


















































































CHEOPS finds KELT-1b darker than expected in visible light

Discrepancy between the CHEOPS and TESS eclipse depths

H. Parviainen^{1,2} , T. G. Wilson³ , M. Lendl⁴ , D. Kitzmann⁵ , E. Pallé^{1,2} , L. M. Serrano⁶ , E. Meier Valdes⁵ , W. Benz^{7,5} , A. Deline⁴ , D. Ehrenreich⁴ , P. Guterman^{8,9} , K. Heng^{5,10} , O. D. S. Demangeon^{11,12} , A. Bonfanti¹³ , S. Salmon⁴ , V. Singh¹⁴ , N. C. Santos^{11,12} , S. G. Sousa¹¹ , Y. Alibert⁷ , R. Alonso^{1,2} , G. Anglada^{15,16} , T. Bárczy¹⁷ , D. Barrado y Navascues¹⁸ , S. C. C. Barros^{11,12} , W. Baumjohann¹³ , M. Beck⁴ , T. Beck⁷ , N. Billot⁴ , X. Bonfils¹⁹ , A. Brandeker²⁰ , C. Broeg^{7,5} , J. Cabrera²¹ , S. Charnoz²² , A. Collier Cameron³ , C. Corral Van Damme²³ , Sz. Csizmadia²¹ , M. B. Davies²⁴ , M. Deleuil⁸ , L. Delrez^{25,26} , B.-O. Demory⁵ , A. Erikson²¹ , J. Farinato²⁷ , A. Fortier^{7,5} , L. Fossati¹³ , M. Fridlund^{28,29} , D. Gandolfi⁶ , M. Gillon²⁵ , M. Güdel³⁰ , S. Hoyer⁸ , K. G. Isaak²³ , L. L. Kiss^{31,32} , E. Kopp³³ , J. Laskar³⁴ , A. Lecavelier des Etangs³⁵ , C. Lovis⁴ , D. Magrin²⁷ , P. F. L. Maxted³⁶ , M. Mecina³⁷ , V. Nascimbeni²⁷ , G. Olofsson²⁰ , R. Ottensamer³⁷ , I. Pagano¹⁴ , G. Peter³³ , D. Piazza⁷ , G. Piotto^{27,38} , D. Pollacco¹⁰ , D. Queloz^{39,40} , R. Ragazzoni^{27,38} , N. Rando⁴¹ , H. Rauer^{21,42,43} , I. Ribas^{15,16} , G. Scandariato¹⁴ , D. Ségransan⁴ , A. E. Simon⁷ , A. M. S. Smith²¹ , M. Steller¹³ , Gy. M. Szabó^{44,45} , N. Thomas⁷ , S. Udry⁴ , V. Van Grootel²⁶ , and N. A. Walton⁴⁶ 

(Affiliations can be found after the references)

Received September 15, 1996; accepted March 16, 1997

ABSTRACT

Recent *TESS*-based studies have suggested that the dayside of KELT-1b, a strongly-irradiated brown dwarf, is significantly brighter in visible light than what would be expected based on *Spitzer* observations in infrared. We observe eight eclipses of KELT-1b with *CHEOPS* (CHAracterising ExOPlanet Satellite) to measure its dayside brightness temperature in the bluest passband observed so far, and model the *CHEOPS* photometry jointly with the existing optical and NIR photometry from *TESS*, LBT, CFHT, and *Spitzer*. Our modelling leads to a self-consistent dayside spectrum for KELT-1b covering the *CHEOPS*, *TESS*, *H*, *Ks*, and *Spitzer* IRAC 3.6 and 4.5 μm bands, where our *TESS*, *H*, *Ks*, and *Spitzer* band estimates largely agree with the previous studies, but we discover a strong discrepancy between the *CHEOPS* and *TESS* bands. The *CHEOPS* observations yield a higher photometric precision than the *TESS* observations, but do not show a significant eclipse signal, while a deep eclipse is detected in the *TESS* band. The derived *TESS* geometric albedo of $0.36^{+0.12}_{-0.13}$ is difficult to reconcile with a *CHEOPS* geometric albedo that is consistent with zero because the two passbands have considerable overlap. Variability in cloud cover caused by the transport of transient nightside clouds to the dayside could provide an explanation for reconciling the *TESS* and *CHEOPS* geometric albedos, but this hypothesis needs to be tested by future observations.

Key words. stars: individual: KELT-1 – brown dwarfs – stars: planetary systems – stars: atmospheres – methods: observational

1. Introduction

KELT-1b is a strongly-irradiated transiting brown dwarf orbiting a 6500 K F5-star on a short-period orbit of 1.2 days discovered by Siverd et al. (2012). It has the third-shortest orbital period of the known transiting brown dwarfs¹ (Carmichael et al. 2021) after TOI-263b ($P = 0.56$ d, Parviainen et al. 2020; Pallé et al. 2021) and NGTS-7Ab ($P = 0.7$ d, Jackman et al. 2019), but receives a significantly higher stellar insolation since TOI-263b and NGTS-7Ab both orbit low-mass M dwarfs with $T_{\text{eff}} \sim 3400$ K. The orbit and insolation level of KELT-1b is similar to ultra-hot Jupiters (Parmentier et al. 2018; Kitzmann et al. 2018; Lothringer et al. 2018) like MASCARA-2b (Lund et al. 2017; Talens et al. 2018), WASP-121b (Delrez et al. 2016), WASP-189b (Anderson et al. 2018), WASP-76b (West et al. 2016), and WASP-33b (Cameron et al. 2010), but its surface gravity is ~ 22 times larger than that of Jupiter. This makes KELT-1b an inter-

esting case to study how surface gravity affects the atmospheres of strongly-irradiated sub-stellar objects.

KELT-1b's emission spectrum² has been studied using ground- and space-based eclipse and phase curve observations covering wavelengths from red-visible (*TESS*) to 4.5 μm (*Spitzer*). Soon after KELT-1b's discovery, Beatty et al. (2014) observed one secondary eclipse using *Spitzer* (in IRAC 3.6 and 4.5 μm passbands) and four eclipses in z' -band using the 0.6 m RCOS telescope at Moore Observatory. Later, Croll et al. (2015) observed an eclipse in the *Ks*-band using the WIRCam on the Canada-France-Hawaii Telescope, Beatty et al. (2017) observed an eclipse in the *H*-band using the LUCI1 spectrograph on the Large Binocular Telescope, and Beatty et al. (2019) observed a full KELT-1b phase curve with *Spitzer*. Finally, the *TESS* telescope observed KELT-1b continuously for 25 days in 2019, and

¹ According to the [Transiting Brown Dwarfs](#) list accessed 16.2.2022.

² e use a very loose definition of "emission spectrum" that also includes the contribution from reflected light.

the photometry spanning 15 full orbits was studied by [Beatty et al. \(2020\)](#) and [von Essen et al. \(2021\)](#).


The previous eclipse and phase curve studies have shown that KELT-1b's eclipse spectrum in near- and mid-IR agrees with a constant dayside brightness temperature of ~ 2900 K ([Beatty et al. 2019](#)). However, a study of the *TESS* observations by [Beatty et al. \(2020\)](#) presented that the brown dwarf's dayside brightness temperature in the *TESS* band is significantly higher than in the *Spitzer* bands. They proposed that this higher-than-expected brightness in visible light could be due to a high albedo caused by silicate clouds forming in the nightside of the brown dwarf. KELT-1b's dayside is too hot for clouds to form, but the nightside temperature is expected to be cool enough for the formation of silicate clouds. These nightside clouds could then be blown over to the dayside by winds, where they could survive all the way to the local noon, boosting the otherwise low dayside albedo significantly.

However, the cloud hypothesis is not the only viable explanation for the unexpected dayside brightness in the *TESS* band. [von Essen et al. 2021](#) made an independent analysis of the *TESS* phase curve and proposed that KELT-1b's dayside emission spectrum can be explained with thermal emission alone. [von Essen et al. \(2021\)](#) suggest that the differences in the *TESS* and *Spitzer* brightness temperatures can be explained by collision-induced absorption due to $\text{H}_2\text{-H}_2$ and $\text{H}_2\text{-He}$ decreasing the brightness temperature in the *Spitzer* bands. So, rather than the brightness of the *TESS* passband being boosted by reflection from clouds, the *Spitzer* band brightness would be suppressed by molecular absorption.

CHEOPS (*Characterising ExoPlanet Satellite*; [Benz et al. 2021](#)) is an ESA S-class mission aiming to characterise transiting exoplanets around bright ($V < 12$) stars based on ultra-high quality photometry ([Broeg et al. 2013](#)). The satellite is equipped with a 30 cm telescope that allows it to reach a photometric precision of 20 ppm in 6 h of integration time for a $V = 9$ star (as a design requirement), which is sufficient to detect Earth-sized planets around G5 dwarf stars ([Benz et al. 2021](#)). *CHEOPS* was launched on 18 December 2019, the science observations started in April 2020, and the observations have already been used to improve the characterisation of new and known exoplanet systems ([Bonfanti et al. 2021](#); [Delrez et al. 2021](#); [Szabó et al. 2021](#); [Barros et al. 2022](#); [Lacedelli et al. 2022](#); [Wilson et al. 2022](#)), improve the characterisation of eclipsing binaries with M-dwarf companions ([Swayne et al. 2021](#)), search for transit timing variations (TTVs, [Borsato et al. 2021](#)), search for planets transiting white dwarfs ([Morris et al. 2021b](#)), and study secondary eclipses and full phase curves of super-Earths and hot Jupiters ([Lendl et al. 2020](#); [Morris et al. 2021a](#); [Hooton et al. 2022](#); [Deline et al. 2022](#)). By now, the satellite has shown it can surpass its design requirements by reaching 10-20 ppm photometric precision for one hour of integration ([Lendl et al. 2020](#)).

In this paper, we present the phase curve analysis of KELT-1b based on new *CHEOPS* secondary eclipse photometry and existing photometry from *TESS*, *Spitzer*, LUCI1, and WIRCam. While the *CHEOPS* and *TESS* passbands have a significant overlap, the *CHEOPS* band emphasises bluer wavelengths than the *TESS* band. This difference allows us to test the two hypotheses about the *TESS*-*Spitzer* dayside brightness temperature discrepancy. If the high-albedo hypothesis is correct, both the *CHEOPS*- and *TESS*-bands are expected to be dominated by reflected light, and the *CHEOPS*-band can be expected to also show a high albedo (albeit this cannot be taken for granted since there are scenarios where KELT-1b could have a low albedo in the *CHEOPS* band and high in the *TESS*-band, as will be discussed later). If the

IR absorption hypothesis is correct, *CHEOPS* passband brightness temperature could be expected to follow closely the model presented in Fig. 9 in [von Essen et al. \(2021\)](#).

All the data and code for the analysis and figures are publicly available from [GitHub](#) , including additional Jupyter notebooks that work as appendices to the paper.

2. Observations

2.1. CHEOPS

We observed eight eclipses of KELT-1b with the *CHEOPS* spacecraft between 2020-10-02 and 2020-12-01 as a part of the Guaranteed Time Observers (GTO) programme (Fig. 1). Each eclipse observation consisted a *CHEOPS* visit of ≈ 7 h of near-continuous observations with an exposure time of 60 s. The length of the visits combined with the high precision of the KELT-1b ephemeris (thanks to recent *TESS* observations) ensured that we obtained at least 2 h of pre- and post-eclipse baseline for each visit. As *CHEOPS* is in a low-Earth orbit, sections of the observations are unobtainable as they may occur during Earth-target occultations, passages through the South Atlantic Anomaly (SAA), or at times when the stray light level passes an acceptable threshold. These effects manifest as gaps in the light curves and result in lower efficiency observations. For the data presented here, we obtain an average efficiency of 56%.

The data were automatically processed using the latest version of the *CHEOPS* Data Reduction Pipeline (DRP v13; [Hoyer et al. 2020](#)) that performs image calibration including bias, gain, non-linearity, dark current, and flat fielding corrections, and amends of environmental and instrumental effects, for example cosmic-ray hits, smearing trails, and background variations. Subsequently, aperture photometry is conducted on the corrected images using a set of standard apertures; $R = 22.5''$ (RINF), $25.0''$ (DEFAULT), and $30.0''$ (RSUP), with an additional aperture that selects the radius based on contamination level and instrumental noise (OPTIMAL), which for these observations yields $20.5''$. Furthermore, the DRP calculates contamination estimates of the visits that comes from background sources, as detailed in Section 6.1 of [Hoyer et al. \(2020\)](#), which we remove from the data.

As the field of view of *CHEOPS* rotates due to the nadir-locked orbit of the spacecraft, there may be short-term, non-astrophysical flux trends on the order of a *CHEOPS* orbital timescale due to nearby contaminants, background variations, or changes in instrumental environment. In previous studies these trends have been corrected via linear decorrelation with instrumental basis vectors ([Bonfanti et al. 2021](#); [Delrez et al. 2021](#)) or Gaussian process regression ([Lendl et al. 2020](#)), however a recent study has identified that these roll angle trends can be corrected by a novel PSF detrending method ([Wilson et al. 2022](#)). To summarise, this tool determines PSF shape changes of a visit by computing vectors associated with these variations by conducting principal component analyses (PCA) of the auto-correlation functions of the *CHEOPS* subarray images. The components that contribute most to the PSF shape changes are subsequently selected by a leave-one-out-cross-validation and are used as covariates in the light curve model. For this study, we perform this method on all visits using the DEFAULT aperture photometry fluxes as these yield the lowest RMS (root mean square) noises.

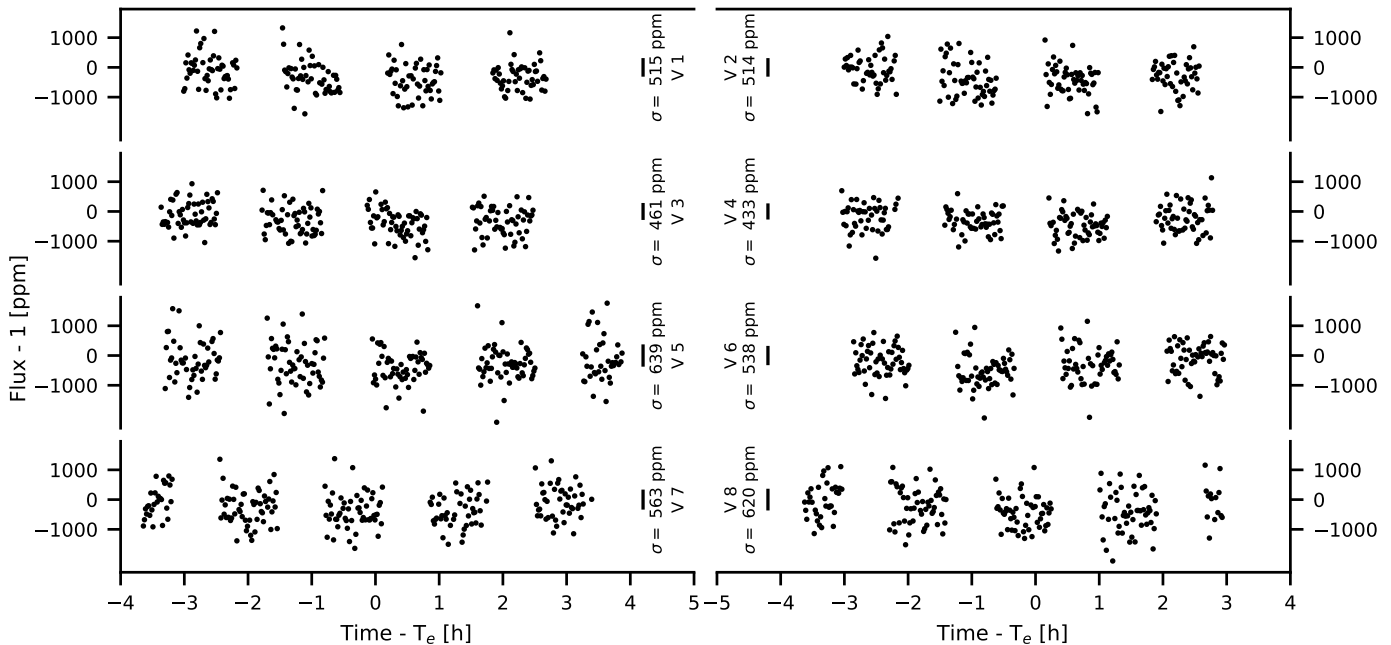


Fig. 1. The detrended photometry from eight KELT-1b eclipses observed with *CHEOPS* centred around the eclipse centre time (T_e). Each eclipse is observed as a single continuous *CHEOPS* visit of ≈ 7 h (labelled as V1-V8 in the figure), but the satellite’s orbital configuration leads to periodic gaps in the photometry, as described in Sect. 2.1.

2.2. TESS

The Transiting Exoplanet Survey Satellite (*TESS*, Ricker et al. 2014) observed KELT-1b during Sector 17 for 25 days (2019-10-08–2019-11-02) with a two-minute cadence. The observations cover 15 orbital periods with a high-enough precision to measure all the significant phase curve components in the *TESS* passband.

We use the Presearch Data Conditioning (PDC-SAP) light curve (Stumpe et al. 2014, 2012; Smith et al. 2012) produced by the SPOC pipeline (Jenkins et al. 2016). As in Beatty et al. (2020), we remove all the exposures with a non-zero quality flag, but we do not apply any additional detrending or outlier rejection. Instead, we use a CELERITE-based (Foreman-Mackey et al. 2017) time-dependent Gaussian process (GP) to calculate the likelihood as explained in more detail later. Furthermore, we ignore the residual light contamination of $\approx 0.82\%$ reported by von Essen et al. (2021), since it will not have any practical effect on the results.

2.3. Spitzer

KELT-1 was observed with the *Spitzer* space telescope using the Infrared Array Camera (IRAC; Fazio et al. 2004) in both *S1* ($3.6 \mu\text{m}$) and *S2* ($4.5 \mu\text{m}$) passbands across multiple programs with the observations covering a secondary eclipse (Beatty et al. 2017) and a full phase curve (Beatty et al. 2019).

Using these data, we extract light curves for all visits using our own custom pipeline. Using the flux-calibrated and artefact-corrected CBCD (Corrected Basic Calibrated Data) frames we constructed light curves by firstly using the IRAC archive contributed IDL program `BOX_CENTROIDER.PRO`³ to locate the target in the images. In addition to utilising these values as decorrelation basis vectors during the joint fitting, these x- and y-centroid

³ https://irsa.ipac.caltech.edu/data/SPITZER/docs/irac/calibrationfiles/pixelphase/box_centroider.pro

positions were used as inputs into the `APER.PRO` code to perform aperture photometry using an aperture radius of 3 pixels and a sky annulus 12–20 pixels. Lastly, we perform the aperture corrections, correct intrapixel gain using the `IRACPC_PMAP_CORR.PRO`⁴ tool, and reject data with fluxes or x- and y-centroid positions 5σ away from the respective, normalised mean.

