J. Parallel Distrib. Comput. 73 (2013) 465-483

Contents lists available at SciVerse ScienceDirect

J. Parallel Distrib. Comput.

journal homepage: www.elsevier.com/locate/jpdc

Foundations of distributed multiscale computing: Formalization, specification, and analysis



Journal of Parallel and Distributed Computing

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ARTICLE INFO

Article history: Received 14 December 2011 Received in revised form 25 June 2012 Accepted 13 December 2012 Available online 11 January 2013

Keywords: Multiscale modeling Distributed multiscale computing Modeling methodology MML MUSCLE Task graph Coupling template Coupling topology Submodel execution loop

1. Introduction

ABSTRACT

Inherently complex problems from many scientific disciplines require a multiscale modeling approach. Yet its practical contents remain unclear and inconsistent. Moreover, multiscale models can be very computationally expensive, and may have potential to be executed on distributed infrastructure. In this paper we propose firm foundations for multiscale modeling and distributed multiscale computing. Useful interaction patterns of multiscale models are made predictable with a submodel execution loop (SEL), four coupling templates, and coupling topology properties. We enhance a high-level and well-defined Multiscale Modeling Language (MML) that describes and specifies multiscale models and their computational architecture in a modular way. The architecture is analyzed using directed acyclic task graphs, facilitating validity checking, scheduling distributed computing resources, estimating library and environment (MUSCLE) is outlined. The methodology is applied to two selected applications in nanotechnology and biophysics, showing its capabilities.

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Nature is a complex system that we wish to unravel, understand and sometimes control. Traditionally, science followed the highly successful approach of studying nature as detailed as possible, one part of the puzzle at a time. Extensive data and knowledge have been accordingly accumulated on all spatio-temporal scales, separately. Now we have started to put the pieces back together by studying natural processes holistically as complex multiscale systems. Driven by the availability of abundant amounts of data on all scales, multiscale modeling and simulation of physical, chemical, biomedical, biological and ecological phenomena has become a major activity in science and engineering.

Despite the evident success and relevance of multiscale modeling in many areas of science such as biology and physiology [48,49, 45,50,24,17], material science [25,10], chemistry [46,58,42], and applied mathematics [27], there is little attention to generic multiscale modeling paradigms [34], and related methods of multiscale

* Corresponding author. E-mail addresses: J.Borgdorff@uva.nl, joris@jorisborgdorff.nl (J. Borgdorff), Jean-Luc.Falcone@unige.ch (J.-L. Falcone), E.Lorenz@uva.nl (E. Lorenz), C.BonaCasas@uva.nl (C. Bona-Casas), B.Chopard@unige.ch (B. Chopard), A.G.Hoekstra@uva.nl (A.G. Hoekstra). computing [20,17]. Moreover, many multiscale models are so computationally expensive that advanced computing capabilities are required, but few initiatives take advantage of the multiscale character of the models to help in this matter [17]. In part, this is because there is no single formal background for multiscale modeling that might help with this [59]. The need for advanced multiscale computing capabilities is expressed by the MAPPER project, representing five different scientific communities facing the need for distributed computing for multiscale models [55]. The main argument for using distributed architecture is that the computational requirements of the single scale models that make up the multiscale model are very heterogeneous, calling for distinct computing resources. As we will argue, our multiscale modeling paradigm naturally maps to a distributed computing ecosystem, resulting in what we call Distributed Multiscale Computing (DMC).

This idea builds upon the earlier COAST project [54]. That project resulted in a theory of Complex Automata (CxA) [32,33, 35,34,15], where several single scale cellular automata that are coupled form a multiscale model. The exact computational architecture of the CxA model can be specified using a Multiscale Modeling Language (MML) [23]. The CxA theory was accompanied by a practical counterpart, a computing environment, first called the Distributed Space Time Coupling Library (DSCL) but later



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renamed to the MUltiScale Coupling Library and Environment (MUSCLE) [29,30].

Although CxA and MML only cover coupled single scale cellular automata, here we propose that both concepts can be generalized to cover coupled single scale models. Similarly, MUSCLE is capable of coupling any type of single scale model in a multitude of programming languages, rather than only cellular automata.

Furthermore, for doing distributed multiscale computing MUS-CLE already works on self-maintained clusters [30] and it is our goal to extend it for computing on heterogeneous grid environments. In order to achieve this, the computational and communicational requirements of given multiscale models must be adequately predicted and scheduled. If the computation of a multiscale model can be represented by a task graph, by partitioning it into indivisible tasks, quite some research has shown how it can be scheduled on a given set of distributed computing resources [21,6,40,14].

In Section 2 we will lay the foundations for distributed multiscale computing by generalizing from CxA theory to a formal and comprehensive multiscale modeling theory. The aim of this theory is to be able to define what scales are and how they can be used in multiscale modeling, as well as indicate which interaction patterns are possible in multiscale models. Given these firm modeling foundations, a multiscale model and its computational architecture can be exactly specified with MML, as shown in Section 3. This specification can be used for analysis of runtime properties of a multiscale model implementation, and as a guideline for actually executing the model. In Section 4 we propose a method to automatically convert an MML specification to a task graph. This task graph serves as an analytical tool to facilitate scheduling decisions on distributed computing resources or as an input to workflow systems. With these tools it is feasible to set up a distributed execution system, using MUSCLE as a coupling library and low-level runtime environment. This approach is sketched in Section 5; however, we will not deeply discuss the practicalities or difficulties of distributed execution of multiscale models.

In Section 6 the concepts in this paper will be illustrated by two selected scientific applications: a three-dimensional model of in-stent restenosis (ISR3D) [12], and a model of the formation of clay-polymer nanocomposite materials [52].

1.1. Related work

A number of methodological papers on multiscale modeling exist, each generalizing multiscale modeling concepts known so far from the perspective of their respective disciplines, physics [19,20] and chemical process engineering [46,37]. They draw from multiscale methods applied to applications so far but do not rigorously define the concepts they use or combine the modeling methodology with concepts useful for implementation. Likewise, Dada and Mendes [17] evaluate the current state of multiscale methodologies and software solutions for multiscale modeling in systems biology and conclude that an all-encompassing solution does not yet exist.

On the other hand, a great number of multiscale concepts, so far loosely described, have been formalized by Yang and Marquardt [59], who define multiscale terms on a conceptual basis rather than an application-driven one. Unfortunately, a fundamental part of their theory considers only spatial scales, which is reflected in their way of representing a hierarchy of submodels based on scale. The formalization in Section 2 offers an alternative to defining multiscale models that considers spatial and temporal scales. One of the achievements of their specification is that they associate it with a machine-readable format in the form of an ontology.

The frameworks classification by Ingram et al. [37] distinguishes different types of couplings between pairs of single scale models. Although this classification shows properties of different frameworks, it does not show why these properties are present. However, by formalizing what single scale models are and how they are coupled in Section 2, the classification follows from the multiscale properties of a model.

A notable multiscale method, the Hierarchical Multiscale Method (HMM) [18] consists for a large part of strategies to decompose a phenomenon to a multiscale phenomenon. It gives guidelines for when to split certain scales, what methods may be appropriate to certain types of decomposition. Indeed, these strategies are complementary to the methodology proposed in this paper, and mostly adds to Section 2.3. Rather, this paper adds to HMM in terms of theoretical scale, and explicit highlevel submodel coupling, specification, analysis and distributed computing.

Although MML is a description language of the multiscale domain of discourse, it is not formalized as an ontology to avoid introducing additional terminology. Other languages that describe how components of a program are coupled exist, such as several Architecture Description Languages (ADL's) [1,26,4], or the Common Component Architecture (CCA) [3,2]. Even though both of these architecture descriptions form a respectable basis that influences MML, unfortunately neither describe multiscale properties, which do offer additional insight in multiscale model coupling. Given the additional detail in formalization since previous work on MML by Falcone et al. [23], we see opportunity to more precisely define MML elements, making them suitable for analysis.

As a general coupling library MUSCLE has alternatives, but as a general multiscale coupling library it does not have an equivalent. Coupling libraries include the open source problem solving environment Cactus [28] CCA-based Ccaffeine [2], the mesh-based MpCCI [38], and earth system modeling frameworks Prism [56] or BFG2 [5], none of which support multiscale models explicitly or directly.

To analyze a distributed execution multiple tools exist besides the task graph, including Petri nets [47,57] and process calculi [44,31]. Depending on future needs, the task graph could also be converted to a Petri net, although it is more verbose and tedious in use. The same limitation holds for process calculi, where the latter is also less flexible. Scientific workflows could also be generated from a task graph, to make use of the multitude of workflow software that already exists [7].

2. Multiscale modeling formalization

To make sense of nature's complexity and to do so in a uniform, rigorous, and general way is a difficult task. Multiscale modelers may approach this complexity by functionally decomposing a problem into a set of single scale models that exchange information across the scales, at the same time taking advantage of data available for those scales. Especially when single scale models represent sufficiently different scales, this approach can simplify a problem and strongly reduce the computational cost of a multiscale model. This approach would benefit greatly from firm foundations that make full use of the multiscale character of the system under study. By determining the multiscale character of a model these foundations may offer directions for specific multiscale methods and establish the runtime behavior of the model (see Fig. 1).

'A multiscale model is,' to quote Ingram et al. [37], 'a composite mathematical model formed from two or more submodels that describe phenomena at different scales. In this context, we define a *submodel* [...] as a component model that describes only one scale of the system.' According to this definition, a multiscale model is

Table 1

Symbols used in this paper with their type and meaning. Regular and point scale formation have a shorthand notation but represent a special case of a scale specification. The type *E* is an abstract type for events and type *F* is an abstract type for submodel states. The last three lines are not mathematical functions but rather procedures that may have side-effects outside their scope.

Symbol	Туре	Meaning	
τ,ξ	\mathbb{R}^+	Characteristic temporal and spatial scale	
δ, Δ	\mathbb{R}^+	Minimum and maximum scale granularity	
ω, Ω	\mathbb{R}^+	Minimum and maximum scale total size	
$S(\delta, \Delta, \omega, \Omega)$	$\mathbb{R}^4 ightarrow Bool$	Scale specification (Definition 4)	
$S(\Delta, \Omega)$	Shorthand for $\mathbb{R}^4 \to Bool$	regular scale specification (Definition 4)	
$S(\Omega)$	Shorthand for $\mathbb{R}^4 \to Bool$	Point scale specification (Definition 4)	
e, t(e)	$E, E \rightarrow \mathbb{R}$	Event and time of that event	
ϑ, ϑ_i	$\mathcal{P}(E)$	Time series and future time series	
f _{init}	Procedure $\mathbb{R} \to F \times \mathcal{P}(E)$	State initialization SEL operator (Algorithm 1)	
S, B	Procedure $F \times E \times \mathcal{P}(E) \to F \times \mathcal{P}(E)$	Solving step and boundary conditions SEL operators (Algorithm 1)	
0 _i , 0 _f	Procedure $F \times \mathbb{R} \times \mathbb{R} \to \emptyset$	Intermediate and final observation SEL operators (Algorithm 1)	

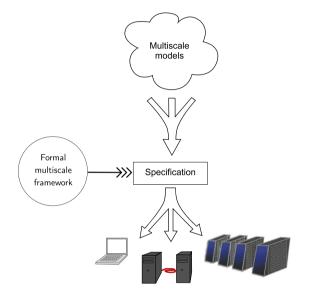


Fig. 1. An overview what our aim with Distributed Multiscale Computing is: taking multiscale models, defining a formal background to specify them, and running them on heterogeneous infrastructure assisted by their specifications.

functionally decomposed into submodels describing phenomena at different scales. How to decompose a model into a multiscale model is not specified and as the underlying terms are not welldefined this remains vague. Thus, to adequately work with the terms used in the definition, each of those terms will have to be clearly defined. This includes the terms scale, phenomenon, domain, scale specification and separation ('different scales'), single scale model, multiscale model, submodel and finally the 'composite mathematical model'. The symbols that are introduced in these definitions and in the text are listed in Table 1.

