Testing for Unemployment Persistence in Nigeria

Ebuh U. Godday

Central Bank of Nigeria Monetary Policy Department 33 Tafawa Balewa Way, Central Business District, Garki Abuja, FCT, Nigeria. guebuh@cbn.gov.ng

Nuruddeen Usman¹

Central Bank of Nigeria Monetary Policy Department 33 Tafawa Balewa Way, Central Business District, Garki Abuja, FCT, Nigeria. <u>nusman2@cbn.gov.ng</u>

Afees A. Salisu

Centre for Econometrics and Applied Research (CEAR), Ibadan, Oyo state, Nigeria.

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Department of Economics, University of Pretoria, South Africa adebare1@yahoo.com

Abstract

In this study, we examine the behavior of unemployment in Nigeria using fractional integration & fractional cointegration techniques. Based on the fractional integration technique, we find that unemployment in Nigeria exhibits mean reverting properties but with a longer time horizon for any shock effect to fizzle out. The fractional cointegration technique reveals that unemployment shares somewhat common long run relationships with macroeconomic variables such as interest rate, inflation and output. Therefore, policy actions by relevant authority targeted at any of these macroeconomic variables may have implications on unemployment in Nigeria and vice versa. However, the results leading to these conclusions are sensitive to sample periods and intervening variables.

Keywords: Unemployment persistence, Fractional integration, Fractional cointegration, Global financial crisis, Nigeria

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1. Introduction

Gauging the extent of persistence in unemployment rates is of vital importance to Nigeria considering its role in African economies. As one of the countries in the world where the level misery is very high (Tule et al, 2017a), determining the degree of unemployment rate by policy makers becomes a sine qua non in choosing appropriate response to external shocks. In the conduct of macroeconomic policy, the implications of time series behaviour of the unemployment rate cannot be overemphasized. As posited in the natural rate hypothesis of Friedman (1968) and Phelps (1967), in the long-run, the unemployment rate should converge to a "natural rate", since it follows a mean reverting process and the variations from the natural rate are transitory. However, high and persistent unemployment has cast aspersion on the natural rate hypothesis. Hence, Blanchard and Summers (1987) formulated the hysteresis hypothesis to account for high and persistent unemployment rates witnessed in some European countries. In line with Blanchard and Summers (1987), there is high likelihood of unemployed workers losing valuable job skills over time. Similarly, stagflation and recession are other likely factors that may have everlasting effects on the skills of workers. Hence, any shock to unemployment may have a permanent effect and by implication, likely to exhibit a non-mean reverting process. Hence, from empirical point of view as documented in the extant literature, suffice it to say that evidence in support of the existence of the hysteresis in the unit root process abound, while on the other hand, stationarity would support the natural rate hypothesis in unemployment.

Theoretically, the dynamics of unemployment are basically underpinned by two views: the hysteresis hypothesis and the non-accelerating inflation rate of unemployment (NAIRU) hypothesis (Romer, 2011). The NAIRU hypothesis is of the view that oscillations in unemployment are "cyclical deviations" from the "natural-rate". Friedman (1968) and, Phelps (1968) who are the first proponents of the NAIRU led hypothesis, argue that unemployment should chart a stationary process. Nevertheless, Blanchard and Summers (1987), who first

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proposed the hysteresis hypothesis opine that shocks on unemployment rate would not have temporary effects and that the "equilibrium rate of unemployment" shifts from one level to another by an exogenous shock.

The literature on unemployment persistence has offered three strands of studies on the basis of the types of unit root tests usually employed. The first strand of studies whose findings generally support the hypothesis of hysteresis in unemployment mainly applies the conventional unit root tests (see for example, Blanchard and Summers, 1987; Perron, 1989; Brunello, 1990; Mitchell, 1993; Jaeger and Parkinson, 1994; and Roed, 1996). Inspired by Perron (1989)'s seminal work (1989) in which it is suggested that normal unit root tests are biased towards non-rejection in the presence of a structural break, the second strand of research focuses on whether incorporating structural breaks in the unit root model is relevant to the hysteresis hypothesis As a consequence, Zivot and Andrews (1992) and Perron (1997) establish models that permit an endogenous break. Lumsdaine and Papell (1997) and Lee and Strazicich (2003) extend the work of Zivot and Andrews (1992) to test for two endogenous breaks.. Exploring some of these structural break-based unit root tests, Mitchell (1993), Bianchi and Zoega (1997), Arestis and Mariscal (1999, 2000) and Papell et al. (2000) unanimously show that when structural breaks are taken into account, the hysteresis hypothesis is rejected. The third strand of studies is based on panel unit root tests with and without structural breaks (see Levin et al., 2002 and Im et al., 2003 in the case of the latter, Papell et al, 2000 , in the case of the former). Thus, both the time series and panel data techniques have been used to evaluate unemployment persistence in the literature.

Consequently, our study will leverage on relevant statistical considerations such as nonlinearities, fractional integration, structural breaks and endogeneity issues to empirically analyze the severity of unemployment in Nigeria. Although, Tule et al (2016) and Tule et al (2017a) have done some work on the composite index of leading indicators of unemployment and the dynamic fragmentation of misery index in Nigeria, respectively, however, to the best of our knowledge, studies that have done similar work include Caporale and Gil-Alana (2018) and Tule et al (2017b). Conversely, their methodology relies on fractional integration, which ignores other stochastic features of time series as previously highlighted. Technically, the consideration of these features when they are found to be evident may upturn the findings of Tule et al (2017b) and Caporale and Gil-Alana (2018). Also, in addition to the analysis of unemployment behavior in Nigeria, a robustness check will also be employed to offer more useful generalizations. From the policy perspective, information about unemployment persistence enables policy makers to evaluate the effectiveness of their policies in influencing the behavior of unemployment. Thus, the study will not only be rigorous analytically, it will also produce results that can serve as input to future policy formulation and implementation process.

Understanding the persistence of unemployment will give important information on its dynamics, the magnitude of shocks it transmits to the economy, and a country's sensitivity to unemployment risk. These elements are critical for the formulation and implementation of economic policy, accelerating the restoration of employment to a steady path commensurate with countries' growth objectives.

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Following the introduction, the paper is organized as follows: Section 2 deliberates on the empirical and theoretical findings on unemployment persistence; Section 3 discusses the methodology while Section 4 discusses the empirical results. Finally, Section 5 concludes the study.

2. Literature Review

2.1 Theoretical underpinnings in unemployment persistence

The theoretical underpinnings for the behaviour of unemployment can be linked to the Non-Accelerating Inflation Rate of Unemployment (NAIRU) hypothesis that states that there exists a unique long run equilibrium for unemployment rates. The implication is that there does not exist a trade-off between inflation and output and the Phillips curve is vertical in the long-run. However, in the short-run, there are transitory deviations from the long run equilibrium making unemployment stationary and mean reverting.

