

CO₂/CH₄ separation by means of Matrimid hollow fibre membranes

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Abstract CO₂/CH₄ mixtures separation was investigated using Matrimid[®]5218 hollow fibre membranes and measuring the membrane flux feeding singly CH₄ and CO₂ and their mixtures, with CH₄ concentration ranging from 5 to 70 %_{molar}. Specific attention was paid to membrane properties at a high temperature (up to 75 °C) and feeding humidified streams, not yet particularly investigated, in a pressure range 400–600 kPa. The membrane properties were restored when water vapour was removed and temperature decreased stating the excellent hydro-thermal stability of these membranes. Maps of the separation performance were also calculated for a range of operating conditions wider than the experimental one paying specific attention to the feed/permeate pressure ratio further to membrane selectivity and permeance. Single and multi-stage membrane separation systems were investigated using these maps. The prepared Matrimid[®]5218 hollow fibres showed very good performance in terms of flux and selectivity for temperatures up to 60 °C, also in steam saturated conditions, allowing a methane concentration meeting the specification for its injection into the grid.

Keywords CO₂/CH₄ separation · Hollow fibre membrane · Matrimid[®]5218 · Membrane performance maps

Introduction

CO₂ is significantly present in mixtures where CH₄ is the major and valuable component. CH₄ is largely utilized fuel for domestic and automotive uses, electricity and power generation, owing to its large production and after its concentration [1]. Natural gas mainly contains CH₄ (60–90 %) and undesired compound such as CO₂ (4–35 %) and H₂O (5–10 %) [2, 3]. CH₄ (50–70 %), CO₂ (30–50 %) and H₂O (5–10 %) are the main components of biogas [4]. The presence of CO₂ not only reduces the calorific power, but increases the costs for gas compression and transport. The removal of CO₂ from CH₄ mixtures is, thus, very important in several industrial processes such as biogas upgrading or natural gas sweetening. To fit the targets for injecting the gas into the natural gas grid [1, 5], CO₂ concentration has to be lowered down to ca. 2–4 % (Table 1) [6–8]. In addition, a cleaning process is required for the removal of the other inert (e.g. N₂), dangerous (e.g. H₂O) and trace of harmful (e.g. H₂S) components for the environment and gas grid (Table 1). Conventional industrial methods used for CO₂ removal include processes such as adsorption [8], water scrubbing [9] and absorption [10].

Usually, the sweetening is achieved by means of absorption with an aqueous alkanolamine solution that has as main drawback the tendency to equipment corrosion and to lose amine properties by degradation increases [11].

As an alternative membrane, separation processes generally offer several advantages over the above-mentioned conventional separation techniques including low capital cost, ease of processing, small footprint area, high energy efficiency and ease of preparation and control [12–14].

To use the membranes, they have to exhibit high separation performance in real condition. Moreover, they have to show important characteristics such as thermal,

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Table 1 Targets for injecting the gas into the natural gas grid [1]

Component	Specification		
	Germany	Austria	US
CO ₂ (%)	<2–4	<2–4	<2–4
Water	<dew point	<dew point	<120 ppm
H ₂ S (ppm)	<3	<4	<3.7
O ₂ dehydrated gas networks (%)	<3	<4	<0.2–1
O ₂ non-dehydrated gas networks (%)	<0.5	<0.5	<0.2–1
Total inert gases (N ₂ , He) (%)	<4	<4	<4

mechanical, chemical resistance and durability, also in the presence of harsh environments, reproducibility at a high scale level, easy handling, etc., to be suitable for industrial use.

Recently, Basu et al. [9] and Zhang et al. [15] published two reviews reporting the membrane materials used for CO₂/CH₄. Cellulose acetates [6] and polyimides [16, 17] exhibit the best combination of permeability and selectivity. Cellulose acetate-based membranes for CO₂/CH₄ separation have become commercial, since the mid-1980s. These membranes make up to 80 % of the market for membranes in natural gas processing, and because of their wide industrial acceptance have become an industry standard for comparison purposes. Cynara [18] and UOP Separex [19] are the two major membrane manufacturers currently supplying cellulose acetate-based modules as hollow fibres and spiral wound, respectively. However, cellulose acetate membranes are sensitive to water vapour and a stream pre-treatment is necessary to use them for the treatment of these gas streams [7].

Polyimide hollow fibre membranes are an alternative to cellulose acetate, because they combine excellent thermal and chemical stability and show a high water resistance [20] in biogas upgrading. They are commercialized by UBE Industries [21] and Air Liquide Medal [22].

In this work, Matrimid[®]5218 asymmetric hollow fibre membranes were prepared by means of the phase inversion dry-jet wet spinning technique [23]. The choice of hollow fibre configuration, among the various possible membrane configurations, was made owing to their high surface/volume ratios, excellent mechanical strength, and low production costs and reduced overall size of the equipment (footprint).

Many studies [24–31] can be found in the open literature on the use of polyimides for the membranes preparation; in them, the mass transport properties were usually evaluated feeding single gas such as CO₂, CH₄, N₂, H₂, O₂ and mixtures of CO₂/CH₄ or CO₂/N₂ in the temperature range 25–75 °C. Most of the studies were also focalized on the improvement of the separation properties of these

membranes by different blends [24, 25] or the addition of fillers [26–28] or introducing new preparation techniques and post-treatments [29–31] for improving durability and mechanical and thermal resistance.

In addition, in real applications, almost all the streams contain water vapour. Even though, it is usually removed by dehydration processes by upfront units; in this work, it was present in the feed stream also for demonstrating that the water removal step is not a mandatory requirement before the separation of gases, since the membrane does not suffer any problem related to the water present in large concentration too. Such a solution, lowering the flow rate of the stream to be dehydrated, would reduce the amount of water to be removed. Thus, a membrane integrating separation has a freedom degree, for placing the dehydration unit, greater than the one in conventional separation cycles. The effect of vapour on the mass transport properties of the membranes is only partially investigated in the literature since, generally, the majority of studies refers to the transport properties measured in dry condition, usually considering single gases. Chenar et al. [32] and Scholes et al. [33] studied the effect of water vapour on the performance of polyimide hollow fibre membranes at 25–35 °C.

