

Accurate Vertical Excitation Energies of BODIPY/Aza-BODIPY Derivatives from Excited-State Mean-Field Calculations

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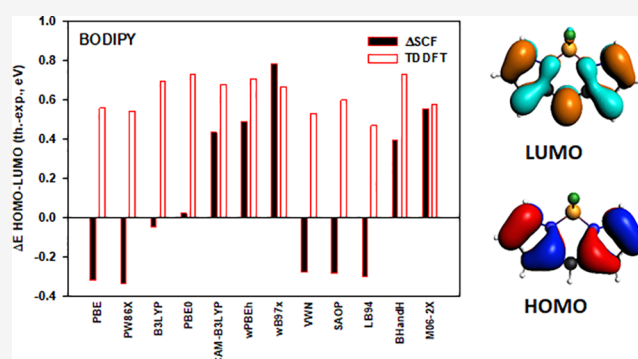
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ABSTRACT: We report a benchmark study of vertical excitation energies and oscillator strengths for the HOMO → LUMO transitions of 17 boron–dipyrromethene (BODIPY) structures, showing a large variety of ring sizes and substituents. Results obtained at the time-dependent density functional theory (TDDFT) and at the delta-self-consistent-field (Δ SCF) by using 13 different exchange correlation kernels (within LDA, GGA, hybrid, and range-separated approximations) are benchmarked against the experimental excitation energies when available. It is found that the time-independent Δ SCF DFT method, when used in combination with hybrid PBE0 and B3LYP functionals, largely outperforms TDDFT and can be quite competitive, in terms of accuracy, with computationally more costly wave function based methods such as CC2 and CASPT2.



I. INTRODUCTION

Boron–dipyrromethenes (BODIPYs), together with their derivatives where the *meso*-carbon atom is substituted by a nitrogen (aza-BODIPYs), constitute an important class of organic dyes,¹ due to the large number of potential applications in numerous fields (see Figure 1 for a sketch of the parent molecule 8-H-BODIPY). Research in these compounds (both experimental and *in-silico*) has sparked in the past decade due to their interesting photophysical properties, such as intense and narrow fluorescence peaks with high quantum yield, and to the ease with which one can

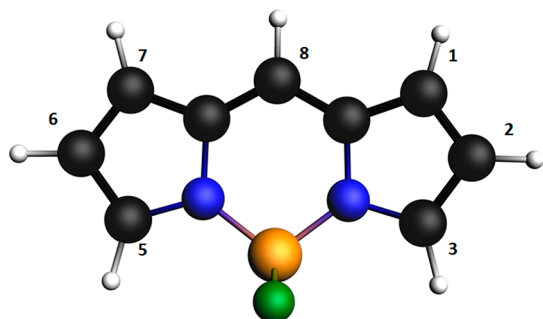


Figure 1. Structure of 8-H-BODIPY (4,4-difluoro-4-bora-3a,4a-diaza-s-indacene) together with a numbering scheme. The *meso* position is position 8. C atoms are in black color, N atoms in blue, H atoms in white, B atoms in orange, and F atoms in green.

play with various substituents to influence their spectroscopic and photophysical signatures.^{1,2} BODIPYs find application in optoelectronics,³ electrochemistry and electroluminescence,⁴ nanomedicine,⁵ photodynamic therapy,^{6–9} photochemical signaling,¹⁰ dye-sensitized solar cells,^{11–13} and fluorescence and cellular imaging.^{14,15}

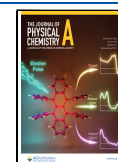
Since BODIPYs are medium to large molecules, time-dependent density functional theory^{16,17} (TDDFT) is the method of choice to investigate their spectroscopic properties, together with a selection of explicit wave function methods such as second-order approximate coupled-cluster,^{18–20} CC2, and multiconfigurational CAS-PT2.²¹ Compared to the latter methods, TDDFT still is computationally much more affordable, also because basis-set requirements for DFT are much less demanding than explicit wave function methods.²² Clearly the selection of a large enough active space proves crucial for the accuracy of CAS-PT2 estimates,²³ and it can severely limit its applicability to even medium-size systems.

Unfortunately in this class of molecules TDDFT excitation energies suffer from low accuracy (>0.3 eV), together with a

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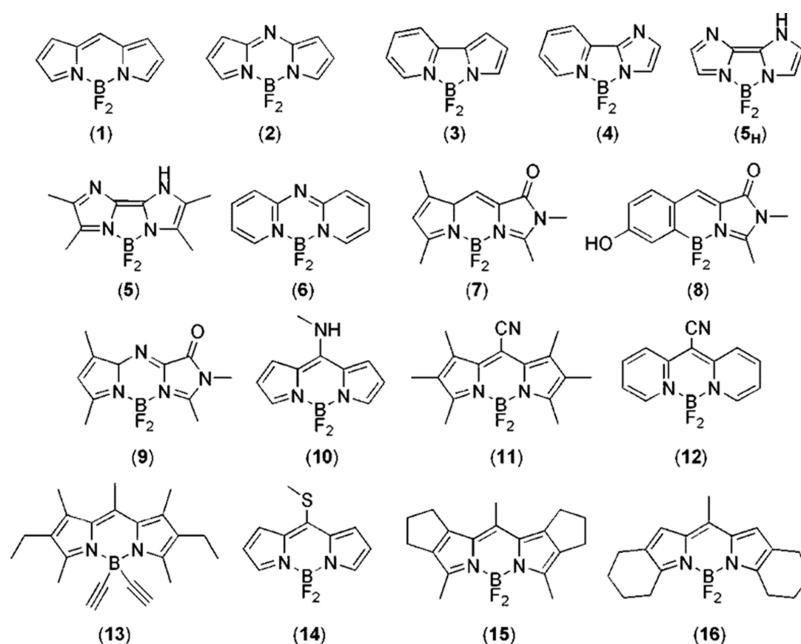