Phelps (1972) in his book on "Inflation Policy and Unemployment Theory" proposes a theoretical model that explains changes in NAIRU due to changes in economic rudiments in the economy i.e. capital, interest rates and productivity. The models incorporate micro foundations to explain structural changes (Layard et al., 2005). Under the structuralist theory of unemployment, empirical analysis should be done by unit root tests such as Augmented Dickey-Fuller (ADF) Test, Kwiatkowski–Phillips–Schmidt–Shin (KPSS) and Phillips-Perron (PP)-test that account for structural changes in unemployment. If not, unit root test carried out may be biased with type 2 error in the presence of structural breaks in the deterministic components of unemployment. (See, among others, Blanchard and Katz, 1992; Decressin and Fatas, 1995).

The second theory links the attitude and behaviour of those in employment to contributing to unemployment persistence and this has been extensively researched by Blanchard and Summers (1986, 1987) and Barro (1995). According to this phenomenon, shocks to unemployment do not die out and the variable never returns to its equilibrium rate, exhibiting an explosive process. The explanations for this process include high real wages, unemployment protection schemes, powerful workers unions and stigma associated with being out of work for a long time. This has been extensively examined by Phelps (1972); Blanchard and Summers (1986, 1987); Barro (1995); and Layard (2005), amongst others. The effect of lagged unemployment on hysteresis, can be explained in terms of insider-outsider effect as Blanchard and Summers (1986, 1987) point out or by the effect of unemployment on the human capital and search intensity of the unemployed by Okun (1973). Finally, in contrast to the NAIRU hypothesis, the hysteresis hypothesis argues that, as aggregate demand can influence the path of actual unemployment, aggregate demand policies can influence the natural rate of unemployment.

3. Empirical review of the literature on unemployment persistence

In the literature, there appears to be different causes of unemployment persistence. Neisson and Plosser (1982), Blanchard and Summers (1986, 1987), Brunello (1990), and Mitchell (1993) are of the view that EU countries' unemployment series contains a unit root. Nonetheless, the presence of structural breaks may render the results of unit root test invalid such that the unemployment data can be assumed to be integrated of order 1 (I(1)) when in fact it is stationary around a drift after accounting for structural breaks. This latter argument is upheld by

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Mithcell (1993), Bianchi and Zoega (1998) Ariesis and Mariscal (1999) and Pappelle et al (2000) who apply unit root test with structural break and find evidence supporting the structuralists' view² of unemployment.

A comparative study by Song and Wu (1997, 1998) finds evidence in support of hysteresis hypothesis in EU countries' unemployment series, while the U.S. unemployment data is characterized by the NAIRU hypothesis (see also, Gil-Alana, 2001, 2002; Caporale & Gil-Alana, 2007, 2008)). Gil-Alana (2001), Gil-Alana (2002) and Caporale and Gil-Alana (2007, 2008) favour the structuralists' view for EU unemployment based on the AFRIMA (Autoregressive Fractionally Integrated Moving Average) model while the NAIRU hypothesis is supported for the U.S. unemployment as reported in Song and Wu (1997, 1998). However, unemployment in the European Community (EC) is found to be highly persistent, relative to the Nordic countries and U.S. (see Alogoskoufis & Manning, 1988). For other climes like the Latin American countries, there is evidence of mean reversion in unemployment (see Ayala et al, 2012).

In relation to the country of focus (i.e., Nigeria), the degree of unemployment persistence is observed within the range of $\{0 \le d \le 1\}$, (see Tule et al., 2017a), and is more likely to be characterized by the NAIRU hypothesis. By way of extension of the existing literature on unemployment persistence, we build on related studies by Caporale and Gil-Alana (2007, 2008) and Caporale et al. (2017, 2018) which allow for breaks in a fractional integration framework and take consideration of the possible autocorrelation in the unemployment series. The fractional integration framework has the advantage that the fractional parameter can take any real value compared to the classical I(0)/I(1) integration dichotomy. In order to obtain information on the relevance of alternative unemployment theories, it is crucial to estimate the differential parameter 'd' in the fractional integration framework. Specifically, an order of integration equal to 0 supports the NAIRU hypothesis, while a positive value of 'd' represents evidence in support of hysteresis hypothesis.

4. Methodology

4.1 The fractionally integrated univariate model for persistence

One of the attractions to the fractional integration approach lies in its ability to exploit the stochastic behavior of economic series in a fractional form unlike the traditional approaches which assume integer values in the determination of stationarity. The fractional integration approach contends that such series may be fractionally integrated such that the impact of shocks only vanishes at very long horizons, rather than assume that economic series are I(1). This methodology has also been used to examine unemployment persistence for different countries (Caporale & Gil-Alana, 2007, 2008; Caporale et al., 2017, 2018). Therefore, we test for unemployment persistence for Nigeria using the fractional integration as specified below:

$$(1-L)^{d} Z_{t} = \alpha + \gamma Trend + \varepsilon_{t}; \qquad (1)$$

² Changes in the underlying equilibrium unemployment rate due to the interplay of changes in real macroeconomic variables and institutions. The structuralist school assumes that unemployment is mean-reverting towards an occasionally changing natural rate

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where L is the lag operator $(LZ_t = Z_{t-1}) d$ can be any real value from (0 to 1), Z_t is integrated of order d and symbolized by $Z_t \approx I(d)$. ε_t is a covariance stationary process with a spectral density function that is positive and is an integrated order 0(I(0)) process and finite at zero frequency. The polynomial $(1-L)^d$ in equation (1) can be formulated on the basis of its binomial expansion such that for all real d,

$$\left(1-L\right)^{d} = \sum_{j=0}^{\infty} \psi_{j} L^{j} = \sum_{j=0}^{\infty} {d \choose j} \left(-1\right)^{j} L^{j} = 1 - dL + \frac{d(d-1)}{2} L^{2} - \dots,$$
(2)

and therefore

$$(1-L)^{d} \pi_{t} = \pi_{t} - d\pi_{t-1} + \frac{d(d-1)}{2}\pi_{t-2} - \dots$$
(3)

Consequently, equation (3) can be expressed as:

$$\pi_{t} = \alpha + \gamma Trend + d\pi_{t-1} + \frac{d(d-1)}{2}\pi_{t-2} - \ldots + \varepsilon_{t}$$

$$\tag{4}$$

Equation (4) is derived to show that d also plays a critical role in appraising the level of persistence as it defines the degree of dependence of the unemployment series (Caporale & Gil-Alana, 2007, 2008; Caporale et al., 2017, 2018; Gil-Alana & Carcel, 2018; Usman & Nduka 2022). Hence, given a higher value of d, would imply a higher level of memory amongst the series and by inference a higher level of persistence (Ebuh et al., 2021). In order to analyze fractional integration, we use the parametric technique, which includes the maximum likelihood estimator of Sowell (1992). This approach has the benefit of obtaining precision by employing data through parameter estimates. However, one shortcoming of this approach is that parameter estimates may be unreliable owing to misspecification. We assume that the errors are uncorrelated (white noise), and we investigate under two different model specifications: (I) with an intercept and (ii) with a linear time trend.