Investigations on mass transport of polyimides membrane coupling humidified feed mixtures with a higher temperature range are still missing in the open literature, at our knowledge. Therefore, this work proposes and discusses separation performance of prepared Matrimid[®]5218 membranes feeding humidified gas mixture also in the temperature range 50–75 °C.

On the basis of the previous considerations, the hollow fibre membrane transport properties were evaluated using, in addition to single gases and dry condition, humidified CH₄:CO₂ mixtures up to 75 °C. The experiments were carried out in a pressure range of 400–600 kPa which is a typical range of biogas upgrading. The higher pressure required by the natural gas sweetening is beyond the aim of this work.

In addition, the experimental data obtained were used as input data for a simulation analysis devoted to investigate the capability of these membranes to separate/purify methane from these streams. In particular, performance maps were developed with which the purity and recoveries of both retentate and permeate streams were predicted in a wider range of operating conditions with respect to the ones used at laboratory scale.

Materials and experimental methods

Materials

Matrimid[®]5218 was supplied by Huntsman Advanced Materials American, the Woodlands (USA). *N*-Methyl-2-

Table 2 Operating conditions used for gas separation measurements

Temperature (°C)	25, 50, 60, 75
Pressure (kPa)	Feed/retentate: 400, 500, 600 Permeate: 100
Feed flow rate	24 dm ³ (STP) h ⁻¹
Relative humidity (%)	0, 50 and 100
Feed composition	Single gases: CO ₂ (purity of 99.99 %) and CH ₄ (purity of 99.99 %)
	CH ₄ :CO ₂ mixtures (molar composition, %)
	50:50
	70:30
	5:95

STP: 0 °C and 100 kPa

pyrrolidone (purity of 99 %) was purchased from VWR International PBI (Italy). The bi-components, Stycast 1266, epoxy resin was used for potting fibres in the preparation of modules, were purchased from Emerson & Cuming (Belgium). Tap water was used as the external coagulant and distilled water was used as the bore fluid. CO₂ and CH₄ used in as single gas had a purity of 99.99 %; they were mixed for producing the mixtures as reported in Table 2.

Hollow fibre preparation

The hollow fibre membranes preparation was carried out according to the dry-jet wet spinning technique. Details on the preparation of the polymer solution (dope), on the spinning setup and on membrane modules were reported in a previous paper [20]. Membrane modules were prepared with the fibres produced, assembling ten fibres 20 cm long for a total membrane area of 52 cm². The skin dense layer being on the outer side of the fibres, the membrane area was calculated taking the external diameter of the fibres.

Mass transport properties evaluation

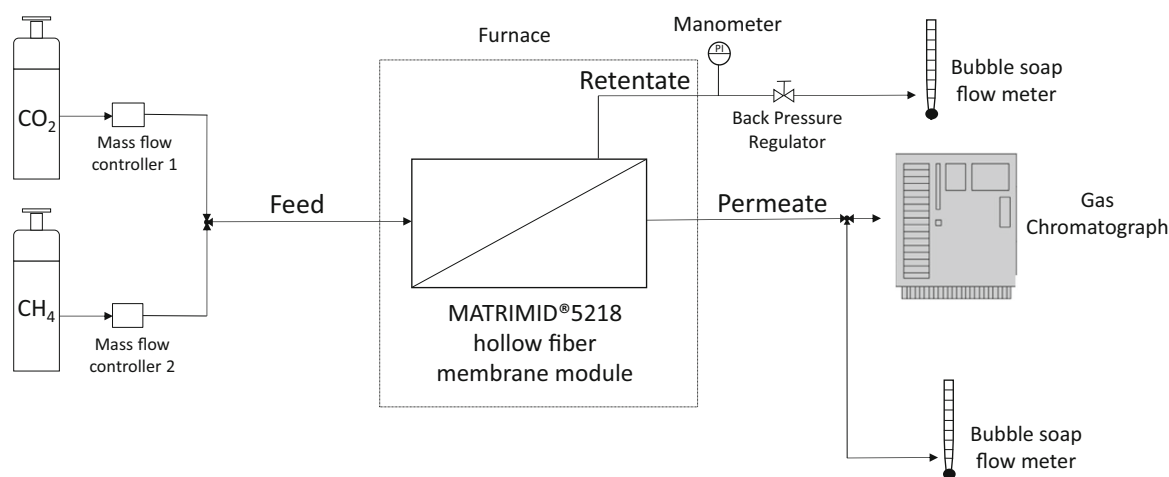
The mass transport properties of the hollow fibre membrane modules were measured with single gases, CH₄ and CO₂, and their mixtures, referred to as molar ratio, CH₄:CO₂ = 50:50, CH₄:CO₂ = 70:30 and CH₄:CO₂ = 5:95. All measurements were carried out at different pressures, temperatures, and relative humidity as reported in Table 2.

During the gas permeation measurements, the modules which have two inputs (feed and retentate) and one output (permeate) were placed in a furnace to keep under control the temperature. The feed and retentate pressures were measured by manometers and their flow rates were measured by bubble soap flow meter.

The gas streams were analysed by an Agilent GC 6890 equipped with two parallel analytical lines, identified as front and back. This means that it was equipped with two sampling valves, two detectors (TCD), and two series of columns (HPLLOT + molesieve). The temperature was 120 °C and 150 °C for both front and back sample valves and detectors, respectively. The oven temperature was kept at 50 °C. Column 1, an HPLLOT, operated at 123 kPa (17.781 psi) under a carrier gas flow rate of 7.08 mL min⁻¹, whereas column 2, a molesieve, operated at 128 kPa (18.533 psi) under a carrier gas flow rate of 7.5 mL min⁻¹, for each analytical line.

The permeation measurements with single gases were performed using the pressure drop method controlling the pressure by means of a forward pressure controller placed on the feed line.

The mixtures measurements were carried out using the concentration gradient method (Fig. 1) and the retentate and permeate compositions were analysed using a gas chromatograph. In this case, the feed/retentate pressure was controlled by means of a back pressure controller placed on

**Fig. 1** Scheme of the experimental setup used for mixture measurements

the retentate line. The mixtures were obtained by mixing CO₂ and CH₄ coming from two different cylinders that were fed to the membrane modules by means of two mass flow controllers [34].

