can hardly change the landscape and rotate the direction of the Mn magnetic moment away from its easy axis. We predict that substantially larger magnetic fields are required to observe a significant field dependence of the tunneling current for impurities located several layers below the GaAs surface.

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**I. INTRODUCTION**

Magnetic semiconductors have attracted strong attention in the last decade because of their potential to combine optoelectronic and magnetic properties in spintronic devices. The most commonly investigated material as a magnetic semiconductor is GaAs doped with transition metal Mn impurities. Mn acts as an acceptor in GaAs and its magnetic properties are mainly determined by the magnetic moment of the half-filled  $d$  shell.<sup>1</sup> In highly Mn doped GaAs, the observed ferromagnetism in GaMnAs has been shown to be hole mediated,<sup>2,3</sup> as a result of exchange coupling between the  $p$ -like acceptor holes residing in the valence band and the electrons in the  $d$  shell, which we will refer to as the Mn core from now on. On the other hand, for applications in spintronic devices, it is important to investigate methods to read, set and manipulate the magnetic orientation of the Mn core, especially at the level of a single Mn impurity. Spectacular results have been achieved with optical polarization and manipulation of low Mn doped GaAs/AlGaAs quantum wells<sup>4</sup> and single Mn doped quantum dots.<sup>5,6</sup> Other important work in the field of single spin reading and manipulation has been done for single nitrogen-vacancy centers in diamond.<sup>7</sup>

In this paper, we investigate low-concentration Mn-doped GaAs. Because Mn has strongly coupled magnetic and electric properties, spin manipulation by electric fields has been suggested as a possibility in addition to manipulation by magnetic and optical fields. Cross-sectional scanning

tunneling microscopy (X-STM) has been used in the past to study the Mn acceptor wave function at the atomic scale and to manipulate its charge state. The experimental study of the Mn acceptor wave function by X-STM showed a strongly anisotropic shape of the acceptor wave function<sup>8</sup> as was predicted by tight-binding calculations.<sup>9</sup> These experimental and theoretical results proved that the observed anisotropy of the acceptor wave function is due to the cubic symmetry of the GaAs crystal. Additional studies showed that the anisotropy of the Mn acceptor wave function is also influenced by (local) strain due to a nearby InAs quantum dot<sup>10</sup> or the relaxation of the surface.<sup>11</sup>

These results indicate that STM can also be an excellent tool to investigate the effects of the orientation of the magnetic moment of the Mn core on the acceptor wave function. In fact, theoretical work<sup>12,13</sup> has predicted that the local density of states (LDOS) of the acceptor-hole wave function can depend strongly on the direction of the Mn moment. Since the LDOS is directly related to the tunneling current, these predictions suggest that it might be possible to control the STM electric current by manipulating the individual Mn core spin, for example, with an external magnetic field. An X-STM and X-STs study of the energetic level of Mn close to the GaAs [110] cleavage surface has already shown that the threefold degeneracy of the  $J = 1$  ground level is split because of the reduced symmetry.<sup>14</sup> Magnetic-field manipulation and control of atomic spins is presently undergoing fast progress, showing

great promise to selectively address individual atoms.<sup>15</sup> Control of atomic spin, combined with the aforementioned sensitivity of the STM current on the dopant magnetic moment direction, could be a crucial step in realizing multifunctional spin-electronic devices based on individual atoms. Apart from addressing electrical properties of single magnetic dopants, STM has been shown to be also well capable of positioning individual dopants within a semiconductor surface.<sup>16,17</sup>

In this paper, we will use STM to explore the effect of an external magnetic field on the magnetic orientation of the magnetic moment of a single Mn impurity in dilute Mn doped GaAs and compare the results with tight-binding model calculations. In Sec. II, we present a review of the theoretical work that has been published in Refs. 12 and 13. These calculations are based on a tight-binding model and show that a change in the spin orientation of the Mn core can sometimes give rise to a detectable change in LDOS of the Mn acceptor wave function. In Sec. III, we present experimental results of STM measurements on single Mn impurities in GaAs in a magnetic field. We will show that the LDOS of the Mn acceptor wave function is not significantly modified by magnetic fields up to 6 T. In Secs. IV and V, we present theoretical results of tight-binding modeling of Mn in GaAs where a magnetic field has been explicitly included in the Hamiltonian. These calculations use a classical approximation for the Mn core spin, and then consider the response of the bound hole fully quantum mechanically; the classical approximation for the Mn core spin biases the hole wave functions towards more polarized quantum numbers, and thus may overestimate the calculated magnetic anisotropy. Nevertheless, these calculations support our experimental observations and show that a dependence of LDOS on external magnetic is, in fact, expected only for Mn acceptors placed several layers below the GaAs (110) and can be detected only with stronger magnetic fields than the ones presently available.

## II. REVIEW

Tang *et al.*<sup>12</sup> and Strandberg *et al.*<sup>13</sup> have reported results of calculations of the dependence the Mn acceptor hole wave function on the orientations of the Mn magnetic moment. The paper by Tang *et al.*<sup>12</sup> describes the Mn LDOS in bulk GaAs with an  $sp^3$  tight-binding model in which the Mn core spin is taken in calculation by a spin dependent term in the potential at the four nearest-neighbor sites in a zinc-blende crystal. It is found that the energy spectrum of the Mn is independent of the Mn core spin orientation. However, the LDOS of the Mn is found to be depending on the Mn spin orientation. A qualitative description of this dependence is given in terms of spin-orbit coupling between the spin of the Mn core and the orbital character of the Mn acceptor hole. In absence of spin-orbit interaction, the LDOS of the Mn acceptor state would have the same  $T_d$  symmetry as the surrounding zinc-blende crystal. However, the spin-orbit coupling is taken into account and the symmetry of the Mn acceptor wave function is reduced. The contour surface of the acceptor LDOS for various Mn core spin directions show that in general, the LDOS has an oblate shape with the short axis aligned with the Mn core spin axis. For a quantitative comparison with X-STM experiments, cross sectional views of the LDOS are calculated in the (110)

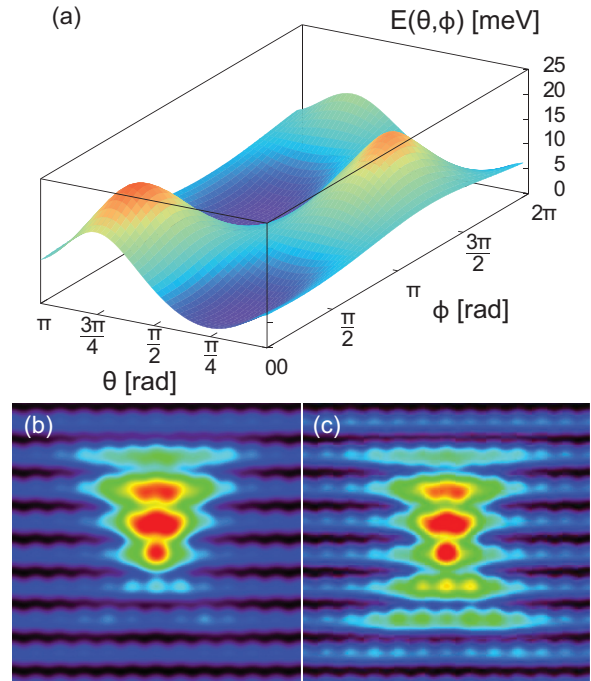


FIG. 1. (Color online) (a) Magnetic anisotropy energy (MAE) of a Mn acceptor according to a tight-binding calculation for strained bulk material. The energy level difference between the easy and the hard axes is about 23 meV, based on a uniform strain estimated in Ref. 11. The angles  $\theta$  and  $\phi$  have the same definition as in Fig. 5. (b) Mn LDOS at five atomic layers from the Mn position when the core spin is oriented along the (b) easy or (c) hard axis.

