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**Topical Review** 

# Progression of group-III sesquioxides: epitaxy, solubility and desorption

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#### Abstract

In recent years, ultra-wide bandgap semiconductors have increasingly moved into scientific focus due to their outstanding material properties, making them promising candidates for future applications within high-power electronics or solar-blind photo detectors. The group-III-sesquioxides can appear in various polymorphs, which influences, for instance, the energy of the optical bandgap. In gallium oxide, the optical bandgap ranges between 4.6 and 5.3 eV depending on the polymorph. For each polymorph it can be increased or decreased by alloying with aluminum oxide (8.8 eV) or indium oxide (2.7–3.75 eV), respectively, enabling bandgap engineering and thus leading to an extended application field. For this purpose, an overview of miscibility limits, the variation of bandgap and lattice constants as a function of the alloy composition are reviewed for the rhombohedral, monoclinic, orthorhombic and cubic polymorph. Further, the effect of formation and desorption of volatile suboxides on growth rates is described with respect to chemical trends of the discussed ternary materials.

Keywords: Ga<sub>2</sub>O<sub>3</sub> thin films, pulsed laser deposition, ternary alloy, desorption of volatile suboxides

(Some figures may appear in colour only in the online journal)

#### 1. Introduction

In the last decades, an increasing number of studies on ultrawide bandgap semiconductors have been reported and more and more oxide semiconductors have come into focus. In this process a variety of publications and reviews on structural, optical and electrical properties of monoclinic  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> [1– 5] appeared. Up to now, successful implementations of  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> based devices, such as high-power switches and transistors [2–4, 6], solar-blind photo detectors [7], gas sensors [8], or thin film transistors [1], have been reported. The

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group-III-sesquioxides and their ternary alloys can crystallize in different crystal structures. The growth of the respective structure can be specifically influenced by the choice of growth parameters (e.g. substrate temperature, pressure, metal flux, etc), substrate material and orientation, additional doping (e.g. tin for the orthorhombic polymorph), or others. The electrically insulating Al<sub>2</sub>O<sub>3</sub> grows in thermodynamic equilibrium in a rhombohedral crystal lattice where it has a very large optical bandgap of 8.7-8.8 eV. Due to its optical transparency, high temperature and chemical stability, high mechanical strength [9] and its low cost industrial manufacturing capabilities,  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> is used commonly as substrate material. Binary Ga<sub>2</sub>O<sub>3</sub> can be synthesized in four different polymorphs identified as rhombohedral  $\alpha$ -, monoclinic  $\beta$ -, defective spinel  $\gamma$ -, or orthorhombic  $\kappa$ -phase (also referred to as  $\varepsilon$ ). Often a cubic  $\delta$ -phase [10] is mentioned, but Playford *et al* showed that this polymorph is just a nanocrystalline form of



**Figure 1.** Ball-and-stick representation of the rhombohedral (corundum)  $\alpha$ -, the monoclinic  $\beta$ -gallia, the orthorhombic  $\kappa$ -, and the cubic bixbyite crystal structure. The blue marked atoms denote the octahedral ( $O_h$ ) and the green ones the tetrahedral ( $T_d$ ) cation sites. The red atoms indicate the oxygen atoms. The structure models were created with VESTA [15].

 $\varepsilon$ -Ga<sub>2</sub>O<sub>3</sub> and not a distinct polymorph [11]. The monoclinic  $\beta$ -gallia structure is the thermodynamically most stable phase for which high-quality bulk single crystals are commercially available and hence most Ga<sub>2</sub>O<sub>3</sub> based publications deal with the  $\beta$ -gallia polymorph. The remaining polymorphs are metastable and can change their structure at different transition temperatures, resulting in a ranking of their thermodynamical stability described by  $\beta > \kappa > \alpha > \gamma$  [10]. Depending on the polymorph, the bandgap of Ga<sub>2</sub>O<sub>3</sub> can range between 4.6 and 5.3 eV. The group-III sesquioxide with the smallest direct bandgap is In<sub>2</sub>O<sub>3</sub> with 3.6–3.8 eV [12–14], which crystallizes in the cubic bixbyite structure in thermodynamical equilibrium. Ball-and-stick models of the rhombohedral, monoclinic, orthorhombic and cubic polymorphs are presented in figure 1. In table 1 the space groups, lattice constants and optical bandgap energies of the binary materials, originating in these polymorphs, are summarized.

The fabrication of Ga<sub>2</sub>O<sub>3</sub> thin films can be realized by a variety of growth techniques such as mist chemical vapour deposition (mist CVD) [17, 24–31], metal organic CVD (MOCVD) [22, 32–45], halide vapour phase epitaxy (HVPE) [46–56], metalorganic vapour phase epitaxy (MOVPE) [57–59], pulsed laser deposition (PLD) [57, 60–69], molecular beam epitaxy (MBE) [57, 70–76], atomic layer deposition (ALD) [77–79], mist epitaxy [80], the sol–gel method [81], and magnetron sputtering [82]. Besides, crystalline  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> bulk crystals can be grown by floating-zone (FZ) [83–85], the edge-defined film-fed growth (EFG) [86], the Czochralski (CZ) [87, 88], the Verneuil [89, 90] and the flux [20, 91–93] methods. In studies about In<sub>2</sub>O<sub>3</sub>, the semiconductor was inter alia fabricated by MOCVD [94–96], PLD [97–101], MBE

[102–107], or sputtering [108–110]. The growth of bulk In<sub>2</sub>O<sub>3</sub> from melt was developed and described by the IKZ Berlin [111]. The growth techniques of the ternary alloys used for (Al,Ga,In)<sub>2</sub>O<sub>3</sub> are summarized for the  $\alpha$ -,  $\beta$ -,  $\kappa$ - and cubic bixbyite phase in table 2.

