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A 21-cm power spectrum at 48 MHz, using the Owens Valley Long Wavelength Array

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ABSTRACT

The Large-aperture Experiment to detect the Dark Age (LEDA) was designed to measure the 21-cm signal from neutral hydrogen at Cosmic Dawn, $z \approx 15$ –30. Using observations made with the ≈ 200 m diameter core of the Owens Valley Radio Observatory Long Wavelength Array (OVRO–LWA), we present a 2D cylindrical spatial power spectrum for data at 43.1–53.5 MHz ($z_{\text{median}} \approx 28$) incoherently integrated for 4 h, and an analysis of the array sensitivity. Power from foregrounds is localized to a 'wedge' within k_{\perp} , k_{\parallel} space. After calibration of visibilities using five bright compact sources including Vir A, we measure $\Delta^2(k) \approx 2 \times 10^{12}$ mK² outside the foreground wedge, where an uncontaminated cosmological signal would lie, in principle. The measured $\Delta^2(k)$ is an upper limit that reflects a combination of thermal instrumental and sky noise, and unmodelled systematics that scatter power from the wedge, as will be discussed. By differencing calibrated visibilities for close pairs of frequency channels, we suppress foreground sky structure and systematics, extract thermal noise, and use a mix of coherent and incoherent integration to simulate a noise-dominated power spectrum for a 3000 h observation and z = 16-37. For suitable calibration quality, the resulting noise level, $\Delta^2(k) \approx 100$ mK² (k = 0.3 Mpc⁻¹), would be sufficient to detect peaks in the 21-cm spatial power spectrum due to early Ly- α and X-ray sources, as predicted for a range of theoretical model parameters.

Key words: techniques: interferometric - cosmology: observations - dark ages, reionization, first stars - software: simulations.

1 INTRODUCTION

Observations of Cosmic Dawn and the epoch of reionization (EoR) are key to unveiling properties of the first population of stars and galaxies. The role of first galaxies in the process of reionization can be probed by the measurements of Gunn–Peterson troughs in the spectra of high-redshift quasars (e.g. Fan et al. 2006; Greig et al. 2017; Greig, Mesinger & Bañados 2019), Ly- α emission from Lyman Break galaxies (Mason et al. 2018), and the measurement of the total optical depth to Thomson scattering of the cosmic microwave background (CMB) radiation (e.g. Planck Collaboration VI 2018). The emergent picture shows growing evidence of late-reionization ending at $z \approx 6$ (e.g. Weinberger, Haehnelt & Kulkarni 2019). However, these measurements cannot reveal much about other processes that occur at early times, such as the heating of the intergalactic medium (IGM)

by the first X-ray sources or the onset of primordial star formation in proto-galaxies.

These processes can be constrained via observations of the redshifted 21-cm line of neutral hydrogen produced at a rest-frame frequency of 1.42 GHz (e.g. Furlanetto, Oh & Briggs 2006; Barkana 2016), which can be observed using low-frequency radio telescopes today. In addition to being sensitive to the process of reionization, the 21-cm signal depends on the temperature of the IGM (e.g. Madau, Meiksin & Rees 1997), Ly- α radiation from stars (Wouthuysen 1952; Field 1958), and the intensity of the radio background at 21 cm (e.g. Feng & Holder 2018). Therefore, this signal can be used to constrain the process of primordial star and galaxy formation (e.g. probe the effect of radiative feedback mechanisms at high redshifts, Fialkov et al. 2013) and probe both thermal and ionization histories of the gas.

The sky-averaged (global) 21-cm signal traces the mean evolution of the Universe and can act as a cosmic clock, revealing the timing of major cosmic events such as the onset of star formation. The

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first tentative detection of the global 21-cm signal at 78 MHz (corresponding to a redshift of $z \approx 17$) was recently reported by the EDGES collaboration (Bowman et al. 2018). This detection is not compatible with theoretical predictions based on standard astrophysical and cosmological assumptions (e.g. Cohen et al. 2017, explored a large grid of 21-cm global signals, broadly varying properties of astrophysical sources within acceptable ranges), calling for alternative theories at Cosmic Dawn. The proposed solutions range from models with over-cooling of gas via dark matter interactions (see Barkana 2018, and the citation history of that work) to the existence of extra radio background radiation in addition to the CMB (e.g. Bowman et al. 2018; Feng & Holder 2018), which is usually assumed to be the only source of background radiation. Moreover, doubts about the signal being of cosmological origin have been expressed, with possible explanations including instrumental systematic errors (Hills et al. 2018; Sims & Pober 2019; Singh & Subrahmanyan 2019), ground plane interference (Bradley et al. 2019), and polarized foregrounds (Spinelli, Bernardi & Santos 2019). Other existing global 21-cm experiments are attempting to verify this detection at high redshifts, including the Large-aperture Experiment to detect the Dark Age (LEDA) (Bernardi et al. 2016; Price et al. 2018), and efforts in progress with experiments such as SARAS3, REACH,¹ EDGES Mid-Band, and MIST.² At lower redshifts, only upper limits on the global 21-cm signal have been published so far (Monsalve et al. 2017; Singh et al. 2017).

Power spectra of 21-cm fluctuations contain information on the initial fluctuations in density and velocity fields, spatial distribution of sources, and their spectral properties. Power spectrum measurements can provide an important validation of the EDGES signal and aid in its theoretical interpretation (Fialkov, Barkana & Cohen 2018; Reis, Fialkov & Barkana 2020). If the EDGES signal is imprinted by astrophysical or cosmological processes at Cosmic Dawn, power spectra from $z \approx 17$ could carry a consistent signature. So far, major experimental effort has been focused on observing the EoR, with several instruments yielding upper limits in the range z $\approx 6 - 9$, including LOFAR (Mertens et al. 2020), MWA (Barry et al. 2019; Li et al. 2019; Trott et al. 2020), PAPER (Kolopanis et al. 2019), and GMRT (Paciga et al. 2013). At the higher redshifts corresponding to Cosmic Dawn, first attempts to measure the power spectrum have been made by Ewall-Wice et al. (2016), who, using 6 h of data from the MWA, reported a sensitivity of 10⁸ mK² on comoving scales $k \leq 0.5$ h Mpc⁻¹ at redshifts $11.6 \leq z \leq 17.9$ (a few orders of magnitude above the expected 21-cm power spectrum). Eastwood et al. (2019) used 28 h collected by the Owens Valley Radio Observatory Long Wavelength Array (OVRO-LWA, Hallinan et al. 2015) and found an upper limit of 10^8 mK^2 at $k \leq 0.10 \text{ Mpc}^{-1}$ at z = 18.4. The AARTFAAC Cosmic Explorer program (Gehlot et al. 2020), using the LOFAR telescope, reported an upper limit of $7.3 \times 10^7 \,\mathrm{mK^2}$ at $k = 0.144 \,\mathrm{h \, cMpc^{-1}}$, z = 17.9 - 18.6, from 2 h of observations. Finally, 14 h collected by LOFAR-LBA were used to obtain upper limits of $2.1 \times 10^8 \text{ mK}^2$ and $2.2 \times 10^8 \text{ mK}^2$ at k $\approx 0.038 \text{ h Mpc}^{-1}$ for two observed fields (3C 220 and NCP) at z =19.8-25.2 (Gehlot et al. 2019). Next-generation experiments such as HERA (DeBoer et al. 2017) and the SKA (Koopmans et al. 2015) are designed to detect the 21-cm power spectrum from a wide range of redshifts and scales, including both the EoR and the Cosmic Dawn.

This paper reports results from the LEDA. The LEDA is working towards a detection of 21-cm fluctuations in the CMB signal at Cosmic Dawn ($z \approx 15-30$), in both global (sky-averaged) spectra and spatial power spectra, using observations from OVRO–LWA. We are currently focused on two experiments: (1) validation of the recent detection by Bowman et al. (2018), and extraction of any other 21-cm absorption/emission profiles observed at Cosmic Dawn; and (2) generation and analysis of power spectra of the 21-cm signal at Cosmic Dawn, and analysis of the sensitivity of power spectra as a function of observation integration time.

A paper reporting on progress on the first experiment is under review (Spinelli et al. 2020); this paper reports results from the second experiment.