plane. The largest variation in the cross sectional images of the LDOS is seen when the Mn core spin direction changes from [001] or  $[1\bar{1}0]$  to  $[110]$ . A variation in LDOS of up to 90% is predicted by these tight-binding calculations when the Mn core spin switches from parallel to perpendicular to the (110) surface. There is also a small difference of 15% in the LDOS when the Mn core spin is aligned in the two directions parallel to the (110) plane. When the spin of Mn core can be changed with an external magnetic field and possibly with ESR techniques,<sup>15,18</sup> the differences in the LDOS are expected to be visible in an X-STM experiment.

This model gives a good description of Mn in bulk GaAs but the effect of the cleavage surface is completely neglected. In fact, it has been shown experimentally<sup>11</sup> that the wave function of a Mn near the (110) cleavage surface can be strongly affected by the strain from the surface relaxation. In the same paper, bulk tight-binding calculations support the observation of a broken symmetry near the surface. The surface is taken into account by applying a uniform strain to the bulk model by shifting the Ga lattice with respect to the As lattice. The calculation results presented in that paper are the average of different Mn core spin orientations. In Fig. 1, the same results are presented but for individual Mn core spin orientations. Figure 1 was unpublished in this form. A clear difference in LDOS can be observed when the Mn core spin changes its orientation from the hard to the easy axis.

In the paper by Strandberg *et al.*,<sup>13</sup> the reconstructed surface is taken into account for the calculation of the LDOS dependence of the Mn acceptor state on the Mn core

spin orientation using a tight-binding model, which includes the exchange interaction, spin-orbit coupling, and Coulomb interaction. This makes a direct comparison with X-STM experiments more justified, and the results, indeed, show the same experimentally observed breaking of the symmetry of the wave function due to the near presence of the surface. In Ref. 13, Mn acceptors in bulk GaAs (neglecting the surface) have also been considered. For Mn in bulk GaAs, the energy level of the Mn state calculated for different orientations of the Mn core spin shows a small magnetic anisotropy, in contrast to the results of Ref. 12, where no magnetic anisotropy was found for Mn in bulk. The easy axis in Ref. 13 for the Mn core spin is oriented along the [001] direction whereas the hard axis is found to be lying in the (001) plane. The energy barrier between the hard and the easy axes is found to be 4.35 meV, which is very small in comparison with the Mn binding energy in GaAs (113 meV). At first, the presence of a magnetic anisotropy is surprising since there is no difference between the [001] and [010] or [100] directions in a zinc-blende crystal. The observed anisotropy can be explained by the use of periodic boundary conditions on finite clusters used in this paper.<sup>13</sup> The influence of other Mn atoms in the area may indeed introduce a small magnetic anisotropy and thus the observed magnetic anisotropy of Mn in bulk GaAs is artificial. Indeed, more recent calculations carried out on much larger clusters show that the bulk magnetic anisotropy decreases monotonically with cluster size, down to a fraction of a meV for the largest clusters of 40 000 atoms.<sup>19</sup>

On the other hand, the calculation of the LDOS for Mn in bulk GaAs in Ref. 13 shows good similarity with the calculations in Ref. 12. The LDOS is found to be spreading in the direction perpendicular to the Mn core spin axis. The change in the shape of the LDOS is explained in terms of the  $p_x$ ,  $p_y$ , and  $p_z$  character of the Mn acceptor hole. For different orientations of the Mn core spin, different components in the character dominate. When the Mn core spin direction is changed from  $[1\bar{1}0]$  to  $[110]$  a drop in LDOS of 74% is observed at four atomic layers from the Mn position. This drop in LDOS is 25% when the core spin direction changes from  $[1\bar{1}0]$  to  $[001]$ , which is again in good agreement with the other calculations in Ref. 12.

In Ref. 13, similar calculations have been done for Mn in or below the GaAs (110) surface layer. For Mn at the surface and the first subsurface layer, a strong localization of the LDOS is observed and a magnetic easy axis in the  $[111]$  direction is found. The difference in LDOS for different Mn core spin orientations is negligible. Thus in an X-STM experiment, we expect to see no effect of the magnetic field on the Mn atoms very close to the surface.

For Mn atoms deeper below the (110) surface, the LDOS becomes more extended and the magnetic anisotropy shows a complex behavior for subsequent depths. However, from the fourth layer beneath the (110) surface and deeper, one can recognize the emergence of an easy plane with its normal in the  $[1\bar{1}0]$  direction. The anisotropy energy is found to be at least 15 meV. Images of the (110) surface LDOS show that there is an increasing difference in LDOS for an increasing depth when the Mn core spin changes from the easy to the hard axis. For Mn atoms placed on fourth subsurface layers and deeper, the difference in LDOS varies between 40% and 82%.

In summary, both Refs. 12 and 13 have treated the behavior of the Mn acceptor hole LDOS in the (110) plane for different Mn core spin orientations. In both papers, it is found that when the Mn core spin direction is changed from  $[1\bar{1}0]$  to  $[110]$ , a drastic change in the LDOS is taking place. The inclusion of the cleavage surface relaxation has resulted in similar observations.

The mechanism for the magnetic anisotropy in Refs. 12 and 13 is the same—the presence of the surface, or strain, lowers the energy of an orbital wave function with quantization axis along a specific direction, and the spin-orbit interaction (which correlates the spin axis with the orbital axis) causes that preferred orbital direction to select a preferred spin axis. The effective energy associated with the correlation between spin and orbital axes is of the same order as the binding energy (Refs. 9, 12 and 13 found it to be  $\sim 40$  meV). At magnetic fields required to overcome the magnetic anisotropy energy, the magnetic length is of order 3 nm, which is three times larger than the effective Bohr radius of the acceptor ( $\sim 1$  nm). Therefore the overall distortion of the acceptor state wave function due to the direct effect of the magnetic field on the orbital wave function is small compared with the spin-orbit term. What is not certain, however, is whether the effect of the magnetic field on the acceptor state wave function can substantially change the magnetic anisotropy; this will be examined in Sec. V.

In an X-STM experiment, one can also check the results of these calculations by applying a magnetic field perpendicular and parallel to the (110) cleavage plane and by measuring the Mn contrast, which can change with a factor as high as 90%. In the next section, we discuss the X-STM experiments that have been performed to observe the predicted effects.