In the present work we review the dependencies of lattice constants and optical bandgaps as a function of the alloy composition of the rhombohedral, monoclinic, orthorhombic, and cubic group-III-sesquioxide polymorphs. The review contains published data as well as own results that we obtained on our thin films grown by PLD. Furthermore, we point out how formation and desorption of volatile suboxides influence the cation composition and under which growth conditions in the PLD chamber desorption can be suppressed. In the course of this, we present thin films with a lateral varying composition, including a short description of the combinatorial PLD approach used.

#### 2. Combinatorial thin film synthesis

Investigations of entire mixtures of ternary solid-solutions within a single thin film sample of ternary  $(Al,Ga)_2O_3$  or  $(In,Ga)_2O_3$  is possible by employing a composition spread approach, e.g. by pulsed laser deposition (PLD). A combinatorial PLD thin film synthesis was introduced by the semiconductor physics group of the Universität Leipzig (UL) [148], which allows the growth of thin films that exhibit a lateral variation of the cation composition. For a thin film with a compositional gradient, a two-fold segmented target has to be utilized. A synchronized rotation speed of target and substrate used in the PLD chamber is a precondition for our approach. The geometric arrangement of target and substrate influences the cation composition as described in detail in [149].

In general, these thin films were synthesized by employing a KrF excimer laser (248 nm) with an energy density of  $2.6 \,\mathrm{J}\,\mathrm{cm}^{-2}$  on the target surface. The ceramic targets used are composed of one half of Ga<sub>2</sub>O<sub>3</sub> (purity 99.999%, Alfa Aeser) and one half of Al<sub>2</sub>O<sub>3</sub> (purity 99.997%, Alfa Aeser) or In<sub>2</sub>O<sub>3</sub> (purity 99.994%, Alfa Aeser), respectively. In addition, the segments can be doped, e.g. to induce electrical conductivity or to stabilize the growth of the  $\kappa$ -phase [76, 69] (tin doping is decisive). The target material is ball-milled and the homogenized powders are sintered in air and high temperatures between 1150 °C and 1350 °C for 72 h, 2 in. diameter c-plane sapphire substrates are placed in a heatable substrate holder located at a distance of 10 cm opposite to the target. The lateral offset between laser spot position on the target and the substrate center is 16-17 mm. Besides the oxygen pressure, the growth temperature in the PLD chamber can be adjusted. Further details on our growth facilities are summarized in [150]. The pulse repetition number of the samples discussed ranges between 25 000 and 30 000 at a pulse frequency of 10 Hz.

The cation distribution was determined by energydispersive x-ray spectroscopy (EDX) using a FEI Nova Nanolab 200 equipped with an Ametek EDAX detector. The crystal structure was identified by XRD  $2\theta$ - $\omega$  scans conducted with a PANalytical X'pert PRO MRD diffractometer equipped with a

Structure	Space group	Polymorph	Lattice constants	Optical bandgap
Rhombohedral	R3c	$\alpha$ -Al <sub>2</sub> O <sub>3</sub>	a = 4.7617  Å [16];	8.7–8.8 eV
			$c = 12.995 \text{\AA} [16]$	
		$\alpha$ -Ga <sub>2</sub> O <sub>3</sub>	a = 4.9825  Å [17];	5.2–5.3 eV
			c = 13.433 Å [17]	
		$\alpha$ -In <sub>2</sub> O <sub>3</sub>	a = 5.487  Å [18];	3.7 eV
			c = 14.510  Å [18]	
Monoclinic	C2/m	$\theta$ -Al <sub>2</sub> O <sub>3</sub>	a = 11.854  Å [19];	No exp. values
			b = 2.904  Å [19];	
			$c = 5.622 \mathrm{A} [19];$	
			$\beta = 103.83^{\circ}$ [19]	
		$\beta$ -Ga <sub>2</sub> O <sub>3</sub>	a = 12.214  A [20];	4.6–5.0 eV
			b = 3.037  A [20];	
			c = 5.798  A [20];	
Outh a shareh i a	D.,		$\beta = 103.83^{\circ} [20]$	NI
Orthorhombic	$Pna2_1$	$\kappa$ -Al <sub>2</sub> O <sub>3</sub>	a = 4.843 / A [21];	No exp. values
			b = 8.5500  A [21]; c = 8.9547  Å [21]	
		$\kappa$ -G2-O-	c = 5.9547  A [21] a = 5.046  Å [22]	40 eV
		n-0a203	a = 5.040  A [22], b = 8.702  Å [22];	4.907
			c = 9.283  Å [22],	
Cubic	Ia3	c-In <sub>2</sub> O <sub>3</sub>	a = 10.117  Å [23]	3.75 eV

Table 1. Space group, lattice parameter and optical bandgap for various binary polymorphs of the group-II sesquioxides.

**Table 2.** Growth methods and highest reported cation incorporation for rhombohedral, monoclinic, orthorhombic, and cubic polymorphs of  $(Al,Ga,In)_2O_3$  alloys.

Polymorph	Growth method	Reported alloy range
$ \begin{array}{c} \alpha - (Al_xGa_{1-x})_2O_3 \\ \alpha - (In_yGa_{1-y})_2O_3 \\ \beta - (Al_xGa_{1-x})_2O_3 \\ \beta - (In_yGa_{1-y})_2O_3 \\ \kappa - (Al_xGa_{1-y})_2O_3 \\ \kappa - (In_yGa_{1-y})_2O_3 \\ \kappa - (In_yGa_{1-y})_2O_3 \\ c - (Ga_zIn_{1-z})_2O_3 \end{array} $	Mist CVD [112–115], PLD [116–118], MBE [119] Mist CVD [113, 120, 121] PLD [122–125], MBE [126–129], sputtering [130] MOCVD [131], PLD [101, 132–135], MBE [71, 75, 136], sol–gel method [137] Mist CVD [139], PLD [140–142] Mist CVD [143], PLD [144, 145] MOCVD [146, 147], PLD [134, 132], MBE [138], sol–gel method [137]	Entire composition range $y \le 0.08, y \ge 0.67$ [120] $x \le 0.61$ [128] $y \le 0.35$ [138] $x \le 0.65$ [140] $y \le 0.35$ [144] $z \le 0.5$ [146, 147]

PIXcel<sup>3D</sup> detector with 255 channels operating in 1D scanning line mode. The thin film thickness (*d*) was determined by spectroscopic ellipsometry employing a dual rotating compensator ellipsometer (RC2, J.A. Woollam M2000) with a spot size of about  $300 \times 500 \,\mu\text{m}^2$ . Then the growth rate *r* was calculated by dividing *d* by the number of pulses during deposition.