2.1. Process

In this contribution we restrict our attention to models of physical processes that are bounded in time and space; in short, natural processes. Studying a natural process means that temporal and spatial coordinates can be assigned to it relative to the natural world. Note that this does not include man-made processes. Also note that by taking a more abstract notion of coordinates, other types of processes could also fit into the methodology, but such issues are not explored in this paper.

In the following definitions, we will take the terms natural, process, and observation as primitive terms, and they will not be further defined. Furthermore, we assume that one process can be a part of another. The next term, scale, is defined here on an abstract level and not yet quantified.

Definition 1. A *scale* is an order of magnitude along a coordinate.

Temporal and spatial scales are commonly used, but a scale could also be assigned along an abstract dimension, such as a fractal dimension or the number of elements in a set. For natural processes, however, at least temporal and spatial scales are considered.

To quantify the intuition of a scale, the notion of a characteristic scale was conceived [37,35]. A characteristic scale refers to a process assigns a single number to a scale that can be used as a variable in some models. For instance in reaction–diffusion equations this would be a characteristic temporal scale for diffusion, determined by the diffusion coefficient, and a characteristic temporal scale for reactions determined by the reaction coefficient [13]. Although in this example the characteristic scale has a well-defined meaning as a model parameter, it will not be defined further here.

The characteristic scale is not set in the process, rather, it is a modeling choice. Even though the characteristic scale may serve intuition, it is difficult to determine how to relate several characteristic scales, or, how far a single scale reaches. Is the characteristic spatial scale of a walking human of 2 m fundamentally larger than the characteristic spatial scale of the moving legs, of for instance 1 m? And muscles in the foot, of 2 decimeter? On the other hand, the same human body can be viewed as a single object with some properties or as a collection of cells. In both views the total size is the same, but the scale is intuitively different, even though the body itself does not change during this observation. The issue here is that it is hard to justify that a natural process itself acts only on a certain scale, as opposed to our observation of that process. This is precisely where the term phenomenon is useful: it describes dynamics over an object in the same manner as the term process, but it includes the notion of observation. It is then our assumption that most observations can in some way be discretized, thereby limited to a certain granularity, determining how far a scale reaches.

Definition 2. A *phenomenon* is a finite amount of data describing a natural process on a given set of scales.

So a phenomenon is a discretization of a process, since it is finite. Likewise, a domain is the discretization of the object of the phenomenon at a certain time. As such, it encompasses all but the temporal dimension of the phenomenon.

Definition 3. Data of a phenomenon that describes a process at a given time point is a *domain*.

A domain D' is a *subdomain* of domain D iff they have the same time point and the process that D' describes is part of the process that D describes.

In contrast to a process, phenomena or domains can be specified by a modeler based on factors such as available data, numerical error, or computational complexity. Concretely, the discretization may for example depend on microscope resolution, measurement



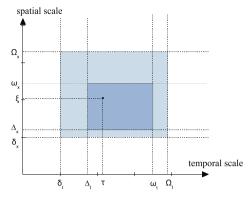


Fig. 2. A scale map with a spatial and temporal axis indicating the scale specifications and characteristic scales of the phenomenon. The area within the scales of the phenomenon is colored; the area between minimum and maximum granularity and total size is a lighter color. The characteristic spatial scale is denoted by ξ and the characteristic temporal scale by τ .

precision or sizes of objects within the phenomenon. The collection of scale specifications is thereby a modeling choice that will be useful for analytic study of the multiscale model, as they are more precise than the characteristic scale. The following paragraphs will be devoted to clarifying what the collection of scale specifications involves.

We assume that the observed phenomenon has a certain size and a discrete granularity, given the data known about it. Thus, a scale specification should include at least a granularity and a total size, forming the minimum and maximum of that scale. Because the granularity may fluctuate within a single phenomenon, a minimum and maximum may be given to the granularity of a scale specification as well, and likewise for the total size. By providing this range of granularity and total size, the bounds of single scale models become specified. This specification will form the basis for interaction patterns between single scale models in Section 2.6.

For example, on a sample of artery tissue of $1.5 \times 1.5 \times 1.5$ mm data was gathered on the lumen size, cell type distribution, and cell sizes. Specifications of the spatial scale of this tissue would have a total size as size of the sample and a variable granularity based on the diversity of cell sizes. If measurements taken are fundamentally more precise than the size of the smallest cell, this can be reflected by taking a very fine granularity. A temporal scale cannot be determined in this example, since data only exists of one time point and most importantly only an *object* of study was identified, not a *process*. On the other hand, the spatial scales can be fully specified based on the data available.

For some domains, for instance a regular Cartesian grid, it is not necessary to consider a minimum and maximum granularity; rather, such a grid has a regular scale, with the same step size for each grid point. More extreme, a single value could be seen as a grid with a total size equal to its step size, giving a point scale.

Definition 4. $(\delta, \Delta, \omega, \Omega) \in \mathbb{R}^4$ is a scale specification, denoted by $S(\delta, \Delta, \omega, \Omega) =$ True or by $S(\delta, \Delta, \omega, \Omega)$, iff

$$0 < \delta \leq \Delta \leq \Omega$$
 and $\delta \leq \omega \leq \Omega$.

A scale specification $S(\delta, \Delta, \omega, \Omega)$ is regular iff $\delta = \Delta$ and $\omega = \Omega$; its shorthand notation is $S(\Delta, \Omega)$. A regular scale specification $S(\Delta, \Omega)$ is point iff $\Delta = \Omega$; its shorthand notation is $S(\Omega)$.

A scale specification $S(\delta, \Delta, \omega, \Omega)$ quantifies a scale of a phenomenon by giving it specific bounds along a coordinate. Here δ and Δ are the minimum and maximum observed granularity, respectively, and ω and Ω the minimum and maximum total observed size, respectively.

Notably, a temporal scale specification is denoted as $S(\delta_t, \Delta_t, \omega_t, \Omega_t)$ and a spatial scale specification as $S(\delta_x, \Delta_x, \omega_x, \Omega_x)$ as is shown in Fig. 2. In the rest of the paper, when a scale is mentioned a scale specification is meant unless stated otherwise.

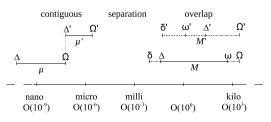


Fig. 3. Contiguous scales, scale separation, and scale overlap according to the scale specifications of given submodels μ , μ' , M, and M', plotted on an arbitrary logarithmic SI scale.

2.2. Scale separation

An important part of multiscale modeling is how the scales of different phenomena relate to each other. As will become clear later this relative scale also affects the structure of the multiscale model and its computation.

Three types of relations will be defined: scale overlap, contiguous scales, or scale separation, each illustrated in Fig. 3. With these three types of scale relations, it is possible to do meaningful multiscale modeling. Scale separation, for instance, is actively exploited with methods such as scale-splitting [13] or the heterogeneous multiscale methods (HMM) [20].

Definition 5. Given scale specifications $s = (\delta, \Delta, \omega, \Omega), s' = (\delta', \Delta', \omega', \Omega')$, for convenience with $\Omega > \Omega'$ or if $\Omega = \Omega'$ then $\Delta \ge \Delta'$:

- *s* and *s'* are overlapping iff $\Delta < \omega'$ and $\Delta' < \omega$;
- *s* and *s'* are *separated* iff $\Omega' < \delta$; and
- *s* and *s'* are *contiguous* iff $\Delta' \leq \delta \leq \Omega' \leq \Delta$.

The above definition of scale separation is more strict than the word different, which means non-equal.

Theorem 1. Two regular scales are either overlapping, separated, or contiguous.

Proof. Take two regular scales $S(\Delta, \Omega), S'(\Delta', \Omega')$, for convenience with $\Omega > \Omega'$ or if $\Omega = \Omega'$ then $\Delta \ge \Delta'$. Because the scales are regular, the condition for being overlapping simplifies to $\Delta < \Omega'$ and $\Delta' < \Omega$, for being separated to $\Delta > \Omega'$, and being contiguous to $\Delta = \Omega'$. These conditions are clearly mutually exclusive.

To show that they are all inclusive, $\Delta < \Omega'$ must imply $\Delta' < \Omega$. When $\Omega > \Omega'$, combining it with the scale specifications condition that $\Omega' \ge \Delta'$, it follows that $\Omega > \Delta'$. When $\Omega = \Omega'$, using the assumption $\Delta \ge \Delta'$ and the premise $\Omega' > \Delta$, this implies $\Omega > \Delta'$. Thus, the three conditions are mutually exclusive and all inclusive for regular scales. \Box

A motivation for defining scale separation as above can be found by taking two interacting phenomena *A* and *B* of a certain granularity and total size, depicted in Fig. 4. For example, let them be phenomena acting on living tissue, both represented by a rectangular grid. If the grid cells of *A* are smaller than the total size of *B* and the other way around, then for them to interact correctly they will need to exchange information about multiple grid cells. In doing so, they resolve at least part of each others domain. In this case, *A* and *B* have spatial scale overlap. When submodels of *A* and *B* are treated as black boxes, unaware of each others structure, they will need to exchange information about the entire part of the domain where they overlap at once.

On the other hand, if one grid cell of *A* is exactly the total size of *B*, and *B* represents exactly one grid cell of *A*, they have contiguous scales and *B* will only need information from the one cell in *A* it represents, and possibly its neighbors. This behavior is more local,

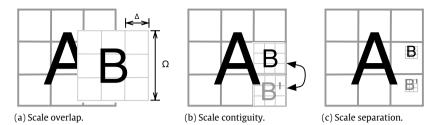


Fig. 4. Two phenomena *A* and *B*, both having a rectangular grid as a domain, with different scale relations. Phenomenon *B'* is of the same type as *B*, and in Fig. 4(b) it might interact with *B*, while in Fig. 4(c) it would not. The granularity Δ and total size Ω of *B* are indicated in Fig. 4(a).

but a submodel of *B* might need to interact with submodels in neighboring cells.

When the total size of *B* is strictly smaller than a grid cell of *A*, scale separation occurs. It means that *B* interacts with few grid cells of *A*, but also that to fully resolve one cell of *A*, multiple instances of *B* might be necessary. Since the scale of *A* is not fine enough to fully resolve *B*, *B* might be treated as a canonical example for a single grid cell of *A*, using its results throughout the cell and not only where *B* itself is located. This final scenario is used to calculate multiscale speedup [33].

2.3. Multiscale model and single scale models

Multiscale modeling takes advantage of data available at distinct scales by modeling interaction between those scales, accordingly managing the complexity of phenomena involved. Practically this can in certain cases be achieved by first functionally decomposing a multiscale phenomenon into single scale phenomena, which will then form the basis for several coupled submodels. Having coupled submodels instead of a monolithic multiscale model has the additional advantage of aiding modular development, which in turn benefits implementation [51]. At this stage, however, submodel implementation is not considered, only the model formulation. Given Definition 2, three types of functional decomposition are relevant: decomposition by process, finite observation (or discretization), and scale.

First, a process consists of dynamics over an object within a time interval. If any of these terms differ, a different submodel could be used. In practice, the same submodel can be used if the dynamics are sufficiently similar. For example, in two human cells similar processes might occur and those might be represented by the same type of submodel. If the cells have differentiating properties such as cell type or contents, however, a different submodel could be used. Also, if the dynamics of an object change over time, such as when the division of one cell starts, then a different submodel might be used for that.

