

STEADY FLOW OF SOME NON-NEWTONIAN FLUIDS THROUGH A
POROUS MEDIUM BY USING ADOMIAN DECOMPOSITION METHOD

FAWZIA MANSOUR ELNIEL DALAM

UNIVERSITI TEKNOLOGI MALAYSIA

STEADY FLOW OF SOME NON-NEWTONIAN FLUIDS THROUGH A
POROUS MEDIUM BY USING ADOMIAN DECOMPOSITION METHOD

FAWZIA MANSOUR ELNIEL DALAM

A thesis submitted in fulfilment of the
requirements for the award of the degree of
Doctor of Philosophy (Mathematics)

Faculty of Science
Universiti Teknologi Malaysia

APRIL 2022

DEDICATION

This thesis is dedicated to my father, who could not see the end of this thesis. I am thankful to Allah that you have been my father, I have been so blessed with your love, and I have overcome the pains, and I wish if you are here because the journey is coming to an end. I will always remember you, and I will forever learn from your wisdom. My Duaa is going to you forever; my thesis is also dedicated to my family, husband, beloved children, and dearest friend, Shaymaa, who gave me unconditional support.

ACKNOWLEDGEMENT

First of all, I thank Allah SWT for blessing me with the opportunity, protection, and ability to complete my Ph.D thesis. My thanks to those who have assisted me and contribute to my ideas and broaden my knowledge. I would particularly like to express my sincere appreciation and gratitude to my thesis supervisors, Professor Dr. Zainal Abdul Aziz and Associate Professor Dr. Arifah Bahar, for their encouragement, guidance, critical review and kind supervision. Without their continued support and interest, this research would not have been completed or presented here.

My gratitude also goes to all my colleagues and friends who have helped make this research possible. I am thankful to all my family members, and I extend the utmost appreciation to my mother, brothers, and sisters. My thesis would never have been completed without those who have continued to provide essential knowledge, information, support, and encouragement to achieve my goals. My profound thanks to them all.

ABSTRACT

Non-Newtonian fluids are employed in a wide range of industrial applications. Non-Newtonian fluids that shows characteristics of both elastic and viscous fluids as a result of shear stress, are referred to as viscoelastic fluids. Constitutive equations of the viscoelastic fluids, flow patterns and viscous response are important challenges that need to be considered when modelling the flow in a porous medium. The predominant idea of this thesis is to find the analytical solutions of viscoelastic fluid in a porous medium. The primary goal of this research is to create a one-dimensional simulation for three different kinds of viscoelastic fluids, namely, Johnson-Segalman, Powell-Eyring, and Sisko fluids, in a porous medium. Further, Darcy's law is selected for simulating permeable media saturated by viscoelastic fluid. The effect of external magnetic field is an additional feature to the innovation of the constructed mathematical models. The system of nonlinear coupled partial differential equations supported by related boundary conditions are solved analytically by using the Adomian decomposition method (ADM). In the analysis, the impact of various physical parameters on velocity and temperature are scrutinized and the results are exhibited graphically. The wall shear stress versus governing constraints are also evaluated, and their results are summarised in the form of tables and graphs. The results demonstrated that for both isothermal and non-isothermal circumstances, the inclination angle causes a variation in shear stress. It is also observed that the viscosity and shear stress have a direct connection in the absence of a heating effect. Moreover, the viscosity of the non-isothermal state is sensitive to temperature variations for both lift and drainage problems. The findings validated the efficacy of the suggested technique, and the solutions are successfully approximated to the exact solutions.

ABSTRAK

Bendalir bukan Newton digunakan dalam pelbagai aplikasi perindustrian. Bendalir bukan Newton yang menunjukkan ciri-ciri bendalir elastik dan likat akibat tegasan ricih dirujuk sebagai bendalir viskoelastik. Persamaan konstitutif bagi bendalir viskoelastik, corak aliran dan gerak balas likat merupakan cabaran penting yang perlu dipertimbangkan semasa memodelkan aliran dalam medium berliang. Idea utama tesis ini ialah untuk mencari penyelesaian analisis bendalir viskoelastik dalam medium berliang. Matlamat utama penyelidikan ini ialah untuk mencipta simulasi satu dimensi untuk tiga jenis bendalir viskoelastik yang berbeza, iaitu bendalir Johnson-Segalman, Powell-Eyring, dan Sisko dalam medium berliang. Selanjutnya, hukum Darcy dipilih untuk mensimulasikan media berliang yang tepu oleh bendalir viskoelastik. Kesan medan magnet luaran merupakan ciri tambahan kepada inovasi model matematik yang dibina. Sistem tak linear yang digandingkan dengan persamaan pembezaan separa disokong oleh syarat sempadan yang berkaitan diselesaikan secara analitik dengan menggunakan kaedah penguraian Adomian (ADM). Dalam analisis ini, kesan pelbagai parameter fizikal terhadap halaju dan suhu diteliti dan hasilnya ditunjukkan secara grafik. Kuantiti fizikal tegasan ricih dinding dan pekali pemindahan haba berbanding kekangan yang mengawal juga dinilai, dan keputusannya diringkaskan dalam bentuk jadual dan graf. Keputusan menunjukkan bagi kedua-dua keadaan isoterma dan bukan isoterma, sudut kecondongan magnet menyebabkan kepelbagaian dalam tegasan ricih. Diperhatikan juga bahawa kelikatan dan tegasan ricih mempunyai sambungan langsung ketika tiada kesan pemanasan. Selain itu, kelikatan keadaan bukan isoterma adalah sensitif kepada suhu yang berubah-ubah untuk kedua-dua masalah angkat dan saluran. Dapatan mengesahkan keberkesanan teknik yang dicadangkan, dan penyelesaian berjaya dilakukan dengan anggaran yang lebih hampir dengan penyelesaian yang tepat.

TABLE OF CONTENTS

	TITLE	PAGE
	DECLARATION	i
	DEDICATION	ii
	ACKNOWLEDGEMENT	iii
	ABSTRACT	iv
	ABSTRAK	v
	TABLE OF CONTENTS	vi
	LIST OF TABLES	x
	LIST OF FIGURES	xi
	LIST OF ABBREVIATIONS	xiv
	LIST OF SYMBOLS	xv
	LIST OF APPENDICES	xvii
CHAPTER 1	INTRODUCTION	1
	1.1 Overview	1
	1.2 Research Background	2
	1.3 Problem Statement	4
	1.4 Research Questions	5
	1.5 Research Objectives	6
	1.6 Research Scope	6
	1.7 Significance of the Study	7
	1.8 Thesis Outline	8
CHAPTER 2	LITERATURE REVIEW	11
	2.1 Introduction	11
	2.1.1 Viscoelastic Fluid	13
	2.1.2 Magnetohydrodynamics (MHD) Flow	15
	2.1.3 Flow in a Porous Medium	16

2.2	On a few Methods for Solving the Nonlinear Equations	19
2.3	Adomian Decomposition Method (ADM)	22
2.3.1	Preliminary Studies used ADM	25
2.4	Steady Flow of Johnson-Segalman Fluid in a Porous Medium	26
2.5	Steady Flow of MHD Powell-Eyring Fluid over an Inclined Plate in A Porous Medium	35
2.6	Temperature Dependent Viscosity of MHD Sisko Fluid in a Porous Channel	38
2.7	Research Gap	40
CHAPTER 3	RESEARCH METHODOLOGY	43
3.1	Introduction	43
3.2	Formulation of the Problem	47
3.3	Description of ADM	56
3.4	Calculation of Adomian Polynomial	59
3.5	Alternative Formula for Calculating Adomian Polynomial	61
3.6	The Convergence of the ADM	62
3.7	Application of the ADM	66
3.8	Advantages of the ADM	66
CHAPTER 4	STEADY FLOW OF JOHNSON-SEGALMAN FLUID IN POROUS MEDIUM OVER AN INCLINED PLATE	69
4.1	Introduction	69
4.2	Lifting Flow of the Johnson-Segalman Fluid	70
4.2.1	Description of the Problem	70
4.2.2	Formulation of the problem	72
4.2.3	Application of the ADM to the Lifting Problem	77
4.2.4	Results and Discussion	83
4.2.4.1	Effects of Material Parameters on Shear Stress	83

	4.2.4.2	Effects of Material Parameters on the Velocity Profile	86
4.3		Drainage Flow of Johnson-Segalman Fluid	91
	4.3.1	The Solution to the Drainage Problem	94
	4.3.2	Results and Discussion	96
4.4		Summary of the Chapter	103
CHAPTER 5		STEADY FLOW OF MAGNETOHYDRODYNAMIC (MHD) POWELL-EYRING FLUID OVER AN INCLINED PLATE IN A POROUS MEDIUM	105
5.1		Introduction	105
5.2		Formulation and Description of the Lift Problem	106
	5.2.1	Non-dimensional Governing Equations	108
	5.2.2	Application of the ADM to the Lifting Problem	109
	5.2.3	Results and Discussion	113
5.3		Drainage Flow of Powell-Eyring Fluid	119
	5.3.1	Results and Discussion	121
5.4		Summary of the Chapter	126
CHAPTER 6		INFLUENCE OF TEMPERATURE DEPENDENT VISCOSITY ON THE MHD SIKO FLUID FLOW BETWEEN TWO VERTICAL BELTS IN A POROUS MEDIUM	127
6.1		Introduction	127
6.2		Formulation and Description of the Lift Problem	128
	6.2.1	Governing Equation	130
	6.2.1.1	Non-dimensional Governing Equations	135
	6.2.2	The Solution to the Lifting Problem by using ADM	136
	6.2.2.1	Shear stress on the Belt	142
	6.2.3	Results and Discussion	143
6.3		Drainage Problem for MHD Sisko Fluid	152
	6.3.1	Governing Equation	152

6.3.2	The Solution to the Drainage Problem by using ADM	154
6.3.2.1	Shear Stress on the Belt	155
6.3.3	Results and Discussion	156
6.4	Summary of the chapter	166
CHAPTER 7	CONCLUSION	169
7.1	Introduction	169
7.2	Summary of the Research	169
7.3	Suggestion for Future Work	172
	REFERENCES	175
	LIST OF PUBLICATIONS	199

