Proceedings of the Society for Computation in Linguistics

Volume 6 Article 42

6-1-2023

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Recommended Citation

Torres, Charles J. and Futrell, Richard (2023) "L0-regularization induces subregular biases in LSTMs," Proceedings of the Society for Computation in Linguistics: Vol. 6, Article 42.

DOI: https://doi.org/10.7275/5ss3-d749

Available at: https://scholarworks.umass.edu/scil/vol6/iss1/42

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L_0 -regularization induces subregular biases in LSTMs

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Introduction Ongoing work attempts to identify the formal language patterns in natural language. In phonology, recent work has identified the subregular languages as a good candidate (Heinz, 2018). However, there remain few explanations for the source of this bias. This abstract proposes a means of investigating formal language learnability. We propose using a variant of minimum description length (MDL) as defined on LSTMs with varying priors on LSTM size. We will show its utility on a test case from Heinz and Idsardi (2013) and Rawski et al. (2017).

Methods The subregular hypothesis is that phonological patterns occupy a well-defined subset of the regular languages (Heinz, 2018). It has enjoyed empirical success, with laboratory experiments demonstrating these preferences in artificial language learning studies (Lai, 2015; Avcu and Hestvik, 2020; McMullin and Hansson, 2019). But explanations for the existence of this bias are lacking. A minimum description length (MDL) or simplicity principle, where the shortest encoding of input data is preferred (Grünwald, 2000; Chater and Vitányi, 2003), is an enticing explanation, but it fails in most explored representation systems (Heinz and Idsardi, 2013). We consider Long Short-Term Memory networks (LSTMs) (Hochreiter and Schmidhuber, 1997) as an alternative representation system for their flexibility in learning formal languages (Weiss et al., 2018), and show that constraining their complexity induces a subregular bias.

With LSTMs, a natural choice of description length is the number of parameters, or number of connections between neurons. Functionally, this means training networks using L_0 -regularization, which penalizes for number of nonzero parameters. While it is generally undifferentiable, we use a differentiable sampling technique from Louizos et al. (2017). We keep the architecture fixed (see

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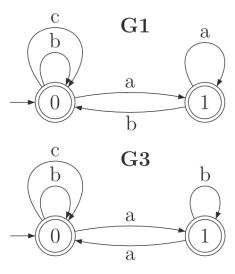


Figure 1: Two regular grammars. G1 is subregular and strictly local, G3 is a counting language and not subregular. Figures adjusted from Heinz and Idsardi (2013).

Appendix A) in order to control for other sources of variation in LSTM complexity.

Our experiment concerns an open question from Heinz and Idsardi (2013). Consider two formal grammars from their paper (depicted as finite state automata (FSA) in Fig. 1). These have equal description lengths as FSAs, but G_1 is subregular and governed by local constraints whereas G_3 is a counting language and not subregular. G_1 is more language-like and thus its purported preference represents an open puzzle for simplicity-based accounts.

To assess this preference using computational complexity we train 5 LSTMs each with 45 different regularization penalties to vary resulting LSTM complexities (N=225). Each LSTM is trained on words drawn from the intersection between G_1 and G_3 using the cross entropy of the predicted next character together with the regularization penalty as the training objective (details in Appendix B).

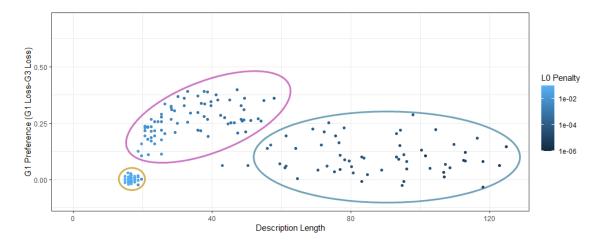


Figure 2: Plot showing relationship between complexity of LSTMs trained on an intersection of G_1 and G_3 , and the performance gap between G_1 and G_3 after training (the G_1 preference). When complexity is unconstrained, performance moderately favors G_1 (blue ellipse). As complexity becomes more constrained, favorability of G_1 as a hypothesis increases (purple ellipse). Extremely tight constraints leads to a collapse in preference (gold ellipse).

After training we assess differences in performance on words drawn from G_1 and G_3 separately to assess generalization. If G_1 is preferred for models of constrained complexity, then complexity constraints may result in an inductive bias for subregular languages.

Results Our results show a bias for the subregular grammar G_1 for almost all levels of complexity. But, this preference is responsive to complexity constraints. As complexity of these LSTMs lowers there is an increase in this preference before a subsequent collapse (Fig. 2). A t-test between the purple and blue regions (defined as the range 20-40, and >40, respectively) is statistically significant $(t=-13.79, p<2.2\times10^{-16})$.

What drives this change can be seen in Fig. 3. Regularizing for complexity causes a drop in the cross entropy for the subregular language after training, a pattern which is most extreme when at the 40 parameter mark. In other words, regularization leads to generalization from the intersection of the two grammars to G_1 exclusively.

Discussion Our results show that a preference for simple LSTMs can enhance subregular preferences in at least some cases. Previous work on GRUs (Prickett, 2021), also show subregular biases, but our work contributes a possible additional explanation for this bias: that this preference is downstream of a preference for solutions involving smaller subnetworks. This is consistent with the Lottery Ticket Hypothesis (Frankle and Carbin, 2019), and may

function with—or be the underlying cause of—other biases, like the recency bias (Ravfogel et al., 2019).

Though this work reinforces the existence of a subregular bias in neural networks, and offers an explanation for its presence, it still leaves several questions unanswered. Is it really the subregular class that is preferred? It is possible that what appears to be a subregular bias is *only* appearance, and that the real bias has yet to be elucidated by formal language theory. Furthermore, how does this preference under regularization constraints compare with human biases? Further research is warranted to describe this bias, and how it compares with the subregular class and human phonology.

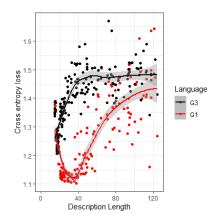


Figure 3: Relationship between description length and cross entropy loss on G_1 and G_3 for LSTMs trained on their intersection.

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A Architecture

Each LSTM is composed of an embedding layer, a single layer LSTM, a linear layer, and decoder layer. The embedding layer has 3 dimensions, and all other layers have 5. The LSTM uses the *tanh* activation function.

B The training objective

Our training objective is a form of MDL, in particular, a two-part code formed from the sum of the cross entropy and the expected value for number of non-zero parameters. It can be idealized as:

$$J = \frac{1}{N} \sum_{i=1}^{N} \log p_{\boldsymbol{\theta}}(x_i) + \beta \sum_{\theta \in \boldsymbol{\theta}} q_{\boldsymbol{\phi}}(\theta \neq 0)$$

Where p_{θ} is our LSTM, parameterized by parameter vector θ and q_{ϕ} probability of a parameter being masked (see Louizos et al. (2017) for details). The constant β , our regularization parameter, allows us to control for relative preference in LSTM size.