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1-16-2013

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Bashar Behnam Broome College, Binghamton, NY

Christopher D. Eamon Wayne State University, Detroit, MI, christopher.eamon@wayne.edu

#### **Recommended** Citation

Behnam, B., and Eamon, C. (2013). "Resistance factors for ductile FRP-reinforced concrete flexural members." *Journal of Composites for Construction*, 17(4), 566-573, doi: 10.1061/(ASCE)CC.1943-5614.0000363 Available at: https://digitalcommons.wayne.edu/ce\_eng\_frp/13

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**Resistance Factors for Ductile FRP-Reinforced Concrete Flexural Members** 

Bashar Behnam<sup>1</sup> and Christopher Eamon<sup>2</sup>

## 5 ABSTRACT

6 To prevent damage caused by corroding reinforcement, fiber reinforced polymer (FRP) 7 reinforcing bars have been used in place of steel in a relatively small but increasing number of structures in the civil infrastructure. A concern with the use of traditional FRP bars, however, is 8 9 the resulting lack of ductility. This problem has been overcome with the development of a new 10 generation of composite reinforcement, ductile hybrid FRP (DHFRP) bars. However, standards 11 that address the design of DHFRP bars are unavailable, and appropriate resistance factors for the 12 use of DHFRP reinforcement are unknown. In this study, a reliability analysis is conducted on 13 tension-controlled concrete flexural members reinforced with DHFRP, with the intent to estimate 14 potential strength reduction factors. Flexural members considered include a selection of 15 representative bridge decks and building beams designed to meet AASHTO LRFD and ACI-318 16 strength requirements and target reliability levels. Nominal moment capacity is calculated from 17 standard analytical models and is taken as first DHFRP material failure. Statistical parameters 18 for load and resistance random variables in the reliability model are consistent with previous 19 code calibration efforts. The resulting resistance factors ranged from 0.61 to 0.64 for tension-20 controlled sections, which indicates a potential increase in allowed strength over flexural 21 members using non-ductile bars.

<sup>&</sup>lt;sup>1</sup> Assistant Professor, Dept. of Civil Engineering Technology, Broom College, Binghamtom, NY 13905. Email: <u>as2732@wayne.edu</u>

<sup>&</sup>lt;sup>2</sup> Associate Professor, Dept. of Civil and Environmental Engineering, Wayne State University, Detroit, MI 48202.

#### 22 Introduction

23 The damage caused by corroding reinforcement is a prevailing problem in the civil infrastructure, where approximately 30% of bridges in the United States have significantly 24 25 deteriorated due to reinforcement corrosion, requiring over \$8 billion to repair (Won et al. 2007; 26 FHWA 2001). Different approaches have been employed to limit corrosion and the resulting 27 concrete damage, including increasing cover, utilizing epoxy-covered bars, changing mix 28 porosities and adding admixtures to prevent chloride penetration, and implementing active 29 cathodic protection systems. Although these methods have been shown to reduce corrosion in 30 some cases, the problem remains prevalent, particularly in colder climates where chloride-31 containing deicing materials are used, as well as on concrete structures exposed to seawater 32 (FHWA 2001; Smith and Virmani 1996).

33 The use of fiber-reinforced polymer (FRP) composites represents an alternative approach, 34 where rather than attempt to protect the steel, it is partially or completely replaced with a non-35 corrosive, FRP alternative. In recent years, various bridges in North America have successfully 36 used FRP reinforcement, and these structures can be found throughout the US from Michigan to 37 Texas (Eamon et al. 2012). Although FRP reinforcement has been commercially available for 38 more than a decade, FRP-reinforced structures represent a small portion of new and renovated 39 concrete bridges. The small use of FRP relative to steel can be explained by various factors, 40 including higher initial costs and designer unfamiliarity with the material and its design process, 41 although design guidelines for FRP-reinforced structural members can be found in the AASHTO 42 LFRD Bridge Design Guide Specifications for GFRP-Reinforced Concrete Bridge Decks and 43 Traffic Railings (AASHTO 2009) and the ACI Guide for the Design and Construction of Structural Concrete Reinforced with FRP Bars, ACI-440.1R (ACI 2006). Other reasons for lack 44

of use include performance concerns such as low elastic modulus, potential degradation in
alkaline environments, and lack of reinforcement ductility. With appropriate selection of FRP
materials, however, many of these drawbacks can be reduced or eliminated (Cheung and Tsang
2010).

49 The high initial cost of FRP remains a concern, although long term benefits can be 50 significant. A recent life-cycle cost analysis of FRP-reinforced bridges revealed that, while FRP 51 bars may be on the order of 6-8 times more expensive than steel, and the resulting cost of a 52 typical bridge superstructure reinforced with FRP may range from 25-75% higher than its steel-53 reinforced equivalent, reduced maintenance costs can be expected to result in a net cost savings 54 near 20 years of service life. Moreover, considering a 50 to 75 year time span, total life-cycle 55 costs for typical FRP-reinforced bridges were generally predicted to be one-half or less of their 56 steel-reinforced alternatives (Eamon et al. 2012).