4.2 Fractionally cointegrated VAR (FCVAR) for Unemployment rates

This study examines the long run association between unemployment and other macroeconomic fundamentals using the FCVAR approach proposed by Johansen and Nielsen (2012). Since the traditional CVAR model is the baseline model for the FCVAR model, we begin our specification of the latter based on the former.³ Assuming Z_t is a vector of I(1) time series of dimension p, the CVAR model can be expressed in the error correction form as:

$$\Delta Z_{t} = \alpha \beta' Z_{t-1} + \sum_{i=1}^{k} \Gamma_{i} \Delta Z_{t-i} + \varepsilon_{i} = \alpha \beta' L Z_{t} + \sum_{i=1}^{k} \Gamma_{i} \Delta L^{i} Z_{t} + \varepsilon_{t}$$
(5)

³ Excluding theoretical papers, the application of the FCVAR approach is limited, to the best of our knowledge, as few papers have been published in this regard. The most prominent involves commodity returns (see Dolatabadi, Nielsen, & Xu, 2016; Dolatabadi et al., 2018) exchange rates (see Gil-Alana & Carcel, 2018), Inflation persistence (Tule et al., 2020), Islamic stocks (Salisu et al., 2020), political support & economic voting (see Nielsen & Shibaev, 2018; Jones, et al., 2014) and interlinkages between precious metals and Oil (Usman & Akadari, 2021).

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The FCVAR model is derived from equation (5) above by replacing the Δ and L in the equation with Δ^d and L_b , respectively. This gives:

$$\Delta^{d} Z_{t} = \alpha \beta' \Delta^{d-b} L_{b} Z_{t} + \sum_{i=1}^{k} \Gamma_{i} \Delta^{d} L_{b}^{i} Z_{t} + \varepsilon_{t}, \qquad (6)$$

where Δ^d represents the fractional difference operator, and $L_b = 1 - \Delta^b$ is the fractional lag operator. Within the context of this study, the most relevant parameters are the long run parameters α and β which are $p \times r$ matrices with $0 \le r \le p$. The rank r is the cointegration, or cofractional, rank. The columns of β constitute the r cointegration (cofractional) vectors such that $\beta' Z_t$ are the cointegrating combinations of the variables in the system, i.e. the long-run equilibrium relations. The parameters in α are the adjustment coefficients which represent the speed of adjustment towards equilibrium for each of the variables. The short-run dynamics of the variables are captured by the parameters $\Gamma = (\Gamma_1, \dots, \Gamma_k)$ in the autoregressive augmentation (Nielsen & Popiel, 2018).⁴ Note that if d = b = 1, the FCVAR model reduces to the CVAR variant. Confirming that the CVAR is a special case of the FCVAR

The procedure for estimation of the FCVAR is presented in the following steps: (i) the optimal lag length model is determined; (ii) the cointegration rank is determined; (iii) information from (i) and (ii) is used to test for fractional cointegration; and finally, (iv) the FCVAR model is compared with the CVAR model using the LR test which restricts d = b = 1 under the null hypothesis. A rejection of the null hypothesis supports the FCVAR approach, if not, the CVAR approach is preferred.

5. Discussion of results

5.1 Preliminary analyses

Quarterly data over the period of 1990 to 2018 is used for the analyses. The data was obtained from Statistical Bulletin of the Central Bank of Nigeria (2019) and the Database of National Bureau of Statistics (2019). Some descriptive statistics are rendered in Table 1 The full sample is segregated into two sub-samples consisting of before and after the global financial crisis, which is denoted as Pre-GFC and Post-GFC, respectively. The Pre-GFC sample is defined as the period before the first quarter of 2008, while the Post-GFC includes the Crisis period and the period after it. From Table 1, it can be inferred that unemployment rates were higher and more volatile during the post-GFC period than the pre-GFC period as the unemployment rate recorded higher mean and standard deviation values during the former than the latter. Also, the unemployment series seem to exhibit more asymmetry during the period of post-GFC than the pre-GFC, while the sub-samples are negatively skewed with longer left tail. Similarly, following Westfall (2014), the sub-samples as shown in Table 1 are platykurtic (shorter and thinner tails).

The descriptive analysis is accompanied by the plot of the unemployment rate which is shown in figure 1, which patently displays a mild undulating trend in unemployment rate during the period before the GFC,

⁴ We use the Nielsen and Popiel (2018) Matlab program to estimate both the CVAR and the FCVAR models.

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particularly between 1990 and 2000, which could be attributed to the aftermath of oil windfall slightly followed by the Structural Adjustment Programme pursued by the Nigerian government. The post-GFC is characterized by a steady rise in unemployment rate, which reached its zenith at 43.3 per cent in 2018Q3. Although this period ironically coincides with the return of Nigeria to democratic rule, however, long decay of infrastructure associated with military intrusion in our democratic space characterized by poor macroeconomic management and political interference in the operation of monetary policy left much to be desired. Also, between 2016 and 2017, the economy witnessed stagflation and recession. The discrepancies in the trend of unemployment rate in Nigeria, over the two sub-samples, constitute the motivation for the empirical analysis.

	Table 1: Descriptive Statistics									
	Unemployment	Inflation	Interest Rate	Output	WTI	Brent				
Mean	15.246	19.041	24.119	16,046,691	48.243	49.588				
Median	13.206	12.785	22.740	16,067,612	42.461	42.508				
Maximum	44.000	89.570	45.300	19,041,438	124.067	122.244				
Minimum	1.500	0.220	17.580	12,583,478	12.897	11.090				
Std. Dev.	11.508	17.968	4.663	1,683,796	29.758	33.515				
Skewness	0.687	2.087	1.317	-0.139	0.660	0.722				
Kurtosis	2.661	6.680	5.870	2.243	2.213	2.227				
Jarque-Bera	9.340***	144.499***	70.835***	0.976	11.013***	12.511***				
ADE	-10.101 ^{***b}	-7.152***b	-9.635***a	-68.084^{***a}	-8.646 ^{***a}	-8.364***a				
ADI	[0] (1)	[0] (1)	[0] (1)	[2] (2)	[0] (1)	[0] (1)				
AR(1)	0.968 ^{***b}	0.916 ^{***b}	0.847^{***a}	0.681^{***a}	0.951 ^{***a}	0.963 ^{***a}				
			Narayan et a	l. (2016)						
Constant	1.035	0.983	1.905	0.165	1.089	1.128				
Collstallt	[0.772]	[5.515]	[1.632]	[0.151]	[1.023]	[0.930]				
Constant & Trend	1.037***	0.984	2.057	0.778	1.146	1.144				
	[0.269]	[5.732]	[1.479]	[2.501]	[1.039]	[0.963]				
Observations	112	112	112	36	112	112				

Note: ***, **,* characterize the significant levels at 1%, 5% and 10% respectively. Values in "[]" are the optimal lags of the Augmented Dickey-Fuller (ADF) tests and the values in "()" are the order of integration after which the respective series reach stationarity The superscripts a, b represent the underlying ADF and AR(1) tests conducted with either constant or with constant and trend respectively. All the ADF tests are conducted with maximum lag 12, except for output at lag 6. The Narayan et al. (2016) is a GARCH model based unit root test that allows for 2 structural breaks.

