# Isothermal anionic polymerization of $\varepsilon$-caprolactam to polyamide-6: Kinetic modeling and application for production process 

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#### Abstract

The in-situ anionic polymerization of $\varepsilon$-caprolactam ( $\varepsilon$-CL) to polyamide-6 enables the production of large, near net shape fiber reinforced composites by thermoplastic resin transfer molding. For the propagation of the flow front as well as for the progress of the solidification, the simultaneous processes of polymerization and crystallization and the corresponding reaction kinetics play a central role. To investigate these processes, preparation of reactive mixtures consisting of $\varepsilon$-CL, activator, and initiator was carried out under inert atmosphere. A solvent-based activator and initiator were used, which hardly have been studied in the literature so far. In analogy to the resin transfer molding process, quasi-isothermal differential scanning calorimetry measurements were performed at various temperatures and the released enthalpy and the degree of crystallization were determined. From these isothermal measurements, a two-stage semi-empirical kinetic model was established for a solventbased system for the first time, which reproduces the experimental data with high precision. To apply the obtained kinetic model to a thermoplastic resin transfer molding process it was finally correlated to dielectric sensor data, allowing real-time prediction of the total conversion.


## KEYWORDS

dielectric properties, differential scanning calorimetry (DSC), kinetics, polyamides, ringopening polymerization

## 1 | INTRODUCTION

Polymer injection processes enable to increase the degree of automation in the production of fiber reinforced composites and thus to improve the efficiency of the value chain. In this processes, dry semi-finished fiber products
are infiltrated in a mold with a reactive, commonly thermoset polymer system and cured at specific temperatures. The use of thermoplastic matrix systems offers some advantages over thermosets for composite materials, such as a higher toughness, the possibility of forming, welding, and recycling. However, thermoplastic melts cannot be

[^0]used to fully impregnate dry fiber semi-finished products due to their high melt viscosity, which is often several orders of magnitude higher than the viscosity of uncured thermosetting resins. To overcome these challenges, instead of the high-viscosity thermoplastic melt, a lowviscosity monomer melt is mixed with suitable additives and injected into the mold, where in-situ polymerization takes place. ${ }^{1-3}$ Due to the initially low-viscosity, complete impregnation of the fibers can be realized without high processing pressures even for large components.

Driven by cost and introduction of composite-based components with reduced mechanical requirements in the automotive and aerospace industries, a number of engineering polymers are coming into focus. A prominent example is semi-crystalline polyamide-6 (PA6), which can be produced by anionic ring-opening polymerization of the monomer $\varepsilon$-caprolactam ( $\varepsilon$-CL). In this process, an initiator and an activator are used to start and accelerate polymerization, respectively, with the anionic polymerization taking place at temperatures of about $160^{\circ} \mathrm{C}$ within a few minutes, that is, the reaction takes place at temperatures below the melting temperature of PA6 of $220^{\circ} \mathrm{C}$. The monomer system is characterized by an extremely low melt viscosity of about $5 \mathrm{mPa} \cdot \mathrm{s}$ at $100^{\circ} \mathrm{C},{ }^{4,5}$ which renders it ideally suitable for injection processes such as thermoplastic resin transfer molding (T-RTM). ${ }^{1-3,6}$

To carry out such a T-RTM process efficiently, an understanding of the reactive behavior of the starting material is essential. For in-situ polymerization of $\varepsilon$-CL, the reaction kinetics and the development of viscosity during anionic polymerization play a central role. The kinetics of the anionic polymerization of $\varepsilon$-CL to PA6 is complicated due to the simultaneous processes of polymerization and crystallization. Furthermore, the chemical composition of the reactive mixture consisting of $\varepsilon$-CL, initiator, and activator, as well as the process temperature strongly influence the reaction kinetics and the polymer characteristics. ${ }^{7-18}$ In addition, a deactivating influence of moisture on anionic polymerization is known to occur. ${ }^{19-22}$ Also, a high process temperature accelerates the polymerization and at the same time slows down the crystallization while a low process temperature leads to a fast crystallization, which in turn causes a slow polymerization. ${ }^{7,23}$

Differential scanning calorimetry (DSC) ${ }^{9,12,24}$ or adiabatic reactors ${ }^{10,13,25}$ are commonly used to study the kinetics of the anionic polymerization of $\varepsilon$-CL to PA6. Here, we prefer the DSC approach because it enables a separation of the processes of polymerization and crystallization. Furthermore, it is possible to determine reaction and melt enthalpies precisely and therefore conclusions about the polymer properties, such as the degree of crystallization, can be drawn.