#### 3. Formation and desorption of volatile suboxides

In several publications the influence of growth conditions on growth rates (r) during deposition of Ga<sub>2</sub>O<sub>3</sub> and its ternary alloys with In or Al was studied systematically. The investigations revealed that under high growth temperatures ( $T_g$ ) and oxygen-poor growth conditions volatile suboxides forms and desorbs leading to lower r and that in ternary alloys a non-stoichiometric incorporation of the provided cations into the thin film can be observed.

Vogt *et al* examined the influence of the O- and Me-fluxes (Me = Ga, In) ratio for binary  $Ga_2O_3$  and  $In_2O_3$ , respectively, during MBE growth [73, 136]. In  $Ga_2O_3$  for oxygen-rich conditions the growth rates are determined by the offered metal

flux and no desorption of cation species was observed, which leads to the assumption that all metal atoms are incorporated into the thin film layer. In a oxygen-poor regime volatile Me<sub>2</sub>O suboxides are formed, which were not incorporated into the thin film. Consistent studies of PLD grown Ga<sub>2</sub>O<sub>3</sub> thin films also revealed the influence of oxygen pressure ( $p(O_2)$ ) and growth temperature on the growth rate. Lower growth rates are observed for decreasing oxygen pressure [65] or increasing growth temperatures [66], respectively.

In the ternary alloys  $(Al,Ga)_2O_3$  and  $(In,Ga)_2O_3$  the desorption of volatile suboxides manifests itself in such a way that, besides decreasing *r*, the cation ratio of Al to Ga or In to Ga is altered. For PLD grown  $(Al,Ga)_2O_3$  thin films a high growth temperature and/or low oxygen pressure result in lower *r* and higher Al incorporation into the layer [123, 124, 142, 151]. Due to the lower dissociation energy of the Ga–O bond compared to the Al–O bond, in an oxygen poor regime Ga atoms form volatile sub-oxides being desorbed, which leads to a preferential incorporation of the Al atoms. In the  $(In,Ga)_2O_3$  alloy desorption of volatile suboxides can be observed, too [131, 136]: the Ga atoms are preferentially incorporated on account of the higher dissociation energy of the Ga–O bond



**Figure 2.** (a) Al cation ratio *x* and (b) Al cation ratio *y* recorded along the gradient direction of CCS-PLD  $(Al_xGa_{1-x})_2O_3$  and  $(In_yGa_{1-y})_2O_3$  thin films on c-sapphire substrates. The growth temperature of each sample was around 640 °C and the oxygen regimes are indicated in the graphs.

compared to the In-O bond. In addition, a metal-exchange has to be taken into account for this alloy. In (In,Ga)<sub>2</sub>O<sub>3</sub> the Ga atoms etches already existing In-O bonds and then replace In [136]. As a result, the released In atoms form either droplets on the thin film surface at low  $T_g$  or will be desorbed as In<sub>2</sub>O suboxide at high  $T_g$ , leading to a further reduction of the In incorporation as well as lower growth rates [136]. To investigate systematically the influence of  $p(O_2)$  on  $(Al,Ga)_2O_3$ and (In,Ga)<sub>2</sub>O<sub>3</sub>, CCS-PLD thin films grown with well-defined lateral variation of the cation flux at a constant temperature of 640 °C and either an oxygen poor regime of  $p(O_2) =$ 0.0003 mbar or an oxygen rich regime of  $p(O_2) = 0.01$  mbar on c-plane sapphire were studied. The composition gradients were determined by EDX and the resulting Al and In contents in terms of the gradient position are presented in figure 2. Position 0 indicates the center of the wafer and the gray solid



**Figure 3.** Growth rates *r* for different cation compositions of  $(Al_xGa_{1-x})_2O_3$  and  $(In_yGa_{1-y})_2O_3$  thin films grown on c-plane sapphire at 640 °C and oxygen rich ( $p(O_2) = 0.01$  mbar) or poor ( $p(O_2) = 0.0003$  mbar) conditions, respectively.

lines, the calculated model curve of the CCS-PLD approach [149].

For oxygen rich conditions, the spatial resolution of the alloy composition fits quite well to the model curve, which indicates a stoichiometric target-to-layer transfer with growth rates between 9 and 10 pm/pulse for all Al contents and low In content (y = 0.1). For higher y the growth rates range between 12.9 and 13.8 pm/pulse as visible in figure 3. In an oxygen poor regime a strong deviation from the stoichiometric cation incorporation in (Al,Ga)<sub>2</sub>O<sub>3</sub> and (In,Ga)<sub>2</sub>O<sub>3</sub>, respectively, can be observed as well as a strong decrease in growth rates. For the  $(Al,Ga)_2O_3$  sample the Al content increases suddenly in the first quarter from 45 at.% to around 80 at.% and increases in the last three quarters slightly up to 99 at.%. The narrow Al valley at position -14/-13 is caused by phase separation, which is not within the scope of this work for which reason this is not discussed further. A similar behaviour is given for the  $(In,Ga)_2O_3$  sample: for oxygen poor conditions the In content increases in the first three quarters only up to approximately 20 at.% and jumps in the last quarter up to 80 at.% (see figure 2).

