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IMPACTS OF PREFERENTIAL FLOW ON Tc-99 AND Np-237 VADOSE  
TRANSPORT IN SOILS AT THE SAVANNAH RIVER SITE

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A Thesis  
Presented to  
the Graduate School of  
Clemson University

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In Partial Fulfillment  
of the Requirements for the Degree  
Master of Science  
Hydrogeology

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by  
Joshua Luke Parris  
May 2023

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Accepted by:  
Dr. Brian Powell, Committee Chair  
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## ABSTRACT

Since the 1950s, the United States has produced approximately 90,000 metric tons of spent nuclear fuel (SNF) (Office of Nuclear Energy, 2022); however, no long-term storage solutions are available. Technecium-99 and neptunium-237, two fission products found in SNF, readily form highly mobile species in oxidizing conditions (Hu, 2008; Bondietti, 1979) and have respective half-lives of  $2.13 \times 10^5$  and  $2.14 \times 10^6$  years (Hu, 2010). Considering these characteristics,  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  are two risk-driving isotopes found in SNF storage. The process of macropore-facilitated preferential flow, transport through cracks within a soil matrix, has been recognized to increase radionuclide mobility (Bundt, 2000). The aim of this study is to clarify the influence of macropore structures (orientation and geometry) on the transport of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  in unsaturated sand and sandy clay loam (SCL) soils.

Unsaturated column flow experiments were completed with Br (tracer),  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  on homogeneous and macroporous soil columns. CT scans of soil columns were acquired to generate 2D and 3D imaging of macropore networks. Retardation factors for  $\text{Tc}^{99}$  breakthrough were 1.30 in homogeneous SCL and ranged from 1.28 to 1.41 in macroporous SCL, indicating that macropore-facilitated bypass flow is limited in unsaturated conditions. However,  $^{99}\text{Tc}$  exhibited earlier initial arrival (IBV) and longer attenuation in macroporous SCL soils. Increasing dispersivity estimates, determined by fitting the two-region nonequilibrium convection dispersion equation (MIM), well describe the anomalous breakthrough trends observed in macroporous SCL soils. From these findings, we conclude that macropore structures oriented transverse to unsaturated flow act as capillary barriers (resulting in longer radionuclide attenuation). If vertically oriented, macropore structures act as capillary boundaries that isolate matrix flow to a fraction of the pore network (increasing the average porewater velocity and IBV).

## ACKNOWLEDGMENTS

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## KEYWORDS

Preferential flow, vadose zone, unsaturated flow, macropore flow, macropore network, capillary exclusion, radionuclide transport, technetium-99, Tc-99, neptunium-237, Np-237, bromine, bromide, Br, Savannah River Site, SRS, non-equilibrium transport, residence time distribution analysis, RTD, temporal moments analysis, spatial moments analysis, two-region non-equilibrium transport model, mobile-immobile model, MIM, mobile-fluid region, immobile-fluid region, convection-dispersion equation, CDE, spent nuclear fuel storage, SNF, dispersivity, mobile water fraction, mass transfer coefficient, CXTFIT, pore volume, sandy clay loam, sand, soil, sorption, partitioning coefficient,  $K_d$ , column flow experiment, column tracer test, mean arrival time, MAT, mean travel time, MTT mean arrival pore volume, MAPV, mean travel pore volume, MTPV, retardation factor, CT scanner, MILabs, U-CT scanner, soil structures, 3D macropore network reconstruction, heterogeneity, and effluent.

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# CHAPTER 1: INTRODUCTION

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## 1.1 Background

The presence of radionuclides in the environment poses long-term impacts on human health and ecosystems. The proliferation of these contaminants across the United States rose with the development of nuclear weapons and nuclear energy in the 1950s (DOE/NE-0088). During this time period, limited regulations enabled the disposal of radioactive byproducts and waste in unlined pits and settling basins. Since then, the United States has produced approximately 90,000 metric tons of spent nuclear fuel (SNF) (Office of Nuclear Energy, 2022). Permanent storage plans of SNF within the vadose zone have been proposed at Yucca Mountain in Nevada (Eckhardt et al., 2000). High-level radioactive liquid waste is also generated as a byproduct of processing nuclear materials. DOE generated high-level waste and Cold War era legacy waste is stored at DOE operated nuclear industrial complexes such as the Savannah River Site (SRS) in Aiken, SC.

The migration of radionuclides in the environment is dependent on physical, geochemical, and biological processes unique to the environment affected (Seaman et al., 2012). A critical component in assessment and remediation efforts is the development of transport models that incorporate the processes that govern radionuclide mobility. To build and validate site-specific radionuclide transport models, interdisciplinary research efforts must be applied.

In recent years, research has been conducted to define the governing transport processes, generate comprehensive transport models, and accurately estimate and scale radionuclide model parameters (Massabó, 2011; Brouyère, 2006; Dagan and Cvetkovic, 1993;

Ababou, 1991; Van Genuchten & Wagenet, 1989). Vadose zone transport is made complex by preferential flow, variable spatiotemporal redox conditions, and chemical non-equilibrium adsorption. Furthermore, predictive modeling of radionuclide transport at the field-scale has been challenged by the issue of scale-dependent parameterization. Thus, the assessment of radionuclide vadose transport requires multi-scale, site-specific studies coupled with reactive and numerical transport models (Moradi, 2020).

## 1.2 Significance: The Savannah River Site

The Savannah River Site (SRS) is a 300,000 square mile nuclear reserve located in Aiken, South Carolina (DOE/NE-0088). SRS is home to 51 underground radioactive waste storage tanks (Area's F and H). Four of these tanks have been permanently closed and 20 tanks are lacking secondary containment, violating EPA regulations. No leaks are currently reported from these tanks; however, 12 of the 20 tanks in violation have a history of leaking (U.S. NRC, 2021). Recent DOE documents report that SRS presently stores  $1.4 \times 10^8$  L (36 Mgal) of liquid radioactive waste, amounting to  $\sim 400$  MCi of radioactivity (Wilmarth, 2011).

Historically, nuclear reactors at this site produced weapons-grade tritium and plutonium. The fabrication of these materials produced uranium-bearing waste that was disposed of on-site in settling basins and unlined pits. Recent studies have estimated that 83% of the uranium released into the environment is now sequestered in a wetland onsite (Kaplan et al., 2020). Kaplan et al. (2020) found that sorption of uranium to wetland soils at SRS effectively immobilized the leached uranium. However, other long-lived actinides with variable sorption characteristics may not have the same fate if released into the environment.

During nuclear fuel reprocessing, waste is generated with significant concentrations of  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  (Hu, 2010). With half-lives of  $2.13 \times 10^5$  and  $2.14 \times 10^6$  years respectively, and high mobility in oxidizing conditions, these radionuclides pose a significant risk for human exposure if leached into surface or groundwater systems. To accurately assess and predict the fate of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  at SRS, site-specific transport models coupling hydrologic and geochemical processes must be expanded upon.

### 1.3 Preferential Flow

Characterizing flow and transport in the vadose zone has been a challenging yet promising field of research in recent years (Zhang, 2018). As many radionuclide contaminant sources are located in the vadose zone, it is critical to further our understanding of transport in this subsurface region. Flow and transport in the vadose zone is, in part, complicated by the phenomena of preferential flow. The physical process of preferential flow was described by Hendrickx and Flury (2001) as the channeling of infiltrating water and solutes through a small fraction of a pore-network. The variable mechanisms of this phenomenon are distinguished by three unique types of preferential flow: macropore flow, fingered flow, and funnel flow (Stumpp, 2022). During funnel flow, the preferential flow of water is dependent on localized heterogeneities. For example, a clay lens within a sandy loam matrix will redirect the flow of infiltrating water to a preferential flow path. Fingered flow occurs in unstructured coarse-grained soils and is described as an unstable wetting front (Zhang, 2018). This unstable wetting front is a product of opposing capillary and gravitational forces that generate fingered flow paths. Lastly, macropore flow refers to the preferential flow of water through soils that contains pore-scale heterogeneities, i.e., fractures (Jarvis, 2016). These macropore structures

can form from both biological and physical processes. The wet-dry cycling of clay soils has been shown to generate macro-pore structures that enable preferential flow (Schlüter 2016; Pires 2020; Al-Mamun 2022), and coarse root systems have also been found to increase soil macro-porosity (Bodner et al., 2014).

Noted by Mamun (2022), the orientation and geometry of macropores largely impacts the advective, diffusive and preferential transport processes that occur during infiltration events. Mamun states that vertical macropores enable matrix bypassing flow and transport during infiltration. Transport across horizontal macropores is mediated by the formation of droplets within the macropore or through capillary bridges. However, they can act as capillary barriers to evaporative upward transport, decreasing the net downward flux (Mamun 2020).

As hydrologic conditions transition from equilibrium flow to macropore flow, spatial variations of both flow velocities and solute concentrations are observed within the pore-network. Radionuclides have an affinity to sorb to soils with high iron-hydroxide (FeOH) compositions (Kaplan et al., 2018). Under the geochemical conditions at the SRS,  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  show weak sorption to soil minerals and are generally mobile in the subsurface (Montgomery, 2017; Powell, 2018; Peruski, 2018). Non-uniform fluid and solute distributions in soils at the macro-scale will reduce the contact between solutes and potential FeOH sorption sites. Effectively, this process can limit a soil's ability to retard radionuclides in transport. The extent to which preferential flow processes impact the adsorption of mobile radionuclides such as  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  is currently not well defined. Moreover, adsorption is just one process that governs the retardation of radionuclides in transport. Advection, and chemical precipitation are all other

processes that influence the transport of radionuclides and can be impacted by preferential flow (Luo et al., 2000).

#### 1.4 Soil Properties and Geochemistry

To properly evaluate the behavior of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  in the environment, the soil properties of the region studied must be determined. In this study, experiments will be designed to replicate vadose zone conditions at the SRS. The soil classification, pH, redox potential, iron content, and natural organic matter (NOM) content are all critical parameters to define at this site. Sand and sandy clay loam (SCL) soil was collected from borrow pits located on-site at SRS. The region is rich in deposits of SCL (66% sand, 14% silt, 20% clay) and acidic with groundwater pH measurements ranging from 3.2 to 6.8 (Otosaka, 2011). Assuming this pH range and aerobic conditions, technetium will dominantly speciate in the heptavalent state as pertechnetate ( $\text{TcO}_4^-$ ), a water-soluble oxyanion of technetium, and neptunium will speciate in the pentavalent oxidation state. The mobility of these species in soil is impacted by the process of adsorption. Iron-bearing surface minerals act as sorption sites in soils; therefore, quantifying the extractable iron in sediments can enable the prediction of a radionuclide's relative mobility at a site (Kaplan et al., 2018). Iron concentrations, extracted via citrate buffered dithionite (CBD), in sandy clay loam (SCL) soils from SRS were found to have a concentration of  $6.01 \pm 0.68$  mg/g (Table 1.1) In SRS SCL soils, sorption of  $^{237}\text{Np}$  is relatively stronger than  $^{99}\text{Tc}$ . Partitioning coefficients ( $K_d$ ) values estimated for  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  in this same soil were -0.2 and  $5.5 \text{ cm}^3 \text{ g}^{-1}$  (Montgomery, 2018).

**Table 1.1** Soil Properties and Characteristics

<u>Parameter</u>	<u>Unit</u>	<u>Value</u>
Soil classification	-	Sandy clay loam (SCL)
Sand / Silt / Clay	%	66 / 14 / 20
Soil porosity, $\theta$	-	0.35
Hydraulic conductivity, $k$	$\text{m s}^{-1}$	6.31E-6
Point of zero charge, $pzc$	-	4.9 <sup>a</sup>
NOM content	%	0.9 <sup>a</sup>
Iron content (CBD-extractable)	$\text{mg g}^{-1}$	6.01 $\pm$ 0.68 <sup>a</sup>
SRS Groundwater pH	-	3.2 – 6.8 <sup>b</sup>

<sup>a</sup> Montgomery, 2017<sup>b</sup> Otsaka, 2011

## CHAPTER 2: OBJECTIVES AND HYPOTHESES

---

### 2.1 Objectives

The objective of this study is to characterize the impacts of macropore structures on  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  transport in unsaturated soils from SRS. The experimental design focuses on the flow and transport processes: macropore flow, matrix diffusion, and capillary exclusion. The aim of this study is to observe macropore generation in soils during wetting-drying events, identify dominant transport processes in macroporous sand and SCL, and clarify the roles macropore orientation and geometry play in radionuclide migration.

This experimental study, broken up into four prominent tasks in Table 2.1, is designed to evaluate the current transport model established for  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  at SRS, and assess the effects of macroporosity on physical and chemical transport processes. These tasks produce: 1) baseline transport datasets for Br,  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  in SRS soils with homogenous soil structures, 2) provide qualitative imaging of macropore structures generated from a wetting and drying event of sandy clay loam soils, 3) quantitatively evaluate  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  mobility under heterogeneous flow conditions, and 4) estimate site-specific modeling parameters. By executing these tasks, one can make conclusions applying to the nature of radionuclide transport at SRS, and how these transport processes are impacted by macropore-facilitated preferential flow.



Table 2.2 Experimental Tasks and Objectives

<u>Tasks</u>	<u>Objectives</u>
<u>Task 1</u> Execute a preliminary lab-scale column flow test under homogenous pore-structure conditions with sand and a sandy clay loam from SRS	Evaluate the experimental design and determine baseline elution curves for Br, <sup>99</sup> Tc, and <sup>237</sup> Np
<u>Task 2</u> Acquire pore-structure imagery of lab-scale soil columns pre- and post-wet-dry event	Assess the impacts of environmental wetting and drying events on macropore structures in unvegetated sands and sandy clay loam soils
<u>Task 3</u> Execute lab-scale column flow experiments on unvegetated soil columns that have been exposed to wet-drying conditions	Determine the influence that macropore structures have on <sup>99</sup> Tc, and <sup>237</sup> Np mobility in unvegetated sands and sandy clay loam soils
<u>Task 4</u> Simulate column flow experiments using non-equilibrium convection-dispersion Eqn. (MIM model) and statistically fit to experimental results	Establish site-specific modeling parameters (i.e., dispersivity, mobile water fraction, and mass transfer coefficient) and quantify the impact of macropore flow on these parameters

## 2.2 Hypotheses

With the objectives outlined in Table 2.1, this study will expand upon environmental transport models previously done for the Radionuclide Field Lysimeter Experiments (RadFLEX) at SRS (Kaplan et al., 2004; Demirkanli et al., 2007; Demirkanli et al., 2008; Demirkanli et al., 2009; Molz et al., 2015). It is hypothesized the presence of macropore networks in soils will decrease the number of active flow paths within a pore network, effectively decreasing the pore volume used by mobile fluid and increasing local flow velocity variations. Flow regimes with a decreased effective pore volume and wider distribution of flow velocities will show both earlier arrival and longer attenuation of <sup>99</sup>Tc and <sup>237</sup>Np. This is simplified by stating the presence macropores networks will separate the soil matrix into mobile and immobile fluid regions, which correspondingly enhances and limits advective (physical) transport. It is also

hypothesized that increases in solute flux through a smaller (mobile) fraction of the pore matrix will decrease chemical adsorption of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  by limiting the number of interactions between radionuclides and sorption sites. These hypotheses will be evaluated by interpreting mean arrival estimates (moments analysis) and parameter fitting of column breakthrough with the 1D mobile-immobile (MIM) transport model.

