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# The puzzle of the formation of T8 dwarf Ross 458c

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#### ABSTRACT

At the lowest masses, the distinction between brown dwarfs and giant exoplanets is often blurred and literature classifications rarely reflect the deuterium burning boundary. Atmospheric characterization may reveal the extent to which planetary formation pathways contribute to the population of very low mass brown dwarfs, by revealing whether their abundance distributions differ from those of the local field population or, in the case of companions, their primary stars. The T8 dwarf Ross 458c is a possible planetary-mass companion to a pair of M dwarfs, and previous work suggests that it is cloudy. We here present the results of the retrieval analysis of Ross 458c, using archival spectroscopic data in the  $1.0-2.4 \,\mu$ m range. We test a cloud-free model as well as a variety of cloudy models and find that the atmosphere of Ross 458c is best described by a cloudy model (strongly preferred). The CH<sub>4</sub>/H<sub>2</sub>O is higher than expected at  $1.97^{+0.13}_{-0.14}$ . This value is challenging to understand in terms of equilibrium chemistry and plausible carbon-to-oxygen (C/O) ratios. Comparisons to thermochemical grid models suggest a C/O of  $\approx 1.35$ , if CH<sub>4</sub> and H<sub>2</sub>O are quenched at 2000 K, requiring vigorous mixing. We find a [C/H] ratio of +0.18, which matches the metallicity of the primary system, suggesting that oxygen is missing from the atmosphere. Even with extreme mixing, the implied C/O is well beyond the typical stellar regime, suggesting either a non-stellar formation pathway or the sequestration of substantial quantities of oxygen via hitherto unmodelled chemistry or condensation processes.

Key words: brown dwarfs.

# **1 INTRODUCTION**

Brown dwarfs span the mass range between stars and giant exoplanets and are found as isolated objects, binary systems, and companions to stars. Most discussions of the formation of brown dwarfs consider them as the substellar extension of the star formation process (e.g. Whitworth et al. 2007; Stamatellos & Whitworth 2009; Whitworth 2018, and references therein). However, the growing sample of isolated planetary-mass brown dwarfs (e.g. Faherty et al. 2013; Liu et al. 2013; Schneider et al. 2016; Theissen et al. 2018; Bouy et al. 2022), wide-orbit (resolved) planetarymass companions (e.g. Burgasser et al. 2010; Miles-Páez et al. 2017; Faherty et al. 2021), and giant exoplanets with masses above

\* E-mail: j.jensen@herts.ac.uk (JG) b.burningham@herts.ac.uk (BB); jfaherty@amnh.org (JF) † 51 Pegasi b Fellow. The compositions of brown dwarfs may provide clues to their formation mechanism. For objects that are companions to stars, we might expect a shared carbon-to-oxygen (C/O) ratio if both formed at the same time and from the same material, whereas a C/O ratio that differs might suggest an alternative formation path to that of the star. For example, very low mass brown dwarfs may have formed like gas giant planets in discs, through either core accretion or gravitational instabilities (Bate, Bonnell & Bromm 2002). Different oxygen-bearing species condense at different locations, removing oxygen from the vapour and yielding a higher C/O ratio in the gas phase. As a result, at the water ice line the C/O ratio of grains would decrease, and then again increase at the CO ice line (Öberg, Murray-Clay & Bergin 2011). An object formed in such a differentiated

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the deuterium burning limit (e.g. Bakos et al. 2009; Rosenthal et al. 2021) raises the question as to the contribution of planetary formation pathways to the low-mass end of the substellar population.

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protoplanetary disc may thus inherit a C/O ratio that is quite unlike its parent star.

For the brown dwarf population that represents the substellar extension of the star formation process, we can expect the distribution of C/O ratios to follow that of the stellar field population. This distribution is generally tight and close to the solar value of 0.54 (Asplund, Grevesse & Sauval 2005), with a C/O > 0.8 very unusual (e.g. Fortney 2012; Nissen 2013; Nakajima & Sorahana 2016). If a significant number of the lowest mass brown dwarf companions, on the other hand, formed via a planet-like formation scenario, we might expect their C/O distribution to be altered by comparison.

In this paper, we present the analysis of the first target of a wider study of the local brown dwarf and substellar companion populations. Ross 458c was discovered by Goldman et al. (2010) and followed up by Burgasser et al. (2010) and Burningham et al. (2011), and is a young T8 dwarf. Comparisons to evolutionary models suggest that it may be a planetary-mass object, while its wide orbit of 1200 au around an M dwarf binary argues against formation via core accretion or disc fragmentation (if the object formed *in situ*).

Another unusual feature of Ross 458c is its apparent cloudiness (Burgasser et al. 2010; Burningham et al. 2011; Morley et al. 2012). Clouds are a possible opacity source in brown dwarfs, as inferred from data, and theoretically expected from condensation of species possible at pressures and temperatures found in substellar objects (see e.g. Kirkpatrick 2005; Lodders & Fegley 2006; Kirkpatrick et al. 2021). Although T dwarfs have been generally thought to be cloud free (e.g. Kirkpatrick 2005), it has been suggested that sulphide and alkali-salt clouds may start to appear in late-T dwarfs (Morley et al. 2012).

In this paper, we use retrieval analysis to investigate the composition and cloudiness of this interesting target. The retrieval technique follows on from and complements analysis using onedimensional, self-consistent, radiative-convective equilibrium 'grid models'. Grid models attempt to simulate the substellar atmosphere self-consistently using a handful of bulk parameters that typically include  $T_{\text{eff}}$ , log g, metallicity, cloud parameters, and (sometimes) C/O (e.g. Saumon & Marley 2008; Marley & Robinson 2015; Marley et al. 2021). Also, vertical mixing can drive certain molecular abundances out of chemical equilibrium (e.g. Noll, Geballe & Marley 1997; Saumon et al. 2006; Marley & Robinson 2015). The extent to which this occurs depends on the mixing time-scale, and this is often included via some additional parameter (e.g. eddy diffusion coefficient  $K_{zz}$ ; Griffith & Yelle 1999; Saumon et al. 2006).

A variety of techniques are used to fit these models to data to draw conclusions, from simple  $\chi^2$  minimization to more sophisticated Bayesian methods (e.g. Zhang et al. 2021). This can result in poor fits to the data, with the grid models inadequate to describe the data (Line et al. 2017). Due to their complexity, it is difficult to identify the poor assumption or missing physics that is driving the bad fit.

Retrievals make fewer assumptions about the state of the atmosphere, and instead parametrize it over many more dimensions with little if any requirement for self-consistency. While this can result in unphysical outcomes, which should be considered when interpreting the result, it also allows data-driven insights that can highlight, or work around, shortcomings in self-consistent approaches (e.g. Burningham et al. 2021). Another benefit of retrievals is that one gets a measure of the C/O ratio from the observations (here using CH<sub>4</sub> and H<sub>2</sub>O) as a retrieved parameter, as opposed to a prescribed ratio that is hardwired into the model. In this work, we will use the BREWSTER retrieval code that has been demonstrated effectively in cloudy atmospheres in the substellar regime (Burningham et al. 2017, 2021; Gonzales et al. 2020).

The paper is organized as follows: In Section 2, we provide an overview of current literature on Ross 458c. Section 3 describes BREWSTER, the retrieval framework. In Section 4, we present the results of the retrievals. Section 5 presents discussion and analysis of the results, and Section 6 presents the conclusion.

#### 2 ROSS 458 SYSTEM

#### 2.1 Ross 458AB

The primary system consists of M0.5 and M7, separated by a distance of 0.5 arcsec (about 5 au; Beuzit et al. 2004). The metallicity of the primary system is supersolar at  $[Fe/H] = +0.2 \pm 0.05$  (Burgasser et al. 2010).

Burgasser et al. (2010) place constraints on the age of the Ross 458 system of 150–800 Myr, the upper limit based on the magnetic activity and H $\alpha$  emission of Ross 458A and the lower limit on the absence of low surface gravity indicators (such as the 7000 Å KI doublet), which would be expected in young M dwarfs.

