

Asymmetric transmission and anomalous refraction in metal nanowires metasurface

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Here we investigated the asymmetric transmission and the anomalous refraction introduced by a metasurface of bent gold nanowires. The refraction follows the generalized Snell's law that takes into account the resonant behavior of metallic nanostructures located at the interface between two dielectrics. Measurements performed in the linear optical regime reveal a large sensitivity to the subwavelength features of the gold nanostructures.

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1 INTRODUCTION

Recently F. Capasso and coworkers [1] shown how it is possible to bend a ray of light by properly design resonant metallic nanostructures at the interface between two dielectrics. The metallic nanostructures in resonant condition can act as nanoantennas producing a large phase shift in the incoming light wavefront that can be of the order the wavelength [1, 2], even if the thickness of the metallic element can be very small (few tenth of nanometers). As a result the ray of light passing through two consecutive dielectric media (labeled 1 and 2 respectively) separated by the nano-patterned metasurface [3], will refract by following a generalized Snell's law [1]:

$$n_2 \cdot \sin(\varphi_2) - n_1 \cdot \sin(\varphi_1) = \frac{\lambda_0}{2\pi} \cdot \frac{d\Phi(x)}{dx} \quad (1)$$

where n_1 and n_2 are the refractive indices of the dielectric 1 and 2 respectively, λ_0 is the beam wavelength in vacuum and $\Phi(x)$ represents the phase discontinuity introduced by the nanostructure at the point x of the interface.

This phenomenon can be used in order to produce very thin optical elements as aberration free lenses [4], but on the other side the generalized Snell's law can be used as a powerful tool in the subwavelength characterization of nanopatterned surfaces. By varying the incidence angle φ_1 from Eq. (1), it is possible to retrieve information on the phase gradient $\frac{d\Phi(x)}{dx}$ introduced by the metasurface by simply measuring the refracted angle φ_2 of the out-coming light. Alternatively by fixing the incoming light at normal incidence ($\varphi_1 = 0$) and by scanning the surface in the transverse direction it is possible to map the phase gradient point-by-point by using the relation

$$\frac{\lambda_0}{2\pi} \cdot \frac{d\Phi(x)}{dx} = n_2 \cdot \sin(\varphi_2) \quad (2)$$

derived by Eq. (1) with the condition $\varphi_1 = 0$. Since the phase gradient $\frac{d\Phi(x)}{dx}$ is highly dependent on the geometrical shape of the nanoantennas, in both the previous cases important information on surface morphology can be obtained with sub-wavelength resolution.

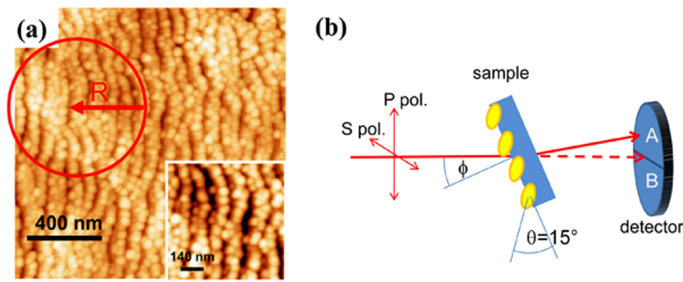


FIG. 1 (a) AFM morphology of the NWs test sample. In the inset a magnified detail show the polycrystalline gold NWs. (b) scheme of the experimental set-up and of the sample cross-section.

In this work we report the measurements in the visible spectral range of the anomalous refraction raised by a metasurface made up of self assembled bent gold nanowires (NWs) arrays with 125 nm of periodicity deposited onto a patterned glass slide. These measurements, synthetically shown in [5] and here extensively discussed, clearly address the dependence on the morphology of the nanowires.

2 SAMPLE DESCRIPTION

As described in [5], the NWs test sample has been realized on a 140 micron thick soda-lime glass substrate that was previously patterned by Ar⁺ ion beam sputtering. The resulting patterning (see Figure 1(a)) forms a periodic corrugations whose wavevector is mainly oriented parallel to the ion beam projection and with periodicity of about 125 nm.

