

A thermal model of the spot welding process

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A THERMAL MODEL OF THE SPOT WELDING PROCESS

A.P.A.J. HULST

A THERMAL MODEL OF THE SPOT WELDING PROCESS

PROEFSCHRIFT

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aan mijn moeder

aan Dorothé

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List of Symbols

The symbols used are defined in the section, figure or equation referred to between brackets.

A_r	area of element perpendicular to r-axis (fig.2.5); area of apparent contact surface (4.3.1)	- m^2
A_z	area of element perpendicular to z-axis (fig.2.5)	-
a	$= \lambda/c$, thermal diffusivity of workpiece metal; radius of microscopic contact spot	$m^2 \cdot s^{-1}$ m
b	$= \pi \sqrt{(\lambda \theta_m / \rho) / 4}$	$A \cdot m^{-1}$
C	electric analogue of heat capacity (fig.2.6)	F
C_o	unit capacitor (2.2.3)	$= 10^{-6} F$
c	volumetric specific heat of workpiece metal	$J \cdot m^{-3} \cdot deg^{-1}$
c, c_1, c_2	various constants	
c_E	volumetric specific heat of electrode metal	$J \cdot m^{-3} \cdot deg^{-1}$
D_E	electrode tip diameter (fig.1.1)	m
D_m	hole diameter (fig.5.2)	m
D_N	weld nugget diameter (fig.1.1)	m
d	electrode displacement (fig.3.5)	m
d_i	indentation of electrode into workpiece (fig.3.5)	m
d_{max}	maximum electrode displacement (fig.3.5)	m
d_s	sheet separation (fig.6.1)	m
F	electrode force (fig.1.1)	N
F_s	tensile shear force (3.3.2)	N
f	$= R'_o/R_o$, in general (eq.(4.5))	-
f'	$= R'_o/R_o$, with artificial current constriction (eq.(5.15))	-
G	unit step function (eq.(2.18))	-
g	heat production function (eq.(4.37))	-

H_V	Vickers hardness	$N.m^{-2}$
h	distance from electrode face to coolant channel (fig.1.1)	m
I	electric analogue of heat production (fig.2.6)	A
i, i_{rms}	r.m.s. value of welding current (fig.1.1)	A
i_p	peak value of welding current (4.3.2)	A
J	$= 4i/\pi D_E^2$, current density in general $= 4i/\pi D_m^2$, with artificial current constriction (5.2.2)	$A.m^{-2}$
k	$= \alpha(i/i_p)\sqrt{2Q_{\theta m}}$	-
k_1	$= k/Q_D$	-
k_2	$= kg/Q_D$	-
L	Lorentz' constant	$\approx 2.4 \times 10^{-8} V^2.deg^{-2}$
m, n	array variables denoting axial and radial position of a model element respectively (fig.2.4); various exponents and constants	-
Q_c	$= c_E/c$	-
Q_D	$= D_E/s$ in general; $= D_m/s$ with artificial current constriction (eq.(5.11))	-
Q_F	$= 4F/\pi D_E^2 H_V$	-
Q_h	$= h/D_E$	-
Q_r	$= r/s$	-
Q_t	$= at/s^2$	-
$Q_{t'}$	$= at'/s^2$	-
Q_v	$= \sqrt{Q_{\theta}}/Q_D^2$	-
Q_z	$= z/s$	-
Q_{θ}	$= \lambda\theta/\rho J^2 s^2$, dimensionless weld temperature, generally in the point B($z = 0, r = D_E/2$)	-
$Q_{\theta c}$	calculated value of Q_{θ} from model measurements (4.3.3)	-
$Q_{\theta m}$	measured value of Q_{θ} from experimental verification, value of Q_{θ} for $\theta = \theta_m$ (4.3.2)	-

Q_λ	$= \lambda_E/\lambda$	-
Q_ρ	$= \rho_E/\rho$	-
q	$= Q_{\theta m}/Q_{\theta c}$	-
R	total resistance of the workpieces	Ω
R_c	constriction resistance (4.3.1)	Ω
R_k	contact resistance (4.3.1)	Ω
R_r	electric analogue of thermal resistance in radial direction (fig.2.6)	Ω
R_s	supply resistance (fig.2.6)	Ω
R_z	electric analogue of thermal resistance in axial direction (fig.2.6)	Ω
R_o	$= 8\rho s/\pi D_E^2$, assumed body resistance in the model in general; $= 8\rho s/\pi D_m^2$, with artificial current constriction (5.2.2); unit resistor (2.2.3)	Ω Ω $= 10^6 \Omega$
R'_o	actual body resistance (4.2)	Ω
r	radial coordinate	m
s	sheet thickness (fig.1.1)	m
t	time coordinate	s
t'	welding time, determined by means of the electrode displacement curve (fig.3.5)	s
t_h	heating time	s
t_m	analogue time (2.2.3)	s
t_s	time at which splashing occurs (fig.3.6)	s
U	electric analogue of temperature (fig.2.6); $= iR$, total voltage across the workpieces (3.3.2); $= iR_k$, contact voltage (4.3.2)	V V V
U_s	$= IR_s$, supply voltage in the analogue model (fig.2.6)	V
V	volume of model element	-
w	width of workpiece specimen	m

w_L	overlap length of workpiece specimens (fig.1.1)	m
Y_t	$= t_m R_o C_o$	-
Y_U	$= U/U_s$	-
z	axial coordinate	m
α	$= (\rho\lambda)'/\rho\lambda$, multiplying factor	-
β	a constant (eq.(4.27))	s^{-1}
Δ	$= d_{max}/s$	-
δ	dimensionless electrode displacement rate (eq.(6.11))	-
ε	dimension of model element (fig.2.4)	-
ζ	a constant (eq.(4.41))	-
θ	supertemperature;	deg
	weld temperature, generally in the point B($z = 0, r = D_E/2$)	deg
θ_e	equilibrium temperature of the weld (eq.(4.28))	deg
θ_m	melting temperature of workpiece metal	deg
λ	thermal conductivity of workpiece metal	$W.m^{-1}.deg^{-1}$
λ_E	thermal conductivity of electrode metal	$W.m^{-1}.deg^{-1}$
μ	coefficient of linear thermal expansion	deg^{-1}
ξ	a constant (eq.(4.8))	-
ρ	electric resistivity of workpiece metal	$\Omega.m$
ρ_E	electric resistivity of electrode metal	$\Omega.m$
σ_M	ultimate tensile strength of workpiece metal	$N.m^{-2}$
σ_s	a constant (eq.(6.3))	$N.m^{-2}$
τ_s	a constant (eq.(6.4))	$N.m^{-2}$
ϕ	total heat production in the weld (eq.(4.40));	J
	angular coordinate	-
ϕ_k	heat production owing to the contact resistance (eq.(4.26))	J
ϕ_o	heat production owing to the body resistance assumed in the model (eq.(4.2))	J

Notes.

- (1) All temperature values used are supertemperatures with respect to the ambience.
- (2) The subscripts 1 and 2 generally denote symbols related to the upper sheet and upper electrode or lower sheet and lower electrode respectively, as shown in fig. 1.1.

Chapter 1. INTRODUCTION

1.1. General Background

Resistance welding embraces that branch of the welding art in which the welding heat in the parts to be joined is generated by the resistance of these parts to the passage of an electric current. It differs from other welding methods in that no extraneous materials are added, and mechanical pressure is applied to forge weld the heated parts together [1].

Spot welding is undoubtedly the most widely used type of resistance welding. The process mainly consists of clamping two or more pieces of sheet metal between two welding electrodes of relatively good electrical and thermal conductivity and passing an electric current of sufficient force and duration through the pieces to cause them to weld together. The type of joint made in this way is called lap-joint, which means that the welded parts overlap each other over a distance of a few times the weld diameter.

The fused zone generally has the form of a nugget, for which reason it is referred to as the weld nugget. Its dimensions and metallurgical structure are of major importance for the strength and the quality of the joint made.

Fig. 1.1 shows an arrangement of the spot welding electrodes and of the position of the workpieces which can be regarded as typical for this kind of welding process. As can be seen, the electrodes have three important functions, viz. to supply the welding force to the workpieces, to guide the electric current through the pieces to be welded, and to carry off the heat generated near the electrode-workpiece contact surface so as to prevent fusion from occurring in this area. As a result of the passage of a current pulse of well-defined shape, magnitude and duration, melting and fusion is caused in the area that is most suited on the basis of the geometric and thermal data, i.e. at the interworkpiece contact plane. A subsequent short forging period allows the nugget to cool down under pressure in order to obtain a good coherence between the welded parts and to prevent porosity as might be caused by shrinkage.

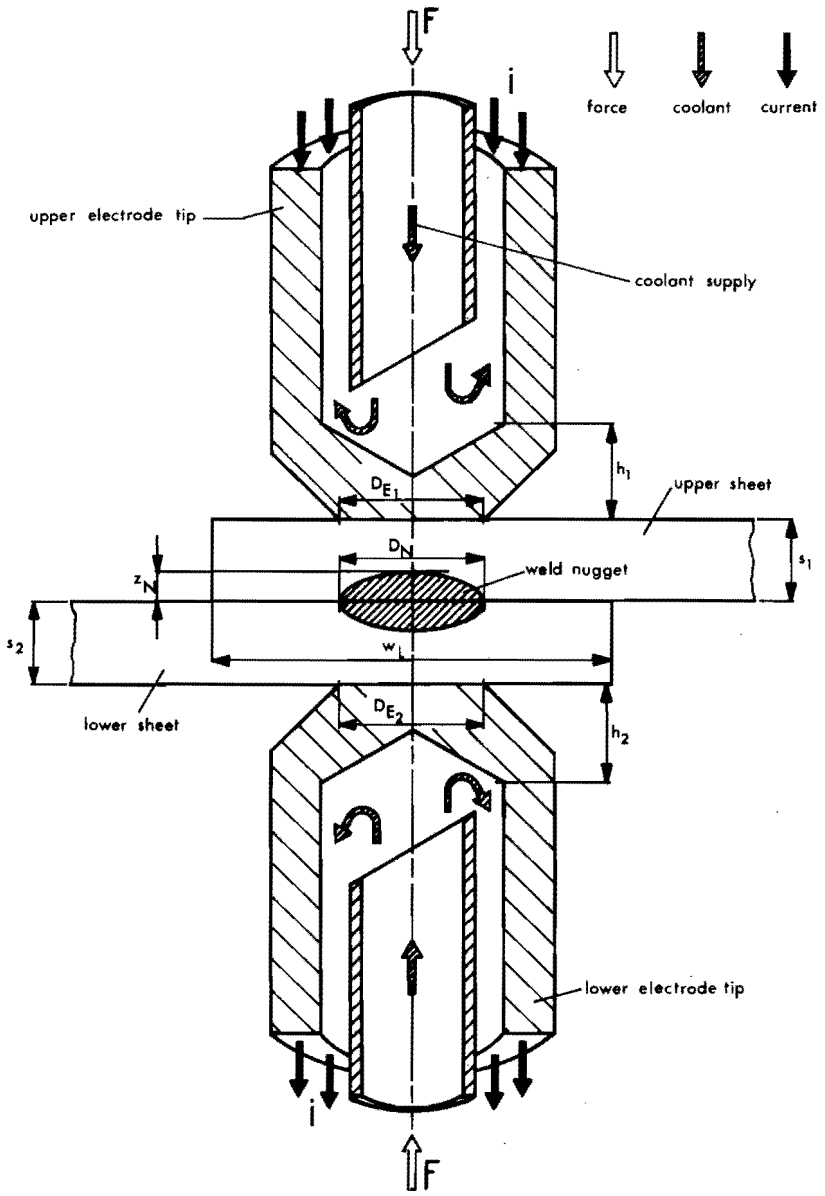


Fig. 1.1. Typical Arrangement of Spot Welding Electrode Tips and Workpieces

Out of the extensive quantity of available literature the following sources may be recommended for general information.

On	ref.
fundamentals	[1,4,5,6,7],
machines and welding controls	[4,5,7,8,9,11,12],
electrodes	[1,4],
power requirements	[1,4,5,11,12],
industrial machine settings	[1,2,4],
standards	[4,10],
applications	[3,8,9,11,12].

1.2. Definition of the Problem

Until some years ago spot welding was chiefly applied for mass-produced articles and for purposes where strength and reliability are not imperative. However, during the last fifteen years the tendency has increased to use the process also in cases where high demands are made with respect to the static and dynamic strength of the joint as well as to the quality of its external appearance. As examples of this kind of applications may be mentioned railway car production [13,14], critical joints in motor-car coach work [11(KRIMIANIS),9,16], aircraft construction [12(FIALA),19], aircraft jet engines [12(SCHLOSSER),17,18] and launch vehicles [12(ROHRMANN)].

For these applications it becomes urgent to gain a better understanding of the fundamentals of the process. This understanding has to be not only qualitative but quantitative as well, because of the need to choose optimum machine settings and especially to design adequate devices for the control of weld quality. As a consequence of the very short duration of the welding process such a control has to act automatically, governed by one or more process variables.

Another demand for an automatic control is brought about by the use of resistance welding techniques for the manufacture of miniature and subminiature products like semi-conductors [20] and for the

assembly of electronic components [21]. Here, the extreme small dimensions of the workpieces make automation almost inevitable. It is the fundamental idea of this work that spot welding primarily can be considered as a thermal process. Factors determining the quality of the weld such as the metallurgical structure of the weld nugget and its surroundings, mechanical deformations resulting from thermal expansion or electrode impression as well as the size of the weld itself can be regarded as consequences of the thermal cycle. Therefore, the first work to be done is to determine the temperatures during spot welding, dependent on both time and space coordinates. However, the problem here is the impossibility of measuring temperatures in an area of a few square millimeters where gradients in the order of 10^6 deg.m^{-1} and time derivatives of some 10^5 deg.s^{-1} exist without disturbing the electric current or heat flux fields.

The only conclusions regarding temperature distributions at the end of the heating cycle can be drawn from the dimensions of the weld nugget and, to a much lower degree of accuracy, from the metallurgical structure of the weld and the heat-affected zone [22]. Generally, a well-distinguishable boundary exists between the areas that have been liquefied or not. At this boundary, temperature has just reached the melting point of the metal concerned. This goes for the circumference of the weld nugget in the workpiece interface as well.

The main subject of these investigations will be to theoretically determine temperatures in spot welding and to try to verify the computations by means of the above-mentioned considerations. For a thorough analysis close attention has to be given to welding parameters, material properties and weld geometry.

A further object will be to consider the possibilities of quality control and adaptive control on basis of this analysis.

1.3. Limitations

Some restrictions have to be made as to the scope of this work in order to limit the number of experiments to a reasonable quantity.

The construction of a satisfactory mathematical and physical model is considered to be of more importance than the investigation of all possible geometrical arrangements or the various designs of workpieces and electrodes. Consequently, only a system consisting of two workpieces of equal dimensions and materials and of two equal electrodes is considered in the first place. The workpieces consist of two sheets, the length and width of which are irrelevant in as far as minimum dimensions as defined in section 2.2.2 are taken into account. An extension of this set-up will be given in section 5.1. A generally applied electrode shape, viz. the truncated cone is used.

The metallurgical structure of the weld is greatly affected by the post-weld cooling rate. It is not only important for medium and high carbon steels or for precipitation hardening alloys, but it also influences the solidification structure of any metal. Grain dimensions, residual stresses and weld ductility are to a high degree defined by the cooling cycle. To improve weld quality, an additional post weld heat treatment is frequently carried out in the welding machine.

Cooling rate, therefore, is to be considered of great importance throughout the weld material. It is easily determined with the aid of the analogue described in chapter 2. However, since no method is known to verify the curves and because of the requirement of limiting the extent of experimental results, no cooling curves are presented in this work.

Chapter 2. THE ANALOGUE MODEL

2.1. Review of the Problem

2.1.1. Introduction

As indicated in chapter 1 the object of the mathematical model will be to evaluate the temperatures during spot welding, dependent on welding parameters, material properties and weld geometry. The most important welding parameters are welding current i , welding time t and electrode force F . Those are the variables regulated on the welding machine by the operator. Significant material properties are of thermal or electrical nature, viz. volumetric specific heat c , thermal conductivity λ and electric resistivity ρ of both workpiece and electrode materials. Weld geometry comprises, as a matter of fact, all dimensions of workpieces and electrodes, but workpiece thickness s , electrode face diameter D_E and the distance h between electrode face and coolant channel are of special importance. The temperature distribution resulting from heat generation and conduction in a solid is governed by Fourier's law

$$c \frac{\partial \theta}{\partial t} = \nabla \cdot (\lambda \nabla \theta) + \rho J^2 \quad (2.1)$$

Since the mean value of the current density J is determined by i and D_E this differential equation contains most of the above-mentioned variables, while the others appear in the boundary conditions. The main exception is the electrode force F which influences the values of the contact resistances occurring at the material interfaces, resulting in an additional heat development in those areas.

The solution of temperatures from equation (2.1) dependent on place and time for the spot weld case offers great mathematical difficulties even if no allowance is made for the role of the contact resistance. A fundamental increase of these difficulties lies in the fact that the thermal and electrical properties c , λ and ρ are temperature-dependent, thus giving a non-linear character to the equation.

The work done by several investigators either to solve equation (2.1) in a more or less simplified form or to approach the problem from an empirical point of view will be considered briefly in the next sections.

2.1.2. Empirical Methods

At the present time, determination of the machine settings required to obtain an adequate weld on a given spot welder is purely empirical. Common practices recommended by welding manuals are used as a guidance, but the experience of the welding engineer is required if high-quality welds are imperative. Of course, these recommended practices originate from numerous experimental results in their turn.

A few investigators have tried to generalize these results by using products of some of the welding variables and by studying their mutual relations. These products may be of an empirical nature themselves [23] or they may be derived from equation (2.1) and its boundary conditions [24]. In both cases some criterion is required to define a weld of sufficient quality.

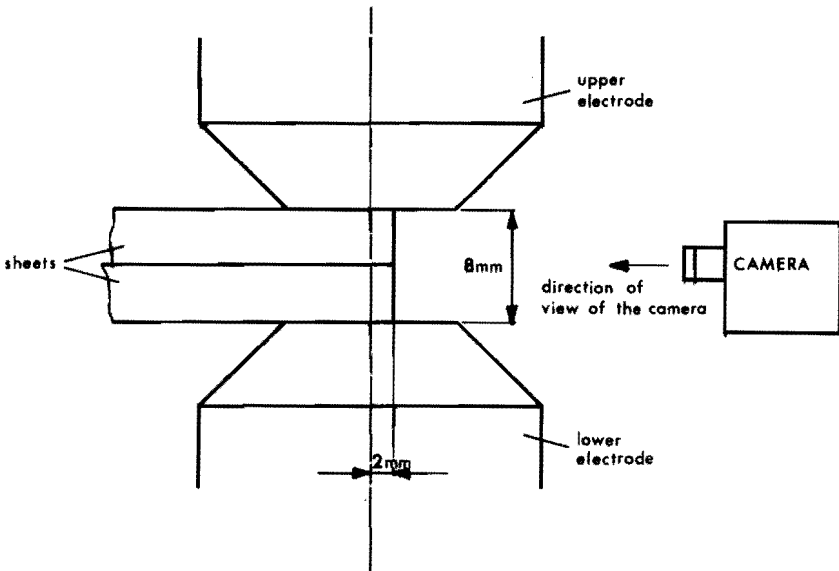


Fig. 2.1. Arrangement for Measuring Temperatures during Spot Welding as described in [25]

A newly developed experimental method to evaluate the temperatures during spot welding is described in reference [25]. Here, the weld is made with the electrodes partly situated over the edge of the sheets, as shown in fig. 2.1. The weld is intersected, as it were, before welding, thus enabling the investigators to record the weld formation on a high speed colour film and to evaluate temperatures afterwards by colour comparison. Although with high energy production rates the maximum temperature level is limited as a result of the tendency of the molten metal to be pushed away in the direction of the camera or to cover less heated parts of the weld, the method seems to offer a useful possibility to determine welding temperatures or to study weld formation.

2.1.3. Analytical Methods

Owing to the complexity of the problem no solution can be obtained in the form of an explicit function of the relevant parameters satisfying equation (2.1) as well as the initial and boundary conditions. However, several investigators have tried to simplify the problem in order to permit the derivation of an analytical solution. The advantages of such a procedure are obvious. The solution can be given in a very compact form; it is valid for the complete range of the variables involved and no expensive and laborious expedients are necessary. Finally, an explicit function offers the possibility to easily differentiate with respect to time in order to determine the values of heating or cooling rates. On the other hand, the problem solved differs substantially from the real situation.

The main characteristic of such solutions is the neglect of electric contact resistance, of electrode properties and of heat production distribution. Simplifications regarding heat transfer to either the surrounding sheet or the electrodes commonly are made, in order to reduce the number of space coordinates.

This results in a one-dimensional solution given by references [26] and [27]. The welding heat is supposed to be generated at the workpiece interface only and to flow in the direction of the electrode face, the temperature of which equals that of the ambience. The analysis is applied to the welding of foil gauges where a one-dimensional heat flow seems to be a fair approximation

indeed because of the very high electrode diameter to sheet thickness ratios employed there.

Two-dimensional radial heat flow resulting from a line source along the z-axis is assumed in [28]. This solution might represent the opposite case, i.e. a very small electrode diameter compared with sheet thickness.

Three-dimensional solutions depart from either a point source in an infinite solid [29] or from a weld nugget of uniform temperature during the whole welding cycle [6]. The first completely disregards the presence of electrodes with high thermal conductivity, while the second uses a single coefficient of surface heat transfer to account for the amount of heat flowing to the surrounding sheet as well as to the electrodes.

Generally, the analytic solutions are useful for a limited range of applications, but they fail to give a coherent description of the thermal aspects of the spot welding process.

2.1.4. Numerical Solutions

Numerical methods must be used to avoid the simplifications required for an analytical approach. With the aid of relation (2.1) difference equations can be established applicable to small elements of the welding work. These elements are defined by space increments. In a three-dimensional set-up the number of elements and thus the number of equations will soon be of such an extent that the employment of a digital or analogue computer becomes indispensable. Since the treatment of the problem on an analogue computer would require at least one integrator for every volume element, the possibilities of this method are limited. In most cases, the storage capacity of a digital computer offers greater facilities for more extensive systems.

The first numerical solution established with the aid of a digital computer was given by GREENWOOD [30]. Here, heat generation distribution throughout the workpiece body and actual weld geometry were taken into account. The cooling effect of the electrodes was included by means of a coefficient of surface heat transfer for the workpiece-electrode interface. The dependence of material properties on temperature and the contact resistances were ignored. The

reason for these neglects was the lack of information about these phenomena particularly on the breakdown of contact resistance during the welding cycle. For the same reason the diameter of the interworkpiece contact area was assumed to have the same dimension as the electrode tip diameter.

One important conclusion can be drawn from this work with regard to the shape of the well nugget in dependence on weld time. Fig. 2,2 shows that for a very short weld time - which means high heat production rate - a ring-shaped welding zone develops, while maximum temperatures of the electrode face occur at its edge. Medium energy input, resulting in a longer weld time yields a cylinder-shaped nugget, whereas at low energy production rate the well-known ellipsoidal nugget form arises and the maximum temperatures of the electrode face occur at its centre.

Experimental verifications of these computations were carried out by several authors [22, 25, 31]. Generally, a fair agreement is observed between theory and experiments especially during the later stages of heat build-up. In the beginning of the heating cycle, however, the contact resistances at the electrodes and at the workpiece interface tend to increase the calculated temperature values. According to [22] further discrepancies between calculated and observed temperatures may have been caused by the influence of temperature on material properties.

Another numerical calculation [32] shows the possibility of accounting for contact resistances, variable material properties and shape of the welding current pulse in the one-dimensional case of welding laminated bars of comparatively small cross-section axially to each other.

2.1.5. Simulation by means of an Analogue

An attractive method of evaluating the temperatures during spot welding is the use of the analogy of the process in question with any other phenomenon subjected to the same differential equation and boundary conditions. This approach of the problem is not merely empirical, since the physical laws which control the process under review as well as the analogue model have to be known in detail. It is noted that this approach is distinctly different from the use of an analogue computer.

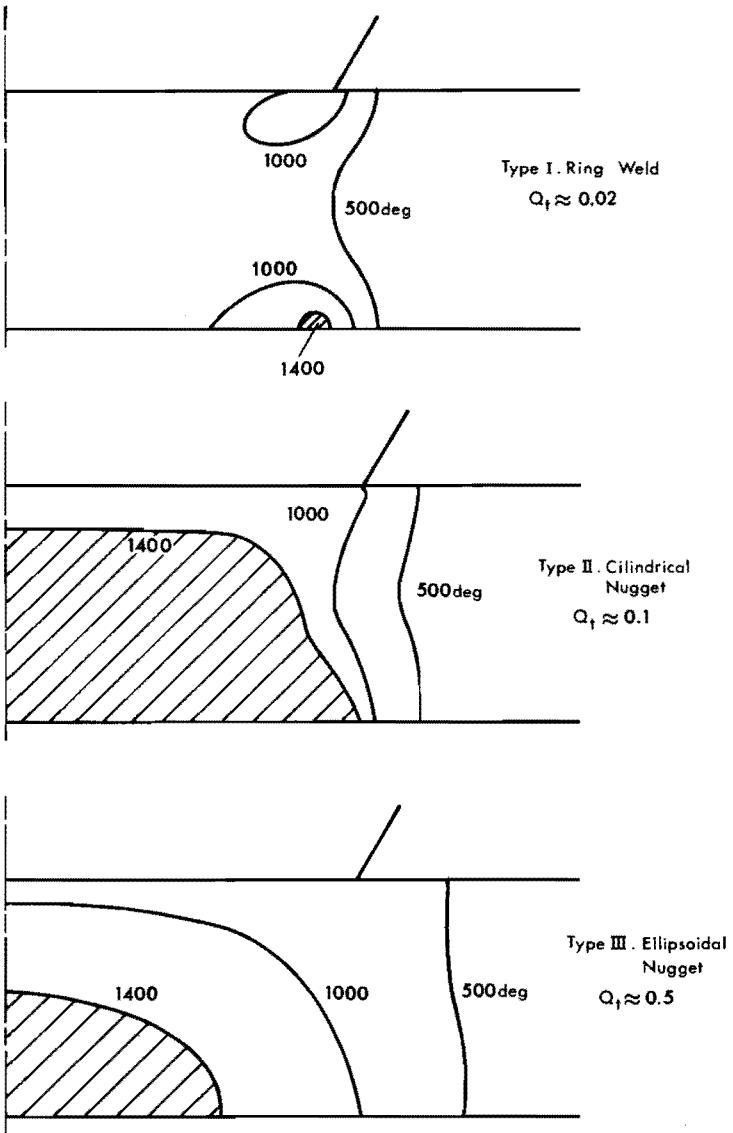


Fig. 2.2. Different Shapes of Weld Nuggets in dependence on Heating Time, as described in [25]
 Temperature values are given for reference only

The most obvious analogue would be the spot welding process itself. The geometric dimensions should then be enlarged to values in the order of ten to hundred times the usual sizes and also the time scale requires sufficient extending in order to permit the measurement of the thermal and electrical potentials. To confine the magnitude of the welding current to reasonable values the electric and thermal conductivities should be diminished by a same factor of ten to hundred. A baked carbon [36] with electric resistivity of about $10^{-4}\Omega.m$ and thermal conductivity of $2 W.m^{-1}.deg^{-1}$ might prove to be useful for the purpose.

However, the analogy most widely used is to relate transient heat transfer to the flow of electric currents through a network of resistors and capacitors representing thermal resistance and heat capacity respectively. Though in a simple form, GENGENBACH [12] used a one-dimensional performance of this Beuken model [33] to determine spot weld temperatures, particularly for the case of series welding.

A more realistic analogue was developed by RIEGER and RUGE [34]. The performance is fundamentally three-dimensional although the existence of axial symmetry in fact reduces the number of space coordinates to two. The RC-network employed resembles very much the model described in this thesis, but the use of it is restricted to the determination of the final temperatures in spot welding 1 mm copper and aluminium sheets.

The absence of a simple method to simulate temperature-dependent material properties may be regarded as a disadvantage of the passive RC analogue compared with a digital computer, although several possibilities arise with the use of active electronic elements [35].

2.1.6. The Role of the Contact Resistance

The contact resistance is an extra resistance between two points on either side of a contact surface, additional to the ordinary body resistance. This additional resistance is due to the imperfection of the contact between the two members, produced by the irregularities of the surfaces that cause them to contact each other only at a number of small spots. Furthermore, the influence

of thin oxide layers or films may reduce the electric conductivity of these spots. If alien substances such as grease or dirt are present the resistance increases to values much higher than the total body resistance of the contact members [6, 36].

In spot welding such contact resistances exist between the workpieces as well as between workpieces and electrodes. However, they have a dynamic character. When the electric current starts to flow the contact spots are rapidly heated to high temperatures [36] so that they tend to grow in dimension and in number as a result of the weakening of the metal. The total resistance thus decreases rapidly. Several investigators observed the contact resistance to break down to zero value during the first half cycle when alternating welding current was used [6, 37, 38].

Nevertheless [22] observes a notable effect of contact resistance on the temperature distribution in spot welding mild steel. For aluminium the value of the initial contact resistance greatly affects the quality of the weld made. Reduction of this resistance to a minimum value will in this case enhance weld consistency, weld nugget shape and electrode tip life [37, 44].

[39], on the other hand, shows that in welding highly resistive metals with only a small tendency towards the forming of oxide films, such as nimonic 80, 18/8 stainless steel and titanium alloys, the heat production is only slightly influenced by the presence of contact resistances. It is demonstrated that when heating a single sheet of these materials or when welding two sheets with unequal thickness (3:1 ratio) the nugget always forms in the middle of the total thickness.

In conclusion, the influence of contact resistance on the welding process is commonly considered to increase if

- (a) the sheet thickness decreases,
- (b) the electrode force decreases,
- (c) the thickness of the oxide film increases,
- (d) the resistivity of the oxide increases in proportion to body resistivity and
- (e) the weld time decreases.

For the obtainance of high-quality welds it is a general practice to minimize surface resistance by mechanical or chemical cleaning methods [1, 10]. From the foregoing it appears to be impossible to

predict the value of contact resistance with universal validity. For both reasons this resistance will be disregarded in the first instance; the resultant deviations will be considered in section 4.3.