LIST OF TABLES

TABLE NO.	TITLE	PAGE
Table 2.1	Comparison between the analytical and the numerical methods and solutions	20
Table 2.2	Example of the advantages and disadvantages of some methods	21
Table 2.3	Comparison between the analytical and the numerical solutions	31
Table 4.1	Comparison of the numerical value of the velocity $u(x)$ in a porous and nonporous surface for the lifting case	91
Table 4.2	Comparison of the numerical value of $u(x)$ in the porous and nonporous surface for the drainage case	102
Table 5.1	Comparing the numerical value of the velocity $u(x)$ to the previous study using a successive linearization method (SLM) for the lifting case	114
Table 5.2	The effect of the inclination on $u(x)$ the drainage case	122
Table 6.1	The different values of the velocity $u(x)$ for the various value of x when $\xi_2 = 0.6, Gr = 0.6, Br = 0.1, \alpha = 1$.	151
Table 6.2	Velocity distribution of thin-film flow of Sisko fluid when fixed $Gr=1, \alpha=0.1, Br=10, \gamma=1$.	165
Table 6.3	Shear thickening fluid (Drainage) when $Gr=0.45, \xi_2=0.2, n=1.5, \gamma=1.2$.	166

LIST OF FIGURES

FIGURE NO.	TITLE	PAGE
Figure 2.1	Classification of fluids	12
Figure 2.2	Relation between shear stress and deformation rate	13
Figure 3.1	Research methodology framework	46
Figure 4.1	Schematic of the lift flow problem	71
Figure 4.2	Shear stress versus velocity	85
Figure 4.3	Effect of the Weissenberg number on the velocity profile	86
Figure 4.4	Effect of the ratio of viscosity on the velocity profile	87
Figure 4.5	Effect of the slip parameter on the velocity profile	87
Figure 4.6	Effect of the Stokes number on the velocity profile	88
Figure 4.7	Effect of the material parameter on the velocity profile	89
Figure 4.8	Effect of the inclination on the velocity profile	90
Figure 4.9	Physical diagram of the drainage problem	93
Figure 4.10	Shear stress versus drainage velocity	96
Figure 4.11	Shear stress versus drainage velocity	97
Figure 4.12	Effect of the Weissenberg number on the drainage velocity profile	97
Figure 4.13	Effect of the ratio of viscosity on the drainage velocity profile	98
Figure 4.14	Effect of the slip parameter on the drainage velocity profile	99
Figure 4.15	Effect of the Stokes number on the drainage velocity profile	100
Figure 4.16	Effect of the porous term parameter on the drainage velocity profile	100
Figure 4.17	Effect of the inclination on the drainage velocity profile	101
Figure 5.1	A schematic diagram of the lifting flow of Powell-Eyring over an inclined plate in a porous medium	106
Figure 5.2	The effect of the shear stress on the plate	115

Figure 5.3	The effect of the Stokes number on the lift velocity	116
Figure 5.4	The effect of the parameter M on the lift velocity	116
Figure 5.5	The effect of the parameter M on the lift velocity	117
Figure 5.6	The effect of the material parameter on the lift velocity	118
Figure 5.7	The influence of non-Newtonian parameter β on the lift velocity	118
Figure 5.8	The effect of the permeability on the lift velocity	119
Figure 5.9	The effect of the Stokes number on the drainage velocity	123
Figure 5.10	The effect of the magnetic parameter M on the drainage velocity	123
Figure 5.11	The effect of the parameter β on the drainage velocity	124
Figure 5.12	The effect of the parameter ξ on the drainage velocity	125
Figure 5.13	The effect of the parameter β on the fluid shear stress	125
Figure 6.1	Geometry of the lift problem	129
Figure 6.2	The influence of the non-Newtonian parameter on the shear stress	144
Figure 6.3	The influence of Grashof number on the lift velocity profile	144
Figure 6.4	The influence of Brinkman number on the lift temperature distribution	145
Figure 6.5	The influence of variable viscosity parameter on the lift velocity profile	146
Figure 6.6	The influence of variable viscosity parameter on the temperature distribution	147
Figure 6.7	The influence of the non-Newtonian parameter on the temperature distribution	147
Figure 6.8	The influence of the heat source parameter on the temperature distribution	148
Figure 6.9	The influence of the permeability parameter on the velocity profile	148
Figure 6.10	Geometry of the drainage problem	152
Figure 6.11	The influence of the non-Newtonian parameter on the shear stress drainage flow when $n=3$	157

Figure 6.12	The influence of the non-Newtonian parameter on the shear stress drainage case when $n = 1$	157
Figure 6.13	The influence of fluid behaviour index on the shear stress for the drainage case when $\xi_2 = 1$	158
Figure 6.14	The influence of Grashof number on the velocity profile for the drainage case	159
Figure 6.15	The influence of Grashof number on the temperature distribution for the drainage case	159
Figure 6.16	The influence of Brinkman number on the velocity profile for the drainage case	160
Figure 6.17	The influence of Brinkman number on the temperature distribution for the drainage case	160
Figure 6.18	The influence of the variable viscosity parameter on the velocity profile for the drainage case	161
Figure 6.19	The influence of the variable viscosity parameter on the temperature distribution for the drainage case	161
Figure 6.20	The influence of the non-Newtonian parameter on the temperature distribution for the drainage case	162
Figure 6.21	The influence of the heat source on the temperature distribution for the drainage case	162
Figure 6.22	The influence of the permeability on the velocity profile for the drainage case	163
Figure A.1	Mass conservation of a volume fixed in space	190

LIST OF ABBREVIATIONS

1D	-	One Dimensional
2D	-	Two Dimensional
ADM	-	Adomian Decomposition Method
BC	-	Boundary Conditions
HAM	-	Homotopy Analysis Method
HPM	-	Homotopy Perturbation Method
IC	-	Initial Conditions
MADM	-	Modified Adomian Decomposition Method
MHD	-	Magnetohydrodynamics
NDM	-	Natural Decomposition Method
OHAM	-	Optimal Homotopy Asymptotic Method
PDE	-	Partial Differential Equation
VIM	-	Variation Iteration Method

LIST OF SYMBOLS

a	-	Slip parameter
\mathbf{b}	-	Induced magnetic field
\mathbf{B}_0	-	Magnetic field strength
D/Dt	-	Material time derivative
\mathbf{E}	-	Electric field
\mathbf{D}, \mathbf{W}	-	Symmetric and antisymmetric part of the velocity
F	-	Total body force
\mathbf{g}	-	Gravity
\mathbf{I}	-	Identity tensor
\mathbf{J}	-	Electric current density
K	-	Permeability
p	-	Pressure
\mathbf{q}	-	Flux
\mathbf{R}	-	Flow resistance given by the rigid matrix
\mathbf{S}	-	Extra stress tensor
S_t	-	Stokes number
\mathbf{T}	-	Cauchy shear stress
U_0	-	Initial fluid velocity
u	-	Model velocity
\mathbf{u}	-	Velocity vector
w_e	-	Weissenberg number
t	-	Time

Greek symbols

δ	-	The fluid layer thickness
ρ	-	Density
μ, η	-	Dynamic viscosity

λ_p	-	Relaxation time
λ_r	-	Retardation time
μ_{eff}	-	Effective viscosity
$\boldsymbol{\tau}$	-	Shear stress tensor
ν	-	Kinematic viscosity
ϕ_i	-	Porosity
ϕ	-	Ratio of viscosities
θ	-	Angle of inclination
Θ_w	-	Wall heat temperature
Θ_1	-	Ambient temperature

Subscripts

xy	-	Dimensionless properties
------	---	--------------------------

Superscripts

T	-	Transpose properties
-----	---	----------------------

LIST OF APPENDICES

APPENDIX	TITLE	PAGE
Appendix A	Derivation of the Fluid Equations	189
Appendix B	Mathematical Codes	195

CHAPTER 1

INTRODUCTION

1.1 Overview

Fluid mechanics is a significant branch of physics and engineering. It deals with the mechanics of fluids at rest or in motion and the forces acting on them. Fluid dynamics is a part of fluid mechanics that deals with the movement of the fluids, and their interaction with solids or other liquids at the boundaries, which describes their behaviour and related phenomena (Yunus and Cimbala, 2006). In recent years, there has been significant growth in fluid dynamics research. Generally, fluids can be categorised as Newtonian or non-Newtonian based on the relationship between shear stress and shear rate in the fluid. The relationship between shear stress and shear rate in the Newtonian fluid is linear. But, it is nonlinear for the non-Newtonian. (Chhabra and Richardson, 1999).

The study of flow of non-Newtonian fluids has considerably increased over the years due to their relevance in many practical applications such as food processing, oil drilling, automotive, and aircraft design. Boundary layer approximations can be a beneficial approach for modelling problems of non-Newtonian fluids. Research into boundary layer flow problems of non-Newtonian fluids in manufacturing processes such as aerodynamic extrusions of plastic sheets has provided a better understanding of the distribution of shear stress in the sheets under various operating conditions. It has also provided insight into current advances in fluid mechanics. This chapter provides a background of the researches related to the non-Newtonian fluid flow in a porous medium under some physical effects including magnetic field, angle of inclination and viscous dissipation. In the following section the problem statement is presented, and the research questions are highlighted. The objectives and scope of this study are defined based on the research questions. The significance of this study applicable to sciences and engineering are also highlighted in this chapter.

1.2 Research Background

Non-Newtonian fluids can be used in several industrial processes and applications including wastewater treatment, food industries, and polymers manufacturing. Most physical phenomena that occur during processing of non-Newtonian fluids such as the flow of plasma and the circulation of shallow-water waves can be described using differential equations (Debnath, 2011). Non-Newtonian fluids do not adhere to the Newton's law of viscosity (Nguyen and Nguyen, 2012). Fluids that exhibit both viscous and elastic characteristics during deformation are known as non-Newtonian viscoelastic fluids.

Non-Newtonian fluids varies in nature therefore many constitutive equations have been proposed to examine the physical properties of these fluids. It is difficult to describe the behaviour of these fluids using a single constitutive equation. Furthermore, the nonlinear properties of viscoelastic fluid make it difficult to obtain precise solutions to the equations of motion of these fluids. No universal method can be used to obtain the solution for the equation of motion. Therefore, many methods have been suggested to solve these equations (Duan et al., 2013; F.A Hendi, 2012).

The non-Newtonian fluid models are usually categorised into three types: differential type, rate type, and integral type. The rate type models describe the response of fluids with slight memory, which means that the state of stress in the fluid depends on the relative history of the fluid deformation. Example of this behaviour can be observed in diluted polymeric solutions. Among the different types of non-Newtonian fluids, the viscoelastic fluids are the most investigated because the fluids exhibit both viscous and elastic behaviour (Christensen, 2012; Malkus et al., 1990). Furthermore, viscoelastic materials exhibit specific flow and relaxation behaviour which makes them complex and challenging to study (Bird, 1976). The importance of viscoelastic fluids in commercial and industrial fields have motivated the scientific community to explore the complex dynamics of these fluids in a porous medium (Denn, 1990). The study of the behaviour of viscoelastic fluid in a porous medium is very important for scientific and engineering industries. Knowledge of the various dynamic phenomena exhibit by viscoelastic fluid in a porous medium can be used to

make predictions of the stability of the fluid. Furthermore, understanding the flow of non-Newtonian fluids in a porous medium has many practical applications in engineering fields, such as the oil displacement in a porous pipe.