The strong non-stoichiometric cation incorporation is caused by the low supply of oxygen atoms during growth leading to the formation and subsequent desorption of volatile suboxides, which can be further approved by the low grates being  $\approx 6-7$  pm/pulse below the values of the oxygen rich samples. The growth rates of the (In,Ga)<sub>2</sub>O<sub>3</sub> sample in the oxygen regime increases with increasing In content, which is caused on the one hand by the higher ionic radii of In compared to Ga and on the other hand by a kinetically favored formation of In<sub>2</sub>O<sub>3</sub> leading to a faster reaction with O<sub>2</sub> and thereby to higher *r*.

Interestingly, the cation ratio of the  $(In_xGa_{1-x})_2O_3$  thin film fits in the last quarter (y > 0.6) with the model curve due to an observable phase separation to the cubic bixbyite phase



**Figure 4.** In content *y* in terms of the spatial location on the wafer for a  $\beta$ - and a  $\kappa$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> thin film on c-plane sapphire. Both thin films were deposited in an oxygen poor regime ( $p(O_2) = 0.0003$  mbar) at  $T_g = 640$  °C.

(for further details see [132]), which allows the assumption that despite formation and desorption of volatile suboxides, both, Ga and In, are incorporated stoichiometrically in this phase.

In summary, it has been shown in this part that in the  $(In,Ga)_2O_3$  alloy mainly  $In_2O$  forms and desorbs, why proportionately more Ga atoms are detected in the layer. Against it, in the  $(Al,Ga)_2O_3$  alloy the significantly higher Al incorporation is due to a stronger Ga<sub>2</sub>O formation and desorption.

Studies of the influence of  $T_g$  and  $p(O_2)$  on  $\beta$ - and  $\kappa$ -(Al,Ga)<sub>2</sub>O<sub>3</sub> thin films, published in [151, 142], demonstrate that desorption occurs for both polymorphs. A direct comparison showed that the formation and desorption of volatile suboxides is stronger in the monoclinic alloy, resulting in an increased Al incorporation in the layer under same growth conditions. A potential reason for the slightly suppressed desorption in the orthorhombic polymorph is surfactant-mediated growth. An additional tin supply during growth, both for PLD and MBE is necessary to synthesize orthorhombic thin films [69, 76]. Tin acts as a surfactant in the growth process and is not incorporated into the thin film [69, 141].

Figure 4 presents  $\beta$ - and  $\kappa$ -(In,Ga)<sub>2</sub>O<sub>3</sub> thin films grown at  $T_g = 640$  °C and oxygen poor conditions ( $p(O_2) = 0.0003$  mbar). The  $\kappa$ -(In,Ga)<sub>2</sub>O<sub>3</sub> thin film was already discussed in [144] and a comparable  $\beta$ -(In,Ga)<sub>2</sub>O<sub>3</sub> thin film in [132] by the University of Leipzig (UL). The  $\beta$ -phase crystallized up to approximately y = 0.28 and the  $\kappa$ -phase up to y = 0.35. For higher In contents phase separation proceeds to the hexagonal InGaO (II) as well as to the cubic (Ga,In)<sub>2</sub>O<sub>3</sub> phase (crystal structure determined by x-ray diffraction [132, 144]). From position -23 to -12, the increase of y of both polymorphs is equal. After this point it can be observed that the content gap of y becomes larger with ongoing positions. At position 11 the gap is  $\Delta y = 0.17$ , which indicates a more extensive formation and desorption of volatile suboxides in the  $\beta$ -phase.



**Figure 5.** Lattice constant *a* of  $\alpha$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> and  $\alpha$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> as a function of the alloy composition. The data was taken from Hassa *et al* [118], Fujita and Kaneko [113] and Dang *et al* [115]. Recent data from our PLD thin films are shown by star-shaped (for lateral homogeneous thin films) or diamond-shaped (for CCS-PLD) markers and are denoted by UL.

#### 4. Crystal structure

The group-III sesquioxides (Al<sub>2</sub>O<sub>3</sub>, Ga<sub>2</sub>O<sub>3</sub> and In<sub>2</sub>O<sub>3</sub>) have different ground state crystal structures, namely the rhombohedral corundum, the monoclinic  $\beta$ -gallia and the cubic bixbyite structure, respectively. The rhombohedral corundumstructure has been reported as the only polymorph for all of the group-III sesquioxides and hence it should in principle be possible to stabilize the  $\alpha$ -phase throughout the entire composition range [121]. Phase separation in the  $(Al,Ga,In)_2O_3$ alloys is expected for all other polymorphs. The miscibility gap will likely depend on the polymorph considered. In table 2 the actual reported maximum cation compositions of the thermodynamically most stable polymorphs are shown. Since Al, Ga and In have different ionic radii the lattice constants will change within ternary alloys. An incorporation of Al into Ga<sub>2</sub>O<sub>3</sub> leads to decreasing lattice parameters, while In incorporation causes an increase. The cation sites have a coordination number of 4 or 6 depending on the distinct polymorph. The ratio and arrangement of the octahedral  $(O_{\rm h})$  or tetrahedral  $(T_d)$  lattice sites differs in the polymorphs discussed below and is distinguished by color in figure 1.