## CHAPTER 3: METHODS

---

### 3.1 Experimental Design and Setup

In this study, unsaturated flow column experiments were executed at the lab scale to progress our understanding of preferential flow and its impacts on  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  transport in sandy clay loam soils. To describe simply, a spike solution containing a contaminant and a non-reactive tracer is first added to the packed sediment column. While maintaining a constant flow rate, the column is then flushed with a wash solution (DI) for a given number of pore volumes. Effluent samples are collected at time intervals throughout this process and analyzed to produce breakthrough curves. In our application, these laboratory experiments were designed to replicate the environmental conditions of the vadose zone at SRS while evaluating contaminant mobility in a laboratory environment.

#### *Column Preparation*

Unsaturated column flow tests were completed using polyethylene columns (column I.D. = 3.75 cm, h = 18 cm) packed with either a sandy clay loam or sand (Figure 1). To ensure sediments were initially packed homogeneously, sediment was added in two-centimeter increments. In between each layered addition, the column was tapped on a hard surface to allow for sediment to settle. Additionally, the top surface of each layer was scarified with a scoopula to ensure any overlying layers were coupled and well mixed. Once packed, select columns were exposed to wetting and drying cycles to replicate the conditions that sediments endure in the vadose zone. This process consisted of fully saturating each column with



Figure 1 Sandy clay loam (SCL) and sand packed columns ( $d \approx 14$  cm) used in column flow experiments. Columns are pictured prior to exposure to wet-drying event.

deionized water, allowing them to fully drain, and then dry at room temperature for over two months. With the exception to sand and sandy clay loam control columns (*SCL\_H\_1* and *S\_H\_1*), all columns were exposed to one wet-drying event (Table 3.1). Pore volume estimates of each column were determined by saturating each column and comparing the dry and saturated weights. The sand and sandy clay loam control columns (*SCL\_H\_1* and *S\_H\_1*) were saturated 48 hours prior to experimental testing to determine their pore volume and initially wet the soils. To minimize the trapping of air in pores during this process, all columns were filled from the bottom up via capillary tubing and a peristaltic pump (Figure 1).

Table 3.3 Outline: Unsaturated Column Flow Experiments

Exp. #	Column ID	Soil Type	Environmental Conditions	Initial Water Saturation
H_1	SCL_H_1	Sandy clay loam	Control	Pre-saturated
	S_H_1	Sand		
M_1	SCL_M_1	Sandy clay loam	Wet-dry cycled	Dry
	S_M_1	Sand		
M_2	SCL_M_2	Sandy clay loam	Wet-dry cycled	Pre-saturated
	S_M_2	Sand		
M_3	SCL_M_3	Sandy clay loam	Wet-dry cycled	Pre-saturated
	S_M_3	Sand		

### Unsaturated Column Flow Experiments

The column flow experiments applied in this study maintained unsaturated conditions by adding the influent solution at a constant volumetric flow rate of  $\sim 0.1$  mL/min. Estimates of the soils hydraulic conductivity are  $6.31 \times 10^{-1} \text{ m s}^{-1}$  and column's inner diameter was 3.75 cm (cross-sectional area =  $1.1 \times 10^{-3} \text{ m}^2$ ). Using this configuration and flow rate, darcy flux through the column is estimated to be  $4.1 \times 10^{-6} \text{ m s}^{-1}$ . As the flux remains smaller than the soils hydraulic conductivity, unsaturated conditions theoretically will be maintained.

During experimentation, a peristaltic pump connected to capillary tubing was used to drip the influent solution onto the top-soil surface at a constant rate (Figure 2). A spike solution containing Br,  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  was prepared in 2%  $\text{HNO}_3$ . Each experiment was initiated by the addition of the spike solution. The spike solution volume added varied between experiments varied from of 0.69 to 1.0 pore volumes. Once the spike solution was added, the influent solution was switched to a bottle of deionized (DI) water which was used to flush the column

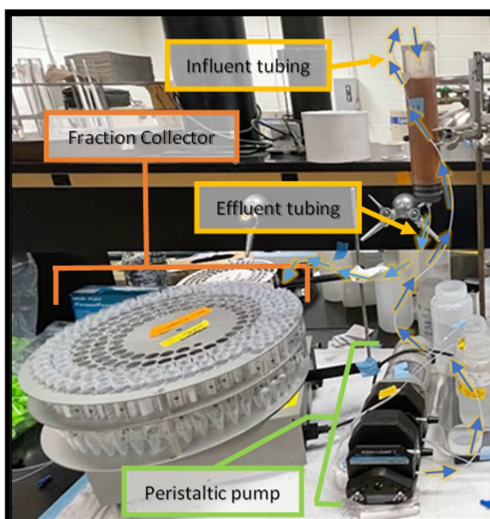


Figure 3 Laboratory setup for unsaturated column flow experiments. Label experimental components include influent line, effluent line, fraction collector, and peristaltic pump.

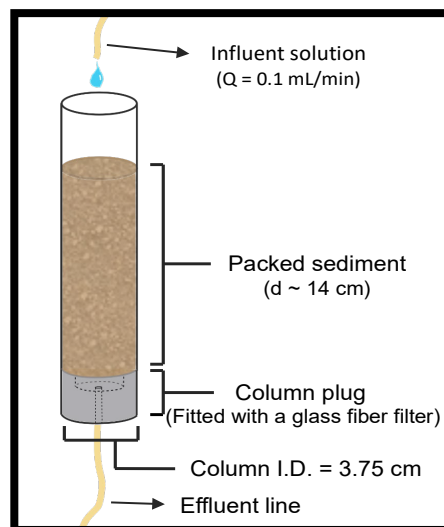


Figure 2 Schematic of unsaturated column flow experiment

for a minimum of 5.0 pore volumes following the spike solution. For the duration of the experiment, the effluent solution gravity drained through a glass fiber filter fitted at the base of the column and was collected with 15 ml centrifuge tubes using an Eldex fraction collector (Figure 2) In each column flow experiment, samples were collected every 30 minutes for the first 80 samples and at one-hour increments for the final 30 samples. With an influent flow rate of 0.1 mL/min, each experiment ran for just over three days.

### *Peristaltic Pump Calibration*

The peristaltic pump, responsible for adding the spike and DI water influent solutions in each column experiment, was calibrated to accurately set and maintain a constant flow rate. The *Masterflex L/S Easy-Load II* peristaltic pump, equipped with dual pump heads and a 1-100 RPM motor, was used for all column flow experiments. For this model, the pump head rotation speed is controlled by a unitless manual dial, also known as a potentiometer. To calibrate this dial to pump at a flow rate of 0.1 mL min<sup>-1</sup>, the pump tubing diameter and length were first configured identically when used for experiments. The pump was then turned on at an arbitrary pump speed, and a volume of pumped water was collected and weighed at 10 min intervals. The dial position of the potentiometer was marked to establish a reference point associated with the calculated flow rate for each collection. The dial was then lowered, and this process was repeated until the flow rate of 0.1 mL min<sup>-1</sup> was bounded on upper and lower ends within a tolerance of 0.02 mL min<sup>-1</sup>. The upper and lower bounds were marked on the potentiometer to reproducibly set the desired flow rate.

### 3.2 Effluent and Sediment Analysis

#### *Core Sectioning*

Within 24 hours after each unsaturated flow experiment, sediment columns were reweighed, scanned via x-ray computed tomography, and sectioned into 1 cm increments. Each sediment column was sectioned from bottom to top with a sediment core extruder. The column plug from the base of the column was first removed to allow for sediment to be extruded from the outlet. A plunger cap was then placed on the top of the sediment core, and the column was inverted. With the column orientation reversed in the press, the bottom sediment was extruded first. All columns were sectioned from bottom to top because the highest sorbed concentrations were estimated to remain in the top 5 cm of the column. Extruding the upper 5 cm last minimized any smearing and cross-contamination of sediment sections in the column.

When mounted in the press, a threaded extrusion rod was tightened with a socket wrench to extrude sediment in controlled increments (Figure 4). Each section was sliced in 1 cm increments, transferred into aluminum dishes, and weighed. Post-sectioning, all sediment samples were immediately placed in an oven and dried at 48°C for 72 hours. Pre- and post-drying sediment weights were recorded and used to calculate water content profiles for each column.



Figure 4 Sediment core extruder used to section sediment columns into ~ 1 cm intervals

### *Sediment Digestions*

Dried core sections were digested to quantify the sorbed mass fraction of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  at depth. Sediments were digested with a 4:1 nitric acid to sediment ratio (by weight). First, approximately 20 g (~ 12.5 mL) of sediment was transferred from aluminum dishes into 50 mL centrifuge tubes, suspended in 30 mL of ~ 5.3 M  $\text{HNO}_3$ , and shaken on a shaker table for 72 hours. The sample digestions were later centrifuged at 4500 rpm for one hour. The supernatant was then decanted into new centrifuge tubes. The efficiency of each digestion was not directly measured with an internal standard; however, each experimental dataset was holistically validated with mass balance calculations.

### *Analytical Instrumentation*

Elemental analysis of effluent samples and sediment digestions was primarily completed via inductively coupled plasma–mass spectrometry (ICP-MS). All ICP-MS analysis was performed with a Thermo Scientific iCAP™ RQ analyzer equipped with a quadrupole mass spectrometer. In preparation for elemental analysis of effluent samples, 0.5 mL subsamples were diluted by a factor of four with ~ 0.5 M  $\text{HNO}_3$ . Similarly, sediment digestions were diluted by a factor of 10 to reduce matrix interferences. During ICP-MS analysis, an internal standard solution containing ~ 10 ppb  $^6\text{Li}$ , Sc, Bi, Ga, In, Tb, and Y was run alongside standards and samples to correct for variations in sample uptake, detector response, and or matrix interference. Once quantified, datasets were used to generate Br,  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  breakthrough curves and sorbed  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  profiles. These datasets were collectively used to complete a mass balance for each experiment. Liquid scintillation counting (LSC) was intermittently used across this study to verify  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  spike and effluent concentrations determined via ICP-MS.



### *Pore-scale Imaging*

Pore-scale imaging of soil columns was achieved via X-ray computed tomography (CT) scanning (MILabs U-CT scanner)(Figure 5). Utilizing the same concepts as medical CT scanners, X-rays are emitted at an object and detected by a digital detector positioned opposite of the beam source. The attenuation, or intensity reduction, of transmitted X-rays, increases with material density. From these scans, cross-sectional images are computed so that pixel intensities are dependent on localized density contrasts across the object. Image processing software can then be used to stack the acquired slices into a reconstructed volume.

Throughout a sediment column, density contrasts exist between soil, pore-water, and air interfaces within the micro- and macro-pore networks. The effective application of computed tomography to identify macropore structures is dependent on the instrument's scanning resolution. The MILabs U-CT scanner has a minimum voxel resolution of  $30 \mu\text{m}^3$  (MILabs 2022). CT scans of soil columns were image processed with a voxel resolution of  $60 \mu\text{m}^3$  to capture alterations of the pore structure at this scale. Equipped with a vertical bore, the MILabs U-CT scanned sediment columns while positioned in an upright orientation.

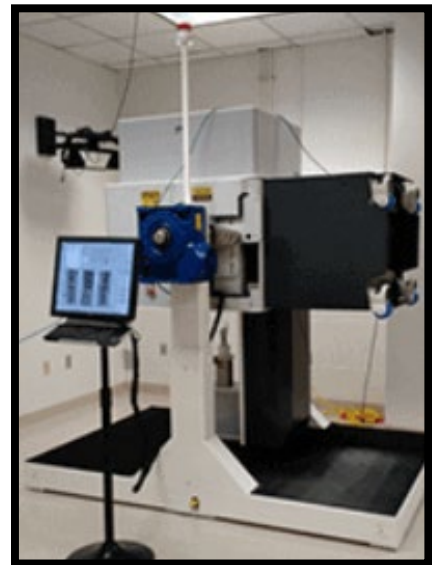


Figure 5 MILabs U-CT scanner equipped with a vertical bore used to investigate soil structures present in SCL and sand packed columns

### 3.3 Data Analysis

#### *Overview: Moments Analysis*

Lab-scale column flow experiments completed in this study were developed to characterize the mobility of  $^{99}\text{Tc}$  and  $^{237}\text{Np}$  in homogenous and heterogeneous pore networks. Moment's analysis was applied to normalize varying factors across column flow experiments, produce mass and volume balances for effluent data, and evaluate solute breakthrough curves and sorbed solute distributions. When applied to outflow data from column flow experiments, characteristic temporal moments indicate the total mass eluted, mean arrival time, the extent of spreading, and skewness. Spatial moments were used to quantify analogous parameters that are determined from sediment concentration profiles.

The zeroeth, first, second, and third moment from Br,  $^{99}\text{Tc}$ , and  $^{237}\text{Np}$  breakthrough curves and  $^{237}\text{Np}$  sorption profiles following general equations 1 and 2 (Shook, 2005). Temporally,  $n^{\text{th}}$  moments correspondingly evaluate the total mass eluted, mean arrival time, variance, and skewness. Spatially, they represent the total adsorbed mass, mean travel distance, variance (plume spread), and skewness.

$$\mu_n = \int_0^{t_f} C t^n dt = \sum C t^n \Delta t \quad \text{Eqn. 1}$$

$$\mu_n = \int_0^{z_f} C z^n dz = \sum C z^n \Delta z \quad \text{Eqn. 2}$$

Equation 1 states that the  $n^{\text{th}}$  moment ( $\mu_n$ ) is generally determined by integrating the product of concentration and time to the  $n^{\text{th}}$  power with respect to time. Spatial moments analysis will follow formulations identical to the temporal moments analysis described in the following sections (*Ch. 3, sect. 3.3 – 5.5*) but with respect to distance ( $z$ ) where  $z$  is equal to sediment depth (*Eqn. 2*).

