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# Adaptive noise suppression for low-S/N microseismic data based on ambient-noise-assisted multivariate empirical mode decomposition

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Microseismic monitoring data may be seriously contaminated by complex and nonstationary interference noises produced by mechanical vibration, which significantly impact the data quality and subsequent data-processing procedure. One challenge in microseismic data processing is separating weak seismic signals from varying noisy data. To address this issue, we proposed an ambient-noise-assisted multivariate empirical mode decomposition (ANA-MEMD) method for adaptively suppressing noise in low signal-to-noise (S/N) microseismic data. In the proposed method, a new multi-channel record is produced by combining the noisy microseismic signal with preceding ambient noises. The multi-channel record is then decomposed using multivariate empirical mode decomposition (MEMD) into multivariate intrinsic mode functions (MIMFs). Then, the MIMFs corresponding to the main ambient noises can be identified by calculating and sorting energy percentage in descending order. Finally, the IMFs associated with strong interference noise, high-frequency and low-frequency noise are filtered out and suppressed by the energy percentage and frequency range. We investigate the feasibility and reliability of the proposed method using both synthetic data and field data. The results demonstrate that the proposed method can mitigate the mode mixing problem and clarify the main noise contributors by adding additional ambient-noise-assisted channels, hence separating the microseismic signal and ambient noise effectively and enhancing the S/Ns of microseismic signals.

## KEYWORDS

microseismic monitoring, seismic signal, interference noise, noise suppression, multivariate empirical mode decomposition

## 1 Introduction

Microseismic monitoring technology is a useful tool for characterizing the structures, physical properties, and dynamic processes in the subsurface within a target region. This technique has been widely used in the monitoring of hydraulic fracturing in hydro-carbon reservoirs [1–3], coal mining [4, 5], geothermal exploration [6, 7], and CO<sub>2</sub> capture and

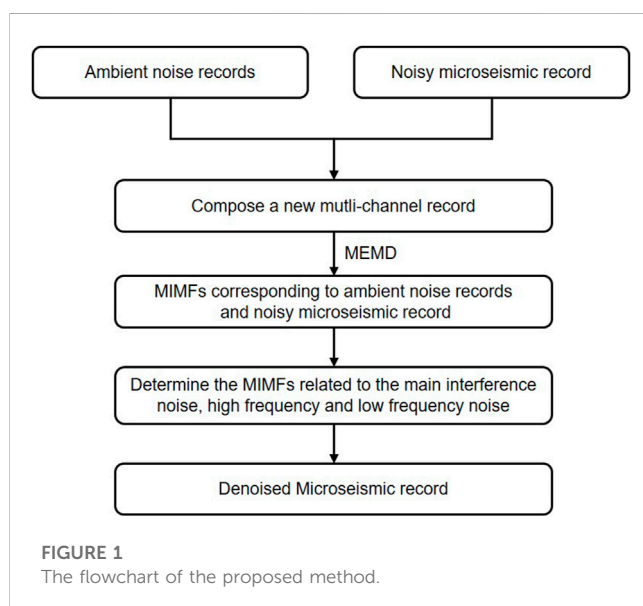
storage (CCS) [8]. Single-component (1-C) or three-component (3-C) receivers installed at the surface and/or in the borehole are anticipated to record not only the seismic event signals but also high-energy interference noises and random noises generated by motions such as mechanical vibrations [9–11]. Various excitations and strong noises could significantly reduce the detectability of weak but useful seismic signals in the monitoring data, thereby compromising the reliability of data processing and interpretation [12–14]. Therefore, it is essential to develop an effective method to suppressing interference noise in microseismic monitoring data.

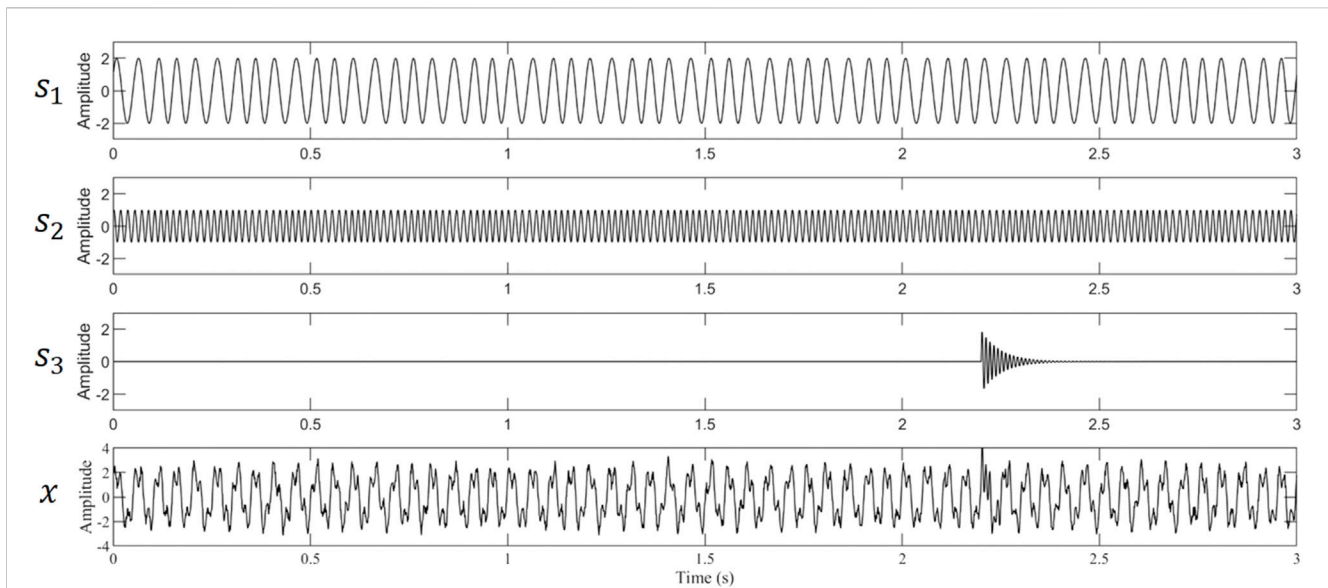
Low signal-to-noise (S/N) microseismic recordings are usually abandoned without applying adequate denoising methods due to the small magnitudes of microseismic events obscured by noisy recording environments. Frequency-domain band-pass filtering is the most commonly used method in seismic monitoring processing for attenuating background noises and extracting microseismic signals, but the effect of this method may not be very satisfying if the background noises and microseismic signals are in the same frequency range. Researchers have made a great effort to develop novel methods for noise suppression and microseismic signal enhancement, such as polarization filtering [15], median filtering [16], mathematical morphology filtering [17], the singular value decomposition-based method [18, 19], and the time-frequency transform-based method [20–24]. In addition to high-frequency noise, the background interference noises are also of concern [13, 17, 21, 22]. Because the characteristics of microseismic signals in the noisy monitoring data are usually unclear, conventional denoising methods struggle to suppress the strong-energy, long-duration interference noises and retain the energy of microseismic signals. Thus, the improvement in the S/N of microseismic data is often limited.

