## Simultaneous Measurement of $\nu_{\mu}$ Quasielasticlike Cross Sections on CH, C, H<sub>2</sub>O, Fe, and Pb as a Function of Muon Kinematics at MINERvA

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This Letter presents the first simultaneous measurement of the quasielasticlike neutrino-nucleus cross sections on C, water, Fe, Pb, and scintillator (hydrocarbon or CH) as a function of longitudinal and transverse muon momentum. The ratio of cross sections per nucleon between Pb and CH is always above unity and has a characteristic shape as a function of transverse muon momentum that evolves slowly as a function of longitudinal muon momentum. The ratio is constant versus longitudinal momentum within uncertainties above a longitudinal momentum of 4.5 GeV/c. The cross section ratios to CH for C, water,

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and Fe remain roughly constant with increasing longitudinal momentum, and the ratios between water or C to CH do not have any significant deviation from unity. Both the overall cross section level and the shape for Pb and Fe as a function of transverse muon momentum are not reproduced by current neutrino event generators. These measurements provide a direct test of nuclear effects in quasielasticlike interactions, which are major contributors to long-baseline neutrino oscillation data samples.

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The charged-current quasielastic (CCQE) neutrino interaction (i.e.,  $\nu_{\mu}n \rightarrow \mu^{-}p$ ) contributes the majority of selected signal interactions in current accelerator-based neutrino oscillation experiments [1-6]. Because the interaction's final state is simple, the lepton flavor is easily identified. The neutrino energy may be estimated assuming two-body kinematics where the target is assumed to be a neutron at rest. However, for those nuclei in use in oscillation experiments these assumptions can bias neutrino energy reconstruction because of finite initial neutron momentum inside the nucleus [7]. In addition, quasielastic scattering can be mimicked by other processes; for example, when final-state particles are absorbed in the nucleus. These biases are already significant in current experiments [1-4] and risk becoming dominant uncertainties in the future, for example in DUNE [5] and Hyper-Kamiokande [6]. Oscillation experiments may also use different target nuclei for their near detector than for their far detector [1], so direct measurements on different nuclei provide insight on biases that might be introduced by that choice.

The MINERvA experiment published a measurement of quasielasticlike cross sections on a variety of nuclei at a mean neutrino energy of 3 GeV [8], using interactions where both a final-state muon and proton were identified. This Letter describes a measurement made with a dataset that is over 20 times as large due to the following factors: the mean neutrino energy is higher by a factor of 2, the integrated number of protons on target is larger by a factor of 4, and the requirement for a final-state proton has been removed. The increased statistics allow a more detailed probe of this process.

MINERvA recently measured charged-current chargedpion production on different nuclei [9]. Using the same neutrino beam as used here, MINERvA found that the ratio of pions produced on Fe or Pb compared to scintillator is lower than predicted by current models. This has implications not only for the background, but also for the signal in this analysis. Neutrino interactions in which pions are produced but absorbed in the nucleus can be quasielasticlike and are thus included as a signal process. In addition, due to the possibility of interactions with nucleon pairs, the quasielasticlike definition allows any number of protons and neutrons in the final state.

The MINERvA detector [10] consists of a nuclear target region of several thin passive targets interspersed with 1.7-cm-thick active scintillator planes, followed by a

scintillator-only region followed by electromagnetic and hadronic calorimetry. The MINOS near detector [11], located 2-m downstream of MINERvA, measures the charge and momentum of final-state muons. MINERvA's targets include regions made up of C, Fe, Pb, and water. The solid targets are configured in such a way that the total amount of passive material a particle traverses between the start of the interaction and the scintillator-only region  $(in g/cm^2)$  is approximately the same. The water target is a flattened circular neoprene balloon that is between 17- and 24-cm thick in the beam direction. The detector is modeled using a hit-level GEANT4-based simulation overlaid with random beam data to simulate beam-related accidental activity. The simulation includes the time dependence of both the proton beam intensity and the configuration of the water target.

The NuMI beam is produced by a 120-GeV proton beam incident on a two-interaction-length graphite target followed by two parabolic focusing horns and a 675-m decay pipe and 200 m of earth to shield the tertiary muons. For these data, the horn currents are set to focus positively charged pions, creating a neutrino-dominated broadband beam with a peak energy of 6.5 GeV.