Figure 2. Chemical structures of BODIPYs and aza-BODIPYs considered in this work. Reprinted with permission from ref 39. Copyright 2015 American Chemical Society. The numbering follows that adopted by Momeni and Brown.³⁹

strong dependence of the results on the particular xc potential used,²⁴ when applied to even the lowest $\pi \rightarrow \pi^*$ excitations.²⁵ This observation applies both to excitation energies calculated within the vertical approximation, which is of widespread use in the dye community, and to computed adiabatic excitation energies with inclusion of solvent effects.^{26,27} TDDFT has well-known shortcomings when dealing with charge-transfer (CT) excitations^{28,29} and, due to the commonly adopted adiabatic approximation to the xc kernel,¹⁷ with excitations involving double-excitation character. While the former issue has been somewhat mitigated with the introduction of range-separated functionals, the latter cannot easily be cured within standard TDDFT. To bypass this problem, Boulanger et al.³⁰ proposed a protocol where vertical excitation energies were calculated with the Bethe–Salpeter formalism or with the scaled opposite spin (SOS) CIS(D) method,³¹ which adds a perturbative correction for double excitations on top of a CIS calculation.²⁶ Actually the importance of double excitations for the description of low-lying excited states is not restricted to BODIPYs and related families,^{32,33} but it appears to be related to the presence of boron in the molecular skeleton and has been recently evidenced in a series of works focused on near-edge X-ray absorption of boroxine-containing compounds.^{34–37} In particular, it was shown in refs 35 and 36 that while transition-state (TS) and TDDFT methods with a selection of xc potentials ranging from GGA to global, meta-separated, and range-separated hybrids fail to account for the correct intensity distribution of the lowest two spectral features, assigned to π^* valence core excited states, a qualitatively correct description was obtained with a computationally inexpensive Δ SCF procedure.³⁵ This observation, together with a recent publication by Worster et al.,³⁸ which showed that Δ SCF is able to predict excitation energies with an accuracy competitive with and sometimes better than that of TDDFT, prompted us to benchmark Δ SCF against TDDFT on a series of 17 BODIPYs and aza-BODIPYs considered by Momeni and Brown³⁹ and Feldt and Brown⁴⁰ (see Figure 2) in the quest for an accurate yet efficient mean-field method that

could be used for a fast screening of candidate dyes for a specific application. In this work, the accuracy of the Δ SCF method is explored and contrasted with that of TDDFT for a quite extensive range of xc potentials. It will be shown that the simple Δ SCF method, coupled with a rational choice of the xc potential, is able to predict vertical excitation energies of BODIPYs and aza-BODIPYs with an accuracy superior to TDDFT and comparable to that of the computationally much more demanding correlated wave function methods.

The plan of the paper is the following: in Section II we provide a brief overview of the theory and of the computational details. Section III is devoted to a discussion of the benchmark of vertical excitation energies against both TDDFT and experimental values, while our conclusions are presented in the final section, section IV.

II. THEORY AND COMPUTATIONAL DETAILS

Excitation energies and oscillator strengths have been calculated at the TDDFT level, in the nonrelativistic approximation, as implemented in the ADF code^{41–43} and within the adiabatic local density approximation¹⁷ (ALDA) to the exchange–correlation (xc) kernel.

In linear response TDDFT, excitation energies and intensities are obtained through the solution of the following eigenvalue equation by means of Davidson’s iterative algorithm:⁴⁴

$$\Omega F_I = \omega_I^2 F_I \quad (1)$$

Here the elements of the Ω matrix are given by

$$\Omega_{ia\sigma, bj\tau} = \delta_{\sigma\tau} \delta_{ij} \delta_{ab} (\epsilon_a - \epsilon_i)^2 + 2\sqrt{(\epsilon_a - \epsilon_i)} \frac{\partial F_{ia}}{\partial P_{jb}} \sqrt{(\epsilon_b - \epsilon_j)} \quad (2)$$

In eq 2, indices i and j run over the set of occupied molecular orbitals (MOs) in the KS ground-state, while indices a and b run over the set of virtual MOs; ϵ_i and ϵ_a are the KS molecular orbital energies. F and P represent the Fock matrix

Table 1. Δ SCF and TDDFT Vertical Excitation Energies and Oscillator Strengths for the HOMO \rightarrow LUMO Transition of **1**, for a Selection of DFT xc Potentials^a