57 Although the use of FRP reinforcement may have long-term economic advantages, the 58 brittle tensile failures associated with traditional FRP bars and the resulting relatively non-ductile 59 response of concrete flexural members reinforced with them is clearly undesirable from a safety 60 perspective. Fundamental advancements have been made by various researchers in the last two 61 decades in the area, however, and numerous FRP bar designs with ductility rivaling that of steel 62 have been achieved (Tamuzs and Tepfers 1995; Harris et al. 1998; Bakis et al. 2001; Belarbi et 63 al. 2001; Cheung and Tsang 2010; Won et al. 2007; Cui and Tao 2009; Wierschem and 64 Andrawes 2010). In each of these cases, ductility is achieved by use of the hybrid concept. 65 Here, the reinforcing bars are made of not one, but multiple fiber types, where each type of fiber 66 has a different ultimate failure strain. When the bar is overloaded in tension, the fibers with the 67 lowest ultimate strain (generally the most stiff) rupture first. As load is further increased, the

68 fibers with the next lowest ultimate strain rupture, and so on, until all materials in the bar fail. 69 This incremental failure reduces stiffness as the materials rupture, and if material properties and 70 their volume fractions are selected properly, the remaining fibers will maintain the applied load 71 until the desired level of ductility is reached. Figure 1 presents analytical stress-strain curves 72 generated for a set of ductile FRP bar designs. The general response shown in the figure closely 73 resembles the discontinuous stress-strain behavior experimentally determined by the various 74 researchers noted above. Experimental results have similarly shown that a significant ductile 75 response similar to, and sometimes exceeding that of, a steel-reinforced concrete flexural 76 member can be achieved with ductile FRP reinforcement (Harris et al. 1998; Cheung and Tsang 77 2010).

78 Ductile hybrid FRP (DHFRP) reinforced members have the potential to eliminate 79 corrosion damage, decrease structure life cycle costs, as well as provide significant ductility. 80 However, it is currently unclear what, if any, design advantage DHFRP reinforcement may have 81 over traditional FRP bars, as resistance factors ( $\phi$ ) for the use of these bars in flexural members 82 have not been developed. The importance of this concern can be illustrated by comparing steel-83 reinforced concrete flexural member design strength requirements per ACI 318-11 (2011) (or 84 AASHTO LRFD (2010)), to that required for FRP-reinforced sections, per ACI 440.1R-06 (2006) 85 (or AASHTO GRFP (2009)).

For the steel-reinforced section, to provide a sufficiently ductile failure, *ACI 318* requires that flexural members are under-reinforced to prevent a much less ductile failure caused by concrete crushing. When such members are designed to an adequate level of ductility, as specified by strain in the extreme layer of tension steel equaling a value of 0.005 or greater while maximum compressive strain in the concrete is 0.003, the resistance factor is taken as 0.90. 91 To account for uncertainties affecting flexural capacity such the yield strength of steel 92 reinforcement, compressive strength of concrete, as well as geometric section properties, the 93 strength reduction factor was derived by considering random variable statistical parameters 94 specifically determined for steel-reinforced flexural members, in order to provide the target level 95 of safety (Szerszen and Nowak 2003).

96 In contrast, for a concrete flexural member reinforced with FRP, ACI 440.1R is 97 considered, where both under-reinforced as well as over-reinforced flexural failure modes are 98 permitted. For the former, moment capacity is governed by FRP rupture in tension, while for 99 the latter, capacity is governed by crushing of the concrete compressive block. The 100 corresponding resistance factor varies with failure mode, and is linearly interpolated between 101 0.55 (for tension-controlled sections) and 0.65 (compression-controlled), as a function of 102 reinforcement ratio. However, the resistance factor of 0.55 given for tension-controlled sections 103 is lower than that actually needed to provide the target reliability level with regard to flexural 104 capacity; it was lowered further to account for the lack of ductility associated with FRP bar 105 failure (Shield et al. 2011).

106 Using ACI 440.1R as a guide for the design of FRP-reinforced sections, the two allowed 107 failure modes (tension- and compression-controlled) theoretically apply to DHFRP as well. If 108 DHFRP bars are used in an over-reinforced design, the resistance factor is appropriately taken as 109 0.65, just as for the case of an over-reinforced beam with brittle FRP or steel, as the uncertainties 110 associated with the concrete, rather than the reinforcement, control the flexural failure and hence 111 reliability. However, it only makes sense to use DHFRP in an under-reinforced member, where 112 bar ductility could actually be utilized in the case of an overload. As ACI 440.1R does not 113 provide a resistance factor specifically for DHFRP-reinforced sections, and the existing tension114 controlled resistance factor of 0.55 was set assuming brittle bar behavior, the design strength of a 115 DHFRP-reinforced section may be unnecessarily penalized. It would be similarly inappropriate 116 to adopt the resistance factor of 0.9 found in *ACI 318* for steel-reinforced, tension-controlled 117 members, as that factor was derived based on random variable statistical parameters only 118 applicable to steel reinforcement, such as uncertainties in yield strength and bar size.