Table 1 presents the descriptive statistics of the data used in this study, which include unemployment rate, inflation rate, interest rate, output, West Texas Intermediate (WTI) and Brent. All the series except output, which commenced from 2010Q1, have the same start dates, commencing from 1991Q1. Consequently, there are about 112 data points for the other series except output data, which has only 36 data points. With the exception of inflation and interest rates that are leptokurtic, all the other series are found to be platykurtic, and have skewness values different from that of the normal distribution. Consequently, we find statistically significant Jarque Bera test statistic for all the series except output.

By way of further examining the series for inherent statistical properties and providing some preliminary results, the ADF unit root test is conducted for all the series. We find all the series to have unit roots, and consequently,

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are non-stationary. While all the series except output are integrated of order one, output is integrated of order two, given that it requires differencing twice. The ADF model with constant and trend is however favoured by unemployment rate and inflation rate, while the ADF model with constant only favours the interest rate, output, WTI and Brent. Consequent upon the foregoing, we estimate an AR(1) model for each of the series, adapting the model framework as depicted by the ADF test. The results reveal some high levels of persistence as the coefficient of the first order autoregressive term is found to range between 0.681 and 0.968. Furthermore, for the purpose of robustness and ascertaining the stationarity of the series, the Narayan et al. (2016) GARCHbased unit root testing framework is also employed. The observed high persistence is not statistically significant, except in the case of the unemployment series. This observed conflicting stance is further subjected to the fractional integration, in order to provide some additional information on the shortness, or otherwise, of the memory; with short memory confirming stationarity, while long memory stance would either be stationary of non-stationary, depending on the observed persistence level.





5.2 Fractional Integration Analyses

Following from the preliminary results in the previous section, we employ the fractional integration technique to ascertain the stance of stationarity. The fractional integration provides information on the memory length of each of the series, in which case, there are three possible outcomes. The first is when the estimated fractional integration parameter is any value between zero and half (i.e., $0 < d \le 0.5$), which indicates that the series is stationary (and as expected have mean reverting properties), though exhibiting long memory feats. In the second case, the fractional integration parameter lies within half and unity (i.e., 0.5 < d < 1), which indicates that the impacts of shock to the series may take a longer time period to decay/fizzle out. Finally, the case where d > 1, indicates that persistence may be permanent. The testing framework is therefore examined with and without deterministic

trend, while adopting the Wald test to ascertain whether the fractional parameter differs significantly from half and unity, separately. The results are presented in Table 2, for the full sample, pre-GFC and post-GFC, respectively.

		Full Sample		Pro	e-GFC	Post-GFC		
		Constant only	Constant & Trend	Constant only	Constant & Trend	Constant only	Constant & Trend	
	J	0.496***	0.495***	0.493***	0.4845**	0.489^{***}	0.488^{***}	
	a	[0.038]	[0.019]	[0.038]	[0.065]	[0.050]	[0.059]	
Brent	<i>d</i> = 0.5	0.009	0.068	0.031	0.055	0.053	0.041	
	<i>d</i> =1.0	175.651***	699.658***	178.943** *	63.719***	105.779***	74.613***	
	d	0.496***	0.496***	0.4936***	0.493***	0.482***	0.481***	
	<i>u</i>	[0.013]	[0.024]	[0.022]	[0.040]	[0.0459]	[0.053]	
Inflation	<i>d</i> = 0.5	0.103	0.036	0.086	0.034	0.162	0.125	
	<i>d</i> =1.0	1574.159** *	439.705***	536.081** *	160.459***	127.518***	97.292***	
	J	0.491***	0.491***	0.483***	0.482***	0.492***	0.467***	
	a	[0.035]	[0.025]	[0.046]	[0.070]	[0.054]	[0.096]	
Interest rate	<i>d</i> = 0.5	0.062	0.125	0.137	0.070	0.020	0.117	
	<i>d</i> =1.0	214.668***	404.695***	128.993** *	55.034***	87.908***	30.749***	
	d	0.498^{***}	0.497***	0.496***	0.491***	0.494***	0.491***	
		[0.024]	[0.030]	[0.042]	[0.047]	[0.088]	[0.046]	
Unemployme nt	<i>d</i> = 0.5	0.005	0.013	0.012	0.037	0.005	0.044	
	<i>d</i> =1.0	446.262***	274.092***	144.651** *	119.269***	33.143***	125.048***	
	d	0.496***	0.494***	0.493***	0.485***	0.486^{***}	0.484^{***}	
	a	[0.039]	[0.019]	[0.037]	[0.064]	[0.052]	[0.060]	
WTI	<i>d</i> = 0.5	0.012	0.102	0.033	0.059	0.074	0.067	
	<i>d</i> =1.0	171.935***	730.469***	184.255** *	65.303***	96.504***	73.625***	
	d					0.448^{***}	0.037	
	<i>u</i>					[0.109]	[0.166]	
Output	d = 0.5					0.229	7.797***	
	<i>d</i> =1.0					25.748***	33.754***	

 Table 2: Persistence using Fractionally Integrated Approach

Note: Values in square brackets are standard errors of the associated d coefficients. ***, **, * represent 1%, 5% and 10% levels of significance respectively

We find five series (Brent, inflation, interest rate, unemployment and WTI) in Table 2 to exhibit long memory consistently across sample periods, regardless of whether the model with constant only or the model with constant and trend is adopted. Each of the statistically significant fractional integration parameter is further subjected to the Wald test statistic, to ascertain the extent of long memory inherent in the corresponding series. There are consistent non-rejections of the Wald test with the null hypothesis that the fractional integration

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parameter is not statistically different from half (i.e., d = 0.5). However, we find consistent rejections of the Wald test with the null hypothesis that the fractional integration parameter is not statistically different from unity. Imperatively, all the series are found to exhibit long memory and are stationary, regardless of the sample period or the model structure adopted. Specifically, Nigeria unemployment rate appears to be stationary, thus confirming absence of unemployment hysteresis in Nigeria as reported by Yaya et al. (2019). We however find the output series differs a little from the other series as the former tends to exhibit short memory (i.e., d = 0), when the model with constant and trend is adopted. Conclusively, unemployment rate, as well as the other macroeconomic variables investigated, except output, exhibit long memory and are stationary with a fractional order. Therefore, the shock to these variables is not likely to a lasting effect.