All the measurements were carried out by feeding the gas on the outer (shell) side of the fibres and the permeate was collected from the inner hole. The permeate and retentate flow rates were measured by means of two bubble soap flow meters.

In the experiments with water vapour, to obtain 100 % relative humidity, the feed stream, either single gas or mixture, was firstly fed into a humidifier at the same temperature and pressure as the membrane module and then, once saturated, into the module. For the measurements at 50 % relative humidity, a part of the feed streams (50 %) is fed into the humidifier and another part not. The two streams are combined before the module and are then fed to reach 50 % relative humidity. The relative humidity, in both cases, was measured by means of two humidity sensors placed on the feed and permeate lines.

In addition, the modules were placed in oblique position inside the furnace to avoid any liquid deposition also on the external surface of the fibres.

All the measurements were performed at a high feed flow rate Table 2 and, consequently, at a low stage cut, 5–10 %, (ratio of the permeate flow rate to the feed flow rate). This condition assures the absence of variation of the species composition in the feed/retentate side.

The performances of the membranes were evaluated in terms of permeating flux (Eq. 1) and permeance (Eq. 2) where A^{Membrane} (52 cm²) is the membrane area and the permeation driving force is given by the difference of the species partial pressure on the two membrane sides (Eq. 3). The single gas selectivity and the selectivity in mixture are given by the ratio of the measured permeances (Eq. 4). In addition, the separation factor was also calculated, however, owing to the low stage cut it coincides with the mixture selectivity. The investigated hollow fibres have an asymmetric structure with a selective and thin dense layer on others of different porosity and pore size. The thickness of the selective layer only was utilized in the permeability evaluation as used for symmetric and asymmetric flat films.

$$\text{Permeating flux}_i = \frac{\text{Permeate flow rate}_i}{A^{\text{Membrane}}} \quad (\text{molm}^{-2}\text{s}^{-1}) \quad (1)$$

$$\text{Permeance}_i = \frac{\text{Permeating flux}}{\text{Driving force}} \quad (\text{molm}^{-2}\text{s}^{-1}\text{Pa}^{-1}) \quad (2)$$

$$\text{Driving force}_i = P_i^{\text{Feed}} - P_i^{\text{Permeate}} \quad (\text{kPa}) \quad (3)$$

$$\text{Selectivity}_{ij} = \frac{\text{Permeance}_i}{\text{Permeance}_j} \quad (4)$$

Tools for membrane system performance analysis

In some previous papers [12, 13], the authors developed a simple tool that uses “maps” to enable analysis of performance and the perspectives of membranes in CO₂ capture. That study focused on the application of membrane gas separation in CO₂ processing with a general approach considering the effect and, eventually, the limitations offered by the main variables that affect the separation performance: the pressure ratio, the feed composition, and the mass transport properties (permeance and selectivity) of the membrane considered in the installation. As performed, the study is a useful guide for readers interested in CO₂ separation independent of the other gases present in the feed stream.

In the dimensionless form of the equations, the terms Θ_i and ϕ can be distinguished as the permeation number and the feed to permeate pressure ratio, respectively.

$$\Theta = \frac{\text{Permeance}_{\text{CO}_2} \times A^{\text{Membrane}} \times \text{Feed pressure}}{\text{CO}_2 \text{ feed mole fraction} \times \text{Flow rate}^{\text{Feed}}} \quad (5)$$

$$\phi = \frac{\text{Feed pressure}}{\text{Permeate pressure}} \quad (6)$$

The permeation number (Eq. 5) expresses a comparison between the two main transport mechanisms involved that are the convective flux along the membrane axis and the maximum permeating flux achievable. A high permeation number corresponds to a high membrane area and/or permeance for the stream and to a high permeation through the membrane with respect to the total flux along the module. The pressure ratio (Eq. 6) is one of the most important and determinant operating parameters affecting the performance of the membrane unit and is the driving force for the separation. More details about the model used and the dimensionless analysis can be found in [12].

Results and discussion

Measurements feeding single gases

The permeating flux was measured up to 75 °C to evaluate the suitability of the prepared membranes for the targeted separation at a relative high temperature.

Figure 2 shows the CH₄ and CO₂ permeating flux as a function of the driving force at 60 °C. Both CO₂ and CH₄ fluxes linearly increased indicating that the permeance of each gas was constant for all the applied values of the driving force. CO₂ flux was always greater than that CH₄ since CO₂ higher solubility in Matrimid®5218 membrane with respect to CH₄ one. The difference in permeance of CO₂ and CH₄ can be explained on the basis of difference in

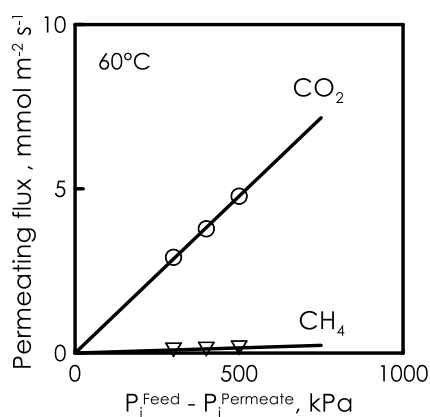


Fig. 2 CH₄ and CO₂ permeating flux measured for single gases as a function of the driving force. Feed pressure range 400–600 kPa and permeate pressure 100 kPa. Solid lines linear correlation of experimental data

the gas–polymer interaction. CO₂ has both a higher solubility and diffusivity than methane (Table 3). For comparing the mass transport properties measured in this work with those available in the literature on the same membrane type, the permeability of hollow fibre membrane is calculated considering the separating layer thickness of 0.4 μm . It resulted from an estimation carried out on SEM images of the cross section of several hollow fibre samples. This comparison gives quite good agreement both in terms of permeability (2.71 versus 2.76 and 0.080 versus 0.081 for CO₂ and CH₄, respectively) and CO₂/CH₄ selectivity which is 34.0 and 34.1 from the literature and developed membranes, respectively.