The in-plane radius of curvature R of the undulations follows a broad distribution centered around 400 nm (Figure 1(a)). In a second stage, Au was thermally evaporated under grazing incidence condition (80° respect to the normal) and orthogonally to the ripple structures in order to localize metal agglomeration in correspondence to the convex side of the ridges. Under these conditions, a 1-D connected polycrystalline Au NWs is formed on top of the supporting illuminated ridges as evidenced in the inset of Figure 1(a), where a magnified image of the atomic force microscopy (AFM) topography is presented. The resulting NWs have a width of about 50 nm, while the height amounts to about 40 nm. The wires are laterally tilted by $\theta=15^\circ$ with respect the average sample surface (see Figure 1(b), where the tilt angle θ is evidenced). The optical transmission spectra obtained by using polarised light was shown in [5] and clearly confirm the excitation of localised plasmon resonances centered around a wavelength of 600 nm for light polarised in the transverse direction with respect to the wires, meanwhile, for light polarised in the longitudinal direction, the transmission spectra resemble those of a continuous connected Au film. The sample dimension is 1 cm \times 1 cm and it is fully patterned all over the surface and fully covered by gold nanowires except for a region of 5 mm \times 5 mm where the gold was removed in order to get a reference area for the forthcoming measurements.

3 EXPERIMENTAL SET-UP

In order to study the anomalous refraction behaviour of the NWs sample a displacement measurement set-up was build-up as shown in Figure 1(b). The collimated light source is a He-Ne laser (emission mode TEM₀₀, wavelength $\lambda_0=633$ nm, divergence 1.7 mrad, beam diameter 0.5 mm) . The wavelength of the source lies closely to the peak of the plasmonic resonance of the NWs. The polarization of the light can be set to s or p polarization state. The light is then sent onto the NWs sample at an incidence angle φ . The angle is controlled by a motorized rotation stage connected to a computer. The light at the output of the sample is detected by a photodiode divided in sectors (labeled A for left side sector and B for right side sector in Figure 1(b)) with a diameter of 8 mm. The detector is posed 30cm far away from the sample rotation axis. The output of the sensor was analysed by a position detector circuit giving at the same time the total power

$$P_T = P_A + P_B \quad (3)$$

impinging on the detector and the normalised difference between the power of the light in the sector A and the power of the light in sector B:

$$X = \frac{P_A - P_B}{P_A + P_B} \quad (4)$$

The normalization is necessary in order to remove the effect of different light intensities, due, for example, to the different transmitted signal for s and p polarization state. The P_T value is supplied in volts at the output of the circuit and is proportional to the total power by a conversion factor of 0.5 mW/V. The X value is proportional to the displacement of the beam with respect to the centre of the detector and was supplied in volts at the output of the circuit. Measurements conversion from the circuit signal (in volts) to the real displacement (in mm) is retrieved by a calibration measurement performed onto a glass slide of known thickness and results to be 0.05 mm/V [5].

Since in [5] we reported exhaustively the displacement introduced at normal incidence ($\varphi_1 = 0$), here all the displacement measurements are reported by setting the zero displacement at normal incidence, in this way it is possible to easily compare measurements obtained in different conditions.

4 RESULTS

In Figure 2(a) we show, as a function of the incidence angle φ , the displacement X and the total power P_T measured when the light passes through the gold NWs and, as a reference, through the bare patterned glass, when the wires are mainly oriented in the vertical direction with the curvature facing the right side.

The polarization was set in order to excite the plasmonic resonance, i.e. with the polarization of the light perpendicular to the wires direction (in [5] we demonstrate that the anomalous deviation disappears when the light is polarized in a off-resonance condition, i.e. with the polarization of the light parallel to the wires direction). The displacement X of the glass