119 Given this concern, the objective of this study is to determine potential resistance factors 120 for tension-controlled, DHFRP-reinforced concrete flexural members. The results may be used 121 to estimate what design advantage, in terms of potential increase in resistance factor, might be 122 obtained by using DHFRP in the place of non-ductile FRP bars. Appropriate resistance factors 123 can be determined with a reliability-based calibration process, where resistance factors are 124 determined such that tension-controlled, DHFRP-reinforced flexural members meet the existing 125 target reliability level established for ductile (i.e. steel-reinforced) flexural members, as designed 126 according to ACI 318 or AASHTO LRFD. In this process, appropriate constraints on section 127 behavior are imposed such that a sufficient level of ductility is maintained

Reliability analysis as well as reliability-based calibration has been conducted for nonductile FRP bars in reinforced concrete members (Shield et al. 2011; Ribeiro and Diniz 2012), and a significant body of work exists examining the reliability of externally-bonded, non-ductile FRP used to strengthen reinforced concrete beams (Plevris et al. 1995; Okeil et al. 2002; Monti and Santini 2002; Zureick et al. 2006; Atadero and Karbhari 2008; Wang et al. 2010; Wieghaus and Atadero 2011; Ceci et al. 2012).

The typical process used for reliability-based calibration is well established. This involves selecting representative designs for consideration; establishing a probabilistic model by identifying the limit state function, the relevant random variables, and their statistical parameters;

selecting a target reliability index; evaluating the reliability of the cases considered; and
adjusting resistance factors such that the target level is met, which is often an iterative process.
Each of these tasks is described below.

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#### 141 **DHFRP bars considered**

Numerous DHFRP schemes have been developed, with regard to constituent material properties, number of materials, and construction technique. A conceptual diagram of a DHFRP bar with four materials is given in Figure 2, where the materials, each composed of a different fiber type, are separated into concentric layers.

146 Although many material combinations are feasible for strength, once other practical 147 design constraints are imposed on bar performance, particularly to ensure adequate ductility, the 148 range of possible arrangements decreases considerably. In this study, five generic bar layouts 149 were considered, for a representative range of configurations that can achieve the required 150 performance results in terms of strength and ductility. Here, 2, 3, and 4-material continuous 151 fiber bars are considered (designated B1, B2, and B3, respectively), the most prevalent type, as 152 well as less common alternative schemes including a bar of 2 continuous and 2 randomly-153 dispersed, chopped-fiber materials (B4), as well as a 4-material bar with 1 continuous layer, 2 154 chopped fiber layers, and a small steel core (8mm diameter), as proposed by Cheung and Tsang 155 (2010) (*B5*).

156 Material volume fractions for each bar are given in Table 1, while pertinent material 157 properties, Young's modulus (*E*) and ultimate strain ( $\varepsilon_u$ ), are given in Table 2. For schemes *B4* 158 and *B5*, bars that include randomly dispersed chopped fiber layers, fiber length is taken as 6 mm, 159 with 65% fiber and 35% resin in the layer. Although other DHFRP bar configurations are possible, the generic configurations considered in this study are meant to represent a selection of reasonable possibilities guided by suggestions in the literature, and adjusted to minimize bar costs. In general, once bar material types and number of layers were chosen, the required volume fractions were then determined in order to meet both strength and ductility requirements, as described below.

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### 166 Deterministic Analysis

For bars composed of fiber and resin only (i.e. no steel), as with *B1-B4*, DHFRPreinforced concrete flexural member moment capacity can be determined as:

 $M_{c} = \left[ d - K_{2} \frac{\varepsilon_{f_{1}}}{K + f' + b} \left( \sum_{i=1}^{n} v_{f_{i}} E_{f_{i}} + v_{m} E_{m} \right) \left( \sum_{i=1}^{n} v_{f_{i}} + v_{m} \right) A_{T} \right].$ 

169

170

$$\left[ \varepsilon_{f_1} \left( \sum_{i=1}^n v_{f_i} E_{f_i} + v_{f_m} E_{f_m} \right) \left( \sum_{i=1}^n v_{f_i} + v_m \right) A_T \right]$$

$$(1)$$

Equation (1) provides the moment capacity at the point where the first FRP material in the bar fails, as governed by the lowest ultimate fiber strain. As shown in Tables 1 and 2, for the schemes considered, this first material failure is IMCF-II for *B1-B3* and IMCF-I for *B4* and *B5*. For design as well as capacity analysis,  $M_c$  is taken as the nominal moment capacity  $M_n$ . The contribution to flexural capacity from the concrete tensile strength is ignored in the expression, which is insignificant for the schemes considered.

In eq. (1), the first term in square brackets is the distance between the tensile reinforcement centroid and that of the concrete compressive block. The second term in square brackets represents the tensile force in the reinforcement at first material failure. In both terms,

180 
$$\sum_{i=1}^{n} v_{f_i} E_{f_i} = v_{f_1} E_{f_1} + v_{f_2} E_{f_2} + \dots + v_{f_n} E_{f_n}$$
, where *n* is the number of material layers;  $v_{f_i}$  and  $E_{f_i}$ 

are the volume fraction and Young's modulus of fiber in layer *i*, respectively;  $f'_c$  is the concrete 181 compressive strength;  $E_m$  and  $v_m$  are the Young's modulus and volume fraction of the resin;  $\varepsilon_{f_1}$ 182 183 is the failure strain of the first fiber layer to fail;  $K_1$  and  $K_2$  define the shape of the concrete 184 compression block in Hognestad's parabolic stress-strain model (Hognestad 1952), where  $K_1$  is 185 the ratio of average concrete stress to maximum stress in the block and  $K_2$  defines the location of 186 the compressive block centroid;  $A_T$  is the total tensile reinforcement area; d is the distance from 187 the centroid of tension reinforcement to the extreme compression fiber in the beam; and b is the 188 width of the concrete compression block. For scheme B5, with a steel core, the resistance 189 moment can be similarly developed as:

$$190 M_{c} = \left[ d - K_{2} \frac{\left( \sum_{i=1}^{n} v_{f_{i}} + v_{s} + v_{m} \right) A_{T}}{K_{1} \cdot f_{c}' \cdot b} \left\{ \left( \sum_{i=1}^{n} v_{f_{i}} E_{f_{i}} + v_{m} E_{m} \right) \varepsilon_{f_{1}} + v_{s} \cdot f_{y} \right\} \right] \cdot \\ 191 K_{1} \cdot f_{c}' \cdot b \left[ \frac{\left( \sum_{i=1}^{n} v_{f_{i}} + v_{s} + v_{m} \right) A_{T}}{K_{1} \cdot f_{c}' \cdot b} \left\{ \left( \sum_{i=1}^{n} v_{f_{i}} E_{f_{i}} + v_{m} E_{m} \right) \varepsilon_{f_{1}} + v_{s} \cdot f_{y} \right\} \right]$$

$$(2)$$

where the second square bracketed term represents the compressive force in the concrete at first material failure;  $v_s$  is the volume fraction of steel; and  $f_y$  is the yield stress of steel. For schemes where chopped fiber layers are used (*B4*, *B5*), the effective modulus of the fibers,  $E_{fi}$ , must be reduced to account for non-continuity. This can be calculated as  $E_{fi} = \eta_{LE} \cdot \eta_{OE} \cdot E_{f} \cdot v_f$ , where  $\eta_{LE}$  accounts for reductions due to fiber length and  $\eta_{OE}$  accounts for fibers that are misaligned with the direction of load (i.e. fibers not oriented parallel to the bar). Various fiber properties affect  $\eta_{LE}$ , including fiber length and diameter, mean distance between fibers, packing

199 geometry, fiber modulus, and resin shear modulus (Cox 1952). The chopped fibers considered have a resulting  $\eta_{LE}$  from 0.98-0.99.  $\eta_{OE}$  is a function of the distribution of fiber orientation, 200 and can be shown to be  $\frac{3}{8}$  for randomly dispersed, in-plane fibers (Krenchel 1964). Note that it 201 202 is assumed that the bars are sand-coated or ribbed for adequate bond (Bank 2006). Using 203 Whitney's stress block to determine ultimate capacity would result in no significant difference 204 from that found with the nonlinear Hognestad model considered. However, the Hognestad 205 model was used as it allows evaluation of section moment-curvature behavior at load levels 206 below ultimate, which is needed to evaluate section ductility.

In this study, ductility index  $\mu_{\phi}$  is evaluated from the moment-curvature response with (Naaman and Jeong, 1995):

209 
$$\mu_{\phi} = \frac{\phi_u}{\phi_y} = \frac{1}{2} \left( \frac{E_{total}}{E_{elastic}} + 1 \right)$$
(3)

210 where  $\phi_u$  is ultimate curvature and  $\phi_y$  is yield curvature (i.e. curvature at first DHFRP 211 material failure), while  $E_{\text{total}}$  is computed as the area under the load displacement or moment-212 curvature diagram and  $E_{\text{elastic}}$  is the area corresponding to the elastic deformation.

In this study, a minimum ductility index of 3.0 is specified for flexural member performance, which represents a lower limit similar to that of corresponding steel-reinforced sections (Maghsoudi and Bengar 2010; Shin et al. 2010). As noted earlier, the source of DHFRP bar ductility results from non-simultaneous material failures, such that after a material fails, the remaining materials have the capacity to carry the tension force until the final material fails, to produce the desired ductility level. Correspondingly, before the desired level of ductility is reached, each bar material must fail before the concrete crushes in compression, which is assumed to occur at an ultimate strain of  $\varepsilon_{cu} = 0.003$ . Enforcing these constraints results in bar performance such that subsequent peaks on the stress-strain diagram do not decrease as bar strain increases (Figure 1), as well as DHFRP-reinforced concrete sections that have reinforcement strain  $\varepsilon_t$  significantly higher (approximately  $0.02 < \varepsilon_t < 0.04$ ) when the concrete compressive block crushes than that required for tension controlled, steel-reinforced sections ( $\varepsilon_t \ge 0.005$ ) according to *ACI 318*.