2.4. Large Binocular Telescope H-band

Beatty et al. (2017) observed a spectrally resolved eclipse of KELT-1b in the *H*-band using the LUCI1 multiobject spectrograph on the 2×8.4 m Large Binocular Telescope (LBT). The observations were carried out on the night of 2013-10-26 and lasted ≈ 5 h. The exposure time was 60 s, leading to 245 exposures in total.⁵

2.5. Canada-France-Hawaii Telescope Ks-band

Croll et al. (2015) observed an eclipse of KELT-1b in the *Ks*-band ($\sim 2.15 \mu\text{m}$) using the Wide-field Infrared Camera (WIRCam) on the 3.6 m Canada-France-Hawaii Telescope (CFHT). The observations were carried out in 2012-10-10 and covered 6.8 h centred around the expected eclipse centre with an exposure time of 8 s, leading to 1440 exposures in total.⁶ The reduction of the photometry is detailed extensively in Croll et al. (2015, see especially the discussion about the sensitivity to different data reduction approaches in Sect. 5.4).

⁴ https://irsa.ipac.caltech.edu/data/SPITZER/docs/dataanalyistools/tools/contributed/irac/iracpc_pmap_corr/

⁵ The LBT *H*-band light curves used in Beatty et al. (2017) were kindly provided by Dr. Beatty, personal communication.

⁶ The CFHT *Ks*-band light curve used in Croll et al. (2015) was kindly provided by Dr. Croll, personal communication.

3. Stellar Characterisation

We revise the stellar radius, mass, and age and show the updated stellar properties in Table 1. The stellar age and mass are compatible with the previous estimates by Siverd et al. (2012) within 1σ , but our new radius is slightly larger than the original estimate of $1.46^{+0.039}_{-0.030} R_{\odot}$.

Using the stellar parameters derived via our spectral analysis as priors, we use a Markov-Chain Monte Carlo (MCMC) modified infrared flux method (IRFM; Blackwell & Shallis 1977; Schanche et al. 2020) to compute the stellar radius of KELT-1. We construct spectral energy distributions (SEDs) using ATLAS Catalogue stellar atmospheric models (Castelli & Kurucz 2003) and subsequently compute synthetic fluxes by integrating the SEDs over passbands of interest with attenuation of the SED included as a free parameter to account for extinction. To calculate the stellar apparent bolometric flux, hence the stellar angular diameter and effective temperature, we compare the synthetic fluxes to the observed broadband photometry retrieved from the most recent data releases for the following passbands; *Gaia* G, G_{BP} , and G_{RP} , 2MASS J, H, and K, and *WISE* W1 and W2 (Gaia Collaboration et al. 2021; Skrutskie et al. 2006; Wright et al. 2010). We convert the angular diameter into stellar radius using the offset-corrected *Gaia* EDR3 parallax (Lindgren et al. 2021) and determine a $R_{\star} = 1.530 \pm 0.009 R_{\odot}$.

We then use T_{eff} , [Fe/H], and R_{\star} to compute the stellar mass M_{\star} and age t_{\star} through two different sets of theoretical evolutionary models. In detail, we retrieved a first pair of mass and age estimates by applying the isochrone placement technique (Bonfanti et al. 2015, 2016) to grids of stellar tracks and isochrones pre-computed by the PARSEC⁷ v1.2S code (Marigo et al. 2017). A second pair of mass and age estimates, instead, was derived by directly inputting T_{eff} , [Fe/H], and R_{\star} into the CLES⁸ code (Scuflaire et al. 2008), which computes the best-fit evolutionary track following the Levenberg-Marquadt minimisation scheme, as presented in Salmon et al. (2021). As described in Bonfanti et al. (2021), once the two pairs of outcomes are available, we checked their mutual consistency through a χ^2 -based criterion and finally merged the posterior distributions obtaining $M_{\star} = 1.370^{+0.047}_{-0.070} M_{\odot}$ and $t_{\star} = 1.8 \pm 0.5$ Gyr.

4. Theory: phase curve modelling

4.1. Phase curve model

We model the light curves using a phase curve model implemented in PYTRANSIT v2.5.21 (Parviainen 2015; Parviainen & Korth 2020; Parviainen 2020) that includes a primary transit, secondary eclipse, thermal emission, reflection, Doppler beaming, and ellipsoidal variation, as illustrated in Fig. 2. The observed flux is presented as a sum of stellar and planetary components divided by a baseline flux model as

$$F = \frac{T \times (f_{\text{EV}} + f_{\text{DB}}) + E \times k^2(f_{\text{R}} + f_{\text{E}})}{f_b}, \quad (1)$$

where f_b represents the baseline flux, T is the transit model, f_{EV} is the ellipsoidal variation component, f_{DB} is the Doppler beaming component, E is the eclipse model, k is the planet-star radius ratio, f_{R} is the reflected flux, and f_{E} is the thermal emission.⁹

⁷ PAdova and TRieste Stellar Evolutionary Code: <http://stev.oapd.inaf.it/cgi-bin/cmd>

⁸ Code Liègeois d'Évolution Stellaire

⁹ Note that the f_{R} and f_{E} represent the phase-dependent planet-star flux ratios from reflection and thermal emission, where the flux ratio

Table 1. KELT-1 identifiers, coordinates, properties, and magnitudes.

Main identifiers			
TIC			432549364
GAIA DR2			2881784280929695360
2MASS			J00012691+3923017
Equatorial coordinates			
RA (J2000)			00 ^h 01 ^m 26 ^s .9
Dec (J2000)			39° 23' 01''66
Stellar parameters			
Spectral type			F5 (1)
Mass	M_{\star}	[M_{\odot}]	$1.370^{+0.047}_{-0.070}$ (2)
Radius	R_{\star}	[R_{\odot}]	1.530 ± 0.009 (2)
Density	ρ	[g cm^{-3}]	0.539 ± 0.025 (2)
Eff. temperature	T_{eff}	[K]	6516 ± 49 (1)
Surf. gravity	$\log g$	[cgs]	4.23 ± 0.02 (1)
Metallicity	[Fe/H]	[dex]	0.05 ± 0.08 (1)
Age		[Gyr]	1.8 ± 0.5 (2)
Proj. rot. velocity	$v \sin i$	[km s^{-1}]	56 ± 2 (1)
Parallax		[mas]	3.684 ± 0.014 (3)
Magnitudes			
Filter		Magnitude	Uncertainty
TESS		10.2242	0.0061
<i>B</i>		11.233	0.11
<i>V</i>		10.632	0.007
Gaia		10.5905	0.00034
<i>J</i>		9.682	0.022
<i>H</i>		9.386	0.030
<i>K</i>		9.437	0.019

References. (1) Siverd et al. (2012); (2) This work; Gaia EDR3 (Gaia Collaboration et al. 2021).

The model parametrisation is shown in Table 2 and the parameter priors are discussed in more detail in Sect. 5.2. We assume a circular orbit since KELT-1b's orbital eccentricity agrees with zero (Siverd et al. 2012), which allows us to model the phase curve simply as a function of the orbital phase, $\phi = 2\pi(t - t_0)/p$, where t is the mid-exposure time, t_0 is the mid-transit time, and p is the orbital period.

The light curves are modelled jointly, and each light curve has its own baseline and noise model. We use a simple constant baseline model (that is, a normalisation factor), and model the systematics as a Gaussian process, as detailed later. All the baseline and noise model parameters are free (or loosely constrained) in the posterior optimisation and sampling.

4.2. Transits and eclipses

The transits are modelled using the quadratic limb darkening model by Mandel & Agol (2002) as implemented in PYTRANSIT (Parviainen 2015), and the limb darkening is parameterised

stands for the ratio of the radiation emitted towards the observer by the brown dwarf and the star per projected unit area. That is, the flux ratio is not the ratio of the disk-integrated fluxes, but this can be obtained by multiplying the flux ratio by the companion-star area ratio, k^2 .

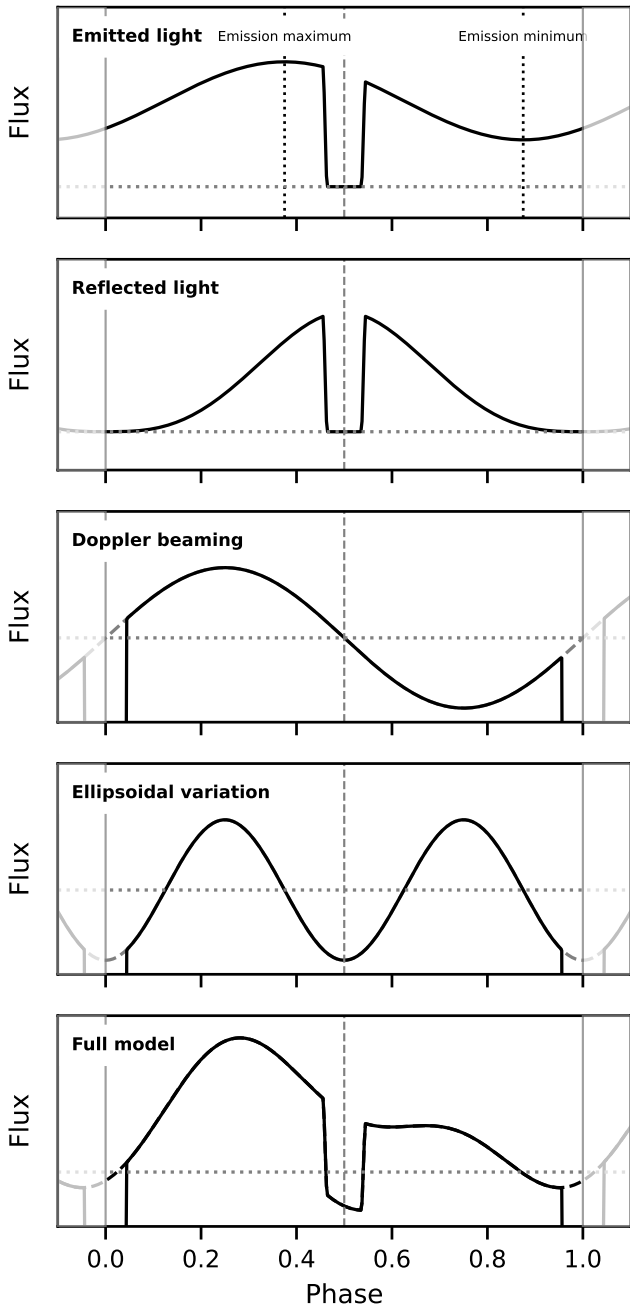


Fig. 2. Components of a phase curve model (transit, eclipse, emitted light, reflected light, Doppler beaming, and ellipsoidal variation) and the full model. The figure is centred around the secondary eclipse, the horizontal dotted line shows the baseline level (flux = 1), the vertical dashed line shows the eclipse centre, and the solid grey line shows the transit centre.

using the triangular parameterisation by [Kipping \(2013\)](#). The secondary eclipses are also modelled using `PyTRANSIT`, using an eclipse model that returns the fraction of visible planetary disk area to the stellar disk area. We do not include light travel time into the eclipse modelling since it is at maximum ≈ 25 s.

Table 2. Phase curve model parameters and priors used in the final joint analysis. The *global* parameters are independent of passband or light curve, the *passband-dependent* parameters are repeated for each passband, and the *light-curve-dependent* parameters are repeated for each separate light curve. $N(\mu, \sigma)$ stands for a normal prior with a mean μ and standard deviation σ , and $U(a, b)$ stands for a uniform distribution from a to b .

Description	Parameter	Units	Prior
<i>Global parameters</i>			
Mid-transit time	t_0	d	$N(T_{S12})^a$
Orbital period	p	d	$N(P_{S12})^a$
Area ratio	k^2	-	$N(0.078, 0.005)$
Stellar density	ρ	g cm^{-3}	$N(0.54, 0.08)$
Impact parameter	b	-	$U(0, 1)$
	$\sqrt{e} \cos \omega$	-	$N(0, 10^{-6})$
	$\sqrt{e} \sin \omega$	-	$N(0, 10^{-6})$
EV offset	o_{EV}	deg	$N(0, 5)$
<i>Passband-dependent parameters</i>			
Quad. LD coeff. 1	q_1	-	LDTk^b
Quad. LD coeff. 2	q_2	-	LDTk^b
EV amplitude	A_{EV}	-	U^c
DB amplitude	A_{DB}	-	N^d
Emission offset	o_e	deg	$N(0, 10)$
Log ₁₀ ds. emission	$\log_{10} f_d$	-	$U(-3, 0)$
Log ₁₀ ns. emission	$\log_{10} f_n$	-	$U(-3, 0)$
Geometric albedo	a_g	-	$N(10^{-5}, 10^{-7})$
<i>Light-curve-dependent parameters</i>			
Baseline level	f_0	-	N^e
Log ₁₀ white noise	$\log_{10} \sigma$	-	N^f
Ln GP input scale	s_i	-	$N(1, 1)^g$
Ln GP output scale	s_o	-	N^g

Notes. ^(a) The zero epoch and orbital period priors are based on the values reported in [Siverd et al. \(2012\)](#) with uncertainties multiplied by three. ^(b) The limb darkening coefficients have normal priors calculated using `LDTk`. ^(c) Ellipsoidal variation is constrained based by EV amplitude ratios as explained in the text and listed in [Table 3](#). ^(d) The Doppler beaming priors are given in [Table 3](#). ^(e) The baseline levels have wide normal priors that are based on the light curve variability. ^(f) The average log white noise parameters have normal priors centred around a numerical white noise estimate. ^(g) The Gaussian process log input scales have wide normal priors while the log output scales have normal priors based on light curve variability.

4.3. Reflected light

The reflected light¹⁰ is approximated using a Lambertian phase function ([Russell 1916](#); [Madhusudhan & Burrows 2012](#)). This choice is based on simplicity since our data is not precise enough to justify a more realistic (and flexible) phase function. The planet to star flux ratio from reflected light is

$$f_R = \frac{a_g \sin \alpha + (\pi - \alpha) \cos \alpha}{a_s^2 \pi}. \quad (2)$$

where a_g is the geometric albedo, a_s the scaled semi-major axis, $a_s = a/R_\star$, and α is the phase angle, $\alpha = |\phi - \pi|$. The reflected

¹⁰ We fix the reflected light component to zero for the main analyses due to its degeneracy with the thermal emission, but describe the component here for consistency.

light reaches its maximum near the eclipse and goes to zero near the transit.

4.4. Thermal emission

The thermal emission from the companion is modelled as a sine wave between the minimum flux ratio, f_n , and maximum flux ratio, f_d , as

$$f_E = f_n + \frac{f_{\max} - f_{\min}}{2} (1 - \cos(\phi + o)), \quad (3)$$

where o is a phase offset that sets the location of the hot spot, moving the minimum and maximum emission phases marked in Fig. 2.

4.5. Ellipsoidal variation

When a star is orbited by a massive companion on a short-period orbit, the companion's gravitational pull distorts the star's shape from a sphere into an ellipse. This causes an ellipsoidal variation (EV) signal (Morris 1985; Faigler & Mazeh 2011; Barclay et al. 2012; Lillo-Box et al. 2014) that can be approximated to a first order as

$$f_{EV} = -A_{EV} \cos(2\phi + o), \quad (4)$$

where o is an angular offset, the amplitude, A_{EV} , depends on the companion-host mass ratio, orbital inclination, i , and scaled semi-major axis, a_s , as

$$A_{EV} = \beta \frac{M_c}{a_s^3 M_\star} \sin^2(i), \quad (5)$$

where β is a factor that depends on the linear limb darkening coefficient, u , and gravity darkening coefficient, g , as

$$\beta = 0.15 \frac{(15 + u)(1 + g)}{3 - u}. \quad (6)$$

The EV signal is usually inconsequential when studying planetary phase curves, but it can dominate over the other phase curve components when a star is orbited by a massive companion on a short-period orbit, such as in the case of KELT-1b. Including the EV component into an eclipse and phase curve model is especially important because the EV signal has its minimum close to the mid-eclipse time (Bell et al. 2019; Beatty et al. 2020, and Sect. 6.3 in von Essen et al. 2021). Unaccounted for EV signal can artificially enhance the eclipse depth estimated from secondary eclipse observations, as happened with some of the previous KELT-1b observations.

4.6. Doppler beaming

Doppler beaming is calculated following Loeb & Gaudi (2003), Barclay et al. (2012), and (Claret et al. 2020) as

$$f_{DB} = A_{DB} \sin \phi, \quad (7)$$

where the Doppler beaming amplitude is

$$A_{DB} = \frac{\hat{B}}{c} \left(\frac{2\pi G}{p} \right)^{1/3} \frac{M_p \sin i}{M_\star^{2/3}}, \quad (8)$$

and c is the speed of light in vacuum, G is the gravitation constant, p is the orbital period, and \hat{B} is the photon-weighted passband-integrated beaming factor (Bloemen et al. 2010). The

passband-integrated beaming factor can be calculated from a stellar spectrum for any given passband as

$$\hat{B} = \frac{\int B \lambda F(\lambda) T(\lambda) d\lambda}{\int \lambda F(\lambda) T(\lambda) d\lambda}, \quad (9)$$

where $T(\lambda)$ is the passband transmission, F_λ is the stellar flux at wavelength λ , and $B = 5 + d \log F_\lambda / d \log \lambda$ is the beaming factor.

Unlike ellipsoidal variations, Doppler beaming has only a minimal effect on the observed eclipse depth. This is because the beaming signal behaves as a linear slope at the vicinity of the eclipse. In addition, beaming is expected to have a much lower amplitude for KELT-1b than EV.

5. Phase curve analysis

5.1. Overview

The goal of our study is to estimate the day- and nightside flux ratios between KELT-1b and its host star in the *CHEOPS*, *TESS*, *H*, *Ks*, and *Spitzer* 3.6 and 4.5 μm passbands. We do this by modelling the light curves described in Sect. 2 jointly using the phase curve model defined in Sect. 4, which will also yield improved orbital and geometric parameter estimates as a by-product. The analysis follows the standard procedures of Bayesian inference (Gelman et al. 2013; Parviainen 2018), where we aim to estimate the posterior probability distributions (posteriors) for the model parameters given a model, observations, and prior probability distributions (priors) for the model parameters.

