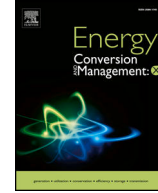


## Journal Pre-proofs



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PII: S2590-1745(20)30024-6  
DOI: <https://doi.org/10.1016/j.ecmx.2020.100052>  
Reference: ECMX 100052

To appear in: *Energy Conversion and Management: X*

Received Date: 29 May 2020  
Accepted Date: 12 July 2020

Please cite this article as: P. Gabrielli, A. Acquilino, S. Siri, S. Bracco, G. Sansavini, M. Mazzotti, Optimization of low-carbon multi-energy systems with seasonal geothermal energy storage: The Anergy Grid of ETH Zurich, *Energy Conversion and Management: X* (2020), doi: <https://doi.org/10.1016/j.ecmx.2020.100052>

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# Optimization of low-carbon multi-energy systems with seasonal geothermal energy storage: The Anergy Grid of ETH Zurich

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## Abstract

We investigate the optimal operation of multi-energy systems deploying geothermal energy storage to deal with the seasonal variability of heating and cooling demands. We do this by developing an optimization model that improves on the state-of-the-art by accounting for the nonlinearities of the physical system, and by capturing both the short- and long-term dynamics of energy conversion, storage and consumption. The algorithm aims at minimizing the CO<sub>2</sub> emissions of the system while satisfying the heating and cooling demands of given end-users, and it determines the optimal operation of the system, i.e. the mass flow rate and temperature of the water circulating through the network, accounting for the time evolution of the temperature of the geothermal fields.

This optimization model is developed with reference to a real-world application, namely the *Anergy Grid* installed at ETH Zurich, in Switzerland. Here, centralized heating and cooling provision based on fossil fuels is complemented by a dynamic underground network connecting geothermal fields, acting as energy source and storage, and demand end-users requiring heating and cooling energy. The proposed optimization algorithm allows reducing the CO<sub>2</sub> emissions of the university campus by up to 87% with respect to the use of a conventional system based on centralized heating and cooling. This improves on the 72% emissions reduction achieved with the current operation strategies. Furthermore, the analysis of the system allows to derive design guidelines and to explain the rationale behind the operation of the system. The study highlights the importance of coupling daily and seasonal energy storage towards the achievement of low-carbon energy systems.

*Keywords:* Multi-energy systems, seasonal storage, geothermal storage, energy networks, MINLP, Yearly scheduling

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## 1. Introduction

The evidence of climate change clearly indicates the necessity of new routes for energy supply, entailing zero-carbon emissions around 2050 and limiting global warming at 1.5 °C [1]. New routes of energy provision are enabled by distributed generation, smart grids and smart energy networks concepts, all seen as a viable solution to reduce primary energy use and carbon dioxide (CO<sub>2</sub>) emissions, as well as to increase the reliability and the flexibility of electrical and thermal networks [2–6].

In this context, multi-energy systems (MES) represent a new paradigm that exploits the interaction among various energy carriers, such as heat and cold, both at design and operation phase, allowing for improved technical, economic and environmental performance of the integrated energy system [7–9]. MES can provide energy to a single dwelling, a group of buildings, a single firm, a district or a region. The coupling of multiple energy vectors determines a greater complexity of urban energy systems [10]. Reference

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[7] provides a detailed overview of MES, focusing on the identification of internal and external energy flows, and proposes criteria for their technical and economic evaluation.

The spread of MES transforms energy end-users into prosumers, which are both self-consumers and providers of the energy supply [11]. Local energy communities arise to optimally operate such MES facilities from both technical, economic and environmental standpoints [12, 13]. Such communities are usually composed of several energy hubs, each characterized by specific electrical, thermal and cooling energy needs. Particularly in the tertiary and residential sectors, often characterized by a significant degree of electrification, heat pumps constitute an efficient technology to provide heat and cooling energy by exploiting different primary sources, i.e. air, water and ground [14–16]. The flexibility of heat pumps can be exploited to provide ancillary services to the electric power system by load modulation strategies [17], and geothermal distributed heat pumps can be operated to provide heat peak demand shaving within a district heating network [18].

Several local, district and city-scale MES are coupled to geothermal sources in urban ground and groundwater [19–21]. In these cases, the optimal design of geothermal heat pumps and borehole heat exchangers is challenging; different local factors have to be examined, such as the available space, the geomorphology of the site and the ground thermal response [21–23]. As far as the geothermal field is concerned, open- or closed-loop systems having a vertical or horizontal arrangement of boreholes, U-tube or spiral shaped, have to be examined very carefully since errors during the design phase can lead to malfunctioning of the whole geothermal system. Innovative solutions consider ground source heat pump systems coupled with PV and solar thermal collectors to reduce the land use [24, 25], or geothermal combined heat and power plants [26–28].

The deployment of MES is often coupled with energy storage technologies, which allow to compensate fluctuations in renewable energy production and energy demand [29–31]. Concerning thermal storage, two categories of systems are used to compensate short-term and long-term fluctuations. Daily or weekly fluctuations can be compensated by water tank storages, referred to as hot water thermal storage (HWTS), whereas long-term fluctuations can be compensated via phase change materials and geothermal installations [15, 32, 33]. However, compensating variable energy generation and demand at the seasonal scale is daunting, because (i) it can only be done through a few, expensive technologies, such as underground geothermal installations, and (ii) the optimal design and operation is complicated by the large number of decision variables, due to the required length and resolution of the time horizon [29, 34, 35], and by the system complexity.

Several tools for energy management systems (EMS) are proposed in the literature to optimally design and operate MES systems with energy storage [10, 36]. EMS can be based on linear or non-linear mathematical models, can be characterized by single- or multi-objective optimization frameworks and capture the physics of the elements of the energy system with different levels of detail [10, 37]. Concerning the optimal design and operation of seasonal storage systems, some studies have recently tackled the complexity of the optimization problem by using time series aggregation methods, i.e. by reducing the number of time intervals while retaining a level of detail sufficient to describe the dynamics of the entire energy system. A review of these methods is provided by Hoffmann et al. [35], Schütz et al. [38], and Gabrielli [39].

Modeling seasonal storage offers the opportunity to assess strategies for offsetting the seasonal variability of heating and cooling demands [40]. A real-world system adopting this concept is the Anergy Grid installed at ETH Zurich, in Switzerland, which consists of an underground network deploying geothermal fields acting as energy sources and storage units [41]. The current system operation allows reducing the CO<sub>2</sub> emissions of the university campus by 72% with respect to the conventional system using centralized heating and cooling [42]. The scope of this contribution is to develop an optimization framework enabling further increase in energy efficiency, hence further emissions reduction.

The full potential of the system can only be exploited by adopting an optimization-based EMS able to (i) describe the underground network structure, (ii) capture the short- and long-term dynamics of energy production, storage and consumption, (iii) account for the different temperature levels at which heat and cold are required during the year, (iv) model the time evolution of the geothermal fields, (v) model the scheduling of the conversion technologies installed in the demand clusters. Whereas previous studies have investigated the optimal design and operation of MES coupled with geothermal systems [43–45], and the optimal design

and operation of MES coupled with heating networks [46–48], two important aspects remain uncovered. On the one hand, such studies do not consider the different temperature levels at which heat and cold demands are required. Although this assumption is reasonable for systems where heat and cold are provided by separate units, and allows preserving the linearity of the optimization problem with the associated computational complexity, it prevents the analysis of systems where heat and cold are provided through the same network. On the other hand, the system behavior is investigated during a few representative days along the year, but the interaction between daily and seasonal system dynamics is not accounted for.

These shortcomings stem from the computational complexity arising when describing the non-linear behavior of the system across different time scales. We tackle them by formulating a mixed-integer nonlinear program (MINLP) that accurately describes the physical behavior of the system, and by reducing it to a mixed-integer linear program (MILP) that is able to capture the most relevant aspects and features a reasonable computational complexity. This optimization algorithm aims at minimizing the CO<sub>2</sub> emissions of the multi-energy system while satisfying the heating and cooling demands of end-users. It determines the optimal operation of the system, i.e. the mass flow rate and temperature of the water circulating through the network, and the resulting time evolution of the temperature of the geothermal fields. The optimal solution requires the knowledge of the energy demands, the energy prices, the carbon intensities of the energy grids, and the parameters characterizing the technical performance of the technologies involved. The developed optimization model builds on previously presented work [29, 49, 50] and introduces novel elements by: (i) developing detailed first-principle models and corresponding linear reduced order models to describe the geothermal fields, acting as seasonal storage devices; (ii) formulating and solving a MINLP optimization problem able to determine the optimal value of both the mass flow rate and the temperature of the water circulating in the network; (iii) modeling the structure of the geothermal network; (iv) determining optimal strategies to reduce the carbon footprint of the system and assessing potential savings with respect to currently adopted strategies.

Several techniques have been proposed to solve MINLP. As an example, Elsidio et al. presented bilevel decomposition algorithms able to determine the most profitable synthesis and design of combined heat and power units within a district heating network with thermal storage, while taking into account the yearly scheduling of the system [51, 52]. Inspired by their work, we present a two-stage algorithm, where the original MINLP is linearized by means of McCormick envelopes [53] and the resulting MILP is used to (i) determine a lower bound of the original optimization problem, and (ii) derive information on the optimal time profile of the mass flow rate.

The paper is structured as follows. Section 2 describes the investigated system. Section 3 presents the MINLP optimization problem, while Section 4 presents the linearization and solution techniques. Section 5 discusses the optimization results for the Anergy Grid of ETH Zurich. Finally, in Section 6 conclusions are drawn.

## 2. System description

The Anergy Grid of ETH Zurich is illustrated in Fig. 1; it consists of various underground geothermal fields, which are connected to the served demand clusters, i.e. clusters of buildings of the campus, through a low-temperature water network. More specifically, the system consists of five demand clusters, namely HPL, HPZ, HWN, HCP, HCO (last two included in HCI in Fig. 1), three geothermal fields, namely HPL, HC, HWO, and the centralized heat and cold generation plant, HEZ. The heat and cold generated by HEZ are directly supplied to the five demand clusters using a dedicated connection to each demand cluster, without transiting to the Anergy Grid. The geothermal fields consist of 200 m deep vertical U-shaped borehole heat exchangers. They are used as the energy source, as well as seasonal storage systems to exploit the seasonal shift between heat and cold demands. Each demand cluster includes a substation, which couples the demand cluster and the thermal network as detailed in Fig. 1 with reference to the HPL substation located in the HPL demand cluster. In the five substations, the heat and cold delivered to the buildings are actually produced. Heat is produced via heat pumps (HP) that transfer energy from the underground water to a working fluid by absorbing electricity; cold is produced via two heat exchangers (HE): a low-temperature heat exchanger (LTHE) supplying the cooling demand of the laboratories, and a high-temperature heat exchanger (HTHE)

114 supplying the cooling demand of air conditioning. If a substation requires heat, it is supplied from one of  
 115 the other clusters or underground storages via the grid. If there is waste heat in a cluster, which cannot be  
 116 directly used, it is either used by other clusters or stored in the underground storage, where it stays available  
 117 for later use. The same applies to cold. The water network consists of two rings, one warm and one cold,  
 118 with the temperatures varying between 8 °C and 22 °C.

119 The flexibility provided by the aforementioned design allows reducing the use of fossil-based technologies  
 120 by exploiting the seasonal storage capacity of the geothermal fields. This is best achieved by keeping the  
 121 temperature level of the storage low at the end of spring (i.e. at the end of the heating period), and high at  
 122 the end of summer (i.e. at the end of the cooling period), so as to maximize the cooling and heating capacity  
 123 in summer and winter, respectively [41]. During summer, the cooling demand of the clusters is high, and  
 124 the water going from the substations to the geothermal fields is warmer than the soil. Hence, by circulating  
 125 in the probes the water is cooled while heating up the ground; in this way, the water can absorb heat in  
 126 the heat exchangers of the substation and provide cold. Such a process is reversed in winter: heat demand  
 127 is high, the water going to the probes is colder than the ground and it is heated up while cooling down  
 128 the ground, so as to provide heat to the clusters through the heat pumps of the substations. Whenever  
 129 the Energy Grid is not able to satisfy the energy demands, these are covered by using the conventional  
 130 centralized boiler and the compression chiller unit.