The same linear behaviour of the permeating flux was also observed at 25, 50 and 75 $^{\circ}\text{C}$; then, CO₂ and CH₄ permeance at all the investigated temperature were calculated using the Eq. (2). Figure 3 shows as the permeance of both gases increases with the temperature, the permeation being an activated mechanism following the Arrhenius law.

CO₂ permeance increased quite linearly (apparently, owing to the Arrhenius plot) with the temperature up to 75 $^{\circ}\text{C}$, the highest temperature value analysed, whereas for

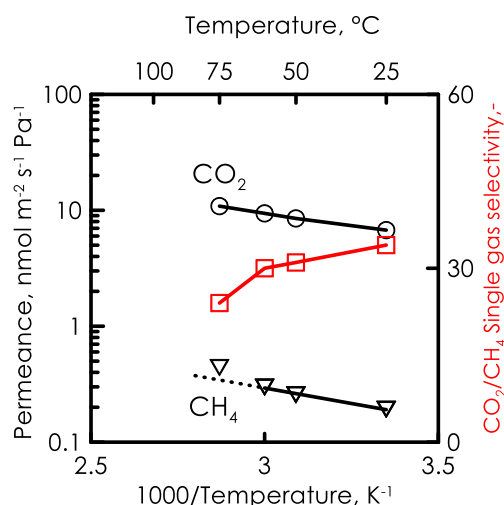


Fig. 3 CO₂ and CH₄ permeance and CO₂/CH₄ single gas selectivity as a function of temperature. Feed pressure range 400–600 kPa and permeate pressure 100 kPa. Experimental measurements (symbols) and lines connecting experimental data

CH₄ the linear trend was kept up to 60 $^{\circ}\text{C}$. In fact, CH₄ permeance value at 75 $^{\circ}\text{C}$ exceeded the prevision given by the linear trend crossing the permeance at the lower temperatures. The temperature dependency of permeability results as a combination of diffusion and sorption components which increases and decreases with the temperature, respectively. However, the evaluation of these components disregards the purpose of this work.

The prepared membrane showed CO₂/CH₄ selectivity decreasing in the range of temperature investigated (Fig. 3) keeping a high value between 34 and 31 up to 60 $^{\circ}\text{C}$. It dropped to 24, a still interesting value, at 75 $^{\circ}\text{C}$. It is worth to notice that the performance of the membranes was restored when the temperature was reduced.

Measurements feeding dry gas mixtures

Three CH₄–CO₂ mixtures (molar composition of 5:95; 50:50 and 70:30, Table 2) were fed to the membrane module kept at a constant temperature up to 75 $^{\circ}\text{C}$.

Table 3 Solubility and diffusivity in Matrimid[®]5218 membranes at 35 $^{\circ}\text{C}$ as reported by [35] and permeance *thickness as measured at 25 $^{\circ}\text{C}$ in this work

	As reported by [35]		This work	
	Solubility (cm ³) (at 25 $^{\circ}\text{C}$)/cm ³ cmHg	Diffusivity (cm ² s ⁻¹)	Permeability** (femto-mol m ⁻¹ s ⁻¹ Pa ⁻¹)	Permeability* (femto-mol m ⁻¹ s ⁻¹ Pa ⁻¹)
CO ₂	31.0×10^{-3}	2.85×10^{-8}	2.71 (88.4×10^{-11})	2.76
CH ₄	2.5×10^{-3}	1.04×10^{-8}	0.080 (2.6×10^{-11})	0.081
CO ₂ /CH ₄ selectivity (-)			34.0	34.1

* Calculated considering a separating layer thickness of 0.4 μm

** Calculates as solubility \times diffusivity

Fig. 4 Permeating flux of CO₂ and CH₄ and in mixture as a function of the driving force. Feed pressure range 400–600 kPa and permeate pressure 100 kPa. Experimental measurements (*symbols*) and linear correlation of experimental data

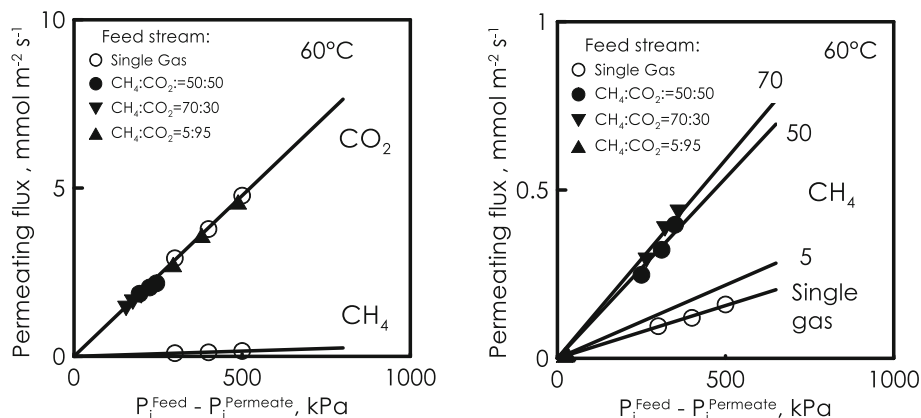


Figure 4 shows the permeating flux of CO₂ and CH₄ feeding the mixtures as a function of the driving force at 60 °C. Single gas values are also shown for comparison reasons. A linear dependence of the fluxes on the driving force was observed for both species at all the temperatures including 75 °C. No change in CO₂ permeance as function of feed composition was observed with respect to the single gas measures: all the measurements (single gas or gas mixtures) are aligned on the same line. On the contrary, the CH₄ permeance (Fig. 4, right side) changes with the feed concentration as detailed in Table 4.