We carry out three analyses that are each further divided into separate scenarios (summarised in Appendix B) with different priors on the phase curve model parameters. The analyses are:

1. **External data analysis** models the *TESS*, LBT, CFHT, and *Spitzer* observations jointly, and is implemented in `ExternalDataLPF` Python class. The external data analysis was carried out to create priors for the *CHEOPS* analysis, and also allows us to test how including the *CHEOPS* observations affects the final parameter estimates.
2. ***CHEOPS* analysis** models only the *CHEOPS*-observed eclipses, and is implemented in the `CHEOPSLPF` class. The main motivation for the *CHEOPS* analysis is to create detrended *CHEOPS* light curves to be used in the final analysis. As mentioned in Sect. 2.1, the *CHEOPS* light curves contain strong instrument-related systematics that are captured as basis vectors (covariates) using the approach described in Wilson et al. (2022). Modelling the *CHEOPS* observations jointly using a linear baseline model leads to a model with 180 free parameters, most of which are baseline model coefficients. This is a lot considering that the external data analysis has 79 free parameters, most of which are physically interesting. After some tests, we decided to carry out the *CHEOPS* analysis with a full baseline model and simplify the final analysis by using the *CHEOPS* analysis posterior baseline model to remove the systematics from the *CHEOPS* light curves included in the final analysis.
3. **Final analysis** models all the data jointly, and is implemented in the `FinalLPF` class.

The posterior estimates from the final analysis are adopted as the final results, but the differences between the analyses and scenarios are discussed in Appendix B.

All the analyses are implemented as Python classes that inherit `pytransit.lpf.PhaseCurveLPF`, where the base class implements the functionality to model phase curves jointly for a

set of heterogeneous light curves¹¹ (including optimisation and Markov Chain Monte Carlo sampling), and the derived classes mainly read in the different light curves, set up the noise models, and set up the model parameter priors based on the analysis scenario.


5.2. Priors

5.2.1. Orbit, geometry, and limb darkening

For the final and external dataset analyses, we set uninformative or only slightly informative priors on the geometric and orbital parameters, such as the orbital period, impact parameter, and companion-star radius ratio, as listed in Table 2. We also assume that the radius ratio is constant from passband to passband because of a small atmospheric scale height caused by KELT-1b's high surface gravity (Beatty et al. 2020). Further, we assume a circular orbit and force eccentricity to zero, since both the RV and eclipse observations agree with a circular orbit (Siverd et al. 2012).

The transit model adopts a quadratic limb darkening law with the Kipping (2013) parametrisation. We set uninformative priors on the *TESS* band limb darkening coefficients since the *TESS* light curve does not feature any strong systematics and the transit SNR is high. However, we set LDTk-calculated normal priors on the limb darkening coefficients for the two *Spitzer* passbands because the strong systematics in the *Spitzer* light curves will not allow us to constrain limb darkening well.

5.2.2. Doppler beaming

Since we have good estimates for the orbital parameters and the brown dwarf to star mass ratio (from Siverd et al. 2012 RV observations), we can set strict priors on the Doppler beaming amplitudes for each passband. We calculate the beaming factors and beaming amplitude priors for each passband with PYTRANSIT (namely using the `doppler_beaming_factor` and `doppler_beaming_amplitude` functions), using the BT-Settl (Allard 2013) model spectra to derive the beaming factors rather than a black body approximation. The beaming amplitude estimates are listed in Table 3, and they are computed in the [Doppler beaming](#)  notebook.

5.2.3. Ellipsoidal variation

As with Doppler beaming, we can calculate theoretical EV amplitudes for all the passbands by combining our prior knowledge about KELT-1b and its host star with stellar spectrum models. We use the companion-star mass ratio estimate from Siverd et al. (2012) and the semi-major axis estimate from Beatty et al. (2020). We estimate the linear limb darkening coefficients for each passband using LDTk (Parviainen & Aigrain 2015), and estimate the gravity darkening coefficients for the *CHEOPS* passband from the tables in Claret et al. (2020), for the *TESS* passband from the tables in Claret (2017), and for the *H*, *Ks*, and *Spitzer* passbands from the tables in Claret & Bloemen (2011).¹² As shown in Table 3, the EV signal amplitude is 10-20 times

larger than the DB signal amplitude, being roughly equal to the amplitude of the brown dwarf's phase curve signal in the *TESS* passband (Beatty et al. 2020; von Essen et al. 2021).

The EV amplitude scales with the semi-major axis as a_s^{-3} , which makes the theoretical EV amplitudes sensitive to our prior a_s choice. This causes a potential problem because EV directly affects our eclipse depth measurements. A biased prior a_s estimate could also significantly bias the eclipse depths measured for passbands with only near-eclipse photometry (*CHEOPS*, *H*, *Ks*) if we were to base the EV amplitude priors on the theoretical amplitudes. Thus, it would be better to try to find a way to constrain the EV amplitudes in a way that is independent of prior mass ratio and semi-major axis estimates.

Fortunately, the *TESS* light curve covers the whole orbital phase with a precision that allows us to estimate the EV amplitude in the *TESS* passband. The EV amplitude ratio between a passband i and the *TESS* passband t is simply

$$\frac{A_{\text{EV},i}}{A_{\text{EV},t}} = \frac{\beta_i}{\beta_t}, \quad (10)$$

where the β are the factors in Eq. (6) that depend on stellar gravity and limb darkening (which both are passband-dependent), but have no dependence on KELT-1b's mass or orbit.

Thus, we can constrain the EV signal by constraining the EV amplitudes relative to *TESS* passband rather than constraining the absolute EV amplitudes themselves. This approach is less likely to introduce biases to EV amplitudes, and so also less likely to bias the secondary eclipse signal. In the final analysis, we set uninformative priors on the absolute EV amplitudes on all passbands, and set informative priors on the EV amplitude ratios between the *TESS* passband any every other passband

$$\frac{A_{\text{EV},i}}{A_{\text{EV},t}} \sim N\left(\frac{\beta_i}{\beta_t}, \sigma\right),$$

where the β factors are calculated using the LDTk and gravity darkening tabulations described earlier and σ is the uncertainty in the β ratio estimate. Further, instead of using the uncertainties listed in Table 3, we set σ to 0.01 to reduce our sensitivity to any biases in the β factors (the chosen value is rather arbitrary but in general 3-10 times larger than the theoretical uncertainties).

5.3. Noise and systematics model

In addition to the planetary signal and the EV and Doppler boosting signals from the star, the photometry contains *systematics* from astrophysical and instrumental sources, as well as from changes in the observing conditions. These systematics need to be taken into account during the phase curve modelling.

We model the variability in the photometry not explained by the phase curve model as a Gaussian process (Rasmussen & Williams 2006; Gibson et al. 2012; Roberts et al. 2013). We use time as the only GP input for the *TESS* data, which allows us to use CELERITE (Foreman-Mackey et al. 2017) to evaluate the GP log likelihood for the whole unbinned *TESS* data set. The other data sets use more complex covariance functions with multiple input variables (e.g., x and y centroids, airmass and seeing), and for those we evaluate the GP log likelihood using GEORGE (Ambikasaran et al. 2014).

Each GP adds a set of hyperparameters into the joint model. We use simple covariance kernels (Matern-3/2 and squared exponential) which add only a log input scale parameter per input variable and a log output scale parameter per GP (detailed later

¹¹ Heterogeneous in the sense that they may have been observed in different passbands, exposure times (some light curves possibly needing model supersampling and others not), and each possibly with their own noise and systematics models.


¹² The EV amplitudes are calculated in the [EV notebook](#)  available from GitHub.

Table 3. Theoretical Doppler beaming and ellipsoidal variation amplitudes, and ellipsoidal variation amplitude ratios relative to the *TESS* passband.

Passband	Doppler beaming amplitude [ppm]	EV amplitude [ppm]	EV amplitude ratio
<i>CHEOPS</i>	63 ± 3.2	479 ± 30	1.083 ± 0.007
<i>TESS</i>	41 ± 2.1	442 ± 28	1.00
<i>H</i>	25 ± 1.3	358 ± 23	0.809 ± 0.004
<i>Ks</i>	19 ± 9.2	352 ± 22	0.796 ± 0.004
<i>Spitzer</i> 3.6 μm	17 ± 8.3	343 ± 22	0.774 ± 0.003
<i>Spitzer</i> 4.5 μm	16 ± 7.9	341 ± 22	0.772 ± 0.003

separately for each data set). These GP hyperparameters are constrained only loosely during the optimisation and MCMC sampling. We standardise the GP input variables (that is, we divide each input variable time series with its standard deviation and remove its mean) and constrain the log input scale parameters using normal priors centred at one with a standard deviation of one. The priors for the log output scale parameters are also normal and centred at log variance of the light curve with a standard deviation of 1.5.

We also fit the average white noise for each light curve. The white noise is parametrised using its log variance, and constrained with loose normal prior centred around a white noise estimate computed from the standard deviation of the flux point-to-point differences as

$$\sigma = \text{median}(\text{sd}(\text{diff}(f))) / \sqrt{2}, \quad (11)$$

where f is a vector containing the fluxes, sd stands for standard deviation, and diff stands for discrete difference.

The noise models are defined in the `_init_inlikelihood` method of the `FinalLPF` and `ExternalDataLPF` analysis classes, and the noise model parameter priors are set in the classes' `_post_initialisation` method. The posterior MCMC sampling marginalises over the whole GP hyperparameter space allowed by the priors and the data to ensure we are not overfitting the data.

TESS We model the variability in the *TESS* data as a Gaussian process with time as the only input variable using the `CELERITE` package. The GP uses basic Matern-3/2 covariance kernel that yields three additional parameters to the joint model, the log input and output scales and the log white noise variance, and these parameters are constrained with relatively loose normal priors as described earlier.

LBT H The systematics in the *H* band light curve are modelled as a GP with eight input variables (including, for example, the airmass and the target and comparison star locations). The covariance kernel is a product of eight squared exponential kernels where each kernel provides an independent input scale parameter into the joint model. This brings the total number of parameters from the *H* band data set noise model to ten.

CFHT Ks The systematics in the *Ks* band light curve are modelled as a GP with two input variables, the x and y centroids. The covariance kernel is a product of two squared exponential kernels where each kernel provides an independent input scale parameter into the joint model, leading in total to four additional parameters.

Spitzer The systematics in the *Spitzer* data are also modelled using a GP with the x and y centroids as the input variables. The [Beatty et al. \(2019\)](#) *Spitzer* phase curve observations were split into three 12 h long stares and the telescope was repointed between the stares. This repointing led to strong discontinuities in the raw photometry, so we decided to treat each 12 h stare as a separate light curve. This gives us four light curves per *Spitzer* passband (one covering the [Beatty et al. 2014](#) eclipse and three covering the phase curve). However, all the eight light curves use the same GP kernel and hyperparameters (we assume the centroid-related systematics in both *Spitzer* passbands have similar input and output scales), so the *Spitzer* GP model adds only four parameters to the joint model.

The *Spitzer* light curves consist of 10 000 (eclipse) and 64 000 (phase curve) flux measurements. This is too much for a standard brute-force GP that requires inversion of the covariance matrix and scales as $O(n^3)$. Splitting the phase curve observations helps, but we still needed to bin the *Spitzer* observations to a two-minute cadence to make a GP noise model computationally feasible.

CHEOPS The *CHEOPS* data is modelled differently in the final analysis and in the initial *CHEOPS*-only analysis. In the *CHEOPS* analysis we use a linear model to model the systematics with basis vectors determined by the pipeline of [Wilson et al. \(2022\)](#) used as covariates. The number of basis vectors used per visit varies from 13 to 29, and the total number of basis vectors (and thus free parameters from the baseline model) is 156.

The noise model for the *CHEOPS* data assumes i.i.d. (independent and identically distributed) normally distributed noise (that is, white noise), and introduces only the logarithm of the average standard deviation of the noise distribution for each visit as an additional free parameter into the full model (that is, we assume the noise does not vary significantly from observation to observation within a single light curve, and marginalise over the average observation uncertainty).

In the final analysis, we detrend the *CHEOPS* data using the posterior median baseline model from the *CHEOPS* analysis and give each visit only a free normalisation term. We do this to simplify the final model, since using the full *CHEOPS* baseline model would add 156 free parameters into the final model. There is a danger that this approach could lead to underestimated uncertainties in some of our quantities of interest, but a comparison of the *CHEOPS* and final analysis results (see Sect. B) shows that any effects from not marginalising over the baseline model coefficients in the final analysis are insignificant.

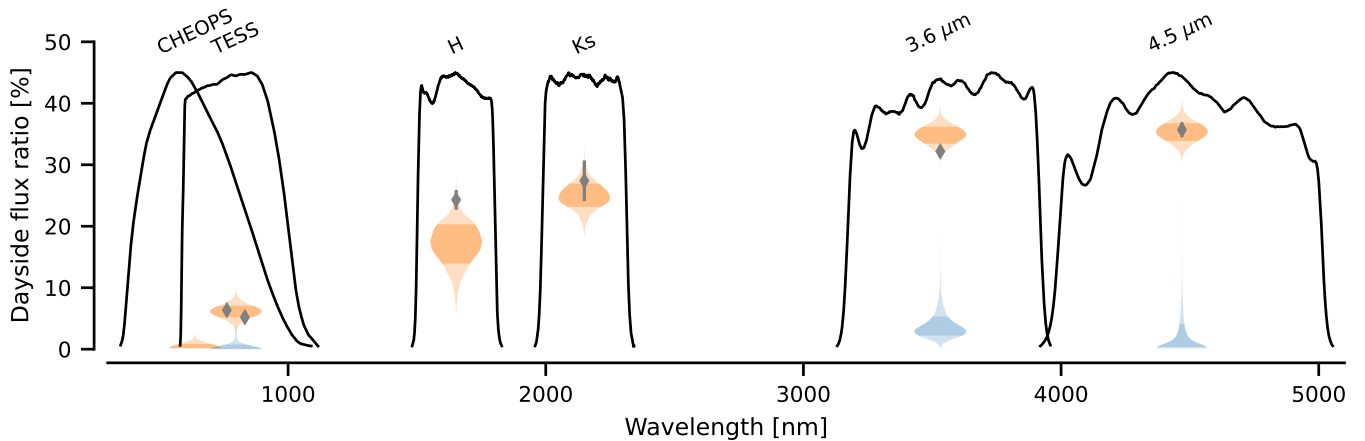


Fig. 3. The dayside (orange) and nightside (blue) planet-star flux ratio posterior distributions for all passbands. The central 68% posterior interval is marked with a dark shade and the previous dayside flux ratio estimates are shown as diamonds with errorbars showing their reported uncertainties. For *TESS*, the Beatty et al. (2020) estimate is shown on the left and the von Essen et al. (2021) estimate is shown on the right.

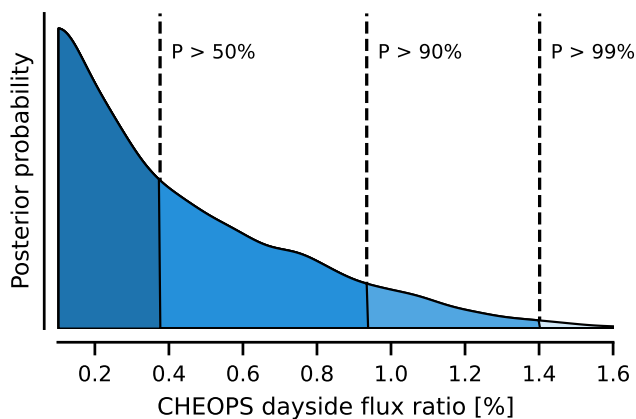


Fig. 4. Dayside flux ratio posterior distribution for the *CHEOPS* passband. The dashed lines show the posterior percentile limits.

6. Results and Discussion

6.1. Results from the phase curve analysis

We show the dayside and nightside planet-star flux ratio posteriors from the final joint modelling for all passbands in Fig. 3, give a more detailed view of the *CHEOPS* band dayside flux ratio posterior in Fig. 4, and show the observations and the model posteriors for all the passbands in Fig. 5. The final flux ratio estimates are reported in Table 4, and the rest of the parameter estimates in Table 5. The results from the external dataset and *CHEOPS*-only analysis scenarios are presented in Appendix B.

Except for the *CHEOPS* band, the dayside flux ratio posteriors are approximately normal with a well-defined non-zero mode, and for these posteriors we report their median values with uncertainties based on the 16th and 84th central percentiles in Table 4. The *CHEOPS* band flux ratio posterior has its mode at zero, and we report its posterior median and 99th percentile upper limits.

The nightside flux ratio posteriors all have their modes at zero, and we report only the 99th posterior percentile upper limits. The nightside flux ratio upper limit for the *TESS* band is 4.6%, while for the *Spitzer* bands it is $\approx 12\%$.

The dayside flux ratios for the *TESS* and *Spitzer* passbands (Fig. 3) agree fairly well with the previous studies by Beatty et al. (2020), von Essen et al. (2021), and Beatty et al. (2019). The flux ratios for the *H* and *Ks* bands are lower than what reported by Beatty et al. (2017) and Croll et al. (2015), but this is expected since neither of the original studies included an ellipsoidal variation signal into their models.

The dayside flux ratio for the $3.6\ \mu\text{m}$ *Spitzer* band is higher than the estimate by Beatty et al. (2019). The *Spitzer* light curves use relatively flexible GP systematics models and all the *Spitzer* light curves are well-fit visually (Fig. 5). Even then, we cannot rule out poorly modelled systematics as the source of the anomalously high $3.6\ \mu\text{m}$ flux ratio since the pre-eclipse baseline is relatively short for the full-phase *Spitzer* observations.

Curiously, the *CHEOPS* and *TESS* bands show a strong discrepancy in their dayside flux ratios. Panel a) of Fig. 6 shows the *CHEOPS* observations with the median posterior model and panel b) shows the same for *TESS*. The combined *CHEOPS* observations have a noise estimate of ≈ 50 ppm over a 20-min bin, half of the *TESS* noise of ≈ 97 ppm, but we do not detect a significant eclipse signal in the *CHEOPS* band. Instead, we are only able to set an upper limit of 1.4% for the *CHEOPS* dayside flux ratio, while in the *TESS* band we detect a clear eclipse corresponding to a flux ratio of $6 \pm 1\%$.

6.2. Dayside brightness temperatures

We estimate the day- and nightside brightness temperatures, T_b , separately for each passband using the flux ratio estimates from the final joint modelling and BT-Settl stellar spectrum models by Allard (2013). We calculate the T_b estimates as averages over three approaches: a) physical-physical, where both the brown dwarf and its host star spectra are modelled with BT-Settl models; b) blackbody-physical, where KELT-1b is modelled as a black body and the star uses a BT-Settl model; and c) blackbody-blackbody, where both KELT-1b and the star are modelled as black bodies.