The first power spectrum obtained from OVRO-LWA observations (Eastwood et al. 2019, mentioned above) was an angular power spectrum generated from 28h of integrated data using m-mode analysis (Shaw et al. 2014) and filtering of foregrounds using the double Karhunen–Loéve transform. In this paper, we also use observations from OVRO-LWA but generate power spectra using the 'delay spectrum' method (Parsons et al. 2012b), which produces a 2D cylindrical power spectrum. Instead of removing foregrounds, the delay spectrum method isolates foreground power in a 'wedge' region of the power spectrum, outside of which the 21-cm signal may be detected, given enough power spectrum sensitivity. Foreground isolation is inherent in the delay spectrum method and relies on the spectral smoothness of foreground emission. The method also has the advantage that it involves minimal manipulation of telescope data and is easy to implement. It does, however, have limitations, which we will discuss below. We operate at a higher redshift of $z \approx 28$, compared to Eastwood et al. (2019), producing a power spectrum at a redshift higher than any other reported to date. On the other hand, we use a smaller number of integrated observations than Eastwood et al. (2019), namely 4 h.

We will show that the sensitivity of our power spectrum is low compared to other reported experiments, but that this can be improved by integrating a larger number of observations and varying the method of integration. If some or all observations are coherently integrated before power spectrum generation, the noise in the power spectrum is substantially reduced. However, the timing of observations is crucial for coherent integration, since observations must be nearly identical, apart from noise. We report the results of simulations and analysis showing that 21-cm Cosmic Dawn fluctuations can be detected using OVRO–LWA observations that are combined using a mix of coherent and incoherent integration, and if the observations and power spectrum are free of any systematics. The number of observations required to detect 21-cm fluctuations is large, i.e. 3000 h in total, but it can be obtained within a reasonable time frame using a scheme that we will describe.

The paper is organized as follows: Section 2 describes the OVRO– LWA and data processing; Section 3 describes the observations used for power spectrum generation, and how they were selected; Section 4 presents the delay spectrum method; Section 5 shows the power spectra generated from observations and discusses their characteristics; Section 6 describes simulations of noise in power spectra, introduces coherent integration, and reports analysis of the sensitivity of OVRO–LWA; Section 7 compares that sensitivity against theoretical models of Cosmic Dawn and demonstrates that OVRO–LWA, and thus compact interferometers, could be used to study Cosmic Dawn; and Section 8 summarizes the results and future work.

For this work, we assume a flat universe with the following cosmological parameter values: $\Omega_{\rm M} = 0.31$, $\Omega_{\Lambda} = 0.69$, $H_0 = 0.68$.

¹https://www.astro.phy.cam.ac.uk/research/research-projects/reach ²http://www.physics.mcgill.ca/mist/



Figure 1. *uv* coverage of the OVRO–LWA baselines used for power spectrum generation, obtained from a frequency channel of width 24 kHz at a frequency of 57 MHz.

2 THE OVRO-LWA TELESCOPE AND PROCESSING PIPELINE

OVRO-LWA is a wide-field, low-frequency, drift-scan, nonredundant, imaging interferometer situated in Owens Valley, California, at a latitude of 37.2398° and a longitude of -118.2817° . Its design and hardware components are based on that of the Long Wavelength Array (LWA) in New Mexico (Taylor et al. 2012). OVRO-LWA provides data for research in several areas of observational astronomy and cosmology, including cosmic rays (Carvalho et al. 2019; Romero-Wolf et al. 2019; Monroe et al. 2020), radio transients surveys (Anderson et al. 2019a), solar weather and coronal mass ejections (Hallinan & Anderson 2017; Chhabra et al. 2019), exoplanet searches (Anderson & Hallinan 2017), radio counterparts to gamma-ray bursts and gravitational waves (Anderson et al. 2018; Anderson, Callister & Hallinan 2019b), emission from compact binaries (Callister, Anderson & Hallinan 2019), properties of the ionosphere (Shume et al. 2017), sky surveys at low frequencies (Eastwood & Hallinan 2018), Cosmic Dawn 21-cm global signal detection (Price et al. 2018), and Cosmic Dawn 21-cm power spectra (Eastwood et al. 2019).

The telescope consists of 256 dual-antenna stands of the same type used in the LWA (Taylor et al. 2012); only the OVRO–LWA core, consisting of 219 stands, was used for experiments reported here. The 219 stands provide 23 871 baselines, with lengths from 4.8 to 212.4 m. The observing bandwidth is 27.384–84.912 MHz (z = 15.7–50.9 for the 21-cm HI line). The *uv*-coverage of the OVRO–LWA core at 57 MHz is shown in Fig. 1; *uv* lengths range from 0.9 to 40.4 wavelengths. The resolution of the telescope is 1.4° at 57 MHz.

Signals from the antennas are processed by an FX correlator on site at the Owens Valley Radio Observatory (Kocz et al. 2015). The observing band is split into 22 sub-bands each containing 109 channels of width 24 kHz, 2398 channels in all. Each stand has a folded cross-dipole for observing X (east–west) and Y (north–south) polarizations. Cross-correlation of antennas generates four polarizations are used for our power spectrum analysis, and they are treated separately.

Antenna signals are correlated, integrated, and saved as visibilities every 9 s, thus producing a single 'observation' every 9 s. Multiple observations are typically integrated for further processing, e.g. for generating power spectra. Observations are calibrated using the realtime system (RTS), which performs self-calibration against a point source sky model (Mitchell et al. 2008). The RTS uses a beam model described in LWA Memo 178.³ The RTS contains an algorithm to detect and flag narrow-band radio-frequency interference (RFI) in each sub-band by finding channels whose amplitude varies significantly from the median amplitude of the sub-band (Mitchell et al. 2010). No other automated flagging is applied; further flagging of data is achieved by a visual inspection of antenna autocorrelations. Post-calibration quality checks (described below) are used to select observations to be used for science experiments.

3 OBSERVATIONS USED FOR POWER SPECTRUM GENERATION

We use 4 h of non-contiguous (in time) observations, selected from all observations made during 2018 May, between LST 11:55 and 13:15. Of the 219 stands available for power spectrum observations, only 165 were deemed usable over the entire 4 h, the rest being flagged due to hardware issues and outages. We also flagged 509 baselines due to suspected cross-talk between their antenna cable connections at back-end electronic-processing units.⁴ During calibration, short baselines were downweighted so that any observed diffuse emission does not interfere with calibration by RTS, which lacks a diffuse emission model.

During observations, both the Sun and the Galactic Centre were below the horizon, and two strong sources, Cygnus A and Cassiopeia A, were on or below the horizon. The brightest source in the sky was Virgo A at an elevation of $\approx 63^{\circ}$. We used Virgo A and four other sources for calibration. These five sources were selected based on the following criteria: (1) at an LST of 12:30, they are above an elevation of 30°, and (2) at an LST of 12:30, they are determined by RTS to be the five brightest sources after primary beam correction. The LST of 12:30 in these criteria was chosen as it is the approximate middle of the LST range of 11:55–13:15. All observations were separately calibrated using the same five sources. The RTS was configured to use the VLA Low-Frequency Sky Survey at 74 MHz (Cohen et al. 2007) to determine source flux densities and locations; the sources are detailed in Table 1. To obtain flux density at frequencies other than 74 MHz, we assume a spectral index of -0.7 for all sources. It is possible that the spectrum of these sources turns over at lower frequencies, but only ≈ 4.5 per cent of sources in the GLEAM catalogue do so (Callingham et al. 2017) and Virgo A does not (de Gasperin et al. 2012), so we do not attempt to correct for this.

A simple method was used to select the 4 h of observations used for power spectrum generation, based on the quality of the observations and their suitability for use in power spectra. The method is described in Appendix A. This produced a set of observations that are not necessarily contiguous in time, and recorded on different days. Fig. 2 shows Stokes I images of the sky generated from one observation at LST = 12:30. The sky is the same in both images, but the right image marks the calibration sources in green, and other sources of interest in red and yellow (see caption). The images were obtained using NRAO CASA software.⁵

³http://www.phys.unm.edu/ lwa/memos/memo/lwa0178a.pdf
 ⁴M. Eastwood, personal communication.
 ⁵https://casa.nrao.edu

Table 1. Details of the five sources used for calibration of the OVRO–LWA observations used for power spectrum generation. Locations and flux densities were obtained from the VLA Low-Frequency Sky Survey at 74 MHz, and flux densities converted by RTS to OVRO–LWA frequencies by assuming a spectral index of -0.7. The flux densities at 74 MHz and 48.324 MHz are shown.