The beam line is modeled with a GEANT4-based [12,13] simulation (G4NuMI [14] version 6, built against GEANT version v.9.4.p2). There are known discrepancies between measurements and GEANT4 predictions of pion production from proton-on-carbon interactions relevant to NuMI flux predictions [14]. MINERvA corrects these predictions using hadron-production data. In addition, measurements of neutrino-electron ( $\nu - e$ ) scattering [15] and interactions with low recoil energy [16] are used to constrain the flux prediction. This analysis uses data that correspond to  $10.61 \times 10^{20}$  protons on target (POT), where the first (second) half of the exposure was with the water target empty (full) to allow the nonwater background interactions to be measured directly and subtracted from the full target sample.

The GENIE 2.12.6 event generator [17] is used to simulate neutrino interactions on nuclei. For quasielastic scattering on nucleons, the Llewellyn-Smith formalism is used [18]. Nuclear effects are incorporated by using a Bodek-Ritchie high momentum tail [19] in the Fermi momentum distribution of the initial-state nucleons. The default GENIE interaction model is adjusted to match previous MINERvA data via a GENIE tune v1 (MnvGENIEv1), which includes three additional modifications. First, the Valencia random phase approximation correction, considered as a "weak nuclear screening" [20,21] for a Fermi gas [22,23], is added as a function of neutrino energy and three-momentum transfer. Second, the prediction for multinucleon scattering given by the Valencia model [24–26] in GENIE 2.12.6 is added and modified with an empirical fit [27] based on previous MINERvA data on CH. The modification increases the integrated two-particle two-hole (2p2h) interaction rate by 49%. This same fractional increase per proton-neutron pair is applied for all nuclei. Finally, nonresonant pion production is reduced by 57% to agree with a fit to measurements on deuterium [28].

Interactions are selected by requiring a muon candidate that originates in the MINERvA detector and is reconstructed in the MINOS near detector, but no requirement on the number of proton tracks. Interactions with electron candidates (resulting from the pion to muon to electron decay chain, "Michel's") within any 600-mm-long, 600-mm-diameter cylinder centered on the interaction vertex or any track endpoint are rejected [29]. Backgrounds and efficiencies are determined separately for the samples with and without the identified proton tracks. To further reject interactions containing charged pions, any nonmuon reconstructed track is required to satisfy proton identification cuts based on the energy deposition pattern. To remove interactions with neutral pions, a cut is made requiring no more than one isolated cluster of energy in the detector.

The muon momentum is found by the addition of the momentum determined by range inside the MINERvA detector plus the momentum determined by range or curvature inside MINOS [30]. The muon angle is measured in the MINERvA detector. To address the MINOS acceptance, only interactions with muons reconstructed within  $17^{\circ}$  of the neutrino beam and with momenta above 1.5 and below 40 GeV/*c* are retained. The cross sections we report are defined as any interaction with a muon in the final state, where the muon has an angle of no more than  $17^{\circ}$  and a momentum between 2 and 20 GeV/*c*. For these interactions, any number of nucleons is allowed, but no photons above 10 MeV (to accommodate nuclear excitations) and no mesons.

There are two primary categories of backgrounds: interactions that originated in the scintillator, but whose vertex is misreconstructed in a target, and nonquasielasticlike interactions that are correctly reconstructed in a nuclear target but are incorrectly reconstructed as quasielasticlike. Predictions for both backgrounds are constrained by comparing the data to the simulation in sidebands. The background between one nuclear target and another at the same vertex z location is small due to fiducial volume cuts and is constrained by interactions in the other target.

The prediction for the scintillator background can be constrained by the ratio between the data and the simulation for interactions reconstructed in the scintillator surrounding



FIG. 1. Reconstructed vertex location in the upstream region of MINERvA along the detector axis shown in data and simulation in the full water target configuration. Interactions correspond to those with two reconstructed tracks.

each of the nuclear targets. Figure 1 shows the reconstructed interaction vertex position as a function of distance along the detector axis for all interactions that have a reconstructed muon in MINOS and an additional reconstructed track: the interactions in the denser nuclear target material show up as clear peaks in this distribution, and the normalization of the scintillator background comes from the interactions at least one scintillator plane away from each target.

The second category of backgrounds comes from interactions that take place in the target of interest, but are not quasielasticlike. In this case, one or more neutral or charged pions have been misidentified as a proton or not seen at all. The single neutral pion background is constrained by MINERvA's earlier measurement of neutral pion production [31]. To determine the backgrounds from other neutrino interaction channels, two different sidebands are used where the data are compared to the simulation. The first sideband requires a Michel electron to provide a sample enriched with charged pions; the second requires at least two extra clusters of energy away from the interaction vertex to provide a sample enriched in neutral pions, as in Ref. [32].