The kinetic models used so far in the literature to describe the anionic polymerization of $\varepsilon$-CL to PA6 have been summarized by Ageyeva et al. ${ }^{26}$ Anionic polymerization can be described in two ways, that is, by mechanistic and semi-empirical models. The mechanistic approach ${ }^{27-31}$ takes into account all chemical side reactions and is of low practicability due to the complex chemistry of anionic polymerization. The semi-empirical approach ${ }^{32-38}$ describes the polymerization process phenomenologically and summarizes all reactions. It is commonly used for the kinetic description of anionic polymerization. For kinetic modeling, it is assumed that the temporal change of a measurand corresponds to the reaction rate of a chemical process. In the modeling of a DSC measurements, for example, it is assumed that the amount of heat released in an exothermic polymerization reaction is directly proportional to the conversion. ${ }^{39}$ Most models have the form of Equation (1), where the reaction rate is defined as the change in conversion $\alpha$ over time.

$$
\begin{equation*}
\frac{d \alpha(T, t)}{d t}=k(T) f(\alpha(t)), \tag{1}
\end{equation*}
$$

Here, $k(T)$ describes the temperature dependent reaction rate and is defined by the Arrhenius temperature dependence and $f(\alpha)$ describes the reaction model. There are different phenomenological models, which describe the polymerization process of the anionic polymerization of $\varepsilon$-CL, such as the Malkin,,${ }^{33,35,36,40,41}$ Camargo, ${ }^{42}$ Lin, ${ }^{30}$ and the Kamal-Sourour model ${ }^{37,38}$ proposed by Teuwen et al. ${ }^{25}$

The crystallization mechanism for anionic polymerization is related to that of crystallization from a melt. Based on the classical models for melt crystallization, ${ }^{43-46}$ some further advanced crystallization models have been proposed, such as the Avrami-Kolmogorov equation by Bolgov et al. ${ }^{32}$ the Malkin model, ${ }^{33,47-49}$ and the Lee-Kim model. ${ }^{50}$ Further, the differential Nakamura model ${ }^{51-53}$ was used by Vicard et al. ${ }^{12,54}$ which is a generalized form of the AvramiKolmogorov equation. This equation is also referred to as the Johnson-Mehl-Avrami-Kolmogorov (JMAK) equation.

To perform a simple description of anionic polymerization, it can be assumed that polymerization and crystallization occur in parallel and independently of each other. ${ }^{24}$ The total heat flow released during synthesis is then the sum of the heat flow of the polymerization and crystallization processes. However, this simplification does not accurately describe the physicochemical processes, since polymerization and crystallization are correlated. ${ }^{33}$ To represent this correlation, it has been proposed that the crystallinity $\beta(t)$ is coupled to the conversion $\alpha(t) .{ }^{32,33}$ This relationship is shown in Equation (2), where $\phi(t)(\mathrm{W} / \mathrm{g})$ is the total heat flow


FIGURE $1 \quad \varepsilon$-caprolactam.
while $Q_{P}$ and $Q_{C}(\mathrm{~J} / \mathrm{g})$ are the total polymerization and crystallization enthalpy, respectively.

$$
\begin{equation*}
\phi(t)=Q_{P} \frac{d \alpha(t)}{d t}+Q_{C} \frac{d \beta(t)}{d t} \alpha(t) . \tag{2}
\end{equation*}
$$

The aim of this work is to develop for the first time a kinetic model for the anionic polymerization of $\varepsilon$-CL applying a solvent-based initiator and activator. The reactive mixture was prepared under inert gas atmosphere and the reaction as well as the crystallization enthalpies of the synthesized PA6 were accurately determined using DSC. Following the isothermal T-RTM process, special isothermal DSC temperature programs were defined. Following Equation (2), a semi-empirical approach with a two-step model A-B-C was chosen for kinetic modeling, in which the first step $\mathrm{A}-\mathrm{B}$ represents the polymerization and the second step B-C the crystallization, which means that only previously polymerized parts can crystallize. In accordance with Teuwen et al. ${ }^{25}$ the Kamal-Sourour and the Avrami model were applied for polymerization and crystallization, respectively.

Dielectric measurements give information about the polarizability and the ion viscosity of a polymer. The developed kinetic model was combined with signals of dielectric sensors, which monitor the anionic polymerization during T-RTM in a production environment. The resulting real-time prediction of the degree of total conversion can demonstrate the applicability of the model on large scale.

## 2 | EXPERIMENTAL

## 2.1 | Materials

Samples were prepared in a glovebox under nitrogen inert gas to prevent a contamination with water of the starting materials of the anionic polymerization of $\varepsilon$-CL. Solventbased additives from the manufacturer Katchem spol. s r. o., that is, the initiator sodium dicaprolactamato-bis-(2-methoxyethoxo)-aluminate (dilactamate) dissolved in toluene and the activator hexamethylene diisocyanate (U7), were used. The monomer was supplied by


FIGURE 2 Hexamethylene-1,6-diisocyanate (U7).