### *Numerical Integration*

Given that breakthrough curve datasets are comprised of a finite set of time-series effluent concentrations, numerical integration was used to approximate these integrals. The trapezoid method, equation 3, was used to evaluate  $n^{\text{th}}$  moments for experimental data. This integration method, approximating the area under a curve from the sum of subdivided trapezoids, was selected because of its ease of application and increased accuracy over numerical integration methods such as the midpoint method.

$$\int_a^b f(t) dt \approx \frac{\Delta t}{2} [f(t_0) + 2f(t_1) \dots 2f(t_{n-1}) + f(t_n)] \quad \text{Eqn. 3}$$

### *Applications: Zeroeth Temporal Moment*

The zeroeth moment,  $(\mu_0)$ , interpreted as the total mass eluted out of the column in units of length, was first calculated to normalize subsequent moment calculations and to generate a mass balance for eluted solutes from the spike solution. Traditional effluent mass balance calculations are made by comparing the ratio of the total mass eluted ( $M_{out}$ ) over the total mass input ( $M_{in}$ ) into the system.  $M_{in}$  is typically calculated as the spike concentration ( $C_0$ ) multiplied by the volume added and  $M_{out}$  is equivalent to the integral of eluted concentration multiplied by the volumetric flow rate with respect to time (Eqn. 4). Alternative to this approach, the zeroeth moment (Eqn. 5 & 6) in which  $C(t)$  was substituted with  $C/C_0$ , was applied to determine  $M_{out}$ . This formulation operates under the assumption that the volumetric flow rate throughout the experiment is constant. This calculation measures the mass input quantity in units of time instead of mass. Assuming a constant injection flowrate, the mass input measured in time ( $M_{t\_in}$ ) is equal to the spike pulse time ( $t_0$ ) (Eqn. 5). For mass balance calculations, the total mass output in units of time is symbolized by  $M_{t\_out}$  but is noted as  $\mu_0^*$  for

subsequent moment calculations. The moment follows equation 6, where effluent concentrations normalized by the spike concentration ( $C/C_0$ ) are integrated over the breakthrough dataset with respect to time (Eqn. 4). For simplification, normalized concentrations are noted as  $C^*$  (Eqn. 7).

$$M_{out} = \int_0^{\infty} Q C(t) dt \quad [M] \quad \text{Eqn. 4}$$

$$\frac{\bar{Q}_{out}}{\bar{Q}_{in}} = 1 \quad \rightarrow \quad M_{t\_out} = \mu_0^* = \int_0^{\infty} \frac{Q_{out}(t) C(t)}{Q_{in}(t) C_0} dt \quad [T] \quad \text{Eqn. 5}$$

$$\mu_0^* = \int_0^{\infty} C^*(t) dt \quad [T] \quad \text{Eqn. 6}$$

$$C^*(t) = \frac{C(t)}{C_0} \quad [-] \quad \text{Eqn. 7}$$

Effluent mass balances were completed for Br <sup>99</sup>Tc and <sup>237</sup>Np across all experiments by integrating normalized concentrations over time. Normalized concentration ( $C^*$ ), ranging from 0 to 1, is dimensionless. This means that when integrated over time, the total mass out ( $\mu_0^*$ ) is approximated in units of time and corresponds to the pulse duration of the spike. Thus,  $\mu_0^*$  increases to  $t_0$  as the effluent tracer or solute recovery approaches 1. Times at which the pulse started and stopped were recorded with a stopwatch for each experiment. However, considering its role in accurately evaluating the percent recovery,  $t_0$  was verified by initial and final volumetric measurements of the spike solution. By recording the change in spike volume after each experiment and calculating the average volumetric injection flow rate some fraction collected samples, the noted  $t_0$  measurements were verified. In summation, the effluent recovery of each solute was calculated from the ratio of mass output ( $M_{t\_out}$ ), determined by the zeroeth moment, divided by mass input ( $M_{t\_in}$ ), determined volumetrically (Eqn. 8).

$$\% \text{ Recovery} = \frac{M_{t\_out}}{M_{t\_in}} = \frac{\mu_0^*}{t_0} \quad \text{Eqn. 8}$$

### *Applications: First Temporal Moment*

The absolute first moment ( $\mu_1^*$ ), found from integrating the product of  $C/C_0$  and time with respect to time, characterizes the absolute mean arrival time of the solute (Eqn. 11). With units of time squared, the absolute mean arrival time must be normalized by a characteristic time unique to the dataset to acquire a first moment that is meaningful in this analysis. The zeroeth moment, representative of the total mass injected in units of time (Eqn. 6), was used to normalize the first moment (Eqn. 10). The normalized first moment ( $\hat{\mu}_1^*$ ) represents the center of mass of the breakthrough curve or the average travel time of the plume. For breakthrough curves with  $\sim 100\%$  recovery, the recovery is 50% at the mean arrival time.

$$\mu_1^* = \int_0^{\infty} C^*(t)t dt \quad [T^2] \quad \text{Eqn. 9}$$

$$\text{normalized } \mu_1^* = \hat{\mu}_1^* = \frac{\int_0^{\infty} C^*(t)t dt}{\int_0^{\infty} C^*(t)dt} = \frac{M_1}{M_0} \quad [T] \quad \text{Eqn. 10}$$

The normalized first moment, also known as the mean arrival time (MAT), was used to determine the mean travel time (MTT). MTT, equivalent to the retardation factor ( $R$ ) in units of pore volumes, was calculated from the MAT minus the average pulse time of the spike solution (Eqn. 11). MTT values were converted from units of time to units of pore volumes injected by multiplying MTT by the average volumetric flow rate and dividing by the pore volume ( $V_p$ ) (Eqn. 12).  $C/C_0$  should reach a value of 0.5 at the mean travel pore volume (MAPV). The partitioning coefficient ( $K_d$ ) was calculated for each analyte across all planned experiments (Eqn. 13). This value describes the sorption affinity of an analyte to the soil. The partitioning coefficient can be determined by dividing the retardation factor minus one ( $R - 1$ ) by the dry bulk density of the soil ( $\rho_b$ ) and multiplying that by the porosity of the soil ( $\theta$ ). This calculation assumes that retardation in experiments is 100% dependent on equilibrium sorption which does not align

with this study's conceptual model; therefore, the contaminant mobility will be evaluated only by experimentally derive  $R$ .

$$MTT = \hat{\mu}_1^* - 0.5 * t_0 \quad \text{Eqn. 11}$$

$$R = \frac{MTT \cdot \bar{Q}}{V_p} \quad \text{Eqn. 12}$$

$$K_d = \left( \frac{R-1}{\rho b} \right) \theta \quad \text{Eqn. 13}$$

Lastly, this formulation allows for the volume fraction of the soil column to be determined.

Considering the presence of macropores in a soil can separate pore matrix into mobile and immobile regions, solving for this value is of interest. The volume fraction [ $L^3$ ], is used as a direct comparison to pore volume measurements completed experimentally (Eqn. 14).

$$V = \frac{\bar{Q}}{\hat{\mu}_1^*} [L^3] \quad \text{Eqn. 14}$$

#### *Applications: Higher Order Temporal Moments*

The second moment ( $\hat{\sigma}$ ), also known as the variance, describes the spread of the plume about its mean arrival ( $\hat{\mu}_1^*$ ) following equation 15. As the variance value increases, the distribution of concentration away from the mean or spreading increases and acts as an indicator of dispersive transport processes.

$$\hat{\sigma} = \frac{\sigma}{\mu_0^*} = \frac{\int_0^{\infty} (t - \hat{\mu}_1^*)^2 C^*(t) dt}{\mu_0^*} \quad \text{Eqn. 15}$$

The third moment ( $SK$ ) signifies the degree of asymmetry for a breakthrough curve. This quality is termed as skewness; whereas  $SK$  decreases towards zero, the shape of the peak approaches a gaussian distribution. For column flow tests, transport processes such as matrix diffusion and non-equilibrium flow conditions can cause an elution curve to show a longer

extended tail as the last fractions of the tracer or spike elute. The skewness value enables the degree of tailing to be quantified (Eqn. 16).

$$SK = \hat{S}^3 = \frac{S^3}{\mu_0^*} = \frac{\frac{1}{\hat{\sigma}^{3/2}} \int (t - \hat{\mu}_1^*)^3 C^*(t) dt}{\mu_0^*} \quad \text{Eqn. 16}$$

### *Temporal Moments Analysis with Variable Flow Rate*

In this study's experimental setup, constant volumetric flow rates were maintained using peristaltic pumps. Even after proper calibration and maintenance, these pumps can introduce unwanted flow rate variations. A moments analysis formulated to account for changes in flow rate was applied to determine if flow rate observations produced deviating results. Using a similar formulation seen in equations 4 through 16, the general formula follows equation 17, where  $Q$  is the volumetric flow rate,  $C$  is concentration, and  $t^n$  is time to the  $n^{\text{th}}$  power corresponding to the order of the moment calculated. The zeroeth moment, assuming variable flow rates are observed, is described in equation 4. The residence time distribution curve, calculated by the function  $E(t)$ , can be defined by *equation 18*, where it represents the fraction of the tracer passing through the outlet at a given time. This function is used to solve for the first temporal moment (Eqn. 18 & 19) and normalizes the data by the total mass recovered, analogous to the purpose of equation 11. Retardation factors were recalculated using this formulation and compared with values generated to evaluate error introduced by volumetric flow rate variations.

$$\mu_n = \int_0^\infty Q C t^n dt = \sum Q C t^n \Delta t \quad \text{Eqn. 17}$$

$$E(t) = \frac{C_{out}(t)Q}{\int_0^\infty C_{out}(t)Q dt} \quad [T^{-1}] \quad \text{Eqn. 18}$$

$$\hat{\mu}_1 = \int_0^\infty tE(t) dt \quad [T] \quad \text{Eqn. 19}$$

### 3.4 Modeling

#### *Two-region Nonequilibrium Convection-Dispersion Model (MIM)*

Many deterministic and stochastic modeling approaches have been successfully applied to simulate solute transport in heterogeneous soils (Dagan and Cvetkovic, 1993; Kabala, 1991; Ababou, 1991). Traditionally, the flow regime of unsaturated and homogenous systems has been well described by Richard's equation and chemical transport by the convection-dispersion equation (CDE) (Richards, 1931; Massabó, 2011). However, flow and transport in heterogeneous soils presents anomalous trends that these approaches have failed to describe. As stated in chapter one, macropore structures in soils can produce preferential flow paths for infiltrating water, effectively bypassing the micropore matrix; however, studies suggest this activity is dependent on saturation and macropore orientation (Brouyère, 2006; Mamun, 2022). This anomalous behavior is indicative of nonequilibrium flow and transport. Van Genuchten and Wagenet (1989) derived an altered CDE that is able to simulate anomalous behavior better than the traditional CDE (Padilla, 1999). The two-region nonequilibrium CDE (MIM) assumes that only a fraction of the liquid phase is mobile in heterogeneous soils. By separating the model domain into mobile and immobile regions, solute transport can be cumulatively described by convective-dispersive (matrix flow) and the rate of exchange between mobile and immobile regions. With a dual porosity-like formulation, the MIM model has been proven to describe equilibrium and nonequilibrium solute transport at field and lab scales (Padilla et al., 1999; Brouyère, 2006; Blackmore et al., 2014).

In the dimensionless form (Eqn. 4 & 5), MIM can be applied to describe physical or chemical nonequilibrium transport. Applications for chemical nonequilibrium adsorption utilize



the “two-site” formulation where, as physical nonequilibrium is described by the two-region formulation (van Genuchten and Wagenet, 1989; Nkedi-Kizza, 1984).

$$\beta R \frac{\partial C_1}{\partial T} = \frac{1}{P} \frac{\partial^2 C_1}{\partial Z^2} - \frac{\partial C_1}{\partial Z} - \omega(C_1 - C_2) - \mu_1 C_1 + \gamma(z) \quad \text{Eqn. 20}$$

$$(1 - \beta)R \frac{\partial C_2}{\partial T} = \omega(C_1 - C_2) - \mu_2 C_2 + \gamma(z) \quad \text{Eqn. 21}$$

The dimensionless terms are presented as,  $\beta$ ,  $R$ ,  $C$ ,  $T$ ,  $P$ ,  $Z$ ,  $\omega$ ,  $\mu$ , and  $\gamma$ . Utilizing the two-region model, subscripts 1 and 2 are indicative of equilibrium (flow) and non-equilibrium liquid regions.  $\beta$  represents the fraction of mobile water in the continuum. By setting  $\beta = 1$ , solute transport is defined only by equilibrium processes where Eqn. 5 is voided, and effectively, the MIM model is restored to the traditional CDE. The peclet number,  $P$ , is defined as the ratio between the mobile liquid velocity ( $v_m$ ) multiplied by a characteristic length ( $L =$  column height) and the dispersion coefficient ( $D_m$ ) (Eqn. 7). The peclet number is interpreted as an indicator of whether advective ( $P \gg 1$ ) or dispersive ( $P \ll 1$ ) transport processes are dominant.

$$P = \frac{v_m L}{D_m} = \frac{vL}{D} \quad \text{Eqn. 22}$$

The mass transfer coefficient,  $\omega$ , governs the rate of exchange between mobile and immobile regions. This term is translated to its dimensional form from the relationship seen in Eqn. 8, where alpha,  $\alpha$ , is the dimensional mass transfer coefficient.

$$\omega = \frac{\alpha L}{\theta v} \quad \text{Eqn. 23}$$

Where  $\mu$ , is the degradation coefficient, and  $\gamma$  is the zeroth order production term for mobile and mobile phases. Within the experimental scope of this study, it was assumed that both degradation and production terms are negligible. Dimensionless time ( $T$ ), concentration ( $C$ ), and distance ( $Z$ ) are respectively defined in equations 24, 25, & 26.

$$T = \frac{vt}{L} \quad (\text{Eqn. 24})$$

$$C = \frac{C_m}{C_0} \quad (\text{Eqn. 25})$$

$$Z = \frac{x}{L} \quad (\text{Eqn. 26})$$

As described by Toride (1993), the two-region nonequilibrium CDE is written in its dimensional form in Eqn. 27 & 28.

$$\begin{aligned} & (\theta_m + f\rho_b k_d) \frac{\partial C_m}{\partial t} \\ &= \theta_m \frac{\partial}{\partial x} \left[ D_m(x) \frac{\partial C_m}{\partial x} \right] - v_m \theta_m \frac{\partial C_m}{\partial x} - \alpha(C_m - C_{im}) \\ & - (\theta_m \mu_{im} + f\rho_b k_d \mu_{s,m}) C_m \end{aligned}$$

Eqn. 27

$$[\theta_{im} + (1-f)\rho_b k_d] \frac{\partial C_{im}}{\partial t} = \alpha(C_m - C_{im}) - [\theta_m \mu_{l,im} + (1-f)\rho_b k_d \mu_{s,im}] C_{im}$$

Eqn. 28

### *Application of the CXTFIT model*

The excel based model, *CXTFIT*, solves the dimensionless MIM equations to simulate the one-dimensional nonequilibrium transport of reactive and nonreactive solutes. *CXTFIT* is predominantly designed to predict or fit breakthrough data from column tracer experiments. Key advantages of this open-sourced code are its accessibility, readiness for modification and its capability of solving both direct and inverse solutions for parameterization and prediction.