The CH₄ sorption in the Matrimid has a specific value and in the ternary system (CO₂–CH₄–Matrimid) the influence of CO₂ has to be taken into account also on this parameter. The presence of CO₂ is expected to reduce CH₄

Table 4 CH₄ permeance measured in mixtures at 60 °C as a function of CH₄ feed concentration

CH ₄ feed concentration (% _{molar})	CO ₂ feed concentration (% _{molar})	CH ₄ permeance (pico-mol m ⁻² s ⁻¹ Pa ⁻¹)
100	0	300
5	95	310
50	50	370
70	30	390

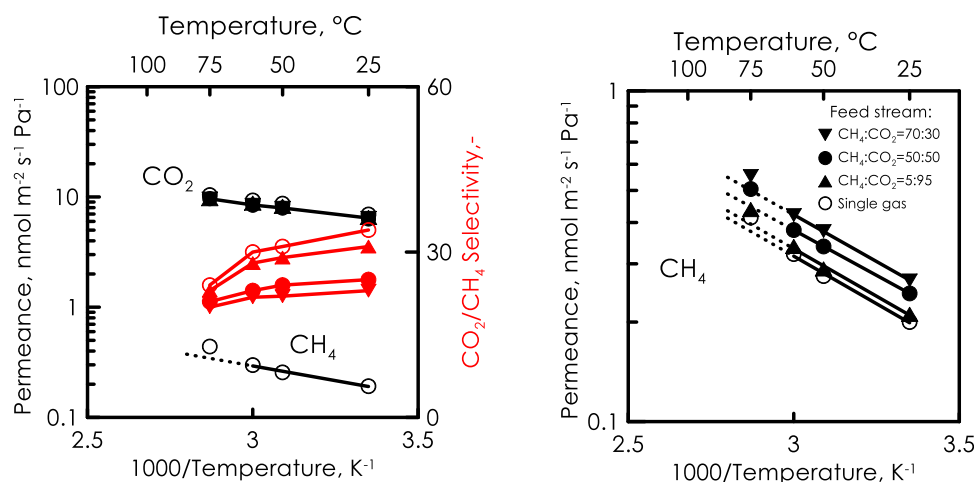
sorption, since CO₂ competes with CH₄. Minelli et al. [36] calculating CH₄ sorption as a decreasing function of the CO₂ concentration for polyphenylene oxide and polymethylmethacrylate confirmed the competitiveness of the absorption of the two gases. Scholes et al. [37] focused on CO₂ and CH₄ competitive sorption in a Matrimid membrane. Lin and Yavari [38] simulated on a free volume-based model the decreasing trend of CO₂/CH₄ selectivity in mixture. As experimentally observed, CO₂ promotes CH₄ permeation; its concentration of 30–50 %_{molar} in the feed mixtures is probably enough to significantly reduce the CH₄–Matrimid interactions (sorption) with respect to CH₄ when fed alone. This should increase, in the meantime, methane diffusion probably owing to the combination of two potential effects: (1) a small swelling of the membrane owing to CO₂ sorption and (2) a facilitated diffusion of CH₄ inside the membrane bulk where polymer chains are partly covered by CO₂ sorbed on them. The overall effect results in a higher CH₄ permeance. A selectivity loss was consequently observed. When CO₂ concentration is 95 %_{molar}, the methane is too low (5 %_{molar}) for showing a permeance increase.

A similar trend was observed by Lin and Yavari [38], by Houde et al. [39] and Scholes et al. [37], who confirmed the competitive sorption between CO₂ and CH₄ (Table 5) in cellulose acetate, polyphenylene oxide and polyimide,

Table 5 CO₂/CH₄ selectivity in mixture at 35 °C

Membrane material	CO ₂ /CH ₄ selectivity (–)		Reference	
	Single gas	Mixture		
Cellulose acetate	35	CH ₄ :CO ₂ = 20:80	CH ₄ :CO ₂ = 80:20 25	Lin et al. [38]
		20		
Polyimide	49	CH ₄ :CO ₂ = 90:10	41	Scholes et al. [37]
		41		
Polyphenylene oxide	42	CH ₄ :CO ₂ = 90:10	CH ₄ :CO ₂ = 76:24 35	Houde et al. [39]
		29		

Fig. 5 CO₂ and CH₄ permeance and CO₂/CH₄ selectivity in mixtures as a function of temperature. Feed pressure range 400–600 kPa and permeate pressure 100 kPa. Experimental measurements (symbols) and lines connecting experimental data



respectively; CO₂ plasticization which causes membrane swelling also plays a crucial role. The CO₂/CH₄ selectivity value in mixtures was lower for ca. 35 % than that obtained for the single gas. CO₂ permeance, mainly owing to CO₂ solubility (and not its diffusion), does not undergo a significant change and CO₂ permeates the membrane in the same way fed singly or in a gas mixture. Differently, CH₄ permeance benefits of the swelling effects with consequent diffusion increase.

The same behaviour was also observed at the other investigated temperatures including 75 °C.

The permeance of CO₂ and CH₄ as a function of the temperature (Fig. 5) shows the same apparently linear (owing to the Arrhenius plot) trend already observed for single gas (Fig. 3) confirming the obedience to the Arrhenius law. Furthermore, the selectivity measured when using mixtures (Fig. 5) shows the same trend as that obtained with single gases. It is lower in relation to the higher CH₄ concentration of the feed mixtures. In the whole temperature range analysed, the values of the selectivity measured with mixture were lower than the single gas selectivity.

The low stage cut (5–10 %) set in the experimental measurements means that the differences between the mixture selectivity and the single gas selectivity cannot be attributed to the eventual presence of partial pressure profiles along the module length, but only to the interactions occurring among gases and membrane.

Figure 6 shows CH₄ retentate concentration as a function of CH₄ feed concentration at the three different feed pressures investigated (400, 500, 600 kPa) at 50 °C feeding dry gas. CH₄ concentration in the retentate increased with the concentration of CH₄ in the feed streams. Under the same experimental conditions feeding a mixture with a major concentration of CH₄ in the feed stream a higher CH₄ retentate concentration was observed. The increase of CH₄ concentration in the retentate was also directly related

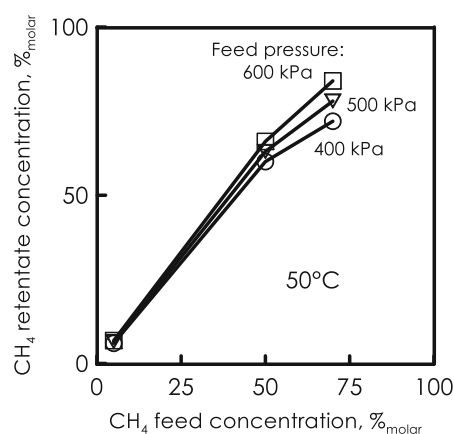


Fig. 6 CH₄ retentate concentration as a function of the CH₄ feed concentration at the three different feed pressures investigated feeding dry mixtures. Experimental measurements (symbols) and lines connecting experimental data

to the feed pressure and, consequently, also to the driving force. This behaviour is particularly evident at a high feed concentration of CH₄. In fact, with a feed mixture containing 70 %_{molar} of CH₄, the retentate composition increased from ca. 75 to ca. 90 %_{molar} at feed pressure of 400 and 600 kPa, respectively. These results indicate that with a feed stream composition similar to that of biogas (see Introduction), it is possible with a single stage membrane operation, to obtain a gas mixture potentially injectable into the grid of CH₄.