5.3 Fractional Cointegration VAR (FCVAR) analyses

Having established that the integration of the unemployment rate as well as inflation rate, interest rate, WTI, Brent and output, is of a fractional order rather than integer numbers, we proceed to examine whether these series are fractionally cointegrated, by estimating both CVAR and FCVAR models of Johansen (1995) and Johansen and Nielsen, (2012), respectively. We examine the integrated parameter estimate for its closeness to unity, while adopting the LR statistics to draw the conclusion of the more preferred model. Significant LR statistics therefore indicate preference in favor of the FCVAR model over the CVAR model. Also, in cognizance of the procedure for estimating the integrated parameter in the FCVAR model framework, we follow the three steps accordingly. First, we determine the optimal lag length, from the set maximum lag of 5, using AIC. Subsequently, the cointegrating rank is also determined using the LR statistic and finally, using the optimal lag and cointegrating rank, the integrated parameters are estimated. We therefore render these analyses for models with and without deterministic trend, first for the full sample and then, as a check for robustness, the pre-GFC and post-GFC sample periods. We also consider in addition to the bivariate cointegration between unemployment and each of the stated macroeconomic variables, a trivariate case that combines unemployment rate, inflation rate and output.

For the bivariate case of unemployment and inflation under the model without deterministic trend, the optimal lag is 1 for full sample, while for the bivariate case of unemployment and interest rate under the model without deterministic trend, the optimal lag is 2 for the full sample. The optimal lag for the bivariate cases under the model with deterministic trend differ depending on the sample period considered. However, in all the cases, the optimal lag length is at least 1 (see results in Table 3). In the trivariate construct, the optimal lag is found to be 3 (Table 4). On the cointegration results (see Table 5 and 6), we find the cointegration rank to be mostly 1. We however do not find any case of no cointegration in the stated bivariate cases, given that the non-rejection of the null hypotheses of no cointegration is observed for at least 1 cointegrating vector, and this cuts across both model constructs. Imperatively, there exists evidence of cointegration between unemployment and each of the examined macroeconomic variables. This therefore informs the further examination of the fractional integrated parameter, for the nature of the cointegrating relationship between unemployment and the other macroeconomic variables.

	Table 3: Lag Selection result for FCVAR (Bivariate Case)									
17	Full	Sample	Pre-	-GFC	Pos	t-GFC				
K	AIC	BIC	AIC	BIC	AIC	BIC				
		Pane	A: Without dete	rministic trend						
			Unemployment an	nd Inflation						
3	1074.55	1126.20	743.32	786.58	245.63*	277.72				
2	1067.15	1107.93	735.18	769.33	259.04	284.38				
1	1061.68^{*}	1091.58	729.71^{*}	754.75	253.62	272.20				
0	1065.82	1084.85^{*}	731.71	747.65*	250.57	262.39*				
	Unemployment and Interest Rate (Max)									
3	888.48	940.13	614.87*	658.13	186.85^{*}	218.93	-			
2	886.30^{*}	927.07	617.85	652.00	204.24	229.58				
1	897.13	927.03	622.94	647.98	200.38	218.95				
0	892.36	911.39*	618.40	634.34*	197.16	208.98^{*}				
		Pan	e B: With deteri	ninistic trend						
			Unemployment an	nd Inflation						
3	1043.97*	1101.05	725.55	773.36	237.93*	273.40	-			
2	1056.22	1102.43	729.62	768.32	240.29	269.00				
1	1060.36	1095.7	725.41*	755.01	244.89	266.85				
0	1063.57	1088.04^{*}	728.36	748.85^{*}	248.39	263.59^{*}				
		Unem	ployment and Inte	erest Rate (Max)			-			
3	890.55	947.63	620.78	668.59	176.63*	212.10^{*}	-			
2	888.05^{*}	934.27	618.44^{*}	657.15	194.62	223.33				
1	899.79	935.13	624.55	654.15	199.90	221.86				
0	895.01	919.48^{*}	619.99	640.48^{*}	197.74	212.94				

Note: AIC is the Akaike Information Criterion; SIC is the Schwartz Information. The optimal lag length is obtained using AIC, while the maximum lag is set at 3. The test equations involve two options: one that allows for intercept only and the other option that involves both the intercept and trend. The Pre-GFC and Post-GFC periods denote periods before and after the global financial crisis

Table 4: Lag Selection result for FCVAR (Bivariate and Trivariate Case for Output)

V -	Unemploymen	t and Output	Unemployment, Inflation and Output			
K -	AIC	BIC	AIC	BIC		
		Pane A: Without d	eterministic trend			
3	1124.97*	1155.05*	1249.54*	1312.88*		
2	1189.38	1213.13	1264.66	1313.75		
1	1206.20	1223.62	1306.81	1341.65		
0	1209.53	1220.62	1324.57	1345.16		
		Pane B: With det	erministic trend			
3	1125.52*	1158.77^{*}	1250.22	1318.31		
2	1178.84	1205.76	1244.91*	1298.75^{*}		
1	1205.69	1226.28	1297.36	1336.94		
0	1204.56	1218.81	1324.07	1349.41		

Note: AIC is the Akaike Information Criterion; SIC is the Schwartz Information. The optimal lag length is obtained using AIC, while the maximum lag is set at 3. The test equations involve two options: one that allows for intercept only and the other option that involves both the intercept and trend. The Pre-GFC and Post-GFC periods denote periods before and after the global financial crisis

Dault		Full Sample			Pre-GFC			Post-GFC		
Kank	D	LR Statistic	P-value	D	LR Statistic	P-value	D	LR Statistic	P-value	
			Pane	e A: Witho	out Determinis	tic Trend				
			Α	1: Unemp	loyment and Inf	lation				
0	0.621	18.241	0.014	1.025	3.070	1.000	0.010	8.939	0.063	
1	1.232	2.849	0.671	1.072	0.109	1.000	0.010	0.981	0.322	
2	1.109			1.099			0.010			
			A2: Un	iemployme	ent And Interest	Rate (Max)				
0	1.223	16.181	0.237	0.939	14.852	0.200	1.132	29.706	0.003	
1	1.347	0.623	0.998	0.777	7.264	0.074	1.563	21.982	0.000	
2	1.312			0.01			0.010			
			Pa	ne B: Witl	h Deterministic	: Trend				
			В	81: Unemp	loyment and Inf	lation				
0	0.089	20.979	0.000	0.972	10.213	0.002	0.010	10.423	0.001	
1	0.095	0.709	0.400	1.011	0.667	0.477	0.010	0.138	0.710	
2	0.149			1.112			0.010			
			B2: Ui	nemploym	ent and Interest	rate (Max)				
0	1.161	15.178	0.000	1.092	12.149	0.001	1.083	40.741	0.000	
1	1.318	0.000	1.000	1.285	2.434	0.150	0.011	0.040	0.842	
2	1.319			1.323			0.010			

Note: d is the fractional parameter; LR stat. is the Likelihood Ratio statistic; the test equations involve two options: one that allows for intercept only and the other option that involves both the intercept and trend. The Pre-GFC and Post-GFC periods denote periods before and after the global financial crisis.