Eggen (1960) selected the system as a possible member of the Hyades open cluster, with an age of around 625 Myr (Lebreton et al. 1997), while Nakajima, Morino & Fukagawa (2010) selected it as a possible member of the IC 2391 Moving Group, with an age of approximately 50 Myr. Any membership association would place further constraint on the age of the system.

Table 1 summarizes previously published parameters for Ross 458A and Ross 458B.

#### 2.2 Ross 458c

Ross 458c is a T dwarf of spectral type T8 (Burgasser et al. 2003) or T8.5p (Burningham et al. 2011) and is a wide-orbit companion to the binary Ross 458AB (Goldman et al. 2010). It is separated from its primaries by 102 arcsec (1200 au). The system is at a distance of  $11.5 \pm 0.2$  pc (Gaia Collaboration 2018).

Burgasser et al. (2010) found  $T_{\rm eff} = 650 \pm 25$  K from fitting selfconsistent grid models. This is in good agreement with the values found by Burningham et al. (2011) (using bolometric luminosity) of 695 ± 60 K. Filippazzo et al. (2015) found a similar value of 721 ± 94 K using their bolometric luminosity method.

One of the key results in those previous examinations of Ross 458c was the somewhat surprising feature of clouds in a late-T dwarf. Burgasser et al. (2010) found that models which included cloud opacity were a better fit to the near-infrared (NIR) spectrum of Ross 458c. They argued that it may indicate a resurgence of iron and silicate clouds that are thought to have disappeared at the low temperatures of the late-T dwarfs.

Morley et al. (2012) investigated possible causes of the apparent cloud opacity. Their best-fitting model for Ross 458c was a 700 K, log g 4.0 model that incorporated sulphide (Na<sub>2</sub>S, MnS, and ZnS) clouds. Manjavacas et al. (2019) find spectrophotometric variability in Ross 458c with an amplitude at the  $\approx$ 2 per cent level, indicating a partial cloud cover rotating in and out of view.

In more recent work, Zhang et al. (2021) attempted to estimate the parameters using the Sonora Bobcat grid models (Marley et al. 2021), using the prism spectra of Ross 458c. However, they struggled to get a good fit. The model spectrum was brighter in the Y and J bands, and had fainter flux in the blue wing of the H and K bands. They argue that this is likely due to clouds,

Table 1.	System	literature	values	for the	Ross	458	system.
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Parameter	Value	Notes/units	Reference
α	13:00:46.5802	J2000	Gaia Collaboration (2018)
δ	+12:22:32.604	J2000	Gaia Collaboration (2018)
π	$86.8570 \pm 0.15$	mas	Gaia Collaboration (2018)
$\mu_{lpha}$	$-632.151 \pm 0.50$	mas yr <sup>-1</sup>	Gaia Collaboration (2018)
$\mu_{\delta}$	$-36.019 \pm 0.19$	mas yr <sup>-1</sup>	Gaia Collaboration (2018)
Ross 458A spectral type	M0.5	_	Hawley, Gizis & Reid (1997)
Ross 458B spectral type	M7.0	_	Beuzit et al. (2004)
Period	14.5	yr	Heintz (1994)
Distance	$11.51\pm0.02$	pc	Gaia Collaboration (2018)
Projected binary separation (minimum) <sup>a</sup>	5.4	au	Beuzit et al. (2004)
Binary separation <sup>a</sup>	0.475	arcsec	Beuzit et al. (2004)
Projected separation (minimum) to Ross 458c <sup>a</sup>	1168	au	Goldman et al. (2010)
Separation to Ross 458c <sup>a</sup>	102	arcsec	Goldman et al. (2010)

<sup>*a*</sup>No uncertainties provided in the sources.

**Table 2.** Parameters' literature values of Ross458c.

Parameter	Value	Notes/units	Reference
α	13:00:41.15	J2000	Gaia Collaboration (2018)
δ	12:21:14.22	J2000	Gaia Collaboration (2018)
Spectral type	$\mathrm{T8.9}\pm0.3$	-	Goldman et al. (2010)
	T8	-	Burgasser et al. (2010)
	T8.5p	-	Burningham et al. (2011)
T <sub>eff</sub>	$695\pm60$	Κ	Burgasser et al. (2010)
	$650 \pm 25$	Κ	Burningham et al. (2011)
	$804^{+30}_{-29}$	Κ	Zhang et al. (2021)
	$721 \pm 94$	Κ	Filippazzo et al. (2015)
	$722^{+11}_{-12}$	Κ	This work
log g	4-4.7	$log(cm s^{-2})$	Burningham et al. (2011)
	4	$\log(\mathrm{cm}\mathrm{s}^{-2})$	Burgasser et al. (2010)
	3.7–4	$log(cm s^{-2})$	Morley et al. (2012)
	$4.50\pm0.07$	-	This work
$\log_{10}L_{\rm bol}/L_{\odot}$	$-5.62\pm0.03$	-	Burgasser et al. (2010)
	-5.61	-	Burningham et al. (2011)
	$-5.27\pm0.03$	-	This work
Metallicity	$-0.06\pm0.20$	-	Goldman et al. (2010)
	0	Assumed	Burgasser et al. (2010)
	+0.3	Cloud free	Burgasser et al. (2010)
	0	Assumed	Burningham et al. (2011)
	$0.18\pm0.04$	[C/H]	This work
Age	<1	Gyr	Manjavacas et al. (2019)
	0.4-0.8	Gyr	West et al. (2008)
	0.15-0.8	Gyr	Burgasser et al. (2010)
Mass	5-14	M <sub>Jup</sub> , inferred	Goldman et al. (2010)
	6.29-11.52	M <sub>Jup</sub>	Burgasser et al. (2010)
	5-20	MJup, inferred	Burningham et al. (2011)
	$2.3^{+2.3}_{-1.2}$	$M_{Jup}$	Zhang et al. (2021)
	$27^{+4}_{-4}$	M <sub>Jup</sub>	This work
Radius	1.19-1.29	R <sub>Jup</sub>	Burgasser et al. (2010)
	1.01-1.23	R <sub>Jup</sub>	Burningham et al. (2011)
	$0.68\pm0.06$	$R_{Jup}$	Zhang et al. (2021)
	$1.45 \pm 0.06$	$R_{Jup}$	This work

reduction in vertical temperature gradient, or CO/CH<sub>4</sub> or  $N_2/NH_3$  disequilibrium chemistry. As a result, the radius and inferred mass are small. The model atmospheres used in their study were cloud free, and with a C/O fixed at solar. These limitations might result in inaccurate estimated parameters. This work will improve upon these shortcomings by having a larger set of less restrictive parameters.

For the retrieval of Ross 458c, we make use of archival data; for full details of the data, see Burgasser et al. (2010). We have fluxcalibrated the data using the same UKIRT Infrared Deep Sky Survey (UKIDSS) *J*-band photometry used in Burningham et al. (2011) to provide consistency between the two studies and remove a source of possible discrepancies between our results.

Table 2 provides an overview of the literature values of Ross 458c.

**Table 3.** Priors for retrieval model. The tolerance factor, o, is to allow to unaccounted sources of uncertainty. The wavelength shift is the shift in wavelength between the data and the model. See Burningham et al. (2017) for a complete description. The cloud decay scale,  $(\Delta \log_{10} P)_{decay}$ , is constrained within the height of the atmosphere by  $\log_{10} P_{top} + 4$ . The cloud thickness,  $(\Delta \log_{10} P)_{thick}$ , is constrained by 2.3, the bottom of the atmosphere.

