



Bolted steel to laminated timber and glulam connections

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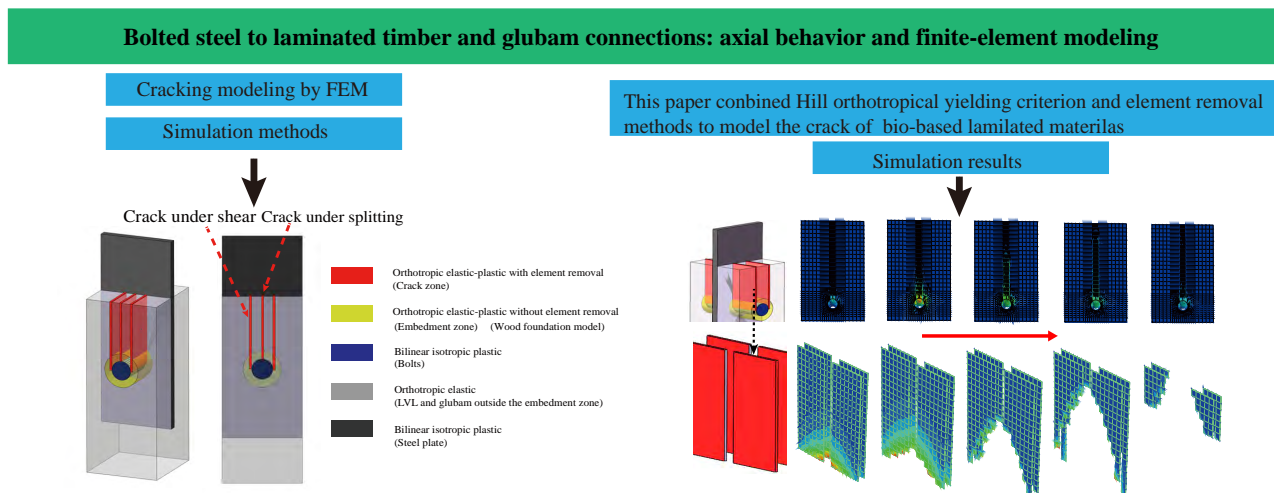
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Graphic abstract



Highlights

Bolted steel to laminated timber and glulam connections: axial behavior and finite-element modeling

Da Shi, Haonan Huang, Ning Li, Yiwei Liu, Cristoforo Demartino

- LVL connections exhibit higher ductility and lower capacity compared to glulam.
- High-fidelity finite-element model integrating Hill's yielding and element removal criteria.
- The proposed element removal criterion can effectively simulate crack growth.
- The Hill yielding criteria in UMAT subroutine can effectively model plastic behavior.
- The proposed theoretical formula can effectively predict the initial stiffness.

Bolted steel to laminated timber and glulam connections: axial behavior and finite-element modeling

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Abstract

This study aims to characterize the axial monotonic and cyclic tensile behavior of bolted steel connections to laminated timber and bamboo, using slotted-in steel plates, and to provide a high-fidelity simulation using finite-element modelling. Forty-eight experimental tests were conducted, including eight different configurations, varying in material (Laminated Veneer Lumber (LVL) and Glued Laminated Bamboo (glulam)), number of bolts, and diameter of bolts, under tension, both monotonic and cyclic (three repetitions). The force and displacement were recorded, and used to define the initial stiffness, yielding strength, ultimate strength, ductility, viscous damping, and energy dissipation. The failure modes of the connections were monitored using Digital Image Correlation (DIC) techniques. A novel high-fidelity finite-element model integrating Hill's yielding and element removal criteria was proposed to predict the mechanical performance and fracture behavior of the examined connections. The numerical simulation was validated by comparing the experimental load-displacement curves and the strain field measurements obtained with DIC. Finally, theoretical formulas for predicting the stiffness of bolted connections were proposed based on the FEM simulations.

Keywords: Bolted connections, Glue laminated materials, Composite wood, LVL, glulam, FEM

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34 1. Introduction

35 The construction industry widely employs bio-based laminated composite materials made from timber and
36 bamboo due to their favorable properties, including mechanical strength, renewable nature, economic viability,
37 and carbon storage capacity [1, 2]. To manufacture such materials, the lamination process is used, which involves
38 joining multiple layers of natural bamboo and timber using adhesives. This results in engineered structural
39 materials that have enhanced properties and are free from the irregularities of the parent natural materials.
40 The mainstream engineered timber products used in the industry include structural composite lumber (SCL),
41 glued-laminated timber (GLT), cross-laminated timber (CLT), and nailed-laminated timber (NCL) [3, 4]. In
42 contrast, the most commonly used engineered bamboo products are laminated bamboo [5], bamboo scrimber
43 [6, 7], and bamboo woven panel [8]. In this context, two different bio-based laminated materials, Laminated
44 Veneer Lumber (LVL) [9, 10] and glued laminated bamboo (glulam) [11, 12, 13], are typically used as the
45 primary component of bolted joints.

46 Wood joints have evolved significantly over time, with various types such as tenon-mortise, tooth, bolted,
47 metal-plate, and planting bar connections being developed to optimize their performance [14]. Bolted con-
48 nections with slotted-in steel plates are among the most commonly used types in wooden truss and moment
49 resisting frame structures. Research has been conducted over many years to analyze the mechanical behaviors
50 of these connections. For instance, Platt and Harries [15] used an experimental program to investigate the
51 bolted lap-splice behaviors of the bolted laminated bamboo connections in an aim to explore potential appli-
52 cations of using laminated bamboo strips to repair timber structures. He et al. [16], Lam et al. [17], Shu et al.
53 [18], Wang et al. [19] used the bolted glulam connections with slotted-in steel plate as knee braces for glulam
54 beam-to-column connections and investigated its moment resisting performance. Leng et al. [20] studied the
55 moment-rotation behavior of beam-to-column bolted connections in bamboo scrimber structures. Three types
56 of beam-to-column connections were designed and the influence of bolt arrangement and the local inclusion of
57 cross-laminated laminae locally in the connection region were investigated [21]. These studies indicates that the
58 specimens having cross-laminated laminae can avoid parallel-to-grain splitting failure initiating at the bolt lines.
59 Stehn and Börjes [22] investigated the influence of ductile connections, slotted-in nailed wood to steel joints, on
60 the total load-carrying capacity and deformability of a glulam truss. Kobel et al. [23] experimentally investi-
61 gated the application of LVL made of European beech wood in timber truss structures showing that dowel-type
62 connections can ensure high load-carrying capacities and ductile behavior. Innovative moment-resisting con-
63 nections for mid-rise timber moment frame structural systems have been proposed by Shu et al. [24]. These
64 connections are reinforced by long steel rods with screwheads and long self-tapping screws, providing a stiff
65 and resilient beam-to-column connection. The proposed system eliminates the need for shear walls or braces.
66 Wu and Xiao [25] proposed a new type of hybrid space truss system composed of steel lower chord and glulam
67 upper chords and web elements. The specially designed steel glulam hybrid space truss system was successfully
68 designed and constructed for a rain-shed canopy of an office building.

69 The Finite Element Model (FEM) of these connections requires an accurate definition of material constitutive
70 [26]. Hill yield criterion was commonly used in the numerical model of wood due to its orthotropic characteristics
71 [27, 28, 29]. Although the softening behavior of LVL and glulam was simulated to some extent by Hill yield
72 criterion, no crack propagation was considered in this criterion. Elasto-plastic material in compression with
73 Hill yield criterion and linear elastic material in tension with the maximum stress failure criterion were used in
74 the numerical model of Kharouf et al. [30]. A three-dimensional elasto-plastic model considering the material
75 degradation was developed by Wang et al. [31]. To better describe the local crushing behavior of the wood
76 near the bolts in connections, a wood foundation model was proposed by Hong and Barrett [32]. The material

77 properties of the wood near the bolts were obtained by embedment tests. Cohesive zone material laws were
78 used by He et al. [16] to trace the crack propagation of glulam connections.