Source	Location (RA/DEC)	Flux density at 74 MHz (Jy)	Flux density at 48.324 MHz (Jy)
Virgo A	12:30:49	1253.4	1689.03
1411 + 5212	+ 12:23:28 14:11:20	120.27	162.07
1229 + 0202	+ 52:12:04 12:29:06	149.96	202.08
1504 + 2600	+ 02:02:56 15:04:59	129.86	174.99
0813 + 4813	+ 26:00:46 08:13:36.34 + 48:13:01	136.40	183.80

For power spectra, we use a frequency band of 10.464 MHz centred at 48.324 MHz. That band was chosen because it is less subject to RFI and produces the highest signal-to-noise ratio over the OVRO–LWA band. It does not cover the EDGES detection frequency, but for our sensitivity analysis, using simulations, we will do so by expanding the frequency range to cover almost the entire OVRO–LWA band. Over the 10.464-MHz band, the 21-cm signal is observed at z =25–31. This corresponds to a time range of 35 million years, when the Universe was 100 Myr old. Power spectra of 21-cm fluctuations should ideally be obtained over a time range when the Universe is not significantly evolving, which is unlikely over z = 25-31, so a narrower frequency band is more appropriate. However, that will produce a power spectrum with a less resolution, and we prefer to maintain a higher resolution for analysis of our first power spectrum (see Pober et al. 2013 for a similar argument).

4 POWER SPECTRUM GENERATION

OVRO–LWA observes 21-cm fluctuations at redshifted 21-cm frequencies, as well as foregrounds emitting at the same frequencies; foreground signals are dominated by Galactic synchrotron and freefree emission and extragalactic sources. To separate the foregrounds from the 21-cm signal in power spectra, several methods have been used (Morales et al. 2019), which fall broadly into two categories: foreground removal and foreground isolation. Examples of the first are reported in Gehlot et al. (2019), Eastwood et al. (2019), and Barry et al. (2019); examples of the second are reported in Pober et al. (2013), Thyagarajan et al. (2015a), Paul et al. (2016), and Ewall-Wice et al. (2016). We implement foreground isolation by generating a 2D, cylindrically averaged, power spectrum using the delay spectrum method (Parsons et al. 2012b).

The delay spectrum method applies a Fourier transform to baseline visibilities, producing a delay spectrum:

$$\mathcal{V}_{\rm b}(\tau) = \int V_{\rm b}(\nu) e^{-2\pi\nu\tau} d\nu, \qquad (1)$$

where $V_b(v)$ are visibilities for a baseline (arrayed by frequency), and τ is the Fourier conjugate of v. τ represents the time delay of foreground signals between the two antennas of the baseline, and foregrounds signals are confined to values of τ less than the horizon delay, thus producing the 'wedge'. The baseline visibilities $V_b(v)$ measure the spatial Fourier transform perpendicular to the line of sight and can all be assigned a wavenumber k_{\perp} . Equation (1) also approximates the spatial Fourier transform of the 21-cm signal along the line of sight, with a wavenumber k_{\parallel} assigned to τ .

The delay spectra from multiple baselines are converted to power and binned by k_{\perp} , producing a 2D power spectrum indexed by $(k_{\perp}, k_{\parallel})$. Power is calculated using the equation

$$P(\mathbf{k}) \approx |\mathcal{V}|^2 \left(\frac{\lambda^2}{2k_{\rm B}}\right)^2 \frac{X^2 Y}{\Omega_{\rm pp} B_{\rm pp}}$$
 (2)

(Parsons et al. 2012a, 2014; Parsons 2017), where $P(\mathbf{k})$ is the power at $\mathbf{k} = (k_{\perp}, k_{\parallel}), \lambda$ is the mean wavelength of the band, $k_{\rm B}$ is Boltzmann's constant, $X^2 Y$ converts angles and frequency intervals to co-moving distance (Hogg 1999), $\Omega_{\rm pp}$ is the integral over the power-squared beam,⁶ and $B_{\rm pp}$ is the effective bandwidth. $B_{\rm pp} = \int |w|^2 dv$, where w is the window function applied to the delay transform. A window function is used to avoid spectral leakage produced by taking the Fourier transform of a finite length of non-periodic data; we use a Blackman–Harris window. We use a beam model of the LWA antenna dipole (Dowell 2011) to obtain $\Omega_{\rm pp}$. The units of $P(\mathbf{k})$ are mK²Mpc³. $P(\mathbf{k})$ is often converted to dimensionless power

$$\Delta^2(k) = \frac{k^3}{2\pi^2} P(\mathbf{k}),\tag{3}$$

where $k = \sqrt{k_{\perp}^2 + k_{\parallel}^2}$, and $\Delta^2(k)$ has units of mK². We will use both power values in this paper.

The delay spectrum method has limitations due to its approximation of the spatial Fourier transform along the line of sight. The delay spectrum method works best for narrow-beam, short-baseline, interferometers (Parsons et al. 2012b), whereas OVRO–LWA is a wide-field, long-baseline interferometer. Liu, Parsons & Trott (2014, equation 9) have determined that the delay spectrum method may be used for observations where

$$b\theta_0 \ll \frac{c}{B_{\text{band}}},$$
 (4)

where *b* is the length of a baseline, θ_0 is the width of the telescope primary beam (1.8 radians), and B_{band} is the bandwidth over which the observations are made. Interpreting ' \ll ' as 'one-half', equation (4) is violated by 99.66 per cent of the OVRO–LWA baselines used for our power spectrum generation, indicating that the baselines are too long and/or the bandwidth too wide. Reducing the maximum baseline length will reduce the k_{\perp} range; reducing the bandwidth will reduce the k_{\parallel} range. For the power spectra reported in this work, we ignore these restrictions, so as to obtain a power spectrum with an extent that allows for some analysis. We will deal with them in future work (see Section 8).

4.1 Additional processing steps

Before generating a delay spectrum from each baseline, flagged channels must be dealt with. Flagged channels represent missing values in the array $V_b(v)$ (Equation 1), which produce a delay spectrum convolved with a point spread function (PSF). This PSF may be deconvolved using a CLEAN algorithm (Högbom 1974). We use an implementation of CLEAN developed by the HERA Consortium⁷ for just this purpose. CLEAN is applied to the delay spectrum within the horizon, including a buffer of 95 ns outside the horizon; 95 ns being the resolution of τ in the delay spectrum of OVRO–LWA baselines (Table 2).

⁶Power-squared indicated by the double p subscript.

⁷pspec_prep.py, https://github.com/HERA-Team



Figure 2. An image of the sky generated from an OVRO–LWA observation used for power spectrum generation at LST = 12:30. The right image is the same as the left but is marked with sources of interest. The five brightest sources (after primary beam correction) at this LST were used for calibration. They are ringed in green and include Virgo A, the brightest source, which is at zenith. The 20 next brightest sources, after the five used for calibration, are ringed in yellow. The two sources on the horizon, ringed in red, are intermittent RFI sources; they are possibly located in the towns of Bishop or Mammoth Lakes, both north-west of OVRO–LWA at distances of 18 and 76 km, respectively. The source on the horizon at the top is Cassiopeia A; the source near the horizon at the bottom is unidentified. The images contain Stokes I observed over a bandwidth of 10.464 MHz centred at 48.324 MHz. They were generated using NRAO CASA with Briggs weighting applied (robust = 0.5). To enhance the visibility of the dimmer sources, an Arcsinh colour scale is used, and the image is clipped to a range of -90 to 300 Jy/beam. The image has not been CLEANed. The confusion limit for OVRO–LWA at this frequency, based on the longest baseline length of 200 m, is 96 Jy/beam.

 Table 2. Size, ranges, and resolution of the power spectrum images in the top row of Fig. 3.