XC	Δ SCF		TDDFT		
	ϵ (eV)	f	ϵ (eV)	f	dominant excitations
BLYP	2.121 (−0.339)	0.48	3.003 (0.543)	0.16	0.49 H \rightarrow L + 0.50 (H−1) \rightarrow L
PBE	2.141 (−0.319)	0.48	3.017 (0.557)	0.15	0.48 H \rightarrow L + 0.51 (H−1) \rightarrow L
PW86X	2.123 (−0.337)	0.48	3.003 (0.543)	0.15	0.48 H \rightarrow L + 0.51 (H−1) \rightarrow L
B3LYP	2.414 (−0.046)	0.51	3.151 (0.691)	0.40	0.84 H \rightarrow L + 0.15 (H−1) \rightarrow L
PBE0	2.482 (0.022)	0.51	3.186 (0.726)	0.44	0.87 H \rightarrow L + 0.11 (H−1) \rightarrow L
CAM-B3LYP	2.894 (0.434)	0.54	3.137 (0.677)	0.52	0.94 H \rightarrow L + 0.037 (H−1) \rightarrow L
wPBEh	2.950 (0.490)	0.51	3.167 (0.707)	0.51	0.94 H \rightarrow L + 0.039 (H−1) \rightarrow L
wB97x	3.242 (0.782)	0.56	3.124 (0.664)	0.52	0.95 H \rightarrow L + 0.021 (H−1) \rightarrow L
VWN	2.184 (−0.276)	0.50	2.991 (0.531)	0.15	0.48 H \rightarrow L + 0.51 (H−1) \rightarrow L
SAOP	2.178 (−0.283)	0.49	3.058 (0.598)	0.23	0.61 H \rightarrow L + 0.37 (H−1) \rightarrow L
LB94	2.159 (−0.302)	0.49	2.93 (0.467)	0.18	0.56 H \rightarrow L + 0.43 (H−1) \rightarrow L
BHandH	2.855 (0.395)	0.55	3.189 (0.729)	0.54	0.95 H \rightarrow L + 0.03 (H−1) \rightarrow L
M06-2X	3.014 (0.554)	0.59	3.036 (0.576)	0.50	0.95 H \rightarrow L + 0.03 (H−1) \rightarrow L

^aThe differences with respect to the experimental value of 2.46 eV are also reported in parentheses. The CASPT2/cc-pVDZ value of the vertical excitation energy is 2.538 eV.³⁹ For TDDFT, the eigenvector corresponding to the lowest energy root is also reported (H, HOMO; L, LUMO).

and the density matrix, respectively, whereas $\frac{\partial E_{ia}}{\partial P_{jb}}$ are the elements of the so-called “coupling matrix”, K , which can be written as a sum of a Hartree (Coulomb) part plus the xc part as follows:

$$K_{ia\sigma,bj\tau} = K_{ia\sigma,bj\tau}^{Coul} + K_{ia\sigma,bj\tau}^{xc} \quad (3)$$

Eigenvalues ω_i^2 in eq 1 correspond to squared excitation energies, while the oscillator strengths are extracted from the eigenvectors F_i according to standard TDDFT.¹⁷

Excitation energies and oscillator strengths for the HOMO \rightarrow LUMO transition have been also calculated at the Δ SCF level. In the Δ SCF method, the initial (Ψ_i) and final (Ψ_f) N -electron wave functions entering the dipole matrix element (computed in the length gauge of the dipole operator)

$$\mu_{i \rightarrow f} = \langle \Psi_f | \hat{\mu} | \Psi_i \rangle \quad (4)$$

are Slater determinants constructed from Kohn–Sham molecular orbitals (MOs) obtained with the SCF procedure relative to the ground state (GS) and excited state occupation numbers, respectively. The GS MOs are obtained from a spin-restricted calculation, while the excited-state MOs are calculated within a spin-polarized scheme with $N_\alpha - N_\beta = 0$, where N_α and N_β denote the number of spin-up and spin-down electrons, respectively. In the specification of the occupation numbers, we removed a β electron from the HOMO. Singlet excitation energies are obtained according to the spin-purification formula.⁴⁵ Denoting with S_{fi} the overlap matrix between the two sets of occupied MOs, $(S_{fi})_{\lambda\mu} = \langle \varphi_\lambda^f | \varphi_\mu^i \rangle$, $\mu_{i \rightarrow f}$ of eq 4 can be written as

$$\langle \Psi_f | \hat{\mu} | \Psi_i \rangle = \sum_{\lambda\mu} \langle \varphi_\lambda^f | \hat{\mu} | \varphi_\mu^i \rangle \text{adj}(S_{fi})_{\lambda\mu} \quad (5)$$

in terms of dipole matrix elements between the two sets of MOs and the adjugate of S_{fi} (i.e., the transpose of its cofactor matrix). When $\langle \Psi_f | \Psi_i \rangle = \det(S_{fi}) \neq 0$, eq 5 reduces to

$$\langle \Psi_f | \hat{\mu} | \Psi_i \rangle = \det(S_{fi}) \sum_{\lambda\mu} \langle \varphi_\lambda^f | \hat{\mu} | \varphi_\mu^i \rangle (S_{fi}^{-1})_{\lambda\mu} \quad (6)$$

Since Ψ_i and Ψ_f do not need to be orthogonal, as they are the wave functions of fictitious systems, their use in the

calculation of transition properties must be carefully justified. We always checked that, when not dictated by symmetry consideration, the overlap of the initial and final wave functions, $\langle \Psi_f | \Psi_i \rangle$, is actually very small (see Tables S18 and S19 of the Supporting Information). Moreover we always enforced the origin independence of the transition matrix elements by adding the dipole of the nuclear charges, weighted by the overlap $\langle \Psi_f | \Psi_i \rangle$. Even if this procedure does not eliminate the transition charge, results of a recent study³⁸ on an extensive set of medium-size molecules indicate that this simple correction gives dipole moments nearly identical with those obtained by enforcing exact orthogonality of Ψ_i and Ψ_f .

