

# INVESTIGATION INTO STABILITY AND THERMAL-FLUID BEHAVIOUR OF HYBRID NANOFLUIDS AS HEAT TRANSFER FLUIDS

by

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### Abstract

Title: Investigation into stability and thermal-fluid behaviour of hybrid nanofluids as heat transfer fluids.

Supervisor: Professor M. Sharifpur and Professor J.P. Meyer

Department: Mechanical and Aeronautical Engineering

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The need to improve the poor thermal conductivity of conventional fluids to produce adequate heat transfer fluid cannot be over-emphasized, knowing fully well that heat transfer is key in any engineering process line. Hence, the birth of nanofluids, which is the formulation of a composite of suspended nanoparticles in a basefluid. Nanofluids have found wide applications ranging from heat exchangers, electronic cooling, automotive industry, medical, military, solar energy, manufacturing industry, to mention but a few. But the limitations of nanofluids led to the entrance of a new working fluid named binary nanofluid and ternary nanofluid.

This study experimented with the trio influence of temperature (*T*), percent weight ratios (PWRs), nanoparticles size (NS) on the thermophysical behaviour of MgO–ZnO/Deionised water binary nanofluids (BNFs). 20 nm nano-size of ZnO nanoparticles were hybridised with MgO nanoparticles of nano-sizes 20 nm and 100 nm, and dispersed in deionised water to prepare 0.1 vol% binary nanofluids for percent weight ratios of MgO:ZnO (20:80, 40:60, 60:40 and 80:20). The viscosity ( $\mu$ ), electrical conductivity ( $\sigma$ ), pH, and thermal conductivity ( $\kappa$ ) of the binary nanofluids were experimentally evaluated for temperature 20 to 50 °C. Morphology was checked, and stability was monitored. The impact of temperature, PWRs, and nano-size on the pH,  $\mu$ ,  $\sigma$ , and  $\kappa$  of the binary nanofluid were ordered as PWR >NS >*T*, NS >PWR, *T*, *T*>NS >PWR, and *T* >NS >PWR, respectively. Using the obtained experimental dataset,

correlations were proposed for the thermal property of each binary nanofluid as a function of temperature.

Also, investigating the trio impact of PWR, temperature and  $\varphi$  on the thermophysical characteristics of MgO-ZnO/DIW BNFs, to help close up the scarce literature gap. 20 nm nanoparticle sizes of MgO and ZnO were hybridized together and dissolved in deionized water to formulate 0.1 vol% and 0.05 vol.% binary nanofluids (NFs) for PWR of 20:80, 40:60, 60:40, 80:20 (MgO:ZnO). The  $\kappa$  for all BNFs was enhanced under the impact of rising temperature, with maximum  $\kappa$  enhancement of 5.60% and 22.07% relative to the deionised water (DIW) achieved for 0.05 vol% and 0.10 vol%, separately. The  $\sigma$  was enhanced slightly under the influence of increasing temperature, with maximum enhancement of 21.82% and 30.91% achieved for 0.050 vol% and 0.10 vol%, respectively. In addition, viscosity under temperature increase exhibited a decreasing pattern for all nanohybrids and basefluid. Furthermore, to better harness the benefit of the BNFs for thermal application, thermoelectrical conductivity (TEC) was evaluated with BNFs of 0.05 vol% observed to have higher TEC values than 0.10 vol% BNFs. The BNFs were found suitable as thermal fluids.

A novel manner of furthering thermo-convection behaviour of thermal applications is the use of BNFs as heat transfer fluids. This study experimented the natural convection behaviour of MgO-ZnO NPs suspended in basefluid for  $\varphi = 0.050$  vol.% and 0.10 vol% at percent weight ratios of 20:80, 40:60, 60:40, 80:20 (MgO:ZnO) inside a square enclosure. Factors like Rayleigh number, Nusselt number ( $Nu_{av}$ ), coefficient of convective heat transfer ( $h_{av}$ ), and heat transfer rate ( $Q_{av}$ ) for various temperatures (20°C to 50°C) were examined. PWRs and temperature gradient of BNPs inside the binary nanofluids was observed to augment  $Nu_{av}$ ,  $h_{av}$ , and  $Q_{av}$ . Also, highest improvement of 72.60% ( $Nu_{av}$ ), 76.01% ( $h_{av}$ ), and 72.20% ( $Q_{av}$ ) was achieved. Employing BNFs in square enclosure yielded fine improvement for natural convection behaviour. Artificial intelligence (AI) methods, like artificial neural network (ANN) and surface fitting method were deployed to model the thermal conductivity of BNFs. For the ANN model, a learning algorithm was developed to determine the optimum neuron number. The ANN having 19 neurons in the inner layer got the optimized performance. A surface fitting method was also used on the experimental data, and the generated surface shows the behaviour of the BNFs. The outcome affirmed that the designed ANN model is best for predicting the thermal conductivity of MgO-ZnO/DIW binary nanofluids for different temperatures, nanoparticle sizes, PWRs and volume concentration over the surface fitting method.

**Keywords:** Artificial intelligence; ANN; binary nanofluids; concentration; electrical conductivity; experimental data; DIW; heat transfer; heat transfer co-efficient; heat transfer improvement; pH; percent weight ratio; MgO; modelling; nano-size; Nusselt number; square cavity; sonication energy; temperature; ternary nanofluids; thermal conductivity; thermo-convection; thermophysical properties; viscosity; volume concentration; ZnO.

### **Publications**

The underlisted publications have been prepared as this study progressed. Some have been submitted for publications. One is accepted for publication while two is published.

#### Published

1. S. O. Giwa, M. Momin, C. N. Nwaokocha, M. Sharifpur, J. P. Meyer (2021). Influence of nanoparticles size, percent weight ratio, and temperature on the thermal properties of water-based MgO-ZnO nanofluid: an experimental approach. *Journal of Thermal Analysis and Calorimetry*, Volume 143: 1063-1079. <u>https://doi.org/10.1007/s10973-020-09870-x</u>.

2. C. Nwaokocha, M. Momin, S. Giwa, M. Sharifpur, S. Murshed, J. Meyer (2022). Experimental investigation of thermo-convection behaviour of aqueous binary nanofluids of MgO-ZnO in a square cavity. *Thermal Sciences and Engineering Progress*, 2022, Volume 28, 101057. <u>https://doi.org/10.1016/j.tsep.2021.101057</u>

#### Submitted

3. C. N. Nwaokocha, M. Sharifpur, S. O. Giwa, M. Momin, Mahyar Ghazvini, Hikmet S. Aybar, J. P. Meyer (2021). Experimental formulation and GMDH modelling of thermal conductivity of MgO-ZnO/deionized water hybrid nanofluid.

4. C. Nwaokocha, M. Momin, M. Sharifpur, J. P. Meyer (2021). Influence of concentration, mixing ratios, and working temperature on the thermal behaviour of binary nanofluids of MgO-ZnO: an experimental investigation.

 C. Nwaokocha, M. Momin, M. Sharifpur, J. P. Meyer (2021). Artificial neural network development to predict thermal conductivity of MgO-ZnO/Deionised Water binary nanofluids.
 C. Nwaokocha, M. Sharifpur, J. P. Meyer (2021). Applications of binary nanofluids – emerging issues. This thesis is dedicated to:

The Good Lord for the privilege of life and His unlimited mercies,

My dear wife, Funmilayo Amarachi, for her prayers, great support, and sacrifices,

My parents, Mr. Nelson and Mrs. Augustina Nwaokocha for the prayers and mentoring.

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# Nomenclature

AgSilverAINAluminium nitrideAIAluminium oxideAlAluminium oxideARAspect ratioAuGoldBFBasefluidCNTCarbon nanotubeCpSpecific heat capacity at constant pressureJ/kg KCTABCetyl trimethyl ammonium bromideI/kg KCuCopperI/kg KCuCopper oxideI/kg KDWDistilled waterI/kg KDWDistilled waterI/kg KEGEthylene glycolIEGEthylene deionised waterIEOEngine oilIFe2O3Iron (II) oxideIFe3O4Iron (II) oxideIGGarpheneGGAGum ArabicIGIGlycerolIGONGraphene oxide nanosheetmMCoefficient of convective heat transferW/m²KHHeightmHNFHybrid nanofluidmHNFHybrid nanofluidIMOMagnesium oxideIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMagnetic nanofluidIMODMag	A	Area of cavity	m <sup>2</sup>
AINAluminium nitrideAIAluminium oxideAIAluminium oxideARAspect ratioAuGoldBFBasefluidCNTCarbon nanotubeCPSpecific heat capacity at constant pressureJ/kg KCTABCetyl trimethyl ammonium bromideICuCopperICuOCopper oxideIDWDeionised waterIDWDistilled waterIDWDouble-walled carbon nanotubeIEGEthylene glycolIEGEthylene glycolIEGEthylene deionised waterIFeaOaIron (II) oxideIFeaQ3Iron (II) oxideIFeaO4Gon apheneIGAGun ArabicIGAGirophene oxideIGONGraphene oxidemGONGraphene oxide nanosheetmhCoefficient of convective heat transferW/m²KHHeightmHNFHybrid nanofluidIHNFMagnesium oxideIMODMargin of deviationIMWCNTMulti-walled carbon nanotubeI	Ag	-	
AlAluminiumAlu			
ARAspect ratioAuGoldBFBasefluidCNTCarbon nanotubeCpSpecific heat capacity at constant pressureJ/kg KCTABCetyl trimethyl ammonium bromideI/kg KCTABCetyl trimethyl ammonium bromideI/kg KCu0CopperCooperCu0Copper oxideI/kg KDWDeionised waterI/kg KDWDistilled waterI/kg KDWDistilled waterI/kg KDWElectrical double layerI/kg KEGEthylene glycolI/kg KEG-DIWEthylene deionised waterI/kg KEOEngine oilI/kg KFeIron (III) oxideI/kg KFe2O3Iron (III) oxideI/kg KGAGum ArabicI/kg KGLGlycerolI/kg KGNFGreen nanofluidI/kg KGONGraphene oxide nanosheetmhCoefficient of convective heat transferW/m²KHHeightmHNFHybrid nanoparticleI/kg KmGradientI/kg KMODMagnesium oxideI/kg KMODMargin of deviationI/kg KMWCNTKulti-walled carbon nanotubeI/kg K	Al	Aluminium	
ARAspect ratioAuGoldBFBasefluidCNTCarbon nanotubeCpSpecific heat capacity at constant pressureJ/kg KCTABCetyl trimethyl ammonium bromideI/kg KCTABCetyl trimethyl ammonium bromideI/kg KCu0Copper oxideI/kg KDWDeionised waterI/kg KDWDistilled waterI/kg KDWDistilled waterI/kg KDWDistilled waterI/kg KDWElectrical double layerI/kg KEGEthylene glycolI/kg KEG-DIWEthylene deionised waterI/kg KEOEngine oilI/kg KFeIronI/kg KFe2O3Iron (III) oxideI/kg KGAGum ArabicI/kg KGLGlycerolI/kg KGNFGreen nanofluidI/kg KGONGraphene oxide nanosheetmhCoefficient of convective heat transferW/m²KHHeightmHNFHybrid nanoparticlemMQOMagnetin oxideI/kg KMNFMagnetin oxideI/kg KMODMargin of deviationI/kg KMWCNTMulti-walled carbon nanotubeI/kg K	Al <sub>2</sub> O <sub>3</sub>	Aluminium oxide	
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MWCNT Multi-walled carbon nanotube	MO	Mineral oil	
	MOD	Margin of deviation	
ND Nano-diamond	MWCNT	Multi-walled carbon nanotube	
	ND	Nano-diamond	
NF Nanofluid	NF	Nanofluid	
Ni Nickel	Ni	Nickel	

NP	Nanoparticles	
Nu	Nusselt number	
PG	Propylene glycol	
PVP	Poly vinyl pyrolidone	
Q	Heat transfer rate	W
Ra	Rayleigh number	
Re	Reynolds number	
SDBS	Sodium dodecyl benzene sulfonate	
SDS	Sodium dodecyl sulphate	
SiC	Silicon carbide	
$SiO_2$	Silicon oxide	
SiO <sub>x</sub>	Silicon oxides	
SWCNT	Single-walled carbon nanotube	
Т	Temperature	°C
TEC	Thermoelectrical conductivity	
TiO <sub>2</sub>	Titanium oxide	
ТО	Transformer oil	
V	Volume	m <sup>3</sup>
W	Water	
Х	Ratio of hybrid nanoparticles	wt.%
Zn	Zinc	
ZnO	Zinc oxide	
$\Delta T$	Temperature difference	°C

### **Greek letters**

$\Delta$	Difference	
ρ	Density	m³/kg
β	Thermal coefficient of expansion	1/K
μ	Dynamic viscosity	mPa.s
σ	Electrical conductivity	μS/cm
κ	Thermal conductivity	W/m K
arphi	Volume concentration of nanoparticles	
δ	Uncertainty	

### Subscripts

Effective
Average
Side
Hot
Cold
Experiment
Predicted

# **CHAPTER 1**

### **INTRODUCTION**

#### **1.1 BACKGROUND**

Energy use and its impact on the environment has called for global concern, hence the need for a sustainable approach that will attenuate the increasing trend of global warming and its attendant environmental problem. Really, energy use remains the thermometer for growth and development. As the search for a sustainable, economical and alternative energy resource is increasing and gaining global attention, so should the concept of energy and environmental balance gain momentum globally [1-3]. Beyond the issue of balance for energy demand and supply, which has led to search for cheap and sustainable energy resource; energy sustainability and efficiency is greatly needed to enable good energy and environmental balance as advocated by the 17-point Sustainable Development Goals (SDGs) agenda of the United Nations (UN). The UN policy was initiated in 2016, to run till 2030 with the global aim of addressing energy and environmental issues [4, 5].

Recent technological innovations keep advancing the need for improvement in energy efficiency and sustainability. Effective thermal energy management is key to numerous process engineering applications. The concept of miniaturization, fins and surface modification for thermal equipment are reaching their limits as regards heat transfer improvement [6-8]. The use of common working fluids (acetone, ethylene glycol (EG), propylene glycol, organic liquid, polymer solution (PS), oils and water) as cooling media in heat transfer applications is no longer sustainable due to the low thermal conductivity of these working fluids. These limitations necessitated a century-long search by Maxwell [9-11] in 1873, who first conceived the idea of developing an energy-efficient fluid with improved thermophysical properties. The formulated suspension-mix (solid particles + basefluid) gave an improved thermal

conductivity, with noticeable drawbacks like pressure drop, channel clogging and sedimentation. Later, a similar investigation was conducted by Ahuja [12, 13] in 1975 by suspending micrometre-sized polystyrene particles in aqueous sodium chloride and glycerin solution (as basefluid). An improved thermal conductivity was observed, three times higher than the basefluid, yet the drawback of rapid sedimentation was noticed. Further investigation was carried out by Liu et al. [14] in 1988 and same like-minded researchers too in 1992 at the Argonne National Laboratory (ANL) [15-17], all on the premise of Maxwell's work. Similar drawbacks were reported, as observed by Maxwell and Ahuja [18]. Sometimes in 1993, Masuda et al. [19] came to the rescue with a concept of using ultrafine particles of alumina, silica and titanium dioxide suspended in water, which yielded an enhanced thermal conductivity, without the drawbacks earlier reported by Maxwell and Ahuja. In 1995, after extensive investigation at the ANL, Choi and Eastman [20] named the innovative fluid as 'Nanofluid', considering the improved results.

The need keeps rising in the thermal energy field for improved thermo-convection performance, requiring the advancement of compact devices with lightweight and miniaturized design, finely stable performance, and augmented thermal efficiency. For better heat transfer performance using working fluids, binary nanofluids and ternary nanofluids have found optimized use over the use of single nanofluids because of blended characteristics of nanoparticles [21-30]. The progress in the study of nanofluids advanced the dispersion of various nanoparticles of various volumes/masses, thermal behaviour and geometries to prepare BNFs and TNFs [21, 31-38]. The newly formulated thermal fluids (BNF and TNF) help to improve thermo-convection characteristics as related to mono-nanofluids and conventional basefluids [39-42]. This progressing investigation which continued over a decade ago was pioneered by Jana et al. [43] and Chopkar et al. [44] who birthed the idea of hybridizing various nano-materials for an optimal thermal fluid.

#### **1.2 PROBLEM STATEMENT**

The need to augment the poor thermal conductivity of traditional fluids to make them efficient cannot be over-emphasized, knowing that heat transfer fluid is key in the process line of many industrial production concerns. Hence, the birth of nanofluids is the formulation of the composite of suspended nanoparticles in a basefluid [16]. Nanofluids have found applications ranging from heat exchangers, electronic cooling, automotive, medical, military, solar energy, manufacturing, to mention but a few [18, 45-51]. However, nanofluids have limitations premised on certain specific benefits due to the characteristics of the dispersed nanoparticle [31, 52-55], thus, the entrance of a new generation heat transfer fluid called binary nanofluids (BNFs) and ternary nanofluids (TNFs) [21, 34, 36-38, 56-58].

Binary nanofluids (HNFs) and ternary nanofluids (TNFs) is an emerging area of nanofluids research where different nanomaterial's physical and chemical properties are blended together to form a new nano-product possessing an improved homogeneous phase [21, 59-63]. This is prepared by suspending two or more different nanoparticles in composite or mixture form in basefluids. The limitation of individual conventional nanofluids necessitates this great enhancement. Literature is limited on the stability of hybrid nanofluids. Thus a comprehensive investigation into the stability of hybrid nanofluids is necessary because it is a key issue that influences the thermal-fluid behaviour of hybrid nanofluids applications. The issue of sample preparation parameters will also be investigated to see how it relates to stability. A research gap apparently exists on the trio influence of percent weight ratios (PWRs), temperature, volume concentration ( $\varphi$ ) on the thermal properties of nanohybrids, which was experimentally examined. Furthermore, the dual effect of volume concentrations and mixing ratios on the thermo-convection performance of binary nanofluids in a squared enclosure of different temperature ranges were experimentally examined, as gaps exist here in literature as regards thermo-convection performance of binary nanofluids in various cavity geometries. Also, the

growth in industrial processes has necessitated commensurate growth in heat transfer systems' efficiency by optimizing thermal processes and properties [21, 64]. Really, experimental setups to determine thermophysical and thermo-convection properties is quite expensive and takes time [64, 65]. So, in handling the occurrence of repeated experiments and encourage optimised big data handling, the application of Artificial Intelligence (AI) techniques [34, 66-72] (like Artificial Neural Network (ANN), Fitting Method and Group Method of Data Handling (GMDH) models, etc) were used to predict the thermophysical properties of BNFs. Considering the future of works in relation to current realities posed by Covid-19, which has led to working remotely, the application of AI option cannot but be adopted in this area of research. The study's novelty led to the development of appropriate correlations for the thermal properties.

#### **1.3 AIM OF STUDY**

This investigation aimed to experimentally formulate stable and homogenized binary nanofluids (MgO-ZnO/deionized water (DIW) and MWCNT-Al<sub>2</sub>O<sub>3</sub>/DIW) and ternary nanofluids (MgO-ZnO-MWCNT/DIW) using an optimized approach, performed experimental investigations by measuring the viscosity ( $\mu$ ), pH, thermal conductivity ( $\kappa$ ) and electrical conductivity ( $\sigma$ ) of the stable nanofluids, investigate the thermo-convection heat transfer performance of the stable nanofluids in a square enclosure, as well as proposed accurate models through artificial intelligence methods to predict some thermophysical properties.

#### **1.4 OBJECTIVES**

The specific objectives of this investigation were:

1. To formulate stable MgO-ZnO/deionized water, MWCNT-Al<sub>2</sub>O<sub>3</sub>//deionised water binary nanofluids (BNFs), and MgO-ZnO-MWCNT/deionised water ternary nanofluids (TNFs), by optimising sample preparation parameters like amplitude, sonication time, and dispersion fraction of surfactants; 2. To characterise nanoparticles and formulated BNFs and TNFs using techniques like transmission electron microscope (TEM) and ultra-violet visible spectrophotometer, respectively;

3. To measure the thermal properties of BNFs and TNFs at various volume concentrations, nanoparticles sizes (NS), temperatures, and percent weight ratio (PWR);

4. To investigate the thermo-convective behaviour of BNFs in a square cavity;

5. To develop correlations for the prediction of the thermal properties and Nusselt number of BNFs.

6. To propose accurate models to predict some thermophysical properties through artificial intelligence methods.

#### **1.5 SCOPE OF STUDY**

In this study, the impact of percent weight ratios (PWRs), nanoparticles sizes (NS), working temperatures, volume concentration ( $\varphi$ ) was examined on the thermal properties of the formulated nanohybrids.

Experiments on thermo-convection behaviour were conducted in a square cavity at diverse temperature range (20 °C to 50 °C) under atmospheric conditions. Data of temperatures and flow rates were automatically measured by a datalogger and fed into the personal computer.

Artificial intelligence models were used to predict thermal properties based on the results of the experimental study. Artificial Neural Network (ANN) and surface fitting models were used to predict some thermophysical properties of the formulated nanohybrids.

#### **1.6 ORGANISATION OF THE THESIS**

A run-through of the structure of the chapters of this thesis is detailed in this sub-section. For proper structuring, chapters are classified as sections and subsections. The thesis comprises eight chapters in total.

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Chapter 1 introduces nanofluid as an innovative working fluid for thermal management in heat transfer applications. First, the background of the study was presented, explaining the advent of nanofluids to the recent ternary nanofluids. The rest of the sub-divisions are problem statement, aim, objectives and scope of the study.

Chapter 2 presents a literature search on the formulation and measurement of thermal properties of nanohybrids. The morphology and thermo-convection performance of nanohybrids were also reviewed. The use of artificial intelligence models to predict thermal properties was reviewed as well.

Chapter 3 details the methods and materials necessary for the formulation and measurement of thermal properties of nanohybrids. The experimental setup for thermo-convection behaviour of nanohybrids in a square enclosure was stated. The chapter also explained the validation of the cavity, data reduction, uncertainty estimation, and model development.

Chapter 4 presents the experimental results for the production and morphology of the stable nanohybrids.

Chapter 5 presents the experimental results and discussion for the measurement of thermal properties of stable nanohybrids. Proposed correlations for the thermal properties of the nanohybrids were presented and discussed.

Chapter 6 details the experimental investigation, results, and discussion for the thermoconvection performance of nanohybrids in a square cavity.

Chapter 7 presents the use of artificial intelligence (AI) models to predict thermal properties based on the results of the experimental study. AI methods, like ANN and surface fitting method are employed to model some thermophysical properties of the formulated nanohybrids. Chapter 8 details the general summary of the thesis and presents recommendations for further study.

# **CHAPTER 2**

## LITERATURE REVIEW<sup>1,2,3,4,5,6</sup>

#### **2.1 INTRODUCTION**

The concept of nanosuspension has gained prominence in the research field of thermal applications and applicable working fluids over the century. It kicked off with Maxwell's [9-11] formulated suspension-mix in 1873 to improve fluid properties. The colloidal suspension improved thermal conductivity, with noticeable drawbacks like pressure drop, channel clogging and sedimentation, which were limitations to achieving a meaningful engineering solution. Similar results and challenges emanated from Ahuja's [12, 13] investigation in 1975.

Choi's [73, 74] work in 1995 which was premised on Maxwell's study came with hope, thus pioneering the nanosuspension concept which has helped produced various nanofluids. Nanofluids (NFs) are better working fluids with better thermophysical properties over conventional basefluids (BFs). Nanofluids are nanosuspensions containing various nanoparticles like:

This chapter is reflected in parts in the following papers:

<sup>&</sup>lt;sup>1</sup>Giwa, S., Momin, M., Nwaokocha, C., Sharifpur, M., and Meyer, J. *Influence of nanoparticles size, per cent mass ratio, and temperature on the thermal properties of water-based MgO–ZnO nanofluid: an experimental approach.* Journal of Thermal Analysis and Calorimetry, 2021. **143**(2): p. 1063-1079.

<sup>&</sup>lt;sup>2</sup>Nwaokocha, C., Momin, M., Giwa S., Sharifpur, M., Murshed S.M.S., Meyer, J.P., *Experimental investigation of thermo-convection behaviour of aqueous binary nanofluids of MgO–ZnO in a square cavity.* Thermal Science and Engineering Progress, 2021. **28**: 101057.

<sup>&</sup>lt;sup>3</sup>Nwaokocha, C., Giwa S., Ghorbani B., Momin, M., Sharifpur, M., Gharzvini M., Chamkha, A.J., Meyer, J.P., *Experimental formulation and GMDH modelling of thermal conductivity of MgO–ZnO/deionised water hybrid nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>4</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Influence of concentration, mixing ratios, and working temperature on the thermal behaviour of binary nanofluids of MgO–ZnO: an experimental investigation.* Ready for submission.

<sup>&</sup>lt;sup>5</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Artificial neural network development to predict thermal conductivity of MgO–ZnO/Deionised Water binary nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>6</sup>Nwaokocha, C., Sharifpur, M. and Meyer, J., *Application of binary nanofluids – Emerging issues*. Ready for submission.

- Metals: copper (Cu) [75-78], silver (Ag) [56, 79-82], iron (Fe) [60, 78, 83], gold (Au) [49, 75, 84-86], zinc (Zn) [85, 87], nickel (Ni) [78, 88-91], alumina (Al) [26, 92-96];
- Metal carbides/carbides ceramics silicon carbide (SiC) [40, 97-99], titanium carbide (TiC) [99-101];
- Nitride ceramics/metal nitrides aluminum nitride (AlN) [47, 102, 103], silicon nitride (SiN) [104, 105], boron nitride (BN) [106-109];
- Metal oxides/oxide ceramics aluminium oxide (Al<sub>2</sub>O<sub>3</sub>) [58, 96, 110-115], Tungsten-oxide (WO<sub>3</sub>) [116-119], copper oxide (CuO) [115, 120-124], Cerium-oxide (CeO<sub>2</sub>) [114, 125-127], titanium dioxide (TiO<sub>2</sub>) [56, 113, 128-131], iron (III) oxide (Fe<sub>2</sub>O<sub>3</sub>) [31, 45, 96, 132, 133], iron (II) oxide (Fe<sub>3</sub>O<sub>4</sub>) [124, 134-136], silicon dioxide (SiO<sub>2</sub>) [61, 99, 110, 137, 138], zirconium oxide (ZrO<sub>2</sub>) [139-141], zinc oxide (ZnO) [21, 142-144];
- Carbon materials carbon nanotube (single wall SWCNT, double walls DWCNT, multi wall MWCNT, or shell composites), graphite, and nano-diamond [61, 115, 128, 130, 134, 135, 137, 145-153].

Nanoparticles (NPs) are dispersed into conventional basefluids (BF) (acetone, bio-glycol, coconut oil, engine oil, ethylene glycol (EG), glycerol, ionic fluid, organic liquid, palm oil, polymer solution (PS), propylene glycol (PG), transformer oil and water) to formulate nanofluids (NFs). This concept was first advanced by Jana et al. [43], and Chopkar et al. [44]. The drawbacks in the efficiency of NFs led to the birth of binary nanofluids (BNFs) and ternary nanofluids (TNFs), which possess improved thermal transport characteristics better than NFs and BFs. BNFs are formulated by hybridizing dissimilar nanoparticles (NPs) of varying sizes, shapes and thermal properties and thereafter dispersed into BFs. Literature abounds with several works investigating the thermophysical properties (electrical conductivity, density, viscosity, specific heat capacity, and thermal conductivity) of NFs, BNFs and THFs. They reported good augmentation at various volume concentrations for different

temperatures [33, 42, 154-162]. As a result, this innovative working fluid has found wider application potentials due to its improved thermal conductivity, homogeneity, and fine stability. In recent time as well, basefluids are also mixed together before suspending nanoparticles in it, examples are: water-ethylene glycol [115, 131, 134, 163, 164], water-propylene glycol [164-167], acetone-water [168, 169], ethanol-water [168-170], etc.

The attendant issues with mono-nanofluids (single-nanoparticle based nanofluid) are assessed using the following parameters - chemical inertness, energy saving level, higher production cost, thermal behaviour, rheological properties, usefulness in diverse fields, increased pumping power defects, heat transfer behaviour, stability, etc – since they do not solely possess suitable ability for specific use. Hence, a trade-off is needed, allowing for dispersing various nanoparticles in basefluid (BF) or binary base-fluid (BBF). This is called binary nanofluid (BNF). An extension by further investigation is the development of ternary-nanofluids (TNF), which contain three different types of nanoparticles. Figure 2.1 presents the graphical summary of commonly used nanoparticles and basefluids to formulate mono-nanofluids, binary nanofluids, binary base-fluids, ternary-nanofluids [21, 31, 39, 119, 131, 149, 152, 153, 163, 171-174].

#### 2.2 CONCEPT OF MONO, BINARY AND TERNARY NANOFLUIDS

After the preliminary works of Maxwell [9, 10] and Ahuja [12, 13], the suspension of nanoparticles was found better than the suspension of micro- sized or millimeter-sized particles. Nanofluids are engineered nanosuspension with good thermophysical properties over conventional basefluids (BFs). NFs are engineered nanosuspension having NPs of nanosizes less than 100 nm. The ground-breaking work of Masuda et al. [19] affirmed that engineered nanosuspension had found good use in heat transfer applications. They investigated the use of ultrafine particles of alumina, silica and titanium dioxide dispersed in water, which yielded an enhanced thermal conductivity than the basefluid. This ground-breaking result in thermal

conductivity enhancement led to further investigation of suspending different types of NPs into conventional fluids. NPs of metals, metal carbides/carbides ceramics, metal oxides/oxide ceramics, nitride ceramics/metal nitrides, carbon materials (nanotubes/shell composites, graphite, and nano-diamond) and biomass are dispersed in different BFs like water, acetone, EG, PS, PG, etc., or mixture of both to form binary base-fluids [21, 110, 115, 119, 134, 135, 144, 164, 166, 168, 169]. The measurements of thermal conductivity gain primacy in the preceding studies, thereafter the measurements of other thermophysical properties, like viscosity, electrical conductivity, density, specific heat capacity.

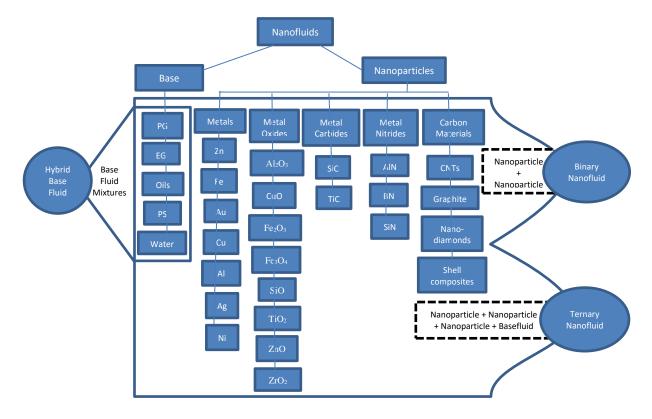


Figure 2.1: Graphical presentation showing the relationship between mono-particle nanofluids, binary nanofluids, binary basefluid, and ternary nanofluids.

The concept of thermal conductivity ( $\kappa$ ) values of solid materials, with reference to metals having higher thermal conductivity than conventional fluids, led to the birth of nanofluids via the process of material size reduction to nano-sizes and subsequent nanosuspension into basefluids. In a similar sense, BNFs and TNFs were conceived because NPs with various thermal properties can be combined together at different weight ratios to produce better heat transfer fluids [21, 28, 31, 36, 39, 57, 96, 144]. Over a decade ago, it was first advanced by Jana et al. [43] and Chopkar et al. [44], who pioneered the idea of hybridizing diverse nanomaterials for optimal thermal management. Their works reported improved thermal conductivity. Chopkar et al. [44] published a thermal conductivity improvement of 50-150% when they synthesized Ag2Al and Al<sub>2</sub>Cu HNPs in EG and water to formulate BNFs for volume concentration ( $\varphi$ ) range of 0.20 to 1.50 vol.%. Contrarywise, Jana *et al.* [43] formulated and measured  $\kappa$  for water-based single-NFs (Au, CNT and Cu) and water-based BNFs (CNT-Au and CNT-Cu). They reported that the single-NFs had an higher  $\kappa$  than the BNFs. Jha et al. [34] published  $\kappa$  of Cu-MWCNT dispersed in DIW and EG has had higher value than that of NFs of MWCNT/EG and MWCNT/DIW, which supported the finding of Chopkar et al. [38] and was consistent with the work of Chen et al. [175], who reported an improved  $\kappa$  of Ag–MWCNT/Water BNF over the MWCNT/water NF.

#### 2.3 PREPARATION OF NANOFLUIDS

The formulation of NFs is done by suspending NPs into conventional fluids, known as basefluid [157, 158, 173]. As well, the formulation of BNFs is done by dispersing two NPs into basefluid or basefluids [21, 31, 96, 172]. Also, the formulation of TNFs is done by suspending three NPs into basefluid or basefluids [36, 38, 39]. In all, the durability, stability, and chemical inertness of nanofluids is very key to real time applications, starting with the measurement of thermophysical properties and thermo-convection studies. It is established that the hybridisation of dual or more nanoparticles for the preparation of binary or ternary nanofluids reveals that an optimized blend (percent weight) ratio will be attained for which enhanced thermal properties are achieved, birthing an engineered nanosuspension with better thermal property.

The formulation of nanofluids uses either a one-step or two-step process. The one-step approach entails the simultaneous synthesis and suspension of nanoparticles in basefluids, the production of nanoparticles and preparation of nanofluids concurrently [176, 177]. This method allows for high stability and uniform dispersion. It also eliminates the burden of drying, storage and dispersals. The limitation with this method is the problem associated with commercial production and capital intensive [176]. The two-step process first entails the synthesis of nanoparticles, nanotubes and nanocomposites in powdery form by using chemical or mechanical processes like grinding, vapor phase, milling and sol-gel method, and subsequent suspension in basefluids. The two-step process is commonly reported in the literature [21, 31, 96, 176, 178], because of its ease of large-scale production for industrial application and cost-effectiveness. The drawback related to the two-step process is sedimentation and agglomeration due to the Van der Waal force of attraction among the particles.

#### 2.4 CHARACTERISATION OF NANOFLUIDS

Different methods abound in literature for the characterisation of NFs, BNFs and TNFs for the nano-properties of their NPs, BNPs and TNPs like crystalline structure, dispersion, distribution, elemental composition, functional groups, nano-shapes/structure, nano-sizes, surface morphology, etc. These methods range from Energy Dispersive X-ray Spectroscopy (EDX or EDS), Field Emission Scanning Electron Microscopy (FESEM), Fourier Transform Infrared Spectroscopy, High-resolution transmission electron microscopy, Light scattering, Raman Spectroscopy, Scanning Electron Microscopy (SEM), Transmission Electron Microscopy (TEM), Vibrating Sample Magnetometer (VSM), X-Ray Diffractometer (XRD) [179-184]. The commonly used technique for characterising NFs, BNFs and TNFs is TEM, SEM and XRD. These methods are adopted on a stand-alone basis or combined for characterisation. TEM helps to ascertain the sizes, shapes and dispersion of NPs, BNPs and TNFs in NFs, BNFs and TNFs, respectively, as SEM is used to identify elemental mapping

and surface morphology. XRD presents the crystalline structure and grain size of NPs, BNPs and TNFs in NFs, BNFs and TNFs respectively [39, 185-190].

#### 2.5 STABILITY OF NANOFLUIDS

The process of suspending NPs, BNPs and TNPs into different BFs establishes charges in the BFs, leading to the generation of an electrical double layer (EDL) on the surface of the suspended nanoparticles. The EDL contributes actively to improving both electrical conductivity and convective heat transfer, which is a result of the active electrophoretic mobility emanating from the charged nano-suspended particles. Furthermore, the formation of EDL strongly correlates with nanosize, volume fraction, and surface charge of the nanoparticles, along with the ionic concentration of the BFs [191-193].

The even or stable distribution of NPs, BNPs and TNPs in BFs is key to using NFs, BNFs, and TNFs for engineering applications. The efficiency, optical property and thermophysical charateristics (mainly thermal conductivity and viscosity) of NFs, BNFs and TNFs has a significant relationship with the concentration of NPs, BNPs or TNPs in the nanosuspension [40, 194-197]. The use of two-step method to improve the stability of NFs, BNFs and TNFs to help remove sedimentation and agglomeration, is achieved using four techniques, viz - surfactant addition, mechanical (sonication), surface modification, and pH control techniques.

#### 2.5.1 Methods For Enhancing The Stability of Nanofluids

#### **2.5.1.1 Use of Dispersant**

Dispersants, also known as surfactants, are chemical compositions used to stabilize nanofluids by diminishing the surface energy of host fluids, thus increasing the dispersibility of nanoparticles [198, 199]. The stability of NFs, BNFs, and TNFs is enhanced as surfactants or dispersants help reduce the interfacial tension within NPs, BNPs and TNPs. Commonly used surfactants or dispersants are Dodecyltrimethylammonium bromide (DTAB) [200], Gum Arabic (GA) [171], Hexadecyltrimethylammonium Bromide (HCTAB) [201], NanoSperse AQ [202, 203], Oleic acid [204], Polyvinyl pyrrolidone (PVP) [171, 204], Salt [204], sodium dodecyl benzene sulfonate (SDBS) [171, 203], Sodium dodecyl Sulfate (SDS) [21, 96]. This procedure is poorly effective at a working temperature greater than 60 °C because of possible weakening of the bonds between nanoparticles and surfactants. Note, the amount of surfactant substantially influences the uniformity of suspension [204].

#### 2.5.1.2 Mechanical (Sonication)

Sonication is a method used to achieve a uniform mixture of NPs or BNPs or TNPs when dispersed in BFs to formulate stable NFs, BNFs and TNFs. Literature affirmed that sonication impacts cluster size, absorbance wavelength, particle size, diameter of CNTs, dispersants/surfactants, thermal conductivity and viscosity [21, 31, 96, 171, 205, 206]. The time lag for sonication has been published to span minutes to hours, thus requiring an optimum sonication time to help achieve enhanced stability. Sonication time may depend on basefluid, concentration, mixing ratio of nanoparticles, shape, size, type, and preparation method, etc. [171, 204]. The ultra-sonification technique reduces the sedimentation and clustering issues in nanosuspension. After a certain time, the increase in sonication time reduces stability, thus resulting in the damage and/or heavy nanoparticle breakdown when the suspension has a low % of volume concentration range. Hence, the concept of optimum sonication time to prevent this, else further increase in sonication results in deterioration of stability and thermal conductivity of NFs, BNFs and TNFs [171, 206].