The flow of non-Newtonian fluid in porous media can be studied from a microscopic or macroscopic point of view. The microscopic study gives information about the bores inside the medium. This information can be used to predict the macroscopic behaviour of the system. The macroscopic approaches consider the global behaviour of the fluid flow, such as viscoelastic fluid properties. Moreover, no constitutive relation can forecast all non-Newtonian fluids (Fetecau and Fetecau, 2003; Hayat et al., 2019b). Under certain circumstances, the flow of non-Newtonian fluid in the porous medium becomes more complicated such as the flow under the Magnetohydrodynamic (MHD), which explains the dynamics of electrically conducting fluid. The critical fact behind the MHD is that the applied magnetic field induces electric current. The consequence of this process produces a Lorentz force which can significantly affect the motion of the fluid. This complexity makes it difficult to find the exact solutions for the fluid motion, compared to the numerical solutions. However, an approximate analytical solution can be found using the Adomian Decomposition Method (ADM). The ADM is very useful for solving linear equations, nonlinear ordinary equations, partial differential equations, algebraic equations, functional equations, and integral differential equations (Wazwaz, 2010).

The current study aims to develop a theoretical framework for understanding the flow of non-Newtonian fluids in porous medium. This study focuses on the processes involved in the lifting and draining of viscoelastic fluid in porous medium. Three non-Newtonian fluid models under steady state, homogeneous and shear flow conditions are investigated. The constitutive models are namely: Johnson-Segalman fluid, Powell-Eyring fluid, and Sisko fluid. The MHD is mathematically formulated for Powell-Eyring fluid and Sisko fluid only. It is not considered for Johnson-Segalman fluid due to the complexity of the fluid equation. The effects of the temperature on the viscosity of Sisko fluid are studied. The current study analyses the impact of effective parameters in porous medium. The ADM method is implemented to solve the governing equations of the three fluid models.

1.3 Problem Statement

Non-Newtonian fluids have nonlinear constitutive equations and complex properties, whereas Newtonian fluids have a linear constitutive relationship. Instabilities such as melt fracture and extrusion die flows were caused by this nonlinearity. These instabilities are caused by the normal fluid stresses (elasticity) or the existence and the nature of the boundary conditions (Phan-Thien and Mai-Duy, 2017). The constitutive equations for viscoelastic fluids determine the fluid viscosity consistency. Some of these constitutive equations are derived from empirical relationships, while others are complex and are derived from advanced molecular theories. Due to the complexity of these nonlinear constitutive equations, obtaining analytical solutions is a difficult task, as described below.

First, constitutive equations, which are the relationship between stress and the rate of strain tensors, predict how much pressure or stress is required to deform a material. For certain non-Newtonian fluids, the shear stress tensor is complicated, such as the Johnson-Segalman fluid because it is derived from molecular theory (Bird, 1976; Johnson Jr and Segalman, 1981). Second, stress control is more important than motion control because stress affects the fluidity and solidification of some substances, such as polymers (Renardy, 2005a). Some non-Newtonian fluids equations, such as Powell-Eyring fluid equation, becomes very complicated when subjected to external circumstances such as shear stress, MHD, body force, porous medium, and inclination (Chhabra and Richardson, 1999). Finally, in temperature-dependent viscosity, the fluid equation's momentum equation is combined with the energy equation, making the governing equation highly nonlinear, such as the heat transfer flow of the Sisko fluid in a porous medium. (Nield et al., 2006).

Understanding viscoelastic fluid flow in a porous medium where the flow becomes more complex is beneficial in many applications such as thermal insulation engineering, water movements in geothermal reservoirs, heat pipes, and nuclear waste. Theoretical research on this type of fluid which moves along various geometries, such as a wide flat plate and two belts with some significant effects: heat dissipation and MHD effects, are rarely studied. Therefore, these will be investigated in the current

study. As a result, the advancement of non-Newtonian fluid modelling appears to be required, in order to investigate these fluid flow types in a porous medium thoroughly. Therefore, this research is conducted to study the lifting and drainage of the thin film of viscoelastic fluid that moves along a flat plate or between two belts. This research also looks at the factors which influence the fluid flow. These factors are inclination, magnetic field, viscosity, and heat effect. One way to solve these problems is to implement an approximate analytical approach using the ADM to explore the following issues:

1. Viscoelastic fluid control is a crucial factor in the design of industrial materials. However, in certain circumstances, the viscoelastic responses of Johnson-Segalman fluid remain difficult.
2. Most of the solutions available for the Powell-Eyring fluid equation are numerical solutions, mainly if the fluid flows in a porous medium (Jalil et al., 2013; Ogunseye et al., 2019; Oyelami and Dada, 2016 ; Zaman et al., 2013). However, the new characteristics of the shear stress of the fluid during its flow in a porous medium encourage the discovery of an approximate analytical solution.
3. The temperature-dependent viscosity of Sisko fluid requires that the energy equation to be coupled to the momentum equations. Moreover, if the induced effect of the no-slip condition, MHD, and a porous medium is considered, an approximate analytical solution is required.

1.4 Research Questions

The following questions are raised based on the problem statement.

1. Is there any influence of shear stress, inclination, and porous medium on the steady flow of Johnson-Segalman fluid?

2. What is the Powell-Eyring fluid behaviour under the MHD effect for the steady flow in a porous medium?
3. To what extent does the temperature-dependent viscosity affect the flow of MHD Sisko fluid between two vertical belts?

1.5 Research Objectives

Based on the above problems, this study focuses on developing mathematical models that describe the incompressible, steady, and one-directional flow of the non-Newtonian fluid in a porous medium. It investigates the related parameters that influence the flow behaviour for the lifting and drainage flow with vertical or inclined geometry. Isotropic porous media is assumed for all the study's objectives to avoid the porous medium's complex nature. The study also aims to implement ADM to obtain the selected models' approximate analytical solution for lifting and drainage flow. The research objectives are as follows:

1. To study the steady flow of Johnson-Segalman fluid over an inclined plate in a porous medium using ADM.
2. To analyse the physical behaviour of the steady flow of MHD Powell-Eyring fluid over an inclined plate in a porous medium using ADM.
3. To investigate the influence of temperature-dependent viscosity on the flow of MHD Sisko fluid between two vertical belts in a porous medium using ADM.

1.6 Research Scope

This research is focused on the steady flow of the incompressible viscoelastic fluids in porous medium. The fluid models employed in this study are the Johnson-Segalman fluid, Powell-Eyring fluid, and Sisko fluid. The lifting and drainage flow

under the gravitational force and the effects of angle of inclination are also considered. For simplicity, the homogeneous model is considered for one-dimensional flow situation. The complexity of the models mentioned in section 1.2 can vary depending on the constitutive equation of the fluid and how the porous term is defined. Darcy's law is implemented for the flow of Johnson-Segalman fluid over an inclined plate. Due to the complexity of the constitutive equation of the Johnson-Segalman fluid, a simple flat plate geometry is selected. The plate is inclined in a porous medium without considering the effects of the magnetic fields. Furthermore, nonlinear differential equation, which relates the stress to the strain rate for Powel-Eyring fluid, is derived based on the interaction between the fluid, the magnetic field and angle of inclination. Finally, Sisko fluid is catalysed by heat flow and viscous dissipation of the magnetic field in the porous medium. MAPLE 2015 software is utilised to find the approximate analytical solution of the proposed problem via ADM. The results obtained are plotted and compared to the related published work.

1.7 Significance of the Study

The flow of viscoelastic fluids in porous medium presents many unique challenges for non-Newtonian fluids. The ability to use a simplified analytical tool to find a solution to the problem of non-Newtonian flow is potentially an important planning and management tool for industries where application of flow of non-Newtonian fluids are important. This research will provide a theoretical insight into the flow behaviour in an inclined system. Hence, the significances of this study can be summarised as follows:

1. A simple and realistic mathematical model is developed to better understand the viscoelastic fluid behaviour in a porous medium, particularly the Johnson-Segalman fluid.
2. This research will shed light on how the magnetic field and other physical conditions which affect the lifting and drainage flow of the Powell-Eyring and Sisko fluid models can help to gain a better understanding of the physical

behaviour and flow characteristics for the non-Newtonian fluid flows in a porous medium.

3. The basic knowledge gains in the areas of magnetic field, shear stress, temperature-dependent viscosity, and non-Newtonian fluid, can be useful information for many applications in science and engineering.
4. The analytical solutions obtained in this study can be used as the basis for future research to verify the solutions of more complex mathematical models obtained utilizing numerical solutions.

1.8 Thesis Outline

This thesis consists of seven chapters. The introduction, research background, statement of the problem, research questions, research objectives, research scope, significance of the research, and the layout are covered in this chapter.

Chapter 2 reviews and analyses the previous work related to the research objectives and covers an extensive review of earlier studies carried out using ADM.

Chapter 3 is divided into two parts. The first part covers the formulation of the problems using the general principles of mechanics, the derivation of governing equations for steady incompressible non-Newtonian fluids related to each objective are taken into consideration. The second part provides a detailed description of ADM and the other alternative formulas of the method.

Chapter 4 presents an approximate analytical solution for steady flow of Johnson-Segalman fluid over an inclined plate in a porous medium. Comparison of the fluid flow behaviour for porous and non-porous medium is conducted. The model is validated by comparing the present solution with the solution obtained by Alam et al. (2012) in the case of non-porous medium.

Chapter 5 considers the steady flow of Powell-Eyring fluid induced by a magnetic field over an inclined plate in the porous medium. As in Johnson-Segalman fluid model, the viscosity is assumed to be constant, and the flow driven by the shear and gravity. Thermal effects are not considered in this chapter.

Chapter 6 investigates the steady flow of the Sisko fluid over a wide belt in porous medium, using temperature dependent viscosity. The effect of the magnetic field and viscous dissipation is also considered.

In Chapters 4, 5, and 6, the solutions of the problems are obtained using the ADM which produced approximate analytical solutions. These solutions satisfy all initial and boundary conditions. Moreover, the graphical representations of the velocity profile are presented to show the impact of essential flow parameters on velocity and temperature. Finally, Chapter 7 presents the overall conclusions and the proposed future work. References and appendixes are listed at the end of the thesis.