131 Based on the continuous monitoring of the overall system, the first operating years have been evaluated.  
 132 In 2016, the coverage of energy requirements using the Anergy Grid was around 85% for the useful heating  
 133 demand and 60% for the useful cold demand. The remaining amount was conventionally covered by using

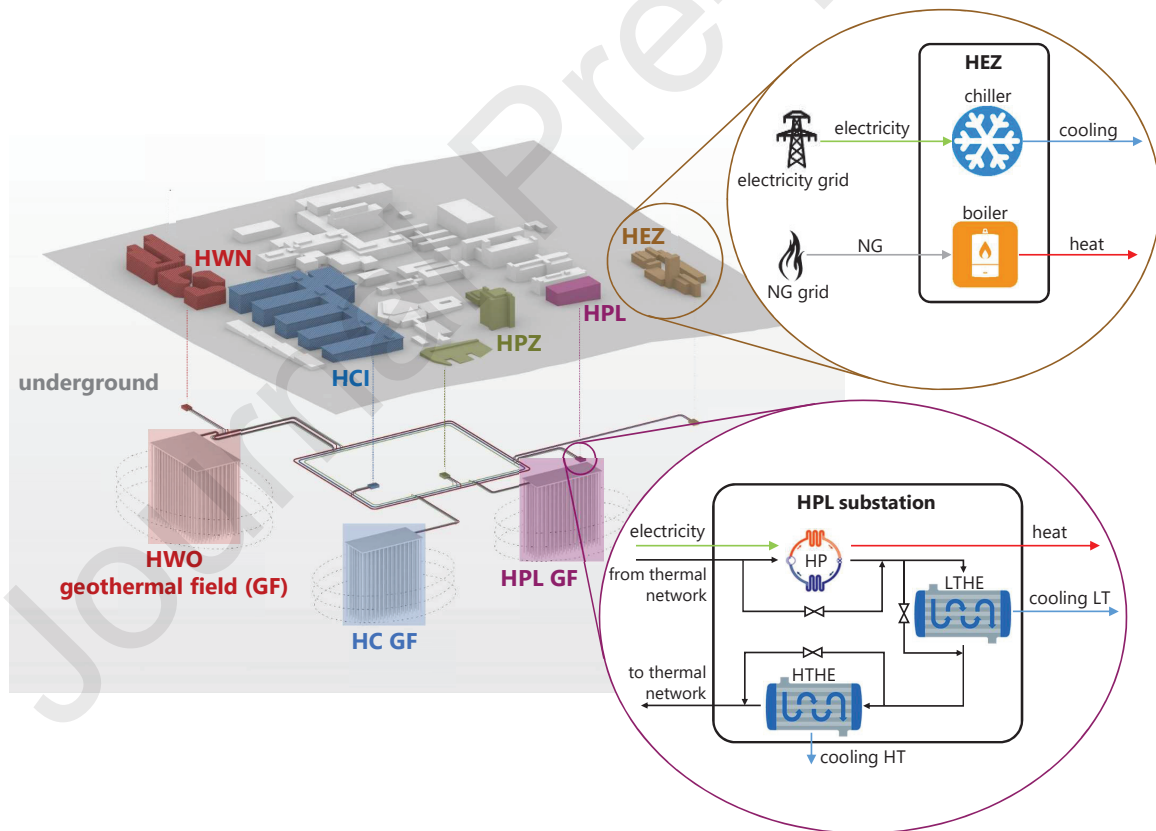


Figure 1: Schematic of the Anergy Grid (AG) system installed at ETH Zurich, adapted from [41].

134 the centralized boiler and compression chiller unit [42].

135 In order to develop a general methodology for optimizing and assessing seasonal energy storage via  
 136 geothermal networks, we model the Anergy Grid as a MES where several geothermal fields are used as  
 137 energy source and storage, and are connected with several demand clusters through a low-temperature  
 138 water network. The scheme of a demand clusters is illustrated in Fig. 2. The yellow box contains the  
 139 cluster substation mentioned above and the energy end-users (buildings). In the substation, heat and cold  
 140 are provided through the heat pump and the heat exchangers, respectively, by using the energy of the  
 141 thermal network. When the thermal network cannot meet the energy demands, heat and cold are provided  
 142 by the central boiler and the central compression chiller. The input and output energy flows defining such  
 143 technologies, as well as the network temperatures, are function of time and are characterized for every time  
 144 interval of the time horizon (one year with hour resolution here). Note that while one heat pump and two  
 145 heat exchangers are installed for each cluster of the Anergy Grid, multiple heat pumps and heat exchangers  
 146 could be used to provide heat and cold at different temperature levels.

147 The water coming from the network enters at temperature  $T_1$ . During the heating season, it goes  
 148 through the heat pump and reduces its temperature to  $T_2$ ; the heat pump uses this low-temperature heat  
 149 and electricity (from renewable energy sources) to provide high-temperature heat to the buildings. During  
 150 the cooling season the water coming from the network goes through the heat exchangers and increases its  
 151 temperature to  $T_3$  (LTHE) and  $T_4$  (HTHE); the heat exchangers use this water to provide cold to the  
 152 buildings. The heat pump and the heat exchanger can be operated separately (e.g. during peak heating or  
 153 cooling seasons) or in combination (e.g., during mid seasons). They can even be operated in a closed loop,

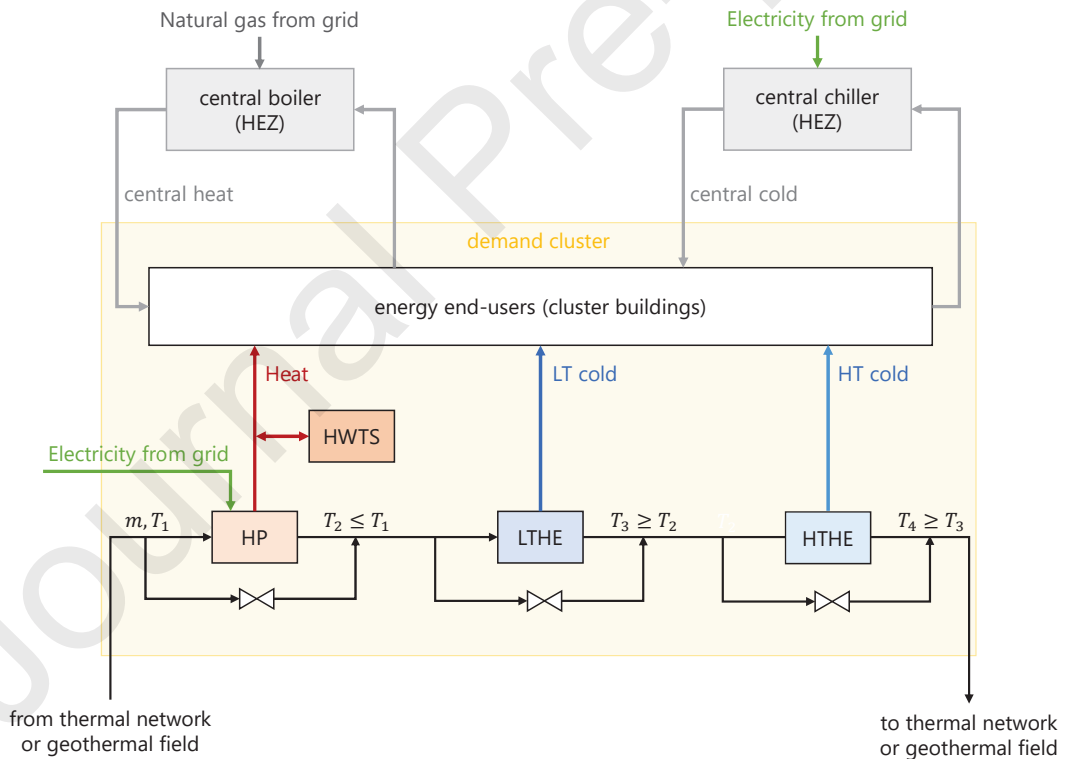


Figure 2: Scheme of a single demand cluster. The yellow box contains the conversion substation and the energy end-users (cluster buildings). The substation consists of a heat pump (HP), a low-temperature heat exchanger (LTHE) and a high-temperature heat exchanger (HTHE) providing heat, LT cold and HT cold, respectively. When needed, heat and cold can be provided by the central system (HEZ).



154 where the heat pump provides water at lower temperature to the heat exchanger, and the heat exchanger  
 155 provides water at higher temperature to the heat pump.

156 The possibility of installing HWTS within the cluster substations is also considered. Due to the relatively  
 157 high thermal losses, low thermal inertia and the low energy density, the HWTS is mostly used to offset short-  
 158 term mismatch between energy production and demand.

### 159 3. System model and optimization framework

160 The optimal operation of the system described in Section 2 is identified through an optimization problem  
 161 that minimizes the CO<sub>2</sub> emissions of the MES by determining the optimal flow rate and temperature of  
 162 the water circulating in the geothermal network, as well as the optimal scheduling of heat pumps and heat  
 163 exchangers, to satisfy the heating and cooling demands of the end-users. The resulting optimization tool  
 164 must account for the different temperatures at which energy is required during the year, and therefore it is  
 165 formulated as a MINLP. This can be written in general form as

$$\begin{aligned} & \min_{\mathbf{x}, \mathbf{y}} (\mathbf{c}_1^T \mathbf{x} + \mathbf{c}_2^T \mathbf{y}) \\ & \text{s.t.} \\ & f(\mathbf{x}, \mathbf{y}) = \mathbf{b} \\ & \mathbf{x} \geq \mathbf{0} \in \mathbb{R}^X, \quad \mathbf{y} \in \{0, 1\}^Y \end{aligned} \quad (1)$$

166 where  $\mathbf{c}_1$  and  $\mathbf{c}_2$  represent the cost vectors associated to the continuous and binary decision variables,  $\mathbf{x}$  and  
 167  $\mathbf{y}$ , respectively;  $f$  is a generic nonlinear function of  $\mathbf{x}$  and  $\mathbf{y}$ , where the nonlinearity arises due to the energy  
 168 balances describing the thermal network and the technology behaviors, and  $\mathbf{b}$  is a constant vector;  $X$  and  
 169  $Y$  indicate the dimension of  $\mathbf{x}$  and  $\mathbf{y}$ , respectively. The binary variables model the non-linearities related to  
 170 the scheduling (i.e. ON/OFF) of the conversion technologies and the direction of the water circulating in  
 171 the thermal network.

172 The complexity of the considered MES requires an optimization tool able to capture both the short-  
 173 and long-term dynamics of the energy production, storage and consumption. Therefore, we consider a  
 174 time horizon of one year with hourly resolution. Time series aggregation (method *M1* in reference [29]) is  
 175 adopted to model the time horizon, thus reducing the computational burden resulting from the large number  
 176 of decision variables, which is due to the complexity of the network and to the length and granularity of  
 177 the time horizon. In the following, all the aspects of the optimization problem, namely input data, decision  
 178 variables, constraints, and objective function are described in detail.

179 In the following, the set of energy carriers is indicated with  $\mathcal{C}$ , the set of clusters with  $\mathcal{D}$ , the set of  
 180 geothermal fields with  $\mathcal{G}$ , and the set of intersection points of the thermal network with  $\mathcal{I}$ . The set of all  
 181 nodes of the thermal network is denoted as  $\mathcal{O}$  and is the union of  $\mathcal{D}$ ,  $\mathcal{G}$  and  $\mathcal{I}$ . The set of branches departing  
 182 from each node of the thermal network is denoted as  $\mathcal{B}$ . The set of available technologies is indicated with  $\mathcal{M}$ ,  
 183 whereas the set of technologies available in the clusters (i.e. heat pumps and heat exchangers) is indicated  
 184 with  $\mathcal{M}_D$ . Unless otherwise indicated, bold symbols indicate vectors in  $\mathbb{R}^N$ , where  $N$  is the length of the  
 185 time horizon.

#### 186 3.1. Input data

187 The carriers considered within the optimization problem are:

- 188 • Electricity (e). It can be imported from the electricity grid and is consumed by the heat pumps and  
 189 by the conventional chiller unit.
- 190 • Natural gas (g). It can be imported from the natural gas distribution grid and is consumed by the  
 191 conventional boiler.
- 192 • Heat (h). It is generated by the heat pumps and by the conventional boiler and is required by the  
 193 clusters.

- 194 • Cold (c). It is generated by the heat exchangers and by the conventional chiller unit and is required  
 195 by the clusters. Here, cold is required at two different levels, denoted as low-temperature (LT) and  
 196 high-temperature (HT) cold (note that any number of cold levels could be considered).

197 Hourly-resolved profiles of 2018 are considered for the carrier demands (see Fig. S1 in the Appendix A).  
 Inputs to the optimization problem are:

- Ambient temperature  $\mathbf{T}^{\text{amb}}$
- Carrier demands  $\mathbf{D}_{i,j} \quad \forall i \in \mathcal{D}, \forall j \in \mathcal{C}$
- Import and export carrier prices  $u_j, v_j \quad \forall j \in \mathcal{C}$
- Carrier carbon intensity  $\epsilon_j \quad \forall j \in \mathcal{C}$
- Technology size  $S_{i,k} \quad \forall i \in \mathcal{O}, \forall k \in \mathcal{M}$
- Parameters describing the performance of the available technologies (reported in Table 1).

198

### 199 3.2. Decision variables

The following decision variables are returned by the optimization problem:

- Scheduling (ON/OFF status) of cluster technologies  $\mathbf{x}_{i,k} \in \{0, 1\}^N \quad \forall i \in \mathcal{D}, \forall k \in \mathcal{M}_D$
- Water mass flow rate in the network nodes and branches  $\mathbf{m}_{i,l} \quad \forall i \in \mathcal{O}, \forall l \in \mathcal{B}$
- Inlet and outlet water temperature for cluster technologies  $\mathbf{T}_{i,k}^{\text{in}}, \mathbf{T}_{i,k}^{\text{out}} \quad \forall i \in \mathcal{D}, \forall k \in \mathcal{M}_D$
- Inlet and outlet water temperature of geothermal fields  $\mathbf{T}_j^{\text{in}}, \mathbf{T}_j^{\text{out}} \quad \forall j \in \mathcal{G}$
- Average temperature of geothermal fields  $\mathbf{T}_j^{\text{F}} \quad \forall j \in \mathcal{G}$
- Average water temperature in the network branches  $\mathbf{T}_l \quad \forall l \in \mathcal{B}$
- Input power for all technologies and carriers  $\mathbf{F}_{i,k,j} \quad \forall i \in \mathcal{D}, \forall k \in \mathcal{M}, \forall j \in \mathcal{C}$
- Output power for all technologies and carriers  $\mathbf{P}_{i,k,j} \quad \forall i \in \mathcal{D}, \forall k \in \mathcal{M}, \forall j \in \mathcal{C}$
- Energy stored in hot water thermal storage  $\mathbf{E}_i \quad \forall i \in \mathcal{D}$
- Flow direction in the network branches  $\mathbf{d}_l \in \{0, 1\}^N \quad \forall l \in \mathcal{B}$

200

### 201 3.3. Constraints

202 The constraints of the optimization problem can be grouped into two categories, namely the constraints  
 203 representing the performance of conversion and storage technologies and the energy balances of the thermal  
 204 network.