Second, the discretization of the phenomenon may be a reason for functionally decomposing a phenomenon. For instance a gridbased model and a agent-based model might both represent the same process, but they allow different aspects of a process to be modeled.

Third, decomposing by scale, also called scale splitting, is possible if several phenomena are taking place on different scales, especially if they have scale separation. For instance, one phenomenon might be changing intrinsically faster than another. A spatial example is suspension flow, which behaves like a fluid on a coarse scale but where the viscosity is determined on a fine scale.

Except scale splitting, none of these functional decomposition methods has a particular dependency on multiscale modeling and arguments for it can be found in a lot of components-oriented literature [3,4,28]. Nevertheless, we consider it good practice to do functional decomposition and it will help while doing distributed multiscale computing. Once a multiscale model is decomposed into submodels, each of those submodels should be single scale models. The term single scale model has the intuitive notion of a scale that spans only few orders of magnitude and on which scale splitting is no longer useful to apply. An alternative sense of the term single scale submodel is that the multiscale model also contains other submodels with different scales.

Apart from single scale models, a multiscale model also consists of the interactions between its submodels, indeed, without them a multiscale model would not add anything beyond being a collection. Generally, the single scale models that are formed by once applying functional decomposition should interact.

Finally, when considering model implementation, practical issues may make decomposing a submodel implementation necessary. For instance, take a submodel implementation with computational requirements that scale with the size of its domain, and suppose the submodel turns out to be computationally too expensive to run on a single machine. In order to reduce the computational time, domain decomposition may be performed to split the submodel into multiple instances, each computing only part of the total domain. Although domain decomposition in this case is inspired by practical considerations, generally the submodel on which domain decomposition is performed also needs to change. This allows it to correctly and efficiently interact between different parts of the domain.

2.4. Scale separation map

A way to assess the scales of the phenomena involved in a multiscale phenomenon is to draw its scale separation map (SSM). It is actively used in Complex Automata theory [33] but it can be extended to multiscale modeling in general, as a more basic version of the scale map by Ingram and Cameron [36] shows. Besides helping to gain intuition about the phenomena and their scales, the SSM also communicates the structure of the multiscale model to others.

Practically, the SSM is a log–log plot of the scales of involved phenomena with on the horizontal axis the temporal scale and on the vertical axis the spatial scale; a simple example with one phenomenon is shown in Fig. 2. Once the scales of the phenomena are visualized with an SSM, interactions between phenomena can be indicated by drawing directed edges between their scales. Edges may be labeled with the type of interaction that is involved. For the sake of clarity phenomena may be removed from the map or merged if they cause confusion or cluttering. During later phases of modeling it may become apparent that the SSM is over- or underspecified and it may be redrawn.

An example of an SSM of a nano materials model [52] is shown in Fig. 5, with a macro phenomenon of the materials processes on a tangible macro scale and a micro phenomenon of molecular dynamics of the material. These two phenomena have scale separation in both their temporal scale (fast quantum mechanics dynamics versus slower molecular dynamics) and their spatial scale (molecules versus fibers).

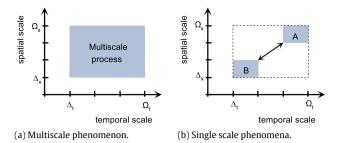


Fig. 5. An example SSM of a classical macro–micro model, showing on the axes spatial and temporal scale, with granularity Δ_x , Δ_t ; and total size Ω_x , Ω_t respectively. In 5(a) the multiscale model without separating the scales; in 5(b) macro single scale model *A* and micro single scale model *B*.

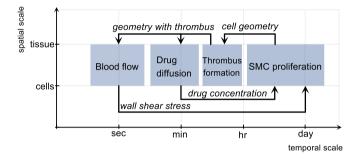


Fig. 6. The SSM of the ISR model, containing four submodels: blood flow, drug diffusion, thrombus formation and smooth muscle cell proliferation. All submodels act at the same spatial scale $S(1 \mu m, 1.5 mm)$ and at a different temporal scale, from $S(100 \mu s, 2 s)$ (blood flow) to S(1.5 h, 30 days) (smooth muscle cells).

Another example, a model of In-stent Restenosis (ISR) as seen in Fig. 6, does not exhibit spatial scale separation: the smooth muscle cell proliferation and blood flow are observed at the same spatial scale. There is temporal scale separation, as blood flow spans a second of a heart beat and a cell cycle lasts a day. The phenomena leading up to ISR, notably the stent placement, are omitted from the map to prevent cluttering.

2.5. Submodel execution loop

In the SSM, edges are drawn to indicate an interaction between phenomena, without stating when information between submodels should be exchanged. To evaluate when information should be exchanged, we will define a few interaction patterns that may be used; and to define these, we will first need to formalize execution patterns of individual submodels. Both submodels and later their implementation should follow these execution patterns.

Of course, a submodel *A* should only exchange information to submodel *B* if a state change in *A* occurs or *B* triggers a state change in *A*. The state change itself can be modeled by an *event* $e \in E$, with a model time $t(e) \in \mathbb{R}$ associated to it. In contrast with the definition by Lamport [41] these events are associated with a model time and not with an execution time. The events are then aggregated into a time series that captures all dynamics of a submodel. By relating the time series to the temporal scale specification $S(\delta_t, \Delta_t, \omega_t, \Omega_t)$ of the underlying phenomenon, δ_t prescribes the minimum time step for events to occur.

Definition 6. A *time series* $\vartheta = \{e_0, \ldots, e_n\}$ is a finite well-ordered set of events with $t(e_i) < t(e_{i+1})$ for all $0 \le i < n$. A future time series ϑ_i contains events occurring after event e_i , so $\vartheta_i = \{e \in \vartheta \mid t(e_i) < t(e)\}$. Modifications to ϑ_i affect ϑ and vice versa.

Time series ϑ adheres to temporal scale specification $S(\delta_t, \Delta_t, \omega_t, \Omega_t)$ iff $\delta_t \leq t(e_{i+1}) - t(e_i) \leq \Delta_t$ for all $0 \leq i < n$ and $\omega_t \leq t(e_n) - t(e_0) \leq \Omega_t$. A time series adhering to a regular scale specification is regular; one adhering to a point scale specification is a point time series.

Event e_0 and e_n in the definition above are used to determine what the initial and final state of the submodel is, respectively.

Corollary 1. *If a time series* ϑ *adheres to a scale specification, then* $|\vartheta| \ge 2$. *A point time series has* $|\vartheta| = 2$.

Because a time series indicates exactly when a state change is observed, it forms a natural guide for executing a submodel. A submodel initializes its state, including boundary conditions, at model time t_0 , after which it observes its own initial state. For each subsequent event, the submodel is solved up to that event and the boundary conditions are updated, after which, again, the intermediate state is observed. During updating the state an event might cause changes in future events, hence the future time series are also updated. The time series should then still adhere to the temporal scale of the submodel. When the last event has been processed a final observation of the state is made, thereby concluding the time series and ending the submodel.

The above description of submodel flow can be formalized in terms of a Submodel Execution Loop (SEL).

Algorithm 1: General submodel execution loop
Input : Starting time t ₀
$i \leftarrow 0$
$f, \vartheta \leftarrow \mathbf{f}_{\text{init}}(t_0)$
while $ \vartheta_i > 0$ do
$\mathbf{O}_{\mathbf{i}}(f, t(e_i), t(e_{i+1}))$
$i \leftarrow i + 1$
$ \begin{array}{c} f, \vartheta_i \leftarrow \mathbf{S}(f, e_i, \vartheta_i) \\ f, \vartheta_i \leftarrow \mathbf{B}(f, e_i, \vartheta_i) \end{array} $
end O (f. t(c))
$\mathbf{O}_{\mathbf{f}}(f, t(e_i))$

Here *f* is the current state of the model, ϑ the time series, *i* the current iteration, e_i the current event, and t_0 the starting time of the submodel. Five operators are used in the SEL: \mathbf{f}_{init} for initialization of the state and the boundary; **S** for solving one modeled step or processing up to the time point of the current event; **B** for re-establishing the boundary conditions; and \mathbf{O}_i and \mathbf{O}_f for an observation of the intermediate and final state, respectively. Each of the operators may contain part of a model or procedures. They are not necessarily mathematical functions, rather they may have side-effects such as reading parameters or writing output. Of these operators, \mathbf{f}_{init} , **S**, and **B** modify the state *f* and future events ϑ_i . Each observation is accompanied by the time point of the last event, and intermediate observations can also take into account the time point of the next event.

Within the SEL, the behavior of a model is determined by how a modeler specifies the operators, i.e. which actions an operator should perform to reflect the specifics of the phenomenon. Also the way the state or the future events are modified is a modeling choice; the only requirement is that the time series still adheres to the temporal scale specification. However, the execution order of the operators is fixed. This should be reflected both in the submodel itself and in its implementation.

The SEL listed in Algorithm 1 can accommodate different types of models. Event-driven modeling is quite obviously possible, by using the time series as an event queue. Time-driven modeling is also possible, by using a regular time series. Implicit functions, without a time step, can be modeled in several ways, depending on the underlying phenomenon and the flexibility and realism of the function. If the phenomenon has a point time series then there is only one event after e_0 that needs to be solved, so the **S** operator can just contain that function. More specific types of models also may fit, for example agent based modeling or cellular automata [32]. This wide range of possible model types will allow most multiscale modelers to make use of the SEL formalism.

Each of these modeling types may use an adapted SEL, as long as the order of the operators remains the same as in Algorithm 1. For a time-driven submodel that does not explicitly consider events and that has a regular temporal scale, Algorithm 2 can be used. Since it has a regular time scale and does not need events, the time series will not be changed during the run and can be abstracted away. The SEL operators **S** and **B** could then be specialized to disregard the time series; in the algorithm these versions are denoted **S**' and **B**'. For example, a submodel computing a new state each discrete time step, based only on its previous state, could use this SEL.

Algorithm 2: SEL of a time-driven submodel
Input : Starting time t_0 and temporal scale $S(\Delta_t, \Omega_t)$
$t \leftarrow t_0$
$f \leftarrow \mathbf{\tilde{f}}_{init}(t)$
while $t - t_0 < \Omega_t$ do
$\mathbf{O}_{\mathbf{i}}(f, t, t + \Delta_t)$
$t \leftarrow t + \Delta_t$
$ \begin{array}{l} f \leftarrow \mathbf{S}'(f,t) \\ f \leftarrow \mathbf{B}'(f,t) \end{array} $
$ f \leftarrow \mathbf{B}'(f, t)$
end
$\mathbf{O_f}(f,t)$

A submodel that consists of single function with point scale $S(\Omega_t)$ can for largely be computed in **S**; other operators can then be left almost empty. As shown in Algorithm 3, the time series can again be abstracted away, and having only two events, even the loop can be removed. This SEL could be used by a submodel that computes a state only once or does not generate meaningful intermediate results.

Algorithm 3: SEL of a single function
Input : Starting time t_0 and point temporal scale $S(\Omega_t)$
$f \leftarrow \mathbf{f}_{\text{init}}(t_0)$ $\mathbf{O}_{\mathbf{i}}(f, t_0, t_0 + \Omega_t)$ $t \leftarrow t_0 + \Omega_t$ $f \leftarrow \mathbf{S}'(f, t)$ $f \leftarrow \mathbf{B}'(f, t)$ $\mathbf{O}_{\mathbf{f}}(f, t)$

The SEL can also be rewritten to that of a cellular automaton, as used in CxA theory [34]. Generally, as long as the execution order of the operators stays the same it can be rewritten to a range of different forms if that facilitates comprehension or implementation.