FIGURE 3 Sodium dicaprolactamato bis-(2-methoxyethoxo) aluminate ${ }^{26}$ (dilactamate ${ }^{\circledR}$ ).

Brüggemann Chemical in form of $\varepsilon$-CL flakes (APNylon ${ }^{\circledR}$ ). The structures of the respective molecules are given in Figures $1-3$. The exact concentrations according to the data sheet for dilactamate are about $82 \mathrm{wt} \%$ of sodium dicaprolactamato bis-(2-methoxyethoxo) aluminate, about $14 \mathrm{wt} \%$ of toluene, and about $4 \mathrm{wt} \%$ of $\varepsilon$-CL. The concentrations of U7 are about $75 \mathrm{wt} \%$ of hexamethylene-1,6-diisocyanate homopolymer, about $12 \mathrm{wt} \%$ of xylenes, about $13 \mathrm{wt} \%$ of 2-methoxy-1-methylethyl acetate, about $0.5 \mathrm{wt} \%$ of hexamethylene-1,6 -diisocyanate, and about $3 \mathrm{wt} \%$ of ethylbenzene.

To prepare a reactive mixture, about 40 g of $\varepsilon$-CL were weighed in a beaker. To ensure good thermal equilibrium between the beaker, which was sealed with a silicon stopper, and a magnetic stirrer hot plate, the beaker was placed in a hollow copper cylinder. The hot plate was adjusted to $80^{\circ} \mathrm{C}$, which is just above the melting temperature and below the polymerization temperature of $\varepsilon$-CL. After 60 min , the $\varepsilon$-CL had completely melted and defined amounts of initiator and activator were added using disposable syringes. A reactive mixture of $92.5 \mathrm{wt} \% \varepsilon$-CL, $5 \mathrm{wt} \%$ initiator dilactamate, and $2.5 \mathrm{wt} \%$ activator U7 was prepared, which was labeled KC-50-25. After the liquid reactive mixture became homogeneous, that is, no additive residue was observed, it was poured into an aluminum sheet featuring 48 molds and quenched to room temperature. The resulting solid mixture remains reactive to almost $100 \%$. To investigate the reactivity, DSC measurements were carried out at a fresh mixture and a mixture held at $80^{\circ} \mathrm{C}$ for 5 h . No significant change in reactivity was observed. This procedure resulted in cylinder shaped samples of 3.5 mm in diameter and 2.0 mm in height and with a mass of about 10 mg , which were used for DSC measurements. The reactive cylindric samples were placed in crucibles of known


FIGURE 4 Exemplary differential scanning calorimetry (DSC) signal and corresponding temperature program for a quasi-isothermal DSC measurement with a reaction temperature of $160^{\circ} \mathrm{C}$ : (1) melting of reactive mixture, (2) anionic polymerization, (3) crystallization, (4) melting of PA6, and (5) recrystallization of PA6. [Color figure can be viewed at wileyonlinelibrary.com]
weight and closed inside the glovebox. Therefore, the samples were protected against the influence of humidity or reactive gases. An empty DSC reference crucible was sealed under identical initial conditions. The pressed DSC crucibles were then removed from the glovebox and reweighed to determine the exact sample mass.

## 2.2 | Differential scanning calorimetry

Quasi-isothermal DSC measurements were performed using a DSC 214 Polyma (Netzsch, Germany). Figure 4 shows an exemplary DSC signal (top) and the corresponding temperature program (bottom) of such a quasiisothermal DSC measurement with a target temperature of $160^{\circ} \mathrm{C}$. The sample was first heated from 25 to $80^{\circ} \mathrm{C}$ at a heating rate of $20 \mathrm{~K} / \mathrm{min}$ and kept isothermal for 1 min . During this process, the reactive mixture melts, which represents an endothermic process ((1) in Figure 4). Then the sample was heated from $80^{\circ} \mathrm{C}$ to the desired target temperature of $140,145,150,155,160$, or $165^{\circ} \mathrm{C}$, respectively, with a heating rate of $300 \mathrm{~K} / \mathrm{min}$. The target temperature was kept constant for 15 min , that is, an isothermal segment was added. The high heating rate of $300 \mathrm{~K} / \mathrm{min}$ allows the anionic polymerization to be carried out under quasi-isothermal conditions, since the heating interval is much shorter than the polymerization time. For this short heating segment, the control parameters of the DSC were chosen to avoid an overshooting of the temperature but to quickly reach the target temperature. At the target temperature, exothermic anionic polymerization (2) and crystallization (3) begin and PA6 is
formed. ${ }^{18,25}$ In the following, the target temperature is labeled reaction temperature and refers to the temperature where both polymerization and crystallization occur. After the isothermal interval, the synthesized PA6 was cooled to $25^{\circ} \mathrm{C}$ at $-40 \mathrm{~K} / \mathrm{min}$ and kept under isothermal conditions for another 5 min . This was followed by a dynamic heating segment, in which the sample was reheated to $240^{\circ} \mathrm{C}$ at $10 \mathrm{~K} / \mathrm{min}$. This latter heating segment is used to confirm the complete anionic polymerization and to determine the crystallinity using the endothermic melting process of the PA6 (4). In the last step, the sample cooled down in a controlled manner at $-40 \mathrm{~K} / \mathrm{min}$ and the PA6 melt solidified and crystallized (5).