Property	Value
Power spectrum dimensions (pixels)	102 horizontal, 108 vertical
k_{\perp} range	$0.001 - 0.018 \text{ Mpc}^{-1}$
k_{\perp} resolution	$0.000175 \text{ Mpc}^{-1}$
k_{\parallel} range	-1.06 to 1.04 Mpc ⁻¹
k_{\parallel} resolution	$0.02 \ {\rm Mpc}^{-1}$
Delay range	-5113.64 to 5018.94 ns
Delay resolution	95 ns
Horizon delay at max k_{\perp}	852 ns
<i>uv</i> lengths used	1–33

After CLEAN, the visibilities in $V_b(v)$ are averaged by groups of 4 to reduce noise. This reduces the frequency resolution by a factor of 4. The bandwidth of 10.464 MHz, which initially contains 436 channels of width 24 kHz, is thus transformed to 109 channels of width 96 kHz.

Instead of converting each baseline delay spectrum to power, we follow Pober et al. (2013) and multiply observing-time adjacent (i.e. LST adjacent) pairs of the same baseline to reduce noise. The LSTs of each multiplied pair must be within the time-smearing limits for OVRO–LWA (see Appendix B), since they are being coherently combined via the multiplication. Fortunately, after ordering all observations by LST, this applies to 99.9 per cent of the observations comprising the 4 h.

5 RESULTS

Fig. 3 shows the power spectrum generated from the 4 h of observations described in Section 3 for polarizations XX and YY. Baselines are binned, i.e. averaged, along the k_{\perp} axis, using a bin size of 0.000175 Mpc⁻¹, being the k_{\perp} of a baseline with u = 0.5 at the lowest observing frequency. There is no binning along the k_{\parallel} axis. The blue lines are the horizon delay, which increases with increasing k_{\perp} , producing the 'wedge' within which foreground emission is isolated. k_{\parallel} wavenumbers are approximated from the delays τ of the delay transform; these delays are plotted on the *y*-axis on the right. k_{\perp} values approximately correlate with baseline uv lengths, which are shown on the top *x*-axis.

The top row of Fig. 3 displays the power spectra using the complete range of k_{\parallel} values derived from the observing frequency band (10.464 MHz); the second row is the same power spectrum but restricts the k_{\parallel} range to ± 0.3 Mpc⁻¹ so that the wedge can be seen in more detail. A summary of the important properties of the power spectrum images in the top row of Fig. 3 is shown in Table 2. The third row of Fig. 3 shows the dimensionless power $\Delta^2(k)$ extracted from the Cosmic Dawn window at various values of *k* (the algorithm for extracting $\Delta^2(k)$ is described in Appendix C).

Fig. 4 shows vertical and horizontal cuts through the power spectra. The top row depicts vertical cuts at three k_{\perp} values of 0.005, 0.01, and 0.015 Mpc⁻¹. The location of the horizon at the different k_{\perp} values is shown by the black vertical lines. The bottom row of Fig. 4 depicts a horizontal cut through the power spectra at a constant $k_{\parallel} = 0.53$ Mpc⁻¹. These cuts show that the power drops by a factor of 10^4 mK²Mpc³ as k_{\parallel} moves away from 0, and that the power levels $P(\mathbf{k})$ and $\Delta^2(k)$ within the foreground wedge and Cosmic Dawn window are listed in Table 3.

5.1 Discussion

Fig. 3 demonstrates that wedge-type power spectra can be generated from OVRO–LWA observations. The power spectra show good isolation of foregrounds within the horizon, although there is some



Figure 3. The power spectra generated from the 4 h of observations described in the text and plots of $\Delta^2(k)$ obtained from the power spectra. The top row shows the power spectra, the second row shows the same power spectra but restricts the k_{\parallel} range to -0.31 to 0.31 Mpc⁻¹, so that the wedge can be seen in more detail. Power values are coloured using a log scale. The third row plots $\Delta^2(k)$ values at various *k*, obtained from within the Cosmic Dawn window of the power spectra (the exact region used is described in Appendix C). Some important properties of the power spectrum images in the top row are listed in Table 2. The left column shows the power spectrum generated from polarization XX and the right column from polarization YY.

spillover. Our power values are high compared to those reported by Eastwood et al. (2019), who obtained a value of $\Delta^2(k) \approx 10^8 \text{ mK}^2$ at $k = 0.1 \text{ Mpc}^{-1}$, compared to our value of $\Delta^2(k) \approx 10^{12} \text{ mK}^2$ at $k = 0.3 \text{ Mpc}^{-1}$. Other telescopes also report lower power; see Section 7. Note that other experiments were using different observing frequencies, total observing time, and telescopes. One reason for the higher power that we obtain is due to our lower observing frequency.

At a lower frequency, foreground emission is brighter (Spinelli et al. 2020), so that systematics and foreground leakage will raise the level of the power spectrum generally.

A visual inspection of the power spectra shows that horizon spillover can be separated into two distinct regions, based on the amplitude of the spillover and its extent beyond the horizon. The regions are depicted in Fig. 5. Both regions exist at all k_{\perp}



Figure 4. Vertical and horizontal cuts through the power spectra in the top row of Fig. 3. The top row panels contain three vertical cuts made at k_{\perp} values of 0.005, 0.01, and 0.15 Mpc⁻¹. The black lines indicate the location of the horizon at these k_{\perp} values. The bottom row shows a horizontal cut made at $k_{\parallel} = 0.53$ Mpc⁻¹. The left column is from power spectra generated from polarization XX and the right column from polarization YY.

Table 3. The top two rows show the average power in the power spectra generated from 4 h of observations (Fig. 3), from the foreground wedge (first row), and the Cosmic Dawn window (second row). The third row shows the ratio of the power in the foreground wedge to the power in the Cosmic Dawn window. The bottom row shows values of dimensionless power $\Delta^2(k = 0.3)$ obtained from the Cosmic Dawn window.

	Pol XX	Pol YY
Observed $P(\mathbf{k})$, foreground wedge	1.1×10^{18}	$1.7 imes 10^{18}$
Observed $P(\mathbf{k})$, Cosmic Dawn window	5.2×10^{14}	6.7×10^{14}
Ratio of $P(\mathbf{k})$ above	2039	2490
$\Delta^2(k = 0.3)$, Cosmic Dawn window	1.7×10^{12}	2.4×10^{12}

values. Region 1 is bounded by the horizon and the dashed line; it extends for approximately $\Delta k = 0.04 \,\mathrm{Mpc}^{-1}$, $\Delta \tau = 192 \,\mathrm{ns}$, beyond the horizon, and is commonly seen in other power spectra (e.g. Pober et al. 2013; Thyagarajan et al. 2015a, b). Spillover in Region 1 could be due to the window function applied to the delay transform, beam chromaticity, intrinsic spectral structure in foreground emission, RFI, and calibration errors (Kern et al. 2020b) . The use of a window function on the delay transform is essential to avoid spectral leakage due to the non-periodic nature of the baseline visibilities. The kernel width of the Blackman Harris window we apply to our delay transforms is 288 ns or $\Delta k_{\parallel} = 0.06$, indicating that it is a substantial contributor to Region 1 spillover.

Region 2 extends from Region 1 to the dashed–dot line; it extends for $\Delta k = 0.12 \,\mathrm{Mpc}^{-1}$, $\Delta \tau = 577 \,\mathrm{ns}$ beyond Region 1. The reason for the spillover in Region 2 is not known but we suggest that it is due to foreground power scattered by systematics that have not been removed by data quality checks or calibration. Unremoved systematics are also likely responsible for the faint lines that can be seen in the upper part of the power spectrum. These are highlighted



Figure 5. The power spectrum for XX polarization (Fig. 3, top left image) overlaid with features of interest. Regions 1 and 2 are regions of spillover in the Cosmic Dawn window. The top section indicates linear features that are approximately horizontal, with a slight downward slope, and run across almost the entire k_{\perp} range. The top section has been clipped to $10^{14} < P(\mathbf{k}) < 10^{16} \text{ mK}^2 \text{ Mpc}^3$ and rescaled to make the features clearer.

in Fig. 5, upper section ('linear features'). The lines begin near $k_{\perp} = 0$, $k_{\parallel} = 1$ and drop linearly and shallowly across the power spectrum to $k_{\perp} = 0.018$, $k_{\parallel} = 0.8$.