The equilibrium structures of the systems investigated, reported in Figure 2, have been optimized at the DFT level by using the PBE0^{46–48} xc functional and the triple ζ polarized (TZP) basis set of Slater type orbitals (STOs) from the ADF database. During the geometry optimization we did not impose any symmetry constraints. For both TDDFT and Δ SCF calculations, excitation energies and oscillator strengths have been calculated for the following classes of xc potentials: LDA VWN,⁴⁹ GGA LB94,⁵⁰ PBE,^{46,47} BLYP,^{51–53} PW86x,⁵⁴ hybrid B3LYP,^{52,55,56} PBE0,^{48,57} BHandH,⁵⁸ the meta-hybrid M06-2x,⁵⁹ and the range-separated hybrid (RSH) CAM-B3LYP.⁶⁰ In addition, two more recent range-separated hybrid functionals with the correct asymptotic potential, namely ω PBEh⁶¹ and ω B97x,⁶² have been tested as well. However, since they provide results that are of similar accuracy of CAM-B3LYP, we only include them in the Supporting Information. In Table S1, we compare, for TDDFT, the accuracy of the three range separated hybrid functionals in predicting the first vertical excitation energy for all the systems included in the benchmark study. As it appears from the statistical analysis reported in Table S1, ω PBEh and ω B97x RSH potentials provide results that are not more accurate than CAM-B3LYP. Furthermore, for BODIPY, we also optimally tuned^{63,64} two different long-range corrected potentials making use of the PLAMS Python library of ADF, namely LCY-PBE,⁶⁵ and CAMY-B3LYP.⁶⁶ However, the results for the first vertical excitation energy (CAMY-B3LYP, 3.153 eV, $\gamma_{\text{opt}} = 0.55$; LCY-PBE, 3.128 eV, $\gamma_{\text{opt}} = 0.35$) are comparable to those obtained with the three RSH potentials without optimal tuning. Optimal tuning the range separation of RSH potentials is therefore not further

Table 2. TDDFT Data for the Lowest Vertical Energy Transition in the Entire Molecular Dataset Considered in This Work, together with a Statistical Analysis of the Results^a

XC type	LDA	model		GGA			hybrid			meta-hybrid	RSH
	VWN	SAOP	LB94	BLYP	PBE	PW86X	B3LYP	PBE0	BHandH	M06-2X	CAM-B3LYP
1	2.991	3.058	2.927	3.003	3.017	3.003	3.151	3.186	3.189	3.036	3.137
2	2.710	2.758	2.643	2.728	2.740	2.725	2.888	2.920	2.894	2.765	2.851
3	2.789	2.864	2.659	2.796	2.816	2.803	3.216	3.330	3.672	3.675	3.637
4	2.835	2.891	2.711	2.835	2.851	2.841	3.277	3.393	3.772	3.562	3.748
5	3.627	3.664	3.484	3.654	3.675	3.659	3.876	3.952	4.129	4.043	4.093
S _H	4.063	4.075	3.903	4.059	4.088	4.071	4.267	4.344	4.524	4.412	4.467
6	3.286	3.382	3.237	3.290	3.310	3.293	3.595	3.677	3.880	3.723	3.799
7	2.987	3.055	2.914	2.994	3.008	2.997	3.127	3.165	3.241	3.075	3.178
8	3.008	3.097	2.946	3.021	3.032	3.021	3.267	3.333	3.543	3.373	3.475
9	2.842	2.886	2.745	2.849	2.863	2.851	2.962	2.988	3.014	2.869	2.963
10	3.236	3.281	3.129	3.237	3.259	3.243	3.418	3.477	3.609	3.462	3.545
11	2.380	2.478	2.332	2.422	2.424	2.415	2.625	2.658	2.684	2.558	2.648
12	2.843	2.922	2.751	2.851	2.866	2.852	3.173	3.256	3.496	3.343	3.428
13	2.751	2.777	2.635	2.760	2.774	2.765	2.921	2.950	2.985	2.822	2.938
14	2.937	3.005	2.888	2.944	2.959	2.945	3.092	3.131	3.167	3.017	3.115
15	2.689	2.788	2.633	2.728	2.728	2.721	2.929	2.965	3.0185	2.856	2.968
16	2.692	2.757	2.633	2.719	2.726	2.732	2.845	2.875	2.900	2.758	2.859
MAE	0.359	0.401	0.342	0.368	0.373	0.368	0.471	0.509	0.589	0.474	0.541
MAE ^b	0.297	0.345	0.272	0.308	0.313	0.307	0.444	0.492	0.601	0.466	0.548
max AE	1.340	1.284	1.464	1.340	1.324	1.334	0.898	0.782	0.814	0.664	0.762
max AE ^b	0.584	0.652	0.600	0.591	0.606	0.592	0.739	0.778	0.814	0.664	0.762
min AE	0.013	0.048	0.004	0.026	0.037	0.026	0.043	0.071	0.386	0.274	0.329
min AE ^b	0.013	0.048	0.004	0.026	0.037	0.026	0.043	0.071	0.386	0.274	0.329
SD	0.295	0.278	0.320	0.295	0.293	0.294	0.214	0.191	0.127	0.104	0.116
SD ^b	0.169	0.174	0.159	0.172	0.177	0.173	0.191	0.183	0.122	0.101	0.116
R ²	0.495	0.494	0.447	0.487	0.491	0.491	0.687	0.728	0.843	0.824	0.858
R ² ^b	0.797	0.805	0.761	0.798	0.801	0.800	0.908	0.925	0.958	0.970	0.965

^aReported are the mean absolute error (MAE), maximum and minimum AE (max AE and min AE, respectively), the standard deviation (SD), and the correlation coefficient (R^2) between theoretical vertical excitation energies and experimental values. Energies in eV. ^bStatistics obtained by removing molecule **4** from the data set.

pursued in the present work. We also tested the model potential SAOP,^{67,68} which, together with LB94, should afford excitation energies somewhat more accurate than the standard GGA potentials.