226 To evaluate the ductility of a DHFRP-reinforced section, the load deflection or moment-227 curvature function is needed; in this study, moment-curvature is considered. Before the section cracks, moment capacity is calculated based on elastic section properties with  $M_{cr} = \frac{f_r I_g}{v}$ , 228 where  $f_r$  is the modulus of rupture of the concrete,  $I_g$  is the uncracked section moment of inertia, 229 and  $y_t$  is the distance from the centroid of the section to the extreme tension fiber. The concrete 230 231 stress-strain behavior for cracked sections is developed based on the modified Hognestad model [33], and the corresponding resisting moment is then determined from:  $M = C_c (d - K_2 c)$ , where 232  $C_c$  is the compressive force in the concrete; d is the distance from the top of the concrete 233 234 compression block to the reinforcement centroid; and c is the distance from the top of the 235 concrete compression block to the section neutral axis. Curvature  $\phi_c$  is then calculated from  $\phi_c = \frac{\varepsilon_c}{c}$ , where  $\varepsilon_c$  is the concrete strain at the top of the compression block. For development of 236 237 the moment-curvature diagram, it is assumed that once the failure strain of a particular bar layer 238 is reached, the entire layer throughout the bar length immediately loses all force carrying 239 capability. This conservative assumption results in non-smooth moment-curvature diagrams as 240 shown in Figure 3. At peak moments on the diagrams, two different capacity values are 241 theoretically associated with the same curvature. This occurs because once the stiffest existing

material in the bar fails, the stiffness of the cracked section decreases and less moment is required to deform the beam the same amount. Experimental results of DHFRP-reinforced beams have developed somewhat smoother curves, closer to that found by drawing a line between the moment peaks and excluding the capacity drops as shown in Figure 3 (Cheung and Tsang 2010; Harris et al. 1998). However, including the theoretically low-capacity points produces conservative ductility indices, and thus this method is used to enforce the ductility constraint imposed in the analysis.

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#### 250 Flexural Members Considered

251 Resistance factors for flexural components in two typical reinforced concrete member 252 applications are considered; a bridge deck and a building floor beam. For the bridge deck, three 253 continuous slab geometries with  $f_c$ '= 31 MPa (4500 psi) spanning over girder spacings of 1.8, 254 2.7, and 3 m (6, 9, and 10 ft), were considered, as shown in Figure 4. Corresponding slab 255 thicknesses were from 200-250 mm (8-10 in), with a 13 mm (0.5 in) wearing surface and 256 allowance for a 65 mm (2.5 in) future wearing surface. The DHFRP bars were placed in the top 257 and bottom of the slab, with diameters of 22 mm (7/8 in) for bars B1-B4 and 19 mm (3/4 in) for 258 bar B5. Although AASHTO GFRP (2009) allows a minimum of 19 mm (3/4 in) cover for a slab 259 reinforced with composite bars, cover was taken as 25 mm (1 in), as used in two FRP-reinforced 260 bridge decks built in Wisconsin (Berg et al., 2006; Bank et al., 2006). The deck is designed as 261 tension-controlled for positive and negative moments using the equivalent strip method 262 according to the AASHTO LRFD Specifications (2010), where the governing design equation is:  $\phi M_n = \gamma_{DC} M_{DC} + \gamma_{DW} M_{DW} + 1.75 M_{LL+IM}$ . Here,  $M_{DC}$  and  $M_{DW}$  are moments caused by the 263 264 weight of the slab and wearing surface, respectively;  $\gamma_{DC}$  and  $\gamma_{DW}$  are load factors that may vary

from 1.25 to 0.9, and 1.5 to 0.65, respectively, to maximize load effect; and  $M_{LL+IM}$  is the live 265 load moment caused by two 72 kN (16 kip) truck wheel loads on the slab, in addition to a design 266 267 impact factor of 1.33. The selection of resistance factor  $\phi$  used for design is discussed in the next section. An environmental factor to account for material degradation is taken as  $C_E = 0.9$ , as 268 269 recommended in ACI 440.1R for carbon FRP bars, as the outer material of the DHFRP bars 270 considered is carbon. The reinforcement ratios for the slabs varied from 0.003-0.009, with the 271 highest values associated with the greatest girder spacings as well as the bars with chopped fiber 272 layers (B4, B5), as expected. Slab ductility indices varied from approximately 3-4 when 273 reinforced with bars B1, B2, and B5, and from 5-6 when reinforced with bars B3 and B4. The 274 upper range of these ductility indices are higher than equivalent slabs reinforced with steel, 275 which is a result of the large post 'yield' (i.e. after first material failure) deformations of DHFRP-reinforced slabs, which are typically greater than those of corresponding steel-276 277 reinforced sections.

278 For the building beam, three span lengths of 6, 7.6, and 9.1 m (20, 25, and 30 ft), were considered, with  $f_c' = 38$  MPa (5500 psi). A rectangular, simple-span beam was considered for 279 280 analysis; T-beams and continuous members were found to have no significant effect on 281 reliability results. The beam width was approximately 405 mm (16 in) for the 6 m span and 510 282 mm (20 in) for the longer spans. Beam height was selected to satisfy the minimum 283 recommendation given in ACI-440.1R for non-prestressed FRP-reinforced beams (1/10 of span 284 length for simply supported beams). The beam is designed to satisfy the same strength 285 requirements for tension-controlled members reinforced with steel bars. The relevant flexural design equation is  $\phi M_n = 1.2M_{DL} + 1.6M_{LL}$ , where  $M_{DL}$  and  $M_{LL}$  are the dead and live load 286 287 moments, respectively. The beam was loaded with a dead load to total load (D/(D+L)) ratio of approximately 0.5. Decreasing this ratio did not change results, while increasing this ratio beyond 0.5 generally resulted in slight decreases in reliability, as similar to the results found by Szersen and Nowak (2003) for steel-reinforced beams. Resulting DHFRP reinforcement ratios were from 0.004-0.005, with the same bar diameters used as for the bridge deck. Ductility indices ranged from approximately 3-3.4 for beams reinforced with bars *B1* and *B2*, and from approximately 5-6 when reinforced with bars *B3*, *B4*, and *B5*.