The enthalpy was calculated from the area between the DSC signal and a linear baseline between two defined temperature limits (see dotted lines in Figure 4). From the isothermal segment, the enthalpy of reaction $\Delta H_{R}$ was determined, which is composed of the heat of polymerization $\Delta H_{P}$ (2) and crystallization $\Delta H_{C}$ (3). Here, the high temperature limit of the baseline was placed at the end of the isothermal segment and a horizontal line was drawn from this point. The intersection of this line with the DSC signal corresponded to the low temperature boundary. For the dynamic heating segment at $10 \mathrm{~K} / \mathrm{min}$, the limits for each curve were determined individually based on the zero points of the first derivative of the DSC signal. The melting enthalpy or enthalpy of fusion of PA6 $\Delta H_{m, P A 6}$ was determined by the area between the melting curve of the synthesized PA6 and the baseline (4).

We assume that the enthalpy of crystallization agrees with the melt enthalpy of PA6 measured reheating the


FIGURE 5 Quasi-isothermal DSC measurements with different reaction temperature for KC-50-25. [Color figure can be viewed at wileyonlinelibrary.com]
sample to $240^{\circ} \mathrm{C} .{ }^{23}$ Using this relationship, the polymerization enthalpy $\Delta H_{P}$ was calculated from the difference of the reaction enthalpy $\Delta H_{R}$ and the crystallization enthalpy $\Delta H_{C}$, which is described by Equation 3 .

$$
\begin{equation*}
\Delta H_{P}=\Delta H_{R}-\Delta H_{C}=\Delta H_{R}-\left|\Delta H_{m, P A \sigma}\right| . \tag{3}
\end{equation*}
$$

The crystallinity of PA6 can be determined from the enthalpy of fusion by relating this value to the theoretical enthalpy of fusion of $240 \mathrm{~J} / \mathrm{g}$, which is characteristic for a PA6 with $100 \%$ crystallinity. ${ }^{55-58}$

## 2.3 | Dielectric measurements

Dielectric analysis (DEA) was performed using the measuring system sensXPERT Digital Mold from Netzsch Process Intelligence consisting of TMM 3c/3R sensors and the DEA 288 Ionic dielectric analyzer, which can measure in a frequency range from 1 to 1 MHz . The sensors are also suitable for temperatures up to $280^{\circ} \mathrm{C}$ and pressures up to 300 bars. Further information concerning the measurement process is given below.

## 3 | RESULTS

## 3.1 | Influence of reaction temperature on anionic polymerization

Figure 5 shows the DSC signals of the reactive mixture KC-50-25 taken during the isothermal segment for
different reaction temperatures. The curves exhibit two maxima due to polymerization and crystallization and then approach the baseline. A strong temperature dependence is observed. With increasing temperature, the curves approach the base line earlier, that is, polymerization and crystallization proceed faster. For reaction temperatures of 165 and $160^{\circ} \mathrm{C}$, respectively, the reaction is completed after about 3 min , whereas for a temperature of $140^{\circ} \mathrm{C}$ about 7 min are required. Furthermore, with increasing reaction temperature, the polymerization and crystallization peaks become more pronounced and the ratio of the two peak heights changes. At low temperatures, only one pronounced (second) peak is observed. With increasing temperature, the relative height of the first peak increases.