REFERENCES

- Abassy, T.A. (2010). Improved Adomian decomposition method. *Computers & Mathematics with Applications*, 59(1), 42-54.
doi:<http://dx.doi.org/10.1016/j.camwa.2009.06.009>
- Abassy, T.A., El-Tawil, M.A. and El Zoheiry, H. (2007). Toward a modified variational iteration method. *Journal of Computational and Applied Mathematics*, 207(1), 137-147.
- Abbaoui, K. and Cherruault, Y. (1994). Convergence of Adomian's method applied to differential equations. *Computers & Mathematics with Applications*, 28(5), 103-109.
- Abbaoui, K. and Cherruault, Y. (1995). New ideas for proving convergence of decomposition methods. *Computers & Mathematics with Applications*, 29(7), 103-108.
- Abuduwali, A., Sakakihara, M. and Niki, H. (1994). A local Crank-Nicolson method for solving the heat equation. *Hiroshima Mathematical Journal*, 24(1), 1-13.
- Abuga, J.G. and Chinyoka, T. (2020). Numerical Study of Shear Banding in Flows of Fluids Governed by the Rolie-Poly Two-Fluid Model via Stabilized Finite Volume Methods. *Processes*, 8(7), 810.
- Adams, J. and Olmsted, P.D. (2009). Nonmonotonic models are not necessary to obtain shear banding phenomena in entangled polymer solutions. *Physical review letters*, 102(6), 067801.
- Adesanya, S.O., Falade, J.A. and Rach, R. (2015). Effect of couple stresses on hydromagnetic Eyring-Powell fluid flow through a porous channel. *Theoretical and Applied Mechanics*, 42(2), 135-150.
- Adomian, G. (1976). Nonlinear stochastic differential equations. *Journal of Mathematical Analysis and Applications*, 55(2), 441-452.
- Adomian, G. (1984). A new approach to nonlinear partial differential equations. *Journal of Mathematical Analysis and Applications*, 102(2), 420-434.
- Adomian, G. (1988). A review of the decomposition method in applied mathematics. *Journal of Mathematical Analysis and Applications*, 135(2), 501-544.
doi:[http://dx.doi.org/10.1016/0022-247X\(88\)90170-9](http://dx.doi.org/10.1016/0022-247X(88)90170-9)
- Adomian, G. (1991). Solving frontier problems modelled by nonlinear partial differential equations. *Computers & Mathematics with Applications*, 22(8), 91-94. doi:[http://dx.doi.org/10.1016/0898-1221\(91\)90017-X](http://dx.doi.org/10.1016/0898-1221(91)90017-X)
- Adomian, G. and Rach, R. (1983). Inversion of nonlinear stochastic operators. *Journal of Mathematical Analysis and Applications*, 91(1), 39-46.
doi:[http://dx.doi.org/10.1016/0022-247X\(83\)90090-2](http://dx.doi.org/10.1016/0022-247X(83)90090-2)
- Adomian, G. and Rach, R. (1996). Modified Adomian Polynomials. *Mathematical and Computer Modelling*, 24(11), 39-46.
doi:[http://dx.doi.org/10.1016/S0895-7177\(96\)00171-9](http://dx.doi.org/10.1016/S0895-7177(96)00171-9)
- Ahmad, N., Ullah, A., Ullah, A., Ahmad, S., Shah, K. and Ahmad, I. (2021). On analysis of the fuzzy fractional order Volterra-Fredholm integro-differential equation. *Alexandria Engineering Journal*, 60(1), 1827-1838.
- Ajibade, A. and Umar, A. (2019). Effects of viscous dissipation and wall conduction on steady mixed convection Couette flow of heat generating/absorbing fluid. *International Journal of Applied Mechanics and Engineering*, 24(4).

- Akbar, N.S., Ebaid, A. and Khan, Z. (2015). Numerical analysis of magnetic field effects on Eyring-Powell fluid flow towards a stretching sheet. *Journal of Magnetism and Magnetic Materials*, 382, 355-358.
- Akinshilo, A.T. and Olaye, O. (2019). On the analysis of the Eyring Powell model based fluid flow in a pipe with temperature dependent viscosity and internal heat generation. *Journal of King Saud University-Engineering Sciences*, 31(3), 271-279.
- Akram, J., Akbar, N.S. and Tripathi, D. (2020). Numerical study of the electroosmotic flow of Al₂O₃-CH₃OH Sisko nanofluid through a tapered microchannel in a porous environment. *Applied Nanoscience*, 1-16.
- Al-Khaled, K. and Rababah, N.a.M. (2020). Fast Convergence Methods for Hyperbolic Systems of Balance Laws with Riemann Conditions. *Symmetry*, 12(5), 757.
- Alam, M.K., Rahim, M.T., Avital, E., Islam, S., Siddiqui, A.M. and Williams, J. (2013). Solution of the steady thin film flow of non-Newtonian fluid on vertical cylinder using Adomian Decomposition Method. *Journal of the Franklin Institute*, 350(4), 818-839.
- Alam, M.K., Siddiqui, A.M., Rahim, M.T. and Islam, S. (2012). Thin-film flow of magnetohydrodynamic (MHD) Johnson–Segalman fluid on vertical surfaces using the Adomian decomposition method. *Applied Mathematics and Computation*, 219(8), 3956-3974.
doi:<http://dx.doi.org/10.1016/j.amc.2012.10.032>
- Alderman, N. (1997). *Non-Newtonian Fluids: Guide to Classification and Characteristics*.
- Ali, A., Underwood, A., Lee, Y.-R. and Wilson, D. (2016). Self-drainage of viscous liquids in vertical and inclined pipes. *Food and Bioproducts Processing*, 99, 38-50.
- Ali, M., Irfan, M., Khan, W., Sultan, F., Shahzad, M. and Khan, M. (2020). Physical significance of chemical processes and Lorentz's forces aspects on Sisko fluid flow in curved configuration. *Soft Computing*, 1-11.
- Aljahdaly, N.H. and El-Tantawy, S. (2020). Simulation study on nonlinear structures in nonlinear dispersive media. *Chaos: An Interdisciplinary Journal of Nonlinear Science*, 30(5), 053117.
- Alrabaiah, H., Jamil, M., Shah, K. and Khan, R.A. (2020). Existence theory and semi-analytical study of non-linear Volterra fractional integro-differential equations. *Alexandria Engineering Journal*.
- Alwatban, A.M., Khan, S.U., Waqas, H. and Tlili, I. (2019). Interaction of Wu's slip features in bioconvection of Eyring Powell nanoparticles with activation energy. *Processes*, 7(11), 859.
- Anderson, J.D. (1992). Governing equations of fluid dynamics. In *Computational fluid dynamics* (pp. 15-51): Springer.
- Asghar, Z., Ali, N., Ahmed, R., Waqas, M. and Khan, W.A. (2019). A mathematical framework for peristaltic flow analysis of non-Newtonian Sisko fluid in an undulating porous curved channel with heat and mass transfer effects. *Computer methods and programs in biomedicine*, 182, 105040.
- Awais, M., Malik, M., Bilal, S., Salahuddin, T. and Hussain, A. (2017). Magnetohydrodynamic (MHD) flow of Sisko fluid near the axisymmetric stagnation point towards a stretching cylinder. *Results in physics*, 7, 49-56.
- Awais, M., Raja, M.A.Z., Awan, S.E., Shoaib, M. and Ali, H.M. (2021). Heat and mass transfer phenomenon for the dynamics of Casson fluid through porous

- medium over shrinking wall subject to Lorentz force and heat source/sink. *Alexandria Engineering Journal*, 60(1), 1355-1363.
- Babolian, E. and Biazar, J. (2002). On the order of convergence of Adomian method. *Applied Mathematics and Computation*, 130(2-3), 383-387.
- Baniamerian, Z. and Mehdipour, R. (2014). Fin geometry optimization of non-Newtonian fluid, flowing through an annulus pipe, using entropy generation minimization method. *Open J Mech Eng*, 2(1), 45-51.
- Basombrío, F.G. (1993). Shocks in shear flows of the Johnson-Segalman type. *Journal of Non-Newtonian Fluid Mechanics*, 49(1), 1-11.
doi:[http://dx.doi.org/10.1016/0377-0257\(93\)85020-B](http://dx.doi.org/10.1016/0377-0257(93)85020-B)
- Bataller, R.C. (2010). Numerical comparisons of Blasius and Sakiadis flows. *MATEMATIKA: Malaysian Journal of Industrial and Applied Mathematics*, 26, 187-196.
- Baytaş, A.C. and Baytaş, A.F. (2005). 8 - ENTROPY GENERATION IN POROUS MEDIA. In D. B. Ingham & I. Pop (Eds.), *Transport Phenomena in Porous Media III* (pp. 201-226). Oxford: Pergamon.
- Bear, J. (2013). *Dynamics of fluids in porous media*: Courier Corporation.
- Bejan, A. (2013). *Convection heat transfer*: John Wiley & sons.
- Bellomo, N., Lods, B., Revelli, R. and Ridolfi, L. (2007). *Generalized collocation methods: solutions to nonlinear problems*: Springer Science & Business Media.
- Benilov, E. and Benilov, M. (2015). A thin drop sliding down an inclined plate. *Journal of Fluid Mechanics*, 773, 75.
- Biazar, J., Babolian, E., Kember, G., Nouri, A. and Islam, R. (2003). An alternate algorithm for computing Adomian polynomials in special cases. *Applied Mathematics and Computation*, 138(2), 523-529.
- Biazar, J. and Hosseini, K. (2017). An effective modification of Adomian decomposition method for solving Emden–Fowler type systems. *National Academy Science Letters*, 40(4), 285-290.
- Biazar, J. and Shafiof, S. (2007). A simple algorithm for calculating Adomian polynomials. *Int. J Contemp. Math. Sciences*, 2(20), 975-982.
- Bilal, M., Khan, S., Ali, F., Arif, M., Khan, I. and Nisar, K.S. (2021). Couette flow of viscoelastic dusty fluid in a rotating frame along with the heat transfer. *Scientific reports*, 11(1), 1-16.
- Bildik, N. and Bayramoglu, H. (2005). The solution of two dimensional nonlinear differential equation by the Adomian decomposition method. *Applied Mathematics and Computation*, 163(2), 519-524.
- Bird, R.B. (1976). USEFUL NON-NEWTONIAN MODELS. *Annual Review of Fluid Mechanics*, 8, 13-34. doi:10.1146/annurev.fl.08.010176.000305
- Briedis, D., Moutrie, M. and Balmer, R. (1980). A study of the shear viscosity of human whole saliva. *Rheologica Acta*, 19(3), 365-374.
- Butcher, J.C. (2000). Numerical methods for ordinary differential equations in the 20th century. *Journal of Computational and Applied Mathematics*, 125(1), 1-29. doi:[https://doi.org/10.1016/S0377-0427\(00\)00455-6](https://doi.org/10.1016/S0377-0427(00)00455-6)
- Callejas, A., Melchor, J., Faris, I.H. and Rus, G. (2021). Viscoelastic model characterization of human cervical tissue by torsional waves. *Journal of the Mechanical Behavior of Biomedical Materials*, 115, 104261.
- Carreau, P.J. (1972). Rheological equations from molecular network theories. *Transactions of the Society of Rheology*, 16(1), 99-127.

