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Local Disturbance Decoupling
with Stability for Nonlinear
Systems



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PREFACE

In the last decade quite some research has been carried out on stabilization problems for nonlinear control systems on the one side and to synthesis problems on the other. Until now, little attention has been paid to the study of systems for which a design objective as well as a stability requirement have to be met at the same time. This monograph fills up part of this gap by developing a local theory for the disturbance decoupling problem with stability.

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Leo van der Wegen

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