### III. EXPERIMENTS

A Mn doped layer 500 nm thick was grown on a  $p$ -type GaAs substrate at high temperature with Mn concentrations of about  $3 \times 10^{19} \text{ cm}^{-3}$ . The experiments are performed with an Omicron Cryogenic STM operating at a base temperature of 2.5 K. A magnetic field vector can be applied with fields of up to 6 T in the  $z$  direction only or maximum 2 T in the  $z$  direction together with maximum 1 T in the  $x$  and  $y$  directions. The  $x$ ,  $y$ , and  $z$  directions are indicated in Fig. 2(a) where two Mn atoms at different depths below the cleaved surface are visible. The magnetic field is indicated in the vector notation in units of tesla:  $\vec{B} = (B_x, B_y, B_z)$ .

From Ref. 11, we estimate that Mn A is approximately eight atomic layers below the cleavage surface and that Mn B is at about five atomic layers below the cleavage surface. In Ref. 13, a change in contrast of 40% is predicted for a Mn A at eight layers below the cleavage surface when the Mn core spin changes from the  $[110]$  direction to the  $[1\bar{1}0]$  direction. For Mn B at five atomic layers beneath the cleavage surface, a change of 60% is predicted when the Mn core spin direction changes from the  $[110]$  direction to the  $[1\bar{1}0]$  direction. As can be seen from the comparison of Figs. 2(a) and 2(b), there is no change at all in the Mn contrast for both Mn atoms when the magnetic field is changed from 1 T in the  $y$  direction to  $-6$  T in the  $z$  direction. In Fig. 3, a more quantitative comparison is made by looking at the contrast of the Mn atoms in different

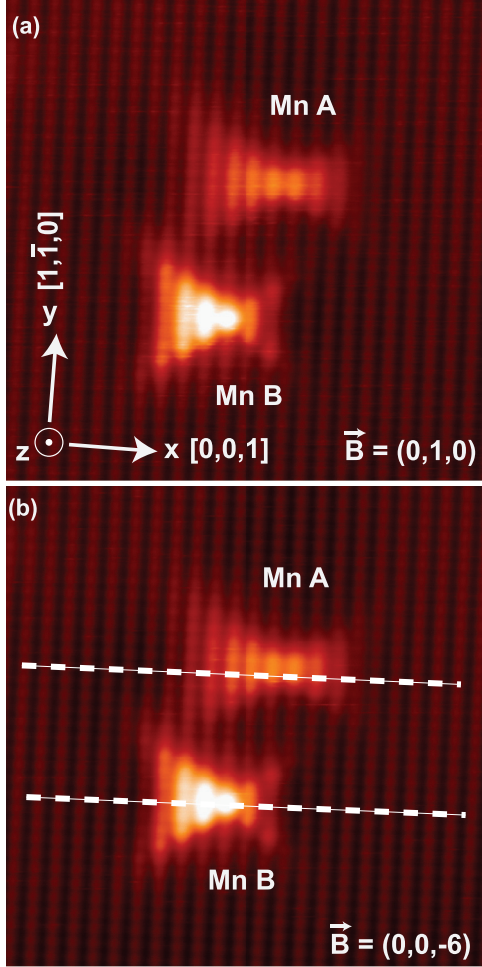


FIG. 2. (Color online)  $13 \times 13$ -nm<sup>2</sup> X-STM images of two Mn atoms at different depths below the (110) cleavage plane. The  $x$  direction corresponds with the crystallographic [001] direction and the  $y$  direction corresponds with the [1 $\bar{1}$ 0] direction. The images are taken at +1.4 V and 50 pA at a temperature of about 2.5 K. In (a), a magnetic field of 1 T is oriented in the [1 $\bar{1}$ 0]  $y$  direction and in (b), a magnetic field of -6 T is oriented in the [110]  $z$  direction.

magnetic fields through the dashed lines in Fig. 2(b). Also in these plots, it can be seen that for both Mn atoms, there is no difference at all in the contrast for different orientations of the magnetic field.

For Mn B, the plots for  $B = (0, 1, 0)$  and  $B = (0, 0, -6)$  are slightly different from the rest because of a small tip modification that has taken place. The tip has become slightly less sharp in the scan direction (the [001]  $x$  direction) and this difference is noticed when sharper objects like Mn B are imaged. Mn A has FWHM of about 4.5 nm in the scan direction, while Mn B has a sharper feature with a FWHM of about 2.0 nm. The different FWHM of the Mn features has been related to the depth below the GaAs surface.<sup>11</sup>

#### IV. THEORETICAL MODEL

We model theoretically substitutional Mn impurities in GaAs following the procedure put forward in Ref. 13. Our second-quantized tight-binding Hamiltonian for (Ga,Mn)As

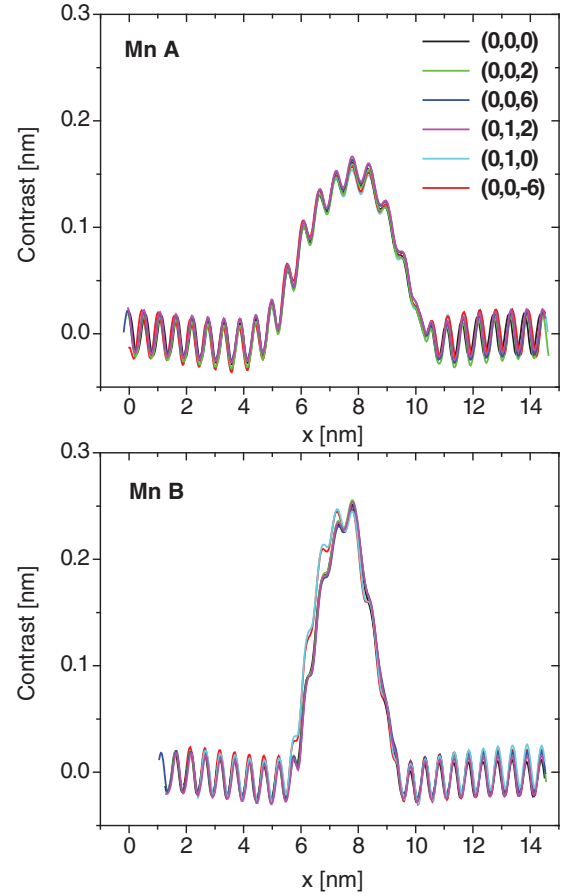


FIG. 3. (Color online) (a) Contrast of Mn A along the [001] direction indicated with a dashed line in Fig. 2(b). (b) Same plot for Mn B. Mn A has FWHM of about 4.5 nm and Mn B has a FWHM of about 2.0 nm.

takes the following form:

$$\begin{aligned}
H = & \sum_{ij, \mu\mu', \sigma} t_{\mu\mu'}^{ij} a_{i\mu\sigma}^\dagger a_{j\mu'\sigma} + J_{pd} \sum_m \sum_{n[m]} \vec{S}_n \cdot \hat{\Omega}_m \\
& + \sum_{i, \mu\mu', \sigma\sigma'} \lambda_i \langle \mu, \sigma | \vec{L} \cdot \vec{S} | \mu', \sigma' \rangle a_{i\mu\sigma}^\dagger a_{i\mu'\sigma'} \\
& + \frac{e^2}{4\pi\epsilon_0\epsilon_r} \sum_m \sum_{i\mu\sigma} \frac{a_{i\mu\sigma}^\dagger a_{i\mu\sigma}}{|\vec{r}_i - \vec{R}_m|} + V_{\text{Corr}}, \quad (1)
\end{aligned}$$

where  $i$  and  $j$  are atomic indices that run over all atoms,  $m$  runs over the Mn, and  $n[m]$  over the nearest neighbors of Mn atom  $m$ .  $\mu$  and  $\nu$  are orbital indices and  $\sigma$  is a spin index. The first term in Eq. (1) contains the near-neighbor Slater-Koster tight-binding parameters<sup>20,21</sup> that reproduce the band structure of bulk GaAs<sup>22</sup> and that are rescaled<sup>13,23,24</sup> when needed to account for the buckling of the (110) surface. The second term implements the antiferromagnetic exchange coupling between the Mn core spin (treated as a classical vector with unit vector  $\hat{\Omega}_m$ ) and the nearest-neighbor As  $p$  spins  $\vec{S}_n = 1/2 \sum_{\pi\sigma\sigma'} a_{n\pi\sigma}^\dagger \vec{\tau}_{\sigma\sigma'} a_{n\pi\sigma'}$ .