Parameter	Prior
$\overline{\text{Gas fraction } (X_{\text{gas}})}$	log-uniform, $\log X_{gas} \ge -12.0$ , $\sum_{gas} X_{gas} \le 1.0$
Thermal profile <sup>a</sup> : $\alpha_1, \alpha_2, P_1, P_3, T_3$	Uniform on resulting T, 0.0 K $< T_i < 5000.0$ K
Thermal profile <sup><i>b</i></sup> : $T_{bot}$ , $T_{botQ}$ , $T_{mid}$ , $T_{topQ}$ , and	Uniform, 0.0 K $< T_i < 5000.0$ K; $T_{bot} < T_{botQ} < T_{mid} <$
T <sub>top</sub>	$T_{\rm topQ} < T_{\rm top}$
Mass <sup>b</sup>	Uniform, $1 M_{Jup} \le R \le 80 M_{Jup}$
Radius <sup>b</sup>	Uniform, 0.5 $R_{Jup} \le R \le 2.0 R_{Jup}$
Scale factor <sup>a</sup> , $R^2/D^2$	Uniform, constrained by 0.5 $R_{Jup} \le R \le 2.0 R_{Jup}$
Gravity <sup>a</sup> , $\log g$	Uniform, constrained by 1 M <sub>Jup</sub> $\leq gR^2/G \leq 80$ M <sub>Jup</sub>
Power-law cloud opacity ( $\tau \propto \lambda^{\alpha}$ ), $\alpha$	Uniform, $-10 \le \alpha \le 10$
Cloud decay scale, $(\Delta \log_{10} P)_{\text{decay}}$	Uniform, $0 < (\Delta \log_{10} P)_{\text{decay}} < \log_{10} P_{\text{top}} + 4$
Cloud thickness $(\Delta \log_{10} P)_{\text{thick}}$	Uniform, constrained by $\log_{10} P_{top} \le \log_{10} P_{top} +$
	$(\Delta \log_{10} P)_{\text{thick}} \le 2.3$
Cloud total optical depth (extinction) at 1 $\mu$ m <sup>3</sup>	Uniform, $0.0 \le \tau_0 \le 100.0$
Hansen distribution effective radius, a	log-uniform, $-3.0 < \log_{10} a(\mu m) < 3.0$
Hansen distribution spread, b	Uniform, $0 < b < 1.0$
Wavelength shift	Uniform, $-0.01 < \Delta\lambda < 0.01 \ \mu m$
Tolerance factor, o	Uniform, $\log(0.01 \times \min(\sigma_i^2)) \le o \le \log(100 \times \max(\sigma_i^2))$
<sup><i>a</i></sup> EMCEE only.	· · ·

<sup>b</sup>Nested sampling only.

#### **3 RETRIEVAL FRAMEWORK**

We use the BREWSTER retrieval framework, for which a more complete description can be found in Burningham et al. (2017, 2021) and Gonzales et al. (2020). The retrieval framework consists of the forward model, which produces the spectrum based on a set of parameters, and the retrieval model, which uses Bayesian inference to explore the posterior, estimate parameters, and perform model selection. The following section contains a brief recap of key features, and updates for this work.

#### 3.1 Forward model overview

BREWSTER divides the atmosphere into 64 pressure layers with properties of temperature, gas opacity, and cloud opacity. The atmosphere is also parametrized by gravity, which sets the scale height. The output of the forward model is the flux at the top of the atmosphere, which must be scaled by the ratio of the squared radius, R, and distance to the target, D, i.e.  $(R^2/D^2)$ . As will be discussed in Section 3.2, we use two different algorithms for exploring the posterior: EMCEE (Foreman-Mackey et al. 2013), and nested sampling using PYMULTINEST (Buchner et al. 2014). These two methods use slightly different parametrizations due to the differences in how the priors are treated in each algorithm. Specifically, mass and radius are retrieved directly in the nested sampling version, whereas they are derived from the  $(R^2/D^2)$  scaling parameter and  $\log g$  in the EMCEE version. The thermal profiles also differ as will be discussed in Section 3.1.1.

The forward model parameters are discussed below, and are listed in Table 3 along with their priors.

#### 3.1.1 Thermal structure

As is typical in atmospheric retrievals, we do not directly retrieve the temperature for all 64 layers in our model atmosphere, but instead use a smaller number of parameters to set the thermal profile. In previous works (e.g. Burningham et al. 2017, 2021; Gonzales et al. 2020), we

thermal profile. This scheme treats the atmosphere as three zones:  $P_0 < P < P_1 : P = P_0 e^{\alpha_1 (T-T_0)^{\frac{1}{2}}}$ (Zone 1),  $P_1 < P < P_3 : P = P_2 e^{\alpha_2 (T-T_2)^{\frac{1}{2}}}$ (Zone 2),

have used the Madhusudhan & Seager (2009) parametrization for the

$$P > P_3 : T = T_3$$
 (Zone 3), (1)

where  $P_0$  and  $T_0$  are the pressure and temperature at the top of the atmosphere that becomes isothermal with temperature  $T_3$  at pressure  $P_3$ . In its most general form, a thermal inversion occurs when  $P_2 > P_1$ . Since  $P_0$  is fixed by our atmospheric model, and continuity at the zonal boundaries allows us to fix two parameters, we consider six free parameters  $\alpha_1$ ,  $\alpha_2$ ,  $P_1$ ,  $P_2$ ,  $P_3$ , and  $T_3$ . If we rule out a thermal inversion by setting  $P_2 = P_1$  (see fig. 1, Madhusudhan & Seager 2009), we can further simplify this to five parameters  $\alpha_1$ ,  $\alpha_2$ ,  $P_1$ ,  $P_3$ , and  $T_3$ .

For our new nested sampling version of BREWSTER, we have employed a simple five point T-P profile, which sets temperatures at the base ( $T_{\text{bot}}$ ), top ( $T_{\text{top}}$ ), mid-point ( $T_{\text{mid}}$ ), and quarter pressure depths ( $T_{\text{top}Q}$ ,  $T_{\text{bot}Q}$ ) in the atmosphere in  $\log_{10} P$ . These points are then joined by spline interpolation to define the 64 layer temperatures. The only restrictions on the values these five points may take is that they lie in the range 0 < T < 4000 K, and decrease towards shallower pressures.

#### 3.1.2 Gas opacity

The gas opacity is set by the gas fractions in each layer. In this work, we directly retrieve these as vertically constant mixing ratios. Previous retrievals of late-T dwarfs using the assumption of chemical equilibrium to allow for vertically varying abundances found such models poorly ranked (see e.g. Gonzales et al. 2020). Moreover, grid model fits in Burningham et al. (2011) suggested that non-equilibrium chemistry is important for this Ross 458c. As such, we have not performed any retrievals under the assumption of chemical equilibrium in this work.

In this work, we consider the absorbing gases  $H_2O$ ,  $CH_4$ , CO,  $CO_2$ , NH<sub>3</sub>, H<sub>2</sub>S, Na, and K. Their opacities are taken from the compendium presented in Freedman, Marley & Lodders (2008) and Freedman et al. (2014). For the Na and K D1 and D2 lines, broadened by collisions with H<sub>2</sub> and He, the Lorentzian line profile becomes inadequate, and line wing profiles are taken from Allard, Kielkopf & Allard (2007a) and Allard, Spiegelman & Kielkopf (2007b, 2016). We also consider the alkali opacities from Burrows & Volobuyev (2003) as an alternative given the uncertainty surrounding the best treatment for this issue, as there is no agreement in literature as to which is the preferred choice. Gonzales et al. (2020) tested both Burrows and Allard alkalis on their L7+T7.5p SDSS J1416+1348AB binary target. The 1416A component (L7) was best fit using the Allard treatment, while the 1416B component (T7.5p) was best fit using the Burrows treatment. The Allard alkalis provide consistent abundances between the co-evolving pair, and is hence the best fit for the pair as a whole. We follow Gonzales et al. (2020) in testing both the Burrows and the Allard treatments for alkalis.

We include continuum opacities for  $H_2-H_2$  and  $H_2$ -He collisionally induced absorption, using cross-sections from Richard et al. (2012) and Saumon et al. (2012). We also include Rayleigh scattering due to  $H_2$ , He, and  $CH_4$ , and continuum opacities due to bound–free and free–free absorption by  $H^-$  (Bell & Berrington 1987; John 1988) and free–free absorption by  $H_2^-$  (Bell 1980).

#### 3.1.4 Cloud opacity

The cloud opacity is parametrized in several ways, which have between three and five parameters. These parameters fall broadly into two categories: those that describe how the cloud opacity is distributed in the atmosphere and those that describe the cloud's optical properties.

**Cloud structures:** The clouds' distribution in the atmosphere is parametrized as either a 'deck' or 'slab' cloud. In the deck cloud, it is not possible to see the bottom of the cloud. The deck cloud has the following parameters:

(1) Pressure at which the optical depth passes 1, looking down.