#### 2.5.1.3 Surface Modification

The functionalisation or surface modification of NPs or BNPs or TNPs is another method used to stabilize NFs, BNFs and TNFs, without dispersants. This technique allows the dispersal of nanoparticles in BFs after functionalizing the surfaces of NPs or BNPs or TNPs using various methods. For the treated NPs or BNPs or TNPs, the sedimentation layer is not found at boiling temperature. The following methods are employed to functionalize: grafting, plasma treatment, wet mechanochemical reaction, etc. [204, 207, 208].

#### 2.5.1.4 pH Modification

The modification of pH value can also achieve the stability of NFs, BNFs and TNFs. The dispersion of NPs or BNPs or TNPs into BFs generates surface electric charges, representing the isoelectric point (IEP) of nanohybrids (NFs, BNFs and TNFs), with zeta potential having zero value. As pH value is farther from the IEP, nanohybrids (NFs, BNFs and TNFs) gain stability and durability due to strengthened repulsive forces within the NPs or BNPs or TNPs, thus improving zeta potential [204, 207, 208]. Choudhary [209] posited that adding NaOH or HCl to NFs or BNFs or TNFs to make it a bit basic or acidic returns a durable result with enhanced zeta potential. Note that optimized pH value differs from sample to sample, thus the need to maintain a safe work environment.

In conclusion, Table 2.1 presents various methods of improving the stability of NFs, BNFs and TNFs.

#### 2.5.2 Methods For Analysing Stability of Nanofluids

#### 2.5.2.1 Visual Observation

Visual observation of sediments of particles (NPs or BNPs or TNPs) remains the simplest and mostly used method to examine the stability of NFs, BNFs and TNFs. Though it takes a lot of time to inspect sediments, it remains a cheap medium for stability analysis. Though not a scientific method, but with the process NFs or BNFs or TNFs can be called stable for a certain period that the nanosuspension remains consistent with time. Literature abounds with the use of this method to capture sediment's image as a guide to viewing stability [21, 31, 96, 204-206, 210, 211]. Visual inspection is used along with scientific monitoring techniques.

Authors	NFs or BNFs	Size	Synthesis method	Temp.	Concen- tration	Stability technique	Stability time
Elias et al. [212]	Al <sub>2</sub> O <sub>3</sub> /Water-EG	13 nm	Two-step	10-50 °C	0-1%	30 min. sonication	3 days
Nikkam et al. [213]	Cu/diethylene glycol	5–100 nm	One-step	20 °C		Sonication	Several weeks
Senthilrala et al. [214]	CuO/distilled water	27 nm	Two-step	50 °C		4 hour ultrasonication	Several hours
Sundar et al. [215]	CuO/EG-water	27 nm	Two-step	15-50 °C	0.2- 0.8%	2 hour ultrasonication	Stable; ZPV = -20 mV
Amiri et al. [216]	SiO <sub>2</sub> /EG, SiO <sub>2</sub> /Water, SiO <sub>2</sub> -Cu/EG, SiO <sub>2</sub> -Cu/Water	SiO <sub>2</sub> – 50– 80nm, Cu–10nm		20-40 °C	0.002- 0.01%	Surface modification by Cu and 2 hr ultrasonication	Two weeks
Sundar et al. [217]	Nanodiamond/distilled water	11.4 nm	Two-step	59.85 °C	1%	Surface modification and 2 hr bath sonication	30 days
Sundar et al. [217]	Nanodiamond/EG- Water	19 nm	Two-step	60 °C		Surface modification and 2 hr bath sonication	ZPV = -30 mV
Choudhary et al [209]	Al <sub>2</sub> O <sub>3</sub> /Distilled Water	20 nm			0.01- 0.1%	Addition of 0.1% HCl or NaOH; 60, 120 and 180 min of sonication	16 days
Kakati et al. [218]	Al <sub>2</sub> O <sub>3</sub> /Deionized Water			10-50 °C	0.1- 0.8%	Addition of 0.03% (wt) SDS	4-5 days
Sundar et al. [219]	Fe <sub>3</sub> O <sub>4</sub> /Distilled Water	13 nm	Two-step			2 hr sonication with CTAB (CTAB to NPs mass ratio – 1:10)	60 days

#### Table 2.1: Methods of improving the stability of NFs, BNFs and TNFs

#### 2.5.2.2 Zeta Potential Test

Zeta potential test is a technique for assessing the stability of nanosuspensions. The electrostatic repulsion existing amidst the particle's surface and the static layer of fluid is called zeta potential [204, 209, 210]. Thus, the correlation between zeta potential value and the stability of NFs or BNFs or TNFs. Higher zeta potential values (positive or negative) indicate a stable condition, while a lower value suggests an unstable condition. Table 2.2 presents the relationship between zeta potential value and stability of nanofluids. Literature reports the use of zeta potential test in measuring the stability of NFs and BNFs [209-211, 220, 221].

 Table 2.2: Zeta potential value and stability of nanofluids [204, 220]

Zeta potential value (mV)	Stability of nanofluids
0	Instability
15	Little stability with fast particle settlement
30	Moderate stability
45	Fine stability, slight settlement
60	Excellent stability

#### 2.5.2.3 Ultra-Violet Visible (UV-vis) Spectroscopy

The ratio of absorbency of NPs or BNPs or TNPs has a proportional relationship with the concentration of NFs or BNFs or TNFs, respectively. Spectral absorbency technique via UV-vis spectrophotometer is one of the most used and authentic techniques used to evaluate the stability of NFs, BNFs and TNFs. This method is able to constantly monitor stability at specific time intervals for a time period running to weeks and months, thus returning quantitative results equal to the concentration of NFs, BNFs and TNFs; which is an advantage over other methods [21, 206, 221, 222]. Like other methods, it is also used along with visual observation and zeta potential.

#### 2.5.2.4 Thermophysical Properties Check

The stability of NFs, BNFs and TNFs is also defined by assessing their thermophysical properties. Giwa et al. [223] used viscosity to assess the stability of formulated MWCNT-Fe<sub>2</sub>O<sub>3</sub>/DIW binary nanofluid (0.5 vol%) for an experimental run time of 2580 min (43 h). Garbadeen et al. [27] used effective viscosity to monitor the stability of MWCNT/DIW for an experimental run time of 250 minutes. Joubert et al. [224] also monitored the stability of Fe<sub>2</sub>O<sub>3</sub>/DIW NFs for 20 hr by measuring effective viscosity.

#### 2.5.2.5 Other Techniques

There are further techniques used to monitor the stability of nanofluids (NFs), binary nanofluids (BNFs) and ternary nanofluids (TNFs), such as centrifugation, etc. [225, 226].

#### **2.6 THERMOPHYSICAL PROPERTIES OF NFs, BNFs and TNFs**

# 2.6.1 Stability of Nanofluids

The thermal conductivity of NFs is widely published in the literature. Since binary nanofluids (BNFs) and ternary nanofluids (TNFs) are emerging nanohybrids, published works are also emerging fast on thermal conductivity measurement. Literature has widely reported dramatic

enhancement in thermal conductivity with the additions of NPs, BNPs, and TNPs into various BFs at very low concentrations [21, 39, 42, 62, 96, 114, 128, 140, 151, 152, 156, 160, 171, 181, 188, 210, 220, 227-232]. However, with the growing volume of literature with time, some key inconsistencies were observed in the research findings. Such discrepancies in thermal properties' enhancement can result from the following factors, like applied stability methods, measurement techniques, mixing ratio, nanoparticle's purity, nanoparticle's size, particle shape, pH of the suspension, scale of agglomeration, temperature, to mention some.

Aybar et al. [233] widely reviewed the system (static and dynamics) suggested to be accountable for the atypical improvement of effective thermal conductivity as a result of the dispersion of NPs or BNPs or TNPs into different BFs. The static system presumed that NPs are stationary in NFs and this entails - aggregation, fractal geometry, interface thermal resistance, nanolayering, and percolation, while the dynamic components assumed chaotic movement of NPs in NFs, like Brownian motion and nanoscale convection. Masuda et al. [19] first measured effective thermal conductivity of NFs and published a k enhancement of 30%, when alumina NPs (13 nm) was suspended into the water at  $\varphi = 4.3$  vol.%. Studies on the formulation and measurement of thermal conductivity ( $\kappa$ ) of NFs seems to be on the increase. Jana *et al.* [43] formulated and measured  $\kappa$  for aqueous-based single-NFs (Au, CNT and Cu) and observed a lower value than the BF. Choi and Eastman [20] reported a 3.5-fold  $\kappa$ improvement for an aqueous-based Cu NF at  $\varphi = 20$  vol.%. Again, Choi et al. [234] studied the  $\kappa$  of water-based NF using SWCNTs. They reported a 19.40% improvement of 0.89 wt% at SWCNT. Also, Agarwal et al. reported an enhancement of 31% and 30% for  $\kappa_{eff}$  for EG- and DW-based Al<sub>2</sub>O<sub>3</sub> NFs at temperature of 70 °C and  $\varphi = 2.0$  vol.%. Next, Pastoriza-Gallego et al. formulated Fe<sub>2</sub>O<sub>3</sub>/EG and Fe<sub>3</sub>O<sub>4</sub>/EG NFs at  $\varphi = 0.011 - 0.069$  vol.% and temperature 10 -50 °C and reported a  $\kappa_{eff}$  enhancements of 2% – 15% and 1% – 11%, respectively. Wang et al. [235] published the  $\kappa_{eff}$  of Cu/DIW and Al<sub>2</sub>O<sub>3</sub>/DIW NFs with an enhancement of 18% and 15% for weight fraction of 0.8% at room temperature.

Recent works were also published on the formulation and measurement of thermal conductivity ( $\kappa$ ) of BNFs and TNFs, majorly on the factor of temperature and  $\varphi$ . Chopkar et al. [44] reported an improved k of 50-150% when Ag<sub>2</sub>Al and Al<sub>2</sub>Cu HNPs were synthesized in water and EG to prepare BNFs for  $\varphi$  range of 0.20 to 1.50 vol.%. Amiri et al. [216] examined the  $\kappa$  of single-NFs (SiO<sub>2</sub>/EG and SiO<sub>2</sub>/water) and compared with  $\kappa$  results of BNFs of SiO<sub>2</sub>-Cu/EG and SiO<sub>2</sub>-Cu/water. The authors reported that the steady addition of SiO<sub>2</sub> NP leads to 2% enhanced  $\kappa$  and increasing deposition of Cu NPs produces about 11% and 11.5% augmentation of  $\kappa$  of EG and water, respectively. They investigated the effect of temperature (25 to 50 °C) and  $\varphi$  range 0.10 - 3.50 vol.%, Toghraie et al. [236] formulated ZnO-TiO<sub>2</sub>/EG BNF and reported an enhanced κ under increasing  $\varphi$  and temperature. The highest  $\kappa$  enhancement of 32% was observed at 3.5 vol.% for temperature 50 °C. Investigating using MWCNT (0.05 vol%)-Fe<sub>2</sub>O<sub>3</sub> (0.020 vol.%) aqueous-based BNF at room temperature, Chen et al. [237] reported augmentation of 27.75% over the BF. Again, Chen et al. [175] published an enhanced κ of Ag–MWCNT/Water BNF over the MWCNT/water NF for a 1.0% volume fraction and temperature range 5-65 °C. Next, Askari et al. [238] studied the  $\kappa$  for Fe<sub>3</sub>O<sub>4</sub>–Graphene (20:80)/DIW nanohybrid at a mass percentage of 0.1–1.0 mass% under the influence of increasing temperature 20–40 °C, which reported an improvement of 14–32%. Furthermore, Esfahani et al. [239] investigated the  $\kappa$  of aqueous-based ZnO-Ag (50%:50%) BNF at temperature 25–50 °C and  $\varphi$  of 0.125–2.0% and reported the highest  $\kappa$  at 50 °C and 2.0 vol%. Recently, Rostami et al. [240] studied the  $\kappa$  for CuO-GO(50:50)/EG-W(50:50 vol%) nanohybrid at increasing  $\varphi$  of 0.10 to 1.60 vol.% for temperatures 25 to 50 °C. They obtained the highest enhancement of 43.4% when  $\varphi$  was 1.6 vol% at 50 °C. In addition, Harandi et al. [241] published 30% improvement for thermal conductivity ratio (TCR) of FMWCNTs-Fe<sub>3</sub>O<sub>4</sub>/EG HNF for the particle concentration 2.30

vol.% at 50 °C. They further discovered that temperature visibly influenced TCR at higher concentrations. Lately, the influence of variation in  $\varphi$  (0.005–0.1 vol%), temperatures (25–40 °C), and PMRs (30:70, 50:50, 70:30) on the  $\kappa$  of Al<sub>2</sub>O<sub>3</sub>-Ag/DW BNF was examined by Aparna et al. [227]. The authors published the highest  $\kappa$  with the 50:50 ratio. The BNF had a maximum  $\kappa$  than the NFs of Ag/DW and Al<sub>2</sub>O<sub>3</sub>/DW. Rostami et al. [123] also published a 30.8% augmentation in k at 0.60 vol.% for CNT-CuO/Water nanohybrid. Also, Du et al. [156] studied TCE of water-based Fe<sub>3</sub>O<sub>4</sub> NF and Fe<sub>3</sub>O<sub>4</sub>-MWCNT BNF for temperature ranges 25–50 °C for  $\varphi = 0.2-1.0$  vol%. The NF and BNF achieved  $\kappa$  enhancement of 32.76% and 33.23% at 50 °C and 1.0 vol%, respectively. The nanohybrid of Fe<sub>3</sub>O<sub>4</sub>-MWCNT obtained  $\kappa$  of 0.47%. Again, Soltani et al. [242] determined  $\kappa$  for MWCNT-Tungsten oxide/engine oil BNF, and reported a highest improvement of 19.85% at 60 °C and 0.6 vol% of the HNPs. More recently, Wole-sho et al [179] also examined the influence of changing temperatures 25 to 40 °C at  $\varphi$  of 0.33–1.67 vol% and NMRs (1:2, 1:1, 2:1) of distilled water-based Al<sub>2</sub>O<sub>3</sub>-Zn nanohybrid. The  $\kappa$ enhancements values are 35%, 36%, and 40% for PMRs of 1:1, 1:2, and 2:1 respectively, at  $\varphi$ = 1.67 vol% and 40 °C. Gangadevi and Vinayagam [243] compared the  $\kappa$  performance for water-based NFs of CuO and Al<sub>2</sub>O<sub>3</sub> and BNF of CuO-Al<sub>2</sub>O<sub>3</sub> (50:50) for changing  $\varphi$  (0.05–0.20 vol%) and temperature (20–60 °C).  $\kappa$  improved at 21%, 12.16%, and 11.2%, for CuO-Al<sub>2</sub>O<sub>3</sub>/W BNF, CuO/W NF and Al<sub>2</sub>O<sub>3</sub>/W NF respectively, at 0.20 vol% and 60 °C in comparison with BF. The nanohybrid effectively reduced the temperature of a hybrid solar collector, thus improving overall system efficiency. Considering changes in temperatures (30-60 °C), PMRs (25:50, 50:50, and 75:25) and  $\varphi$  (0.1–0.5 vol%), Mechiri et al. [244] evaluated experimentally for  $\kappa$  of Cu–Zn (50:50)/groundnut HNF. They observed that  $\varphi$  and temperature had impact on  $\kappa$  more than PMR.

In addition, the formulation of green NFs (GNFs) was also noticed to enhance thermal conductivity ( $\kappa$ ), with great potential for the future considering environmental factors. Khdher

et al. [48] examined the  $\kappa_{eff}$  of Al<sub>2</sub>O<sub>3</sub> NPs suspended in different BFs - green BF (bio-glycol), EG, and PG and reported  $\kappa_{eff}$  augmentation of 17%, 9%, and 3.6% (1.0 vol.% and 30 °C), respectively. Yarmand et al. [102] also studied the  $\kappa_{eff}$  of BNF (0.02 – 0.6 wt.% and 20 – 40 °C) formulated using synthesised NPs of fruit bunch and GO NPs dispersed in EG, and published a maximum augmentation of 6.47% at 0.06 wt.% and 40 °C.

Considering TNFs, Ahmed et al. [189] examined  $\kappa_{eff}$  of ZnO-Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>/DW TNF for temperatures 20 to 45 °C for wt.% concentrations of 0.025, 0.05, 0.075, and 0.1. The authors reported an increasing trend in  $\kappa_{eff}$  as temperature values increases. The suspension of all metal oxide NPs in distilled water resulted in an enhancement in  $\kappa_{eff}$  steadily by the variations in nanofluids temperature, which makes it good for heat transfer applications. Also, Mousavi et al [24] elucidated the effects of NPs volume concentration (0.1–0.5%) and temperature (15– 60 °C) on the  $\kappa$  of aqueous-based CuO–MgO–TiO<sub>2</sub> TNF. The authors published an increased  $\kappa$  at increasing temperature and solid particles volume concentration. Next, Xuan et al. [39] reported that mixing ratio 40:40:20 (Al<sub>2</sub>O<sub>3</sub>:TiO<sub>2</sub>:Cu) had the optimum thermal conductivity for a water-based Al<sub>2</sub>O<sub>3</sub>:TiO<sub>2</sub>:Cu TNF, measured at 0.005-1 vol.% over temperature 20 – 60 °C. Again, Cakmak et al. [245] formulated a rGO-Fe<sub>3</sub>O<sub>4</sub>-TiO<sub>2</sub> TNPs dispersed in EG for 0.01–0.25 mass.% and over temperature 25 – 60 °C. They reported a significant  $\kappa$  increase with increase in mass concentration and temperature, with maximum enhancement achieved at 13.3% at 60 °C for 0.25 wt.%, making it useful for both cooling and heating applications with long term stability.

#### 2.6.2 Viscosity

Viscosity ( $\mu$ ) is a thermal property that defines the resistance to flow of fluid under shear stress. The dispersion of NPs, BNPs and TNPs into BFs produced an increased effective viscosity ( $\mu_{eff}$ ). The enhancement in  $\mu_{eff}$  associated a related increase in  $\kappa_{eff}$  (with an increase in  $\varphi$ ) through improved heat transfer of NFs, BNFs and TNFs for thermal applications, at the cost of high pump power. Hence, the challenge of using nanofluids for thermal transport applications. It is of note that at high  $\varphi$ , high  $\mu_{eff}$  overrules the advantage of high  $\kappa_{eff}$  and thus deteriorates heat transfer rather than enhancement when nanofluids is adopted as coolants for thermal systems. But, at lower  $\varphi$ , which denotes lower  $\mu_{eff}$ , nanofluids works well as heat transfer fluid. Viscosity is reported to be dependent on parameters like temperature, pH, nano-shape, nanosize, sonication time and intensity, and volume concentration [246]. The entrance of BNFs and TNFs for thermal applications also calls for µ<sub>eff</sub> measurements [21, 30, 32, 68, 83, 96, 119, 148, 151, 160, 172, 185, 188, 205, 210, 223, 228, 247-255]. It is well observed for the trio of NFs, BNFs and TNFs that temperature increase leads to a reduction in  $\mu_{eff}$ , while a rise in  $\varphi$  produced an increment in µeff. Soltani and Akbari [256] examined the effect of temperature 30 to 60 °C and particle concentration 0 to 1.0% on  $\mu$  of MgO-MWCNT/EG BNF and reported a Newtonian behavior with  $\mu$  in a reducing trend at temperature increase and enriched  $\mu$  at increased particle concentration. Also, Esfe et al. [257] evaluated the  $\mu$  of an aqueous-based nanohybrid of Ag–MgO (50:50) for  $\varphi = 0-2\%$ , and achieved enhancement with increasing  $\varphi$ . Suresh et al. [258] achieved an enhancement of 8–115% for  $\mu$  for an aqueous-based Cu-Al<sub>2</sub>O<sub>3</sub> (10%:90%) BNF at  $\varphi = 0.1-2\%$ . Next, Asadi and Asadi [252] examined the  $\mu$  of MWCNT-ZnO/Engine Oil (10W40) BNF and reported temperature having a higher impact on  $\mu$  than particle concentration, thus achieving a maximum deterioration in dynamic viscosity of 85% for temperature 55 °C. Also, Afrand et al. [250] computed a recent model to predict  $\mu$  of hybrid nanolubricant of MWCNT-SiO<sub>2</sub>/AE40 using experimental values. They further developed an optimized ANN model to predict  $\mu$ , making a comparison. They reported the ANN model having better performance than the empirical model. Next, Gangadevi and Vinayagam [243] compared  $\mu$  performance for water-based NFs of CuO and Al<sub>2</sub>O<sub>3</sub> and BNF of CuO-Al<sub>2</sub>O<sub>3</sub> (50:50) for increasing  $\varphi$  (0.05–0.20 vol%) and temperature (20–60 °C).  $\mu$  improved at 2–11% as compared with aqueous-based CuO NF, Al<sub>2</sub>O<sub>3</sub>/W NF had the minimum. The nanohybrid

effectively reduced the temperature of a hybrid solar collector, thus improving overall system efficiency. In addition, Alirezaie et al. [259] examined the rheological behaviour of *f*MWCNT-MgO/Engine oil BNF and reported an abrupt reduction in  $\mu$  with temperature. Further observation was a non-Newtonian behaviour at reduced temperature and Newtonian at higher temperatures. Recently, Motahari et al. [260] experimentally studied the  $\mu$  of MWCNT-SiO<sub>2</sub>/SAE20W50 nanohybrid at  $\varphi = 0.05-1.0$  vol% and temperature range 40 to 100°C. The nanohybrid exhibited Newtonian behaviour for all concentrations and temperatures, with an enhanced  $\mu$  of 171% at peak particle concentration and temperature.

Considering changes in temperatures (30–60 °C), PMRs (25:50, 50:50, and 75:25) and  $\varphi$  (0.1– 0.5 vol%), Mechiri et al. [244] evaluated experimentally for  $\mu$  of Cu–Zn (50:50)/groundnut HNF. They observed that  $\varphi$  and temperature affect  $\mu$  more than PMR. Both BF and nanohybrid exhibited Newtonian behaviour. Also, Hamid et al. [261] studied  $\mu$  for TiO<sub>2</sub>–SiO<sub>2</sub> (40–60)/W-EG (60:40) BNF for varying PMRs (20:80–80:20) for temperatures 30–80 °C at  $\varphi = 1.0$  vol%. They reported a maximum improvement for  $\mu$  for PMR 40:60, which makes it good for thermal cooling purposes. PMR of 50:50 has the poorest cooling properties. Also, Giwa et al. [172] investigated the impact of PMRs (20:80, 40:60, 60:40, 80:20, and 90:10) and different temperatures 15–55 °C on the  $\mu$  of Al<sub>2</sub>O<sub>3</sub>–MWCNT/DIW BNF. They obtained a peak augmentation of 288.0% and 442.9% for  $\mu$  of Al<sub>2</sub>O<sub>3</sub>–MWCNT/DIW BNF at PMRs of 20:80 and 90:10, respectively, compared to DIW. Also observed is that with increasing temperatures,  $\mu$  deteriorates significantly, making it viable for engineering systems. Again, Giwa et al. [96] first investigated the trio effects of temperatures 20–50 °C,  $\varphi$  (0.05–0.75 vol.%), and BFs (EG-DIW and DIW) on the performance of  $\mu$  of nanohybrid of Al<sub>2</sub>O<sub>3</sub>– Fe<sub>3</sub>O<sub>4</sub>(25:75). They reported that  $\mu$  was improved by 3.23–43.64% and 2.79–49.38% for the DIW-based and EG–DIWbased nanohybrid compared to the individual BF. They further discovered that enhancing  $\varphi$ improves  $\mu$  for the two BNFs, while an augmented temperature deteriorated  $\mu$ . The DIW-based BNF possessed minimal  $\mu$  over the EG–DIW-based nanohybrid. Furthermore, Giwa et al. [154], for the first time, experimented with the trio influence of PWRs (20:80, 40:60, 60:40, 80:20), NS and temperature (20–50 °C) on the thermal behaviour of MgO (20 and 100 nm)-ZnO/DIW BNF at 0.1 vol%. Authors reported that BNF with 100 nm MgO NP had higher values of  $\mu$  than that of BNF with 20 nm MgO NP. Also, it observed that temperature increase deteriorates  $\mu$ . The highest augmentation for  $\mu$  was 8.29–17.46% (60:40). More recently, Wanatasanapan et al. [262] studied the impact of Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub> NPs mixing composition on the thermal-fluid behaviour of the water-based BNFs. The water-based BNFs were formulated with five various ratios of Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> NPs at a constant 1.0 vol% for temperatures 30–70 °C. The BNFs exhibited a Newtonian fluid pattern for all NPs temperature and mixing ratios, with ratio 80:20 having the maximum  $\mu$  of 1.98 mPas.

In addition, the formulation of green NFs (GNFs) for the measurement of viscosity was reported. Adewumi et al. [247], Kallamu et al. [254], and Sharifpur et al. [158] published the  $\mu_{eff}$  of GNFs formulated by dispersing synthesised NPs of coconut fibre carbon, banana fibre, and mango bark into EG-DIW (60:40), DIW, DIW, respectively. They reported a similar pattern for  $\mu_{eff}$  of GNFs compared with NFs under increasing temperature and  $\varphi$ . Adewumi et al. [247] and Kallamu et al. [254] reported  $\mu_{eff}$  enhancement of 50% (1 wt.% and 60 °C) and 22% (60 °C and 1.5 vol.%) for the coconut fibre carbon and banana fibre NFs in comparison to EG-DIW and DIW, respectively. In addition, Yarmand et al. [263] [102] first formulated and measured the  $\mu_{eff}$  of binary green-metallic nanofluid, prepared by despersing synthesised NPs of fruit bunch and GO NPs into EG. They published a maximum  $\mu_{eff}$  improvement of 4.16% (0.06 wt.% and 40 °C) compared to EG.

For TNFs, Zayan et al. [38] reported that the deionised water dispersed graphene-based TNFs (GO-TiO2-Ag and rGO-TiO2-Ag) exhibited a Newtonian behaviour at higher concentrations. Also, Ahmed et al. [189] reported higher viscosity values at 0.1 wt.% concentrations of ZnO-

Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>/DW TNF, compared to the other three concentrations (0.025, 0.05 and 0.075 wt.%) at similar experimental conditions. Furthermore, Mousavi et al. [24] elucidated the effects of NPs volume concentration (0.1–0.5%) and temperature (15–60 °C) on the dynamic viscosity of aqueous-based CuO–MgO–TiO<sub>2</sub> TNF. The authors published an increased dynamic viscosity at increasing temperature and solid particles volume concentration. All TNF samples displayed Newtonian behaviour. Next, Xuan et al. [39] reported that mixing ratio 40:40:20 (Al<sub>2</sub>O<sub>3</sub>:TiO<sub>2</sub>:Cu) had the lowest viscosity for a water-based Al<sub>2</sub>O<sub>3</sub>:TiO<sub>2</sub>:Cu TNF, measured at 0.005-1 vol.% over temperature 20 – 60 °C.

#### 2.6.3 Electrical Conductivity

The electrical conductivity ( $\sigma$ ) of nanohybrids is the ability to enhance the mobility of electrical charges due to ionized nanoparticles activated during nanodispersion, thus making it conduct electricity upon applying an electric potential across it. This property aids the monitoring of stability and the extent of suspension of NPs in the basefluids [21, 31, 96, 172, 204, 255, 264, 265]. Unlike viscosity and thermal conductivity, literature are emerging on the  $\sigma$  of NFs, BNFs and TNFs, compared to viscosity and thermal conductivity. This thermal property  $\sigma$  has direct and strong relation with electrostatic characteristics (IEP, EDL, and zeta potential),  $\varphi$ , nanosheets  $\varphi$ , NPs size, and nanosheets charge and stability of NFs/BNFs/TNFs [21, 30, 172, 223, 266-269].

The formulation of various NFs, BNFs and TNFs from different NPs and basefluids, literature reports that the electrical conductivity of NFs, BNFs or TNFs either augmented with temperature increase and mass/volume fraction or concentration [21, 30, 103, 172, 223, 238, 267, 269-271] or independent of temperature [30, 272, 273], or distracted with a rise in volume/mass concentration or fraction [274, 275]. Considering the impact of  $\varphi$  (0.5 – 3.0 vol.%), temperature (20 – 70 °C) and nano-sizes (20 nm and 100 nm), Adio et al. [271] published a highest enhancement of 6000% for  $\sigma_{\text{eff}}$  of MgO/EG NF, which increases as

temperature,  $\varphi$ , nano-size increases too. For temperature 25 – 45 °C and  $\varphi$  (0 – 100 vol.%), Guo et al. [276] formulated SiO<sub>2</sub>/EG-W nanofluids for 0.3 wt.% and measured an augmented  $\sigma_{eff}$  at increased temperature and reduced EG content of basefluid. Next, Shoghl et al. [277] investigated the  $\sigma_{eff}$  of aqueous-based nanofluids of Al<sub>2</sub>O<sub>3</sub>, CNT, CuO, MgO and ZnO, at 27 °C and noticed that the augmentation of  $\sigma_{eff}$  is dependent on an increase in  $\varphi$  and types of nanoparticles. ZnO/W nanofluid produced the highest  $\sigma_{eff}$  for lower  $\varphi$  and CNT/W nanofluid yielded the maximum  $\sigma_{eff}$  at high  $\varphi$ .

Also engaging BNFs, Yarmand et al. [263] investigated the  $\sigma_{eff}$  of green-metallic BNF and observed augmentation as temperature and  $\varphi$  increases, with maximum enhancement of 787.5% at 0.06 wt.% for 45 °C. Similar results align with the works of Adio et al. [269, 271], Awua et al. [32], Giwa et al. [21, 96, 223], Heyhat et al. [278], Naddaf et al. [279]. For TNFs, Manjunatha et al. [280] mathematically defined the  $\sigma$  of aqueous based TiO<sub>2</sub>-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> TNF.

# 2.6.4 Specific Heat Capacity

Specific Heat Capacity ( $C_p$ ) is another significant thermal property of NFs, BNFs and TNFs. It is described as a measure of the heat retentive property or heat storage capacity of NFs, BNFs and TNFs [281, 282]. Thus, defining the thermal behaviour of the NFs/BNFs/TNFs. It is a key parameter for assessing energy and exergy performance [282, 283]. Also useful for computing thermal conductivity [282, 284], thermal diffusivity [285, 286], spatial temperature within a flow [287] and for assessing the convective flow positions [288] of NFs/BNFs/TNFs. A huge research gap exists on the latter. The limited literature on the measurement of  $C_p$  posits that two sets of BFs (high and low temperature) are needed for suspending various NPs, BNPs and TNFs in it at different temperatures and mass/weight/volume fractions or concentrations [30, 283]. For the type with high temperature, molten nanosalts is used as BFs, while conventional BFs (DW, DIW, EG-DIW, EG, EO, ionic liquids, PG, thermal oil, W, etc.) is used for the lowtemperature category. Note, measured values of  $C_{p-eff}$  will differ in line with the BFs type, all a function of temperature,  $\varphi$ , and nano-size.

A lot of disparity is reported in the literature on the impact of temperature and  $\varphi$  on the C<sub>p-eff</sub> property of NFs/BNFs/TNFs. Reviewing NFs, Robertis et al. [289] examined the C<sub>p-eff</sub> of Cu– EG NF and observed a C<sub>p</sub> enhancement with rise in temperature, while a rise in  $\varphi$  led to reduction in C<sub>p-eff</sub> (values lower than C<sub>p</sub> BF). A similar pattern was noticed by Vajjha and Das [290], who investigated the C<sub>p-eff</sub> of EG-DW(60:40)-based Al<sub>2</sub>O<sub>3</sub>, ZnO, and SiO<sub>2</sub> NFs for increasing temperature (42 – 90 °C) and  $\varphi$  (2 – 10 vol.%). Similar temperature rise improved C<sub>p-eff</sub>, but reduced with an increased  $\varphi$ , and C<sub>p-eff</sub> of NFs found lower than that of the BF. A slight shift was published by Ijam et al. [272], who reported a C<sub>p-eff</sub> enhancement for  $\varphi$  < 0.05 wt.% by 3.59% – 5.28% as temperature rises when GO/DW-EG NF was examined for temperature (25 – 60 °C) and  $\varphi$  (0.01 – 0.1 wt.%).

A contrasting pattern was advanced by Oster et al. [291], who reported a C<sub>p-eff</sub> enhancement for ionanofluids at both temperatures (25 – 90 °C) and  $\varphi$  (0.5 – 3.0 wt%) increases. Similar trend was published by Yarmand et al. [263], who reported a C<sub>p-eff</sub> enhancement as both temperature and  $\varphi$  increases for an EG-based green-metallic BNF. At 50°C, C<sub>p-eff</sub> was enhanced by 2.25% for  $\varphi$  of 0.060 wt.%. For TNFs, Mousavi et al [24] elucidated the effects of NPs volume concentration (0.1–0.5%) and temperature (15–60 °C) on the specific heat capacity of aqueous-based CuO–MgO–TiO<sub>2</sub> TNF. The authors published an initial decrease of up to 35 °C and thereafter enhanced with increasing temperature. These values will be due to the individual C<sub>p</sub> of NPs and the nanolayer effect.

# 2.6.5 Density

Density ( $\rho_{eff}$ ) has a direct relationship with Nusselt number (*Nu*), Rayleigh number (*Ra*), friction factor, Reynolds number (*Re*), and pressure drop of NF for convective heat transfer.

As a thermal property of NFs/BNFs/TNFs, it is scarce in the literature but reported along with other thermal properties [24, 56, 105, 155, 189, 238, 263, 277]. Literature report an augmentation in  $\rho_{eff}$  as NPs, BNPs and TNPs is dispersed in various basefluids and detracts as temperature rises, because NPs, BNPs and TNPs possess higher density than basefluids [24, 30, 155, 189, 238]. For NFs, Sharifpur et al. [155] reported a  $\rho_{eff}$  augmentation for NFs (CuO-GL, MgO-GL, SiO<sub>x</sub>-EG/Water (60:40), and SiO<sub>2</sub>-W) as  $\varphi$  raised from 1.0 – 6.0 vol.% and detracted as temperature progressed 10 – 40 °C. Shoghl et al. [277] published a similar pattern of enhanced  $\rho_{eff}$  as  $\varphi$  rises from 0.01 – 2 wt% and detracts with temperature rises 30 – 40 °C for water-based Al<sub>2</sub>O<sub>3</sub>, CuO, MgO, MWCNT, TiO<sub>2</sub>, and ZnO NFs.

For BNFs and TNFs, literature reporting the measurement of  $\rho_{eff}$  is quite limited. Yarmand et al. [263] published a highest augmentation of 0.090% for 20°C at  $\varphi$  of 0.060 wt.% for EGbased green-metallic BNF. Askari et al. [238] reported similar trend for  $\rho_{eff}$  enhancement for Fe<sub>3</sub>O<sub>4</sub>-G/DIW BNF. For TNFs, Mousavi et al. [24] elucidated the effects of NPs volume concentration (0.1–0.5%) and temperature (15–60 °C) on the density of aqueous-based CuO– MgO–TiO<sub>2</sub> TNF. The authors reported a light enhancement in a linear pattern concerning NPs loading. Note, density is linearly deteriorated as the temperature of the TNFs increases. Also, Ahmed et al. [189] reported a reduction in density as temperature increases for all wt.% (0.025, 0.05 and 0.075 wt.%) for ZnO-Al<sub>2</sub>O<sub>3</sub>-TiO<sub>2</sub>/DW TNF.

#### 2.6.6 Other Properties

Other measured thermal properties of NFs in open literature are breakdown voltage [292-294], contact angle [295-297], extinction coefficient [153, 196, 298], flash point [299, 300], shear stress [301, 302], surface tension [142, 297], transmittance [153, 196, 303], volumetric heat capacity [153, 304]. Also, for BNFs, the following are reported - breakdown voltage [305, 306], contact angle [143, 307], extinction coefficient [308, 309], flash point [310], shear stress [39, 311], surface tension [143, 312], transmittance [308, 309]. Using TNFs, the following

were measured - contact angle [313], extinction coefficient [314, 315], shear stress [24, 188], surface tension [24, 316], transmittance [314].

### 2.7 THERMO-CONVECTION OF NFs, BNFs and TNFs IN CAVITIES

Thermo-convection or natural convection persists in finding increasing use [78, 161, 317-325] in thermal-based systems, with the growing application of BNFs and TNFs as optimum thermal fluids due to their improved thermal properties when compared to NFs and traditional fluids. Thermo-convection or natural convection is a heat transfer method in which thermal transport is basically dependent on the density gradients of applied working (thermal) fluid. Thermo-convection applications span agriculture, aviation, desalination, electronic cooling system, geophysical systems, heat exchangers, industrial processes, nano-lubrication, nuclear energy, photovoltaic modules, power generation, solar energy transport, telecommunication, to thermal energy storage systems.

Khanafer *et al.* [326] analytically pioneered the natural convective properties of nanofluids (Cu/Water) inside a squared enclosure. Thus, more investigation with the use of nanofluids, BNFs and TNFs for free convection in different enclosure shapes (more prominent is squared enclosure, others are cylinder, porous, rectangular, and triangular) continue to accumulate momentum, either by numerical method or experiment-based [25-27, 29, 70, 102, 253, 317, 321, 327-332]. The parameters that impact thermo-convection performance are cavity design, the concentration of NPs, nanofluids types, PWRs, and particle density. Putra et al. [333] first experimentally studied the thermo-convection behaviour of nanofluids inside a cavity. The laboratory set-up employed distilled water-based Al<sub>2</sub>O<sub>3</sub>, and CuO NFs at  $\varphi$  of 1-4 vol%, charged inside a differentially-heated cylindrical shaped (positioned horizontal-wise) with aspect ratio (AR) equals to 0.5 - 1.5. The experimental set-up yielded a detracted theirconvection performance, as estimated by aspect ratio,  $\varphi$  and  $\rho$  of nanoparticle sample.

#### 2.7.1 Square Cavities

Using NFs, Kouloulias et al. [159] investigated the thermo-convection heat transfer of Al<sub>2</sub>O<sub>3</sub>/W (0.01 – 0.12 vol%) NF within a square enclosure. The authors observed a heat transfer deterioration compared to the BF. Next, Hu et al. [334] investigated the impact of various weight concentrations (3.85 – 10.71 wt.%) of TiO2/DIW nanofluid inside a square enclosure experimentally and observed a heat transport depletion as related to basefluid. Li et al. [335] studied the impact of ZnO nanoparticles dispersed in EG/DIW (25/75; 15/85; 5/95 vol%) basefluid with  $\varphi$  of 5.25 wt.% inside a square enclosure. Authors published a heat transfer detraction compared to EG-DIW, but augments as EG rises in the mixture ratio of basefluid. Also, studying the impact of volume concentrations, Garbadeen *et al.* [27] examined the thermo-convection behaviour of MWCNT/Water nanofluid experimentally inside a squared enclosure for  $\varphi$  of 0 to 1.0 vol.%, and *Ra* = 10<sup>8</sup>. An optimal heat transfer enhancement of 45% was recorded at 0.1 vol.%.