294

#### 295 Reliability Analysis

296 Resistance random variables (RVs) pertinent for moment capacity analysis of DHFRP-297 reinforced concrete members include those that account for variations in material and resin properties such as volume fractions (v), moduli of elasticity (E), and failure strains ( $\varepsilon_{f}$ ); 298 299 concrete compressive strength  $(f_c)$ ; reinforcement depth (d); and the professional factor (P), 300 which is the ratio of actual section capacity to the capacity predicted by analysis. Additional 301 RVs specific to select cases include beam width (b) for building beams, and steel core yield 302 strength ( $\sigma_v$ ) for cases that consider bar B5. RV statistical parameters relevant to this study are 303 coefficient of variation, V, bias factor  $\lambda$  (ratio of mean to nominal value), and distribution type, 304 and are given in Table 3. To maintain consistency with previous code calibration efforts, load 305 and resistance RVs for building beam cases are taken from Nowak and Szerszen (2003), as used 306 to calibrate the ACI 318 Code; bridge deck RVs are taken from Nowak (1999), as used for the 307 AASHTO LRFD Code calibration; and FRP RV data are taken from Shield et al. (2011), as used 308 for the ACI 440.1R calibration, as well as from Eamon and Rais-Rohani (2008). For the bridge 309 slab, load RVs include dead load of the slab (DS), wearing surface (DW), and parapets (DP), and 310 truck wheel live load (*LL*); while for the building beam, load RVs are dead load (*DL*) and 311 transient live load (50-year maximum). These values are shown in Table 4.

312 For reliability analysis, the relevant limit state is:  $g = M - M_a$ . Failure is defined when 313 flexural member moment capacity M exceeds maximum applied moment on the flexural member 314  $M_a$  (i.e. when  $g \leq 0$ ). M is defined as  $M_c P$ , where  $M_c$  is the moment capacity of the section, as 315 given by eqs. 1 or 2, as appropriate for the DHFRP bar type used, and corresponds to the first 316 peak of the moment-curvature diagram in Figure 3. *M* is a function of the resistance RVs given 317 in Table 3, while P is the professional factor given in Table 3.  $M_a$  is the applied moment effect, 318 as a function of the dead and live load RVs given in Table 4. Note for consistency with existing 319 code calibration efforts, the reliability analysis in this study is similarly based on strength, 320 although serviceability limits typically govern design. Probability of failure  $p_f$  of the limit state 321 for each case considered was calculated with Monte Carlo simulation, then transformed to reliability index  $\beta$  with  $\beta = -\Phi^{-1}(p_f)$ . As the MCS procedure progressed, the number of 322 simulations was increased until  $\beta$  converged, which occurred close to  $2x10^6$  simulations for most 323 324 cases.

For each flexural member considered, a resistance factor  $\phi$  is determined for design that is required for the reliability index of the member to meet the minimum target of 3.5, as used for the *AASHTO LRFD* as well as *ACI-318* Code calibrations (Nowak 1999; Szerszen and Nowak 2003). It was found that designs with DHFRP bars using the resistance factor of 0.55 specified by *ACI 440.1R* for tension controlled sections resulted in reliability indices near 3.9, an overdesign from the target of 3.5 for ductile sections. This finding is close to that found for tension-controlled designs considering non-ductile FRP, for which Shield et al. (2011) estimated reliability indices from 3.5 to 4.8 when using  $\phi = 0.55$ . For *ACI 440.1R*, however,  $\phi$  was not increased due to the non-ductile failures anticipated with traditional FRP.

- 334
- 335 Results

336 The results are presented in Tables 5 and 6, which show the final reliability indices and 337 corresponding resistance factors needed. For both the bridge deck as well as the building beam, 338 to achieve the target reliability index of 3.5, it appears that  $\phi$  can be increased to approximately 339 0.61-0.64, above the current value of 0.55 specified for non-ductile FRP bars. For comparison, 340 the calculations were repeated to determine resistance factors needed to obtain higher reliability 341 indices of 3.75 and 4.0. Similar results were found to those in Tables 5 and 6, but with a typical 342  $\phi$  of 0.58 (with a range of 0.57-0.60 for all cases) required for a reliability index of 3.75, and a  $\phi$ 343 of 0.52 (with a range of 0.51-0.53 for all cases) required for a reliability index of 4.0.

344 Although the resistance factor range of 0.61-0.64 is above that specified for non-ductile 345 bars, it is still much below the 0.90 for tension controlled, steel-reinforced members needed to 346 produce the same target reliability index of 3.5. Clearly then, if designed with the same 347 reduction factor, a steel-reinforced member would be significantly more safe than one using 348 FRP. It should be note that this discrepancy in safety level is not related to ductility, and is 349 observed only from consideration of moment capacity. It is a direct result of the different levels 350 of uncertainty inherent in steel as opposed to DHFRP (or FRP) reinforcement, as described by 351 the different statistical parameters of critical reinforcement random variables.