Within the *CXTFIT* program file, many user-designed functions are written in VBA code to predict and analyze column flow tracer experiments. The MIM function initiates the analytical solution for the nonequilibrium CDE which is further detailed by Eqn. 3.20 - 3.22 in Toride's *CXTFIT Manual V2.0* (1995). The setup of *CXTFIT* incorporates input parameter cells for dispersivity ( $\lambda$  [cm]), mobile water fraction ( $\beta$  [-]), mass transfer coefficient ( $\omega$  [-]), and

retardation factor ( $R$  [-]), column length ( $L$ ), average pore water velocity (cm/day), and pulse duration ( $T_0$ ) (Figure 6). Approximate values for  $\lambda$ ,  $\beta$ , and  $\omega$  were initially assigned to fit experimental breakthrough curves. However, parameterization accuracy and efficiency was improved by using a nonlinear least squares optimization code where parameters were iteratively evaluated with the objective of minimizing the regression sum of squares (SSR) (Eqn. 14). Experimentally measured parameters such as column length ( $L$  [cm]), average velocity ( $v$  [cm/d]), and pulse duration ( $T_0$  [-]) remained fixed during parameter optimization. Additionally, statistical values such as the coefficient of determination ( $r^2$ ) and root squared mean error (RMSE) were calculated to evaluate the model fit accuracy (Eqn. 30 & 31).

$$SSR = \sum_{i=1}^N (C_i - f_i)^2 \quad \text{Eqn. 29}$$

$$r^2 = 1 - \frac{SSR}{\sum_{i=1}^N (C_i - \bar{C})^2} \quad \text{Eqn. 30}$$

$$RMSE = \sqrt{\frac{\sum_{i=1}^N (C_i - f_i)^2}{N}} \quad \text{Eqn. 31}$$

Equations 14, 15, and 16 were applied so that the measured or normalized ( $C/C_0$ ) effluent concentration were noted by  $C_i$ , predicted concentrations as  $f_i$ , the total number of data points as  $N$ , and the mean observed concentrations as  $\bar{C}$ .

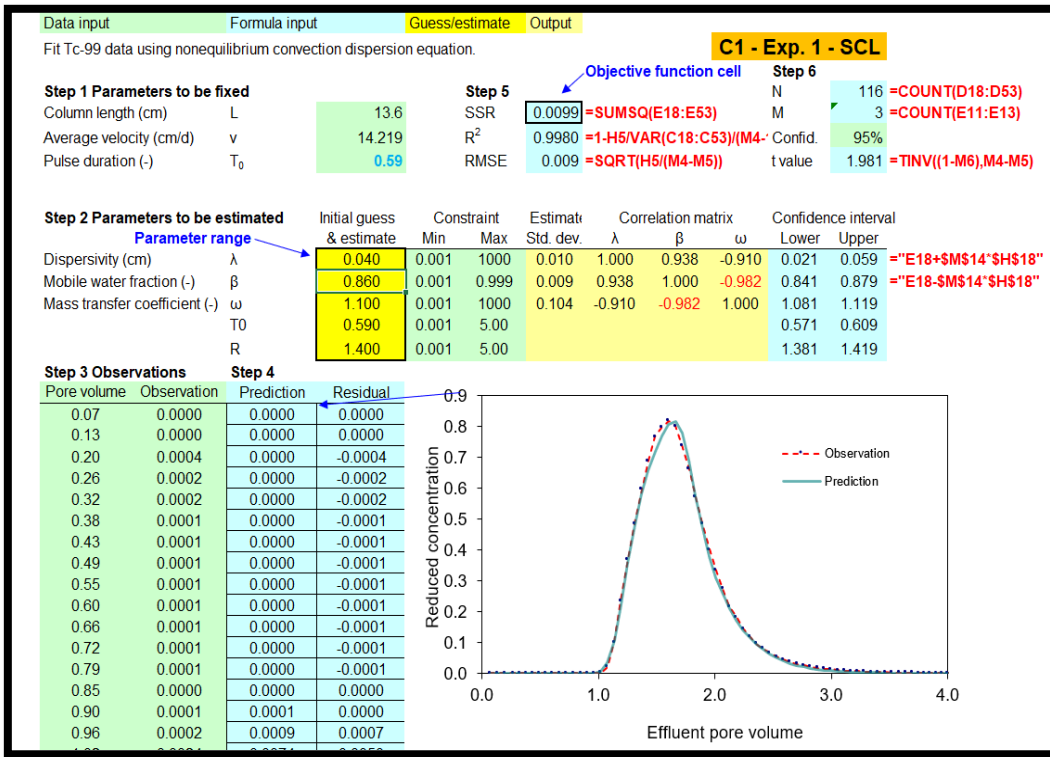


Figure 6 Parameter estimation template used by Excel based CXTFIT program

## CHAPTER 4: RESULTS

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### 4.1 Pore-scale Imaging

Both vertical and horizontally oriented macropores were observed in all three wet-dry cycled SCL columns. Notably, imaging of column *SCL\_M\_2* revealed a vertical macropore structure extending from  $\sim 2$  to 13 cm depth with a maximum diameter of  $\sim 1.5$  mm (Figure 8). Connectivity of this structure throughout its  $\sim 12$  cm length was proven to be continuous and meandering by examination of cross-sectional CT images through the Z axis (increasing sediment column depth) (Figure 9). No macropores were observed in wet-dry cycled sand columns (Figure 7). CT scans taken of SCL columns pre-wet dry cycling showed a homogeneous structure, confirming that packing methods did not induce the alterations observed post-exposure to a wet-drying event (Appendix, Figure 21-24).

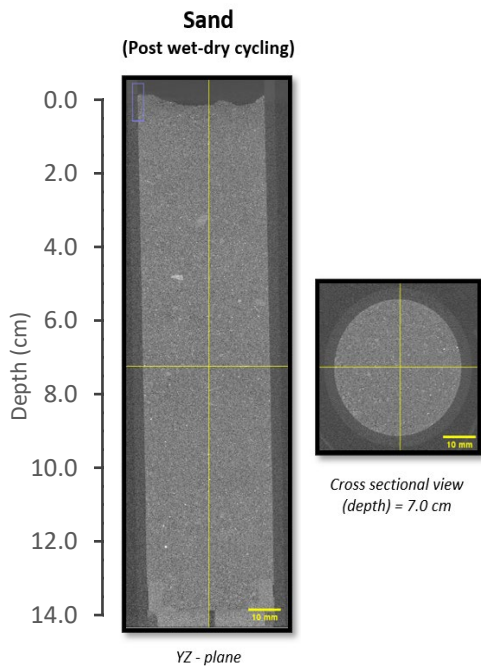


Figure 7 YZ and XY orthogonal views of *SCL\_M\_2* taken from CT imaging post wet-drying

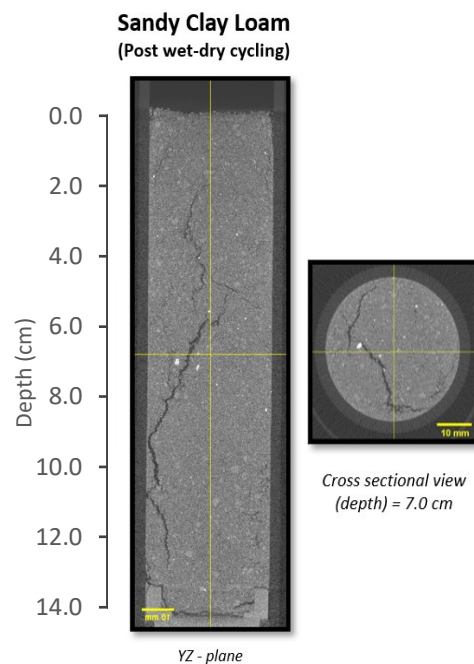


Figure 8 YZ and XY orthogonal views of *S\_M\_2* taken from CT imaging post wet-dry cycling

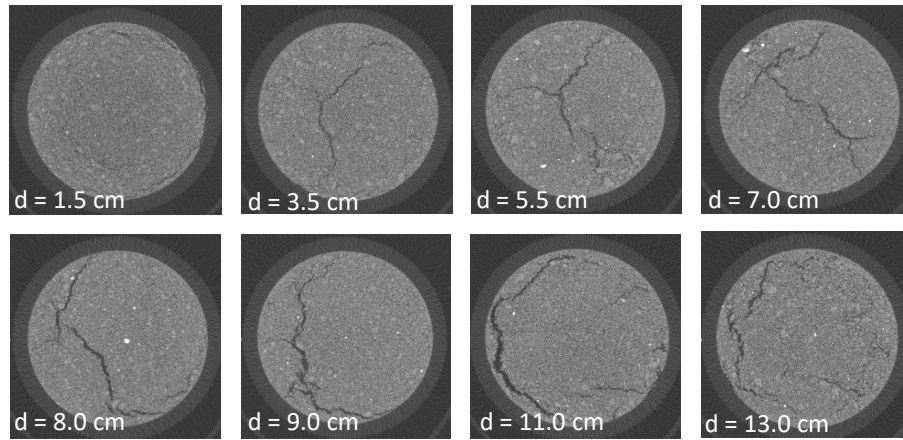


Figure 9 CT images showing cross sectional views (XY plane) of column *SCL\_M\_2* increasing in depth (Z plane) from top left to top right. Scans show the connectivity of the vertical macropore network throughout the column

The *SCL\_M\_2* macropore network begins at an approximate depth of 2 cm where three symmetrical fractures converge (Figure 9). Increasing to a depth of 7 cm, the convergent cracks propagate vertically and form a “T” shaped fracture (in cross-section). The cracks then conform into a single fracture (d = 8 cm) that meanders towards the inner wall of the column. The fracture then closes at a depth of 13 cm as it approaches the column plug. Consistent with *SCL\_M\_2* imaging, the orientation of macropores in *SCL\_M\_1* and *SCL\_M\_3* were predominantly vertical and connected through the column.

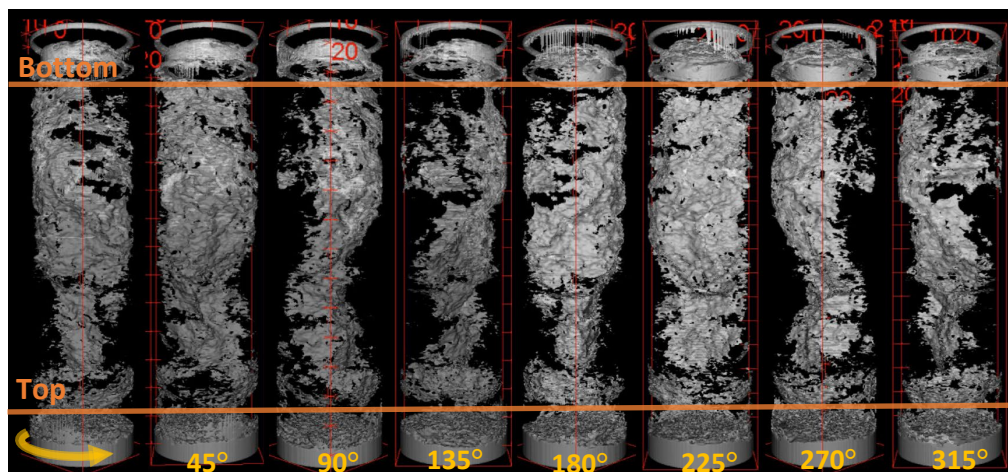


Figure 10 Three-dimensional reconstruction of macropore network in *SCL\_M\_2* (generated from CT imaging). Clockwise rotating views shown every 45°. Orange lines delineate macropore network (middle) from column apparatus (top and bottom)

## 4.2 Column Flow Experiments in Homogeneous Soils

### *Br and <sup>99</sup>Tc Breakthroughs in Homogeneous Soils*

A preliminary unsaturated column flow experiment was completed to compare Br (a conservative tracer), <sup>99</sup>Tc, and <sup>237</sup>Np breakthroughs in columns packed homogeneously with SCL and sand sediment. During these experiments, no ponding occurred. In both column flow experiments (*SCL\_H\_1* and *S\_H\_1*), Br and <sup>99</sup>Tc breakthrough curves showed the similar shape and mean arrival times (MAT) respective to soil type (Figure 11). Br and <sup>99</sup>Tc mean arrival pore volumes (MAPV), calculated from the normalized first temporal moment (Eqn. 10, 11), were 1.63 and 1.61 for column experiment *SCL\_H\_1* and 1.43 and 1.46 for *S\_H\_1* (Table 5.1). Mean travel pore volume (MTPV) estimates for Br and <sup>99</sup>Tc, equivalent to the retardation factor (R), were 1.33 and 1.30 for *SCL\_H\_1* and 1.07 and 1.08 for *S\_H\_1*. The remaining <sup>99</sup>Tc sorbed to SCL and sand-packed columns after column flow experiments were found to be at analytically insignificant concentrations.