Systematics can have many causes, including unmodelled diffuse emission, an inadequate beam model and/or source model for calibration, RFI, cable reflections, cross-coupling, and mutual coupling, which we discuss as follows. Models of point sources are incomplete or approximate at OVRO– LWA frequencies. We generated calibration models using the VLA Low-Frequency Sky Survey at 74 MHz, calculating source flux densities at 48 MHz by assuming a spectral index of -0.7, and assuming that the location of emission at 48 MHz is the same as it is for 74 MHz. These assumptions likely lead to inaccurate models. Diffuse emission also exists within our observations, but we have not modelled it for calibration. Using more accurate source models, and including diffuse emission using a Global Sky Model (de Oliveira-Costa et al. 2008; Dowell et al. 2017), will improve calibration.

OVRO-LWA observations are affected by cross-coupling of antenna signals, where cables are in close proximity as they enter backend hardware-processing units. It is known to impact 509 baselines, and these are ignored when generating power spectra, but they may not be the only ones affected. A more detailed investigation is needed.

Electromagnetic interaction between neighbouring antennas (mutual coupling) may be present in OVRO–LWA observations, including coupling between the X and Y dipoles on the same OVRO–LWA stand, leading to polarization leakage. A study of mutual coupling in the LWA reported that it exists but has no consistent positive or negative effect (Ellingson 2011); however, more investigation of these effects is needed for OVRO–LWA.

Electrical signals travelling via cable from an antenna to backend components may reflect from those components, introducing sinusoidal structure in the antenna frequency response. For the most part, cross-correlations between antennas (i.e. visibilities) do not suffer this systematic as the noise waves along a pair of cables are not correlated. However, systematics due to cable reflections have been reported in other power spectra (e.g Beardsley et al. 2016) and may be present in ours. The linear features in Fig. 5 may be due to cable reflections, but in that case, we expect the features to be horizontal.

RFI flaggers such as AOFlagger (Offringa, van de Gronde & Roerdink 2012) will provide better RFI detection compared to the simple algorithm implemented within RTS. Flaggers will be implemented in the future within the OVRO–LWA pipeline. More sophisticated beam models can be generated through the use of simulation packages (e.g. FEKO,⁸ NEC,⁹ and CST¹⁰), direct measurements of the radiation field of the antenna [for example by using drones (Üstüner et al. 2014) or satellites (Neben et al. 2015)], or by observing radio sources transiting through the fringes of the interferometer (Parsons et al. 2016).

Methods for the detection, analysis, and removal of systematics in power spectra are being developed by other groups and reported in the literature. For example, Kern et al. (2020b) demonstrate the usefulness of analysing antenna-based gains in delay and fringe-rate space, using gain-smoothing to suppress delay modes that appear to be abnormal, and using temporal analysis and temporal smoothing of gains using autocorrelations. Cross-coupling can be removed by applying a high-pass filter in fringe rate space (Kern et al. 2020a). Window functions can be analysed for their contribution to horizon spillover, and alternative window functions selected (Lanman et al. 2020). Use of these and other methods will improve the quality of power spectra generated from OVRO–LWA.

6 THE SENSITIVITY OF OVRO-LWA

We now turn to the analysis of the sensitivity of power spectra generated from OVRO–LWA using the delay spectrum method and investigate the sensitivity that can be achieved using a large number of observations and a different integration strategy.

We determine the level of noise in OVRO–LWA observations – 'noise' includes thermal instrumental and sky noise. We use simulations to generate power spectra containing only noise; these allow us to find the noise floor in our power spectra from observations (Fig. 3). We then investigate the noise floor in power spectra generated from observations that are partly coherently integrated before power spectrum generation. Coherent integration should significantly reduce the noise level in power spectra.

6.1 Measuring the OVRO-LWA thermal noise

The noise in our observations is extracted from observed visibilities using a simple data-differencing technique (Bernardi et al. 2010; Chatterjee & Bharadwaj 2019) that subtracts visibilities in adjacent frequency channels. We assume that subtracting visibilities at slightly different frequencies will subtract out the sky signal and systematics, leaving only subtracted noise values. From the distribution of these noise values, we obtain the statistical properties of the noise, from which we can generate noise-only power spectra using simulations. The noise level in these power spectra is interpreted as the level of noise that would be present in power spectra generated from telescope observations. For visibility differencing, we use all the visibilities in all the calibrated observations used for the power spectra in Fig. 3, ignoring flagged visibilities.

Fig. 6 shows histograms of the values obtained from frequency differencing, for XX and YY polarizations, and for the real and imaginary parts of the values. The distributions are close to Gaussian, with a zero mean, giving us confidence that we have in fact extracted mostly thermal noise. However, there are wings in the data distribution indicating an excess of values around ± 3000 Jy, and the data peak is higher than the fitted peak. To investigate these, we generated images of the visibility differences from one of the OVRO–LWA observations. The images mostly contained noise, but showed that Virgo A and the RFI sources on the horizon (Fig. 2) were not always completely removed, leading to an excess of values at the location of the wings.

The standard deviations σ of the Gaussian fits to the noise histograms are listed in Table 4, top row. These fits include the wings previously mentioned; if the wings were not present, we would expect a narrower distribution and smaller σ values. To estimate what these would be, we fit a Gaussian to the noise histograms in the *x*-axis range of ± 2000 Jy only. The standard deviations for these fits are shown in Table 4, second row, and produce σ that are about 5 per cent smaller than those resulting from fitting the entire *x*-axis range.

To be conservative, we use the higher values of σ for our noise simulations.

6.2 Measuring the noise floor in the power spectra generated from 4 h of telescope observations (incoherent integration)

We simulate noise-only observations by replacing all the visibilities in all the 4 h of telescope observations with noise values drawn from a Gaussian distribution with zero mean and standard deviation listed in Table 4. Baselines that were flagged in the observations are flagged in the simulated noise-only observations, but flagged channels are filled in with a noise value. A 'noise-only' power spectrum is generated

⁸https://altairhyperworks.com/product/Feko/Applications-Antenna-Design ⁹https://www.qsl.net/4nec2/

¹⁰https://uk.mathworks.com/products/connections/product_detail/cst-micr owave-studio.html



Figure 6. Histograms of noise values (ΔV) obtained from differencing visibilities in adjacent frequency channels, over all observations used to generate power spectra. These represent the distribution of thermal noise in OVRO–LWA (although some systematics are present in the noise distributions, as described in the text). The top row is obtained from the XX polarization visibilities and the bottom row is from polarization YY. The real and imaginary values of the complex noise values are shown separately; the real values in the left column and the imaginary values in the right column.

Table 4. The standard deviations (σ) of Gaussian fits to the distributions of noise values obtained from the 4 h of observations (Fig. 6). The units are Jy. The values in the first row are obtained from fitting the histograms using the complete *x*-axis range of ±8000 Jy; the values in the bottom row are obtained from fitting in the range of ±2000 Jy.

	Pol XX	Pol YY
Real/Imag values (fit all data)	1313.0/1312.8	1543.3/1543.1
Real/Imag values (fit ±2000 Jy)	1265.8/1265.6	1472.2/1472.1

from the 4 h of simulated noise-only observations; these power spectra are shown in Fig. 7, and the power values extracted from them are listed in Table 5. The power spectra generated from observations have a value of $P(\mathbf{k}) \approx 5 \times 10^{14}$ in the Cosmic Dawn window (Table 3), but the noise-only power spectra have $P(\mathbf{k}) \approx 3 \times 10^{13}$ in the same region, demonstrating that there are systematics in the observed data.

All the power spectra presented so far were generated using incoherent integration; we now turn to experiments with coherent integration.

6.3 Measuring the noise floor in the power spectra generated from 4 h of telescope observations (if coherent integration is used)

We follow a method suggested by Paul et al. (2014), where observations are made within several short time intervals t_A , repeated over many days. Each time interval begins at the same LST each day, and all observations made during time t_A , at the same LST, may be coherently integrated. The scheme is depicted in Fig. 9. t_A is the 'time-averaging limit': the length of time over which observations may be safely coherently integrated (see Appendix B). By following this method, *N* coherently integrated observations are produced, which must then be incoherently integrated. We refer to this scheme as 'partial coherent integration'.