Figure 7 shows the approach-averaged brightness temperatures together with the best-fitting constant dayside temperature (the T_b estimates are also included in Table 4, and the per-approach estimates are shown in Appendix C). The dayside temperatures mostly agree with each other within the uncertainties.

Table 4. Final day- and nightside planet-star flux ratios and eclipse depths with their uncertainties and upper limits.

Passband	Ns. flux ratio [%]	Ns. T_b [K]	Ds. flux ratio [%]	Eclipse depth [ppm]	Ds. T_b [K]
<i>CHEOPS</i>			< 1.50	< 90	2100 – 2900
<i>TESS</i>	< 4	< 3000	6.1 ± 0.9	360 ± 50	3100 – 3500
<i>H</i>			17.3 ± 3.2	1000 ± 190	2100 – 3400
<i>Ks</i>			24.9 ± 1.9	1460 ± 110	2900 – 3400
<i>Spitzer</i> 3.6 μm	< 11	< 1900	34.9 ± 1.4	2040 ± 80	3000 – 3400
<i>Spitzer</i> 4.5 μm	< 12	< 1800	35.3 ± 1.5	2070 ± 80	2800 – 3200

Notes. The nightside estimates give an upper limit corresponding to the 99th posterior percentiles. The dayside estimates correspond to posterior medians with uncertainties based on the 16th and 84th posterior percentiles (except for *CHEOPS*, for which we only give the upper limit). The reported dayside brightness temperature values are lower and upper limits corresponding to 2.5th and 97.5th posterior percentiles.

Table 5. Final estimates for the geometric and orbital parameters of KELT-1b and its host star.

<i>Ephemeris</i>			
Transit epoch	T_0	[BJD]	$2455914.1624 \pm 4 \times 10^{-4}$
Orbital period	P	[days]	$1.2174942 \pm 2 \times 10^{-7}$
Transit duration	T_{14}	[h]	2.74 ± 0.01
<i>Relative properties</i>			
Area ratio	k^2	[A_\star]	$0.00585 \pm 7 \times 10^{-5}$
Radius ratio	k	[R_\star]	$0.0765 \pm 5 \times 10^{-4}$
Semi-major axis	a	[R_\star]	3.53 ± 0.09
Impact parameter	b	[R_\star]	$0.35 (-0.08) (+0.06)$
<i>Absolute properties</i>			
KELT-1b radius	R_c	[R_{Jup}]	1.138 ± 0.010
KELT-1b surface gravity	$\log g_c$	[cgs]	4.73 ± 0.02
KELT-1b eq. temperature ^(a)	T_{eq}	[K]	2550 ± 170
Semi-major axis	a	[AU]	0.0251 ± 0.0006
Orbital inclination	i	[deg]	$84.3 (-1.1) (+1.4)$
Stellar density	ρ_\star	[g cm^{-3}]	0.56 ± 0.04
<i>TESS</i> emission offset	O_T	[deg]	3 ± 9
<i>Spitzer</i> 3.6 μm emission offset	O_{S1}	[deg]	-29 ± 5
<i>Spitzer</i> 4.5 μm emission offset	O_{S2}	[deg]	4 ± 6

Notes. The estimates correspond to the posterior median with the uncertainties based on the 16th and 84th posterior percentiles. ^(a) The equilibrium temperature is calculated using the stellar T_{eff} estimate, scaled semi-major axis distribution, heat redistribution factor distributed uniformly between 0.25 and 0.5, and albedo distributed uniformly between 0 and 0.4.

In agreement with Beatty et al. (2020), the *TESS* passband has a somewhat higher T_b than the *Spitzer* bands, but the disagreement is less significant for us (for example, the *TESS* and *Spitzer* 3.6 μm band 68% central posterior intervals overlap). Our T_b estimate for the *TESS* passband agrees well with the Beatty et al. (2020) result, but our *Spitzer* T_b estimates are higher than what reported in Beatty et al. (2019).

As expected from the differences in the dayside flux ratios, the dayside T_b estimate for *CHEOPS* is significantly lower than for *TESS*.

6.3. Nightside brightness temperatures

We can measure the nightside brightness temperatures only for the passbands where we have observations over the full orbital phase (*TESS* and *Spitzer*), and the estimates are rather poorly constrained. Both *Spitzer* passbands support cool night sides, with 99th T_b posterior percentiles ≈ 1850 K, while in the *TESS*

passband we can only set a 3000 K upper limit. These results support a significant temperature difference between the night- and dayside, and agree with the previous *Spitzer* and *TESS* analyses by Beatty et al. (2020) and von Essen et al. (2021)

6.4. Atmospheric modelling

For the atmospheric modelling, we follow the same basic approach as done in Lendl et al. (2020). In particular, we employ the self-consistent atmosphere model HELIOS (Malik et al. 2017, 2019) to generate a grid of possible atmospheres for KELT-1b. As discussed in Lendl et al. (2020), in the context of 1D models, the flux of the host star impinging upon the top of the atmosphere (TOA) of KELT-1b is (Cowan & Agol 2011)

$$F_{\text{TOA}} = F_\star \left(\frac{R_\star}{a} \right)^2 (1 - A_B) \left(\frac{2}{3} - \frac{5\epsilon}{12} \right), \quad (12)$$

where F_\star is the stellar photometric flux, R_\star the radius of the host star KELT-1, a the orbital distance of KELT-1b, A_B its Bond

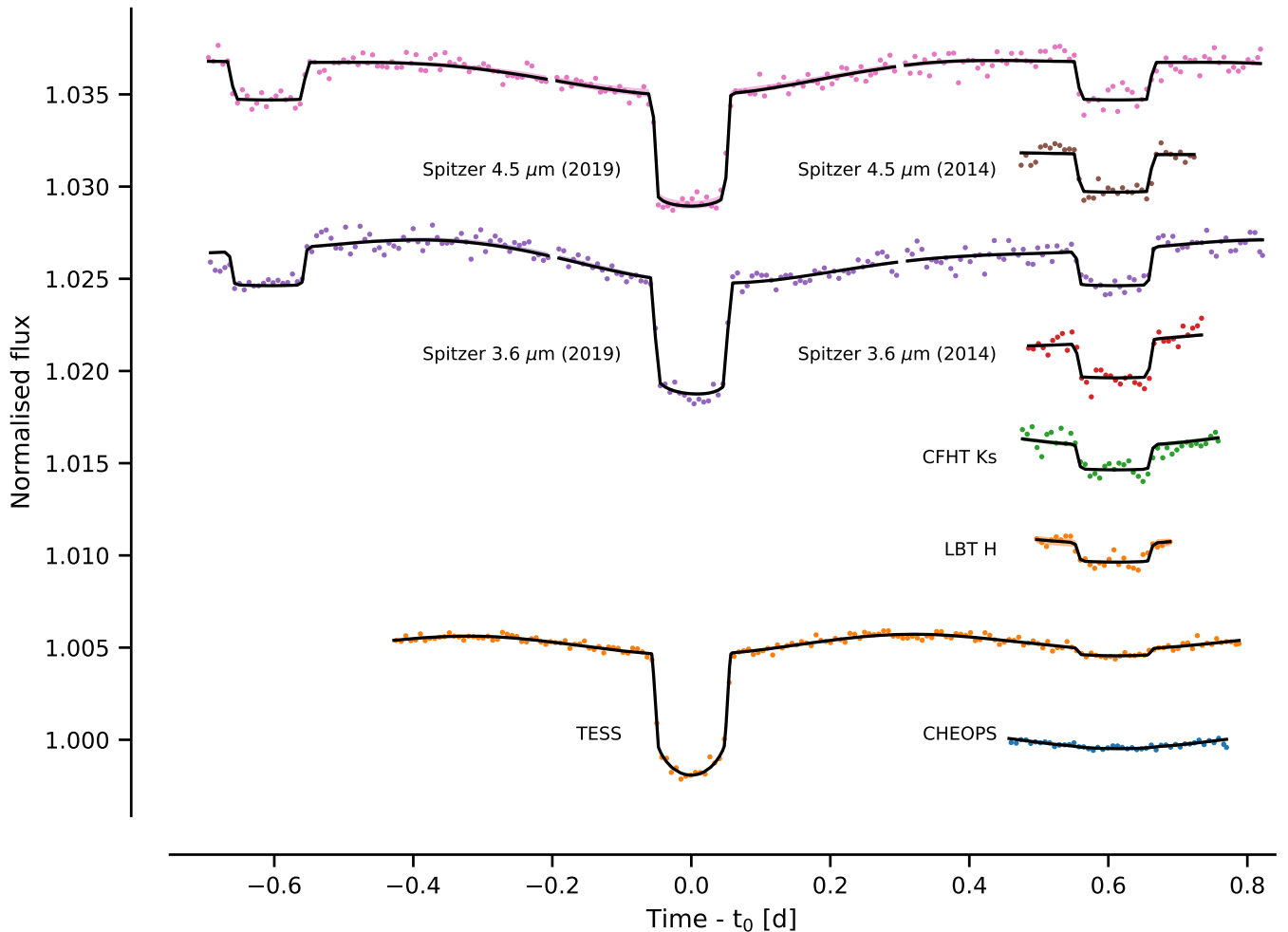



Fig. 5. The observed light curves from *CHEOPS*, *TESS*, *LBT*, *CFHT*, and *Spitzer* (points) and the posterior median phase curve model (black line). The systematics model has been removed from the observations, the *TESS* and *CHEOPS* observations have been folded over the phase, and the data has been binned to 10 min for visualisation purposes. The figure is produced by the [final light curve plot](#)  notebook.

albedo, and ϵ the heat redistribution efficiency ($0 \leq \epsilon \leq 1$). In terms of the atmosphere model HELIOS, the term

$$E_* = (1 - A_B) \left(\frac{2}{3} - \frac{5\epsilon}{12} \right) \quad (13)$$

is fully degenerate with respect to A_B and ϵ , such that we only vary E_* rather than A_B and ϵ independently.

Since KELT-1b is a brown dwarf, its emission might also have a considerable contribution from an internal energy flux, described by an internal temperature T_{int} . In case of an isolated object without exterior insolation, T_{int} would be the object's effective temperature. For the construction of the model grid, we therefore use T_{int} as an additional free parameter. Given the lack of any spectrally-resolved data for KELT-1b and the fact that the host star's $[\text{Fe}/\text{H}]$ value is consistent with 0 (see Table 1), we use solar element abundances for the model grid, for simplicity. The general modelling parameters for KELT-1b (surface gravity, stellar radius, orbital distance) are taken from Tables 1 & 5.

Using HELIOS, we generate a model grid of self-consistent forward atmosphere models for KELT-1b in terms of the free parameters T_{int} and E_* . In total we compute 165 different atmospheric model structures for internal temperatures between 0 K and 3000 K and E_* values from 0.667 to 0.06. The former value

is the highest possible one for E_* , with a Bond albedo and heat redistribution ϵ of 0. The latter value represents a case with a high Bond albedo and/or very efficient heat redistribution.

Besides the atmospheric structure, we also obtain the brown dwarf's emission spectrum for each model in a postprocess procedure. For this postprocess, we exclude any scattering contribution, such that the obtained emission spectra describe only the atmosphere's thermal emission. These spectra are then integrated over the passbands shown in Table 4

$$F_{\text{pb}} = \int \mathcal{F} F_{\lambda} d\lambda \quad (14)$$

to calculate the flux F_{pb} inside each passband. Here, \mathcal{F} is the corresponding filter transmission function and F_{λ} the calculated emission spectrum of KELT-1b.

Since these F_{pb} are a smooth function of T_{int} and E_* , we parameterise them as a two-dimensional, fifth-order polynomial in each passband. This allows us to evaluate the passband-integrated fluxes $F_{\text{pb}}(T_{\text{int}}, E_*)$ as a continuous function of T_{int} and E_* directly, rather than having to perform an interpolation in two dimensions.

These passband-integrated fluxes are then added to a forward model in the Bayesian retrieval framework Helios-r2 ([Kitz-](#)

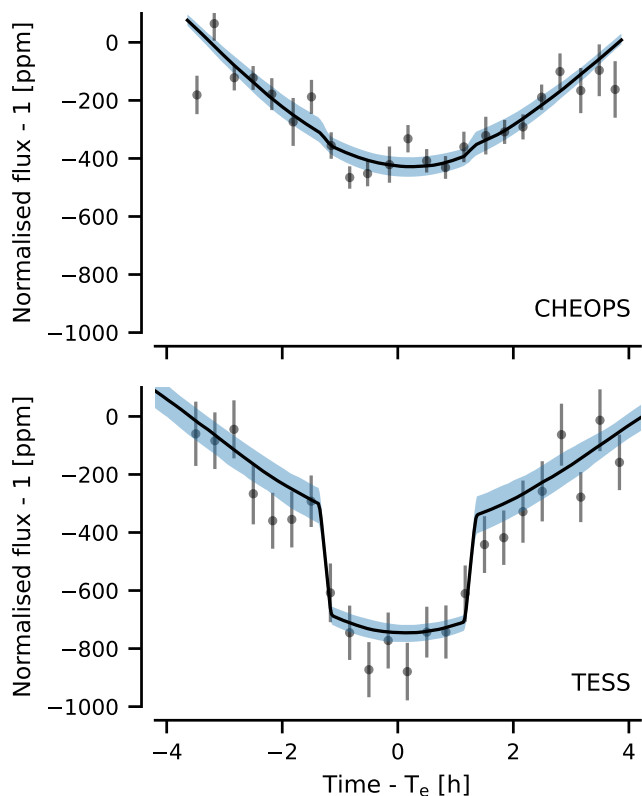


Fig. 6. The *CHEOPS* eclipse observations binned to a 20-minute cadence with the phase curve model (panel a) and *TESS* observations with a similar binning (panel b). The median posterior phase curve model is shown as a black line and its 68% central posterior interval is shown as a shaded blue region.

mann et al. 2020) to constrain the geometric albedos in the *TESS* and *CHEOPS* passbands ($A_{g,T}$ and $A_{g,C}$). This forward model calculates the secondary eclipse depths dF_{se}

$$dF_{se} = A_g \left(\frac{R_p}{a} \right)^2 + \frac{F_{pb}(T_{int}, E_*)}{\int \mathcal{F} F_* d\lambda} \left(\frac{R_p}{R_*} \right)^2 \quad (15)$$

as a function of the free parameters A_g , R_p/a , R_p/R_* , T_{int} , and E_* in each photometric passband. The stellar photospheric spectrum F_* is taken from the grid of PHOENIX stellar atmosphere models (Husser et al. 2013), based on the stellar parameters given in Table 1.

Within the retrieval forward model we assume that only the *CHEOPS* and *TESS* passbands have contributions by a geometric albedo, whereas the other ones are dominated by thermal emission rather than reflected light. This is based on the fact that the stellar spectrum peaks at lower wavelengths, where the *CHEOPS* and *TESS* passbands are located. The *TESS* band receives 64% of the stellar flux received by the *CHEOPS* band, and the *H*, *Ks*, 3.6 μm , and 4.5 μm bands receive 7%, 3%, 1%, and 0.5% of the flux received by the *CHEOPS* band, respectively. The four photometric measurements (*H*, *Ks*, *Spitzer*) in the infrared are dominated by the brown dwarf’s own thermal emission rather than by scattering of its host star’s incident flux.

The posterior distributions of our retrieval calculations are shown in Fig. 8 while the posterior photometric points are depicted in Fig. 9. The posterior distributions show a strong correlation between the parameters E_* and T_{int} . When the retrieval is performed only on the *TESS* and *Spitzer* data points, bimodal

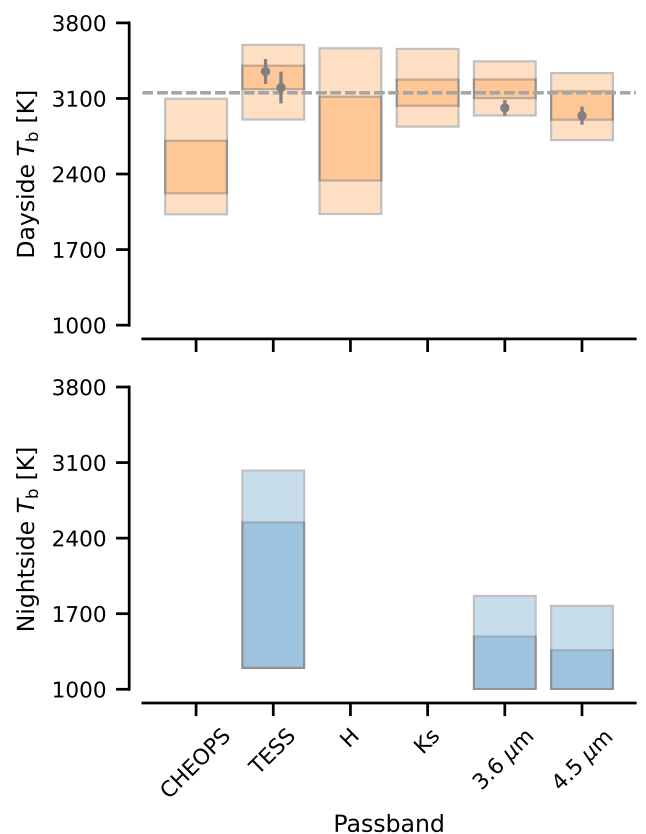


Fig. 7. Day- and nightside brightness temperatures estimated from the flux ratios using the BT-Settl stellar model spectra by Allard (2013). The shading marks the 68% and 99.7% central posterior intervals, from the darkest to the lightest shade, and the dashed horizontal line shows the best-fitting constant brightness temperature. The previous dayside T_b estimates for the *TESS* and *Spitzer* passbands by Beatty et al. (2019), Beatty et al. (2020), and von Essen et al. (2021) are shown as points with errorbars.

solutions for these two quantities are obtained (see Appendix D). This bimodality is broken primarily by the *H* and *Ks* data points, while the *CHEOPS* data point further narrows the posterior distribution on E_* . The retrieved value of $T_{int} = 2670_{-150}^{+190}$ K implies that the brown dwarf has a very strong contribution from an internal heat flux to the total energy budget of the atmosphere and corroborates the findings of Beatty et al. (2020). As already noted by Beatty et al. (2019), an isolated brown dwarf with the same age and mass would have an internal temperature of about 850 K. The relatively low value of $E_* = 0.22 \pm 0.08$, on the other hand, suggests that the heat recirculation ϵ must very high, or that the atmosphere has a large Bond albedo A_B .

For the *TESS* passband, we obtain a geometric albedo of about $0.36_{-0.13}^{+0.12}$, while in the *CHEOPS* passband the results are consistent with a geometric albedo of 0.