Apart from the electric contact resistance there is also a thermal contact resistance in the same planes. Its influence on the welding process, however, is far less pronounced. At the workpiece interface it does not play a role at all because of the absence of thermal flow on account of symmetry. At the electrode face its value is relatively small compared with its electric equivalent; this is due to the fact that oxides and air gaps do not act as insulators for heat flow as they do for electric current [41]. Its influence is therefore disregarded.

2.1.7. The Use of Dimensionless Parameters

The use of dimensionless parameters offers important advantages in experimental work in which a great number of variables is concerned. According to [40] the number of dimensionless parameters equals the number of variables minus the number of fundamental dimensions involved. In this way the thirteen significant variables - including temperature - (see section 2.1.1) can be reduced to eight dimensionless parameters, being products of those variables. The five fundamental dimensions are length, mass, time, electric current and temperature.

The quantity of experiments required to verify a theoretical calculation is therefore reduced substantially, since this quantity tends to increase with the n-th power of the number of parameters to be considered, n representing the number of levels on which each parameter is varied. If the results of calculations or experiments are not given in the form of analytic formulas but in graphs or tables, this representation is simplified and diminished in size as well.

To evaluate the relevant dimensionless products the differential equation (2.1) and its boundary conditions have to be considered. In the case of constancy of coefficients and axial symmetry the equation can be written

$$c \frac{\partial \theta}{\partial t} = \lambda \left(\frac{\partial^2 \theta}{\partial z^2} + \frac{\partial^2 \theta}{\partial r^2} + \frac{1}{r} \frac{\partial \theta}{\partial r} \right) + \rho J^2 \quad (2.2)$$

Dimensionless variables can now be introduced

$$Q_z = \frac{z}{s}; \quad Q_r = \frac{r}{s} \quad (2.3)$$

$$Q_\theta = \frac{\theta}{\theta_{ch}}; \quad Q_t = \frac{t}{t_{ch}} \quad (2.4)$$

where θ_{ch} and t_{ch} denote characteristic values still to be defined for temperature and time respectively. By introducing the products Q_1 and Q_2 equation (2.2) can be rewritten

$$\frac{\partial Q_\theta}{\partial Q_t} = Q_1 \left(\frac{\partial^2 Q_\theta}{\partial Q_z^2} + \frac{\partial^2 Q_\theta}{\partial Q_r^2} + \frac{1}{Q_r} \frac{\partial Q_\theta}{\partial Q_r} \right) + Q_2$$

$$\text{with } Q_1 = \frac{\lambda t_{ch}}{s^2 c} = \frac{at_{ch}}{s^2}$$

$$\text{and } Q_2 = \frac{\rho J^2 t_{ch}}{c \theta_{ch}}.$$

If t_{ch} and θ_{ch} are chosen to satisfy $Q_1 = Q_2 = 1$ it follows

$$t_{ch} = \frac{s^2}{a} \quad \text{and} \quad \theta_{ch} = \frac{\rho J^2 s^2}{\lambda} \quad (2.5)$$

and hence

$$\frac{\partial Q_\theta}{\partial Q_t} = \frac{\partial^2 Q_\theta}{\partial Q_z^2} + \frac{\partial^2 Q_\theta}{\partial Q_r^2} + \frac{1}{Q_r} \frac{\partial Q_\theta}{\partial Q_r} + 1 \quad (2.6)$$

$$\text{where } Q_\theta = \frac{\lambda \theta}{\rho J^2 s^2} \quad \text{and} \quad Q_t = \frac{at}{s^2} \quad (2.7)$$

The other six products result from boundary conditions, electrode properties and weld geometry

$$\begin{aligned}
 Q_c &= \frac{c_E}{c} ; & Q_\lambda &= \frac{\lambda_E}{\lambda} ; & Q_\rho &= \frac{\rho_E}{\rho} ; \\
 Q_F &= \frac{4F}{\pi D_E^2 H_V} ; & Q_D &= \frac{D_E}{s} ; & Q_h &= \frac{h}{D_E}
 \end{aligned} \tag{2.8}$$

2.2. The Mathematical Model

2.2.1. Choice of the Computation Method

In order to obtain a coherent physical model of spot welding suitable as a basis for workshop practice, some degree of the mathematically achievable accuracy has to be relinquished in favor of easier interpretation by the employer. This does not only mean that variables with relatively little influence on the results are omitted. It also indicates that a variable of which the influence can be quantitatively expressed by multiplying the results by a known factor may be excluded from the model in the initial stages. This will be shown to be more or less applicable to

- (a) temperature-dependent material properties,
- (b) latent heat of fusion, and
- (c) the influence of the contact resistance.

As a matter of fact, the described model is based on the assumption of a simplified current distribution. It will be shown by the experimental results that the introduction of an adequate multiplier sufficiently accounts for the deviations caused by this simplification.

As already pointed out, various investigators have developed methods to determine spatial temperature distributions during the welding of specified materials and geometries, using the above assumptions. For technical applications, however, the need for

general information regarding temperature-time relations is considered of primary importance in order to facilitate the setting of welding variables when a given strength or dimension of the weld is desired. Therefore, the determination of the interrelation of temperature and time for a few important areas of the weld will be emphasised in the present work.

It may be concluded from the foregoing review of computation methods that only a numerical approach or the application of an analogue will yield acceptable results. The advantages of a digital computer over an analogue model, viz. its higher accuracy and its disposition to solve a non-linear form of equation (2.1), are not relevant if the accuracy is already affected by the introduction of necessary simplifications and if the equation is linearized by means of the statements (a) and (b). In this situation the analogue has pronounced advantages. The results are more easily perceptible as they can immediately be read from an oscillograph and necessary changes in the computation programme are less laborious [35]. For these reasons the RC analogue is chosen to determine temperatures in spot welding, especially as functions of time. Besides, the use of dimensionless variables is considered to be of great convenience.

2.2.2. Assumptions, Initial and Boundary Conditions

The mathematical model comprises a combination of specifications, appropriate physical laws, boundary conditions with respect to space and time and assumptions. It is assumed to describe the process quantitatively with an accuracy sufficient for practical applications.

If a coordinate system is chosen with its origin in the centre of the weld, the positive z-axis coinciding with the electrode axis and the r-axis lying in the interworkpiece contact plane, obviously axial symmetry exists. If, in accordance with section 1.3, the dimensions of the electrodes and those of the sheets are equal, plane symmetry exists with regard to the plane $z = 0$ as well. This implies that no heat can flow across this plane, hence only the system consisting of one sheet and one electrode has to be considered.

Since [30] demonstrates that heat loss by radiation or convection from the free surface of the sheets is negligible compared with the total heat production, these surfaces are supposed to be insulated. A uniform temperature is assumed to be present in the workpiece-electrode contact plane. No serious deviation from the real situation is introduced by this assumption [22, 25]. As a result, the heat flow to the electrode can be considered to be one-dimensional. This greatly simplifies the study of variable electrode dimensions and properties.

The effect of the latent heat of fusion on the temperature development of the weld cannot easily be predicted quantitatively. Of course, the time in which the centre of the weld reaches the melting point is not influenced by latent heat. The same applies to the region $r < 0.3D_E$ in the plane $z = 0$, since local temperature gradients are comparatively small before melting initiates. During the growth of the melting area the surrounding region will no longer receive heat from the centre, since there the gradients reduce to zero. Consequently the temperatures in the surrounding region increase at a slower rate. To some extent this effect is compensated by the higher energy production rate due to the increase of electrical resistivity with temperature.

As indicated earlier the latent heat of fusion as well as the influence of temperature on physical properties will be neglected mathematically. Their effects are accounted for by means of empirical values of the variables ρ , c and λ as to be defined in chapter 3.

In accordance with section 2.1.6 the thermal contact resistances are neglected, the electrical contact resistances being considered in chapter 4.

Minor simplifications regard the coolant temperature, which is assumed to be equal to the ambient temperature, the electrode shape (see fig. 2.3) and the shape of the welded sheets, which are supposed to be circular and to have a diameter of 100,s. Our experiments indicate that this shape has no influence at all on the results as long as a minimum diameter of $5D_E$ is maintained. Finally, an approximate method is used to account for the non-uniform distribution of electric current and, consequently, of heat generation in the workpiece. This method consists in comparing the real body resistance of the sheets between the electrodes with the

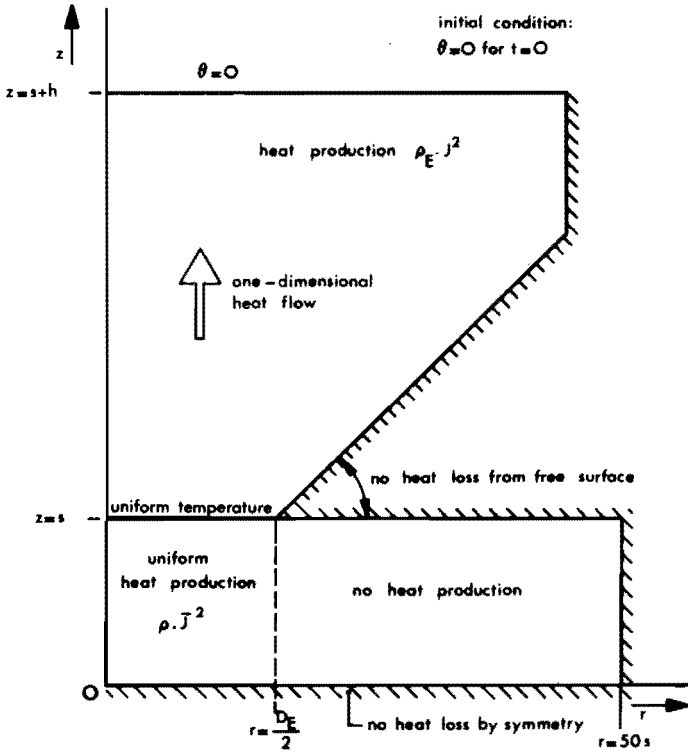


Fig. 2.3. Cross-section of the Mathematically Relevant Part of the Weld.
Main Assumptions and Boundary Conditions

resistance of a cylinder of diameter D_E and height $2s$. The total quantity of heat developed in this cylinder is adjusted by means of the resistance ratio thus found.

In doing so, the assumed distribution of the heat generation in the analogue model is substantially simplified, viz.

$$\left. \begin{aligned}
 \rho J^2 &= \frac{16\rho i^2}{\pi^2 D_E^4} = \rho \bar{J}^2 & \text{for } r &\leq \frac{D_E}{2} \\
 \rho J^2 &= 0 & \text{for } r &> \frac{D_E}{2}
 \end{aligned} \right\} \quad (2.9)$$

In section 4.2 the required adjustment will be shown to depend on Q_D only.

Fig. 2.3 shows a cross-section of the mathematically relevant part of the weld geometry, in which the main assumptions and boundary conditions are demonstrated.

2.2.3. Description of the Analogue Model

At this point, the object of the analogue model can be defined more closely. The aim is to solve equation (2.6) along with the assumptions, initial and boundary conditions mentioned in the foregoing section. As a first step this differential equation will be linearised with respect to the space derivatives. For this purpose the sheet is thought of as divided in ring-shaped elements having a cross-section ϵ^2 as shown in fig. 2.4. The volume of an element $[m,n]$ depends on n only

$$V[m,n] = \frac{1}{2}(2n - 1)\phi\epsilon^3 \quad (2.10)$$

Its surfaces perpendicular to the Q_z -axis are

$$A_z[m-1,n] = A_z[m,n] = \frac{1}{2}(2n - 1)\phi\epsilon^2 \quad (2.11)$$

and perpendicular to the Q_r -axis

$$A_r(Q_r) = \phi Q_r \epsilon \quad (2.12)$$

as illustrated in fig. 2.5.

Subsequent integration of the terms of equation (2.6) over the volume element $[m,n]$, assuming that the potential Q_θ does not vary within the element, yields for the first term

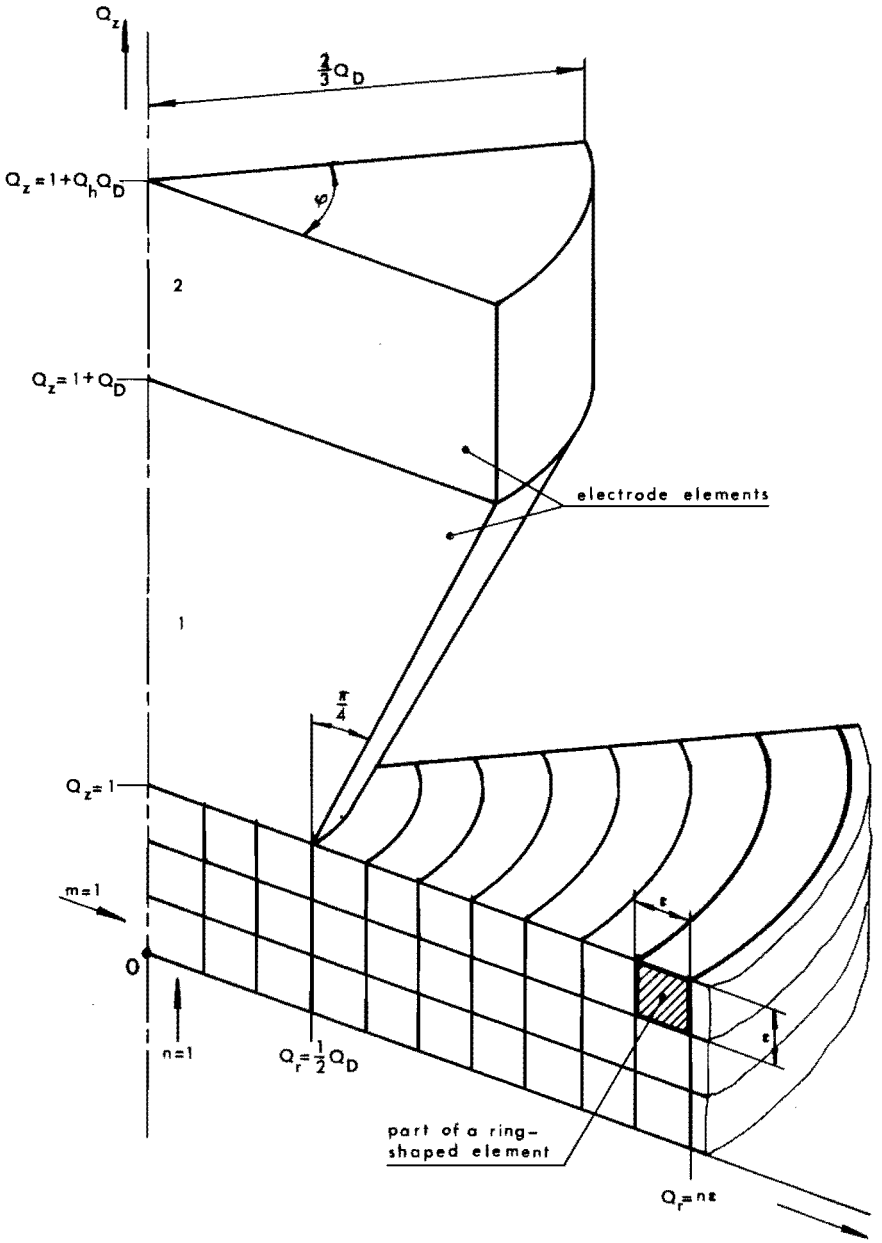


Fig. 2.4. Division of the Workpiece and the Electrode in Volume Elements, drawn for the case $Q_D = 2$

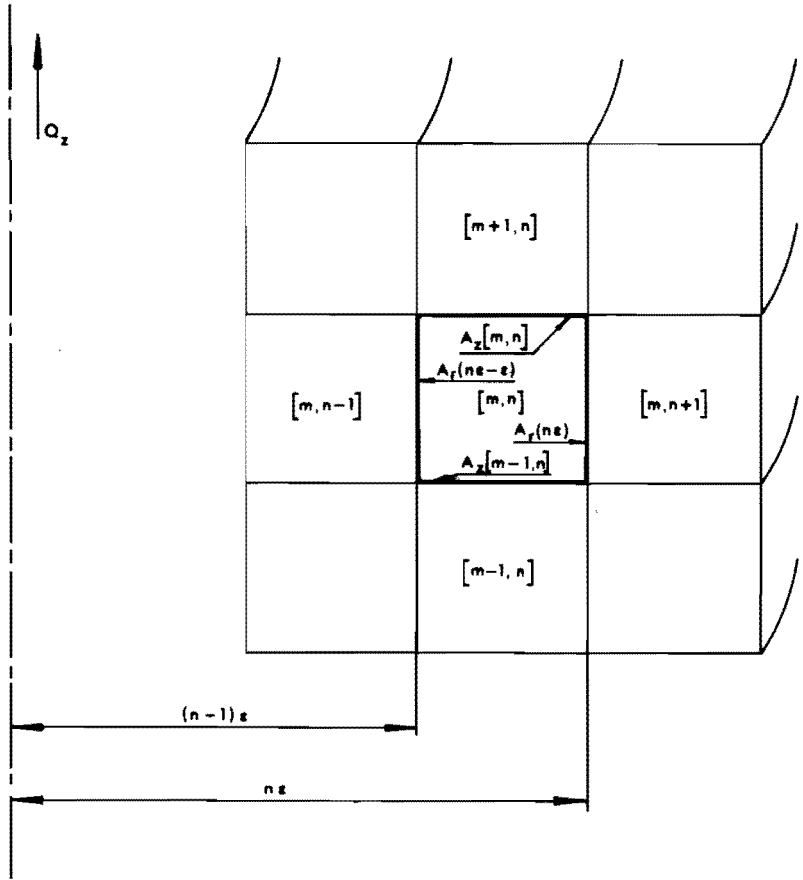


Fig. 2.5. Position of the Element $[m, n]$ amid its neighbouring Elements.
Nomenclature of the bounding surfaces

$$\iiint_{V[m, n]} \frac{\partial Q_\theta}{\partial Q_t} [m, n] dV = \frac{\partial Q_\theta}{\partial Q_t} [m, n] \cdot \frac{1}{2} (2n - 1) \phi \epsilon^3 \quad (2.13)$$

To the second term Gauss' theorem is applied

$$\iiint_{V[m, n]} \left\{ \frac{\partial^2 Q_\theta}{\partial Q_z^2} + \frac{\partial^2 Q_\theta}{\partial Q_r^2} + \frac{1}{Q_r} \frac{\partial Q_\theta}{\partial Q_r} \right\} dV =$$

$$\begin{aligned}
&= \iint_{A_Z} \frac{\partial Q_\theta}{\partial Q_Z} d A_Z + \iint_{A_R} \frac{\partial Q_\theta}{\partial Q_R} d A_R = \\
&= \left\{ \frac{\partial Q_\theta}{\partial Q_Z} [m, n] - \frac{\partial Q_\theta}{\partial Q_Z} [m-1, n] \right\} \cdot \frac{1}{2} (2n - 1) \phi \varepsilon^2 + \\
&+ \left\{ \frac{\partial Q_\theta}{\partial \log Q_R} [m, n] - \frac{\partial Q_\theta}{\partial \log Q_R} [m, n-1] \right\} \cdot \phi \varepsilon
\end{aligned} \tag{2.14}$$

This term is linearised by means of

$$\frac{\partial Q_\theta}{\partial Q_Z} [m, n] = \frac{1}{\varepsilon} (Q_\theta [m+1, n] - Q_\theta [m, n]) \tag{2.15}$$

and

$$\frac{\partial Q_\theta}{\partial \log Q_R} [m, n] = \frac{Q_\theta [m, n+1] - Q_\theta [m, n]}{\log (n+\frac{1}{2}) - \log (n-\frac{1}{2})} \tag{2.16}$$

According to equation (2.9) the third term becomes

$$\iiint_{V[m, n]} G(Q_R) dV = \frac{1}{2} (2n - 1) \phi \varepsilon^3 G(Q_R) \tag{2.17}$$

$$\text{where } \left. \begin{aligned} G(Q_R) &= 1 \quad \text{for } Q_R \leq \frac{Q_D}{2} \\ G(Q_R) &= 0 \quad \text{for } Q_R > \frac{Q_D}{2} \end{aligned} \right\} \tag{2.18}$$

Eventually, equation (2.6) transforms into ¹⁾

$$\begin{aligned}
 (2n - 1) \frac{\partial Q_{\theta}}{\partial t} [m, n] &= \varepsilon^{-2} (2n - 1) (Q_{\theta} [m+1, n] - Q_{\theta} [m, n]) + \\
 &+ \varepsilon^{-2} (2n - 1) (Q_{\theta} [\bar{m}-1, n] - Q_{\theta} [\bar{m}, n]) + \\
 &+ 2\varepsilon^{-2} \log^{-1} \left(\frac{2n+1}{2n-1} \right) (Q_{\theta} [m, n+1] - Q_{\theta} [m, n]) + \\
 &+ 2\varepsilon^{-2} \log^{-1} \left(\frac{2n-1}{2n-3} \right) (Q_{\theta} [\bar{m}, n-1] - Q_{\theta} [\bar{m}, n]) + \\
 &+ (2n - 1) G(Q_r)
 \end{aligned} \tag{2.19}$$

It is observed that the angular coordinate ϕ disappears from the formula.

Next, the nodal point $[m, n]$ of the RC-network of fig. 2.6 is considered. The application of Kirchhoff's first law to this point yields

$$\begin{aligned}
 C [m, n] \frac{dU}{dt} [m, n] &= \frac{1}{R_z [m, n]} (U [m+1, n] - U [m, n]) + \\
 &+ \frac{1}{R_z [\bar{m}-1, n]} (U [\bar{m}-1, n] - U [\bar{m}, n]) + \\
 &+ \frac{1}{R_r [m, n]} (U [m, n+1] - U [m, n]) + \\
 &+ \frac{1}{R_r [\bar{m}, n-1]} (U [\bar{m}, n-1] - U [\bar{m}, n]) + \\
 &+ I [m, n]
 \end{aligned} \tag{2.20}$$

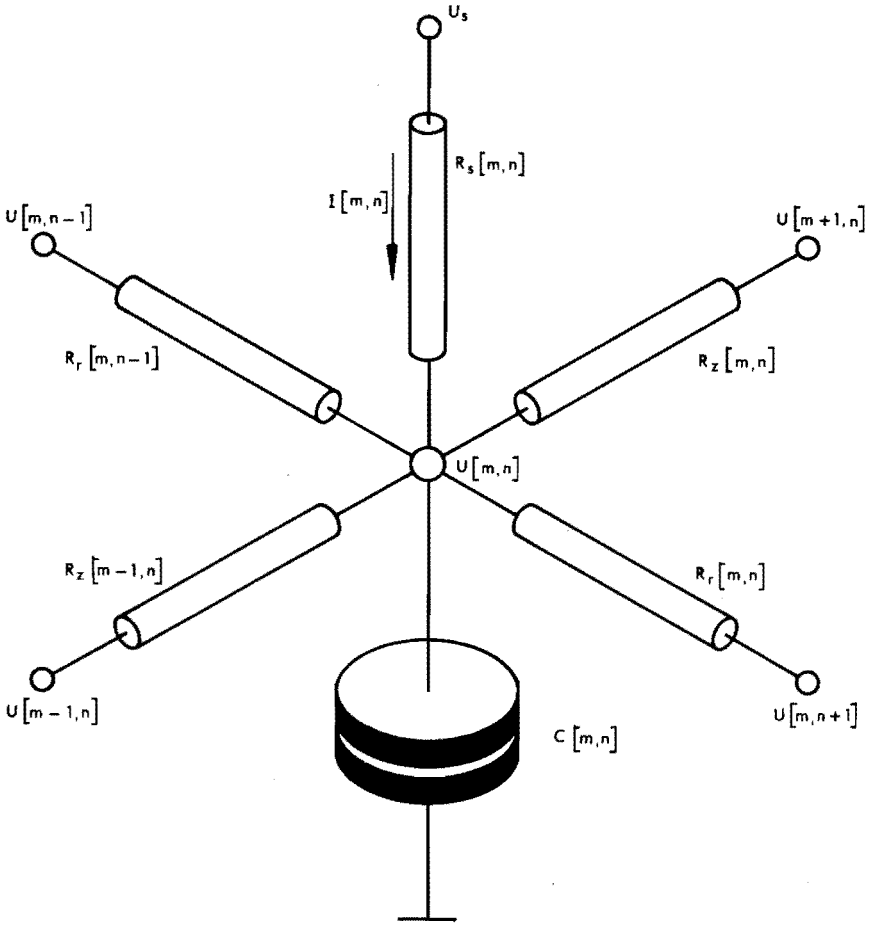


Fig. 2.6. Analogue Network Element $[m,n]$

If $U[m,n] \ll U_s$ then for $I[m,n]$ can be written

$$I[m,n] = \frac{U_s}{R_s[m,n]} \quad (2.21)$$

By introducing the basic resistor R_0 and capacitor C_0 as arbitrary units and by defining the dimensionless products

$$Y_U[m, n] = \frac{U[m, n]}{U_s} \quad \text{and} \quad Y_t = \frac{t_m}{R_o C_o} \quad (2.22)$$

equation (2.20) can be written

$$\begin{aligned} \frac{C[m, n]}{C_o} \frac{dY_U[m, n]}{dY_t} &= \frac{R_o}{R_z[m, n]} (Y_U[m+1, n] - Y_U[m, n]) + \\ &+ \frac{R_o}{R_z[m-1, n]} (Y_U[m-1, n] - Y_U[m, n]) + \\ &+ \frac{R_o}{R_r[m, n]} (Y_U[m, n+1] - Y_U[m, n]) + \\ &+ \frac{R_o}{R_r[m, n-1]} (Y_U[m, n-1] - Y_U[m, n]) + \\ &+ \frac{R_o}{R_s[m, n]} \end{aligned} \quad (2.23)$$

Comparison of the equations (2.19) and (2.23) shows that both relations are homologue if

$$\frac{C[m, n]}{C_o} = 2n - 1 \quad (2.24)$$

$$\frac{R_z[m, n]}{R_o} = \frac{10^{-2}}{2n - 1} \quad (2.25)$$

$$\frac{R_r[m,n]}{R_o} = \frac{10^{-2}}{2} \log \left(\frac{2n+1}{2n-1} \right) \quad (2.26)$$

$$\frac{R_s[m,n]}{R_o} = \frac{1}{2n-1} \cdot \frac{1}{G(Q_r)} \quad (2.27)$$

$$Q_u = 10^2 \epsilon^2 Y_u \quad (2.28)$$

$$Q_t = 10^2 \epsilon^2 Y_t \quad (2.29)$$

where C_o and R_o may still be given any value. The factor 10^2 is added in order to obtain that

$$R_s[m,n] = 10^2 \cdot R_z[m,n]$$

which ensures the validity of relation (2.21).

An electric network representing the geometric arrangement of fig. 2.4 can now be designed. The set-up of the complete analogue is shown in fig. 2.7. The inner part of the sheet is divided in forty-five elements arranged in three rows of fifteen elements. The corresponding nodal points represent the centres of the volume elements. From the number of rows it follows that $\epsilon = \frac{1}{3}$. The outer part of the sheet is divided in coarser elements 16, 17 and 18, the centres of which lie at distances of 19.3ϵ , 43.0ϵ and 102.7ϵ from the symmetry axis respectively. The electrode is divided in only two elements, 1 and 2.

The value of Q_D is varied by connecting the electrode network to the required number of nodal points of the fourth row of the workpiece network, by applying the supply voltage U_s to the appropriate points and by adjusting the values of the electrode network components. These values are determined in dependence on the electrode dimensions, expressed in multiples of ϵ , and the variables Q_c , Q_λ and Q_p by dealing with the differential equation

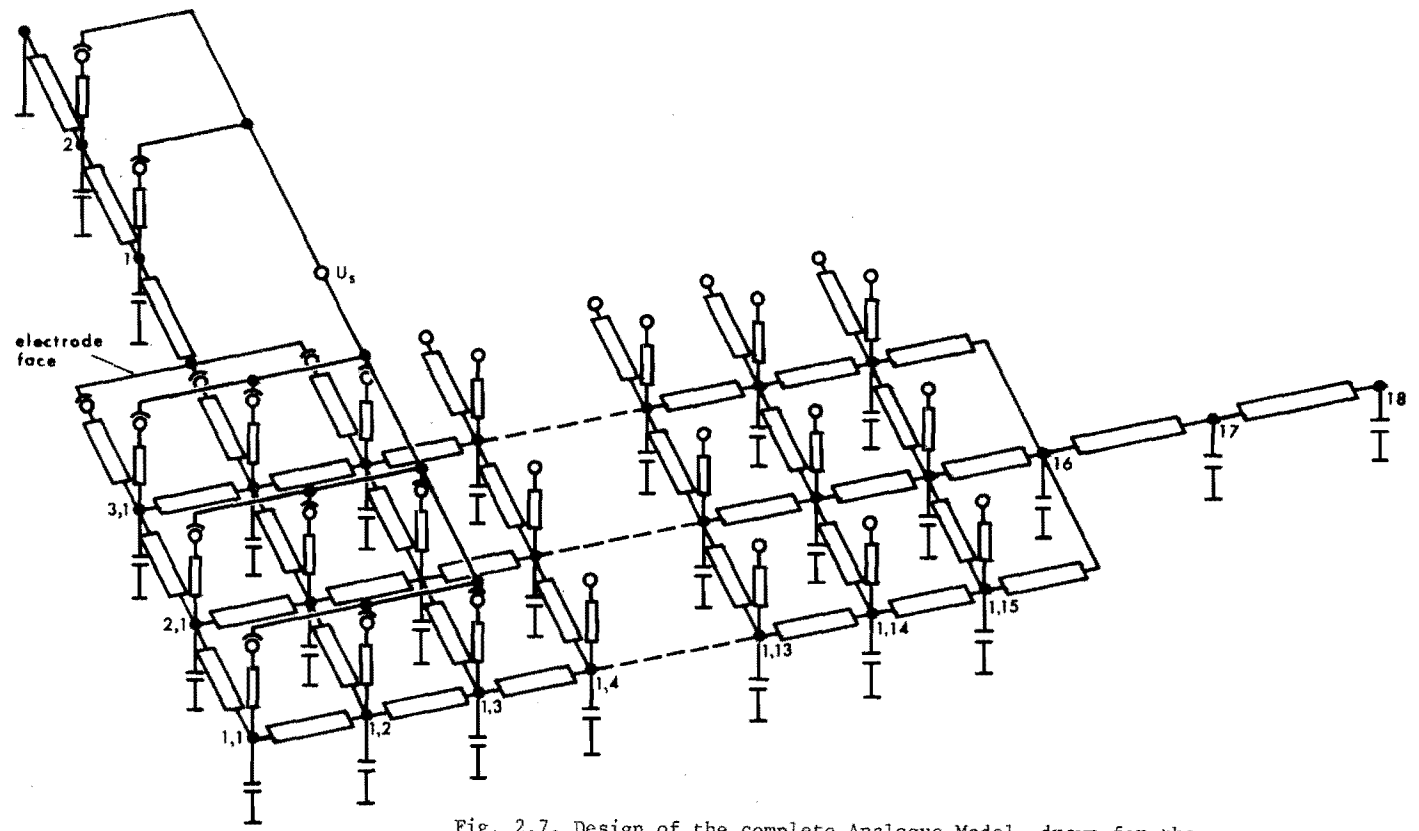


Fig. 2.7. Design of the complete Analogue Model, drawn for the case $Q_D = 2$

$$Q_c \frac{\partial Q_\theta}{\partial Q_t} = Q_\lambda \frac{\partial^2 Q_\theta}{\partial Q_z^2} + Q_\rho \quad (2,30)$$

in the same way as with (2.6).