(2) The decay height, the pressure over which the optical depth drops by a factor of 2.

In contrast to the deck cloud, in the slab cloud, it is possible to see the bottom of the cloud. The slab cloud has the following parameters:

(1) The total optical depth of the cloud at 1  $\mu m$  (reached at the base of the cloud).

(2) Pressure at the top of the cloud (where  $\tau_{cloud} = 0$ ).

(3) The thickness of the cloud slab (in  $d\log P$ ).

**Cloud optical properties:** The cloud opacity can be parametrized in one of three ways. The optical depth is either grey (wavelength independent), a power law ( $\tau = \tau_0 \times \lambda^{\alpha}$ ) where  $\tau_0$  is the optical depth at 1 µm, or Mie scattering. If the cloud opacity is powerlaw dependent as opposed to grey, an extra parameter is added, the power index  $\alpha$ , defining the wavelength-dependent cloud opacity as  $\tau \propto \lambda^{\alpha}$ . In both the grey and the power-law cases, scattering is neglected, and the cloud is assumed to be absorbing. When using Mie scattering, we have two additional parameters, the Hansen *a* and *b* parameters (Hansen 1971). The Hansen *a* parameter is the particle size distribution effective radius in log( $r/\mu$ m). Hansen *b* parameter is the particle size distribution spread. Therefore, for a deck cloud, we then have four parameters, and five for the slab.

Table 4. Sources for optical data for condensates used in this work.

Condensate	Reference
MnS	Huffman & Wild (1967)
KCl	Querry (1987)
MgSiO <sub>3</sub>	Scott & Duley (1996)
Na <sub>2</sub> S	Khachai et al. (2009)
Soot	Dalzell & Sarofim (1969)

A variety of condensates are potentially able to form in cool T dwarf atmospheres and contribute to the cloud opacity. Burgasser et al. (2010) hypothesized a re-emergence of iron and silicate clouds for late-T dwarfs, which would have broken up at the L-T transition. Of the iron and silicate clouds, it is the silicate clouds that will be found at the lowest temperatures and shallowest pressures. These silicate clouds are expected to be composed of enstatite (MgSiO<sub>3</sub>), forsterite (Mg<sub>2</sub>SiO<sub>4</sub>), or SiO<sub>2</sub> (quartz: e.g. Lodders & Feglev 2006: Visscher, Lodders & Fegley 2010; Burningham et al. 2021). Since we are unlikely to be able to distinguish between these species using only NIR data, we have only tested one: MgSiO<sub>3</sub>. Morley et al. (2012) argue that sulphide clouds may be present in late-T dwarfs and test Na<sub>2</sub>S, MnS, and ZnS, as they are expected to condense at lower temperatures. The abundance of ZnS is low and they find that it does not create an observable change in the spectrum; its optical depth is negligible, so ZnS is not included in the models we test here. KCl is also expected to condense at cooler temperatures (Morley et al. 2012), and is one of the models tested here. Graphite clouds can appear in carbon-rich atmospheres with supersolar C/O ratio (Moses et al. 2013a,b). As a proxy for graphite, we used optical data for soot, due to its high carbon content.

Only one cloud type is tested per model run. We don't expect spectral features arising from Mie scattering of particular condensate compositions from any of the expected cloud species to be observable in the 1.0–2.5  $\mu$ m region. So, we judged that the additional computational load and complexity due to adding extra model combinations in the form of multiple cloud models, would not be justified in terms of improvements to the fit.

We calculate scattering and absorption Mie coefficients from real and imaginary refractive indices for our condensate species obtained from the sources of optical data shown in Table 4. For grey and power-law opacities, no optical data are used.

#### 3.2 Posterior sampling

In previous works, BREWSTER used the EMCEE sampler (Foreman-Mackey et al. 2013). However, this method of sampling has some drawbacks such as uncertainty surrounding convergence; the challenge of exploring the entire probability volume to avoid sensitivity to initial values due to local maxima; and difficulty surrounding the calculation of the Bayesian Evidence for model selection. For this work, BREWSTER has been updated to also include nested sampling by incorporating the PYMULTINEST sampler (Buchner et al. 2014), which avoids these issues. We test both the EMCEE and PYMULTINEST posterior sampling techniques to check for consistency between the two methods.

#### 3.3 Model selection

The EMCEE sampler does not allow for the evaluation of the Bayesian evidence, but provides a maximum likelihood, which is used to calculate the Bayesian information criterion (BIC). The model with

Table 5. BIC.

$\Delta BIC$	Strength
0–2	No preference worth mentioning
2-6	Positive
6-10	Strong
>10	Very strong

Table 6. Bayesian evidence difference.

ΔlogEv	Strength
0-0.5	No preference worth mentioning
0.5-1	Substantial
1-2	Strong
>2	Decisive

the lowest BIC is the preferred model. The strength of the preference of one model over another is defined by Kass & Raftery (1995) as shown in Table 5.

The PYMULTINEST sampler returns the nested importance sampling global log-evidence (logEv; Feroz et al. 2019). For two competing models, model selection between models 1 and 0 of the preferred model is achieved as follows:

$$R = \frac{\mathcal{Z}_1}{\mathcal{Z}_0} \frac{\Pr(H_1)}{\Pr(H_0)}.$$
(2)

Z is the Bayesian evidence.  $Pr(H_1)/Pr(H_0)$  is the prior probability ratio for the two models, which can in most cases, including this, be set to unity. The preferred model is the model with the larger value for Z, with the strength of the preference of one model over another being the ratio of their evidences (Feroz et al. 2019). The MULTINEST algorithm returns the logEv, and hence the strength of the preference is defined as the difference between the models' logEv ( $\Delta$ logEv). Narrative statements corresponding to boundaries in the values for  $\Delta$ logEv are defined by Kass & Raftery (1995) as shown in Table 6.

# 4 RESULTS

#### 4.1 Summary

We tested both the EMCEE and the PYMULTINEST options for sampling the posterior, to confirm consistency between results. The results quoted here are from PYMULTINEST, as it is preferred due to sampling the entire parameter space, avoiding being stuck in local minima and maxima. The best-fitting model for the nested sampling is a cloudy model, with a power-law slab cloud. For nested sampling, we use the Bayes factor to compare the different models. The evidence difference to the winning model is listed in Table 7. The evidence difference to the second-ranked model is substantial.

For the EMCEE sampling, the top-ranked model is the powerlaw slab cloud, with the alternative treatment of the alkali line broadening. The second-ranked model is the power-law slab cloud. Both PYMULTINEST and EMCEE have the same two models ranked in top, the order is just switched. For EMCEE, we use the  $\Delta$ BIC for model selection. The  $\Delta$ BIC is shown in Table 8. There is a strong preference for the top-ranked model as opposed to the second ranked, and a very strong preference against the lower ranked models.

The top-ranked models are cloudy models with the cloud opacity as a power law. 'Real' clouds with Mie scattering are rejected, as is the cloud-free model. We consider two different alkali profiles. For the PYMULTINEST sampler, the Allard alkalis are ranked second, whereas for the EMCEE sampler, the Allard alkali profiles are ranked first, with the Burrows profile second. We cannot assert which is the right profile to use, as it is dependent on methodology.

#### 4.2 Retrieved spectrum

Fig. 1 shows the spectrum with cloud-free Sonora models overplotted, of  $T_{\text{eff}} = 800$  and 700 K,  $\log g = 4.5$  and 5.0, and the main absorption features. The models are all 'normalized' to the *J* band. All of the plotted grid models underestimate the flux in the *Y*, *H*, and *K* bands compared to the data for Ross 458c. This may indicate that one of the key issues for the grid models is that their predicted flux in the *J* band is too bright relative to the rest of the NIR spectrum.

Our retrieval model provides a much better fit to the data across the entire NIR wavelength range covered. This likely reflects the greater flexibility available to a retrieval model, and its ability to allow for non-solar abundance ratios. A key feature in our ability to fit the *J*-band peak is the inclusion of clouds (as will be discussed in Section 4.4). The only region that the retrieval model struggles to fit well is the *Y*-band peak, and this likely reflects challenges associated with the pressure-broadened wings of the alkali D-lines, which is shared by the grid models.