The exchange coupling  $J_{pd}$  can be inferred from theory<sup>25</sup> and experiment,<sup>26</sup> as done in Ref. 13. Reference 25 considers a Hubbard model approach that treats perturbatively the hybridization between Mn  $d$  orbitals and As  $p$  orbitals,

accounting realistically for its nonlocality. The hybridization leads to an effective exchange interaction between the spin of the acceptor hole and the impurity spin, which in the limit  $k \rightarrow 0$  is described by a single parameter  $J_{pd}$ . For reasonable values of the Hubbard model parameters, Ref. 25 finds  $J_{pd} \approx 50 \text{ meV nm}^3$ . As pointed out in Ref. 25, this value is close but somewhat smaller than value inferred from experiment.<sup>26</sup> In order to use this parameter in the expression of the exchange interaction of Eq. (1), this value has to be divided by  $4 \times V_{\text{cell}}$ , and multiplied by  $S = 5/2$ , where  $V_{\text{cell}} = a^3/8$  is the volume of the unit cell. We finally find<sup>13</sup>  $J_{pd} \approx 1.5 \text{ eV}$ , which is the value that we will use when using Eq. (1) in this paper. As a result of this term, the acceptor hole that is weakly bound to the Mn will become spin polarized. This model contains only  $s$  and  $p$  orbitals, and the effect of the Mn  $3d^5$  electrons is encoded in the exchange term.

Next, we include an on-site spin-orbit one-body term, where the renormalized spin-orbit splittings are taken from Ref. 22. Spin-orbit coupling will cause the total energy to depend on the Mn spin direction, defined by a collinear variation of  $\hat{\Omega}_m$ .

The fourth term is a long-range repulsive Coulomb part that is dielectrically screened by the host material. To account in a simple way for weaker dielectric screening at the surface, the dielectric constant  $\epsilon_r$  for a Mn on the surface is reduced from the bulk GaAs value 12 to 6 for the affected surface atoms.

This crude choice is qualitatively supported by experimental results.<sup>17,27</sup>

The last term  $V_{\text{corr}}$  is a one-particle correction potential for the Mn central cell. This term is the least known and understood theoretically. It consists of on- and off-site parts,  $V_{\text{corr}} = V_{\text{on}} + V_{\text{off}}$ , which influence the Mn ion and its As nearest neighbors, respectively. The on-site Coulomb correction is estimated to be 1.0 eV from the ionization energy of Mn. The off-site Coulomb correction affects all the nearest-neighbor As atoms surrounding the Mn ion and together with the exchange interaction, it reflects primarily the  $p$ - $d$  hybridization physics and is the parameter that in the model primarily controls the binding energy of the hole acceptor state. The off-site Coulomb correction value is set by tuning the position of the Mn-induced acceptor level in the bulk to the experimentally observed position<sup>28–31</sup> at 113 meV above the first valence band level. The value thus obtained is  $V_{\text{off}} = 2.4 \text{ eV}$ . When the Mn impurity is on the GaAs surface, the value of  $V_{\text{off}}$  is reduced to ensure that the position of the acceptor level is consistent with the value attained via STM spectroscopy.

The off-site Coulomb correction is in fact a repulsive potential for the electrons. If we use the bulk value (2.4 eV) for the surface, the acceptor level lies deep in the gap at 1.3 eV above the valence band, which means the acceptor wave function is now much more localized around the Mn than its bulk counterpart. In order to guarantee the experimentally observed

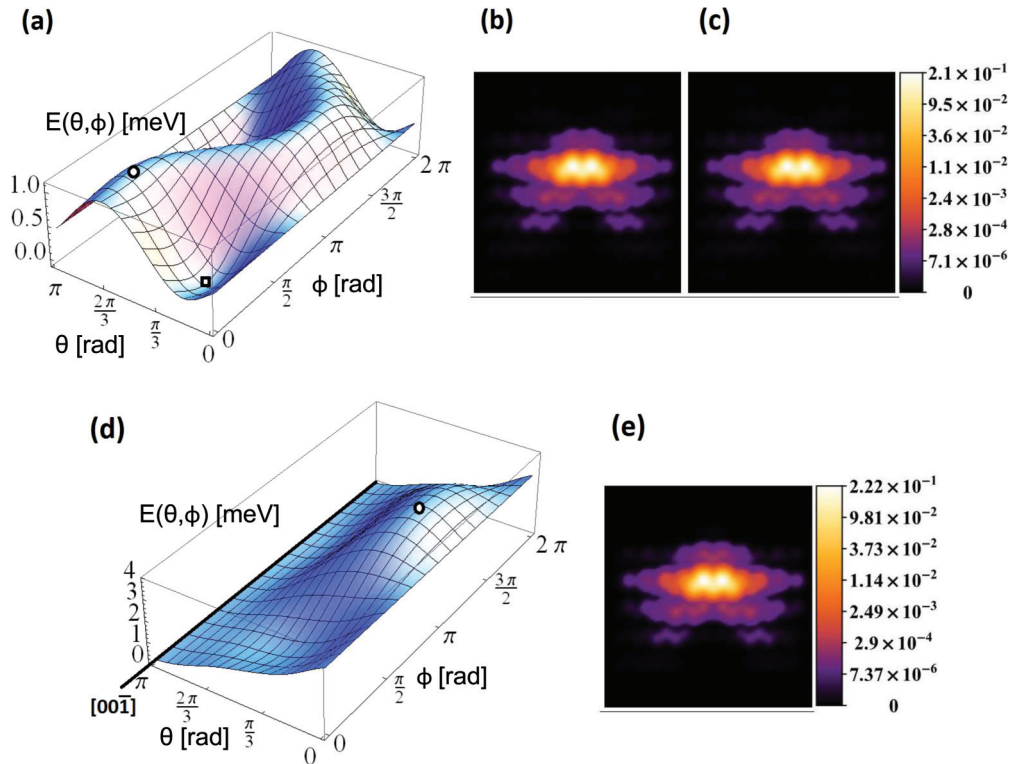


FIG. 4. (Color online) Magnetic anisotropy energy (MAE) landscape and the Mn-acceptor-level local density of states (LDOS) for one Mn at the [110] surface. (a) The MAE in the absence of an external magnetic field, as a function of the angles  $\theta$  and  $\phi$  defining the direction of the Mn spin  $\hat{\Omega}$ . The barrier (hard) direction is marked with a circle and the minimum energy (easy direction) with a square. (b) and (c) LDOS of the Mn acceptor level when the Mn magnetic moment points in the easy and hard direction respectively, as defined in panel (a). (d) The MAE in the presence of a 6-T external magnetic field applied along the hard direction ( $\theta = 3\pi/4, \phi = \pi/4$ ). (e) The LDOS in the presence of a 6-T magnetic field. Here, the Mn magnetic moment is along the easy direction determined by the landscape (d) modified by the presence of the external field. The barrier (hard) direction is marked with a circle and the minimum energy (easy direction) with a solid line.