We note that it may be possible to apply this mix of incoherent/coherent integration to the 4 h of telescope observations that were used to generate the power spectra in Fig. 3, but it depends on the LSTs of the observations, as they must fit into appropriate time intervals as described above. An investigation of this possibility, and publication of power spectra that may result, is reserved for future work.

To demonstrate the use of the partial coherent integration method, and the noise reduction that can be achieved, we use the 4hof simulated noise-only observations from the previous section,



Figure 7. Noise-only power spectra generated from 4 h of simulated noise-only observations, and $\Delta^2(k)$ values obtained from them. The visibilities in the 4 h observations are replaced with noise values drawn from a Gaussian distribution with zero mean, and standard deviation obtained from the histograms of OVRO–LWA thermal noise in Fig. 6. These simulated noise-only observations are used to generate the power spectra shown. Different distributions are used for XX and YY polarization noise visibilities, producing separate power spectra for XX polarization (left column) and YY polarization (right column). The top row shows the power spectra; the bottom row plots $\Delta^2(k)$ values obtained from Cosmic Dawn window within each power spectrum (the regions from which the values are obtained are described in Appendix C).

Table 5. Values of $P(\mathbf{k})$ and $\Delta^2(k)$ extracted from simulated noise-only power spectra. The top two data rows are obtained from the power spectra in Fig. 7, which simulates the noise in a power spectrum generated from 4 h of incoherently integrated observations. The bottom two data rows are obtained from Fig. 8, which simulates the noise in a power spectrum generated from 4 h of partially coherently integrated observations (the integration method is described in Section 6.3).

	Noise power in 4 h of observations, incoherently integrated	
	Pol XX	Pol YY
$P(\mathbf{k})$	2.8×10^{13}	3.8×10^{13}
$\Delta^2(k = 0.3)$	4.7×10^{10}	6.3×10^{10}
	Noise power in 4 h of observations when	1
	partial coherent integration is used	
	Pol XX	Pol YY
$P(\mathbf{k})$	1.3×10^{7}	1.8×10^{7}
$\Delta^2(k=0.3)$	2.3×10^4	3.2×10^4

altering the observation LSTs so that we can apply the method. At 48.342 MHz, $t_A = 36$ s (Appendix B), so we simulate observing at four different LSTs (N = 4, Fig. 9) for 36 s each, over 100 d (D = 100). It is assumed that the thermal noise in the telescope does not vary over the 100 d, so that all noise values can be obtained from the distributions in Fig. 6.

Fig. 8 shows the power spectrum generated as a result, and Table 5 (bottom two rows) shows the average $\Delta^2(k)$ extracted from the power

spectra. These show that we can reduce the noise level in the power spectrum by a factor of $\approx 10^6$, when using partial coherent integration, instead of fully incoherent integration.

6.4 Measuring the noise floor in a power spectra generated from 3000 h of telescope observations (partial coherent integration)

Following on from the previous experiment, we obtain the noise level in power spectra generated from 3000 h of partially coherently integrated observations. These will be compared with the power in 21-cm fluctuations in the next section.

We set the number of observing days to D = 750, or 2 yr. An observing schedule over 2 yr may be difficult to sustain but feasible. For OVRO–LWA, it will also generate 169 TiB of data per sub-band, or 3.5 PiB in total, also feasible using a large computer cluster. We fix the observing time per day to 4 h, so as to avoid transits of the Galactic Centre and other bright sources. We assume that there are no transits of local bodies. We again assume that the noise properties of the telescope do not change over the 750 d, and that there are also no changes in telescope performance, availability, and reliability. The time-averaging limit t_A varies by frequency, so the number of intervals N (Fig. 9) must be different for each sub-band to accumulate 4 h per day. At 48.342 MHz with $t_A = 36$ s, N = 400; at 30 MHz with $t_A = 54$ s, N = 267.

We use a frequency range of 37.848-84.912 MHz (z = 15.7-36.5), dividing it into 18 sub-bands, each of width of



Figure 8. Simulated noise-only power spectra, the same as for Fig. 7, but some observations have been coherently integrated before power spectrum generation, as described in the text (Section 6.3).



Figure 9. A scheme for making observations with a drift-scan interferometer that can be partially coherently integrated. Observe for *N* short time intervals $(LST_i \rightarrow LST_{i+t_A})$ each day, repeat the observations over several days, and coherently integrate all observations within each interval across all days. The time range t_A is the time-averaging limit. The resulting *N* coherently integrated observations must be combined incoherently.

5.232 MHz. Each sub-band overlaps the next by 2.616 MHz and is separated in frequency by 2.616 MHz. The centre frequency is used to determine the redshift of the sub-band.

Observations at different frequencies will have different noise properties. We assume that the noise distribution will be Gaussian as depicted in Fig. 6, but that the σ of the noise distribution will vary by frequency. Since the noise distributions were derived from observed visibilities, we assume that σ varies as a power law with exponent -0.7, as was assumed for the source flux densities in Section 3. Therefore, σ_{ν} for the noise distribution at frequency ν is calculated

as:

$$\sigma_{\nu} = \sigma_{48.324} * \left(\nu/48.324 \times 10^6\right)^{-0.7}.$$
(5)

A power spectrum is generated for each sub-band, and the value of $\Delta^2(k)$ at k = 0.3 extracted from the power spectra. This gives a $\Delta^2(k)$ noise level for a range of redshifts, which can be compared against expected power based on theoretical models of the cosmological 21-cm signal, in the next section.

Generating 3000 h of noise-only observations is very compute intensive and generates 3.5 PiB of data, so we implement it in a Graphics Processing Unit (GPU). Since the observations all contain the same number of baselines and channels (none are flagged), a GPU thread is created for every channel in every baseline, and each thread generates and manipulates noise values 'on the fly', avoiding the need to store the values. A full description of the GPU implementation will be published elsewhere.

7 INVESTIGATING COSMIC DAWN USING OVRO-LWA OBSERVATIONS

From the simulations described in the previous section, we obtain the noise power in OVRO–LWA 21-cm power spectra, generated from 3000 h of partially coherently integrated observations, over a range of redshifts. If noise is the only contributor to power in the Cosmic Dawn window, apart from the 21-cm fluctuations, then the noise power determines whether a 21-cm detection is possible. In this section, we assume that this is so and discuss in detail what may be detected according to theoretical models. However, ensuring that noise is the only other source of power in the Cosmic Dawn window requires the elimination of all systematics that we have discussed above. This may be difficult at present, as methods that exist for removal of systematics are still being proven (e.g. see Kern et al. 2020b), but it is plausible in the future, at least, we suggest, to a level where systematic effects are insignificant. We base the following discussion on this 'best case' scenario.

Being a high-redshift instrument, OVRO–LWA is by design observing the 21-cm signal from the epoch of primordial star and black hole formation. Thus, observations with this instrument could be used to infer properties of the first sources as well as to constrain exotic physics at Cosmic Dawn.

The noise power $\Delta^2(k = 0.3)$ from 3000 h of partially coherently integrated observations is plotted as crosses in Fig. 10 for the redshift range of $17 \le 1 + z \le 38$. To demonstrate that OVRO–LWA is able to detect the 21-cm signal at these redshifts, the figure also contains $\Delta^2(k)$ for a sample of theoretical models, including the envelope of all possible signals in the standard astrophysical scenario (as explained below, and in Cohen et al. 2017), and an exotic physics case, which was proposed to explain the deep EDGES absorption feature (here for illustrative purposes we show a model with enhanced radio background over the CMB, see Fialkov & Barkana 2019). The models are described in the figure caption. Some of the standard astrophysical models, along with the exotic scenario, are well above the sensitivity of OVRO–LWA at these redshifts, indicating that OVRO–LWA is expected to be sensitive enough to dig deep into the discovery space of the predicted 21-cm signals.