205 (I) **Performance of conversion and storage technologies.** The constraints reported in the following  
 206 hold for all time intervals  $t \in \{1, \dots, N\}$  and the parameters describing the performance of the available  
 207 technologies are reported in Table 1. The index specifying the energy carrier relative to the input and  
 208 output powers is described in the text and is not reported in the equations for the sake of simplicity.

- *Conventional boiler and chiller.* For the boiler,  $P_t$  and  $F_t$  refer to generated thermal power and  
 209 consumed fuel power (natural gas LHV), respectively. For the the chiller,  $P_t$  and  $F_t$  refer to  
 210 generated cooling power and consumed electrical power, respectively. For both technologies, the  
 211 generated power is  
 212

$$P_t = \eta F_t \quad (2)$$



Table 1: Technology and network parameters with reference to the Anergy Grid of ETH Zurich, see Fig. 1. A different number of boreholes,  $n$  is installed in the different geothermal fields, namely 101 (HPL), 128 (HC) and 200 (HWO). The profiles of heat and cold demands of the different clusters are reported in Fig. S1 in the Appendix A.

Quantity	Unit	Value
<i>Central generation (HEZ)</i>		
Boiler efficiency, $\eta$	–	0.92
Chiller efficiency, $\eta$	–	3.5
<i>Demand Clusters</i>		
Cooling low temperature, $T_{LT}^c$	°C	12
Cooling high temperature, $T_{HT}^c$	°C	16
Heat pump performance parameter, $\eta_1$	–	6.493
Heat pump performance parameter, $\eta_2$	kW / °C	5.285
Heat pump performance parameter, $\eta_3$	kW	-36.1
Heat pump performance parameter, $\beta_1$	s / kg	1.063
Heat pump performance parameter, $\beta_2$	–	-0.006
Heat pump power parameter, $\delta$	–	0.1
HWTS self-discharge efficiency, $\Lambda$	1 / h	0.005
HWTS ambient loss contribution coefficient, $\Pi$	–	0.001
HWTS charging efficiency, $\eta^{\text{in}}$	–	0.95
HWTS discharging efficiency, $\eta^{\text{out}}$	–	0.95
HWTS charging/discharging time, $\tau$	h	3
<i>Water network</i>		
Specific heat of water, $c$	kJ / (kg K)	4.186
Minimum mass flow rate, $m^{\text{min}}$	kg/s	0
Maximum mass flow rate, $m^{\text{max}}$	kg/s	80
<i>Geothermal fields</i>		
Undisturbed soil temperature, $T^0$	°C	14
Soil thermal conductivity, $\lambda$	W / (K m)	1.8
Soil thermal diffusivity, $\alpha$	m <sup>2</sup> /s	$5.1 \cdot 10^{-7}$
Euler-Mascheroni constant, $\gamma$	–	0.577
Borehole thermal resistance, $R^b$	(m K) / W	88
Depth, $L$	m	200
Minimum temperature, $T^{\text{min}}$	°C	8
Maximum temperature, $T^{\text{max}}$	°C	24

213

where

$$0 \leq F_t \leq S \quad (3)$$

214

Here,  $\eta$  is a constant conversion efficiency and  $S$  the size of the technology, i.e. the rated input

215 power. Heat and cold from conventional technologies are provided via dedicated connections and  
216 are always available to all the clusters.

217 • *Heat pump.* This generates heat by using electricity and by decreasing the temperature of the  
218 water transiting through the demand cluster (see Fig. 2). For all clusters  $i \in \mathcal{D}$ , the generated  
219 thermal power,  $P_{t,i}$ , the absorbed electrical power,  $F_{t,i}$ , the mass flow rate of the water circulating  
220 through the heat pump,  $m_{t,i}$  and its temperatures,  $T_{t,i}^{\text{in}}$  and  $T_{t,i}^{\text{out}}$ , are computed as

$$P_{t,i} = \eta_{t,i} F_{t,i} \quad (4)$$

221

$$P_{t,i} = F_{t,i} + cm_{t,i} (T_{t,i}^{\text{in}} - T_{t,i}^{\text{out}}) x_{t,i} \quad (5)$$

222

$$\delta S_i x_{t,i} \leq F_{t,i} \leq S_i x_{t,i} \quad (6)$$

223 Here,  $x_{t,i}$  is a binary variable indicating whether device  $i$  is turned on at time interval  $t$ , producing  
224 power but also incurring in a minimum power consumption  $\delta S_i$ ;  $c$  is the specific heat of water.  
225 The conversion efficiency,  $\eta_{t,i}$ , is a function of the heat pump operating temperatures as

$$\eta_{t,i} = \frac{T^{\text{cond}}}{T^{\text{cond}} - T_{t,i}^{\text{eva}}} \xi \quad (7)$$

226 where  $\xi$  is the Carnot efficiency;  $T^{\text{cond}}$  is the heat pump condensation temperature, which is  
227 defined by the heat demand and considered to be constant at 40 °C.  $T_{t,i}^{\text{eva}}$  is the heat pump  
228 evaporation temperature, which is a function of the inlet and outlet temperatures of the water  
229 going through the heat pump, and is computed by

$$T_{t,i}^{\text{out}} = T_{t,i}^{\text{in}} - (T_{t,i}^{\text{in}} - T_{t,i}^{\text{eva}}) \left[ 1 - \exp\left(-\frac{UA}{cm_{t,i}}\right) \right] x_{t,i} \quad (8)$$

230 where  $U$  is the overall heat transfer coefficient and  $A$  the heat exchange area of the evaporator.

231 • *Heat exchanger.* This is modeled as a counter-current heat exchanger that provides the cooling  
232 power  $P_{t,i}$ , at temperature  $T_{t,i}^{\text{in}}$ , according to

$$P_{t,i} = cm_{t,i} (T_{t,i}^{\text{out}} - T_{t,i}^{\text{in}}) x_{t,i} \quad (9)$$

233

where

$$0 \leq P_{t,i} \leq S_i \quad (10)$$

234 Here,  $x_{t,i}$  is a binary variable enabling the bypass of the heat exchanger when the inlet temper-  
235 ature exceeds the value specified by the demand cluster,  $T^c$ :

$$T_{t,i}^{\text{in}} \leq T^c \quad (11)$$

236 Two heat exchangers, characterized by two different values of  $T_c$ , are present in the Energy Grid  
237 of ETH Zurich (see Section 2).

238 • *Geothermal field.* The heat diffusion through the soil is studied by modeling the boreholes as  
239 infinite line heat sources. Assuming a homogeneous soil with constant properties, the temperature  
240 distribution resulting from each borehole is given by the solution reported by Carslaw and Jaeger,  
241 who determined the dynamic response of the ground temperature to a constant heat step [54].  
242 This is usually referred to as the  $g$ -function,  $g$ , or the dimensionless temperature response factor,  
243 of the borehole [55], and it can be approximated by a logarithmic function of time that depends

244 on the geometry of the borehole (i.e. depth and radius) and the properties of the soil (i.e. thermal  
245 diffusivity and conductivity):

$$g_b(r, t) = \log\left(\frac{4\alpha t}{r^2}\right) - \gamma \quad (12)$$

246 where  $r$  is the radius of the borehole and  $t$  the time instant;  $\alpha$  is the thermal diffusivity of  
247 the soil and  $\gamma$  the Euler-Mascheroni constant; the subscript "b" indicates that Eq. (12) applies  
248 to a single borehole. The  $g$ -function is computed with hourly resolution along the time horizon  
249 of one year. Later, more accurate numerical solutions [56–59] and analytical approximations  
250 [60, 61] were presented.

251 The geothermal fields are modeled by considering the thermal interference among individual  
252 boreholes. More specifically, we adopt the spatial superposition principle proposed in references  
253 [58, 62], which results in an aggregated dynamic response of the overall geothermal fields, i.e.  
254 the  $g$ -function appearing hereafter and shown in Fig. S3 in Appendix B. This depends on the  
255 properties of the soil and on the geometry of the field (i.e. depth, radius and location of the  
256 boreholes). Furthermore, since the aggregated  $g$ -function describes the thermal response of the  
257 geothermal field to a heat step, the time varying heat injection/extraction is modeled through  
258 the temporal superposition of several heat steps. Therefore, the average temperature of the  $j$ -th  
259 geothermal field,  $\forall j \in \mathcal{G}$ , is described as follows [63, 64]:

$$T_{t,j} = T^0 + \frac{1}{2\pi\lambda Ln_j} \sum_{k=1}^t (Q_{k,j} - Q_{k-1,j}) g(r_j, t - k) \quad (13)$$

260 where  $T^0$  is the undisturbed soil temperature,  $\lambda$  the thermal conductivity of the ground,  $L$  the  
261 depth of the borehole heat exchangers,  $n_j$  the number of boreholes, and  $r_j$  the radius of the  
262 geothermal field;  $Q$  indicates the net injected thermal power, i.e.  $P - F$ , which is positive if  
263 heat is extracted and negative if heat is injected. The same depth and properties of the soil are  
264 considered for all geothermal fields, whereas these can differ in terms of radius and number of  
265 boreholes. The net injected thermal power is expressed as

$$Q_{t,j} = cm_{t,j} (T_{t,j}^{\text{out}} - T_{t,j}^{\text{in}}) \quad (14)$$

266 where  $m$ ,  $T_{t,j}^{\text{in}}$  and  $T_{t,j}^{\text{out}}$  are the mass flow rate, inlet and outlet temperature of the water circu-  
267 lating through the geothermal field.

268 The energy balance at the wall of a single borehole allows to write

$$\frac{Q_{t,j}}{Ln_j} = \frac{1}{R^b} (T_{t,j} - T_{t,j}^w) \quad (15)$$

269 where  $R^b$  is the thermal resistance of the borehole and  $T_{t,j}^w$  the water average temperature, which  
270 is approximated as the average between the inlet and outlet water temperatures. The model of  
271 the geothermal field is validated using the measurements shown in Fig. S2 in Appendix B.

272 Within the system optimization, the temperature of the geothermal fields is constrained between  
273 a minimum and a maximum value because of environmental limitations:

$$T^{\text{min}} \leq T_{t,j} \leq T^{\text{max}} \quad (16)$$

274 Furthermore, a periodicity constraint is imposed on the geothermal fields. This forces the same  
275 field temperature at the beginning and at the end of the year, thus enabling a sustainable field  
276 operation across the years,

$$T_{0,j} = T_{N,j} \quad (17)$$

- 277 • *Hot water thermal storage (HWTS)*. This type of thermal storage is the cheapest and most  
 278 deployed thermal storage technology. Due to its high energy losses and low energy density,  
 279 HWTS is mostly used to offset short-term mismatch between thermal energy generation and  
 280 use. For all clusters  $i \in \mathcal{D}$ , the energy stored within the HWTS,  $E_{t,i}$ , is expressed through the  
 281 following linear dynamics [49]

$$E_{t,i} = E_{t-1,i} (1 - \Lambda \Delta t) - \left( \Pi S_i h_t + \eta^{\text{in}} F_{t,i} - \frac{1}{\eta^{\text{out}}} P_{t,i} \right) \Delta t \quad (18)$$

282 where

$$E_{0,i} = E_{N,i} \quad (19)$$

283

$$h_t = \frac{T^{\text{min}} - T_t^{\text{amb}}}{T^{\text{max}} - T^{\text{min}}} \quad (20)$$

284

$$0 \leq E_{t,i} \leq S_i \quad (21)$$

285

$$-\frac{S_i}{\tau} \leq F_{t,i}, P_{t,i} \leq \frac{S_i}{\tau} \quad (22)$$

286 Here,  $\Lambda$  and  $\Pi$  are self-discharge parameters, and  $h_t$  expresses the influence of ambient temper-  
 287 ature on the energy losses of the storage unit, as suggested in [65];  $\eta^{\text{in}}$  and  $\eta^{\text{out}}$  indicate the  
 288 charging and discharging efficiency, respectively;  $\Delta t$  is the duration of the  $t$ -th time interval  
 289 (between time steps  $t - 1$  and  $t$ );  $\tau$  is the time required to fully charge or discharge the storage.  
 290 Here, we consider water stored at  $T^{\text{max}} = 55^\circ\text{C}$  and cooled to  $T^{\text{min}} = 40^\circ\text{C}$ . Also, we consider  
 291 the same value for charging and discharging efficiency. The periodicity constraint, Eq. (19),  
 292 imposes the same storage level at the beginning and at the end of the yearly time horizon.

293 (II) **Thermal network mass and energy balances.** The mass and energy balances are defined for all  
 294 intersection points of the thermal network, as well as for the demand clusters.