79 However, an high-fidelity FE model of the axial monotonic and cyclic tensile behavior of bolted steel to
80 laminated timber and bamboo connections, using slotted-in steel plates has not been investigated and is still
81 not available.

82 In this framework, this study experimentally investigates the axial monotonic and cyclic tensile behavior
83 of bolted steel to laminated timber (LVL) and bamboo (glulam) connections, using slotted-in steel plates,
84 and provides a high-fidelity simulation using finite-element modeling. Results of the material property are
85 presented and discussed in Section 2.1. Section 2.2.1 provides detailed information on the specimens and their
86 fabrication process. Forty-eight experimental tests were conducted, including eight different configurations
87 that varied by material (Laminated Veneer Lumber (LVL) and Glued Laminated Bamboo (glulam)), bolt
88 number, and diameter. Each configuration was repeated three times under monotonic and cyclic loading,
89 respectively. The test set-up and loading regime are introduced in Sections 2.2.2. The experimental results
90 (monotonic and cyclic) are summarized in Section 2.3. Based on the experimental findings, this study provides
91 an innovative finite-element model for high-fidelity simulations (Section 3). In particular, this study attempts
92 to simulate the cracking behavior by combining Hill yield criterion with other failure criteria [33, 34]. The
93 proposed model implements the element removal criterion in the observed cracking area that can be determined
94 through experimental observations. On the basis of previous researches [35], Section 4 provides the derivation
95 of theoretical formulas for the initial stiffness of double bolted connections calibrated based on the outcomes of
96 the FEM simulations. Finally, conclusions and perspectives are drawn in Section 5.

97 2. Experimental tests

98 This Section describes the experimental test adopted to validate the proposed FE model and reports the
99 results. Section 2.1 describes the tests performed on the LVL and glulam together with the found material
100 properties. Section 2.2 reports the experimental tests performed providing an extensive description of the
101 specimens and test set-up. Finally, Section 2.3 provides results of the monotonic and cyclic tests. The failure
102 modes are also discussed.

103 2.1. Materials testing

104 The materials adopted in this study are: LVL, glulam, high-strength bolts (grade 8.8) with a length of
105 120 mm and a diameter of 8 and 10 mm, washers with external diameters of 14 and 16 mm for bolts of 8 and
106 10 mm, respectively, and Q235 steel plate with a thickness of 8 mm. LVL is an engineered timber composite
107 manufactured by laminated wood veneers with a thickness of 2 – 4 mm using exterior-type adhesives [36]. LVL is
108 made of poplar. Glulam is a type of engineered bamboo composite that resembles timber-based glued-laminated
109 lumber [37, 38]. Glulam is composed of Moso Bamboo strips that undergo cleaning and drying processes to
110 reach a moisture content of 18%. Subsequently, the strips are saturated in phenol formaldehyde resin.

111 Material tests were carried out to determine parallel-to-the-grain compression strength ($f_{c,0}$), elastic mod-
112 ulus (E_0), parallel-to-the-grain shear strength ($f_{v,90}$), perpendicular-to-the-grain tensile strength ($f_{t,90}$), dowel
113 bearing strength or embedment strength ($f_{h,0}$) and stiffness ($k_{h,0}$), and density (ρ). The subscript 0 indicates
114 parallel-to-the-grain direction while 90 refers to perpendicular-to-the-grain direction. Figure 1 [39] summarizes
115 the specimen geometry and test setup adopted to define the material properties previously discussed. All the
116 tests were repeated six times.

117 $f_{c,0}$ and E_0 were determined according to GB/T 50329-2002 [40]. $f_{v,0}$ is determined according to ASTM
118 D143 [41] with specimens having geometry reported in Figure 1b. $f_{v,0}$ is the peak load measured on the testing
119 machine divided by the applied area (50×50 mm, see Figure 1b). $f_{t,90}$ is determined according to ASTM D143
120 [41] with specimens having geometry reported in Figure 1c. $f_{h,0}$ was measured according to ASTM D 5764-97a
121 [42] using four specimens for each material having geometry reported in Figure 1d. A 8- and 10-mm-diameter
122 smooth tungsten steel dowel was employed in the tests. $k_{h,0}$ is the elastic stiffness calculated in the 10 – 40%
123 of peak load range as the stress divided by the corresponding displacement.

124 Table 1 presents the average test results and coefficient of variations (CV) of LVL and glulam. E_0 is
125 larger for LVL and $f_{c,0}$ for glulam. Similar results were reported in the literature for LVL [43, 44, 45] and for
126 glulam [46, 38]. $f_{v,0}$ and $f_{t,90}$ are slightly larger for glulam and consistent with those reported in the literature
127 [25, 38, 47]. $f_{h,0}$ and $k_{h,0}$ are calculated from the stress-displacement curves of dowel bearing strength tests.
128 $f_{h,0}$ and $k_{h,0}$ is larger for glulam and similar results were reported in the literature for LVL [48, 49] and for
129 glulam [46, 50, 38]. It is noteworthy that $k_{h,0}$ is expressed in the form of stress divided by the displacement,
130 therefore $k_{h,0}$ should be multiplied by d to obtain the stiffness per unit length in Winkler model [51].

131 The bolts were tested to determine the bending yield moment (M_y) and nominal yield strength (f_{yb}) accord-
132 ing to ASTM F1575-2003 [52]. The average M_y and f_{yb} are $62 \text{ N} \cdot \text{m}$ and 721 MPa for 8 mm bolt and $137 \text{ N} \cdot \text{m}$
133 and 824 MPa for 10 mm bolt.