#### 4.3 Thermal profile

Fig. 2 shows the thermal profile for the winning model along with comparison to self-consistent grid models and cloud condensation curves. The placement of the cloud in pressure space is plotted on the side. The thermal profiles for comparison are the Sonora Bobcat models (Marley et al. 2021) with  $T_{\rm eff} = 700$  and 800 K and log g = 4.5 and 5.0. The comparison models were selected based on the retrieved  $T_{\rm eff}$  and log g.

Generally, the models match the retrieved profile best at deeper pressures, where they follow the retrieved gradient well. The model that matches the retrieved profile best at deeper pressures is the  $T_{\rm eff} = 800$  K, log g = 5.0. The models do not match closely at shallower pressures, where the differences are significant, as our retrieved profile is warmer (see Fig. 2). At the shallowest pressures in our model [log (*P*/bar)  $\sim -3$  to -4] there is little contribution to the flux (see Fig. 3), and a correspondingly large scatter in the retrieved temperature of atmosphere. However, at slightly deeper pressures [log (*P*/bar)  $\sim -1$  to -2] there is significant contribution of flux, and the retrieved thermal profile is quite tightly constrained and diverging from the grid models with a more isothermal gradient.

This difference between the retrieved profile and other grid models at shallow pressures is also seen in other works, such as the warmer L dwarfs in Burningham et al. (2021), and in works such as Line et al. (2017) sample of late-T dwarfs. It is not seen in Gonzales et al. (2020) L7+T7.5p pair, nor in Gliese 570D (Line et al. 2015; Burningham et al. 2017).

# 4.4 Cloud properties

In agreement with previous works (Burgasser et al. 2010; Burningham et al. 2011; Morley et al. 2012), we find that the atmosphere of Ross 458c is best described with a cloudy model. The winning model is a cloudy one, structured as a slab cloud. Burgasser et al. (2010), using grid models, found that enstatite cloud models provided a good fit to the data, whereas Morley et al. (2012), though not testing enstatite clouds, found that sulphide clouds fit the data

Model type	Nparams	$CH_4/H_2O$	logEv difference
Power-law slab cloud	20	$1.97^{+0.13}_{-0.14}$	0
Power-law slab cloud, Allard alkalis	20	$2.13_{-0.15}^{+0.14}$	-0.83
MgSiO <sub>3</sub> slab cloud	21	$1.86^{+0.19}_{-0.18}$	-8.29
Na <sub>2</sub> S slab cloud	21	$1.82^{+0.20}_{-0.19}$	-8.80
Cloud free	16	$1.74_{-0.19}^{+0.20}$	-9.27
Grey deck cloud	18	$1.68^{+0.20}_{-0.20}$	-10.85
KCl deck cloud	20	$1.79_{-0.18}^{+0.17}$	-12.05
MgSiO <sub>3</sub> deck cloud	20	$1.76_{-0.18}^{+0.19}$	-12.08
Power-law deck cloud	19	$1.70_{-0.21}^{+0.20}$	-12.31
Soot deck cloud	20	$1.32_{-0.23}^{+0.28}$	-13.57
KCl slab cloud	21	$1.73_{-0.17}^{+0.18}$	-13.88
Grey slab cloud	19	$1.63_{-0.16}^{+0.17}$	-14.40
MnS slab cloud	21	$1.71_{-0.17}^{+0.17}$	-14.49
MnS deck cloud	20	$1.75_{-0.21}^{+0.19}$	-18.20
Soot slab cloud	21	$1.45_{-0.37}^{+0.23}$	-18.37

 Table 7. List of models tested in this work for Ross 458c, along with the logEv difference, using the PYMULTINEST sampler.

Table 8.	List of	models	tested in	this	work	for	Ross	458c,	along	with	the
$\Delta$ BIC, us	ing the	EMCEE S	ampler.								

Model type	Nparams	$\mathrm{CH}_4/\mathrm{H}_2\mathrm{O}$	$\Delta BIC$
Power-law slab cloud, Allard alkalis	21	$1.82^{+0.31}_{-0.46}$	0
Power-law slab cloud	21	$1.69^{+0.31}_{-0.51}$	+6
Grey slab cloud	20	$1.67^{+0.28}_{-0.56}$	+25
Soot slab cloud	21	$1.79_{-0.24}^{+0.22}$	+27
Na <sub>2</sub> S slab cloud	21	$1.83^{+0.19}_{-0.23}$	+35
MnS slab cloud	21	$1.71_{-0.29}^{+0.24}$	+44
MgSiO <sub>3</sub> slab cloud	21	$1.42_{-0.42}^{+0.37}$	+51
KCl slab cloud	21	$1.28^{+0.32}_{-0.21}$	+68
Cloud free	16	$1.66^{+0.23}_{-0.25}$	+81
Power-law deck cloud	20	$1.61\substack{+0.36 \\ -0.80}$	+84
MnS deck cloud	20	$1.66_{-0.64}^{+0.32}$	+87
Na <sub>2</sub> S deck cloud	20	$1.76_{-0.19}^{+0.18}$	+91
Grey deck cloud	19	$1.57^{+0.32}_{-0.57}$	+92
MgSiO <sub>3</sub> deck cloud	20	$1.71_{-1.06}^{+0.41}$	+92
KCl deck cloud	20	$1.71_{-0.31}^{+0.27}$	+96
Soot deck cloud	20	$1.52\substack{+0.26 \\ -0.23}$	+100

best. Model selection rejects 'real' clouds with Mie scattering, so we are unable to distinguish the cloud species based on optical properties.

Fig. 2 shows the condensation curves for the tested cloud species alongside our retrieved thermal profile. The curves do not mean that the particular cloud *will* condense, but rather they indicate where it *can* condense. So, a given cloud species *can* condense to the left (cooler) of its condensation curve on Fig. 2. Two clouds that could condense at our retrieved cloud location are the MnS and MgSiO<sub>3</sub> clouds. KCl and Na<sub>2</sub>S condense at cooler temperatures. So, our thermal profile and the placement of the cloud deep in the atmosphere is suggestive of enstatite or other silicate clouds due to the retrieved cloud location with respect to the condensation curves. We note that the other silicates that were not tested (see Section 3.1.4) have very similar condensation temperatures, so this



**Figure 1.** Spectrum of Ross 458c in the 1–2.4  $\mu$ m range with retrieved spectrum of winning model (power-law slab cloud) in green, and errors in grey. Overplotted are self-consistent cloud-free Sonora grid models. The models are scaled to match the *J*-band flux.

cloud may actually be a mix of these very similar silicates. This will be difficult to test since these clouds appear to be so deep in the atmosphere. The *JWST* data will likely incorporate the spectral features around  $8-10 \ \mu m$  arising from Mie scattering of these silicates. However, at those wavelengths clouds are likely to be well below the photosphere.

Fig. 3 shows the contribution function. This shows where in the atmosphere the flux is coming from. The shading of the area indicates the relative contribution of flux from that layer. The darker shaded the area, the more flux from that layer. The blue line is the gas opacity where  $\tau_{gas} = 1.0$ . The cloud is the purple line (at  $\tau_{cloud} = 1.0$ ), and is placed in the bottom of the atmosphere, below the photosphere, except for an overlap at the *J* band, at around 1.3 µm.

This suggests that the cloud has the biggest impact in the *J*-band peak, where it reduces the flux from the deep atmosphere that escapes between the deep water and methane absorption bands on either side. This is what drives the much improved fit for our retrieval model compared to the cloud-free grid models shown in Fig. 1.



Figure 2. Pressure–temperature profile of winning model (power-law slab cloud). The dashed lines are condensation curves for the different clouds tested. The curves do not mean that the particular cloud will condense, it just means that it can condense at that pressure and temperature. The right part of the figure is the placement of the cloud in the atmosphere, the grey shaded parts are the  $1\sigma$  errors. The solid coloured lines are the self-consistent Sonora Bobcat grid models.