#### 4.1. Rhombohedral crystal structure

In the corundum structure (space group  $R\bar{3}c$ ) all Me<sup>3+</sup> (Me = Al, Ga, In) cations occupy  $O_h$  lattice sites and grow within a hexagonal close-packed O<sup>2-</sup> array. The unit cell presented in figure 1 contains six Me<sub>2</sub>O<sub>3</sub> formula units with the space group  $R\bar{3}c$ . As indicated, all group-III-sesquioxides can be synthesized in the rhombohedral structure and alloying in the whole composition range should be possible as observed for  $\alpha$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub>. It is interesting that so far In in  $\alpha$ -Ga<sub>2</sub>O<sub>3</sub> has only been



**Figure 6.** Lattice constants *a*, *b*, *c* and  $\beta$  in dependence on the cation composition for monoclinic  $\beta$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> and  $\beta$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub>. Literature data were compiled for powder samples [23, 92, 152–154], thin films [137] and bulk crystals [155]. The Recent data from our PLD thin films are shown by star-shaped markers and are denoted by UL.

reported up to 8 at.%, while Ga has been incorporated up to 33 at.% into  $\alpha$ -In<sub>2</sub>O<sub>3</sub> [120]. The pseudo-hexagonal lattice constants (*a/c*) in the corundum-structured (Al,Ga,In)<sub>2</sub>O<sub>3</sub> thin films range between a = 4.7617 Å/c = 12.995 Å [113] for Al<sub>2</sub>O<sub>3</sub>, a = 4.9825 Å/c = 13.433 Å for Ga<sub>2</sub>O<sub>3</sub> [17], and a = 5.487 Å/c = 14.510 Å for In<sub>2</sub>O<sub>3</sub> [18]. Figure 5 presents the evolution of the *a*-lattice constant as a function of the composition for relaxed thin films [113, 115, 118], which follow Vegard's law. The linear fit of the *a*-lattice constant can be found in table 3. The slope in  $\beta$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> is much higher than for  $\beta$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> due to a higher relative percentage difference in the atomic radii of In with respect to Ga (14% larger) compared to Al to Ga (6.5% smaller).

#### 4.2. Monoclinic $\beta$ -gallia crystal structure

Monoclinic  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> belongs to space group *C2/m* [20] and the unit cell is formed by four Ga<sub>2</sub>O<sub>3</sub> molecules, where the Ga atoms occupy either the *O*<sub>h</sub> or the *T*<sub>d</sub> lattice site with a ratio of 1:1. By alloying  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> with In or Al, these cations prefer the *O*<sub>h</sub> lattice sites [92, 154]. After Al has occupied all *O*<sub>h</sub> lattice sites (50 at.%), the *T*<sub>d</sub> lattice sites are then also occupied [154]. There exist three possibilities of connections between the octahedrally and tetrahedrally ordered cations. In the [010]-direction the *T*<sub>d</sub> are connected with each other as well as the *O*<sub>h</sub>. The *O*<sub>h</sub> are also connected along the [102]-direction. In the remaining directions, there exists

**Table 3.** Dependence of the lattice constants of rhombohedral, monoclinic, orthorhombic, and cubic  $(Al,Ga,In)_2O_3$  thin films on the cation incorporation. The equations represent the linear fittings from figures 5–7 and [23, 158, 159].

Material	Lattice parameter
$\overline{\alpha}$ -(Al <sub>x</sub> Ga <sub>1-x</sub> ) <sub>2</sub> O <sub>3</sub>	a(x) = (4.983 - 0.225x) Å
$\alpha$ -(In <sub>y</sub> Ga <sub>1-y</sub> ) <sub>2</sub> O <sub>3</sub>	a(y) = (4.999 + 0.471y)  Å
$\beta$ -(Al <sub>x</sub> Ga <sub>1-x</sub> ) <sub>2</sub> O <sub>3</sub>	a(x) = (12.217 - 0.455x) Å
	b(x) = (3.039 - 0.128x) Å
	c(x) = (5.808 - 0.184x)  Å
	$\beta(x) = (103.88 + 0.415x) \text{ Å}$
$\beta$ -(In <sub>y</sub> Ga <sub>1-y</sub> ) <sub>2</sub> O <sub>3</sub>	a(y) = (12.241 + 1.332y)  Å
	b(y) = (3.046 + 0.325y) Å
	c(y) = (5.812 + 0.353y)
	$\beta(y) = (103.88 - 3.098y) \text{ Å}$
$\kappa$ -(Al <sub>x</sub> Ga <sub>1-x</sub> ) <sub>2</sub> O <sub>3</sub>	c(x) = (9.274 - 0.347x)  Å
$\kappa$ -(In <sub>y</sub> Ga <sub>1-y</sub> ) <sub>2</sub> O <sub>3</sub>	c(y) = (9.268 + 1.121y)  Å
$c-(Ga_zIn_{1-z})_2O_3$	a(z) = (10.113 - 0.803z) Å

only linkings between the  $T_d$  and  $O_h$  cation sites [156]. The oxygen atoms can occupy three different lattice sites, two of them, namely O(1) and O(2), are threefold and O(3) is fourfold coordinated.

Since only Ga<sub>2</sub>O<sub>3</sub> crystallizes in the  $\beta$ -phase, the solubility of Al and In in this structure is limited. The highest reported Al content in  $\beta$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> thin films is x = 0.61



**Figure 7.** Lattice constant *c* of  $\kappa$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> and  $\kappa$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> as a function of the alloy composition. The data was taken from: Hassa *et al* [144, 141], Kneiß *et al* [145], Nishinaka *et al* [143], Tahara *et al* [139], and Storm *et al* [140].

[128] and x = 0.78 in ceramic samples [157]. The maximum In incorporation into  $\beta$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> thin films is y = 0.35 [71] and y = 0.44 [23] in ceramic samples. The lattice constants of  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> are a = 12.214 Å, b = 3.037 Å, c = 5.798 Å and  $\beta = 103.83^{\circ}$  [20]. Figure 6 presents published lattice parameters of monoclinic (Al,Ga)<sub>2</sub>O<sub>3</sub> and (In,Ga)<sub>2</sub>O<sub>3</sub> alloys as a function of the Al or In content, respectively [23, 92, 137, 152, 154, 155]. The data points exhibit a linear dependency and thus follow Vegard's law. The fits of each lattice parameter are shown in table 3. Interestingly, for x = 0 the lattice constants are in close agreement with the values of binary  $\beta$ -Ga<sub>2</sub>O<sub>3</sub>, while for y = 0 the lattice constants a, b and c are 1%–1.7% higher. The angle  $\beta$  is for both alloys the same of about 103.88° fitting well to the binary value of 103.83° [20]. Extrapolations to x = 1 show a close agreement of the lattice parameters with those of monoclinic  $\theta$ -Al<sub>2</sub>O<sub>3</sub>, with the exception of the lattice parameter  $\beta$ , which should be nearly identical for both materials.