The free convective heat transfer of DW-based Al<sub>2</sub>O<sub>3</sub> (0.1 – 4 vol.%) NF charged into three separate square cavities was examined by Ho et al. [336], with a heat transfer enhancement at lower  $\varphi$  (0.1 vol.%) for all cavities and augmented with cavity size. Heat transfer enhancement at was maximum with the largest cavity at 18% when compared to DW. In addition, Joshi and Pattamatta [337] examined by experiment the thermo-convection behaviour of Al<sub>2</sub>O<sub>3</sub>/Water and MWCNT/Water nanofluids inside a square enclosure, at  $\varphi$  of 0.1-2 vol.% for Al<sub>2</sub>O<sub>3</sub>/Water nanofluids and 0.10-0.50% for MWCNT/Water nanofluids. An improved Nusselt number was recorded for the two nanofluids at enhanced *Ra*, and maximum *Nu* enhancement at 0.10 vol.%, while MWCNT/Water nanofluids possessing maximum *Nu* improvement. Solomon et al. [338] experimented with the impact of aspect ratios (1, 2, 4) on enclosures on the natural convection of water-based Al<sub>2</sub>O<sub>3</sub> NFs. They observed that the aspect ratios of the enclosure had a major impact on the heat transfer coefficient and *Nu*. They reported an optimal heat transfer for each aspect ratio of the enclosures to correlate with NF concentration. For an aspect ratio of 1, the convective heat transfer coefficient and highest heat transfer were achieved for 0.10 vol%. It was also observed that Ra had a big influence on buoyancy and the Nu.

Open literature is just gaining numbers as regards BNFs. Thus an excellent thermo-convective performance is observed when compared to nanofluids. Giwa et al. [329] pioneered the laboratory study of natural convection behaviour of Al<sub>2</sub>O<sub>3</sub>-MWCNT (95:5 and 90:10)/DIW BNF inside a squared enclosure at  $\varphi$  of 0.10 vol%, that produced an enhanced heat transfer over that of Al<sub>2</sub>O<sub>3</sub>/DIW NF and BF. Further study by Giwa et al. [317] investigated the effect of percent weight ratios (80:20, 60:40, 40:60, 20:80 for MWCNT/Al<sub>2</sub>O<sub>3</sub>) for 0.10 vol.% at *Ra* of  $1.65 \times 10^8$ – $3.80 \times 10^8$  on natural convection behaviour in a squared cavity. The BNF sample with 40:60 PWR got the maximum values for *Ra*, *Nu*<sub>av</sub>, *h*<sub>av</sub>, and *Q*<sub>av</sub> at various temperatures. When compared with basefluid, the highest enhancement of 16.20%, 20.50% and 19.40% were achieved for *Nu*<sub>av</sub>, *h*<sub>av</sub>, and *Q*<sub>av</sub>, respectively, at  $\Delta T = 50$  °C. Results demonstrate an increase of heat transfer coefficient with increasing temperature difference. However, nanoparticles concentrations reveal interesting trends, such that the lowest concentration (0.05 vol.%) produced maximum heat transfer coefficient, which detracts with growing concentration.

# 2.7.2 Triangular Cavities

Literature is limited on the experimental investigation of thermo-convection performance using triangular enclosures. Umar et al. [339] conducted a thermo-convection experiment for  $ZrO_2/W$  nanofluid in triangular and rectangular channel geometry and recorded HTC improvement of 5–10% for volume concentration ( $\varphi$ ) of 0.05 vol.% in comparison to BF. Next, the influence of two empirical models with an experimental-based model on the *Nu* and *h* ratio of water-based SiO<sub>2</sub> (0.5 – 2.0 vol.%) nanofluid inside a triangular enclosure was examined by Mahian et al. [340]. The authors recorded a detraction in Nusselt number (*Nu*) with increased volume

concentration ( $\varphi$ ), an independent parameter of *Ra*. For any *Ra*, *h* of nanofluid was noticed to be more than BF. Maximum heat transfer was achieved at volume concentration ( $\varphi$ ) of 0.5 vol.%.

# 2.7.3 Rectangular Cavities

Open literature is replete with the use of rectangular cavities for thermo-convection heat transfer. Sharifpur et al. [330] studied the thermo-convection performance of TiO<sub>2</sub>-DIW (0.05 -0.8 vol.%) NF inside a rectangular cavity and noticed enhanced heat transfer between 0.05 -0.2 vol.% and detracted thereafter. The highest augmentation of 8.2% was reported at 50 °C and 0.05%. Ghodsinezhad et al. [25] published a 15% increase for convective heat transfer coefficient (HTC) for Al<sub>2</sub>O<sub>3</sub> (0.05 – 0.6 vol.%)/DIW nanofluid in a rectangular cavity at  $\varphi$  = 0.1 vol.%. For weight concentration of 0-1.0 wt% for MWCNT/thermal oil nanofluids, charged in a rectangular cavity (vertical), Ilyas et al. [341] observed a detraction for Nu and h, while  $\varphi$  rises. In addition, Nnanna et al. examined the free convection behaviour of Al<sub>2</sub>O<sub>3</sub> (0.2–8 vol.%)/DIW NF within a rectangular cavity and noticed a heat transfer augmentation for 0.2-2.0 vol.% thereafter deteriorated at over 2%. Maximum enhancement was observed at 0.2 vol.%. Next, Solomon et al. [331] investigated the thermo-convection heat transfer behaviour of green (Mango bark/DIW) nanofluid in a rectangular enclosure for  $\varphi$  of 0.01–0.50 vol%. They recorded a detracted heat transfer coefficient in relation to basefluid. A rectangular cavity having MWCNT-hexylamine/TO (0.001 – 0.005 wt.%) NFs was studied by Amiri et al. [292] for thermo-convection performance [143] and recorded an enhanced Nu and h of NFs over the BF, which increased with  $\varphi$ . Choudhary [342] tested the impact of  $\varphi$  (0.01% & 0.1%) for DIWbased Al<sub>2</sub>O<sub>3</sub> NFs with ARs (0.3-2.5) for a rectangular enclosure for heat transfer behaviour. They recorded that natural convection behaviour is dependent on AR,  $\varphi$ , and *Ra*, for the highest enhancement of 29.50% for 0.010 vol.% (for AR of 0.5 and  $Ra = 7.89 \times 10^8$ ). Lately, Sharifpur et al. [173], for the first time, investigated the free convective heat transfer of ZnO/DIW

nanofluid inside a rectangular enclosure for diverse  $\varphi$  (0.100, 0.180, 0.360, 0.50, and 1.0 vol.%). They published an improved heat transfer coefficient of 9.14% when related to DIW, for 0.1 vol.% and change in temperature 32 °C. So, the free convection performance of the nanofluid detracted when volume concentration ( $\varphi$ ) increased over 0.10 vol%. Then, *Nu* and heat transfer rate enhanced by 8.42% and 6.75% for 0.10 vol%, respectively.

# 2.7.4 Cylinder Cavities

Putra et al. [333] tested the natural-convection within a cylinder (horizontal) geometry of aspect ratio (0.5–1.5) having DW-based Al<sub>2</sub>O<sub>3</sub> and CuO ( $\varphi = 1-4$  vol.%) nanofluid. The authors recorded a detraction in heat transfer due to AR,  $\varphi$  and nanoparticle density. Next, Ali et al. [343] experimented with free convection inside a cylinder geometry of aspect ratio (0.0635 and 0.127) and  $\varphi$  (0.21–0.75 vol.%) for Al<sub>2</sub>O<sub>3</sub>/DW nanofluid. A diminishing heat transfer performance was observed due to aspect ratio and  $\varphi$  when compared to basefluid. Also, Mahrood et al. [344] examined the thermo-convection behaviour within a cylinder (vertical) geometry of AR (0.5 - 1.5) with carboxymethyl cellulose-based TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> nanofluid. They published maximum enhancement of 23.5% and 19.5% for  $\varphi = 0.1$  vol.% and 0.2 vol.% for TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub> nanofluid, respectively. Also, AR improvement augments Nu for both nanofluids. In addition, Suganthi and Rajan examined the convective heat transfer performance for PG-based ZnO (0.25 - 2.0 vol.%) nanofluids inside a cylindrical cavity under fixed heat flux and temperature factors. An enhanced heat transfer at increased volume concentration ( $\varphi$ ) was observed for both factors. For fixed heat flux, the highest improvement of 4.24% was achieved, while 25.6% enhancement for a fixed temperature, both at volume concentration of 2.0 vol.%. Note, enhanced viscosity ( $\mu_{eff}$ ) detraction and enhanced thermal conductivity ( $\kappa_{eff}$ ) aided augmentation.

#### **2.7.5 Porous Cavities**

Solomon et al. [345] experimented with a porous media for the thermo-convection heat transfer performance of Al<sub>2</sub>O<sub>3</sub>/EG-DIW(60:40) nanofluid. The nanofluid was charged into a rectangular enclosure with porous media under  $\Delta T = 20 - 50$  °C for  $\varphi$  of 0.05 – 0.4 vol.%. Authors reported an enhanced Nusselt number (*Nu*) for the clear cavity than the porous cavity, where an increase in *Ra* enhanced *Nu*. At  $\varphi$  of 0.05 vol.% and temperature 50 °C, *Nu* was maximum and reduced with increased volume concentration ( $\varphi$ ).

# 2.8 ARTIFICIAL INTELLIGENCE MODELS TO PREDICT THERMAL PROPERTIES OF NANOFLUIDS

Progress in industrial concern has afforded commensurate growth in heat transfer systems' efficiency by optimizing thermal processes and properties [21, 64]. Binary nanofluids (BNFs) have found a good use for enhancing heat transfer applications, since BNFs have very good thermal behaviour than BFs [176, 346]. The improvement of thermal properties of BNFs has caught the attention of global research. Really, the experimental design for determining the thermal characteristics is costly and time-consuming [65]. Thermophysical properties like thermal conductivity and viscosity has to be defined experimentally, as numerical method is scanty or inadequate, while convective heat transfer rate can be calculated numerically [64, 347]. So, to handle the event of repeated experiments and encourage optimum data handling for big data, research is gradually shifting towards using artificial intelligence methods (like machine learning models, etc.) to industrial, engineering and scientific systems. Artificial Neural Network (ANN) is an iterative algorithm used to learn processes and has found good use in predicting the thermophysical properties of binary nanofluids [34, 35, 64, 66, 82, 96, 179, 181, 348-351]. Comparing with the classical approach, artificial neural network (ANN) is simple in design, of wide capacity and high process speed [72, 352-355]. Using generated

experimental data, developed ANN models have great potential in accurately predicting thermal conductivity.

Literature abounds with artificial neural network application used for predicting the thermal conductivity of nanofluids. Papari et al. [356] proposed an artificial neural network model to predict the thermal conductivity of MWCNTs dispersed in ethylene glycol (EG), oil, and water, which gave a very good value than theoretical methods. Next, Esfe et al. [352] also developed a model for the thermal conductivity (k) of Al<sub>2</sub>O<sub>3</sub>/Water NF using an artificial neural network, which presented a consistent value with experimental data. Also, Longo et al. [357] used the ANN model to predict the thermal conductivity of oxide-water NFs, with good values. In addition, Tahani et al. [358] used an artificial neural network to model the prediction of TC of GO/W nanofluid, which resulted in brilliant precision with the experimental dataset. Aghayari et al. [359] also used an artificial neural network approach for predicting the thermal conductivity of Fe<sub>3</sub>O<sub>4</sub>/W nanofluid, which gave a good thermal conductivity prediction. Also, Hosseinian Naeini et al. [360] employed artificial neural network modelling to predict the thermal conductivity of Fe<sub>2</sub>O<sub>3</sub>/water NF, the model had an effective result. Verma et al. [361] equally deployed an artificial neural network model to predict the TC of TiO<sub>2</sub> with different basefluids (EG, EO and W), a brilliant consistency with Laboratory data sets was noticed. The deployment of the artificial neural network model gave an excellent consistency with the generated datasets from experiments.

A lot of literature addressed the use of artificial neural network (ANN) for predicting thermal conductivity (*k*) of binary nanofluids. Esfe et al. [362] deployed a MLP-ANN of two input parameters (temperature and volume concentration ( $\varphi$ )) to predict the thermal conductivity of Cu-TiO<sub>2</sub>/W-EG BNF. Results showed good performance. Amani et al. [363] deployed artificial neural network to predict viscosity and thermal conductivity (*k*) of MnFe<sub>2</sub>O<sub>4</sub>/Water nanofluid,

using various experimental values of nanoparticles concentration, temperature, and magnetic field as inputs to the model. Esfe et al. [364] employed a MLP-ANN to predict the thermal conductivity of SWCNT–Al<sub>2</sub>O<sub>3</sub>/EG BNFs with a higher deviation of 1.94% when predicted values were compared to experimental values. Adun et al. [66] applied seven input parameters: thermal conductivity, nanosize, volume concentration, NMR, temperature, nanoparticle bulk density, and basefluid, to predict the thermal conductivity of binary nanofluids. A multilayer perceptron artificial neural network and support vector regression (SVR) models were developed with the accurate capacity to predict the thermal conductivity of binary nanofluids for ranges of binary nanoparticles combinations. He et al. [348] also used an artificial neural network to effectively predict the thermal conductivity of Ag-ZnO(0.5:0.5)/Water binary nanofluid depending on volume fraction and temperatures of nanoparticles.

Esfe et al. [65, 365] predicted the thermal conductivity of ZnO–DWCNT/EG hybrid nanofluids and ferromagnetic nanofluids respectively with good accuracy and minimal error. Rostamian et al. [366] used artificial neural networks (ANN) to predict the thermal conductivity of CuO–SWCNTs hybrid nanofluids and proved that ANN predicted a good thermal conductivity. Moghaddari et al. [367] also used artificial neural networks (ANN) for prediction of thermal conductivity of MWCNT-OH-(Au, Ag, Pd) composites. Sharifpur et al. [368] employed the group method of data handling (GMDH-NN) to model the effective viscosity of  $Al_2O_3$ –glycerol nanofluid. The obtained correlations gave better accuracy in predicting the experimental dataset compared with cited models in open literature. Maleki et al. [369] applied the group method of data handling (GMDH) to determine the thermal conductivity of nanofluids and achieved good  $R^2$  value. Mohamadian [370] confirmed that GMDH artificial neural network is a reliable model to predict the dynamic viscosity of Ag/water nanofluid when concentration, temperature, and size of particles were used as input data. The achieved results for  $R^2$  was equal to 0.9996, indicative of perfect precision. Ahmadi et al. [371] also used the group method of data handling (GMDH) artificial neural networks to model the dependency of thermal conductivity on nanosize, temperature and concentration considered as input parameters. Results obtained were precise and accurate for prediction.. For a solar working fluid, Loni et al. [372] used the group method of data handling (GMDH) artificial neural networks to propose a model for thermal efficiency and the cavity heat gain of the Hemispherical Cavity Receiver. Ambient temperature, solar irradiation, outlet temperature were used as input variables for the model. Achieved  $R^2$  values based on a 3-variable model, were 0.9567 and 0.9709 for thermal efficiency and the cavity heat gain of the Hemispherical Cavity Receiver, respectively. Results proved a precise and applicable model. A whole lot of artificial intelligence model is predicted for nanofluids than binary nanofluids, hence a good research gap

# 2.9 APPLICATIONS OF BINARY NANOFLUIDS

# 2.9.1 Automobile and Manufacturing Applications

#### 2.9.1.1 Nanofluid Coolant

Over a long time, the crises of inadequate energy led automobile manufacturers to think of improved aerodynamic designs of new and smart vehicles and later fuel economy. This competition led to manufacturers reducing the quantity of energy used to overcome drag force. An optimum design of radiator shape, size and repositioning aided an improved cooling effect of incoming air. Binary nanofluids serves as a viable substitute to augment engine cooling rate and thereby reduce the complexity of the thermal management system design. Enhancement in the heat transfer rates leads to the design of lighter and compact radiators, particularly for the heavy-duty engines and machinery [40, 45, 47, 110, 147, 302, 373-382]. Machining procedures entails high friction and high-temperature environments. Thus the need for a fast cooling system is essential [383-388].

#### 2.9.1.2 Brake Nanofluid

Lately, smart vehicle design aims at advanced aerodynamics and detraction in drag forces, hence the need for a sophisticated braking system with efficient heat dissipation capability with the use of brake nanofluids. In the process of applying brakes, kinetic energy is dispersed through the heat produced and transmitted throughout the brake fluid in the hydraulic braking system. This affects the brake oil, so a binary nanofluid with improved properties will optimize performance and handle safety issues. Copper-oxide brake nanofluid (CBN) is a good example [50, 57, 126, 374, 389-392]

# 2.9.1.3 Transmission Nanofluid

The application of binary nanofluids can also be employed in cooling automatic transmission systems in engines. When nanoparticles are suspended into engine transmission oil for the engine, this augments its thermal performance by possessing the least transmission temperatures at low and high speeds [163, 374, 392-395].

# 2.9.1.4 Nanofluid in Fuels

The addition of water-based aluminium and alumina nanoparticles in a diesel engine fuel augments the combustion property. At combustion, pure aluminium particles serve as an oxidizing agent, and alumina nanofluid serves as a catalyst. The wide contact surface area of aluminium nanoparticles increases the decomposition of water; thus, it enhances hydrogen yield and detracts the concentration of exhaust emissions [101, 121, 126, 147, 374-377, 396, 397].

#### 2.9.1.5 Nano-Lubricant

Deploying binary nanofluids for lubrication taps from it's optimal and rheological properties. Literature reports that stable dispersal of nanoparticles with surface-modification in mineral oils produces enhanced tribological properties, thereby reducing wear, friction and improving load-carrying capacity [89, 100, 130, 374, 390, 398-404].

#### 2.9.1.6 Corrosion Control

Aside nano-cooling, binary nanofluids also works as corrosion inhibitors to metals. Literature is emerging on the corrosion behaviour of binary nanofluids [405-410].

# 2.9.2 Heat Transfer Applications

#### 2.9.2.1 Heat Pipes

This is heat-transfer devices that possess fine thermal conductivity and phase transition for effective transfer of heat between two solid interfaces. They are a compact system used in electronic device cooling, heat exchangers and renewable energy systems. The natural attributes of higher thermal conductivity possessed by binary nanofluids are used to augment heat pipes' thermal performance [54, 411-416].

# 2.9.2.2 Heat Exchanger

Heats exchangers are devices employed to transport heat between two fluids without been mixed. It has wide industrial applications. The demand for smart design of heat exchangers to handle maximum possible load led to the deployment of binary nanofluids for heat extraction. Research study in this area is receiving a remarkable increase, since energy conservation is of significant challenge [47, 88, 92, 101, 121, 124, 327, 417-429].

# 2.9.2.3 Nuclear Reactor

The removal of heat from the reactor core is of great concern for the operation of the nuclear power plant. Binary nanofluids (BNFs) is employed to improve the cooling capacity, thus enhancing the efficiency of nuclear reactor, while detracting thermal-hydraulics problems [81, 379, 430-434].

#### 2.9.2.4 Geothermal Power

The global geothermal power resource can provide the world's energy need with technological improvement. Nanofluids can be used to cool equipment that works in a high temperature and friction environment during drilling operations. Like a "fluid superconductor," nanofluids is a working fluid used for energy extraction from the earth's core, and thus produces large amounts of energy because the heat transfer capability of geothermal systems is enhanced. The use of BNFs helps to augment the efficiency of a power generation cycle using geothermal energy [48, 435-441]

# 2.9.2.5 Boiling

Boiling is a major industrial process useful in various engineering thermal processes like metallurgy, power generation, desalination, chemical, etc. Boiling as a heat transfer process is a key phase phenomenon in many thermal systems, thus the use of binary nanofluid to improve heat transfer properties. Binary nanofluids catalyze the boiling process by enhancing the critical heat flux (CHF). Studies are increasing in using binary nanofluids for boiling [136, 442-447].

# 2.9.2.6 Cooling Applications

As the quest for better living standards continues, the need arises for thermal comfort in vehicles and buildings, thus resulting in improved energy consumption. The integration of nanohybrid based phase change materials (PCMs) helps to decrease energy use and thus enhances the thermal comfort in buildings. Building parts like concrete, floors, wallboards, etc. are integrated with PCMs to help enhance their performance. Furthermore, the constraint of space, energy and weight allows for an effective cooling system for aircraft, space and defence application, which BNFs handle better than conventional fluids [33, 37, 51, 448-452].

#### 2.9.3 Biomedical Applications

# 2.9.3.1 Nanomedicine

Binary nanofluids has also found commercial applications in the medical and pharmaceutical field. The methods entail biosensors, microfluidics, drug delivery, tissue engineering, nanobiotechnology, etc. Their properties allow for their use as a drug delivery system. Hence, the use of nanogels to produce nanodrugs, for both *in vitro* and *in vivo* assay. For example, a nanohybrid called Graphene quantum dots (GQDs) has found numerous applications, especially in biomedical research, as a result of its unique physico-chemical characteristics and excellent biocompatibility. Emerging research and developments are on, especially in synthesis methods, in vivo imaging, and in vitro biosensing applications [86, 453-458].

# 2.9.3.2 Cancer Therapeutics

Magnetic nanohybrids have found usefulness for cancer imaging and drug delivery. The idea is that magnetic-based nanohybrids are employed to guide the particles along the bloodstream to locate a tumour using magnets to supply the drug to the tissue without damage to surrounding healthy tissue. This happens to be a key side effect of using the traditional cancer treatment approach [456, 457, 459-464].

#### 2.9.3.3 Nanocryosurgery

Nanocryosurgery is a medical procedure that uses a lower temperature to destroy unwanted tissues. This ground-breaking approach is finding popularity due to its relevant clinical advantages, like cancer and tumour treatment. Aside from being less invasive when compared to traditional surgical resection, it reduces bleeding, pain, and attendant complications of surgery. It is also cheaper than other treatment methods and needs a more reduced recovery time and hospital stay [457, 465-471].

#### 2.9.3.4 Cryopreservation

Nanofluids has also found usefulness in preserving organ against damage during surgical operations. For vaccines, PCMs are used to maintain them at recommended temperature during transport [457, 460, 465, 472-476].

#### **2.9.4 Electronic Applications**

# 2.9.4.1 Microchip Cooling

Fast heat dissipation is a key challenge in developing miniature microchips and nanochips. However, due to their high thermal conductivity, BNFs are used for the liquid cooling of computer processors. New generation computer chips or microprocessors incorporate nanofluids for super-high-heat flux electronic systems. Nguyen et al. [477] studied the heat transfer improvement and behaviour of Al<sub>2</sub>O<sub>3</sub>-water nanofluid for application in a closedcooling system meant for a microprocessor or similar electronic devices. The result was remarkable [477-484].

#### 2.9.4.2 Microfluidic Applications

Binary nanofluids have also found usefulness for fluidic digital display devices, optical devices and majorly in microelectromechanical systems (MEMS). Also, it finds practical applications in the pharmaceuticals industry [457, 476, 477, 485-488].

#### 2.9.5 Renewable Energy Applications

#### 2.9.5.1 Photovoltaic-Thermal System

Photovoltaic (PV) modules are applied to direct solar energy conversion to domestic electricity. The PV modules absorb about 81% of the radiations striking the module surface. Still, a small quantity is converted to electric power, and the rest is transformed to heat, hence reducing the efficiency of the cell and the overall lifespan of the module. This operational constraint can be solved by cooling the surface of the module using a binary nanofluid, thus yielding improved electrical efficiency [489-494].

# 2.9.5.2 Solar Collectors

Binary nanofluids augment the performance of photothermal conversion, unlike traditional fluids. In addition, the improved thermal properties and optical characteristics of binary nanofluids as working fluids make room for an excellent absorption range [120, 124, 135, 150, 162, 449, 495-498].

# 2.9.5.3 Micropower Generation

The optical and thermal properties of binary nanofluids were used to absorb and transform light to heat for electrical generation purposes. An open-circuit voltage of 1.6 mV was achieved at 900  $\mu$ L nanofluid. Emerging research is opening room for improvement [55, 489, 490, 493, 499-502].

# 2.9.6 Other Applications

Binary nanofluids has numerous use in other areas like detergency [46, 503-505], soil remediation [46, 506-509], oily soil removal [508-510], enhanced oil recovery [55, 71, 139, 511-514], military application [51, 147, 515-517], etc. Figure 2.2 details the applications of applications of binary nanofluids.

#### 2.10 CHALLENGES WITH BINARY NANOFLUIDS AND FUTURE DIRECTIONS

Running through numerous applications and utilization of binary nanofluids, a few challenges need to be addressed to enable the extensive use of binary nanofluids. The major issues are:

#### 2.10.1 Stability

Generally, instability remains the key issue with nanofluids. Parameters that affect nanofluid's stability are stirring time, type of surfactant, nanoparticle combinations, nanoparticle

concentration, fluid temperature, pH value, ultrasonication and base fluid. Nanosuspension of nanoparticles in basefluid faces challenges due to surface charge (negative or positive), which varies amidst particles, thus leading to abatement in heat transfer. For proper suspension of nanoparticles, the aforementioned factors are gaps for future studies [55, 63, 120, 328, 518-523]. Open literature is gaining momentum with nanofluids' meaningful stability time span, especially binary nanofluids and ternary nanofluids. A sixty (60) days stability time span was published by Sundar et al. [524] for MWCNT- Fe<sub>3</sub>O<sub>4</sub>/water; Ali et al. [120] for CNTs-Fe<sub>3</sub>O<sub>4</sub>/water; Hussein [525] for AlN/EG; Yarmand et al. [526] for GNP-Ag/water; while Farbod et al. [527] recorded a stability time span of eighty (80) days for MWCNTs/water; Tiwari et al. [171, 528] published for ninety (90) days for CeO<sub>2</sub>+MWCNT binary nanoparticles for various basefluids (ethyl glycol, water, silicone oil and therminol VP-I). Frequently used methods for estimating stability of binary nanofluids are centrifugation, spectroscopy, sedimentation analysis and zeta-potential [36, 39, 41, 120, 176, 346, 529].

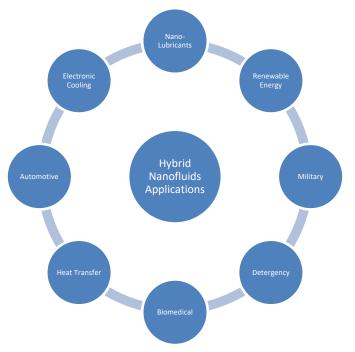


Figure 2.2: Practical application of binary nanofluids.

#### 2.10.2 Selection of Nanohybrid Materials

Binary nanofluids exhibit individual behaviour. To select optimum nanomaterial, a comprehensive comparison is essential. This selection has an impact on the thermal conductivity and stability performance. Suresh et al. [258] affirmed that ceramic substances possess chemical inertness and good stability, but lower thermal conductivity when related to metallic nanoparticles. Metallic nanoparticles possess maximum thermal conductivity compared with ceramic nanoparticles, so when hybridized, binary nanofluids with augmented thermal conductivity and stability are produced [31, 40, 45, 160, 171, 204, 258. The basefluid choice relates to the primary area of application [53]. The methods for formulating binary nanofluids or ternary nanofluids should also be examined - aerosol method, chemical reduction method, polymerization, wet chemical [530-533].

# 2.10.3 Production Cost

The production cost of binary nanofluids depends on the production approach used and suspension in basefluids. The choice of basefluid also affects cost. The methods for producing binary nanofluids are named one step and two-step methods. The equipment used is expensive and sophisticated [53, 55, 388, 534, 535].

# 2.10.4 Pumping Power

The viscosity of binary nanofluids is a function of temperatures, as it varies with it. The dispersed nanoparticles aid the viscosity, enhancing friction factor and enabling pumping power [53, 120, 526, 536].

# 2.10.5 Model For Thermal Conductivity

Progress in industrial processes has necessitated commensurate growth in heat transfer systems' efficiency by optimizing thermal processes and properties with the use of binary nanofluids. Really, experimental set-up to determine the thermophysical properties of binary nanofluids is

expensive and time-consuming, thus using modelling techniques. So, in handling repeated experiments and encouraging optimised big data handling, researchers are gradually shifting to applying artificial intelligence techniques (like machine learning models, etc) to engineering, industrial and scientific applications. Literature abounds with a prediction model for binary nanofluids. Predicted values agrees with experimental results [61, 64, 67, 92, 96, 141, 148, 160, 174, 181, 350, 362, 433, 537].

# 2.11 CONCLUSION

The need to augment the poor thermal conductivity of conventional fluids to produce efficient heat transfer fluid cannot be over-emphasized, knowing fully well that heat transfer is a key component in the process line of many industrial production concerns. Hence, the birth of nanofluids is the formulation of a composite of suspended nanoparticles in a basefluid. Nanofluids have found wide applications ranging from heat exchangers, electronic cooling, automotive industry, medical, military, solar energy, manufacturing industry, to mention but a few. But nanofluids has limitations premised on certain specific benefits due to the characteristics of the dissolved nanoparticle. Thus, the entrance of a new class heat transfer fluid named binary nanofluid and ternary nanofluid. This Chapter presented a wide range of recent and future applications of nanofluids with a focus on related issues that allow for suitability for industrial applications. Note, the few noticed gaps must be addressed to allow for effective industrial applications.

The review focused on the preparation and application of binary nanofluids. Binary nanofluids and ternary nanofluids are advanced mixture of heat transfer fluids with optimized thermal properties. Thus, the need to develop an optimized model for the formulation of binary nanofluids for improved industrial applications. Artificial neural network (ANN) possesses a strong possibility in modelling the thermal properties of binary nanofluids. Emerging issues of optimized concern are stability and instability, nanomaterials selection, enhanced formulation methods, use of binary basefluids, temperature, bias in experimental outcomes and simulated predictions, thermal network mechanism, environmental impact, to mention a few.

# **CHAPTER 3**

# METHODOLOGY<sup>1,2,3,4</sup>

# **3.1 INTRODUCTION**

This chapter explains the method and material for the experimental study and the artificial intelligence model applied to nanofluids properties. It details the information about materials, equipment, stability, sample preparation, measurement of thermophysical properties, nanofluid characterisation, and natural convection properties of BNFs engaged in the experimental study. The details will be discussed in the following sub-sections.

# **3.2 MATERIALS AND EQUIPMENT**

#### 3.2.1 Materials

For the study, nanoparticles of MgO (20 nm, 40 nm and 100 nm,  $\geq$ 99% purity), ZnO (20 nm,  $\geq$ 99.5% purity), and  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> (7nm diameter and ~98% purity) were purchased at Nanostructured and Amorphous Materials Inc., Houston, Texas, USA, while. Functionalised MWCNT (inner diameter of 3-5 nm, outer 10-20 nm and length of 10-30 µm) obtained from MKnano Company, Ontario, Canada. To enhance the stability of the formulated NFs, BNFs and TNFs, a surface activator Sodium-dodecyl sulphate (SDS) with purity  $\geq$  98.50% was purchased from Sigma-Aldrich, Germany. Deionised water (DIW) was the basefluid and obtained in the laboratory.

This chapter is reflected in parts in the following papers:

<sup>&</sup>lt;sup>1</sup>Giwa, S., Momin, M., Nwaokocha, C., Sharifpur, M., and Meyer, J. *Influence of nanoparticles size, per cent mass ratio, and temperature on the thermal properties of water-based MgO–ZnO nanofluid: an experimental approach.* Journal of Thermal Analysis and Calorimetry, 2021. **143**(2): p. 1063-1079.

<sup>&</sup>lt;sup>2</sup>Nwaokocha, C., Momin, M., Giwa S., Sharifpur, M., Murshed S.M.S., Meyer, J.P., *Experimental investigation of thermo-convection behaviour of aqueous binary nanofluids of MgO–ZnO in a square cavity.* Thermal Science and Engineering Progress, 2021. **28**:101057.

<sup>&</sup>lt;sup>3</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Influence of concentration, mixing ratios, and working temperature on the thermal behaviour of binary nanofluids of MgO–ZnO: an experimental investigation.* Ready for submission.

<sup>&</sup>lt;sup>4</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Artificial neural network development to predict thermal conductivity of MgO–ZnO/Deionised Water binary nanofluids*. Ready for submission.

The free convection experiment of MgO-ZnO/deionised water BNF was done inside a squared enclosure (breadth 96.0 mm × length 96.0 mm × height 105.0 mm). Polyurethane material was used for insulation during the thermo-convection investigation. The opposite walls of the cavity were differentially heated, while insulation (20 mm with k = 0.033) was done for other walls, along with the pipe networks. The temperature in the enclosure was measured employing the

T-type thermocouple manufactured by Omega Engineering Inc., USA, (accuracy 0.1 °C), set at particular points within (spaces (11) and walls (6)) and without (2 inlet and 4 outlet pipes) the enclosure. Thermocouples are calibrated before performing the experiment with temperature 10 - 50 °C, for the uncertainty of 0.16 °C. Glass wares like beakers, conical flasks and volumetric flasks were also used for the experiment.

#### 3.2.2 Equipment

A meter rule and vernier calliper were used to measure the dimensions (within and without) of the cavity. The quantity of the nanoparticles and dispersants/surfactants used for the study were measured with a digital weigh balance (Radwag AS220.R2; 10 mg – 220 g and  $\pm$  0.01 g precision). The mixtures of SDS, BNPs and DIW were stirred at a controlled temperature employing a magnetic stirrer (Lasec hotplate stirrer - H4000-HSB, 500 W, 50Hz) to attain an even suspension before sonicating. Homogenizing was achieved employing an Ultrasonicator (QSonica Q-700; 20 kHz and 700 W). Water baths were employed to retain a constant temperature for the test samples (LAUDA ECO RE1225 and PolyScience, USA: PR 20R-30-A12E, -30 °C and 200 °C, precision 0.0050 °C). Employing an electrical conductivity meter (EUTECH Instrument (CON700, precision  $\pm$  1%)), the electrical conductivity ( $\sigma$ ) of the prepared nanofluids (mono, binary and ternary) were measured and applied to indicate the optimization of amplitude, dispersion fraction, and sonication time. The pH is measured using a pH meter (Jenway 3510; range of – 2 to 19.999; accuracy  $\pm$  0.3%). The stability of formulated nanofluids is measured using an Ultraviolet (UV) visible Spectrophotometer (Jenway Model

7315). TEMPOS thermal properties analyzer (METER Group) measures thermal conductivity. Volumetric flow rates were valued by employing a flow meter (Burkert Type 8081). A Vibro-viscometer (SV-10, A&D, Japan) measures viscosity. Transmission electron microscope (JEOL JEM-2100F) measures morphology. Experimental values for flow rate and temperature were logged with a National Instrument Data logger (Type SCXI-1303; 32 channels) into the computer with a LABVIEW<sup>®</sup> software (2014 version) interface. A summary of the equipment and the accuracies are presented in Table 3.1.

Instrument	Range	Accuracy
Electrical conductivity meter	0 μS - 200 mS	± 1%
Flow meter	0.0666 - 0.3333 l/s	±0.01% of full-scale flow rate + 2% (measured value)
Graduated cylinder	250 ml	$\pm 2.0$ ml
Thermal bath	-200 – 150 °C	$\pm 0.005$ °C
Thermal conductivity meter	$0.2-2.0 \ W/m \ K$	$\pm 10\%$
Thermocouple	< 150 °C	±0.1 °C
Vernier calipers	0.02 mm	0.02 mm
Viscometer	0.3 – 10,000 mPa.s	$\pm 3\%$
Weighing balance	10 mg – 220 g	0.01

Table 3.1: Accuracy of equipment.

# **3.3 FORMULATION OF BINARY NANOFLUIDS**

As published in [21], a two-step method was used in formulating a MgO-ZnO/DIW BNFs with four percent weight ratios (PWR) of 20:80, 40:60, 60:40, and 80:20 (MgO: ZnO). MgO nanoparticles with nano-sizes of 20 nm, 40 nm and 100 nm were employed. A SDS surfactant was used to help the dispersion of the binary nanoparticles in deionised water. To enhance the stability of the binary nanofluids, amplitude (70 – 80%), dispersion fraction (0.60 – 1.20), and sonication time (30 – 120 min) were optimised. The remaining parameters are constant to optimize a particular variable while one is varied. Sonication time was optimised first for a fixed dispersion fraction and amplitude. Thereafter, the dispersion fraction was optimized and last, the amplitude.

A certain percent weight ratio (80:20 (MgO: ZnO)) for the binary nanofluid for volume concentration of 0.05 vol% was formulated and employed in the optimisation study. The specified nanoparticles and dispersant were weighed using the digital weight balance (Radwag AS 220.R2; 10 mg – 220 g and accuracy  $\pm$  0.01 g) by the estimate derived from Equation 3.1 [239] based on the volume of deionised water (70 ml) and concentration (0.05 vol%). With an electrical conductivity instrument (EUTECH Meter (CON700);  $\pm$ 1% accuracy), the electrical conductivity of the synthesised binary nanofluids was evaluated and employed to indicate the optimised amplitude, dispersion fraction, and sonication time. The pH (Jenway 3510; –2 to 19.999 range; precision  $\pm$ 0.30%) was also valued to estimate the optimized results of the variables. The blend of basefluid, surfactant, and binary nano-particles were first stirred for 30 minutes at 40 °C with a magnetic stirrer prior to sonicating. An Ultra-sonicator (QSonica; Q-700; 700 W and 20 kHz) was employed to homogenise the blend to afford good suspension of the binary nano-particles in basefluid. A beaker containing the mixture was immersed in a water bath (LAUDA ECO RE1225) and sustained at 20 °C while sonicating.

$$\varphi = \left(\frac{X_{Mg0}\left(\frac{M}{\rho}\right)_{Mg0} + X_{Zn0}\left(\frac{M}{\rho}\right)_{Zn0}}{X_{Mg0}\left(\frac{M}{\rho}\right)_{Mg0} + X_{Zn0}\left(\frac{M}{\rho}\right)_{Zn0} + \left(\frac{M}{\rho}\right)_{DIW}}\right)$$
3.1

Where;

 $X_{MgO}$  = ratio of MgO nanoparticles with 20 nm or 100 nm;

 $X_{ZnO}$  = ratio of ZnO nanoparticles with 20 nm;

M = nanoparticle mass;

 $\rho$  = nanoparticle density;

DIW = basefluid.