If $C_o = C[m,1] = 10^{-6}$ F and $R_o = R_s[m,1] = 10^6 \Omega$,

and t_m is expressed in seconds, it can be concluded from equation (2.22) that the numerical values of Y_t and t_m are equal.

1) Division of both members of equation (2.19) by a factor $(2n - 1)$ would simplify the set-up of the model. In doing so, $C[m,n]$ in equation (2.24) would acquire the same value for all nodal points. The same applies to $R_z[m,n]$ and $I[m,n]$. This fact became plain after the model network had been built. However, it does not change the results of the measurements.

2.3. Analogue Measurements

2.3.1. Design of the Measurements

With the aid of the analogue described in the foregoing sections the dependence of the potential Q_θ on Q_t for a few selected points of the weld can be established. These points are the centre of the weld C ($Q_z = 0, Q_r = 0$), where temperatures are generally maximum, the border of the weld nugget B ($Q_z = 0, Q_r = \frac{1}{2}Q_D$), where the temperature just reaches the melting point, and the electrode face E ($Q_z = 1, Q_r < \frac{1}{2}Q_D$), the temperature of which determines electrode life [31].

The six dimensionless products defined in (2.8) are to be considered independent parameters for these measurements. However, in order to limit the number of variables the shape and the geometric proportions of the electrode are not varied. Thus Q_h is kept constant to 1.5. This value is relatively low compared with

standard practice [43], but as shown in [44] and [45] a thin wall between electrode face and coolant channel substantially reduces electrode wear. As indicated in section 1.3, a flat-faced electrode is used with a 45 deg truncated cone in order to control adequately the size of the electrode-workpiece contact area during welding.

As contact resistances are neglected in this stage of the investigation, the influence of the product Q_p is left out of consideration.

From the Wiedemann-Franz-Lorenz law

$$\rho(\theta) \cdot \lambda(\theta) = L \cdot \theta \quad (2.31)$$

where L is a constant which is practically independent of the material choice and θ the absolute temperature, it follows that

$$Q_p = Q_\lambda^{-1} \quad (2.32)$$

The three remaining parameters are varied numerically in such a way that most of the usual machine settings or material properties are covered, viz.

$$Q_c = 1 \text{ and } 2,$$

$$Q_\lambda = Q_p^{-1} = 1, 3 \text{ and } 9,$$

$$Q_d = \frac{2}{3}, 2, 4 \text{ and } 8.$$

In this way continuous curves can be drawn showing the relation $Q_\theta(Q_t)$ for each combination of parameter values and for each of the three points defined earlier in this section. Fundamentally, Q_t varies from zero to infinity, although only the interval $0.1 < Q_t < 10$ is of interest in practical cases.

2.3.2. Results of the Analogue Measurements

The measurements were carried out by applying the voltage U_s to the network for a well-defined time lapse and by recording the potentials of the chosen points simultaneously on a multi-channel

recording oscillograph. Fig. 2.8 shows the analogue and the measuring devices. As a matter of course, any current shape can be simulated by means of the form of the function $U_s(t_m)$ instead of the direct welding current used in the present work.

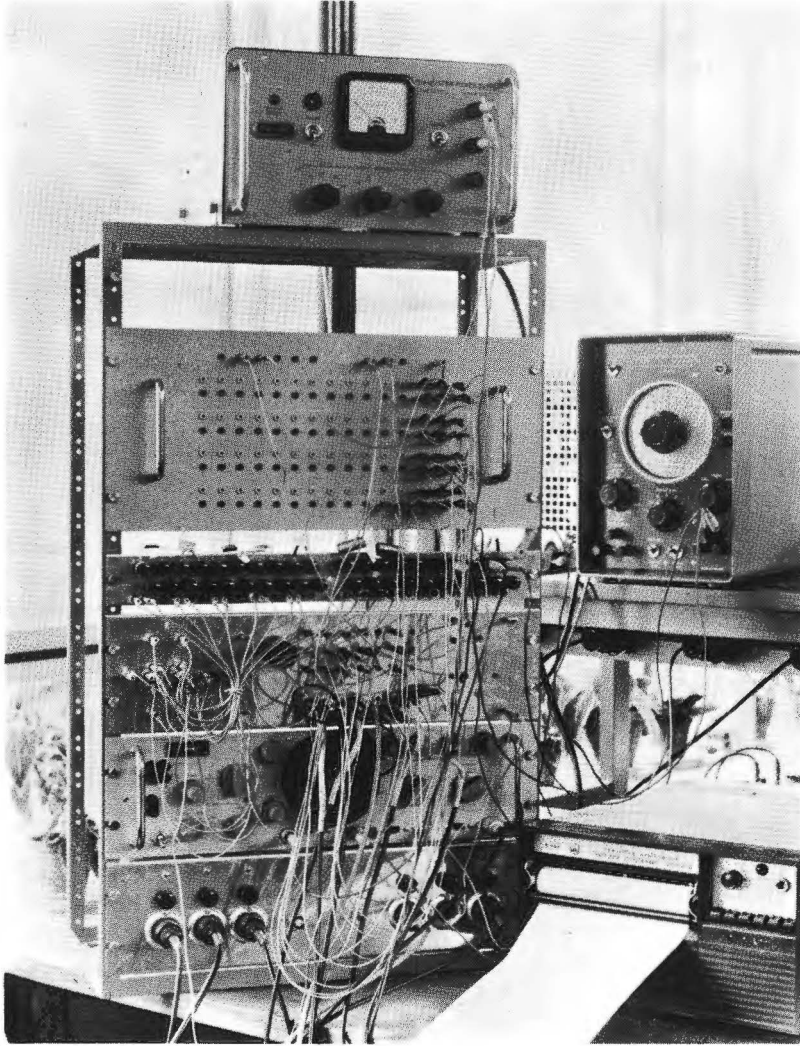


Fig. 2.8. View of the Analogue and the Measuring Devices. In the centre from top to bottom, Voltage Supply, Sheet Network, Electrode Network with interchangeable Components, Switch Panel, Oscilloscope and 6-channel Recorder Pre-amplifier. To the right, Time Switch and Galvanometer Recorder

As an example, some of the heating curves obtained in this way are shown in fig. 2.9 for the centre of the weld. As can be concluded from equation (2.6) the derivative $\partial Q_\theta / \partial Q_t$ approaches 1 for small values of Q_t , since $\nabla^2 \rho_\theta = 0$ initially. From the measurements it appears that ρ_c has no perceptible influence on the course of the

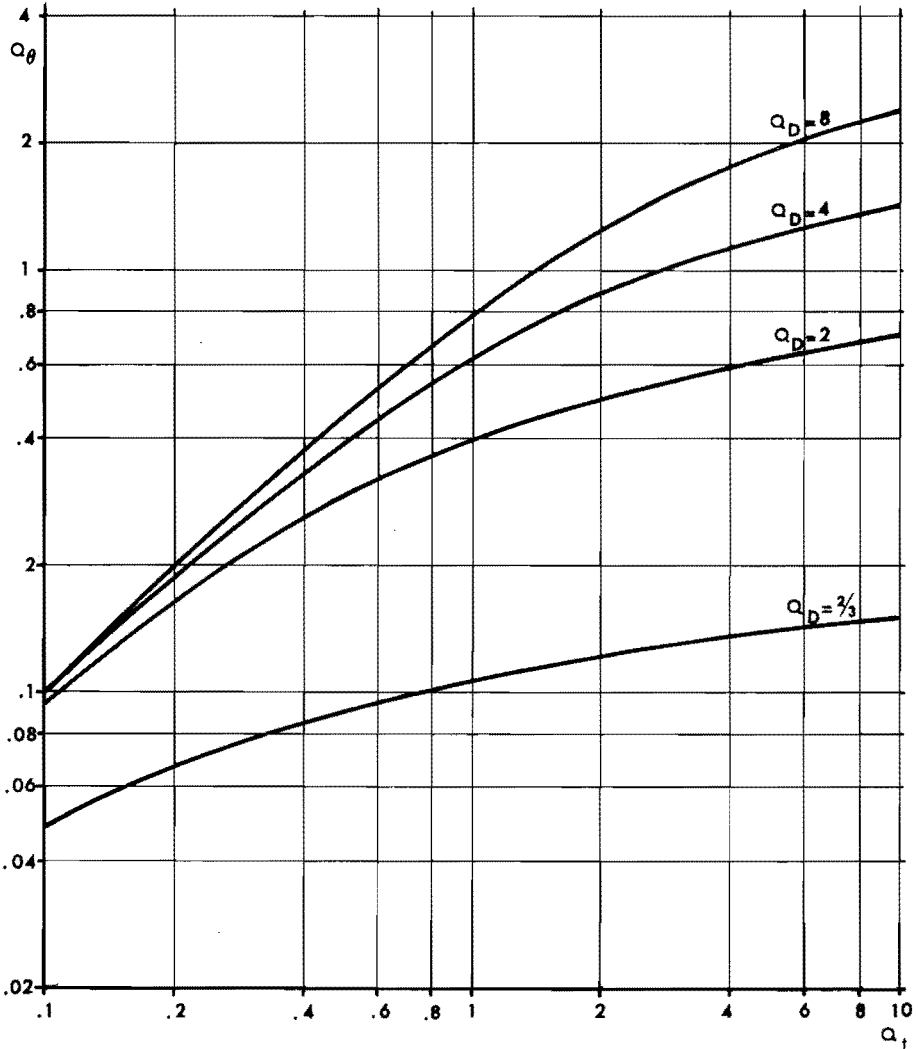


Fig. 2.9. Q_θ as a function of Q_t for different values of Q_D
(Centre of the Weld, $Q_\lambda = 1$)

curves. On the other hand, the product Q_λ considerably affects the value of Q_θ . Its influence is greater according as Q_D and Q_t increase, as is illustrated by fig. 2.10.

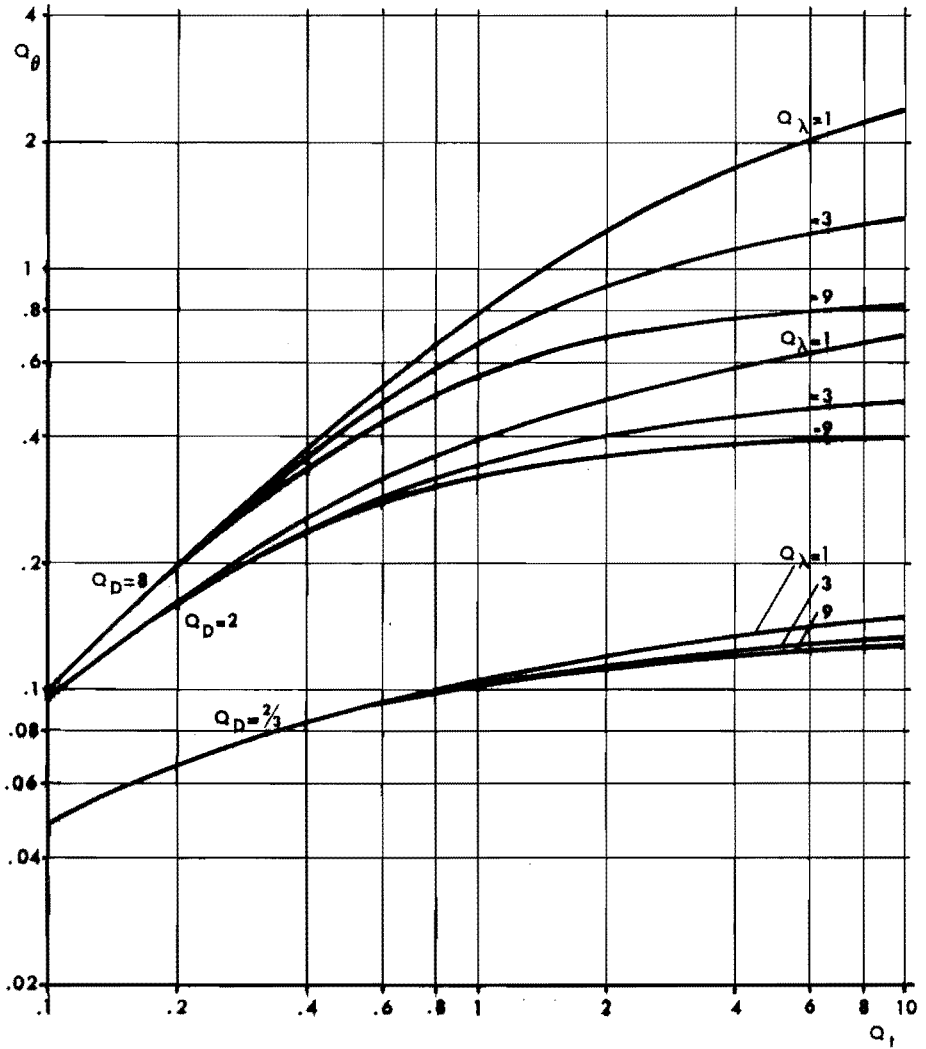


Fig. 2.10. The Influence of Q_λ on the Function $Q_\theta(Q_t)$ for some values of Q_D (Centre of the Weld)

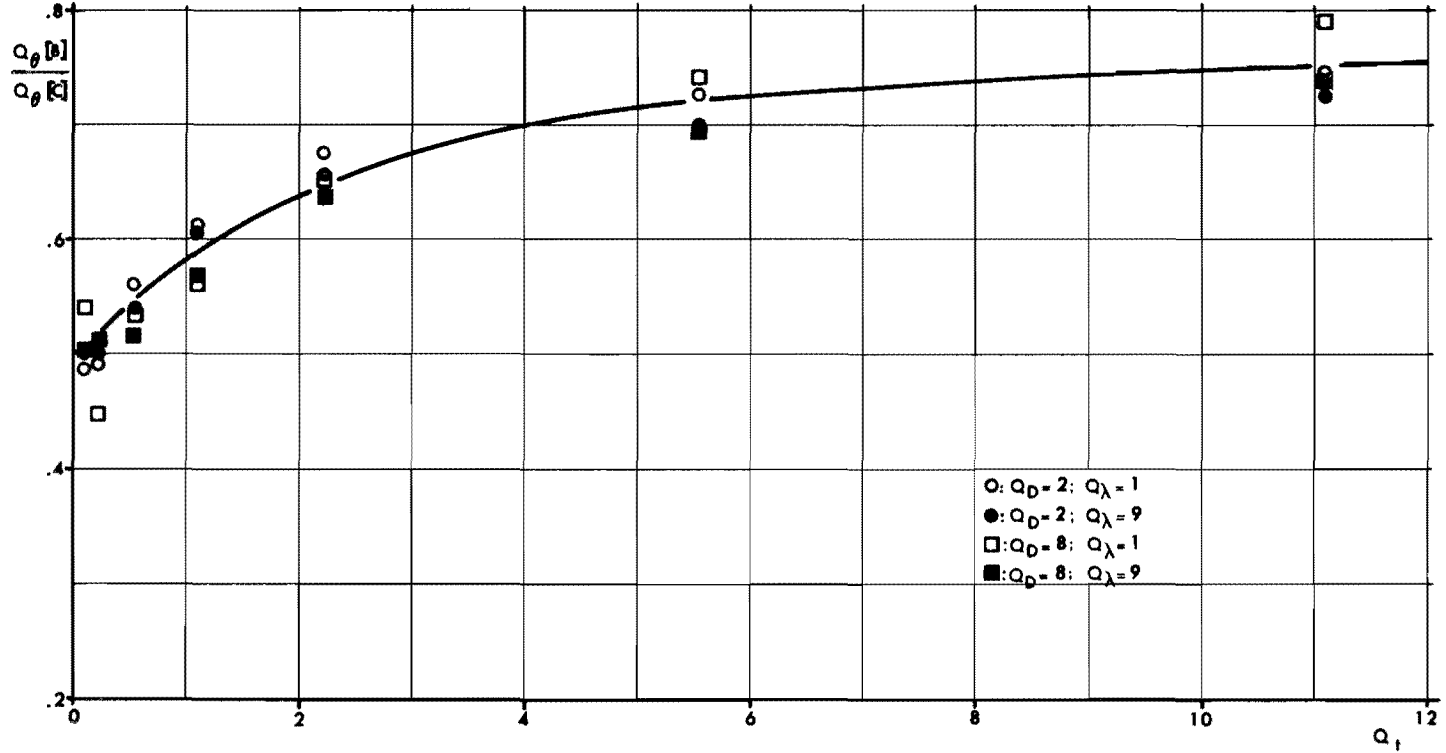


Fig. 2.11. The ratio of the Q_θ values at the Nugget Border B and in the Centre of the Weld C in dependence on Q_t

The ratio of the Q_θ values at the nugget border B and in the centre of the weld C seems to be dependent on Q_t only, as demonstrated in fig. 2.11. This ratio is $\frac{1}{2}$ for small Q_t and approaches a constant value of $\frac{3}{4}$ for $Q_t > 5$. Since the relative deviations from the curve are generally less than five per cent., it is sufficiently accurate for technical applications.

If it is desired that the weld nugget diameter should become equal to that of the electrode, the temperature at the nugget border must reach the melting point of the welded material. In this case the electrode face temperature is determined by the ratios graphically shown in figs. 2.12 to 2.14 inclusive. From these graphs the importance of a high Q_λ value, i.e. of thermally well conducting electrode material is evident. For example, when welding copper sheet, it can be seen from fig. 2.12 that the copper electrodes can only be prevented from being welded to the workpieces by choosing low Q_D and high Q_t values. On the other hand, the welding of stainless steel, where $Q_\lambda \approx 8$, will offer no problems as is known from practice.

Summarising it can be concluded that Q_D is of major importance to the welding process, especially for $Q_t > 0,1$; Q_λ is important for $Q_t > 1$, and Q_c has no influence on the process.

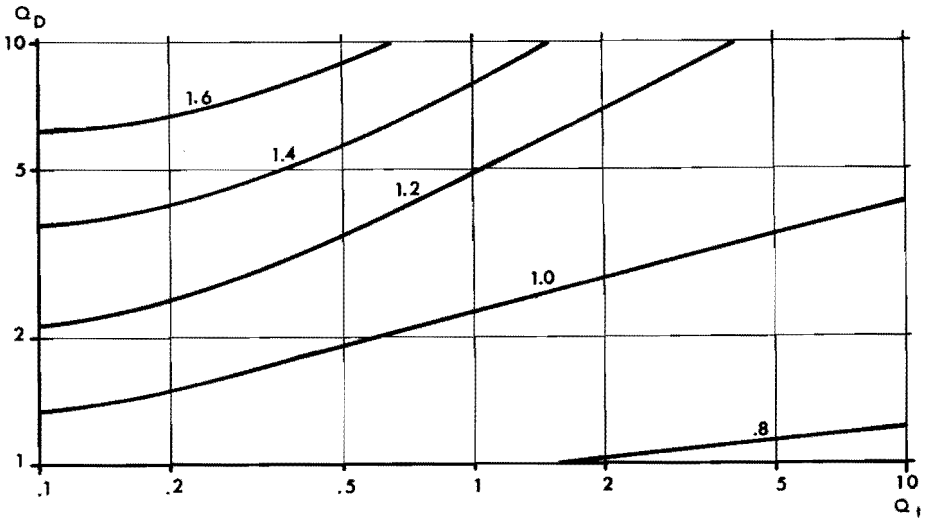


Fig. 2.13. The ratio of the Q_θ values at the Electrode Face and at the Nugget Border for $Q_\lambda = 3$

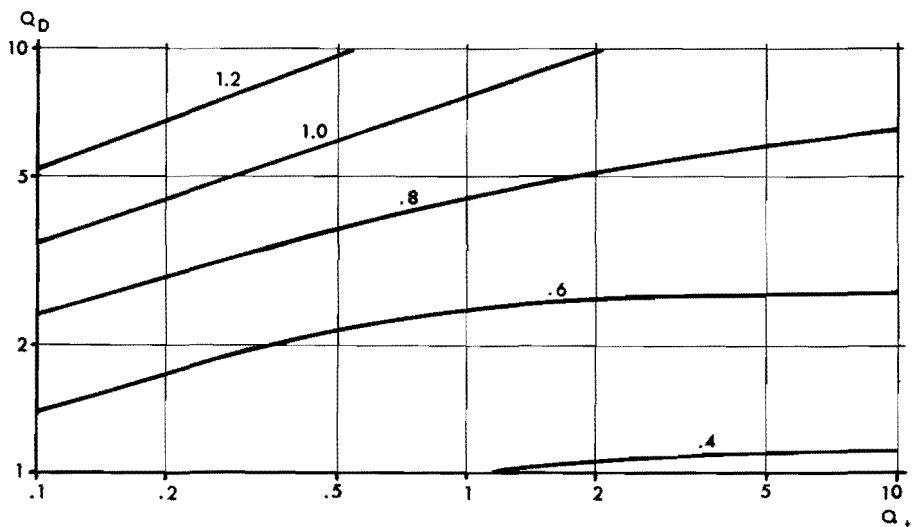


Fig. 2.14. The ratio of the Q_θ values at the Electrode Face and at the Nugget Border for $O_\lambda = 9$

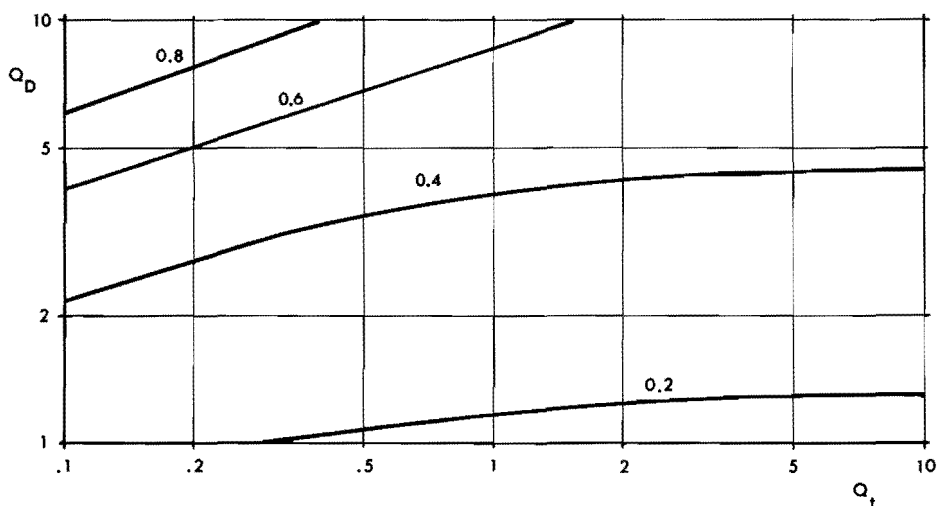


Fig. 2.12. The ratio of the Q_θ values at the Electrode Face and at the Nugget Border for $O_\lambda = 1$

Chapter 3. EXPERIMENTAL VERIFICATION

3.1. Verification Method

As pointed out in section 1.2 the weld temperature can only be determined accurately after welding in those places where it just reached the melting point during the process, viz. at the bounding surface between weld nugget and surrounding metal. This boundary is easily perceptible after shearing the weld as is illustrated for different materials in fig. 3.1.

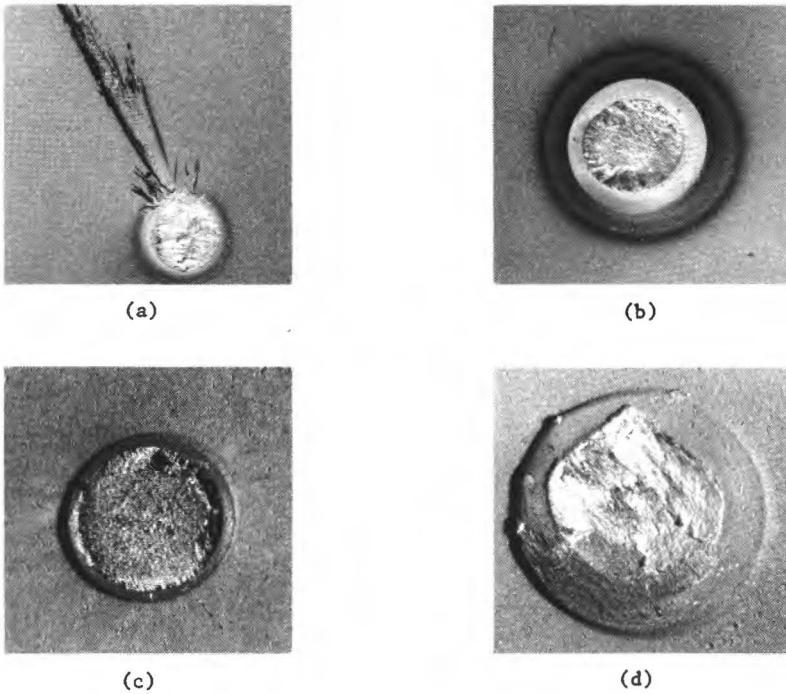


Fig. 3.1. Test Specimens after Shearing

- (a) stainless steel
- (b) low carbon steel
- (c) zinc
- (d) aluminium

The fundamental procedure in verifying the results of chapter 2 is as follows. First, for a given material and geometry a value of the welding time t is chosen. By means of an adequate graph of the type of fig. 2.9 valid for the border of the weld nugget the value of the current i , required to make this border just reach the melting point, is calculated. Then, a set of about five welds is made with the same heating time t and with a number of different current intensities, starting with the computed value. In the following welds the current is adjusted either to higher values if the first proved to be too low or to lower values in the opposite case. The current setting is judged to be right if the diameter of the nugget D_N , measured after shearing the weld, does not deviate more than five per cent. from the electrode diameter D_E . This is necessary in order that the assumption $\theta = \theta_m$ at the nugget border holds. When the current intensity is too high molten material frequently splashes from between the workpieces before the heating time is over. In these cases, the time at which splashing occurs is considered to be the right welding time for the current setting used.

In this way a number of i, t combinations is found for constant values of Q_D and Q_λ , from which Q_θ and Q_t values are computed by putting $\theta = \theta_m$ in Q_θ .

3.2. Design of the Experiments

3.2.1. Workpieces

In order to verify the analogue results for a wide range of applications, workpiece materials with highly divergent physical properties are chosen. Thus, for instance, low carbon steel with a high melting point is compared with zinc having a very low one, highly resistive stainless steel is compared with copper, which has a very good thermal and electrical conductivity. Aluminium is added to this set because of its well-known property to form an insulating oxyde layer on its surface when exposed to air.

The materials used are

SS, an austenitic chromium-nickel stainless steel, AISI number 316, composition $\leq 0.05\%$ C; 17 - 18.5% Cr; 10.5 - 11.5% Ni; 2.0 - 2.3% Mo,

St, a commercial low carbon steel, $\leq 0.06\%$ C; 0.38% Mn; 0.01% Si,

Zn, a commercial hot rolled zinc, $\leq 0.10\%$ Pb,

Al, commercial pure aluminium, ASTM designation 1100-H18, $\leq 99.2\%$ Al,

Cu, electrolytic copper, annealed, $\geq 99.92\%$ Cu

The physical properties of these materials are given in table 3.1.

Table 3.1. Physical Properties of Workpiece Materials

material	λ W.m ⁻¹ .deg ⁻¹	c J.m ⁻³ .deg ⁻¹	ρ Ω.m	θ_m deg	ref.	H_V N.m ⁻²	σ_M N.m ⁻²
SS	23	4.90	108	1375	[46]	171	61.4
St	36.2	5.37	84.5	1480	[46]	119	38.8
Zn	104	2.78	11.1	393	[47]	58	14.1
Al	199	2.88	6.9	630	[48]	37	10.8
Cu	360	2.88 $\times 10^6$	5.6 $\times 10^{-8}$	1056	[48]	89 $\times 10^7$	25.8 $\times 10^7$

The mechanical properties H_V and σ_M were measured at room temperature; the thermal and electrical properties were taken from literature as functions of the temperature and averaged by means of the relation

$$k = \frac{1}{\theta_m} \int_0^{\theta_m} k(\theta) d\theta \quad (3.1)$$

where $k(\theta)$ denotes any of the properties c , ρ or λ , and k its mean value of table 3.1. Generally, this definition gives satisfactory results when computing the dimensionless products Q . However, from the results of the experiments described in section

3.4 and discussed in chapter 4 it appears that the choice of slightly deviating values for the electric resistivity ρ improves the agreement between theory and experiments. These values, given in table 3.2, are further used throughout the present calculations.