The resulting photometry posteriors in comparison to the measured data are shown in the lower panel of Fig. 8. The results imply that atmosphere forward models can explain most of the measured data points while especially the *Spitzer* 3.6 μm band shows larger deviations. This mismatch in the *Spitzer* 3.6 μm band might point to non-equilibrium chemistry effects. The predicted *CHEOPS* photometry secondary eclipse depth also deviates from the measured one. In fact, even without including an additional geometric albedo contribution, the measured eclipse

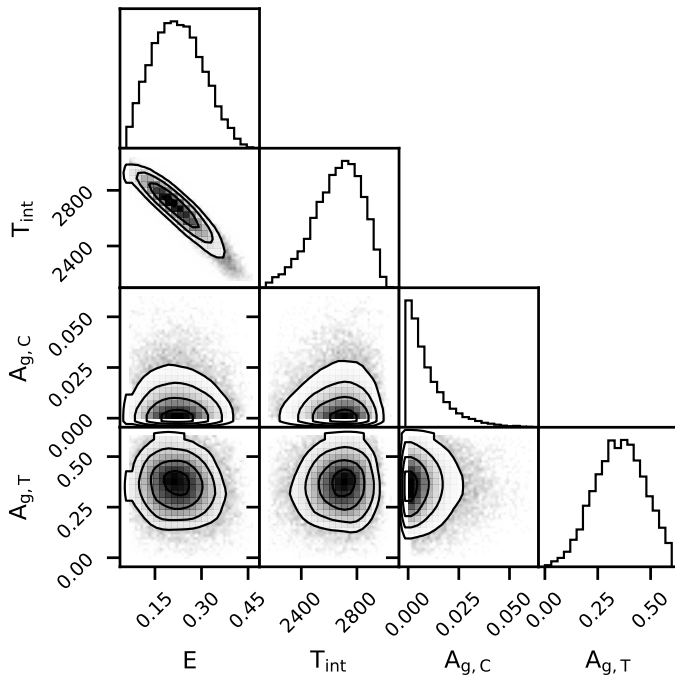


Fig. 8. Posterior distributions for the retrieval calculations using *Helios-r2*. We show only the four most important parameters. The rest are strongly constrained by priors and do not show significant correlations between other parameters.

depth cannot be described by the expected thermal emission of the planet.

The upper panel of Fig. 10 depicts the heat recirculation efficiencies ϵ and Bond albedos A_B that are consistent with the retrieved value of $E_* = 0.22 \pm 0.08$ and the upper nightside T_b limit of 1900 K. If the heat redistribution is very efficient ($\epsilon \approx 1$), then the Bond albedo has to be close to 0. On the other hand, if only very little heat gets transported to the nightside ($\epsilon \approx 0$), then the Bond albedo has to be in the range of 0.7, implying that potentially clouds scatter almost 70% of the incident stellar radiation back to space. In principle, given constraints on T_{int} , the dayside temperature and the nightside temperature, the degeneracy between A_B and ϵ could be broken.

Additionally, we calculate a separate *HELIOS* model for the above stated retrieved median values of E_* and T_{int} . The resulting temperature-pressure profile is shown in the bottom panel of Fig. 10. Due to the very high T_{int} , the temperature increases very strongly in the lower atmosphere, while being close to isothermal around 0.1 bar, and showing a temperature inversion in the upper atmosphere, originating from the absorption of stellar light. The plot also depicts a set of stability curves for selected high-temperature condensates. These stability curves in combination with the atmosphere’s temperature profile imply that most likely condensates do not form on the dayside of KELT-1b. This is not surprising given its high equilibrium temperature.

The derived geometric albedo of $0.36^{+0.12}_{-0.13}$ in the *TESS* passband is challenging to explain, since even the most refractory mineral (corundum) does not condense at the derived dayside temperatures. However, it agrees with the scenario where silicate clouds form on the nightside of the brown dwarf and are then transported to the dayside by winds, as well as with geometric albedos for silicate cloud-covered planets of ~ 0.4 predicted by Sudarsky et al. (2000). It is nevertheless difficult to reconcile this high value of the *TESS* geometric albedo with a *CHEOPS*

geometric albedo of essentially zero, because the two passbands have considerable overlap.

6.5. Chromatic albedo variability as a possible source of discrepancy between *CHEOPS* and *TESS*

The albedo spectrum of a planet (or, as in our case, a brown dwarf) can feature clear distinct regions of low and high reflectivity in wavelength space (Sudarsky et al. 2000; Burrows et al. 2008). In theory, a low blue-optical albedo combined with a high NIR albedo could be explained with silicate clouds and a strong optical absorber above the silicate cloud deck (such as gaseous TiO/VO or S₂/HS, Schwartz & Cowan 2015), and there is a possibility that the discrepancy between the *CHEOPS* and *TESS* dayside flux ratios could be explained by a high-contrast feature in KELT-1b’s albedo spectrum.

We modelled whether the *CHEOPS-TESS* discrepancy could be explained by chromatic variations in KELT-1b’s albedo using a simple two-level albedo spectrum model parametrised by the geometric albedo in blue, $A_{g,0}$, geometric albedo in red, $A_{g,1}$, and step location, λ_0 , dictating where the blue albedo changes to red. The modelling is detailed in Appendix A and carried out in the [chromatic albedo variation test](#) notebook.

As a conclusion, the discrepancy is challenging to explain with a simple two-level albedo spectrum model due to the large overlap between the *CHEOPS* and *TESS* bands. The largest *TESS* to *CHEOPS* reflected light contrast, $C = (F_T - F_C)/(F_T + F_C)$, of 0.41 is obtained for a step model with $A_g = 0.01$ for $\lambda < 860$ nm and $A_g = 0.4$ for $\lambda \geq 860$ nm, as illustrated in Fig. A.1. A geometric albedo of 0.01 is not unheard of for a highly irradiated body, but is similar to what has been estimated for TrES-2b (Kipping & Spiegel 2011), while the geometric albedo of 0.4 corresponds to the silicate cloud models by Sudarsky et al. (2000), and is in line with the previous KELT-1b study by Beatty et al. (2020). However, the maximum contrast of 0.4 is at the lower tail of the measured C posterior distribution that has its mode at 0.9 (Fig. A.2). Even a blue A_g of 0.001 with $\lambda_0 = 940$ nm would lead to C of only 0.6, so it is unlikely that a physically plausible albedo spectrum would be able to reproduce the observed *CHEOPS-TESS* discrepancy.

6.6. Temporal variability as a possible source of discrepancy between *CHEOPS* and *TESS*

Since the upper limits on the nightside temperature are low enough that clouds could conceivably form, it is plausible that nightside clouds could be transported to the dayside (Beatty et al. 2020), where they could survive transiently. This raises the possibility of dayside cloud cover being transient. Variability in cloud cover could be one possible explanation for the dayside flux ratio discrepancy between the *CHEOPS* and *TESS* passbands. von Essen et al. (2021) reported possible temporal variation in the eclipse depths in the *TESS* data, but concluded that the variations were most likely associated with stellar variability. We likewise carried out per-eclipse analyses for the *TESS* and *CHEOPS* data, but also need to conclude that the per-eclipse precision is not high enough to study whether the eclipse depths show systematic variations that would securely not be caused by stellar variability or systematics.

The spatial distribution of transient dayside clouds transported from the brown dwarf’s nightside can be expected to be strongly nonuniform, which would lead to asymmetric reflection phase curve as with Kepler-7b (Demory et al. 2013). While our

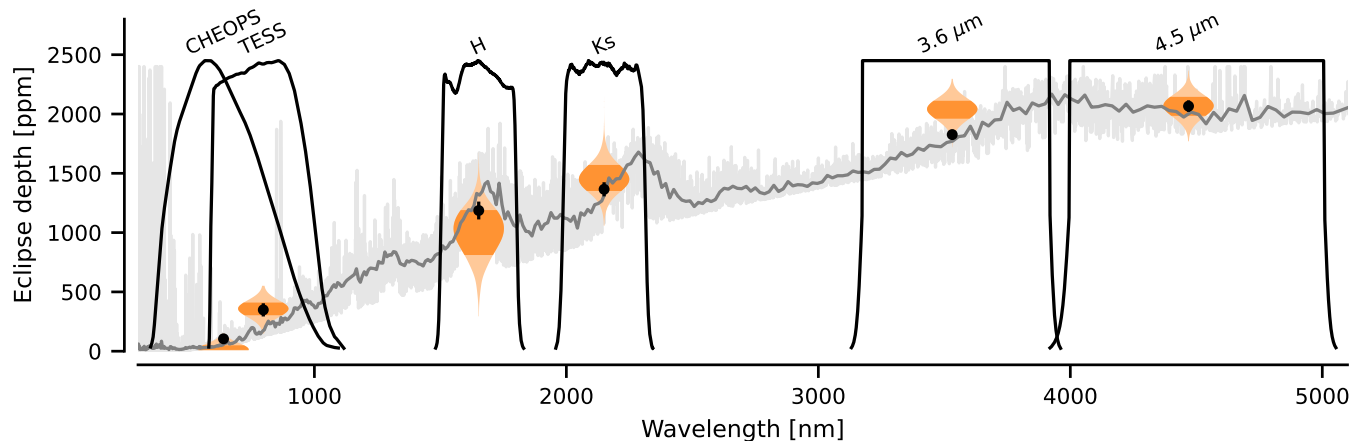


Fig. 9. Posterior model spectrum for the retrieval calculations using Helios-r2. The light gray line shows the high resolution version of the posterior thermal emission model median, and the darker gray line shows the same spectrum in medium resolution. The black points show the retrieval eclipse depths with their corresponding 1σ intervals, and the orange shaded areas show the eclipse depth posteriors estimated from the photometry as given in Table 4. The black labelled lines show the passbands, where the *Spitzer* passbands are simplified for visualisation.

analyses simplify the KELT-1b's flux contribution by using only the emission component, the emission component has a loosely constrained phase offset that allows it to catch any existing phase curve asymmetries.

The emission offset (see Table 5) agrees with zero for the *TESS* and *Spitzer* 4.5 μm bands, but is significantly non-zero for the *Spitzer* 3.6 μm band. Of these three, only the *TESS* band phase curve is expected to have a significant contribution from reflection, and the lack of measurable phase curve asymmetry speaks against the cloud transport hypothesis. Then again, were the dayside cloud coverage to be variable, the variability could blur the asymmetry when averaged over the *TESS* observations of 25 days.

The *TESS* and *Spitzer* phase offsets disagree with the ones estimated by Beatty et al. (2019) and Beatty et al. (2020). They observe slight eastward shifts for the *TESS* and *Spitzer* 4.5 μm bands and a strong eastward shift for the *Spitzer* 3.6 μm band, while our shifts are westwards.

The phase curve asymmetry in *Spitzer* 3.6 μm band is curious. The *Spitzer* phase curve observations were carried out eight days apart of each other, so the differences could be explained by temporal variability in emission and reflection. This could also explain the higher-than expected dayside eclipse depth for the 3.6 μm band (Fig. 9). Our eclipse depth estimate differs from the result from Beatty et al. (2019) (whose estimate agrees with the theoretical models) and we extracted the *Spitzer* light curves using our own pipeline, so we cannot completely rule out untreated systematics. However, the time-scale of the variability (smooth over KELT-1b phase) combined with our use of a flexible GP to model the *Spitzer* systematics lead us to believe the differences in the two *Spitzer* phase curves arise from true variability in the KELT-1b's phase curve.

6.7. Comparison between emission spectrum models

We compare our retrieved emission spectrum with the spectra by von Essen et al. (2021), the BT model spectra (Allard 2013)¹³ and DRIFT-PHOENIX spectra (Witte et al. 2011)¹⁴ for isolated

¹³ Downloaded from F. Allard's [Star, Brown Dwarf, and Planet simulator](#).

¹⁴ Obtained from the [SVO Theoretical spectra web server](#).

brown dwarfs in Fig. 11. The "Helios-r2" results correspond to the modelling described earlier in Sec. 6.4 and the "VE21a" and "VE21b" results correspond to the modelling detailed in von Essen et al. (2021). The rest of the results correspond to best-fitting BT-SETTL, BT-NextGen, BT-COND, BT-Dusty, and DRIFT-PHOENIX models where the host star was modelled using a BT-SETTL spectrum with $T_{\text{Eff}} = 6500$ K, $\log g = 4.0$ and $z = 0.0$.

The best fitting BT and DRIFT-PHOENIX models correspond to a dayside temperatures of 3000 K (DRIFT-PHOENIX) and 3100 K (BT models) and fit even the *CHEOPS* passband surprisingly well. However, none of the isolated brown dwarf models can simultaneously explain both the *CHEOPS* and *TESS* eclipse depths.

6.8. Sensitivity on parametrisation and priors

The choice of parametrisation and priors generally affects the parameter posteriors, and this effect can be significant when studying weak signals. We parameterise the day- and nightside emission using log flux ratios and set uniform priors on these, which equals to setting log-uniform (reciprocal) priors on the day- and nightside emission flux ratios. This differs from previous studies using uniform priors on the flux ratios.

We repeated our final joint analysis parametrisation it with flux ratios rather than log flux ratios to study how sensitive our posteriors are on the choice of parametrisation. The most notable difference was in nightside flux ratios, where uniform priors led to distributions with non-zero modes and the maximum flux ratios (99th posterior percentile) were somewhat higher than when using log-uniform priors. The second notable difference was in the *CHEOPS* band dayside flux ratio posterior, which again had a non-zero mode with slightly larger maximum values. However, the difference in the maximum flux ratio was not large enough to change the main outcome of the analysis. The dayside flux ratio posteriors for other passbands were not significantly affected.

We adopt the log flux ratio parametrisation since this should be more suitable for a "scale" parameter with an unknown magnitude. This ensures that we do not give too much weight on apparent posterior modes if in reality we can only estimate the upper limit securely.

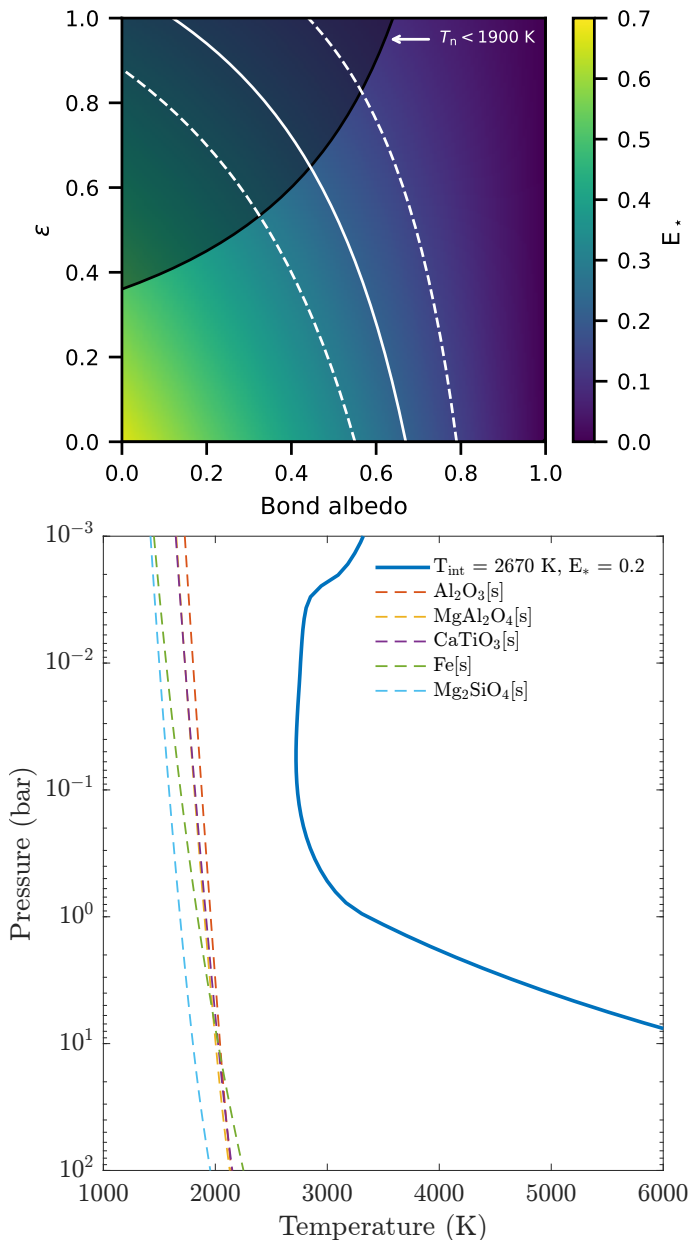


Fig. 10. The upper panel depicts the values of E_* as function of the heat recirculation parameter ϵ and Bond albedo A_B . The solid white line represents the retrieved median value of E_* , the dashed lines are its corresponding 1σ interval, and the shaded region corresponds to the parameter space excluded by the upper nightside T_b limit of 1900 K. The lower panel shows the temperature-pressure profile of a HELIOS model (solid line), computed for the median values of E_* and T_{int} . Besides the temperature-pressure profile, the lower panel also includes a set of condensate stability curves (dashed lines) for a selected set of species.

6.9. The role of ellipsoidal variation in the CHEOPS band

Our *CHEOPS* band eclipse depth estimate is very sensitive on the amplitude of the ellipsoidal variation signal, as illustrated in Fig. B.3 in Appendix B. However, the two approaches leading to physically expected EV amplitudes yield similar *CHEOPS* band eclipse depths, and only nonphysically low EV amplitudes can lead to eclipse depths that would agree with the *TESS* measurement.

7. Conclusions

We have estimated a self-consistent dayside emission spectrum of KELT-1b covering the *CHEOPS*, *TESS*, *H*, *Ks*, and *Spitzer* IRAC 3.6 and 4.5 μm passbands by modelling new *CHEOPS* secondary eclipse photometry of KELT-1b jointly with the existing ground- and space-based light curves. The study adds so-far the bluest point to KELT-1b’s emission spectrum, improves the two ground-based NIR measurements by using a phase curve model that includes a stellar ellipsoidal variation signal, and improves the *Spitzer* measurements by modelling the Beatty et al. (2017) and Beatty et al. (2019) observations jointly with all the other light curves.

The emission spectrum largely agrees with the previous studies. The *H* and *Ks* dayside flux ratios are lower than the prior estimates but this was expected since the previous modelling ignored the stellar ellipsoidal variation signal. The *TESS* and *Spitzer* 4.5 μm bands also agree with the results by Beatty et al. (2019), Beatty et al. (2020), and von Essen et al. (2021). The 3.6 μm *Spitzer* band dayside flux ratio estimate deviates both from previous results by Beatty et al. (2019) and theoretical expectations. This difference can either be due to insufficiently modelled systematics or non-equilibrium chemistry effects in the brown dwarf atmosphere, but we cannot securely determine its cause.