Mode decomposition algorithms can adaptively decompose the nonlinear and nonstationary signals to analyze the local characteristic time scale and have been widely applied in seismic/microseismic signal processing, mechanical fault detection, structural health monitoring, and biomedical signal analysis [19,

25–31]. To overcome the problems of mode mixing, end effect, and lack of adaptability, mode-decomposition algorithms have progressed from empirical mode decomposition (EMD) [25] to ensemble empirical mode decomposition (EEMD) [27], complementary ensemble empirical mode decomposition (CEEMD) [28, 29], and variational mode decomposition (VMD) [30, 31]. By iteratively extracting the high-frequency components and their associated envelopes, the complex signal is decomposed into a set of intrinsic mode functions (IMFs) in the empirical mode decomposition based algorithms. Similarly, the VMD methods employ an optimization framework to separate the complex signal into multiple modes. To deal with multivariate data, the multivariate extension of EMD (i.e., multivariate EMD, or MEMD for short) and VMD (i.e., multivariate VMD, or MVMD for short) are proposed for processing multivariate data to obtain the IMFs with aligned frequency ranges [32–35]. Noise-assisted MEMD (NA-MEMD) [33], partial noise-assisted MEMD (PNA-MEMD) [36], and sinusoidal signal-assisted MEMD (SA-MEMD) [37] and harmonic-assisted MEMD (HA-MEMD) [38] are subsequently proposed to improve the performance of the MEMD method by adding additional channels with independent white noise, high-frequency band-limited noise, and a sinusoidal assisted signal, respectively.

These mode-decomposition algorithms have been widely employed in seismic/microseismic data denoising and arrival picking [19, 39–44]. The separation or reconstruction of signals is often accomplished in the mode decomposition based methods and their improvement approaches by the selection of IMF components. When reconstructing the signal, metrics like as correlation coefficient, kurtosis, mutual information entropy, and other parameters that characterize the signals of each IMF are calculated to provide various weight coefficients that emphasize the target signal. However, the study of low signal-to-noise ratio microseismic signals are hampered by noise because real-world signals are typically nonlinear and accompanied by strong ambient noise, and the features extracted directly from these signals usually contain a large amount of useless as well as noisy information that cannot effectively distinguish seismic signals from noise. Compared to the interference noises with long durations and high energies, the microseismic signals show very short duration (<1s) and unpredictable energies in the field data. The Low-S/N microseismic event may be identified from continuous recordings using rigorous detection thresholds, thus, the adaptive and effective separation of background noise and weak microseismic signal is critical for subsequent data processing. In this paper, we develop an adaptive noise suppressing method for microseismic data processing based on ambient-noise-assisted multivariate empirical mode decomposition (ANA-MEMD). In the proposed method, a new multichannel record that combines the noisy microseismic recording with preceding ambient noises is decomposed by the MEMD method into multivariate intrinsic mode functions (MIMFs). Then, the ambient records are utilized to assist in decomposing microseismic data and identifying main noise contributors. In this study, we first introduce the theory of EMD and MEMD, then elaborate on the ANA-MEMD method for noise suppression in microseismic data. Finally, we evaluate





**FIGURE 2**  
Single-component synthetic noisy microseismic recording.

the performance of the proposed method by using synthetic and field data.

## 2 Methods

### 2.1 Empirical mode decomposition

As a data-driven approach, empirical mode decomposition (EMD) decomposes a signal adaptively into a finite set of oscillatory components known as intrinsic mode functions (IMFs) [25]. The original signal can be recovered by reconstructing all IMFs, which represent different vibrations whose instantaneous frequency reflects the local characteristics of the input signal. Two conditions are essential for calculating an IMF: 1) the number of extrema and the number of zero crossings should be different only by one; 2) the mean value of the upper and lower envelopes should be roughly zero [25]. In the EMD method, the decomposition is accomplished by removing the slowly oscillatory modes and separating the rapidly oscillating modes from the data. For a real-valued signal  $x(t)$ , it can be decomposed into

$$x(t) = \sum_{m=1}^M d_m(t) + r(t), \quad (1)$$

where  $d_m(t)$  represents the  $m$ th IMF and  $r(t)$  is the residual component.

Although a complex signal can be decomposed into several IMFs by EMD, the application of real data may be restricted by the mode-mixing problem due to the intermittency of a signal component or closely spaced spectral tones. To address the limitation of mode mixings, ensemble empirical mode decomposition (EEMD) [27, 40] and complementary ensemble empirical mode decomposition (CEEMD) [28, 29] are proposed successively by taking the noises into consideration. The purpose of incorporating white noise is to

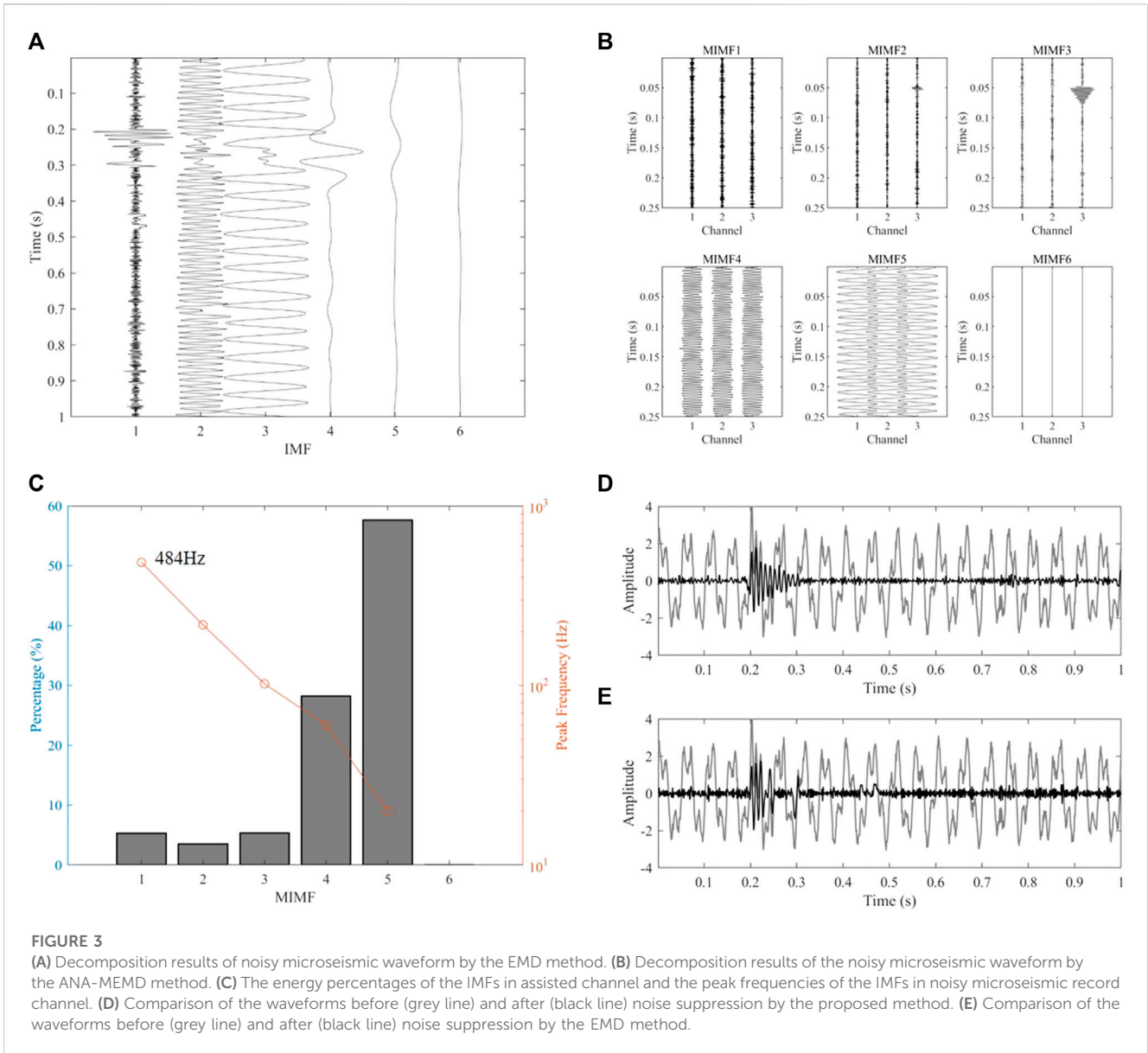
perturb the signal in its true solution neighborhood and ensure the extreme value points are distributed uniformly during the sifting process, therefore restraining mode-mixing.