#### 4.3. Orthorhombic crystal structure

In the orthorhombic structure the  $T_d$  to  $O_h$  coordinated cations exhibit a ratio of 1:3 and are formed by six molecules in space group  $Pna2_1$ . Often the orthorhombic polymorph of Ga<sub>2</sub>O<sub>3</sub> is also denoted as  $\varepsilon$ -phase. Since some literature, probably Cora or Kneiß *et al*, the isostructurality to  $\kappa$ -Al<sub>2</sub>O<sub>3</sub> demonstrated, the orthorhombic polymorph is named  $\kappa$  and not  $\varepsilon$  [22, 69]. The Me<sup>3+</sup> cations can be arranged as pure  $O_h$  or mixed  $T_d$  and  $O_h$  layer along the [001]-direction or as zigzag ribbons consisting of edge-shared  $O_h$  and corner-shared  $T_d$  layers [22, 21]. The oxygen atoms arrange themselves as an ABAC pseudoclose-packed stacking [21].

Since the Al<sub>2</sub>O<sub>3</sub> can form an orthorhombic lattice, the whole composition range of  $\kappa$ -(Al<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> should be feasible. Actually the highest reported Al content on c-sapphire substrates is x = 0.46 [141], which can be significantly



**Figure 8.** Lattice constants of the rhombohedral, monoclinic and orthorhombic polymorph of  $(Al_xGa_{1-x})_2O_3$  and  $(In_xGa_{1-x})_2O_3$  as function of the alloy composition. The graphs are based on the equations depicted in table 3. The solid lines mark the maximum experimental cation ratio and the dashed lines are extrapolated to  $Al_2O_3$  (x = 1) and  $In_2O_3$  (y = 1).

increased up to x = 0.65 using a  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub> buffer layer between substrate and thin film [140]. For  $\kappa$ -(In<sub>y</sub>Ga<sub>1-y</sub>)<sub>2</sub>O<sub>3</sub> on csapphire a maximum In incorporation of x = 0.35 [144] was realized, up to now.

The lattice constants for  $\kappa$ -Al<sub>2</sub>O<sub>3</sub> are identified to be a = 4.8437 Å, b = 8.3300 Å and c = 8.9547 Å [21] and for  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub> as a = 5.046 Å, b = 8.702 Å and c = 9.283 Å [22]. The influence of the Al content [139–141] or rather In content [143–145] on the lattice parameter c is presented in figure 7. As for the monoclinic alloys causes the Al (In) incorporation a linear decrease (increase) of c according to Vegard's law. Linear fittings of the experimental values results in the equations listed in table 3. Assuming again x = 0 and y = 0, c fits well with the experimental result of binary  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub>. By extrapolating the lattice constant up to x = 1, 8.927 Å is obtained being in close agreement with binary  $\kappa$ -Al<sub>2</sub>O<sub>3</sub> [21], too.

#### 4.4. Cubic crystal structure

The cubic structure, also called bixbyite, is body-centered cubic (bcc) and belongs to the space group Ia3. The bcc unit cell consists of 16 molecules. The sixfold coordinated cations can occupy the Wyckhoff position 8b (cation lies on the space diagonal between two oxygen vacancies) or the Wyckhoff position 24d (within the bcc cell with the oxygen vacancies located on the surface diagonal), respectively. The ratio of the b to d cation positions is 8:24 in the unit cell. As substrates (100)ZrO<sub>2</sub> or (006)Al<sub>2</sub>O<sub>3</sub> are mostly used. The solubility limit of Ga atoms into phase pure cubic In<sub>2</sub>O<sub>3</sub> is 50 at.% [146, 147]. For higher Ga contents an additional phase, usually the monoclinic  $\beta$ -gallia and/or hexagonal InGaO<sub>3</sub> phase can be observed. The lattice parameter in binary  $In_2O_3$  is a = $10.117 \pm 0.001$  Å [158] and can be decreased by alloying with Ga [23, 159] following for the *a*-lattice constant Vegard's law presented in table 3.



**Figure 9.** Optical bandgap as function of the Al, In or Ga incorporation *x*, *y* or *z* for the (a) rhombohedral, (b) monoclinic, (c) orthorhombic and (d) cubic polymorphs of the group-III sesquioxides. The data were extracted for the  $\alpha$ -polymorph from [112, 115, 120], for  $\beta$ - from [122, 133, 134, 137, 151, 155, 160, 161], for  $\kappa$ - from [139–141, 143–145], and for the cubic phase from [134, 146, 147].

**Table 4.** Linear fits of the optical bandgaps in dependence on the Al incorporation x or In content y for the  $\alpha$ -,  $\beta$ -,  $\kappa$ - and cubic phase of (Al,Ga,In)<sub>2</sub>O<sub>3</sub>. The data are taken for  $\alpha$  from [115, 112], for  $\beta$  from [122, 133, 134, 137, 155, 160, 161], and for  $\kappa$  from [139–141, 143–145].