position for the acceptor level, 0.85 eV,<sup>16</sup> we have to decrease this repulsive potential for the electrons, which causes the hole wave function to be less localized with a corresponding smaller binding energy. The value of  $V_{\text{corr}}$ , combined with  $J_{pd}$ , produces a potential on the nearest-neighbor As, which is within 20% of that used in the independent calculations of Refs. 8–12 to fit the Mn acceptor level energy.

The electronic structure of GaAs with a single substitutional Mn atom is obtained by performing a supercell type calculation with a cubic cluster of a few thousands atoms and periodic boundary conditions in either two or three dimensions, depending on whether we are studying the (110) surface or a bulklike system. The (110) surface of GaAs is simplified from both theoretical and experimental points of view, by the absence of large surface reconstruction. In order to remove artificial dangling-bond states that would otherwise appear in the band gap, we include relaxation of surface layer positions following a procedure introduced in Refs. 23 and 24. For more details, the reader is referred to Ref. 13.

The treatment of the Mn core spin as a classical vector is an approximation that would not correctly describe optical transition selection rules or electron paramagnetic resonance measurements of dilute Mn acceptors in GaAs, and hence was not used in Refs. 4–6 and 18. Although the calculations here do consider the fully quantum mechanical response of the heavy and light holes to the presence of this classical vector, a full quantum mechanical treatment including the quantum character of the Mn core spin would also allow the core spin to mix with the heavy- and light-hole states to comprise the ground state. For the classical Mn core spin oriented along an axis, only the bound hole wave function with total angular momentum projection  $-3/2$  (summed from the envelope and Bloch functions) along the core spin would be included. For the fully quantum treatment of the core spin, bound hole wave functions with total angular momentum projection of  $3/2$ ,  $1/2$ , and  $-1/2$  would also be present in the ground state.<sup>18</sup> As the magnetic anisotropy we find here is governed by the response

of the bound hole to the local environment, the contribution of other hole quantum numbers is likely to reduce the magnetic anisotropy from the value we find here. Nevertheless, for a quantization axis  $\hat{z}$ , half<sup>18</sup> of the composition of the quantum mechanical  $J = 1$ ,  $J_z = 1$  state comes from the core spin  $5/2$  along  $\hat{z}$ , and the bound hole spin  $3/2$  along  $-\hat{z}$  (which is well described by our calculations). Therefore the effects described here may be expected to be qualitatively accurate.

We would like to emphasize that the strength of the off-site Coulomb correction is the only important fitting parameter of the model, and its value is fixed once for all by the procedure described above. All the other parameters in Eq. (1) are either determined by theoretical considerations, or for the cases when this is not possible (e.g., short-range onsite potential) their values are extracted from experiment. In any case, they affect weakly the properties of the acceptor level. Once the parameters of the Hamiltonian of Eq. (1) are chosen in the way indicated above, the model has to be viewed as a microscopic description, with predictive power, of the properties of Mn impurities in GaAs surfaces and subsurfaces. In this sense, the model of Ref. 13 has been quite successful in capturing some of the salient features of the STM experiments,<sup>14,32</sup> probing the Mn-dopant acceptor hole near the GaAs (110) surface. For example, it correctly describes the dependence of the acceptor binding energy<sup>14</sup> and the shape of the hole wave function<sup>32</sup> on the layer depth below the surface on which the magnetic dopant is positioned. The model also makes a prediction on how the magnetic anisotropy barrier for the Mn-impurity-hole magnetic complex changes as a function of the layer depth. These predictions can be indirectly checked by the magnetic-field studies that are the main scope of the present paper.

In order to study the response of the system to an external magnetic field, we introduce the Zeeman term

$$H_z = -\frac{\mu_B}{\hbar} \sum_i \sum_{\mu\mu'\sigma\sigma'} \langle \mu\sigma | (\vec{L} + g_s \vec{S}) \cdot \vec{B} | \mu'\sigma' \rangle a_{i\mu\sigma}^\dagger a_{i\mu'\sigma'} - g_s \frac{\mu_B}{\hbar} \sum_m \hat{\Omega}_m \cdot \vec{B}, \quad (2)$$

where the first term runs over all  $s$  and  $p$  orbitals of all atoms, and the second term represents the coupling of the magnetic field with the magnetic moment of the Mn impurities, treated as a classical vector. Here,  $\mu_B = \frac{\hbar e}{2m} = 5.788 \times 10^{-2}$  meV T<sup>-1</sup> is the Bohr magneton,  $g_s = 2$ , and we follow the incorrect but common convention that spins and magnetic moments are parallel to each other.<sup>33</sup> Therefore, in the paper, we will loosely refer to the direction of  $\hat{\Omega}$  as the direction of the Mn magnetic moment.

## V. THEORETICAL RESULTS AND DISCUSSION

We start by analyzing the magnetic anisotropy properties for one Mn at the (110) GaAs surface layer and the immediate subsurface layers, and see how these are modified by the presence of an external magnetic field of a few tesla. The magnetic anisotropy landscape as a function of  $\hat{\Omega}$  for one Mn at the surface and the first nine subsurfaces has been studied in detail in Ref. 13. Typically the system has an uniaxial anisotropy with two minima separated by an energy barrier.

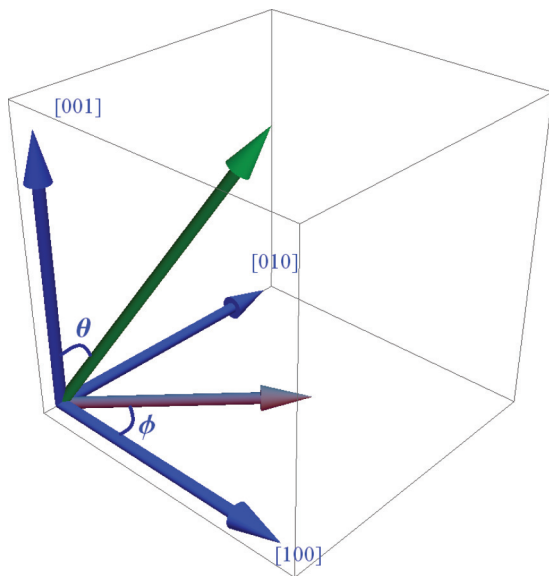


FIG. 5. (Color online) Direction of  $\theta$  and  $\phi$  with respect to the crystal axis.