- 295 • *Network mass and energy balances.* Each intersection point in the thermal network is a connec-  
 296 tion of three branches, which are in turn connected to three different nodes (with references to  
 297 Section 3.2,  $\mathcal{B} = \{1, 2, 3\}$ ). Each node can be a cluster, a geothermal field, or another intersection  
 298 point. The mass balance for the  $i$ -th intersection point,  $\forall i \in \mathcal{I}$ , is

$$\sum_{l=1}^3 d_{t,i,l} m_{t,i,l} = \sum_{l=1}^3 (1 - d_{t,i,l}) m_{t,i,l} \quad (23)$$

299 where  $m_{t,i,l}$  is the mass flow rate of the water entering or exiting the intersection point  $i$  through  
 300 the branch  $l$  at time interval  $t$ ;  $d_{t,i,l}$  is a binary variable specifying whether the water flow is  
 301 entering ( $d = 1$ ) or exiting ( $d = 0$ ) the intersection point.

302 The energy balance for the  $i$ -th intersection point is

$$\sum_{l=1}^3 d_{t,i,l} m_{t,i,l} T_{t,i,l}^{\text{out}} = \sum_{l=1}^3 (1 - d_{t,i,l}) m_{t,i,l} T_{t,i,l}^{\text{in}} \quad (24)$$

303

$$y_{t,i} [d_{t,i,l} T_{t,i,l}^{\text{out}} + (1 - d_{t,i,l}) T_{t,i,l}^{\text{in}}] = \gamma_{t,i}, \quad l = \{1, 2, 3\} \quad (25)$$

where

$$y_{t,i} = 2 - \sum_{l=1}^3 d_{t,i,l} \quad (26)$$

where Eq. (25) imposes that, in the case of an entering flow being split into two exiting flows, the temperatures of all flows are the same; Eq. (26) defines the binary variable  $y_{t,i}$ , which states whether a node mixes two flows ( $y_{t,i} = 0$ , i.e. the temperature of each branch is defined by Eq. (24)) or split one flow ( $y_{t,i} = 1$ , i.e. all branches are at the same temperature).

- *Cluster energy balance.* The energy balance within the  $i$ -th cluster states that the generated energy must equal the energy demand for each energy carrier  $j \in \mathcal{C}$ . This is expressed as

$$\sum_{k \in \mathcal{M}} (P_{t,i,k,j} - F_{t,i,k,j}) - D_{t,i,j} = 0 \quad (27)$$

where  $P_{t,i,k,j}$  and  $F_{t,i,k,j}$  are the produced and consumed power of carrier  $j$  by technology  $k$  in cluster  $i$  at time interval  $t$ ;  $D_{t,i,j}$  is the demand required by the end-users.

Eq. (27) states that the power demand of each cluster must be satisfied exactly, which represents the reference case for our analysis. However, the Anergy Grid system allows for the flexibility to produce power beyond the demand and to release the excess power to the environment (i.e. to dissipate energy), if this improves the value of the objective function. In this case, Eq. (27) is replaced by the following equations

$$\sum_{k \in \mathcal{M}} (P_{t,i,k,j} - F_{t,i,k,j}) - D_{t,i,j} \geq 0 \quad (28)$$

$$\sum_{t=1}^N \sum_{i \in \mathcal{D}} \sum_{j \in \mathcal{C}} \left[ \sum_{k \in \mathcal{M}} (P_{t,i,k,j} - F_{t,i,k,j}) - D_{t,i,j} \right] \leq \phi \sum_{t=1}^N \sum_{i \in \mathcal{D}} \sum_{j \in \mathcal{C}} D_{t,i,j} \quad (29)$$

where  $\phi$  is defined as the amount of energy that can be released to the environment normalized over the total annual energy demand ( $\sum_{t=1}^N \sum_{i \in \mathcal{D}} \sum_{j \in \mathcal{C}} D_{t,i,j} \Delta t$ ).

### 3.4. Objective function

The objective function to be minimized is given by the annual CO<sub>2</sub> emissions of the system,  $e$ . These are due to electricity and natural gas imported from the distribution grids to run the heat pumps and the centralized chiller and boiler. They are expressed as

$$e = \sum_{j \in \mathcal{C}} \epsilon_j \sum_{i \in \mathcal{I}} \sum_{k \in \mathcal{M}} \sum_{t=1}^N F_{t,i,k,j} \Delta t \quad (30)$$

where  $\epsilon_j$  is the carbon intensity (inclusive of the entire life cycle) of carrier  $j$ . Here, the carbon intensity of electricity and natural gas are  $\epsilon_e = 30 \text{ g}_{\text{CO}_2}/\text{kWh}$  (corresponding to the life cycle assessment emissions of low-carbon electricity produced by renewable energy sources) and  $\epsilon_g = 237 \text{ g}_{\text{CO}_2}/\text{kWh}$ , respectively.

## 4. Optimization strategy

We aim at minimizing the CO<sub>2</sub> emissions of the system while satisfying the heating and the cooling demands. To do so, we determine the hourly scheduling (ON/OFF) and operations of the heat pumps and of the heat exchangers for the five demand clusters, the heat exchanged with the three geothermal fields and their temperature evolution, and the temperature and mass flow rate profiles for all branches of the network. The implemented optimization procedure, illustrated in Fig. 3, proceeds as follows:

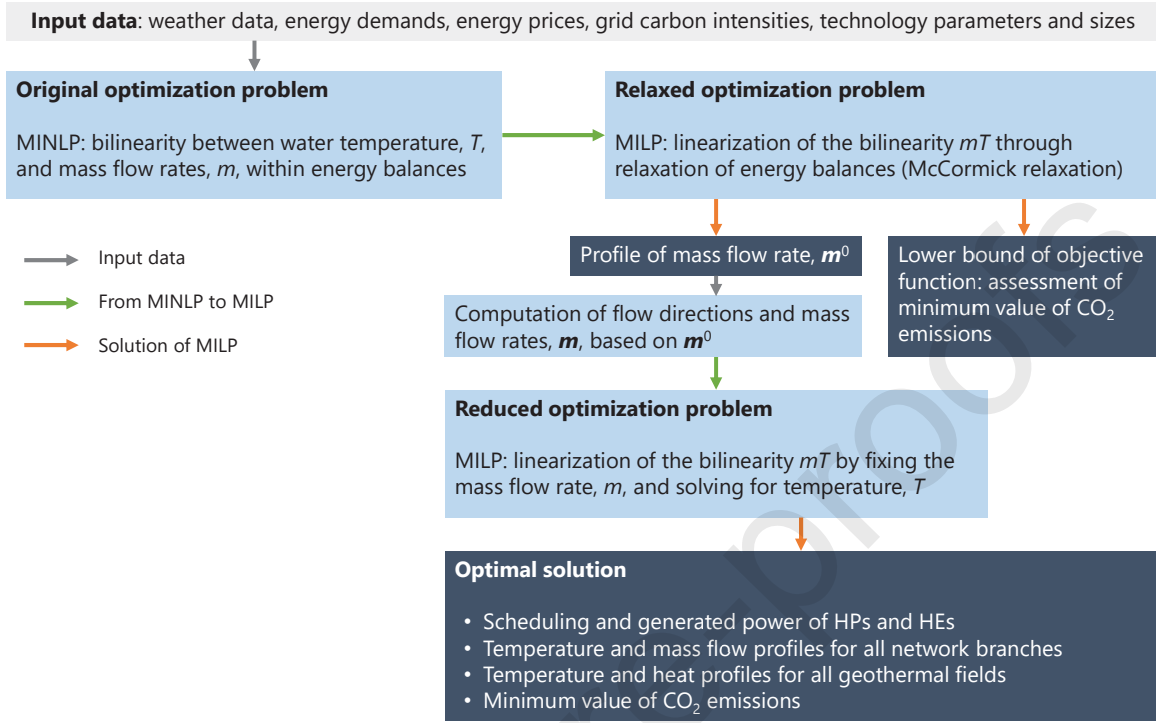


Figure 3: Summary of the optimization procedure developed to determine the system operation that minimizes  $\text{CO}_2$  emissions while satisfying the energy demands.

- 334 (1) A MINLP problem is formulated that describes the nonlinear behavior of the system, i.e. Eqs. (2)-  
 335 (30). Two major sources of nonlinearity are (i) the efficiency of the heat pumps, given by Eqs. (4),  
 336 (7) and (8), which is a nonlinear function of inlet and outlet temperatures, and (ii) the energy output  
 337 of the heat exchangers, which is proportional to the product of mass flow rate and temperature (i.e.  
 338 product of decision variables). The dynamic response of the geothermal fields (i.e. the g-function) is a  
 339 known quantity, not subject to optimization, and therefore does not introduce nonlinearities. Also, the  
 340 nonlinearities arising from the product of continuous and binary decision variables can be eliminated by  
 341 reformulating them as combination of linear constraints [66].
- 342 (2) The MINLP problem formulated in (1) cannot be solved efficiently due to the large number of decision  
 343 variables for this class of mathematical optimization problems. Therefore, it is relaxed into a MILP  
 344 problem by (i) defining a linear approximation of the heat pump performance described by Eqs. (4), (7)  
 345 and (8), and (ii) adopting a linear relaxation of the heat exchange model in Eqs. (5), (9), (14) and (24).  
 346 For the heat pumps, Eqs. (4), (7) and (8) are replaced by the following linear approximations:

$$P_{t,i} = \eta_1 F_{t,i} + (\eta_2 T_{t,i}^{\text{in}} + \eta_3) x_{t,i} \quad (31)$$

$$T_{t,i}^{\text{out}} = T_{t,i}^{\text{in}} - (T_{t,i}^{\text{in}} - T_{t,i}^{\text{eva}})(\beta_1 m_{t,i} + \beta_2) x_{i,t} \quad (32)$$

348 For the heat exchange, the product  $mT$  appearing in Eqs. (5), (9), (14) and (24) is written through its  
 349 McCormick relaxation [67, 68], i.e. by introducing an auxiliary variable  $\tilde{m} = mT$ , which is bounded  
 350 between the minimum and the maximum value of the product itself. Namely, the equality constraints  
 351 involving  $mT$  are replaced by inequality constraints involving  $\tilde{m}$ . This represents the most relevant



source of nonlinearity. The resulting MILP, which is hereafter referred to as the *relaxed MILP*, is then solved. The flow direction in all the network branches is optimized but remains constant during the year so as to reduce the computational complexity of the problem.

- (3) The relaxed MILP has a greater feasibility space than the original MINLP, which implies that (i) the solution of the relaxed MILP might be unfeasible when used as input to the original MINLP, and (ii) the optimal values of the objective function of the MILP is lower than or equal to that of the MINLP, i.e. the value of CO<sub>2</sub> emissions of the system cannot be lower than that found through the relaxed MILP.

The relaxed MILP is solved by modeling the yearly time horizon through ten typical days. This value is chosen after a sensitivity analysis showing deviations smaller than 1% with respect to the full-resolution optimization for a number of typical days greater than eight. The value of 1% represents the MIP gap of the MILP, which defines the precision of the optimal solution.

- (4) The profile of mass flow rate obtained through the relaxed MILP, denoted as  $\mathbf{m}^0$ , describes the time evolution of the mass flow rate within the clusters, the geothermal fields and the network branches. However, we note this solution generally underestimates the optimal value of the mass flow rate, because it selects the lower bound identified by the McCormick inequality constraints imposed on  $\tilde{m}$ . Therefore, we determine the actual mass flow rate circulating through the thermal network, denoted as  $\mathbf{m}$ , by increasing the value of  $\mathbf{m}^0$  through three different heuristic approaches:

- (i) by replacing  $\mathbf{m}^0$  with a higher constant value  $\nu$ , i.e.  $m_t = \nu, \forall t \in \{1, \dots, N\}$ ;
- (ii) by scaling up  $\mathbf{m}^0$  through a constant multiplication factor  $\zeta$ , i.e.  $m_t = m_t^0 \zeta, \forall t \in \{1, \dots, N\}$ ;
- (iii) by shifting  $\mathbf{m}^0$  through a constant additive factor  $\kappa$ , i.e.  $m_t = m_t^0 + \kappa, \forall t \in \{1, \dots, N\}$ .

The profile of mass flow rate obtained in this way is fixed and used as an input to the original MINLP problem, resulting in a *reduced MILP* having only temperatures as decision variables. The results in Section 5 are obtained by solving this reduced MILP, which is the ultimate end point of the optimization procedure.

To compare the different heuristic approaches, we introduce the normalized average mass flow rate,  $\mu$ , which is the ratio of the average value of  $\mathbf{m}$  to the average value of  $\mathbf{m}^0$ :

$$\mu = \frac{\sum_{t=1}^N m_t}{\sum_{t=1}^N m_t^0} \quad (33)$$

For the three heuristic approaches introduced above  $\mu$  is expressed as

$$\begin{aligned} \text{(i)} \quad \mu &= \frac{N\nu}{\sum_{t=1}^N m_t^0} \\ \text{(ii)} \quad \mu &= \zeta \\ \text{(iii)} \quad \mu &= \frac{N\kappa}{\sum_{t=1}^N m_t^0} + 1 \end{aligned}$$

where larger values of  $\nu$ ,  $\zeta$  and  $\kappa$  result in larger values of mass flow rate and therefore  $\mu$ .