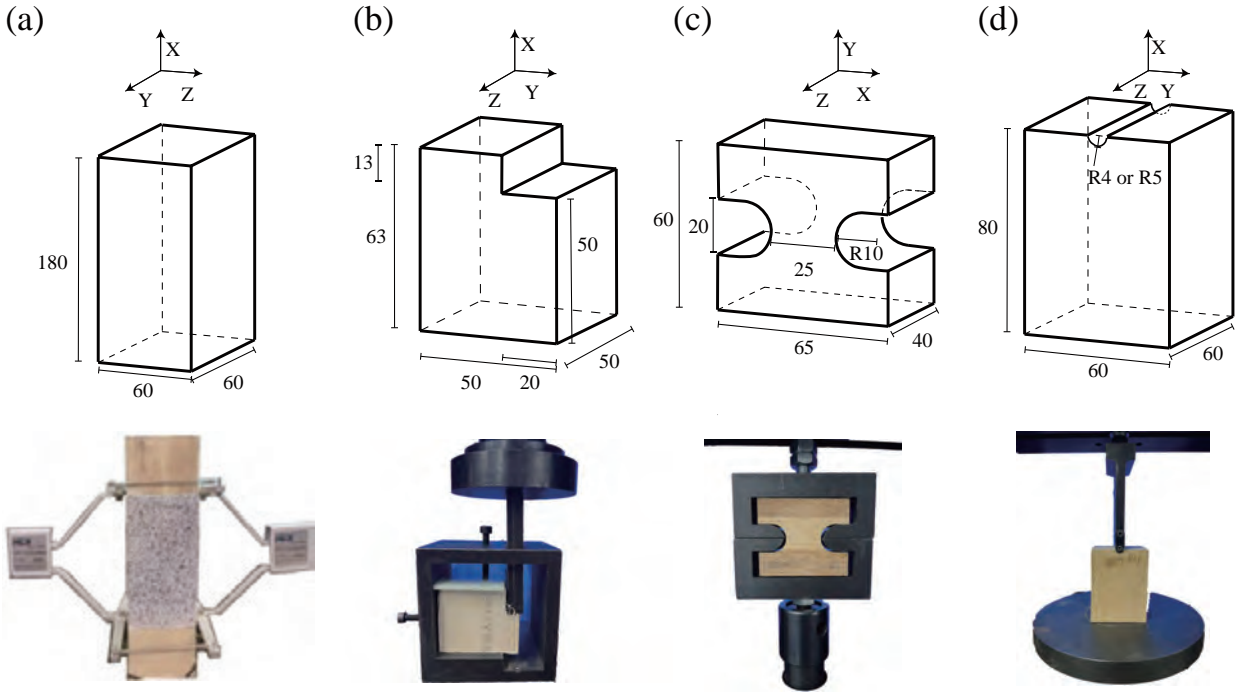


Figure 1: Specimen geometry and test setup for measuring compression strength and elastic modulus (a), parallel-to-the-grain shear strength (b), perpendicular-to-the-grain tension strength (c) and dowel bearing strength (d). Adapted from [39].

Table 1: Properties of LVL and glubam. The number in the parenthesis indicates the Coefficient of Variation (CV). After [39].

Material	E_0 [GPa]	$f_{c,0}$ [MPa]	$f_{v,0}$ [MPa]	$f_{t,90}$ [MPa]	$f_{h,0}$ (8 mm) [MPa]	$f_{h,0}$ (10 mm) [MPa]	$k_{h,0}$ (8 mm) [MPa/mm]	$k_{h,0}$ (10 mm) [MPa/mm]	ρ [kg/m ³]
LVL	11.45 (13%)	38 (6%)	6.98 (7%)	1.81 (25%)	40 (3%)	37 (8%)	42 (4%)	45 (10%)	614 (7%)
Glubam	8.56 (8%)	62 (13%)	8.18 (11%)	2.69 (14%)	86 (4%)	81 (7%)	79 (4%)	61 (6%)	749 (5%)

134 2.2. Experimental tests

135 2.2.1. Specimens: design and fabrication

136 The specimens were purposely fabricated to be affixed to the clamps of the testing machine, see Figure 3. To
 137 prevent any local damage or significant deformation of the LVL or glulam block, steel plates were consistently
 138 used to connect the specimens to the two clamps. Consequently, the specimens are equipped with two dissimilar
 139 slotted-in steel plates at either end (refer to Figure 2). The tested side, where connection damage is anticipated
 140 to occur (left side in each subfigure of Figure 2), is connected with fewer bolts. The other side is intended to
 141 have an adequately high capacity to endure the tests without damage. Hence, a larger number of bolts (four)
 142 is always utilized. The length of the connection specimen was established to strike a balance between the two
 143 conflicting requirements of having a sufficient length to evade interaction between the two connections at either
 144 end and the limited space available in the testing apparatus (refer to Section 3).

145 Four different configurations were investigated in this study, namely single and double bolts ($n = 1$ or
 146 2) and with a diameter of $d = 8$ and 10 mm. Moreover, LVL and glulam members are considered leading
 147 to a total of eight different configurations. Connections on the tested side are designed following geometric
 148 requirements of GB50005 [53]. The specimen configurations for single bolt and double bolts are summarized in
 149 Figure 2. The same geometry was considered for LVL and glulam and for $d = 8$ and 10 mm. Three identical
 150 specimens are tested to ensure the repeatability of the results under tensile axial monotonic and cyclic loading
 151 conditions. The geometric information of all specimens is displayed in Table 2. Specimens were named following
 152 the designation L (G)-M (C)-S (D)-X-Y. L (G) indicates materials (LVL or glulam), M (C) indicates the loading
 153 regime (Monotonic or Cyclic), S (D) is used to designate the amount of bolt used on the upper part (Single or
 154 Double), X indicates the bolt diameter (8 mm or 10 mm), Y indicates specimen number (1, 2 or 3). Therefore,
 155 a total of 48 specimens are realized. The three specimens adopted for test repetitions are fabricated using the
 156 same original blocks having a length of 4 m to ensure similar characteristics of the material employed.

157 The LVL and glulam member are 550 mm long and have the cross sectional dimensions of 60×60 mm and
 158 both of them are fabricated from the same batch of block with cross sectional dimensions of 60×60 mm. In all
 159 the cases, two 8 mm-wide slots are considered in the members for inserting steel plates. Holes are drilled on the
 160 LVL, glulam components and steel plates. Bolts protruding from these holes are adopted to connect the steel
 161 plate with LVL and glulam components. The steel plates were manufactured by laser cutting of Q235 steel
 162 plate and by drilling holes at specific locations. The steel plates are rectangular with a base equal to 60 mm