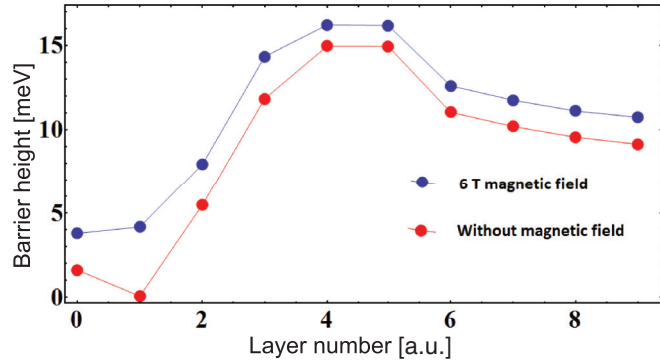


FIG. 6. (Color online) Maximum MAE barrier height as a function of the Mn depth. Red dots are the MAE barrier height in the absence of an external magnetic field, while blue dots represent the height in the presence of a 6-T external magnetic field.

We will refer to the  $\hat{\Omega}$  direction of minimum energy as the *easy* direction and the one of maximum energy as the *hard* direction.

We first consider the case of one Mn impurity at the (110) surface. To facilitate the comparison with the case in which a magnetic field is present, we recalculated and

plotted here anisotropy landscapes and LDOS in the absence of the magnetic field, originally published in Ref. 13, using an improved code.

In Fig. 4(a), we plot the anisotropy energy landscape in the absence of the magnetic field, as a function of the angles  $\theta$  and  $\phi$  defining the direction of  $\hat{\Omega}$ . The coordinate system used for this and the other plots in the paper has  $\theta = 0$  parallel to the [001] axis,  $(\theta = \pi/2, \phi = 0)$  parallel to [100], and  $(\theta = \pi/2, \phi = \pi/2)$  parallel to [010], see Fig. 5.

The anisotropy landscape displays two minima, identifying the easy direction [111], separated by an energy barrier of the order of 1 meV. Note that these tight-binding results of the magnetic anisotropy of a Mn at the (110) GaAs surface are consistent with recent first-principles estimates.<sup>34</sup> Figures 4(b) and 4(c) show the LDOS for the Mn acceptor state when the Mn spins point along the easy and hard directions, respectively, determined from the landscape in (a). As discussed in Sec. II and shown clearly in the figures, the acceptor state wave function for a Mn on the surface is very localized around the impurity, and the dependence of the LDOS on the Mn spin orientation is negligible. The acceptor wave function, itself strongly anisotropic, seems to be completely decoupled from the orientation of the Mn magnetic moment. Figures 4(d) and 4(e) show the effect of a

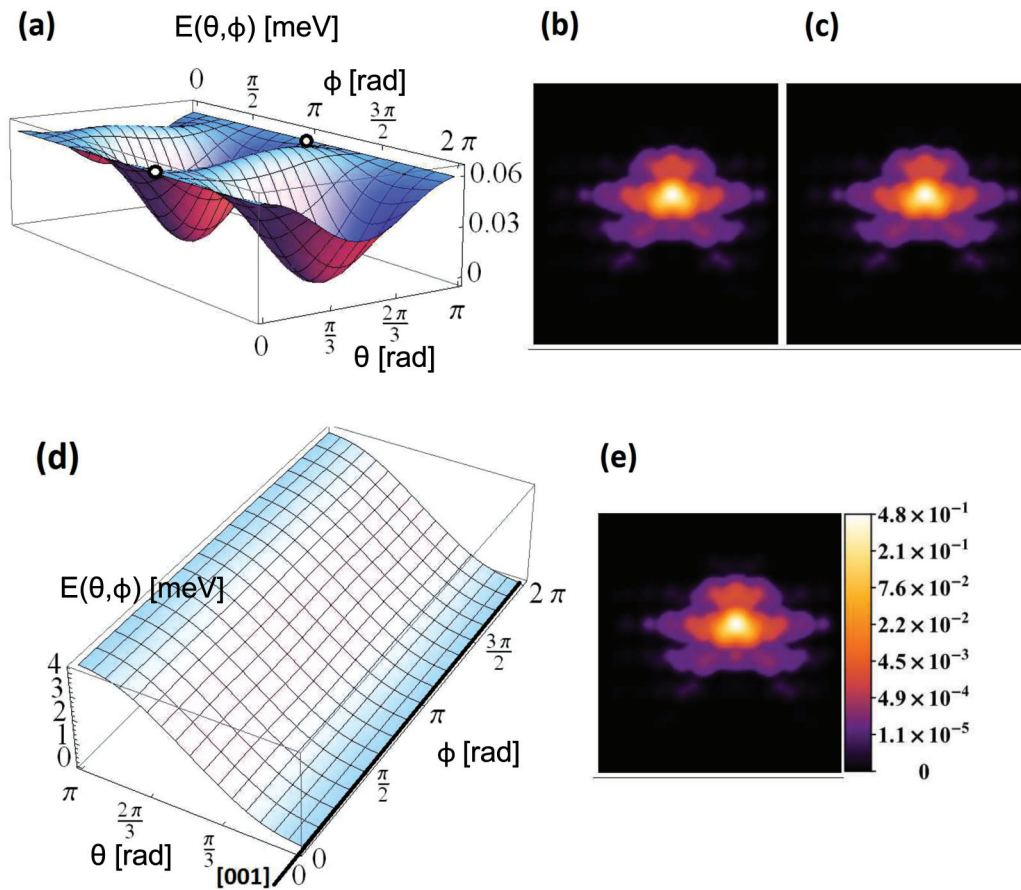


FIG. 7. (Color online) MAE landscape and the Mn-acceptor-level LDOS for one Mn in the first subsurface (i.e., one layer below the [110] surface). (a) MAE in the absence of an external magnetic field. The barriers (hard) directions are marked with a circle. (b) and (c) Mn acceptor LDOS for the case in which the Mn magnetic moment points in the easy and hard directions, respectively. (d) MAE in the presence of a 6-T external magnetic field pointing along the (original) hard direction ( $\theta = 0, \phi = \pi$ ). The minimum energy (easy direction) is shown with a solid line. (e) Mn acceptor LDOS in the presence of a 6-T magnetic field. Here, the Mn magnetic moment points in the new easy direction determined by the magnetic field, as shown in (d). The color scale in (b) and (c) is the same as in (e).



6-T magnetic field on the anisotropy and LDOS, respectively, when the field is applied in the hard direction of the anisotropy landscape in (a).

We can see that the magnetic field changes considerably the anisotropy landscape, which has now an easy axis at  $\theta = \pi$  (the direction of the field). Note that in the presence of the field the anisotropy barrier has increased up to 4 meV. The LDOS in Fig. 4(e) is now calculated for  $\hat{\Omega}$  pointing along the new easy axis, determined by the magnetic field. Despite the strong change in the anisotropy landscape brought about by the magnetic field, the acceptor LDOS is essentially identical to the one calculated in the absence of the field, in agreement with the experimental results.