A similar trend of CO₂ concentration is evident in the permeate stream in Fig. 7. As experimentally observed, CO₂ concentration increases with the feed pressure. The driving force allowing the molecules permeation directly depends on the feed pressure and, consequently with the driving force, increases CO₂ permeate concentration too. The strongest increase of CO₂ concentration is obtained at 600 kPa at the lowest CO₂ concentration (30 %_{molar}) in the

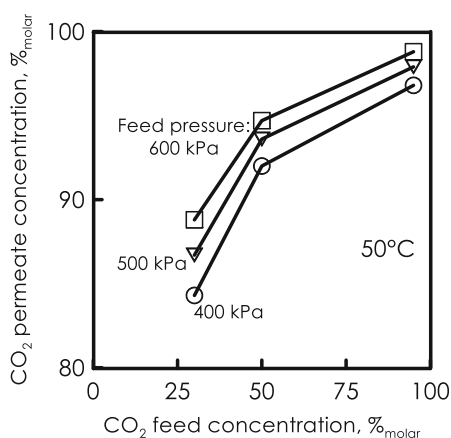


Fig. 7 CO₂ permeate concentration as a function of the CO₂ feed concentration at the three different feed pressures investigated (400, 500, 600 kPa) at 50 °C feeding dry mixtures. Experimental measurements (symbols) and lines connecting experimental data

feed stream. For the feed mixture at 50 %_{molar} CO₂, the CO₂ permeate concentration was ca. 95 %_{molar} at a feed pressure of 600 kPa. These results are very interesting since the high CO₂ permeate concentration is the fundamental requirement for the capture and storage of the CO₂ streams. The CO₂ capture by means of membrane could be identified as one potential solution to reduce greenhouse gas emissions which causes climate change.

Measurements feeding humidified gas mixtures

Most often the permeation measurements are carried out with dry gas. However, most of the industrial streams to be treated contain a large amount of water vapour, thus membrane performances are affected by it. Indeed, to better evaluate the membrane module application for CO₂/CH₄ mixture separation, experimental measurements using CO₂/CH₄ mixtures humidified at different values of relative humidity (50 and 100 %) were carried out.

Figure 8 shows the CO₂ and CH₄ permeance, feeding CH₄:CO₂ = 50:50 (left side) and CH₄:CO₂ = 70:30 (right side) mixtures, as a function of relative humidity at 25 and 60 °C. In both mixtures, the water influenced the transport properties of the membrane modules by inducing a decrease in permeance of the two gases as the relative humidity increased. The same behaviour was also observed at 75 °C.

From 0 to 50 % of relative humidity, the CO₂ permeance decrease was only ca. 10 % whereas for CH₄ it was ca. 5 % for all the temperatures investigated. This result is interesting because 50 % relative humidity does not change the transport property of the membrane significantly.

From 50 to 100 % relative humidity, the permeance decrease was larger, being ca. 40 % for CO₂ and ca. 20 %

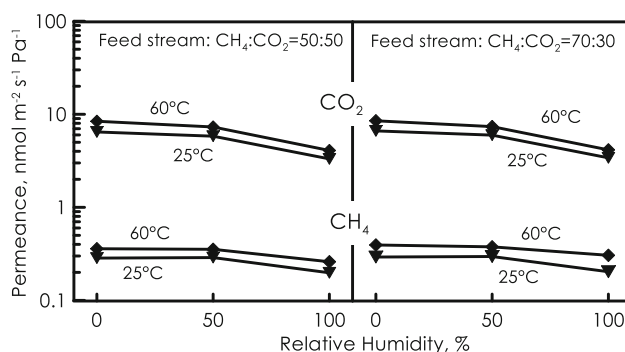


Fig. 8 CO₂ and CH₄ permeance in mixtures CH₄:CO₂ = 50:50 (left side) and CH₄:CO₂ = 70:30 (right side) as a function of relative humidity at the two temperatures investigated (25 and 75 °C). Feed pressure range 400–600 kPa, permeate pressure 100 kPa. Experimental measurements (symbols) and lines connecting experimental data

for CH₄. This different trend, between CO₂ and CH₄, could be attributed to the different solubility of CO₂, CH₄ and water in the polymeric matrix. As Scholes et al. [37] and Li et al. [38] demonstrated, water is the more soluble species (0.4 cm³ STP/cm³ cmHg at 35 °C) and its molecules fill the sorption sites available, present between the polymeric chains, used by CO₂ or CH₄ for passing through the membrane. Also CO₂ has a good solubility (28 × 10⁻³ cm³ STP/cm³ cmHg at 35 °C) even though significantly lower than that of water; therefore, it can fill only the sites not occupied by water when competitive sorption of both occurs. The reduced CO₂ sorption produces a lower permeation of this species. CH₄ solubility (2.5 × 10⁻³ cm³ STP/cm³ cmHg at 35 °C) is much lower in the polymeric matrix, consequently also its sorption and thus permeance significantly reduces. The same behaviour was observed for both mixtures and the effect on the selective properties is illustrated in Fig. 9 where CO₂/CH₄ selectivity is shown as a function of the relative humidity, at 25 and 60 °C feeding CH₄:CO₂ = 50:50 and CH₄:CO₂ = 70:30 on left and right sides, respectively. In both cases, the selectivity decreases with the relative humidity. The decreasing was not so significant at 50 % relative humidity but was more evident in vapour-saturated condition. The same behaviour was also observed at 50 and 75 °C.