Table 3.2. Comparison between Calculated and Empirical Values for the Electrical Resistivity ρ in $10^{-8}\Omega.m$

material	calculated from equation (3.1)	empirical (best fitting) value
SS	108	74
St	84.5	61
Zn	11.1	9.5
Al	6.9	9.5
Cu	5.6	6.8

Rectangular workpiece specimens were used with width

$$w = 6 D_{E_{max}} \quad (3.2)$$

in accordance with section 2.2.2 and length

$$\left. \begin{array}{l} l \geq 2.w \\ l \geq 60 \text{ mm} \end{array} \right\} \quad (3.3)$$

where $D_{E_{max}}$ denotes the maximum electrode diameter to be used on the specimen. The minimum length of 60 mm is maintained to facilitate the pinching of the specimens in the tensile testing machine. When welding, the specimens overlap each other over a distance $w_L = w$; the weld is made in the middle of the common contact square, according to [4].

To minimize the influence of contact resistances, caused by the presence of oxide films, grease or dirt, the specimens are sand-

blasted and oiled afterwards. The oil is removed by means of an adequate organic cleaning agent (trichloroethylene) immediately before welding.

3.2.2. Electrodes

The electrode materials are chosen according to the specifications given by the manufacturer of the welding machine [49]. These specifications are based on the Resistance Welder Manufacturer's Association standards [4]. For the welding of copper sheet electrodes made of the same material were used. A description of the electrode materials is given in table 3.3; the physical properties at room temperature can be found in table 3.4.

Table 3.3. Description of the Electrode Materials

manufacturer's designation	composition	RWMA class	used for the welding of
electrolytic copper	99.97% Cu	-	Cu
Soudalox 100	1% Ag; bal. Cu	1	Al, Zn
Soudalox 200	.5% Cr; .1% Be; bal. Cu	2	St
Soudalox 300	2.5% Co; .5% Be; bal. Cu	3	SS

Table 3.4. Physical Properties of the Electrode Materials

material	λ_E W.m ⁻¹ .deg ⁻¹	c_E J.m ⁻³ .deg ⁻¹	ρ_E Ω.m	$\theta_{max}^1)$ deg	H_V N.m ⁻²
el.copper	402	2.5	1.75	200	94
Soud. 100	320	2.5	2.1	320	99-124
Soud. 200	290	2.5	2.45	470	153-181
Soud. 300	180	2.5	3.6	520	208-245
		$\times 10^6$	$\times 10^{-8}$		$\times 10^7$

¹⁾ θ_{max} = maximum operating temperature

The electrode dimensions are as defined in fig. 2.4, except that the shaft diameter does not exceed 20 mm, whereas the coolant channel has a diameter of 12 mm and a short conical end-surface for all types (cf. fig. 1.1).

3.2.3. The Experimental Range

An inspection of standard welding practices [1] reveals that the values of Q_t generally lie in the range $0.1 < Q_t < 10$ as indicated in section 2.3.1. This fact is quite comprehensible because for very low values of Q_t the large welding current required will soon exceed the capacity of the welding equipment. For large Q_t values, on the other hand, an increase in the welding time would not yield an appreciable increase in the weld temperature, as can be seen from figs. 2.9 or 2.10. Consequently, the present experiments are confined to the above-mentioned range of Q_t . Then, the expected Q_θ values follow from the analogue measurements. They lie in the range $0.01 < Q_\theta < 1$.

As for Q_D , most standards recommend a certain dependence of the "optimum" electrode diameter on the sheet thickness to be welded. In Europe, the relation

$$D_E = 5 \sqrt{s} \quad (3.4)$$

is used for steel, where D_E and s are expressed in mm [7, 49], whereas in the United States the formula

$$D_E = 2.s + 0.1 \quad (3.5)$$

is applied, where D_E and s are expressed in inches [4]. For $0.3 < s < 5$ mm the resultant electrode diameter is about the same. In both cases Q_D has a value as low as 1.5 for sufficiently thick sheets and as high as 20 or more for very thin sheets. Such a choice of the electrode diameter does not necessarily have a physical background. It might as well be made for practical reasons, for instance in order to enlarge the working range of

the welding equipment. This range is limited both by the ratio of maximum to minimum welding current and by the ratio of maximum to minimum electrode force that can be applied. So a small range of electrode diameters and hence of current intensities and electrode forces is attractive.

Because of the availability of a welding machine with a large range of current and force settings, the relation (3.4) and (3.5) were disregarded and a number of Q_D values was investigated for each sheet gauge. The applied combinations of s and D_E are summarised in table 3.5. The underlined experiments have been carried out twice.

In order to minimise the initial values of the contact resistance, the electrode force is chosen so that the dimensionless product

$$Q_F = \frac{4F}{\pi D_E^2 H_V} = 0.2 \quad (3.6)$$

which means that the average contact pressure between workpiece and electrode lies well above the yield stress of the material. In this way the occurrence of plastic deformations in the contact areas and hence of small initial contact resistances is ensured [36].

For each combination of D_E and s from table 3.5 five welding times were computed in such a way that Q_t obtained values of 0.1, 0.3, 1, 3 and 10 approximately. For each welding time a set of five measurements was carried out as described in section 3.1, as far as the current and welding time settings could be realised with the equipment used. After a set the electrodes were carefully cleaned by grinding or polishing. In this way a number of 1070 welds was made.

As pointed out in section 1.2 it is a further aim of the present work to consider the possibilities of quality control and adaptive control. In order to determine the static strength of the weld the tensile-shear force F_g was recorded [4]. The appearance of the weld was judged by means of the maximum electrode indentation

Table 3.5. Investigated Combination of Sheet Thickness and Electrode Diameter. Values of Q_λ and Q_D

	$Q_D =$	1	1.25	1.5	2	2.5	3	4	5	6	8	10	12	16
SS $Q_\lambda = 7.8$	s and D_E in mm s = 4 $D_E =$ 2 1 0.5	4	5	6 3	4	2.5	6 3	4	2.5	6 3	4	5	6	
St $Q_\lambda = 8.0$	s = 4 $D_E =$ 2 1 0.5	4	5 2.5	6 3	4	5 2.5	3	8 4	5	6 3	8 4	5	6	8
Zn $Q_\lambda = 3.1$	s = 1.5 $D_E =$ 0.8					3.75	4.5		7.5 4	4.8	6.4	8		
Al $Q_\lambda = 1.6$	s = 4 $D_E =$ 2 1 0.5			6	<u>8</u>	<u>10</u>	<u>6</u>	<u>8</u>	<u>10</u>	6	<u>8</u>		6	
Cu $Q_\lambda = 1.1$	s = 3 D $D_E =$ 1 0.5				6			4	5		4			

d_1 (cf. section 6.1). For the purpose of adaptive control the electrode potential drop U across the electrodes and the electrode displacement d during welding were recorded (cf. section 6.2). Besides, the potential drop U can be used to verify the resistance of the weld material, whereas the actual welding time can be derived from the variation of d .

3.3. Experimental Equipment

3.3.1. The Welding Machine

The welding machine is a single phase press welder SCIAKY type E 260, accomodated for spot welding by means of a special electrode die set mounted on the platens of the machine. It is equipped with a heavy transformer SCIAKY type TI 732 C having a rated power of 340 kVA at 50% and a maximum of 650 kVA at 9% duty cycle. The secondary e.m.f. can be set at 5.7 or 11.4 volts, the maximum secondary short-circuit current being 68 kA. In practice, with the electrode die set mounted, the secondary current intensity can be controlled up to 54 kA and by means of an electronic synchronous phase shift control down to a minimum value of about 2 kA. Continuous heating times can be realised from 0.02 up to 4 seconds in steps of 0.02 s, whereas a current modulator allows of numerous possibilities arise as regards pulsation welding. The moving head of the machine is operated by direct acting air pressure, governed by the electronic control unit. The maximum adjustable electrode force is 15 kN. A minimum value of about 1.5 kN is caused by the action of static packing friction in the air cylinder resulting in insufficient pressure during the weakening of the workpiece.

The welding machine, the electronic control unit and the measuring devices are shown in fig. 3.2. In fig. 3.3 a closer view is given of the electrode arrangement and some of the measuring transducers.

3.3.2. Measuring Devices

A number of devices were used to measure the values of the rele-

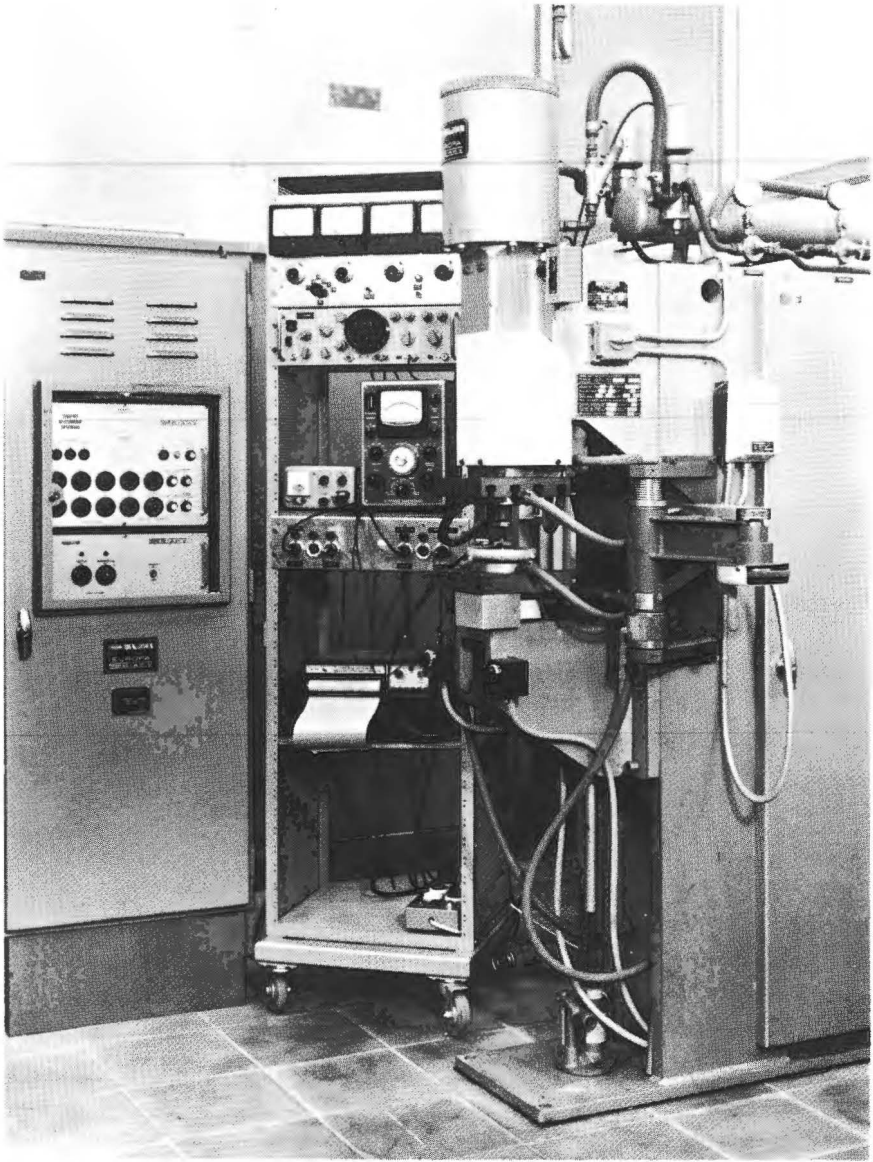


Fig. 3.2. The Experimental Equipment. From left to right, welding control unit, instruments rack, press welder. In the rack from top to bottom, r.m.s. ammeter unit, oscilloscope, displacement transducer power source and strain indicator, recorder pre-amplifier, recording oscillograph

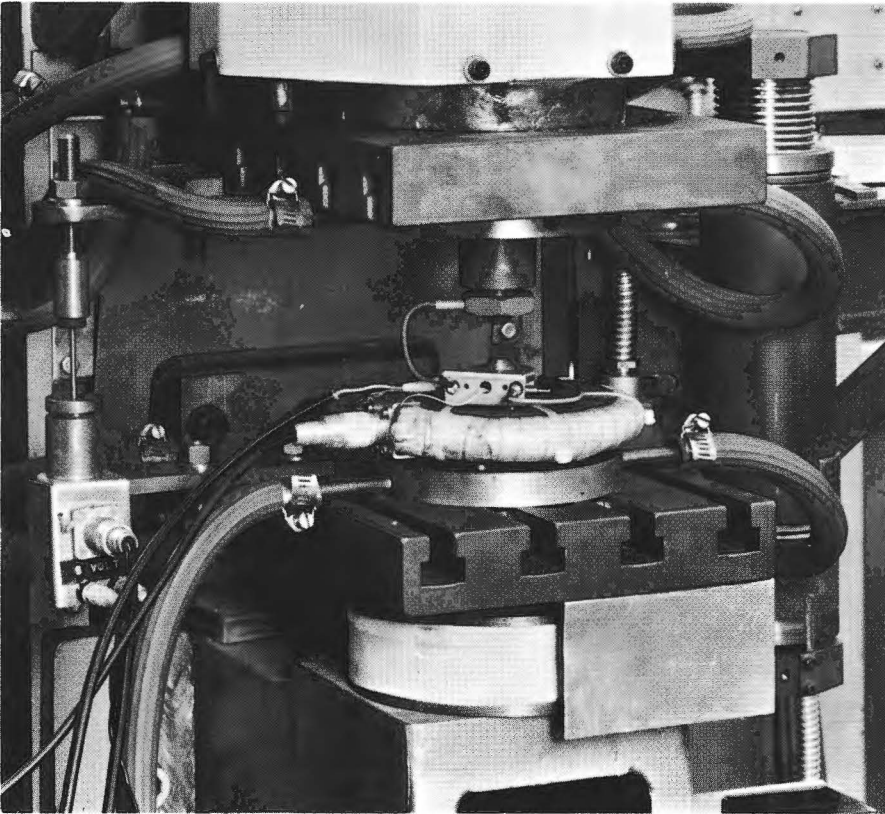


Fig. 3.3. Electrode Arrangement and Measuring Transducers.

Around the lower electrode, the current toroid; under the lower platen, the strain gauge element; to the left, displacement transducer.

The potential drop across the electrodes is taken from the nuts near the electrode tips

vant parameters. Some of these parameters may vary considerably during the heating period, hence they were recorded on a CEC model 5-124 oscillograph at a paper speed of 80 mm.s^{-1} for analysis afterwards. This goes for the current intensity i , the potential drop across the workpieces U , the electrode displacement d and the electrode force F . The following variables were measured.

(a) Intensity of the Welding Current. Owing to the application of

phase-shift to control the intensity of the welding current the resultant secondary current wave form is far from sinusoidal [51]. In order to determine the r.m.s. value defined by

$$i_{\text{rms}} = \sqrt{\frac{1}{t'} \int_0^{t'} i^2(t) dt} \quad (3.7)$$

for a heating time t' , the true r.m.s. ammeter, diagrammatically shown in fig. 3.4, was developed. A toroidal measuring transformer (Rogovskii belt) supplies a voltage proportional to the first derivative di/dt of the welding current with respect to time. After passing a calibrated attenuator (used to fix the measuring range) and an integrator, the signal - then proportional to i - is led to the recording oscillograph. Besides, in order to facilitate the reading of the current value after welding, the signal is squared and transferred to a second integrator after being divided by the welding time t' by means of a pre-set potentiometer. The second integrator is followed by a direct-reading voltmeter, and designed to hold the pointer of that instrument in its position for a few seconds after the current has ceased to flow. In fact, there are four of these integrating branches, thus permitting the subsequent reading of the currents during the pre-weld, first and second weld and post-weld heating periods, if required. The signal is guided to the right branch by means of the reed relays 1 through 4, operated by synchronised pulses from the welder control unit. The error of this instrument is estimated to be smaller than 2 per cent. of the measured value.

(b) Voltage across the Workpieces. The knowledge of the electric potential difference U across the workpieces permits the calculation of the workpiece resistance if the current is measured simultaneously. This voltage is taken from two points of the electrode tip bodies and recorded on the oscillograph. In order to cancel the pick-up of an undesirable e.m.f. induced by the magnetic field of the welding current in the voltage signal leads, a compensation toroid may be added to the design [50]. However, the compensation voltage is more easily taken from the current toroid, as was done in the present investigation. In computing the resistance of the welding work that part of the voltage that is

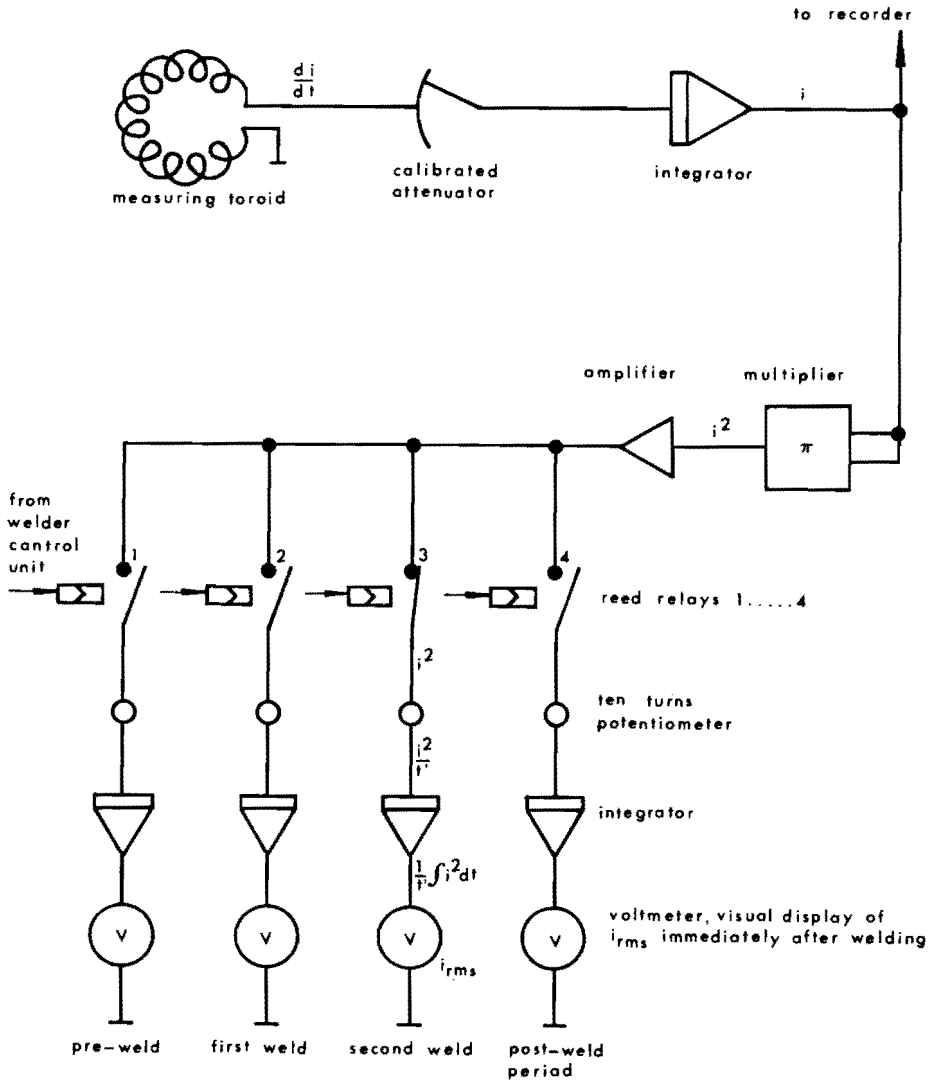


Fig. 3.4. Diagrammatic Representation of the True R.M.S. Current Measuring Device

caused by the potential drop across the electrode bodies is arithmetically subtracted. The estimated error of the voltage measurement is smaller than 5 per cent.

(c) Electrode Displacement. Owing to the expansion of the workpiece materials during the heating cycle and the weakening of the weld

at higher temperatures, an electrode movement d occurs, which is useful as an indication of weld quality [50]. This movement is measured by means of a SANBORN model 7 DCDT 050 differential transformer displacement transducer, the output voltage of which is recorded on the oscillograph. The error is estimated to be smaller than 2 per cent.

(d) Electrode Force. The electrode force F is measured by means of resistance wire strain gauges, cemented on an elastic element, viz. a specially designed thin-walled cylinder, mounted under the lower platen of the welder (cf. fig. 3.3). The strain is read from a HOTTINGER type KWS II/50 universal strain indicator and recorded on the oscillograph. The readings are calibrated in newtons. The estimated error is smaller than 2 per cent. of the measured value.

(e) Tension-Shear Strength of the Welds. The tension-shear strength of the weld F_s is measured by subjecting the welded specimen to a tensile pull in a standard WOLPERT model U6 testing machine until fracture occurs. The ultimate strength of the specimen and the manner of failure, whether by shear of the weld metal or by tear of the parent metal is recorded. The error of this measurement is estimated to be smaller than 5 per cent.

(f) Dimensions. The sheet thickness s and the workpiece indentation d_1 were measured by means of a standard dial indicator. The electrode diameter D_E and the nugget diameter after shearing D_N were determined with the aid of a measuring microscope. The error in these measurements does not exceed 0.01 mm.

3.4. Results

3.4.1. Types of Weld

A classification of spot welds can be made using various criteria. In order to facilitate the comprehension of the welding process an arrangement based on the behaviour of a few parameters that vary significantly during the process is of particular interest. The electrode movement d as well as the total resistance R of the weld material during the heating period have proved to be very useful in this respect.

In fig. 3.5 a general shape of the $d(t)$ curve is shown. After the electric current is switched on, the workpieces are rapidly heated,

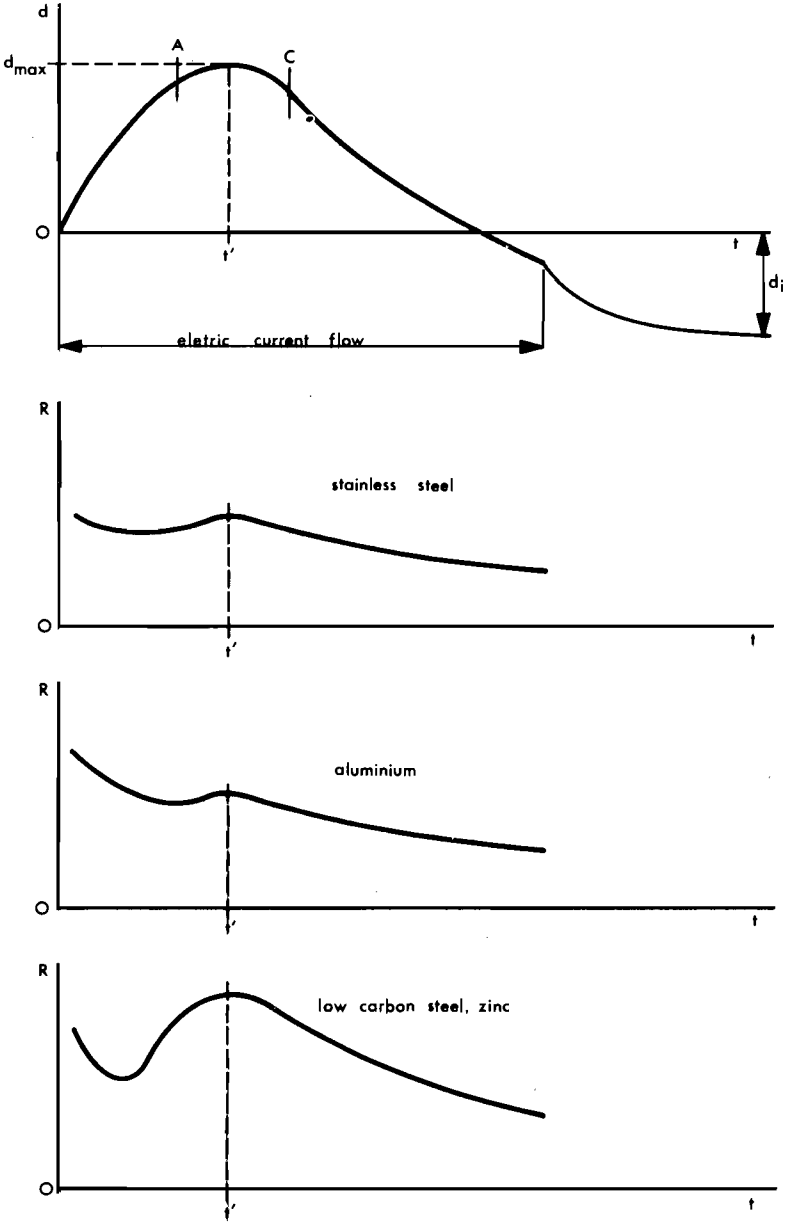


Fig. 3.5. Typical Electrode Movement and Workpiece Resistance Curves

resulting in thermal expansion of the weld material. This expansion mainly takes place along the electrode axis owing to the constraint offered by the cold metal surrounding the heated spot [50, 52]. As the material softens, plasticises and melts the electrodes force their way towards each other in the weakened metal so that the electrode movement changes its direction, resulting in a marked indentation d_i in the workpiece surfaces after the weld has cooled.

The shape of the curves representing the total resistance R of the workpieces as a function of time, depends on the material welded. For stainless steel the resistance of the weld is practically constant before the metal reaches the weakening point, where a slight maximum appears. Afterwards, the value of the resistance decreases substantially, owing to a decrease in the material thickness and to the increase in the effective electrode contact diameter, resulting from the penetration of the electrode into the weld material. In extreme cases, d_{\max} may reach values of 30 per cent. and d_i of 60 per cent. of the sheet thickness. For aluminium, the initial resistance is generally much higher than that at the weakening point, whereas for low carbon steel and zinc the opposite is true. A further analysis of the workpiece resistances will be given in chapter 4.

While leaving the other welding parameters unchanged, the heating time may be reduced to a value $t > t'$ in fig. 3.5. For example, the welding current is interrupted in point C. It then appears that a satisfactory weld with a diameter $D_N \geq D_E$ is made in all cases. If the welding time is greater than t' , the growth speed of the weld nugget is substantially reduced. This is due to the reduction of the sheet thickness and to the apparent growth of the electrode diameter, resulting in a lower current density in the weld.

If the welding time is further reduced, so that $t < t'$ (point A), generally no weld is formed, unless the heat input is increased to such an extent that the point t' is also shifted to the left. Only when applying very high heat input values, the weakening of the weld material in the surroundings of the nugget takes place at a lower rate, and a weld can be formed with a type A electrode displacement curve. From figs. 2.13 and 2.14 it can be seen that

this may be the case for low Q_L values, where the ratio of the temperatures at the electrode face to those at the nugget border is comparatively low, premised that Q_λ has a sufficiently high value.

On the basis of the foregoing the time required to reach the maximum electrode displacement d_{max} is considered to be the proper heating time for obtaining a weld nugget with a diameter equal to that of the electrode tip.

Splashing of molten material between the workpieces, mentioned in section 3.1, mainly takes place if $Q_D > 4$. Radial thermal expansion, which is greater in the plane $z = 0$ than at the electrode contact area as a result of the higher temperature in the first plane, forces the workpiece sheets apart. This phenomenon, called sheet separation, is a form of bending of the sheet, which occurs more easily for comparatively thin workpieces. A wall of solid material that carries the welding force, surrounds the molten pool in the centre, but at high energy input rates that wall may burst at its weakest point, permitting the molten metal to be splashed away between the sheets. This results in an electrode displacement curve as represented in fig. 3.6. As the illustration shows,

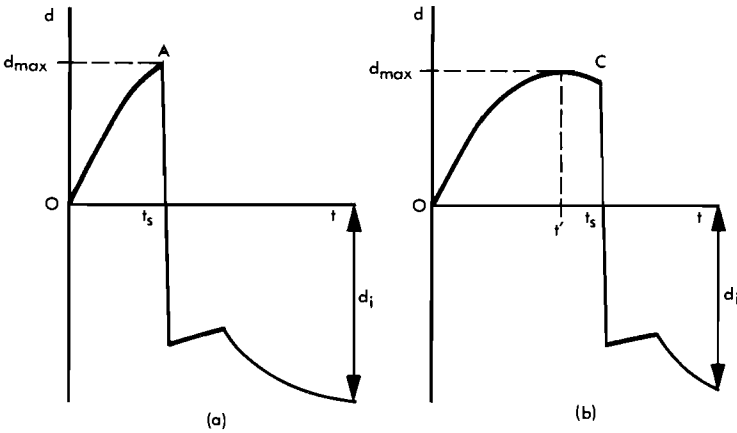


Fig. 3.6. Electrode Movement for Splashing Welds

(a) type AS, splashing occurs at point A of fig. 3.5

(b) type CS, splashing occurs at point C of fig. 3.5

splashing may occur at point A of fig. 3.5 or at point C not too far beyond the point of maximum electrode displacement. The total

workpiece resistance R falls to a significantly lower level, depending on the amount of metal splashed away and on the local reduction in sheet thickness. Various investigators have observed the phenomenon of splashing [50, 53, 54]. They agree that a sound weld is formed whenever splashing occurs, although equally good welds can be produced without it [55].