Figure 2 (top) shows the data and simulation in the two sidebands for the Pb target as a function of transverse momentum ( $P_T$ ) in the peak longitudinal momentum ( $P_{\parallel}$ ) region (4.5 <  $P_{\parallel}/\text{GeV}/c < 5.5$ ). The top left plot shows the Michel electron sideband, and the center plot shows the interactions with two or more clusters of energy. The plots on the bottom show the data and prediction with the signal prediction tuned to match the data in that region in the Pb (left) and scintillator (right). The background levels from nonquasielasticlike interactions are 36% in the scintillator and are 33%–45% in the nuclear targets, with the lowest background in the Pb targets. The fact that the physics backgrounds are lower in Pb than in the lighter nuclei stems from the fact that pions produced in heavier nuclei are more likely to be absorbed before leaving the nucleus [9].

After background subtraction, there are  $1 \times 10^6$  interactions in the scintillator tracker region, 25 000 interactions



FIG. 2. Top: data and prediction for the (left) single Michel electron sideband, (right) extra energy cluster sideband for Pb. Bottom: signal region in Pb (left) and CH (right), all after the backgrounds and the signal have been tuned, for the peak longitudinal momentum  $(P_{\parallel})$  bin. The scintillator background to Pb has been constrained and subtracted.

in the C target (used as a control region), and 20000, 92 000, and 124 000 interactions in the water, Fe, and Pb targets, respectively. The analysis unfolds the distributions to correct for detector resolution using the D'Agostini prescription [33,34] and then corrects each of the different target regions for efficiency. Finally, the cross section is found by dividing by the number of target nucleons and by the total integrated flux appropriate for each target. Figure 3 shows the cross section in data and simulation in all five target materials as a function of  $P_T$  for one  $P_{\parallel}$  bin. There is a clear excess above the prediction that grows as a function of the mass number A and is consistent across  $P_{\parallel}$ , as shown in Fig. 4. The prediction includes not only quasielastic and multinucleon interactions, but also interactions where some original final-state particles were absorbed in the nucleus, for example resonance production (Res) and Deep Inelastic Scattering (DIS). The quasielastic interactions dominate at the highest  $P_T$ , but at low  $P_T$  there are significant contributions from both 2p2h interactions and pion production followed by absorption.

The neutrino flux changes at the few percent level as a function of position across the front face of the MINERvA detector [16]. The nuclear targets do not all have the same integrated neutrino flux because each target covers only a part of the hexagonal shape of the scintillator planes. In order to calculate the cross section on each nuclear target material, a different flux must be used for each material [9]. The cross sections shown in Fig. 3 have been calculated using this prescription. The systematic uncertainties in the absolute cross sections are dominated in most bins by the flux uncertainties.



FIG. 3. Cross section versus transverse muon momentum  $(P_T)$  in the highest statistics  $P_{\parallel}$  bin in data and simulation for the nuclear target materials and for scintillator. Inner (outer) error bars represent the statistical (total) uncertainties.

In order to minimize the flux uncertainties, the ratio of cross sections between a given target material and scintillator are reported, whereby construction the incident neutrino flux is the same to better than a percent in both targets. To do this, the analysis extracts the cross section in the scintillator in 12 different transverse wedges of the detector and then the scintillator cross section used in the ratio is the one calculated using the linear combination of wedges that most closely matches the illumination of each target material.

Systematic uncertainties on the cross section measurement arise from three different sources: the flux, neutrino interactions, and the MINERvA detector (both the detector response and the target masses). These uncertainties are evaluated using a multiuniverse technique, where the cross section is reextracted after varying each source of uncertainty, and the correlations between different bins (and different nuclear targets) are taken into account. The flux uncertainty comes from uncertainty in hadron production and focusing effects and is constrained at 3.9% using neutrino-electron scattering interactions from the same exposure [15]. Neutrino interaction uncertainties are dominated by the modeling uncertainties in background processes, in particular, the final-state interaction uncertainties. Detector uncertainties are dominated by uncertainties in muon reconstruction, which are small, but increase at high  $P_T$  where the cross section is falling steeply and small changes in the muon energy scale have a large effect on the accepted interactions. Because the systematic uncertainties are highly correlated between different targets, there is significant reduction of the total uncertainty in the cross section ratio measurements.