III. RESULTS AND DISCUSSION

The set of molecules considered in the present work are those reported in the works of refs 39 and 40. Except for molecule **4** (see Figure 2), for which the $\pi \rightarrow \pi^*$ excitation shows a partial CT character, for all other systems, the transition has a local excitation character (see Supporting Information for B3LYP and PBE0 HOMO and LUMO MOs plots for systems **1–16**). For all xc functionals investigated in ref 39, it was shown that TDDFT cannot provide accurate results for the HOMO \rightarrow LUMO vertical excitation (with positive deviations from experimental data greater than 0.3 eV), unless properly rescaled (for range-separated functionals). Moreover, the discrepancies with respect to experimental values could not be attributed to the neglect of solvent effects, which is estimated to be modest for all investigated systems. For correlated wave function methods, it was found that local CC2 (LCC2) and the DPLNO-STEOM-CCSD methods⁶⁹ were suitable for the computation of vertical HOMO \rightarrow LUMO excitation energies, the former method being able to afford a high linear correlation with the experimental measurements.⁴⁰ It is interesting to analyze, for the first singlet excited state calculated at the TDDFT level, the eigenvector of the Ω

matrix, which is reported for **1** in Table 1 and for all other systems in Tables S2–S17 of the Supporting Information. In Table 1, we also report, for each xc potential used, the Δ SCF and TDDFT excitation energies and their signed error compared to the experimental value. For completeness, when available, also the CASPT2/cc-pVDZ vertical excitation values reported in ref 39 are reported in all tables. Focusing for the moment our attention on **1**, an analysis of the Ω matrix first eigenvector reveals that the transition does not correspond to a pure HOMO \rightarrow LUMO excitation and that the multi-determinant character of the excitation strongly depends on the fraction of exact exchange included in the xc potential. While for all functionals the eigenvector can be described as a linear combination of HOMO \rightarrow LUMO and HOMO-1 \rightarrow LUMO single-particle excitations, the weight of the former increases roughly with the fraction of Hartree-Fock (HF) exchange in the potential, and it is a maximum for BHandH (50% of HF exchange) and for the meta-hybrid M06-2X potential (54% of HF exchange included). This trend is also reflected in the computed oscillator strength for the transition. All TDDFT functionals overestimate the excitation energy, and the disagreement with the experiment is larger for the hybrid/meta-hybrid and range-separated potentials. The trend on the signed error is different for the Δ SCF results (see also Figure S1 of the Supporting Information). For LDA GGA and model xc potentials the error is negative, and it progressively changes sign as the fraction of HF exchange included in the potential

Table 3. Δ SCF Data for the Lowest Vertical Energy Transition in the Entire Molecular Dataset Considered in This Work, together with a Statistical Analysis of the Results^a

xc	LDA	model		GGA			hybrid			meta-hybrid	RSH
	VWN	SAOP	LB94	BLYP	PBE	PW86X	B3LYP	PBE0	BHandH	M06-2X	CAM-B3LYP
1	2.184	2.178	2.159	2.121	2.141	2.123	2.414	2.482	2.855	3.036	2.894
2	1.921	1.957	1.927	1.885	1.912	1.901	2.200	2.288	2.639	2.765	2.711
3	2.943	2.972	2.935	2.892	2.915	2.893	3.135	3.196	3.487	3.675	3.479
4	3.073	3.113	3.066	3.023	3.042	3.023	3.265	3.319	3.599	3.562	3.592
5	3.209	3.339	3.237	3.197	3.222	3.201	3.525	3.623	3.989	4.043	3.974
5 _H	3.596	3.685	3.601	3.555	3.588	3.566	3.891	3.996	4.387	4.412	4.338
6	2.824	2.848	2.803	2.755	2.773	2.748	3.048	3.101	3.444	3.723	3.472
7	2.115	2.176	2.123	2.097	2.108	2.098	2.485	2.576	3.051	3.075	-
8	2.321	2.4206	2.359	2.329	2.338	2.329	2.807	2.932	3.503	3.373	3.413
9	1.917	2.007	1.946	1.919	1.934	1.929	2.311	2.415	2.868	2.869	-
10	2.702	2.684	2.653	2.615	2.643	2.621	2.847	2.910	3.223	3.462	3.255
11	1.746	1.799	1.764	1.737	1.751	1.744	2.055	2.133	2.508	2.558	2.548
12	2.509	2.526	2.467	2.438	2.449	2.426	2.702	2.745	3.086	3.343	3.087
13	2.088	2.080	2.055	2.030	2.042	2.029	2.313	2.371	2.741	2.822	2.784
14	2.236	2.220	-	2.163	2.185	2.165	2.412	2.476	2.806	3.017	-
15	2.080	2.095	2.063	2.032	2.043	2.030	2.323	2.384	2.755	2.856	-
16	1.968	1.990	1.956	1.923	1.934	1.921	2.203	2.259	2.611	2.758	2.662
MAE	0.416	0.377	0.440	0.459	0.440	0.457	0.158	0.101	0.364	0.497	0.362
MAE ^b	0.374	0.335	0.396	0.416	0.397	0.413	0.111	0.054	0.351	0.494	0.343
max AE	1.102	1.062	1.109	1.152	1.133	1.152	0.910	0.857	0.576	0.624	0.583
max AE ^b	0.674	0.5745	0.636	0.666	0.657	0.666	0.247	0.142	0.508	0.624	0.459
min AE	0.117	0.133	0.288	0.190	0.168	0.188	0.046	0.0072	0.228	0.328	0.200
min AE ^b	0.117	0.133	0.288	0.190	0.168	0.188	0.046	0.0072	0.228	0.328	0.200
SD	0.217	0.197	0.199	0.206	0.206	0.205	0.196	0.192	0.093	0.072	0.102
SD ^b	0.137	0.101	0.102	0.114	0.115	0.113	0.057	0.037	0.079	0.073	0.083
R ²	0.893	0.911	0.914	0.909	0.907	0.910	0.918	0.914	0.879	0.850	0.875
R ² ^b	0.939	0.967	0.967	0.960	0.9583	0.961	0.990	0.993	0.998	0.991	0.992