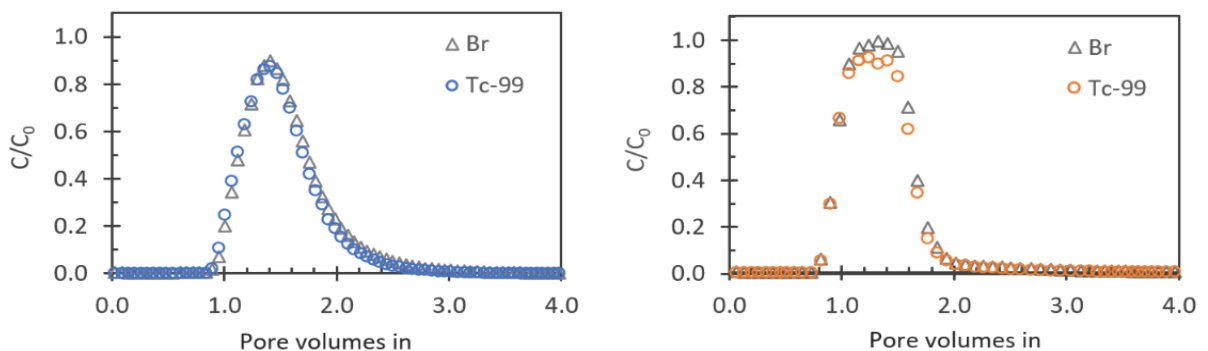


Figure 11 Br and <sup>99</sup>Tc breakthrough curves from columns *SCL\_H\_1* (Left) and *S\_H\_1* (Right) plotted as normalized concentration ( $C/C_0$ ) vs. pore volumes added during column flow testing

### Neptunium-237 Sorption and Breakthrough in Homogeneous Soils

Analysis of SCL soil and effluent samples from experiment *SCL\_H\_1* indicated 99% of the recovered  $^{237}\text{Np}$  remained adsorbed to SCL soil after the experiment. In total, 7.6 pore volumes of water were flushed through the *SCL\_H\_1* column. Approximately 75% of the  $^{237}\text{Np}$  in the SRS soil resided at depths between 2 – 6 cm (Figure 12). With a mean travel distance (MTD) of 4.6 cm,  $^{237}\text{Np}$  travel velocity was calculated to be  $1.6 \text{ cm d}^{-1}$  (Table 5.4).

In experiment *S\_H\_1*, the column was homogeneously packed with sand. After flushing *S\_H\_1* with  $\sim 9$  pore volumes of water, only 21% of the  $^{237}\text{Np}$  injected remained adsorbed to the soil in the bottom 4 cm of the column. Sorbed  $^{237}\text{Np}$  concentrations increased with depth to a maximum of  $1.6 \text{ ng g}^{-1}$  (Figure 12). Correspondingly, the  $^{237}\text{Np}$  effluent pulse had a mean arrival time (MAT<sub>n</sub>) of 2088 minutes (5.1 pv) and trended with a non-uniform profile and long tail that extended to the final time point (Figure 13).

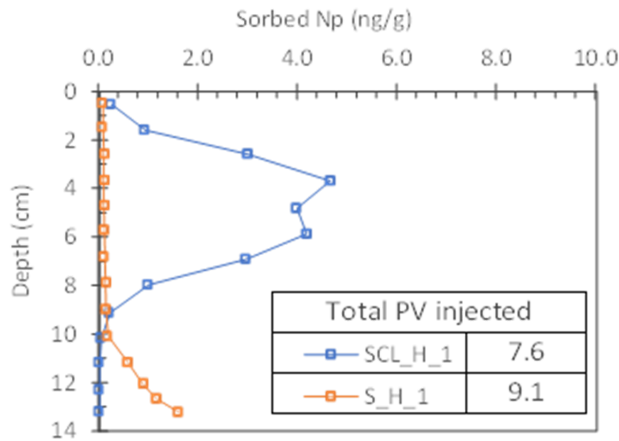


Figure 12 Sorbed  $^{237}\text{Np}$  ( $\text{ng g}^{-1}$ ) soil distributions from homogeneous SCL and sand experiments (*SCL\_H\_1*, *S\_H\_1*). Total number of pore volumes flushed through the column during respective experiments seen in table above.

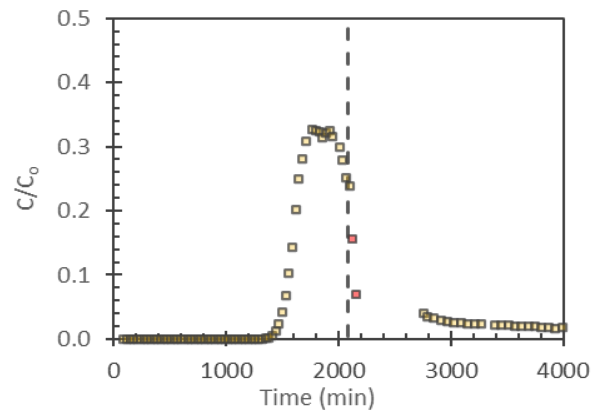


Figure 13  $^{237}\text{Np}$  elution curve from experiment *S\_H\_1* plotted as normalized concentration ( $C/C_0$ ) vs. elapsed time (min). Data points marked in red indicate compromised effluent samples. Loss of effluent samples occurred from 2200 through 3700 minutes



### 4.3 Column Flow Experiments in Wet-dry Cycled Soils

Column flow experiments completed on wet-dry cycled columns packed with sand or sandy clay loam soils were conducted in experiments  $M_1 - 3$ . Discussed further in *Ch. 4 Sect. 1*, macropores were visible in CT scans of columns  $SCL\_M_1-3$  post-wet-dry cycling but not in sand columns  $S\_M_1 - 3$ . For  $M_1$  column flow experiments, the average water content directly before the spike addition was  $\sim 0.1$ , while experiments  $M_2$  and  $M_3$  were initiated with an initial water content of  $\sim 0.25$ .

#### *99-Techneceium Breakthrough in Wet-Dry Cycled soils*

MAPV calculations for  $^{99}\text{Tc}$  in SCL experiments  $M_1, M_2,$  and  $M_3$  were 1.74, 1.73, and 1.66, while MAPV values in corresponding sand experiments were 1.45, 1.60, and 1.49 (Table 5.1). The total number of pore volumes flushed through each column ranged from 7.6 – 6.8 in SCL and 9.1 to 7.0 in sand (Table 5.4). Coinciding with results in homogeneous soils,  $^{99}\text{Tc}$  was not found sorbed to sand or sandy clay loam sediments analyzed after column flow experiments.

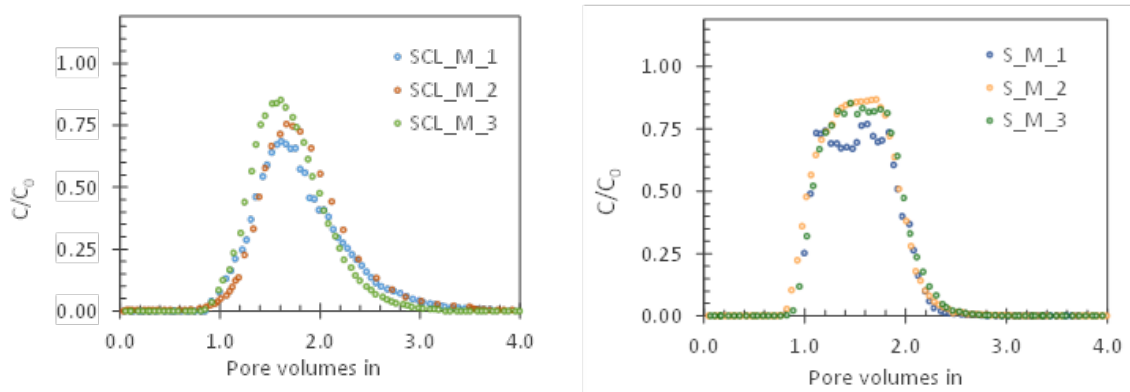


Figure 14  $C/C_0$  ( $^{99}\text{Tc}$ ) plotted against pore volumes injected during unsaturated column flow experiments on sandy clay loam (left) and sand (right) sediments varying in heterogeneity

## Neptunium-237 Sorption in Wet-Dry Cycled Soils

$^{237}\text{Np}$  was not detected at analytically significant concentrations in effluent samples across all macropore experiments. In SCL experiments  $M_1$  and  $M_3$ , mean travel distances (MTD) were 2.6 and 2.0 cm, with resulting contaminant velocities ( $v_c$ ) of 1.0 and 0.8  $\text{cm d}^{-1}$  (Table 5.4). Contaminant velocities  $^{237}\text{Np}$  were determined by dividing the mean travel distance (MTD) by the total elapsed time during the column flow experiment. In corresponding sand experiments ( $S_M_1$  and  $S_M_3$ ),  $^{237}\text{Np}$  MTD values were 1.2 and 2.3 cm. Resulting  $v_c$  values were 0.5 and 1.0  $\text{cm d}^{-1}$ .

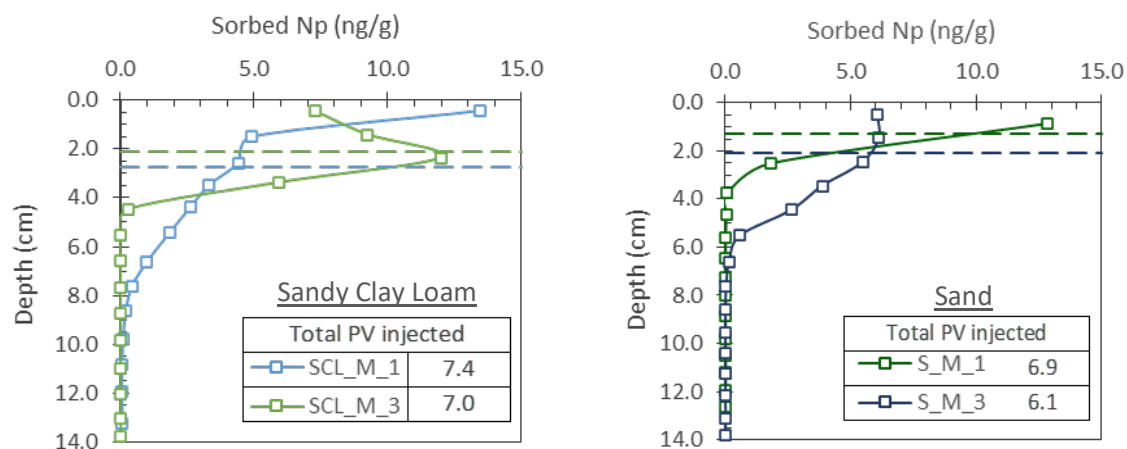


Figure 15 Sediment  $^{237}\text{Np}$  concentration ( $\text{ng g}^{-1}$ ) profiles acquired by sectioning experimental sediment columns.  $^{237}\text{Np}$  migration relative to the total number of pore volumes flushed through the column (see legend). Dashed lines indicate the mean travel distance (MTD) for respective experiments

### 4.4 Effluent pH

The pH of the spike solution in the preliminary column flow experiment ( $SCL_H_1$  and  $S_H_1$ ) was 3.0. Resulting effluent pH values for  $SCL_H_1$  were averaged at 4.8 while  $S_H_1$  effluent pH averaged at 5.1. Over the duration of experiment 1, the pH of  $SCL_H_1$  effluent exponentially dropped from 7.3 to 4.4 over the first 17 hours (2.1 PV) (Figure 16). Effluent pH for  $SCL_H_1$  remained stable at 4.5 for the final  $\sim 4$  pore volumes. The pH of  $S_H_1$  effluent

remained stable at  $\sim 6.1$  for the first 10 hours (2.3 pv) of the experiment. Over the following 1.7 pore volumes (pv), pH dropped steadily from 6.5 to 4.5, where it remained stable.

The spike solution used in experiment  $M_1-3$  measured to a pH of 5.6. The overall trend of effluent pH measurements taken throughout macropore experiments was consistent respective to soil type. For sand-packed columns ( $S_M_1-3$ ), pH measurements remain consistent at  $\sim 6.1$  from 0 to 4 PV, then decrease at an average rate of 0.3 pH per pv for the remainder of the experiment (Figure 16).

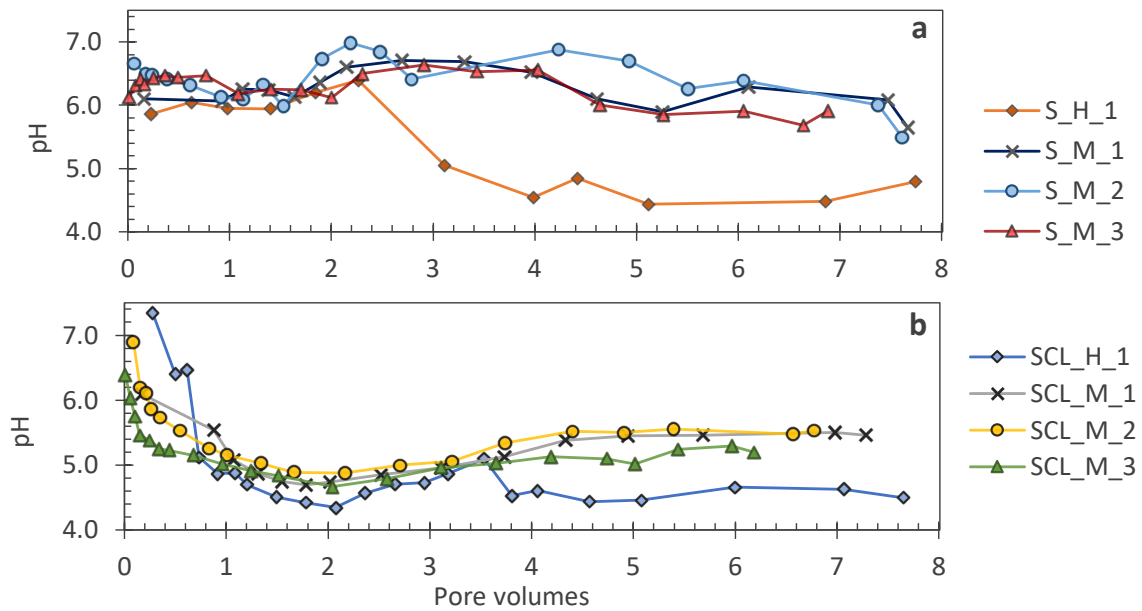


Figure 16 Effluent pH measurements taken from sand (16a) and SCL (16b) column flow experiments plotted

## 4.5 Flowrate

Across all column flow experimental datasets, flow rate measurements varied with standard deviations ranging from 8E-3 to 2E-2 mL min<sup>-1</sup> (RSD = 7 to 18%). Notably, recorded effluent flow rates for *SCL\_M\_2* and *S\_M\_2* dropped from ~ 0.09 to ~ 0.06 mL min<sup>-1</sup> and remained stable at that minimum rate for a span of 660 minutes (540 to 1200 min). (Appendix, Figure 25). With a mean flow rate ( $\bar{Q}$ ) of 0.085 and 0.089 mL min<sup>-1</sup> for *SCL\_M\_2* and *S\_M\_2*, deviations increased the RSD to 18.9% and 18.2%, respectively (Table 4.1). Flowrate deviations are suspected to be caused by improper potentiometer settings of the peristaltic pump. Flowrate deviations for all experiments except for *SCL\_M\_1*, *S\_M\_1* and *S\_H\_1* were less than 13% (Table 4.1).