2.6. Coupling templates

As mentioned, the interaction between submodels is essential to create a multiscale model from a collection of single scale models. Indeed, this coupling of submodels may be the primary object of interest in the model and may be as computationally expensive as the submodels themselves. In contrast to scale bridging techniques used in a coupling, which may differ from one model to the next, we argue that the frequency of interaction between single scale models exhibits regularity. Analyzing patterns in the frequency of interaction gives insights into the dynamics of the multiscale model itself as well as its runtime behavior.

Coupling templates, defined as a data transfer between the SEL operators of two submodel instances, are a means to specify

these patterns. To limit the number of possible data flow patterns, and thus coupling templates, the operators O_i and O_f are only allowed to send data while the operators f_{init} , **B** and **S** may only receive data. This restriction makes coupling templates inherently unidirectional, as they are defined only between a pair of operators, transferring data from one to the other. There are six possible combinations of operators, each with its own interpretation, four of which are listed in Table 2.

The **B** operator is not listed separately among the coupling templates in Table 2, having a similar role as **S** concerning the frequency of interaction. Instead, their role is distinguished by the concepts of multidomain and single domain coupling.

Definition 7. A coupling between two submodels A and B with domains D and D', respectively, is *single domain* (*sD*) iff D is a subdomain of D' or D' is a subdomain of D. Otherwise, the coupling is *multidomain* (*mD*).

The general distinction between boundary operator **B** and solving operator **S** in coupling templates is that **B** is used to receive messages in mD couplings while **S** is used in sD couplings. The motivation for this distinction is that boundary conditions generally should not deal with what happens within their own domain, but rather what happens when interacting with another domain.

For example in the ISR model, the blood flow in the lumen has two type of boundaries: the first is the blood vessel wall, which is defined by the smooth muscle cell proliferation; the second is the artificial boundary of the vessel, with a certain amount of blood flowing in and out of the domain. In this case, the artificial boundary is resolved within the blood flow model, whereas the blood vessel wall is resolved as a mD coupling with the smooth muscle cell domain. On the other hand, the drug diffusion submodel in the uses the same domain as the smooth muscle cell proliferation submodel, making it an sD coupling.

The use of coupling templates can be interpreted to a certain extent. First, if two single scale models A and B have temporal scale overlap then they will need to resolve multiple time steps of each other. Within the SEL this is possible by using the **O**_i and **S** (or **B**) operators, so they will interact for each event in both submodels. This interaction will only occur after the event has happened, so calling $\mathbf{O}_{\mathbf{i}}$ will happen at an earlier time than that it is processed by S. Conversely, if the single scale models are scale separated and A has a larger temporal scale than B, then there is the possibility that *B* needs to be resolved completely once per time step of *A*. Hence, A may call B during each time step and when B is finished it may release its observations and send them to A. When calling B, A gets the time of **O**_i as starting time, and it must release, according to their contiguous or separated scales, before the next solving step of A. If A is an initialization or ab-initio single scale model and it is finished, it may dispatch its state to B, which will continue computation at the time that A left off. Alternatively, A may just dispatch part of its state to a next instance of itself, making A stateful.

These interpretations of the coupling templates are not allencompassing but do in our view provide the main reasons for using them.

In the example of the ISR model, none of the submodels has temporal scale overlap with another, so the interact template is not used. The dispatch template is used when a submodel calculates the initial conditions for the model and sends them to the smooth muscle cell proliferation submodel. This submodel then calls thrombus formation, which in turn dispatches to blood flow and drug diffusion. These submodels then release to smooth muscle cell proliferation, after which the loop continues.

Table 2

Coupling templates between submodels *A* and *B*, listing: its name and operator; what the temporal relation between the operators in *A* and *B* is; what the temporal scale relation between *A* and *B* is; and a common scenario in which the template is used.

	Coupling template		Time	Temporal scale	Scenario
1	Interact	$\mathbf{O}^{A}_{\mathbf{i}} ightarrow \mathbf{S}^{B}$	$t_A < t_B$	Overlap	Reciprocated by the same template
2	Call	$\mathbf{O}_{\mathbf{i}}^{A} ightarrow \mathbf{f}_{\mathrm{init}}^{B}$	$t_A \leq t_B$	Contiguous or separation	Reciprocated by template 3
3	Release	$\mathbf{O}_{\mathbf{f}}^{\scriptscriptstyle B} o \mathbf{S}^{\scriptscriptstyle A}$	$t_B \leq t_A$	Contiguous or separation	B was started by template 2
4	Dispatch	$\mathbf{O}_{\mathbf{f}}^{A} ightarrow \mathbf{f}_{\mathrm{init}}^{B}$	$t_A \leq t_B$	Any	Loosely coupled or stateful.

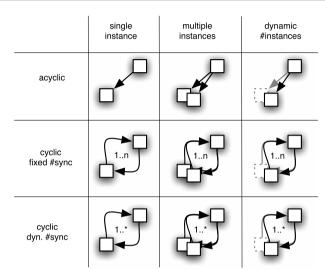


Fig. 7. Graphical overview of different coupling topology properties, like being cyclic or acyclic, having a fixed or dynamic number of submodel instances, and having a fixed or dynamic number of synchronization points. Shown here are only examples with two submodels, but this can be generalized to any number of submodels.

2.7. Coupling topology

Coupling templates indicate what data flow may occur between a pair of submodels, but for interpreting a multiscale model its full topology has to be considered. A coupling topology can be defined as a graph representation of a multiscale model, with coupling templates as its edges, weighted by the number of times data is sent over them, and instances of submodels as its nodes. This is similar to a scale separation map, although the latter does not have submodels instances but only submodels, and does not know how often couplings are used. This edge weight, combined with the SEL, will help understand how often a particular part of a model will be run.

A few properties of coupling topologies are of interest when computing or distributing a multiscale model. Three properties are listed here and visualized in Fig. 7.

- 1. Is the coupling topology cyclic or acyclic, or does only parts contain cycles?
- 2. Are there multiple instances of certain submodels, and if so, can the number of instances be statically determined?
- 3. Can the number of synchronization points be statically determined?

If a multiscale model has an acyclic coupling topology, computation becomes quite straightforward: the submodels can then be ordered and executed consecutively. Otherwise, a more complicated execution model has to be used, like dynamic execution or one that predicts which parts of submodels are scheduled when. When the interact coupling template is used and reciprocated, a coupling topology is cyclic, but a cycle can also be formed with any of the other coupling templates. A cycle can include any number of submodels. The second property, multiplicity, gives an indication for the number of submodel instances that are needed. If there is more than one instance per submodel, these instances need to be addressed separately and a means for forking and joining data might be necessary. If the multiplicity is determined during the runtime of the model, there needs to be a mechanism for the model to spawn new instances of submodels, increasing the complexity of the model and the framework that would run the model.

Having spatial scale separation can be a reason for needing multiple instances of a submodel. Take two submodels A and B with spatial scale separation and A being the larger of the two. The domain of A can then contain a multitude of subdomains modeled by B, needing many instances of B to model them all. If the phenomenon modeled by A is not regular in time or space it might not be predictable how many instances of B are needed and the number of instances needed could even change over time.

Finally, the third property indicates the number of times each submodel will transfer data and do computation. If static, such as when the temporal scales of all submodels are regular, data transfers and submodel execution times can be predicted and thus scheduled. Otherwise, if the model communication is selforganized within the model then the amount of running time is harder to estimate, or if communication is scheduled then the scheduler must be informed of the number of communications and calculations that will take place.

The three properties defined here have a large impact on the complexity of software to compute the multiscale model, where a more dynamic property means more complex software.

3. Specifying a multiscale model

The previous section introduced scales, submodels and coupling templates and topologies. The Multiscale Modeling Language (MML) is a high-level way to describe and specify these concepts, along with the computational architecture of a multiscale model [23]. First of all, MML describes the code implementation of submodels and coupling templates as computational elements. At this stage MML only needs an overview of the implementation, like inputs and outputs and the scale that is used. Second, it introduces computational elements to specify how messages will be distributed between submodels and how they will be affected during transit. Finally, code characteristics of computational elements may be specified to guide a runtime environment in how to execute those elements.

MML has multiple forms:

- a graphical format, hereafter denoted gMML and
- a human-writable, machine-readable XML-based format, denoted xMML.

Between them, xMML is more complete and precise while gMML is more human-friendly. First gMML can be created in a graphical editor and form part of the documentation of a multiscale model or serve as input for creating an xMML file. Then xMML serves as input for generating a scientific workflow or a rudimentary code implementation. Most concepts sketched here were already available in the original presentation of MML, but below they are refined and adapted to the terminology of the previous section. Moreover, the concepts here do not depend on Complex Automata, but rather they are extended to the multiscale modeling formalism sketched in the previous section.

3.1. Computational elements in MML

The primary computational element in MML is a submodel implementation. Both the submodel and its implementation can be described in MML. A computational element has input ports, on which it receives messages, and output ports, on which it sends messages. Connections between computational elements are made with conduits. A conduit is a unidirectional connection between an output port and an input port and it transfers data in the form of messages. A message contains data, for instance an observation of a submodel state, the time point of the event it is associated with, and the time point of the next message that will be sent over the conduit, if any.

Submodels may define ports based on their SEL operator. This means, that output ports may be defined for operators O_i and O_f and input ports for $f_{\rm init}$, **S** and **B**. A coupling template between the operators of two submodels can then be translated as a conduit between an in- and output port defined for those operators. For predictability and to prevent deadlocks, submodels should send a message each time the operator that a port is defined for is reached.

The multiscale modeling framework used for MML could be data-driven, allowing each submodel to execute independently until a message from another submodel is needed, which the submodel will await. A multiscale model can then be initialized by starting a subset of submodel instances, and ended by consequence of the final operator of the SEL of a subset of submodel instances.

Submodels so far defined do not have a state once their SEL is finished. A way to explicitly save a state outside the SEL is to have a coupling from the final observation of the submodel instance to the initialization of the next time that it is called. Since this iteration will only be instantiated if another submodel needs it, it does need separate semantics.

To increase the independence of different submodels, one submodel should not concern itself with sending a data format that is acceptable for the other, nor should the other submodel concern itself with what submodel it is getting data from. Instead, MML has a conduit filter or just filter that can be applied to a conduit. The filter is then applied to messages transferred over that conduit to ensure that both submodels handle the data in a way most convenient to themselves and still communicate correctly. Conduit filters should not model phenomena, but rather do a physically correct data transformation that enables each submodel to reason about its own data. The modeling of these filters alone can be a challenging part of multiscale modeling, for instance when mapping grid-based data to particle based data or doing finegraining or coarse-graining. Filters are allowed to have a state, so they can do time averaging by aggregating data coming in, possibly altering the associated time point in the process. They are reactive as they may not produce data if no data is sent over the conduit, but not inherently predictable, as they may send multiple or zero messages when receiving a single message. Instead, they are predictable by specification, the ratio of the number of messages sent versus the number of messages received has to be specified in advance. In contrast to submodels, filters may know exactly what kind of data the sending submodel will generate and what kind of data the receiving submodel expects. This allows submodels to stay modular.

Consider for instance two submodels *A* and *B* with temporal regular scales $S_A(2 \text{ s}, 1 \text{ h})$ and $S_B(1 \text{ s}, 1 \text{ h})$ that are coupled on a single domain. They have temporal scale overlap and should use the interact coupling templates $\mathbf{O}_i^A \rightarrow \mathbf{S}^B$ and $\mathbf{O}_i^B \rightarrow \mathbf{S}^A$. However,

to allow each submodel to have their own time step and to let the coupling stay correct, a temporal conduit filter should be used on conduits between *A* and *B*. Events should be interpolated in the direction from *A* to *B* to ensure there are enough messages for *B* to process; in the other direction, events should be aggregated to ensure that *A* does not receive too many. Appendix shows an algorithm for a temporal scale conduit filter that does this, accompanied by a proof of being deadlock-free.