Material	Bandgap (eV)	
$\overline{\alpha - (Al_xGa_{1-x})_2O_3}$ $\beta - (Al_xGa_{1-x})_2O_3$ $\beta - (In_yGa_{1-y})_2O_3$ $\kappa - (Al_xGa_{1-y})_2O_3$	$E_{g}(x) = 5.25 + 3.31x$ $E_{g}(x) = 4.98 + 1.56x$ $E_{g}(y) = 4.99 - 2.32y$ $E_{r}(x) = 4.91 + 2.10x$	
$\kappa$ -( $\ln_x Ga_{1-x}$ ) <sub>2</sub> O <sub>3</sub> $\kappa$ -( $\ln_y Ga_{1-y}$ ) <sub>2</sub> O <sub>3</sub> $c$ -( $Ga_z In_{1-z}$ ) <sub>2</sub> O <sub>3</sub>	$E_{g}(x) = 4.91 + 2.16x$ $E_{g}(y) = 4.90 - 1.95y$ $E_{g}(z) = 3.73 + 0.56z$	

#### 5. Optical bandgap

One of the most important aspects of the group-III sesquioxides is the possibility of bandgap engineering in a broad range. Actually,  $Al_2O_3$  and  $Ga_2O_3$  are indirect semiconductors, but with such a small difference in the band-to-band transition that both behave much as direct bandgap semiconductors [3, 162]. For In<sub>2</sub>O<sub>3</sub> a distinct classification of direct or indirect bandgap is also possible and widely discussed. As introduced by Weiher and Ley, In<sub>2</sub>O<sub>3</sub> can exhibit an indirect, forbidden band-to-band transition of  $E_g^{\text{indirect}} = 2.62 \text{ eV}$  and a direct transition of  $E_g^{\text{direct}} = 3.75 \text{ eV}$  [13]. Further investigations of Walsh *et al* showed that the direct optical band-to-band transitions are parity-forbidden, resulting in an upper bandgap limit of 2.9 eV [163]. The first dipole allowed band-to-band transition can be observed at 3.7 eV, which could be experimentally confirmed [164, 13].

For  $Ga_2O_3$  the bandgap energy depends strongly on the respective formed polymorph. For instance, the bandgap of the monoclinic polymorph can range between 4.6 and 5.0 eV [3]. Due to the optical anisotropy, the bandgap depends strongly on the orientation and polarization [166]. The orthorhombic Ga<sub>2</sub>O<sub>3</sub> exhibits an optical bandgap of 4.9 eV [38, 55, 69] and the rhombohedral phase a slightly higher one of 5.2-5.3 eV [24, 46, 48, 58]. The optical bandgap of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> was found to be 8.7–8.8 eV [115, 167] and for binary  $\kappa$ -Al<sub>2</sub>O<sub>3</sub> no experimental bandgaps are available. Figure 9 summarizes experimental results of optical bandgaps as a function of the alloy composition for rhombohedral  $(\alpha)$ , monoclinic ( $\beta$ ), orthorhombic ( $\kappa$ ) and cubic polymorphs of (Al,Ga,In)<sub>2</sub>O<sub>3</sub> thin films. The linear fits of the separate polymorphs are summarized in table 4. The highest bandgap variance is observed in the rhombohedral  $\alpha$ -phase, since each sesquioxide can crystallize in the rhombohedral structure



**Figure 10.** Optical bandgap in dependence on the lattice parameter (a) *a* for rhombohedral, (b) *a* for monoclinic and (b) *c* for orthorhombic (Al,Ga)<sub>2</sub>O<sub>3</sub> and (In,Ga)<sub>2</sub>O<sub>3</sub>. The solid line presents linear fittings of recently published data. The dashed lines shows the extrapolation to binary Al<sub>2</sub>O<sub>3</sub> and In<sub>2</sub>O<sub>3</sub>. The lattice parameters and bandgap energies for  $\alpha$ -,  $\beta$ - and  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub> as well as for  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> and In<sub>2</sub>O<sub>3</sub> are taken from table 1.



**Figure 11.** Optical bandgap in dependence on the cation incorporation *x* or *y* based on table 4 for the rhombohedral (black), monoclinic (blue), orthorhombic (red) and cubic polymorphs (orange) of the sesquioxides. The solid lines represents the maximum reported cation incorporation for the distinct polymorphs and the dashed lines are extrapolated to the binary sesquioxides. Reprinted by permission from Springer Nature Customer Service Centre GmbH: [Springer Nature] [Springer eBook] [165], (2020).

allowing bandgap engineering between 3.7 eV [120] and 8.7 eV [115], except a range of  $4 < E_g < 4.95$  eV [120]. For the  $\beta$ - and  $\kappa$ -phase alloys is the bandgap engineering limited by the solubility and therefore phase separation.

Using the linear fits (see table 4), extrapolations to the current maximum Al and In incorporation allows declaration of the possible bandgap engineering. It follows that for  $\beta$ -(Al,Ga,In)<sub>2</sub>O<sub>3</sub> thin films the bandgap can be varied between approximately 4.2 and 5.9 eV corresponding to an In content of 35 at.% and an Al content of 61 at.% into  $\beta$ -Ga<sub>2</sub>O<sub>3</sub>. For the ternary alloys of the orthorhombic structure ensues a similar range of about 4.25–6.2 eV (35 at.% In, 65 at.% Al).

For phase pure cubic  $(Ga_zIn_{1-z})_2O_3$  amounts the maximum reported Ga incorporation z = 0.5 [146, 147] leading to a small bandgap variation of 3.7-4.05 eV. Figure 11 illustrates the actual possible and extrapolated bandgap energies of all polymorphs discussed in dependence on the alloy compound. In addition, figure 10 summarizes the data fits from tables 3 and 4 for  $\alpha$ -,  $\beta$ - and  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub> alloyed with Al or In and represents the relation of the optical bandgap as a function of the lattice parameter. For this purpose, these equations were resolved according to x/y and then put on a par. Assuming that monoclinic and orthorhombic (Al,Ga,In)<sub>2</sub>O<sub>3</sub> thin films are achievable up to binary  $Al_2O_3$  and  $In_2O_3$ , the plots ( $E_g$ vs. x/y and  $E_{q}$  vs. lattice constant) were extrapolated up to the maximum and minimum possible values of x = 1 or y = 1(dashed lines in figure 11), respectively. As a result of these extrapolations for the monoclinic phase a maximum bandgap range of 2.67-6.54 eV and for the orthorhombic polymorph a range of 2.95-7.01 eV. Compared with experimental results of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> (8.7–8.8 eV [115, 167]), the extrapolated monoclinic and orthorhombic Al<sub>2</sub>O<sub>3</sub> bandgaps are much smaller. The extrapolated values for  $\beta$ -In<sub>2</sub>O<sub>3</sub> reflect the value of the parity-forbidden direct bandgap of cubic In2O3, whereby the extrapolated value of  $\kappa$ -In<sub>2</sub>O<sub>3</sub> is near the fundamental bandgap [163].