The enthalpy as well as the degree of crystallization resulting from evaluation of the quasi-isothermal DSC measurements on KC-50-25 are shown in Figure 6. For the reaction temperature of $160^{\circ} \mathrm{C}$, a total of seven measurements were performed under identical conditions to determine the statistical deviations of the DSC analysis. The measurements showed a standard deviation of $1 \%$, which was estimated for all other reaction temperatures. The enthalpy of reaction amounts to $206 \mathrm{~J} / \mathrm{g}$ for the lowest reaction temperature of $140^{\circ} \mathrm{C}$, it increases slightly with increasing temperature to a maximum of $211 \mathrm{~J} / \mathrm{g}$ for $150^{\circ} \mathrm{C}$, and finally decreases to $190 \mathrm{~J} / \mathrm{g}$ for the highest reaction temperature of $165^{\circ} \mathrm{C}$. The enthalpy of fusion decreases with increasing reaction temperature. It amounts to $144 \mathrm{~J} / \mathrm{g}$ for $140^{\circ} \mathrm{C}$ and decreases steadily to $99 \mathrm{~J} / \mathrm{g}$ for $165^{\circ} \mathrm{C}$. The enthalpy of polymerization resulting from the difference between these two quantities, first increases from $92 \mathrm{~J} / \mathrm{g}$ for a reaction temperature of $140^{\circ} \mathrm{C}$ to a maximum of $102 \mathrm{~J} / \mathrm{g}$ for $155^{\circ} \mathrm{C}$ and then decreases to $91 \mathrm{~J} / \mathrm{g}$ for the highest temperature of $165^{\circ} \mathrm{C}$. The degree of crystallinity is determined by the enthalpy of fusion and steadily decrease from about $48 \%$ for $140^{\circ} \mathrm{C}$ to $41 \%$ for $165^{\circ} \mathrm{C}$.

The reaction temperature strongly influences the polymerization and crystallization processes. With increasing reaction temperatures, anionic polymerization proceeds faster while crystallinity decreases, in agreement with data from literature. ${ }^{7,23}$

The crystallization process has been described, for example, by Vicard et al. ${ }^{23}$ and Komoto et al. ${ }^{59}$ The prerequisite for crystallization is the formation of oligomers, which act as nucleators for crystallization.

At low temperatures, anionic polymerization proceeds slowly, leaving the oligomers very mobile in the lowviscosity reactive mixture with high $\varepsilon$-CL content. This facilitates alignment of the oligomers relative to each other in the highly supercooled system. This situation results in a high crystallization rate and large and stable lamellae,


FIGURE 6 Enthalpies of reaction, fusion, and polymerization, as well as crystallinity for different reaction temperatures for KC-50-25. [Color figure can be viewed at wileyonlinelibrary.com]
which increase the enthalpy of fusion. ${ }^{23}$ Polymerization then continues at the chain ends in the crystalline phase and the growth of the lamellae continues, for example, by folding of the growing polymer chains. ${ }^{59}$ The described process corresponds to the observed high enthalpies of fusion and concomitant high crystallinity in the range of low reaction temperatures. However, large crystallization rates can result in the trapping of reactive species, such as $\varepsilon$-CL anions, thus reducing conversion. ${ }^{17,60}$ This could contribute to the observed low enthalpy of polymerization for low reaction temperatures.

At high reaction temperatures the polymerization rate increases, as indicated by the time dependence of the DSC curves, and the degree of crystallization decreases. These processes explain the decrease of the reaction enthalpies for higher reaction temperatures. This might be due to the decreased mobility of the oligomers resulting from an further advanced growth process of the polymer chains and the increased viscosity of the medium. ${ }^{14}$ Increased branching can also occur in the polymer chains at this temperature, which additionally interferes with crystallization. ${ }^{7}$

In the literature, a maximum for the conversion is reported between 150 and $155^{\circ} \mathrm{C},{ }^{7,16}$ which is in good agreement with the observed maximum of the polymerization enthalpy at $155^{\circ} \mathrm{C}$.

## 3.2 | Kinetic model of the isothermal anionic polymerization process

In order to set up a kinetic model of a chemical reaction, the amount of released heat $Q(t)$ as measured by DSC is


FIGURE 7 DSC signal and corresponding total conversion for $\mathrm{KC}-50-25$ with a reaction temperature of $160^{\circ} \mathrm{C}$. [Color figure can be viewed at wileyonlinelibrary.com]
assumed to be directly proportional to the conversion $\alpha(t)$ in an exothermic polymerization reaction. ${ }^{39}$ Since both polymerization and crystallization contribute to the DSC signal at a time $t$, the fit of the model to the DSC signal integrated over time was performed. This integrated DSC signal corresponds to the amount of heat $Q(t)$ released up to the time $t$. $Q(t)$ defines a total conversion of the reaction $\Omega(t)$, which consists of the sum of the conversion of the polymerization and the crystallization of the polymer (see Equation 4). Here, $Q_{R}$ is the total enthalpy of reaction released, that is, the DSC signal integrated over the complete polymerization and crystallization peaks.