Since the filter applies to only one conduit, it cannot do a data transformation for which multiple sources are necessary, nor can it distribute the transformed data to multiple submodels, For these situations a fan-in or fan-out mapper should be used. A fan-in mapper has one output port and *n* input ports, which may accept different types of data. Formally, a fan-in mapper is a procedure $m: I^n \to 0$, where I is an abstract data type of the input ports that may be further specified per port, and O is the output data type. A mapper is procedure rather than a function, since it may interact with the world. A fan-out mapper has one input port and a *n* output ports, which may produce different types of data. Again, formally, a fan-in mapper is a procedure $m : I \rightarrow O^n$, where *I* is the input data type, and *O* is an abstract data type of the output ports that may be further specified per port. Mappers can also have conduits to other mappers, and those conduits may also have conduit filters. For convenience, mappers may perform nontrivial data transformations, reducing the need for filters and thus simplifying the computational architecture. However, combining trivial join and split operations in mappers with filters can in principle yield any data transformation.

When doing domain decomposition or when the number of submodel instances is dynamic it can be useful to instantiate a number of submodel instances at the same time. However, to maintain their modularity, a submodel should not know how many submodel instances it should communicate with. Otherwise, the submodel implementation would have to change each time the domain is decomposed over a different number of submodel instances. By having an intermediate fan-out mapper between the submodels, submodels only need to know what data to send and not how to divide it among submodel instances. Conversely, those submodel instances should not have to know how the workload or domain is divided among themselves, and just send any data to a fan-in mapper that will take care of that. For the disassembly and assembly to happen correctly, the fan-out mapper could also send a message to the fan-in mapper on how it distributed the workload so that the fan-in mapper can correctly reconstruct the data again. With a fan-out and fan-in mapper it is thus easy to create multiple submodel instances simultaneously and address them throughout the multiscale model.

3.2. Graphical MML

Being inspired by UML, gMML is a graphical representation of MML with some UML icons. An example of the gMML of the instent restenosis model is shown in Fig. 8. A submodel instance is shown as a rectangle with a name label inside. Mappers are drawn as a hexagons, with their name labels inside, and a conduit filter as a rounded square, with a name label inside or close to it. If a number of submodels have a single domain coupling, this may be emphasized by drawing a dotted rectangle around the involved submodels, optionally with the name of the domain involved.

Conduits are represented as edges between elements, which may be labeled with the type of data that is sent over it. Based on coupling templates, edge head and tail decoration depends on the SEL operator that a conduit is sending to and from, respectively, as shown in Fig. 9. Operators \mathbf{f}_{init} and \mathbf{O}_{f} are shown as a diamond; operators \mathbf{O}_{i} and \mathbf{S} as a circle, being called within the loop; and operator \mathbf{B} is shown as an empty arrowhead. Edge tails are filled

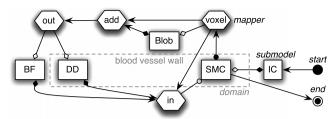


Fig. 8. The gMML of the ISR3D model, which is described in Section 6.1. Labels in italics indicate the different types of computational elements. The different edge heads and tails show the operators that are used, depicted in Fig. 9.

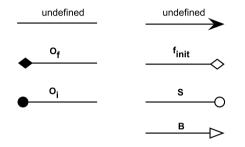


Fig. 9. The different edge heads and tails corresponding to the SEL operators. Undefined means no SEL operator is associated with the coupling.

black, edge heads are empty. Since a mapper does not have an SEL, edges from or to it have no tail or a simple arrow head, respectively.

The submodel instances that are initially instantiated have an edge from a filled black circle; submodel instances that determine when the model will finish have an edge to a filled black circle with a black round border. These circle icons correspond to the start and end state of a UML state diagram.

Limitations of gMML include having no way to see the scales involved, and not being very detailed. Its advantage is that it is a visual way of thinking about the computational architecture of a multiscale model.

3.3. XML format of MML

To automatically process the specification of a multiscale model a machine-readable format is needed, which is preferably also human-writeable. The XML specification has the advantage that it is well-known and that there are many software tools available to edit or parse it. The xMML format is specified with an XML Schema, with which a minimal specification can be enforced and xMML elements may be validated. By using namespaces, the format can be extended with XML extensions such as XInclude, XPointer or RDF, adding some flexibility to the language. These specifications combined form the basis for xMML.

The content of xMML is aimed to be both descriptive and prescriptive. It is descriptive in the sense that it describes in detail the submodels, their computational requirements, and the couplings that they have. It is prescriptive in the sense that: during execution submodels should conform to the scales specified; and a port of a submodel should only be used at the SEL operator it is defined for. The descriptive part enables an execution framework to run and schedule a multiscale model by reading its xMML specification. The prescriptive part allows predicting and possibly enforcing when messages will be sent to which computational element. Together, the descriptive and prescriptive sides of xMML allow a correct execution of a multiscale model.

In Listing 1 an example of the xMML of a macro-micro model is given, with a two-dimensional macro submodel *A* and a set *B* of ten one-dimensional micro submodels. The corresponding gMML is depicted in Fig. 10. The macro submodel starts executing, then

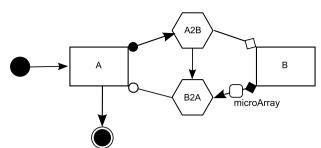


Fig. 10. The gMML of a simple macro-micro coupling, corresponding to Listing 1.

transfers an observation in the form of a grid to a fan-out mapper, which distributes different values to the micro submodels. Afterwards, the reverse direction is executed using a fan-in mapper, after a filter has been applied to reduce the resulting 1D array to a single value. All this is specified within the <topology> tag. The combination is a classical case of macro-micro scale separation, using the coupling templates call ($\mathbf{O}^A_i \rightarrow \mathbf{f}^B_{init}$) and release ($\mathbf{O}^B_f \rightarrow \mathbf{S}^A$) with a single domain coupling, since the micro submodels use a subdomain of the macro submodel. In general, to make the domain used explicit, an <instance> tag may contain a domain attribute.

More detailed specifications are available within the <definitions> tag. Here, the scales of the submodels are specified using SI notation or with time notation in terms of minutes, hours, etc. If no SI unit is given, the default SI unit is presumed, seconds for time and meters for space. In the example, all scales are regular, except that of the second spatial dimension of the macro submodel, which uses the complete scale specification. In the <ports> tag, inputs and outputs of the submodel to which conduits may attach are defined. An SEL operator is assigned to them to associate conduits with a coupling template, and to predict, together with the temporal scale, how often the port will be used. A data type is also assigned to the ports, to later ensure that both the sender and receiver use the same type of data. With <mapper> tags the ports and function of fan-in and fan-out mappers can be specified; with the <filter> tag a datatype converter or scale reduction or interpolation may be specified. Moreover, a model and submodels may be versioned, described and named, and all implementable computational elements may be given an executable class name. With these elements, xMML covers the subjects defined for MML in Section 3.1.

The root element <model> lists the name of the multiscale model, the version of the current document and the version of xMML that is used.

In addition to the modeling aspects, the implementation and computational aspects of a multiscale model can be specified using xMML. Above, the size estimate included in the data type, based on the scales of the involved submodels, is used to estimate the size of messages with that data type. Instead of relying on this implied message size, the expected size may also be explicitly listed for each coupling. With this size estimate, submodels instances may be placed closer together in a distributed environment based on the amount of data transferred between them. In submodels, mappers, and filters an <implementation> tag may be added to specify the estimated memory and CPU requirements, as well as stating library or platform dependencies. Combined, the implementation descriptions allow scheduling software to make more informed decisions on distributing submodels, mappers, and conduits.

4. Multiscale model analysis

Being able to predict the runtime behavior of a modular program has benefits for scheduling, estimating computational costs,

```
<?xml version="1.0"?>
<model id="MacroMicro" xmlns="http://www.mapper-project.eu/xmml" name="Macro-micro model" version="1.0"
    xmml_version="0.3.3">
  <description>A macro-micro model, having a macro grid representation and a micro cell
      representation.</description>
  <definitions>
           <datatype id="lattice2DDouble" size_estimate="x*y*sizeof(double)"/>
           <datatype id="arrayDouble" size_estimate="x*sizeof(double)"/>
                  <filter id="microArray" type="converter"
                                    datatype_from="arrayDouble" datatype_to="valueDouble"/>
      <submodel id="Macro" name="2D Macro model" init="yes">
<timescale delta="1 s" total="1 min"/>
      <spacescale delta="1 mm" total="1 dm"/>
      <spacescale>
                                    <delta min="0.7 mm" max="1.3 mm"/>
                                    <total min="0.7 dm" max="1.3 dm"/>
                           </spacescale>
      <ports>
         <out id="grid" operator="Oi" datatype="lattice2DDouble"/>
         <in id="gridDiff" operator="S" datatype="lattice2DDouble"/>
      </ports>
    </submodel>
    <submodel id="micro" name="1D Micro model">
    <timescale delta="1E-7" total="1E-5"/>
      <spacescale delta="1E-5" total="1E-3"/>
      <ports>
         <in id="start" operator="finit" datatype="valueDouble"/>
         <out id="diff" operator="Of" datatype="arrayDouble"/>
      </ports>
    </submodel>
                  <mapper id="gridDivide" type="fan-out">
                           <ports>
                                     <in id="grid" datatype="lattice2DDouble"/>
                                    <out id="mapping" datatype="latticeMapping"/>
                                    <out id="value" datatype="valueDouble"/>
                           </ports>
                  </mapper>
                  <mapper id="gridCombine" type="fan-in">
                           <ports>
                                    <in id="value" datatype="valueDouble"/>
                                    <in id="mapping" datatype="latticeMapping"/>
<out id="grid" datatype="lattice2DDouble"/>
                           </ports>
                  </mapper>
  </definitions>
  <topology>
    <instance id="A" submodel="Macro"/>
<instance id="B" submodel="micro" multiplicity="10"/>
                  <instance id="A2B" mapper="gridDivide"/>
<instance id="B2A" mapper="gridCombine"/>
    <coupling name="grid" from="A.grid" to="A2B.grid"/>
    <coupling name="values" from="A2B.value" to="B.value"/>
<coupling name="mapping" from="A2B.mapping" to="B2A.mapping"/>
<coupling name="diffs" from="B.diff" to="B2A.value">
                           <apply filter="microArray"/>
                  </coupling>
    <coupling name="grid diffs" from="B2A.grid" to="A.gridDiff"/>
  </topology>
```

```
</model>
```

deadlock detection, and overall validity checking. A multiscale model, as we are proposing, is modular and has internal structure through the submodel execution loop, coupling templates, coupling topology, and computational elements. In this section we obtain the coupling topology of a multiscale model and propose a method to predict the models data flow from its MML specification.

Several formal models for task dependencies and data flow in general exist, for instance task graphs, Petri nets, process algebra, or I/O Automata. In addition, the more informal scientific workflows also have associated tools to predict runtime behavior of modular software. All these methods importantly have some form of software support, as automation gives a feasible and consistent way to predict runtime behavior. We will use task graphs, being the simplest for our purposes.

4.1. Coupling topology: deduction and implications

The coupling topology of a multiscale model can be deduced from its xMML specification. Firstly, whether a coupling topology is cyclic or acyclic can be determined from this specification in linear time by constructing the graph formed by submodel instances as nodes and couplings as edges.

Secondly, the multiplicity of the submodels is explicitly specified in xMML, and can again be verified in linear time.

Finally, whether the number of synchronization points is dynamic can be determined by evaluating the temporal scales of the coupled submodel instances. If all submodels with an output port at their intermediate observation have regular scales then the number of synchronization points will be static (or 'fixed').