- (5) The solution of the reduced MILP returns the minimum value of CO<sub>2</sub> that can be attained and the corresponding optimal operation strategy. This is given by the time evolution of (i) the scheduling and the generated power of heat pumps and heat exchangers, (ii) the heat injected/extracted to/from the geothermal fields, (iii) the temperature of the geothermal fields, (iv) the mass flow profiles across the network.

The optimization problem is formulated in Matlab [69] by using the YALMIP interface [70]. The reduced MILP is solved by using CPLEX 12.8.0 [71], set to have a relative MIP gap of 1%.

## 5. Results and discussion

First, the results of the analysis are described and discussed by referring to a single demand cluster connected to a single geothermal field, namely the HPL demand cluster and the HPL geothermal field. This allows deriving general trends valid for all demand clusters and helps understanding the behavior of the entire Energy Grid of ETH Zurich, which is then presented.

The scope of the analysis is to determine the operation strategy that minimizes the CO<sub>2</sub> emissions of the system. To this end, we identify the most relevant operation and design quantities and we investigate their optimal values. The most relevant quantities prove to be the mass flow rate circulating through the thermal network, the minimum-power fraction of the heat pump, the presence of hot water thermal storage, the operation of the conversion technologies (i.e. heat pump and heat exchangers), and the possibility of dissipating energy to the environment. Overall, the CO<sub>2</sub> emissions are minimized when the system flexibility is maximized, i.e. when the thermal network is able to meet both the heating and cooling demands at the same time.

### 5.1. HPL demand cluster and geothermal field

The system showed in Fig. 2 is considered, where the water circulating through the cluster substation (i.e. heat pump and heat exchangers) comes from and goes to a geothermal field. This describes the HPL demand cluster connected to the HPL geothermal field. The flow direction in the network is fixed, with the following steps: a given mass flow rate,  $m$ , leaves the geothermal field at temperature  $T_1$ ; the water decreases its temperature by going through the HP, if this is ON, or it maintains the same temperature by bypassing it, if this is OFF, hence  $T_2 \leq T_1$ ; the water increases its temperature by going through the LTHE, if this is ON, or it maintains the same temperature by bypassing it, if this is OFF, hence  $T_3 \geq T_2$ ; the same applies to the HTHE, hence  $T_4 \geq T_3$ ; the water increases or decreases its temperature by going through the boreholes of the geothermal field, depending on the field temperature (see Eqs. (13) to (15)).

#### 5.1.1. Minimum CO<sub>2</sub> emissions

Fig. 4 shows the specific CO<sub>2</sub> emissions of the system as function of the mass flow rate circulating in the network,  $\mu$  (Fig. 4-a), of the minimum-power fraction of the heat pump,  $\delta$ , and of the presence of hot water thermal storage, HWTS (Fig. 4-b), which have proved to be the most relevant quantities to determine the minimum attainable value of CO<sub>2</sub> emissions of the single HPL cluster. The specific CO<sub>2</sub> emissions are normalized over the total annual heating and cooling demand, and the normalized average mass flow rate is used to express the mass flow rate (see Eq. (33) in Section 4). For comparison, Fig. 4 reports (i) the value of CO<sub>2</sub> emissions of the HPL demand cluster obtained by using the centralized heating and cooling technologies, without deploying the thermal network (horizontal black dashed line), and (ii) the value of CO<sub>2</sub> emissions of the HPL demand cluster achieved with the current operation (horizontal gray dotted-dashed line) [42, 72].

Fig. 4-a reports the CO<sub>2</sub> emissions obtained when fixing the mass flow rate through the three heuristic approaches described in Section 4, which are indicated by (i) the orange squares - constant mass flow rate, (ii) the green diamonds - time-dependent mass flow rate, and (iii) the blue circles - time-dependent mass flow rate. Two main considerations can be made. First, a time-dependent mass flow rate results in lower values of the CO<sub>2</sub> emissions, as it allows following the time evolution of heating and cooling demands. In fact, the differences between the three strategies are small, as the system can adapt to different mass flow rates via different technology operations, as detailed in the following. Second, for all approaches there is an optimal value of  $\mu$  (i.e. an optimal value of average mass flow rate) that minimizes the CO<sub>2</sub> emissions. This stems from the trade-off between low values of mass flow rate, for which only a small fraction of the energy demand is satisfied, and high values of mass flow rate, for which the heating and cooling demands cannot be satisfied at the same time because one of the two would be exceeded (and no partial bypass is allowed by the system). To clarify this concept, consider a high value of water mass flow rate during a time of the year in which the heating demand is higher than the cooling one (e.g. autumn). The water would circulate through the heat pump, hence meeting the heating demand; however, it would bypass the heat exchangers (as too much cooling would be provided), hence not providing any cooling. Similar considerations hold true

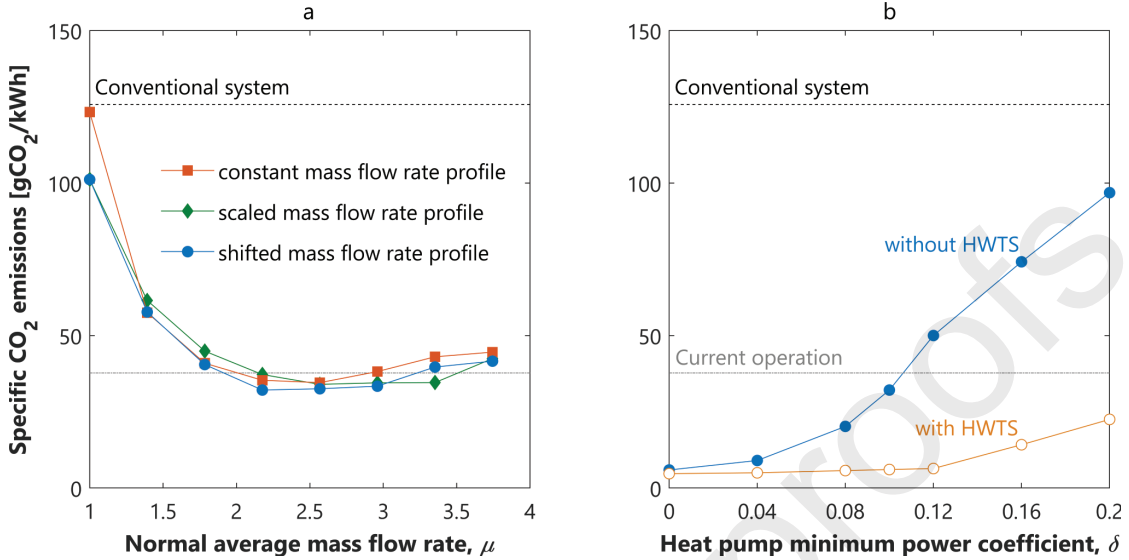


Figure 4: Specific CO<sub>2</sub> emissions of the HPL demand cluster as function of (a) normalized average mass flow rate circulating in the network,  $\mu$ , and (b) minimum-power fraction of the heat pump,  $\delta$ , and of the presence of hot water thermal storage, HWTS. Three different mass flow rate profiles are shown in (a), corresponding to the three strategies introduced in Section 4. A shifted mass flow rate profile with  $\mu = 2.18$ , which enables the lowest value of CO<sub>2</sub> emissions, is used in (b).

435 when the cooling demand is higher than the heating one. Hereafter, we use strategy (iii) to fix the water  
 436 mass flow rate, as it results in the lowest values of CO<sub>2</sub> emissions and allows operating the system with the  
 437 lowest mass flow rates.

438 Fig. 4-b shows the impact of the HP minimum-power fraction on the total CO<sub>2</sub> emissions of the system  
 439 (see Eq. (6)). The same analysis is performed with and without the possibility of installing the HWTS. The  
 440 value of  $\delta$  identifies the minimum heating demand the can be satisfied by the heat pump; lower values of  $\delta$   
 441 imply the possibility of covering a wider range of heating demand and result in lower CO<sub>2</sub> emissions. From a  
 442 design perspective, this allows quantifying the advantage of having a modular heat pump installation (lower  
 443 minimum-power fraction) over having a unique technology (higher minimum-power fraction).

444 Deploying the HWTS allows to reduce the CO<sub>2</sub> emissions at high values of  $\delta$ , where the storage system  
 445 is needed to satisfy heating demands smaller than the HP minimum-power fraction. The larger the value  
 446 of  $\delta$ , the larger the fraction of heating demand satisfied by the HWTS, the larger the benefit in terms of  
 447 CO<sub>2</sub> emissions; when  $\delta = 0$  there is no advantage in installing the HWTS, since the HP can cover the entire  
 448 range of heating demand. Overall, the short-term flexibility provided by the storage system allows to (i)  
 449 operate the HP during more hours of the year, and (ii) directly compensate the mismatch between heat  
 450 generation and demand. HWTS is a mature and relatively cheap technology, which makes its installation a  
 451 low hanging fruit for reducing the system's emissions. A reference value of  $\delta = 0.1$  is considered across the  
 452 paper, which characterizes the technologies installed in the Anergy Grid system [42, 72].

### 453 5.1.2. System operation

454 Let us now investigate in more detail the optimal operation of the single HPL cluster. Fig. 5 shows the  
 455 optimal operation of the heat pump and of the heat exchangers during every hour of the year. On the left-  
 456 hand side we compare the hourly energy production with the corresponding energy demand (transparent).  
 457 On the right-hand side we show the frequency with which the technologies are switched ON and OFF, by  
 458 defining the ON/OFF switching time as the number of hours after which a technology changes its status  
 459 from ON to OFF or viceversa. The yearly operating hours,  $H$ , and the yearly switches,  $s$ , are also reported.

460 The HP supplies about 98% of the heating demand required by the cluster, either directly or through  
 461 the HWTS, with the central boiler mostly contributing during the winter peaks. During the year, the heat

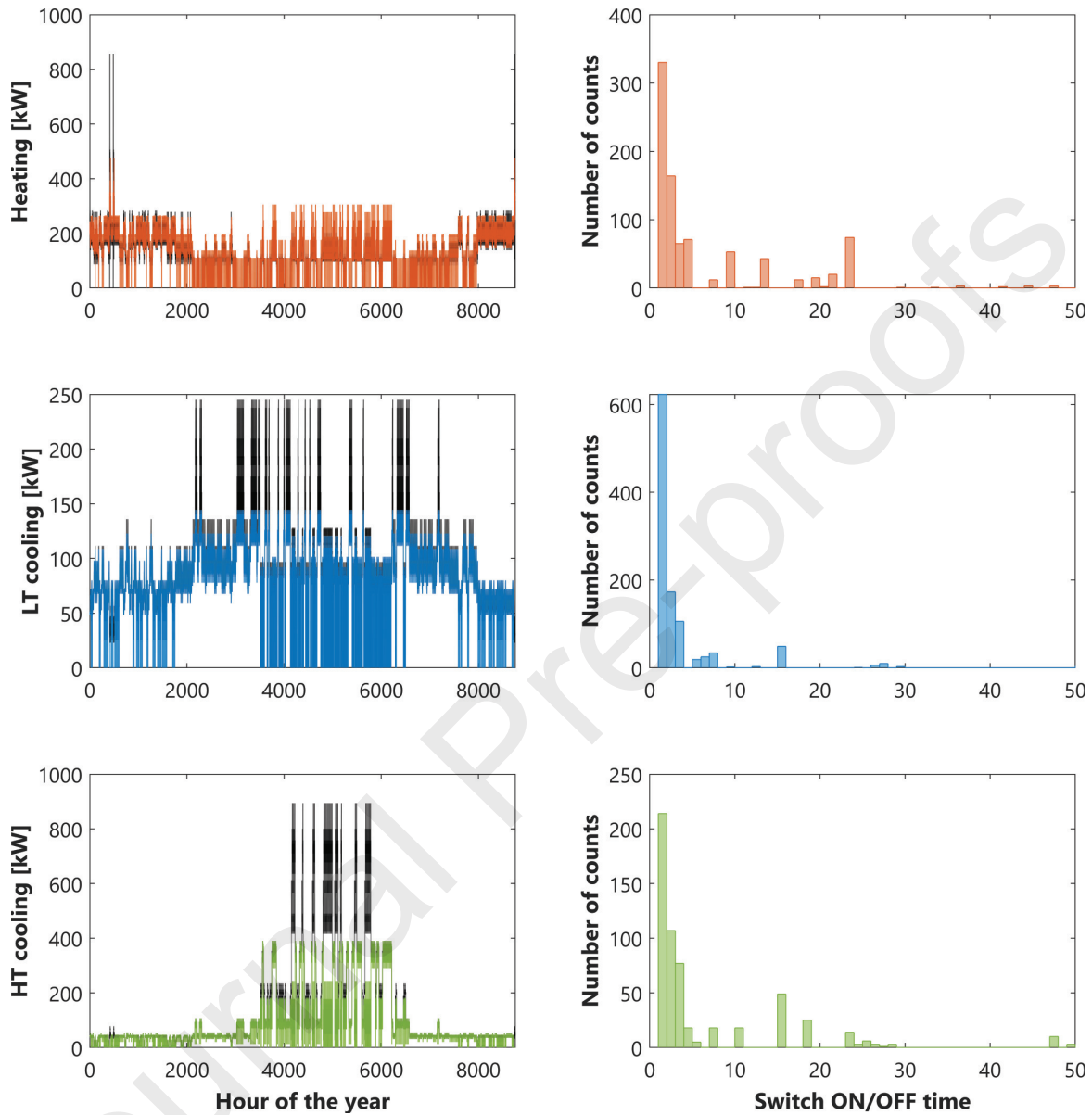


Figure 5: Optimal operation of HPL demand cluster. Time profiles of energy generation (left) and number of counts of ON/OFF switch times (right) for heating, LT cooling and HT cooling. Heating is supplied via HP, LT cooling via LTHE, and HT cooling via HTHE. On the left, the energy generation is superposed to the corresponding energy demand (transparent). On the right, the number of yearly operating hours,  $H$ , and the number of yearly switches,  $s$ , are reported. Shifted mass flow rate profile with  $\mu = 2.18$  and  $\delta = 0.1$ .