^aReported are the mean absolute error (MAE), maximum and minimum AE (max AE and min AE, respectively), the standard deviation (SD), and the correlation coefficient (R^2) between theoretical vertical excitation energies and experimental values. Energies in eV. ^bStatistics obtained by removing molecule **4** from the data set.

increases. The error is very small in magnitude for PBE0 and B3LYP, and it becomes larger for the range-separated potentials and M06-2X. On the other hand, the computed oscillator strength of the transition is less dependent on the particular xc potential used. The fact that the linear-response TDDFT shows a strong dependency of predicted excitation energies and oscillator strengths on the xc functional used can be traced back to the interplay between the Hartree and xc terms of the coupling matrix of eq 3. It is also interesting to note that the multideterminantal nature of the first excited state (S_1) was clearly revealed in the analysis of the CI eigenvector of the CASSCF/cc-pVDZ results reported in ref 39. Also, at the CASSCF level, S_1 can roughly be described as a linear combination of HOMO \rightarrow LUMO and HOMO-1 \rightarrow LUMO excitations, but the coefficients of doubly excited determinants are not negligible, both in the excited state and in the ground state. Even if the CASSCF wave function cannot afford an accurate description of the excited state wave function, it is clear that the importance of doubly excited states can be used to explain the poor performance of TDDFT in this class of systems. We note here that the effect of double and higher excitations can at least be partly described at the Δ SCF level, where excited state orbitals are self-consistently determined and can be used in principle as a better reference determinant for the excited state than single excitations built from the ground state reference KS determinant. The fact that orbital relaxation cannot be properly described only by single

excitations out of the KS reference wave function can explain the higher accuracy, compared to TDDFT, of the excitation energies and oscillator strengths computed at the Δ SCF level, the latter being, for every system studied, quite close to the CASPT2 estimates (see also Tables S2–S17 of the Supporting Information). By inspecting the signed error of TDDFT and Δ SCF as a function of the xc potential for the other systems (Figures S2–S17 of the Supporting Information), some interesting trends can be identified. For the majority of the systems, an analysis of the errors similar to that of **1** can be made: TDDFT overestimates the transition energy for all xc potentials, while Δ SCF in combination with LDA and GGA xc potentials underestimates the transition energy. As the fraction of exact exchange included in the xc potential increases, the Δ SCF error becomes positive. This is however not a general behavior: at the Δ SCF level, the transition energy of the lowest energy excitation is overestimated for **5**, and in some systems, TDDFT is seen to outperform Δ SCF when used in combination with LDA and GGA potentials. In this respect, we should also note that CASPT2 estimates from ref 39 were used in instances where the experimental data were not available (systems **2**, **3**, **5_H**, and **9**), and this can affect the comparison between TDDFT and Δ SCF performances. The accuracy of both Δ SCF and TDDFT methods is rather poor in **4**, and this is due to the partial CT character of the lowest energy transition in this system.^{39,40} It is anyway apparent that, with the exception of **4**, the Δ SCF method, when used with

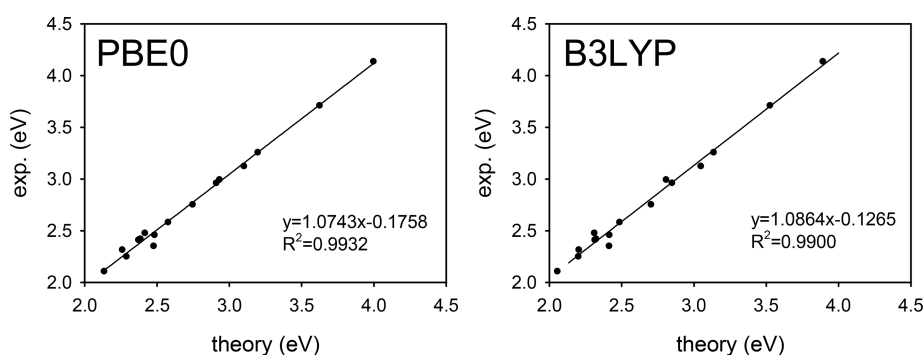


Figure 3. Comparison between Δ SCF calculated vertical excitation energies and experimental excitation energies of the set of molecules (4 is excluded) investigated in this work. Left panel: PBE0 xc potential. Right panel: B3LYP xc potential.