Another, significantly more difficult-to-explain discrepancy occurs between the *CHEOPS* and *TESS* passbands: the *TESS* observations show a deep secondary eclipse with a depth of 360 ± 60 ppm, but the *CHEOPS* observations strictly rule out an eclipse with a depth larger than 80 ppm (Fig. 6). The *CHEOPS* observations yield nearly twice higher photometric precision than the *TESS* observations, so an eclipse similar to the *TESS* band one would be easily detected.

Atmospheric models can reproduce KELT-1b’s emission spectrum fairly well in most of the passbands considered, but generally manage to fit only either the *CHEOPS* or *TESS* band well. Atmospheric modelling with HELIOS leads to a solution where KELT-1b’s geometric albedo is ≈ 0.3 in the *TESS* passband but consistent with 0 in the *CHEOPS* band. A contrast like this in the geometric albedo is difficult to explain due to the overlap between the two passbands. The models by von Essen et al. (2021) explain the *TESS* band without reflection but cannot explain the *CHEOPS* band eclipse depth (Fig. 11). Finally, the BT and DRIFT-PHOENIX models (Allard 2013; Witte et al. 2011) for isolated brown dwarfs also reproduce the observed KELT-1b emission spectrum fairly well, but have trouble reconciling the *CHEOPS* and *TESS* eclipse depths.

It is challenging to explain the discrepancy between the *CHEOPS* and *TESS* band eclipse depths. Temporal variability in cloud cover caused by the transport of transient nightside clouds to the dayside (as suggested by Beatty et al. 2020) could provide a potential explanation. High contrast features in KELT-1b’s albedo spectrum could also play a role in explaining a part of the discrepancy, and could be caused by a layer of strong optical absorber such as gaseous TiO/VO or S_2/HS residing above a silicate cloud layer (Schwartz & Cowan 2015), but are unable to explain the discrepancy fully.

All in all, instead of shedding light on which of the previously proposed theories might work best to explain KELT-1b’s atmosphere, our additional blue-optical eclipse depth measurement has introduced a new open question that is challenging to explain with our current knowledge. Further observations combined with comprehensive modelling are required to study whether KELT-1b’s dayside brightness spectrum is explained by

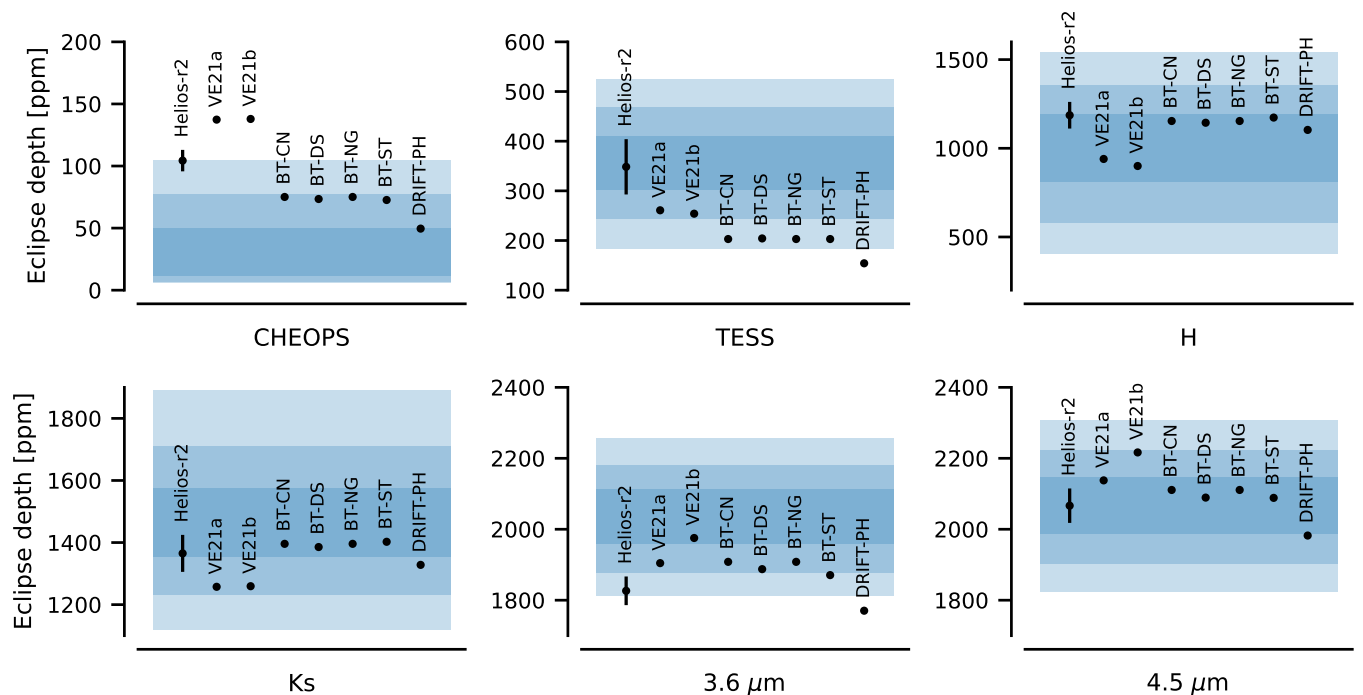


Fig. 11. Comparison between different emission spectrum models. The shaded areas show the 68%, 95%, and 99.7% central posterior intervals for the eclipse depths as estimated from the joint modelling, and the black points show the passband-integrated emission spectrum models. Helios-r2 corresponds to the model presented here, VE21a and VE21b to the models in von Essen et al. (2021), BT-CN, BT-DS, BT-NG, and BT-ST to the best-fitting BT-Cond, BT-Dusty, BT-NextGen, and BT-Settl models by Allard (2013), respectively, and DRIFT-PH to the best-fitting Drift-PHOENIX model (Witte et al. 2011).

transient silicate clouds (Beatty et al. 2020), thermal emission (von Essen et al. 2021), or something else, and how the discrepancy between the *CHEOPS* and *TESS* band eclipse depths can be explained.

Acknowledgements. We thank the anonymous referee for their insight and useful comments. We kindly thank T.G. Beatty and B. Croll for providing their observations to our use, and C. von Essen, M. Mallonn, N. Madhusudhan, and A. Piette for providing their model spectra from von Essen et al. (2021). *CHEOPS* is an ESA mission in partnership with Switzerland with important contributions to the payload and the ground segment from Austria, Belgium, France, Germany, Hungary, Italy, Portugal, Spain, Sweden, and the United Kingdom. The *CHEOPS* Consortium would like to gratefully acknowledge the support received by all the agencies, offices, universities, and industries involved. Their flexibility and willingness to explore new approaches were essential to the success of this mission. ACC and TGW acknowledge support from STFC consolidated grant numbers ST/R000824/1 and ST/V000861/1, and UKSA grant number ST/R003203/1. ML acknowledges support of the Swiss National Science Foundation under grant number PCEFP2_194576. This project has received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme (project FOUR ACES, grant agreement No 724427). It has also been carried out in the frame of the National Centre for Competence in Research PlanetS supported by the Swiss National Science Foundation (SNSF). DE acknowledges financial support from the Swiss National Science Foundation for project 200021_200726. This work was supported by FCT - Fundação para a Ciência e a Tecnologia through national funds and by FEDER through COMPETE2020 - Programa Operacional Competitividade e Internacionalização by these grants: UID/FIS/04434/2019, UIDB/04434/2020, UIDP/04434/2020, PTDC/FIS-AST/32113/2017 & POCI-01-0145-FEDER-032113, PTDC/FIS-AST/28953/2017 & POCI-01-0145-FEDER-028953, PTDC/FIS-AST/28987/2017 & POCI-01-0145-FEDER-028987, O.D.S.D. is supported in the form of work contract (DL 57/2016/CP1364/CT0004) funded by national funds through FCT. LMS gratefully acknowledges financial support from the CRT foundation under Grant No. 2018.2323 ‘Gaseous or rocky? Unveiling the nature of small worlds’. S.G.S. acknowledge support from FCT through FCT contract nr. CEECIND/00826/2018 and POPH/FSE (EC). YA and MJH acknowledge the support of the Swiss National Fund

under grant 200020_172746. We acknowledge support from the Spanish Ministry of Science and Innovation and the European Regional Development Fund through grants ESP2016-80435-C2-1-R, ESP2016-80435-C2-2-R, PGC2018-098153-B-C33, PGC2018-098153-B-C31, ESP2017-87676-C5-1-R, MDM-2017-0737 Unidad de Excelencia Maria de Maeztu-Centro de Astrobiología (INTA-CSIC), as well as the support of the Generalitat de Catalunya/CERCA programme. The MOC activities have been supported by the ESA contract No. 4000124370. S.C.C.B. acknowledges support from FCT through FCT contracts nr. IF/01312/2014/CP1215/CT0004. XB, SC, DG, MF and JL acknowledge their role as ESA-appointed *CHEOPS* science team members. ABr was supported by the SNSA. ACC acknowledges support from STFC consolidated grant numbers ST/R000824/1 and ST/V000861/1, and UKSA grant number ST/R003203/1. This project was supported by the CNES. The Belgian participation to *CHEOPS* has been supported by the Belgian Federal Science Policy Office (BELSPO) in the framework of the PRODEX Program, and by the University of Liège through an ARC grant for Concerted Research Actions financed by the Wallonia-Brussels Federation. L.D. is an F.R.S.-FNRS Postdoctoral Researcher. B.-O.D. acknowledges support from the Swiss National Science Foundation (PP00P2-190080). MF and CMP gratefully acknowledge the support of the Swedish National Space Agency (DNR 65/19, 174/18). DG gratefully acknowledges financial support from the CRT foundation under Grant No. 2018.2323 ‘Gaseous or rocky? Unveiling the nature of small worlds’. M.G. is an F.R.S.-FNRS Senior Research Associate. SH gratefully acknowledges CNES funding through the grant 837319. KGI is the ESA *CHEOPS* Project Scientist and is responsible for the ESA *CHEOPS* Guest Observers Programme. She does not participate in, or contribute to, the definition of the Guaranteed Time Programme of the *CHEOPS* mission through which observations described in this paper have been taken, nor to any aspect of target selection for the programme. This work was granted access to the HPC resources of MesoPSL financed by the Region Ile de France and the project Equip@Meso (reference ANR-10-EQPX-29-01) of the programme Investissements d’Avenir supervised by the Agence Nationale pour la Recherche. PM acknowledges support from STFC research grant number ST/M001040/1. GSc, GPi, IPa, LBo, VNa and RRa acknowledge the funding support from Italian Space Agency (ASI) regulated by ‘Accordo ASI-INAF n. 2013-016-R.0 del 9 luglio 2013 e integrazione del 9 luglio 2015 *CHEOPS* Fasi A/B/C’. This work was also partially supported by a grant from the Simons Foundation (PI Queloz, grant number 327127). IRI acknowledges support from the Spanish Ministry of Science and Innovation and the European Regional Development Fund through

grant PGC2018-098153-B-C33, as well as the support of the Generalitat de Catalunya/CERCA programme. GyMSz acknowledges the support of the Hungarian National Research, Development and Innovation Office (NKFIH) grant K-125015, a PRODEX Institute Agreement between the ELTE Eötvös Loránd University and the European Space Agency (ESA-D/SCI-LE-2021-0025), the Lendület LP2018-7/2021 grant of the Hungarian Academy of Science and the support of the city of Szombathely. V.V.G. is an F.R.S-FNRS Research Associate. NAW acknowledges UKSA grant ST/R004838/1. M.F. gratefully acknowledge the support of the Swedish National Space Agency (SNSA; DNR 177/19, 174/18, and 65/19). S.S. has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreement No 833925, project STAREX).

References

- Allard, F. 2013, *Proceedings of the International Astronomical Union*, 8, 271
- Ambikasaran, S., Foreman-Mackey, D., Greengard, L., Hogg, D. W., & O’Neil, M. 2014 [arXiv:1403.6015]
- Anderson, D. R., Temple, L. Y., Nielsen, L. D., et al. 2018, 10, 1
- Barclay, T., Huber, D., Rowe, J. F., et al. 2012, *The Astrophysical Journal*, 761, 53
- Barros, S. C., Akisanmi, B., Boué, G., et al. 2022, *Astronomy and Astrophysics*, 657, 1
- Beatty, T. G., Collins, K. A., Fortney, J., et al. 2014, *The Astrophysical Journal*, 783, 112
- Beatty, T. G., Madhusudhan, N., Pogge, R., et al. 2017, *The Astronomical Journal*, 154, 242
- Beatty, T. G., Marley, M. S., Gaudi, B. S., et al. 2019, *The Astronomical Journal*, 158, 166
- Beatty, T. G., Wong, I., Fetherolf, T., et al. 2020, *The Astronomical Journal*, 160, 211
- Bell, T. J., Zhang, M., Cubillos, P. E., et al. 2019, *Monthly Notices of the Royal Astronomical Society*, 489, 1995
- Benz, W., Broeg, C., Fortier, A., et al. 2021, *Experimental Astronomy*, 51, 109
- Blackwell, D. & Shallis, M. 1977, *MNRAS*, 180, 177
- Bloemen, S., Marsh, T. R., Østensen, R. H., et al. 2010, *Monthly Notices of the Royal Astronomical Society*, 410, no
- Bonfanti, A., Delrez, L., Hooton, M. J., et al. 2021, *Astronomy & Astrophysics*, 646, A157
- Bonfanti, A., Ortolani, S., & Nascimbeni, V. 2016, *\aap*, 585, A5
- Bonfanti, A., Ortolani, S., Piotto, G., & Nascimbeni, V. 2015, *\aap*, 575, A18
- Borsato, L., Piotto, G., Gandolfi, D., et al. 2021, *Monthly Notices of the Royal Astronomical Society*, 506, 3810
- Broeg, C., Fortier, A., Ehrenreich, D., et al. 2013, *EPJ Web of Conferences*, 47, 03005
- Burrows, A. S., Ibgui, L., & Hubeny, I. 2008, *The Astrophysical Journal*, 682, 1277
- Cameron, A. C., Guenther, E. W., Smalley, B., et al. 2010, *Monthly Notices of the Royal Astronomical Society*, 407, 507
- Carmichael, T. W., Quinn, S. N., Zhou, G., et al. 2021, *The Astronomical Journal*, 161, 97
- Castelli, F. & Kurucz, R. 2003, in *IAU Symposium*, Vol. 210, *Modelling of Stellar Atmospheres*, ed. N. Piskunov, W. Weiss, & D. Gray, A20
- Claret, A. 2017, *Astronomy & Astrophysics*, 600, A30
- Claret, A. & Bloemen, S. 2011, *Astronomy & Astrophysics*, 529, A75
- Claret, A., Cukanovaite, E., Burdge, K., et al. 2020, *Astronomy & Astrophysics*, 641, A157
- Cowan, N. B. & Agol, E. 2011, *Astrophysical Journal*, 729
- Croll, B., Albert, L., Jayawardhana, R., et al. 2015, *The Astrophysical Journal*, 802, 28
- Deline, A., Hooton, M. J., Lendl, M., et al. 2022, *Astronomy and Astrophysics*, 659, 1
- Delrez, L., Ehrenreich, D., Alibert, Y., et al. 2021, *Nature Astronomy*, 5, 775
- Delrez, L., Santerne, A., Almenara, J.-M., et al. 2016, *Monthly Notices of the Royal Astronomical Society*, 458, 4025
- Demory, B.-O., de Wit, J., Lewis, N., et al. 2013, *The Astrophysical Journal*, 776, L25
- Faigler, S. & Mazeh, T. 2011, *Monthly Notices of the Royal Astronomical Society*, 415, 3921
- Fazio, G. G., Hora, J. L., Allen, L. E., et al. 2004, *The Astrophysical Journal Supplement Series*, 154, 10
- Foreman-Mackey, D., Agol, E., Ambikasaran, S., & Angus, R. 2017, *The Astronomical Journal*, 154, 220
- Gaia Collaboration, Brown, A., Vallenari, A., et al. 2021, *\aap*, 649, A1
- Gelman, A., Carlin, J. B., Stern, H. S., et al. 2013, *Bayesian Data Analysis*, 3rd edn. (CRC Press), 1–646
- Gibson, N. P., Aigrain, S., Roberts, S., et al. 2012, *Monthly Notices of the Royal Astronomical Society*, 419, 2683
- Hooton, M. J., Hoyer, S., Kitzmann, D., et al. 2022, *Astronomy & Astrophysics*, 658, A75
- Hoyer, S., Guterman, P., Demangeon, O., et al. 2020, *Astronomy & Astrophysics*, 635, A24
- Husser, T. O., Wende-Von Berg, S., Dreizler, S., et al. 2013, *Astronomy and Astrophysics*, 553, A6
- Jackman, J. A. G., Wheatley, P. J., Bayliss, D., et al. 2019, *Monthly Notices of the Royal Astronomical Society*, 489, 5146
- Jenkins, J. M., Twicken, J. D., McCauliff, S., et al. 2016, in *Software and Cyberinfrastructure for Astronomy IV*, ed. G. Chiozzi & J. C. Guzman, Vol. 9913, 99133E
- Kipping, D. M. 2013, *Monthly Notices of the Royal Astronomical Society*, 435, 2152
- Kipping, D. M. & Spiegel, D. S. 2011, *Monthly Notices of the Royal Astronomical Society*, 417, L88
- Kitzmann, D., Heng, K., Oreshenko, M., et al. 2020, *The Astrophysical Journal*, 890, 174
- Kitzmann, D., Heng, K., Rimmer, P. B., et al. 2018, *The Astrophysical Journal*, 863, 183
- Lacedelli, G., Wilson, T. G., Malavolta, L., et al. 2022, *Monthly Notices of the Royal Astronomical Society*, 511, 4551
- Lendl, M., Csizmadia, S., Deline, A., et al. 2020, *Astronomy and Astrophysics*, 643, 1
- Lillo-Box, J., Barrado, D., Moya, A., et al. 2014, *Astronomy & Astrophysics*, 562, A109
- Lindgren, L., Bastian, U., Biermann, M., et al. 2021, *\aap*, 649, A4
- Loeb, A. & Gaudi, B. S. 2003, *The Astrophysical Journal*, 588, L117
- Lohringer, J. D., Barman, T., & Koskinen, T. 2018, *The Astrophysical Journal*, 866, 27
- Lund, M. B., Rodriguez, J. E., Zhou, G., et al. 2017, *The Astronomical Journal*, 154, 194
- Madhusudhan, N. & Burrows, A. S. 2012, *ANALYTIC MODELS FOR ALBEDOS, PHASE CURVES, AND POLARIZATION OF REFLECTED LIGHT FROM EXOPLANETS*
- Malik, M., Grosheintz, L., Mendonça, J. M., et al. 2017, *The Astronomical Journal*, 153, 56
- Malik, M., Kitzmann, D., Mendonça, J. M., et al. 2019, *The Astronomical Journal*, 157, 170
- Mandel, K. & Agol, E. 2002, *The Astrophysical Journal*, 580, L171
- Marigo, P., Girardi, L., Bressan, A., et al. 2017, *\apj*, 835, 77
- Morris, B. M., Delrez, L., Brandeker, A., et al. 2021a, *Astronomy and Astrophysics*, 653, 1
- Morris, B. M., Heng, K., Brandeker, A., Swan, A., & Lendl, M. 2021b, *Astronomy & Astrophysics*, 651, L12
- Morris, S. L. 1985, *The Astrophysical Journal*, 295, 143
- Palle, E., Luque, R., Zapatero Osorio, M. R., et al. 2021, *Astronomy & Astrophysics*, 650, A55
- Parmentier, V., Line, M. R., Bean, J. L., et al. 2018, *Astronomy & Astrophysics*, 617, A110
- Parviainen, H. 2015, *Monthly Notices of the Royal Astronomical Society*, 450, 3233
- Parviainen, H. 2018, in *Handbook of Exoplanets* (Cham: Springer International Publishing), 1–24
- Parviainen, H. 2020, *Monthly Notices of the Royal Astronomical Society*, 499, 1633
- Parviainen, H. & Aigrain, S. 2015, *Monthly Notices of the Royal Astronomical Society*, 453, 3821
- Parviainen, H. & Korth, J. 2020, *Monthly Notices of the Royal Astronomical Society* [arXiv:2009.09965]
- Parviainen, H., Palle, E., Zapatero-Osorio, M. R., et al. 2020, *Astronomy and Astrophysics*, 633, A28
- Rasmussen, C. E. & Williams, C. 2006, *Gaussian processes for machine learning* (The MIT Press)
- Ricker, G. R., Winn, J. N., Vanderspek, R., et al. 2014, *Journal of Astronomical Telescopes, Instruments, and Systems*, 1, 014003
- Roberts, S., Osborne, M., Ebdon, M., et al. 2013, *Philosophical transactions. Series A, Mathematical, physical, and engineering sciences*, 371, 20110550
- Russell, H. N. 1916, *The Astrophysical Journal*, 43, 173
- Salmon, S., Van Grootel, V., Buldgen, G., Dupret, M. A., & Eggenberger, P. 2021, *\aap*, 646, A7
- Schanche, N., Hébrard, G., Collier Cameron, A., et al. 2020, *\mnras*, 499, 428
- Schwartz, J. C. & Cowan, N. B. 2015, *Monthly Notices of the Royal Astronomical Society*, 449, 4192
- Scuflaire, R., Théado, S., Montalbán, J., et al. 2008, *\apss*, 316, 83
- Siverd, R. J., Beatty, T. G., Pepper, J., et al. 2012, *The Astrophysical Journal*, 761, 123
- Skrutskie, M., Cutri, R., Stiening, R., et al. 2006, *\aj*, 131, 1163