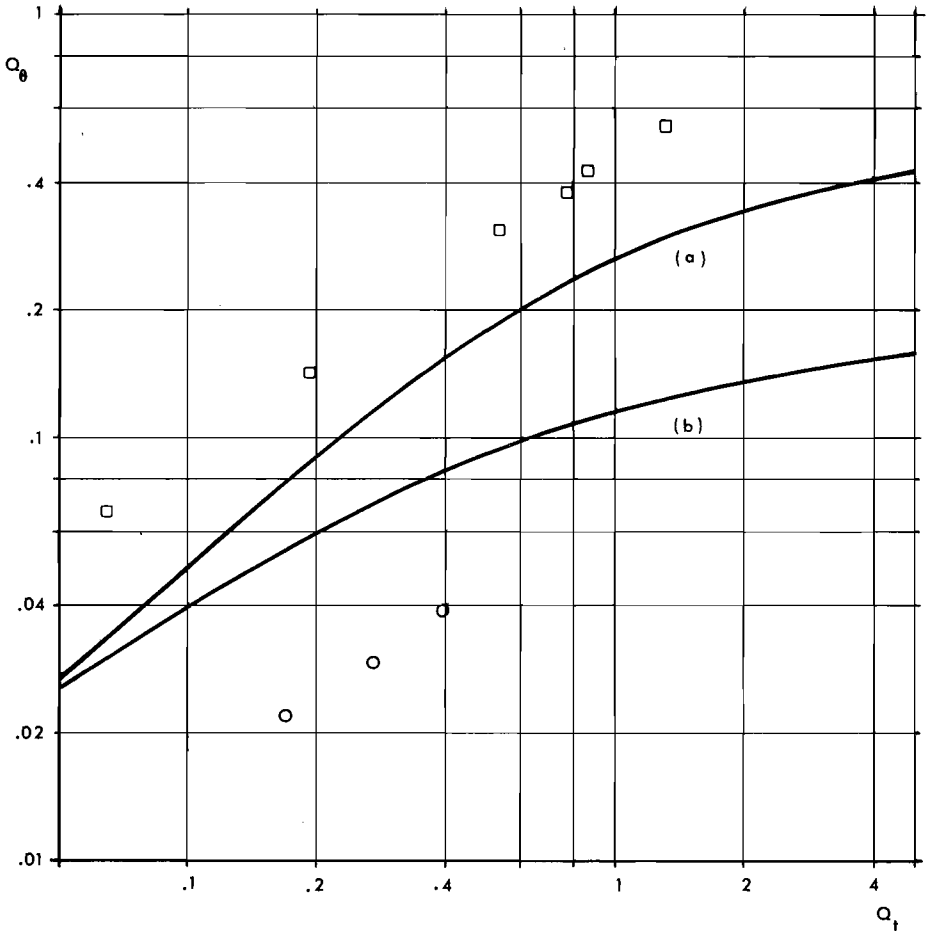


Fig. 3.7. Comparison of Experimental Results (Dots) and Analogue Measurements (Drawn Curves) when Spot Welding Stainless Steel

(a) $Q_\lambda = 7.8$; $Q_D = 5.9$; square dots; $q = 1.72$

(b) $Q_\lambda = 7.8$; $Q_D = 1.07$; circular dots; $q = 0.43$

From our experiments it appeared that the weld type C occurs for $Q_t > 1$, type A and AS for $Q_t < 1$, while the transition type CS chiefly occurs in the range of $0.5 < Q_t < 1.5$. The boundaries mentioned, however, are not strict. In reference [54] the time t_s is shown to depend on the electrode force F . From the discussion in this section it seems justified to use the time at which the maximum electrode displacement is realised as the proper welding time for all the types of weld described.

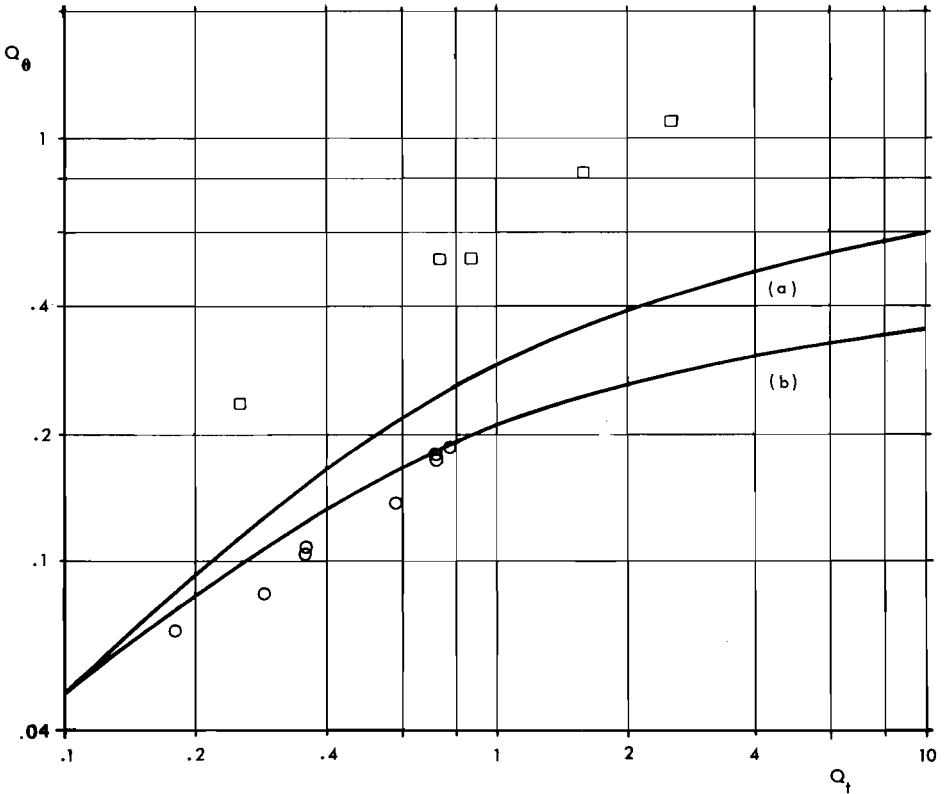


Fig. 3.8. Comparison of Experimental Results (Dots) and Analogue Measurements (Drawn Curves) when Spot Welding Low Carbon Steel

(a) $Q_\lambda = 8.0$; $Q_D = 8.8$; square dots; $q = 2.14$

(b) $Q_\lambda = 8.0$; $Q_D = 2.65$; circular dots; $q = 0.91$

3.4.2. Discussion

The measurements were carried out as described in section 3.1. The results of each series of experiments having constant Q_λ and Q_D values are compared with the appropriate $Q_\theta(Q_t)$ curve for the nugget border obtained from the analogue measurements. These curves were interpolated for those values of Q_λ and Q_D that are

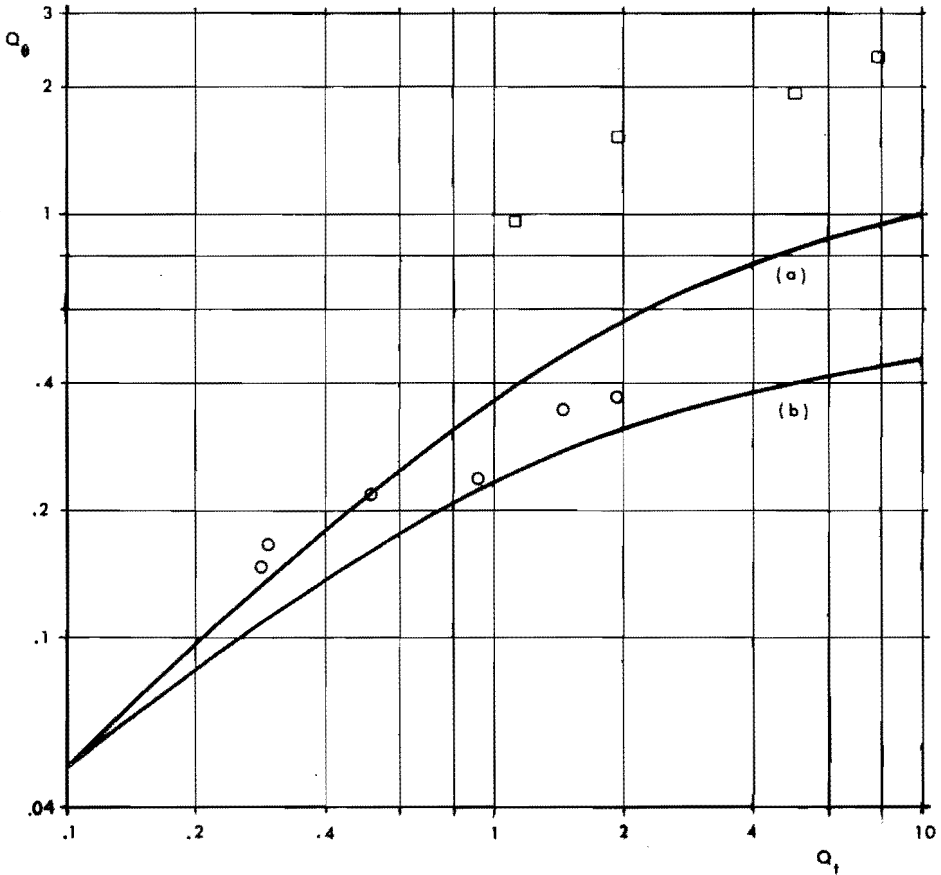


Fig. 3.9. Comparison of Experimental Results (Dots) and Analogue Measurements (Drawn Curves) when Spot Welding Zinc
 (a) $Q_\lambda = 3.1$; $Q_D = 9.7$; square dots; $q = 2.48$
 (b) $Q_\lambda = 3.1$; $Q_D = 2.67$; circular dots; $q = 1.09$

not mentioned in section 2.3.1. It appeared to be impossible to spot weld pure copper sheet with the aid of copper electrodes in the normal way, as could be expected from long-standing workshop

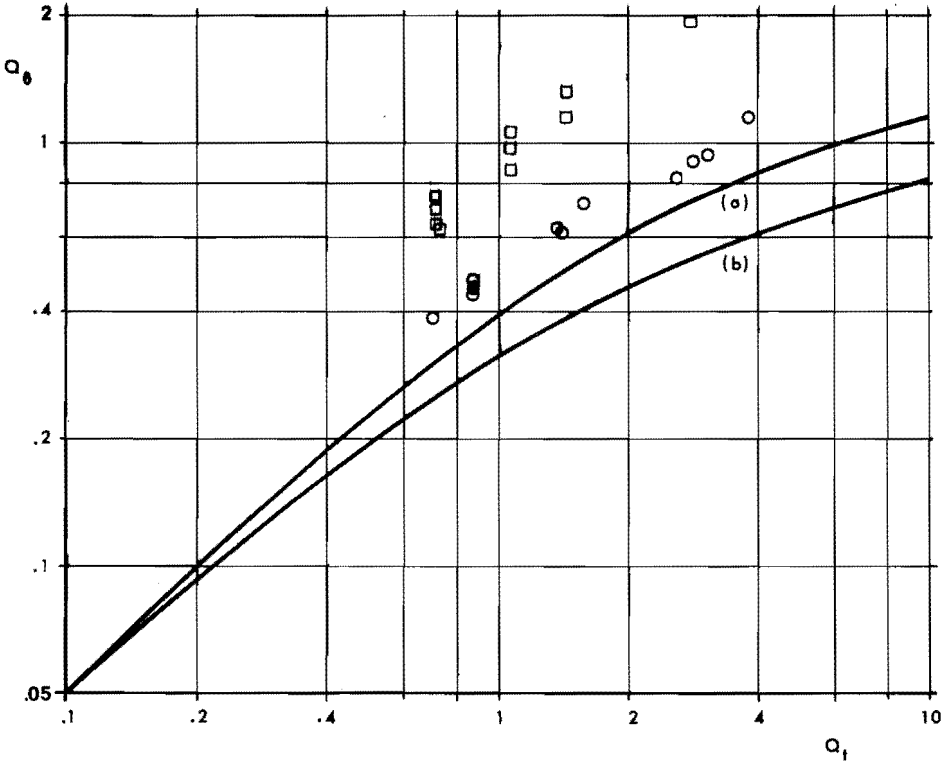


Fig. 3.10. Comparison of Experimental Results (Dots) and Analogue Measurements (Drawn Curves) when Spot Welding Aluminium
 (a) $Q_\lambda = 1.6$; $Q_D = 6.5$; square dots; $q = 2.24$
 (b) $Q_\lambda = 1.6$; $Q_D = 4.1$; circular dots; $q = 1.62$

experience [2]. A method of welding copper, based on the theoretical considerations of chapter 4 will be dealt with in section 5.2.

As an example, the results of two series for each of the other workpiece materials investigated are shown in figs. 3.7 to 3.10 inclusive. From these graphs two important conclusions can be drawn.

(a) The course of the curves which may be drawn through the experimental plottings of the dimensionless product Q_θ as a function of Q_t is fundamentally the same as of those predicted by the analogue measurements.

(b) However, a very distinct deviation exists between the positions of the experimental and of the analogue curves.

This deviation can be expressed in a multiplying factor

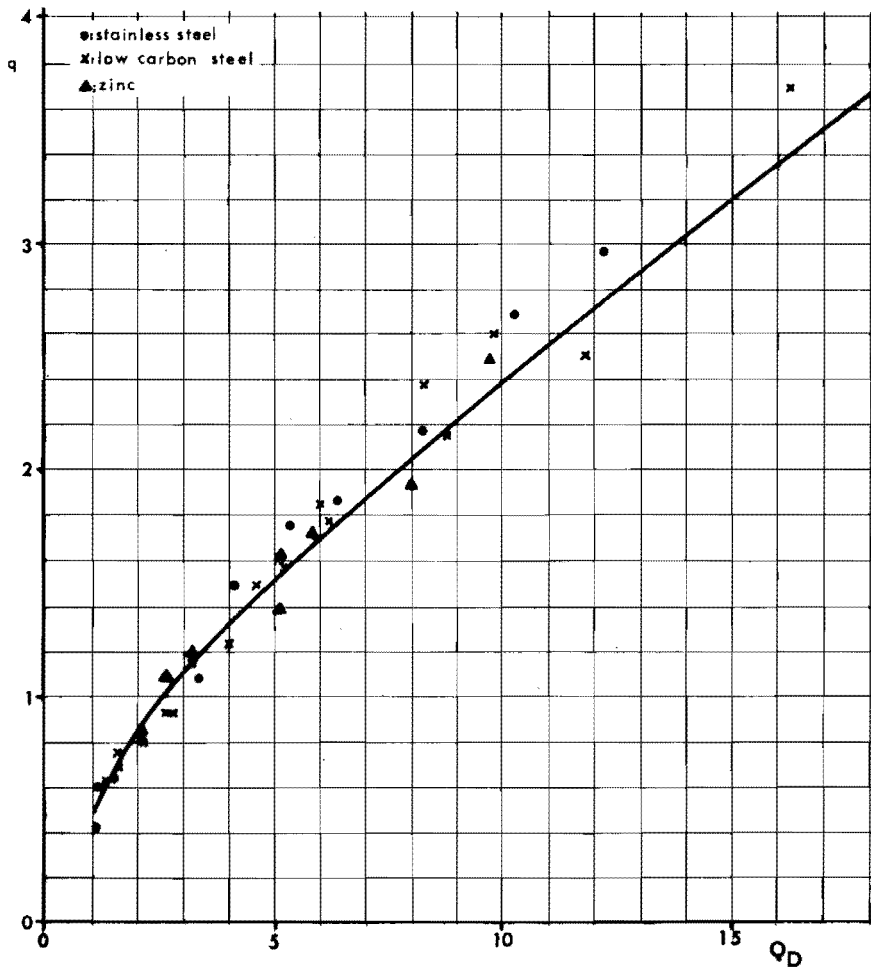


Fig. 3.11. The Ratio q as a Function of Q_D for Stainless Steel, Low Carbon Steel and Zinc

$$q = \frac{Q_{\theta} \text{ observed}}{Q_{\theta} \text{ calculated}} \quad (3.8)$$

This factor appears to be a function of Q_D only. As such it is

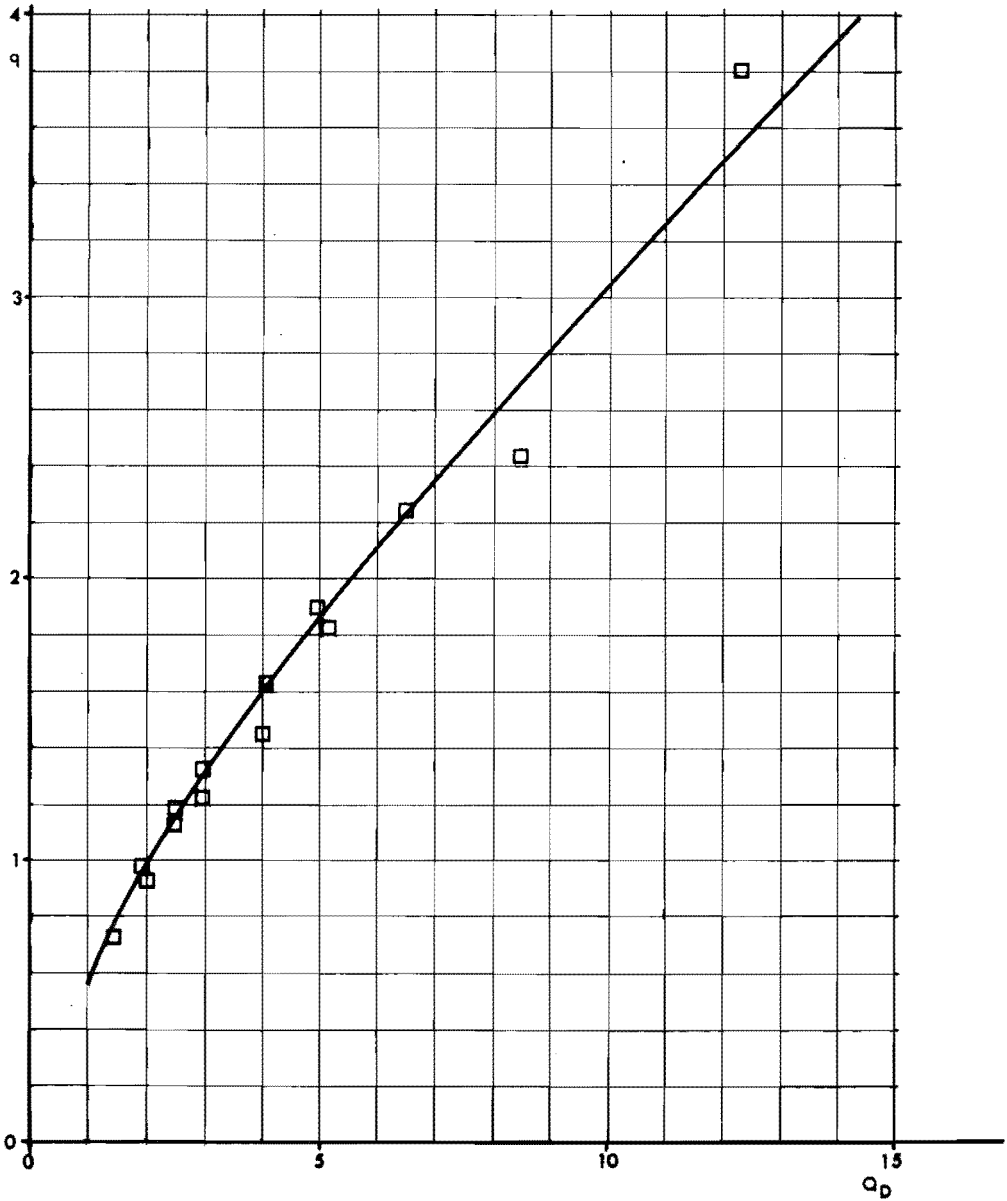


Fig. 3.12. The Ratio q as a Function of Q_D for Aluminium

recorded in figs. 3.11 and 3.12.

In conclusion, it appears that an important and systematic deviation exists between the model described in chapter 2 and the results of the experiments presented in this chapter. The deviation seems to be chiefly dependent on the dimensionless product Q_D . In the next chapter an interpretation of the phenomena leading to this deviation will be offered.

Chapter 4. IMPROVEMENT OF THE THEORY

4.1. Introduction

In chapter 3 a discrepancy between the experiments and the results of the analogue measurements was observed. It is shown there that this can be expressed in the form of a function $q(Q_D)$, as defined in equation (3.8). Since the value of q varies between 0.4 and 4 in the investigated range of Q_D , it can be concluded that for low Q_D values the mean current density \bar{J} , and thus the current intensity i required to make a satisfactory weld, is greater than that expected on the basis of the analogue model. On the other hand, the opposite is true for high Q_D values.

From this it might be concluded that the total resistance R of the workpieces substantially differs from that assumed in the model of chapter 2. There, only the resistance

$$R_0 = \frac{8\rho s}{\pi D_E^2} \quad (4.1)$$

of a cylinder of diameter D_E and height $2s$ is taken into account, whilst a uniformly distributed current is assumed to flow through this cylinder (cf. section 2.2.2). In that case, the heat development in the workpieces is equal to

$$\phi_0 = \int_0^{t'} i^2 R_0 dt = i^2 R_0 t', \quad (4.2)$$

since i is constant during the heating time t' and R_0 is regarded to be so, because of the use of a mean value for the resistivity, as defined in section 3.2.1.

However, if $R \neq R_0$ and, moreover, if R is not constant during the heating period, the real heat production becomes

$$\phi = \int_0^{t'} i^2 R dt = i^2 \int_0^{t'} R dt, \quad (4.3)$$

assuming that i remains constant when the total resistance of the workpieces varies. This is caused by the rather high impedance value of $270\mu\Omega$ of the secondary circuit of the welder.

It will be shown in the next sections that a correction of the computed Q_θ value by means of a factor ϕ/ϕ_0 fully accounts for the discrepancy observed in the foregoing chapter. This means that the relation

$$q = \frac{\phi}{\phi_0} = \frac{1}{t'} \cdot \int_0^{t'} \frac{R}{R_0} dt \quad (4.4)$$

will be proved to be applicable.

4.2. The Influence of the Current Distribution

The assumption made in section 2.2.1 concerning a uniform distribution of the electric current in the cylinder of the workpiece metal between the electrode faces does not hold. Especially for low Q_D values the error introduced by this simplification becomes inadmissible. As a matter of fact, the current entering the workpiece sheet via the electrode-workpiece contact plane "bulges" in the sheet metal outside the cylinder mentioned and crosses the interworkpiece contact plane over a circular area, having a diameter considerably greater than D_E (cf. fig. 4.1).

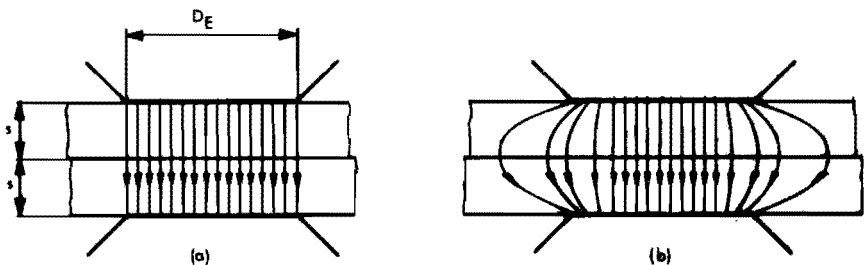


Fig. 4.1. Comparison of Assumed (a) and Actual (b) Current Distribution in Spot Welding

This phenomenon, as well as its dependence on the value of Q_D , has been known for a long time [1, 4, 5]. It means a lower current density at the interworkpiece contact plane than at the electrode face, and a less favourable value of the ratio of the electrode face temperature and the nugget temperature.

Besides, it means a lower resistance of the workpieces. Consider the cylinder in fig. 4.2 with diameter w_L and height $2s$. At the top and

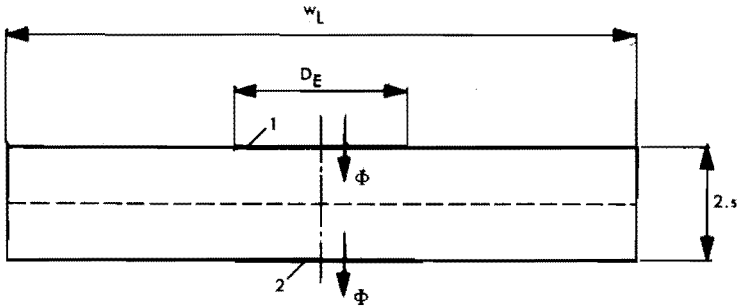


Fig. 4.2. Model of the Workpiece Sheets for the Computation of the Electric Resistance between the Points 1 and 2

the bottom of the cylinder a constant flux ϕ is supplied and removed over concentric circular areas 1 and 2 respectively, each having a diameter D_E . Reference [42(p. 223)] gives an expression for the average temperature difference between these areas for the case that ϕ is a flux of heat. The solution is easily transformed in an expression for the average potential difference for the case that ϕ is an electric current, because of the homology of the potential equation for heat flow and of that for the flow of electric charge. It may be recalled to mind that this homology was used earlier as a basis of the analogue model. Using the above-mentioned expression, the actual resistance R'_O of the workpieces, measured between the electrode faces, can be written

$$R'_O = R_O \cdot f(Q_D, \frac{w_L}{s}) \quad (4.5)$$

with

$$f(Q_D, \frac{w_L}{s}) = 1 - \frac{16}{\pi^2} \sum_n \left\{ \frac{I_1(n\pi Q_D/4)}{n^2 I_1(n\pi w_L/4s)} \cdot \left[I_1\left(\frac{n\pi w_L}{4s}\right) \cdot K_1\left(\frac{n\pi Q_D}{4}\right) - K_1\left(\frac{n\pi w_L}{4s}\right) \cdot I_1\left(\frac{n\pi Q_D}{4}\right) \right] \right\} \quad (4.6)$$

where the summation is over odd values of n , and where I_1 and K_1 denote the first order modified Bessel functions of the first and second kind respectively. When computing the values of this function f for different combinations of Q_D and w_L/s it appears that the latter has no influence on the result if

$$\left. \begin{array}{l} w_L > 4D_E \quad \text{for} \quad Q_D > 1 \quad \text{or} \\ w_L > 2D_E \quad \text{for} \quad Q_D > 2 \end{array} \right\} \quad (4.7)$$

Since these conditions are always fulfilled in practical cases, f may be regarded as a function of Q_D only. It is graphically shown as such in fig. 4.3. Experimental values, given by TARASOV [24] are plotted in this figure additionally.

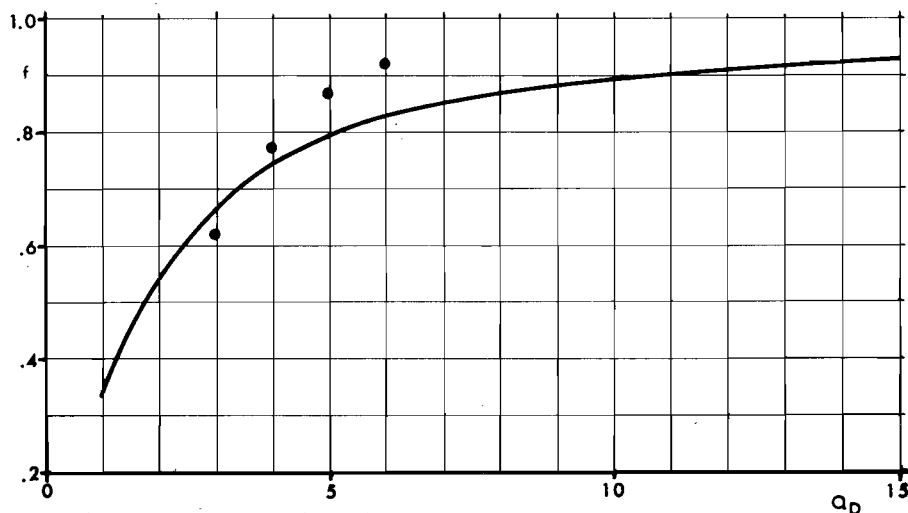


Fig. 4.3. The Function $f(Q_D)$.

The dots indicate experimental values from [24]

An affirmation of this approach is found in the results of the resistance measurements. The total resistance R between the electrode faces at the instant when the nugget reaches the melting point, i.e. at the time t' of fig. 3.5, reflects the course of $f(Q_D)$ for the lower range of Q_D . As an example, the ratio R/R_0 for low-carbon steel is plotted in fig. 4.4. It appears that

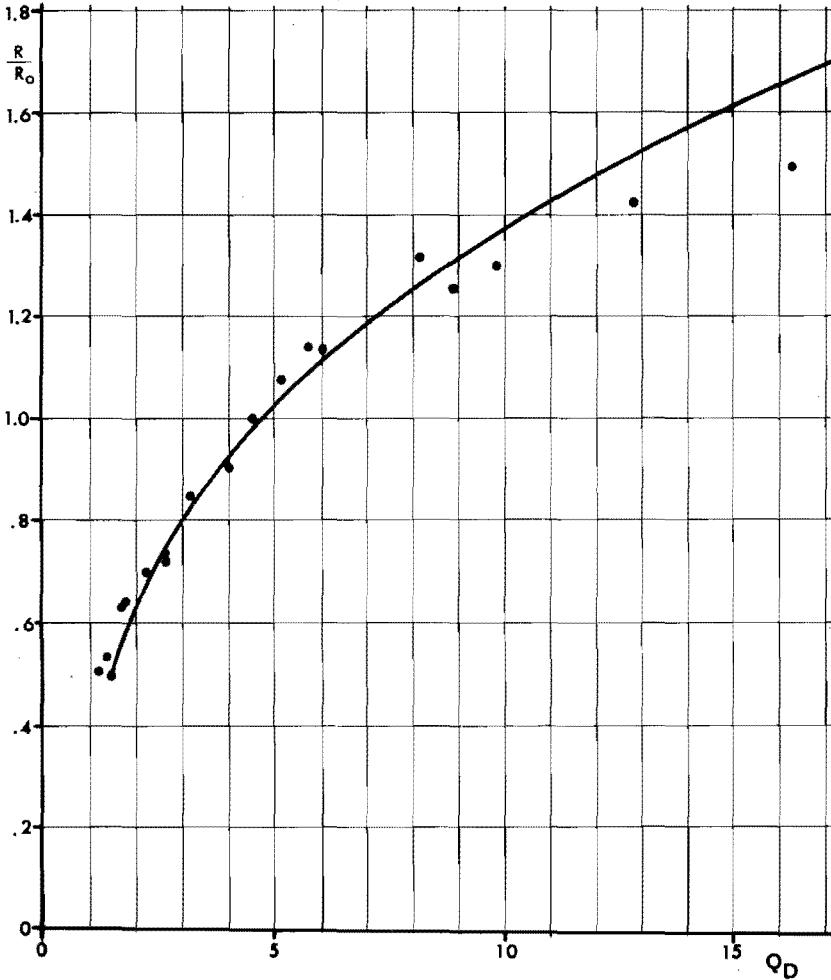


Fig. 4.4. The Ratio R/R_0 as a Function of Q_D for Low Carbon Steel.
For the curve the relation $R/R_0 = f + 0.047 Q_D$ holds

$$\frac{R}{R_o} = f(Q_D) + \xi \cdot Q_D \quad (4.8)$$

The extra term $\xi \cdot Q_D$ will be proved to result from the influence of the contact resistance. The curves for the other materials investigated show an analogous behaviour. The values of ξ are presented in table 4.1.