Table 4.4 Column Flow Experiments: Flow Rate Variability

Column ID	$\bar{Q}$ , <sup>a</sup> mL min <sup>-1</sup>	$\bar{Q}_{inj}$ , <sup>b</sup> mL min <sup>-1</sup>	SD <sub>Q</sub> , <sup>c</sup> mL min <sup>-1</sup>	RSD <sub>Q</sub> , <sup>d</sup> %
<u>Homogenous</u>				
SCL_H_1	1.1 x 10 <sup>-1</sup>	1.2E-01	0.8E-2	7.2
S_H_1	1.1E-01	9.6E-02	1.7E-2	15.9
<u>Wet-dry cycled</u>				
SCL_M_1	9.3E-02	8.4E-02	1.2E-2	12.6
SCL_M_2	8.5E-02	8.9E-02	1.6E-2	18.9
SCL_M_3	9.5E-02	9.5E-02	0.6E-2	6.5
S_M_1	9.3E-02	8.8E-02	1.1E-2	11.9
S_M_2	8.9E-02	9.5E-02	1.6E-2	18.2
S_M_3	9.8E-02	9.0E-02	0.8E-2	8.5

<sup>a</sup> Average volumetric flowrate ( $\bar{Q}$ ) calculated by the arithmetic mean of  $Q(t)$  from  $t_0$  to  $t_f$ . For each experimental dataset,  $Q(t)$  was determined volumetrically from fraction collected effluent samples

<sup>b</sup> Average volumetric flowrate during spike injection

<sup>c</sup> Volumetric flowrate variance about the mean flowrate ( $\bar{Q}$ )

<sup>d</sup> Percent standard deviation determined relative to the mean volumetric flowrate (RSD =  $\frac{SD}{\bar{Q}} * 100$ )

## 4.6 Mass Balances

Bromide and  $^{99}\text{Tc}$  recoveries were determined by comparing  $M_{t_{out}}$ , the mass output calculated as  $\int \frac{c}{c_0} dt [t]$ , to  $M_{t_{in}}$ , equivalent to the pulse duration in units of time. This analysis evaluates the mass balance in units of time under the assumption that flowrates remained constant during the injection of the spike. Further explanation of this analysis is provided in *Ch. 3 sect. 3.3*. Recoveries of  $^{99}\text{Tc}$  ranged between 88% to 108% across all experiments (Table 4.2).  $^{237}\text{Np}$  recoveries, calculated directly from sorbed concentrations, ranged from 87% to 98% in SCL experiments and 74% to 77% in sand.

Table 4.5 Measured Experimental Parameters and Effluent Mass Balance

Column ID	$V_{\text{pore}}$ mL	$T_0$ -	<u>Mass in</u> <sup>a</sup>		<u>Mass out</u> <sup>b</sup>		<u>Recovery</u> <sup>c</sup>	
			$M_{t_{in}}$ min		$M_{t_{out}}$ min		%	
			Br	$^{99}\text{Tc}$	Br	$^{99}\text{Tc}$	Br	$^{99}\text{Tc}$
<u>Homogeneous</u>								
SCL_H_1	57.1	0.62	354.1	354.1	351.1	347.0	99	102
S_H_1	47.5	0.77	310.1	310.1	292.6	284.5	94	93
<u>Wet-dry cycled</u>								
SCL_M_1	50.0	0.78	-	405.5	-	396.0	-	98
SCL_M_2	53.5	0.80	-	481.3	-	517.6	-	108
SCL_M_3	53.9	0.80	-	462.0	-	416.0	-	90
S_M_1	46.5	0.93	-	405.0	-	420.5	-	104
S_M_2	49.2	0.87	-	504.4	-	535.3	-	106
S_M_3	49.3	0.85	-	462.0	-	405.3	-	88

<sup>a</sup> Mass injected determined from initial spike concentrations and measured volumetric flow rates.

<sup>b</sup> Total mass recovered from effluent in units of time ( $M_{t_{out}} = \mu_0 = \int \frac{c}{c_0} dt [T]$ ) where effluent concentrations, normalized by the spike concentration, are integrated with respect to time.

<sup>c</sup> Recovery calculated by dividing the mass output, measured in units of time, by  $t_0$ , the mass input equivalence ( $\text{Recovery} = M_{t_{out}} * M_{t_{in}}^{-1} = \int \frac{c}{c_0} dt * t_0^{-1}$ )

## CHAPTER 5: DISCUSSION

### 5.1 Impacts of Macropores on Tc-99 Transport

#### *Mean Arrival*

Results from this study show that macropore structure present in sandy clay loam soils had no statistically significant impact on the mean arrival of <sup>99</sup>Tc in unsaturated flow conditions. <sup>99</sup>Tc retardation factors were 1.30 in homogeneous SCL and ranged between 1.28 and 1.41 in SCL experiments with macropores. The initial breakthrough pore volumes (IBPV), the pore volume injected at which 1% of the solute has eluted, slightly decreased in both SCL and sand experiments for <sup>99</sup>Tc. The IBPV was 1.08 in homogeneous SCL and ranged between 0.92 and 1.0 in SCL experiments with macropores (Table 5.1). This indicates that shorter flow paths may be more active in macroporous soils but further experimentation with more accuracy is needed to

Table 5.6 Temporal Moments Analysis of Br and <sup>99</sup>Tc Breakthrough Data

Column ID	MAT <sub>n</sub> , <sup>a</sup>		MAPV, <sup>b</sup>		MTT, <sup>c</sup>		MTPV, <sup>d</sup>		IBPV <sup>e</sup>
	min		-		min		-		-
	Br	<sup>99</sup> Tc	Br	<sup>99</sup> Tc	Br	<sup>99</sup> Tc	Br	<sup>99</sup> Tc	<sup>99</sup> Tc
Homogeneous									
SCL_H_1	883.3	862.9	1.63	1.61	717.8	697.4	1.33	1.30	1.08
S_H_1	652.9	628.6	1.43	1.46	487.2	476.3	1.07	1.08	0.95
Wet-dry cycled									
SCL_M_1	-	935.0	-	1.73	-	730.5	-	1.35	0.92
SCL_M_2	-	1164.1	-	1.74	-	1006.3	-	1.41	0.94
SCL_M_3	-	1005.6	-	1.66	-	775.3	-	1.28	1.0
S_M_1	-	726.8	-	1.45	-	522.3	-	1.04	-
S_M_2	-	909.7	-	1.60	-	632.2	-	1.12	0.85
S_M_3	-	811.2	-	1.49	-	580.2	-	1.07	0.88

<sup>a</sup> Normalized mean arrival time ( $MAT_n$ ), or mean residence time ( $t_m$ ), representing the time corresponding to a breakthrough curve's center of mass ( $MAT = \mu'_1 = \frac{\mu_1}{\mu_0}$ ;  $\mu_1 = \int \frac{C}{C_0} t dt$ ;  $\mu_0 = \int \frac{C}{C_0} dt$ )

<sup>b</sup> Mean arrival pore volume ( $MAPV$ ), converted from  $MAT_n$ , with the average volumetric flow rate ( $\bar{Q}$ ) and pore volume measurements ( $MAPV = MAT_n * \bar{Q} * V_{pore}^{-1}$ )

<sup>c</sup> Mean travel time ( $MTT$ ) calculated from the  $MAT_n$  minus the average injection time ( $MTT = MAT - 0.5 * t_0$ )

<sup>d</sup> Mean travel pore volume, equivalent to retardation factor ( $R$ ), converted from  $MTT$  to units of pore vol. inj.

<sup>e</sup> Initial breakthrough pore volume defined as the # of pore volumes inj. corresponding to elution of 1% of the solute

make this claim. Macropores were not observed in sand packed columns post wet-dry cycling; thus, definitive conclusions relating macropore structures and  $^{99}\text{Tc}$  mobility in sand cannot be made. However,  $^{99}\text{Tc}$  retardation factors were consistent across homogeneous sand and wet-dry cycled sand experiments and IBV also decreased in sand columns exposed to a wet-drying event (Table 5.1).

### *Mobile Water Fraction*

Macropore structures in SCL soils showed no statistically significant impacts for MIM estimated mobile water fractions ( $\beta$ ). The mobile water fraction parameter accounts for the stratification of a soil matrix into mobile and stagnant fluid regions (conditions of non-equilibrium). In this model, transport is governed by the convection dispersion equation in mobile regions and by the rate of exchange between regions (mass transfer coefficient) in immobile regions. The mobile water fraction term controls the degree to which transport is partitioned by either equilibrium or non-equilibrium transport processes. It assumes that when  $\beta = 1$  the CDE is restored and if  $\beta$  drops below 1, nonequilibrium conditions are introduced.

Mobile water fractions estimated from  $^{99}\text{Tc}$  breakthrough were  $0.90 \pm 0.02$  and  $0.92 \pm 0.03$  in homogeneous SCL and sand experiments (Table 5.3). CDE ( $\beta = 1$ ,  $\lambda = 0.15$  cm,  $R = 1.4$ ) describes  $^{99}\text{Tc}$  breakthrough for *SCL\_H\_1* with a best fit  $R^2$  of 0.968; however, MIM predictions ( $\beta = 0.90$ ,  $\lambda = 0.08$  cm,  $\omega = 0.65$ ,  $R = 1.41$ ) fit  $^{99}\text{Tc}$  breakthrough with an  $R^2$  of 0.997 (Figure 17). Based on  $R^2$  fit estimates, better curve fitting was acquired with MIM for all sand experiments as well. These results suggest that in homogeneously packed SCL and sand, unsaturated flow conditions reduce the number of flow paths and induce nonequilibrium flow and transport, supporting claims by Padilla (1999).

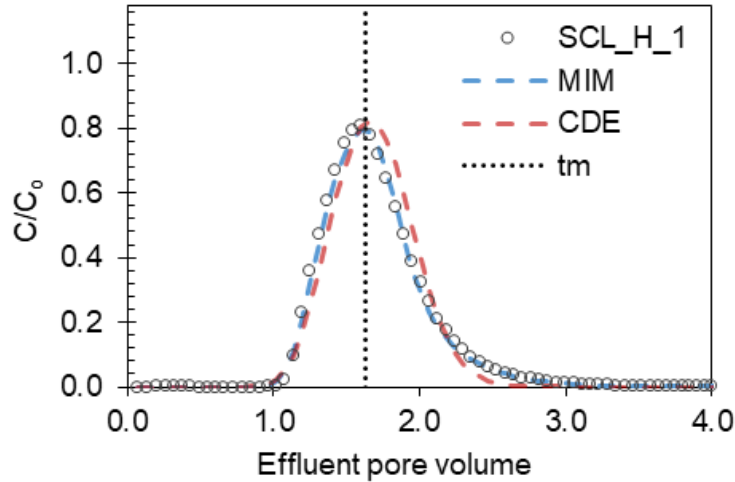


Figure 17 Comparison of CDE and MIM best fits to SCL\_H\_1 <sup>99</sup>Tc breakthrough plotted as C/C<sub>0</sub> vs. effluent pore volumes. (CDE R<sup>2</sup> = 0.968, MIM R<sup>2</sup> = 0.997)

### *Dispersivity*

Although <sup>99</sup>Tc mean arrivals were not significantly impacted, dispersivity ( $\lambda$ ) in wet-dry cycled SCL and sand soils increased relative to breakthrough curves in respective homogeneous soils (Figure 18). Dispersivity, estimated with the nonequilibrium convection-dispersion equation (MIM), were fit to experimental data with R<sup>2</sup> values ranging from 0.933 to 0.997. MIM estimates of <sup>99</sup>Tc dispersivity in homogeneous SCL were  $0.08 \pm 0.02$  cm while dispersivity for macroporous SCL experiments *M\_1*, *M\_2*, and *M\_3* were  $0.26 \pm 0.1$ ,  $0.19 \pm 0.04$ , and  $0.21 \pm 0.05$  cm (Table 5.3). Variance, the second temporal moment indicative of plume spread, also increased in all wet-dry cycled SCL and sand flow experiments relative to homogeneous experiments (Figure 19).

MIM best fits of  $\lambda$  for <sup>99</sup>Tc in sand showed no statistically significant deviations in wet-dry cycled experiments. However, variance, determined via temporal moments analysis, increased from homogeneous sand to wet-dry cycled sand experiments (Table 5.2).



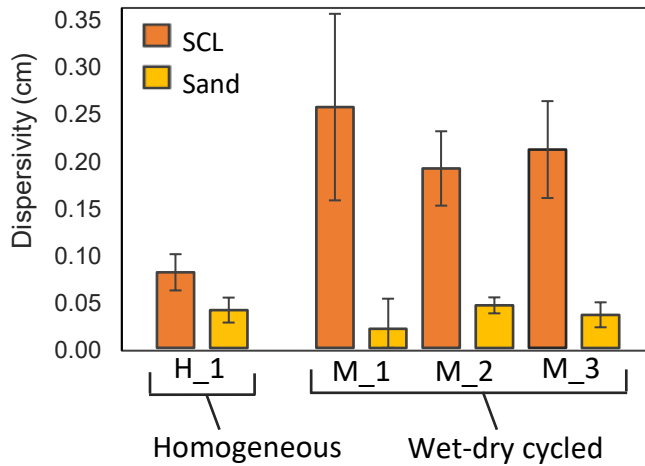


Figure 18 Comparison of  $^{99}\text{Tc}$  dispersivities in homogeneous ( $H_1$ ) and wet-dry cycled ( $M_1 - 3$ ) SCL and sand. Dispersivity determined from MIM best fits for unsaturated SCL and sand column flow experiments.