(Divariate and Trivariate Case for Output)										
Douls	Unem	ployment and (Dutput	Unemplo	Unemployment, Inflation and Output					
Капк	d	LR Statistic	P-value	d	LR Statistic	P-value				
Pane A: Without Deterministic Trend										
0	1.536	5.054	0.998	0.010	25.117	0.003				
1	1.579	0.011	1.000	1.557	5.794	0.990				
2	1.576			1.563	0.002	1.000				
3				1.564						
		Pane B: V	Vith Deterr	ninistic Tre	end					
0	1.489	7.056	0.013	0.010	70.610	0.000				
1	1.492	1.611	0.287	0.010	2.373	0.123				
2	1.504			0.010	0.122	0.727				
3				0.010						

Table 6: Likelihood Ratio Test for Cointegrating Rank (Bivariate and Trivariate Case for Output)

Note: *d* is the fractional parameter; *LR* stat. is the Likelihood Ratio statistic; the test equations involve two options: one that allows for intercept only and the other option that involves both the intercept and trend.

On the comparison between FCVAR and CVAR (see Tables 7 and 8), we find the integrated parameter to be greater than 1, in all the bivariate cases using the full sample periods and adapting models with and without deterministic trend, except in the case where unemployment is paired with inflation rate and adapting model with deterministic trend. In the trivariate case, which combines unemployment, inflation and output, the

integrated parameter is found to be far less than 0.5 when model with deterministic trend was adopted, and greater than 1 for the model without deterministic trend. Consequently, the FCVAR model is preferred over the CVAR model in all the bivariate cases, except the bivariate construct that paired unemployment with inflation in model without deterministic trend. Under a different model structure, when deterministic trends are incorporated, the FCVAR model is consistently preferred over the CVAR model. The bivariate case, pairing unemployment and output, unarguably favours FCVAR over CVAR, regardless of the model structure. This feat of FCVAR preference is also observed in the trivariate case. Imperatively, while FCVAR model is more likely to be preferred over the CVAR when a model without deterministic trend is employed, the incorporation of a deterministic trend could further improve the preference of FCVAR over the CVAR model. While unemployment appears to share common long run relationships individually with inflation, interest rate and output, the observed long run relationships are better formed with FCVAR, rather than CVAR. Also, Nigeria unemployment rate therefore exhibits long memory but is non-stationary, thus shock to rate of unemployment may be permanent.

Daired	Full Sample		Pre-	GFC	Post-GFC				
Variables	d (Std. err.)	d LR-stat. Std. err.) (p-value)		LR-stat. (p-value)	d (Std. err.)	LR-stat. (p-value)			
Pane A: Without Deterministic Trend									
Unemployment & Inflation	1.232(0.07	1.885(0.170	1.025(0.11	0.043(0.83	0.010(0.00	19.610(0.00			
Unemployment & innation	7))	9)	6)	0)	0)			
Unemployment & Interest	1.223(0.08	4.317(0.038	0.939(0.12	0.218(0.64	0.010(0.00	24.469(0.00			
Rate	3))	8)	1)	0)	0)			
	1	Pane B: With De	eterministic Tre	nd					
	0.095(0.00	30.218(0.00	1.011(0.18	0.003(0.95	0.010(0.00	20.093(0.00			
Unemployment & Inflation	0)	0)	7)	6)	0)	0)			
Unemployment & Interest	1.318(0.08	9.731(0.002	1.285(0.11	4.459(0.03	0.011(0.00	35.362(0.00			

Table 7: FCVAR versus CVAR (Bivariate Case)

Note: The LR test restricts the fractional parameter to 1 under the null. Thus, the non-rejection of the null implies the adoption of the CVAR model, while the reverse favours the FCVAR. The Pre-GFC and Post-GFC periods denote periods before and after the global financial crisis

2)

5)

0)

Table 8: FCVAR versus CVAR (Output)

6)

	Without deter	rministic trend	With deterministic trend		
Variables	D (Std. err.)	LR-stat. (p-value)	d (Std. err.)	LR-stat. (p-value)	
Bivariate (Unemployment & Output)	1.536(0.047)	53.162(0.000)	1.492(0.079)	21.938(0.000)	
Trivariate (Unemployment, Inflation and Output	1.557(0.062)	20.083(0.000)	0.010(0.000)	75.324(0.000)	

Note: The LR test restricts the fractional parameter to 1 under the null. Thus, the non-rejection of the null implies the adoption of the CVAR model, while the reverse favours the FCVAR.

6. Robustness Check

Following from the foregoing, having established the consistency in the preference in favour of the FCVAR over the CVAR, we proceed to examine the sensitivity of the result to different choices, with respect to the sample periods (Pre-GFC and Post-GFC) and incorporation of a global factor as an exogenous variable. The sensitivity of our results to these factors are discussed subsequent sections.

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Rate

6.1 Are results sensitive to the sample periods?

Following the consistent preference of the FCVAR over the CVAR model, when the full sample data is examined under the models with and without a deterministic trend, we further ascertain if the results would be sensitive to the sample period considered. Consequently, the same analyses, as with the full sample data, are conducted using the pre-GFC and post-GFC samples. On the optimal lag, for the bivariate case of unemployment and inflation, under the models with and without deterministic trend, optimal lags of 1 and 3 are observed for the pre-GFC and post-GFC sample periods, respectively. In the case of unemployment and interest rate, under the model without deterministic trend, the optimal lag is 3 for both pre-GFC and post-GFC, and lags 2 and 3 for pre-GFC and post-GFC, respectively, when the model with a deterministic trend is estimated (see results in Table 4a). Across pre-GFC and post-GFC periods, cointegration rank is observed to be mostly 1. However, with reference to the pre-GFC period, we only reject the null of no cointegration at rank 1, only when the model with deterministic trend is adapted, but not so with the model without deterministic trend. This is indicative of presence (absence) of a long run relationship between unemployment and any of the macroeconomic variables - inflation and interest rate, when model with (without) deterministic trend is used. Interestingly, the stance of long run relationship between unemployment and the macroeconomic variables is established for the post-GFC period, as with the full sample period, earlier discussed. Consequently, the rejection of the null hypotheses of no cointegration of at least 1 cointegrating vector is observed in all the subcategorizations except the bivariate models pairing separately unemployment with inflation and interest rate under the model without deterministic trend (see results in Tables 5a and 5b).