Table 4.1. Values of ξ in Relation (4.8)

material welded	ξ
stainless steel	0.022
low-carbon steel	0.047
zinc	0.040
aluminium	0.169

Because of the deviation of the real current distribution from that assumed in the analogue model, the real heat production ϕ_o' is lower than the assumed value ϕ_o . Since R_o' and R_o are considered independent of the time t , it follows from the equations (4.4) and (4.5) that

$$\frac{\phi_o'}{\phi_o} = \frac{R_o'}{R_o} = f(Q_D) \quad (4.9)$$

4.3. The Influence of the Contact Resistance

4.3.1. Introduction

In section 2.1.6, mention was made of the divergence of the results obtained by various investigators with respect to the influence of the contact resistance R_k . The conclusion was that it appears to be impossible to predict the value of R_k with universal validity.

Nevertheless, in the following sections an attempt will be made to obtain a useful estimation of the influence of the contact resistance on the spot welding process.

According to HOLM [36], only a small fraction of the apparent contact area is electrically conducting, owing to the unevenness of the contacting surfaces. Hence, the contact resistance R_k always implies or is a constriction resistance R_c , which is the consequence of the current flow being constricted through small conducting spots. The extra resistance between the contact members, owing to the presence of one spot, which is assumed to be circular and to have a radius a , can be shown to be equal to

$$R_c = \frac{\rho}{2a} \quad (4.10)$$

if the contact is a pure metallic one.

If a number of n of these "a-spots", uniformly distributed over the apparent contact surface A_r at an average distance of 2ℓ between neighbouring centres, is present, the total constriction resistance [36] reduces to

$$R_c(n, a, \ell) = \frac{\rho}{\pi n a} \cdot \arctan \frac{\sqrt{\ell^2 - a^2}}{a} \quad (4.11)$$

where n and ℓ are related by means of

$$A_r = 4n\ell^2 \quad (4.12)$$

An alien film with resistivity ρ_f and thickness s_f in the contact may give rise to an additional film resistance

$$R_f = \frac{\rho_f s_f}{A_c} \quad (4.13)$$

where A_c is the total conducting area. In practical cases the film resistance may be some orders of magnitude greater than the constriction resistance.

The influence of the contact force F on the value of the total contact resistance R_k can empirically be expressed as follows

$$R_k = R_c + R_f = cF^{-m} \quad (4.14)$$

where the constant c depends on the contact materials and the exponent m depends on the conditions of the contacting surfaces, on the presence of films or oxide layers and on the fact whether the deformations of the surface asperities caused by the load F are of an elastic nature or of a plastic one. Generally m lies between the values 0.33 and 1.

From the summary of the properties of static contacts given above, the conclusions of section 2.1.6 are well comprehensible. From equation (4.13) follow the conclusions (a), (c) and (d). Conclusion (b) is explained by equation (4.14). The value of the static contact resistance restricts the maximum permissible current intensity because of the increasing probability of excessive heat production in the contact areas with increasing R_k . This also explains conclusion (e) because of the higher welding current intensities required for short welding times.

The application of mechanical or chemical cleaning methods improves weld quality and reduces the fouling of the electrode tips [37], for which reason the maximum surface resistances are bound to a prescribed level in standard specifications for high-quality resistance welding [10]. These cleaning methods may remove the oxide films and thus reduce the value of the static contact resistance by a factor 100 [37], but of course do not reduce the influence of R_c . Owing to the lack of information about the number, the distribution and the dimensions of the microscopic contact spots no computation of the constriction resistance can be made in the case of spot welding.

4.3.2. The Dynamic Contact Resistance during Welding

Resistance measurements during welding have shown the contact resistance to have an essentially dynamic character [6, 37, 38]. As soon as the welding current starts to flow the resistance decreases rapidly below the initial static value described in the foregoing section. The resistance attains its minimum value at the moment the current reaches its top, after which the static resistance does not change appreciably any more. Consequently, when using a 50-cycle

alternating welding current, this minimum is reached after 5 ms. ROBERTS [38] observed the following relation between the peak current intensity i_p and the ultimate value of the total workpiece resistance after 1 half current cycle,

$$R = c_1 + \frac{c_2}{i_p} \quad (4.15)$$

where c_1 and c_2 are constants for a given material and set of conditions. He also observed the electrode force to play no role with respect to the ultimate value of R as it did for the initial resistance.

The dynamic character of the contact resistance is due to the heating of the contact spots, resulting in a weakening of the surface asperities, which causes the a-spots to grow rapidly in dimension as well as in number.

A relation between the temperature θ_c of a single current constriction and the contact voltage U is given by [36]

$$\int_{\theta_a}^{\theta_c} \rho \lambda d\theta = \frac{U^2}{8} \quad (4.16)$$

where θ_a is the temperature of the bulk of the metal in the vicinity of the contact spot.

In spot welding, the current intensity has such a high value that the melting temperature θ_m is always reached before the current is at its top in the first half cycle. When the melting point is reached, the above mentioned weakening of the surface asperities and the consequent growth of the a-spots result in a rapidly decreasing contact resistance [36]. If it is assumed that for this reason θ_c does not exceed the melting point of the metal and if the weld temperature θ is taken for θ_a , equation (4.16) becomes

$$\int_{\theta}^{\theta_m} \rho \lambda d\theta = \frac{i_p^2 R_k^2}{8} \quad (4.17)$$

after the current intensity has reached its top value for the first

time. By means of numerical evaluation it appears that the first member of equation (4.17) can be written

$$\int_{\theta}^{\theta_m} \rho \lambda d\theta = (\rho \lambda)' \cdot (\theta_m - \theta) \quad (4.18)$$

where the quantity $(\rho \lambda)'$ varies from 0.8 to 1.2 times the mean value given in table 4.2 for $0 < \theta < \theta_m$. The exposed values of $(\rho \lambda)'$, which are further regarded - as an approximation - to be constant, differ markedly from the product of λ and ρ from the tables 3.1 and 3.2 respectively, thus giving rise to a multiplying factor

$$\alpha^2 = \frac{(\rho \lambda)'}{\rho \lambda} \quad (4.19)$$

which is also represented in table 4.2.

Table 4.2. Values of $(\rho \lambda)'$ compared with $\rho \lambda$

material	$(\rho \lambda)'$	$\rho \lambda$	α^2
SS	3220	1700	1.89
St	3390	2210	1.54
Zn	1360	985	1.38
Al	1540	1890	0.815
Cu	2350	2450	0.96
	$\times 10^{-8}$	$\times 10^{-8}$	

Using the equations (4.17), (4.18) and (4.19), the contact resistance can be expressed in known variables

$$R_k^2 = \alpha^2 \cdot \frac{8\rho\lambda}{i_p^2} (\theta_m - \theta) \quad (4.20)$$

in accordance with relation (4.15) if for c_1 the body resistance R_o' is read. Both members of this equation are divided by the body resistance R_o , defined in relation (4.1), thus yielding

$$\begin{aligned} \frac{R_k}{R_o} &= \alpha \sqrt{2} \cdot \left(\frac{i}{i_p}\right) \cdot \sqrt{\frac{\pi^2 \lambda \theta_m D^4}{16 \rho i^2 s^2}} \cdot \sqrt{1 - \frac{\theta}{\theta_m}} = \\ &= k \sqrt{1 - \frac{\theta}{\theta_m}} \end{aligned} \quad (4.21)$$

with

$$k = \alpha \sqrt{2} \cdot \left(\frac{i}{i_p}\right) \cdot Q_{\theta_m}^{0.5} \quad (4.22)$$

in which formula Q_{θ_m} denotes the ultimate value of this product, obtained by putting $\theta = \theta_m$ in equation (2.7) and by defining $\rho \bar{J}^2$ as in equation(2.9).

With the aid of (4.21) the form of the resistance curves of fig. 3.5 can be explained. The body resistance R_o' of the workpieces increases during the heating period because of the increase in electric resistivity with weld temperature. The contact resistance R_k falls rapidly from an initial high value to that predicted by (4.21) and decreases at a slower rate with increasing weld temperature. The total resistance R , being the sum of R_o' and R_k consequently descends or rises, depending on the fact which term prevails.

In the interworkpiece contact area the contact resistance will be zero when the welding temperature is reached. In the electrode-workpiece interfaces a small contact resistance may be left, because $\theta < \theta_m$ in those areas (cf. table 4.1).

From our experiments it appears that the relation between the peak value of the current intensity i_p in amperes and the r.m.s. value i in amperes can be expressed as

$$i_p = 18.1 \times i^{0.765} \quad (4.23)$$

for a secondary e.m.f. of 11.4 V of the welder. As a matter of course, this relation is dependent on the electrical characteristics of the equipment used. With the use of this relation the expression for the factor k transforms into

$$k = \alpha \frac{i^{0.235}}{12.8} Q_{\theta m}^{0.5} \quad (4.24)$$

The factor k was computed for a large number of cases with the aid of equation (4.24). As expected from the figures 3.11 and 3.12 and from relation (4.9) its mean value - at constant Q_D - appeared to be dependent on the product Q_D as follows

$$k = k_1 Q_D \quad (4.25)$$

where the constant k_1 has the values of 0.074 for stainless steel, 0.077 for low-carbon steel, 0.140 for zinc and 0.143 for aluminium.

4.3.3. The Heat Development in the Contact Areas

As indicated in section 4.1 the ratio of the real heat production ϕ and that assumed in the analogue model, ϕ_o , will be used to correct the Q_θ values found by means of the model. The heat production ϕ_k in the contact areas owing to the presence of contact resistances can be written

$$\frac{\phi_k}{\phi_o} = \frac{1}{t'} \cdot \int_0^{t'} \frac{R_k}{R_o} dt = \frac{k}{t'} \cdot \int_0^{t'} \sqrt{1 - \frac{\theta}{\theta_m}} dt \quad (4.26)$$

analogous to equation (4.4) and using equation (4.21). In order to evaluate the integral an assumption must be made with respect to the relation $\theta(t)$. It seems to be a fair approximation to write

$$\theta = \theta_e \cdot (1 - e^{-\beta t}) \quad (4.27)$$

where

$$\theta_e = \theta_e(Q_D, Q_\lambda) = \lim_{t \rightarrow \infty} \theta \quad (4.28)$$

It follows from equation (4.27) that

$$\lim_{t \rightarrow 0} \left(\frac{d\theta}{dt} \right) = \beta \theta_e \quad (4.29)$$

In order to facilitate the comparison of equation (4.29) with the experimental results, the former has to be expressed in the dimensionless products Q_θ and Q_t by using the equalities

$$\frac{\theta}{\theta_m} = \frac{Q_\theta}{Q_{\theta m}} \quad \text{and} \quad \frac{t}{t'} = \frac{Q_t}{Q_{t'}} ,$$

which follow from the definition (2.7). This results in

$$\lim_{t \rightarrow 0} \left(\frac{d\theta}{dt} \right) \equiv \frac{\theta_m}{t'} \cdot \frac{Q_{t'}}{Q_{\theta m}} \cdot \lim_{Q_t \rightarrow 0} \left(\frac{dQ_\theta}{dQ_t} \right) \quad (4.30)$$

where $Q_{t'}$ and $Q_{\theta m}$ denote the observed ultimate values of these products at the time $t = t'$. The experiments have shown that the relation

$$\lim_{Q_t \rightarrow 0} \left(\frac{dQ_\theta}{dQ_t} \right) = q \cdot \lim_{Q_t \rightarrow 0} \left(\frac{dQ_{\theta c}}{dQ_t} \right) = q \cdot \frac{1}{2} \quad (4.31)$$

is valid. Here, the value of $\frac{1}{2}$ originates from the analogue measurements, in analogy with the value of 1, observed in section 2.3.2 for the centre of the weld. $q = Q_\theta / Q_{\theta c}$ is a consequence of the discrepancy to be explained in this chapter, $Q_{\theta c}$ denoting the value

of this product obtained from the analogue measurements (cf. equation (3.8)).

Combination of the equations (4.29), (4.30) and (4.31) yields

$$\beta t' = \frac{q}{2} \cdot \frac{\theta_m}{\theta_e} \cdot \frac{Q_{t'}}{Q_{\theta m}} \quad (4.32)$$

The ratio θ_m/θ_e is known from (4.27)

$$\frac{\theta_m}{\theta_e} = 1 - e^{-\beta t'}$$

Substitution in relation (4.32) results in an implicate equation from which $\beta t'$ may be solved,

$$\beta t' = \frac{q}{2} \cdot \frac{Q_{t'}}{Q_{\theta m}} \cdot (1 - e^{-\beta t'}) = \frac{1}{2} \cdot \frac{Q_{t'}}{Q_{\theta c}} \cdot (1 - e^{-\beta t'}) \quad (4.33)$$

From equation (4.27) follows

$$1 - \frac{\theta}{\theta_m} = 1 - \frac{1 - e^{-\beta t}}{1 - e^{-\beta t'}} = \gamma^2 \cdot \{e^{\beta(t' - t)} - 1\} \quad (4.34)$$

where

$$\gamma^2 = (e^{\beta t'} - 1)^{-1}$$

After the combination of the equations (4.34) and (4.26) the latter becomes

$$\frac{\phi_k}{\phi_o} = \frac{\gamma k}{t'} \cdot \int_0^{t'} \sqrt{e^{\beta(t' - t)} - 1} dt \quad (4.35)$$

By substitution of the variable

$$v^2 = e^{\beta(t' - t)} - 1$$

the integral is transformed into

$$\begin{aligned} \frac{\phi_k}{\phi_0} &= -\frac{2\gamma k}{\beta t'} \cdot \int_0^0 \frac{v^2 dv}{\sqrt{e^{\beta t'} - 1} (1 + v^2)} = \\ &= \frac{2\gamma k}{\beta t'} \cdot \left\{ \sqrt{e^{\beta t'} - 1} - \arctan \sqrt{e^{\beta t'} - 1} \right\} = \\ &= \frac{2k}{\beta t'} \cdot \left\{ 1 - \frac{\arctan \sqrt{e^{\beta t'} - 1}}{\sqrt{e^{\beta t'} - 1}} \right\} = \\ &= k \cdot g_1(\beta t') \end{aligned} \tag{4.36}$$

The value of $\beta t'$ can be calculated from equation (4.33), since the ratio $Q_{t'}/Q_{\theta c}$ is known from the analogue measurements for given values of $Q_{t'}$, and the welding parameters Q_D and Q_λ . As $g_1(\beta t')$ and $\beta t'(Q_{t'}/Q_{\theta c})$ are both single-valued functions the former can be replaced by

$$g_1 \left\{ \beta t' \left(\frac{Q_{t'}}{Q_{\theta c}} \right) \right\} = g \left(\frac{Q_{t'}}{Q_{\theta c}} \right) \tag{4.37}$$

This function g is calculated numerically from the relations (4.33) and (4.36) and graphically represented in fig. 4.5.

Eventually, the expression for the heat production in the contact areas becomes

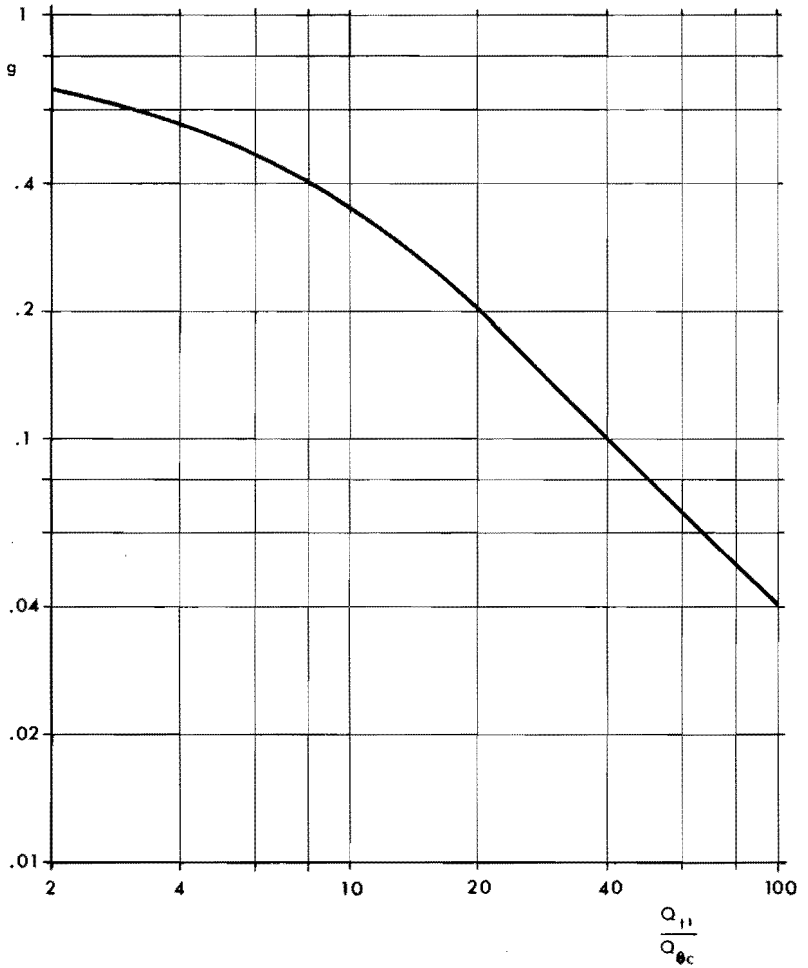


Fig. 4.5. The Function $g(Q_{t'}/Q_{\theta c})$

$$\frac{\phi_k}{\phi_o} = k \cdot g\left(\frac{Q_{t'}}{Q_{\theta c}}\right) = \alpha \cdot \frac{i^{0.235}}{12.8} \cdot Q_{\theta m}^{0.5} \cdot g\left(\frac{Q_{t'}}{Q_{\theta c}}\right) \quad (4.38)$$

The values computed for the ratio ϕ_k/ϕ_o are plotted in fig. 4.6 as a function of Q_D . It appears that the formula

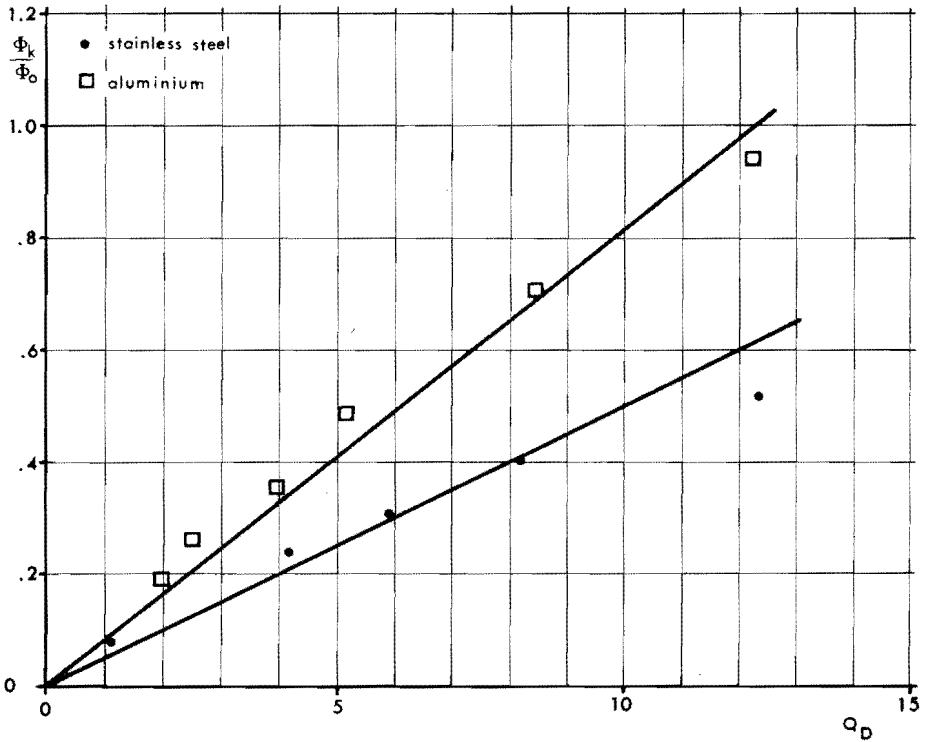


Fig. 4.6. The Ratio ϕ_k/ϕ_0 as a Function of Q_D for Stainless Steel and Aluminium

$$\frac{\phi_k}{\phi_0} = k \cdot g = k_2 \cdot Q_D \tag{4.39}$$

describes the position of the calculated points to a fair degree of correctness, although an extension of the range of Q_D might prove a second order approximation to yield more accurate results. In (4.39) the constant k_2 has the values of 0.045 for stainless steel, 0.046 for low-carbon steel, 0.073 for zinc and 0.081 for aluminium.

4.4. The Total Heat Production

4.4.1. Correction of the Analogue Results

On the basis of the derived relations (4.9) and (4.39) the total heat

production in the weld material can now be written

$$\frac{\phi}{\phi_o} = \frac{\phi_o'}{\phi_o} + \frac{\phi_k}{\phi_o} = f(Q_D) + 3.k_2.Q_D = q \quad (4.40)$$

where the factor 3 is added as an approximation, assuming the existence of three equally important contact areas. Comparison of this relation with the experimental result from section 3.4.2 shows that the latter is covered by curves of the form

$$q = f(Q_D) + \zeta.Q_D, \quad \text{for } Q_D < 16 \quad (4.41)$$

in such a way that no deviations occur of more than ten per cent. of the value of q . In table 4.3 the derived values of $3.k_2$ are compared with the experimental values of ζ for the workpiece materials investigated.

Table 4.3. Comparison of Theoretical and Experimental Results

material	$3.k_2$	ζ
SS	0.135	0.15
St	0.138	0.15
Zn	0.219	0.15
Al	0.243	0.22

As demonstrated, the computed values agree rather well with the experimental ones, except for the welding of zinc.

4.4.2. Discussion

By introducing the factor 3 in equation (4.40) the following assumptions were made.

(a) The heat production in the electrode contact surfaces is equal to

that in the interworkpiece contact area, i.e. equation (4.17) is valid for the three contacts. This is only true if θ_m is smaller than the melting temperature of the electrode materials, as is the case for the welding of aluminium and zinc. For steel, however, the weakening temperature of the contact spots will be equal to the melting point of the electrode material. The solution of the integral (4.17) will therefore yield a lower value.

(b) All the heat developed in both electrode-workpiece contact areas flows to the workpieces and raises the temperature of the weld. Although this is not very probable, the existence of a temperature barrier in the contact spots during the formation of the weld diminishes the passage of heat to the electrodes.

From the results it seems that the effects of these simplifications balance each other to a considerable extent.

A final remark must be made with respect to the values used for the electric resistivity ρ . As appears from table 3.2, the best fitting values of ρ are much lower than those defined by equation (3.1) for the welding of steel, whereas for aluminium the opposite is true. However, equation (3.1) is a rather arbitrary definition of the average values of the physical material properties. The average temperature in the sheet during the heating period, determined for the region $0 < z < s$, is lower when welding steel than when welding aluminium. This is because of the influence of Q_λ (cf. fig. 2.12 and 2.14). It is therefore acceptable that the mean value of ρ is relatively low for the former and high for the latter metal.

4.5. Conclusions

4.5.1. The Validity of the Analogue Model

The discrepancy between the experimental results and the predictions of the analogue model, noted in chapter 3, has been demonstrated to be due to two important shortcomings of the mathematical model in the present chapter. These shortcomings are the assumed current distribution, which differs markedly from the true distribution for low Q_D values, and the neglect of the contact resistances, which may cause deviations of a factor 4 or more from the computed temperatures

for high Q_D values. It is shown that these deviations are accounted for by means of a correction factor q , the value of which can be derived with acceptable correctness. In this way the temperatures of the weld are predicted satisfactorily as far as the border of the weld is concerned. Presumably, this is also true for the centre of the weld, in as far as the melting point of the weld metal is not exceeded.

Because of the extra heat production in the electrode-workpiece contact surfaces, however, the real temperature values in those areas become uncertain. As a consequence, the curves of the figures 2.11 to 2.14 inclusive can only be used as indications of the influence of the welding parameters on the mean electrode face temperatures.

A possible future research on the spot welding process might include the improvement of the RC-network with respect to both the electric contact resistances and the distribution of heat generation throughout the weld material.

In the present work it is shown that neither a solution of spot weld temperatures based on the production of the welding heat in the workpiece bodies only [6, 30, 31, 34], nor an approach based on the exclusive heat production in one or more contact surfaces [27, 34], will yield satisfactory results for a wide range of the electrode diameter to sheet thickness ratio.

4.5.2. The Choice of the Electrode Diameter

The electrode diameter D_E can be chosen from a wide range for a given thickness s of the sheets to be welded. The choice should be based on the weld diameter required to obtain a weld of sufficient strength [56]. In workshop practice, the working range of the welding equipment will play an important role in this choice, as has been demonstrated in section 3.2.3.

4.5.3. The Influence of the Electrode Material

It appears from the analogue as well as from the experimental results that the thermal and electrical conductivities of the

electrode material are of great importance to the temperature development in the weld, especially for long welding times and at the electrode tips. From a thermal point of view, these conductivities should be as high as possible. In practice, a compromise must be made between good conductivity on the one hand and satisfactory mechanical properties at high temperatures on the other.

From the analogue measurements it appeared that the volumetric heat capacity of the electrode c_E has no influence on the process (cf. section 2.3.2).

4.5.4. The Influence of the Electrode Force

The evaluation of the contact resistance R_k in section 4.3.2 is based on the assumption that the electrode force F has no influence on the value of R_k , in as far as F has a sufficiently high value to press the contact members towards each other when the contact spots are weakened by the passage of the electric current.

Nevertheless, references [54, 57] observe that for $Q_D > 4$ a decrease in electrode force

(a) not only decreases the maximum permissible welding current, but also reduces the current intensity required to obtain a weld of prescribed dimensions ($D_N < D_E$);

(b) reduces the maximum nugget diameter that can be formed.

Observation (a) may be explained by the following considerations. If the electrode tips are not exactly flat and parallel, a decrease in electrode force will reduce the macroscopic area of contact between electrode and workpiece, thus yielding a smaller effective electrode diameter and consequently, a lower Q_D value. For this reason, the body resistance R'_0 of the workpieces increases. The contact resistance will increase too, owing to the lower current intensity applied.

In this way, the total heat production i^2R may vary little for small variations in the effective electrode diameter. Observation (b) may be explained by the same mechanism, viz. a decreasing effective electrode diameter for lower electrode forces. Here, D_{Nmax} , which may be much greater than D_E , is brought about by the weld temperature reaching the equilibrium value θ_e .

In conclusion, a high value of the electrode force will cause smaller

deviations of the true contact diameter, which may equally originate from the presence of dirt particles between the contacting surfaces. Consequently, the variation in weld quality is lower for high electrode forces [4]. The often undesirable indentation of the electrodes into the workpieces when the weld weakens is reduced by the application of a programmed force. This force should have a high value at the beginning of the heating period and be substantially decreased before the end of that period.

Besides, the influence of the static packing friction in the air cylinder and of the inertia of the moving parts of the welding machine is also reduced by the application of high electrode forces.

4.5.5. Representation of the Results

A definitive version of the dependence of Q_{θ} on Q_t for the nugget border is graphically represented in fig. 4.7. In order to obtain the curves demonstrated, the results of the analogue measurements for $Q_{\lambda} = 8$ are corrected by means of formula (4.41) with $\zeta = 0.15$ and $f(Q_D)$ taken from fig. 4.3.

An experimental affirmation for conditions outside the range of our experiments is found in [24] for very thin sheets. It concerns the spot welding of 0.15 mm mild steel with a 0.75 mm electrode tip diameter by means of a capacitor discharge welder. The author has determined the current intensities required for welding times of 0.8 and 4 ms to be 2.15 and 1.36 kA respectively. Calculation of Q_t and Q_{θ} with the aid of the data from the tables 3.1 to 3.4 inclusive yields values of 0.24 and 1.2 respectively for the first product, and 0.164 and 0.41 respectively for the second. These results agree very well with the curve for $Q_D = 5$ of fig. 4.7.

From the universally usable curves of fig. 4.7 graphs can be derived which are easily to be interpreted in workshop practice. As an example, conditions are calculated for the spot welding of 1 mm low-carbon steel sheet, using electrode diameters of 3 up to 8 mm and a wide range of welding times and current intensities (see fig. 4.8). The electrode forces given are calculated from $Q_F = 0.2$, in accordance with equation (3.6).

It should be realised that the graphs given originate from a thermal

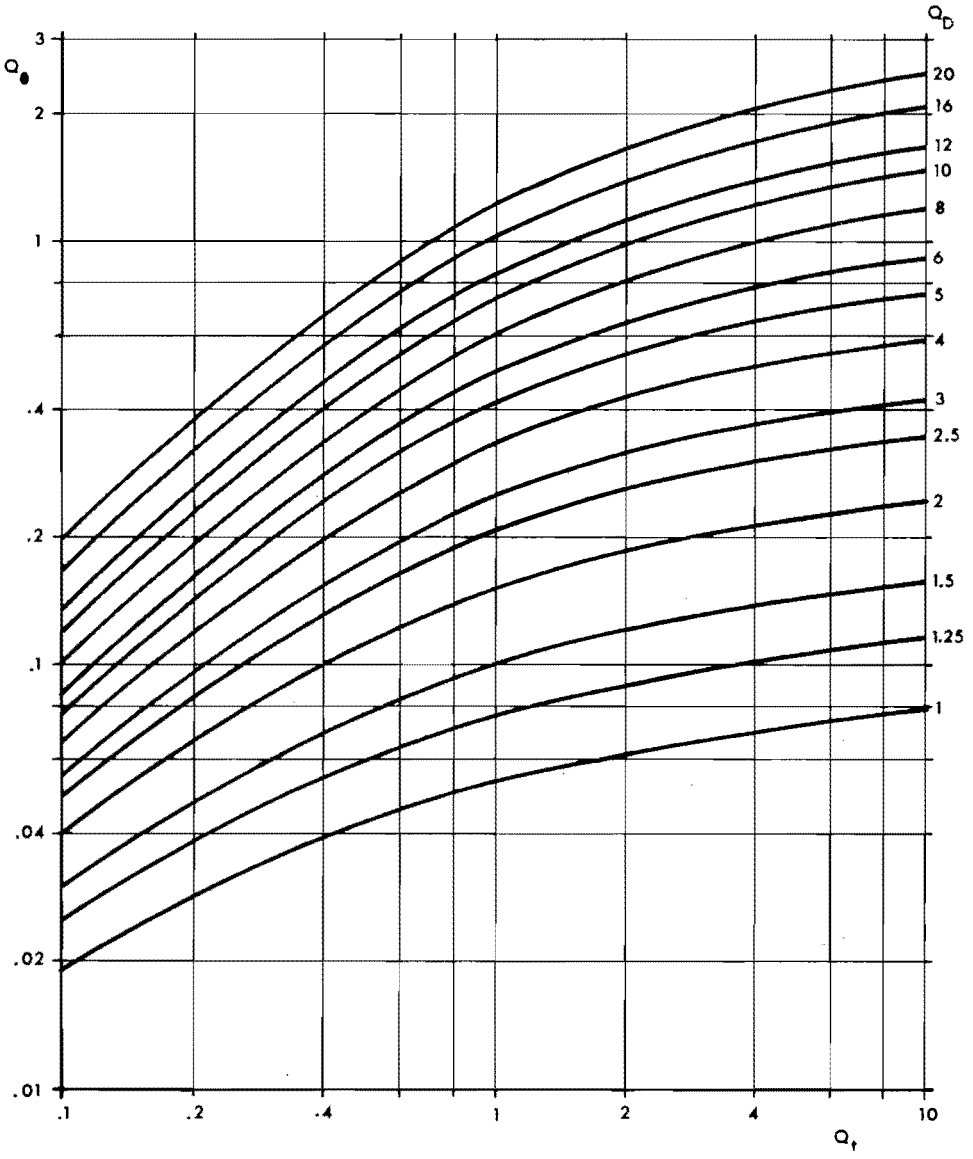


Fig. 4.7. Definitive Representation of Q_0 as a Function of Q_t for Different Values of Q_D .
 The graphs are valid for low-carbon steel and stainless steel ($Q_\lambda = 8$)

analysis only. In order to facilitate the choice of optimum welding conditions, data should be available from which the quality of the weld, made with any combination of welding parameters from these graphs, can be predicted. In chapter 6, an attempt will be made to link the thermal data to some quality criteria.