$$
\begin{equation*}
\Omega(t)=\frac{Q(t)}{Q_{R}} \tag{4}
\end{equation*}
$$

For the kinetic modeling, the temperature program of the isothermal DSC measurements was further optimized. In order to reduce the effect of thermal inertia on the fast-heating process at $300 \mathrm{~K} / \mathrm{min}$, the sample is exposed to the temperature program consisting of the fast-heating process at $300 \mathrm{~K} / \mathrm{min}$ and the isothermal segment twice in succession. After differencing the DSC signals of the two runs, the influence of the thermal inertia of the samples can be eliminated. Furthermore, nearly identical sample masses were used for the isothermal DSC measurements, which minimizes a methodical influence of the DSC on the measurement results. Figure 7 shows an example of the corrected DSC signal for $\mathrm{KC}-50-25$ at $160^{\circ} \mathrm{C}$ isothermal reaction temperature and the corresponding total conversion.

To develop the isothermal reaction model, only the reaction regions of the isothermal DSC measurements with a target temperature of $145,150,155$, and $160^{\circ} \mathrm{C}$ were considered. Due to the simultaneous polymerization and crystallization, a semi-empirical approach with a two-step model A-B-C was chosen, where the first step (A-B) represents the polymerization and the second step (B-C) represents the crystallization. Following Teuwen et al. ${ }^{25}$ a polymerization model in the form of the KamalSourour equation was applied for the first step (A-B) and a crystallization model in the form of the JMAK equation was used for the second step (B-C). The total heat flux $\phi(t)$ as function of time can then be written as shown in Equation (5). This total heat flux describes the measured DSC signal and the reaction rate, originating from polymerization and crystallization. Equation (5) takes into account that the crystallization process cannot proceed until initial polymer chains have been formed.

$$
\begin{align*}
& \qquad \phi(t)=Q_{R}\left[c_{1} \frac{d(A \rightarrow B)}{d t}+c_{2} \frac{d(B \rightarrow C)}{d t}\right]  \tag{5}\\
& \text { Polymerization : } \frac{d(A \rightarrow B)}{d t}=k_{1} A^{\tilde{n}}+k_{2} A^{\tilde{n}} B^{\tilde{m}} \\
& \text { Crystallization : } \frac{d(B \rightarrow C)}{d t}=k_{3} n B[-\ln (B)]^{\frac{n-1}{n}} \\
& \text { with } k_{i}=p_{i} \exp \left(\frac{-E_{i}}{R T}\right)
\end{align*}
$$

The concentrations of monomer and polymer molecules are abbreviated as $A$ and $B$, respectively, while $C$ represents the fraction of the crystalline phase. The partial reaction orders are $\tilde{n}$ and $\tilde{m}, n$ is the Avrami


FIGURE 8 Fitting of the total experimental conversion $\Omega(t)$ of the isothermal DSC measurements for KC-50-25 with the two-step kinetic model consisting of Kamal-Sourour and JMAK $\left(\phi(t) / Q_{R}\right)$. [Color figure can be viewed at wileyonlinelibrary.com]

TABLE 1 Calculated parameters for the two-step kinetic model consisting of Kamal-Sourour and JMAK for the isothermal DSC measurements on KC-50-25.

| A-B: Kamal-Sourour | B-C: JMAK |  |  |
| :--- | :--- | :--- | :--- |
| $E_{1}(\mathrm{~kJ} / \mathrm{mol})$ | 77.4 | $E_{3}(\mathrm{~kJ} / \mathrm{Mol})$ | 134.1 |
| $p_{1}\left(\mathrm{~s}^{-1}\right)$ | $1.8 \cdot 10^{7}$ | $p_{3}\left(\mathrm{~s}^{-1}\right)$ | $5.3 \cdot 10^{14}$ |
| $\tilde{n}(-)$ | 1.1 | $n(-)$ | 1.0 |
| $p_{2}\left(\mathrm{~s}^{-1}\right)$ | $1.8 \cdot 10^{7}$ | $c_{2}(-)$ | 0.53 |
| $\tilde{m}(-)$ | 2.2 |  |  |
| $E_{2}(\mathrm{~kJ} / \mathrm{mol})$ | 72.1 |  |  |
| $c_{1}(-)$ | 0.47 |  |  |

constant, and $c_{1}$ and $c_{2}$ are weighting factors, respectively. The optimization of the two-step model was performed after entering the starting parameters using the least squares method. To facilitate the convergence of the model to the measured data, parameter bounds were defined. Values were further specified for the weighting factors $c_{1}$ and $c_{2}$, which were derived from the average of the ratios of polymerization enthalpy and crystallization enthalpy derived for the isothermal temperatures used. The fitting results for the isothermal reaction model are shown in Figure 8. The experimental data of the total conversion $\Omega(t)$ are reproduced in very good agreement by the isothermal reaction model with a correlation coefficient of 0.97 .