### 2.2 Multivariate empirical mode decomposition

Signal acquisition using multicomponent receivers or multiple receivers is prevalent in engineering applications. The characteristic analysis of the system may be impacted by a scale arrangement uncertainty problem when each signal is decomposed independently using the EMD approach. Multivariate empirical mode decomposition has been introduced to overcome this issue by performing the same mode analysis on multivariate signals in various frequency scales and ensuring that each signal's IMF number after decomposition is identical [32]. In the MEMD approach, a uniform sampling scheme based on the Hammersley sequence is used to calculate direction vectors. The  $n$ -dimensional signal envelopes are obtained by taking a sequence of projection vectors along different directions in the  $n$ -dimensional space. After interpolating their extrema, the envelopes are averaged to generate the local mean of signals. One multivariate intrinsic mode function (MIMF) is produced by calculating the difference of the mean of all envelopes with respect to the original signals. This process is repeated until a sufficient number of MIMFs has been obtained or the stopping criterion is met. The MEMD decomposes a multivariate signal  $\mathbf{X}(t)$  as

$$\mathbf{X}(t) = \sum_{m=1}^M \mathbf{d}_m(t) + \mathbf{r}(t), \quad (2)$$

where  $\mathbf{d}_m(t)$  represents the  $m$ -th MIMF and the residual component  $\mathbf{r}(t)$  represents the final trend. The detail procedures of the MEMD algorithm can be described as follows.

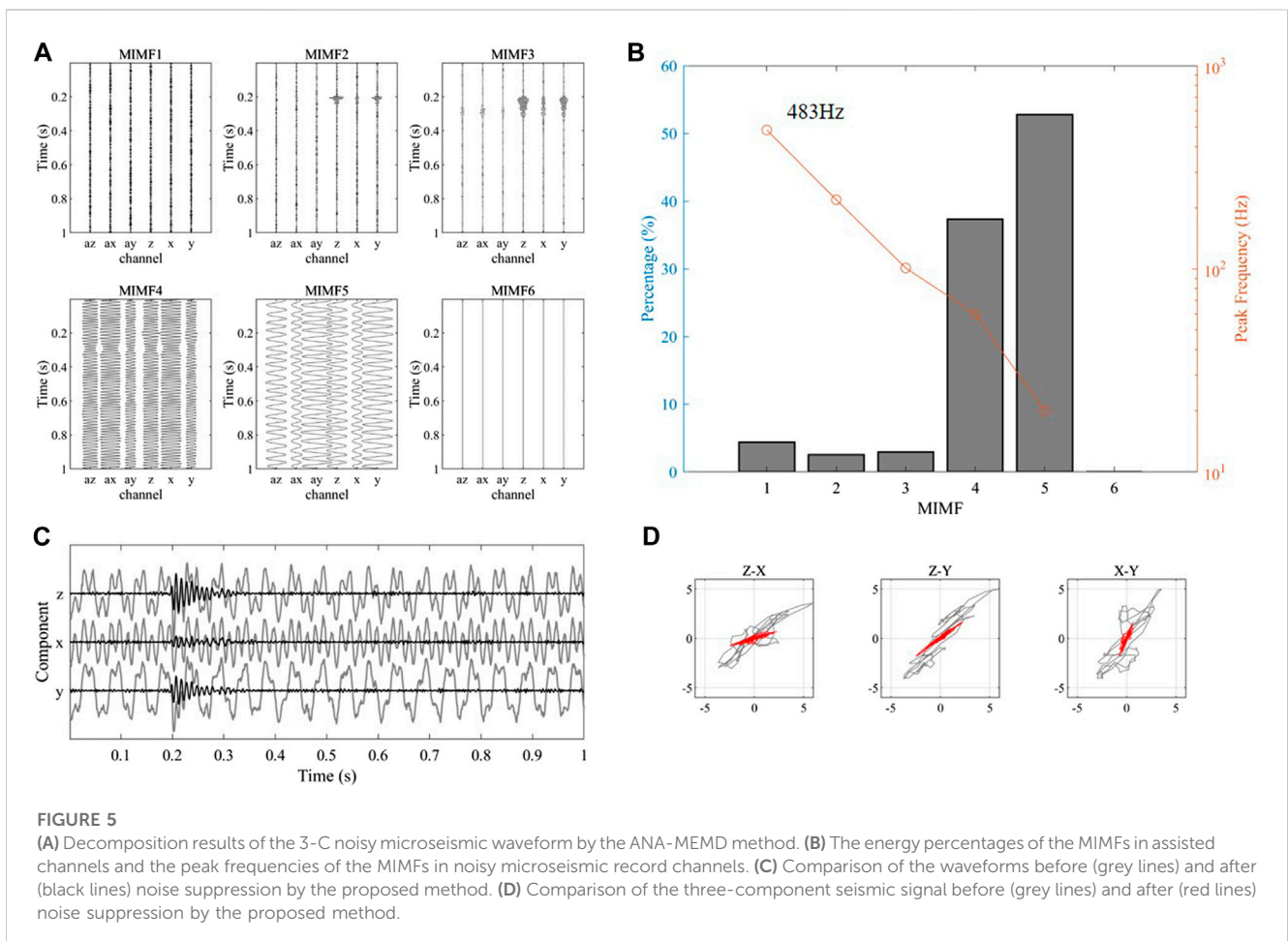
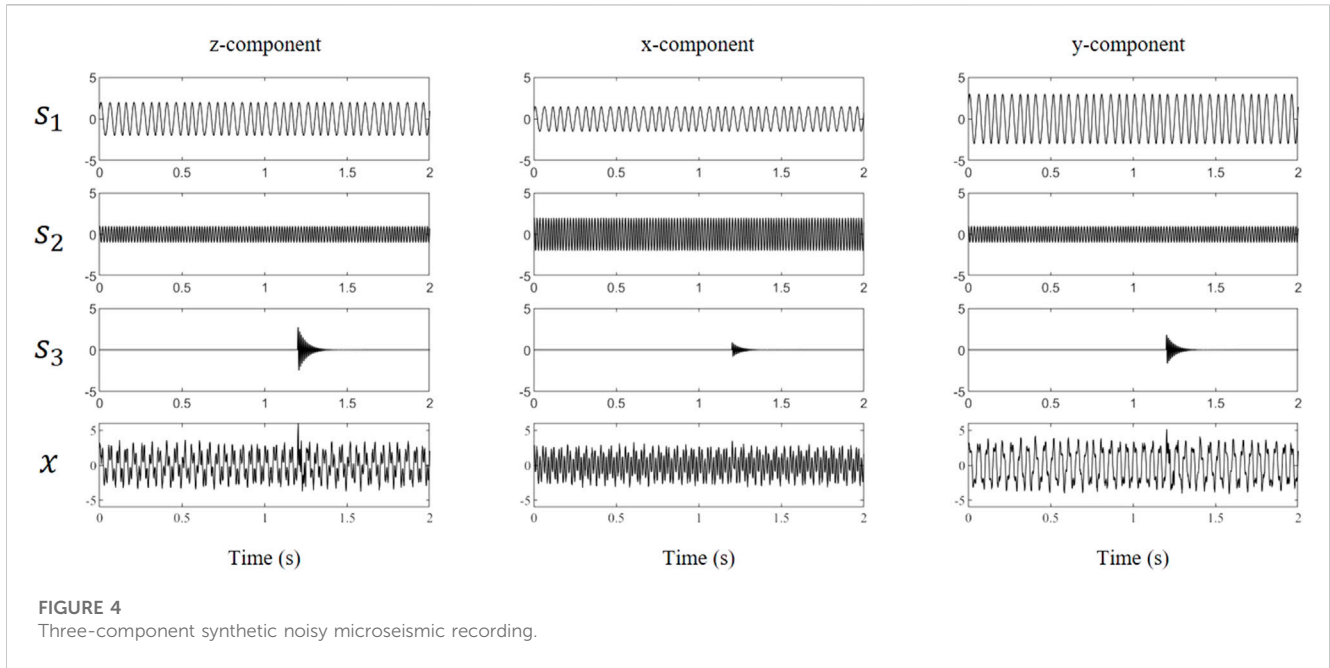