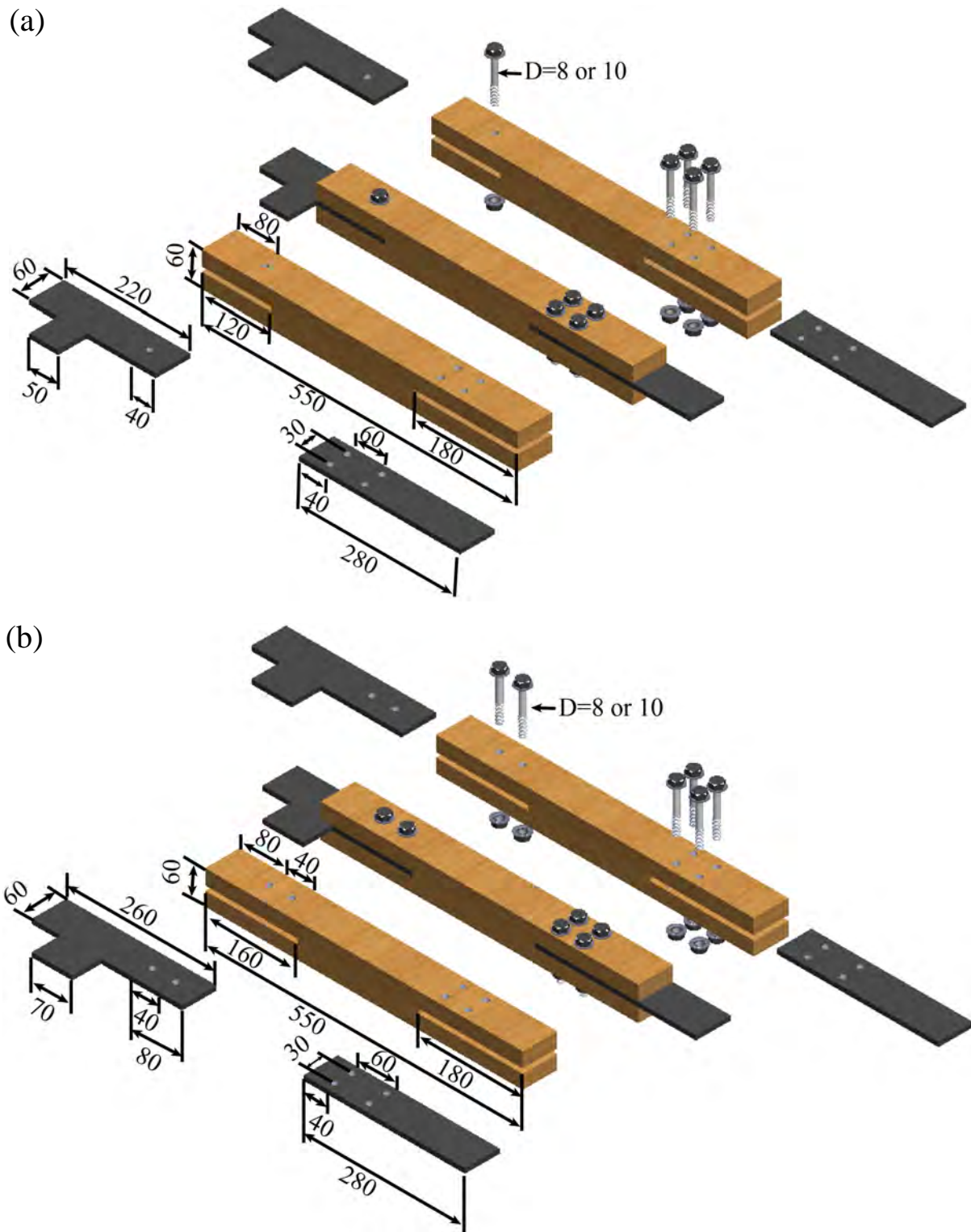


Figure 2: Configurations of single-bolted specimen (a) and double-bolted specimen (b). For each case, different diameters of bolts (8 mm or 10 mm) are considered. The specimens have two dissimilar slotted-in steel plates at each end. The tested side, where connection damage is expected, has fewer bolts. The other side has a higher capacity and always uses four bolts. The connection length is balanced between avoiding interaction between the two end connections and the limited space in the testing apparatus.

Table 2: Geometric information of different configurations. The table lists various configurations indicating the bolt diameter, bolt number, loading regime, and material used. The configurations include LVL and glulam materials, with monotonic or cyclic loading and different bolt diameters and numbers.

Configuration	Bolt diameter (mm)	Bolt number	Loading regime	Material	
L-M-S-8	8	1	Monotonic	LVL	
L-M-S-10	10				
L-M-D-8	8	2	Cyclic		
L-M-D-10	10				
L-C-S-8	8	1	Cyclic		
L-C-S-10	10				
L-C-D-8	8	2	Cyclic		
L-C-D-10	10				
G-M-S-8	8	1	Monotonic		Glulam
G-M-S-10	10				
G-M-D-8	8	2	Cyclic		
G-M-D-10	10				
G-C-S-8	8	1	Cyclic		
G-C-S-10	10				
G-C-D-8	8	2	Cyclic		
G-C-D-10	10				

and variable length (Figure 2). In particular, the length is equal to the sum of the slot length and 100 mm which is the zone of the plate adopted for clamping to the test machine. The steel plates on the tested side have an additional flag (rectangular area) used to connect a displacement transducer (Figure 3(c)). To ensure adequate tolerances during specimen assembly, the holes in LVL and glulam blocks were designed to be 0.5 mm larger. Torque control was a critical aspect, with high-strength bolts being tightened using a calibrated torque wrench. The torque was carefully controlled to prevent significant local deformation around washers, such as the penetration of the washer into the LVL or glulam block surface. Preliminary tests showed a pre-load torque of 0.7 N·m and 1 N·m for 8 mm and 10 mm diameter bolts, respectively, providing controlled friction conditions at the interface between the steel plate and slot surfaces.

The surfaces of the specimen opposite to the tested side, where bolt head and nuts are located, were treated for performing Digital Image Correlation (DIC) measurements, as described in Section 2.2.2. Specifically, the upper part of the specimen, located 230 mm from the end, was modified to create a high contrast texturing effect using white paint with a black speckle pattern, as depicted in Figures 3 (d).

2.2.2. Test set-up and measurements

Figure 3 illustrates the test setup used for the bolted connections. A 100 kN hydraulic actuator (186E, WANCE Ltd.) is used for the load application. The force is recorded by the actuator and the displacements at the connection through one displacement transducer. The upper end of the displacement transducer is fixed on the upper steel plate and the bottom end is fixed on the middle part of LVL and glulam elements.

Before testing, the surface of the specimens was painted with a high-contrast texturing effect, using white paint with a black speckle pattern, as shown in Figure 3(d), to carry out a strain field analysis over the surface of the specimens by DIC setup. Figure 3 provides a view of the DIC test setup. The photos were taken at a frame rate of 2/s with two cameras (body and a 25 mm lens), positioned symmetrically in front of two speckle surface, with the lens direct towards the centre of the speckle area and in perpendicular position in respect to the specimen surface. A speckle field with a size of 60mm×230mm was monitored. Two light sources of constant luminosity were used to maintain consistency in the measurements.

The software GOM Correlate was used to carry out the DIC analyses. GOM Correlate gives the displacement/strain field at each loading step by defining square-shaped sub-zones, called “facets”, in the initial image and tracking these sub-zones in subsequent images. The facets were defined over the random speckle pattern sprayed on the sample surface, which facilitated the definition of a grey level distribution sufficient to differentiate the sub-zones. A facet size of 19 pixels and a spacing of 16 pixels (point distance) (for full field analysis) were defined to accommodate both a good resolution and computational viability. A standard analysis, as defined by the software, was carried out.

Tensile monotonic and cyclic tests were performed according to EN12512 [54]. The monotonic loading protocol is comprised of a preloading phase and a normal loading phase. In the first phase, the specimen was loaded up to 10% of the ultimate load (estimated using some preliminary tests) followed by a constant load for 120 s. Then, the load was decreased to zero followed by a pause of 30 s. Subsequently, the loading was