The corresponding fit parameters for the two-step isothermal reaction model are listed in Table 1. Considering the polymerization, in the Kamal-Sourour equation the
pre-exponential factors $p_{1}$ and $p_{2}$ are identical. The value is $1.8 \cdot 10^{7} \mathrm{~s}^{-1}$ and describes the number of collisions of the molecules during a chemical reaction.

For the non-autocatalytic part of the Kamal-Sourour equation, a first-order reaction results with $\tilde{n}$ of 1.1. The activation energy $E_{1}$ is $77.4 \mathrm{~kJ} / \mathrm{mol}$. The autocatalytic part of the Kamal-Sourour equation has a reaction order $\tilde{m}$ of 2.2 and the activation energy $E_{2}$ here is $72.1 \mathrm{~kJ} / \mathrm{mol}$. Overall, the total order of the reaction is 3.3 . The autocatalytic part of the polymerization lies at a slightly lower activation energy compared to the first-order reaction pathway. In the literature, activation energies for anionic polymerization using sodium caprolactamate as initiator are reported in the range of $59-92 \mathrm{~kJ} /$ mol, ${ }^{13,25,27,29,32,36,50,61}$ consistent with our result. The Arrhenius terms describe the temperature dependence of the reaction rate and represent a constant at a fixed temperature. At a reaction temperature of $160^{\circ} \mathrm{C}$, values for $k_{1}$ of $8.6 \cdot 10^{-3} \mathrm{~s}^{-1}$ for the first-order reaction and for $k_{2}$ of $3.7 \cdot 10^{-2} \mathrm{~s}^{-1}$ for the autocatalytic part result. The rate constant of the autocatalytic part of the polymerization is about four times larger than that of the first-order reaction for a temperature of $160^{\circ} \mathrm{C}$. For crystallization, which is described by the JMAK equation, the activation energy is $134.1 \mathrm{~kJ} / \mathrm{mol}$ and is about twice as large as the activation energies for polymerization. The Avrami constant $n$ is 1.0 and the Arrhenius term $k_{3}$ for $160^{\circ} \mathrm{C}$ results in $3.5 \cdot 10^{-2} \mathrm{~s}^{-1}$.

In the following we want to compare our results to those of Teuwen et al. ${ }^{25}$ The parameters of the KamalSourour equation for polymerization fitted here are of the same order of magnitude and partially in agreement with the parameters of Teuwen et al., although the additives used and the reaction conditions are significantly different. Teuwen et al. carried out the anionic polymerization in an adiabatic reactor and used $1,2 \mathrm{~mol}-\%$ sodium caprolactamate as initiator and $1,2 \mathrm{~mol}$ - $\%$ hexamethylene- $1,-$ 6-dicarbamoyl caprolactam as activator. Even though different additives are used, the concentration of the reactive species of $\mathrm{KC}-50-25$ in the present work is almost identical. For the nonautocatalytic part of the KamalSourour equation, Teuwen et al. give a reaction order for $\tilde{n}$ of 1.2 with an activation energy of $68.6 \mathrm{~kJ} / \mathrm{mol}$. The reaction order of the autocatalytic part $\tilde{\mathrm{m}}$ is 1.6 and the activation energy for this is $59.4 \mathrm{~kJ} / \mathrm{mol}$. Overall, the total order of the reaction is 2.8 . The autocatalytic part of the polymerization lies at a lower activation energy than of the nonautocatalytic part, in agreement with our results. However, the reported activation energies of Teuwen et al. are somewhat lower. The Arrhenius term for the nonautocatalytic part of the reaction has a value for $k_{1}$ of $2.9 \cdot 10^{-3} \mathrm{~s}^{-1}$ and for $k_{2}$ of $3.8 \cdot 10^{-2} \mathrm{~s}^{-1}$ for the autocatalytic part for the temperature of $160^{\circ} \mathrm{C}$. Thus, the rate


FIGURE 9 Dielectric monitoring of polymerization and crystallization during the T-RTM process at the sprue and at the fringe of the mold: ion viscosity as function of time at 100 kHz . [Color figure can be viewed at wileyonlinelibrary.com]
constant of the autocatalytic part of the polymerization is about an order of magnitude larger than that of the nonautocatalytic part. Compared with our isothermal reaction model, the rate constants of the autocatalytic part of the Kamal-Sourour equation $k_{2}$ are almost identical and those of the non-autocatalytic part $k_{1}$ are of the same order of magnitude. In particular, the agreement of $k_{2}$ confirms the theoretical assumptions of the KamalSourour model that the reaction mechanism for chain growth, and thus for the rate constant for the autocatalytic part of polymerization, should be independent of the initiator and activator used. ${ }^{62}$

## 3.3 | Application of the kinetic model in a production environment

The kinetic model, developed in a laboratory scale study, can be applied to monitor the polymerization and crystallization process in a production environment in real time. To this end, it has been combined with the signal of dielectric sensors. This allows to calculate the degree of total conversion in real-time. Such real-time monitoring allows an online control of the process parameters, for example, the conversion and the temperature. Therefore, a correlation between the process parameters and the quality of the sample is achieved. In addition, the in-situ monitoring allows a validation of our thermochemical modeling in real industrial processing environments.