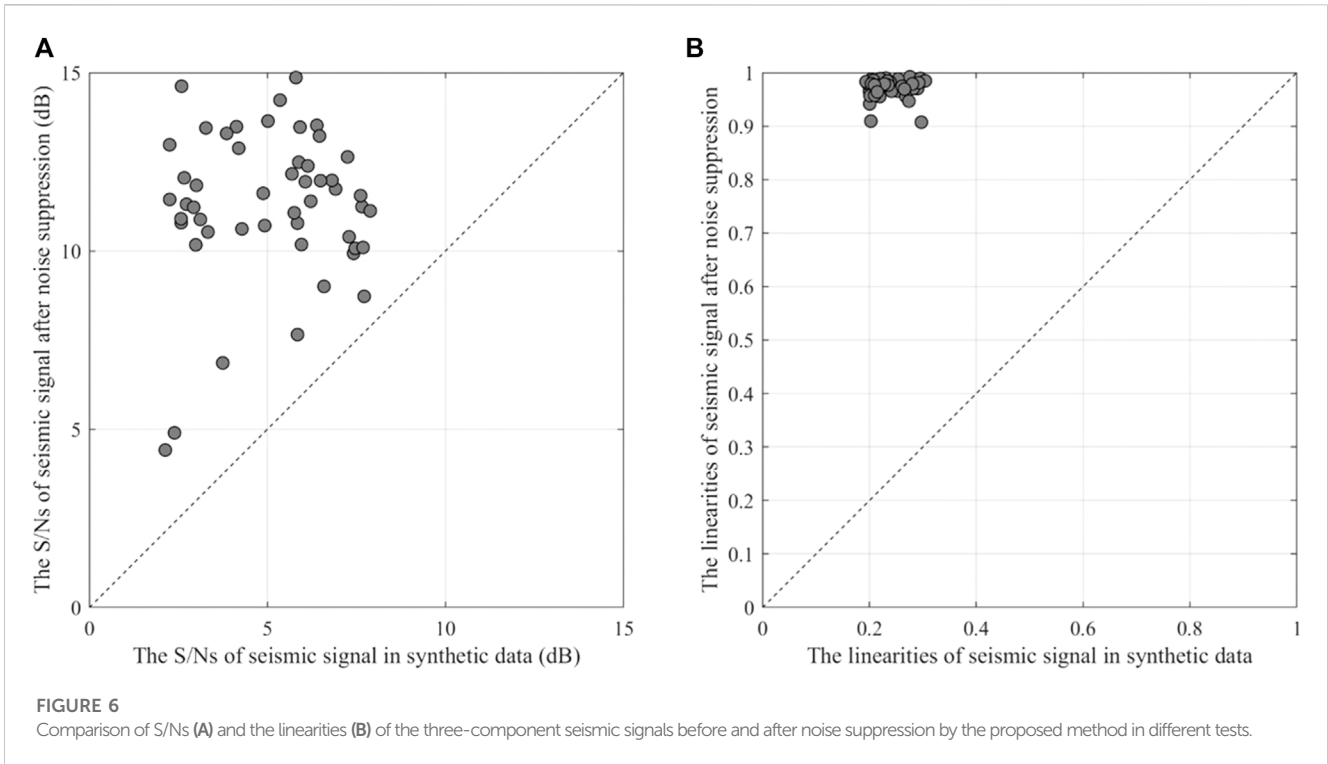
- (1) Create a uniform sampling point set on an  $(n-1)$ -dimensional sphere using the Hammersly sequence, and establish an  $n$ -dimensional spatial direction vector.
- (2) Obtain the project sets  $P^{\theta_k}(t)$  of the input signal  $\mathbf{X}(t)$  along all direction vector  $\mathbf{V}^{\theta_k}$  for a set of  $K$  direction vectors.
- (3) Find the time instants  $t_i^{\theta_k}$  corresponding to the maxima of the set of projected signals  $P^{\theta_k}(t)$ , and obtain multivariate envelop curves  $e^{\theta_k}(t)$  using the spline interpolation function.
- (4) Calculate the mean value using  $\mathbf{m}(t) = \sum_{k=1}^K e^{\theta_k}(t)/K$ .
- (5) Extract the detail  $\mathbf{d}(t)$  by calculating  $\mathbf{d}(t) = \mathbf{x}(t) - \mathbf{m}(t)$ , and check whether  $\mathbf{d}(t)$  satisfies the stopping criterion for a multivariate IMF. If  $\mathbf{d}(t)$  satisfies the stopping criterion, apply the above procedure to  $\mathbf{X}(t) - \mathbf{d}(t)$ ; otherwise, apply it to  $\mathbf{d}(t)$ .

As a multivariate extension of EMD, the MEMD is a significant improvement in multichannel signal processing, allowing for adequate alignment between the same index IMFs and facilitating inherent

multiscale analysis. Similar to the standard EMD method, the mode mixing problem still exists in the MEMD method. To solve this issue, additional channels containing auxiliary signals are used to help the decomposition of the original multivariate signal, such as noise-assisted MEMD (NA-MEMD) [33], partial noise-assisted multivariate EMD (PNA-MEMD) [36], a sinusoidal signal-assisted MEMD (SA-MEMD) [37], and high-frequency harmonic-assisted MEMD (HA-MEMD) [38]. For the original  $n$ -dimensional multivariate signal,  $l$ -dimensional extra channels are added and then processed using the MEMD method as an  $(n + l)$ -dimensional signal. These methods can be summarized as follows.

- (1) Generate  $l$ -dimensional assisted channels that are of the same length as the original multivariate signal;
- (2) Combine the  $n$ -dimensional input multivariate signal with the assisted channels created in Step 1) to construct an  $(n + l)$ -dimensional signal;





- (3) Decompose the new multivariate signal using the MEMD algorithm to extract the multivariate IMFs;
- (4) Remove the  $l$ -dimensional IMFs related to the assisted signals from the multivariate IMFs in Step 3) and retain the  $n$ -dimensional IMFs related to the original signal.