The contest for preference between CVAR and FCVAR as presented in Tables 6a and 6b, reveals a higher preference in favour of CVAR over the FCVAR in the pre-GFC period and a higher preference in favour of the later over the former in the post-GFC period. The integrated parameter is observed to be slightly greater or less 1 (ranging between 0.939 and 1.285), in the pre-GFC period, while it is within the domain of 0.010 and 0.011, which is far less than 0.5, in the post-GFC period. While the pre-GFC period is characterized by integrated parameters that are closer to unity and long run relationships that are better formed by CVAR, the post-GFC period integrated parameters are closer to zero and the long run relationship between unemployment and the macroeconomic variables are better formed by FCVAR. Imperatively, the sample periods have differing stances in terms of the preferred model and the integrated parameter estimates, which is indicative of the sensitivity of estimated results to the sample period.

6.2 Are FCVAR results sensitive to incorporated intervening variables?

Here, we consider two global crude oil prices separately as intervening variables and introduce same in the subsequent analyses of fractional cointegration between unemployment and selected macroeconomic variables. The global oil prices are WTI and Brent and are incorporated as exogenous variables. While attempting to examine the impact of incorporating an intervening variable, we simultaneously check for the sensitivity of the results to the choice of global oil price used. We therefore compare the extended fractional cointegration model, which incorporates the global oil price as an intervening variable, with the version without any intervening variables (baseline). The comparison is done using the log-likelihood and the LR test statistic. While the former

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is used to compare the extended version with the baseline, the latter is employed to determine how best to treat the intervening variable; whether as endogenous or exogenous. Rejection of the null hypothesis of the LR test implies that the intervening variable should be treated endogenously, and exogenously, if otherwise. The results for the bivariate and trivariate model constructs, with and without deterministic trend; are presented in Tables 9 and 10.

	D P	E	xtended (WT	ſ I)	Ex	xtended (Brent)			
	Baseline	Endogenous	s Exogenous	LR Statistic	Endogenous	Exogenous	LR Statistic		
		I	Full Sample						
Without deterministic trend									
Unemployment & Inflation	-521.263	-921.903	-921.909	0.012	-919.787	-919.734	-0.106		
Unemployment & Interest Rate	-436.238	-824.691	-826.147	2.913*	-822.117	-823.301	2.367		
		With d	leterministic t	rend					
Unemployment & Inflation	-501.337	-897.161	-901.238	8.155***	-896.438	-900.109	7.341***		
Unemployment & Interest Rate	-427.026	-821.925	-823.548	3.247*	-819.628	-820.941	2.625		
Pre-GFC									
Without deterministic trend									
Unemployment & Inflation	-355.388	-601.613	-607.562	11.899***	-602.379	-607.673	10.588^{***}		
Unemployment & Interest Rate	-295.86	-515.821	-533.158	34.674***	-517.294	-533.513	32.437***		
		With d	eterministic t	rend					
Unemployment & Inflation	-350.04	-601.509	-603.933	4.847^{**}	-602.245	-603.98	3.472^{*}		
Unemployment & Interest Rate	-293.438	-530.056	-538.791	17.469***	-531.307	-539.095	15.576***		
			Post-GFC						
		Without	deterministic	trend					
Unemployment & Inflation	-104.307	-220.261	-220.332	0.141	-221.182	-221.272	0.181		
Unemployment & Interest Rate	-74.423	-200.515	-203.912	6.793***	-192.47	-198.196	11.453***		
With deterministic trend									
Unemployment & Inflation	-98.036	-210.783	-209.527	-2.511	-211.368	-210.913	-0.91		
Unemployment & Interest Rate	-67.338	-186.331	-187.212	1.76	-181.634	-185.965	8.663***		

 Table 9: Sensitivity of the FCVAR results to common global factors using log-likelihood and likelihood ratio test

Note: The figures in the tables are the log-likelihood values obtained from the FCVAR analyses, corresponding to the baseline and the extended FCVAR models. The baseline model does not include the intervening variables, while the extended version controls for them. The likelihood ratio (LR) test is employed to formally test whether the intervening variables should be treated as endogenous or exogenous. The restricted (unrestricted) model is evaluated under the null (alternative) hypothesis. The restricted FCVAR model treats the factors as exogenous, while the unrestricted model treats them as endogenous.

Table 10: Sensitivity of the FCVAR results to common global factors using log-likelihood and likelihood ratio test

	D		WTI			Brent		
	Baseline	Endogenous	s Exogenous	Endogenous	s Exogenous	LR Statistic		
Without deterministic trend								
Bivariate (Unemployment & Output)	-546.010	-668.998	-669.636	1.276	-666.883	-667.074	0.383	
Trivariate (Unemployment, Inflation and Output	-587.665	-697.177	-697.218	0.082	-695.103	-695.139	0.072	
	W	ith determir	istic trend					
Bivariate (Unemployment & Output)	-542.566	-664.904	-668.580	7.353***	-661.254	-666.518	-10.527***	
Trivariate (Unemployment, Inflation and Output	-589.641	-696.023	-698.063	4.081**	-695.982	-701.128	10.292***	

Note: The figures in the tables are the log-likelihood values obtained from the FCVAR analyses, corresponding to the baseline and the extended FCVAR models. The baseline model does not include the intervening variables, while the extended version controls for them. The likelihood ratio (LR) test is employed to formally test whether the intervening variable should be treated as endogenous or exogenous. The restricted (unrestricted) model is evaluated under the null (alternative) hypothesis. The restricted FCVAR model treats the factors as exogenous, while the unrestricted model treats them as endogenous.

A careful look through all the sub-categorizations shows that regardless of the global oil price proxy used as the intervening variable and also, regardless of how the intervening variable is treated, the extended fractional cointegration model does not perform better than the baseline fractional cointegration model. The feat is also replicated across the different sample periods, for all the bivariate and trivariate cases for models with and without deterministic trend. The extended FCVAR models are consistently observed to have smaller loglikelihood than the baseline FCVAR models, indicating that the inclusion of oil price in the FCVAR analyses of Nigeria's unemployment rate may have little or no impact. However, on the treatment of the intervening variable in the extended FCVAR model, we adjudge the intervening variable to be treated as endogenous (exogenous) if we reject (do not reject) the null hypothesis. Consequently, we find the exogenously incorporated oil price to have smaller log-likelihood in most cases than the endogenized oil price, across all the subcategorizations, when WTI is used, and something somewhat similar when Brent is used. Although, oil price does not seem to significantly improve the fit of the FCVAR model, it must be endogenized if at all it has to be incorporated in the FCVAR analyses.