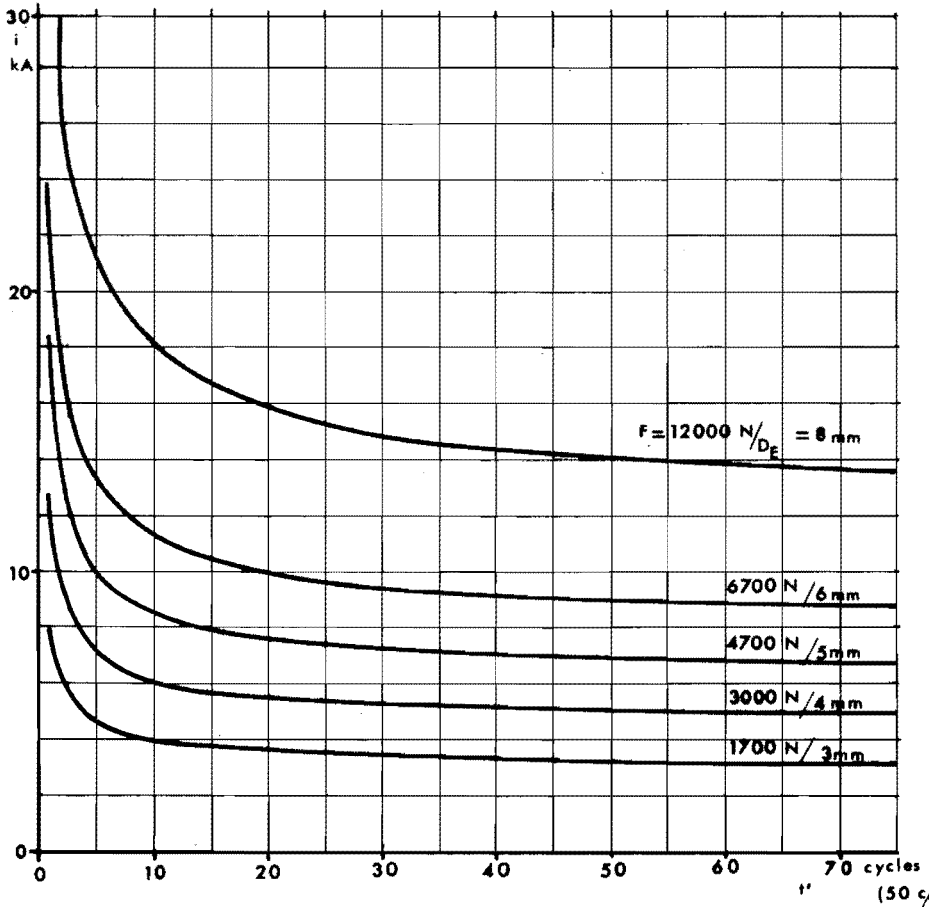


Fig. 4.8. Conditions for the Spot Welding of 1 mm Low Carbon Steel Sheet.
Electrode material is RWMA Class 2 [4]

Chapter 5. APPLICATIONS

5.1. Asymmetrical Geometry

5.1.1. Introduction

In this chapter, two cases are considered in which the geometrical arrangement differs from that described in chapter 1. They can be treated with the aid of the foregoing analysis, for which reason they are looked upon as applications of the present theory.

The first case concerns the welding of sheets differing either in thickness or in material, or in both. It is referred to as the case of asymmetrical geometry since there is no longer symmetry with respect to the plane $z = 0$.

In the foregoing analysis it was assumed that no heat would flow across the plane $z = 0$ for symmetry reasons. Hence, only the system consisting of one sheet and one electrode was considered. If, however, two different "weld halves", in which the temperature gradients in the direction of the z -axis are zero, are placed together and if certain conditions of continuity are fulfilled, this abstraction can still be applied.

The continuity conditions to be fulfilled are

- (a) the welding current in both "halves" should have the same intensity and distribution in $z = 0$,
- (b) the welding times should have the same values,
- (c) the temperature distributions in the plane $z = 0$ should be congruent at any instant.

As a matter of course, these requirements are exactly met only in the case of symmetry. However, if some of this exactness is relinquished a suitable set of requirements is left. This means that (a) is reduced to the requirement of equal current intensities and that (c) is simplified to the requirement of equal temperatures at the nugget border.

If the "weld halves" are labelled 1 and 2 the following conditions thus remain

$$\left. \begin{aligned}
 i_1 &= i_2 = i \\
 t'_1 &= t'_2 = t' \\
 \theta_1[B] &= \theta_2[B] = \theta[B]
 \end{aligned} \right\} \quad (5.1)$$

In the case of dissimilar sheet thicknesses only the following inequalities may exist

$$\left. \begin{aligned}
 s_1 &\neq s_2 \\
 D_{E1} &\neq D_{E2}
 \end{aligned} \right\} \quad (5.2)$$

and

$$\lambda_{E1} \neq \lambda_{E2} \quad (5.3)$$

while in the case of dissimilar workpiece materials the inequalities

$$\left. \begin{aligned}
 \lambda_1 &\neq \lambda_2 \\
 \rho_1 &\neq \rho_2 \\
 c_1 &\neq c_2
 \end{aligned} \right\} \quad (5.4)$$

may, in addition, be valid.

Since it is assumed that in the first case s_1 and s_2 are given, and in the second case the material properties, the conditions (5.1) can be fulfilled only by an adequate choice of the electrode tip diameters and/or of the electrode materials.

5.1.2. Choice of the Welding Conditions

The application of the results of the present investigations to the welding of workpieces having dissimilar thicknesses or physical properties is illustrated in this section by means of a few examples. First, however, the graphical representation of the experimental

results of chapter 3 has to be adapted to the purpose. In order to remove the electrode diameter D_E from the product Q_θ the latter is transformed into

$$Q_v = Q_\theta^{0.5} \cdot Q_D^{-2} = \frac{\pi}{4} \sqrt{\frac{\lambda \theta}{\rho}} \cdot \frac{s}{i} = b \frac{s}{i} \quad (5.5)$$

The definition (2.7) for Q_t is maintained,

$$Q_t = a \frac{t'}{s} \quad (5.6)$$

where a and b are averaged material constants.

The dimensionless product Q_v , as derived from the data of fig. 4.7, is graphically shown in fig. 5.1. These curves are valid for the spot welding of low-carbon steel and stainless steel, which metals are used in the present section for the examples to follow. The values of a and b are derived from the tables 3.1 and 3.2 and rearranged in table 5.1.

Table 5.1. Material Constants and Electrodes Used

material	a $m^2 \cdot s^{-1}$	b $A \cdot m^{-1}$	H_V $N \cdot m^{-2}$	electrode material
SS	4.7×10^{-6}	0.162×10^6	171×10^7	Class 3
St	6.74×10^{-6}	0.233×10^6	119×10^7	Class 2

It was supposed that the materials to be welded to each other, their thickness and the required diameter of the weld nugget were given. Since Q_{t1} and Q_{t2} will generally have different values, which should neither be extremely high nor extremely low, in order to avoid too slow heating or excessive currents, it appears to be good practice to choose the welding time in such a way that their geometric mean has a value of about 1.

Thus,

$$\sqrt{Q_{t1} \cdot Q_{t2}} \approx 1 \quad (5.7)$$

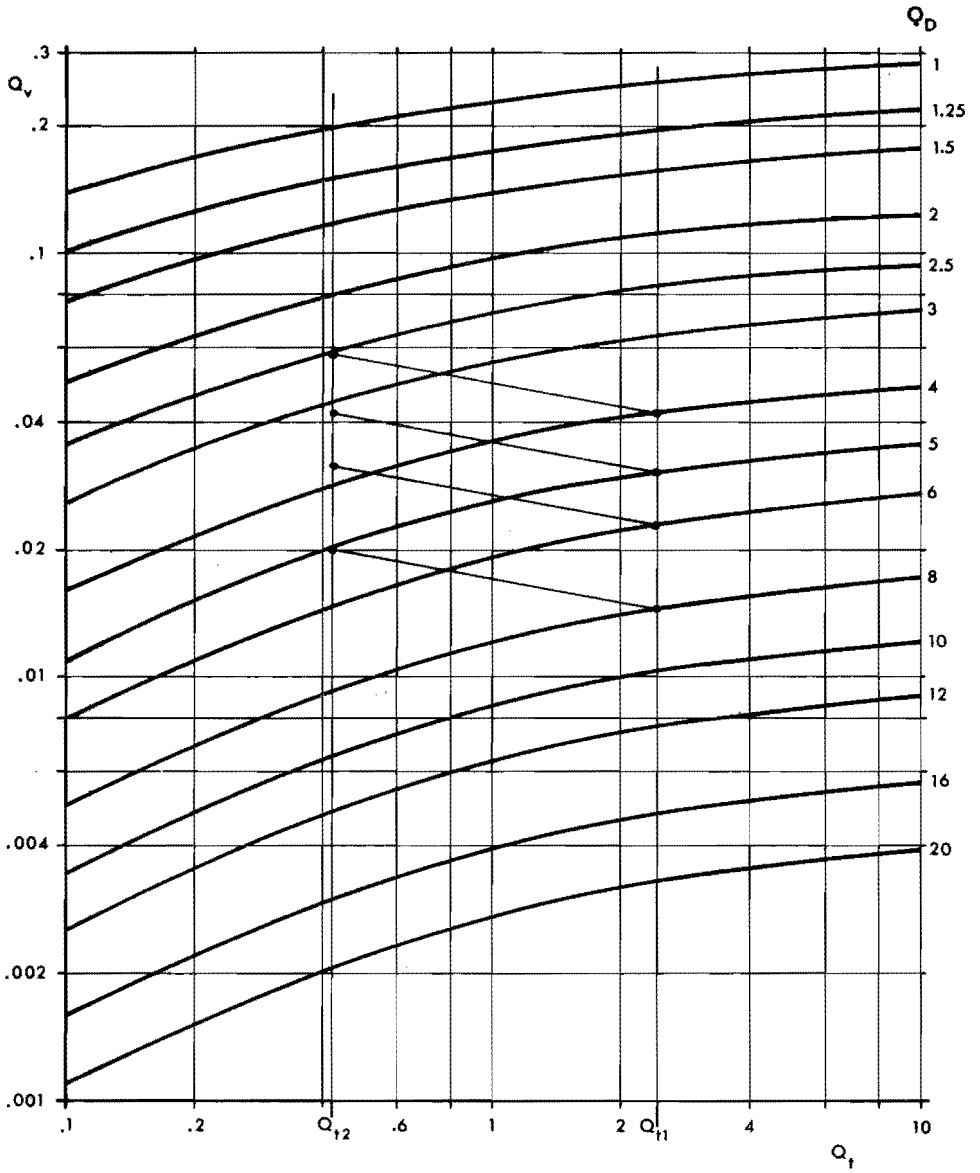


Fig. 5.1. Representation of the Dimensionless Product $Q_v = Q_0^{0.5} \cdot Q_D^{-2}$ as a Function of Q_t for Different Values of Q_D , as derived from Fig. 4.7.

which means that the welding time t' becomes

$$t' \approx \frac{s_1 s_2}{\sqrt{a_1 a_2}} \quad (5.8)$$

For the welding of 1 mm low-carbon steel sheet to a 2 mm stainless steel sheet, subscripted 1 and 2 respectively, t' attains the value of 0.36 s (18 current cycles). Then, $Q_{t1} = 2.43$ and $Q_{t2} = 0.423$. For $D_{E1} = 8$ mm, and hence $Q_{D1} = 8$, the value of Q_{v1} can be read to be 0.0145 from fig. 5.1.

Since

$$Q_{v2} = \frac{b_2 s_2}{b_1 s_1} Q_{v1} \quad (5.9)$$

and Q_{t2} is already known, the value of Q_{D2} is easily interpolated from the graph, thus yielding D_{E2} . The current intensity is calculated from

$$i = \frac{b_1 s_1}{Q_{v1}} = \frac{b_2 s_2}{Q_{v2}} \quad (5.10)$$

The same calculations can be carried out for different values of D_{E1} . The results are shown in table 5.2. The electrode forces are obtained by applying equation (3.6) to both weld halves and by choosing the lower value.

The calculation method demonstrated above was successively applied to the following combinations of sheets

- I $s_1 = 0.5$ mm SS; $s_2 = 1$ mm SS; $D_{E1} = 3, 4, 5$ and 6 mm;
- II $s_1 = 0.5$ mm SS; $s_2 = 2$ mm SS; $D_{E1} = 3, 4, 5$ and 6 mm;
- III $s_1 = 1$ mm SS; $s_2 = 2$ mm St; $D_{E1} = 4, 5, 6$ and 8 mm;
- IV $s_1 = 1$ mm St; $s_2 = 2$ mm SS; $D_{E1} = 4, 5, 6$ and 8 mm.

The welding conditions thus determined were experimentally verified afterwards.

Table 5.2. Calculation of the Conditions for the Welding of 1 mm St to 2 mm SS Sheet with the Aid of Fig. 5.1

$s_1 = 1 \text{ mm St}; s_2 = 2 \text{ mm SS}; t' = 0.36 \text{ s}$							
D_{E1}	Q_{D1}	Q_{V1}	Q_{V2}	Q_{D2}	D_{E2}	i	F
mm					mm	kA	kN
4	4	0.042	0.058	2.5	5	5.5	2.9
5	5	0.030	0.042	3.1	6.2	7.6	4.5
6	6	0.023	0.032	3.7	7.4	10.1	6.4
8	8	0.0145	0.020	5.0	10	16.0	11.5

5.1.3. Verification

The verification of the welding conditions determined in the foregoing section for the spot welding of dissimilar workpieces, showed the applied calculation method to be very successful. Yet, it seemed to be necessary to increase the computed current intensities by 0 to 8 per cent., especially for low Q_D values. Apparently, the weld nugget tends to form in the area half-way the distance between the electrode faces when the influence of the contact resistance is small, which is the case for low Q_D values [39]. Besides, the errors both of the predicted values and of the measurements should not be expected to be smaller than five per cent.

The values of the current intensity required to obtain a weld nugget of prescribed dimension appeared to be very critical. However, this is true for any spot welding condition, owing to the fact that for a given welding time the temperature reached in an arbitrary point of the workpiece is proportional to the square of the current intensity. Principally, the described method is applicable to any combination of metals to be welded, premised that the melting temperatures do not differ too much, and that the metals concerned tend to alloy with each other to some degree [1].

5.2. The Spot Welding of Pure Copper

5.2.1. Method

Since the weldability of a metal varies inversely with its electrical and thermal conductivities [2], the spot welding of pure copper (more than 99.9% Cu) is extremely difficult. This is demonstrated in fig. 2.12 where copper electrodes are used. According to this figure, only relatively long welding times and extremely small ratios of electrode tip diameter to sheet thickness would prevent the electrodes from welding to the workpieces, producing as a consequence small weld nugget diameters. The presence of contact resistances makes the situation still worse. The value of the electrode-to-workpiece resistance is fundamentally the same as that of the workpiece-to-workpiece resistance. Since the heat production in the first is confined to a smaller area than in the second, owing to the "bulging" of the current in the workpieces, this heat tends to increase the electrode temperature in particular. A solution for this problem is found in using an electrode material with a very high melting point, such as tungsten [58].

Another method was used in the present investigations, based on the theoretical considerations of section 4.2. This method is elucidated in fig. 5.2. It consists in inserting a very thin foil of an

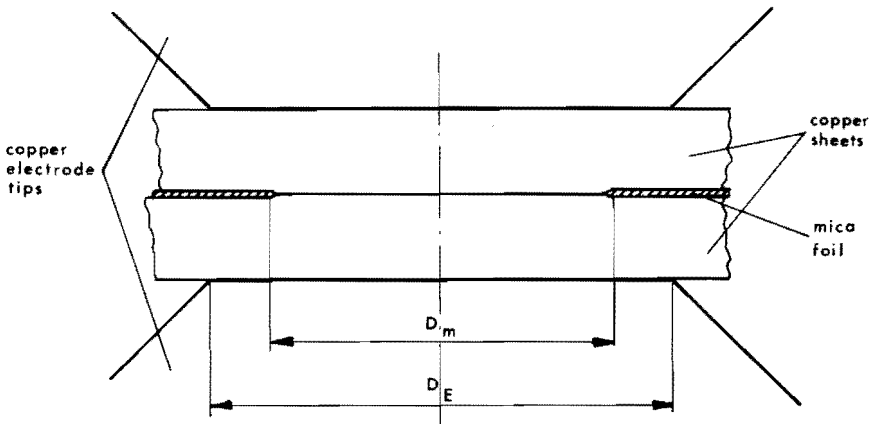


Fig. 5.2. The Spot Welding of Copper by Means of an Artificial Current Constriction

electrically non-conducting material between the sheets to be welded. A hole, having a diameter D_m , equal to that of the weld nugget required, is punched in the foil. The electrode tips have diameters which are substantially greater than D_m . They are positioned centrally with respect to the hole. The electrodes press the copper sheets upon each other, with such a force that in the area of the hole there is metallic contact between them before the welding current starts to flow.

High demands are made on the material of the foil. In fact, it must be able to withstand very high pressures and temperatures. The foil must be extremely thin to facilitate the metallic contact. A mica foil of about 0.02 mm proved to give satisfactory results.

The objective of such a geometry is to obtain a high current density, and thus a high specific heat production in the area where the weld has to form, without affecting the heat flow to the electrodes. In this way the bulging of the electric current near the workpiece interface is effectively prevented.

5.2.2. Experimental Results

The spot welding of electrolytic copper sheets was carried out for the welding conditions given in table 3.5. Except for the geometrical arrangement of fig. 5.2 the general method was the same as that described in section 3.1. A somewhat deviating definition of the dimensionless products Q_D and Q_θ was applied by using the hole diameter D_m instead of the electrode tip diameter D_E in the equations (2.7) and (2.8), thus

$$Q_D = \frac{D_m}{s} \quad (5.11)$$

$$Q_\theta = \frac{\lambda \theta_m}{\rho j^2 s^2} = \frac{\pi^2 \lambda \theta_m D_m^4}{16 \rho i^2 s^2} \quad (5.12)$$

The electrode diameter D_E was maintained at a value of about 8.5 mm in all cases.

The resultant joints were sound welds with high strength and nugget

diameters of the same dimension as D_m . The welding time t' proved to be more critical than for the welding of the previous metals, since the tendency of the workpieces to weld to the electrodes was considerably greater.

On the basis of the considerations of chapter 4 it might be expected that the ratio q , defined in equation (3.8), would depend on Q_D in the same way as in relation (4.40). This, indeed, appeared to be true if the definitions (5.11) and (5.12) were applied, viz.

$$q = \frac{\phi}{\phi_0} = f' \left(\frac{D_m}{D_E} \right) + \zeta Q_D \quad (5.13)$$

However, the significance of the function $f'(D_m/D_E)$ differs from that of the previous $f(Q_D)$ because of the deviating geometry of fig. 5.2 (cf. section 4.2). Here, the body resistance R'_0 of the welding work is written

$$R'_0 = \frac{8\rho s}{\pi D_m D_E} \quad (5.14)$$

as an approximation. R'_0 represents twice the resistance of the truncated cone of fig. 5.3. The result (5.14) is easily obtained by

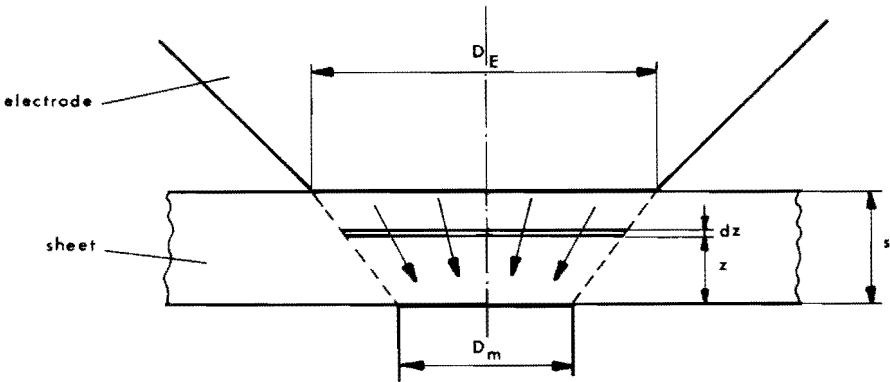


Fig. 5.3. Assumed Path of Current Flow for the Case that $D_E > D_m$

integrating the resistance of an infinitely thin cylindrical slice with radius

$$r(z) = \frac{D_m}{2} + \frac{D_E - D_m}{2s} z$$

and thickness dz over the range $0 < z < s$.

If in the expression for R_o (4.1) the electrode diameter is replaced by D_m as well, the function f' becomes

$$f' \left(\frac{D_m}{D_E} \right) = \frac{R_o'}{R_o} = \frac{D_m}{D_E} \quad (5.15)$$

Thus, f' represents the ratio of the true body resistance between the electrode tips and the resistance of the cylinder with height $2s$ and diameter D_m , which resistance was exclusively considered in the analogue model. Because of the considerations of section 4.2, the function f' also represents the ratio between the true and the assumed heat development in the workpiece bodies, as in equation (5.13). The constant ζ in that equation appeared to have the value of 0.12 for the spot welding of pure copper.

In fig. 5.4 the correspondence of the relation (5.13) with the experimental results is demonstrated.

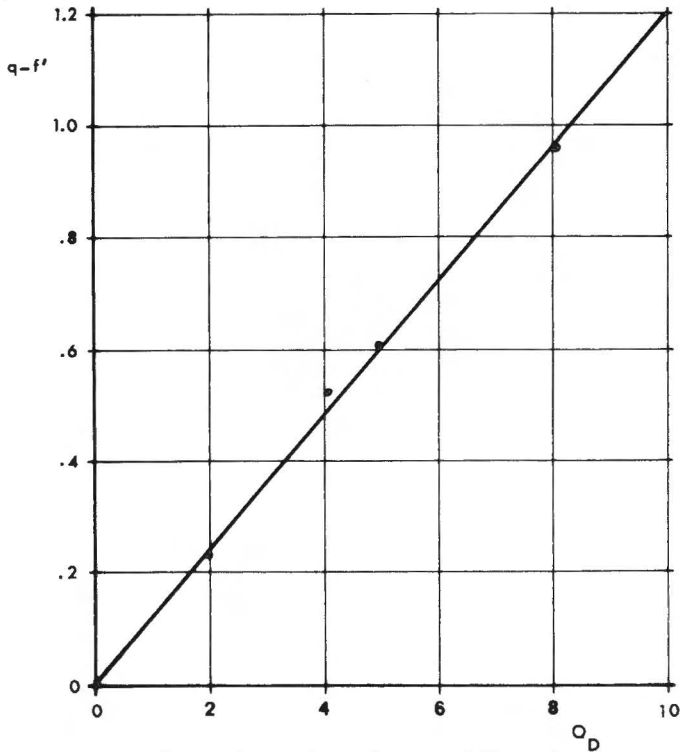


Fig. 5.4. Experimental Results of the Welding of Copper Sheet

5.2.3. Conclusions

By inserting a non-conductive foil of a few hundredths of a mm thickness between the sheets, the weldability of electrolytic copper is considerably improved with respect to the following points.

(a) The welding current required to make a weld of prescribed dimensions is lowered.

(b) The tendency of the workpieces to weld to the electrode tips is reduced.

(c) The appearance of the weld is improved by the use of larger electrode tip diameters, resulting in smaller indentations in the surfaces of the workpieces.

The method described looks very much like the projection welding process, to which the same advantages are adjudged [1]. Relative to the plain spot welding geometry, both methods have the disadvantage of a more laborious preparation of the welding work.

In the scope of the present work, however, the most important aim in using the described method was not the development of a new method of spot welding but a further verification of the assumptions made in the last paragraph of section 4.1.

In conclusion, the errors, introduced in the mathematical model of chapter 2 by the use of too unrealistic simplifications regarding current distribution and contact resistances, are fully removed by correcting the heat development assumed in the model. This correction has to depend on the ratio R/R_0 of the true total resistance of the workpieces to that assumed in the mathematical model, in the way described in relation (4.4).

Chapter 6. QUALITY CONTROL

6.1. Quality of Spot Welds

6.1.1. Introduction

In the foregoing chapters an analysis of the thermal aspects of the spot welding process was presented. With the aid of the derived relations between the welding parameters it appeared to be possible to determine adequate welding conditions if the materials to be welded, their dimensions and the required size of the weld were given. A graphical representation of these conditions was suggested in fig. 4.8. From this figure it appears that either the welding current or the welding time may be chosen freely for the obtainance of a weld of prescribed dimensions.

In order to facilitate the choice of optimum welding conditions, attention must be paid to the quality of the welds thus made. However, a fundamental difficulty lies in the concept of weld quality, since this concept cannot be defined without referring to the demands made on the application for which the joint under consideration is intended. As a consequence, a great number of quality criteria is in use in industry. A review of commonly applied testing methods of spot welds is found in literature [4, 59, 60]. Each of these methods implies the use of its intrinsic quality criterion.

The variety of criteria may be reduced to the investigation of a few important weld characteristics, viz.

- (a) the external appearance of the joint made,
- (b) the mechanical strength of the weld under various conditions.

Other criteria used, such as the structure and the homogeneity of the weld metal and the presence of residual stresses owing to the thermal cycle, generally are a means of investigating characteristic (b).

A third important characteristic concerns the technology of the welding process rather than the quality of the weld made, viz. the life of the electrode tips. This factor is considered in literature [31, 45]; it was not investigated explicitly in the experiments

under review, although general conclusions may be drawn from section 2.3.2 as to the height of the electrode tip temperatures, which strongly influence electrode tip life [31], in dependence on Q_D and Q_λ .

The characteristics (a) and (b) will be discussed in the following sections.

6.1.2. The Appearance of Spot Welds

The appearance of the spot weld, involving the phenomena of sheet separation and of surface indentation (cf. fig. 6.1), in addition to external defects such as pits, tip pickup and external cracks, is of importance for a number of applications. These applications concern especially those cases, where aerodynamic considerations play an important role, where demands are made on the tightness of the joint or where a good appearance is necessary, as in the manufacture of motor-car bodies or household appliances.

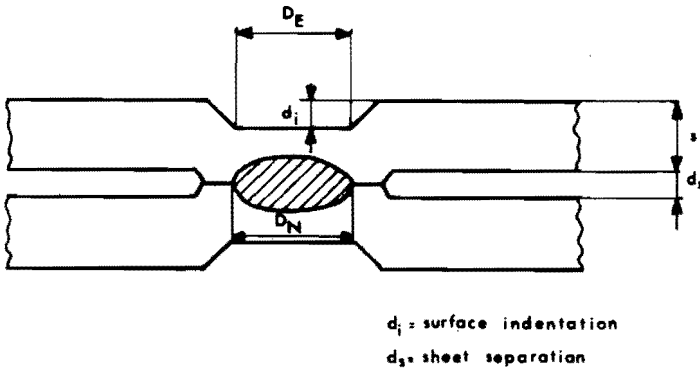


Fig. 6.1. Appearance of a Spot Welded Joint

d_i = surface indentation

d_s = sheet separation

The American Military Specifications [10] consider both the sheet separation d_s and the surface indentation d_i unacceptable for high-quality welds if values of 10 per cent. of the sheet thick-

ness are surpassed. The corresponding German Recommendation [14] gives a same value for d_i , but does not mention sheet separation. A phenomenological description of the deformations occurring in the environment of the weld as a consequence of the thermal cycle was given in section 3.4.1. From our experiments it appeared that the greater part of the total sheet deformation takes place after the weld nugget has formed. The following two cases are to be distinguished.

(a) Weld type AS or CS (cf. fig. 3.6). If the weld metal splashes away between the sheets when the weld nugget reaches its required size, a markable indentation d_i results, the value of which is unpredictable since it depends on the accidental weakness of the wall surrounding the molten pool (cf. section 3.4.1).

(b) Other weld types (cf. fig. 3.5). Our statistical analysis of the influence of a number of welding parameters, among which were the products Q_D and Q_θ and the ratio t_h/t' of the applied heating time to the required welding time, revealed that

$$\frac{d_i}{s} \sim Q_D^n \cdot \left(\frac{t_h}{t'} - 1 \right)^{0.5} \quad (6.1)$$

The effect of the ratio t_h/t' is far more pronounced than that of the product Q_D , the exponent n of which seemed to have a value of about 0.25, whilst the influence of Q_θ appeared to be insignificant.