It is worth noting that, except from differences in additional channels, these improved methods maintain the same processing flow as standard MEMD method.

### 2.3 Adaptive noise suppression based on ambient-noise-assisted MEMD (ANA-MEMD)

Microseismic monitoring data can be expressed as

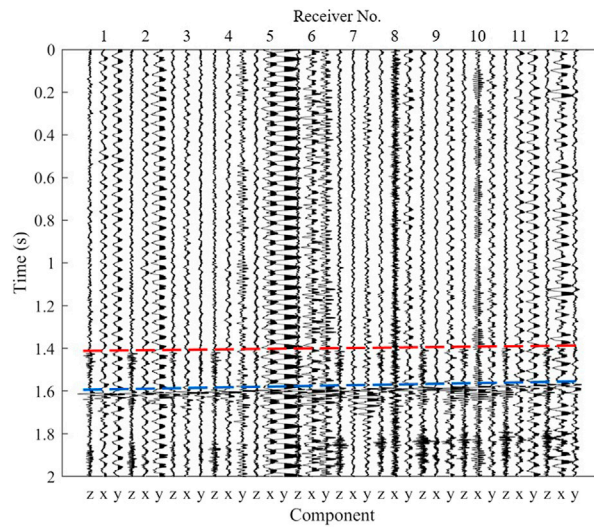
$$\mathbf{X} = \mathbf{A}\mathbf{S}. \tag{3}$$

where  $\mathbf{S} = [s_1, s_2, \dots, s_K]^T$  represent  $K$  source signals,  $\mathbf{X} = [x_1, x_2, \dots, x_M]^T$  represent  $M$  observation signals, and  $\mathbf{A}$  is the relation matrix between source signals and observation signals. The source signal could be seismic signal or noise. The observation signal can represent recordings at different locations, time windows, and components. In continuous recordings, the duration of ambient noise (e.g., interference noises produced by pumps or industries in continuous operation,  $\gg 1$  min) is substantially longer than that of seismic events ( $< 1$  s). The interference noises in the ambient recording persist throughout successive time windows.

In this study, we present ambient-noise-assisted multivariate empirical mode decomposition (ANA-MEMD) for decomposing noisy microseismic data and remove non-effective components for

S/N enhancement of microseismic data. The auxiliary channels containing ambient noise are introduced in the decomposition process, which differs from the standard MEMD technique. To determine whether one MIMF (or IMF for single-component microseismic data) contains ambient noise, we calculate the energy percentage of the assisted ambient noise in each decomposed MIMF (or IMF for single-component microseismic data). In our method, strong interference noise is considered to persist and constitute the predominant portion of the ambient record. Finally, the MIMFs (or IMFs) components associated with ambient noise and outside the desired signal band are eliminated during the reconstruction process. Our method is organized as follows.

- (1) For a low-S/N microseismic signal recording with a time window length of  $N_{win}$ , we select ambient recordings with the same time window length preceding the microseismic data as additional assisted channels. In general, two window for single-component microseismic data, and one window for 3-C microseismic data. Strong random signals (including coherent seismic signals) must not be present in the additional assisted channels.
- (2) After constructing a new multivariate signal by adding the noisy microseismic data with the above-assisted channels, we obtain the multivariate IMFs  $\mathbf{d}_m(t)$  and  $\mathbf{c}_m(t)$  using the MEMD algorithm.  $\mathbf{d}_m(t)$  and  $\mathbf{c}_m(t)$  are the  $m$ -th MIMFs corresponding to noisy microseismic data and assisted ambient noise, respectively.
- (3) We calculate and sort the energy percentage of each MIMF  $\mathbf{c}_m(t)$  in descending order, and obtain the peak frequency of each MIMF  $\mathbf{d}_m(t)$ .



**FIGURE 7** The waveforms of one low-S/N microseismic event. Red and blue dashed line represent the arrival times of P-wave and S-waves, respectively.

(4) Pre-set the band range  $[f_l, f_h]$  determine high frequency and low frequency noise, and find the dominant noise according to a threshold value of the energy percentage. The IMFs with a large energy percentage are potential interference noise. The microseismic data after noise suppression can be reconstructed by  $X'(t) = X(t) - \sum d_{M_I}(t)$ , where  $M_I$  is the index of qualified MIMFs.

The above procedure is applicable to both single-component data and three-component microseismic data. The flowchart of the proposed method is shown in [Figure 1](#).

### 3 Numerical examples

In this section, we demonstrate the performance of the proposed method using both single-component and three-component synthetic microseismic data. The synthetic signal is composed of two time-varying oscillation signals (regarded as persistent interference noises) with dominant frequencies of 20 Hz and 60 Hz, and an attenuated sine wave (regarded as seismic signal), which has the peak frequency of 100 Hz. Its composed components are expressed as the following equations.

$$\begin{cases} s_1 = \sin (2\pi 20t + 0.5 \cos 2\pi 5t) \\ s_2 = \sin (2\pi 60t + 0.8 \cos 2\pi 6t) \\ s_3 = \sin (2\pi 100(t - t_0)) * e^{-0.02(t - t_0)} \end{cases} \quad (4)$$

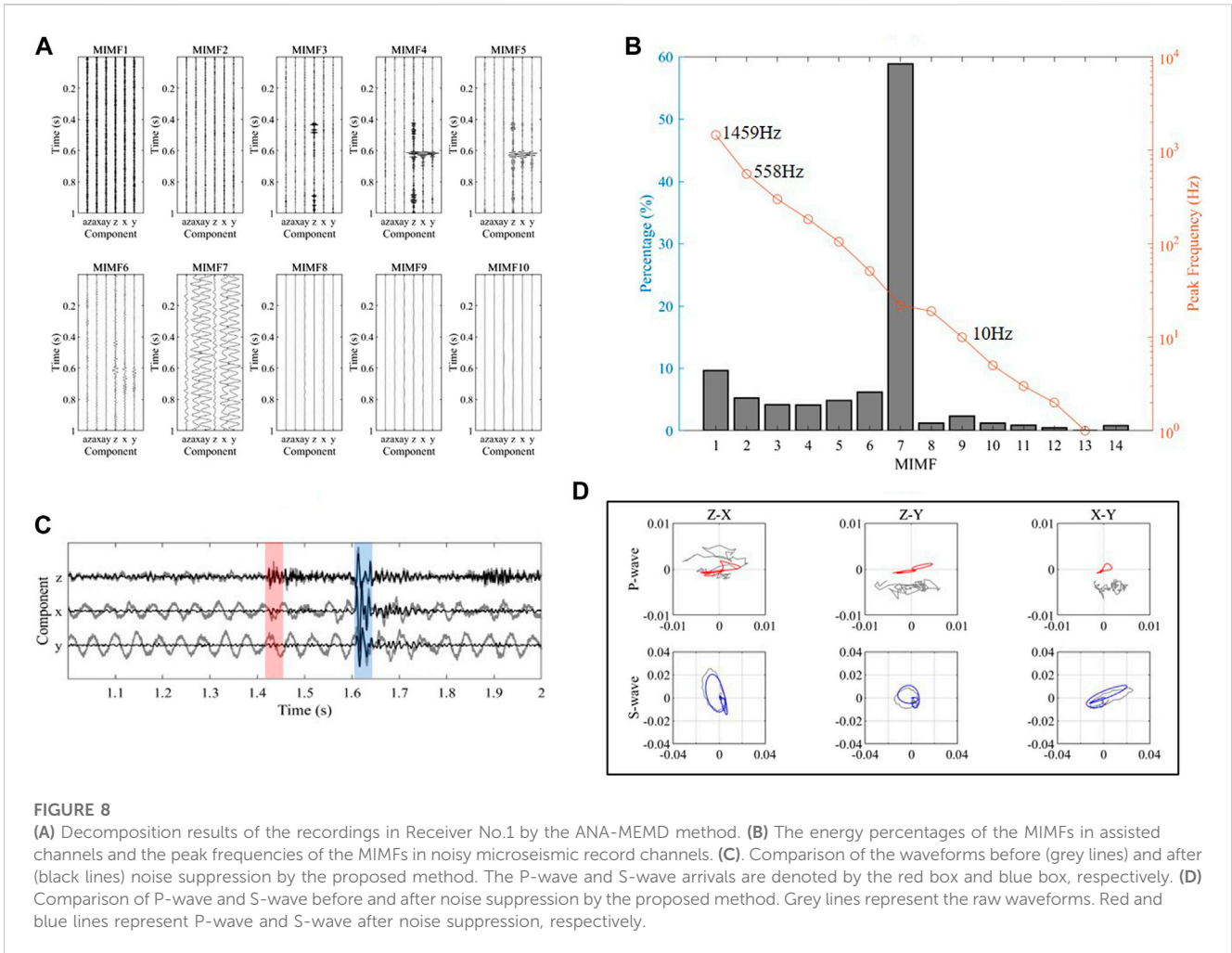
Where  $t_0$  is the arrival time of seismic signal.