- Smith, J. C., Stumpe, M. C., Van Cleve, J. E., et al. 2012, Publications of the Astronomical Society of the Pacific, 124, 1000
- Stumpe, M. C., Smith, J. C., Catanzarite, J. H., et al. 2014, Publications of the Astronomical Society of the Pacific, 126, 100
- Stumpe, M. C., Smith, J. C., Van Cleve, J. E., et al. 2012, Publications of the Astronomical Society of the Pacific, 124, 985
- Sudarsky, D., Burrows, A. S., & Pinto, P. 2000, ApJ, 538, 885
- Swayne, M. I., Maxted, P. F. L., Triaud, A. H. M. J., et al. 2021, Monthly Notices of the Royal Astronomical Society, 506, 306
- Szabó, G. M., Gandolfi, D., Brandeker, A., et al. 2021, Astronomy and Astrophysics, 654, 1
- Talens, G. J. J., Justesen, A. B., Albrecht, S., et al. 2018, Astronomy & Astrophysics, 612, A57
- von Essen, C., Mallonn, M., Piette, A., et al. 2021, Astronomy & Astrophysics, 648, A71
- West, R. G., Hellier, C., Almenara, J. M., et al. 2016, Astronomy and Astrophysics, 585, 1
- Wilson, T. G., Goffo, E., Alibert, Y., et al. 2022, Monthly Notices of the Royal Astronomical Society, 511, 1043
- Witte, S., Helling, C., Barman, T., Heidrich, N., & Hauschildt, P. H. 2011, Astronomy & Astrophysics, 529, A44
- Wright, E. L., Eisenhardt, P. R., Mainzer, A. K., et al. 2010, \aj, 140, 1868
- Space Research and Technology Centre (ESTEC), Keplerlaan 1, 2201-AZ Noordwijk, The Netherlands
- Centre for Mathematical Sciences, Lund University, Box 118, 221 00 Lund, Sweden
- Astrobiology Research Unit, Université de Liège, Allée du 6 Août 19C, B-4000 Liège, Belgium
- Space sciences, Technologies and Astrophysics Research (STAR) Institute, Université de Liège, Allée du 6 Août 19C, 4000 Liège, Belgium
- INAF, Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, 35122 Padova, Italy
- Leiden Observatory, University of Leiden, PO Box 9513, 2300 RA Leiden, The Netherlands
- Department of Space, Earth and Environment, Chalmers University of Technology, Onsala Space Observatory, 439 92 Onsala, Sweden
- University of Vienna, Department of Astrophysics, Türkenschanzstrasse 17, 1180 Vienna, Austria
- Konkoly Observatory, Research Centre for Astronomy and Earth Sciences, 1121 Budapest, Konkoly Thege Miklós út 15-17, Hungary
- ELTE Eötvös Loránd University, Institute of Physics, Pázmány Péter sétány 1/A, 1117
- Institute of Optical Sensor Systems, German Aerospace Center (DLR), Rutherfordstrasse 2, 12489 Berlin, Germany
- IMCCE, UMR8028 CNRS, Observatoire de Paris, PSL Univ., Sorbonne Univ., 77 av. Denfert-Rochereau, 75014 Paris, France
- Institut d'astrophysique de Paris, UMR7095, CNRS, Sorbonne Université, 98bis blvd. Arago, 75014 Paris, France
- Astrophysics Group, Keele University, Staffordshire, ST5 5BG, United Kingdom
- Department of Astrophysics, University of Vienna, Tuerkenschanzstrasse 17, 1180 Vienna, Austria
- Dipartimento di Fisica e Astronomia "Galileo Galilei", Università degli Studi di Padova, Vicolo dell'Osservatorio 3, 35122 Padova, Italy
- ETH Zurich, Department of Physics, Wolfgang-Pauli-Strasse 2, CH-8093 Zurich, Switzerland
- Cavendish Laboratory, JJ Thomson Avenue, Cambridge CB3 0HE, UK
- ESTEC, European Space Agency, 2201AZ, Noordwijk, NL
- Zentrum für Astronomie und Astrophysik, Technische Universität Berlin, Hardenbergstr. 36, D-10623 Berlin, Germany
- Institut für Geologische Wissenschaften, Freie Universität Berlin, 12249 Berlin, Germany
- ELTE Eötvös Loránd University, Gothard Astrophysical Observatory, 9700 Szombathely, Szent Imre h. u. 112, Hungary
- MTA-ELTE Exoplanet Research Group, 9700 Szombathely, Szent Imre h. u. 112, Hungary
- Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge, CB3 0HA, United Kingdom
-
- ¹ Instituto de Astrofísica de Canarias (IAC), E-38200 La Laguna, Tenerife, Spain
- ² Departamento de Astrofísica, Universidad de La Laguna (ULL), E-38206 La Laguna, Tenerife, Spain
- ³ Centre for Exoplanet Science, SUPA School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews KY16 9SS, UK
- ⁴ Observatoire Astronomique de l'Université de Genève, Chemin Pégasi 51, Versoix, Switzerland
- ⁵ Center for Space and Habitability, University of Bern, Gesellschaftsstrasse 6, 3012 Bern, Switzerland
- ⁶ Dipartimento di Fisica, Università degli Studi di Torino, via Pietro Giuria 1, I-10125, Torino, Italy
- ⁷ Physikalisches Institut, University of Bern, Sidlerstrasse 5, 3012 Bern, Switzerland
- ⁸ Aix Marseille Univ, CNRS, CNES, LAM, 38 rue Frédéric Joliot-Curie, 13388 Marseille, France
- ⁹ Division Technique INSU, CS20330, 83507 La Seyne sur Mer cedex, France
- ¹⁰ Department of Physics, University of Warwick, Gibbet Hill Road, Coventry CV4 7AL, United Kingdom
- ¹¹ Instituto de Astrofísica e Ciências do Espaço, Universidade do Porto, CAUP, Rua das Estrelas, 4150-762 Porto, Portugal
- ¹² Departamento de Física e Astronomia, Faculdade de Ciências, Universidade do Porto, Rua do Campo Alegre, 4169-007 Porto, Portugal
- ¹³ Space Research Institute, Austrian Academy of Sciences, Schmiedlstrasse 6, A-8042 Graz, Austria
- ¹⁴ INAF, Osservatorio Astrofisico di Catania, Via S. Sofia 78, 95123 Catania, Italy
- ¹⁵ Institut de Ciències de l'Espai (ICE, CSIC), Campus UAB, Can Magrans s/n, 08193 Bellaterra, Spain
- ¹⁶ Institut d'Estudis Espacials de Catalunya (IEEC), 08034 Barcelona, Spain
- ¹⁷ Admatis, 5. Kandó Kálmán Street, 3534 Miskolc, Hungary
- ¹⁸ Depto. de Astrofísica, Centro de Astrobiología (CSIC-INTA), ESAC campus, 28692 Villanueva de la Cañada (Madrid), Spain
- ¹⁹ Université Grenoble Alpes, CNRS, IPAG, 38000 Grenoble, France
- ²⁰ Department of Astronomy, Stockholm University, AlbaNova University Center, 10691 Stockholm, Sweden
- ²¹ Institute of Planetary Research, German Aerospace Center (DLR), Rutherfordstrasse 2, 12489 Berlin, Germany
- ²² Université de Paris, Institut de physique du globe de Paris, CNRS, F-75005 Paris, France
- ²³ Science and Operations Department - Science Division (SCI-SC), Directorate of Science, European Space Agency (ESA), European

Appendix A: Chromatic albedo variability

Appendix A.1: Albedo spectrum model

We use a simple two-level albedo spectrum model to study whether the discrepancy between the *CHEOPS* and *TESS* band dayside flux ratios could be caused by chromatic variability in albedo. The model is parametrised by two geometric albedo levels, $A_{g,0}$ (blue) and $A_{g,1}$ (red), and a step location λ_0 , so that

$$A_g(\lambda) = \begin{cases} A_{g,0} & \text{if } \lambda < \lambda_0 \\ A_{g,1} & \text{if } \lambda \geq \lambda_0 \end{cases}, \quad (\text{A.1})$$

as illustrated in the middle panel of Fig. A.1.

Our main quantity of interest is the contrast between the reflected light in the *CHEOPS* and *TESS* bands,


$$C = \frac{F_T - F_C}{F_T + F_C}, \quad \text{where } F = \int S(\lambda) A_g(\lambda) T(\lambda) d\lambda, \quad (\text{A.2})$$

S is the stellar spectrum (a BT-Settl spectrum by Allard 2013), A_g is the albedo spectrum model, and T is the transmission function for either *TESS* (F_T) or *CHEOPS* (F_C).

We assume $A_{g,1}$ that matches the geometric albedo for a "roaster" planet with silicate clouds from Sudarsky et al. (2000), compute C for a set of $A_{g,0}$ values between 0.01 (similar to TrES-2b, Kipping & Spiegel 2011) and 0.05, and λ_0 values between 400 and 1000 nm and show the results in the lower panel of Fig. A.1. The maximum C is achieved for $\lambda_0 \sim 800$ nm and varies from 0.17 to 0.41. We obtain $C = 0.41$ for the lowest included blue A_g (as expected), $A_{g,0} = 0.01$, and C decreases quickly with increasing $A_{g,0}$.

Appendix A.2: Comparison between modelled and observed reflection ratio

Before we can compare our theoretical C values to the C distribution from the light curve analysis, we need to estimate and remove the contribution from thermal emission in the latter. This contribution should be small for the *CHEOPS* and *TESS* bands, but is not necessarily negligible.

We calculate a set of "reflection only" flux ratio samples from the original dayside flux ratio samples using a Monte Carlo approach. We draw a set of KELT-1b temperatures from a uniform distribution from 2800 to 3200 K (corresponding to the KELT-1b *Spitzer* 4.5 μm T_b ranges given in Table 4), we calculate the emission contribution in the *CHEOPS* and *TESS* bands using BT-Settl model spectra by Allard (2013) for each temperature sample, and finally we remove these contributions from a random sample of *CHEOPS* and *TESS* dayside flux ratios. The full process is carried out in the [chromatic albedo variation test notebook](#) . Figure A.2 shows the original dayside flux ratios with emission and reflection, and the "reflection-only" flux ratios. The correction is rather small for the *CHEOPS* band, but significant for the *TESS* band. The bottom panel of Fig. A.2 shows the final observed R distribution.

Our maximum C of 0.41 is at the lower tail of the observed C distribution. The maximum C corresponds to a low but still physically realistic red A_g of 0.01, which is similar to what has been measured for TrES-2b (Kipping & Spiegel 2011). However, while both $A_{g,0}$ and $A_{g,1}$ are physically plausible separately, it is unclear if this is the case for an albedo spectrum combining the two.

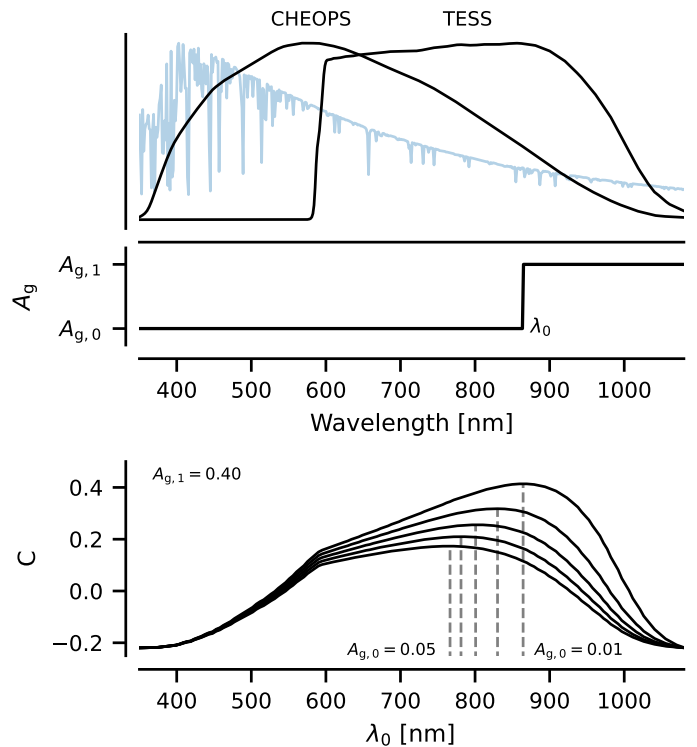


Fig. A.1. Top: a model spectrum of KELT-1 (light blue line), the *CHEOPS* and *TESS* passband transmission functions (black lines). Middle: the step-function albedo spectrum model. Bottom: *TESS* to *CHEOPS* reflected light contrast as a function of $A_{g,0}$ and λ_0 . The step locations corresponding to the maximum flux ratios are marked as dashed vertical lines.

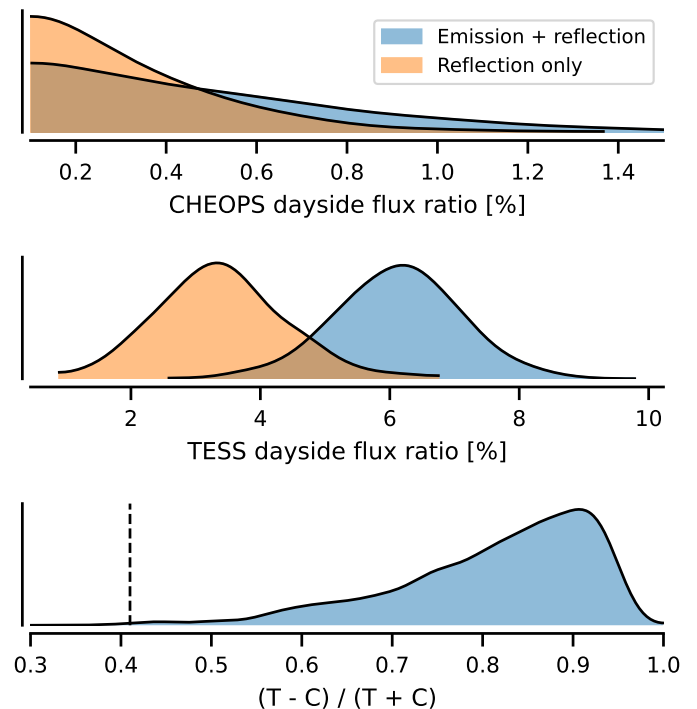


Fig. A.2. Top and middle: original *CHEOPS* and *TESS* dayside flux ratio distribution estimates together with versions of the distributions with the thermal emission removed as described in Appendix A.2. Bottom: the final *TESS* to *CHEOPS* contrast (C) distribution and the maximum C of ≈ 0.4 from the albedo spectrum modelling marked with a dashed vertical line.

Appendix B: Comparison between EV scenarios

In addition to the final joint analysis, we carried out a set of analyses for the external dataset (ED) consisting of the *TESS*, *H*, *Ks*, and *Spitzer* photometry, and another set of analyses for the *CHEOPS* photometry alone. The ED analysis was carried out to provide priors on the orbital and geometric parameters for the *CHEOPS* analysis and to study how different approaches to constrain the EV amplitudes affect our parameter estimates. The *CHEOPS* analysis was carried out to also study how the EV amplitude constraints affect the eclipse depth estimate, and to provide detrended *CHEOPS* light curves for the final joint analysis.