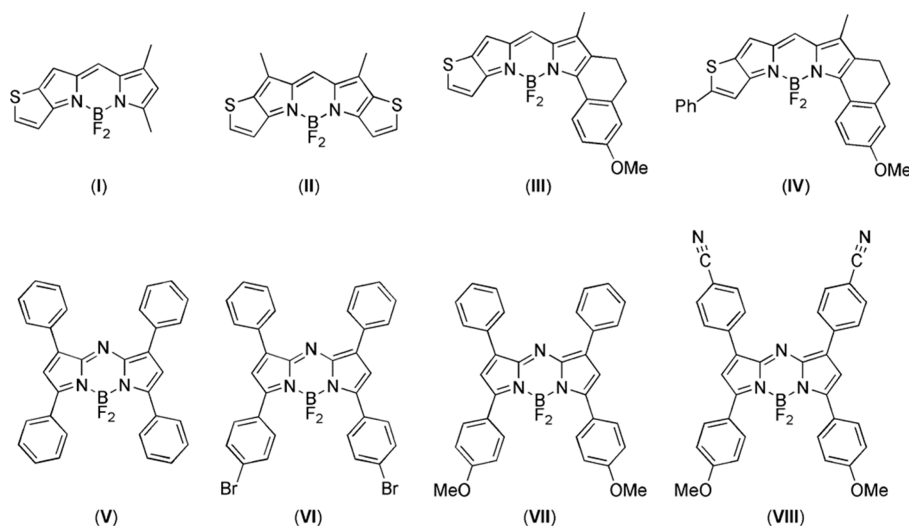


Figure 4. Conjugated BODIPYs and aza-BODIPYs considered in this work. Reprinted with permission from ref 40. Copyright 2021 Wiley.

PBE0 and B3LYP xc potentials, is able to give results in remarkable good agreement with both the experiment and the CASPT2/cc-pVDZ estimates from ref 39. This last observation is put on a quantitative basis by performing a statistical analysis of the results, reported in Table 2 and Table 3 for TDDFT and Δ SCF respectively. In the tables, we perform the analysis both by including and by excluding system 4 from the set of molecules. From an inspection of Table 2, where the TDDFT results are reported, we note that irrespective of the choice of the xc potential, the mean absolute error (MAE) is quite large, ranging from values greater than 0.3 for LDA and GGA potentials to about 0.5 for xc potentials with some fraction of exact exchange included. The correlation (R^2) between theoretical estimates and the experiment is also generally rather poor, but unlike the trend observed in the MAE, it is better for hybrid/meta-hybrid and range-separated potentials compared to LDA and GGA potentials. When 4 is excluded from the set, the statistics generally improve. In particular, the correlation reaches high values for M06-2X and CAM-B3LYP potentials (the R^2 index also generally gets closer to the ideal value of 1.0 with increasing fraction of exact exchange). Therefore, even if the MAE is still large, in the interval between 0.3 to 0.5 eV, one can argue that if properly scaled TDDFT results with M06-2X or range separated xc potentials (see also Table S1 of the Supporting Information) can be used for a rough estimate of vertical excitation energies in similar systems. These observations agree with those reported in ref 27 about

the performance of the M06-2X potential in predicting vertical excitation energies of BODIPY derivatives.

From an analysis of the Δ SCF results (see Table 3), the general better accuracy of this method compared to TDDFT becomes quite clear. In particular, when Δ SCF is combined with xc potentials, which include a small fraction of exact exchange from HF theory (B3LYP with 20% and PBE0 with 25% respectively), in addition to relatively small MAE and standard deviation, an almost perfect linear correlation with the experimental data is obtained. (see Figure 3) Notably, the correlation is high (R^2 greater than 0.9) irrespective of the xc potential, at variance with the TDDFT results. We could say that the accuracy afforded by the Δ SCF method for this class of systems is similar to that which is usually expected from the application of TDDFT to the calculation of HOMO \rightarrow LUMO transitions in organic molecules. This observation and the effect of the fraction of exact exchange included in the xc potential on the accuracy of the Δ SCF estimate of the lowest $\pi \rightarrow \pi^*$ excitation parallel the observations made by Ziegler et al. when studying the first $\pi \rightarrow \pi^*$ excitation of cyanine dyes.⁷⁰ There, the optimal fraction of exact exchange to be included in the xc potential for obtaining quite accurate Δ SCF transition energies was found at roughly 50%, while from our results, we find an optimal value around 20–25% for the BODIPY and aza-BODIPY families.