First, the above three source signals with the maximum amplitude ratio of 2:1:2 and Gaussian noise with the amplitude variance of 0.1 were applied to generate one single-component synthetic microseismic recording. The arrival time of seismic signal is 2.2 s and the sampling frequency is 1000 Hz. [Figure 2](#) shows the waveforms of the synthetic microseismic data, it can be

seen that the seismic signal becomes blurred due to the strong interference noise.

We compared the decomposition results of the synthetic microseismic record using the EMD method and the proposed ANA-MEMD method. Two 1-s long background noise recordings (0~1 s and 1~2 s) before the seismic signals were employed as extra assisted channels. [Figures 3A, B](#) illustrate the six IMFs that decomposed by above two methods, respectively. Channel 1, 2, and 3 in [Figure 3B](#) represent the IMFs corresponding to two background noise recordings and noisy microseismic signal, respectively. There is no doubt that the phenomenon of mode mixing has been alleviated by the addition of auxiliary noise channels. We demonstrated the viability of the proposed method in noise suppression using the aforementioned decomposition results. We calculated the energy percentage of each IMF in the ambient noise assisted channels (channel 1–2 in [Figure 3B](#)) and the peak frequency of each IMF in the noisy microseismic signal channel (channel 3 in [Figure 3B](#)), as shown in [Figure 3C](#). By determining IMF related to the top two energy percentage (IMF 4 and 5, cumulative percentage greater than 80%), the high frequency noise (IMF1, the peak frequency >200 Hz), and the low frequency noise (IMF 6, the peak frequency <10 Hz), the IMF that contains the ambient noise can be identified. The denoised microseismic records by the proposed method and EMD method can be obtained by reconstructing the remaining IMFs, as shown in [Figures 3D, E](#). Compared to the result of EMD method (black line in [Figure 3E](#)), the arrival of the seismic signal is clearly visible in the denoised waveform (black line in [Figure 3D](#)), while preserving as much the microseismic signal as possible.

Three-component synthetic microseismic recording was constructed by the above three source signals and a mixing matrix and Gaussian noise with the amplitude variance of 0.2. The mixing matrix is given as



**FIGURE 8**

(A) Decomposition results of the recordings in Receiver No.1 by the ANA-MEMD method. (B) The energy percentages of the MIMFs in assisted channels and the peak frequencies of the MIMFs in noisy microseismic record channels. (C). Comparison of the waveforms before (grey lines) and after (black lines) noise suppression by the proposed method. The P-wave and S-wave arrivals are denoted by the red box and blue box, respectively. (D) Comparison of P-wave and S-wave before and after noise suppression by the proposed method. Grey lines represent the raw waveforms. Red and blue lines represent P-wave and S-wave after noise suppression, respectively.

$$A = \begin{bmatrix} 2 & 1 & 3 \\ 1.5 & 2 & 1 \\ 3 & 1 & 2 \end{bmatrix} \quad (5)$$

The arrival time of seismic signal is 1.2s and the sampling frequency is 1000 Hz. Figure 4 shows the waveforms of the synthetic microseismic data.

In the process of three-component microseismic data, one 1-s long background noise recordings (0~1 s) before the seismic signals (1~2 s) were employed as extra assisted channels. Figure 5A illustrates the six MIMFs that decomposed by the ANA-MEMD method. Channels (az, ax, and ay) and (z, x, and y) in Figure 5B represent the MIMFs corresponding to the background noise recordings and noisy microseismic signals, respectively. Similar to the processing flow for the above single-component data. We calculated the energy percentage of each MIMF in the ambient noise assisted channels and the peak frequency of each MIMF in the noisy microseismic signal channels, as shown in Figure 5B. By determining MIMF related to the top two energy percentage (MIMF 4 and 5, cumulative percentage greater than 80%), the high frequency noise (MIMF1, the peak frequency >200 Hz), and the low frequency noise (MIMF 6, the peak frequency <10 Hz), the MIMFs that contains the ambient noise can be identified. The