Before continuing our LDOS analysis, it is useful to consider how the anisotropy-energy barrier depends on the Mn-impurity depth from the (110) surface. In Fig. 6, we plot the largest value of the anisotropy energy barrier as a function of the subsurface layer index (layer 0 is the (110) surface). In general, in the absence of a magnetic field (red dots in the picture) the anisotropy barrier increases with Mn depth, reaching a maximum of 15 meV for layers 4 and 5. It then starts to decrease and it should eventually reach a very small value corresponding to the case where the Mn is effectively in the bulk. For the finite clusters that we have considered here

(20 layers in the  $z$  direction), the anisotropy remains large also when the impurity is effectively in the middle of the cluster (corresponding to layer 9 from the surface). Bulk calculations on considerably larger clusters show that the anisotropy for impurities in the middle of the clusters does decrease to a fraction of one meV.<sup>19</sup> For these larger clusters, the magnetic anisotropy of the Mn positioned in on layers  $\geq 8$  is expected to decrease a bit with cluster size. However, the qualitative behavior of the first 7–8 layers shown in Fig. 6, and the corresponding numerical values of the magnetic anisotropy are controlled by the vicinity to the surface and as such should not depend strongly on cluster size.<sup>19</sup>

Layer 1 (the first subsurface layer) is a special case in the sense that the anisotropy is very small, on the order of 0.1 meV. The first subsurface represents the cross over from the case in which the Mn is at the surface, with three nearest-neighbor As, to a bulklike environment characterized by four nearest-neighbor As atoms. The properties of the acceptor level found in STM experiments for a Mn positioned on this subsurface are also quite anomalous.<sup>35</sup> When a magnetic field of 6 T is applied along the hard direction (blue dots in Fig. 6) the anisotropy barrier increases by a couple of meV. The exception is again the first subsurface (layer 1), whose anisotropy is now completely controlled by the magnetic field and behaves

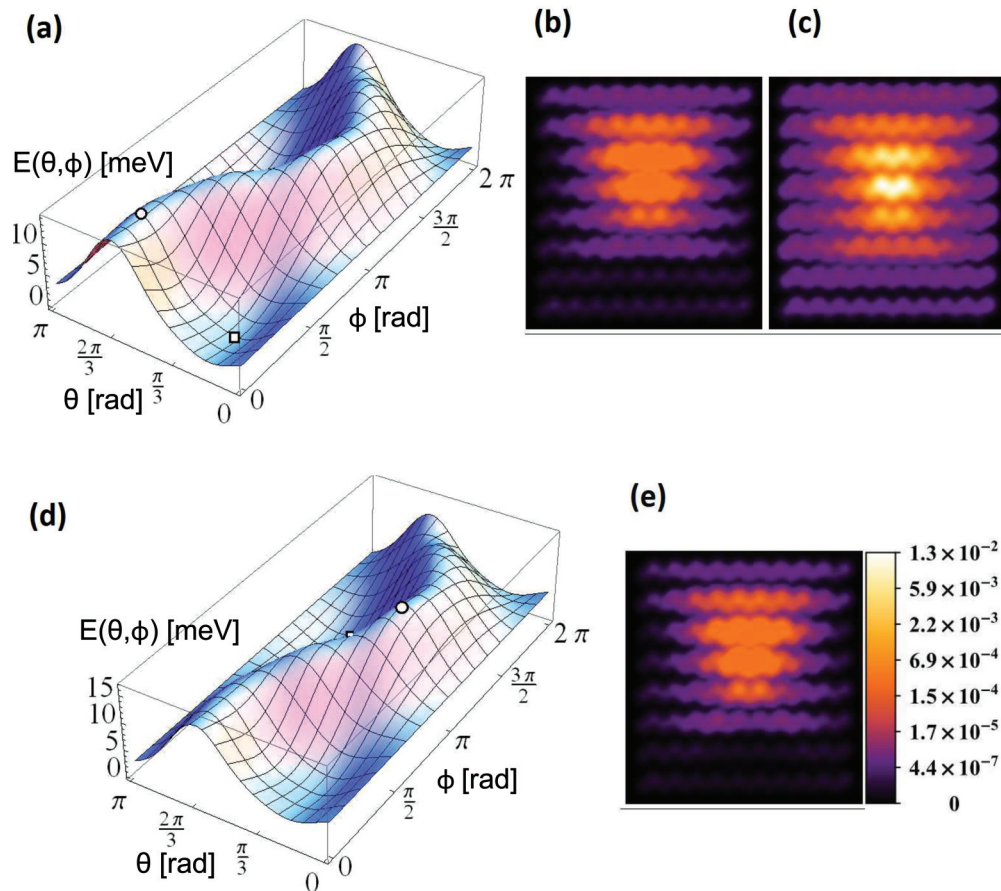


FIG. 8. (Color online) Magnetic anisotropy energy (MAE) and the LDOS for one Mn in the fourth subsurface (fourth layer below the [110] surface). (a) MAE in the absence of an external magnetic field. (b) and (c) LDOS of Mn acceptor level for the case that Mn magnetic moment points in the easy and hard direction respectively. (d) MAE in the presence of a 6-T external magnetic field, which points along the hard direction ( $\theta = \pi/2, \phi = 3\pi/4$ ). (e) LDOS in the case that magnetic moment points in the easy direction in the presence of a 6-T magnetic field. The barrier direction in (a) and (d) is marked with a circle and the easy direction with a square. The color scale in (b) and (c) is the same as in (e).

in a similar way to the surface layer. The behavior of the first subsurface anisotropy landscape is shown explicitly in Figs. 7(a) and 7(d).

As for the case of a Mn atom placed at the (110) surface, the acceptor LDOS for a Mn on the first subsurface [see Figs. 7(b) and 7(c)] is completely insensitive to the direction of the Mn magnetic moment. Again a 6-T magnetic field, which is able to completely modify the magnetic anisotropy landscape and orient the Mn moment parallel to its direction, does not have any detectable effect on the acceptor wave function, as shown in Fig. 7(d).

As the Mn is placed in successively deeper layers below the surface and the acceptor wave function becomes less localized around the impurity, the situation changes. In Figs. 8 and 9, we plot the anisotropy landscape and the acceptor LDOS for the fourth and fifth subsurfaces (layers 4 and 5 below the surface), respectively. As we discussed before, when the direction of the Mn moment is forced to point in the hard direction [panel (c) of Fig. 8] the LDOS around the Mn increases sensibly. The two cases, easy [panel (b)] and hard axes LDOS are now clearly distinguishable. Since the acceptor wave function is always normalized, an increase of the LDOS in the core region implies that the acceptor wave function is

considerably more localized when the Mn magnetic moment points in the hard direction. On the other hand, in contrast to the surface and the first subsurface, the energy barrier in this case is considerably larger. A magnetic field of the order of those applied experimentally are now not strong enough to modify appreciably the anisotropy landscape. This can be seen by comparing panel (a)—no magnetic field—with panel (d), where magnetic field of 6 T is applied in the hard direction. Consequently, the direction of the easy axis is only slightly modified in the presence of a magnetic field, and as a result, the corresponding acceptor LDOS appears now very similar to the zero-magnetic field case [panel (b)]. This is again in agreement with the experiments presented in this paper.