Both the ED and *CHEOPS*-only analyses consider three scenarios that differ in the priors set on the EV amplitude:

- Theoretical EV*: the EV amplitudes are given normal priors based on theoretical estimates in Table 3. This is the most constraining scenario, but can lead to biased eclipse depth estimates if the semi-major axis estimate used to calculate the amplitudes is biased.
- Constrained EV ratios*: the EV amplitudes are constrained relative to the EV amplitude in the *TESS* passband and the *TESS* passband EV amplitude is given a uninformative prior. This scenario works as a stepping stone between the strongly constrained and completely unconstrained EV cases, and is not sensitive to our prior semi-major axis estimate.
- Unconstrained EV*: all the EV amplitudes are given uninformative priors to see whether the EV amplitudes from the *TESS* and *Spitzer* passbands (where we have coverage over the full orbital phase) agree with the theoretical expectations.

The *CHEOPS*-only analysis considers also an additional scenario with EV amplitude forced to zero:

- No EV*: the EV amplitude is forced to zero. The motivation for this scenario is to see how ignoring EV would affect our *CHEOPS* eclipse depth estimate.

Except for the data included, the models are identical to the full joint model. The baseline and noise models for the ED analyses are the same as in the final analysis. However, the baseline in the *CHEOPS*-only analysis is modelled differently than in the final analysis. In the *CHEOPS* analysis, we use the basis vectors determined by the pipeline by Wilson et al. as covariates and each visit is given its own set of baseline coefficients. The number of basis vectors per visit varies from 13 to 29, and the total number of basis vectors (and thus free parameters from the baseline model) is 156. This approach allows us to detrend the *CHEOPS* light curves together with the phase curve model to be used in the final joint analysis (this is safe and does not affect the final parameter estimates). The *CHEOPS* analysis uses the posteriors from the external dataset analysis as priors for the zero epoch, orbital period, stellar density, impact parameter, and planet-star area ratio.

We show the EV amplitude posteriors for all the analyses in Fig. B.1, the dayside flux ratio posteriors in Fig. B.2, and the *CHEOPS* dayside posteriors in Fig. B.3. All in all, the dayside flux ratio posteriors all agree with each other for the final joint modelling and EV prior scenarios a and b. The flux ratio posteriors also agree for scenario d for passbands with photometry covering a full orbital phase, but the free- and no-EV scenarios (c and d) lead to overestimated flux ratios for *CHEOPS* photometry.

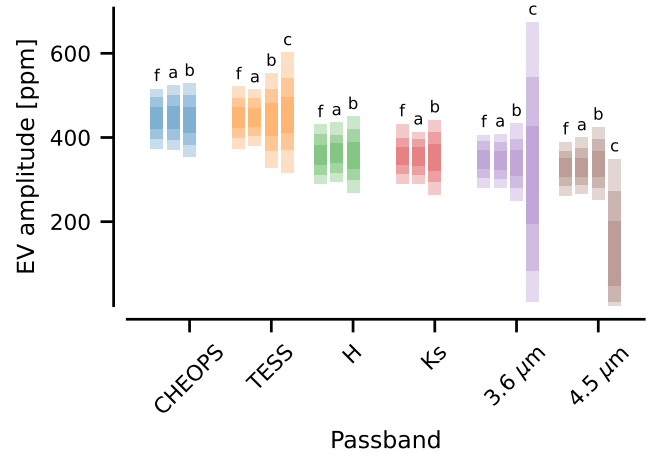


Fig. B.1. Ellipsoidal variation amplitude posteriors for f) final joint analysis with relative prior on the EV amplitude, a) theoretical prior on EV amplitude, b) relative prior on EV amplitude, and c) uninformative prior on EV amplitude. The case c with an uninformative prior on EV is shown only for the *TESS* and *Spitzer* passbands with full phase coverage.

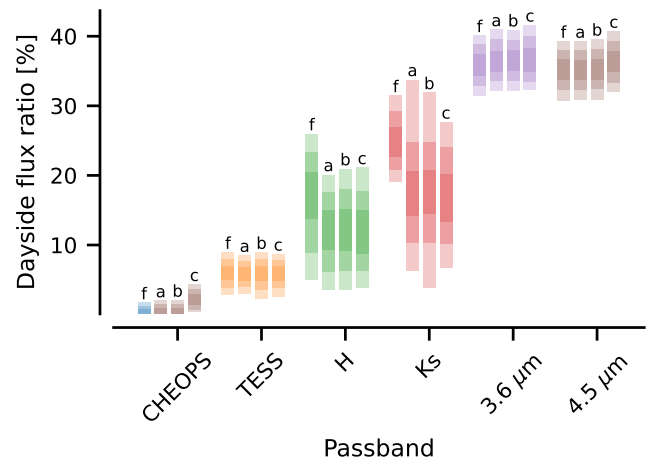


Fig. B.2. As in Fig. B.1, but for the dayside flux ratio.

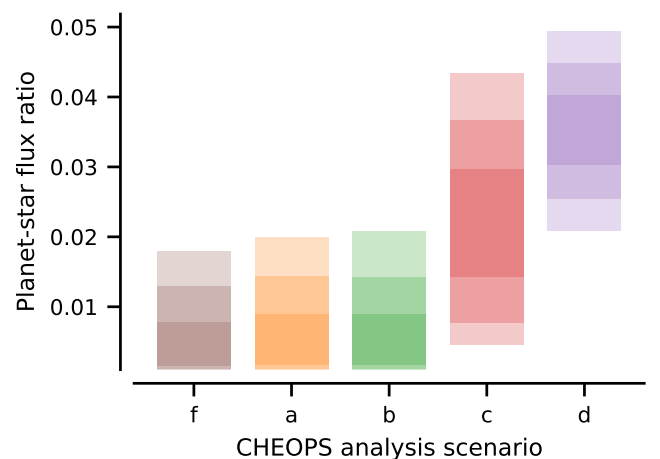


Fig. B.3. Dayside flux ratios the *CHEOPS*-only analysis scenarios. The scenario labels are the same as in Fig. B.1 with an additional no-EV scenario d.

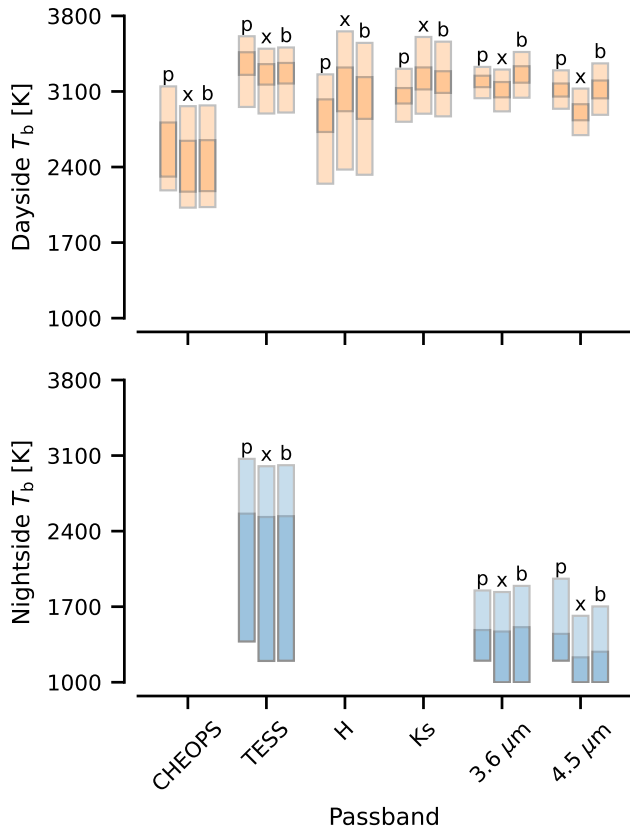


Fig. C.1. Day- and nightside brightness temperatures estimated from the flux ratios using the p) physical-physical, x) blackbody-physical, and b) blackbody-blackbody approaches. The shading marks the 68% and 99.7% central posterior intervals.

Appendix C: Comparison between brightness temperature calculation approaches

We calculate the brightness temperatures discussed in Sect. 6.2 using three approaches: physical-physical, where both the star and the brown dwarf are modelled using the BT-Settl spectra by Allard (2013); blackbody-physical, where KELT-1b is modelled as a black body and its host star using a BT-Settl spectrum; and blackbody-blackbody, where both the brown dwarf and its host star are modelled as black bodies. Our reported brightness temperature values correspond to averages over the three approaches, but we also tested whether the different approaches agree with each other or not.

We present the day- and nightside brightness temperatures separately for each approach in Fig. C.1. All the three approaches agree with each other within uncertainties.

Appendix D: Additional retrievals to explore dependence of outcomes on data

Figure D.1 shows the degeneracy between T_{int} and E_* when the model accounts for the *TESS* secondary eclipse. Within this family of solutions, the solution of von Essen et al. (2021), which explains the dayside emission spectrum without the need for reflected light, is included.

In Fig. D.2, we perform a retrieval with just the *TESS*, *Spitzer* 3.6 μm and 4.5 μm data points reported by Beatty et al. (2019). The left panel of D.2 shows a retrieval with the full prior

ranges. This yields a bimodal solution for T_{int} and E_* : a high value of E_* and a low value of T_{int} , or a low value of E_* and a high value of T_{int} . The two different solutions are isolated in the other two panels of Fig. D.2.

When the *H* and *Ks* data points are added to the retrieval, the bimodality is broken (not shown). This can be understood by looking at the ranges of T_{int} and E_* values that are consistent with the measurements in this passbands depicted in D.1. The results presented in this figure suggest that the *H* and *Ks* secondary eclipse measurements are only consistent with high values of T_{int} .

Finally, in Fig. D.3 we perform a retrieval using all available measurements but with the *Spitzer* secondary eclipse depths from Beatty et al. (2019). The addition of the *CHEOPS* data point now further narrows the posterior on E_* down to a median value of 0.2. this behaviour can also be easily understood by comparison with the theoretically calculated eclipse depths in Fig. D.1. For *CHEOPS*, the results indicate that the measured eclipse depth is only compatible with a maximum E_* of about 0.2.

We also note that the results using the *Spitzer* data from Beatty et al. (2019) essentially provides the same posterior distribution than using the reduction of the *Spitzer* of this work (see Fig. 8). . In particular, the very high geometric albedo in the *TESS* passband is consistently obtained with either dataset. Despite the difference in the reported *Spitzer* 3.6 μm eclipse depth, the retrieval outcome is, thus, unaffected because the solution with $T_{\text{int}} \approx 2700$ K has a blackbody peak at shorter wavelengths, within the *H* and *Ks* passbands.

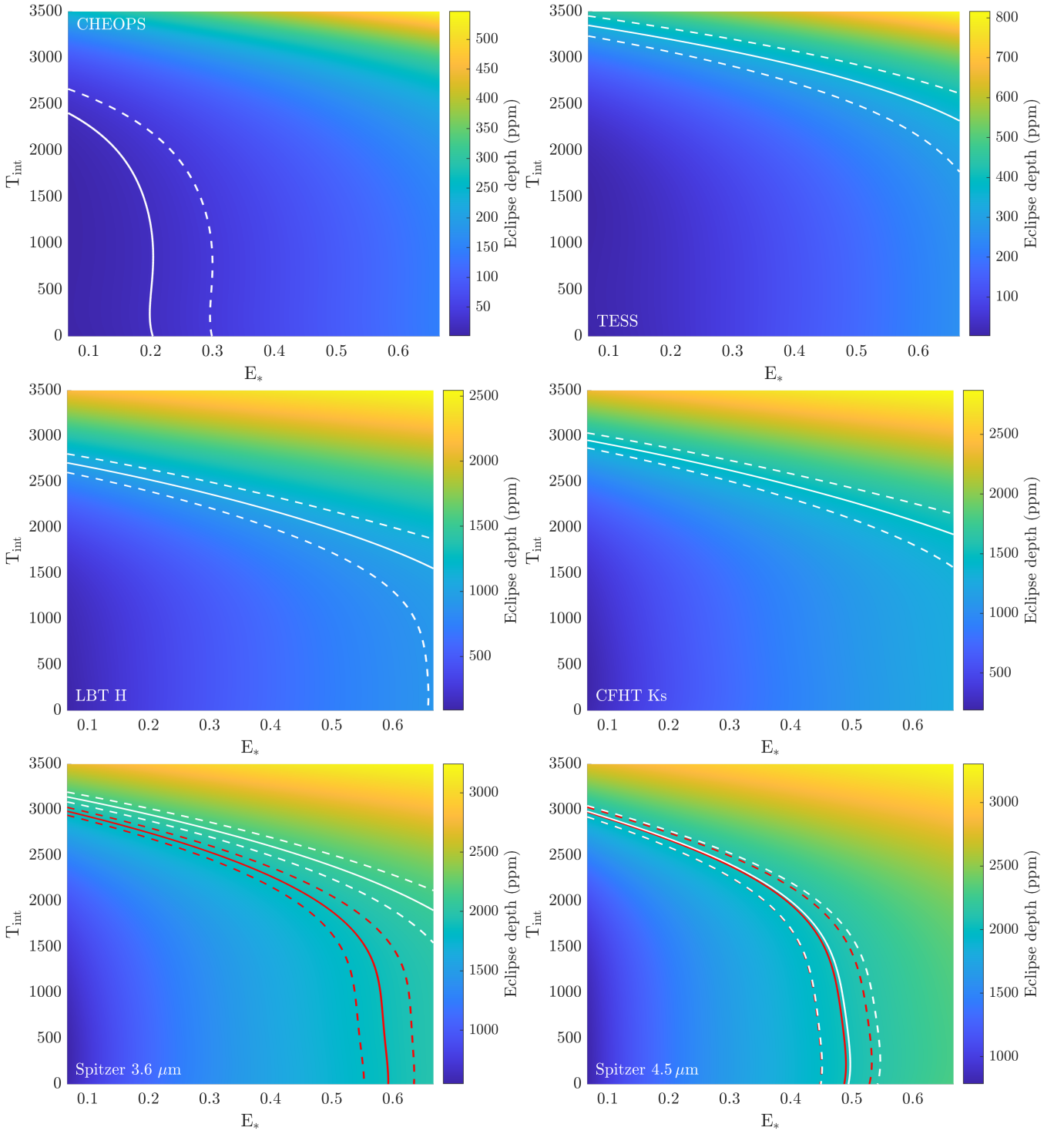


Fig. D.1. Eclipse depths in ppm as a function of the internal temperature T_{int} and the parameter E_* based on the HELIOS model calculations described in Sect. 6.4. The six panels show the eclipse depths in the various passbands. White, solid lines depict the measured occultation depths from Table 4, dashed lines refer to their 1σ error bars. The red lines for the two Spitzer passbands refer to the eclipse depths reported by Beatty et al. (2019).

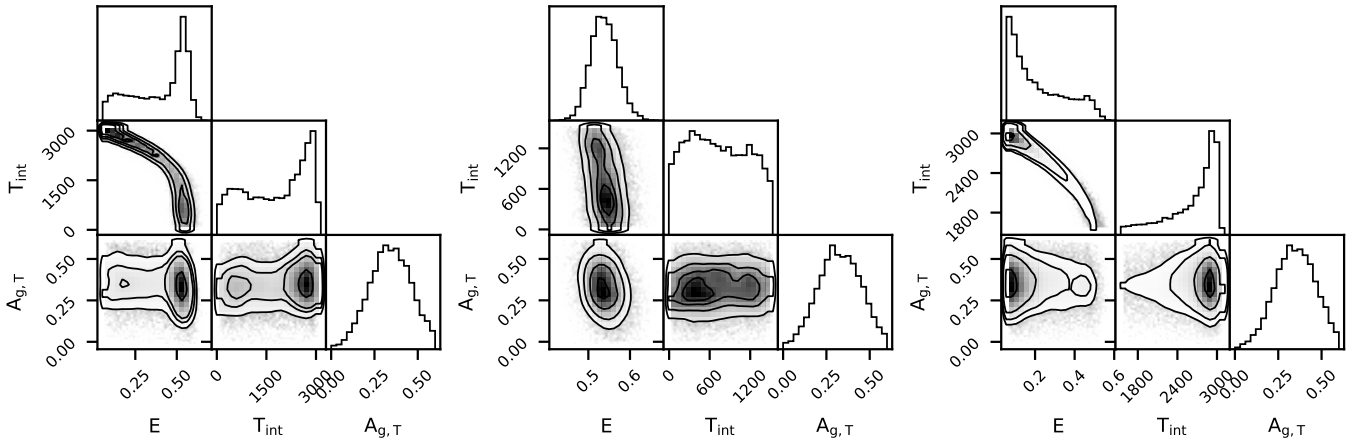


Fig. D.2. Posterior distributions for a retrieval with *Helios-r2* using only the *TESS* secondary eclipse measurement and the two *Spitzer* points from [Beatty et al. \(2019\)](#). The left panel shows the results for the full range of prior distributions discussed in Sect. 6.4, which yields a bimodal solution with respect to T_{int} and the parameter E_* . The two other panels isolate the two solution modes.

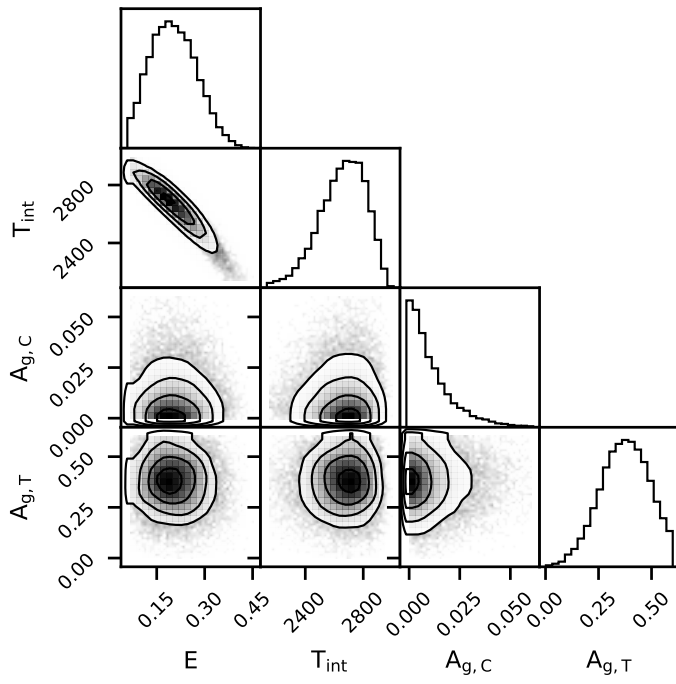


Fig. D.3. Posterior distributions for a retrieval with *Helios-r2* using all secondary eclipse measurement from Table 4 but with the two *Spitzer* points from [Beatty et al. \(2019\)](#).