Increases in dispersivity of  $^{99}\text{Tc}$  in macroporous SCL soils are attributed to increased fluid mixing during transport and capillary exclusion. Effectively, solute mixing in porous media is controlled by travel distances, tortuosity, and spatial variations in flow velocity. Unsaturated fractures throughout the matrix act as capillary barriers, either isolating transport to subsections of the matrix (vertical macropores) or blocking flow and infiltration (horizontal macropores). Column flow studies conducted in homogeneous soils by Padilla (1999) suggest that in unsaturated conditions, dispersivity is indirectly proportional to water content. Padilla asserts that as water content decreases below saturation, the number of flow paths decrease and pore-water velocity variations increase, effectively increasing solute dispersivity. In this study, breakthrough curves indicate that increases in  $^{99}\text{Tc}$  dispersivity are related to analogous processes (velocity variations and tortuosity) but is induced by increasing macroporosity.

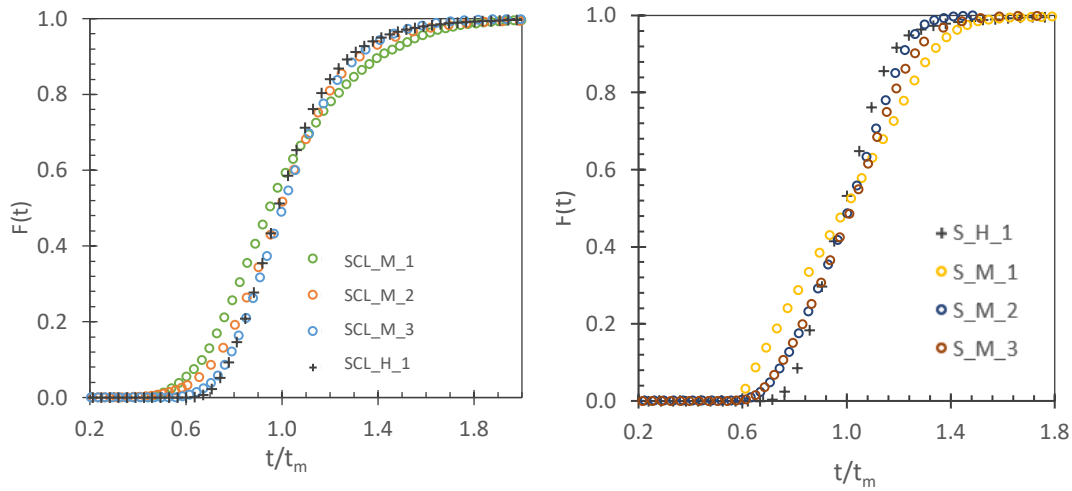


Figure 19  $^{99}\text{Tc}$  cumulative distribution curves ( $F(t)$ ) plotted vs. dimensionless time for column flow experiments in homogeneous and wet-dry cycled soils.  $F(t) = \int E(t) dt$  and  $T = t/t_m$  where  $t$  is time and  $t_m$  is the first temporal moment (solute mean arrival time)

Table 5.7 Temporal Moments with Variable Flowrate

Temporal Moments (Br and Tc-99)				
ID	1 <sup>st</sup> moment <sup>a</sup> , $t_m$		Variance <sup>b</sup> , $\sigma$	Skewness <sup>c</sup> , $SK$
	Br	$^{99}\text{Tc}$		
<u>Homogeneous</u>				
SCL_H_1	852.5	862.9	31740	1.20
S_H_1	621.7	626.1	8445	0.89
<u>Wet-dry cycled</u>				
SCL_M_1	-	929.2	64798	0.59
SCL_M_2	-	1167.9	74712	0.80
SCL_M_3	-	1007.6	44258	0.77
S_M_1	-	736.0	34483	0.34
S_M_2	-	909.9	41077	0.28
S_M_3	-	811.6	25470	0.28

<sup>a</sup> Mean residence time ( $t_m$ ) calculated as  $t_m = \int t * E(t)dt$  where  $E(t) = \frac{C_{out}(t)Q}{\int_0^{\infty} C_{out}(t)Q dt}$

<sup>b</sup> Variance indicating the degree of spreading

<sup>c</sup> Skewness indicating the extent of asymmetry

Table 5.8 1D Nonequilibrium CDE (MIM): Parameter Estimation

ID	Input Parameters				Estimated Model Parameters						R <sup>2</sup>
	L cm	v cm d <sup>-1</sup>	T <sub>o</sub> -	R -	λ <sup>a</sup> cm	±	β <sup>b</sup> -	±	ω <sup>c</sup> -	±	
<u>Homogeneous</u>											
SCL_H_1	13.6	14.61	0.62	1.41	0.08	0.02	0.90	0.02	0.65	0.05	0.997
S_H_1	13.5	14.62	0.77	1.14	0.04	0.01	0.92	0.03	0.79	0.72	0.992
<u>Wet-dry cycled</u>											
SCL_M_1	14.2	12.42	0.78	1.33	0.26	0.10	0.85	0.05	0.65	0.41	0.992
SCL_M_2	14.1	11.32	0.80	1.44	0.19	0.04	0.87	0.02	0.63	0.24	0.996
SCL_M_3	14.1	12.69	0.80	1.40	0.21	0.05	0.88	0.03	0.65	0.35	0.996
S_M_1	14.1	12.38	0.93	1.36	0.02	0.03	0.88	0.07	0.88	1.67	0.933
S_M_2	13.5	11.91	0.87	1.15	0.05	0.01	0.89	0.01	0.80	0.55	0.997
S_M_3	14.1	13.10	0.85	1.17	0.04	0.01	0.90	0.02	0.88	0.46	0.997

<sup>a</sup> Dispersivity [cm]

<sup>b</sup> Mobile water fraction [-]

<sup>c</sup> Mass transfer coefficient [-]

## 5.2 Impacts of Macropores on Neptunium-237 Transport

<sup>237</sup>Np travel velocities increased on average by 53% in homogenous SCL when compared to macroporous SCL. Travel velocity estimates were 1.6, 1.0, 0.8 cm d<sup>-1</sup> for *SCL\_H\_1*, *SCL\_M\_1*, and *SCL\_M\_3*. This increase in <sup>237</sup>Np mobility is attributed and increase in the spike solution pH differences from homogenous and heterogeneous experiments. As discussed in *Ch. 4 sect. 4*, the spike pH was 3.0 in homogeneous sand and SCL experiments and 5.6 in heterogeneous experiments. Powell (2018) shows that the <sup>237</sup>Np sorption is fully reversible and dependent on pH. In Powell's desorption experiments using similar SCL soils collected from SRS, <sup>237</sup>Np fraction sorbed (%) is ~ 100% at a pH of 8.5, ~ 15% at a pH of 5.5, and < 5% at a pH of 4.6 (Powell, 2018).

Reactive kinetic transport simulations (PHREEQC) were run to assess how pH differences between homogenous and heterogeneous SCL experiments impacted <sup>237</sup>Np mean travel distances. The 1D transport model was comprised of 50 cells which cumulatively spanned 14

cm. The simulation was run for a total of 1000 shifts with each shift equivalent to a time step of 600 seconds. Assuming a 50 mL pore volume, every 50 shifts is equivalent to 1 pore volume of water run through the model domain.

Table 5.9 Sorbed Np-237: Spatial Moments Analysis and Mobility Characteristics

ID	Experimental Measurements			Spatial Moments Analysis ( $^{237}\text{Np}$ )			
	pH <sub>spike</sub>	$\overline{\text{pH}}_{\text{effluent, }^a}$	Total PV <sub>inj</sub>	x <sub>m, }^b</sub> cm	MTD, <sup>c</sup> cm	v <sub>c, }^d</sub> cm d <sup>-1</sup>	R, <sup>e</sup> -
<u>Homogeneous</u>							
SCL_H_1	3.0	4.9	7.6	4.9	4.6	1.6	9.3
S_H_1	3.0	5.1	9.1	-	-	10.3	4.2
<u>Wet Dry - Cycled</u>							
SCL_M_1	5.5	5.2	6.9	2.8	2.6	1.0	12.2
SCL_M_2	5.5	5.3	6.6	-	-	-	-
SCL_M_3	5.5	5.1	6.1	2.1	2.0	0.8	16.5
S_M_1	5.5	6.2	7.4	1.3	1.2	0.5	22.0
S_M_2	5.5	6.4	7.0	-	-	-	-
S_M_3	5.5	6.2	7.0	2.5	2.3	1.0	14.0
PHREEQC	<u>Model Input Parameters</u>						
Sim_1	-	4.9	7.6	4.8	4.6	1.5	9.5
Sim_2	-	5.2	6.9	0.6	0.6	0.2	66.7

<sup>a</sup> pH averaged over the full duration of respective column experiments as  $\int \text{pH} Q(t) dt \bar{Q}^{-1}$

<sup>b</sup> Normalized first spatial moment (center of mass) calculated as  $x_m = \frac{\int C(x) x dx}{\int C(x) dx}$

<sup>c</sup> Mean travel distance [cm] determined by  $MTD = x_m - (0.5 * t_0 * v_c)$

<sup>d</sup> Contaminant velocity [cm d<sup>-1</sup>] where  $v_c = x_m * t_{final}$

<sup>e</sup> Retardation factor defined as the ratio between  $v_w$  (tracer velocity) and  $v_c$  ( $R = \frac{v_w}{v_c}$ )

PHREEQC simulations run with porewater pH fixed at 4.9 estimated the  $^{237}\text{Np}$  MTD to be 4.8 cm, within 0.1 cm of experimental results, after flushing with 7.6 pore volumes (Table 5.4).

This simulation was rerun with a fixed pH of 5.2, equivalent to the average pH of effluent in heterogeneous SCL experiments which estimated that  $^{237}\text{Np}$  mean travel distances would be 0.01 cm (Figure 20). These simulations indicate that  $^{237}\text{Np}$  transport is largely dependent on pH, thus, accurate comparisons of  $^{237}\text{Np}$  transport in homogeneous and wet-dry cycled soils cannot be made.

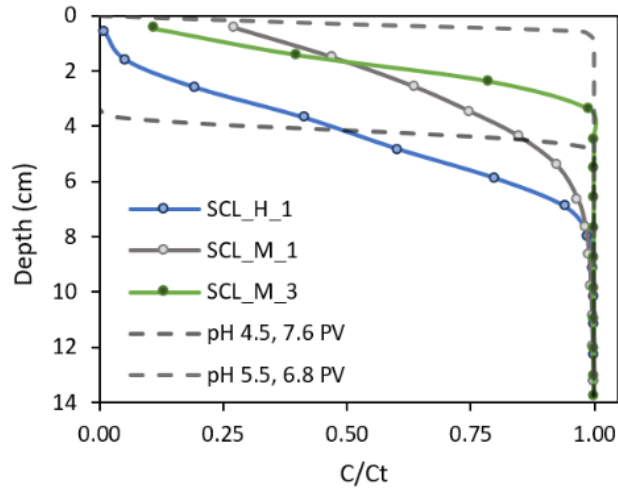


Figure 20 Comparison of  $^{237}\text{Np}$  soil distributions for homogeneous and macroporous SCL. Dashed lines correspond to PHREEQC simulated estimates of  $^{237}\text{Np}$  transport in SCL. Simulations were run varying only pH (pH = 4.9, pH = 5.5)

### 5.3 Comparison and Implications of Br and Tc-99 Breakthrough

Due to analytical difficulties, bromine was not added as a tracer for wet-dry cycled SCL and sand column flow experiments; however, results from preliminary experiments in homogeneous soils showed that Br and  $^{99}\text{Tc}$  have similar mobilities in both experimental soil types. Bromide retardation factors in homogenous SCL and sand experiments were found to be 1.33 and 1.07. Retardation factors for  $^{99}\text{Tc}$  were 1.30 and 1.08 for these same experiments (Table 5.1). Furthermore, plume spreading, and peak shapes were nearly identical respective to soil types (Figure 11). Corresponding  $R$  measurements between Br (non-reactive tracer) and  $^{99}\text{Tc}$  breakthroughs suggest that  $^{99}\text{Tc}$  should be considered non-reactive to produce precautionary transport estimates.

## CHAPTER 6: CONCLUSIONS

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This study finds that in unsaturated conditions, macropore structure in SCL soils increases  $^{99}\text{Tc}$  dispersivity estimates. However, mean arrivals of  $^{99}\text{Tc}$  were not impacted by macropore structures present in SCL soils. The retardation factor determined from unsaturated column flow experiments for  $^{99}\text{Tc}$  were 1.30 in homogeneous SCL and 1.35, 1.41, and 1.28 in macroporous SCL. Exposing SCL soil to a wetting and drying event proved to generate macropores in all exposed SCL columns. Macropores visible in SCL soil were predominantly vertical. We conclude that macropores can facilitate capillary exclusion in unsaturated macroporous soils. In this process, cracks create capillary barriers separating the matrix into mobile fluid and immobile regions, which increases the spatial variability of flow velocities dependent on macropore orientation (faster if vertically oriented and slower if horizontal).

CT scans of sand-packed columns showed no indications of macropore formation post-exposure to wet-dry cycling; however, breakthrough and IBPV increased in macroporous experiments increased, suggesting that macropores may be present but were not visible in CT scans. Retardation factors for  $^{99}\text{Tc}$  were similar between exposure groups. Homogeneous sand  $^{99}\text{Tc}$   $R$  was estimated to be 1.08, while in wet-dry cycled experiments, estimates were 1.04, 1.12, and 1.07. Large uncertainties in parameters estimated from MIM predictions data presented challenges when interpreting mobile water fraction ( $\beta$ ) and mass transfer coefficients ( $\omega$ ).