A dielectric measurement monitors the microscopic properties of a polymer such as dipole-dipole interactions and the mobility of molecular chains. An alternating voltage is applied across the dielectric sensor, which induces


FIGURE 10 Relative permittivity at 100 kHz during the T-RTM process at the sprue and at the fringe of the mold (uncalibrated measurement). [Color figure can be viewed at wileyonlinelibrary.com]
a movement of the charge carriers within the polymer, that is, motion of ions and an alignment of dipoles. An alternating current with a phase shift relative to the applied voltage results, which characterizes the ion and dipole mobility. It allows to calculate the ion viscosity and the relative permittivity of the polymer. Figure 9 shows the real-time in-mold ionic viscosity as function of time close to the sprue and at fringe of the mold during a T-RTM process (geometry of the mold see Reference 63) The dielectric sensors allow for the characterization of the flow-front arrival (first drop of dielectric signal), the injection process and the flow behavior (minimal ion viscosity), and the solidification due to polymerization and crystallization (increase of ion viscosity). The temporal shift between the two signals demonstrates the course of the flow-front, which first passes at the sprue and then arrives at the fringe. In addition to the DEA signal, the temperature is monitored. The only small temperature changes of about $3^{\circ} \mathrm{C}$ at the sprue and $2^{\circ} \mathrm{C}$ at the fringe demonstrate the thermal stability of the system.

The polymerization and the partially overlapping crystallization process is characterized by a decrease of mobility and an increase of polarizability. The relative permittivity is a quantity that can follow both (see Figure 10).

The time interval starting with the maximum value of permittivity at roughly 4 min up to the minimum around 4.5 min is dominated by the polymerization, whereas the subsequent increase of permittivity is dominated by the crystallization.

Finally, the measured dielectric signal can be used to calculate the degree of total conversion in real-time. To this end, the kinetic model predicts the concentration of monomers as a function of time and temperature. The


FIGURE 11 Ion viscosity at 100 kHz and total conversion calculated by the kinetic model. [Color figure can be viewed at wileyonlinelibrary.com]
monomer concentration determines the ion viscosity of the system. Combining the two, the conversion as function of time can be determined. Both, the measured DEA signal and the resulting prediction of the conversion are shown in Figure 11. This allows to control cycle times and to increase the efficiency during component manufacturing using the T-RTM process. Such an inline monitoring of the manufacturing process can help to recognize process deviations and therefore to automatically adapt production in real-time. This concept, developed in the funded project CosiMo, has now become commercially available within the solution of sensXPERT provided by Netzsch Process Intelligence.

## 4 | CONCLUSION

Applying a specially adapted DSC temperature program, it was possible to investigate the anionic polymerization of $\varepsilon$-CL to PA6 quasi-isothermally. The influence of the reaction temperature on the released enthalpies was shown. It was found that the polymerization rate increases with increasing temperature and that anionic polymerization proceeds faster. At the same time, the degree of crystallization of the synthesized PA6 decreases with increasing temperature. A maximum of the polymerization enthalpy, and thus probably the highest conversion, is observed at $150^{\circ} \mathrm{C}$.

Using an optimized isothermal DSC measurement, a semi-empirical two-stage kinetic model for the solventbased material system of the manufacturer Katchem was established for the first time. With a coupled modeling of polymerization and crystallization a very good fit of the kinetic model to the total conversion of the isothermal

DSC measurement data was achieved. The resulting parameters of the Kamal-Sourour equation for polymerization agree with values from the literature.

This kinetic model was finally coupled with dielectric sensor data for application in the T-RTM process. This enables real-time prediction of total conversion.

## AUTHOR CONTRIBUTIONS

Samet Kurt: Project administration (lead); writing - original draft (lead); writing - review and editing (lead). Thomas Bratzdrum: Investigation (supporting). Alexander Chaloupka: Software (lead); writing - review and editing (supporting). Siegfried Horn: Writing - review and editing (equal). Judith Moosburger-Will: Project administration (equal); writing - review and editing (equal).

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## DATA AVAILABILITY STATEMENT

The data that support the findings of this study are available on request from the corresponding author. The data are not publicly available due to privacy or ethical restrictions.

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