Let us first examine the standard astrophysical case, i.e. models that assume the CMB as background radiation, with a conventional cold dark matter scenario, and hierarchical structure formation. The astrophysical model contains seven parameters (see Cohen et al. 2020, for a recent summary of the astrophysical modelling), including star formation efficiency $f_{*:}$ minimum halo mass suitable for star formation (or, equivalently, minimum circular velocity of



Figure 10. The simulated noise level of OVRO-LWA from 3000 h of partially coherently integrated observations at $k = 0.3 \,\mathrm{Mpc}^{-1}$ (crosses), plotted on top of a selection of 21-cm models (note the x-axis is in log scale). We show standard models with $V_c = 4.2$ km/s (light blue), 24.2 km/s (blue), and 52.1 km/s (dark blue) for fixed values of $f_* = 3$ per cent, $f_X =$ 0.07, $\alpha = 1.5$, and $\nu_{\min} = 0.1$ keV (the EoR parameters, although they do not matter much at these redshifts, are chosen to be $R_{\rm mfp} = 30 \,\mathrm{Mpc}$ and $\tau =$ 0.064). For comparison, we also show the case of higher $f_X = 1.7$ for $V_c =$ 24.2 km/s (dashed blue). We also show the model with maximum signal to noise in the LEDA band (magenta, out of examined 11164 models). This case has the following values of the astrophysical parameters: $f_* = 50$ per cent, $V_{\rm c} = 35.5$ km/s, $f_{\rm X} = 1$ with $\alpha = 1.5$ and $\nu_{\rm min} = 0.1$ keV, $R_{\rm mfp} = 40$ Mpc, and $\tau = 0.07$. We also show the envelope of all possible signals in the standard astrophysical scenario (thick grey lines, Cohen, Fialkov & Barkana 2018). Finally, we show an external radio background model (orange) that has the maximum signal to noise for LEDA: $f_* = 12$ per cent, $V_c = 4.2$ km/s, $f_X =$ 0.01 with hard X-ray SED, $\tau = 0.056$, and the excess radio background of 1.2 per cent over the CMB at 1.42 GHz (from Fialkov & Barkana 2019).

such haloes, V_c); X-ray efficiency of sources compared to their present-day counterparts f_X ; and the spectral properties of X-ray sources (namely, the slope of X-ray spectral energy distribution, α , and the minimum frequency, ν_{min}). We model the process of reionization using two more free parameters (the total CMB optical depth, τ , and the mean free path of UV photons, R_{mfp}); however, reionization does not play a significant role at the high-redshift regime probed by OVRO–LWA.

Astrophysics is in its simplest form at high redshifts accessible using OVRO-LWA. With first stars forming in small and rare dark matter haloes, and owing to the absence of massive galaxies and AGN, there are relatively few processes that affect the early 21-cm signal. Thus, constraining the 21-cm signal at high redshifts with OVRO-LWA would offer one of the purest probes of primordial star formation. The most prominent feature of the 21-cm signal from this epoch is the high-redshift peak in the power spectrum imprinted by the non-homogeneous Ly- α field (Barkana & Loeb 2005). The amplitude and central frequency of the peak depend on just two parameters in our case (f_* and V_c), and the peak is above the sensitivity of OVRO-LWA for models with efficient star formation in small dark matter haloes. Thus, using 3000 h of observations, OVRO-LWA can probe properties of the first star-forming haloes, star formation efficiency, and put constraints on stellar feedback. The second effect that can be constrained by OVRO-LWA is the onset of the IGM heating by the first X-ray sources. Although in some scenarios Xray heating is delayed, in many of the examined models X-ray sources turn on early and could imprint heating fluctuations in the gas

temperature in the OVRO–LWA band. Examining a set of $\approx 11\,000$ models with different combinations of astrophysical parameters, we find that the strongest signal to noise in the OVRO–LWA band has a model with efficient star formation ($f_* = 50$ per cent), with a minimum mass of star-forming haloes of $M_h \approx 3 \times 10^8 M_{\odot}$, and close to present-day X-ray heating efficiency (magenta curve in Fig. 10). For this model, both the Ly- α peak at $z \approx 22$ and the X-ray peak at $z \approx 16.5$ can be measured by OVRO–LWA.

For the other standard models shown in Fig. 10 (shades of blue), either the X-ray or the Ly- α peaks can be detected. We compare the case of dark matter haloes with $V_c = 4.2$, 24.2, and 52.1 km/s for otherwise fixed parameters. The Ly- α peak for $V_c = 4.2$ km/s occurs at high redshifts where the sensitivity of OVRO-LWA is weak and, thus, cannot be observed. However, the rise of the power imprinted by the temperature fluctuations can be measured in the highest frequency channels. For the other two cases ($V_c = 24.2$ and 52.1 km/s), the Ly- α peak is at lower redshifts and happens to be above the noise curve and, thus, is detectable. However, for these models the X-ray peak is shifted to higher frequencies out of the OVRO-LWA band. Finally, varying X-ray parameters can also play a role; compare the case of $V_{\rm c} = 24.2$ km/s with weak X-ray sources (solid blue, $f_{\rm X} = 0.07$) to a case with the same V_c but stronger X-ray heating ($f_X = 1.7$, dashed blue). Because the effects of heating and Ly- α coupling on the 21-cm signal anticorrelate, more efficient X-ray heating results in a lower Ly- α peak, which is difficult to detect, but also in an earlier and stronger X-ray peak that shifts into the OVRO-LWA band.

If the anomalously deep global signal detected by EDGES Low-Band is astrophysical, the 21-cm power spectrum is expected to be boosted by a few orders of magnitude (e.g. Fialkov et al. 2018; Fialkov & Barkana 2019; Reis et al. 2020). The exact amount of the enhancement relative to a standard scenario with the same astrophysical parameters depends on the underlying theory which explains the EDGES observation. Owing to this boost, it would be much easier to detect such signals. As an illustration, we show one example of such a signal in Fig. 10 (orange line) for a theory in which the 21-cm signal is enhanced due to an excess radio background over the CMB at high redshifts (from Fialkov & Barkana 2019).

Finally, in Fig. 11, we compare the sensitivity level obtained from 3000 h of observations with the power obtained from the 4 h of observations (Section 5) and the power obtained from other telescopes as reported in the literature (Table 6). We include a sample of models with excess radio background (Fialkov & Barkana 2019).

8 CONCLUSIONS

We have demonstrated that the delay spectrum method can be used to generate power spectra from OVRO–LWA observations, although they contain systematics that prevent us from reaching the level of 21-cm fluctuations in the Cosmic Dawn window. Many systematics can influence power spectrum sensitivity, including inaccurate sky models for calibration (including unmodelled diffuse mission), undetected RFI, inaccurate beam model (shape and chromaticity), gain calibration errors, cross-coupling and mutual coupling, and cable reflections; all of which are present, or likely to be present, in our power spectra. Mitigating systematics in the context of 21cm power spectra is an active area of research, and we will borrow promising techniques developed for use with other telescopes, such as the MWA, HERA, SKA, and LOFAR.

We have also demonstrated that a compact, imaging interferometer is able to generate a 21-cm power spectrum, indicating that such interferometers have a role to play in detecting the 21-cm signal in power spectra.



Figure 11. We show our limit of 2×10^{12} mK² at z = 28 and at k = 0.3 Mpc⁻¹ obtained from 4 h of observations (black triangle) in the context of limits from other high redshift 21-cm probes including LOFAR (NCP, red line) derived from 14 h of data at 54–68 MHz (z = 19.8-25.2) at $k \approx 0.038$ h Mpc⁻¹ (Gehlot et al. 2019), MWA (green line) derived from 3 h of data at 75–113 MHz (corresponding to z = 11.6-17.9) at k = 0.5 h Mpc⁻¹ (Ewall-Wice et al. 2016), OVRO–LWA (blue triangle) obtained using 28 h of data at 73.152 MHz (z = 18.4) at k = 0.1 h Mpc⁻¹ (Eastwood et al. 2019), and AARTFAAC (black line) obtained using 2 h of data at 72–75 MHz (z = 17.9-18.6) at k = 0.144 h cMpc⁻¹ (Gehlot et al. 2020). We also show the predicted OVRO–LWA sensitivity curve from the 3000 h of noise data (black crosses) obtained as described in the previous section, and a hundred randomly selected 21-cm power spectra modelled with extra radio background, from Fialkov & Barkana (2019).