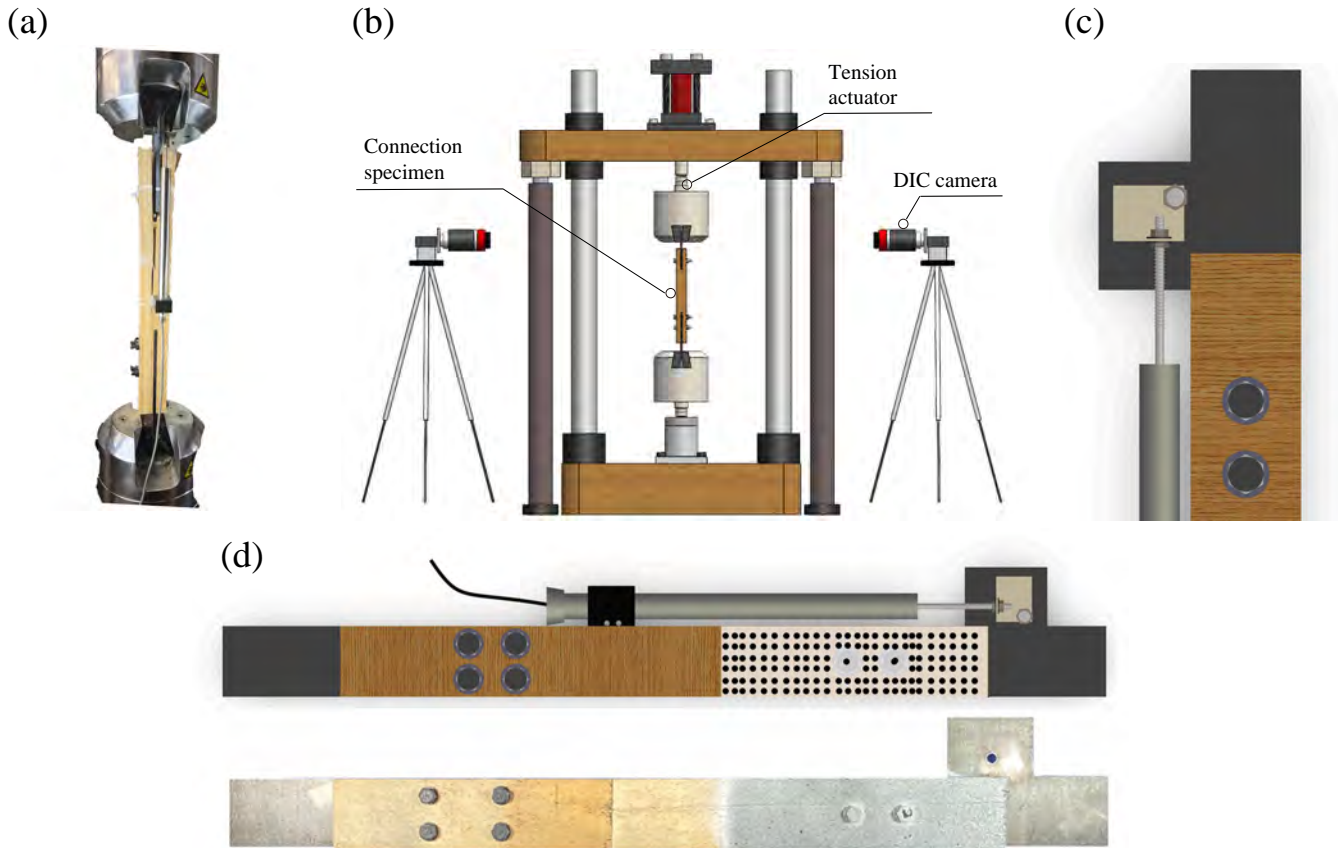


Figure 3: Test setup and instrumentation: photo (a), sketch (b), detail of the LVDT and steel flag (c,d), and speckle pattern for DIC analyses (d).

199 monotonically increased at a loading rate of 1.5 mm/min. The test was stopped at a displacement of 40 mm.
 200 The reason for the preloading phase was to eliminate the internal friction between the LVL, glulam component
 201 and steel plate and the settlement of the connection [55]. The cyclic loading protocol was conducted according
 202 to EN12512 [54]. However, a non-reversed modification of the procedure outlined in EN 12512 [54] was used to
 203 perform the cyclic test. The displacement was cycled from zero to a positive (tension) value without excursions
 204 into negative (compression) values [56], as shown in Figure A.23(a). The V_y varied among the configurations,
 205 depending on experimental yield values obtained from the monotonic tests in agreement with EN 26891 [57].
 206 The cyclic loading was conducted under displacement control mode at a loading rate of 0.2 mm/s until a slip of
 207 30 mm was reached.

208 Load vs. displacement curves were processed to obtain some synthetic indicators according to ASTM
 209 D5764-97a [42]. The following indicators are considered (Figure A.23(b)): initial stiffness (k_e), yielding load
 210 (F_y), maximum load (F_u), and ductility (D).

211 The specimens performance under cyclic loading conditions are also characterized in terms of the equivalent
 212 viscous damping (V_{eq}) and energy dissipation [58, 59, 60]. The equivalent viscous damping V_{eq} , defined as a
 213 ratio of the dissipated energy E_d to the available potential energy E_p (see Figure 4) multiplied by 2π (i.e.,
 214 $V_{eq} = E_d/2\pi E_p$) can be used for evaluating the cyclic performance of the bolted connections in terms of their
 215 energy dissipation capacity.

216 2.3. Results

217 2.3.1. Monotonic loading

218 Load vs. displacement curves of tensile monotonic tests are shown in Figure 5. Results are reported as each
 219 of the three tests (gray lines) and average across displacements (continuous red lines). Moreover, k_e , F_y , F_u ,
 220 and D (see Section 2.2.2 for their definition) of the tests reported in Figure 5 are summarized in Table B.7.

221 Figure 5 demonstrates the reproducibility of results for the three repetitions. The LVL and glulam con-
 222 nections exhibit similar trends in the elastic stage, but display different behaviors leading to various loading
 223 plateaus and failure modes. The load-displacement curves of glulam specimens exhibit a shorter load plateau
 224 stage and experience an abrupt failure due to longer propagating cracks. Conversely, the load-displacement
 225 curves of LVL connections are smoother, displaying a longer-lasting loading plateau stage. This distinction can

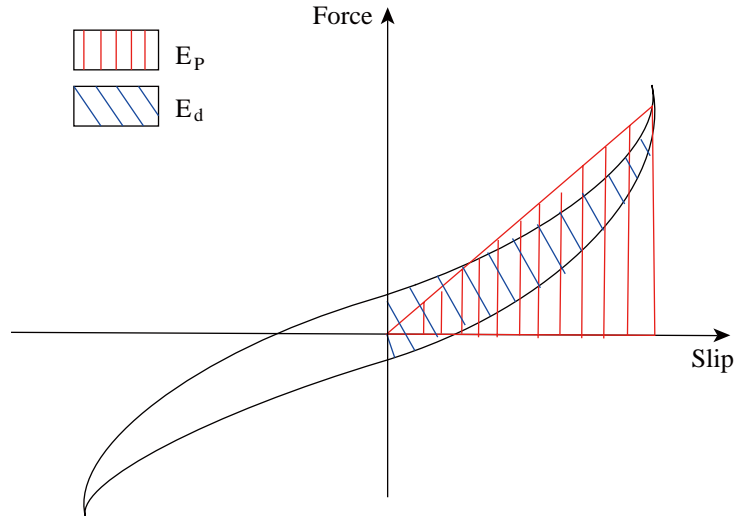


Figure 4: Determination of equivalent viscous damping on the hysteretic curve (force vs. displacement). The black line is the hysteretic curve for one cycle. The blue shaded area corresponds to the dissipated energy E_d and the red shaded area corresponds to the available potential energy E_p .

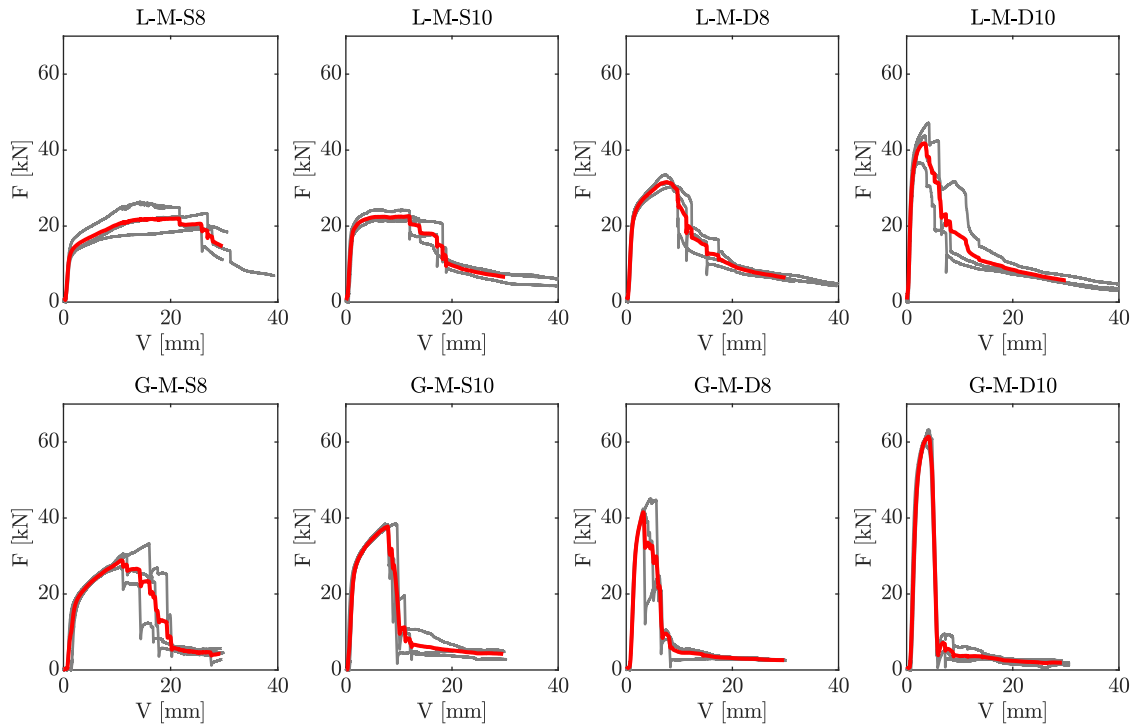


Figure 5: Load (F in kN) vs. displacement (V in mm) curves of tensile monotonic tests. The first row refers to tests performed on LVL while the second refers to glubam. The first two columns refers to single bolt and the last two to double bolts cases. The three gray lines are the three tests repetitions. The red line is the average of three tests across displacements. The average line ends when one of the test data is not available. After [39].