As the optimised variables were achieved, the binary nanofluids at the preset percent weights and at 0.1 vol.% were prepared for 200 mL of basefluid. To achieve optimized stability for the formulated binary nanofluids and allow for repeatability of this experiment (which is scarce in literature), optimization of sonication parameters (time: 30–120 minutes, amplitude frequency: 70–80%, and a 7 seconds PULSE ON and 2 seconds PULSE OFF) and surfactant's dispersion fraction (0.6 – 1.2) was done ab initio. Dispersion fraction is expressed as Equation 3.2. For the formulation of BNF,  $\varphi$ , percent weights of BNPs, and volume of BF type were employed in Equation 3.1 to estimate the weights of the BNPs that would be used to formulate the BNF. Volumes of 70 ml, 100 ml and 1400 ml of different basefluids (DIW) were used for the optimisation process, thermal properties measurement and thermo-convection experiment, respectively. The weights of surfactants and BNPs used for formulating the MHNFs are estimated and provided in Appendix A.

$$Dispersion\ fraction = \frac{weight\ of\ surfactant}{weight\ of\ binanoparticles}$$
3.2

A parameter was varied and others fixed until optimum results were achieved. Also, the margin of deviation (MOD) of measured properties of the BNFs were estimated using Equation 3.3 [538].

$$MOD(\%) = \left(\frac{M_{Exp.} - M_{Pred.}}{M_{Exp.}}\right) \times 100$$
3.3

Where  $M_{\text{Exp.}}$  and  $M_{\text{Pred.}}$  are the experimental and predicted readings for a specific property, respectively.

Note, three sets of MgO (20 nm)-ZnO/DIW BNFs, MgO (40 nm)-ZnO/DIW BNFs and MgO (100 nm)-ZnO/DIW BNFs were produced to allow for the investigation of nanosize effects on thermal characteristics. Single-particled nanofluids of MgO(20 nm)/DIW nanofluids, MgO

(100 nm)/DIW nanofluids, and ZnO (20 nm)/DIW nanofluids were prepared to allow for comparison in the enhancement of thermal characteristics compared to binary nanofluids.

# **3.4 STABILITY AND MORPHOLOGY OF BINARY NANOFLUID**

A transmission electron microscope (TEM) (JEOL JEM-2100F) was used to check the morphology of the hybrid and mono-particle nanofluids. To keep an eye on the stability of mono-particle nanofluids and binary nanofluids, both visual inspection and absorbance test using UV-visible spectrophotometer (Jenway Model 7315) were employed. An Ultra-Violet (UV) visible spectrophotometer (Jenway Model 7315) was employed to measure the absorbance of the formulated binary nanofluids, which is indicative of stability [338]. Absorbance test was conducted for 20 hours for samples of MgO (20 nm)-ZnO/DIW BNF and MgO (100 nm)-ZnO/DIW BNF at a percent weights of 20:80 and 80:20 and for all single-particled nanofluids. Also of note, as each property was measured for each volume concentration, 6 hours was used, while the absorbance test covered 20 hours to allow for good observation of stability. Visual inspection was done on the BNF samples for a week and on a daily basis.

#### **3.5 MEASURED THERMAL PROPERTIES OF BINARY NANOFLUID**

# **3.5.1 Measurement of Thermal Conductivity**

Thermal conductivity ( $\kappa$ ) was measured using TEMPOS thermal property analyser (METER Group; 0.2 – 2.0 W/m K range; ± 10% accuracy). The meter was calibrated for temperature ranging 20–50 °C in intervals of 5 °C for this experimental investigation. To get an accurate value, readings were measured for twelve rounds. As a self-calibrating device, readings were taken after switching it on and allowed to stabilize. Measured  $\kappa$  readings of BF was compared with standard measurements [539] for the studied temperature range to confirm the reliability of the measurement meter. A good agreement existed at an error 0.4890%. The associated uncertainty of  $\kappa$  readings was ± 02.00%. Thermal conductivity ratio (TCR) or effective thermal

conductivity ( $\kappa_{eff}$ ) and thermal conductivity enhancement (TCE) were estimated by Equations 3.4 and 3.5, respectively.

$$TCR = \kappa_{eff} = \frac{\kappa_{bnf}}{\kappa_{bf}}$$
 3.4

TCE (%) = 
$$\left(\frac{\kappa_{bnf} - \kappa_{bf}}{\kappa_{bf}}\right) \times 100$$
 3.5

where  $\kappa_{bnf}$  and  $\kappa_{bf}$  are the thermal conductivity (TC) of the binary nanofluids (BNFs) and DIW, respectively.

# 3.5.2 Measurement of pH

After calibrating the meter using standard fluids, the pH of binary nanofluids (BNFs) samples and DIW were estimated for the studied temperatures 20–50 °C, after calibrating the meter using standard fluids. The uncertainty related to the pH readings was  $\pm 2.49\%$ .

# **3.5.3 Measurement of Electrical Conductivity**

Electrical conductivity was measured using a Eutech meter (CON700 model,  $\pm 10\%$  accuracy). The device was calibrated using the manufacturer's standard calibration fluid (glycerine). Glycerine was measured at 25 °C thrice, and an average reading of 1414 µS.cm<sup>-1</sup> was achieved, which is near to the manufacturer's reading of 1413 µS.cm<sup>-1</sup>. Thereafter, the  $\sigma$  for DIW and formulated BNFs were valued for temperatures 20 to 50 °C. The uncertainty related to the  $\sigma$  measurement was  $\pm 2.99\%$ . Figure 3.1 presents the experimental set-up for the investigation. The relative  $\sigma$  ( $\sigma$ <sub>rel</sub>) and the  $\sigma$  improvement ( $\sigma$ <sub>enhan</sub>) of the nanohybrids was estimated with Equations 3.6 and 3.7, respectively [540, 541].

$$\sigma_{\rm rel} = \frac{\sigma_{bnf}}{\sigma_{bf}}$$
 3.6

$$\sigma_{\rm enh} (\%) = \left(\frac{\sigma_{bnf} - \sigma_{bf}}{\sigma_{bf}}\right) \times 100$$
3.7

where  $\sigma_{bnf}$  and  $\sigma_{bf}$  are the viscosity of the BNFs and DIW, respectively.

#### **3.5.4 Measurement of Viscosity**

Viscosity ( $\mu$ ) of BNFs and BF were measured using a Vibro-viscometer (SV-10, A&D Japan, accuracy  $\pm$  3%) at temperatures 20–50 °C, after calibrating using basefluid (DIW). The accuracy of the device was determined by comparing the  $\mu$  of DIW with standard values of water published in the literature [539, 541], with an error of 2.78% and uncertainty of  $\pm$  2.85%.

Figure 3.1 presents the experimental set-up for the investigation. The  $\mu_{rel}$  and  $\mu_{enh}$  of the nanohybrids as related to basefluid (DIW) were estimated using Equations 3.8 and 3.9, respectively [540, 541].

$$\mu_{\rm rel} = \frac{\mu_{bnf}}{\mu_{bf}}$$
 3.8

$$\mu_{\text{enh}}(\%) = \left(\frac{\mu_{bnf} - \mu_{bf}}{\mu_{bf}}\right) \times 100$$
3.9

where  $\mu_{bnf}$  and  $\mu_{bf}$  are the viscosity of the BNFs and DIW, respectively.

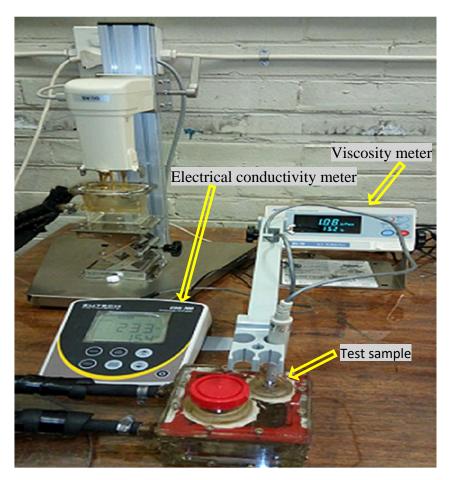


Figure 3.1: Experimental set-up for electrical conductivity and viscosity.

#### **3.5.5 Other Properties**

The density ( $\rho$ ), specific heat capacity (C<sub>p</sub>), and thermal coefficient of expansion ( $\beta$ ) of BNFs were necessary for data reduction (detailed in Sub-Section 3.7). They are estimated from empirical models modified for BNFs, as they are not experimentally measured. Equation 3.10 and Equations 3.11 – 3.13 presents the theoretical and empirical correlations [542] for determining density, specific heat, and coefficient of thermal expansion of BNFs, respectively.

$$\frac{k_{nf}}{k_{bf}} = \left( \left( k_{Mg0} X_{Mg0} + k_{Zn0} X_{Zn0} \right) + 2k_{DIW} + 2 \left( \varphi_{Mg0} k_{Mg0} X_{Mg0} + \varphi_{Zn0} k_{Zn0} X_{Zn0} \right) - 2\varphi_{bnp} k_{DIW} \right) \times \left( \left( k_{Mg0} X_{Mg0} + k_{Zn0} X_{Zn0} \right) + 2k_{DIW} - \left( \varphi_{Mg0} k_{Mg0} X_{Mg0} + \varphi_{Zn0} k_{Zn0} X_{Zn0} \right) + \varphi_{bnp} k_{DIW} \right)^{-1}$$

$$3.10$$

$$\rho_{bnf} = \varphi_{Mg0} \rho_{Mg0} + \varphi_{Zn0} \rho_{Zn0} + (1 - \varphi_{bnf}) \rho_{DIW}$$
3.11

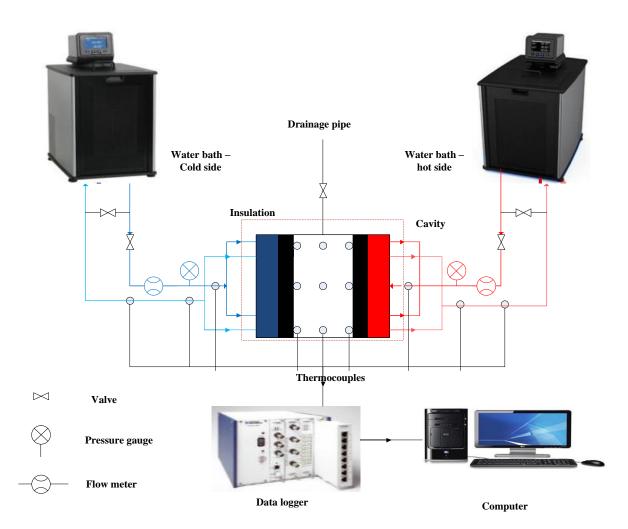
$$(\rho\beta)_{bnf} = \varphi_{Mg0}(\rho\beta)_{Mg0} + \varphi_{Zn0}(\rho\beta)_{Zn0} + (1 - \varphi_{bnf})(\rho\beta)_{DIW}$$
 3.12

$$(\rho C_p)_{bnf} = \varphi_{Mg0}(\rho C_p)_{Mg0} + \varphi_{Zn0}(\rho C_p)_{Zn0} + (1 - \varphi_{bnf})(\rho C_p)_{DIW}$$
3.13

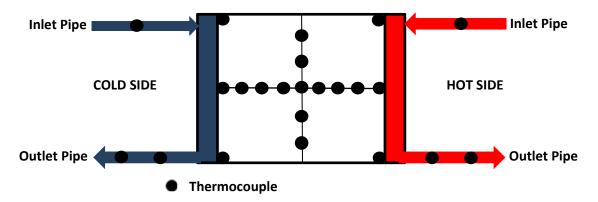
# **3.6 THERMO-CONVECTION OF BINARY NANOFLUIDS IN CAVITY**

The natural convection behaviour of MgO-ZnO/DIW BNF inside a squared enclosure of 96 mm length by 96 mm breadth by 105 mm height) was studied by experiment. A squared enclosure was employed due to its wide application compared to other cavity types. The opposite walls of the enclosure were heated differentially, and other walls were insulated (20 mm with k = 0.033), alongside the pipe connection. A T-type thermocouple was employed to measure temperature within the cavity, arranged at certain points within (6 walls and 11 spaces) and without (2 inlet and 4 outlet pipes) the enclosure, as featured in Figures 3.2 and 3.3. Thermocouples were calibrated before conducting the experiments, with temperature 10-50°C,

and uncertainty of 0.16°C. Details regarding calibration procedure and estimating uncertainty associated with the thermocouples are briefed in Appendices B and C.









For thermocouples arranged outside of the enclosure, it was observed that 5% heat loss happened due to temperature difference between cavity and the environ. Shell heat exchanger (counter-flow) and isothermal tube were employed to sustain the constant temperature of the two differentially heated walls. So, water maintained at a constant temperature (20 °C and 50 °C) was transported within the heat exchangers employing two Programmable water baths (PolyScience, USA: PR 20R-30-A12E, -30 °C and 200 °C, precision 0.0050 °C), one for hot side and the other cold side. Flow meters were positioned at the inlet of heat exchangers to measure flow rates between water baths and heat exchangers. Measure values for flow rate and temperature were logged using a National Instrument Data logger (Type SCXI-1303; 32 channels) linked to the Desktop computer interfaced with a LABVIEW<sup>®</sup> software (2014 version). BNFs samples and DIW were charged inside the squared enclosure and permitted thermal equilibrium. The experiments were done for a uniform temperature change of 30 °C, amidst 20 to 50°C for all samples.

#### **3.7 DATA REDUCTION**

Main variables like Ra,  $Nu_{av}$ ,  $h_{av}$   $Q_{av}$ , etc., were determined by employing the valued flow rates, temperatures, and thermal properties of basefluid and BNF in the data reduction process. Heat transfer rate within an enclosure as a function of differential heating on the vertical walls is presented employing Equation 3.14,

Where;

$$\Delta T = \left(T_i - \left(\frac{T_{0,1} + T_{0,2}}{2}\right)\right)_h = \left(\left(\frac{T_{0,1} + T_{0,2}}{2}\right) + T_i\right)_c$$
3.15

The  $h_{av}$ , Ra and  $Nu_{av}$  related with the thermo-convection of the BNF sample within the square enclosure was estimated using Equations 3.16 - 3.18,

$$h_{av} = \frac{Q_{av}}{A(T_h - T_c)}$$

$$3.16$$

$$Ra = \frac{g\beta(T_h - T_c)(\rho)^2(C_p)(L)^3}{\mu \kappa}$$
3.17

$$Nu_{av} = \frac{h_{av}L}{\kappa_{eff}}$$
3.18

#### **3.8 MODEL DEVELOPMENT**

### **3.8.1** Thermophysical Properties

The entrance of BNFs and increasing investigation into their thermal characteristics have advanced the need to develop models to help predict these properties. Note, MgO-ZnO/DIW BNF was studied for the first time, hence no existing models in the literature to predict their  $\kappa_{eff}$  and  $\mu_{eff}$ . Thus, the need to develop new models for the thermal properties of the BNF.

#### 3.8.2 Nusselt Number

As a result of scarce literature on the experimental studies of thermo-convection characteristics of binary nanofluids in cavities and few existing models derived from experimental data for the prediction of Nu, this present study was conducted to develop a model in that regard for the BNF sample. Experimental datasets of  $Nu_{av}$  for the binary nanofluid was used for model development to predict  $Nu_{av}$ . The margin of deviation (MOD) for the developed models was expressed using Equation 3.3.

#### **3.9 CAVITY VALIDATION**

Cavity validation were achieved by employing the experimental dataset of  $Nu_{av}$  for basefluid measured while conducting the experiment, related with Nu values of published numerical models. The developed models of Berkovsky & Polevikov [543], Cioni *et al.* [544], and Leong *et al.* [545] to predict Nusselt Number of water within an enclosure were described in Equations 3.18 [543], 3.19 [544] and 3.20 [545], respectively. The Pr and Ra results of DIW were included in Equations 3.18 to 3.20 to get *Nu*.

$$Nu = 0.18 \left(\frac{Pr}{0.2 + Pr} Ra\right)^{0.29} \quad (Pr \le 10^5; Ra \le 10^{10}; 1 \le H/L \le 10)$$
Where  $\Pr = \frac{\mu C_P}{k}$ 

$$Nu = 0.145 \times Ra^{0.292} \quad (3.70 \times 10^8 \le Ra \le 7 \times 10^9)$$
3.19

 $Nu = 0.08461 \times Ra^{0.3125} \qquad (10^4 < Ra < 10^8)$  3.20

# **3.10 ESTIMATION OF UNCERTAINTY**

# 3.10.1 Thermophysical Properties

The estimation of uncertainty related with the measurements of  $\mu_{eff}$  and  $\kappa_{eff}$  for BNF was premised on the method employed by Adio et al. [205]. To estimate  $\mu$  uncertainty, errors from the formulation (weights of BNPs and volumes of BFs) of BNFs, temperature, and  $\mu$  readings were considered, whereas weights of BNPs, volumes of BFs, and  $\kappa$  measurement were error sources for the  $\kappa$  uncertainty (as expressed in Equations 3.21 and 3.22). Total uncertainty for  $\kappa$  and  $\mu$  measurements were determined employing Equations 3.24 and 3.25 with the bias components expressed in Equations 3.21 and 3.22, and the precision components described in Equation 3.23. The accuracy of the equipment is provided in Table 3.1. The accuracy of the applicable instruments and the obtained data for the viscosity and thermal conductivity of BNF were substituted in Equation 3.21 – 3.25. Details of the uncertainty estimation are provided in Appendices C.

$$U_{b\mu} = \sqrt{\frac{\Delta m}{m} + \frac{\Delta V}{V} + \frac{\Delta T}{T} + \frac{\Delta \mu}{\mu}}$$
3.21

$$U_{b_{\kappa}} = \sqrt{\frac{\Delta m}{m} + \frac{\Delta V}{V} + \frac{\Delta \kappa}{\kappa}}$$
3.22

$$U_{p_{\mu/\kappa}} = \pm (t_{\nu,p} \times SD_{\mu/\kappa})$$
3.23

$$\delta\mu = U_{\mu} = \pm \sqrt{\left(U_{b_{\mu}}\right)^2 + \left(U_{p_{\mu}}\right)^2}$$
3.24

$$\delta\kappa = U_{\kappa} = \pm \sqrt{\left(U_{b_{\kappa}}\right)^2 + \left(U_{p_{\kappa}}\right)^2}$$
3.25

# 3.10.2 Thermo-convection

The derivation of uncertainty related to the study was done to ascertain the degree of reliability of the experimental dataset. Datasets of temperature and flow rate were observed as the foundational error sources and disseminated using Equations 3.26 - 3.28 to determine the uncertainty related with *Nu*, *Q* and *h*, respectively. Table 3.2 features the determination of uncertainties.

$$\delta Q = \left( \left( \frac{\partial Q}{\partial \dot{m}} \delta \dot{m} \right)^2 + \left( \frac{\partial Q}{\partial C_{P_{DIW}}} \delta C_{P_{DIW}} \right)^2 + \left( \frac{\partial Q}{\partial T_H} \delta T_H \right)^2 + \left( \frac{\partial Q}{\partial T_C} \delta T_C \right)^2 \right)^{\frac{1}{2}}$$
 3.26

$$\delta Nu = \left( \left( \frac{\partial Nu}{\partial h} \delta h \right)^2 + \left( \frac{\partial Nu}{\partial L_C} \delta L_C \right)^2 + \left( \frac{\partial Nu}{\partial \kappa_{eff}} \delta \kappa_{eff} \right)^2 + \left( \frac{\partial Nu}{\partial T_C} \delta T_C \right)^2 \right)^{\frac{1}{2}}$$
3.27

$$\delta h = \left( \left( \frac{\partial h}{\partial Q} \delta Q \right)^2 + \left( \frac{\partial h}{\partial A} \delta A \right)^2 + \left( \frac{\partial h}{\partial T_H} \delta T_H \right)^2 + \left( \frac{\partial h}{\partial T_C} \delta T_C \right)^2 \right)^{\frac{1}{2}}$$
3.28

Heat Transfer Rate	$\frac{\partial Q}{\partial \dot{m}} = C_{p-bf} \Delta T$	Substitute into Equations 3.26
	$\frac{\partial Q}{\partial C_{p-bf}} = \dot{m} \Delta T$	
	$\frac{\partial Q}{\partial \Delta T} = \dot{m}C_{p-bf}$	
Nusselt Number	$\frac{\partial Nu}{\partial h} = \frac{L_c}{\kappa}$	Substitute into Equations 3.27
	$\frac{\partial Nu}{\partial L_c} = \frac{h}{\kappa}$	
	$\frac{\partial Nu}{\partial h} = \frac{-hL_c}{\kappa}$	

# **Table 3.2: The estimation of uncertainties.**

Convective Heat Transfer	$\frac{\partial h}{\partial Q} = \frac{1}{(T_h - T_c)A}$	Substitute into Equations 3.28
Coefficient	$\frac{\partial h}{\partial A} = \frac{-Q}{(T_h - T_c)A^2}$	
	$\frac{\partial h}{\partial T_h} = \frac{-Q}{(T_h - T_c)^2 A}$	
	$\frac{\partial h}{\partial T_c} = \frac{Q}{(T_h - T_c)^2 A}$	

## **3.11 ARTIFICIAL INTELLIGENCE**

In recent times, the concept of future work has necessitated applying artificial technique (AI) techniques to simulate real-life engineering problems. However, the experimental estimation of the thermal properties of nanofluids (mono, binary and ternary nanofluids) is quite expensive and at times complex. So, to limit the cost and time of experiments, researchers and scientists adopted the idea of developing models and correlations, such as using machine learning models to predict the accurate thermal conductivity of binary nanofluids. Artificial neural network (ANN) is a commonly used machine learning model and mathematical model that are good tools for regression analysis. Literature abound with developed ANN models deployed to predict the thermal conductivity of nanofluids and binary nanofluids for use as heat transfer fluids (HTFs). To achieve a robust and reliable result, these techniques are hybridised with other techniques, as individual method may be deficient in handling high non-linear complex systems.

# 3.11.1 ANN Architecture

Works on MgO-ZnO/DIW hybrid nanofluids using data-driven techniques like artificial neural network are scarce in the literature. Literature [64, 123, 156, 181, 348, 351, 365, 546-548] affirm that data-driven techniques are good to predict fast, simple and reliable results compared to conventional mathematical approaches under-estimate or over-estimate predicted outputs. The common mathematical approach is either complex or takes a long time to compute predicted output.

The artificial neural network is a combination of components called neurons. The individual layer has many neurons with an activation function to process input data. The mathematical detail for data processing is presented in Equation (3.29).

$$T_i = f_i \left( \sum_{j=1}^n w_{ij} x_j + b_i \right)$$
 3.29

In Equation 3.29, *T* stands for the ANN output, while *n* is the amount of data sets, *f* is for activation function,  $x_j$  is the *j*th input parameter, and  $b_i$  is the bias of the ith neuron and  $w_{ij}$  is the mass. For this work, the activation parameter for every layer is presented as  $\tan sig(x)$  aside output layer. The activation function for the output layer is called Purelin. The Tan *sig* parameter is Tangent Sigmoid and presented in Equation 3.30, and the linear (Purelin) transfer functions presented as Equation 3.31.

$$Tan \ sig(x) = \frac{2}{2 + e^{-2x}} - 1$$
3.30

$$Purelin(x) = x 3.31$$

Purelin represents a linear transfer parameter used to determine the outcome of the model. The Levenberg–Marquardt back-propagation algorithm was used as the learning algorithm for less training time. The algorithm was proposed first in 1944 by Kenneth Levenberg and in 1963 retooled by Donald Marquardt.

Using ANN method in a MATLAB (R2021a) software, experimental data sets were classified as training, validation, and testing randomly. The training data generates biases and masses for the testing, the validation data was used to modify the masses during training session, while the test data sets were used to determine the performance of the neural network. For this work, an optimized ANN to predict  $k_{bnf}$  was determined by comparing the performances of the varied neuron numbers within the inner layers, then finally using the best neuron number. This was done by modifying the ANN architecture to determine the optimized neuron number. The suggested learning algorithm is presented as Figure 3.4.

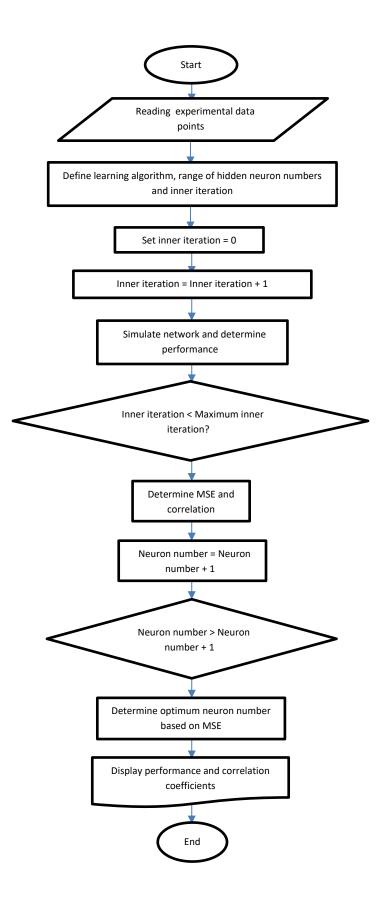


Figure 3.4: Proposed learning algorithm to determine optimized ANN.

# 3.12 CONCLUSION

The details of equipment, materials, measurements, characterisation, and experiments entailed in this study was given in this chapter. The process for formulating BNFs, the measurements of thermal properties of BNFs, and the thermo-convection performance of BNFs in a squared enclosure were presented. Also, model development for thermophysical properties and *Nu*, and the estimation of uncertainty for thermophysical properties and thermo-convection experiments were detailed in this chapter. ANN as an artificial intelligence method was discussed.

# CHAPTER 4 PREPARATION, MORPHOLOGY, AND STABILITY OF BINARY NANOFLUIDS<sup>1,2,3</sup>

# **4.1 INTRODUCTION**

This chapter presents the start of the result presentation obtained in this experimental work. The optimisation of parameters needed for the formulation of BNFs were presented. Then, the morphology of the formulated BNF are identified using TEM analysis and reported. Also, the stability of BNF was monitored and reported.

# 4.2 PREPARATION OF BINARY NANOFLUIDS

In formulating MgO–ZnO/DIW binary nanofluids (BNF), a two-step approach was used by suspending required volumes of nanoparticles (NPs) samples of MgO (20 nm, 40 nm and 100 nm,  $\geq$ 99% purity) and ZnO (20 nm,  $\geq$ 99.5% purity) in basefluid (DIW), for percent weight ratio (PWR) of 20:80, 40:60, 60:40, and 80:20 (MgO/ZnO). A dispersant/surfactant (SDS) was applied to help the nanosuspension process in the basefluid. To augment the stability of the binary nanofluids, three operating parameters of amplitude (70–80%), dispersion fraction (0.6 – 1.2), and sonication time (30 – 120 min) were optimised by measuring electrical conductivity ( $\sigma$ ). With this, the Critical micelle concentration (CMC) was obtained via measuring electrical conductivity ( $\sigma$ ). The optimisation of the dispersion fraction of BNF is shown in Figure 4.1. The weights of MgO nanoparticles, ZnO nanoparticles, SDS, and basefluid employed in the formulation of BNF are detailed in Appendix A.

This chapter is reflected in parts in the following papers:

<sup>&</sup>lt;sup>1</sup>Giwa, S., Momin, M., Nwaokocha, C., Sharifpur, M., and Meyer, J. *Influence of nanoparticles size, per cent mass ratio, and temperature on the thermal properties of water-based MgO–ZnO nanofluid: an experimental approach.* Journal of Thermal Analysis and Calorimetry, 2021. **143**(2): p. 1063-1079.

<sup>&</sup>lt;sup>2</sup>Nwaokocha, C., Giwa S., Ghorbani B., Momin, M., Sharifpur, M., Gharzvini M., Chamkha, A.J., Meyer, J.P., *Experimental formulation and GMDH modelling of thermal conductivity of MgO–ZnO/deionised water hybrid nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>3</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Influence of concentration, mixing ratios, and working temperature on the thermal behaviour of binary nanofluids of MgO–ZnO: an experimental investigation.* Ready for submission.

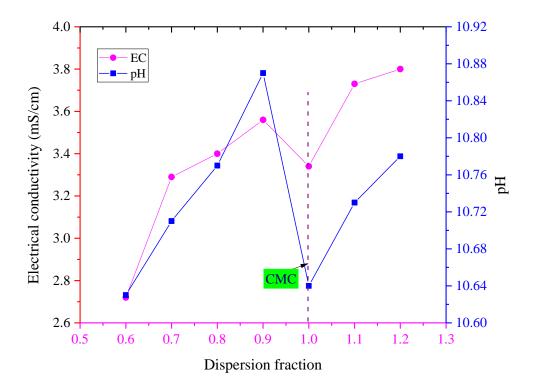


Figure 4.1: Optimization of dispersion fraction using pH and electrical conductivity.

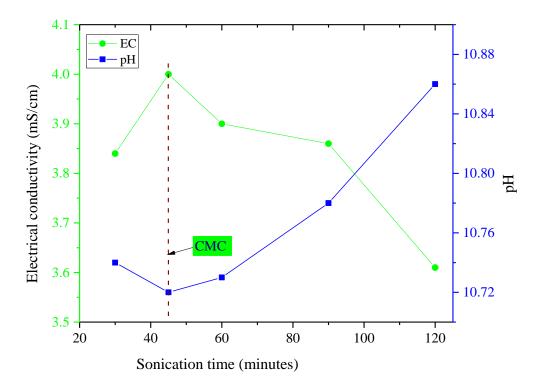


Figure 4.2: Optimization of sonication time employing pH and electrical conductivity.

To achieve the optimized values of three operating parameters (amplitude, dispersion fraction and sonication time), the electrical conductivity ( $\sigma$ ) of the binary nanofluid for a percent weight ratio 80:20 (MgO/ZnO) was estimated to derive the Critical micelle concentration. The point for which a deflection was noticed in the  $\sigma$  values trend indicated the CMC which is the optimized result of the variable parameter. Thus, Figures 4.1 and 4.2 depicts the sonication time and optimized dispersion fraction for the prepared DIW-based binary NF. For a dispersion fraction of 1 and a 45 minutes sonication time, CMC (optimal values) was achieved as shown in Figures 4.1 and 4.2. A detraction in the pH and  $\sigma$  values was noticed after improving the two parameters, which later enhanced as the dispersion fraction increased. The dropping point in value is referred to as the point of inflection: the CMC and finally, the optimal dispersion fraction [549, 550]. Also, Figure 4.3 presents the optimized amplitude of the formulated binary nanofluid as 75%. The electrical conductivity ( $\sigma$ ) was noticed to detract as the amplitude rises from 70% to 75%, and  $\sigma$  augments as amplitude keeps rising to 80%. The obtained optimized values were used in the formulation of BNF for  $\varphi = 0.05$  vol.% and 0.1vol.% using Equation 3.1 for the measurement of thermal properties and thermo-convection experiment. Three class of binary nanofluids of MgO(20 nm)-ZnO/DIW, MgO (40 nm)-ZnO/DIW and MgO (100 nm)-ZnO/DIW was prepared to examine the influence of nano-size on thermal properties. Single-particled nanofluids of MgO (100 nm)/DIW, MgO (20 nm)/DIW, and ZnO (20 nm)/DIW were also prepared for comparison.

Giwa et al. [96] dispersed binary nanoparticles of 75% (Fe<sub>2</sub>O<sub>3</sub>):25% (Al<sub>2</sub>O<sub>3</sub>) into DW and EG/DW(50:50) basefluids using a two-step method for an optimized dispersion fraction of 1.1, sonication time of 120 minutes and amplitude of 70%. Also, Giwa et al. [31] formulated MWCNT-Fe<sub>2</sub>O<sub>3</sub>/DIW binary nanofluids (0.1 vol%) using SDS as dispersant for an optimized dispersion fraction of 0.5, sonication time of 120 minutes and amplitude and amplitude of 70%. Sundar et al. [551] used a surfactant to formulate CNT-Fe<sub>3</sub>O<sub>4</sub>/DIW nanofluid at an optimized dispersion

fraction of 0.5. The optimized sonication time (120 minutes) and amplitude (70%) were within the published range when compared with previous works. Garbadeen et al. [27] formulated MWCNT/DIW nanofluid using Gum Arabic as dispersant for a dispersion fraction of 4, sonication time of 40 minutes and amplitude of 75%. Joubert et al. [224] also formulated Fe<sub>2</sub>O<sub>3</sub>/DIW nanofluid using SDS surfactant for a 1.0 dispersion fraction, a 42 minutes sonication time and amplitude of 65%.

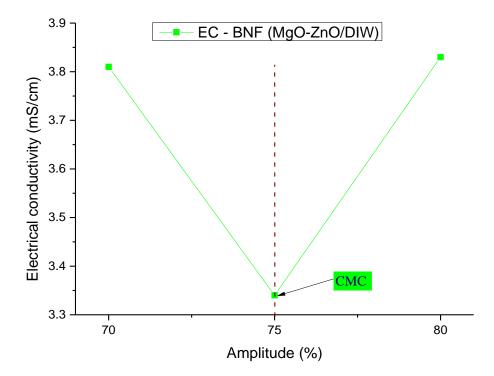


Figure 4.3. Determination of optimized amplitude for BNF.

# 4.3 MORPHOLOGY AND STABILITY OF MONO-NANOFLUIDS

In monitoring the stability of single-particled nanofluid (DIW-based MgO-100 nm, MgO-20 nm and DIW-based ZnO nanofluid), absorbance was monitored for 20 hours duration using a UV-visible spectrophotometer. Figure 4.4 shows that the absorbance of individual samples was stable with time along a nearly straight-line in the horizontal axis. It observed that the absorbance of DIW-based ZnO nanofluid was higher when compared to DIW-based MgO-100 nm and MgO-20 nm nanofluids. In like manner, the wavelength of ZnO/DIW NF (369 nm)

was observed to be more than that of DIW-based MgO (100 nm and 20 nm) NFs (291 nm), as shown as in Table 4.1. In addition, visual checks of mono-nanofluids samples showed nil or little sedimentation for the duration considered.

#### 4.4 MORPHOLOGY AND STABILITY OF BINARY NANOFLUIDS

In monitoring the stability of MgO-ZnO/DIW binary nanofluids, absorbance was also monitored for a 20-hour duration using a UV-visible spectrophotometer. Figure 4.5 shows that MgO/ZnO (20:80) binary nanofluids have more absorbance than MgO/ZnO (80:20) binary nanofluids. In a similar pattern, MgO/ZnO (20:80) binary nanofluids had more wavelengths (330 nm and 362 nm) over that of MgO/ZnO (80:20) binary nanofluids (293 nm and 298 nm). The feedback (for wavelength and absorbance) can be ascribed to hybridizing MgO and ZnO nanoparticles. So, Table 4.1 presents the absorbances and wavelengths of the selected BNFs.

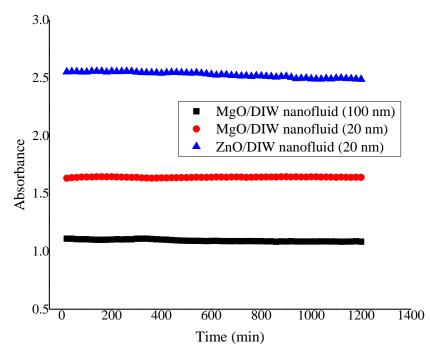


Figure 4.4. Monitoring of stability of single-particle nanofluids

Open literature affirms that the absorbances of 1.631, 2.125, 2.341, 2.602, and 3.138 at a wavelength range of 289 nm – 292 nm was published for 0.05 vol%, 0.10 vol.%, 0.30 vol.%, and 0.40 vol.%, respectively. The wavelengths of 225, 252, 264 and 410 nm were reported

for nanofluids of Al<sub>2</sub>O<sub>3</sub>/DIW, CNT/DW, MWCNT-Ag/W and Ag/DW nanofluids, respectively [552, 553]. The absorbance for the BNF was observed to be slightly higher than that of single-particle nanofluids of MgO and ZnO, which makes for a reasonable degree of hybridisation of ZnO and MgO nanoparticles in the BNF. Visual inspection of single-particle nanofluids and binary nanofluids showed nil or little sediments for the duration considered, further supporting these samples' stability.

Table 4.1: Wavelength and absorbance of mono- and binary nanofluids

Variable	MgO (20 nm)	MgO (100 nm)	ZnO (20 nm)	MgO-ZnO (20:80)-20 nm	MgO-ZnO (20:80)-100 nm	MgO-ZnO (80:20)-20 nm	MgO-ZnO (80:20)-100 nm
Absorbance	1.650	1.773	2.565	4.364	4.468	2.869	1.839
Wavelength	291	291	368	362	330	298	292

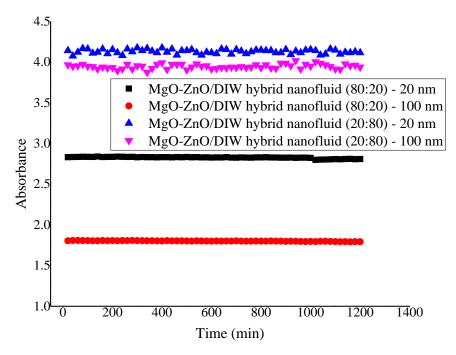


Figure 4.5. Monitoring of stability of selected binary nanofluids

In addition, the binary nanofluids samples were observed to be stable as visual checks showed nil or little sediments for the duration considered. The TEM image as presented in Figure 4.6 showed that the nanoparticles of MgO and ZnO were observed to be well dispersed in DIW. Figures 4.6 showed light spots representing ZnO nanoparticles, while Dark spots represented MgO nanoparticles. The examined samples revealed more light spots than dark spots, which means the TEM discovered more ZnO nanoparticles over MgO nanoparticles. This outcome agrees with the binary nanofluids samples employed for the TEM analysis. In Figure 4.6a, TEM images discovered almost 20 nm for ZnO nanoparticle, and 100 nm for MgO nanoparticles, while Figure 4.6b shows 20 nm was detected for ZnO nanoparticles and 20 nm for MgO nanoparticles, and Figure 4.6c shows 20 nm was detected for ZnO nanoparticles and 40 nm for MgO nanoparticles. That is, results were close to that specified by the manufacturers of the BNPs. In summary, Figure 4.6 reveals a good degree of nanoparticles dispersion was achieved for all percent weights ratio.

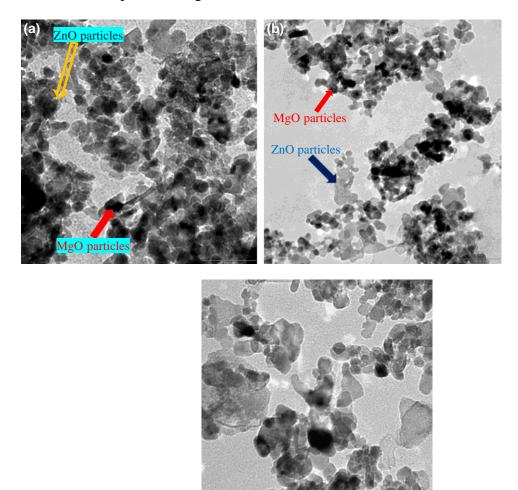


Figure 4.6. The TEM image for: (a) MgO(100 nm)–ZnO(20:80)/DIW binary nanofluids, (b) MgO(20 nm)–ZnO(20:80)/DIW binary nanofluids, and (c) MgO(40 nm)–ZnO (20:80)/DIW binary nanofluid.