In contrast, the alloy of cubic  $In_2O_3$  with Ga exhibits direct band-to-band transitions with a possible bandgap range of 3.7 eV to an extrapolated maximum of 4.28 eV for cubic Ga<sub>2</sub>O<sub>3</sub>. A possible reason for the strong difference of the extrapolated values for  $\beta$ - and  $\kappa$ -In<sub>2</sub>O<sub>3</sub> with the actual cubic In<sub>2</sub>O<sub>3</sub> bandgaps can be that the calculation for the  $\beta$ - and  $\kappa$ -polymorph starts at the Ga<sub>2</sub>O<sub>3</sub> of the phase diagram where no parity-forbidden transitions were reported. Since the graphs intersect each other at an average In content of 40 at.%, this could indicate the critical cation composition where phase separations proceeds.

However, for  $\alpha$ -(In,Ga)<sub>2</sub>O<sub>3</sub> and cubic (Ga,In)<sub>2</sub>O<sub>3</sub> thin films, a bandgap bowing of b = 1.69 eV [168] can be observed

resulting in a minimum bandgap of 3.7 eV [113, 120, 146]. Such a bowing cannot be excluded for the monoclinic and orthorhombic polymorph, so it should be kept in mind for higher potential In contents.

#### 6. Summary and outlook

In this report, we pointed out that for the group-IIIsesquioxides, oxygen pressure has a strong influence on the alloy composition and cation incorporation of PLD grown thin films. At low oxygen pressures, volatile suboxides are formed and desorb. Due to different dissociation energies of the Me– O bonds, the provided cations are incorporated with different preferences. The dissociation energy of the Al–O bond is higher as the Ga–O bond, which is higher than the In–O bond, resulting in a preferentially incorporation of Al into the (Al,Ga)<sub>2</sub>O<sub>3</sub> alloy or Ga into the (In,Ga)<sub>2</sub>O<sub>3</sub> alloy.

Besides, we have reviewed the dependence of lattice constants and optical bandgap on the group-III sesquioxide alloy composition for the rhombohedral, monoclinic, orthorhombic, and cubic crystal structures. The summarized data revealed different solubility limits of the distinct polymorphs of  $(Al_xGa_{1-x})_2O_3$  and  $(In_yGa_{1-y})_2O_3$  due to different ground state crystal structures of the binary materials. For instance, in the rhombohedral structure the cation incorporation of Ga in  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> or Al in  $\alpha$ -Ga<sub>2</sub>O<sub>3</sub> is possible in the entire compositional range, while Ga in  $\alpha$ -In<sub>2</sub>O<sub>3</sub> was only reported up to 33 at.% and In in  $\alpha$ -Ga<sub>2</sub>O<sub>3</sub> has a solubility limit of around 8 at.%. For the monoclinic and orthorhombic polymorphs of Ga<sub>2</sub>O<sub>3</sub>, which are not reported for binary Al<sub>2</sub>O<sub>3</sub> and  $In_2O_3$ , the maximum reported cation incorporations are similar: the Al content reaches a maximum of 61-65 at.% and In is included up to 35 at.% in  $\beta$ - or  $\kappa$ -Ga<sub>2</sub>O<sub>3</sub>. The highest reported Ga content in the cubic In<sub>2</sub>O<sub>3</sub> phase was reported to be 50 at.%. Starting from Ga<sub>2</sub>O<sub>3</sub> the lattice constants decreases (increases) with increasing Al (In) incorporation and follow for all reviewed polymorphs Vegard's law. We also reviewed the evolution of the bandgap, which leads to bandgap ranges from 3.7–4 and 4.95–8.7 eV for the  $\alpha$ -polymorph, 4.2–5.9 eV for the  $\beta$ -polymorph, 4.2–5.7 eV for the  $\kappa$ -polymorph, and 3.7-4.05 eV for the cubic phase. The bandgaps and corresponding miscibility limits are summarized in figure 12 for all polymorphs discussed.

Future studies and investigations should continue to focus on expanding the phase limits of the ternary alloys for each polymorph of the group-III sesquioxides. Since the  $\alpha$ -phase can be stabilized across the entire composition range of the (Al,Ga)<sub>2</sub>O<sub>3</sub> alloy and this is also—at least theoretically feasible for the (In<sub>x</sub>Ga<sub>1-x</sub>)<sub>2</sub>O<sub>3</sub> alloy, this structure is particularly suitable for the realization of wavelength-selective photodetectors, such as deep UV-photodetectors or QWIP's. With the availability of native  $\beta$ -Ga<sub>2</sub>O<sub>3</sub> substrates, alloys of this phase are a prime candidate for the realization of high performance power devices and possibly QWIP's. The  $\kappa$ -phase is due to it is spontaneous polarization especially interesting for confining extremely high 2DEG densities, which can be potentially exploited in HEMT's. The



**Figure 12.** Current miscibility limits and corresponding optical bandgap energies for the rhombohedral  $\alpha$ -, monoclinic  $\beta$ - and orthorhombic  $\kappa$ -polymorph of  $(Al_xGa_{1-x})_2O_3$  and  $(In_yGa_{1-y})_2O_3$  as well as for cubic  $(In_yGa_{1-y})_2O_3$ . Reprinted by permission from Springer Nature Customer Service Centre GmbH: [Springer Nature] [Springer eBook] [165], (2020).

emphasis should also remain on optimizing or realizing the electrical conductivity of all polymorphs of  $(In_xGa_{1-x})_2O_3$  or  $(Al_xGa_{1-x})_2O_3$ , respectively.

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