Accurate comparisons of  $^{237}\text{Np}$  transport in homogeneous and wet-dry cycled SCL and sand could not be made due to variations in influent pH across experiments. With an average effluent pH of 4.9, the mean travel distance (MTD) for  $^{237}\text{Np}$  was 4.8 cm ( $K_d = 1.7 \text{ cm}^3 \text{ g}^{-1}$ ). In

macroporous experiments, the average pH was 5.4 resulting in SCL MTD's of 2.6 and 2.0 cm (SCL\_M  $K_d = 2.2, 3.0 \text{ cm}^3 \text{ g}^{-1}$ ). Sand experiments showed similar trends, with  $K_d$  estimates increasing from  $0.7 \text{ cm}^3 \text{ g}^{-1}$  in homogeneous experiments (average effluent pH = 4.9) to 4.3 and  $2.5 \text{ cm}^3 \text{ g}^{-1}$ . PHREEQC 1D transport simulations (CDE) run at fixed pH's of 4.9, and 5.2 showed that dropping the pH in these ranges increased the mean travel distance from 0.1 to 4.9 cm (Fig. 14). PHREEQC simulations support claims that the dominant factor affecting  $^{237}\text{Np}$  mobility across these experiments is pH.

# APPENDICES

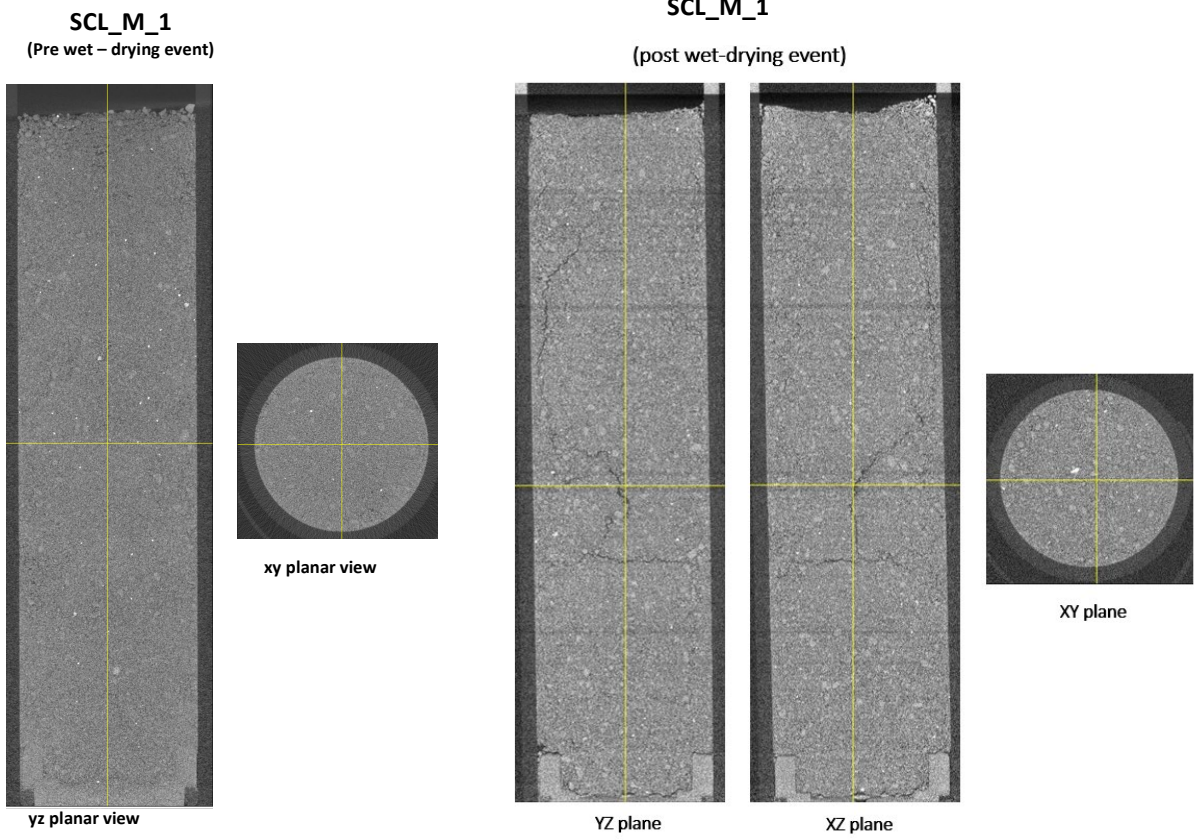


Figure 21 CT imaging of SCL\_M\_1 Pre (left) and post (right) wet - drying event (YZ, XZ, and XY planar views)



SCL\_M\_3  
(Post wetting – drying event)

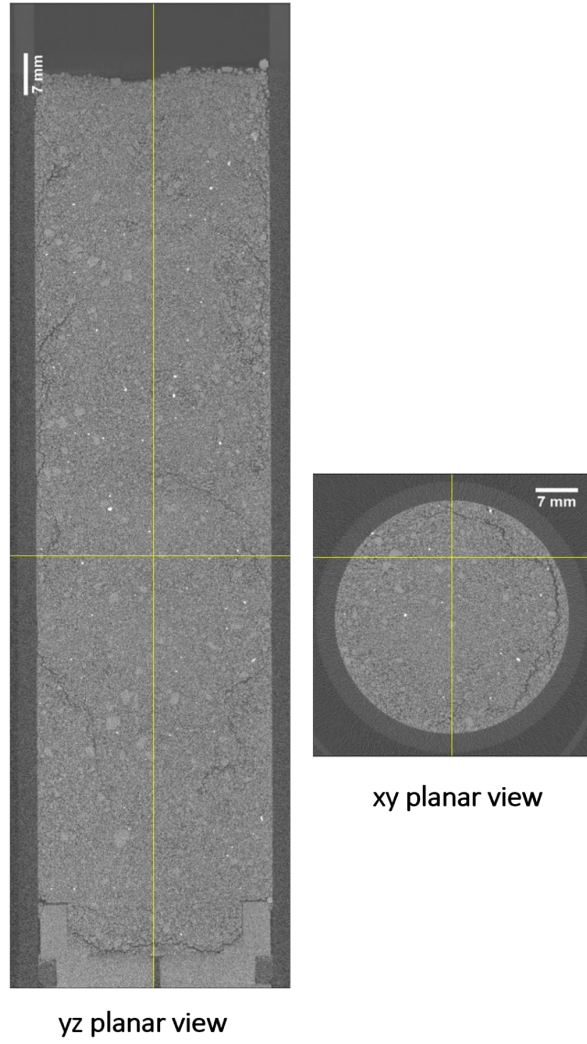


Figure 22 CT imaging of SCL\_M\_3 post wet-drying event

**SCL\_M\_2**  
(Post wet - drying event)

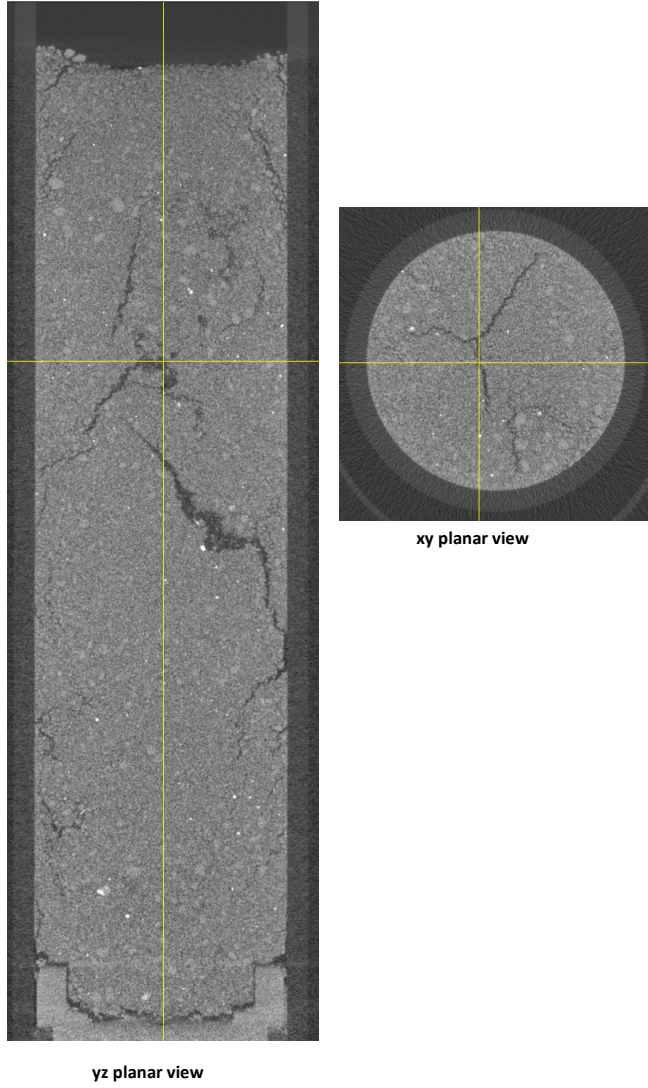


Figure 23 CT imaging of SCL\_M\_2 post wet-drying event

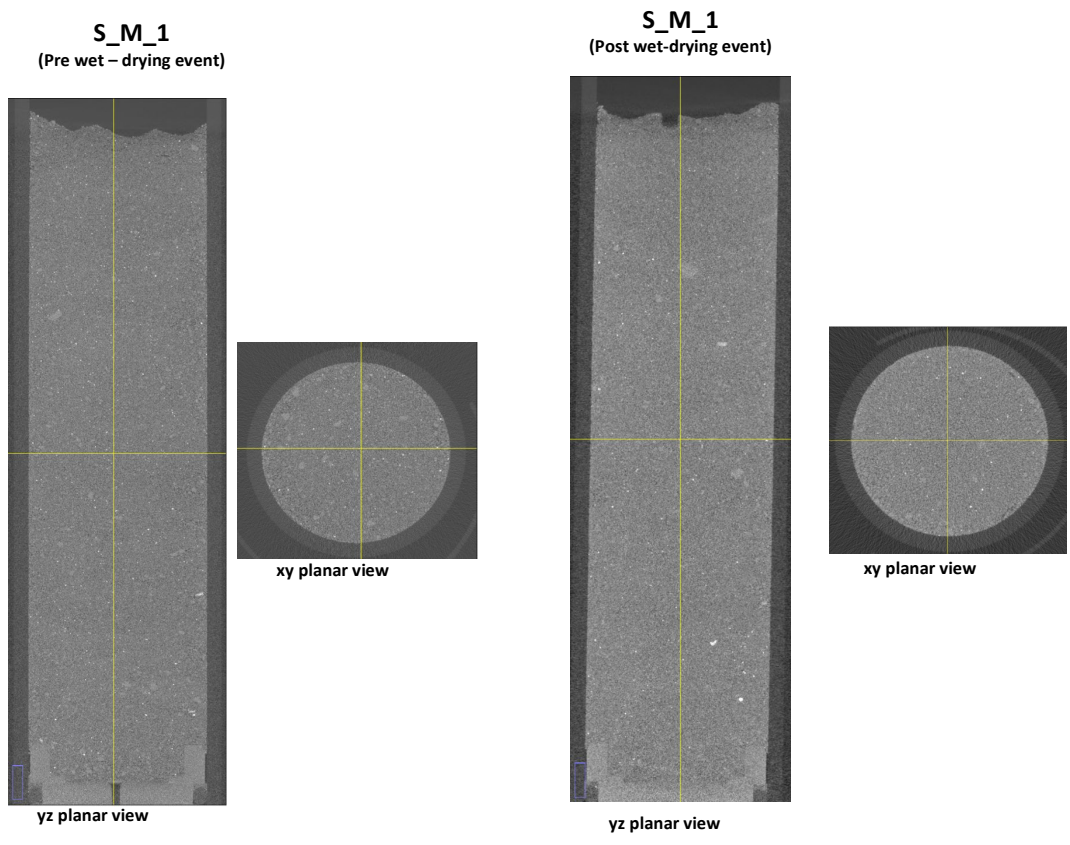


Figure 24 CT imaging of S\_M\_1 Pre (left) and post (right) wet - drying event (YZ, XZ, and XY planar views)

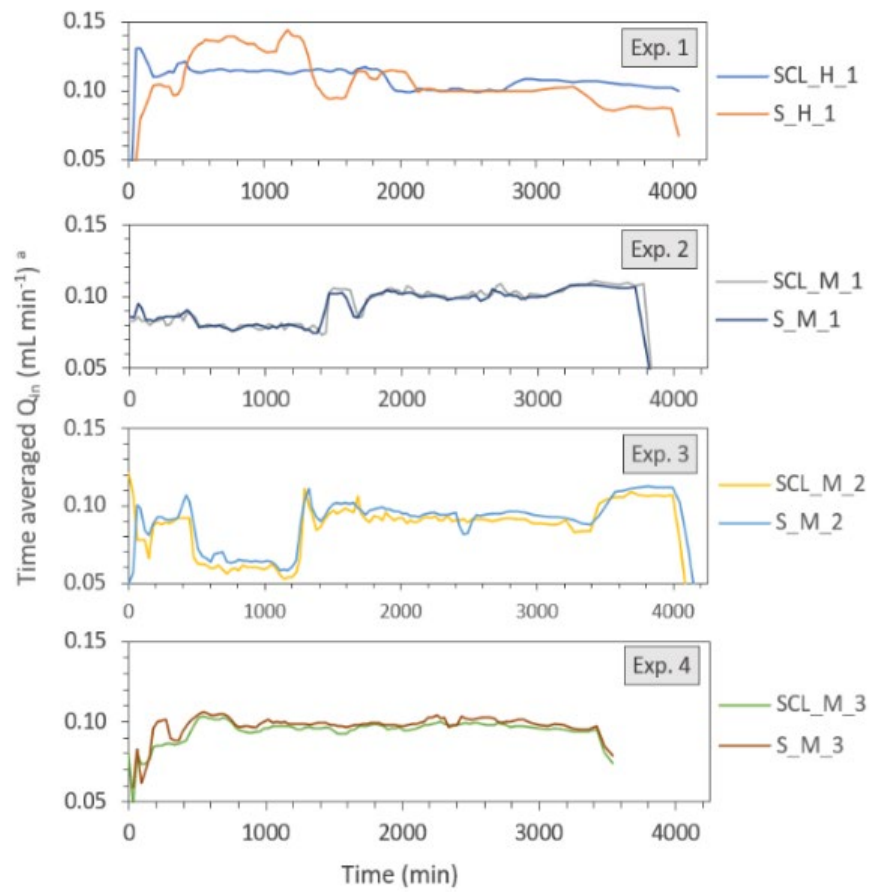


Figure 25 Time-average volumetric flowrate ( $\text{mL}/\text{min}$ ) for column flow

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