However, for the mixture CH₄:CO₂ = 50:50, CO₂/CH₄ selectivities were very interesting with values between 25 and 18 and in the range 18–13 at 25 and 75 °C, respectively. For the CH₄:CO₂ = 70:30 mixture, the selectivity was between 23 and 17 at 25 °C and between 13 and 11 at 75 °C.

It is important to notice that the performance of the membranes was restored when the water vapour was removed. These results show that the membrane module

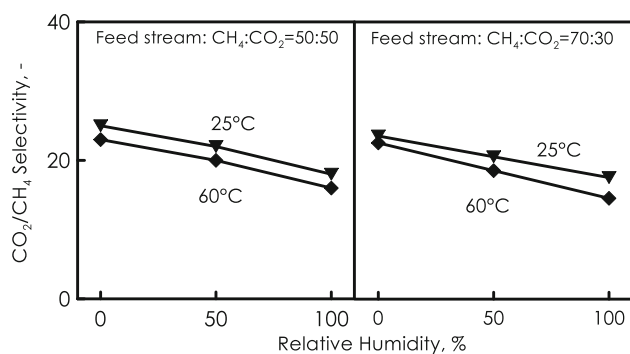


Fig. 9 Selectivity in mixture for CH₄:CO₂ = 50:50 (left side) and CH₄:CO₂ = 70:30 (right side) as a function of relative humidity at the two temperatures investigated (25 and 60 °C). Feed pressure range 400–600 kPa, permeate pressure 100 kPa. Experimental measurements (symbols) and lines connecting experimental data

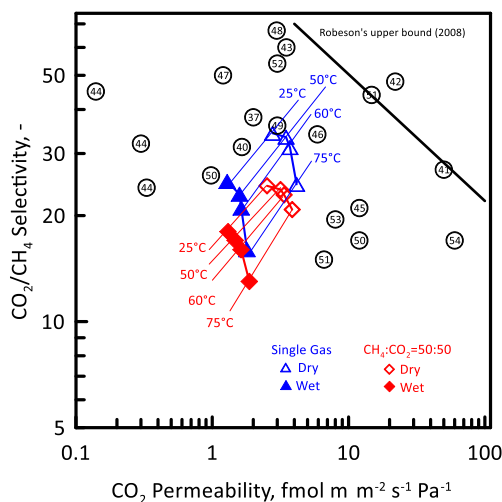


Fig. 10 CO₂/CH₄ single gas selectivity or mixture selectivity of gases measured as a function of the CO₂ permeability; Symbols: triangles and diamonds refer to experimental data; circles refer to the literature data: Ayala et al. [40]; Xiao et al. [41]; Chan et al. [42]; Staudt Bickel et al. [43]; Peter et al. [44]; Shao et al. [45]; Hillock et Koros [46]; Suzuki et al. [47]; Swaidan et al. [48]; Sanders et al. [49]; Vinh-Thang et al. [50]; Nik et al. [51]; Qui et al. [52]; Hosseini et al. [53]; Askari et al. [54]; Scholes et al. [37]

developed can separate the CH₄ from CO₂ in the presence of water vapour.

A wide comparison of mass transport properties measured in this work with those currently available in the open literature, the state of the art (the Robeson's upper-bound), can be done only through the permeability. Thus, the permeability was calculated considering the separating layer thickness of 0.4 μm, as estimated by SEM analysis. Figure 10 compares the mass transport properties measured in this work, with the current state of art on the Matrimid[®] 5218 and polyimide, a material similar to Matrimid[®] 5218.

The better results in terms of selectivity and permeance were obtained for the single gas measurements. There was no change in CO₂ permeance feeding single gas or a gas mixture. A reduction of selectivity of ca. 20 % was observed when a dry CH₄:CO₂ = 50:50 mixture was fed. The membrane selectivity was reduced of ca. 25 and 50% in presence of 50 and 100 % of relative humidity in the feed stream, respectively. Permeability and selectivity of the developed membranes were lower than the better values (ca. 50 as selectivity and ca. 20 nmol m⁻² s⁻¹ Pa⁻¹ as CO₂ permeance) of literature data of 6FDA-based polyimides. However, the membranes prepared in this work show interesting gas transport properties, also a temperature of 75 °C and feeding dry and humidified streams. In particular, CO₂/CH₄ selectivity in the range of 34–24 and 25–21 was obtained feeding dry single gas and dry mixture, respectively. In humidified conditions, the CO₂/CH₄ selectivity was between 25 and 12 and between 18 and 13 feeding single gas and mixture, respectively. It is important to notice that the performance of the membranes was restored when the water vapour was removed and when the temperature was reduced.

Some remarks on the membrane system performance

One of the main points of discussion which often interfaces material scientists with process engineers is the possibility of using the materials produced and that gave interesting performance in mixtures in the laboratory. Apart from the necessity to test the performance in mixtures, a crucial role for the application of membrane technology in CO₂ separation is played by the membrane engineering who knows how to operate the membrane unit and to design the separation process to obtain the best performance. By means of the performance maps developed elsewhere, it is possible to elaborate a predictive analysis of the membrane unit performance in a wider range of operating conditions.

Figure 11 shows the CO₂ permeate concentration versus recovery for different values of feed compositions experimentally tested at various values of pressure ratio and permeation number.

Once, on the basis of global economic considerations the optimal performance (that is, a point on the plot of CO₂ permeate concentration versus CO₂ recovery) has been chosen, it can be univocally individuated on the maps; the parametric curves crossing this optimal point provide the corresponding pressure ratio and permeation number. This leads to the identification of the operating conditions, membrane characteristics (permeance, area, etc.), or feed conditions required to obtain the final product with certain characteristics.