462 pump is operated for about 7000 hours and it is most often switched ON/OFF every one or two hours,  
 463 though longer operating periods of about 10 and 20 hours are not uncommon. The longest periods without  
 464 switches last about 800 hours, but periods longer than 60 hours occur about 20 times per year.

465 The LTHE supplies about 79% of the LT cooling demand and is operated for about 7900 hours. It is  
 466 most often switched ON/OFF every one or two hours and common operating periods are shorter than 10

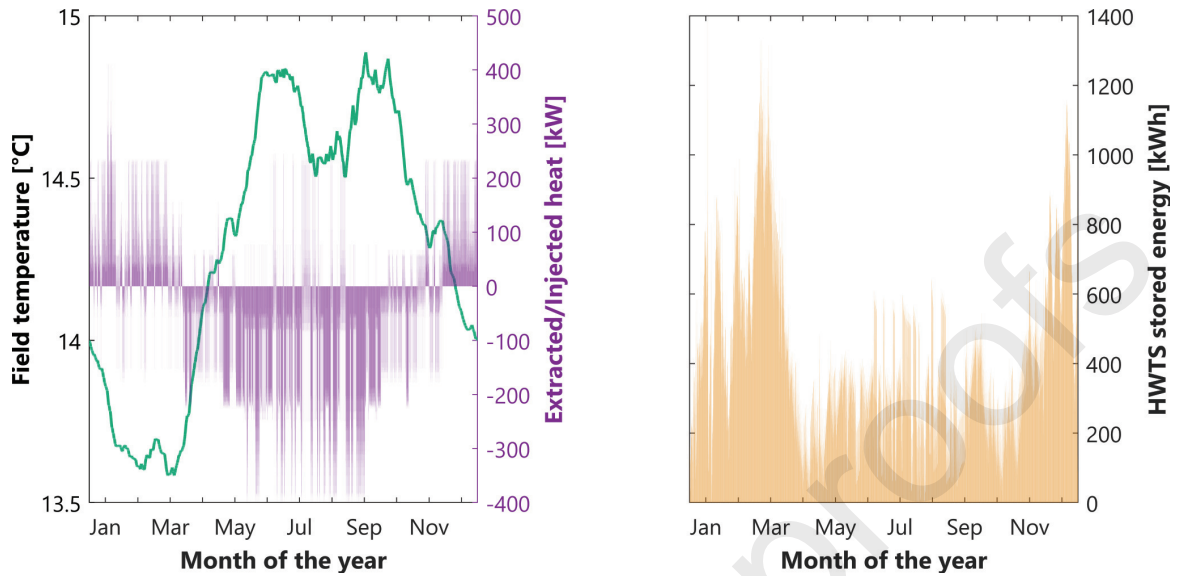


Figure 6: Optimal storage operation for the HPL demand cluster. (a) Optimal temperature profile of the geothermal field (green line - left vertical axis) and of the injected/extracted heat (positive/negative values of the yellow line - right vertical axis). (b) Optimal profile of stored energy within HWTS. Shifted mass flow rate profile with  $\mu = 2.18$  and  $\delta = 0.1$ .

467 hours. The longest periods without switches last about 1700 hours, but periods longer than 50 hours occur  
 468 about 20 times per year.

469 Similar considerations can be made for the HTHE, which supplies about 66% of the HT cooling demand,  
 470 with the central chiller mostly contributing during the summer peaks. It is most often switched ON/OFF  
 471 every one, two or three hours, but longer operating periods up to 30 hours are not uncommon. The longest  
 472 periods without switches last about 1100 hours, but periods longer than 70 hours occur about 20 times per  
 473 year.

474 Furthermore, the relatively low coverage of cooling demand demonstrates that the heating demand is  
 475 the major responsible for  $\text{CO}_2$  emissions. This is because conventional heat generation is based on natural  
 476 gas, while conventional cold generation is based on electricity coming from renewable energy sources [73].

477 The optimal behavior of the storage systems is illustrated in Fig. 6, which shows (a) the temperature  
 478 profile and the extracted/injected heat of the geothermal field and (b) the energy stored within the HWTS.  
 479 In Fig. 6-a the heat (yellow line - right vertical axis) is positive when extracted from the ground (the water  
 480 circulating through the geothermal field is heated up) and negative when injected into the ground (the water  
 481 circulating through the geothermal field is cooled down). Heat is extracted during winter, which results  
 482 in a decreasing temperature of the geothermal field (green line - left vertical axis), and is injected during  
 483 summer, which results in an increasing temperature of the geothermal field. Two distinct temperature  
 484 peaks are observed in summer following two greater heat injections. After these, the temperature tends to  
 485 settle to the undisturbed value of  $14^\circ\text{C}$ . The periodicity constraint given by Eq. (17) imposes that the field  
 486 temperature at the beginning and at the end of the year is equal to the undisturbed value, hence constraining  
 487 the heat extraction/injection and ensuring a long-term sustainable operation of the field.

488 Fig. 6-b shows the operation of the HWTS. While this is mostly used to compensate the short-term  
 489 mismatch between heat generation and demand, longer storage cycles are observed in winter, where heat  
 490 storage is most needed. This increases the flexibility of the heat pumps, which can operate also when no  
 491 heat is required. Furthermore, it complements the use of the geothermal field, which is intrinsically more  
 492 suited to compensate longer-term, i.e. seasonal mismatches between energy generation and demand because  
 493 of its slower storage dynamics.

494 5.2. Entire Anergy Grid of ETH Zurich

495 The analysis performed in Section 5.1 for the HPL cluster and geothermal field is applied to the entire  
 496 network shown in Fig. 7, which describes the Anergy Grid of ETH Zurich, and where the blue and red  
 497 arrows indicate the direction of the water flowing in the network branches, which is optimized but remains  
 498 constant during the year. All demand clusters are modeled as described for the HPL cluster, i.e. series  
 499 of HP, LTHE and HTHE, with the possibility of storing heat in the HWTS. Here we do not present the  
 500 impact of the HP minimum-power fraction, which is similar for all clusters, but we present and discuss the  
 501 possibility of dissipating energy to the environment, i.e. of exceeding the energy demands, which becomes  
 502 more relevant when optimizing the entire system.

503 5.2.1. Minimum CO<sub>2</sub> emissions

504 Fig. 8 shows the specific CO<sub>2</sub> emissions of the entire system as function of the normalized average mass  
 505 flow rate circulating in the network,  $\mu$  (Fig. 8-a), of the amount of energy dissipated to the environment,  $\phi$   
 506 (see Eqs. (28) and (29)), and of the presence of HWTS (Fig. 8-b). The value of  $\mu$  is calculated by considering  
 507 all the branches of the thermal network. For comparison, Fig. 8 reports (i) the value of CO<sub>2</sub> emissions of  
 508 the Anergy Grid obtained by using the centralized heating and cooling technologies, without deploying the  
 509 thermal network (horizontal black dashed line), and (ii) the value of CO<sub>2</sub> emissions of the Anergy Grid  
 510 achieved with the current operation (horizontal gray dotted-dashed line) [42, 72]. Currently the system is  
 511 operated by following seasonal patterns, with heat pumps and heat exchangers determining the operation  
 512 in winter and summer, respectively.

513 In the Anergy Grid of ETH Zurich, energy dissipation to the environment is permitted and represents an  
 514 additional form of flexibility, which allows (i) to satisfy a higher fraction of energy demand via the Anergy  
 515 Grid by better handling the unbalance between the overall heating and cooling demands of every cluster,  
 516 and (ii) to balance the heat injection and extraction to and from the geothermal fields, respectively, hence  
 517 enabling sustainable field operations (i.e. same ground temperature at the beginning and the end of the

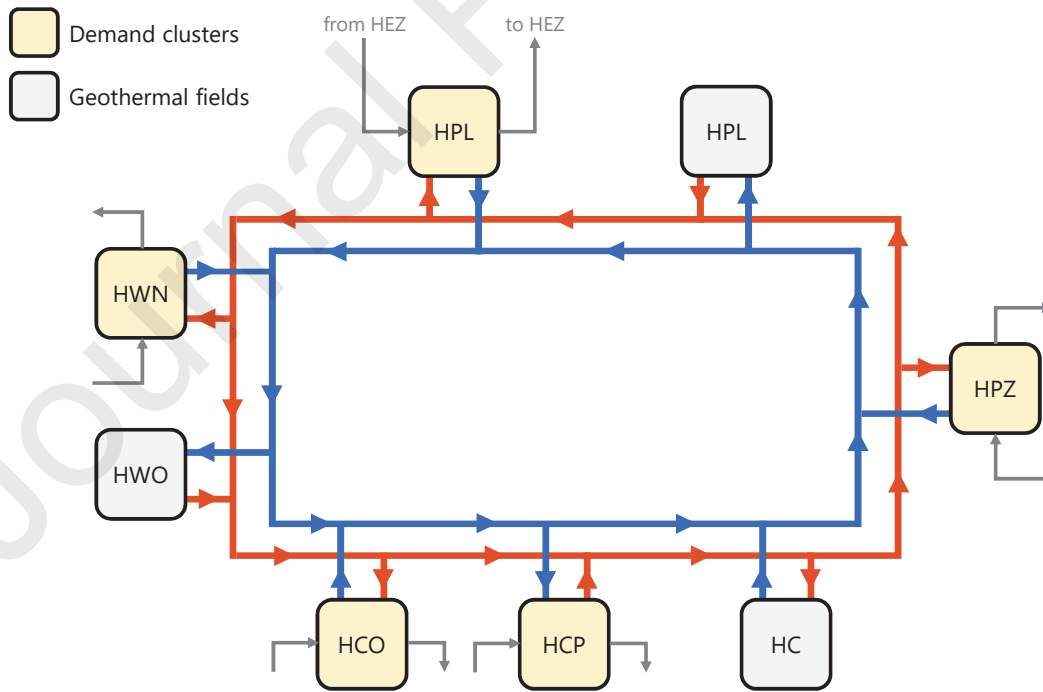


Figure 7: Schematic of the Anergy Grid of ETH Zurich reporting the demand clusters (yellow) and the geothermal fields (gray).



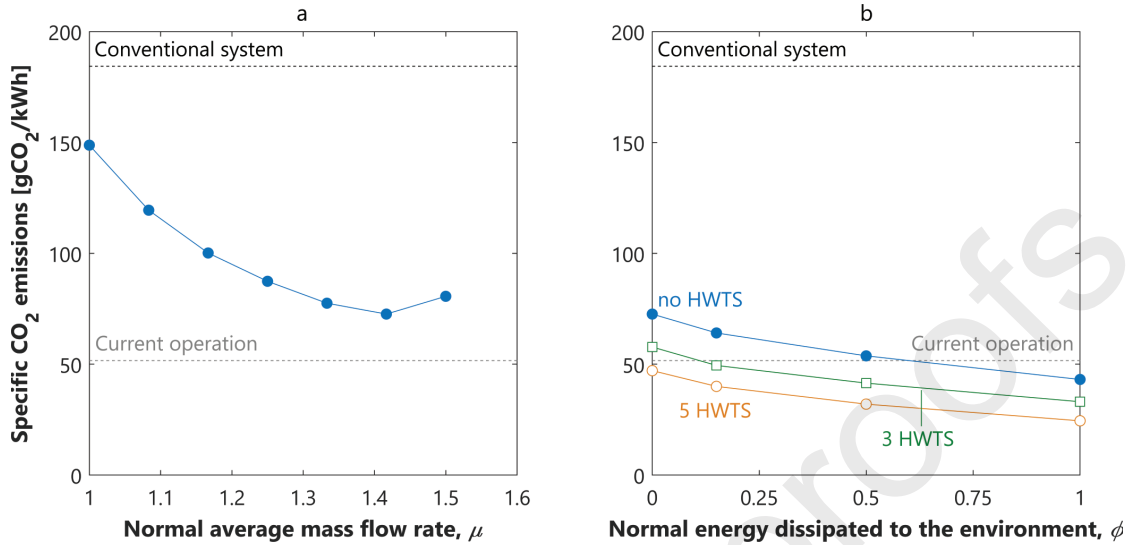


Figure 8: Specific CO<sub>2</sub> emissions of the Anergy Grid (AG) of ETH Zurich as function of (a) normalized average mass flow rate circulating in the network,  $\mu$ , and (b) normalized amount of energy dissipated to the environment,  $\phi$ , and of the presence of hot water thermal storage, HWTS. A shifted mass flow rate profile with  $\mu = 1.42$ , which enables the lowest value of CO<sub>2</sub> emissions, is used in (b).