The systematic uncertainties in the absolute cross sections, shown in the Supplemental Material [35], are dominated by the flux uncertainties and the muon energy scale. Those uncertainties cancel to first order when taking



FIG. 4. Quasielasticlike cross section ratios to scintillator versus muon momenta on Pb, Fe, water, and C. The points are the data and the solid lines are the predictions from the model described in the text.

ratios between the target material and the scintillator target, and the remaining largest systematic uncertainties come from the reconstruction uncertainties that do not cancel, for example, those from final-state interactions in the target nuclei.

The systematic and statistical uncertainties on the cross section ratios, also shown in the Supplemental Material [35], are of comparable size in the most populated longitudinal momentum bin; in other bins, the uncertainty is dominated by the statistical uncertainty. Since most of the neutrino momentum is forward, the broad neutrino energy beam populates the  $P_{\parallel}$  bins between 3.75 and 6.5 GeV/*c*. In most kinematic regions, the cross section ratio uncertainty is well below ten percent.

Figure 4 shows the measurement and prediction for ratios of the cross sections per nucleon as a function of  $P_T$ for different  $P_{\parallel}$  bins. Each panel in the plot shows the ratio for Pb, Fe, water, and C compared to scintillator. The ratios themselves grow as a function of mass number, as expected, since the higher A nuclei have a higher neutron to nucleon ratio. However, the discrepancy with the base model also grows as a function of mass number. The cross section ratio between Pb and CH changes dramatically as a function of  $P_T$  and less dramatically as a function of  $P_{\parallel}$ . This indicates that the size of the nuclear effects varies more as a function of momentum transfer than as a function of neutrino energy. The cross section ratio between Fe and CH appears flatter as a function of  $P_T$  and  $P_{\parallel}$ , with a scaling per nucleon of about 1.4-1.5. MINERvA's underlying model, which was not tuned to Fe or Pb data, predicts a ratio that is closer to 1.2.

The discrepancy between data and simulation at high  $P_T$ implies that the total quasielasticlike cross section scaling versus A is higher than modeled, and that effect increases with increasing momentum transfer. The discrepancy at low  $P_T$  does not appear to grow with  $P_{\parallel}$ ; this implies that the A dependence of interactions coming from 2p2h and/or pion



FIG. 5. Comparison between several models for quasielasticlike scattering and the data on the Pb to CH cross section ratio, along with the  $\chi^2$  between each model and the data.

absorption is underpredicted, although there is not a strong energy dependence. The A scaling for single pion production on Fe and Pb has been measured to be lower than predicted [9]. This could come from more pion absorption than current models predict, which would then present as higher A scaling for quasielasticlike interactions that result from pion absorption. The cross section ratios between water and scintillator appear to be consistent with unity with no significant dependence on the muon kinematics seen at the 10% level, as shown in Fig. 4.

Figure 5 shows the cross section ratios for Pb/CH compared to different model choices in GENIE and NuWro [36]. A comparison to GiBUU [37], which uses a microscopic cascade model to describe final-state interactions, is also shown. None of the generator predictions are in good agreement with the data. Different final-state interaction models in GENIE change in the cross section ratio prediction, especially at high  $P_T$ . The data prefer GENIE's hA model, which approximates intranuclear rescattering as a single effective interaction within the nucleus, to its hN model, which is a microscopic cascade model. However, the overall performance of GiBUU in Fig. 5 may indicate that models of the latter type are better suited to characterize pion intranuclear absorption in heavy nuclei.

The difference in *A* scaling that arises between using the relativistic Fermi gas with the Bodek-Ritchie tail (BRRFG) and the local Fermi gas (LFG) initial-state nucleon models is much smaller than what arises from different final-state interaction models in GENIE. This may be because the choice of BRRFG or LFG only affects the quasielastic process and not 2p2h or resonance production. Changing the initial nucleon state makes a larger change in the NuWro model, where the data prefer the spectral function (SF) over the LFG treatment, although neither agrees as well with the data as the GENIE hA models.

MINERvA has measured quasielasticlike cross section ratios and sees evidence of scaling as a function of A that is not constant over the momentum transferred to the nucleus and not predicted by any generators considered. MINERvA's measurement of pion production on these same nuclei [9] implies that, for higher *A* nuclei, more pions are being absorbed compared to what one would predict given the pion production measured on CH. These measurements combined provide key benchmarks for the field's description of how the nucleus impacts neutrino interactions.

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