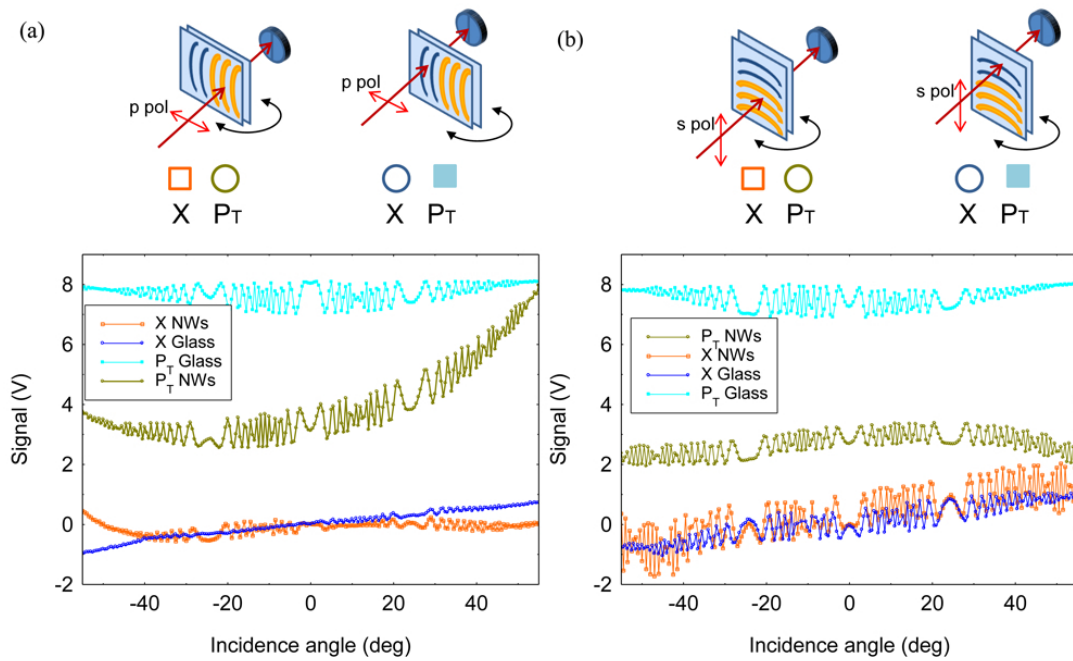


FIG. 2 Measurements of the displacement X and of the transmitted power P_T as a function of the incident angle on glass and on NWs, in the case of NWs oriented in (a) vertical direction and (b) horizontal direction. The circle arrows aside the samples schematic show the measurement rotation axis.

(blue circles) follows the standard trend of a planar glass slab (see [5]), meanwhile the gold NWs behaves anomalously (red squares). Even the total power P_T gives interesting information, in fact the P_T behaviour of the glass (blue squares) is perfectly symmetric while the P_T of NWs is very asymmetric (green circles).

In [5] we shown that by reversing the orientation of the NWs, i.e. with the sample rotated by 180° around the axis of the motorized rotation stage and so by entering from the substrate side, the displacement follows a reverse behaviour with respect to the starting case, but the tilt angle of the wires remains unchanged. Here, in Figure 2(b), we show the measurements when NWs are mainly oriented in the horizontal direction with the curvature facing down, so there is any predominance of the left or right side in the radius of curvature. It is very interesting to notice that the displacement X introduced by the NWs (red squares) follows almost exactly the trend of the bare glass (blue circles) and no anomalous deviation is observed. This fact confirm that the displacement X is sensitive to the curvature of the wires and to its orientation with respect the incidence plane. Also the total power P_T (green circles) results almost symmetric even if the polarization is set in the on-resonance condition (s pol.).

In Figure 3 we show the measurements of the total power P_T as a function of the incidence angle ϕ , for different sample orientation, but with the wires mainly oriented in the vertical direction and the polarization of the light set in the on-resonance condition (p pol.). As a reference is considered the P_T of the sample when the light is polarized in the off-resonance condition (s pol.); in this case (black triangles) the curve results to be symmetric, indicating that any asymmetry must be ascribed to the plasmonic response of the nanowires.

It is interesting to observe that if the sample is flipped (see the

schematic in Figure 3) the P_T changes the symmetry (green circles) with respect to the P_T obtained when the sample is in the original orientation (red squares). In this case the change in the symmetry cannot be ascribed to the curvature of the wires, in fact, by flipping the sample, the radius of curvature lies in the same direction. It is the tilt θ of the NWs that change the sign passing from 15° to -15° (see the schematic in Figure 3). If the sample is rotated by 180° around the rotation axis ϕ , the curvature of NWs change the sign of their direction (from right to left), meanwhile the tilt of NWs remains the same; in this case the P_T (blue circles) remains with the same symmetry of the original orientation (red squares). This indicates that the P_T is sensitive to the projection of the tilt of the NWs in the incidence plane.