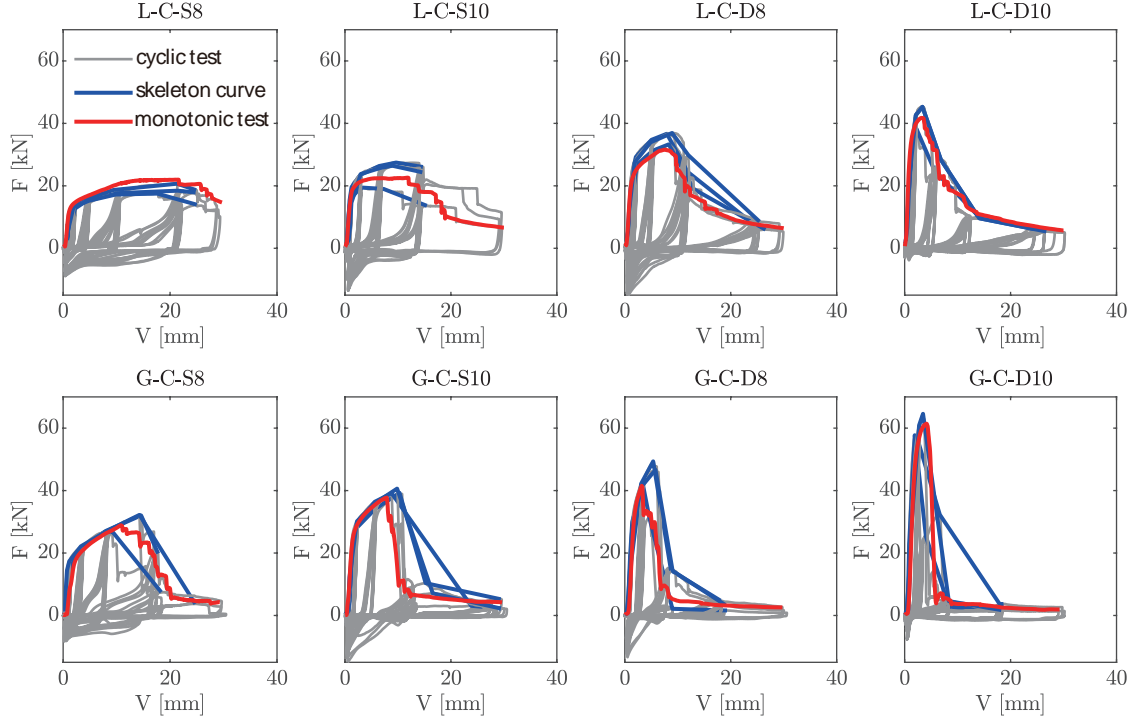


Figure 6: Load (F in kN) vs. displacement (V in mm) curve of cyclic loading tests. The first row refers to tests performed on LVL while the second refers to glubam. The first two columns refer to single bolt and the last two to double bolts cases. The three gray lines are the three test repetitions. The three blue lines are the skeleton curves of the three repetitions. The skeleton lines are calculated as the envelope of the cyclic tests. The red line is the average of three monotonic tests across displacements (see Figure 5). The average line ends when one of the test data is not available.

226 be attributed to the denser but thinner layers of LVL, resulting in a more homogeneous but softer material
 227 nature.

228 Table B.7 summarizes the initial stiffness, yield load, yield displacement, maximum load, and ultimate
 229 displacement, with statistical analysis performed on the results. The initial stiffness, yielding load, and maximum
 230 load capacity increase with increasing bolt diameter and number, while ductility exhibits an inverse relationship.
 231 Notably, the initial stiffness, yield load, and maximum load of D8 are generally higher, with lower ductility,
 232 compared to counterparts of S10, except for the initial stiffness of glubam. This finding suggests that the
 233 number of bolts have a strong influence on the observed mechanical properties more than the bolt diameter.

234 2.3.2. Cyclic loading

235 The hysteresis curves of three identical specimens of two types of materials (LVL and GLB) under cyclic
 236 loading are presented in Figure 6. As shown, the three replicates for each group of specimen exhibited similar
 237 response generally.

238 The equivalent viscous damping values, V_{eq} , obtained from experimental results for each cycle are presented
 239 in Figure 7(a). It can be observed that the equivalent viscous damping value is directly proportional to the
 240 diameter of the fastener. Moreover, the energy dissipation capacity of the system is significantly enhanced by
 241 doubling the number of fasteners. Generally, the equivalent viscous damping value increases with an increase
 242 in the number of loading cycles. However, the viscous damping during the initial loading cycles is considerably
 243 larger and not directly proportional to the cycle count due to the larger observed damage. The damping values
 244 shown in Figure 7(a) indicate that the equivalent viscous damping for both materials is primarily in the range
 245 of 0.03 to 0.3 and reaches its maximum value at approximately 12 to 15 cycles.

246 Figure 7(b) presents the variation of the total energy dissipation ΣE_{di} of the connections as a function of
 247 the loading cycles. It is notable that the energy dissipation of the component remains relatively constant during
 248 the initial loading cycles. However, during the later loading cycles, the energy dissipation of LVL connections
 249 increases at a faster rate compared to glubam connections. The total energy dissipation of all the bolted
 250 connections shows an approximate exponential relationship with the increase in loading cycles. The findings
 251 suggest that the energy dissipation capacity of LVL connections surpasses that of glubam connections. This is
 252 consistent with the higher ductility observed in Figure 7.

253 *2.3.3. Failure modes*

254 Figure C.24 presents failure modes and bolt deformation after test for a typical specimen in each group. The
 255 failure mode of bolted connections varies with material type and the number and diameter of the bolts adopted.
 256 The failure mode can be divided into shear failure and splitting failure. Moreover, the failure can happen after
 257 reaching embedded strength in the form of a combined failure mode [61, 62, 63, 64, 65] and/or formation of the
 258 plastic hinge in the bolt. LVL-S-8 connections present the highest ductility and tend to deform significantly
 259 with the formation of the plastic hinge (Table Appendix B) with embedment effect near the steel plate and
 260 large rope effect [47]. LVL-S-8 connections fail in the form of splitting crack, which could be related to the lower
 261 embedment strength and perpendicular-to-the-grain tensile strength (Table 1). LVL-S-10 connections exhibit
 262 a similar final crack pattern but a full embedment effect along the entire hole surface is observed. To sum up,
 263 LVL-S connections tend to fail in the form of splitting failure consistently with the literature [66].

264 Compared to LVL, GLB-S connections exhibit both shear failure and splitting failure without any dominating
 265 behavior without any embedment of the bolt in the block since glubam has much higher embedment strength
 266 compared with LVL (see Table 1).