100 nm

#### **4.5 CONCLUSION**

Open literature has affirmed scarcity in the values for optimum parameters (amplitude, dispersion fraction, pulse used, and sonication time) for formulating mono-particle nanofluids and binary nanofluids. This affects the repeatability of such experiments. This investigation formulated mono-particle nanofluids of MgO and ZnO, for comparison with binary nanofluids of MgO-ZnO/DIW for  $\varphi$  of 0.10 vol.% and 0.05 vol.% via optimized operating parameters leading to a stable BNFs. TEM images detected nanoparticle sizes close to the manufacturers and a good degree of nanosuspension stability. In addition, the stability of BNFs as observed by the absorbance was found stable. Thus stability and morphology is confirmed satisfactory. Hence, further investigation on thermal properties and thermo-convection was done, and the results were presented and discussed in subsequent chapters.

# CHAPTER 5 MEASUREMENT OF THERMAL PROPERTIES OF BINARY NANOFLUIDS<sup>1,2,3</sup>

# **5.1 INTRODUCTION**

The estimation of thermal properties of binary nanofluids is of great interest as it serves as indicators for its potential use in engineering applications, especially for thermo-convection investigation as done in this study. This Chapter presents the thermal properties of stable BNF as measured under study temperatures and volume concentration, using applicable equipment. Measured thermophysical characteristics of MgO–ZnO/DIW binary nanofluids are pH, viscosity ( $\mu$ ), thermal conductivity ( $\kappa$ ), and electrical conductivity ( $\sigma$ ), under temperatures of 20-50 °C. In addition, models were developed for the BNF samples using measured datasets, as models are scarce in the open literature for BNFs.

# 5.2 THERMAL CONDUCTIVITY OF BINARY NANOFLUIDS

To affirm the degree of correctness for the measuring instrument for the thermal conductivity ( $\kappa$ ) of binary nanofluids (BNFs), a validation check was necessary to examine temperatures 20 <sup>o</sup>C to 50 <sup>o</sup>C. This was ascertained by relating the experimental dataset with documented standards in the ASHRAE standard handbook. Figure 5.1 depicts the compared dataset, which shows a deviation from experimental values compared to the data in the ASHRAE standard handbook [555] as 1.3%, which has been the measurement accuracy.

This chapter is reflected in parts in the following papers:

<sup>&</sup>lt;sup>1</sup>Giwa, S., Momin, M., Nwaokocha, C., Sharifpur, M., and Meyer, J. *Influence of nanoparticles size, per cent mass ratio, and temperature on the thermal properties of water-based MgO–ZnO nanofluid: an experimental approach.* Journal of Thermal Analysis and Calorimetry, 2021. **143**(2): p. 1063-1079.

<sup>&</sup>lt;sup>2</sup>Nwaokocha, C., Giwa S., Ghorbani B., Momin, M., Sharifpur, M., Gharzvini M., Chamkha, A.J., Meyer, J.P., *Experimental formulation and GMDH modelling of thermal conductivity of MgO–ZnO/deionised water hybrid nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>3</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Influence of concentration, mixing ratios, and working temperature on the thermal behaviour of binary nanofluids of MgO–ZnO: an experimental investigation.* Ready for submission.

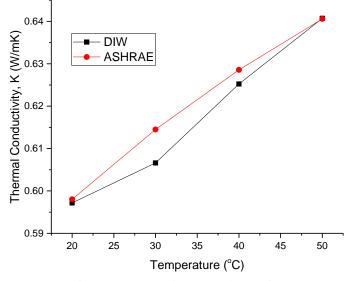


Figure 5.1. Comparison of DIW with reference values.

The thermal conductivity ( $\kappa$ ) of DIW-based mono-particles nanofluids (100 nm-MgO, 20 nm-MgO and 20 nm ZnO) is shown in Figure 5.2. It was noticed that by dispersing nanoparticles into basefluid, its  $\kappa$  enhanced notably with an increase in temperature, which agrees with the literature [132, 215, 217, 554, 555]. Figure 5.2 shows a higher  $\kappa$  for MgO/DIW NFs over ZnO/DIW nanofluids. Also, MgO(20 nm)/DIW NF was observed to have a more effective  $\kappa$  over MgO(100 nm)/DIW NF.

# 5.2.1 Influence of Nanosize, Percent Weight Ratios and Temperature on Thermal Conductivity

The trio influence of nanoparticle size (NS), various percent weight ratios (PWRs) under rising temperature on the thermal conductivity of MgO-ZnO/DIW binary nanofluid for 0.1 vol.% is presented in Figures 5.2 to 5.4. From Figures 5.2 to 5.4, it can be deduced that dispersing nanoparticles into DIW, its  $\kappa$  enhanced significantly with steady increase in temperature, which agrees with open literature [42, 132, 152, 171, 215, 217, 554, 555]. As presented in Figure 5.3 for 20 nm-MgO, the 40:60 BNF sample had the maximum effective thermal conductivity ( $\kappa$ ), then other BNF samples follow in order of 60:40, 80:20, and 20:80. A similar trend was noticed for MgO(100 nm)-ZnO/DIW binary nanofluid, as seen in Figures 5.4. The synergy between

the thermal conductivity of MgO (54.9 W/mK) and ZnO (29 W/mK) nanoparticles [556] could be responsible for the obtained results. Also, the 20 nm-MgO based binary nanofluids had more effective thermal conductivity over 100 nm-MgO BNFs, for the studied PWRs. Figures 5.3 and 5.4 deduced that MgO nano-size had a great influence on  $\kappa$ , then PWR and finally temperature.

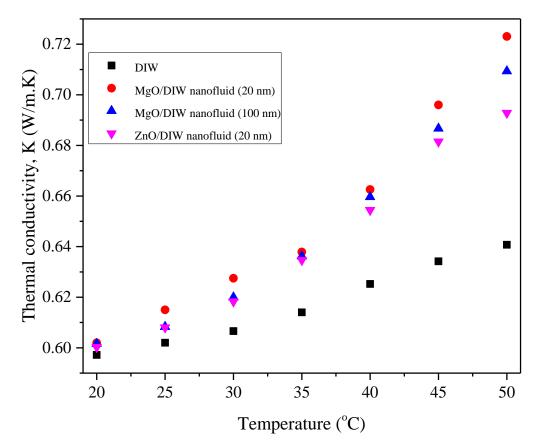


Figure 5.2. Effective thermal conductivity of single-particled nanofluids as temperature rises.

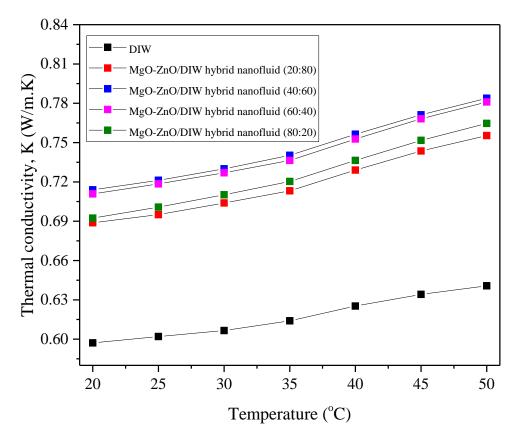


Figure 5.3. Effective thermal conductivity for MgO(20 nm) based binary nanofluids as temperature rises.

From Figure 5.3, the effective  $\kappa$  of 20 nm-based binary nanofluids was enhanced by 15.35% – 22.33% under rising temperature, while it improved by 9.52% – 17.91% for 100 nm-based binary nanofluids as presented in Figure 5.4 when compared to DIW. Maximum augmentation of 19.56% – 22.33% and 14.95% – 17.91% was observed for 40:60 BNF sample of 20 nm-MgO and 100 nm-MgO nanoparticle's sizes, respectively. In the same vein, the lowest detraction in effective  $\kappa$  was observed for 15.35%–17.89% and 9.52%–12.97% for 20 nm-MgO and MgO (100 nm) based 20:80 BNFs, respectively. Siddiqui et al. [557], and Hamid et al. [261] published a maximum  $\kappa$  augmentation for 50:50 (Cu-Al<sub>2</sub>O<sub>3</sub>/DIW) and 20:80 (TiO<sub>2</sub>-SiO<sub>2</sub>/W-EG). An enhancement of 14.17% was reported by Giwa et al. [132] for  $\kappa$  for Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> (75:25)/DIW BNF for 0.3 vol% and 40 °C. Aparna et al. [227] published a maximum  $\kappa$  augmentation of 23.82% for Al<sub>2</sub>O<sub>3</sub>-Ag (50:50)/DIW binary nanofluids at 0.1 vol% for 52 °C. Also, Zadkhast et al. [349] published an effective  $\kappa$  enhancement of 30.38% [45] for CuO-

MWCNT (50:50)/DIW binary nanofluids for 0.60 vol.% at 50 °C. Next, Sundar et al. [551] reported an effective  $\kappa$  improvement of 24.46% for CNT-Fe<sub>3</sub>O<sub>4</sub> (26:74)/DIW binary nanofluids at 0.30 vol.% for 60 °C. In addition, Sundar et al. [90] attained the highest  $\kappa$  enhancement of 29.39% for ND-Ni/DIW BNF at 0.3 vol% and 60 °C. Taherialekouhi et al. [558] also achieved a maximum  $\kappa$  augmentation of 33.9% for GO-Al<sub>2</sub>O<sub>3</sub>/DIW BNF. The obtained results from this current investigation were noticed to be within published range in the open literature.

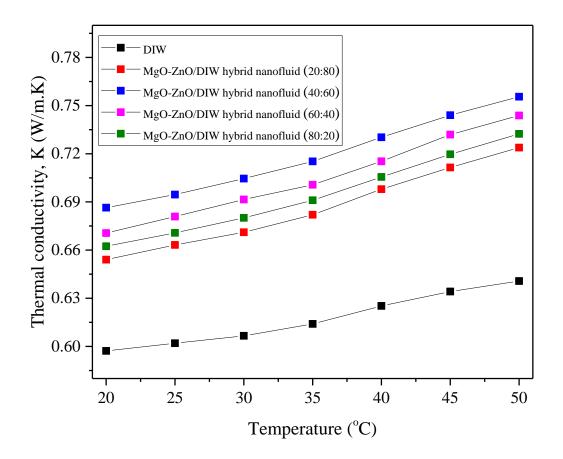


Figure 5.4. Effective thermal conductivity for MgO(100 nm) based binary nanofluids as temperature rises.

# 5.2.2 Influence of Concentration, Mixing Ratios and Temperature on Thermal Conductivity

The thermal conductivity ( $\kappa$ ) of BNFs as a function of  $\varphi$  (0.05 and 0.1 vol.%) for different PWRs and temperatures 20–50 °C is presented in Figures 5.5 and 5.6. The nanosuspension of

BNPs into DIW clearly enhanced  $\kappa$ . The  $\kappa$  of BNFs was observed to show good improvement for all PWRs at rising temperature. This supports published works [33, 96, 154, 156, 262, 278, 362, 559-561]. As presented in Figure 5.5 for 0.05 vol% BNFs, the 60:40 nanohybrid samples were observed to possess a maximum  $\kappa$ , next 40:60, 80:20 and 20:80 BNFs samples. For 0.10 vol% BNFs illustrated in Figure 5.6, it was observed that 40:60 BNF sample was observed to possess maximum  $\kappa$  and then trailed by 60:40, 80:20, and 20:80 samples.

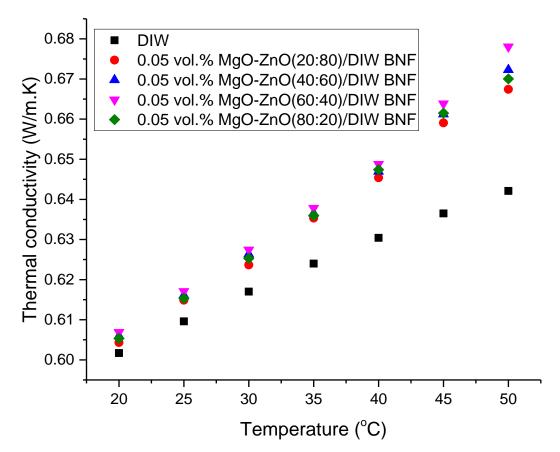


Figure 5.5. Thermal conductivity of MgO-ZnO/DIW binary nanofluids (0.05 vol%) with temperature increase for different percent weight ratios.

The synergy between  $\kappa$  of NPs, PWR and volume concentration may be responsible for the results. Maximum  $\kappa$  of 0.67803 W/mK was observed for BNF (60:40) for  $\varphi = 0.05$  vol% at temperature 50 °C, while lowest  $\kappa$  value of 0.60433 W/mK was obtained for BNF (20:80) at temperature 20 °C. For BNFs of  $\varphi = 0.10$  vol%, highest  $\kappa$  result was 0.78381 W/m.K for BNF (40:60) at temperature 50 °C, while lowest  $\kappa$  value of 0.68883 W/m.K was observed for BNF

(20:80) at temperature 20 °C. Increase in temperature augmented  $\kappa$  for the BNFs as compared to the BF, due to the impact of Brownian motion on NPs at higher temperatures. The influence of Brownian motion on  $\kappa$  of NFs is published in the literature [69, 145, 261, 561-565].

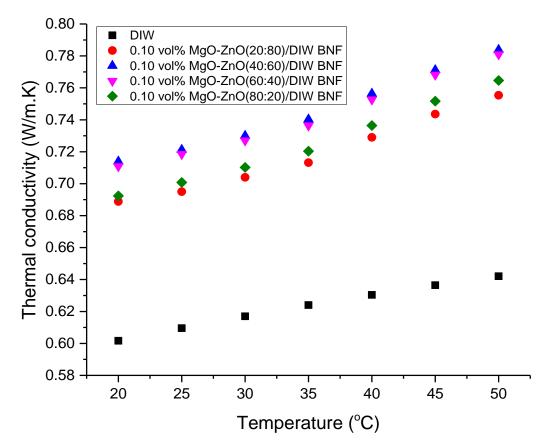
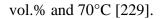


Figure 5.6. Thermal conductivity of MgO-ZnO/DIW binary nanofluids (0.1 vol%) with temperature increase for different percent weight ratios.

Thermal conductivity enhancement (TCE, %) of BNFs under the influence of temperature (20 °C to 50 °C) is presented as Figures 5.7 and 5.8 for two-volume concentrations (0.05 vol% and 0.1 vol%) and four PWRs. Figure 5.7 presents maximum TCE enhancement of 5.60% for 60:40 nanohybrid sample of 0.05 vol% BNFs, while for 0.1 vol.% BNFs, highest improvement of 22.07% for 40:60 BNF sample was achieved as shown in Figure 5.8. Figures 5.7 and 5.8 shows that the dispersion of MgO-ZnO NPs augments  $\kappa$  greatly, especially at higher temperatures. Open literatures reported  $\kappa$  improvement of 66.5% for TiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub>(50:50)/W at 1.0 vol.% and 70°C [262], 17.7% for ND- Fe<sub>3</sub>O<sub>4</sub>(72:28)/W at 0.2 vol.% and 60°C [566], 14.17% for

MWCNT-Fe<sub>2</sub>O<sub>3</sub>/DIW at 0.4 vol.% and 40°C [28], 22.1% for TiO<sub>2</sub>-SiO<sub>2</sub>(60:40)/W-EG at 3.0



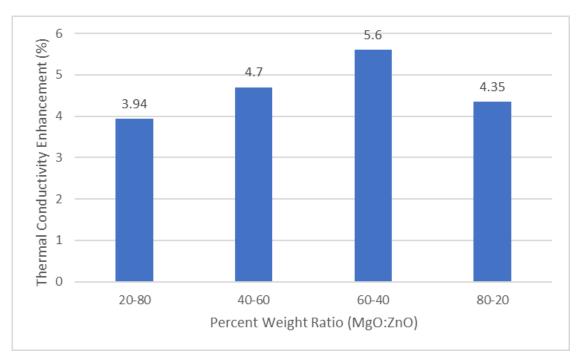


Figure 5.7. Thermal conductivity enhancement (%) for 0.05 vol% BNF.

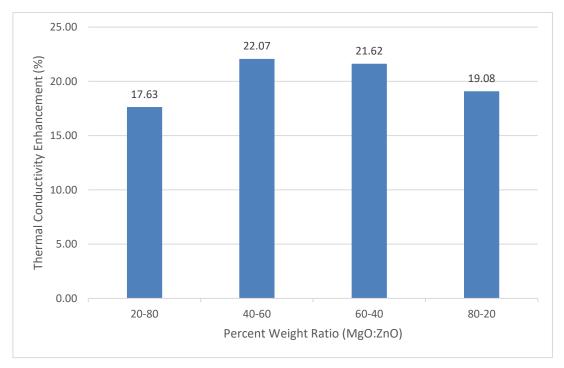


Figure 5.8. Thermal conductivity enhancement (%) for 0.10 vol% BNF.

Figures 5.9 and 5.10 also presents the influence of PWRs on  $\kappa$  of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for the studied temperatures. It is observed in Figure 5.9 that  $\kappa$  increases as PWR of MgO increase steadily to a higher value for 60:40 sample and then detracts. Also, the lowest  $\kappa$  was observed for the 20:80 BNF nanohybrid sample has had the least composition of MgO NP between the temperature range 20°C to 50°C. It is observed in Figure 5.10 that  $\kappa$ increases as PWR of MgO increase steadily to a higher value for 40:60 sample. In addition, a further rise in MgO NP detracted thermal conductivity, with the least  $\kappa$  for the lowest composition of MgO NP (20:80) for the studied temperature. The detraction in  $\kappa$  could be attributed to the deterioration in dispersion stability as observed visually.

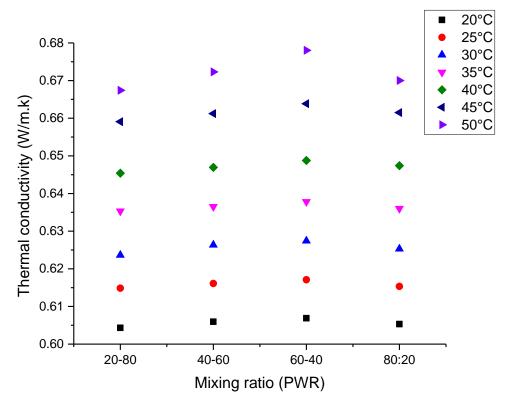


Figure 5.9. Influence of PWRs on the thermal conductivity of 0.05 vol% BNF.

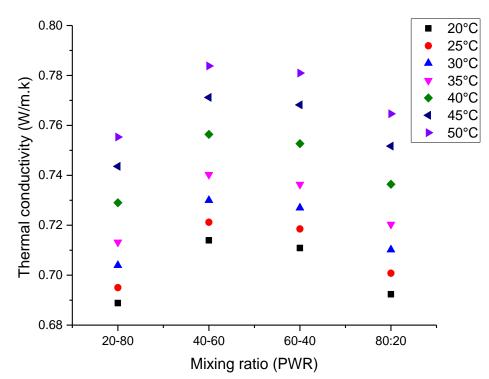


Figure 5.10. Influence of PWRs on the thermal conductivity of 0.10 vol% BNF.

# **5.3 VISCOSITY OF BINARY NANOFLUIDS**

Viscosity ( $\mu$ ) explains the resistance to the flow of fluid under shear stress. In investigations that involves the estimation of the thermal properties of nanofluid, viscosity follows thermal conductivity measurement.

#### 5.3.1 Influence of Nanosize, Percent Weight Ratio and Temperature on Viscosity

MgO and ZnO possess nano--densities of 3.56 g/m<sup>3</sup> and 5.606 g/m<sup>3</sup> [556], respectively, with the viscosity of ZnO NPs higher than MgO NPs. Hence, the viscosity of the binary nanofluids is the offshoot of the blend between the density of MgO and ZnO nanoparticles and DIW, as naratted in Figure 5.11. So in Figure 5.11, it was noticed that ZnO/DIW nanofluid had a more effective viscosity over MgO/DIW nanofluids for both nano-sizes of 20 nm and 100 nm. This observation is in agreement with the investigation of Assdi et al. [556], who published a more viscosity for ZnO/EO nanofluid than MgO/EO nanofluid. Also, MgO(20 nm)/DIW nanofluid had the least viscosity over 100 nm MgO/DIW nanofluid. This negates the result of Adio et al.

[32] for MgO/EG nanofluids with nano sizes of 15, 21, and 125 nm. This discrepancy may be accounted for by density and basefluid type.

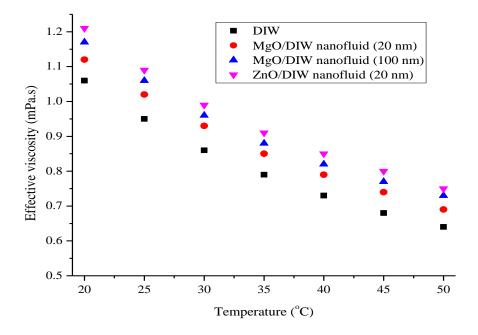


Figure 5.11. Effective viscosity of single-particle nanofluids with temperature rise.

In Figures 5.12 and 5.13, the impact of temperature and PWRs on the viscosity of binary nanofluid samples was depicted for MgO nanoparticles (20 nm and 100 nm). From Figures 5.12 and 5.13, as temperature increases from 20 to 50 °C, it gradually detracts the relative viscosity of binary nanofluids. This outcome agrees with published results on the effect of temperature on the effective viscosity of nanofluids [21,32–35]. As observed in Figure 5.12, the PWR 60:40 had the maximum effective viscosity, while 20:80 sample BNF sample had the least effective viscosity for 20 nm-MgO based BNFs. A similar trend was noticed in Figure 5.13 for the 100 nm-MgO based binary nanofluids with the 60:40 and 20:80 binary nanofluids possessing the highest and lowest effective viscosity, respectively. Open literature posits a different result for highest effective viscosity compared with Giwa et al. [36] (80:20; Al<sub>2</sub>O<sub>3</sub>-MWCNT) and Hamid et al. [21] (50:50; TiO<sub>2</sub>-SiO<sub>2</sub>), who published the viscosity of DIW and W/EG based binary nanofluids with Al<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> nano-particles being denser than MWCNT and SiO<sub>2</sub> nanoparticles, respectively.

When comparing Figures 5.12 and 5.13, a minor discrepancy was observed for the effective viscosity results of the experimental formulation of MgO-ZnO/DIW binary nanofluid with various nano-sizes of MgO nanoparticles and different PWRs. Also, using the MgO nano-size of 20 nm to formulate the BNF, a detraction in  $\mu$  was observed. A rise in the nano-size of MgO NPs from 20 nm to 100 nm enhanced the  $\mu$  for all BNF samples. Adio et al. [32] reported a different result, such that a rise in NPs' size (21 nm to 125 nm) led to a  $\mu$  detraction for MgO/EG nanofluids. However, a different outcome was reported for  $\mu$  based on the nano-size of nanofluids [246]. In summary, MgO nano-size greatly influenced the  $\mu$  of BNFs, trailed by the impact of temperature and, finally, PWR of binary nano-particles.

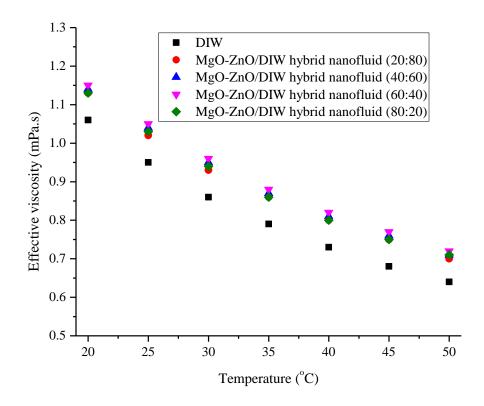


Figure 5.12. Effective viscosity of MgO (20 nm) based binary nanofluids as temperature rises.

Upon comparison to the basefluid (DIW), an enhanced  $\mu$  for single-particle nanofluid was observed as 5.46% – 9.52% for 20 nm-MgO/DIW nanofluids, 10.17% – 15.87% for 100 nm-MgO/DIW nanofluids, and 13.94% – 19.05% for DIW-based ZnO (20 nm), for the

temperature range studied. This supports the works of Asadi and Pourfattah [37] who reported a 75% and 124% enhancements for EO-based MgO and ZnO nanofluid for 1.5 vol% at 55 °C. For 20 nm-MgO based binary nanofluids,  $\mu$  improvements of 6.40% – 11.1% and 8.29% – 14.29% were observed for PWRs of 60:40 and 20:80, respectively compared to DIW. For 100 nm-MgO based binary nanofluids,  $\mu$  improvements of 11.11% – 15.87% and 12.99% – 17.46% was also observed for PWRs of 60:40 and 20:80, respectively when related to DIW for the examined temperatures. Sundar et al. [90] published the highest viscosity enhancement of 23.24% for ND-Ni/DIW BNF at 0.30 vol% and 60 °C. Giwa et al. [36] reported the highest  $\mu$ enhancements of 24.56% for 0.1 vol% at 55 °C for a DIW-based Al<sub>2</sub>O<sub>3</sub>-MWCNT (80:20). Sundar et al. [11] achieved the highest 1.5-fold viscosity enhancement at 0.3 vol% and 60 °C for DIW-based CNT-Fe<sub>3</sub>O<sub>4</sub> (26:74). Giwa et al. [39] achieved  $\mu$  enhancements of 4.55 – 20.43% for at 0.05 – 0.30 vol% and 20 – 60 °C) for DIW-based Al<sub>2</sub>O<sub>3</sub>-Fe<sub>2</sub>O<sub>3</sub> (25:75) nanofluids.

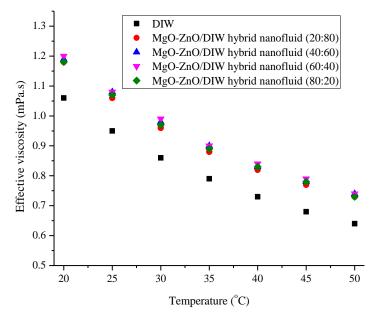


Figure 5.13. Effective viscosity of MgO (100 nm) based binary nanofluids as temperature increases.

#### 5.3.2 Influence of Concentration, Mixing Ratio and Temperature on Viscosity

As viscosity ( $\mu$ ) plays major role in defining the pumping power requirements of heat exchangers, hence nanofluid's viscosity behaviour is key. Figures 5.14 and 5.15 presents the  $\mu$  of BNFs for  $\varphi$  of 0.05 and 0.1 vol.% for four separate nanoparticle mixing ratios for each  $\varphi$  under the influence of rising temperatures from 20–50 °C. From Figures 5.14 and 5.15, it was observed that at rising temperature,  $\mu$  of the BNFs and DIW detracted steadily, which agrees with the literature [21, 31, 39, 96, 248, 261, 262, 368, 567, 568]. This observation is premised on the improvement of the kinetic energy of nanoparticles at higher temperatures, leading to a faster rate of movement of molecules. Figures 5.16 and 5.17 presents the impact of PWRs on  $\mu$  of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for the considered temperatures. It is observed in Figures 5.16 that  $\mu$  rises gradually to a peak for PWR of MgO-ZnO at 40:60 and detracts thereafter. But for Figures 5.17,  $\mu$  rises steadily to a peak value when PWR of MgO-ZnO is 60:40 and reduces after that.

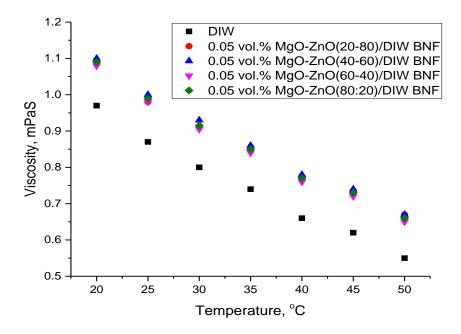


Figure 5.14. Viscosity of MgO-ZnO/DIW BNFs(0.05 vol%) under temperature increase for different percent weight ratios.

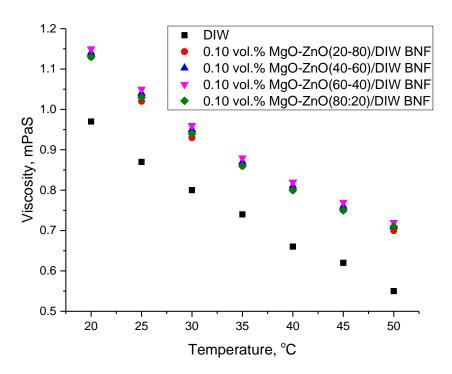


Figure 5.15. Viscosity of MgO-ZnO/DIW BNFs (0.1 vol%) under temperature increase for different percent weight ratios.

For the 0.05 vol.% BNFs in Figure 5.14 and 5.16, it was observed that maximum  $\mu$  of 1.1 mPaS was achieved for BNF sample of PWR 40:60 for temperature 20 °C, while the 60:40 sample had the least  $\mu$ . However, with a steady rise in temperature, the  $\mu$  of all the BNF samples and DIW exhibited a decreasing trend, which agrees with the literature. For the 0.10 vol.% BNFs in Figures 5.15 and 5.17, the 60:40 BNF sample had the highest  $\mu$ , while the least is 20:80. The mixing ratio influenced the variation in  $\mu$  for the BNFs.

Figures 5.18 and 5.19 present BNFs' viscosity enhancement (%) over DIW under rising temperature for the two-volume concentrations (0.05 vol% and 0.1 vol%) and four separate mixing ratios. The BNFs of 0.05 vol.% as depicted in Figure 5.18, presents 20:80 and 40:60 BNF samples with the highest enhancement of 21.82%, while for 0.1 vol.% BNF samples, the highest enhancement was 30.91% for 60:40 BNF sample as presented in Figure 5.19. This outcome agrees with literature [21, 58, 90, 91, 132, 144, 162, 568-570]. To compare Figures 5.18 and 5.19, a discrepancy was noticed for the  $\mu$  results for the two different volume

concentrations used to formulate the BNFs. It can be deduced that using 0.05 vol% to formulate the BNFs led to reduced  $\mu$  values, while an increase to 0.1 vol% produced enhanced  $\mu$  values for its BNFs.

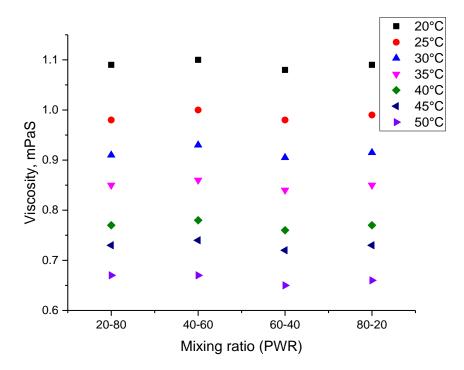


Figure 5.16. Influence of mixing ratio on the viscosity of 0.05 vol% BNFs.

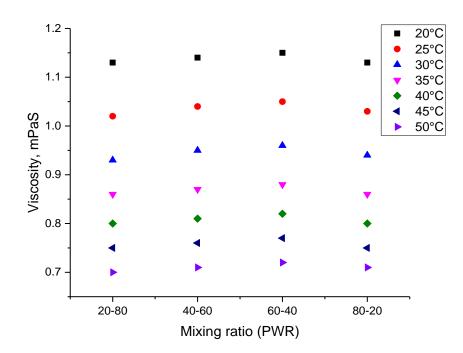


Figure 5.17. Influence of mixing ratio on the viscosity of 0.10 vol% BNFs.

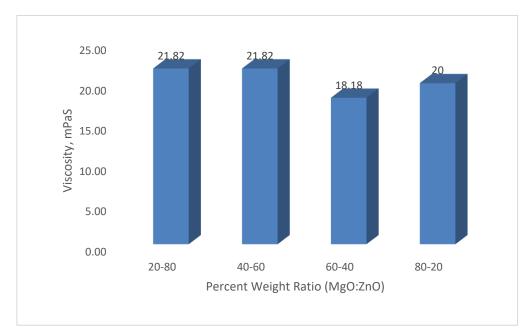


Figure 5.18. Viscosity enhancement (%) for 0.05 vol% BNFs.

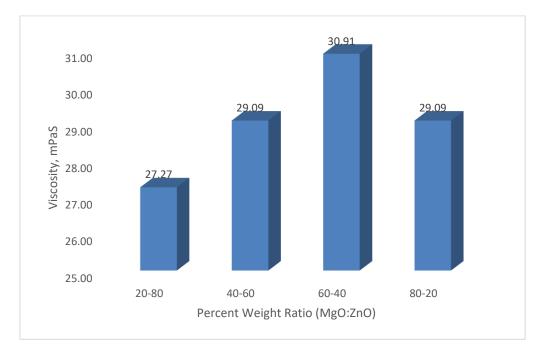


Figure 5.19. Viscosity enhancement (%) for 0.10 vol% BNFs.

### **5.4 pH OF BINARY NANOFLUIDS**

The pH of an aqueous medium indicates its level of basicity or acidity, so the pH of monoparticle and binary nanofluids were valued in this investigation. An optimized pH value defines a good nanosuspension due to improved electrostatic repulsive forces, which detracts the agglomeration impact of particles and improves the stable limit of nanofluids.

## 5.4.1 Influence of Nanosize, Percent Weight Ratio and Temperature on pH

Figure 5.20 depicts that the pH of single-particle nanofluid was more than basefluid, because of the nanosuspension influencing the pH of the basefluid. Also, a rise in temperature detracted the pH of DIW and nanofluids. This agrees with Adio et al. [271] for 0.1 - 3.0 vol.% MgO/EG NFs at 20–70 °C but contrasted with Adio et al. [269], who recorded Al<sub>2</sub>O<sub>3</sub>/glycerol at volume concentration  $\leq 0.5$  vol% and 20–70 °C. The dispersion of 100 nm-MgO NPs into basefluid produced the maximum pH improvement (38.23%), while ZnO nano-particles led to pH improvement (least) by 22.652%. Figure 5.20 showed a variation in pH of 20 nm- and 100 nmbased MgO/DIW NFs were reducing for an increased temperature with a huge change amidst them and the pH of ZnO/DIW nanofluid closed slightly with increase in temperature. Adio et al. [271] published a more pH for MgO (20 nm)/EG nanofluid than 100 nm-MgO/EG nanofluid, which differs from the results in the current study.

Figures 5.21 and 5.22 presents the pH of 20 nm- and 100 nm-MgO based BNFs for different percent weight ratios at varying temperatures. It is observed in Figure 5.21 that the least pH enhancement (30.20% – 39.59%) was measured when compared with Figure 5.22, which had a higher enhancement (31.99% – 40.68%). In Figures 5.21 and 5.22, 40:60 BNF had the highest pH while 20:80 sample had the least. A rise in temperature was observed to detract pH for both BNFs and nanofluids. For the single-particle and binary nanofluids with over pH of 7, basic-natured aqueous fluid was prepared as the nanoparticles were dispersed in DIW. This is consonant with the dispersion of ZnO nanoparticles in water [571] and with MgO nanoparticles

in EG [271], with individual nanofluid having a basic pH (above 7). Figures 5.21 and 5.22 posits that temperature possessed a higher influence on the pH of binary nanofluids, trailed by nano-size of MgO, and then percent weight ratios.

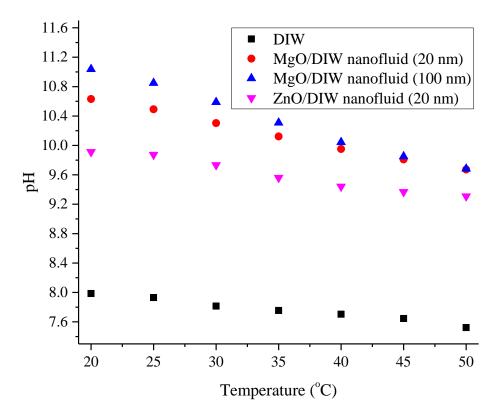


Figure 5.20. pH of single-particle nanofluid as temperature rises.

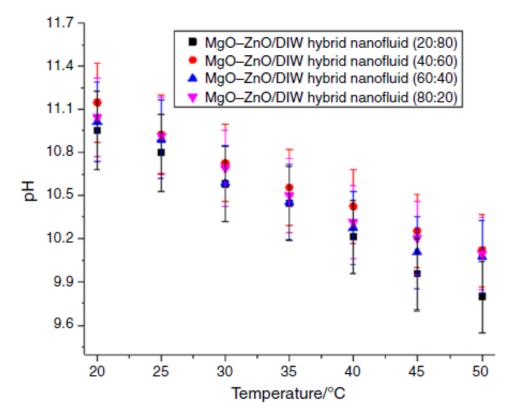


Figure 5.21. pH of MgO (20 nm) based binary nanofluids as temperature increase.

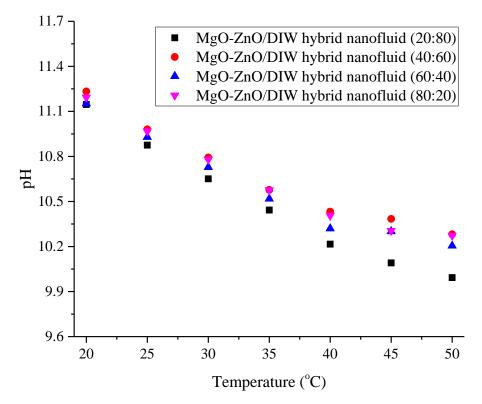


Figure 5.22. pH of MgO (100 nm) based binary nanofluids with temperature increase.

### 5.4.2 Influence of Concentration, Mixing Ratio and Temperature on pH

Figures 5.23 and 5.24 provides the pH values for the BNFs (at  $\varphi = 0.05$  and 0.1 vol%), respectively, for different PWRs for the studied temperatures (20–50 °C). The suspension of BNPs into DIW clearly improved the pH. The pH for all PWRs of the BNFs reflects a gradual decline with increasing temperature, which is consonant with published works [21, 32, 171, 265, 271, 572]. Since the BNFs has a pH over 7, an alkaline nanosuspension was formulated. Hence, Figures 5.23 and 5.24 depict temperature's influence on the pH, followed by volume concentration and finally PWRs.