The implications of different coupling topologies have the same tendency: a more dynamic setting makes it more difficult to manage and predict the runtime behavior of a multiscale model. In each case the executing framework must anticipate dynamic changes in the number of computational resources required, and manage communication in a dynamic environment. Moreover, since it is up to the model to decide what the dynamic requirements are, the model must also be adapted to communicate dynamic needs to the execution framework.

4.2. Predicting runtime behavior with a task graph

In this article we analyze the runtime behavior of multiscale models using task graphs, a formal but concise way of representing task dependencies and data flow between tasks. A task graph is a directed acyclic graph of tasks as nodes and their dependencies or data flows as edges, as for example in Fig. 12(a). It is used primarily for scheduling on parallel and/or distributed computing resources [40]. A close concept is that of the wait-for graph [43], used for deadlock detection in distributed computing. It can also be seen as a serialized or unfolded graph of the MML description, which may be cyclic. Although task graphs themselves are wellknown, converting a problem to a task graph in a nice way is problem-specific. In this section we convert an MML description to a task graph, which has not been done before.

A multiscale model can be subdivided into submodel instances, and those can be subdivided into SEL operators in conjunction with the iteration of the execution loop. These SEL operators are the main nodes of the task graph. Mappers are also explicit nodes in the task graph, conduit filters on the other hand may be implicit as long as they do not aggregate or interpolate over the temporal scale. Conduits are modeled as dependencies and thereby form the edges. Submodel instances, mapper instances, or conduit instances that are initiated multiple times, for instance from the loop of another submodel, are distinguished by an initiation number. Multiple submodel instances that are initiated at once, for instance for purpose of domain decomposition, form a set. Another type of dependency is that of the internal flow of a submodel, from one of its SEL operators to the next; or more broadly, the state of a submodel to the next in stateful submodels. These dependencies are implicit to the submodel flow and are consequently displayed with a dashed edge instead of a solid one. Together, SEL operators and mappers form the nodes of the task graph, and conduits and internal submodel transitions the edges.

A task graph node representing an SEL operator has a label showing that operator. The full format is *instanceName*_{*j*}[k](o, i), where *instanceName* is the name of the computational element, othe SEL operator and i the iteration. Then j indicates the initiation number of a submodel instance that is initiated multiple times. If a set of submodel instances is concerned, an index k is added. This format can be simplified by leaving out any part, as long as a task remains uniquely identifiable.

The task graph of models with a static number of synchronization points and submodel instances can be statically generated in a linear fashion, as shown in Algorithm 4. The algorithm depends on the SEL and on the coupling of MML's computational elements and as far as we know is an original contribution. If it were to be dynamically generated, while the model is executed, it would not require significant changes, other than some form of communication with that model. The algorithm starts with a number of submodel instances that are specified to be initial, and keeps track of active computational elements. These computational elements have to be well-specified, so mappers and submodels work quite straightforward, although they do have to keep track of their timestamps. A submodel additionally has edges to its next operator and if it is stateful, also to its next instance. Mappers need a message on each input, and once a message has been received on that input, subsequent messages are buffered. In a task graph, this can be modeled by sending the message to the next instance of the mapper. For conduit filters, Algorithm 5 must be evaluated to see where it will send its output, and when all required messages are received.

In order to keep Algorithm 4 relatively brief, it does not include the temporal conduit filter. Support for it can be added at lines B and D, by keeping track of how many messages the filter must receive before it sends a message, and how many messages the filter sends when it finally does send. Likewise, the algorithm does not support conduits with multiplicity, which could be added with a simple for loop at line D.

Deadlock detection happens in two places: while building the task graph and afterwards. During building the task graph, a task that has been active before could be referenced again. Since this can only happen if that task already had all dependencies resolved before, there must be a cycle that causes a message to be sent to it twice. The second time deadlock detection becomes active is after building the task graph, when it can find that some elements were still waiting for input but could somehow not receive it.

In Algorithm 4 three lines A, B, and C indicate what part of the task graph may be distributed. At A, a computational element doing a computation at a certain operator may decide to send a number of messages. Deadlock detection is done by the receiving computational element, which will detect that the timestamp is not correct. At B, it has to wait for all messages to arrive before it can do its own computation, which is built in to the MML specification of an element. The deadlock detection at C, however, has to be changed to distribute efficiently, seeing that it is activated only after all operators and submodels were executed as long as they could. At this point, alternative distributed deadlock detection algorithm should be used.

4.2.1. Task graph acyclicity

The task graph algorithm presented indeed gives an acyclic task graph, simply because any cycle will throw a deadlock. Here we show that in most well-defined cases, deadlock as caused by a cycle will not present itself. To show this, assume that for the interact, call, and release coupling templates; scale separation, overlap, or contiguity is strictly adhered to. To begin with, we will show when pairs of submodels yield an acyclic graph. Thereafter, we will show when this will also yield a total acyclic task graph. The timelines of the different submodels, determining the eventual structure of the task graph, are shown in Fig. 11.

For the first part, consider submodels *A* and *B* with temporal scales $S(\delta_t, \Delta_t, \omega_t, \Omega_t)$ and $S(\delta'_t, \Delta'_t, \omega'_t, \Omega'_t)$ that have temporal scale separation with $\Omega'_t < \delta_t$, and that they are coupled with the call and release coupling templates. A message sent by *A* at **O**_i at time *t*, arrives at *B* at **f**_{init} at time *t*, a message sent by *B* at release arrives at time at most $t + \Omega'_t$. By that time, it reaches the next iteration of *A*, which has time at least $t + \delta_t > t + \Omega'_t$. In terms of task graph nodes this can be expressed as

 $A(i, \mathbf{O}_i) \rightarrow B(0, \mathbf{f}_{init}) \rightsquigarrow \cdots \rightsquigarrow B(n_B, \mathbf{O}_f) \rightarrow A(i+1, \mathbf{S}),$

for any $0 \le i < n_A$, $n_A + 1$ and $n_B + 1$ being the length of the time series of *A* and *B*.

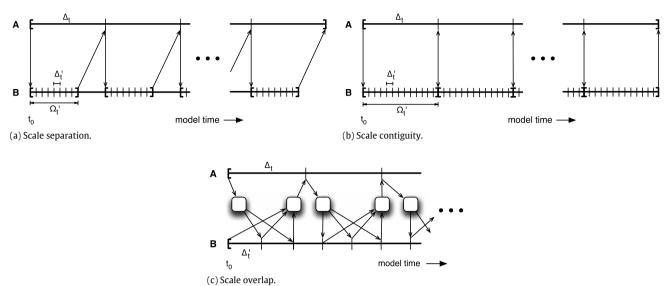


Fig. 11. Timelines of two submodel instances *A* and *B* with temporal scales $S(\Delta_t, \Omega_t), S(\Delta'_t, \Omega'_t)$. The submodels show temporal scale separation, contiguity and overlap, respectively, and they start at time t_0 . Initialization is done at opening braces (\mathbf{f}_{init} and \mathbf{O}_i), the last solving step and finalization at closing braces ($\mathbf{S}, \mathbf{B},$ and \mathbf{O}_i), and each intermediate step at a tick ($\mathbf{S}, \mathbf{B},$ and \mathbf{O}_i). Arrows indicate messages sent, rounded rectangles denote temporal scale conduit filters aggregating or interpolating between messages.

Next, if *A* and *B* have contiguous scales instead, specifically $\Delta'_t \leq \delta_t \leq \Omega'_t \leq \Delta_t$, then it is not clear that the time $t^A \in [t + \delta_t, t + \Delta_t]$ for one iteration of *A* is longer than the time $t^B \in [t + \omega'_t, t + \Omega'_t]$ for *B* to release. On the contrary, this might create an overshoot of at most $\Omega'_t - \delta_t \leq \Delta_t - \delta_t$. It is up to the modeler to prevent this overshoot; failing to do so can lead to cycles or deadlocks. With regular scales, however, this problem does not arise.

Finally, *A* and *B* can have temporal scale overlap, with $\Delta_t < \omega'_t$ and $\Delta'_t < \omega_t$. As mentioned in Section 3.1, we only consider this case under the condition that the granularity of the receiving submodel is fixed, so if the interact coupling template $\mathbf{O}_i^A \rightarrow \mathbf{S}^B$ is used then $\delta'_t = \Delta'_t$, and if the coupling is reciprocated then also $\delta_t = \Delta_t$. This case is the most involved, and to ensure that the task graph becomes acyclic, it is important to reiterate that the interact coupling template specifies that the observation made by \mathbf{O}_i at a certain time *t*, will only be used by the first solving step \mathbf{S} with time t' > t. However, then multiple events in *B* may occur before the next event of *A*. If the ratio between *A* and *B* of events occurred is static, then a time filter may be used on the conduit, which can aggregate events in one direction and interpolate between events in the other as shown in Appendix. This time filter must know the time step of the receiving submodel for this to behave correctly.

So, a message is never sent backwards in time between pairs of submodels. For more submodels, the problem remains submodels with overlapping temporal scales with a varying granularity, which cannot be the receiver of the interact coupling template. Indeed, this remains true for indirect interactions, such as when submodel A uses the call coupling template for B, which then has a release template to C. As long as there is no path of coupling templates starting at **O**_i of one submodel and ending at **S** of another submodel with a varying granularity, this problem does not appear. Likewise, when A uses the call coupling template for B, which uses the dispatch template for C, which uses the release template for A, the combined total time of *B* and *C* might be more than the granularity of A. This problem can only be prevented by a modeler, and it might point to a larger problem with the model: if the combined time of B and C is more than the granularity of A, it might well be that the computed results of *B* and *C* are not valid within the timeframe of one step of A. By constructing the task graph, the task graph will detect a cycle and prevent the mistake from happening.

Mappers, not considered so far, cannot introduce cycles that were not present in the description above because of their behavior of sending a message when a message is received.

4.3. Task graph reduction

Task graphs can get extremely large, growing exponentially in the number of temporal scale separated submodels, exacerbated by submodels that have a lot of iterations. A methods to reduce the number of nodes is collapsing redundant nodes as in Fig. 12(b). This reduction can be performed while the task graph is constructed or after it is finished. The reduction is straightforward, and can be performed no matter how dynamic the multiscale model is.

Nodes of the task graph can be collapsed only if the graph is guaranteed to remain acyclic. For example, a submodel instance *A* that only has a input port at \mathbf{f}_{init} and an output port at $\mathbf{O}_{\mathbf{f}}$ could list all its SEL operators for each iteration as separate nodes, but that would not add any information regarding its dependencies on other submodels. Instead, *A* can be collapsed to a single node in the task graph, while retaining its dependencies of initialization and final observation. To mark it as a collapsed node, a range is assigned to the iteration number and SEL operator in the label. The label of a collapsed node encompassing iterations i_0 to i_1 and SEL operator o_0 to o_1 then becomes *instanceName* (i_0-i_1, o_0-o_1). In general, node *p* can be collapsed with node *q*, forming node *r*, if the following conditions hold:

- *p* and *q* represent the same submodel instance, initialization number and set number;
- *p* has an edge to *q*; and
- *p* has exactly one outgoing edge *or q* has exactly one incoming edge.

If this is the case, *p* and *q* can be removed and replaced by *r*, which will have the edges of *p* and *q*, while excluding the edge from *p* to *q*.