	Develope	V	VTI	B	Brent			
	Baseline	Endogenous	Exogenous	Endogenous	Exogenous			
	FULL SAMPLE							
Without Deterministic Trend								
Unemployment and Inflation	1.232[0.077]	0.905[0.114]	0.905[0.113]	1.175[0.067]	0.949[0.111]			
Unemployment and Interest	1.223[0.083]	1.248[0.078]	1.240[0.079]	1.266[0.074]	1.264[0.074]			
1 5		With Determinis	tic Trend		LJ			
Unemployment and Inflation	0.095[0.000]	0.148[0.000]	0.188[0.048]	0.155[0.043]	0.175[0.047]			
Unemployment and Interest	1.318[0.086]	1.201[0.088]	1.197[0.087]	1.228[0.081]	1.228[0.080]			
		Pre-GF0	С					
Without Deterministic Trend								
Unemployment and Inflation	1.025[0.119]	1.112[0.106]	1.061[0.138]	1.113[0.108]	1.044[0.143]			
Unemployment and Interest	0.939[0.128]	0.010[0.000]	0.840[0.138]	0.010[0.000]	0.905[0.103]			
		With Determinis	tic Trend					
Unemployment and Inflation	1.011[0.187]	1.097[0.112]	1.062[0.177]	1.105[0.112]	1.043[0.192]			
Unemployment and Interest	1.285[0.112]	0.033[0.001]	0.960[0.170]	0.010[0.000]	1.000[0.135]			
		Post-GF	С					
		Without Determin	istic Trend					
Unemployment and Inflation	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]			
Unemployment and Interest	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]			
		With Determinis	tic Trend					
Unemployment and Inflation	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]			
Unemployment and Interest	0.011[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]	0.010[0.000]			
Note: The figures are the fractic	onal parameter e	estimates and the o	corresponding stan	dard errors.				

Table 11: Sensitivity of the FCVAR results to common global factors using fractional parameter

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Furthermore, on the fractional parameter estimates that are obtained from the extended and baseline FCVAR models (see results in Table 11 and 12), it is shown that baseline model seems to have greater fractional parameter estimates than the extended version with unemployment and inflation, while for the case of unemployment and interest rate, the baseline is less than the two extended versions.

¥	6	W	TI	Brent				
	Baseline	Endogenou s	Exogenous	Endogenou s	Exogenous			
FULL SAMPLE								
Without Deterministic Trend								
Bivariate (Unemployment & Output)	1.536[0.04 7]	1.498[0.033	1.492[0.03 6]	1.585[0.072	1.572[0.05 9]			
Trivariate (Unemployment, Inflation and Output	1.557[0.06 2]	1.719[0.038]	1.717[0.03 9]	1.790[0.040]	1.792[0.04 1]			
	With Determi	nistic Trend						
Bivariate (Unemployment & Output)	1.492[0.07 9]	1.481[0.031]	1.394[0.02 2]	1.531[0.057]	1.550[0.05 6]			
Trivariate (Unemployment, Inflation and Output	0.010[0.00 0]	0.010[0.000]	0.010[0.00 0]	0.010[0.000]	0.010[0.00 0]			

Table 12: Sensitivity of the FCVAR results to common global factors using fractional parameter

Note: The figures are the fractional parameter estimates and the corresponding standard errors.

7. Conclusion

Information about unemployment persistence facilitates adequate evaluation of the effectiveness of enacted policies. Rigorous analytic research efforts are thus required to provide the necessary information that would serve as input for subsequent policy formation and implementation. This study therefore sets out to test for unemployment persistence in Nigeria, using fractional integration and fractional cointegration techniques. We complement the research works in this area (see Tule et al., 2016; Tule et al., 2017a;b; and Caporale and Gil-Alana, 2018), given that they also adopt that the fractional integration technique and, we in addition provide robustness checks for possible generalization of results.

We utilize quarterly data spanning a period of 1990 to 2018 and obtained from Statistical Bulletin of the Central Bank of Nigeria (2019) and the database of National Bureau of Statistics (2019). Our variables include unemployment rate, inflation rate, interest rate, output, and West Texas Intermediate and Brent crude oil prices. We offer some preliminary data analyses to establish the presence, or absence, of some salient statistical features. From the ADF test and the estimated coefficient of the AR(1) model, the series are found to have unit roots and exhibit some differing levels of persistence. For the purpose of robustness in the unit root test framework, the Narayan et al (2016) GARCH-based unit root test is also conducted.

Furthermore, the individual series are examined using the conventional fractional integration technique, under different model specifications – model with constant only and model with constant and trend; and different sample periods – full sample, pre-GFC and post-GFC. We find that all the series are fractionally integrated with values in the neighbourhood of 0.5. The Wald test is thereafter employed to ascertain whether the estimated integrated parameter values differ statistically, first from a hypothetical value 0.5 and then, 1.0. We find that $17 \mid P \mid a \mid g \mid e$

the estimated integrated parameter estimates are not significantly different from 0.5, but are significantly different from unity. Imperatively, all the series exhibit long memory but are stationary and consequently have mean reverting properties. Nigeria unemployment rate is here shown to be stationary in support of Yaya et al.'s (2019) stance of absence hysteresis of unemployment in Nigeria. This translates to quick fizzling out of the impacts of shocks to these variables, especially unemployment.

Following a three step procedure for the estimation of the FCVAR model, we ascertain the optimal lag, the cointegration rank and finally, the integrated parameter estimates, along with the log-likelihood and likelihood ratio test statistics. The integrated parameter is thus estimated for models with and without deterministic trend, using all the three sample periods earlier stated. We pair unemployment with each of the other macroeconomic variables, resulting in different bivariate relationships and thereafter, combine unemployment with inflation and output, in a trivariate relationship structure. While we find differing optimal lags and cointegration rank to be mostly 1, we estimate the FCVAR model, and by default, the CVAR model, with which we compare the fit of our model. Generally, the FCVAR model is preferred to the CVAR model, across the sub-categorizations particularly with the incorporation of a deterministic trend. Convincingly, we state here that unemployment shares common long run relationships with inflation, interest rate and output, which is better formed with the FCVAR model. Also, Nigeria unemployment rate exhibits long memory but is non-stationary, thus shocks to rate of unemployment may be permanent. This implies that the hysteresis of unemployment does hold in the Nigerian context, going by the result of the FCVAR estimated integrated parameter, and opposes the stance of Yaya et al. (2019). The presence of cointegration estimation yielded different results.

As a good practice, we further subject our results to robustness checks, in a bid to answer two pertinent questions. The first hinging on the sensitivity of our results to sample period, while the second ascertains the sensitivity of our results to the incorporation of an intervening variable, say global oil price. On the sensitivity to sample period, we find the integrated parameters in pre-GFC period to be closer to unity with long run relationships that are better formed by the CVAR model, while the integrated parameters in the post-GFC period are closer to zero, with the established long run relationships between unemployment and the macroeconomic variables being better formed by the FCVAR model. The pre-GFC stance differs markedly from the full sample and the post-GFC periods. Thus, our results appear sensitive to the sample periods. On the sensitivity to intervening variables, we find that the choice of oil price does matter. Also, the model incorporating oil price appears to underperform the one without it, and exogenously incorporated oil price tends to have smaller log-likelihood compared to when oil price is treated endogenously. However, there seems to be no empirical validation for including oil price as an intervening variable in the estimation of integrated parameters using the FCVAR model, and if at all it has to be included, it must be treated endogenously.

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