**Figure 3.** Contribution function of winning model (power-law slab cloud) with  $\tau_{cloud} = 1$  in purple and  $\tau_{gas} = 1$  in blue.

#### 4.5 Gas abundances

Fig. 4 shows the retrieved bulk properties of Ross 458c, including the retrieved values for the gas abundances, along with log g. Some gases, such as CO, CO<sub>2</sub>, and H<sub>2</sub>S, are not well constrained, as seen on the histogram distribution. This has been the case for all NIR late-T dwarf retrievals using low-resolution NIR spectra (Line et al. 2017; Gonzales et al. 2020). To date, only Tannock et al. (2022) have detected H<sub>2</sub>S in a NIR T dwarf spectrum, and it required spectroscopy with  $R \sim 45000$ , 100x higher than used here. Even at this high resolution, CO is still invisible due to masking by stronger CH<sub>4</sub> absorption.

We do detect and constrain the abundances of  $H_2O$ ,  $CH_4$ ,  $NH_3$ , and Na + K. This is the same set of molecules constrained by other works in this temperature regime (Line et al. 2017; Zalesky et al. 2022).

The corner plot also shows the C/O (here using the  $CH_4/H_2O$  ratio), of 1.97, the calculation of which will be discussed in Section 5.

Our retrieved abundance for  $NH_3$  is consistent with chemical equilibrium predictions, while CO and  $H_2O$  are not. The abundance profiles for  $H_2O$  and  $CH_4$  are close to vertical, somewhat justifying our vertically constant mixing ratio assumption in the retrieval model.  $H_2O$  and  $CH_4$  match their abundances at 100 bar (2000 K), and this may be suggestive of their chemistry being quenched at this level due to rapid vertical mixing. This is discussed further in Section 5.2.3.

#### **5 ANALYSIS AND DISCUSSION**

In line with earlier studies of Ross 458c, we find that the atmosphere is best described by a cloudy model. The best-fitting cloud model is a power-law slab cloud, this is consistent for both the EMCEE and the nested sampling.

#### 5.1 T<sub>eff</sub>, luminosity, radius, and mass

The bulk properties of mass, radius,  $T_{\rm eff}$ , and luminosity are a mixture of retrieved values, and values extrapolated from the forward model in post-processing. The mass and radius are retrieved directly in the PYMULTINEST version of BREWSTER, having been previously inferred from log g and distance scaling in the EMCEE version. The luminosity is found by extrapolating the forward model for the retrieved parameters across a wide wavelength range from 0.5 to 20  $\mu$ m, encapsulating essentially all the flux from the target. The  $T_{\rm eff}$  is then found using the extrapolated  $L_{\rm bol}$ , and the retrieved radius.

Our extrapolated luminosity for Ross 458c is  $-5.27 \pm 0.03$ , which is much higher than the value of  $\log(L_{bol}/L_{\odot}) = -5.61 \pm 0.03$  that was found in Burningham et al. (2011). This is may be due to missing absorption from CO and/or CO<sub>2</sub>, which occur in the 4–5 µm region, but which are unconstrained in our model, since it is based on the NIR only.

Fig. 6 shows that our extrapolated spectrum is a good match to the *Spitzer* Channels 1 and 2 photometry, which are driven by well-characterized CH<sub>4</sub> absorption. The Wide-field Infrared Survey Explorer (WISE) *W1*-band photometry also matches our model flux reasonably well. However, our extrapolated model is much brighter than the WISE *W2* photometry. This filter coincides more strongly with the 4.6  $\mu$ m CO absorption, and this supports our assertion that this is the origin of the mismatch between our extrapolated luminosity and that measured previously by Burningham et al. (2011). We also note that our extrapolated spectrum shows a strong CO<sub>2</sub> absorption starting at 4.3  $\mu$ m, which is extrapolated from our NIR spectrum where its abundance is unconstrained. This is likely spurious and does not warrant further interpretation.

It is also plausible that our poorly constrained temperatures at shallower pressures are also impacting the flux at longer wavelengths. Our inferred  $T_{\rm eff}$  that is based on this suspect luminosity should be similarly treated with caution.

We do not think that photometric or astrometric uncertainties have a significant effect on our extrapolated luminosity. The astrometric uncertainties are marginalized over in the retrieval model, and so are already incorporated into the radius uncertainty. We have not marginalized over the photometric uncertainty contribution to the flux calibration. However, the photometric uncertainty is at the 1 per cent level and thus smaller than our 3 per cent uncertainty in luminosity.



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Figure 4. Median retrieved gas fractions compared to equilibrium predictions for [M/H] = 0.2, which matches Ross 458AB (Burgasser et al. 2010). The assumed C/O = 1.35 is the highest available in the thermochemical grid. The solid red lines are the retrieved gas fractions, and the shaded areas the 16th and 84th percentiles, and the dashed lines are the equilibrium predictions.

Fig. 4 also shows the values for mass and radius, of  $27 \pm 4 M_{Jup}$  and  $1.45 \pm 0.06 R_{Jup}$ , respectively. The mass and radius are retrieved directly. However, the value for the retrieved radius is driven by the retrieved model scaling factor ( $R^2/D^2$ ) and the *Gaia* parallax. The retrieved mass value is driven by the influence it has on log g and the retrieved radius.

Burgasser et al. (2010) estimate a lower age limit for Ross 458 system of 150 Myr based on the absence of spectroscopic features suggestive of low surface gravity that are seen in young M dwarfs up to the age of the Pleiades. However, this system has a metallicity of [M/H] = +0.2 (and possibly higher), which is higher than the

Pleiades (Soderblom et al. 2009), and thus may not follow the same trend in spectroscopic features. Burgasser et al. (2010) find the absence of Li I absorption at 6708 Å suggesting a more robust lower age limit of 30–50 Myr, which is consistent with the age of the IC 2391 Moving Group, as found by Nakajima et al. (2010).

Fig. 7 shows the radius as a function of age, with two lower limits for the age of 50 and 150 Myr highlighted in Burgasser et al. (2010). Our retrieved radius of  $R = 1.45 \text{ R}_{\text{Jup}}$  coincides with the evolutionary model predictions for [M/H] = +0.5 and an age near lower of the two limits. The retrieved mass and gravity are similarly consistent with this lower age limit.



**Figure 5.** Nested sampling corner plot of highest ranked model, the powerlaw slab cloud, showing posterior probability distributions in 1D histograms with confidence interval. The 2D histogram shows the correlation between the parameters. The corner plot showing the retrieved gas abundances, radius, and mass and extrapolated parameters, log *g*,  $T_{\rm eff}$ ,  $L_{\rm bol}$ , C/O, [C/H], and [O/H]. See explanation for extrapolated parameters. The gas abundances are shown as  $\log_{10}(X)$ , where *X* is the gas fraction. [C/H] and [O/H] are relative to solar.

However, if the older age limit of 150 Myr is applied, then both the mass and radius are larger than expected from these models. None the less, they result in a value for log *g* that is consistent with previous estimates, for which values are seen in Table 2. We note, also, that the EMCEE-based retrievals (see Appendix A) find a value for log  $g = 5.13^{+0.20}_{-0.37}$ , which is somewhat higher. Although its large error, particularly towards lower values means that it is also consistent with previous estimates.

# 5.2 C/O ratio

The C/O ratio can be calculated using the CH<sub>4</sub> to H<sub>2</sub>O ratio, as CO and CO<sub>2</sub> are undetected in the NIR. This method for calculating the C/O ratio from methane and water is also used in Line et al. (2015, 2017) and Gonzales et al. (2020) (the latter with the addition of CO for the L dwarf). If we naively apply this here, we arrive at an improbably high value of  $1.97^{+0.13}_{-0.14}$ . This is likely to be outside the scope of any stellar C/O ratio, for which C/O > 1 is rarely seen. Generally, the distribution of stellar C/O is tight, with a peak near the solar value (Nissen 2013; Nakajima & Sorahana 2016; Brewer & Fischer 2017).



**Figure 6.** Extrapolated retrieval spectrum of Ross 458c, with the photometry points from WISE 1 and 2, and *Spitzer* 1 and 2 added, as well as transmission regions of the filters, and the 700 K, log g = 4.5 Sonora model.

