

## On the numerical analysis of coronary artery wall shear stress

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# On the Numerical Analysis of Coronary Artery Wall Shear Stress

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> > Velocity distribution

#### Objective

To determine whether the time-averaged wall shear stress in the coronary artery can be accurately modelled by means of steady flow of a Newtonian fluid through a rigid geometry.

## Geometry



**Figure 1** *Measured geometry (left) and curved tube model (right) of the right coronary artery.* 

## Motion and flow rate



**Figure 2** Motion interpolation function (left) and flow rate wave form (right), after Berne and Levy (1967).

## Viscosity modeling

The shear thinning viscosity of blood is modeled using a Carreau-Yasuda model:  $\frac{\eta - \eta_{\infty}}{\eta_0 - \eta_{\infty}} = [1 + (\lambda \dot{\gamma})^a]^{\frac{n-1}{a}}$ .

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	10 10
Viscosity model	η
Shear thinning Unscaled Newtonian Scaled Newtonian	$\eta(\dot{\gamma}) \ \eta_{\infty} \ \eta(\dot{\gamma}_c)$

Table 1 Viscosity models, with  $\dot{\gamma}_c$ the characteristic shear rate in 2DPoiseuille flow.



(cross: measured; solid: fit), after Thurston (1979).



**Figure 4** Axial velocity profiles for steady mean flow through the rigid end-diastolic geometry (dash-dotted: unscaled Newtonian; dashed: scaled Newtonian; solid: shear thinning).



time average

**Figure 5** Contour and vector plots of the axial and in-plane velocities at 0.75 tube length distance from the inflow: moving/shear thinning (extrema and time average) vs. rigid/Newtonian (steady mean).

## Wall shear stress distribution



**Figure 6** Wall shear stress contours (outer bend at 0°): moving/shear thinning (time average) vs. rigid/Newtonian (steady mean).

#### Conclusion

The time-averaged wall shear stress distribution in a right coronary artery model applying time varying, non-Newtonian flow in a moving and deforming geometry can be approximated well by modeling steady mean flow in the end-diastolic geometry using a shear-rate scaled Newtonian viscosity.

## /department of biomedical engineering