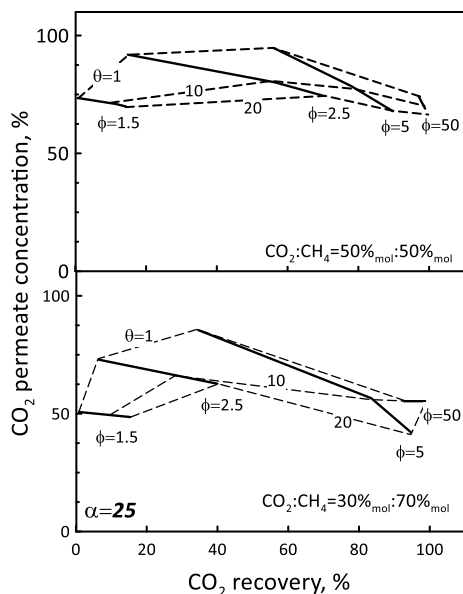


Fig. 11 Maps of CO₂ concentration in permeate streams, respectively, as a function of recovery at various values of pressure ratio and permeation number

For instance, if 60 %_{molar} CO₂ recovery in the permeate is desired, the pressure ratio required is close to 2.5 in the case of the equimolecular mixture (CH₄:CO₂ = 50:50), whereas it increases to 5 for the mixture with the higher concentration of methane (CH₄:CO₂ = 70:30). Assuming this latter as reference mixture, for a pressure ratio of 5, the CO₂ concentration in the permeate can range between 50 to more than 80 to 90 %_{molar}, according to the permeation number chosen with consequent changes on the recovery which can pass from 80 down to 40 %_{molar}, respectively.

Following the indications of the International Energy Agency [55–58] for which a purity higher than 80 %_{molar} and a recovery >60 %_{molar} are desirable targets, the permeation number selected should be close to 1. For defined feed conditions and membrane characteristics, it is possible to calculate the membrane area required to treat certain feed flow rates. At a greater pressure, the ratio would correspond to a reduction in membrane area.

Apart from the details of the calculation, it appears evident that in a single stage the proposed membranes cannot contemporarily reach high recovery and purity. However, this analysis provides an indication on the possibility of using these membranes as the first stage in a multistage system to concentrate the feed stream or as a single stage unit when the recovery target is not important.

In the case of biogas separation or natural gas sweetening, still much more important than the CO₂ characteristics are the characteristics of the methane stream which remains as retentate. The treatment of these gas streams leads not only to the recovery and sequestration of CO₂, but also to much greater purification and recovery of value-

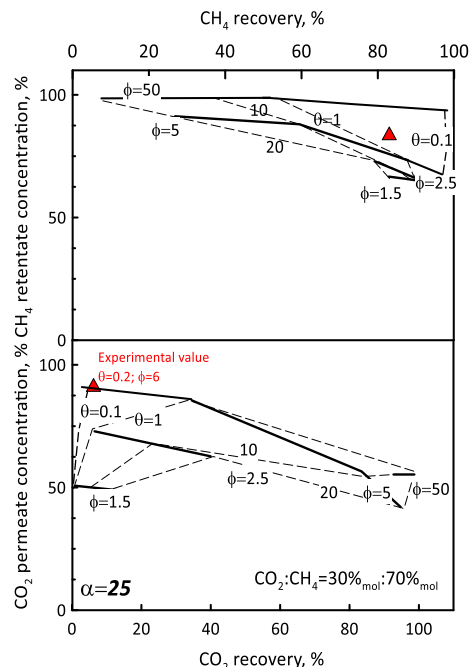


Fig. 12 Maps of CH₄ and CO₂ concentration in retentate and permeate streams, respectively, as a function of correspondent recovery at various values of pressure ratio and permeation number

added CH₄ to feed it directly to pipelines for domestic or stationary uses. From this perspective, since CH₄ has to be fed to pipelines at a high pressure, the possibility of installing a compressor before the membrane system and recovering the methane already concentrated and compressed as a retentate stream makes this operating option quite realistic. Figure 12 depicts the performance map not only for CO₂ characteristics but also for CH₄ ones. From the figure, the advantage achieved both in terms of purity and recovery when a high pressure ratio can be used appears evident. For example, at $\phi = 50$, it is possible to obtain a CH₄ purity greater than 97 %, the limit imposed for directly feeding in pipelines, even though with recovery not so high (ca. 50 %_{molar} for a permeation number equal to 1). To this corresponds a CO₂ recovery greater than 90 % but with a CO₂ concentration of ca. 55 %, at all permeation numbers considered. This stream would require a further separation treatment to fit the indications imposed for CO₂ storage; therefore, a multistage cascade system has to be applied for this solution.

Conclusions

The transport properties of Matrimid[®] 5218 hollow fibre membranes prepared by dry-jet wet spinning were evaluated by feeding singly CH₄ and CO₂ and as CH₄–CO₂ mixtures (of molar composition of 50:50, 70:30 and 5:95).

Specifically, relatively high temperatures for polymeric membranes up to 75 °C and wet condition were operated in measuring the membrane separation properties.

The permeation measurements in the range 25–60 °C showed CO₂/CH₄ selectivity values between 34 and 31 and between 30 and 23 feeding single gases or gas mixtures, respectively. At 75 °C, no difference in CO₂ permeance was observed feeding the different streams, whereas the permeance of CH₄, the less permeating specie, was little higher feeding a mixture stream than that measured as single gases; consequently, the membrane selectivity ranges 22–13 when feeding mixtures. Good CO₂ and CH₄ permeance and selectivity measured up to 75 °C and under water vapour presence. In addition, the membrane properties were restored when water vapour was removed and temperature decreased stating the excellent hydro-thermal stability of these membranes.

The membrane, in fact, shows very good water vapour resistance (50 and 100 % as relative humidity) even though a loss in CO₂/CH₄ selectivity (e.g. 22 at 25 °C; and 11 at 75 °C) was observed. The water vapour, owing to its high solubility in the polymeric matrix, also causes a permeance decrease of 50 and 25 % (at 100 % of relative humidity) of CO₂ and CH₄, respectively.

The measurements in the presence of water vapour (50 and 100 % relative humidity) showed water resistance and a certain loss of selectivity, although not so significant. The measurements also highlight a really good thermal stability because the performance of the membrane was restored when the temperature decreased.

Performance maps calculated for the specific case in a wider range of operating conditions with respect to the ones analysed in laboratory foresee the possibility of using these membranes both as the first stage for stream concentration in a multi-stages system or as single stage membrane unit, particularly when high pressure ratio can be applied.

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