518 year, see Eq. (17)). To clarify this concept, consider the same example above, namely a high value of mass  
 519 flow rate circulating through the network during a time of the year in which the heating demand is higher  
 520 than the cooling one. With reference to Fig. 2, assume a mass flow rate of 5 kg/s, a temperature variation  
 521 of 3.6 °C across the heat pump and the heat exchangers, 100 kWh of heating demand, and 10 kWh of LT  
 522 and HT cooling demands (i.e. 120 kWh of total energy demands). Such mass flow rate and temperature  
 523 variations result in the production of about 100 kWh of heat and 75 kWh of LT and HT cold. Therefore, we  
 524 can decide among the following three options for operating the system: (i) satisfying both the heating and  
 525 cooling demands via the Anergy Grid and release 130 kWh of cold to the environment (65 kWh each of LT  
 526 and HT cold -  $\phi = 130/120 = 1.1$ ), (ii) only satisfying the heating demand via the Anergy Grid and inject  
 527 the cold into the geothermal fields ( $\phi = 0$ ), (iii) satisfying both the heating and cooling demands via the  
 528 conventional system ( $\phi = 0$ ). The algorithm minimizes the CO<sub>2</sub> emissions by selecting option (ii), as this  
 529 allows storing the excess energy for later use. However, the prolonged injection of cold into the geothermal  
 530 field would result in a sustained cooling of the geothermal field, hence provoking a ground temperature at  
 531 the end of the year lower than at the beginning. This is not compatible with sustainable field operations.  
 532 When option (ii) is not feasible because it would impair future operations of the geothermal field, the  
 533 algorithm selects option (i). If option (i) is not feasible (e.g. because no more energy can be released to the  
 534 environment), the algorithm is forced to select option (iii) resulting in high CO<sub>2</sub> emissions, mostly because  
 535 the conventional heat generation is based on natural gas. Similar considerations apply when the cooling  
 536 demand is higher than the heating one.

537 Fig. 8-a reports the CO<sub>2</sub> emissions obtained with  $\phi = 0$  and by fixing the mass flow rate through the  
 538 heuristic approach (iii) described in Section 4, namely by considering a time-dependent mass flow rate profile  
 539 computed by shifting up the one obtained with the relaxed MILP optimization problem. When comparing  
 540 to the single HPL cluster, one can see that (i) smaller values of  $\mu$  are obtained, which means that the  
 541 optimal value of average mass flow rate (i.e. the value leading to minimum CO<sub>2</sub> emissions) is more similar  
 542 to the one obtained with the relaxed MILP optimization problem; (ii) overall, larger mass flow rates are  
 543 circulating into the thermal network, implying that the optimal operation strategy consists in satisfying  
 544 either the heating or the cooling demand at a given point in time (with one of the two being bypassed);  
 545 (iii) overall, higher CO<sub>2</sub> emissions can be attained, as a smaller fraction of the overall energy demand is

546 satisfied through the thermal network. This is because the entire system must comply with the constraints  
 547 of several demand clusters coupled with different geothermal fields and with their simultaneous heating and  
 548 cooling requirements, which results in a lower flexibility than the case of a single demand cluster exploiting  
 549 a dedicated geothermal field. Contrary to the single-cluster case, the CO<sub>2</sub> emissions of the system can be  
 550 reduced with respect to the current operation only by installing HWTS and/or dissipating energy to the  
 551 environment.

552 As shown in Fig. 8-b, such emissions are decreased by installing HWTS, with 7% emissions reduction  
 553 obtained with one HWTS, 19% with three HWTS and 35% with five HWTS (these two cases are reported  
 554 in Fig. 8-b). Similar to the single cluster, this is because the HWTS enables a wider range of operation for  
 555 the HP and allows satisfying a larger fraction of the energy demand.

556 Moreover, a further reduction in CO<sub>2</sub> emissions is achieved by dissipating energy, as this allows to satisfy  
 557 simultaneously the heating and cooling demands even when one of the two is exceeded. The benefit resulting  
 558 from dissipating energy (i) does not vary significantly when increasing the number of installed HWTS, since  
 559 HWTS is mostly used to meet high energy demands and energy dissipation is mostly used to meet low  
 560 energy demands; (ii) is greater for the entire system than for the single HPL cluster, where both high and  
 561 low energy demands can be satisfied via HWTS. A value of CO<sub>2</sub> emissions similar to the current operation  
 562 is obtained for three HWTS and  $\phi = 0.15$ , i.e. an amount of energy equal to 15% of the total energy  
 563 demand can be dissipated to the environment. For five HWTS, and for values of  $\phi$  equal to 0.15, 0.5 and  
 564 1, a CO<sub>2</sub> emissions reduction of 78%, 83% and 87% is obtained with respect to conventional technologies,  
 565 respectively (an improvement compared to the value of 72% obtained with the current operation). A value  
 566 of  $\phi = 1$  results in a system where the excess energy is released to the environment rather than stored  
 567 underground. The fact that this allows reducing the CO<sub>2</sub> emissions highlights the difficulties in controlling  
 568 the ground temperature in a sustainable long-term fashion (i.e. same ground temperature is enforced at  
 569 the beginning and at the end of the year for the sustainability of the geothermal field design) and points  
 570 towards an optimal expansion of the Anergy Grid where heating and cooling demands are better balanced.

571 Both CO<sub>2</sub> emissions and operation costs are calculated based on the amount of consumed electricity  
 572 and natural gas, and therefore a parallel exists between minimizing CO<sub>2</sub> emissions and the operation costs.  
 573 However, minimizing the CO<sub>2</sub> emissions results in a shift from natural gas to electricity, hence in a higher  
 574 share of electricity consumption with respect to the conventional system. Considering unit costs of natural  
 575 gas and electricity equal to 60 EUR/MWh and 120 EUR/MWh, respectively, the conventional system using  
 576 centralized heating and cooling incurs in operation costs of about EUR 55 per MWh of total energy demand.  
 577 The proposed optimization strategy allows decreasing the operations to 33 EUR/MWh with three HWTS  
 578 and  $\phi = 0$ , and to 15 EUR/MWh with five HWTS and  $\phi = 1$ .

### 579 5.2.2. System operation

580 The detailed investigation of the optimal operation of the HPL cluster when inserted within the entire  
 581 Anergy Grid provides additional insights into the management of multi-energy systems coupled with seasonal  
 582 geothermal energy storage. Compared to the stand-alone operation of the HPL cluster, the conversion  
 583 technologies are generally operated for less hours during the year and are switched ON and OFF more  
 584 often, due to the larger average mass flow rates circulating through the network and to the difficulty in  
 585 simultaneously meeting the heating and energy demands of several clusters.

586 When resorting to three HWTS and in case of no energy dissipation ( $\phi = 0$ ), the HP supplies about  
 587 68% of the heating demand required by the cluster, being operated for about 4900 hours during the year.  
 588 It is most often switched ON/OFF every one, two or three hours, but longer operating periods of about  
 589 10 and 20 hours are not uncommon. The low coverage of heating demand is the reason why higher CO<sub>2</sub>  
 590 emissions are attained in the case of the entire system. In this case, all the tools available to enhance the  
 591 system flexibility, i.e. HWTS and energy dissipation, are needed to increase the fraction of heating demand  
 592 satisfied by the thermal network. The LTHE supplies about 73% of the LT cooling demand and is operated  
 593 for about 6000 hours a year on an hourly basis. It is most often switched ON/OFF every one, two, and  
 594 three hours and common operating periods are shorter than 15 hours. Similar considerations can be made  
 595 for the HTHE, which supplies about 77% of the HT cooling demand.

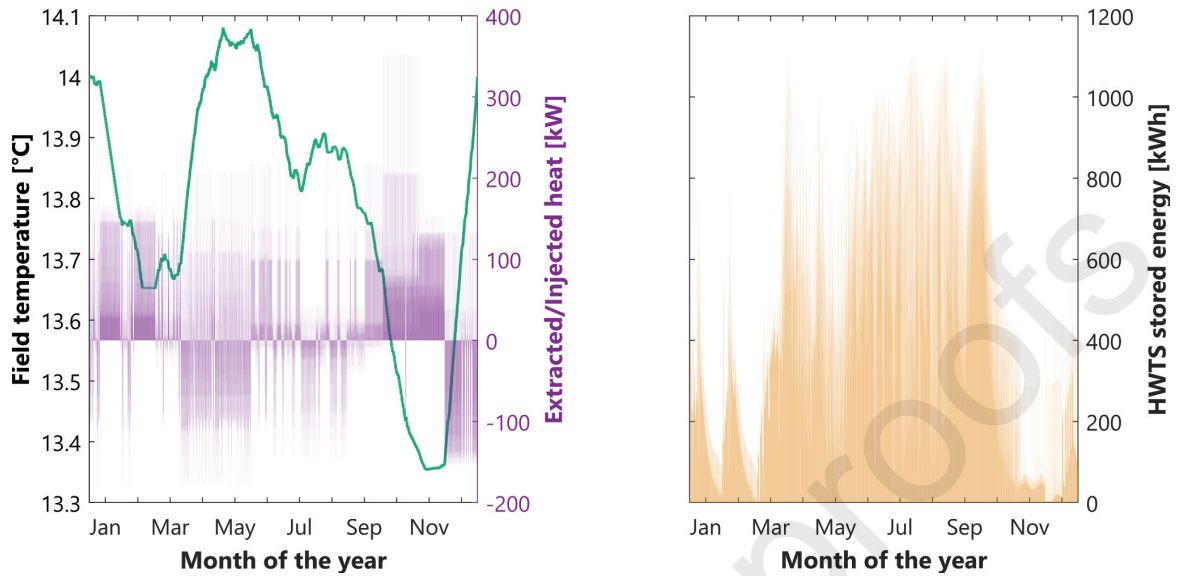


Figure 9: Optimal storage operation of the Energy Grid of ETH Zurich. (a) Optimal temperature profile of the HPL geothermal field (green line - left y-axis) and of the corresponding injected/extracted heat (positive/negative values of the yellow line - right-axis). (b) Optimal profile of stored energy within the HWTS installed in HPL. Shifted mass flow rate profile with  $\mu = 1.42$ ,  $\delta = 0.1$  and  $\phi = 0$ .

596 The optimal behavior of the HPL geothermal field and cluster HWTS is illustrated in Fig. 9. As shown  
 597 in Fig. 9-a, the temperature variation is less pronounced than for the HPL cluster when considered stand-  
 598 alone. In both cases, such a temperature variation is significantly smaller than the exploitable range (from  
 599  $8^{\circ}\text{C}$  to  $22^{\circ}\text{C}$ , see Table 1) and than the temperature variation experienced by the geothermal fields under  
 600 the current operation [42]. This suggests that a smaller geothermal storage capacity would be enough for  
 601 the optimal operation of the Energy Grid. Together with the evidence that lower  $\text{CO}_2$  emissions can be  
 602 achieved by coupling a demand cluster with a dedicated geothermal field (see comparison between Fig. 4-a  
 603 and Fig. 8-a), this suggests an improved design of the Energy Grid with more and smaller geothermal fields.  
 604 Furthermore, two peaks are observed both in summer and winter, indicating a storage dynamic faster than  
 605 seasonal. This is due to the necessity of meeting the variable energy demands of all clusters at the same  
 606 time, and therefore to exploit the geothermal field through two storage cycles per year.

607 Fig. 9-b shows the operation of the HWTS. This is mostly used to compensate the short-term mismatch  
 608 between heat generation and demand, and it is mostly exploited in summer, hence allowing the heat pump  
 609 to operate even in moments of low heat demand (low heat demands must be satisfied via HWTS since no  
 610 energy dissipation occurs, i.e.  $\phi = 0$ ).

## 611 6. Conclusions

612 This paper investigates the optimal operation of MES deploying geothermal energy storage to cope with  
 613 the seasonal variability of heating and cooling demands. The benefits of seasonal geothermal storage are  
 614 assessed and optimized with reference to a real-world system, namely the Energy Grid installed at ETH  
 615 Zurich, in Switzerland. In such a system, centralized heat and cold production based on fossil fuels is replaced  
 616 by a dynamic underground thermal network connecting geothermal fields, which serve as energy source and  
 617 storage, with demand clusters requiring thermal and cooling energy. The current system operation allows  
 618 reducing the  $\text{CO}_2$  emissions of the university campus by 72% with respect to the conventional system using  
 619 centralized heating and cooling. The scope of this contribution is developing an optimization framework  
 620 enabling further increase in energy efficiency, hence further emissions reduction.

621 To this end, we develop a novel optimization model that is able to address the complexity of the physical  
622 system, and that improves on the state-of-the-art by (i) accounting for the nonlinearities of the physical  
623 system, and (ii) capturing both the short- and long-term dynamics of energy conversion, storage and con-  
624 sumption. These features allow improving the current operation strategies and explaining the rationale  
625 behind the optimal system operation and design.

626 More specifically, the optimal system operation enables a CO<sub>2</sub> emissions reduction up to 87% with  
627 respect to the conventional system using centralized heating and cooling (though such a value comes at the  
628 cost of dissipating to the environment an amount of energy equal to the energy demand). This is achieved  
629 by operating the heat pumps and the heat exchangers on an hourly basis, i.e. by switching them ON/OFF  
630 every one, two and three hours. Furthermore, only deploying seasonal energy storage through geothermal  
631 fields enables a CO<sub>2</sub> emissions reduction up to 76% with respect to the conventional system. The full  
632 potential of the Anergy Grid is obtained by (i) selecting the optimal value of mass flow rate circulating  
633 through the network, which should vary with time and be high enough to satisfy the heating and cooling  
634 demands, but without exceeding either of the two, (ii) coupling the geothermal fields with HWTS, which  
635 allows maximizing the efficiency of energy storage from daily to seasonal cycles, (iii) releasing energy to the  
636 environment, which provides additional system flexibility when the heating and cooling demands are very  
637 different from each other. Finally, the optimal temperature evolution of the geothermal fields suggests that  
638 the design of the Anergy Grid could be improved by installing more and smaller geothermal fields, with  
639 each geothermal field having a dedicated demand cluster. Also, the positive effect of releasing energy to the  
640 environment points towards an optimal expansion of the Anergy Grid where heating and cooling demands  
641 are better balanced, and the geothermal fields better exploited.