We find that the power level in 21-cm fluctuations at 48.324 MHz is $\Delta^2(k) \approx 2 \times 10^{12} \text{ mK}^2$ at $k = 0.3 \text{ Mpc}^{-1}$, after incoherently integrating 4 h of observations. Simulations of OVRO–LWA thermal noise indicate that the noise floor in the power spectra is $\Delta^2(k) \approx$ $5 \times 10^{10} \text{ mK}^2$. This level is too high to detect 21-cm fluctuations at Cosmic Dawn, but we may take the value of $\Delta^2(k) \approx 2 \times 10^{12} \text{ mK}^2$ as an upper limit. Simulations show that if we were able to implement our partial coherent integration method, and apply it to 3000 h of observations, the noise floor would drop to 10^2 mK^2 , allowing for a detection according to theoretical models.

However, the noise simulations are simplistic. First, properties of the noise were obtained from visibility differencing. A more rigorous treatment would involve precise measurements and simulations of the noise in telescope components (e.g. as for the MWA, Ung et al. 2020), followed by an analysis of how this converts to noise power $\Delta^2(k)$ in a 21-cm power spectrum. Secondly, observing over a period of many years, to obtain observations that can be coherently integrated, will require that the telescope remains stable, along with atmospheric and environmental conditions, and that observations are not affected by transient events and unwanted objects passing through the field of view. It is unlikely that these can all be controlled, so some observations may need to be discarded, increasing the total observing time to compensate, or their effects will have to be mitigated in the data. These issues will have to be planned for.

We also mentioned that the delay spectrum technique is not suitable for the frequency range and baseline lengths that we have used. Long baselines can be excluded from power spectra, which will result in a shortened k_{\perp} range. Restricting the frequency range is problematic as it will result in few frequency channels being used for power spectrum generation. For example, using Equation (4) and

Table 6. Summary of 21-cm power spectrum limits obtained from observations using different telescopes.

System	Total observing time	Redshift	<i>k</i> for which power reported	Reported power
OVRO–LWA (Eastwood et al. 2019)	28 h	z = 18.4 (73.152 MHz)	$k = 0.1 \; {\rm Mpc^{-1}}$	$\Delta^2 < 10^8 \text{ mK}^2$
LOFAR LBA (Gehlot et al. 2019)	14 h	z = 19.8 - 25.2 (54 - 68 MHz)	$k \approx 0.038 \mathrm{h}\mathrm{Mpc}^{-1}$	$\Delta^2 < 2.2 \times 10^8 \text{ mK}^2$
MWA (Ewall-Wice et al. 2016)	3 h	z = 11.6 - 17.9 (75 - 113 MHz)	$k = 0.5 h Mpc^{-1}$	$\Delta^2 < 10^8 \text{ mK}^2$
AARTFAAC (Gehlot et al. 2020)	2 h	z = 17.9 - 18.6 (72 - 75 MHz)	$k = 0.144 \mathrm{h} \mathrm{cMpc}^{-1}$	$\Delta^2 < 7 \times 10^7 \text{ mK}^2$
This work	4 h	z = 25 - 31 (43 - 54 MHz)	$k = 0.3 \mathrm{Mpc}^{-1}$	$\Delta^2 < 2 \times 10^{12} \text{ mK}^2$

again interpreting \ll as 'one-half', and limiting baseline lengths to 50 m, the allowable bandwidth is 1.6 MHz. This means that only 70 OVRO–LWA frequency channels (of width 24 kHz) can be used, compared to the 436 that were used for the power spectra in this paper, resulting in fewer k_{\parallel} modes available for analysis.

The redshift range over which a power spectrum can be made at high redshift, so that it measures a static Universe, is uncertain and will not be determined until we have more knowledge of the actual rate of change of state of the early Universe, perhaps from global 21-cm experiments. The range will depend on the redshift of the observation; at $z \approx 9$, Pober et al. (2013) suggest a redshift range of $\Delta z \approx 0.5$ as being acceptable. At $z \approx 28$, as used here, a redshift range of 0.5 corresponds to a frequency range of 0.8 MHz, which allows for only 33 OVRO–LWA channels to be used for power spectrum generation. This and the discussion in the previous paragraph indicate that the OVRO–LWA frequency resolution should be increased for future work.

We may also expand future work to include other methods of power spectrum generation, such as removing foregrounds from observations using foreground models (e.g. as in Gehlot et al. 2019), or adopting the m-mode analysis used by Eastwood et al. (2018). However, many of the issues mentioned above still remain and should be addressed before doing so.

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DATA AVAILABILITY

The data used to generate the results reported in this paper are not publicly available, but will be shared, on reasonable request to the corresponding author.

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APPENDIX A: SELECTION OF TELESCOPE OBSERVATIONS USED FOR POWER SPECTRUM GENERATION

The selection criteria are simple and heuristic. Observations for integrated power spectra are selected first on the accuracy of their calibration and then on the quality of the power spectrum that each observation produces.

Each 9 s observation is calibrated, and a calibration score assigned, based on how closely the calibrated observation reproduces the flux densities of the calibration sources. A score of 1 indicates perfect calibration, and we select all observations with a score of 0.8-1.2.

Each observation selected by the previous step is then assigned a score obtained from the power spectrum that the observation generates. A high score indicates (a) that the power outside the wedge is low compared to the power inside the wedge, and (b) that the power outside the horizon is flat, i.e. does not vary much but maintains a constant value. The scores are obtained from mean and rms values of the power in regions in the power spectrum (Table C1, row 1).

The 4 h of observations selected for power spectrum generation are the 4 h of observations that scored the highest in the previous step.

APPENDIX B: TIME-AVERAGING LIMIT FOR OVRO-LWA

Coherent integration of visibilities recorded at different times may result in amplitude loss, due to sky sources changing position relative to interferometer fringes. This is referred to as time-smearing or time-averaging loss. When observing continuously, only visibilities recorded within a short-time range t_A may be coherently integrated.

Following equations (16.5) and (16.6) in Thompson, Moran & Swenson (2017), the fractional loss in amplitude, ξ , in integrated visibilities observed over some time range *T*, for an east–west oriented baseline, can be expressed as

$$\xi = 1 - \operatorname{sinc}(\pi \omega_{\rm e} \cos \delta [D_{\rm EW} \nu/c]T), \tag{B1}$$

where $D_{\rm EW}$ is the length of the baseline, $\omega_{\rm e}$ is the sidereal rate, δ is the observing declination of a source, and ν is the observing frequency. For an interferometer containing many baselines, the most restrictive value for *T* is found by setting $D_{\rm EW}$ equal to the maximum east–west baseline length and setting δ to 0.

For the OVRO–LWA telescope observations that were used for power spectrum generation, we allow that the fractional loss in amplitude can be no more than 0.01. Therefore, we set $\xi = 0.01$, $D_{\rm EW} = 200$ m, $\delta = 0$, and $\nu = 48.324$ MHz, and solve for *T*, giving $t_{\rm A} = 33$ s. Observations whose times are separated by no more than 33 s may be coherently combined. We increase it to 36 s so as to be a multiple of the OVRO–LWA observation integration time (9 s). The time limit for other frequencies can be similarly obtained.

APPENDIX C: REGIONS USED TO OBTAIN POWER VALUES FROM POWER SPECTRA

When extracting values from a power spectrum, for example to report statistics or generate $\Delta^2(k)$, we use only certain regions. The regions avoid artefacts in the power spectrum and select areas appropriate for the required statistic; for example, statistics for the Cosmic Dawn window avoid the foreground wedge and high power at low k_{\perp} . Table C1 shows the regions used for each type of data analysis; they are the area in white plotted on top of a power spectrum. The

first two rows in the table apply only to power spectra generated from observations; the next two rows apply only to power spectra generated from simulations of noise.

When a value for $P(\mathbf{k})$ is reported for a power spectrum, this is the average value of $P(\mathbf{k})$ within the region being discussed.

To obtain $\Delta(k)^2$ values from a region, all the pixels within the region are assigned a *k* value, converted to dimensionless power via equation (3), and binned (averaged) by *k* using 16 logarithmic bins within the range of the obtained *k* values.

Table C1. Regions in the power spectrum used for obtaining power $P(\mathbf{k})$ and $\Delta^2(k)$.



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