Figures 5.25 and 5.26 illustrates the influence of  $\varphi$  (0.05 and 0.1 vol%), different PWRs and temperature (20–50 °CS) on pH enhancement (pHE). Figure 5.25 had a pHE of 27.04% to 40.74% for 0.05 vol% BNFs, with 60:40 nanohybrid sample having the maximum enhancement. While Figure 5.26 had pHE ranging 30.20% to 39.59% for 0.10 vol% BNFs, with the highest improvement for 40:60. Figures 5.27 and 5.28 illustrates the impacts of PWRs on pH of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for the studied temperatures. Figure 5.27 depicts that pH rises gradually as MgO's PWRs also increase and get to the highest value for PWR 60:40. But, a least pH for PWR 80:20 at a temperature range of 20°C to 50°C. Also, Figure 5.28 provides pH increasing gradually and peaked PWR 40:60.

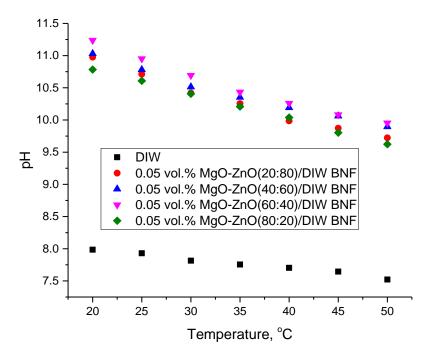


Figure 5.23. pH of MgO-ZnO/DIW BNFs (0.05 vol%) with temperature increase for different percent weight ratios.

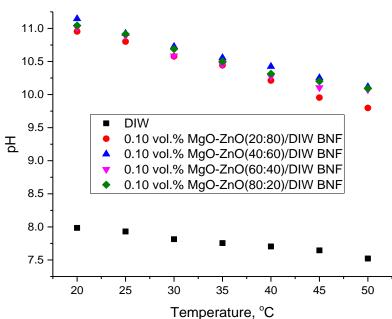


Figure 5.24. pH of MgO-ZnO/DIW BNFs (0.1 vol%) with temperature increase for different percent weight ratios.

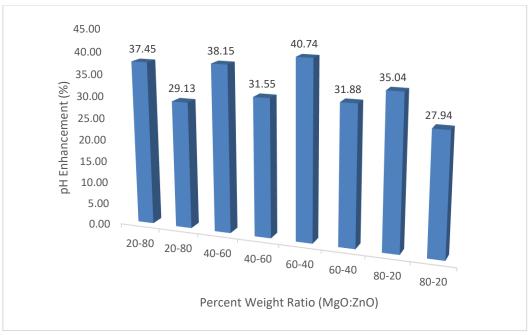


Figure 5.25. pH enhancement (%) for 0.05 vol% BNF.

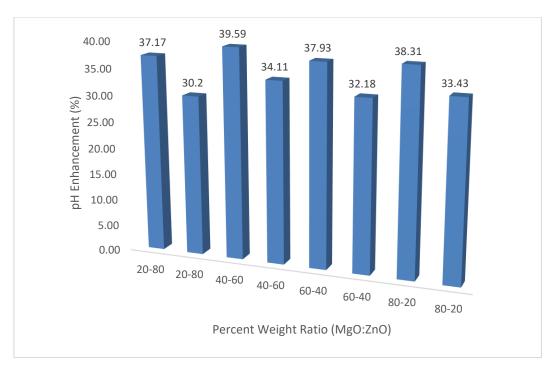


Figure 5.26. pH enhancement (%) for 0.10 vol% BNF.

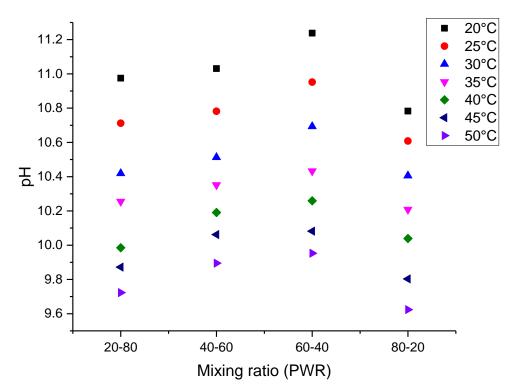


Figure 5.27. Influence of mixing ratio on the pH of 0.05 vol% BNF.

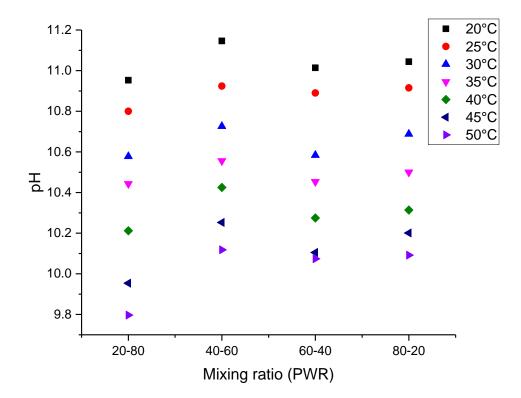


Figure 5.28. Influence of mixing ratio on the pH of 0.10 vol% BNF.

### 5.5 ELECTRICAL CONDUCTIVITY OF BINARY NANOFLUIDS

The electrical conductivity ( $\sigma$ ) of nanohybrids is the ability to enhance the movement of electrical charges, due to ionized nanoparticles activation during dispersion, thus making it conduct electricity upon applying an electric potential across it. This property aids the keen observation of stability and the extent of suspension of nanoparticles in the basefluids [21, 31, 96, 172, 204, 264, 265]. However, unlike the measurement of viscosity and thermal conductivity, literature is scarce on the measurement of  $\sigma$  of binary nanofluids.

## 5.5.1 Influence of Nanosize, Percent Weight Ratio and Temperature on EC

Figure 5.29 presents the impact of percent weight ratios, rise in temperature and nanosize on the effective  $\sigma$  for MgO (20 nm)-based BNFs. The dispersion of binary nanoparticles into DIW significantly enhanced electrical conductivity over DIW. The PWR of 40:60 yielded the maximum effective electrical conductivity (2.99 – 3.19 mS/cm), while sample 80:20 had the least  $\sigma$ . An increase in temperature (20 – 50 °C) led to a gradual improvement in electrical conductivity for all binary nanofluids (Figures 5.29 – 5.30) and DIW (Figures 5.31), as reported in the literature [96, 269, 270, 278, 573]. Figure 5.30 illustrates the influence of percent weight ratios, rise in temperature and nanosize on the effective electrical conductivity ( $\sigma$ ) for 100 nm-MgO based BNFs. Also, an increase in temperature (20 – 50 °C) slightly improved effective electrical conductivity for all PWRs of binary nanofluids. Highest effective electrical conductivity of 3.31 – 3.65 mS/cm was observed for PWR 40:60, and the lowest effective electrical conductivity (2.38–2.50 mS/cm) was noticed for PWR 80:20 for a temperature rise of 20 – 50 °C.

In comparing Figures 5.29 and 5.30, effective  $\sigma$  for 100 nm-MgO based BNFs was noticed to possess more effective  $\sigma$  of 20 nm-MgO based BNFs. This agrees with Adio et al. [271], who examined the effective  $\sigma$  of EG-based MgO (20 nm) and MgO (100 nm). For PWR 40:60, maximum effective  $\sigma$  was observed for both 20 nm-MgO and 100 nm-MgO based BNFs. Also,

Figures 5.29 and 5.30 showed that temperature had a significant impact than MgO nano-size and PWRs in augmenting effective  $\sigma$  for the BNFs. PWRs had the least influence.

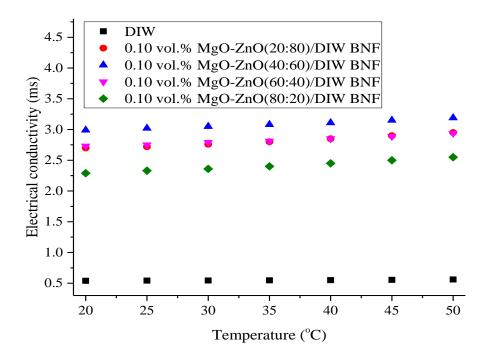


Figure 5.29. Electrical conductivity of MgO (20 nm) based binary nanofluids with temperature increase.

From Figure 5.31, it was observed that for a rise in temperature, effective  $\sigma$  of MgO/DIW NFs (2.05 – 2.16 mS/cm) was higher than the effective electrical conductivity of ZnO/DIW NF (1.95 – 2.13 mS/cm). Using MgO(100 nm)/DIW nanofluids, a lightly more effective electrical conductivity (2.08–2.20 mS/cm) was observed in comparison to MgO(20 nm)/DIW nanofluids (2.05 – 2.16 mS/cm). Adio et al. [271] reported a relatively more effective  $\sigma$  for MgO(20 nm)/EG nanofluid over that of MgO(100 nm)/EG nanofluid at 0.1 – 3 vol% and 20 – 70 °C.

For Figures 5.29 and 5.30, an effective  $\sigma$  for 40:60 sample of 20 nm-MgO based BNFs was augmented by 453.70% – 468.63%, whereas 100 nm-MgO enhanced by 512.96% – 550.62%. Also, the PWR 80:20 of 20 nm-MgO based BNFs was improved by 324.07% – 354.55% while 100 nm-MgO augmented by 340.74% – 345.63%. They were compared to DIW for studied temperature (20 – 50 °C). The result obtained agrees with the following literature - Giwa et al.

[34] reported enhancements of 163.37 - 1692.16% for Fe<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> (75:25)/DIW nanofluids at 0.05 - 0.75 vol% and temperature 20 - 50 °C. Sundar et al. [18] reported improvements of 1339.81% - 853.15%, for Ni-ND (15:85)/DW nanofluids at 0.10 vol.% and temperature 24 - 65 °C. Qing et al. [19] reported 97% - 557% improvements for SiO<sub>2</sub>-G/naphthenic mineral oil nanofluids for 0.01 - 0.08 wt% at room temperature.

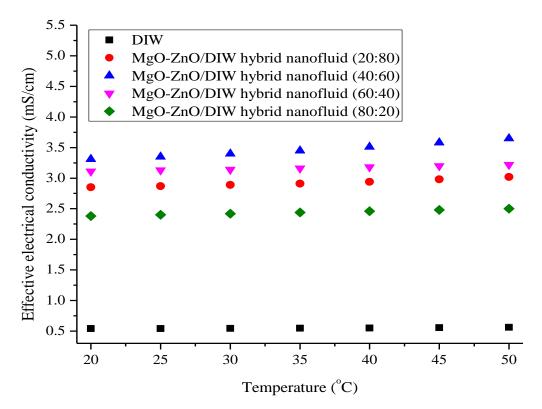


Figure 5.30. Electrical conductivity of MgO (100 nm) based BNFs as temperature rises.

However, improvements of 262.04% - 279.68%, 279.63% - 285.03%, and 285.19% - 292.16% were determined for ZnO/DIW nanofluids, MgO (20 nm)/DIW nanofluids, and MgO (100 nm)/DIW nanofluids, respectively when related with DIW. Adio et al. [271] published a 6000% augmentation for MgO/EG NF at 25 °C and 0.5 vol%. Also, literature confirmed improvements of 2370% for Al<sub>2</sub>O<sub>3</sub>/water nanofluid at 2 vol% and 25.9 °C [264], enhancements of 833% for Al<sub>2</sub>O<sub>3</sub>/water nanofluid at 0.5 vol% and 24 °C [273], enhancements of 360% for Fe<sub>3</sub>O<sub>4</sub>/water nanofluid at 0.50 vol.% and 60 °C [268]. The outcomes above show that the effective electrical conductivity of binary nanofluids had good augmentation compared to

mono-particle nanofluids. Nanosuspension was observed to possess a positive influence on the  $\sigma$  of BNFs.

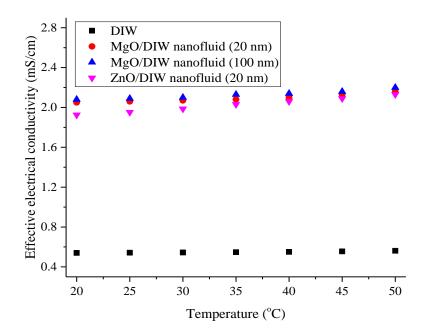


Figure 5.31. Effective electrical conductivity of single-particle nanofluid as temperature rises.

# 5.5.2 Influence of Concentration, Mixing Ratio and Temperature on EC

Figures 5.32 and 5.33 explains the impact of volume concentration (0.05 and 0.10 vol%), PWRs and increasing temperatures on the electrical conductivity ( $\sigma$ ) of BNFs. In Figure 5.32, PWR 40:60 had maximum  $\sigma$  (2.26-2.59 ms), whereas PWR 20:80 had the least  $\sigma$  values (1.93-1.97 ms). Also, in Figure 5.33, PWR 40:60 had maximum  $\sigma$  (2.99-3.19 ms), whereas PWR 80:20 had the least  $\sigma$  values (2.29-2.55). Figures 5.32 and 5.33 illustrate that at rising temperature of 20 to 50 °C, a gradual  $\sigma$  enhancement of DIW and the BNFs were observed, in agreement with literature [21, 31, 32, 96, 143, 270, 271, 278, 574-576]. Comparing Figures 5.32 and 5.33,  $\sigma$  of MgO-ZnO/DIW BNFs (0.10 vol%) was observed to be higher than that of MgO-ZnO/DIW BNFs (0.05 vol%), with 40:60 PWR BNF recording the maximum  $\sigma$  for both volume concentrations. Also, the effect of temperature was more notable in improving  $\sigma$  for the BNFs, than  $\varphi$  and PWR.

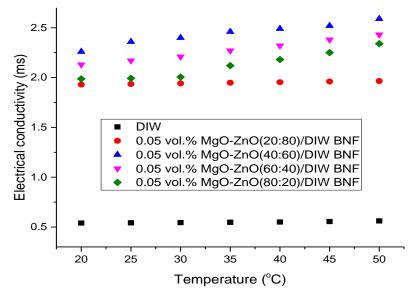


Figure 5.32. Electrical conductivity of MgO-ZnO/DIW BNFs (0.05 vol%) under temperature increase for various PWRs.

In addition, Figures 5.34 and 5.35 illustrates that  $\sigma$  of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) had a maximum improvement for 40:60 BNF samples for the two volume concentrations. Upon comparing with DIW, PWR 40:60 (0.05 vol%) was augmented by 318.52-361.68%, whereas PWR 40:60 BNF (0.10 vol%) had an enhancement of 453.70-468.63%, which agrees with published results [21, 31, 32, 41, 96, 172, 264, 270, 271, 569].

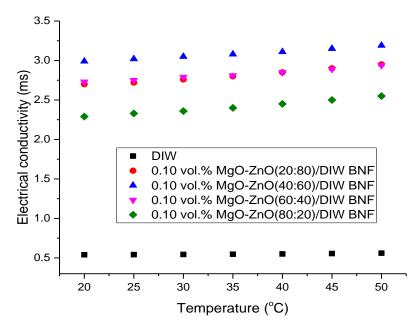
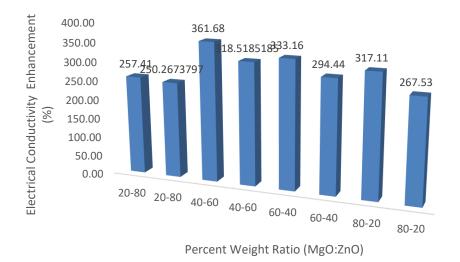


Figure 5.33. Electrical conductivity of MgO-ZnO/DIW BNFs (0.10 vol%) under temperature increase for various PWRs.



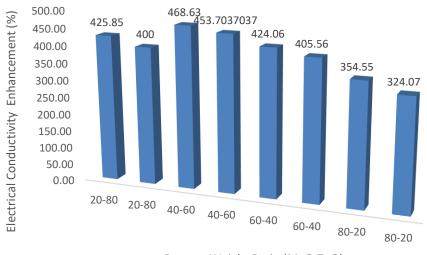


Figure 5.34. Electrical conductivity enhancement (%) for 0.05 vol% BNF.

Percent Weight Ratio (MgO:ZnO)

## Figure 5.35. Electrical conductivity enhancement (%) for 0.10 vol% BNF.

Figures 5.36 and 5.37 illustrates the impact of PWRs on  $\sigma$  of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for rising temperatures. Figure 5.36 reveals that  $\sigma$  rises slightly as MgO's PWRs gradually increase to a maximum value PWR of 40:60 for MgO-ZnO. But the least  $\sigma$  was observed for PWR 20:80, which has the lowest composition of MgO NP for rising temperatures of 20°C to 50°C. Also, Figure 5.37 illustrates  $\sigma$  rising gradually as mixing rates of MgO is enhanced and attained the highest value when PWR of MgO-ZnO is 40:60. But, further increase of MgO NP detracted electrical conductivity, but least  $\sigma$  was observed for the BNF

sample with the maximum composition of MgO NP (80:20) under rising temperature. The nanoparticles' hybridisation was noticed to have a good impact on the BNFs'  $\sigma$ . The difference in  $\sigma$  is enhanced by the differences in  $\varphi$ , temperature, and particle ratios of binary nanoparticles employed to formulate the BNFs.

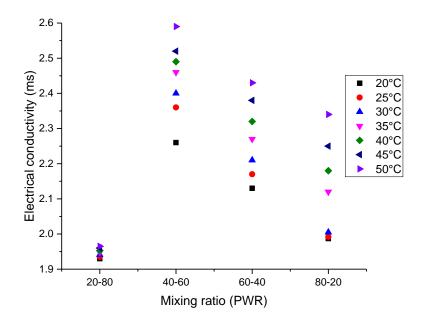


Figure 5.36. Influence of mixing ratio on the electrical conductivity of 0.05 vol% BNF.

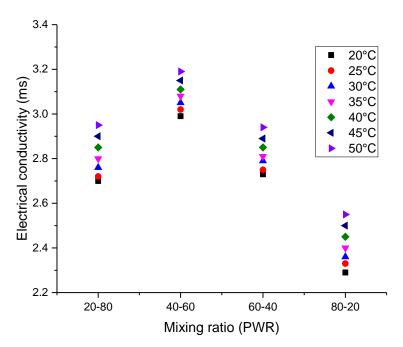


Figure 5.37. Influence of mixing ratio on the electrical conductivity of 0.10 vol% BNF.

### **5.6 DEVELOPMENT OF CORRELATIONS**

The originality of this work handles the inadequacy of documentation of thermal behaviour of MgO-ZnO/DIW binary nanofluids and the use of correlations for engineering design of thermal applications. Advancement in nanofluids research has led to an increased need for model development that will accurately predict thermophysical properties of new nanofluids [35, 39, 64, 66, 96, 181, 232, 577-579]. This work employed the experimental datasets of the studied BNFs' thermal properties (thermal conductivity, electrical conductivity, and viscosity) to develop prediction models. Table 5.1 shows the developed correlations for the three thermal properties as a function of temperature.

	-				
Variable	MgO-ZnO	MgO-ZnO	MgO-ZnO	MgO-ZnO	
	(20:80)	(40:60)-100	(60:40)-	(80:20)	
	Viscosity (MgO – 20 nm)				
$\mu_{BNF}$	$= 1.053 + 4.22 \times 10^{-3}T$	$= 1.070 + 4.23 \times 10^{-3}T$	$= 1.075 + 4.50 \times 10^{-3}T$	$= 1.054 + 4.36 \times 10^{-3}T$	
$\mu_{DIW}$					
		Viscosity (MgO – 1	00 nm)		
$\mu_{BNF}$	$= 1.098 + 4.07 \times 10^{-3}T$	$= 1.117 + 4.08 \times 10^{-3}T$	$= 1.123 + 4.12 \times 10^{-3}T$	$= 1.105 + 4.16 \times 10^{-3}T$	
$\mu_{DIW}$					
		Electrical conductivity (N	/IgO – 20 nm)		
$\sigma_{BNF}$	$= 5.159 - 8.86 \times 10^{-3}T$	$= 5.832 - 1.66 \times 10^{-2}T$	$= 5.43 - 1.03 \times 10^{-3}T$	$= 4.346 - 5.37 \times 10^{-3}T$	
$\sigma_{DIW}$					
_		Electrical conductivity (M	8		
$\sigma_{BNF}$	$= 5.568 - 1.5 \times 10^{-2}T$	$= 6.309 - 9.55 \times 10^{-3}T$	$= 6.168 - 2.02 \times 10^{-2}T$	$= 4.686 - 1.35 \times 10^{-2}T$	
$\sigma_{DIW}$					
		Thermal conductivity (N			
$\kappa_{BNF}$	$= 1.038 + 7.26 \times 10^{-4}T$	$= 1.093 + 5.78 \times 10^{-4}T$	$= 1.065 + 7.90 \times 10^{-4}T$	$= 1.052 + 6.97 \times 10^{-4}T$	
$\kappa_{DIW}$					
	2	Thermal conductivity (M	0	2	
$\kappa_{BNF}$	$= 1.118 + 1.50 \times 10^{-3}T$	$= 1.079 + 9.93 \times 10^{-3}T$	$= 1.058 + 1.09 \times 10^{-2}T$	$= 1.053 + 9.76 \times 10^{-3}T$	
$\kappa_{DIW}$					
K		Thermal conductivity (M			
$\kappa_{BNF}$	$= 1.097 + 4.65 \times 10^{-4}T$	$= 1.137 + 5.07 \times 10^{-4}T$	$= 1.132 + 5.13 \times 10^{-4}T$	$= 1.099 + 6.91 \times 10^{-4}T$	
$\kappa_{DIW}$					

 Table 5.1.
 Developed correlations for 0.10 vol% BNFs

For the developed relative viscosity correlations,  $R^2$  and average absolute deviation (AAD) results of 94.93%–98.80% and 0.1558% –0.4682% (20 nm-MgO based binary NFs) and 91.10%–98.54% and 0.1836%–1.0582% (100 nm-MgO based binary nanofluids), respectively, were achieved. For developed correlations for electrical conductivity, predicted performance and AAD of 98.77% –99.83% and 0.0903% – 0.1763% (20 nm-MgO based binary nanofluids) and 98.17% –99.91% and 0.0565%–0.5281% (100 nm-MgO based binary nanofluids)

respectively, were achieved. Finally, the prediction accuracy and AAD of 97.85% - 99.00% and 0.1084% –0.1387% for 20 nm-MgO based binary nanofluids, and 98.29% - 99.66% and 0.0681% –0.1534% for 100 nm-MgO based BNFs, respectively, were obtained for correlations related to thermal conductivity.

Figures 5.38 – 5.40 compare fitted correlations of the studied thermal conductivity, viscosity, and electrical conductivity with existing published correlations. Figure 5.38 presents the proposed correlations of Sundar et al. [270] and Giwa et al. [96] for predicting the electrical conductivity of BNFs, which was found inadequate to define the electrical conductivity of MgO-ZnO/DIW BNFs (as the highest (40:60 (20 nm and 100 nm)) and least (80:20 (20 nm and 100 nm)) values upon comparison. As presented in Figure 5.39, Zadkhast et al. [349] proposed correlations for thermal conductivity, which was noticed to predict 20:80 finely (20) nm-MgO) BNF with absolute errors of 3.78% and 4.64%, 20:80 (100 nm-MgO) with absolute errors of 0.41 - 0.66%, and 40:60 (100 nm-MgO) for absolute errors of 3.91 - 4.37%. Else, the proposed correlations of Taherialekouli et al. [558] and Esfahani et al. [239] for effective thermal conductivity underpredicted the MgO-ZnO/DIW BNFs (40:60 and 20:80 of 20 nmand 100 nm MgO based NPs) when compared. Also, the developed correlations of Hamid et al. [261], as presented in Figure 5.40, underpredicted the relative viscosity of 60:40 (20 nm-MgO) and 20:80 (100 nm-MgO) binary nanofluids while the correlations of Sundar et al. [580] overestimated them. Then, the proposed correlations of Giwa et al. [96] estimated the 20:80 (20 nm-MgO), 60:40 (20 nm-MgO) and 20:80 (100 nm-MgO) binary nanofluids for absolute errors of 0.15% - 1.40%, 1.19% - 4.10%, and 3.00% - 4.56%, respectively. From Figure 5.41, the fitted correlations for the optimum thermal conductivity (with binary nanofluids with particle weight ratio of 40:60 and MgO nano-sizes of 20, 40, and 100 nm) were compared with those of previous studies, and the latter was observed to underpredict the former.

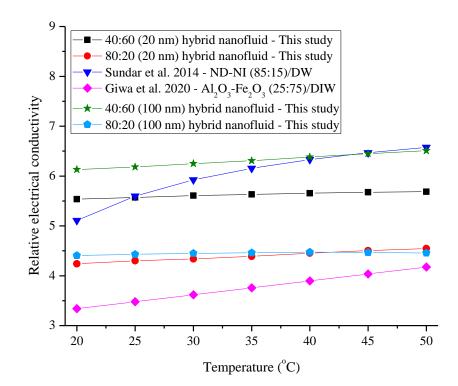


Figure 5.38. Comparing proposed correlations of electrical conductivity of MgO-ZnO/DIW BNFs with existing correlations as a function of temperature.

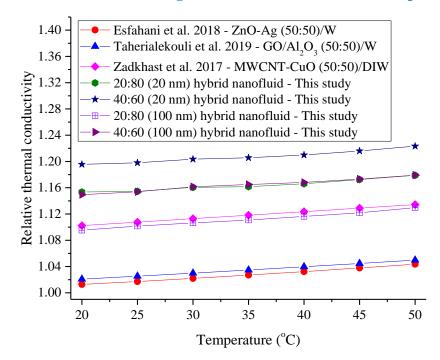
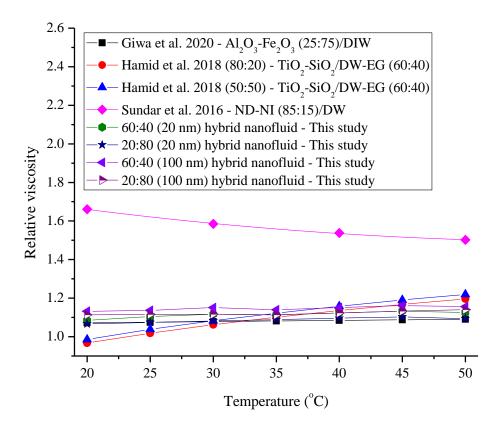
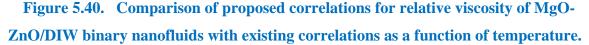


Figure 5.39. Comparing proposed correlations of relative thermal conductivity of MgO-ZnO/DIW binary nanofluids with existing correlations as a function of temperature.





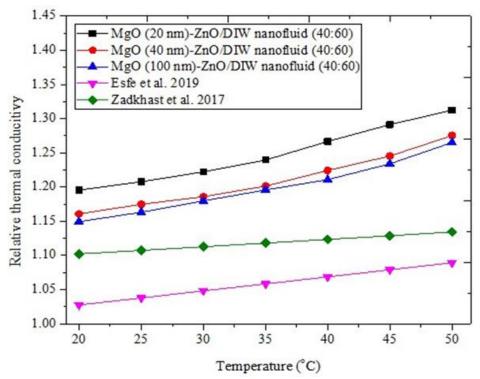


Figure 5.41. Comparison of obtained thermal conductivity correlations in this present study with proposed correlations in literature.

The facts above developed correlations with good prediction ability and of essence. Since different types of nanoparticles, particle ratio of nanoparticles, size of nanoparticles, temperature, basefluid, etc., influence the thermal conductivity of binary nanofluids, the need to propose unique correlations of experimental data of thermal properties related to different nanofluids is very crucial [145, 227, 366, 554, 581-583].

## 5.7 THERMOELECTRICAL CONDUCTIVITY RELATIONS

The thermoelectrical conductivity (TEC) relation between the  $\sigma$  and  $\kappa$  is essentially useful in selecting an optimized BNFs to be used in an electrically active system for thermal applications. Figures 5.42 and 5.43 illustrate BNFs' TEC with different volume concentrations and PWRs under increasing temperatures. The effective decision for selecting BNFs as thermal fluids is a function of the TEC value. BNFs of 0.05 vol% were observed to have higher TEC values than that of 0.10 vol% BNFs (Figures 5.42 and 5.43). Also noticed is that an increment in temperature reduced the TEC values for both volume concentrations, which falls in agreement with the literature [21, 84, 274, 278, 584]. Therefore, the BNFs samples investigated in this work under studied temperature were suitable for thermal application considering the calculated TEC results.

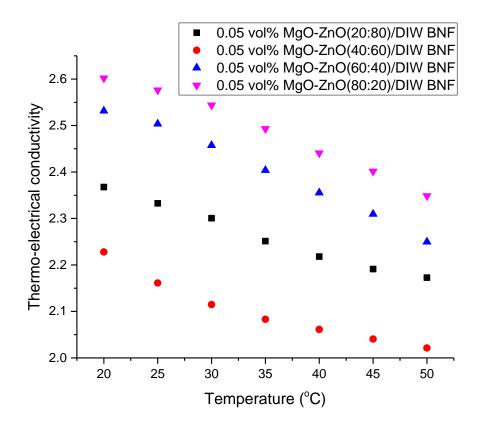


Figure 5.42. Thermoelectrical conductivity values for 0.05 vol% BNFs.

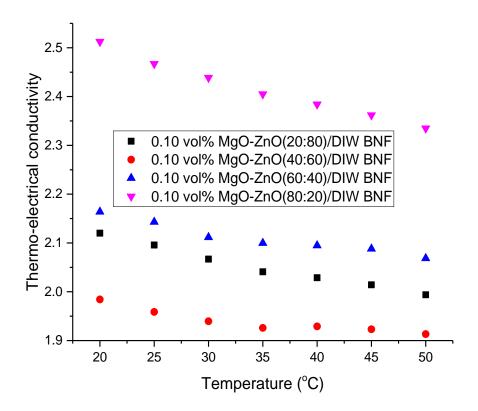


Figure 5.43. Thermoelectrical conductivity values for 0.10 vol% BNFs.

#### **5.8 PROPERTIES ENHANCEMENT RATIO**

Property enhancement ratio (PER) is a factor employed to determine the convective heat transfer behaviour of nanofluids for laminar flow within thermal applications [540]. This is based on nanofluids' augmentation capability of thermal conductivity and viscosity. So, PER is the relationship existing between the enhancement of thermal conductivity and viscosity enhancement as presented in Equation 5.1.

$$PER = \frac{C_{\mu}}{C_{\kappa}} = \frac{\mu_r - 1}{\kappa_r - 1} \le 4$$
5.1

Where:  $C_{\mu}$ ,  $C_{\kappa}$ ,  $\kappa_r$ , and  $\mu_r$  were effective viscosity enhancement, effective thermal conductivity enhancement, relative thermal conductivity, and relative viscosity, respectively.

Figures 5.44 and 5.45 give the PER of 20 nm- and 100 nm-MgO based binary nanofluids (0.1 vol.%), which reduced with enhancement in temperature. It can be observed in the Figures that as the temperature rises, PER is enhanced. For 20 nm-MgO based BNFs, lowest and highest PER values are 0.38 - 0.57 (for 40:60) and 0.44 - 0.65 (for 60:40), while 0.81 - 0.97 (40:60) and 1.17 - 1.22 (for 20:80) were reported for the 100 nm-MgO based BNFs, respectively. Prasher et al. [540] posited that binary nanofluids are considered useful as thermal fluids when the thermal conductivity improvement is 4-fold more or equal to the enhancement of viscosity. Figures 5.44 and 5.45 further posits that all BNFs samples were below PER of 4 and thus beneficial as thermal fluids (up to 50 °C) for thermal applications subject to further investigation on the convective heat transfer performance. Related results were reported by Akilu et al. [98] for EG-based SiC-CuO/C (4:1) binary nanofluids and Hamid et al. [261] for TiO<sub>2</sub>-SiO<sub>2</sub> (20:80 – 80:20)/DW-EG binary nanofluids.

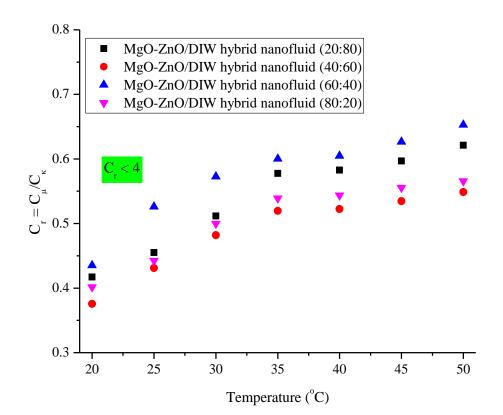


Figure 5.44. PER of MgO (20 nm) based binary nanofluids (0.1 vol.%) with temperature increase.

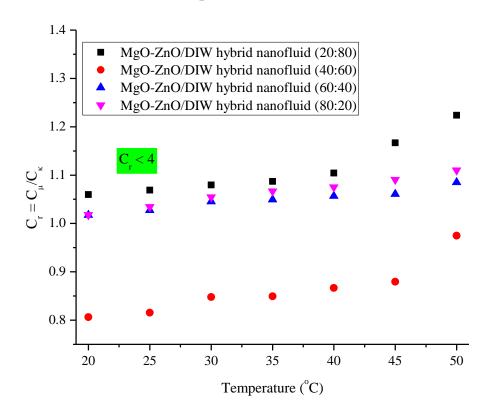


Figure 5.45. PER of MgO (100 nm) based binary nanofluids (0.1 vol.%) with temperature increase.

#### **5.9 CONCLUSION**

In this experimental investigation, the thermal conductivity ( $\kappa$ ), pH, viscosity ( $\mu$ ) and electrical conductivity ( $\sigma$ ) of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) were successfully studied for PWR of 20:80, 40:60, 60:40, 80:20 (MgO:ZnO) at temperatures gradients of 20 to 50°C. The  $\kappa$  of the BNFs for all PWR was augmented under the influence of increasing temperature as compared to DIW. The highest  $\kappa$  enhancement of 5.60% and 22.07% relative to the basefluid was obtained at 0.05 and 0.10 vol.%, respectively, which shows that the dispersion of MgO-ZnO NPs enhances  $\kappa$  greatly, especially at higher temperatures. Also, the pH of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for all mixing ratios reflects a steady decline as temperature increases. The BNFs possessed pH values more than 7, thus formulating an alkaline fluid. It was observed that temperature greatly influenced the pH of the BNFs, then volume concentration and finally PWR. pH enhancements of 27.04% to 40.74% and 30.20% to 39.59% were achieved for BNFs (at  $\varphi$  of 0.05 and 0.1 vol%, respectively) at different PWRs for temperature ranges of 20–50 °C. Then, the BNFs' electrical conductivity ( $\sigma$ ) for all the PWR was slightly enhanced under the influence of increasing temperature. Dispersing hybrid NPs into DIW significantly improved the  $\sigma$  of DIW. Maximum enhancement of 21.82% and 30.91% were observed for 0.05 and 0.1 vol%, respectively. In addition, the viscosity ( $\mu$ ) of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) as temperature improves gradually exhibited a detracting trend for all nanohybrids and basefluid. Thus, it was deduced that using 0.05 vol% to formulate the BNFs led to reduced  $\mu$  values, while an increase to 0.1 vol% produced enhanced  $\mu$  values for its BNFs. The difference in MgO-ZnO NPs mixing ratio led to variation in  $\mu$  for the BNFs for temperatures examined. The effective criteria in selecting BNFs for thermal applications is a function of the TEC value. It was observed that BNFs of 0.05 vol% were observed to have higher TEC values than that of 0.10 vol% BNFs. Also noticed is that an increment in temperature reduced the TEC values for both volume concentrations. The BNFs samples investigated in this work under the studied temperature range are suitable for thermal application. The PER revealed that at 0.10 vol.% and temperature of 20 - 50 °C, all binary nanofluids are applicable for thermal cooling purposes. The 40:60 binary nanofluids happens to be suitable sample with minimum viscosity and maximum thermal conductivity which was beneficial to engineering use. Using the experimental results, correlations were proposed to estimate the studied BNFs' thermophysical properties.

# CHAPTER 6 THERMO-CONVECTION PERFORMANCE OF BINARY NANOFLUIDS<sup>1</sup>

## **6.1 INTRODUCTION**

This chapter experimentally examined the natural convection performance of MgO-ZnO nano-particles suspended in DIW for volume concentrations of 0.05 and 0.10 vol% for PWRs of 20:80, 40:60, 60:40, 80:20 (MgO:ZnO) charged inside a square enclosure. The temperature profile of the cavity when filled with samples of DIW under varying  $\Delta T$  was presented. This involved the temperatures at the centre and heated walls of the cavity. The thermo-convection behaviour of the binary nanofluid samples for parameters such as *Ra*, *Nu*<sub>av</sub>, *h*<sub>av</sub>, and *Q*<sub>av</sub> at various temperature range (20°C to 50°C) were studied and duly reported. A new model linked to volume concentration ( $\varphi$ ) and percent weight ratios were introduced to predict *Nu*<sub>av</sub>.

# **6.2 CAVITY VALIDATION**

For the validation of the performance of the square cavity employed in the thermo-convection experiment, the measured Nusselt number (*Nu*) dataset for basefluid (DIW) were compared with published numerical models for thermo-convection [25, 161, 325, 543-545, 585]. Figure 6.1 shows the validation of the squared cavity using basefluid (DIW), by way of illustrating *Nu* plotted with Rayleigh number (*Ra*) for basefluid, with experimental values and published models. At *Ra* of  $8.05 \times 10^8$ , it is observed that the experimental Nusselt number dataset was minimum in comparison to the forecasted dataset by the correlations. This is indicative that the correlation predicts the experimental dataset accurately.

This chapter has been published in part as:

<sup>&</sup>lt;sup>1</sup>Nwaokocha, C., Momin, M., Giwa S., Sharifpur, M., Murshed S.M.S., Meyer, J.P., *Experimental investigation of thermo-convection behaviour of aqueous binary nanofluids of MgO–ZnO in a square cavity.* Thermal Science and Engineering Progress, 2022, **28**: 101057.

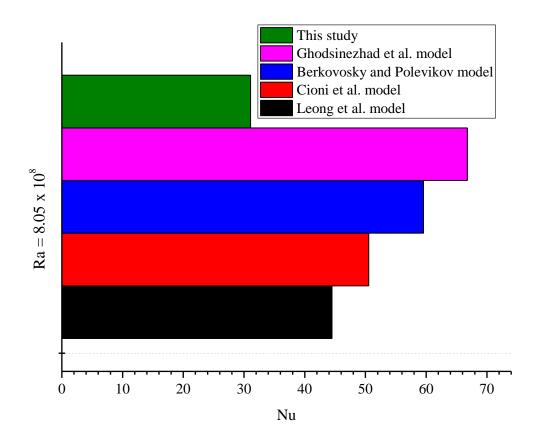


Figure 6.1: Comparison of measured *Nu* of MgO-ZnO/DIW BNFs with the proposed correlations of Leong et al. [545], Cioni et al. [544], Berkovosky and Polovikoy [543] and Ghodsinezhad et al. [25].