5 DISCUSSION

These results show that the use of the deviation measurement set-up can be a sensitive method for sub-wavelength morphological analysis of nano-structured samples. Usually linear optics is used in order to retrieve information on samples with details that are in the scale of the wavelength [18] and the sensitivity can increase in the presence of geometrical resonances such as for example in the case of optical gratings [6] or photonic band-gap structures [7, 19]. In our case it is the plasmonic resonance of the metal that, even if the thickness is in the nm scale, allows a good sensitivity in the visible wavelength scale. A larger sensitivity can be achieved by using nonlinear optical phenomena such as second harmonic generation SHG [8, 9], but of course short optical pulses with high intensities are needed and the measurement set-up results to be more complex. In particular SHG can be effectively used [10, 11] in order to detect the presence of extrinsic chirality [12, 13]. In [14] J. B. Pendry demonstrated that optical activity [15] can be used in order to obtain anomalous refraction and in [12] N. I. Zeludhev showed that bent metallic wires

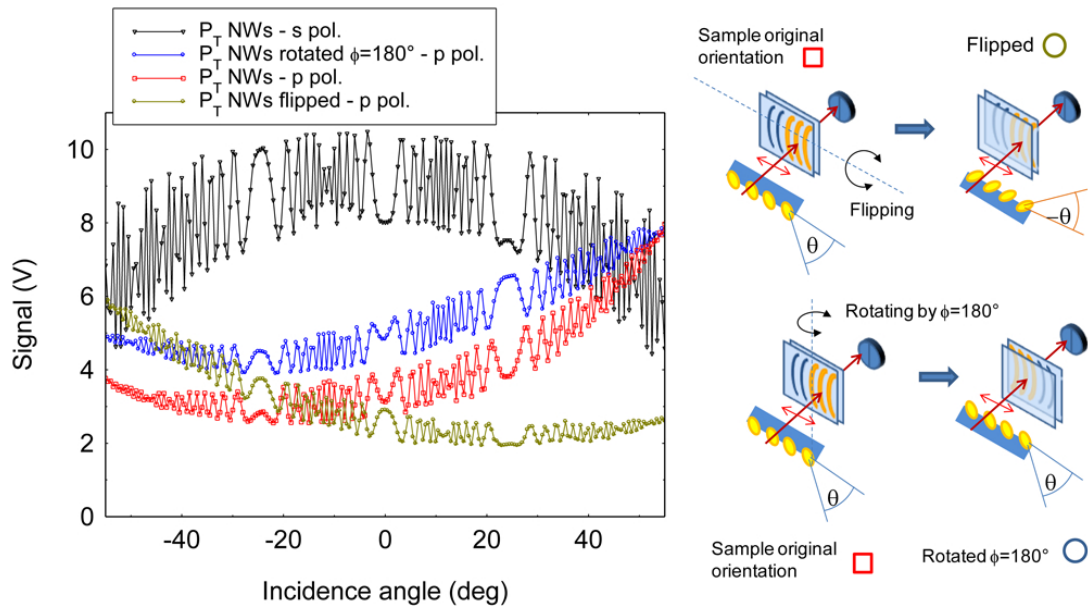


FIG. 3 Measurement of the total transmitted power P_T as a function of the incidence angle for different geometrical orientation of the sample; with NWs which curvature faces the right side (red squares for p polarized light, black triangles for s polarized light), with the sample flipped (green circles) and with the sample rotated by 180° (blue circles).

present extrinsic chirality and, at the same time, present very unusual refractive properties. In [16] by using circularly polarized SHG measurements we demonstrated that gold bent NWs, similar to the one here presented, give rise to evident extrinsic optical chirality that is closely linked to the curvature R of the NWs, meanwhile in [17] we used linear polarised SHG measurements on the same sample and we demonstrated that the SHG signal is sensitive to the tilt θ of NWs. Here both of these issues (radius of curvature and tilt) can be investigated by using a simple linear optical set-up.

6 CONCLUSIONS

In conclusion here we have investigated the anomalous refraction introduced by curved gold nanowires deposited onto a glass slide. The section of the wires (40 nm) and their periodicity (125 nm) are comparably smaller than the wavelength used in the measurement (633 nm), nevertheless the results are very clear and different morphological aspects can be detected. We shown that the direction of the average radius of curvature of the wires can be determined by measuring the displacement of the light on a detector divided in sectors. At the same time the total amount of the transmitted intensity of the light brings information on the average tilt of the wires. These behaviour is due to the cooperative effect of geometrical aspects and plasmonic resonance. The overall structure acts like a low-cost and large-area effective metasurface. The simplicity of the experimental set-up and his high sensitivity can be used in order to investigate different kind of nanostructured materials.

7 ACKNOWLEDGEMENTS

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