In other words, the ultimate deformations are very sensitive for the precise value of the heating time. They are very small if the heating time is just long enough to permit the formation of a full-sized weld ($t_h = t'$). A similar relation is valid for the relative sheet separation d_s/s ,

$$\frac{d_s}{s} \sim Q_D^m \cdot \left(\frac{t_h}{t'} - 1 \right)^{0.5} \quad (6.2)$$

although the statistical significance of the influence of Q_D is smaller than in (6.1).

The observations regarding the disadvantageous effects of too long heating times are in agreement with workshop experience [10, 14].

The other external defects of spot welds mentioned above, appear to be dependent on the electrode face temperature. Especially the tendency of the electrodes towards sticking to the sheets, and hence the occurrence of electrode pickup on the outer contact surfaces of the workpieces, increases with higher electrode face temperatures [31]. Our observations indicate that these phenomena become more serious if the heating time is too long ($t_h > t'$), i.e. if the electrodes indent considerably into the sheets, thus resulting in both a higher effective Q_D value and increasing electrode face temperatures.

6.1.3. The Strength of Spot Welds

The most widely used quality criteria for resistance welds are those regarding the strength of the weld made. Direct tests having a destructive character, are generally used to check the strength of the joint under circumstances identical to those of the actual application. Commonly applied examples of these tests determine the shear strength, the fatigue strength or the impact strength. Since the first is comparatively easy to be determined, it is frequently used as a quality criterion [4, 10, 14].

However, several investigators observe that the static shear strength F_s of a spot weld exclusively depends on the diameter D_N of the weld nugget formed [56, 57]. Since this diameter can be influenced at will by adjusting the welding parameters current and heating time, and by choosing an adequate electrode diameter, the authors consider neither the shear strength nor the nugget diameter a yardstick for weld quality. They reject the prescription of one special electrode and weld nugget diameter for a given sheet thickness to be welded, i.e. the use of equations (3.4) and (3.5). An affirmation of these points of view is found in the present work. Two different modes of fracture are observed for welds having a nugget diameter $D_N \approx D_E$, depending on the dimensionless product Q_D , viz.

$$F_s = \sigma_s D_N \left(s - \frac{d_1}{2} \right) \quad \text{for} \quad Q_D > 4, \text{ approximately} \quad (6.3)$$

and

$$F_s = \tau_s \frac{\pi}{4} D_N^2 \quad \text{for} \quad Q_D < 4, \text{ approximately} \quad (6.4)$$

The average values of the constants σ_s and τ_s are given in table 6.1, compared with the ultimate tensile strength σ_M of the materials investigated (cf. table 3.1).

Table 6.1. The Constants σ_s and τ_s from the Relations (6.3) and (6.4)

material	σ_s	τ_s	σ_M	σ_s/σ_M	τ_s/σ_M
SS	159	54.2	61.4	2.6	0.88
St	150	57.3	38.8	3.9	1.48
Zn	34.6	10.0	14.1	2.5	0.71
Al	22.1	5.6	10.8	2.1	0.52
Cu	57.5	15.3	25.8	2.2	0.59
	$\times 10^7 \text{ N.m}^{-2}$	$\times 10^7 \text{ N.m}^{-2}$	$\times 10^7 \text{ N.m}^{-2}$		

As pointed out, equation (6.3) is valid for $Q_D > 4$. The fracture occurs in the circumference of the weld nugget, resulting in the nugget being entirely torn out of one of the sheets. In fact, the joint does not yield in the weld nugget, but beside it. The other type of fracture, for which relation (6.4) holds, occurs by shearing of the original sheet interface.

Though it is not the author's intention to present a thorough analysis of the strength of spot welds, the high values for the constants σ_s and τ_s , given in table 6.1 for low-carbon steel need some comment.

It was observed that instead of a sound weld nugget, in which the metal has been liquefied and well stirred, a different type of bond develops between the workpieces when the welding current or the

heating time have insufficient values. In contrast with the sound weld, with its rough-looking fracture face after shearing, the appearance of the fracture face, which always coincides with the original plane $z = 0$, is very smooth in the other type. Although the dimension of the area of coherence cannot be easily determined, since it gradually shades off into the surrounding non-bonded sheet surface, the maximum value of the constant τ_s can be estimated to be equal to about $23 \times 10^7 \text{ N.m}^{-2}$ both for stainless and for low-carbon steel. This type of bond was observed in particular in welding steels and copper. Since an area of this type always surrounds any well-developed weld nugget in these materials, part of the shearing force will be carried by it, which results in high values of σ_s and τ_s .

The existence of the described area of partial coherence may be explained by the presence of a large number of grown-out current constrictions, the temperatures of which equal the melting point as described in section 4.3.2 (cf. fig. 3.1).

So far, no experimental results are available with regard to the influence of the welding parameters i and t' on the fatigue strength or the impact strength of spot welds. It appears that a more extensive welding cycle, comprising pre-heating and especially a post-weld heat treatment or forging period, or both, is required in order to obtain welds with optimum fatigue strength [61, 62, 63].

6.1.4. Conclusions

In the foregoing section the static shear strength appeared to be no useful criterion in determining the quality of spot welds. Instead, GLAGE [56] suggests to judge weld quality on the basis of the following criteria.

- (a) Deformation of the workpiece surfaces (cf. section 6.1.2);
- (b) the size of the heat-affected zone outside the weld nugget;
- (c) the corrosion resistance of the weld;
- (d) sheet separation (cf. section 6.1.2);
- (e) the statistical standard deviation of the strength properties (cf. [64]);
- (f) position, shape and metallurgical structure of the weld nugget;
- (g) the presence of cracks in the welded material.

Such a definition of weld quality only has practical value if there is a relation between this quality and the behaviour of welds in actual constructions. It seems that particularly the criteria (b), (f) and (g) are of importance to the fatigue strength of the joint [62], especially in so far as they influence the presence of residual stresses after welding [61, 63]. At any rate, the criteria (a) to (g) should be defined unambiguously and numerically in order to facilitate a uniform interpretation by any investigator. Further research must decide whether GLAGE's suggestions contain useful quality criteria compared with the results of fatigue tests. Using these criteria when comparing welds made in 1 mm low-carbon steel with different combinations of D_E , i and t' , GLAGE made a division into five quality classes I, A, B, C and D in order of quality. When the nugget diameter is chosen on the basis of the shear strength required, and the electrode diameter D_E is taken equal to D_N , the welding time t' and the current intensity i follow from

$$t' = v_1 D_E \quad (6.5)$$

$$i = v_2' t' = v_2 D_E \quad (6.6)$$

where the constants v_1 and v_2 depend on the weld quality as in table 6.2.

Table 6.2. The Constants v_1 and v_2 from Relations (6.5) and (6.6)

quality class	v_1	v_2
I	14	2.5
A	30	1.63
B	70	1.5
C	134	1.38
D	226	1.2
	ms.mm ⁻¹	kA.mm ⁻¹

The values of i and t' computed from table 6.2 with the aid of the relations (6.5) and (6.6) agree very well with the data of fig. 4.8, which are likewise valid for the welding of 1 mm low-carbon steel, in as far as the highest quality class I is considered. For lower quality and large diameters, however, the computed current intensities are up to 20% too low, compared with those of fig. 4.8. This is undoubtedly due to the low electrode force, which was chosen in dependence on i only. So when welding with $D_E = 8$ mm and $i = 11$ kA (class C) the electrode force F had a value of 2.5 kN instead of the value of 12 kN given in fig. 4.8. The influence of a too small electrode force was explained in section 4.5.4.

In conclusion, a shorter welding time and consequently a higher current intensity appears to result in welds with a better quality if the criteria (a) to (g) are used. The application of high current values, on the other hand, increases the probability of molten metal splashing from between the workpieces during the heating period (cf. section 3.4.1), possibly resulting in excessive surface indentations and sheet separation.

If the external appearance of the welds is not of primary importance, high welding currents and short heating times may be applied. If splashing is undesirable, the welding time should not be taken too small. In that case, it seems to be a good compromise to choose t' in such a way that $Q_t \approx 1$. Another possibility of controlling the weld appearance lies in the application of a programmed force, being high at the beginning of the heating period and low when the weld metal is molten (cf. section 4.5.4).

In all cases, both the surface preparation (cf. section 4.3.1) and the accurate adjustment of the welding variables current and time are extremely important.

6.2. Adaptive Control of the Spot Welding Process

6.2.1. The Necessity of Adaptive Control

Resistance spot welding has two distinctive features. First, welds can be made very quickly (speeds of 100 spots/min are often used); second, most of the parameters can be preset on the control unit.

This in turn explains why the process is favoured for mass production and automation. Unfortunately, the speed with which welds are made implies that, when the process functions incorrectly, a large number of defective welds could be made before they are detected. Where spot welding is completely automated, there is a particular demand for a reliable test of weld quality. In addition, where every spot weld must be of high quality, there is a demand for effective quality assurance for each weld [53].

It was concluded in the foregoing sections that the accurate adjustment of the main welding variables current and time is of predominant importance for weld quality. Owing to the influence of relatively small variations in the welding conditions this adjustment should have a variable character. Examples of such variations are deviations of the nominal supply voltage or of the sheet thickness, increase in electrode tip diameter owing to electrode wear, variations in the surface quality of the sheet welded and shunting effects of the welding current [26].

Since the conditions for each individual weld may thus vary, it is necessary that the welding variables are adjusted while the weld is made. Because of the short duration of the process such an adjustment should be effectuated automatically, governed by a process variable, the behaviour of which is a useful indication of the quality of the weld being made. Consequently, for the purpose of such an "adaptive control" an adequate control variable must be available.

6.2.2. The Selection of a Control Variable

The object is to find a process variable that gives an indication of the quality of the developing weld during the initial phase of the heating cycle. This control variable must allow an interpretation of the direction in which the welding parameters are to be changed during the heating period if the weld is likely to become inferior.

If the size of the weld nugget being formed, or the ultimate values of the temperatures developing in the weld are taken as a satisfactory criterion for weld quality, a number of such control variables is available. The most important of them were mentioned

in section 3.4.1, viz. the electrode movement d and the total electric resistance R of the weldment.

Adaptive control mechanisms using the variation of the total resistance or of the voltage across the workpieces as a control variable are described in references [26] and [65]. Although this type of control mechanism is very useful in a number of cases, a more generally applicable system is that using the electrode movement as the control variable [50, 66], since the latter is a direct measure for the mean value of the temperatures developing during the heating cycle, as will be shown in the next section.

6.2.3. The Electrode Displacement

A detailed analysis of the magnitude of the electrode displacement, which is a consequence of the thermal expansion of the workpiece materials during the heating cycle, is considered to be outside the scope of the present work. However, a few interesting observations were made with respect to the electrode movement, which will more easily be understood if the general physical background is considered.

The linear expansion d of a slab with thickness $2s$ and an average temperature $\bar{\theta}$ may be written

$$d = 2\mu s \bar{\theta} \quad (6.7)$$

where μ is the coefficient of linear thermal expansion. The average value $\bar{\theta}$ is assumed to be dependent on the temperature θ of the point $B(z = 0, r = D/2)$, defined in section 2.3.1, as

$$\bar{\theta} = c_1 \theta \quad (6.8)$$

with c_1 being a specific function of Q_D and Q_t (cf. figs. 2.11 to 2.14). The derivative of d with respect to time at the beginning of the heating period can then be written, neglecting the dependence of c_1 on Q_t ,

$$\lim_{t \rightarrow 0} \frac{dd}{dt} = 2\mu_0 c_1 s \lim_{t \rightarrow 0} \frac{d\theta}{dt} \quad (6.9)$$

where μ_0 denotes the value of μ at room temperature. Using the equations (3.8), (4.30) and (4.31) this formula can be rewritten

$$\lim_{t \rightarrow 0} \frac{dd}{dt} = \mu_0 c_1 s q \frac{\theta_m Q_t'}{t' Q_{\theta m}} = \frac{\mu_0 c_1 \theta_m a}{s Q_{\theta c}} \quad (6.10)$$

By introducing the dimensionless quantity

$$\delta = \frac{s}{a} \lim_{t \rightarrow 0} \frac{dd}{dt} \quad (6.11)$$

relation (6.10) is simplified to

$$\delta = c_2 Q_{\theta c}^{-1} \quad (6.12)$$

in which relation $c_2 = \mu_0 c_1 \theta_m$ depends on the metal welded and on the distribution of the temperatures throughout the heated zone. Some other important factors influencing the value of the rate of electrode displacement at the beginning of the heating period are neglected in the above derivation.

(a) The expansion of the workpiece metal in the radial direction is partly impeded by the presence of the cold metal surrounding the heated area. As a result of this, the expansion in the direction of the electrode axis will exceed the value given by relation (6.7).

(b) The electrode force F counteracts the thermal expansion. Since the electrode pressure is kept constant according to relation (3.6) in the present investigations, no serious deviations from (6.12) are expected. Only where the value of F is of the same order as that of the static friction force in the air cylinder F_f , the resultant electrode force, lying somewhere between the limits F and $F + F_f$ during the expansion of the workpiece metal, becomes too high.

The initial values of dd/dt were graphically determined from the oscillograph registrations and converted to values of δ in order to

check relation (6.12). It appeared that the true relation differs slightly from that formula, viz.

$$\delta = cQ_{\theta c}^{-4/3} \quad (6.13)$$

for $F > 3$ kN. For smaller electrode forces the influence of F_f

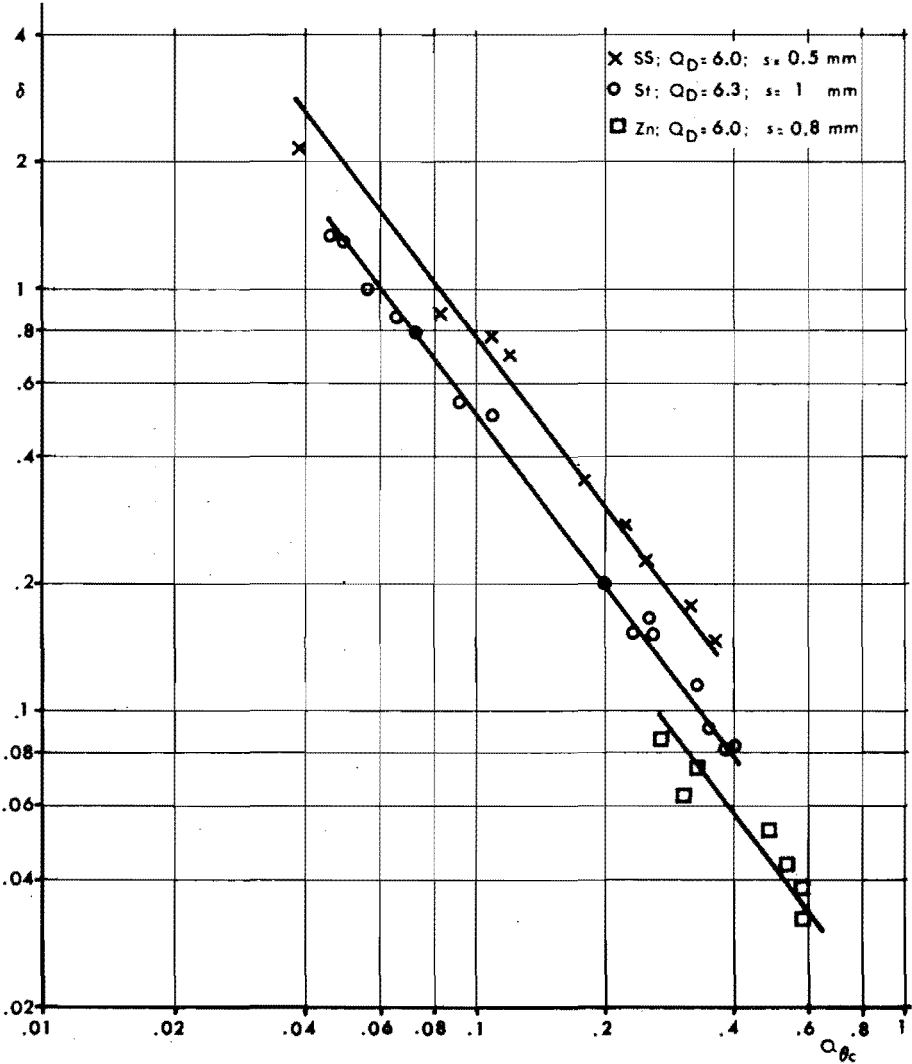


Fig. 6.2. The Initial Expansion Rate δ as a Function of $Q_{\theta c}$ for the Welding of Different Materials

prohibits a clear interpretation of the results. The appearance of the exponent of $4/3$ instead of 1 in (6.13) may be explained by the influence of the rate of heat production on the temperature distribution in the heated area. A high heat production rate, i.e. a low Q_t value, results in high ratios of both $\theta[C]/\theta[B]$ and $\theta[E]/\theta[B]$, which means high average temperatures, and thus a high value of c_1 in equation (6.8). This was illustrated earlier in figures 2.11 to 2.14. According to the first figure, dc_1/dQ_t and dc_1/dQ_θ are negative, resulting in an exponent <-1 in (6.13). Figs. 2.12 to 2.14 explain the influence of the product Q_D . High Q_D values result in high $\bar{\theta}$ so that the constant c has a high value. Fig. 6.2. shows the dependence of δ on $Q_{\theta c}$ for a few illustrative cases, and fig. 6.3 demonstrates the dependence of c on Q_D for the welding of stainless steel. The latter figure suggests a generalisation of equation (6.13), viz.

$$\delta = c_0 Q_D^n Q_{\theta c}^{-4/3} \quad (6.14)$$

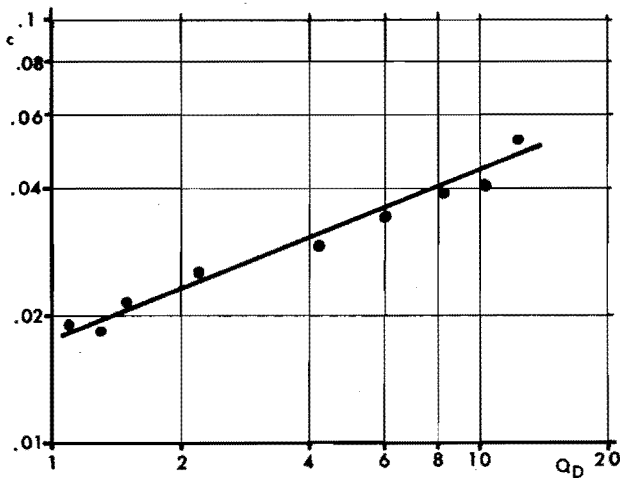


Fig. 6.3. The Dependence of the Constant c from Relation (6.13) on Q_D for the Welding of Stainless Steel

Another important characteristic of the electrode movement is the maximum displacement d_{\max} reached during the welding cycle. The relative maximum displacement

$$\Delta = \frac{d_{\max}}{s} \quad (6.15)$$

is expected to be dependent on $\bar{\theta}$, analogously to δ . This proved to be true in our experiments, although the influence of the static friction force F_f again camouflages the true relation between the welding variables under review. Generally, Δ increases with higher values of Q_D , although the relation is not simply one of linear proportionality, as is shown in fig. 6.4. It even seems that there is a maximum value of Δ at $Q_D \approx 7$ for aluminium. It is improbable that a thorough analysis of the electrode movement can be given

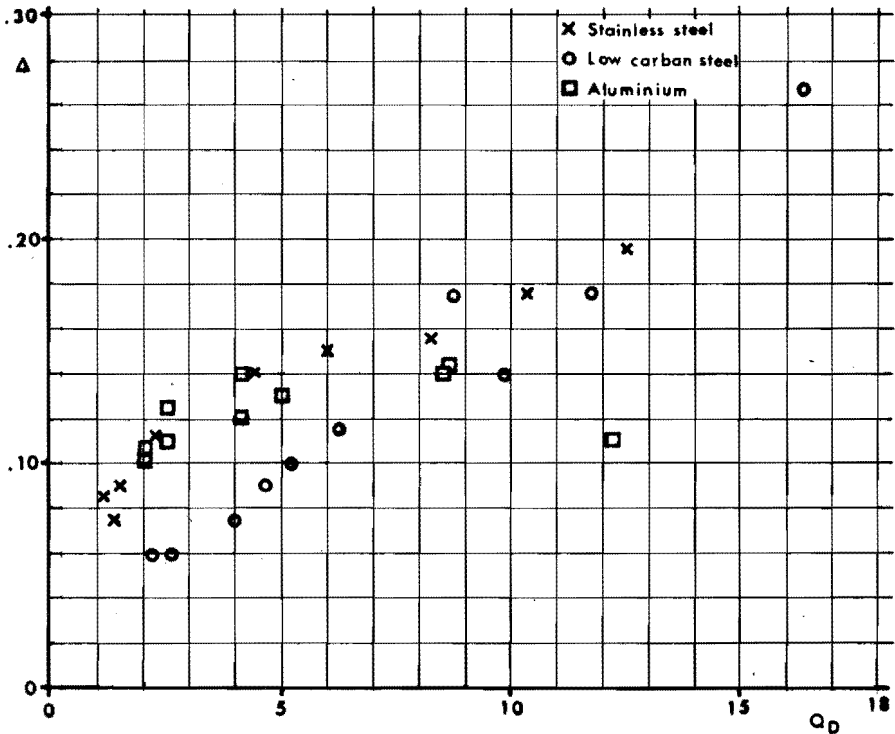


Fig. 6.4. The Dependence of Δ on the Value of Q_D for Different Materials

without taking the mechanical stress distribution and the creep properties of the welded metal at high temperatures into consideration. Further research on this subject will be necessary. Nevertheless, an experimental determination of the maximum

electrode displacement offers an excellent possibility of controlling the proper welding time, as was concluded earlier in section 3.4.1.

6.2.4. Conclusions

From the observations described in the foregoing sections the following important conclusions may be drawn with respect to the control of resistance weld quality.

(a) The initial rate of electrode displacement δ is an adequate measure for the quantity $Q_{\theta c}$ calculated with the aid of the analogue model, or, since the factor q is known from chapter 4, for the actual value $Q_{\theta m}$.

(b) Since the quality of the weld seems to depend to a considerable extent on the rate of energy production (cf. section 6.1.4) and thus on the value of Q_{θ} , the quantity δ can be considered a measure for the quality of the developing weld.

(c) The proper adjustment of the heating time is of predominant importance for the quality of the weld made, especially in so far as the appearance of the weld is considered (cf. section 6.1.4).

(d) At the time when the maximum electrode displacement is reached, the weld nugget has obtained a diameter equal to that of the electrode tip (cf. section 3.4.1). Hence, the ultimate value of the electrode displacement is a means of controlling the proper weld time.

Obviously, the design of an adaptive control mechanism should be realised on the basis of the foregoing conclusions. An electric voltage signal u , proportional to the electrode displacement d is easily obtained from a displacement transducer. Then, the first derivative of this signal with respect to time is proportional to δ , and thus a univalued function of Q_{θ} and i . When this signal du/dt is obtained after the first few cycles of the welding current, it might be utilised to adjust the proper current intensity if for any of the reasons mentioned in section 6.1.1 the energy production were too small or too high. Such a system can only perform well if the welding time has not a too small value. Besides, a predetermined value u_{\max} , proportional to d_{\max} , of the voltage signal may be used to limit the heating time to the required value through interruption of the ignitron injection

voltage at the given level of u_{\max} . Considerable research will be required for the effectuation of the control system described. The undesired influence of the static friction force acting on the moving part of the welding machine must be eliminated as much as possible in order to avoid unacceptable spreadings of the displacement values.

CONCLUSIONS

As to the investigated geometrical arrangement exclusively concerning spot welding by means of flat-faced electrode tips, the following conclusions may be drawn.

(a) The relationship between the main welding parameters for the obtainance of a weld of prescribed strength and dimensions in any workpiece metal can be established with the aid of an improved version of the applied mathematical model.

(b) It was shown that both the electric current distribution and the electric contact resistances are of great importance in the spot welding process, although each of these factors has its typical range of influence.

(c) The improved model, though developed for symmetrical arrangements, can be applied to the welding of dissimilar metals or thicknesses as well.

(d) The electrode force should be given a sufficiently high value, especially at the beginning of the heating period, in order to minimise electric contact resistances and to enhance weld quality. The friction force, acting on the moving head of the welding machine, must be minimised.

(e) The static shearing force of the weld exclusively depends on the thickness of the welded material and on the dimensions of the weld nugget formed.

(f) The accurate adjustment of welding current and welding time is of predominant importance for the quality control of the weld made.

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SAMENVATTING

Het belangrijkste onderwerp van dit proefschrift is de analyse van de tijdens het puntlassen optredende temperaturen in het materiaal van het werkstuk. Voor dit doel werd een vereenvoudigd analoog model ontworpen teneinde een kwantitatief inzicht te verkrijgen in de grootte van de optredende temperaturen. Met behulp van dit model kon de invloed van een aantal belangrijke lasparameters, alsmede van de materiaaleigenschappen van werkstukken en elektroden en van enkele facetten van de lasgeometrie worden nagegaan. De juistheid van het model werd experimenteel gecontroleerd voor een aantal representatieve werkstukmaterialen. Geconstateerd wordt, dat er een systematische afwijking bestaat tussen de uitkomsten van het mathematisch model en de resultaten van de experimenten. Deze afwijking kan kwantitatief verklaard worden als een gevolg van de discrepantie tussen dit model en de experimentele situatie met betrekking tot de elektrische stroomverdeling tussen de elektroden en de invloed van de kontaktweerstand.

Vervolgens worden de verkregen inzichten op bevredigende wijze toegepast op het lassen van onderling verschillende werkstukken en op het lassen van electrolytisch koper met behulp van een kunstmatige stroomvernaauwing. Tenslotte wordt een beschouwing gegeven over de invloed van de lasparameters op de kwaliteit van de las en wordt een methode aangegeven voor het automatisch regelen van het proces en het beheersen van de las-kwaliteit.

CURRICULUM VITAE

De schrijver van dit proefschrift werd in 1938 te Utrecht geboren. Hij bezocht daar de Sint Gerardus Majella school, waar hij in 1954 het diploma MULO-B behaalde. Daarna volgde hij onderwijs aan de Gemeentelijke Hogere Technische School voor de Mechanische Technologie te Utrecht, alwaar hij in 1958 het eindexamen met goed gevolg aflegde. Van 1958 tot 1960 vervulde hij zijn militaire dienstplicht.

In 1960 begon hij zijn studie aan de Technische Hogeschool te Eindhoven; in 1965 verwierf hij daar met lof het diploma van werktuigkundig ingenieur. Van augustus 1965 tot en met december 1968 was hij als medewerker verbonden aan het Laboratorium voor Mechanische Technologie en Werkplaatstechniek van eerder genoemde hogeschool, in welke functie hij de gelegenheid vond dit proefschrift te bewerken.

Sinds januari 1969 is hij als wetenschappelijk medewerker verbonden aan het Natuurkundig Laboratorium van de N.V. Philips Gloeilampenfabrieken te Eindhoven.

STELLINGEN

I

Indien de betekenis van de wetenschap moet worden afgemeten naar de mogelijkheden die zij de mens biedt voor zijn zelfontplooiing, dienen futurologische beschouwingen zich niet te beperken tot het aangeven van te verwachten wetenschappelijke en technische mogelijkheden op basis van extrapolatie van de actuele stand van onderzoek en ontwikkeling. Deze beschouwingen behoren tevens een basis te vormen voor het toekennen van prioriteiten binnen de wetenschappelijk-technische ontwikkeling. Daarbij moeten als criteria gehanteerd worden:

1. het lenigen van elementaire menselijke noden,
2. de mate waarin de mens inderdaad mogelijkheden tot zelfontplooiing geboden worden.

A.G.M. van Melsen, De Betekenis van de
Wetenschap.
Voordracht gehouden tijdens het congres
"Leven met de Wetenschap".
Utrecht, Oosthoek, 1968.

II

De kwantitatieve statistische analyse van de resultaten van metingen verricht aan een te verklaren proces moet niet gekoppeld worden aan een willekeurig gekozen wiskundig model, teneinde verder fundamenteel onderzoek niet bij voorbaat te bemoeilijken.

III

Een thermische analyse van het puntlasproces leidt in het algemeen niet tot bevredigende resultaten indien òf alleen van de warmte-ontwikkeling in de kontaktplaatsen òf alleen van de warmte-ontwikkeling in het werkstukmateriaal wordt uitgegaan.

IV

Het is ongewenst de diameter van een te maken puntlas groter te kiezen dan noodzakelijk is voor het verkrijgen van een mechanisch voldoende sterke verbinding.

V

De geringe mate van creativiteit die de kandidaatsstudie in de afdeling der werktuigbouwkunde van deze hogeschool vraagt van de studerenden kan wellicht wezenlijk vergroot worden door het invoeren van een weldoordacht systeem van project-onderwijs.

VI

De relatie, die het Welding Handbook geeft voor de grootte van de benodigde energie als functie van de materiaaldikte en de hardheid bij het ultrasoon lassen van plaatmateriaal, is in zijn algemeenheid onjuist. Met name voor metalen met een vlakken-gecenterd kristalrooster en voor edele metalen treden grote afwijkingen op.

Welding Handbook (5th edition),
Section 3, p. 49.5
New York, American Welding Society, 1965.

VII

De kwalificatie "ideaal-plastisch" voor een metaal dat bij plastische deformatie niet versterkt, is voor technologische toepassingen misleidend omdat hij suggereert dat het betreffende metaal zeer goed plastisch te bewerken zou zijn.

VIII

Bij het draaiproces kan voor gegeven beitelgeometrie, werkstukmateriaal en snedediepte het verloop van de spaankontaktlengte in de tijd beschreven worden door middel van een dimensieloze grootheid, gevormd door de verhouding van de draaitijd en de levensduur van de beitelpunt.

A.P.A.J. Hulst, De spaankontaktlengte
bij draaien.
Eindhoven, Laboratorium-rapport WT 129, 1965.

IX

Het verdient aanbeveling om de verplichte stellingen bij een proefschrift niet af te schaffen, omdat deze de promovendus een unieke gelegenheid bieden zijn gemoed te luchten, c.q. zijn geweten te ontlasten.

Eindhoven, 15 april 1969

A.F.A.J. Hulst