## **6.3 THERMAL TRANSPORT PERFROMANCE**

The performance of the thermal transport for various PWRs of MgO–ZnO/DIW binary nanofluids for 0.05 vol% and 0.10 vol.% charged in a squared cavity under the influence of temperature change was examined. Temperatures were measured using thermocouples at various locations within and without the square enclosure. Figure 6.2 presents the influence of *Ra* on *Nu*<sub>av</sub> for various  $\varphi$  and different  $\Delta T$  for the DIW and BNF. As *Ra* augments, *Nu*<sub>av</sub> rises for all BNF samples, with basefluid possessing the highest *Ra* value over BNF, which agrees with Giwa et al. [28] and Sharifpur et al. [173]. The detraction in the values of *Ra* for all BNFs was due to the suspension of BNPs (MgO and ZnO) in DIW, which improved *Nu* for BNF samples under different  $\Delta T$  than for DIW. As  $\varphi$  increases from 0.05 to 0.1 vol.%, a reduction in *Nu* was observed, as published by Sharifpur et al. [173]. An augmented Ra was observed at rising temperature, with DIW possessing maximum *Ra*. Thus, *Ra*, *Nu*, and  $\Delta$ T were observed to be closely linked, and in agreement with the literature [25, 330, 586, 587], this explains the changes in the thermal property of basefluid as influenced by the dispersion of BNPs in it. Figure 6.2 also presents 0.05 vol% BNF samples that has had the maximum *Nu* values when related with 0.10 vol.% BNF samples, with sample (80:20) attaining the highest *Nu*<sub>av</sub> (53.62) for *Ra* = 4.32 × 10<sup>8</sup> at  $\Delta$ T = 18.09°C. This is seconded by 0.05 vol.% BNFs 40:60 (49.03), 20:80 (48.95), 60:40 (48.57) and trailed by 0.10 vol.% BNF samples 60:40 (40.41), 20:80 (37.77), 80:20 (37.48), 40:60 (37.47), in that order and finally, the basefluid (DIW). The *Nu* values differ from the result of Sharifpur et al. [173], which difference could be attributed to the various *Ra* ranges for all PWRs and both experiments.

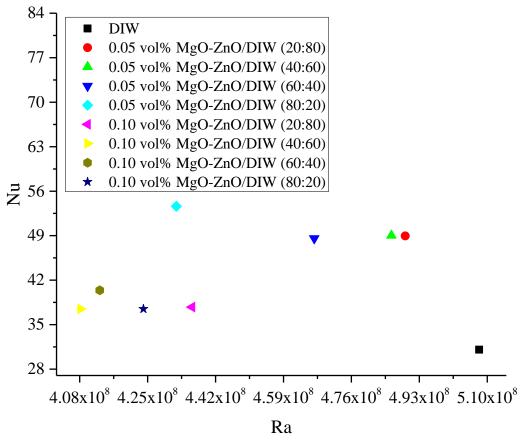
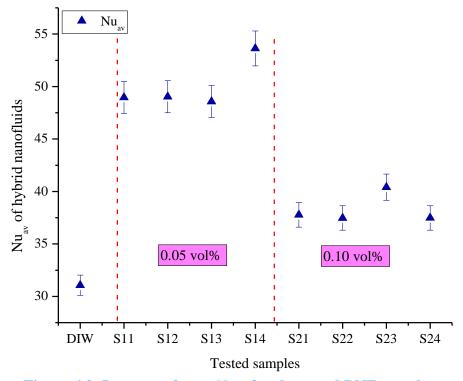


Figure 6.2: The impact of Ra on  $Nu_{av}$  at various  $\varphi$ .

Figure 6.3 presents the impact of  $\Delta T$  and  $\varphi$  on the *Nu*<sub>av</sub> for studied samples. For rising  $\Delta T$ , an undeviating influence was observed for *Nu*<sub>av</sub> by way of enhancement, but otherwise, as  $\varphi$  enhances, it improves for 0.05 vol.% and detracts for 0.10 vol.%. When related to DIW, an augmented *Nu*<sub>av</sub> of 56.33% - 72.60% for 0.05 vol.% BNFs was observed detracted by 20.61% - 30.08% for 0.10 vol.% BNFs. The highest augmentation (72.60%) of *Nu*<sub>av</sub> was attained in the investigation, which was over 8.42% highest enhancement published by Sharifpur et al. [173] when compared to basefluid, supports thermo-convection enhancement when binary nanofluids are employed for thermo-convection studies. Table 6.1 illustrates the contents of the tested samples. It is reported that effective viscosity of BNF was enhanced with increase in  $\varphi$ , giving room for buoyant forces in the square enclosure to be reduced at the highest concentration of the BNPs due to enhanced viscosity. An increase in  $\varphi$  results in improved thermal conductivity and enhanced viscosity of binary nanofluids at maximum  $\varphi$  resulting in the convective flow of binary nanofluids inside the enclosure decreasing. Thus, a detracting *Nu*<sub>av</sub> as  $\varphi$  rises will continue to enhance the viscosity of binary nanofluids.



**Figure 6.3: Impact** of  $\varphi$  on  $Nu_{av}$  for the tested BNF samples.

<b>Tested samples</b>	0.05 vol.%	0.10 vol.%
MgO-ZnO (20:80)	S11	S21
MgO-ZnO (40:60)	S12	<b>S</b> 22
MgO-ZnO (60:40)	<b>S</b> 13	S23
MgO-ZnO (80:20)	S14	S24

**Table 6.1. Tested BNF samples** 

The experimental dataset of *Ra*, *Nu*<sub>av</sub> and PWR (*R*) was employed to propose a model as presented in Equation 6.1, such that *Nu*<sub>av</sub> was estimated from  $\varphi$  and *R* with good precision. Published models for predicting *Nu*<sub>av</sub> of nanofluid's performance in different enclosures mainly depends on  $\varphi$  and *R*. This is not applicable in the current study [25, 341, 588-593]. A fit of the proposed model is depicted by Figure 6.4.

$$Nu = 0.6184R - 235.24\varphi + 60.81$$
 6.1

The proposed model could predict the experimental dataset with a margin of deviation (MOD) of -5.74% to 5.75%. So, Figure 6.4 illustrates the relationship amidst the experimental and predicted *Nu*<sub>av</sub> results.

Figure 6.5 illustrates the results of the impact of  $\Delta T$  and  $\varphi$  on  $h_{av}$  for the studied BNFs in the investigation. <u>*h*</u><sub>av</sub> was enhanced with rising temperature difference and the use of binary nanofluids. Still, the situation changed when  $\varphi$  was enhanced as 0.05 vol.% rises to 0.10 vol%. Figure 6.5 further explains that the *h*<sub>av</sub> of the binary nanofluids peaked for 0.05 vol.% BNF samples S11 to S14 and detracted for 0.10 vol.% samples S21 to S24, this is a clear indication of the effect of PWR and  $\varphi$  of the BNPs playing key roles in each *h*<sub>av</sub> values [562, 585, 593]. For 0.05 vol.% BNFs, *h*<sub>av</sub> of basefluid was enhanced by 61.28%, 61.79%, 60.33% and 76.01% for samples S11 (20:80), S12 (40:60), S13 (60:40), and S14 (80:20), while 0.10 vol.% samples S21 (20:80), S22 (40:60), S23 (60:40), and S24 (80:20). The detraction in the augmentation of *h*<sub>av</sub>

for 0.10 vol.% binary nanofluids can be related to improved viscosity for this concentration, which reduced the convective heat transfer within the enclosure and eventually detracted  $h_{av}$  values. The highest  $h_{av}$  improvement attained in the experiment was over 25.6% enhancement reported by Suganthi and Rajan [594], who examined free convection of ZnO/PG nanofluid at 2.0 vol.% in a cylinder enclosure. The big difference can be related to the use of BNPs, basefluid,  $\varphi$  and cavity type. In some rectangular enclosures, Ho *et al.* [336] reported an improvement of 18% for  $h_{av}$  for Al<sub>2</sub>O<sub>3</sub>/DIW nanofluid at 0.10 vol.%; Ghodsinezhad et al. [25] published the highest enhancement of 15% for  $h_{av}$  for Al<sub>2</sub>O<sub>3</sub>/DIW NF; and Giwa et al. [329] achieved 19.4% as a maximum enhancement for  $h_{av}$  for Al<sub>2</sub>O<sub>3</sub>-MWCNT/DIW BNF (90:10 weight ratio) at 0.10 vol.%.

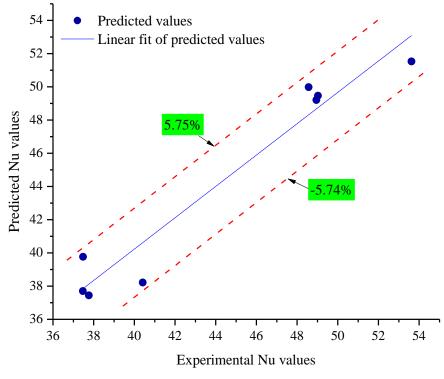


Figure 6.4: Fit of the developed model to predict Nu.

Analyzing the free convection thermal transfer capability of binary nanofluids within the enclosure, the  $Q_{av}$  as a relation of  $\varphi$  at different PWR and  $\Delta T$  were investigated and illustrated as Figure 6.6. Figure 6.7 presents the quantity of heat transferred by the studied samples across

the enclosure as a factor of various  $\varphi$ , PWR and  $\Delta$ T. As the same pattern recorded for *Ra*, *Nu*<sub>av</sub> and *h*<sub>av</sub> was replicated for *Q*<sub>av</sub>, obvious that an enhanced *Q*<sub>av</sub> is a function of PWRs of BNPs in the binary nanofluid and  $\Delta$ T. So, an augmentation of  $\varphi$  for binary nanofluids was observed to both augment and decrease *Q*<sub>av</sub> for all BNF samples [562, 585, 593]. Figure 6.8 also presents a steady maximum improvement for 0.05 vol% binary nanofluid samples more than 0.10 vol.% binary nanofluid samples. The highest augmentation achieved was for 0.05 vol% binary nanofluid sample S12 (40:60) by 72.20% in relation to the basefluid. Sharifpur et al. [173] reported a *Q*<sub>av</sub> enhancement of 6.75% at 0.10 vol% for ZnO/DIW nanofluid square enclosure. Also, Suganthi and Rajan [594] published *Q*<sub>av</sub> augmentation of 4.24% at 2.0 vol% inside a cylindrical enclosure. Using a rectangular enclosure, Garbadeen et al. [27] recorded a 45% enhancement for *Q*<sub>av</sub> for MWCNT/DIW nanofluid for 0.10 vol%, while Giwa et al. [329] published 9.80% for Al<sub>2</sub>O<sub>3</sub>-MWCNT/DIW BNF for 0.10 vol.%.

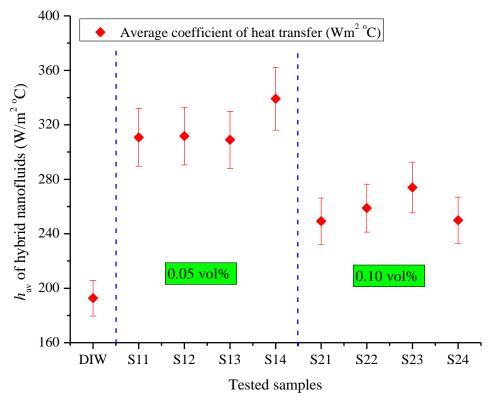


Figure 6.5: Effect of  $\varphi$  on  $h_{av}$  for the tested samples.

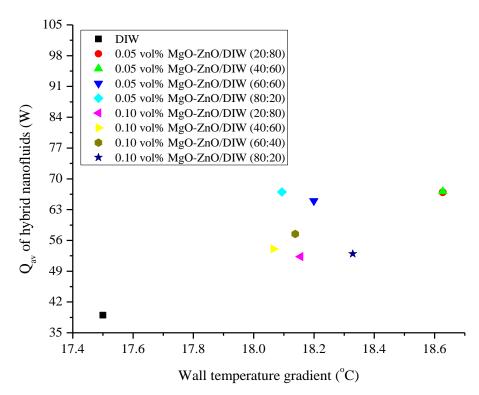


Figure 6.6:  $Q_{av}$  versus  $\phi$  at different wall temperature ranges.

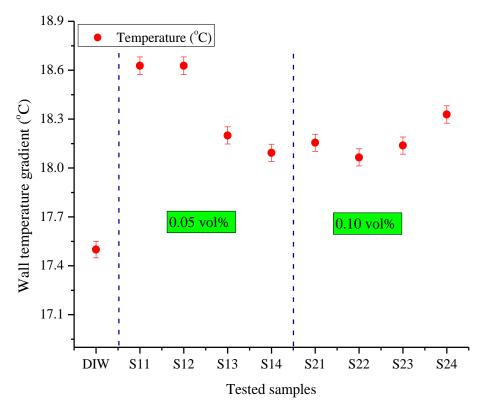


Figure 6.7: Effect of  $\phi$  on wall temperature gradients on the tested samples.

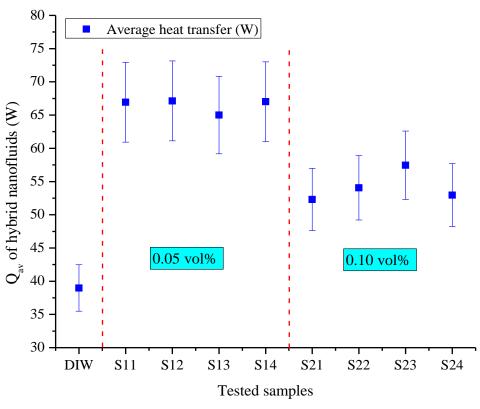


Figure 6.8: Effect of  $\varphi$  on  $Q_{av}$  on the tested BNF samples.

# 6.4 CAVITY TEMPERATURE DISTRIBUTION

The heat transfer investigation was done within uniform thermal conditions and measured temperatures with thermocouples at specific locations inside and outer side of the enclosure, as explained before now. The mean temperature of the basefluid and tested BNF samples under the effect of  $\varphi$  is illustrated in Figure 6.9. Figures 6.10 and 6.11 presents the temperature distribution profile across the hot side, cold side and the inner section of the cavity for all tested samples (basefluid and BNFs) under various temperature change and volume concentrations [562, 585, 592, 593, 595].

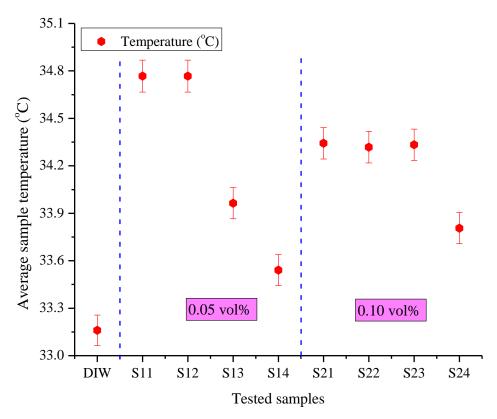


Figure 6.9: Effect of φ on temperatures of the tested BNF samples.

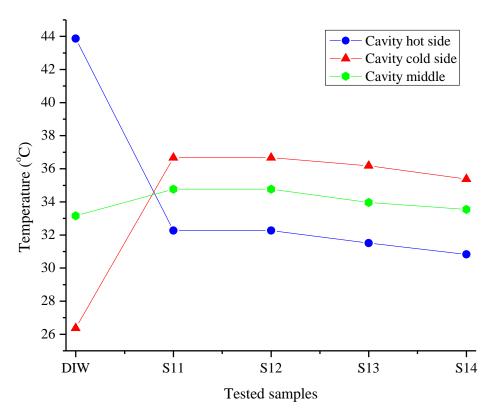


Figure 6.10: Cavity temperature profile for DIW and the tested BNF samples for 0.05 vol.%.

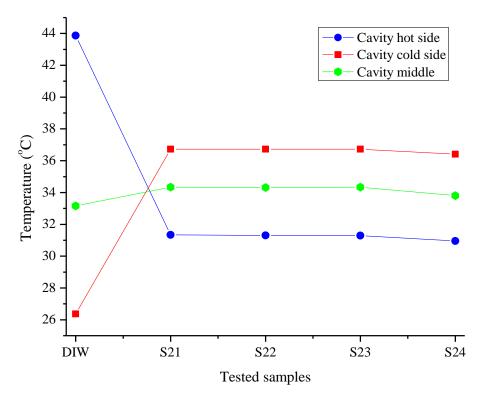


Figure 6.11: Cavity temperature profile for DIW and the tested BNF samples for 0.10 vol.%.

#### **6.5 CONCLUSION**

The natural convection behaviour of DIW and BNFs within a squared enclosure was conducted under various temperature change and estimated using four parameters:  $Nu_{av}$ , Ra,  $h_{av}$ , and  $Q_{av}$ . Stable binary nanofluids (0.05 vol.% and 0.10 vol%) were formulated and thermophysical properties (thermal conductivity and viscosity) were measured at temperature 20 - 50°C. The temperature distribution profile of the enclosure for the BNF samples employed in the investigation was discussed. Also, for all studied samples, a rise in temperature difference impacted an equivalent improvement for Ra,  $Nu_{av}$ ,  $h_{av}$ , and  $Q_{av}$ . For this investigation,  $Nu_{av}$  was observed to have a close relation with  $\varphi$ ,  $\Delta T$ , Ra, and PWRs while  $h_{av}$  and  $Q_{av}$  were functions of  $\varphi$ ,  $\Delta T$ , and PWRs for all studied samples. Maximum Ra was achieved as related to open literature for natural convection of nanofluids in enclosures. Optimal  $Nu_{av}$  attained is 53.62 for  $Ra = 4.32 \times 10^8$  at  $\Delta T = 18.09$  °C. Also, highest augmentation attained were 72.60% ( $Nu_{av}$ ), 76.01% ( $h_{av}$ ), and 72.20% ( $Q_{av}$ ). This study present the hybridisation of ZnO and MgO nanoparticles into basefluid to prepare the binary nanofluid enhanced the thermal-fluid behaviour of basefluid, which helped the free convection behaviour of the binary nanofluid within a squared enclosure. The innovative results also support the benefit of using binary nanofluids over nanofluids. In conclusion, the application of suitably experimentally achieved models of experimental dataset for getting thermal properties is central to an experimental investigation of free convection heat transfer of BNF in enclosures.

## CHAPTER 7 DEVELOPMENT OF ARTIFICIAL INTELLIGENCE MODELS TO PREDICT THERMAL CONDUCTIVITY OF BINARY NANOFLUIDS<sup>1,2,3</sup>

#### 7.1 INTRODUCTION

Open literature confirms studies conducted related to experimental measurement of the thermal conductivity of different binary nanofluids with and without the development of empirical correlations to estimate the thermal conductivity, and modelling of the thermal conductivity using curve fitting via regression analysis and machine learning tools to develop empirical correlations to predict the same [72, 96, 141, 155, 368, 370-372, 596, 597]. The use of machine learning tools such as an Artificial neural network (ANN), Group method of data handling (GMDH), curve fitting, decision tree, dimensional analysis, random forest, generic algorithm, support vector machine, Adaptive Neuro-Fuzzy Inference System (ANFIS), Least squares support vector machine (LSSVM), etc. Their hybrids have been reported in the literature [66, 82, 96, 174, 248, 249, 368, 371, 596, 598]. This is due to the cost and complex nature of the experimental measurement of thermal properties of nanofluids. So, to limit the cost and time of experiments, researchers and scientists adopted the idea of developing models and correlations using the above-mentioned machine learning methods. Obtained artificial neural network (ANN) results were presented.

This chapter is reflected in parts in the following papers:

<sup>&</sup>lt;sup>1</sup>Nwaokocha, C., Giwa S., Ghorbani B., Momin, M., Sharifpur, M., Gharzvini M., Chamkha, A.J., Meyer, J.P., *Experimental formulation and GMDH modelling of thermal conductivity of MgO–ZnO/deionised water hybrid nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>2</sup>Nwaokocha, C., Momin, M., Sharifpur, M. and Meyer, J., *Artificial neural network development to predict thermal conductivity of MgO–ZnO/Deionised Water binary nanofluids*. Ready for submission.

<sup>&</sup>lt;sup>3</sup>Nwaokocha, C., Sharifpur, M. and Meyer, J., *Application of binary nanofluids – Emerging issues*. Ready for submission.

## 7.2 ARTIFICIAL NEURAL NETWORK MODEL TO PREDICT THERMAL CONDUCTIVITY OF BINARY NANOFLUIDS

Using the ANN method in MATLAB R2021a software, experimental data sets were classified as training, validation and testing on a random basis. The training data generates biases and masses for the testing, the validation data was used to modify the masses during training session, while the test data sets were used to determine the performance of the neural network. For this work, an optimized ANN to predict  $k_{\text{bnf}}$  was determined by comparing the performances of the varied neuron numbers within the inner layers, then finally using the best neuron number. This was done by modifying the ANN architecture to determine the optimized neuron number. The suggested learning algorithm is presented as Figure 7.1.

Using the proposed learning algorithm, eight hundred (800) experimental data set were obtained from the experimental thermal conductivity measurements of MgO-ZnO/DIW BNFs, which was classified as 560 (70%) data points for training, 120 (15%) data sets for validation and 120 (15%) data points for testing purpose. The performance values for the training, validation and testing were sorted in neuron number order and presented in Table 7.1. The loop worked using 6 to 23 neurons, simulating for 27 iterations, with the optimized network was finally selected based on performance. The best network was at neuron 19 due to having the best performance, as depicted in Figure 7.2. Table 7.2 presents the correlation existing amidst data inputs and output results for varying neuron numbers. As the values approach 1, a perfect positive correlation is established, meaning the target data and predicted values are related. The train, validating and testing figures of ANN are presented in Figures 7.3 to 7.6, which depicts that they are finely predicted by the ANN. Figure 7.6 shows that the neural network will predict the  $\kappa bmf$  for various temperatures, nanosizes, PWR and volume concentration.

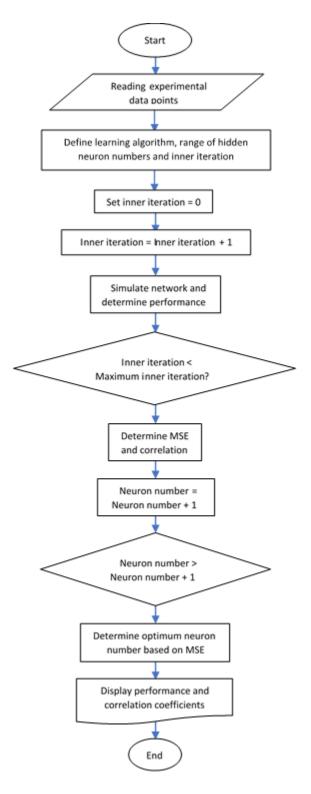


Figure 7.1. Proposed learning algorithm to determine optimized ANN.

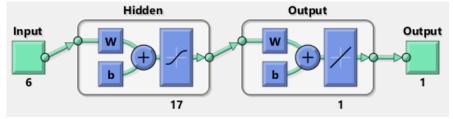


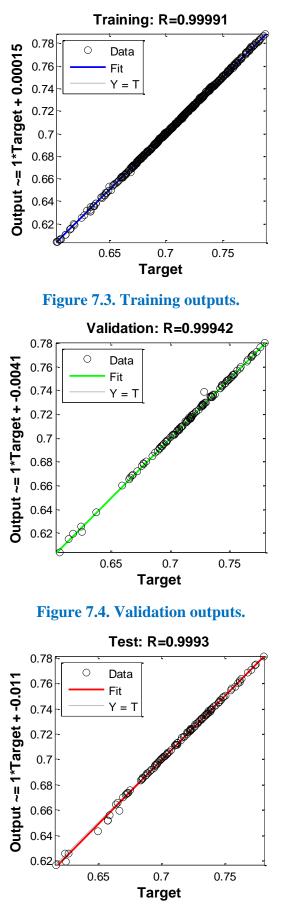
Figure 7.2. The optimized ANN.

		-		
Neuron	Overall	Train	Validation	Test
number	performance	performance	performance	performance
19	2.18000E-07	2.40267E-07	1.40680E-06	1.89317E-06
20	3.96000E-07	4.45651E-07	1.49020E-06	1.78486E-06
21	4.32000E-07	4.57133E-07	4.28085E-06	1.89977E-06
23	5.59000E-07	7.55047E-07	1.71477E-06	1.52975E-06
15	6.05000E-07	6.12132E-07	1.07121E-06	6.82498E-06
22	7.25000E-07	8.09382E-07	1.00912E-06	1.71285E-06
14	7.45000E-07	7.95710E-07	3.56513E-06	3.73645E-06
9	7.53000E-07	8.57089E-07	9.88912E-07	1.88241E-06
17	7.65000E-07	8.35581E-07	7.92507E-07	1.68368E-06
12	7.91000E-07	7.98940E-07	2.51440E-06	1.29637E-06
18	8.60000E-07	1.27263E-06	2.56084E-06	2.46100E-06
16	9.47000E-07	9.82306E-07	2.28093E-06	1.21286E-06
13	9.83000E-07	1.00320E-06	1.05626E-06	1.48523E-06
11	1.30000E-06	1.61032E-06	3.29324E-06	2.82686E-06
8	1.31000E-06	1.33776E-06	4.20892E-06	1.08940E-06
10	1.54000E-06	1.66113E-06	3.35907E-07	1.91464E-06
7	1.63000E-06	2.17039E-06	3.17441E-06	4.51185E-06
6	2.36000E-06	2.42394E-06	2.56614E-06	3.60712E-06

### Table 7.1. ANN performances.

## Table 7.2. Correlation coefficients of data sets for varying neuron numbers.

				0
Neuron numbers	All	Training	Validation	Testing
19	0.99974	0.99991	0.99942	0.99930
20	0.99968	0.99983	0.99931	0.99933
21	0.99974	0.99981	0.99983	0.99937
23	0.99961	0.99969	0.99935	0.99956
15	0.99973	0.99976	0.99948	0.99977
22	0.99962	0.99968	0.99962	0.99935
14	0.99935	0.99969	0.99859	0.99857
9	0.99960	0.99966	0.99958	0.99933
17	0.99962	0.99967	0.99969	0.99936
12	0.99955	0.99966	0.99926	0.99946
18	0.99935	0.99949	0.99902	0.99918
16	0.99952	0.99963	0.99913	0.99943
13	0.99957	0.99960	0.99956	0.99947
11	0.99921	0.99936	0.99889	0.99892
8	0.99932	0.99946	0.99850	0.99957
10	0.99923	0.99936	0.99896	0.99894
7	0.99895	0.99913	0.99887	0.99832
6	0.99897	0.99906	0.99888	0.99872



**Figure 7.5. Testing outputs.** 

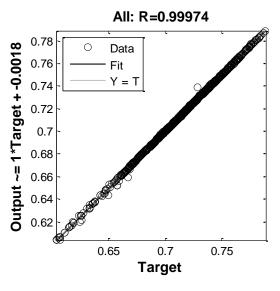


Figure 7.6. All outputs.

Figure 7.7 presents the error histogram, which projects the error rates for data received at the train, verification and testing stages of the ANN. This is used to estimate error values of the designed ANN and found to be low, as the error distribution was loaded around the zero-error line, which confirms that the developed ANN using MLP model will predict the thermal conductivity of MgO-ZnO/DIW BNFs with the required accuracy. Figure 7.8 presents the variation patterns amidst tentative results and ANN outcomes for experimental thermal conductivity outcomes of MgO-ZnO/DIW HNFs in terms of Epochs (presented on the horizontal axis) versus MSE (indicated on the vertical axis). The MSE values were high ab initio and thereafter decreased gradually with increasing epochs until an optimized MSE value of 1.4068e-6 just after 21 iterations was reached, as shown in the small green circle in the Figure. The graph's pattern signified a well-designed training phase for the ANN model.

## 7.3 SURFACE FITTING METHOD TO PREDICT THERMAL CONDUCTIVITY OF BINARY NANOFLUIDS

Here, the fitting method is used to predict the behaviour of BNFs so that *x* represents  $\varphi$  (vol.%) and *y* presents temperature. Using polynomials for the input data points (*x*,*y*), a fitted surface

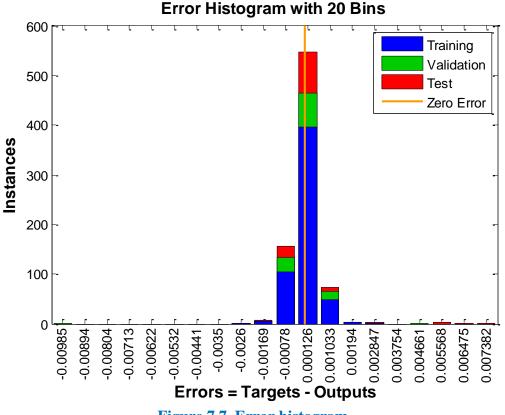
was produced for  $k_{bnf}$  as presented in Equation 7.1 and Figure 7.9. Table 7.3 depicts the surface coefficients.

$$k_{\text{bnf}}(\mathbf{x}, \mathbf{y}) = P00 + (P10 \times x) + (P01 \times \mathbf{y}) + (P20 \times x^2) + (P11 \times x\mathbf{y}) + (P02 \times \mathbf{y}^2)$$
7.1

Figure 7.9 revealed a variation in BNFs' behaviour for various temperatures and  $\varphi$ . It depicts an increase for  $k_{\text{bnf}}$  as temperatures and  $\varphi$  increase. It shows that temperature and  $\varphi$  has a direct relationship with  $k_{\text{bnf}}$ .

Table 7.3. Surface coefficients

P00	P10	P01	P20	P11	P02
0.8809	1.301	0.001203	1.868	0.04198	3.378e-05





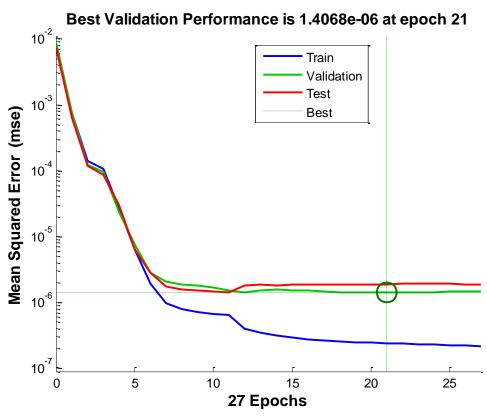


Figure 7.8. Variations of epoch against MSE.

#### 7.4 COMPARING THE RESULTS OF ANN MODEL AND FITTING METHOD

Table 7.4 presents results for the MSE, the maximum absolute value of error, and correlation coefficients of ANN and Surface fitting methods. Correlation coefficients explain the relationship between output and targets for values 1 to -1, where 1 is positive and -1 is negative and zero is nil association among two types of data. The equation to estimate the coefficient of correlation is described as Equation 7.2.

Table	7.4.	<b>Statistical</b>	parameter.
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	ANN	Fitting
Maximum absolute value of error	0.0018	0.2374
Mean Square Error	1.4068e-6	0.01731
Correlation Coefficients	0.99930	0.7662

 $\mathbf{r} = \frac{n \sum xy - (\sum x)(\sum y)}{\sqrt{[\sum x^2 - (\sum x)^2][n \sum y^2 - (\sum y)^2]}}$ 

7.2

where, r is the correlation coefficient, x is target, y is ANN outputs, and n is the number of data points. It is obvious that the ANN method has good performance over the fitting methods [174, 599, 600].

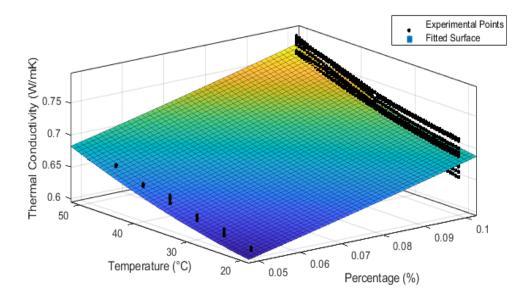


Figure 7.9. *κ*<sub>bnf</sub> versus temperature and φ.

#### 7.5 CONCLUSION

An artificial neural network (ANN) and surface fitting method was employed to predict the *k* of MgO-ZnO/DIW BNFs, using the experimental data sets of *k* for 0.1 vol.% MgO-ZnO/DIW BNFs. In both models, percentage weight ratio (PWR - 20:80, 40:60, 60:40, 80:20 (MgO-ZnO)), nanoparticles sizes (20 nm, 40 nm and 100 nm for MgO NPs and 20 nm for ZnO NPs), temperature (T - 20 to 50 °C) and volume concentration (0.05% and 0.1%) were used as input parameters, and TC obtained as output parameter. A learning algorithm was developed for the ANN model to determine the optimum neuron number. The ANN having 19 neurons in the inner layer got the optimized performance. A surface fitting method was also used on the experimental data, and the generated surface shows the behaviour of the binary nanofluids. The outcome affirmed that the designed ANN model is best for predicting the thermal conductivity of MgO-ZnO/DIW binary nanofluids for various temperatures, nanoparticle sizes, percent weight ratios and volume concentration over the surface fitting method.

# CHAPTER 8 SUMMARY, CONCLUSIONS AND RECOMMENDATIONS

#### 8.1 SUMMARY

The shortcomings in thermal management of energy applications led to the concept of nanosuspension, leading to the formulation of the new class of thermal fluids named nanofluids. The shortcomings range from surface modification, use of conventional fluids, area/volume ratio reduction, miniaturisation, etc. It is established that nanofluids possess enhanced thermal properties when compared to traditional working fluids, thus beneficial for thermo-convention application. The further improvement led to the formulation of binary nanofluids and ternary nanofluids to handle the limitations observed with mono-particle nanofluids. Mono-particle nanofluids and binary nanofluids were formulated using the two-step method. Optimization of parameters (amplitude, dispersion fraction and sonication time) was employed during formulation to allow for repeatability.

Thermo-convection heat transfer has found vast application in engineering applications, thus spurring continuous investigations of free convection heat transfer performance of nanofluids in different enclosure. Numerical methods have gain numbers than experimental studies for thermo-convection heat transfer behaviour using nanofluids in enclosures. To boost the thermo-convection performance of nanofluids in cavities, enhancing methods are cavity inclination, aspect ratio, magnetic stimulus, porous cavity, green base fluids, binary basefluids, green nanofluids, binary nanofluids, and ternary nanofluids.

The use of artificial intelligence models to predict the thermophysical properties of nanofluids is just gaining increase in the public domain, hence the focus of the current study in that direction. Also, the experimental investigation of thermo-convection heat transfer

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augmentation using binary nanofluids is scarce in the public domain, so the current study also focused on it with brilliant contributions.

#### **8.2 CONCLUSIONS**

Chapter 1 of this thesis presented the general introduction of the investigation, thus outlining the study's objectives and scope.

Chapter 2 presented a literature search on nanofluid as an innovative working fluid for thermal management in heat transfer applications. The search entails the formulation and measurement of thermal properties of nanohybrids. The parameters that influence nanohybrids' thermal properties, like basefluid, temperature, nano-shapes, nano-size, volume concentration, were reviewed based on available datasets in the open literature. The morphology and thermo-convection performance of nanohybrids were also reviewed. The use of artificial intelligence models to predict thermal properties were reviewed as well. The Chapter also presented a wide range of recent and future applications of nanofluids with focus on related issues that allow for suitability for industrial applications.

Chapter 3 detailed the experimental methodology needed for the formulation and measurement of thermal properties of nanohybrids (MgO-ZnO/DIW) for percentage weight ratio (PWR -20:80, 40:60, 60:40, 80:20 (MgO-ZnO)), nanoparticles sizes (20 nm, 40 nm and 100 nm for MgO NPs and 20 nm for ZnO NPs), temperature (T - 20 to 50 °C) and volume concentration (0.05% and 0.1%). It entails the process for formulating binary nanofluids, the measurements of thermal properties of binary nanofluids, and the thermo-convection performance of binary nanofluids in a square cavity. The experimental setup for thermo-convection behaviour of nanohybrids in a squared cavity was conducted. The chapter also presented the validation of the cavity and data reduction. Also, model development for thermophysical properties and *Nu*, and the estimation of uncertainty for thermophysical properties and thermo-convection experiments were detailed in this chapter. Artificial intelligence method like ANN was introduced in predicting the thermal properties of MgO-ZnO/DIW binary nanofluids.

Chapter 4 presented the optimum parameters (amplitude, dispersion fraction, pulse used, and sonication time) for formulating mono-particle nanofluids and binary nanofluids. This enables the repeatability of such experiments. This investigation formulated mono-particle nanofluids of MgO and ZnO, for comparison with binary nanofluids of MgO-ZnO/DIW for  $\varphi$  of 0.05 vol.% and 0.1 vol.% via optimized operating parameters leading to a stable BNFs. TEM images detected nanoparticle sizes close to the manufacturers and a good degree of nanosuspension stability. In addition, the stability of BNFs as observed by the absorbance was found stable. Thus stability and morphology are confirmed satisfactory. Hence, further investigation on thermal properties and thermo-convection were done, and results were presented and discussed in subsequent chapters.

Chapter 5 presented the experimental measurement of thermal conductivity ( $\kappa$ ), electrical conductivity ( $\sigma$ ), pH, and viscosity ( $\mu$ ) of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) were successfully studied for PWR of 20:80, 40:60, 60:40, 80:20 (MgO:ZnO) at temperatures gradients of 20 to 50°C. The  $\kappa$  of the BNFs for all PWR was augmented under the influence of increasing temperature as compared to DIW. The highest  $\kappa$  enhancement of 5.60% and 22.07% relative to the basefluid was obtained at 0.05 and 0.10 vol.%, respectively, which shows that the dispersion of MgO-ZnO NPs enhances  $\kappa$  greatly, especially at higher temperatures. Also, the pH of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) for all mixing ratios reflects a steady decline as temperature increases. The BNFs possessed pH values more than 7, thus formulating an alkaline fluid. It was observed that temperature greatly influenced the pH of the BNFs, then volume concentration, and finally PWR. pH enhancements of 27.04% to 40.74% and 30.20% to 39.59% were achieved for BNFs (at  $\varphi$  of 0.05 and 0.1 vol%).

respectively) at different PWRs for temperature ranges of 20–50 °C. Then, the BNFs' electrical conductivity ( $\sigma$ ) for all the PWR was slightly enhanced under the influence of increasing temperature. Dispersing hybrid NPs into DIW significantly improved the  $\sigma$  of DIW. Maximum enhancement of 21.82% and 30.91% were observed for 0.05 and 0.1 vol%, respectively. In addition, the viscosity ( $\mu$ ) of MgO-ZnO/DIW BNFs (0.05 and 0.10 vol%) as temperature improves gradually exhibited a detracting trend for all nanohybrids and basefluid. Thus, it was deduced that using 0.05 vol% to formulate the BNFs led to reduced  $\mu$  values, while an increase to 0.1 vol% produced enhanced  $\mu$  values for its BNFs. The difference in MgO-ZnO NPs mixing ratio led to variation in  $\mu$  for the BNFs for temperatures examined. The effective criteria in selecting BNFs for thermal applications is a function of the TEC value. It was observed that BNFs of 0.05 vol% were observed to have higher TEC values than that of 0.10 vol% BNFs. Also noticed is that an increment in temperature reduced the TEC values for both volume concentrations. The BNFs samples investigated in this work under the studied temperature range are suitable for thermal application. The PER revealed that at 0.10 vol% and temperature 20 - 50 <sup>o</sup>C, all studied binary nanofluids were fine for thermal cooling purposes. The 40:60 binary nanofluids was the best sample with minimum viscosity and maximum thermal conductivity, which is beneficial to engineering application. Using experimental results, correlations were proposed to estimate the studied BNFs' thermophysical properties.