Above conditions ensure that dependencies between submodels remain visible, and that no cycle is introduced in the task graph, as we will show now. Given an acyclic task graph and a reduction from nodes p and q, and suppose a cycle is introduced in the reduction, so that besides a path from s to t, where s and t are non-equal nodes, there is also a path from t to s. First, replacing p and q with

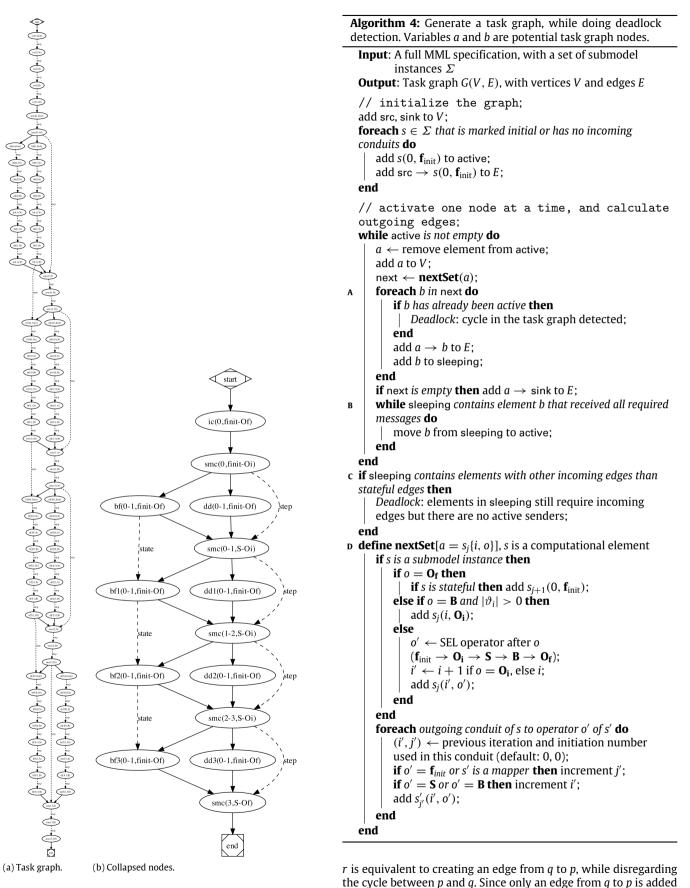


Fig. 12. A task graph of a simplified ISR3D model, which is described in Section 6.1, before and after the reduction described in the text. The actual label text is not important in this example, rather the structure of the task graph can be seen to remain intact.

1. a path from t to q not containing p and

and this causes a path from t to s to be created, there must be

2. a path from p to s not containing q.

Suppose this is the case, and suppose that the condition holds that q has exactly one incoming edge, which is from p, then any path to q must contain p, ruling out item 1. Now, suppose that p has exactly one outgoing edge, then any path from p must also contain q, ruling out item 2. Combined, this contradicts that the given task graph was acyclic. Thus, a reduction performed under listed the conditions yields an acyclic graph.

As long as the conditions above hold, the degree of collapse can vary depending on the intended use of the task graph. If, for example, the exact receiving SEL operator of submodel *A* in the example above must be known, then submodel *A* can be collapsed into two parts; one node for \mathbf{f}_{init} : $A(0, \mathbf{f}_{init})$; and another for the rest: $A(0-n, \mathbf{O}_i - \mathbf{O}_f)$. The above list of conditions is then appended with

- *p* does not have incoming edges from a node of another submodel instance, initialization number or set number and
- *q* has exactly one incoming edge.

If the exact sending SEL operator is also of importance, then in the example $\mathbf{O}_{\mathbf{f}}$ must also be kept separate: $A(n, \mathbf{O}_{\mathbf{f}})$; ensured by appending the conditions with

- *p* has exactly one outgoing edge and
- *q* does not have outgoing edges to a node of another submodel instance, initialization number or set number.

With these simple guidelines, it is possible to reduce the number of nodes in the task graph of a multiscale model.

5. Distributed multiscale execution

A multiscale model, once specified with MML, can be executed in a multitude of ways such as a workflow system, the GridSpace workbench [16], or, as outlined here, a specialized framework. Because of the modular setup we propose for multiscale models, it is feasible to distribute the computation among multiple heterogeneous machines. For example, a setup with a single laptop possible, but also an execution over a university network or full use of networked supercomputers. Outlined below is an automatic method that reads the model specification and executes it.

At this point we assume that a multiscale model needs distributed computing capabilities. If, however, the multiscale model has sufficiently homogeneous submodels in terms of computational requirements, a single computer or cluster might in fact be sufficient. Again, the task graph that was presented in the previous section can be analyzed using existing task graph algorithms, whether it makes sense to schedule the different modules to distributed computing resources.

5.1. Implementing a model in MUSCLE

A framework that can execute multiscale models is the Multiscale Coupling Library and Environment (MUSCLE) [30]. It consists of two base elements: the kernel, which contains the submodel code, and the conduit, which transfers information unidirectionally between the ports of two kernels. The core of MUSCLE is implemented in Java, but it has bindings for C++, using the Java Native Interface (JNI), which form a link to Fortran or C. Although MUSCLE has its own configuration format, an xMML file can be converted to that format in a straightforward way.

As said, MUSCLE supports conduits and submodels, the latter of which should be implemented by the model developer as a kernel. However, the SEL is currently not enforced by the kernels and has to be coded by the model developer, simply by making a loop in which sending and receiving messages are ordered in the same way as the SEL. Conduit filters are explicitly supported, and quite a few have already been pre-defined, but others can also be implemented. On the other hand, mappers are only implicitly supported; they can be implemented as kernels with a simple loop.

Submodels can be parallelized by using, for instance, threads, OpenMP, or MPI. Although the support for threads with MUSCLE is good, MPI is more laborious to use. Since MUSCLE has a Java core, it is not straightforward to call it as an MPI program. Currently, either submodels call code that uses MPI as a separate executable, excluding the benefits of having native conduits and adding overhead [8], or they use a recently added MPI interface. MUSCLE is still in development and a native C++ client is underway to simplify these issues.

5.2. Execution with MUSCLE

The library part of MUSCLE, as outlined in the previous section, could in principle be executed by different runtime engines. In practice, however, MUSCLE is the only runtime engine that supports executing MUSCLE code.

A multiscale model can be computed by specifying its submodel instances and conduits, and then starting each submodel instance on the command-line. Not all submodel instances have to be called in the same command-line statement, and by starting different instances on different machines, providing an IP-address of one of those machines, the submodel computation can be distributed. Where to execute the submodels depends on their computational requirements and resources available. If the entire model can easily run on a single computer one can use MUSCLE on that single computer, with a single command. If the submodels need to be distributed, they can, as long as there is TCP/IP communication possible between the machines they will run on, and they just need to be started on each machine separately.

If on the other hand the targeted machines are not directly available, but are part of a grid or e-Infrastructure, it is possible and advisable to make use of grid middleware. For example the tools from the QosCosGrid software stack [39] can take care of reserving and co-allocating different resources to run MUSCLE on. Given that an MML description can be converted to a task graph, such middleware or scheduling system could also make use of the task graph for scheduling submodels on several resources. In this contribution, we do not consider the specifics of scheduling the different parts of a multiscale model to a distributed infrastructure. Rather, we refer to existing task graph literature that addresses this [21,6,40,14].

6. Example applications

The methodology outlined in this paper is being applied to several multiscale applications in the MAPPER project [55] from five scientific communities: biomedical physics, nano materials, hydrology, fusion and systems biology. By way of example, we will highlight two multiscale models from this project: in-stent restenosis [12] and the formation of clay–polymer nanocomposite materials [52].

6.1. ISR3D

First, the methodology is applied to a three-dimensional multiscale model of in-stent restenosis (ISR3D) of a stent deployment in a coronary artery and subsequent processes. The objective of the model is to help understand restenosis and to indicate improvements in stent design. An extended multiscale model, in terms of an SSM is described by Evans et al. [22]. A simplified version as well as a detailed description of the implementation of the submodels and the coupling with MUSCLE is provided by Caiazzo et al. [12], Hoekstra et al. [33]. Some detailed two-dimensional simulations are reported by Tahir et al. [53]. The ISR3D model consists of five submodels: initial cell positions and stent deployment as initial conditions (IC), thrombus formation (Blob), blood flow (BF), drug diffusion (DD) and smooth muscle cell proliferation (SMC). First, IC initializes the model by placing a stent in an artery. These initial conditions are sent to SMC and for each iteration of SMC, the thrombus formed by placement of the stent is calculated by Blob. The calculated geometry is used by DD and BF, which are calculated in parallel. Their results are then used by SMC. For performance reasons BF keeps track of its last state to simplify subsequent flow calculations.

As seen in Fig. 6, the submodels of ISR3D all have temporal scale separation, except with IC, which scales from seconds of stent deployment to days of thrombus formation before the rest of the model is started. They all have spatial scale overlap, since they range over the same part of an artery. DD happens on a corresponding domain to that of SMC, in the vessel wall, so they have a sD coupling. The coupling between SMC and Blob and BF, on the other hand, is mD, as BF and Blob are calculated in the blood vessel lumen. In IC and SMC, a Lagrangian or particle based domain is used, while Blob, DD, and BF have a Eulerian or grid-based domain.

The coupling topology of ISR3D is cyclic, and each has a single instance per submodel. It has a fixed number of synchronization points: a modeler chooses a fixed timespan that the stenosis will be evolved over.

The gMML of ISR3D is shown in Fig. 8. It has four mappers: voxel, add, fanOut and fanIn. First, the voxel mapper converts the Lagrangian domain to a Eulerian one, converting positions and radii of particles to a binary 3D grid, with grid cells valued to true if they contain part of a particle. That grid is sent to Blob, and the result of Blob is added to the domain in the add mapper. Then the fanOut mapper distributes the domain to BF and DD, and the fanIn mapper collects the results. The fanIn mapper also converts the grids used by BF and DD back to a particle representation using the mapping created by the voxel mapper.

The model is implemented using MUSCLE. Except BF, each of the submodels was implemented specifically for this model. BF uses the general purpose Lattice-Boltzmann library Palabos.¹ All mappers and DD are completely written in Java, other submodels use C++ or Fortran. The BF submodel uses most of the computational time, although it is also most parallelized.

In total and with one core allocated, ISR3D takes two weeks to do a single run on a iMac with an Intel i5 3.6 GHz processor. When parallelizing BF, and running it on a node with a 32 core IBM Power6 4.7 GHz processor, this is reduced to 5 days. Although the gain is then large for BF, especially SMC then becomes a bottleneck since it is not parallelized. By using MUSCLE it runs on distributed infrastructure [8], by combining it with the QosCosGrid stack it can also be automatically scheduled [9].

6.2. Nano materials

Another example, is a multiscale model of the formation of clay–polymer nanocomposite materials, which in certain formations can be fire-retardant or extremely sturdy. Between multiple clay sheets, it evaluates quantum mechanics (QM) for the placement of individual atoms, fine-grained molecular dynamics (FGMD) for the placement of individual molecules, and coursegrained molecular dynamics (CGMD) for the placement of groups of molecules. The simulation starts by evaluation QM properties, then the computed values are used in the FGMD submodel, and finally the placement of the molecules is used in the CGMD submodel. Domain decomposition is performed on the QM and



Fig. 13. The gMML of the Nano materials application. It starts with a few QM submodels, after which their output is collected by the C fan-in mapper. The output is then preprocessed by fan-out mapper M to send it to a number of FGMD submodels. Their output, and the mapping used by M, is collected by the CM fan-in mapper to be used by the final CGMD submodel.

FGMD submodels, the first into 6 instances and the second to between 10 and 20 instances.

The three submodels have a typical macro-micro coupling, from QM to FGMD to CGMD, with spatial and temporal scale separation, and a scale ranging from picometer to micrometer and from picosecond to millisecond. Smaller submodels are in a subdomain of larger submodels, so all couplings are sD.

The gMML of Nano materials is shown in Fig. 13, and also features mappers to manage information coming from the submodels with decomposition. The coupling topology is acyclic, as can be seen from the gMML, so it also has a fixed number of synchronization points. Also the number of submodel instances is fixed before the model starts.