As mentioned before, the experiments presented in Ref. 14 showed the energy level splitting of Mn in GaAs close to the cleavage surface. For a typical Mn position, at fifth subsurface layer, a total splitting of 14 meV is found between the three peaks, which are attributed to the different projections of the total momentum  $J = 1$ , which is the result of antiferromagnetic coupling between the  $5/2$  Mn core spin and  $3/2$  Mn acceptor total angular momentum. In Fig. 9, it can be seen that the MAE is indeed about 15 meV, which corresponds well with the findings in Ref. 14.

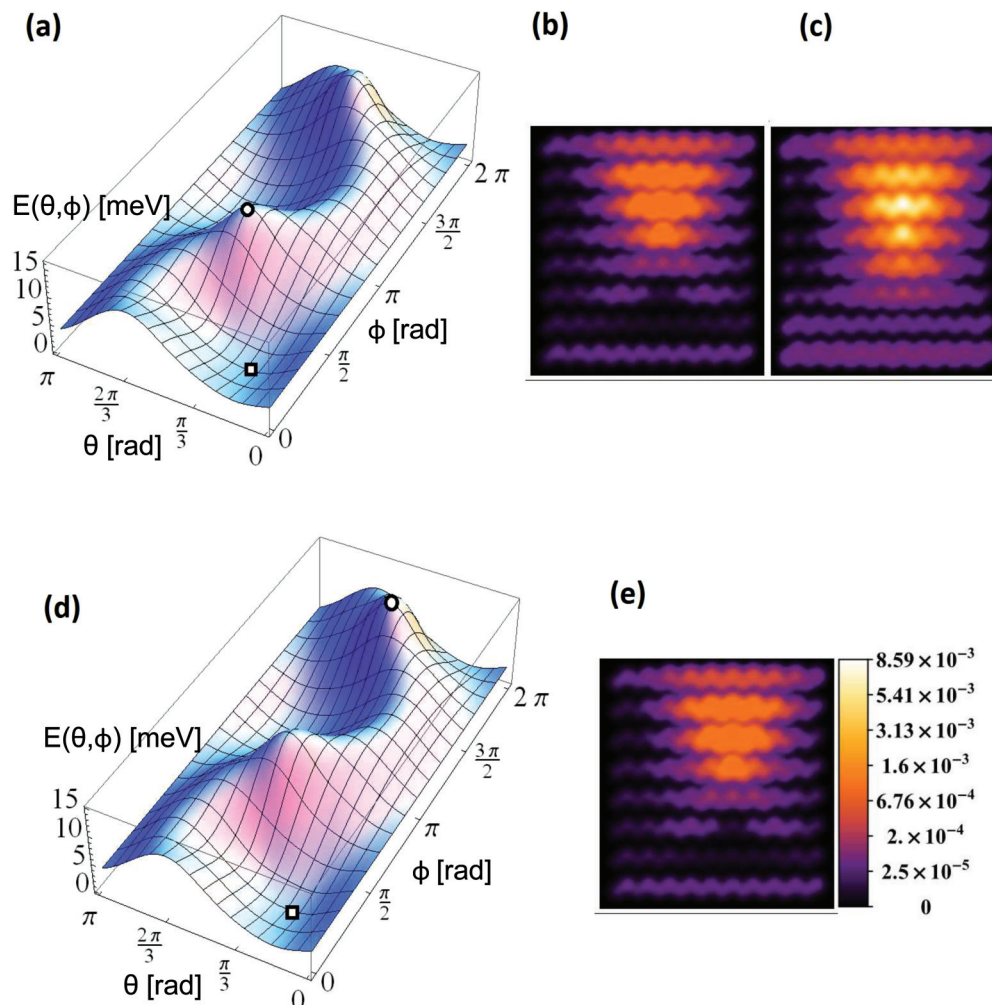


FIG. 9. (Color online) As in Fig. 8, but for the fifth subsurface (fifth layer below the [110] surface). The color scale in (b) and (c) is the same as in (e).

In Fig. 1, the MAE as calculated in another tight-binding calculation (strained bulk GaAs) is about 23 meV. This is more than the 15 meV of the supercell calculations (see Fig. 9) possibly because of the overestimated strain or its assumed uniformity.

We conclude that, although the LDOS of deep-subsurface Mn acceptors is, in principle, strongly dependent on the Mn magnetic moment direction, its actual manipulation with an external magnetic field is not suitable at field strengths presently used in experiment.

## VI. CONCLUSIONS

In conclusion, this work is the first systematic study of the effect of an external applied magnetic field on the acceptor properties of individual Mn impurities in GaAs. Specifically, we have investigated theoretically and experimentally the effect of an external magnetic field on the acceptor hole wave function and LDOS of Mn impurities placed near the (110) surface of GaAs. The acceptor LDOS is directly accessible via X-STM experiments.

The motivation of this study was in part provided by previous theoretical studies that predicted that the LDOS in some cases strongly depends on the orientation of the magnetic impurity magnetic moment. The theoretical model used in this analysis is essentially parameter free, once the energy of the surface acceptor state is fixed to reproduce the experimental value.

Experimentally, we find that there is no detectable difference in the STM images of the acceptor hole LDOS when a magnetic field up to 6 T is applied in several directions with respect to the crystal structure. To reconcile theory and experiment, we have carried out a theoretical analysis of the magnetic anisotropy energy and acceptor hole wave function in the presence of a magnetic field. We have shown that for Mn impurities placed in deep sublayers below the surface, the calculated magnetic anisotropy landscape is characterized by energy barriers of the order of 10–20 meV, which are only minimally affected by magnetic fields used in experiment. The magnetic anisotropy may be overestimated by the consideration of the Mn core spin as a classical object in this theory. However, the calculated required fields to overcome the anisotropy (on the order of tens of tesla to modify significantly the anisotropy landscape and rotate the magnetic moment) are so much larger than the experimentally applied field that our conclusions should be robust. We estimate that one needs to employ much stronger fields (on the order of tens of tesla) to modify significantly the anisotropy landscape and rotate the

magnetic moment of the impurity. This estimate is based on the idea of manipulating a spin= $5/2$  object with  $g$  factor= $2$  with an external field to overcome an energy barrier of 15 meV.

For impurities placed near the surface, the magnetic anisotropy is small enough to be considerably affected by a magnetic field of a few tesla. However, for this case, the acceptor hole LDOS is much less sensitive to the orientation of the Mn magnetic moment. The combination of these two facts seem to explain the experimental finding that the STM images of the acceptor hole wave function is essentially unaffected by an external magnetic field.

Our studies show that the Mn-dopant behavior close to the GaAs surface depends on the layer depth in a complex and highly nontrivial way. These studies also suggest that it could be interesting to carry out a similar investigation for other magnetic dopants and other semiconductors. It might be possible that for some of these systems the acceptor wave function for a dopant near the surface be more delocalized and amenable to an easier manipulation by a static magnetic field, displaying the effects originally predicted for Mn in GaAs. It should also be possible to use resonant techniques, such as those commonly used in electron spin resonance and ferromagnetic resonance, to map out the anisotropy landscape presented here for Mn near the GaAs surface. Finally, excitations of the spin that would correspond to the quantized spin in the anisotropy landscape here should be visible in inelastic tunneling spectroscopy. Thus these new predictions do not mean that Mn spin dynamics is impossible to see near the surface of GaAs, merely that it is more challenging to observe.

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