267 Double bolted connections exhibit lower ductility but higher bearing capacity compared with single bolt
 268 connections (Table Appendix B). LVL-D-8 connections perform the best ductility among double bolted connec-
 269 tions (same as for the single bolt case). The failure of LVL-D-8 always originates from a shear failure in the
 270 part between the two bolts, then followed by a splitting crack in the part above the first bolt (similar to the
 271 single bolt case). No evident differences were observed for LVL-D-10 connections tending to fail with a shear
 272 failure in the part between the two bolts and splitting above the first bolt. Similar to single bolt connections,
 273 GLB-D specimens exhibit both shear failure and splitting failure without any dominating behavior above the
 274 first bolt. Similar to LVL-D, shear failures in the part between the two bolts were observed in GLB-D tests.

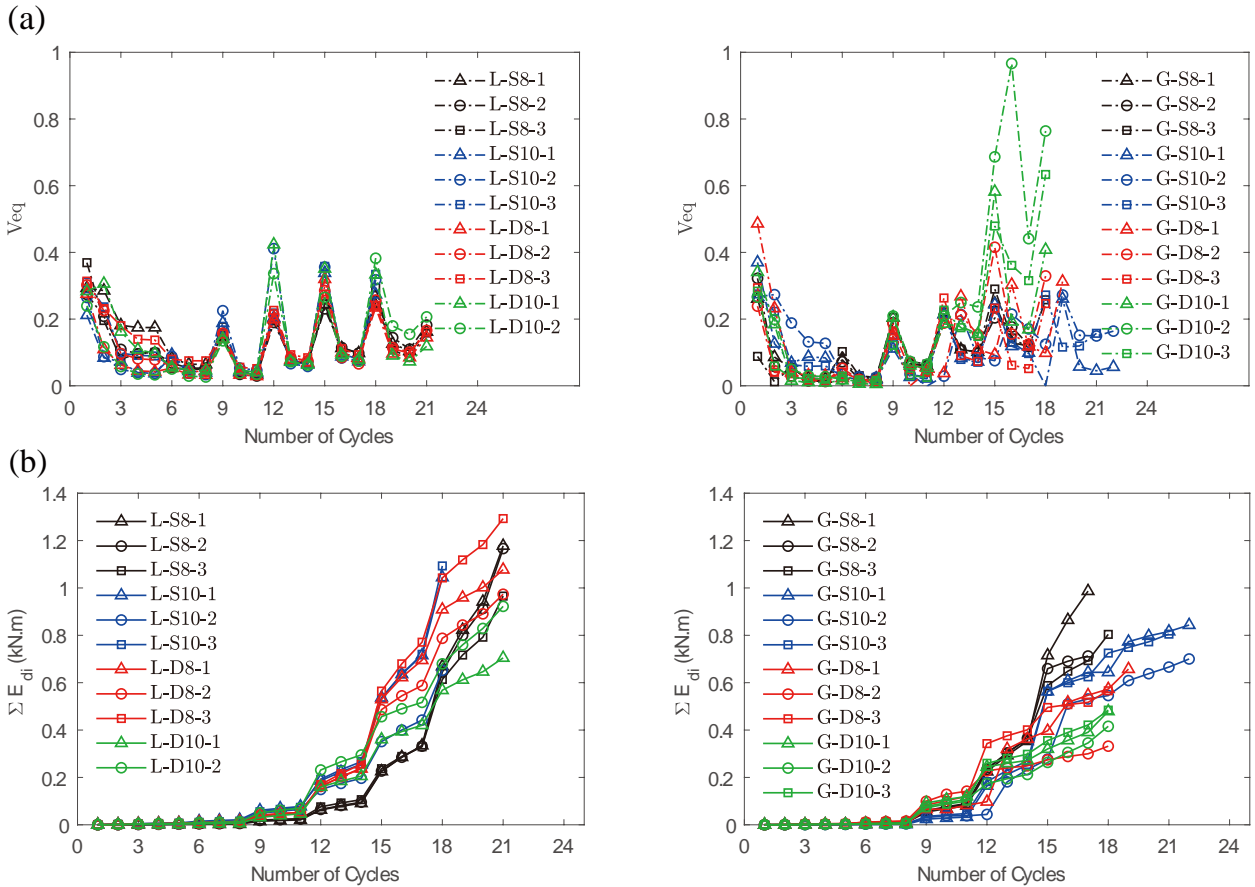


Figure 7: Equivalent viscous damping V_{eq} (a) and evolution of cumulative energy dissipation ΣE_{di} (b) with the increases of loading cycles. Lines with the same color refer to the three repeated test of the same configuration.

275 **3. Finite element modeling**

276 This Section describes the innovative finite element model proposed and reports the validation performed
 277 adopting the experimental results. Section 3.1 describes the material constitutive law adopted for LVL and
 278 glubam. In particular, Sections 3.1.1, 3.1.2, 3.1.3, and 3.1.4 describe the elastic behavior modeling, plastic

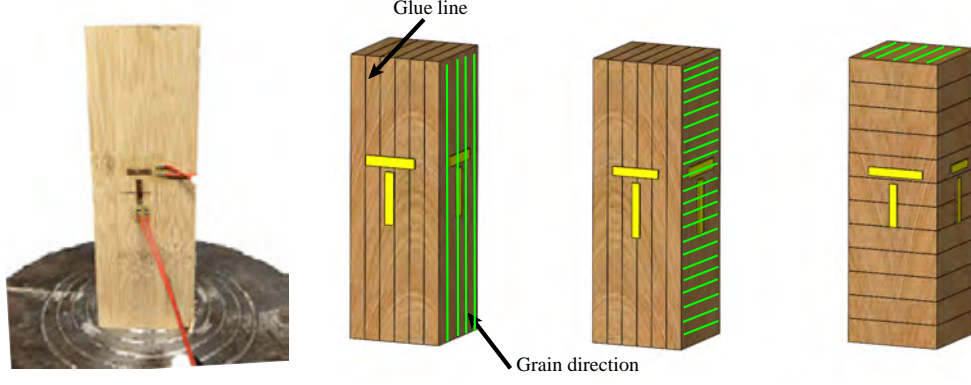


Figure 8: Specimen for elastic constants measurements. The green line shown in the sketch of specimen refers to the grain direction and the black line is the glue line of products.

Table 3: Engineering constants used in the ABAQUS model to define LVL and glubam elastic material (GPa).

	E_1	E_2	E_3	μ_{12}	μ_{13}	μ_{23}	μ_{21}	μ_{31}	μ_{32}	G_{23}	G_{13}	G_{12}
LVL	11.45	4.25	0.81	0.182	0.351	0.364	0.068	0.05	0.069	0.377	0.462	0.510
Glubam	8.56	5.65	2.81	0.282	0.336	0.316	0.180	0.160	0.157	0.410	0.568	0.612

behavior, effective foundation model properties, and crack modeling, respectively. Section 3.1.5 describes the utilization of ABAQUS user subroutine and the validation of materials constitutive law defined in subroutine. Section 3.2 describes the finite element implementation in ABAQUS. An assessment of the validity of the FE predictions is required, before the FE model can be further used for relevant investigations and engineering design analysis [67]. Finally, in Section 3.3, the 3D FEM model is validated against experimental load-displacement curves and experimental strain field.