Here there are three important differences in variability: reinforcement geometry, reinforcement stiffness, and analytical prediction of moment capacity. With regard to reinforcement geometry, the variation in cross-sectional area of steel reinforcement is negligible,

355 and is generally taken as deterministic in reliability analysis (Nowak and Szerszen 2003). 356 However, for DHFRP bars, variation in material volume fractions has a significant effect on 357 reliability. Similarly, as variations in reinforcement elastic modulus do not affect the capacity 358 calculation of steel-reinforced sections, these uncertainties do affect DHFRP-reinforced section 359 moment capacity, as per eqs. 1 and 2. Finally, the professional factor P considered for FRP reinforced sections ( $\overline{P} = 0.89$ ,  $V_P = 0.16$ ) not only has a lower mean value but much greater 360 variability than P used for steel-reinforced members ( $\overline{P} = 1.02$ ,  $V_P = 0.06$ ) (Shield et al. 2011: 361 362 Nowak and Szerszen 2003). Each of these changes in RV statistical parameters serves to lower 363 the reliability of DHFRP-reinforced sections.

364

#### 365 Conclusions

366 Resistance factors needed for tension controlled DHFRP-reinforced flexural members to 367 meet ACI 318 and AAASTHO LRFD target reliability levels were estimated with a reliability 368 analysis and calibration process. Using the models considered, it was found that the resistance 369 factor has the potential to be increased above the currently specified value of 0.55 for tension 370 controlled members reinforced with non-ductile FRP bars. Recall that the range of resistance 371 factors specified by ACI 440.1R for non-ductile FRP bars (0.55-0.65) varies due to the expected 372 failure mode, where compression controlled failures correspond to  $\phi = 0.65$  and tension-373 controlled FRP-reinforced beams are given  $\phi = 0.55$ . The use of DHFRP bars, however, 374 practically only concerns tension-controlled failures. That is, it is appealing to use DHFRP bars 375 only in tension-controlled members, where bar ductility could be taken advantage of in a failure. 376 In this case, rather than specifying a resistance factor of 0.55, the findings of this study suggest 377 that  $\phi$  might be reasonably increased to a value between 0.61-0.64. This is not a large increase,

378 but is a significant difference, particularly given the relatively high cost of FRP. If DHFRP bars 379 are used in compression-controlled sections, the properties of the DHFRP bars do not 380 significantly affect the reliability analysis, and it can be demonstrated that  $\phi$  should 381 appropriately remain unaltered at 0.65, as specified for all concrete-controlled failures. Thus, 382 using DHFRP bars, a linear interpolation might be made between 0.65 for compression 383 controlled failures to a value between (0.61-0.64) for tension-controlled failures, based on 384 reinforcement ratio, rather than from 0.65 to 0.55 as for non-ductile bars. The specific choice of 385 an appropriate  $\phi$  value for a tension-controlled condition (i.e. perhaps between 0.61-0.64) is an 386 issue in need of further study, as this directly effects the target reliability index. In this study, the 387 target index of 3.5 for steel-reinforced beams was considered as a baseline for comparison due to 388 the ability of DHFRP-reinforced sections to meet ductility indices and tensile strains similar to 389 steel-reinforced beams at section ultimate capacity. However, it can be argued that due to other 390 performance differences between DHFRP and steel (such as, the inability of the DHFRP-391 reinforced section to behave in a ductile manner for more than a single overload, which is clearly 392 disadvantageous for cyclic forces), a different target level may be deemed appropriate. Raising 393 this target level would provide the need for a lower range of resistance factors.

Although strength and ductility requirements can be addressed, an additional consideration with the use of DHFRP, as well as non-ductile FRP bars, is cracked section stiffness for cost-effective bar configurations. As the effective elastic modulus of DHFRP reinforcement is lower than that of steel, deeper sections as well as higher concrete strengths are generally required to simultaneously meet strength, ductility, as well as deflection constraints. For the girder spacings considered, this required minimum bridge deck thicknesses from 200400 250 mm (8-10 in). For building beams, it is suggested that ACI 440.1R recommendations are
401 used to establish minimum depths.

The results of this study suggest that an increase in resistance factor for tension controlled, DHFRP-reinforced flexural members may be warranted. However, for better statistical quantification, additional experimental research data is desirable for DHFRP-specific random variables, including fabrication and manufacturing variations as well as professional factor. A larger database of experimental results would allow greater refinement of the results found in this study.

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Bar Number:	<i>B1</i>	<i>B2</i>	<i>B3</i>	<i>B4</i>	B5
No. of Layers:	2	3	4	4	4
IMCF-I*	-	-	-	0.189	0.147
IMCF- II	0.29	0.20	0.20	-	-
SMCF-I	-	0.06	0.07	-	-
SMCF-II*	-	-	-	0.0875	0.063
AKF-I	-	-	-	0.04	0.10
AKF-II	0.29	0.25	0.10	-	-
EGF	-	-	0.17	0.06	-
Steel	-	-	-	-	0.20
Resin	0.42	0.49	0.64	0.6235	0.49