- Chaudhuri, S. and Rathore, S.K. (2020). An analytical investigation of pressure-driven flow and heat transfer of a Sisko fluid flowing through parallel plates with viscous dissipation. *Sādhanā*, 45(1), 1-17.
- Cherruault, Y. and Adomian, G. (1993). Decomposition methods: a new proof of convergence. *Mathematical and Computer Modelling*, 18(12), 103-106.
- Cherruault, Y., Adomian, G., Abbaoui, K. and Rach, R. (1995). Further remarks on convergence of decomposition method. *International Journal of Bio-Medical Computing*, 38(1), 89-93.
- Cherruault, Y., Saccomandi, G. and Some, B. (1992). New results for convergence of Adomian's method applied to integral equations. *Mathematical and Computer Modelling*, 16(2), 85-93. doi:[http://dx.doi.org/10.1016/0895-7177\(92\)90009-A](http://dx.doi.org/10.1016/0895-7177(92)90009-A)
- Chhabra, R.P. and Richardson, J.F. (1999). Chapter 1 - Non-Newtonian fluid behaviour. In R. P. C. F. Richardson (Ed.), *Non-Newtonian Flow in the Process Industries* (pp. 1-36). Oxford: Butterworth-Heinemann.
- Chinyoka, T. (2011). Suction-injection control of shear banding in non-isothermal and exothermic channel flow of Johnson-Segalman liquids. *Journal of Fluids Engineering*, 133(7), 071205.
- Christensen, R. (2012). *Theory of viscoelasticity: an introduction*: Elsevier.
- Civera, M., Grivet-Talocia, S., Surace, C. and Fragonara, L.Z. (2021). A generalised power-law formulation for the modelling of damping and stiffness nonlinearities. *Mechanical Systems and Signal Processing*, 153, 107531.
- Daftardar-Gejji, V. and Jafari, H. (2005). Adomian decomposition: a tool for solving a system of fractional differential equations. *Journal of Mathematical Analysis and Applications*, 301(2), 508-518. doi:<http://dx.doi.org/10.1016/j.jmaa.2004.07.039>
- Debnath, L. (2011). *Nonlinear partial differential equations for scientists and engineers*: Springer Science & Business Media.
- Deiber, J. and Schowalter, W. (1981). Modeling the flow of viscoelastic fluids through porous media. *AIChE Journal*, 27(6), 912-920.
- Denn, M.M. (1990). Issues in viscoelastic fluid mechanics. *Annual Review of Fluid Mechanics*, 22(1), 13-32.
- Disu, A. and Dada, M. (2017). Reynold's model viscosity on radiative MHD flow in a porous medium between two vertical wavy walls. *Journal of Taibah University for Science*, 11(4), 548-565.
- Dong, X., Liu, H., Wang, Q., Pang, Z. and Wang, C. (2013). Non-Newtonian flow characterization of heavy crude oil in porous media. *Journal of Petroleum Exploration and Production Technology*, 3(1), 43-53.
- Duan, J.-S. (2011). New recurrence algorithms for the nonclassic Adomian polynomials. *Computers & Mathematics with Applications*, 62(8), 2961-2977.
- Duan, J.-S., Rach, R., Wazwaz, A.-M., Chaolu, T. and Wang, Z. (2013). A new modified Adomian decomposition method and its multistage form for solving nonlinear boundary value problems with Robin boundary conditions. *Applied Mathematical Modelling*, 37(20–21), 8687-8708. doi:<http://dx.doi.org/10.1016/j.apm.2013.02.002>
- El-Masry, Y., Abd Elmaboud, Y. and Abdel-Sattar, M. (2020). The impacts of varying magnetic field and free convection heat transfer on an Eyring–Powell fluid flow with peristalsis: VIM solution. *Journal of Taibah University for Science*, 14(1), 19-30.

- Ellahi, R., Raza, M. and Vafai, K. (2012). Series solutions of non-Newtonian nanofluids with Reynolds' model and Vogel's model by means of the homotopy analysis method. *Mathematical and Computer Modelling*, 55(7-8), 1876-1891.
- Ellahi, R., Shivanian, E., Abbasbandy, S. and Hayat, T. (2016). Numerical study of magnetohydrodynamics generalized Couette flow of Eyring-Powell fluid with heat transfer and slip condition. *International Journal of Numerical Methods for Heat & Fluid Flow*, 26(5), 1433-1445.
- Ervin, V.J. and Lee, H. (2006). Defect correction method for viscoelastic fluid flows at high Weissenberg number. *Numerical Methods for Partial Differential Equations: An International Journal*, 22(1), 145-164.
- F.A Hendi, H.O.B., M.Almazmumy and H. Alzumi. (2012). A simple programing for solving nonlinear initial value problem using Adomian decomposition method *IJRRAS*, 121(3).
- Fälthammar, C.-G. (2007). The discovery of magnetohydrodynamic waves. *Journal of atmospheric and solar-terrestrial physics*, 69(14), 1604-1608.
- Fetecau, C. and Fetecau, C. (2003). The first problem of Stokes for an Oldroyd-B fluid. *International Journal of Non-Linear Mechanics*, 38(10), 1539-1544. doi:[http://dx.doi.org/10.1016/S0020-7462\(02\)00117-8](http://dx.doi.org/10.1016/S0020-7462(02)00117-8)
- Fielding, S.M. and Olmsted, P.D. (2003). Kinetics of the shear banding instability in startup flows. *Physical Review E*, 68(3), 036313.
- Fox, V., Erickson, L. and Fan, L. (1969). The laminar boundary layer on a moving continuous flat sheet immersed in a non-Newtonian fluid. *AIChE Journal*, 15(3), 327-333.
- Franchi, F., Lazzari, B. and Nibbi, R. (2015). Mathematical models for the non-isothermal Johnson–Segalman viscoelasticity in porous media: stability and wave propagation. *Mathematical Methods in the Applied Sciences*, 38(17), 4075-4087.
- Gau, C., Huang, T. and Aung, W. (1996). Flow and mixed convection heat transfer in a divergent heated vertical channel. *Journal of heat transfer*, 118(3), 606-615.
- Genovese, A., Carputo, F., Maiorano, A., Timpone, F., Farroni, F. and Sakhnevych, A. (2020). Study on the Generalized Formulations with the Aim to Reproduce the Viscoelastic Dynamic Behavior of Polymers. *Applied Sciences*, 10(7), 2321.
- Greco, F. and Ball, R.C. (1997). Shear-band formation in a non-Newtonian fluid model with a constitutive instability. *Journal of Non-Newtonian Fluid Mechanics*, 69(2–3), 195-206. doi:[http://dx.doi.org/10.1016/S0377-0257\(96\)01521-2](http://dx.doi.org/10.1016/S0377-0257(96)01521-2)
- Grosso, P., De Felice, A. and Sorrentino, S. (2021). A method for the experimental identification of equivalent viscoelastic models from vibration of thin plates. *Mechanical Systems and Signal Processing*, 153, 107527.
- Gul, T., Ghani, F., Islam, S., Shah, R.A., Khan, I., Nasir, S., et al. (2016). Unsteady thin film flow of a fourth grade fluid over a vertical moving and oscillating belt. *Propulsion and Power Research*, 5(3), 223-235. doi:<http://dx.doi.org/10.1016/j.jprr.2016.07.002>
- Gul, T., Islam, S., Shah, R.A., Khan, I. and Shafie, S. (2014). Thin film flow in MHD third grade fluid on a vertical belt with temperature dependent viscosity. *PloS one*, 9(6), e97552.

- Gutfinger, C. and Tallmadge, J.A. (1964). Some remarks on the problem of drainage of fluids on vertical surfaces. *AIChE Journal*, 10(5), 774-780.
- Hassan, A.R., Disu, A.B. and Fenuga, O.J. (2020). Entropy generation effect of a buoyancy force on hydromagnetic heat generating couple stress fluid through a porous medium with isothermal boundaries. *Heliyon*, 6(6), e04156.
- Hayat, T., Asghar, S. and Siddiqui, A.M. (2004). Stokes' second problem for a Johnson–Segalman fluid. *Applied Mathematics and Computation*, 148(3), 697-706. doi:[http://dx.doi.org/10.1016/S0096-3003\(02\)00928-1](http://dx.doi.org/10.1016/S0096-3003(02)00928-1)
- Hayat, T., Aslam, N., Khan, M.I., Khan, M.I. and Alsaedi, A. (2019a). MHD peristaltic motion of Johnson–Segalman fluid in an inclined channel subject to radiative flux and convective boundary conditions. *Computer methods and programs in biomedicine*, 180, 104999.
- Hayat, T., Hussain, Z., Farooq, M. and Alsaedi, A. (2018). Magneto hydrodynamic flow of Powell–Eyring fluid by a stretching cylinder with Newtonian heating. *Thermal Science*, 22(1 Part B), 371-382.
- Hayat, T., Iqbal, Z., Qasim, M. and Obaidat, S. (2012). Steady flow of an Eyring–Powell fluid over a moving surface with convective boundary conditions. *International Journal of Heat and Mass Transfer*, 55(7), 1817-1822.
- Hayat, T., Iqbal, Z., Sajid, M. and Vajravelu, K. (2008a). Heat transfer in pipe flow of a Johnson–Segalman fluid. *International Communications in Heat and Mass Transfer*, 35(10), 1297-1301. doi:<http://dx.doi.org/10.1016/j.icheatmasstransfer.2008.07.008>
- Hayat, T., Javed, M. and Asghar, S. (2008b). MHD peristaltic motion of Johnson–Segalman fluid in a channel with compliant walls. *Physics Letters A*, 372(30), 5026-5036. doi:<http://dx.doi.org/10.1016/j.physleta.2008.03.065>
- Hayat, T., Moitsheki, R.J. and Abelman, S. (2010). Stokes' first problem for Sisko fluid over a porous wall. *Applied Mathematics and Computation*, 217(2), 622-628.
- Hayat, T., Nawaz, S. and Alsaedi, A. (2019b). Entropy generation and endoscopic effects on peristalsis with modified Darcy's law. *Physica A: Statistical Mechanics and its Applications*, 536, 120846.
- Hayat, T., Wang, Y., Siddiqui, A.M. and Hutter, K. (2003). Peristaltic motion of a Johnson–Segalman fluid in a planar channel. *Mathematical Problems in Engineering*, 2003(1). doi:10.1155/s1024123x03308014
- Heidarzadeh, H., Mashinchijoubari, M. and Asghari, R. (2012). Application of Adomian decomposition method to nonlinear heat transfer equation. *J Math Comput Sci*, 4(3), 436-447.
- Hemingway, E., Clarke, A., Pearson, J. and Fielding, S. (2018). Thickening of viscoelastic flow in a model porous medium. *Journal of Non-Newtonian Fluid Mechanics*, 251, 56-68.
- Hemingway, E.J. and Fielding, S.M. (2020a). Interplay of edge fracture and shear banding in complex fluids. *Journal of Rheology*, 64(5), 1147-1159.
- Hemingway, E.J. and Fielding, S.M. (2020b). Interplay of edge fracture and shear banding in complex fluids. *arXiv preprint arXiv:2005.09405*.
- Himoun, N., Abbaoui, K. and Cherruault, Y. (1999). New results of convergence of Adomian's method. *Kybernetes*, 28(4), 423-429.
- Huang, H. and Ayoub, J.A. (2006). *Applicability of the Forchheimer equation for non-Darcy flow in porous media*. Paper presented at the SPE Annual Technical Conference and Exhibition.