#### 642 **Acknowledgment**

643 The authors thank Raphael Wu (Reliability and Risk Engineering laboratory at ETH Zurich) for the  
644 very helpful and fruitful discussions during the analyses that led to the paper, Maria Yliruka (Department of  
645 Chemical Engineering at Imperial College London) for setting up the analysis of the geothermal fields, and  
646 Viola Becattini (Separation Processes Laboratory at ETH Zurich) for sharing helpful material concerning  
647 the analysis of the geothermal fields. Furthermore, the authors thank Dominik Brem, Wolfgang Seifert and  
648 Urs Hinnen (ETH Immobilien), as well as Marc Hausermann and Matthias Mast (Amstein-Walthert) for  
649 the very helpful discussions and insights on the operation of the Anergy Grid of ETH Zurich.

#### 650 **Supporting information**

651 The supporting information include the hourly profiles of the energy demands (see Appendix A) and of  
652 the  $g$ -function used for the geothermal fields (see Appendix B).

653 **Nomenclature****Symbols**

$A$	heat exchange area, [m <sup>2</sup> ]
$c$	specific heat of water, [kJ/(kg K)]
$D$	carrier demand, [kWh]
$d$	binary defining flow direction in network branches
$E$	energy stored in hot water thermal storage, [kWh]
$e$	CO <sub>2</sub> emissions, [g <sub>CO2</sub> ]
$F$	input power, [kW]
$g$	function defining dynamic behavior of geothermal fields
$H$	number of yearly operating hours
$h$	function defining thermal losses of hot water thermal storage
$L$	depth of geothermal fields, [m]
$m$	mass flow rate, [kg/s]
$\tilde{m}$	auxiliary variable for MILP relaxation [kg °C/s]
$n$	number of boreholes
$P$	output power, [kW]
$Q$	net injected thermal power, [kW]
$R$	thermal resistance, [m K/W]
$r$	radius of the geothermal field, [m]
$S$	technology size, [kW]
$s$	number of yearly switches
$T$	temperature, [°C]
$U$	overall heat transfer coefficient, [W/K m <sup>2</sup> ]
$u$	import energy price, [EUR/kWh]
$v$	export energy price, [EUR/kWh]
$x$	binary defining scheduling of cluster technology
$y$	binary defining node configuration

**Greek symbols**

$\alpha$	thermal diffusivity of soil, [m <sup>2</sup> /s]
$\beta$	parameter defining temperature dependence of technology performance
$\gamma$	Euler-Mascheroni constant
$\delta$	parameter defining minimum size constraint
$\epsilon$	carrier carbon intensity, [g <sub>CO2</sub> /kWh]
$\zeta$	mass flow rate multiplication factor
$\eta$	technology efficiency
$\kappa$	mass flow rate additive factor
$\Lambda$	self-discharge efficiency, [1/h]
$\lambda$	thermal conductivity of soil, [W/(K m)]
$\mu$	normalized average mass flow rate
$\nu$	mass flow rate constant factor
$\xi$	Carnot efficiency
$\Pi$	ambient thermal losses
$\tau$	charging/discharging time, [1/h]
$\phi$	normalized energy dissipated to the environment

**Sets**

$\mathcal{B}$	set of branches of thermal network
$\mathcal{C}$	set of energy carriers
$\mathcal{D}$	set of clusters

$\mathcal{G}$	set of geothermal fields
$\mathcal{I}$	set of intersection points of thermal network
$\mathcal{M}$	set of available technologies
$\mathcal{M}_{\mathcal{D}}$	set of technologies available in the clusters
$\mathcal{O}$	set of all nodes of thermal network

**Subscripts**

HT	high temperature
LT	low temperature

**Superscripts**

amb	ambient
b	borehole
c	cooling
cond	condensation
eva	evaporation
F	geothermal field
in	inlet
int	internal
max	maximum
min	minimum
out	outlet
w	wall

**Acronyms**

AG	Energy Grid
B	Boiler
C	Compression Chiller
EMS	Energy Management Systems
GF	Geothermal Field
HE	Heat Exchanger
HP	Heat Pump
HT	High-Temperature
HTHE	High-Temperature Heat Exchanger
LT	Low-Temperature
LTHE	Low-Temperature Heat Exchanger
MES	Multi-Energy Systems
MILP	Mixed-Integer Linear Program
MINLP	Mixed-Integer NonLinear Program
HWTS	Hot Water Thermal Storage
PV	Photo-Voltaic



654 **Appendix A: Energy demand profiles of all demand clusters**

655 The hourly-resolved heating and cooling demand profiles of 2018 for all clusters of the Anergy Grid of  
 656 ETH Zurich (see Section 5.2) are shown in Fig. S1 and provided in the [Supporting Information](#). These are  
 657 the experimental values measured by the system operator [42, 72]. The total annual value,  $D^{\text{tot}}$ , is reported  
 within each box.

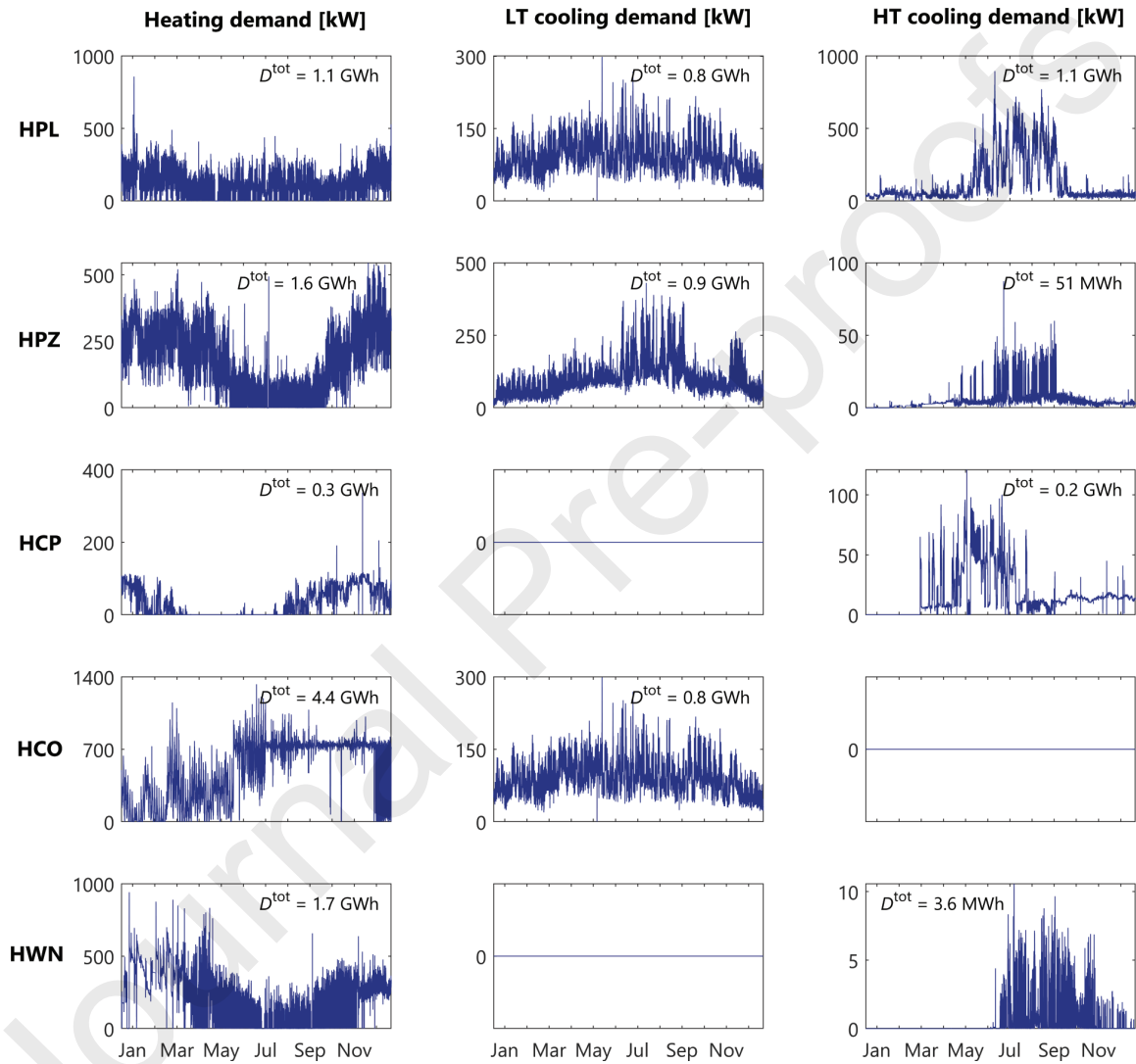


Figure S1: Hourly-resolved heating and cooling demand profiles of 2018 for all clusters of the Anergy Grid of ETH Zurich. Experimental values measured by the system operator [42, 72]. The total annual value is reported in each box.

658

659 **Appendix B: Model of the geothermal field**

660 With respect to the Anergy Grid of ETH Zurich, and specifically to the HPL geothermal field (see  
 661 Fig. 1), Fig. S2 compares the temperature evolution provided by our model with the one measured by  
 662 the system operator for the profile of injected/extracted heat in 2018 [42]. The model predicts well the  
 663 qualitative behavior of the temperature dynamics. The discrepancy between the modeled and the measured  
 664 evolution (with the latter decreasing/increasing faster than the former) might be due to the position of the  
 665 temperature sensors, to the modeling assumptions, as well as to the impact of previously injected/extracted  
 heat not considered in the model.

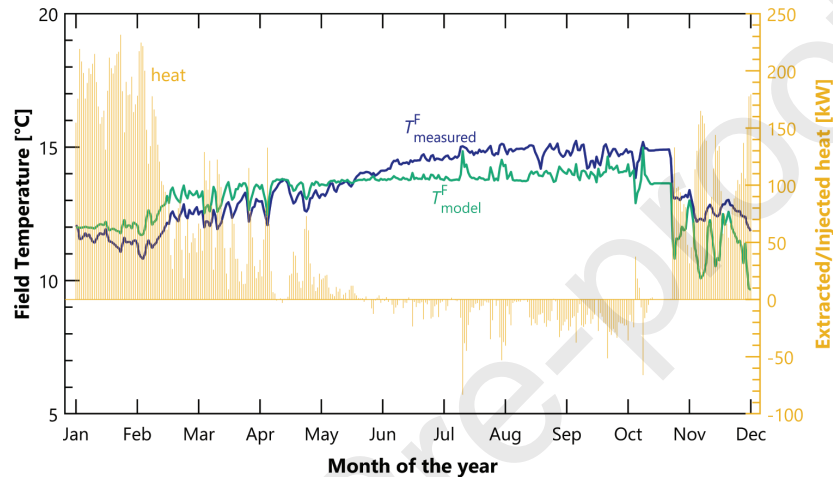


Figure S2: Temperature evolution provided by the model (green line) and measured by the system operator (blue line) following the measured profile of injected/extracted heat (red bars) in 2018 [72].

666

667 The hourly-resolved  $g$ -function used to describe the dynamic behavior of all geothermal fields (see  
 668 Eq. (13)) is shown in Fig. S3 and provided in the [Supporting Information](#). Such a  $g$ -function is modeled on  
 the behavior of the HPL geothermal field [42].

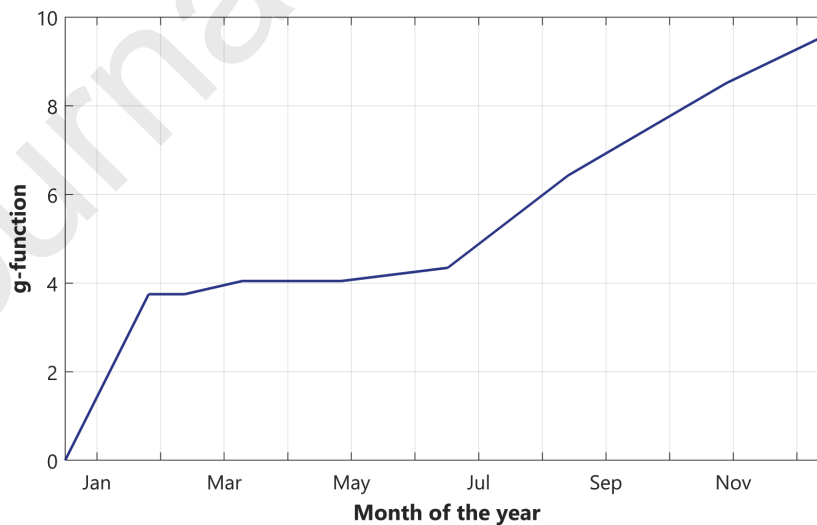


Figure S3:  $g$ -function used to describe the dynamic behavior of the geothermal fields [42].

669

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