The model is implemented using multiple libraries: the LAMMPS and CASTEP, with Perl scripts acting as mappers. The workflow is straightforward to implement. It can be run in a distributed environment using Gridspace 2 as a workflow manager and the Application Hosting Environment (AHE) [60] as a middle-ware stack.

7. Conclusions and further work

Multiscale modeling is being embraced as a paradigm to study and better understand nature. Models produced in this way can be computationally expensive, leading the way to distributed multiscale computing. In this contribution, we have laid foundations for distributed multiscale computing, from a formal background to a full computational specification, which can be analyzed to execute on distributed infrastructure. Moreover, using this methodology it is already possible to do distributed multiscale computing.

The formal part has been inspired largely by Complex Automata theory [34] by generalizing it to multiscale modeling, and is duly influenced by the Heterogeneous Multiscale Method (HMM) [18], Ingram et al. [37] and the multiscale ontology by Yang and Marquardt [59]. By formally defining concepts as phenomenon, scale and scale separation, we were able to restrict and classify the flow of a submodel and the interaction between submodels. Moreover, the definitions form a basis for decomposing and thus modularizing a multiscale model.

The frameworks classification by Ingram et al. [37] is the following: multidomain, embedded, parallel, serial, and simultaneous. The first, multidomain integration consists of a macroscale model *M* coupled to a microscale model μ on a separate domain. In our methodology this is represented by a mD coupling between μ and *M*, and suppose these models have temporal scale overlap, then the interact coupling template with the SEL **B** operator will be used. If there are multiple micromodels, their data can first be aggregated by a mapper before M processes it. In an embedded integration, μ models a subdomain of M, which is a sD interaction. The call and release coupling templates could be used here if there is no temporal scale overlap. With parallel integration, two submodels 1 and 2 model the same domain using a different representation. They will have to have a cyclic coupling topology and have temporal scale overlap, and will use the interact coupling templates. With serial integration, one submodel is executed after the other. This is exactly what the dispatch coupling template, and the acyclic coupling topology is meant for. Finally, with simultaneous integration

¹ http://palabos.org.

all submodels run at a microscale and information is integrated after they run. In our methodology this can be achieved by computing the microscale models and sending the output to a fan-in mapper, which can process and aggregate the information computed. The strength of our methodology is that it allows multiple of these strategies to be combined, having for instance parallel integration on one part and multidomain integration on another.

Finally, the multiscale ontology by Yang and Marquardt [59] provides a formal background to multiscale modeling. Unfortunately, although their definitions of domain are very thorough, their definition of scale is too hierarchical to be suitable for multiple dimensions. By redefining scale in this paper, we have a clear way to identify the scale of a submodel and relate it to the scales of other submodels. Their definition of a coupling is similar to ours, although we do not impose laws on the couplings. Instead, we offer conduit filters that modelers can use to enforce a rule on a conduit, which is a more low-level way to represent a coupling laws. Interesting definitions that we do not reproduce are those of couplings between elements or subdomains of two submodels and composing submodels to form a system that again acts as a submodel.

From the restricted behavior of our formalism, a computational specification language, the Multiscale Modeling Language (MML) [23], is refined and firmly based. It takes advantage of scales but also includes well-defined computational elements such as one-way conduits, conduit filters and mappers, used to interconnect the different submodels. It is a high-level language, leaving the implementation of those elements free. Additionally, since it is constrained by the definitions in multiscale modeling, it is more specific and concrete than other component-based modeling specifications, such as CCA [3].

Given such a focused multiscale model specification with welldefined elements, its properties can be deduced: how dynamic it is, what dependencies and possibilities for deadlock appear between submodels, and how the model could be scheduled over multiple resources. We propose a method to represent the execution of a multiscale model with a task graph, which can in turn be used to schedule submodels over multiple (distributed) resources [21,14]. Additionally, if all computational elements adhere to the MML specification, possible deadlocks can be detected before execution while constructing the task graph.

Finally, a properly defined and analyzed multiscale model can be executed for example by the Multiscale Coupling Library and Environment (MUSCLE) [30]. Within MUSCLE, conduits and some filters are already supplied and submodels and mappers can be implemented in Java or C++, or any programming language that has an interface with C++, such as Fortran or C. MUSCLE is under active development, which will be the basis for a separate contribution. MUSCLE does not do scheduling, so for distributed multiscale computing a combination with grid middleware such as QosCosGrid tools [39] is being explored.

Alternatives to MUSCLE for executing a multiscale model are possible, seeing that MML is not tied to a specific implementation. Particularly, if a multiscale model has a acyclic coupling topology then there are much simpler systems than to execute it. In such a case, a lot of workflow composition tools would also suffice, of which multiple are guite suited for distributed execution [11,2].

One of the goals of the MAPPER project is to further automate the combined workflow of specifying, analyzing, and doing distributed execution of a multiscale model by developing additional MML tools and integrating them with QosCosGrid and GridSpace 2 [16]. To get thorough support for grid computing and highperformance machines, more parts of MUSCLE will be adapted to have a more independent C++ code, instead of relying on its Java core for all submodel management. This has the additional advantage that MPI can become more transparent and integrated within MUSCLE. Even though this paper addresses *how* distributed multiscale computing can be achieved, in future research we will focus on the *performance* of doing distributed multiscale computing as opposed to local computing. This research aims to show exactly when distributed multiscale computing is advantageous. With MML and the task graph it is possible to reason about this and make precise calculations.

In this paper no solution is offered for models with cyclic coupling topologies that contain submodels with non-regular temporal scales. For full inclusion of event-based submodels, as well as handling other types of more dynamic models, this will prove important. At the least an extension to the fan-in mapper is needed to solve this, with which the mapper may accept a different number of messages on certain input ports than on others. This possibly introduces non-determinism for the dependencies in the task graph, and its full implications should be further studied.

Acknowledgments

We would like to thank James Suter, Derek Groen, and Peter Coveney of University College London for providing information about the nano materials application. The MAPPER project receives funding from the EC's Seventh Framework Programme (FP7/2007-2013) under grant agreement No. RI-261507.

Appendix. An algorithm for a conduit filter

The conduit filter used as a computational element in MML and described in Section 3.1 can alter the data flow between submodels. As such, it is good to explore what algorithm would be good to do this, and show that this algorithm does not introduce deadlocks.

Consider again, two submodels *A* and *B* with temporal regular scales $S_A(2 \text{ s}, 1 \text{ h})$, $S_B(1 \text{ s}, 1 \text{ h})$ that are coupled on a single domain. They have temporal scale overlap and use the interact coupling templates $\mathbf{O}_A^A \rightarrow \mathbf{S}^B$ and $\mathbf{O}_B^B \rightarrow \mathbf{S}^A$. To allow these submodels to have their own time step, while still handling the coupling correctly, a temporal conduit filter should be used on conduits between *A* and *B*. Messages from *A* to *B* should be interpolated to give *B* enough messages to process, and in the other direction messages should be aggregated to ensure *A* does not receive too many, as shown in Algorithm 5.

The filter in the direction from *A* to *B* has to know the time series $\vartheta = (e_0, \ldots, e_n)$ of *B*, in order to send the correct number of messages, for instance by the modeler specifying it. It does not need to know the time step of *A*, as *A* sends, with each message, both the timestamp of the message and the timestamp of the next event. Thus, the filter can decide whether the next event of *A* will need to be aggregated, or, that a message can be sent to *B* immediately.

The communication from *A* to *B* is correct if the filter sends the right number of messages at the right time. This statement can be assessed by three filter properties, with filter *f* and events e_1, \ldots, e_n of the receiving submodel:

- 1. for each event e_i with $1 \le i \le n, f$ sends exactly one message;
- 2. if *f* receives a message with time $t \ge t(e_i)$, $1 \le i \le n$, it has already sent a message for event e_i ; and
- 3. if *f* receives a message with time $t < t(e_i)$, $1 \le i \le n$, it has not yet sent a message for event e_i .

Due to the well-ordering of time series, messages received are inorder. Also given, is that a conduit filter may only send messages if a message is received. Then the first two properties combined prevent a deadlock, while the third property ensures that messages sent to B can be meaningful, that is, it prevents the trivial algorithm where upon the first message received, n messages are sent. Algorithm 5: Example of a temporal scale conduit filter, where *i* is the index of the last event *e*, for which the receiving

submodel already received a message.	g			
Input : Time series $\vartheta = (e_0, \ldots, e_n)$ of receiving submodel				
$1 i \leftarrow 0;$				
2 while $i < n$ do				
$m \leftarrow \text{receive()};$				
add <i>m</i> to messages;				
5 $t_{m*} \leftarrow \text{time of message after } m, \text{ or } \infty \text{ if } m \text{ is the last}$				
message;				
6 if $t(e_n) \leq t_{m*}$ then				
$7 \mid i' \leftarrow n;$				
8 else				
9 $i' \leftarrow k$ such that $t(e_k) \leq t_{m*} < t(e_{k+1});$				
10 end				
11 if $i' > i$ then				
12 $(s_{i+1}, \ldots, s_{i'}) \leftarrow \text{interpolate within messages;}$				
13 send(s_{i+1}),, send($s_{i'}$);				
$14 i \leftarrow i';$				
15 end				
16 end				

The first property is straightforward and prevents a deadlock for B, without considering other submodels or couplings. The second property prevents a deadlock that would occur if: the filter waits for a message from A; B waits for a message from the filter; and A waits for a message from B. Suppose that all properties above hold, and that a deadlock occurs due to the filter. Submodel A and B would have model time t_A and t_B , respectively, which is, by their SEL, also the time of the next message they will send. Because of property 2, the conduit filter cannot receive a message with time t_A if $t_A \ge t_B$, so $t_A < t_B$. Now A would only wait for a message from B if $t_A > t_B$, following the definition of the interact coupling template in Table 2. Combined, these statements imply that $t_A > t_B$ and $t_A < t_B$, contradicting that a deadlock can occur under the stated conditions.

Take Algorithm 5 as filter *f* and apply it to the conduit from A to B. Assume that A starts at model time $t_0 < t(e_1)$, with event e_1 of B. In words, A must start before or at same model time as *B*, approximately, since a conduit filter cannot produce output without input.

Before showing that f satisfies the properties of a deadlock-free conduit filter, observe that lines 13 and 14, combined with ϑ being well-ordered and messages of f being sent in-order, ensure that at the end of each loop, exactly i messages are sent.

First, A will send a last message since it has a finite number of time steps. At that point line 5 will assign $t_{m*} \leftarrow \infty$. After that, line 7 will ensure that i = n at the end of the algorithm, fulfilling property 1. Second, starting time t_0 of A has $t_0 < t(e_1)$ by assumption, so the first message *f* receives will obey property 2 with time $t = t_0 < t(e_1)$. Suppose message *m* with next event time t_{m*} obeyed property 2, then the next message m' has time $t_{m'} = t_{m*}$. Now suppose that f violates property 2, by assuming that it sent a message for e_k and that $t_{m'} > t(e_k)$. Then in the previous iteration of the while loop, $t_{m*} > t(e_k)$. Because time series ϑ is well-ordered, the conditions on line 6 and 9 will ensure that i' > k. Now line 13 ensures that a message has been sent for e_k before m'is received. This is a contradiction, showing that f fulfills property 2. Finally, suppose f has sent a message for event e_k . Then line 13 has been executed with $i' \ge k$, so lines 6 or 9 had $t_{m*} \ge t(e_k)$. Since *f* receives messages in-order, this means it cannot receive a message with time $t_m < t(e_k)$, fulfilling property 3.

This shows that the three properties for a deadlock-free filter have been satisfied by Algorithm 5.

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