This section investigates several possibilities to assess their impact on the C/O ratio. We first consider observational and analytical sources of bias, before considering atmospheric origins.

#### 5.2.1 Observational and model biases

Telluric water bands are common in the infrared and originate from water absorption in the Earth's atmosphere, which may bias our C/O ratio. We performed a test to check if removing telluric water bands alters our estimate for the H<sub>2</sub>O abundance and hence the C/O ratio. This was done by removing all data points in the 1.35–1.42 and the 1.80–1.95  $\mu$ m ranges, where telluric water features are present, and running the nested sampling winning model (power-law slab cloud) with the bands removed. Removing the telluric absorption bands did not change the retrieved water abundance significantly, and the CH<sub>4</sub>/H<sub>2</sub>O remained high at 1.88.

As listed in Tables 8 and 7, the C/O was consistently high across all cloud models tested and sampling methods tested.

#### 5.2.2 Oxygen depletion by condensation

Examination of our [C/H] and [O/H] values can reveal whether the atmosphere is carbon rich or oxygen poor. The primary stars, Ross 458A and B, are known to have supersolar metallicities of [Fe/H] = +0.2 (Burgasser et al. 2010), which agree with the retrieved [C/H] = +0.18 of Ross 458c, meaning that the carbon abundance is consistent with the primary. However, Ross 458c's [O/H] =  $-0.37 \pm 0.05$ , suggesting that it is oxygen poor or otherwise depleted.

A certain amount of oxygen can be tied up via silicate condensation and would be 'missing' from the atmosphere. However, under typical assumptions for T dwarf atmospheres this would not account for all of the missing oxygen. By allowing 25 per cent of oxygen to be tied up in silicate clouds (Burrows & Sharp 1999), the C/O ratio would lower to 1.47, which is still extremely high.

Water clouds in the atmosphere of Ross 458c would account for the missing water and lower the C/O ratio substantially, but the temperature is too high for water clouds. Water clouds are expected to become a significant opacity source in brown dwarfs of temperatures less than 400 K (Morley et al. 2014).



Figure 7. Sonora Bobcat evolutionary models (Marley et al. 2021) of radius against age. The vertical lines and shaded pink area are lower age estimates of Ross 458c. The retrieved radius with shaded errors is shown at  $R = 1.45 \text{ R}_{Jup}$ . The radius is shown for two different metallicities, of solar and [M/H] = +0.5, and the masses chosen are in the range of our retrieved mass.

#### 5.2.3 Non-equilibrium chemistry

The value of the  $CH_4/H_2O$  ratio is likely impacted by non-equilibrium chemistry, which will lead to more oxygen being tied up in CO and  $CO_2$  than would otherwise be expected at the low temperatures of late-T dwarfs. Previous work has highlighted the importance of non-equilibrium chemistry, leading to higher CO and  $CO_2$  abundances.

In the cooler T dwarfs, convection drives the disequilibrium chemistry. Miles et al. (2020) find that disequilibrium chemistry plays an important role in directly imaged exoplanets and brown dwarfs, leading to important CO absorption in the spectra.

Noll et al. (1997) found that for Gliese 229B, CO was also present at larger abundances than expected, such as in the 4.7  $\mu$ m band, as a disequilibrium species high up in the atmosphere, suggesting transport-induced quenching.

CO is favoured as the dominant C-bearing gas at high temperatures (deep in the atmosphere), whereas  $CH_4$  is favoured as the dominant C-bearing gas at low temperatures (higher altitudes; Lodders & Fegley 2002; Visscher 2012). Through atmospheric mixing, the chemical composition can be driven out of equilibrium. Rapid vertical mixing can transport a gas to higher altitude (and lower temperatures) before the chemical constituents have had time to reach chemical equilibrium. If the mixing time is faster than the chemical reaction time, disequilibrium can occur.

At the quench point (where the chemical time-scale = mixing timescale) the abundance of the species is 'quenched' at a fixed value as it is mixed to higher altitudes.  $CO + CO_2$  are subject to transportinduced quenching, which may lead to a quenched abundance in the upper atmosphere far in excess of that predicted by equilibrium, if undergoing rapid vertical mixing (Visscher et al. 2010).

Fig. 5 shows a good match with thermochemical predictions at high pressure and temperature ( $T \approx 2000$  K). This suggests that the observed CH<sub>4</sub>/H<sub>2</sub>O ratio can be consistent with C/O = 1.35 (the maximum modelled value in our thermochemical grid), if carbon–



**Figure 8.** The impact on the implied C/O ratio of incorporating CO and CO<sub>2</sub> that may have been missed by our NIR spectrum. The base case indicated by the point with error bars at the top left of the plot is where we estimate C/O assuming that all carbon and oxygen (after depletion by condensing clouds) exist in the H<sub>2</sub>O and CH<sub>4</sub> that we have measured. The lines indicate how the C/O changes as we allow for increasing quantities of CO and CO<sub>2</sub> at the proportions indicated and tracked by the corresponding increase in [C/H]. The top dashed line indicates C/O = 0.8, the upper range seen in solar-type stars, and the Asplund et al. (2009) solar value is indicated by the lower line.

oxygen chemistry is quenched at the 100 bar, 2000 K level. However, at 2000 K the chemical reactions converting CO/CH<sub>4</sub> will be fast, suggesting that it is unlikely that the observed abundances can be attributed to quench chemistry alone (Visscher & Moses 2011).

We have simulated how the estimated C/O ratio can be affected by incorporating CO and CO<sub>2</sub> that might have been missed by our NIR spectroscopy. In Fig. 8, we show how the C/O ratio decreases as more CO and CO<sub>2</sub> are incorporated, as indicated via the associated increase in the [C/H] metallicity. The plot is based on our condensationcorrected C/O = 1.47, based on CH<sub>4</sub>/H<sub>2</sub>O alone, which corresponds to [C/H] = +0.18 (see Fig. 4). As expected, adding CO drags the C/O ratio closer to 1. However, a substantial (0.5) fraction of CO<sub>2</sub> is required to bring the C/O ratio to within the typical stellar range (i.e.  $\leq \sim 0.8$ ; see Section 5.2.4).

As discussed in Burningham et al. (2011), there are disagreements as to the full network of CO–CO<sub>2</sub>–CH<sub>4</sub> reactions, and where their equilibria lie. However, even the most pro-CO<sub>2</sub> cases in the BT Settl model grids discussed in that paper have CO outnumbering CO<sub>2</sub> by a factor of 20, which is the most CO<sub>2</sub> *poor* case illustrated in Fig. 8.

In addition to the high abundance of  $CO_2$  required to bring the implied C/O ratio towards the expected stellar range, it is also clear that the implied [C/H] must rise significantly also. In all cases, allowing for enough CO and  $CO_2$  to bring C/O below 1.0 implies [C/H] > +0.5, which is significantly higher than suggested by the metallicity of the primary stars in the system and beyond the range of carbon abundances or metallicities seen in the solar neighbourhood (e.g. Nissen 2013; Hinkel et al. 2014).

In the absence of spectroscopy covering the missing CO and CO<sub>2</sub> absorption, we argue that the estimate of the C/O ratio made via comparison of our retrieved abundances with our thermochemical model grids (Fig. 5) is the most reasonable, i.e. C/O  $\approx$  1.35. We note that this value implicitly includes the impact of rainout of oxygen in condensates according to phase-equilibrium chemistry at solar abundance ratios.

# 5.2.4 C/O of primary system

The C/O ratio of the primary system, Ross 458AB, is unknown, and it may not share the solar value of 0.54 (Asplund et al. 2005). However, the range of stellar C/O ratios for solar-type stars is relatively narrow, with C/O > 0.8 very rare. As the primaries are not carbon stars, a C/O > 0.8 would be highly unlikely. The peak of the distribution is around 0.47, with a tail towards lower and higher C/O ratios (Nissen 2013; Brewer & Fischer 2017). This makes the high implied value for Ross 458c particularly interesting.