- Hussain, A., Malik, M., Bilal, S., Awais, M. and Salahuddin, T. (2017). Computational analysis of magnetohydrodynamic Sisko fluid flow over a stretching cylinder in the presence of viscous dissipation and temperature dependent thermal conductivity. *Results in physics*, 7, 139-146.
- Imran, N., Javed, M., Sohail, M., Gokul, K. and Roy, P. (2020a). Exploration of thermal transport for Sisko fluid model under peristaltic phenomenon. *Journal of Physics Communications*, 4(6), 065003.
- Imran, N., Javed, M., Sohail, M. and Tlili, I. (2020b). Utilization of modified Darcy's law in peristalsis with a compliant channel: applications to thermal science. *Journal of Materials Research and Technology*, 9(3), 5619-5629.
- Iqbal, N., Yasmin, H., Kometa, B.K. and Attiya, A.A. (2020). Effects of Convection on Sisko Fluid with Peristalsis in an Asymmetric Channel. *Mathematical and Computational Applications*, 25(3), 52.
- Ishak, A., Nazar, R. and Pop, I. (2006). Mixed convection boundary layers in the stagnation-point flow toward a stretching vertical sheet. *Meccanica*, 41(5), 509-518.
- Ishigaki, Y. (2020). Diffusion wave phenomena and L_p decay estimates of solutions of compressible viscoelastic system. *Journal of Differential Equations*, 269(12), 11195-11230.
- Jalil, M., Asghar, S. and Imran, S. (2013). Self similar solutions for the flow and heat transfer of Powell-Eyring fluid over a moving surface in a parallel free stream. *International Journal of Heat and Mass Transfer*, 65, 73-79.
- Jamil, M. and Khan, N.A. (2011). Slip effects on fractional viscoelastic fluids. *International Journal of Differential Equations*, 2011.
- Javed, M. (2020). A mathematical framework for peristaltic mechanism of non-Newtonian fluid in an elastic heated channel with Hall effect. *Multidiscipline Modeling in Materials and Structures*.
- Jeffreys, H. (1930). *The draining of a vertical plate*. Paper presented at the Mathematical Proceedings of the Cambridge Philosophical Society.
- Johnson, J.M.W. and Segalman, D. (1977). A model for viscoelastic fluid behavior which allows non-affine deformation. *Journal of Non-Newtonian Fluid Mechanics*, 2(3), 255-270. doi:[http://dx.doi.org/10.1016/0377-0257\(77\)80003-7](http://dx.doi.org/10.1016/0377-0257(77)80003-7)
- Johnson Jr, M.W. and Segalman, D.J. (1981). Description of the non-affine motions of dilute polymer solutions by the porous molecule model. *Journal of Non-Newtonian Fluid Mechanics*, 9(1-2), 33-56. doi:[http://dx.doi.org/10.1016/0377-0257\(87\)87005-2](http://dx.doi.org/10.1016/0377-0257(87)87005-2)
- Joseph, D.D. (1985). HYPERBOLIC PHENOMENA IN THE FLOW OF VISCOELASTIC FLUIDS. In A. S. Lodge, M. Renardy, & J. A. Nohel (Eds.), *Viscoelasticity and Rheology* (pp. 235-321): Academic Press.
- Kamran Alam, M., Rahim, M.T., Haroon, T., Islam, S. and Siddiqui, A.M. (2012). Solution of steady thin film flow of Johnson–Segalman fluid on a vertical moving belt for lifting and drainage problems using Adomian Decomposition Method. *Applied Mathematics and Computation*, 218(21), 10413-10428. doi:<http://dx.doi.org/10.1016/j.amc.2012.03.095>
- Kaya, D. and El-Sayed, S.M. (2004). Adomian's decomposition method applied to systems of nonlinear algebraic equations. *Applied Mathematics and Computation*, 154(2), 487-493. doi:[http://dx.doi.org/10.1016/S0096-3003\(03\)00729-X](http://dx.doi.org/10.1016/S0096-3003(03)00729-X)

- Kelesoglu, O. (2014). The Solution of Fourth Order Boundary Value Problem Arising out of the Beam-Column Theory Using Adomian Decomposition Method. *Mathematical Problems in Engineering*, 2014, 6. doi:10.1155/2014/649471
- Khaled, A.-R. and Vafai, K. (2003). The role of porous media in modeling flow and heat transfer in biological tissues. *International Journal of Heat and Mass Transfer*, 46(26), 4989-5003.
- Khan, I., Malik, M., Salahuddin, T., Khan, M. and Rehman, K.U. (2017). Homogenous–heterogeneous reactions in MHD flow of Powell–Eyring fluid over a stretching sheet with Newtonian heating. *Neural Computing and Applications*, 1-8.
- Khan, M. (2016). Flow and heat transfer to Sisko fluid with partial slip. *Canadian Journal of Physics*, 94(8), 724-730.
- Khan, M., Abbas, Z. and Hayat, T. (2008). Analytic solution for flow of Sisko fluid through a porous medium. *Transport in Porous Media*, 71(1), 23-37.
- Khan, M., Munawar, S. and Abbasbandy, S. (2010). Steady flow and heat transfer of a Sisko fluid in annular pipe. *International Journal of Heat and Mass Transfer*, 53(7–8), 1290-1297. doi:<http://dx.doi.org/10.1016/j.ijheatmasstransfer.2009.12.037>
- Khan, M., Munir, A. and Shahzad, A. (2015a). Convective Heat Transfer to Sisko Fluid over a Nonlinear Radially Stretching Sheet. In *Heat Transfer Studies and Applications: InTech*.
- Khan, M., Munir, A. and Shahzad, A. (2015b). Convective heat transfer to Sisko fluid over a nonlinear radially stretching sheet. *Heat Transfer Studies and Applications; Kazi, SN, Ed.; Intech: Rijeka, Croatia*, 341-361.
- Khan, M., Shahzad, A., Anjum, A. and M. Mahomed, F. (2014a). Analytic approximate solutions for time-dependent flow and heat transfer of a Sisko fluid. *International Journal of Numerical Methods for Heat & Fluid Flow*, 24(5), 1005-1019.
- Khan, N., Riaz, M., Hashmi, M.S., Khan, S.U., Tlili, I., Khan, M.I., et al. (2020). Soret and Dufour features in peristaltic motion of chemically reactive fluid in a tapered asymmetric channel in the presence of Hall current. *Journal of Physics Communications*, 4(9), 095009.
- Khan, N.A., Aziz, S. and Khan, N.A. (2014b). MHD flow of Powell–Eyring fluid over a rotating disk. *Journal of the Taiwan Institute of Chemical Engineers*, 45(6), 2859-2867.
- Khan, N.Z., Rana, M.A., Siddiqui, A.M. and Nayyar, I.W. (2014c, 14-18 Jan. 2014). *Numerical solution of thin film steady MHD flow of a Johnson-Segalman fluid on a vertical surfaces*. Paper presented at the Proceedings of 2014 11th International Bhurban Conference on Applied Sciences and Technology (IBCAST), , Islamabad, Pakistan.
- Khuzhayorov, B., Auriault, J.-L. and Royer, P. (2000). Derivation of macroscopic filtration law for transient linear viscoelastic fluid flow in porous media. *International Journal of Engineering Science*, 38(5), 487-504.
- Kierkus, W.T. (1968). An analysis of laminar free convection flow and heat transfer about an inclined isothermal plate. *International Journal of Heat and Mass Transfer*, 11(2), 241-253. doi:[https://doi.org/10.1016/0017-9310\(68\)90153-1](https://doi.org/10.1016/0017-9310(68)90153-1)
- Kolkka, R.W., Malkus, D.S., Hansen, M.G. and Ierley, G.R. (1988). Spurt phenomena of the Johnson-Segalman fluid and related models. *Journal of*