Chapter 6 presented the thermo-convection behaviour of binary nanofluid and basefluid within a squared enclosure was conducted under various temperature differences and estimated using four parameters:  $Nu_{av}$ , Ra,  $h_{av}$ , and  $Q_{av}$ . Stable binary nanofluids (0.05 vol.% and 0.10 vol.%) were formulated and thermophysical properties (thermal conductivity and viscosity) measured at temperature 20–50 °C. The temperature distribution profile of the enclosure for all BNF samples employed in this investigation was presented. In addition, for all the studied samples, a rise in temperature difference impacted an equivalent improvement for Ra,  $Nu_{av}$ ,  $h_{av}$ , and  $Q_{av}$ . For this investigation,  $Nu_{av}$  was observed to possess a close affinity with  $\varphi$ ,  $\Delta T$ , Ra, and PWRs while  $h_{av}$  and  $Q_{av}$  were dependent on  $\varphi$ ,  $\Delta T$ , and PWRs for tested samples. Maximum Ra was achieved in comparison to open literature for free convection of nanofluids in enclosures. Optimal  $Nu_{av}$  attained is 53.62 for  $Ra = 4.32 \times 10^8$  at  $\Delta T = 18.09$  °C. Also, highest improvement attained were 72.60% ( $Nu_{av}$ ), 76.01% ( $h_{av}$ ), and 72.20% ( $Q_{av}$ ). This study showed the hybridisation of ZnO and MgO nanoparticles into basefluid to prepare the binary nanofluid enhanced the thermal-fluid behaviour of basefluid, which supported the free convection behaviour of the binary nanofluid within a squared enclosure. The innovative results also support the benefits of using binary nanofluids more than nanofluids. In conclusion, using appropriate experimentally achieved models of experimental dataset for estimating thermophysical properties is central to an experimental investigation on natural convection heat transfer of a BNF in an enclosure.

Chapter 7 presented the use of artificial intelligence (AI) models to predict thermal properties, based on results of the experimental study. AI methods, like artificial neural network (ANN) and surface fitting method were deployed to model some thermophysical properties of the formulated nanohybrids. For ANN model, a learning algorithm was developed to determine the optimum neuron number. The ANN having 19 neurons in the inner layer got the optimized performance. A surface fitting method was also used on the experimental data and the generated surface shows the behaviour of the binary nanofluids. The outcome affirmed that the designed ANN model is best for predicting the TC of MgO-ZnO/DIW binary nanofluids for different temperatures, nanoparticle sizes, PWRs and volume concentration over the surface fitting method.

#### **8.3 RECOMMENDATIONS**

For future works, the following points were recommended:

- The influence of sonication energy on the thermophysical properties of binary nanofluids.
- The use of machine learning-based approaches for modelling the thermophysical properties of binary nanofluids.
- The use of computational fluid dynamics (CFD) simulation in modelling the thermophysical properties and thermo-convection heat transfer performance of binary nanofluids.
- Experimental studies of thermo-convection heat transfer performance of binary nanofluids in different cavity shapes such as a rectangle and cylinder.
- Experimental studies using green binary nanofluids for measurement of thermophysical properties and thermo-convection heat transfer performance.

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# **APPENDICES**

# A. Weights of NPs and Surfactants

# A.1 Introduction

This section of the appendix presents the estimation of the amounts of nanoparticles and surfactants used to form binary nanofluids (BNFs) samples. The optimum dispersion fractions obtained for the formulation of BNFs were used to estimate the weights of nanoparticles and surfactants. The amounts of nanoparticles employed in the formulation of BNFs depended on  $\varphi$ , nanoparticles percent weight, and types of nanoparticles hybridised.

# A.2 Calculation for Weights of Nanoparticles and Surfactants for BNFs

Nanoparticles of MgO (20 nm and 100 nm) and ZnO (20 nm) at percent weight ratio of 20:80, 40:60, 60:40, and 80:20 (MgO/ZnO) were suspended in DIW (1400 mL) to formulate 0.1 vol.% BNFs using a two-step method. The dispersion fraction of the surfactant (SDS) was 1.0.

Equation 3.1 was used to estimate the weights of MgO and ZnO nanoparticles as a function of  $\varphi$  (0.05 and 0.10) as given in Table A1. Also, the weights of SDS were calculated using Equation 3.2 and as a dependent of  $\varphi$ .

S/N	MgO-ZnO (wt%)	MgO (g)	ZnO (g)	SDS (g)	<b>BF</b> ( <b>l</b> )
		0.05 vol.%	ý 0		
1	20-80	1.0408	4.1633	5.2041	1400
2	40-60	2.3650	3.5475	5.3212	1400
3	60-40	2.9494	1.9662	4.9156	1400
4	80-20	2.7114	0.6779	3.3893	1400
		0.1 vol.%			
1	20-80	2.0827	8.3308	10.4135	1400
2	40-60	4.7323	7.0985	11.8308	1400
3	60-40	5.9017	3.9345	9.8361	1400
4	80-20	5.4255	1.3564	6.7819	1400

 Table A.1: Weights (g) of NPs and surfactant (SDS) engaged in BNF formulation.

## A.3 Conclusion

The weights of nanoparticles and surfactants used in the formulation of BNFs in this present investigation were estimated and presented. These weights were observed to be dependent primarily on  $\rho$  and percent weight of individual NPs, and  $\varphi$ , as related to the type of BNFs to be formulated. Additionally, the total amounts of materials (BNPs and surfactants) depended on the type of BNFs to be formulated, which was related to  $\varphi$ , type of surfactants, dispersion fraction of surfactants, NPs percent weight, and the types of NPs combined as BNPs.

# **B.** Calibration of Thermocouples

#### **B.1 Introduction**

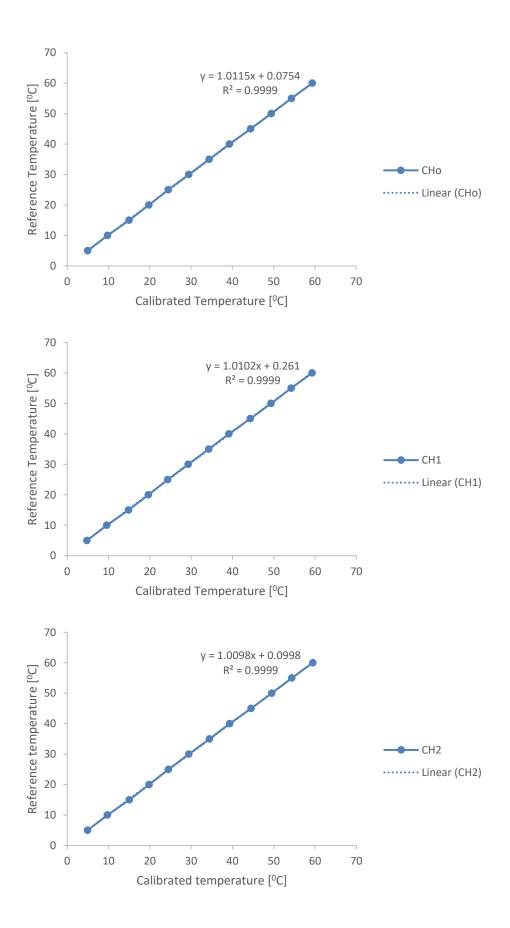
The calibration of the thermocouples employed in the square cavity for the thermo-convection investigation of BNFs was discussed in this appendix. In addition, the calibration factors of individual thermocouples were also shown.

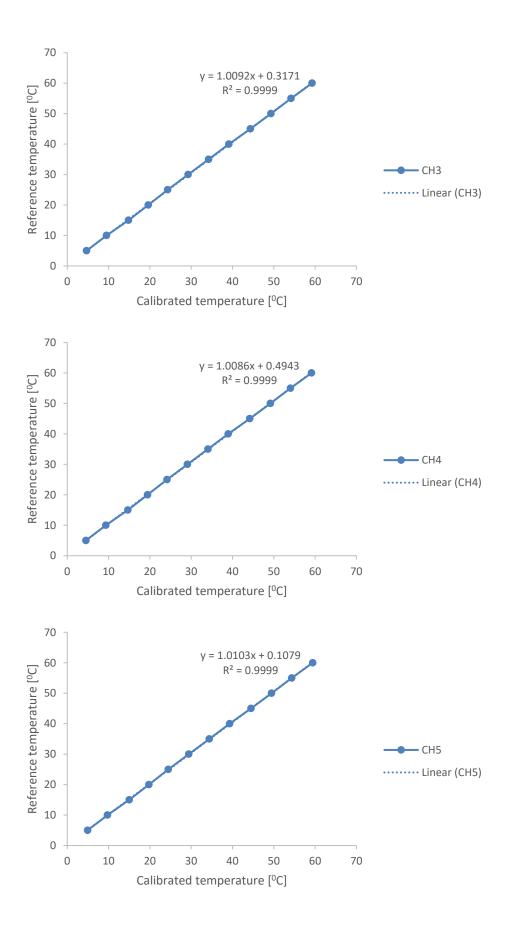
## **B.2** Calibration of Thermocouples

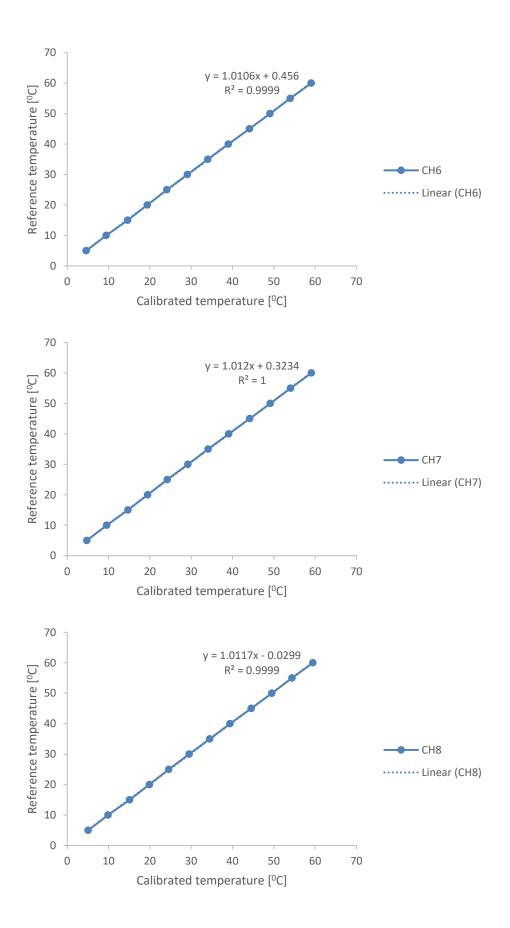
A Programmable water baths (PolyScience, USA: PR 20R-30-A12E,  $-30^{\circ}$ C and 200°C, precision 0.0050 °C), was employed for the in-situ calibration of the thermocouples at temperatures of 5 – 60 °C at 2.5 °C intervals. Temperature measurements of 400 points were measured at the predetermined temperature using a frequency of 2 Hz, and the average was determined. The calibration procedure was conducted in triplicates (to minimize error), and the means of the measured temperature dataset for the thermocouples were estimated. For each thermocouple, the average measured temperature was plotted against the reference temperature as measured using PT-100 (thermal bath internal thermocouple) as provided in Figure B.1. Fitting of the reference and average measured temperature for each thermocouple was done to estimate the calibration factors using Equation B.1.

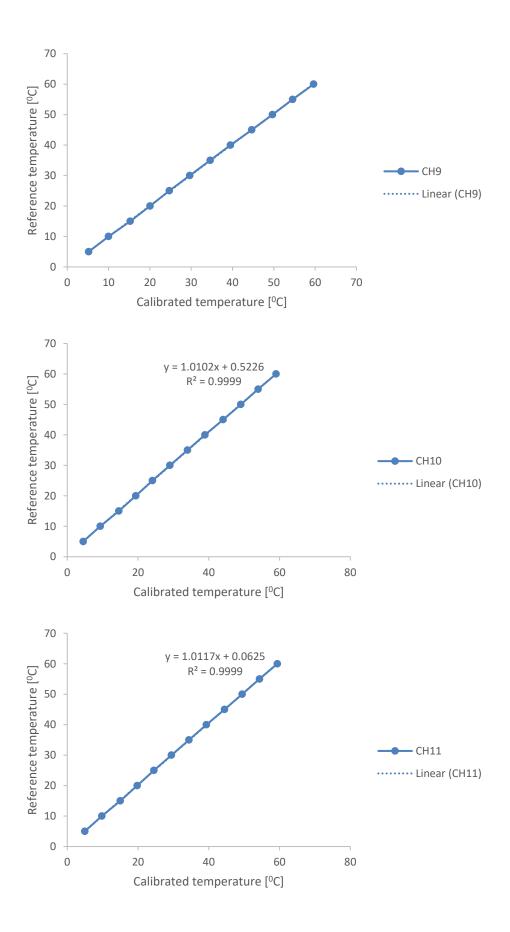
$$T_{cal} = mT_{uncali} + c$$
 B.1

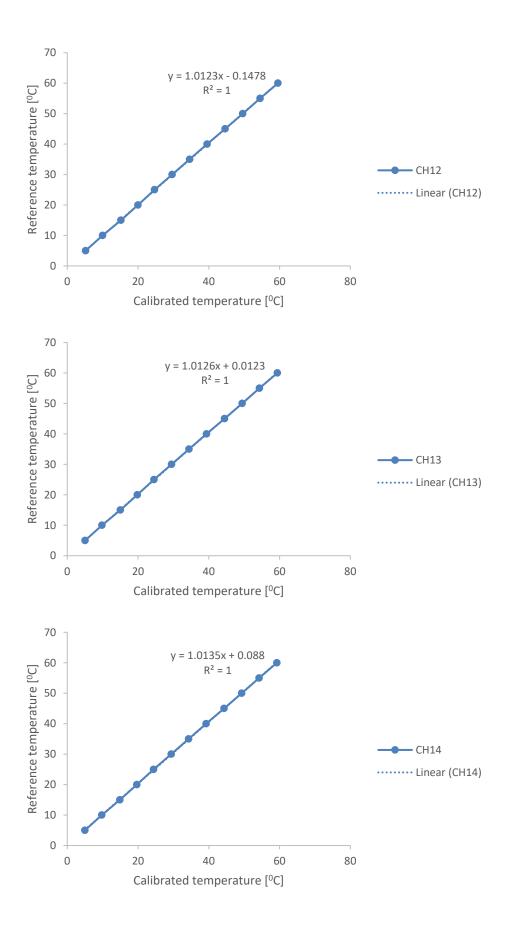
For the thermocouples, the m and c were used as the calibration parameters. A linear relationship with  $R^2 \approx 1$  was noticed amidst the mean measured temperature and the reference temperature for all the thermocouples. This revealed a good correlation between both variables showing excellent performance of the thermocouples in valuing the reference temperatures.

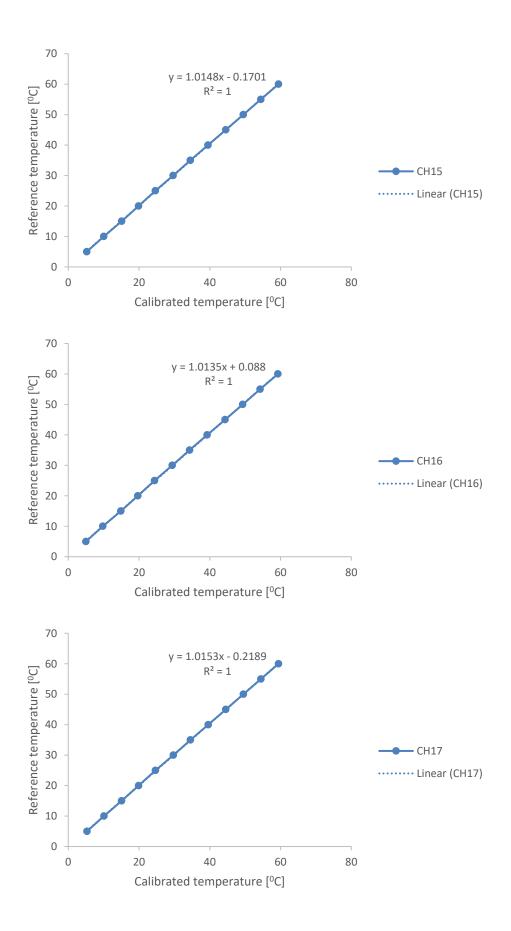


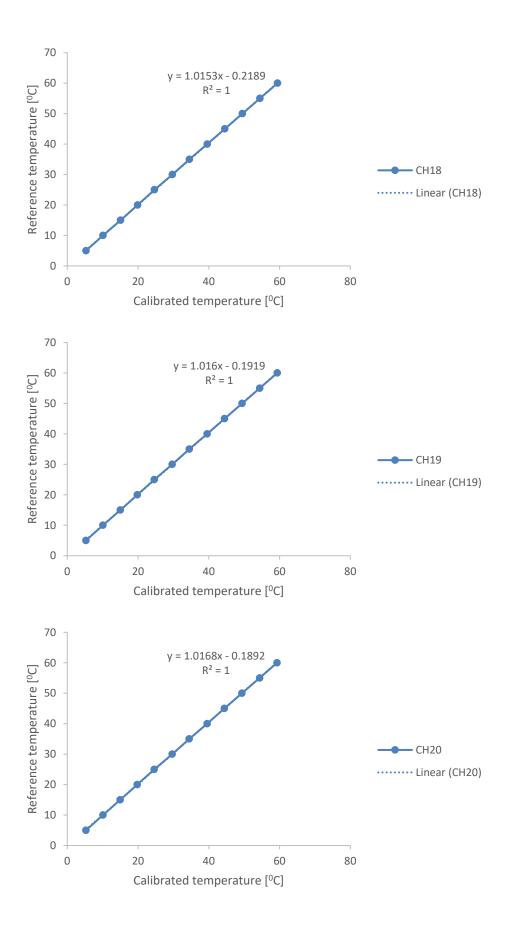












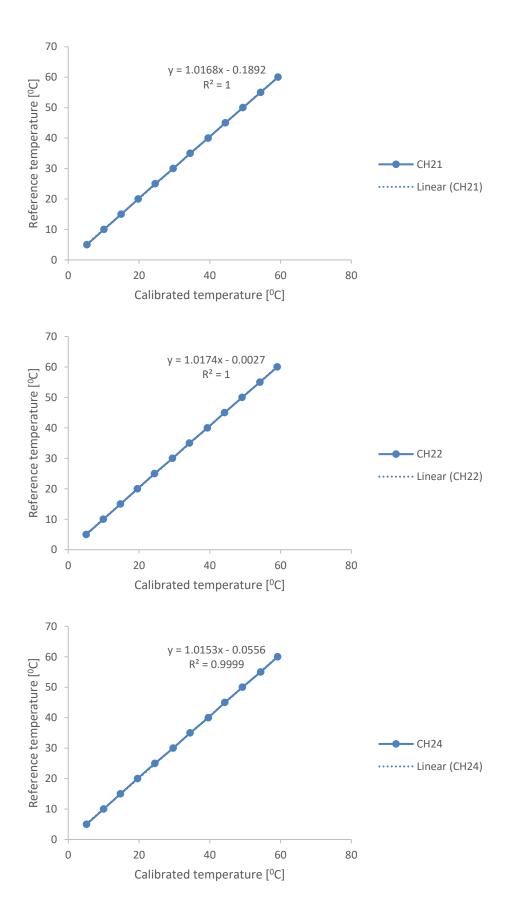


Figure B.1: Average measured temperatures of thermocouples against reference temperatures (CH 0 - 22, 24).

The use of various channels of the data logger could be ascribed to the variations in the calibration parameters achieved for the thermocouples. Also, the changes in the characteristics of the junction of the thermocouples after soldering them to the various positions can be responsible for the variation in the calibration factors of the thermocouples. After calibration, the average deviation between the average measured temperature of the thermocouples and reference temperatures was 0.169 °C.

#### **B.3** Conclusion

The calibration of the thermocouples was performed and presented. The thermocouples were calibrated for temperature 10-50 °C using a thermal bath of the accuracy of  $\pm 0.005$  °C. Linear relationships were observed between the average measured temperature of the thermocouples and the reference temperature. The average deviation of the thermocouples was 0.169 °C.

# **C. Uncertainty Analysis**

#### **C.1 Introduction**

Uncertainty analysis was employed to analyse the uncertainty associated with the variables relevant to this investigation. This appendix entails the content of the uncertainty analysis approach, precision of the instrument used for the investigation (thermophysical properties and thermo-convection) and the associated results for the uncertainties [601, 602].

## C.2 Theory

In measurement processes, two types of errors happen – bias and precision. The bias error estimates the precision of measurement, as specified by the instrument's manufacturer. These errors arise from calibration, imperfection of measuring tools and equipment, etc. Precision errors relate to data spread, which defines the precision of dataset. These errors emanate from differences in the measurement process, electrical noise, etc [601, 602].

The magnitude of the bias and precision errors relates to a 95% probability in which the actual error is more than the estimated error. For a single measurement, uncertainty is related to both precision and bias [601, 602]. Uncertainty is presented in Equation C.1 [205]:

$$\delta x_i = \sqrt{\left(b_i^2 + p_i^2\right)}$$
C.1

Where:

 $x_i$  is a single measurement and  $\delta x_i$  relates to standard deviation multiplied by Student's *t*-variable [603]. The reading *R* of measurement is related to various parameters and can be calculated using a series of equations.

$$R = R(x_1, x_2, x_3, \dots, x_n)$$
 C.2

With the uncertainties of  $x_i$  known, the uncertainty in R can be estimated as expressed in Equation C.3.

$$\delta R = \frac{\partial R}{\partial x_i} \delta x_i$$
 C.3

Where  $\delta R$  is the sensitivity coefficient employed to determine the influence of  $x_i$  on the general uncertainty. The root sum square method is used to estimate the uncertainty of various independent variables.

$$\delta R = \left(\sum_{i=1}^{n} \left(\frac{\partial R}{\partial X_i} \delta x_i\right)^2\right)^{\frac{1}{2}}$$
 C.4

The accuracy of the thermocouples was determined by applying regression analysis, which is a statistical tool used to establish a mathematical relationship between two or more variables. The x value is the known parameter while the y value is determined via measurements. Hence, the uncertainty was propagated from the y parameter [603]. Equation C.5 was applied to evaluate the uncertainty of the y factor."

$$\delta y = \pm t S_{yx} \sqrt{\frac{1}{N} + \frac{1}{M} + \frac{(x_i - \bar{x})^2}{S_{xx}}}$$
C.5

Where  $S_{xx}$  is defined as:

$$S_{xx} = \sum_{i=1}^{N} (x_i - \bar{x})^2$$
 C.6

 $S_{yx}$  is determined by first estimating  $S_{xy}$ , a, and b.

$$S_{xy} = \sum_{i=1}^{N} (x_i - \bar{x})(y_i - \bar{y})$$
 C.7

$$b = \frac{S_{xy}}{S_{xx}}$$

$$a = \bar{y} - b\bar{x}$$

$$y_{ci} = a + bx_i$$
 C.10

$$S_{yx} = \sqrt{\frac{\sum_{i=1}^{N} (y_i - y_{ci})^2}{N - 2}}$$
 C.11

The uncertainty in the x variable was evaluated by dividing the uncertainty in y by the slope of the regression line.

$$\delta x = \frac{\delta y}{m}$$
C.12

### C.3 Equipment

The accuracy specified by the manufacturer was considered as the bias for the instruments while the precision was evaluated using the standard deviation of the 1000 measurement points acquired via the data logger for temperature and flow rate measurements. For the viscometer and thermal conductivity meter, the accuracy (bias) specified by the manufacturer was used. The determined precision was multiplied by Student's *t*-value with a confidence limit of 95% [601, 602]. The accuracy of the instruments used in this study is given in Table C.1.

	• • •	e e e e e e e e e e e e e e e e e e e	
Instrument	Range	Accuracy	
Electrical conductivity meter	0 μS - 200 mS	$\pm 1\%$	
Flow meter	0.0666 – 0.3333 l/s	$\pm 0.01\%$ of full-scale flow rate $+2\%$ (measured value)	
Graduated cylinder	250 ml	$\pm 2.0 \text{ ml}$	
Thermal bath	-200 – 150 °C	$\pm 0.005$ °C	
Thermal conductivity meter	$0.2-2.0 \ W/m \ K$	$\pm 10\%$	
Thermocouple	< 150 °C	±0.1 °C	
Vernier calipers	0.02 mm	0.02 mm	
Viscometer	0.3 – 10,000 mPa.s	±3%	
Weighing balance	10 mg – 220 g	0.02	

Table C.1: Accuracy of equipment used in this investigation.

#### **C.3.1** Thermocouples

The calibration of thermocouples was discussed earlier in B.3, where the accuracy of the thermal bath and thermocouples were  $\pm 0.005$  °C and 0.1 °C, respectively. The precision was evaluated using Equation C.2.5 to C.2.12 with the uncertainty evaluated using Equation C.1. The average uncertainty of the thermocouples was  $\pm 0.159\%$ .

#### C.3.2 Flow Meters

Each of the flow meters has an accuracy of  $\pm 0.01\%$  of full-scale flow rate + 2% (measured value) used as the bias. The precision was calculated by multiplying the standard deviation of the flow rate acquired by the data logger by the Student's *t*-value. The uncertainty was then estimated using Equation C.1.

#### **C.3.3 Digital Weighing Balance**

The accuracy of the digital weighing balance was 0.001 g, and this was used as the bias. The standard deviation of the BNPs and surfactants (total) weights for each BNFs as presented in Table A.1 was obtained and used as the precision. This was multiplied by the Student's *t*-value, and Equation C.1 was used to estimate uncertainty.

### **C.3.4 Thermal Conductivity Meter**

Similarly, the accuracy of the thermal conductivity meter was engaged as the bias. The standard deviation of the measurements taken for each BNFs and basefluid was multiplied by the Student's *t*-value and used as the precision. Using Equation 3.26, an extension of Equation C.1, the uncertainty of  $\kappa$  for BNFs and basefluids was estimated. As mentioned in Appendix A, the volume of the basefluids (DIW) used in this study was 1400 mL, and the graduated cylinder had an accuracy of ±2.0 ml.

#### C.3.5 Viscometer

With the accuracy of the viscometer used as the bias and the precision calculated from the multiplication of the standard deviation of the measured  $\mu$  (for BNFs and basefluids) by Student's *t*-value, the uncertainty of  $\mu$  (for BNFs and basefluids) was estimated using Equation 3.25 (an extension of Equation C.1). It is important to note that the viscometer has an accuracy specified for the temperature sensor related with  $\mu$  measurement.

#### **C.4 Parameters**

#### **C.4.1 Temperatures**

From the known uncertainty of the thermocouples, the uncertainty related with the measurement of temperatures inside and outside the cavity was obtained. The uncertainty of the temperature of water flowing from and to the thermal baths was assumed to be equal under adiabatic conduction of close to perfect insulation. This is expressed by Equation C.13.

$$\delta T_{in} = \delta T_o$$
 C.13

The uncertainties of the bulk temperature, temperature gradient, temperature hot and cold side of the cavity were estimated using Equations C.14 - C.17, respectively. It is of note that *T* is the absolute temperature used in the correlations for estimating the uncertainty of other properties.

$$\delta T_{Bulk,H} = \frac{1}{3} \sqrt{\left(\delta T_{o,1}\right)^2 + \left(\delta T_{o,2}\right)^2 + \left(\delta T_i\right)^2}$$
 C.14

$$\delta\Delta T = \sqrt{\left(\frac{1}{2}\delta T_{o,1}\right)^2 + \left(\frac{1}{2}\delta T_{o,2}\right)^2 + (\delta T_i)^2}$$
C.15

$$\delta T_{H} = \frac{1}{3} \sqrt{\left(\delta T_{H,1}\right)^{2} + \left(\delta T_{H,2}\right)^{2} + \left(\delta T_{H,3}\right)^{2}}$$
C.16

$$\delta T_{C} = \frac{1}{3} \sqrt{\left(\delta T_{C,1}\right)^{2} + \left(\delta T_{C,2}\right)^{2} + \left(\delta T_{C,3}\right)^{2}}$$
C.17

## C.4.2 Cavity Area

The uncertainty of the cavity area was determined using Equation C.18.

$$\delta A = \sqrt{\left(\frac{\partial A}{\partial W}\delta W\right)^2 + \left(\frac{\partial A}{\partial H}\delta H\right)^2}$$
C.18

Where:  $\partial W = \partial H = \partial L$ 

## **C.4.3 Thermophysical Properties**

To estimate the uncertainty of  $\mu$  and  $\kappa$  of the basefluids, Equations C.19 – C.20 representing the correlations developed from the experimental data obtained in this work for  $\mu$  and  $\kappa$  of the basefluids were used.

$$\kappa_{DIW} = 0.5741 + 1.393 \times 10^{-3}T$$
 C.19

$$\mu_{DIW} = 1.18357 - 0.1271T$$
 C.20

The empirical formula [539, 604] employed for the evaluation of the uncertainty of other thermal properties for the BFs are presented as Equations C.21 - C.23.

$$\rho_{DIW} = (999.842594 + 0.067939952T - 0.00909529T^2 + 1.00168 \times 10^{-4}T^3 - 1.120083 \times 10^{-6}T^4 + 6.536332 \times 10^{-9}T^5$$
 C.21

$$\beta_{DIW} = 8.41 \times 10^{-7} T^3 - 1.55704 \times 10^{-4} T^2 + 0.015892349T - 0.055807193$$
C.22

$$C_{p-DIW} = 4.214 - 2.286 \times 10^{-3}T + 4.991 \times 10^{-5}T^2 - 4.519 \times 10^{-7}T^3 + 1.857 \times 10^{-9}T^4$$
 C.23

The uncertainty of  $\kappa$ ,  $\rho$ ,  $\beta$ , and C<sub>p</sub> of the basefluids (DIW) was estimated using Equations C.24 – C.27, respectively.

$$\delta \kappa_{bf} = \sqrt{\left(\frac{\partial \kappa_{bf}}{\partial T} \delta T\right)^2}$$
C.24

$$\delta \rho_{bf} = \sqrt{\left(\frac{\partial \rho_{bf}}{\partial T} \delta T\right)^2}$$
 C.25

$$\delta\beta_{bf} = \sqrt{\left(\frac{\partial\beta_{bf}}{\partial T}\delta T\right)^2}$$
 C.26

$$\delta C_{p-bf} = \sqrt{\left(\frac{\partial C_{p-bf}}{\partial T}\delta T\right)^2}$$
 C.27

With the use of Equation C.28 for  $\varphi$  which is a simple version of Equation 3.1, the uncertainty of  $\varphi$  was estimated using Equation C.29.

$$\varphi = \frac{\nu_{hnp}}{\nu_{hnp} + \nu_{bf}} = \frac{\frac{m_{hnp}}{\rho_{hnp}}}{\frac{m_{hnp}}{\rho_{hnp}} + \nu_{bf}}$$
C.28

$$\delta\varphi = \sqrt{\left(\frac{\partial\varphi}{\partial m_{hnp}}\delta m_{hnp}\right)^2 + \left(\frac{\partial\varphi}{\partial\nu_{bf}}\delta\nu_{bf}\right)^2}$$
C.29

Where:

$$\frac{\partial \varphi}{\partial m_{hnp}} = \frac{\rho_{hnp} v_{bf}}{\left(m_{hnp} + \rho_{hnp} v_{bf}\right)^2} \quad \text{and} \quad \frac{\partial \varphi}{\partial v_{bf}} = \frac{-m_{hnp} \rho_{hnp}}{\left(m_{hnp} + \rho_{hnp} v_{bf}\right)^2}$$

Empirical models for  $\rho_{hnf}$ ,  $C_{p-hnf}$ , and  $\beta_{hnf}$  as expressed using Equations C.30 – C.32 were used to determine their uncertainty as expressed in Equations C.33 – C.35, respectively.

$$\rho_{hnf} = (1 - \varphi)\rho_{bf} + \varphi\rho_{hnp}$$
C.30

$$C_{p-hnf} = \frac{(1-\varphi)(\rho C_p)_{bf} + (\rho C_p)_{hnp}}{\rho_{hnf}}$$
C.31

$$\beta_{hnf} = \frac{(1-\varphi)(\rho\beta)_{bf} + (\rho\beta)_{hnp}}{\rho_{hnf}}$$
C.32

$$\delta\rho_{hnf} = \sqrt{\left(\frac{\partial\rho_{hnf}}{\partial\varphi}\delta\varphi\right)^2 + \left(\frac{\partial\rho_{hnf}}{\partial\rho_{bf}}\delta\rho_{bf}\right)^2}$$
C.33

Where:

 $\delta C_{p-hnf} =$ 

$$\frac{\partial \rho_{hnf}}{\partial \varphi} = \rho_{hnp} - \rho_{bf}$$
 and  $\frac{\partial \rho_{hnf}}{\partial \rho_{bf}} = 1 - \varphi$ 

$$\sqrt{\left(\frac{\partial C_{p-hnf}}{\partial \varphi}\delta\varphi\right)^2 + \left(\frac{\partial C_{p-hnf}}{\partial \rho_{bf}}\delta\rho_{bf}\right)^2 + \left(\frac{\partial C_{p-hnf}}{\partial C_{p-bf}}\delta C_{p-bf}\right)^2 + \left(\frac{\partial C_{p-hnf}}{\partial \rho_{hnf}}\delta\rho_{hnf}\right)^2 \mathbb{C}.34}$$

Where:  

$$\frac{\partial C_{p-hnf}}{\partial \varphi} = \frac{-(\rho C_p)_{bf}}{\rho_{hnf}}, \frac{\partial C_{p-hnf}}{\partial \rho_{bf}} = \frac{C_{p-bf}(1-\varphi)}{\rho_{hnf}}, \frac{\partial C_{p-hnf}}{\partial C_{p-bf}} = \frac{\rho_{bf}(1-\varphi)}{\rho_{hnf}}, \text{ and } \frac{\partial C_{p-hnf}}{\partial \rho_{hnf}} = \frac{-\left((1-\varphi)(\rho C_p)_{bf} + (\rho C_p)_{hnp}\right)}{(\rho_{hnf})^2}$$

$$\delta\beta_{hnf} = \sqrt{\left(\frac{\partial\beta_{hnf}}{\partial\varphi}\delta\varphi\right)^2 + \left(\frac{\partial\beta_{hnf}}{\partial\rho_{bf}}\delta\rho_{bf}\right)^2 + \left(\frac{\partial\beta_{hnf}}{\partial\beta_{bf}}\delta\beta_{bf}\right)^2 + \left(\frac{\partial\beta_{hnf}}{\partial\rho_{hnf}}\delta\rho_{hnf}\right)^2} \quad C.35$$

Where:

$$\frac{\partial \beta_{hnf}}{\partial \varphi} = \frac{-(\rho\beta)_{bf}}{\rho_{hnf}}, \quad \frac{\partial \beta_{hnf}}{\partial \rho_{bf}} = \frac{\beta_{bf}(1-\varphi)}{\rho_{hnf}}, \quad \frac{\partial \beta_{hnf}}{\partial \beta_{bf}} = \frac{\rho_{bf}(1-\varphi)}{\rho_{hnf}}, \quad \text{and} \quad \frac{\partial \beta_{hnf}}{\partial \rho_{hnf}} = \frac{-\left((1-\varphi)(\rho\beta)_{bf} + (\rho\beta)_{hnp}\right)}{\left(\rho_{hnf}\right)^2}$$

To estimate the uncertainty of  $\kappa_{hnf}$ , Equation C.36 was employed.

$$\delta \kappa_{hnf} = \sqrt{\left(\frac{\partial \kappa_{hnf}}{\partial \varphi} \delta \varphi\right)^2 + \left(\frac{\partial \kappa_{hnf}}{\partial \kappa_{bf}} \delta \kappa_{bf}\right)^2}$$
C.36

# C.4.4 Heat Transfer Rate

The estimation of the uncertainty of the heat transferred (Q) involved the substitution of Equations C.37 – C.39 into Equation 3.28.

$$\frac{\partial Q}{\partial \dot{m}} = C_{p-bf} \Delta T$$
C.37

$$\frac{\partial Q}{\partial c_{p-bf}} = \dot{m} \Delta T$$
 C.38

$$\frac{\partial Q}{\partial \Delta T} = \dot{m} C_{p-bf}$$
C.39

# C.4.5 Convective Heat Transfer Coefficient

Equations C.40 - C.43 were substituted into Equation 3.28 to estimate the uncertainty of *h*.

$\frac{\partial h}{d} =$	1	C.40	1
		C.40	$-\frac{1}{(T_h - T_c)A}$

$$\frac{\partial h}{\partial A} = \frac{-Q}{(T_h - T_c)A^2}$$
C.41

$$\frac{\partial h}{\partial T_h} = \frac{-Q}{(T_h - T_c)^2 A}$$
C.42

$$\frac{\partial h}{\partial T_c} = \frac{Q}{(T_h - T_c)^2 A}$$
C.43

## C.4.6 Nusselt Number

Similarly, the uncertainty of Nu was estimated by substituting Equations C.44 – C.46 into Equation 3.27.

$$\frac{\partial Nu}{\partial h} = \frac{L_c}{\kappa}$$
 C.44

$$\frac{\partial Nu}{\partial L_c} = \frac{h}{\kappa}$$
C.45

$$\frac{\partial Nu}{\partial h} = \frac{-hL_c}{\kappa}$$
 C.46

## C.5 Conclusion

The theory and method of uncertainty were highlighted. The accuracy of instruments engaged as the bias and the precision were used to estimate the uncertainty associated with the relevant parameters involved in this present study.