# 5.3 Interpretation of C/O ratio

Taking the above considerations into account, the fact that the C/O ratio appears to be so different from its primaries may suggest a planetary formation route for Ross 458c. This formation would have to be such that it is not enriched with oxygen. Ross 458c has not necessarily formed *in situ* but could have migrated to its current position. The protoplanetary disc would have different compositions at different radii, at the various ice lines. In order for the atmosphere to be oxygen poor, the formation must have taken place outside of the H<sub>2</sub>O snow line, with a process that inhibits accretion of oxygenbearing silicates and allows for more carbon-rich gas to accrete. The suggestion of a planetary formation route for Ross 458c seems unlikely due to its mass ratio with the primaries and our own large retrieved mass (driven up by the large retrieved radius).

This oxygen depletion that we are seeing is also noted in other retrievals, such as Calamari et al. (2022), who find a supersolar C/O ratio for Gliese 229B. They compare their work to other works done on T dwarf, which likewise see the trend of supersolar C/O (Line et al. 2017; Zalesky et al. 2019, 2022). They speculate that unanticipated chemistry may provide additional oxygen sinks, such as unmodelled magnesium silicates and/or iron-bearing condensates, which could drive an apparently supersolar C/O.

# 6 CONCLUSION

In this work, we have presented the first retrieval of Ross 458c. Ross 458c is best parametrized by a non-grey (power-law) cloud, structured as a slab. Both the radius and the mass are overestimated, based on evolutionary models. The bolometric luminosity is higher than found in Burningham et al. (2011).

The  $CH_4/H_2O$  ratio is much higher than expected, at 1.97. This is due to missing oxygen from a low water abundance. Comparisons to thermochemical grid models suggest a still high C/O ratio of 1.35, if  $CH_4$  and  $H_2O$  are quenched at 2000 K due to vigorous mixing.

The [C/H] = +0.18 matches up with the metallicity of Ross 458AB of [Fe/H] = +0.2 (Burgasser et al. 2010).

Even with oxygen sequestered into clouds and accounting for transport-induced quenching, the C/O ratio remains high. This points to either a planetary origin of Ross 458c or the presence of an unidentified sink for the gas-phase oxygen.

These retrieval results are the first in an analysis of a larger sample of late-T dwarfs that seek to answer the following questions: Do companion T dwarfs have a different composition than their host star? Is the C/O ratio of free-floating T dwarfs different to that of the stellar population and to that of companion T dwarfs? What trends in C/O ratio are present across the T dwarf range?

# 6.1 Future work

In order to compare the C/O ratios of companions to their primary star(s), we need the abundances of the primary. This could be done following the method of Tsuji & Nakajima (2014, 2016), which uses high-resolution spectra of  $H_2O$  and CO in the NIR bands.

Additionally, by extending the spectrum of Ross 458c to 5  $\mu$ m, we would include CO and CO<sub>2</sub> absorption that might be a significant contributor to carbon and oxygen abundances, altering the C/O ratio. No spectroscopic data at those wavelengths exist yet. The data for Ross 458c that will be obtained through *JWST* at NIR and mid-IR wavelengths and at greater sensitivity will aid our understanding of absorbers in the atmosphere, such as CO and CO<sub>2</sub>, and the thermal profile over wider range of pressures.

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# DATA AVAILABILITY

All data underlying this article are publicly available from the relevant observatory archive or upon reasonable request to the author.

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# APPENDIX A: COMPARISON OF EMCEE AND PYMULTINEST RESULTS

Table A1 shows the comparison of retrieved parameters between the EMCEE and the PYMULTINEST samplers. The values are consistent with each other to 1  $\sigma$  for the most part, with a couple of exceptions that differ by under 2  $\sigma$ .

Fig. A1 shows the comparison of the thermal profiles of the EMCEE and PYMULTINEST samplers for the power-law slab cloud.

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They follow similar profiles, with the EMCEE profile being slightly warmer at deeper pressures.

The location of the EMCEE cloud is unconstrained within the atmosphere at the top of the cloud.

Table A2 shows the comparison of  $CH_4/H_2O$  for the different models tested, for both the PYMULTINEST and the EMCEE samplers. The  $CH_4/H_2O$  stays consistently high across all models, for both sampling methods.

The two highest ranking models are the same for both samplers, just with the order switched. See Tables 7 and 8 for model rankings for both samplers.

**Table A1.** Comparison of parameters between EMCEE and PYMULTINEST for the power-law slab cloud (the winning model from PYMULTINEST, and the second-ranked model from EMCEE), in order to allow for a more direct comparison.

Parameter	EMCEE	PYMULTINEST
H <sub>2</sub> O	$-3.00^{+0.16}_{-0.24}$	$-3.47^{+0.04}_{-0.04}$
CH <sub>4</sub>	$-2.76_{-0.30}^{+0.14}$	$-3.16_{-0.04}^{+0.04}$
СО	$-7.81^{+2.73}_{-2.83}$	$-8.28^{+2.42}_{-2.16}$
CO <sub>2</sub>	$-7.36^{+3.07}_{-3.87}$	$-8.00^{+2.65}_{-2.28}$
NH <sub>3</sub>	$-4.38^{+0.20}_{-2.01}$	$-4.62\substack{+0.04\\-0.04}$
$H_2S$	$-8.82^{+2.63}_{-2.11}$	$-8.54_{1.90}^{1.81}$
Na + K	$-6.12_{-1.31}^{+0.37}$	$-5.80\substack{+0.04\\-0.05}$
log g	$5.13^{+0.20}_{-0.37}$	$4.50\substack{+0.07 \\ -0.07}$



Figure A1. Comparison of the thermal profiles with their errors, for the power-law slab cloud of the EMCEE (in blue) and PYMULTINEST (in black) samplers with the cloud condensation curves overplotted. Also, plotted are the cloud locations in the bars on the rights (cloud N being PYMULTINEST sampler and cloud E being the EMCEE sampler), with their associated errors in grey.

Model type	CH <sub>4</sub> /H <sub>2</sub> O pymultinest	$CH_4/H_2O$ emcee
Power-law slab cloud	$1.97^{+0.13}_{-0.14}$	$1.69^{+0.31}_{-0.51}$
Power-law slab cloud, Allard alkalis	$2.13_{-0.15}^{+0.14}$	$1.82^{+0.31}_{-0.46}$
MgSiO <sub>3</sub> slab cloud	$1.86_{-0.18}^{+0.19}$	$1.42_{-0.42}^{+0.37}$
Na <sub>2</sub> S slab cloud	$1.82_{-0.19}^{+0.20}$	$1.83_{-0.23}^{+0.19}$
Cloud free	$1.74_{-0.19}^{+0.20}$	$1.83^{+0.19}_{-0.23}$
Grey deck cloud	$1.68^{+0.20}_{-0.20}$	$1.57_{-0.57}^{+0.32}$
KCl deck cloud	$1.79_{-0.18}^{+0.17}$	$1.71_{-0.31}^{+0.27}$
MgSiO <sub>3</sub> deck cloud	$1.76_{-0.18}^{+0.19}$	$1.71_{-1.06}^{+0.41}$
Power-law deck cloud	$1.70_{-0.21}^{+0.20}$	$1.61_{-0.80}^{+0.36}$
Soot deck cloud	$1.32_{-0.23}^{+0.28}$	$1.52_{-0.23}^{+0.26}$
KCl slab cloud	$1.73_{-0.17}^{+0.18}$	$1.28^{+0.32}_{-0.21}$
Grey slab cloud	$1.63^{+0.17}_{-0.16}$	$1.67^{+0.28}_{-0.56}$
MnS slab cloud	$1.71^{+0.17}_{-0.17}$	$1.71_{-0.29}^{+0.24}$
MnS deck cloud	$1.75^{+0.19}_{-0.21}$	$1.66^{+0.32}_{-0.64}$
Soot slab cloud	$1.45_{-0.37}^{+0.23}$	$1.79_{-0.24}^{+0.22}$

Table A2. Comparison of the  $\rm CH_4/\rm H_2O$  ratio between <code>PYMULTINEST</code> and <code>EMCEE</code>, for the different models tested.

This paper has been typeset from a  $T_{\ensuremath{E}} X/I \!\! \ensuremath{\Delta} T_{\ensuremath{E}} X$  file prepared by the author.