- Non-Newtonian Fluid Mechanics*, 29, 303-335.
doi:[http://dx.doi.org/10.1016/0377-0257\(88\)85059-6](http://dx.doi.org/10.1016/0377-0257(88)85059-6)
- Kumar, M. (2020). Numerical solution of singular boundary value problems using advanced Adomian decomposition method. *Engineering with Computers*, 1-11.
- Kumar, M.A., Reddy, Y.D., Goud, B.S. and Rao, V.S. (2021). Effects of sores, dufour, hall current and rotation on MHD natural convective heat and mass transfer flow past an accelerated vertical plate through a porous medium. *International Journal of Thermofluids*, 9, 100061.
- Kumar, V., Gangacharyulu, D. and Tathgir, R.G. (2007). Heat transfer studies of a heat pipe. *Heat Transfer Engineering*, 28(11), 954-965.
- Kundu, P.K., Cohen, I.M. and Dowling, D. (2008). Fluid Mechanics 4th. In: Elsevier.
- Kurdyumov, V.N. and Linan, A. (2001). Free and forced convection around line sources of heat and heated cylinders in porous media. *Journal of Fluid Mechanics*, 427, 389-409.
- Lai, F. and Kulacki, F. (1990). The effect of variable viscosity on convective heat transfer along a vertical surface in a saturated porous medium. *International Journal of Heat and Mass Transfer*, 33(5), 1028-1031.
- Lasseux, D. and Valdés-Parada, F.J. (2017). On the developments of Darcy's law to include inertial and slip effects. *Comptes Rendus Mécanique*, 345(9), 660-669.
- Letelier, M.F., Siginer, D.A., Almendra, D.L. and Stockle, J.S. (2019). Resonance in laminar pipe flow of non-linear viscoelastic fluids. *International Journal of Non-Linear Mechanics*, 115, 53-60.
- Li, W. and Pang, Y. (2020). Application of Adomian decomposition method to nonlinear systems. *Advances in Difference Equations*, 2020(1), 1-17.
- Liao, S. (2005). Comparison between the homotopy analysis method and homotopy perturbation method. *Applied Mathematics and Computation*, 169(2), 1186-1194.
- Lienhard, I. and John, H. (2005). *A heat transfer textbook*: Phlogiston press.
- Lisbôa, T.V. and Marczak, R.J. (2020). Modified decomposition method applied to laminated thick plates in nonlinear bending. *Communications in Nonlinear Science and Numerical Simulation*, 81, 105015.
- Loeb, L.B. (2004). *The kinetic theory of gases*: Courier Corporation.
- Lu, T.-T. and Zheng, W.-Q. (2021). Adomian decomposition method for first order PDEs with unprescribed data. *Alexandria Engineering Journal*, 60(2), 2563-2572.
- Malik, M. (2017). *Application of shooting method on MHD thermally stratified mixed convection flow of non-Newtonian fluid over an inclined stretching cylinder*. Paper presented at the Journal of Physics Conference Series.
- Malik, M., Hussain, A., Salahuddin, T., Awais, M., Bilal, S. and Khan, F. (2016). Flow of Sisko fluid over a stretching cylinder and heat transfer with viscous dissipation and variable thermal conductivity: A numerical study. *AIP Advances*, 6(4), 045118.
- Malkus, D.S., Nohel, J.A. and Plohr, B.J. (1990). Dynamics of shear flow of a non-Newtonian fluid. *Journal of Computational Physics*, 87(2), 464-487.
- Malkus, D.S., Nohel, J.A. and Plohr, B.J. (1991). Analysis of New Phenomena in Shear Flow of Non-Newtonian Fluids. *SIAM Journal on Applied*

- Mathematics*, 51(4), 899-929. Retrieved from <http://www.jstor.org/stable/2101824>
- Manzoor, N., Bég, O.A., Maqbool, K. and Shaheen, S. (2019). Mathematical modelling of ciliary propulsion of an electrically-conducting Johnson-Segalman physiological fluid in a channel with slip. *Computer methods in biomechanics and biomedical engineering*, 22(7), 685-695.
- Mehta, R.P. and Kataria, H.R. (2021). Influence of Magnetic Field, Thermal Radiation and Brownian Motion on Water-Based Composite Nanofluid Flow Passing Through a Porous Medium. *International Journal of Applied and Computational Mathematics*, 7(1), 1-24.
- Migler, K., Hervet, H. and Leger, L. (1993). Slip transition of a polymer melt under shear stress. *Physical review letters*, 70(3), 287.
- Mohyud-Din, S.T. and Noor, M.A. (2007). Homotopy perturbation method for solving fourth-order boundary value problems. *Mathematical Problems in Engineering*, 2007.
- Molokov, S.S., Moreau, R. and Moffatt, H.K. (2007). *Magnetohydrodynamics: Historical evolution and trends* (Vol. 80): Springer Science & Business Media.
- Moosavi, M., Momeni, M., Tavangar, T., Mohammadyari, R. and Rahimi-Esbo, M. (2016). Variational iteration method for flow of non-Newtonian fluid on a moving belt and in a collector. *Alexandria Engineering Journal*, 55(2), 1775-1783.
- Moosavi, R., Moltafet, R., Lin, C.-X. and Chuang, P.-Y.A. (2021). Numerical modeling of fractional viscoelastic non-Newtonian fluids over a backward facing step–Buoyancy driven flow and heat transfer. *Thermal Science and Engineering Progress*, 21, 100767.
- Mungkasi, S. and Dheno, M.F.S. (2017). *Adomian decomposition method used to solve the gravity wave equations*. Paper presented at the AIP Conference Proceedings.
- Munir, A., Shahzad, A. and Khan, M. (2015). Mixed convection heat transfer in Sisko fluid with viscous dissipation: Effects of assisting and opposing buoyancy. *Chemical Engineering Research and Design*, 97, 120-127.
- Nadeem, S. and Akbar, N.S. (2009). Influence of heat transfer on a peristaltic flow of Johnson Segalman fluid in a non uniform tube. *International Communications in Heat and Mass Transfer*, 36(10), 1050-1059. doi:<http://dx.doi.org/10.1016/j.icheatmasstransfer.2009.07.012>
- Nazeer, M., Ahmad, F., Saeed, M., Saleem, A., Naveed, S. and Akram, Z. (2019). Numerical solution for flow of a Eyring–Powell fluid in a pipe with prescribed surface temperature. *Journal of the Brazilian Society of Mechanical Sciences and Engineering*, 41(11), 518.
- Nguyen, Q.-H. and Nguyen, N.-D. (2012). Incompressible non-Newtonian fluid flows. *Continuum Mechanics-Progress in Fundamentals and Engineering Applications, IntechOpen, DOI, 10(26091)*, 47-72.
- Nield, D.A., Bejan, A. and Nield-Bejan... (2006). *Convection in porous media* (Vol. 3): Springer.
- Nield, D.A., Junqueira, S. and Lage, J.L. (1996). Forced convection in a fluid-saturated porous-medium channel with isothermal or isoflux boundaries. *Journal of Fluid Mechanics*, 322, 201-214.
- Niethammer, M., Marschall, H., Kunkelmann, C. and Bothe, D. (2018). A numerical stabilization framework for viscoelastic fluid flow using the finite volume

- method on general unstructured meshes. *International Journal for Numerical Methods in Fluids*, 86(2), 131-166.
- Ogunseye, H.A., Salawu, S.O., Tijani, Y.O., Riliwan, M. and Sibanda, P. (2019). Dynamical analysis of hydromagnetic Brownian and thermophoresis effects of squeezing Eyring–Powell nanofluid flow with variable thermal conductivity and chemical reaction. *Multidiscipline Modeling in Materials and Structures*.
- Oyelami, F. and Dada, M. (2016). Transient magnetohydrodynamic flow of Eyring–Powell fluid in a porous medium. *Ife Journal of Science*, 18(2), 463-472.
- Phan-Thien, N. and Mai-Duy, N. (2017). *Understanding viscoelasticity: an introduction to rheology*: Springer.
- Polyanin, A.D. (2019). Comparison of the Effectiveness of Different Methods for Constructing Exact Solutions to Nonlinear PDEs. Generalizations and New Solutions. *Mathematics*, 7(5), 386.
- Powell, R.E. and Eyring, H. (1944). Mechanism for relaxation theory of viscosity. *Nature*, 154(55), 427-428.
- Prasad, V.R., Gaffar, S.A., Reddy, E.K. and Beg, O.A. (2014). Computational study of non-Newtonian thermal convection from a vertical porous plate in a non-Darcy porous medium with Biot number effects. *Journal of Porous Media*, 17(7).
- Prasannakumara, B., Gireesha, B., Krishnamurthy, M. and Kumar, K.G. (2017). MHD flow and nonlinear radiative heat transfer of Sisko nanofluid over a nonlinear stretching sheet. *Informatics in Medicine Unlocked*, 9, 123-132.
- Qiu, X., Duan, J., Luo, J., Kaloni, P.N. and Liu, Y. (2013). Parameter effects on shear stress of Johnson–Segalman fluid in Poiseuille flow. *International Journal of Non-Linear Mechanics*, 55(0), 140-146.
doi:<http://dx.doi.org/10.1016/j.iinonlinmec.2013.04.008>
- Qiu, X., Wang, H., Luo, J. and Liu, Y. (2015). Characteristics of velocity gradient jumping discontinuity in steady Poiseuille flow of Johnson–Segalman fluid. *International Journal of Non-Linear Mechanics*, 71(0), 72-82.
doi:<http://dx.doi.org/10.1016/j.iinonlinmec.2015.02.001>
- Rach, R. (1984). A convenient computational form for the Adomian polynomials. *Journal of mathematical analysis and applications*, 102(2), 415-419.
- Rajagopal, K.R. and Na, T.-Y. (1985). Natural convection flow of a non-Newtonian fluid between two vertical flat plates. *Acta Mechanica*, 54(3-4), 239-246.
- Rawashdeh, M.S. and Maitama, S. (2015). Solving nonlinear ordinary differential equations using the NDM. *J. Appl. Anal. Comput*, 5(1), 77-88.
- Rawashdeh, M.S. and Maitama, S. (2020). On Finding Exact Solutions to Coupled Systems of Partial Differential Equations by the NDM. *Thai Journal of Mathematics*, 18(2), 621-637.
- Ray, A.K., Vasu, B., Murthy, P. and Gorla, R.S. (2020). Non-similar solution of Eyring–Powell fluid flow and heat transfer with convective boundary condition: Homotopy Analysis Method. *International Journal of Applied and Computational Mathematics*, 6(1), 16.
- Ree, F., Ree, T. and Eyring, H. (1958). Relaxation theory of transport problems in condensed systems. *Industrial & Engineering Chemistry*, 50(7), 1036-1040.
- Renardy, M. (2005a). Are viscoelastic flows under control or out of control? *Systems & Control Letters*, 54(12), 1183-1193.
doi:<http://dx.doi.org/10.1016/j.sysconle.2005.04.006>