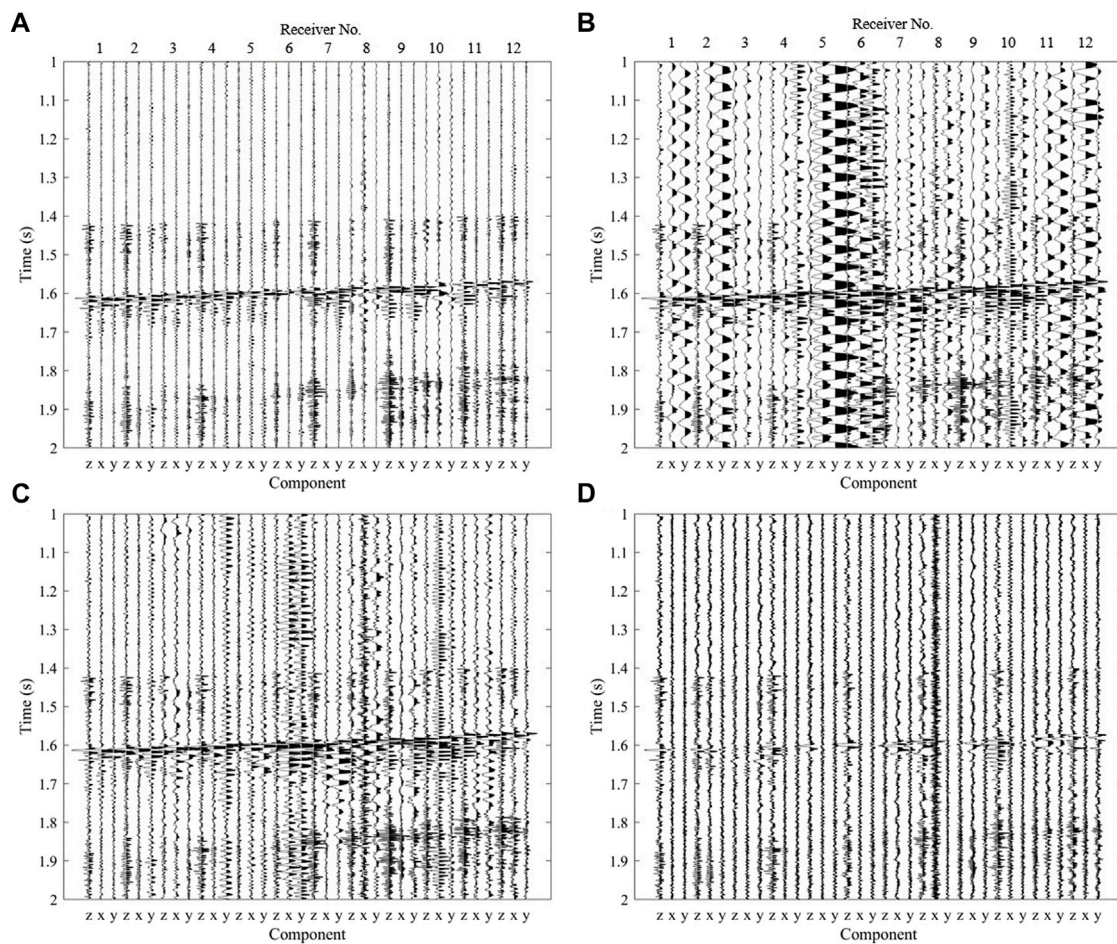
denoised microseismic record can be obtained by reconstructing the remaining MIMFs, as shown in Figure 5C. The arrivals of the seismic signals are obvious in the denoised waveform (black line in Figure 5C), and the linearity of the three-component seismic signal is significantly enhanced (as shown in red lines in Figure 5D).

Without loss of generality, the above test is repeated 50 times using synthetic three-component data with different S/Ns (1.9~5.5 dB) to verify the stability of the proposed method. To simulate varying S/Ns, we kept the amplitude of the background noise recordings and changed the amplitudes of the noise-free seismic signal. In addition, we also calculated the S/Ns and the linearities of the seismic signal before and after processing to quantitatively assess the method's performance. The S/N is calculated using the following equation [12]:

$$S/N = 20\log_{10}\left(\frac{A_{signal}}{A_{noise}}\right) \quad (6)$$

where  $A_{noise}$  and  $A_{signal}$  are the root-mean-square amplitudes of the signals before and after seismic arrivals, respectively. The linearity  $L$  for three component seismic data can calculated using the following quation,





**FIGURE 9** The microseismic signals after noise suppression using different methods. (A) The proposed method. (B) Band-pass filter method. (C) MEMD method with kurtosis criteria. (D) Multivariate wavelet denoising (MWD) method. The amplitude ranges of four microseismic waveforms subgraphs are the same.

$$L = \frac{(\lambda_1 - \lambda_2)^2 + (\lambda_2 - \lambda_3)^2 + (\lambda_1 - \lambda_3)^2}{2(\lambda_1 + \lambda_2 + \lambda_3)^2} \quad (7)$$

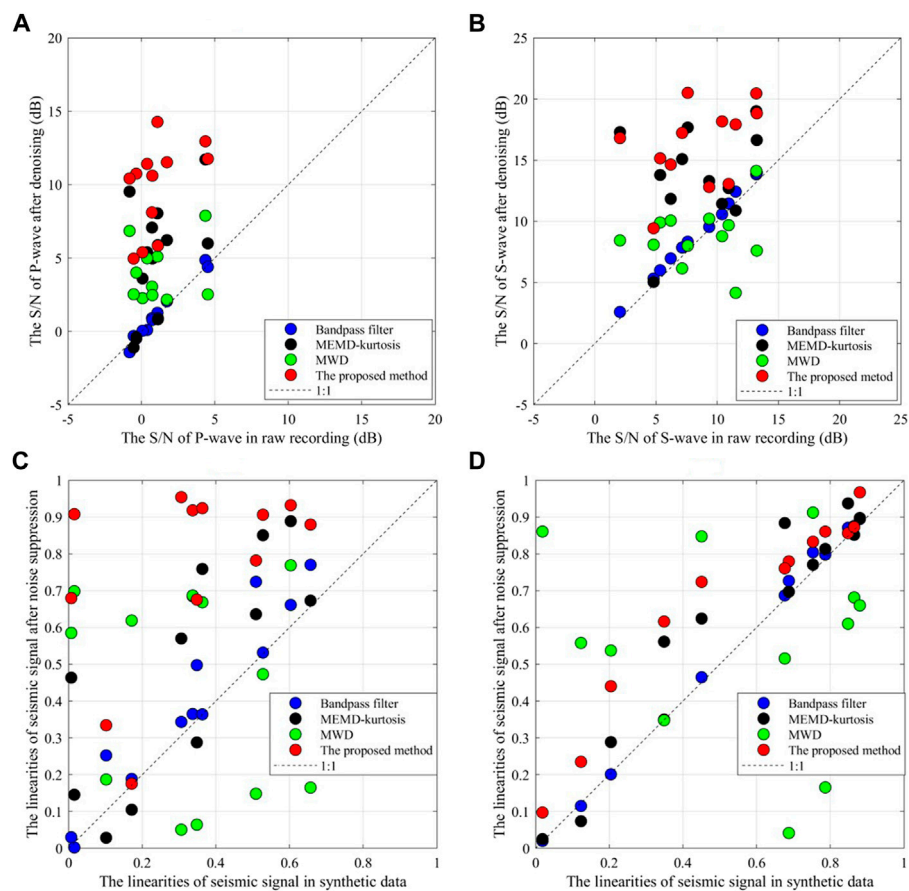
Where  $\lambda_1, \lambda_2, \lambda_3 (\lambda_1 > \lambda_2 > \lambda_3)$  are the eigenvalues of the covariance matrix for the three-component seismic signal. The S/Ns and the linearities of the microseismic signals before and after processing are shown in Figure 6. The S/Ns and the linearities of seismic signals in all tests increase using the proposed method demonstrate the effectiveness of this method for noise suppression reliability.

### 4 Field data application

In this section, we evaluated the performance of the proposed method using field microseismic data. The field data in this study come from a hydraulic fracturing surveillance job in a shale play in the Fulin gas field of China. A temporary array comprising 12 levels of triaxle 15 Hz geophones was placed in the inclined section (the inclination is

about 40°) of a horizontal well adjacent to the treatment well and used for monitoring the stimulation. A total of 63 microseismic events were detected during a hydraulic fracturing stage. Figure 7 shows the 3-C waveforms of one Low-S/N microseismic event, in which the red and blue line represent the arrival times of P- and S-waves, respectively. It is evident that significant background noises obscure the microseismic signal, and the arrivals of direct P- and S-waves are masked by strong interference noise. Observed interferences are most likely due to pumping operations or pumping-fluid-wellbore interactions.