#### Table 1. Material Volume Fractions in Considered DHFRP Bars 543

544

\*Chopped fiber layers

Label	Material	E GPa (ksi)	$\mathcal{E}_{u}$
IMCF-I	IM-Carbon Fiber Type I	650 (94000)	0.0045
IMCF-II	IM-Carbon Fiber Type II	400 (58000)	0.0050
SMCF-I	SM-Carbon Fiber Type I	238 (34500)	0.0150
SMCF-II	SM-Carbon Fiber Type II	230 (33400)	0.0150
AKF-I	Aramid Kevlar-49 Fiber Type I	125 (18000)	0.0250
AKF-II	Aramid Kevlar-49 Fiber Type II	102 (15000)	0.0250
EGF	E-Glass fiber	74 (11000)	0.0440
Steel	Steel, Grade 60	200 (29000)	0.0021*
Resin	Ероху	3.5 (540)	0.0600
	IMCF-I IMCF-II SMCF-I SMCF-II AKF-I AKF-I EGF Steel	IMCF-IIM-Carbon Fiber Type IIMCF-IIIM-Carbon Fiber Type IISMCF-ISM-Carbon Fiber Type ISMCF-IISM-Carbon Fiber Type IIAKF-IAramid Kevlar-49 Fiber Type IAKF-IIAramid Kevlar-49 Fiber Type IIEGFE-Glass fiberSteelSteel, Grade 60	IMCF-I         IM-Carbon Fiber Type I         650 (94000)           IMCF-II         IM-Carbon Fiber Type II         400 (58000)           SMCF-I         SM-Carbon Fiber Type I         238 (34500)           SMCF-II         SM-Carbon Fiber Type I         230 (33400)           AKF-I         Aramid Kevlar-49 Fiber Type I         125 (18000)           AKF-II         Aramid Kevlar-49 Fiber Type II         102 (15000)           EGF         E-Glass fiber         74 (11000)           Steel         Steel, Grade 60         200 (29000)

# 545 Table 2. DHFRP Bar Material Properties

546 \*Yield strain is given for steel, not ultimate.

RV*	Description	V	λ
V <sub>IM-Carbon</sub>	Volume fraction of IM-Carbon	0.05	1.00
V <sub>SM-Carbon</sub>	Volume fraction of SM-Carbon	0.05	1.00
V <sub>Kevlar-49</sub>	Volume fraction of Kevlar-49	0.05	1.00
$\mathcal{V}_{E-Glass}$	Volume fraction of E-Glass	0.05	1.00
V <sub>Steel</sub>	Volume fraction of steel	0.05	1.00
V <sub>resin</sub>	Volume fraction of resin	0.05	1.00
$E_{\rm IM-Carbon}$	Modulus of elasticity of IM-Carbon	0.08	1.04
$E_{\rm SM-Carbon}$	Modulus of elasticity of SM-Carbon	0.08	1.04
$E_{\rm Kevlar-49}$	Modulus of elasticity of Kevlar-49	0.08	1.04
$E_{E-glass}$	Modulus of elasticity of E-glass	0.08	1.04
$E_{resin}$	Modulus of elasticity of resin	0.08	1.04
$\sigma_{y}$	Yield strength of steel	0.06	1.14
$\mathcal{E}_{f_1}$	Failure Strain of IM-Carbon	0.05	1.20
$f_c'$	Compressive strength of concrete	0.10	1.14
d	Depth of reinforcement	0.04	0.99
b	Building beam width	0.04	1.01
Р	Professional factor	0.16	0.89

**Table 3. Resistance Random Variables** 

551	Table 4. Luau	Kalluolli vallables		
	RV*	Description	V	λ
	Bridge Slab			
	DS	Dead load, slab	0.10	1.05
	DW	Dead load, wearing surface	0.25	1.00
	DP	Dead load, parapet	0.10	1.05
	LL	Truck wheel load	0.18	1.20
	Building Beam			
	DL	Dead load	0.10	1.00
	LL	Live load	0.18	1.00
552	*All RVs are norma	al except building live load, which is	extreme	type I.
553				
554				
555				
556				
557				
558				
559				

# **Table 4. Load Random Variables**

Beam Spacing (m)	В	1	E	32	В	3	В	4	В	5
+/- Moment	β	$\phi$								
1.8 (+M)	3.50	0.64	3.51	0.63	3.51	0.63	3.52	0.63	3.50	0.63
1.8 (- M)	3.50	0.63	3.50	0.61	3.50	0.61	3.51	0.64	3.50	0.61
2.7 (+M)	3.50	0.64	3.51	0.63	3.50	0.63	3.52	0.62	3.50	0.61
2.7 (- M)	3.51	0.63	3.50	0.63	3.50	0.61	3.50	0.61	3.51	0.62
3.0 (+M)	3.52	0.63	3.50	0.62	3.50	0.62	3.51	0.61	3.50	0.63
3.0 (- M)	3.50	0.63	3.52	0.63	3.50	0.62	3.52	0.64	3.51	0.62

**Table 5. Resistance Factors for Bridge Deck** 

	E	81	E	32	В	3	В	4	В	5
span (m)	β	$\phi$								
6.0	3.50	0.60	3.50	0.61	3.50	0.61	3.50	0.62	3.52	0.62
7.6	3.50	0.62	3.50	0.63	3.52	0.63	3.51	0.63	3.50	0.65
9.1	3.51	0.64	3.50	0.63	3.50	0.64	3.50	0.63	3.52	0.63

**Table 6. Resistance Factors for Building Beam**