- Renardy, M. (2005b). Shear flow of viscoelastic fluids as a control problem. *Journal of Non-Newtonian Fluid Mechanics*, 131(1–3), 59-63.
doi:<http://dx.doi.org/10.1016/j.innfm.2005.08.008>
- Renardy, M. (2008). Chapter 5 Mathematical Analysis of Viscoelastic Fluids. In *Handbook of Differential Equations: Evolutionary Equations* (Vol. Volume 4, pp. 229-265): North-Holland.
- Romig, M.F. (1964). The influence of electric and magnetic fields on heat transfer to electrically conducting fluids. In *Advances in Heat Transfer* (Vol. 1, pp. 267-354): Elsevier.
- Saelao, J. and Yokchoo, N. (2020). The solution of Klein–Gordon equation by using modified Adomian decomposition method. *Mathematics and Computers in Simulation*, 171, 94-102.
- Sakiadis, B.C. (1961). Boundary-layer behavior on continuous solid surfaces: I. Boundary-layer equations for two-dimensional and axisymmetric flow. *AIChE Journal*, 7(1), 26-28.
- Salah, F., Alzahrani, A., Sidahmed, A.O. and Viswanathan, K. (2019). A note on thin-film flow of Eyring-Powell fluid on the vertically moving belt using successive linearization method. *INTERNATIONAL JOURNAL OF ADVANCED AND APPLIED SCIENCES*, 6(2), 17-22.
- Shah, S. and Hussain, S. (2021). Slip effect on mixed convective flow and heat transfer of magnetized UCM fluid through a porous medium in consequence of novel heat flux model. *Results in physics*, 20, 103749.
- Sheth, S.S. and Singh, T.R. (2020). *Analytical Approximate Solutions of Non Linear Partial Differential Equations using VIM, VIADM and New Modified KVIADM*. Paper presented at the Journal of Physics: Conference Series.
- Shivamoggi, B. (2002). *Perturbation methods for differential equations*: Springer Science & Business Media.
- Siddiqui, A., Ahmed, M. and Ghori, Q. (2007). Thin film flow of non-Newtonian fluids on a moving belt. *Chaos, Solitons & Fractals*, 33(3), 1006-1016.
- Siddiqui, A., Ashraf, H., Haroon, T. and Walait, A. (2015a). On the analytic solution for the steady drainage of magnetohydrodynamic (MHD) Sisko fluid film down a vertical belt. *Applications and Applied Mathematics*, 10(1), 267-286.
- Siddiqui, A., Ashraf, H., Walait, A. and Haroon, T. (2015b). On study of horizontal thin film flow of Sisko fluid due to surface tension gradient. *Applied Mathematics and Mechanics*, 36(7), 847-862.
- Siddiqui, A., Haroon, T. and Zeb, M. (2014). Analysis of Eyring-Powell fluid in helical screw rheometer. *The Scientific World Journal*, 2014.
- Siddiqui, A., Walait, A., Haroon, T. and Smeltzer, J. (2016). Transient drainage of the thin film of linearly viscous MHD fluid on a slippery flat belt. *Canadian Journal of Physics*, 94(4), 393-399.
- Siddiqui, A.M. and Ansari, A.R. (2010). A note on the Darcy - Forchheimer-Brinkman equation for fully developed flowthrough a porous channel bounded by flat plates. *Journal of Porous Media*, 13(12), 1111-1117.
doi:10.1615/JPorMedia.v13.i12.60
- Siddiqui, A.M., Farooq, A. and Babcock, B. (2013). Two Analytical Methods Applied to Study Thin Film Flow of an Eyring-Powell Fluid on a Vertically Moving Belt. *Applied Mathematical Sciences*, 7(70), 3469-3478.
- Sirohi, V., Timol, M. and Kalthia, N. (1987). Powell-Eyring model flow near an accelerated plate. *Fluid dynamics research*, 2(3), 193-204.

- Sisko, A. (1958). The flow of lubricating greases. *Industrial & Engineering Chemistry*, 50(12), 1789-1792.
- Slattery, J.C. (1967). Flow of viscoelastic fluids through porous media. *AIChE Journal*, 13(6), 1066-1071.
- Sobamowo, G.M. (2019). On Heat transfer analysis in pipe flow of Johnson-Segalman Fluid: Analytical Solution and Parametric Studies. *AUT Journal of Mechanical Engineering*, 3(2), 187-196.
- Soto-Castruita, E., Ramírez-González, P.V., Martínez-Cortés, U. and Quiñones-Cisneros, S.E. (2015). Effect of the temperature on the non-Newtonian behavior of heavy oils. *Energy & Fuels*, 29(5), 2883-2889.
- Soundalgekar, V. (1967). *On the flow of an electrically conducting, incompressible fluid near an accelerated plate in the presence of a parallel plate, under transverse magnetic field*. Paper presented at the Proceedings of the Indian Academy of Sciences-Section A.
- St W, C. and Churchill, R. (1975). A general model for the effective viscosity of pseudoplastic and dilatant fluids. *Rheologica Acta*, 14(5), 404-409.
- Swarnalathamma, B., Krishna, M.V. and Prakash, J. (2021). Hall Effects on MHD Free Convective Flow Through Porous Medium in Vertical Channel. In *Advances in Fluid Dynamics* (pp. 1027-1040): Springer.
- Tallmadge, J.A. and Gutfinger, C. (1967). Entrainment of Liquid Films—Drainage, Withdrawal, and Removal. *Industrial & Engineering Chemistry*, 59(11), 18-34.
- Tan, W. and Masuoka, T. (2005a). Stokes' first problem for a second grade fluid in a porous half-space with heated boundary. *International Journal of Non-Linear Mechanics*, 40(4), 515-522.
doi:<http://dx.doi.org/10.1016/j.ijnonlinmec.2004.07.016>
- Tan, W. and Masuoka, T. (2005b). Stokes' first problem for an Oldroyd-B fluid in a porous half space. *Physics of Fluids*, 17(2), 023101. doi:10.1063/1.1850409
- Tanner, R.I. (1979). Some useful constitutive models with a kinematic slip hypothesis. *Journal of Non-Newtonian Fluid Mechanics*, 5(0), 103-112.
doi:[http://dx.doi.org/10.1016/0377-0257\(79\)85006-5](http://dx.doi.org/10.1016/0377-0257(79)85006-5)
- Tanveer, A., Hayat, T. and Alsaedi, A. (2018). Variable viscosity in peristalsis of Sisko fluid. *Applied Mathematics and Mechanics*, 39(4), 501-512.
- Tanveer, A. and Salahuddin, T. (2019). Emission of electromagnetic waves from walls of esophagus under domination of wall slip effect. *Chaos, Solitons & Fractals*, 127, 110-117.
- Teertstra, P., Culham, J. and Yovanovich, M. (1997). Comprehensive review of natural and mixed convection heat transfer models for circuit board arrays. *Journal of Electronics Manufacturing*, 7(02), 79-92.
- Terekhov, V. and Ekaid, A.L. (2011). Laminar natural convection between vertical isothermal heated plates with different temperatures. *Journal of Engineering Thermophysics*, 20(4), 416-433.
- Turkyilmazoglu, M. (2011). Some issues on HPM and HAM methods: a convergence scheme. *Mathematical and Computer Modelling*, 53(9-10), 1929-1936.
- Turkyilmazoglu, M. (2018). A reliable convergent Adomian decomposition method for heat transfer through extended surfaces. *International Journal of Numerical Methods for Heat & Fluid Flow*, 28(11), 2551-2566.
- Umavathi, J., Chamkha, A. and Mohiuddin, S. (2016). Combined effect of variable viscosity and thermal conductivity on free convection flow of a viscous fluid

- in a vertical channel. *International Journal of Numerical Methods for Heat & Fluid Flow*, 26(1), 18-39.
- Umavathi, J. and Shekar, M. (2016). Combined effect of variable viscosity and thermal conductivity on free convection flow of a viscous fluid in a vertical channel using DTM. *Meccanica*, 51(1), 71-86.
- Van Rossum, J. (1958). Viscous lifting and drainage of liquids. *Applied Scientific Research, Section A*, 7(2-3), 121-144.
- Vossoughi, S. (1999). Flow of non-newtonian fluids in porous media. In *Rheology Series* (Vol. 8, pp. 1183-1235): Elsevier.
- Wazwaz, A.-M. (1999). A reliable modification of Adomian decomposition method. *Applied Mathematics and Computation*, 102(1), 77-86.
doi:[http://dx.doi.org/10.1016/S0096-3003\(98\)10024-3](http://dx.doi.org/10.1016/S0096-3003(98)10024-3)
- Wazwaz, A.-M. (2010). *Partial differential equations and solitary waves theory*: Springer Science & Business Media.
- Wazwaz, A.M. (2001). Construction of solitary wave solutions and rational solutions for the KdV equation by Adomian decomposition method. *Chaos, Solitons & Fractals*, 12(12), 2283-2293. doi:[http://dx.doi.org/10.1016/S0960-0779\(00\)00188-0](http://dx.doi.org/10.1016/S0960-0779(00)00188-0)
- Xue, C. and Nie, J. (2008). Exact solutions of Rayleigh-Stokes problem for heated generalized Maxwell fluid in a porous half-space. *Mathematical Problems in Engineering*, 2008.
- Yamaguchi, H. (2008). *Engineering fluid mechanics* (Vol. 85): Springer Science & Business Media.
- Yasmin, H., Iqbal, N. and Hussain, A. (2020). Convective Heat/Mass Transfer Analysis on Johnson-Segalman Fluid in a Symmetric Curved Channel with Peristalsis: Engineering Applications. *Symmetry*, 12(9), 1475.
- Yoon, H. and Ghajar, A. (1987a). A note on the Powell-Eyring fluid model. *International Communications in Heat and Mass Transfer*, 14(4), 381-390.
- Yoon, H.K. and Ghajar, A.J. (1987b). A note on the Powell-Eyring fluid model. *International Communications in Heat and Mass Transfer*, 14(4), 381-390.
doi:[https://doi.org/10.1016/0735-1933\(87\)90059-5](https://doi.org/10.1016/0735-1933(87)90059-5)
- Yunus, A.C. and Cimbala, J.M. (2006). Fluid mechanics fundamentals and applications. *International Edition, McGraw Hill Publication*, 185201.
- Zaman, H., Shah, M.A. and Ibrahim, M. (2013). Unsteady incompressible Couette flow problem for the Eyring-Powell model with porous walls. *American Journal of Computational Mathematics*, 2013.
- Zhang, M., Zhang, W., Wu, Z., Shen, Y., Wu, H., Cheng, J., et al. (2019). Modulation of viscoelastic fluid response to external body force. *Scientific reports*, 9(1), 1-11.

LIST OF PUBLICATIONS

Journal papers

1. Fawzia, M.E., Bahar, A., Mustafa, S.D., Aziz, Z.A., Salah, F. (2021). Effects of Shear Stress on Magnetohydrodynamic (MHD) Powell Eyring Fluid over A Porous Plate: A Lift and Drainage Problem. *IAENG International Journal of Applied Mathematics*, (Q3, Correction submitted - **IJAM_2020_11_18b**).
2. Fawzia, M.E., Bahar, A., Mustafa, S.D., Aziz, Z.A. (2021). Magnetic Resistive Flow of Sisko Fluid in A Porous Channel with Variable Viscosity. *Numerical Methods for Partial Differential Equations*, (Q1, Correction submitted - **NMPDE-2020-4151**).
3. Fawzia, M.E., Mustafa, S.D., Bahar, A., Aziz, Z.A. (2019). Steady Flow of Johnson-Segalman Fluid through Porous Medium over an Inclined Plate. *Journal of Porous Media*. 22(5), 583- 598.
4. Fawzia, M.E., A., Aziz, Z.A. Salah, F., Mustafa, S.D., (2017). Approximate analytical solution of the MHD Powell-Eyring fluid flow near accelerated plate. *Malaysian Journal of Fundamental and Applied Sciences*. 416-420