Based on the results of the above benchmark, we decided to further test the accuracy of the Δ SCF method in conjunction

with hybrid B3LYP and PBE0 xc potentials, by calculating the first vertical excitation energy of a set of eight BODIPYs/azaBODIPYs derivatives, whose structure is presented in Figure 4. The same set of conjugated BODIPYs and aza-BODIPYs were used to test the accuracy of LCC2 and RI-CC2 methods for predicting excitation energies for systems of increasing conjugation length.³⁹ Results for the two xc potentials are reported in Table 4, together with their

Table 4. Δ SCF PBE0/TZP and B3LYP/TZP Lowest Vertical Transition Energy for the Conjugated BODIPYs and aza-BODIPYs Shown in Figure 4, together with a Statistical Analysis of the Results^a

	PBE0	B3LYP	expt
I	2.299	2.222	2.331 ^b
II	2.184	2.103	2.206 ^c
III	2.023	1.948	2.049 ^e
IV	1.875	1.802	1.922 ^c
V	1.867	1.777	1.907 ^{d,e}
VI	1.836	1.744	1.884 ^f
VII	1.747	1.662	1.802 ^{d,e,g}
VIII	1.662	1.579	1.732 ^h
mean AE	0.043	0.125	
min AE	0.022	0.101	
max AE	0.070	0.153	
SD	0.015	0.0180	
R ²	0.9985	0.9979	

^aReported are the mean absolute error (MAE), maximum and minimum AE (max AE and min AE, respectively), the standard deviation (SD), and the correlation coefficient (R^2) between theoretical vertical excitation energies and experimental values. Energies in eV. ^bReference 71. ^cReference 72. ^dReference 73. ^eReference 74. ^fReference 75. ^gReference 76. ^hReference 77.

statistical analysis. A previous work³⁹ has shown that typical errors of TDDFT for this set of conjugated systems are in the range 0.3–0.6 eV and that the errors associated with the LCC2/cc-pVTZ method could be as large as 0.4 eV, although characterized by a high R^2 value when compared with the experimental values so that LCC2 rescaled energies based on a linear fit with the experimental values were in remarkably good agreement with the experiment.⁴⁰ From the results reported in Table 4, we note that for both xc functionals an almost perfect correlation with the experimental data is obtained, comparable to that reported in ref 40 for LCC2 and the resolution-of-identity based CC2 methods, but with a much lower mean absolute error, the latter being largely below 0.1 eV when the PBE0 xc potential is used.

IV. CONCLUSIONS

We computationally demonstrate that, provided a careful choice of xc potential is made, the Δ SCF method is able to deliver results of accuracy comparable to much more sophisticated wave function methods, at a fraction of the cost, for BODIPY and aza-BODIPY derivatives, which are challenging systems for the application of TDDFT. The poor performance of TDDFT in this class of systems seems to be related to the multideterminantal nature of the excited state with a character of double excitations, which are not included in standard TDDFT within the adiabatic approximation to the xc kernel. Based on the general greater accuracy afforded by the Δ SCF method, which includes naturally correlation effects

due to electronic relaxation, we argue that the double excitation character of the first excited state of this class of systems is actually a reflection of relaxation effects following the electronic excitation.

Due to the spin-contamination of the HOMO \rightarrow LUMO excited SCF wave function, it is not easy to quantify the amount of double-excitations in the excited state wave function. We attempted to perform such an analysis by calculating the overlap of the HOMO \rightarrow LUMO excited SCF wave function with both the ground-state KS reference determinant and the manifold of single excitations out of the reference determinant. Results are reported in Tables S18 and S19 of the Supporting Information. As a consequence of spin-contamination, the weights of the HOMO \rightarrow LUMO excited Slater determinant (which has by far the largest weight in the excited wave function) and of all single excitations are largely underestimated, and as a consequence, the weights of higher excitations are grossly overestimated. The importance of doubly and higher excited states in the accurate description of the lowest excited state of BODIPY/aza-BODIPY class of compounds has been evaluated on the basis of explicit wave function calculations by Momeni et al.³⁹ Also, a recent benchmark paper using time-dependent double hybrid DFT on a similar class of systems⁷⁸ support these findings.

In past computational studies dealing with the simulation of core–electron spectroscopies of boroxine-containing systems, we observed the superior accuracy of the Δ SCF method compared to both TDDFT and TP calculations with several xc potentials (ranging from LDA, GGA, hybrid, and RSH), so we are led to conclude that these electronic correlation (relaxation) effects should be quite widespread in B-containing systems and, therefore, not restricted to BODIPYs and aza-BODIPYs systems only. We could also argue that orbital-optimized excited state methods are to be preferred, compared to standard TDDFT within ALDA, for the description of electronically excited states of these systems, since orbital relaxation cannot be properly described only by single excitations out of the KS reference wave function. At variance with TDDFT, which can produce, with a single calculation, a large part (for medium-sized systems) of the absorption spectrum, the application of Δ SCF becomes challenging for the description of several excitations in the same molecule, since it is known to be plagued by convergence issues: in this work we could not converge the SCF cycle in some instances with the range-separated and LB94 xc potentials. We note however that excited state methods based on time-independent DFT have been put forward in recent years^{79–82} that are expected to be of similar accuracy to Δ SCF, and can be valid and cost-effective alternatives to TDDFT for problematic systems. These mean-field methods could represent an efficient computational strategy for a fast screening applied to a rational design of new chromophores with desired optical and spectroscopic properties.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpca.2c04473>.

Box charts showing, for systems 1–16, the comparison between Δ SCF and TDDFT signed error of the first excitation energy with respect to the experimental value for the selection of xc potentials used; B3LYP and PBE0

HOMO and LUMO MO plots for systems 1–16; comparison of the wPBEh, wB97x, and CAM-B3LYP lowest TDDFT vertical energy transition for systems 1–16, together with a statistical analysis of the results; Δ SCF and TDDFT vertical excitation energies and the associated TDDFT eigenvector for systems 1–16; and weight of the ground-state KS determinant and of the single-excitations out of the reference KS determinant in the PBE0 and B3LYP HOMO \rightarrow LUMO excited SCF wave function for systems 1–16 (PDF)

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Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Notes

The authors declare no competing financial interest.

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