In this field data processing, we intercepted ambient noise recording with 1-s long time window (0~1s in Figure 7) before the microseismic signal (1~2s in Figure 7). The recordings in the shallowest receiver (Receiver No.1) were analyzed as an example. The multi-channel recordings are decomposed into 14 MIMFs, and their first ten MIMFs are shown in Figure 8A, with their frequencies decreasing sequentially. The seismic signal is divided into multiple MIMFs due to its wide frequency range. We calculated the energy proportion of each MIMF in the ambient noise assisted channels and the peak frequency of each MIMF in the noisy microseismic signal



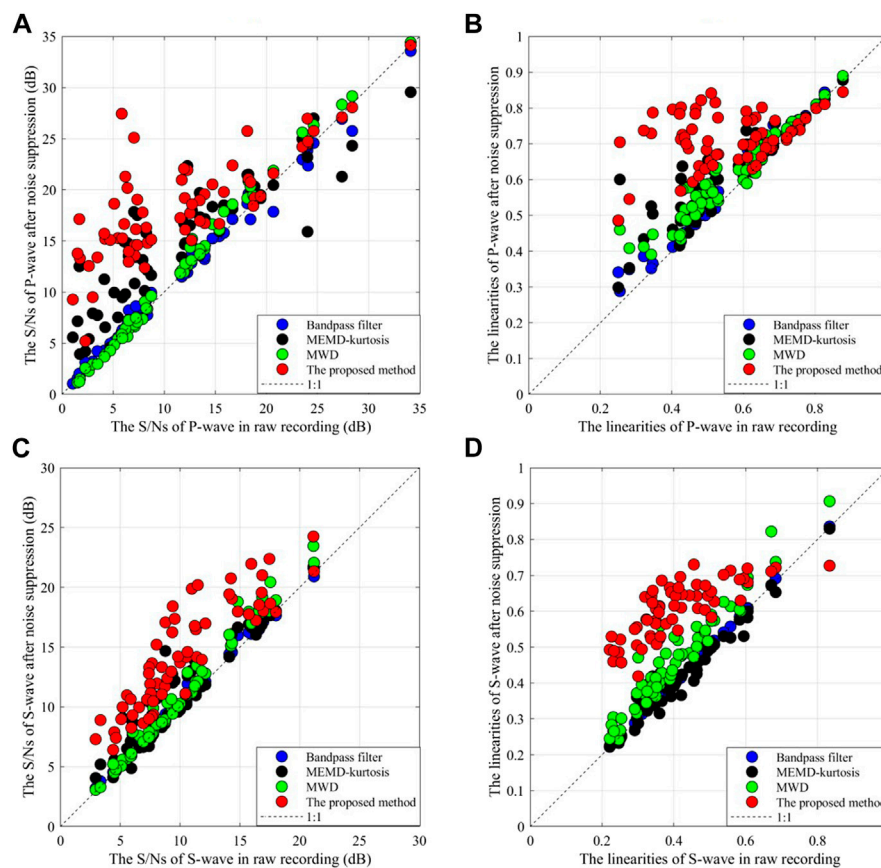
**FIGURE 10** Comparison of S/Ns and the linearities of microseismic signals before and after noise suppression by the different methods. (A) the S/Ns of P-wave. (B) the S/Ns of S-wave. (C) the linearities of P-wave. (D) the linearities of S-wave.

channels, as shown in Figure 8B. The energy percentages of each MIMF shows that the energy of background noise accounts for about 60% of the total energy, demonstrating the necessity of removing these strong noises. By determining MIMF related to the top energy proportion (MIMF 7), the high frequency noise (MIMF1 and MIMF2, the peak frequencies >300 Hz), and the low frequency noise (MIMF 9–14, the peak frequencies <10 Hz), the MIMFs that contains the ambient noise can be identified. The denoised microseismic record can be obtained by reconstructing the remaining MIMFs, as shown in Figure 8C. The P-wave (denoted by the red box) and S-wave (denoted by the blue box) arrivals of the seismic signals are clearly visible in the denoised waveforms (black line in Figure 8C), and the linearities of the three-component microseismic signal are greatly improved, particularly in P-wave.

We have processed the microseismic recordings of all 12 receivers in Figure 7. Band-pass filter (10,300 Hz), traditional MEMD based method, and multivariate wavelet denoising (MWD) method were also used to process the field data for comparison. In the traditional MEMD method, we calculated the kurtosis value of each MIMFs, and the microseismic signal is regarded as existing if the threshold of the kurtosis value is surpassed (the threshold is set to 3). Figure 9 shows the results using these methods. The S/Ns and the linearities of the microseismic signals before and after processing are shown in

Figure 10. Band-pass filter only removes high-frequency and partial low-frequency noise. There remain strong interferences in the denoised microseismic data. Part of the arrivals of P-wave and S-wave after MEMD method with kurtosis criteria are highlighted, there remain strong interferences in the several receiver recordings. It demonstrates that uniform kurtosis criteria are incapable of dealing with complicated and variable noise. The noise reduction effect on S-wave of MWD method is not obvious, which is also reflected in the S/Ns after denoising. Although the traditional MEMD method and MWD method can increase the S/Ns, they decrease the linearities of P-wave and S-wave, showing that the denoising result cannot effectively preserve the amplitude of the seismic signals. It can be seen that the proposed method performs better with the consideration of increasing the S/N and maintaining the microseismic signal adaptively.

We processed all 63 microseismic events using our method and compared the results with above three methods. For each event, we calculated the S/Ns and the linearities of P-wave and S-wave in different receivers and obtained the corresponding average values. Figure 11 displays the average values of the S/Ns and the linearities of P wave and S wave for all detected microseismic events before and after noise suppression by different methods. We can see that the proposed method can generally increase the S/Ns and the linearities



**FIGURE 11**

Comparison of the S/Ns and the linearities of microseismic events before and after noise suppression by the different methods. (A) the S/Ns of P-wave for all events. (B) the linearities of P-wave for all events. (C) the S/Ns of S-wave for all events. (D) the linearities of S-wave for all events.

of the microseismic signals more robustly than the other methods, especially for the P-wave of low S/N microseismic events. It is worth noting that the results of the proposed method are not necessarily better than those of the other methods. This is because the proposed method may also retain part of the ambient noise while preserving as much the microseismic signal as possible. Nevertheless, the fact that the S/Ns of the majority of microseismic signals increase when using the proposed method demonstrate the effectiveness of this method for microseismic signal denoising.

## 5 Conclusion

In this study, we have developed an adaptive noise suppressing method based on ambient-noise-assisted multivariate empirical mode decomposition (ANA-MEMD) for microseismic data. Multivariate empirical mode decomposition (MEMD) is employed to decompose multichannel seismic recording into multivariate intrinsic mode functions (MIMFs). To address the problem of mode mixing, ambient noise is used as assisted channels. Additionally, the dominant noise can be removed by calculating energy percentage with the ambient noise in the assisted channels. We have applied the proposed method to synthetic data and field data. The decomposing results show that

the proposed method can successfully separate and remove the strong background interference noises. In the comparison to the results of conventional filtering methods, the proposed method is demonstrated to be able to improve the S/Ns of the microseismic signals. Thus, it is favorable for microseismic signal denoising. We must emphasize that while this study tested the feasibility of the proposed method using microseismic data, this method can be applied straight forward to the active seismic data (i.e., artificial exploration seismic data) or any other multicomponent geophysical dataset that can be represented as time series.

## Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## Author contributions

ZY developed the method and wrote the original draft. YT and CH revised the manuscript. All authors participated in designing this research work. All authors contributed to the article and approved the submitted version.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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