3.1. Material constitutive law of LVL and glubam

3.1.1. Elastic behavior modeling

LVL and glubam are treated as orthotropic materials and their elastic behavior is modeled by stiffness matrix characterized by engineering constants [27, 28, 29]:

$$\boldsymbol{\sigma} = \mathbf{S}_{orth}\boldsymbol{\varepsilon} \quad (1)$$

where $\boldsymbol{\sigma}$ and $\boldsymbol{\varepsilon}$ are the vectors containing the stress and strain components, respectively, and \mathbf{S}_{orth} is defined as:

$$\mathbf{S}_{orth} = \begin{bmatrix} \frac{1}{E_1} & -\frac{\mu_{21}}{E_2} & -\frac{\mu_{31}}{E_3} & 0 & 0 & 0 \\ -\frac{\mu_{12}}{E_1} & \frac{1}{E_2} & -\frac{\mu_{32}}{E_3} & 0 & 0 & 0 \\ -\frac{\mu_{13}}{E_1} & -\frac{\mu_{23}}{E_2} & \frac{1}{E_3} & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{G_{12}} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1}{G_{13}} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1}{G_{23}} \end{bmatrix} \quad (2)$$

where E_1 , E_2 , and E_3 are the three Young's moduli, G_{12} , G_{23} , and G_{31} are the shear moduli, and μ_{12} , μ_{23} , and μ_{31} are the three Poisson's ratios. The subscripts 1, 2 and 3 indicates the three mutual orthogonal orientations.

LVL and glubam constants were determined performing experimental tests carried out using a compression testing machine [68]. The rate of loading is 2 kN/min. The dimension of the specimens was 60 mm \times 20 mm \times 20 mm. The layouts of the strain gauges on the specimens are shown in Figure 8. Six groups of six specimens were tested: three groups of compressive specimens in X, Y, and Z directions (matching the 1, 2, and 3 directions in Eq. 2) for measuring Young's moduli; three groups of 45° eccentric compression loading specimens for measuring the shear moduli.

All the measured constants are summarized in Table 3 where E , G , and μ refer to the modulus of elasticity, shear modulus, and Poisson ratio, respectively. Similar results were reported in the literature for LVL [69] and for glubam [50].

3.1.2. Plastic behavior modeling

The Hill's yielding criterion is adopted herein to characterize plastic behavior of orthotropic materials [46, 70, 71, 72], which takes into considerations material and yielding orthotropy [73]. The Hill's yielding criteria

Table 4: Input yield stresses for nonlinear behavior in ABAQUS model (MPa).

	$\bar{\sigma}_{11}$	$\bar{\sigma}_{22}$	$\bar{\sigma}_{33}$	$\bar{\sigma}_{12}$	$\bar{\sigma}_{13}$	$\bar{\sigma}_{23}$
LVL	38.91	14.03	13.23	6.27	6.27	5.53
Glubam	73.77	36.15	33.38	18.13	6.58	22.59

has been successfully applied in other researches such as CLT dowel-type connections [69], timber joints with glued-in rods [74] and traditional timber mortise-tenon joints [75]. The Hill's yielding criterion is defined by Hill's potential function where the input parameter is the yield stress ratio in each direction of orthotropic materials:

$$f(\sigma_{ii}) = \bar{\sigma} = \sqrt{F_{11}(\sigma_{22} - \sigma_{33})^2 + F_{22}(\sigma_{33} - \sigma_{11})^2 + F_{33}(\sigma_{11} - \sigma_{22})^2 + 2N_{23}\sigma_{23}^2 + 2N_{31}\sigma_{31}^2 + 2N_{12}\sigma_{12}^2} \quad (3)$$

where $\bar{\sigma}$ is the equivalent stress, σ_{11} , σ_{22} and σ_{33} are the normal stresses, σ_{12} , σ_{23} and σ_{31} are the shear stresses. F_{ii} and N_{ij} are constants obtained by tests of the material in different orientations, and are defined as follows:

$$F_{ii} = \frac{(\sigma^0)^2}{2} \left(\frac{1}{\bar{\sigma}_{jj}^2} + \frac{1}{\bar{\sigma}_{kk}^2} - \frac{1}{\bar{\sigma}_{ii}^2} \right) = \frac{1}{2} \left(\frac{1}{R_{jj}^2} + \frac{1}{R_{kk}^2} - \frac{1}{R_{ii}^2} \right), N_{ij} = \frac{3}{2} \left(\frac{\tau^0}{\bar{\sigma}_{ij}^2} \right)^2 = \frac{3}{2R_{ij}^2} \quad (4)$$

where σ^0 and τ^0 are reference yielding stresses defined by using the Mises plasticity definition syntax ($\tau^0 = \sqrt{3}\sigma^0$), $\bar{\sigma}_{ij}$ are the yielding stresses with respect to the axes of anisotropy from the pure uniaxial and shear tests, and R_{ij} are yield ratios which relate the yield level for stress component σ_{ij} to the reference yield stress σ^0 of the material. The yield ratios are defined as follows:

$$R_{11} = \frac{\bar{\sigma}_{11}}{\sigma^0}, R_{22} = \frac{\bar{\sigma}_{22}}{\sigma^0}, R_{33} = \frac{\bar{\sigma}_{33}}{\sigma^0}, R_{12} = \frac{\bar{\sigma}_{12}}{\tau^0}, R_{13} = \frac{\bar{\sigma}_{13}}{\tau^0}, R_{23} = \frac{\bar{\sigma}_{23}}{\tau^0} \quad (5)$$

The six yielding stresses are needed for defining the yielding criterion for the LVL and glubam: $\bar{\sigma}_{11}$, $\bar{\sigma}_{22}$, $\bar{\sigma}_{33}$, $\bar{\sigma}_{12}$, $\bar{\sigma}_{13}$ and $\bar{\sigma}_{23}$. In this study, the compressive yield strength was opted as the reference yield stress and the final yield stresses adopted are presented in Table 4.

For the orthotropic material plasticity, the associated flow rule used is given by:

$$d\{\varepsilon\}_{pl} = \lambda \left\{ \frac{\partial f}{\partial \{\sigma\}} \right\}, \lambda = d\bar{\varepsilon}_{pl} = \frac{d\bar{\sigma}}{H} \quad (6)$$

where λ is a proportionality constant termed the plastic multiplier, and $d\bar{\varepsilon}_{pl}$ and $d\bar{\sigma}$ are equivalent plastic strain and equivalent stress, respectively. $1/H$ is a hardening modulus equal to the slope of $\bar{\sigma} - \bar{\varepsilon}_{pl}$ curve which can be obtained from embedment experiment (Figure 9).

In this study, for the laminated timber and bamboo elements in the embedment zone (the area around the bolt, see yellow area in Figure 14), wood foundation model was used to describe the local crushing behavior due to embedment compression. In wood foundation model, material hardening was considered by bi-linear fitting the performance curves obtained from the embedment compression tests and the test methods is shown in Figure 9 (b). As observed in Figure 9 (a), the fitted bilinear relationship (red line) is in a good agreement with the embedment test curves (both 8 and 10 mm-diameter dowel-bearing test are shown). The relative LVL and glubam constitutive in the embedment zone are then determined by the fitting result shown in Figure 9 (a) according to the analysis method proposed by Hong and Barrett [32]. The foundation modulus and foundation yield point are defined based on the load-embedment displacement curve from embedment compression tests. In the fitted bilinear curve, an initial slope and a break point between two linear regions were identified. The nominal foundation modulus and the nominal yield point can then be calculated as:

$$k = \frac{P_y}{W_y} \quad (7)$$

where k is nominal foundation modulus (MPa), P_y is the yield load in the bilinear load/unit length-embedment displacement curve (N/mm), and W_y is the yield deformation in the load/unit length-embedment displacement curve (mm).

3.1.3. Effective foundation model properties

In the wood foundation model, the nominal foundation modulus along parallel-to-grain directions ($E_{1,F}$ in Table 5) are determined according to experimental results as discussed above, while the effective foundation modulus [32] along other directions ($E_{2,F}$, $E_{3,F}$, etc.) are derived by proportional transformation using the same ratio of E_1 and $E_{1,F}$ as following:

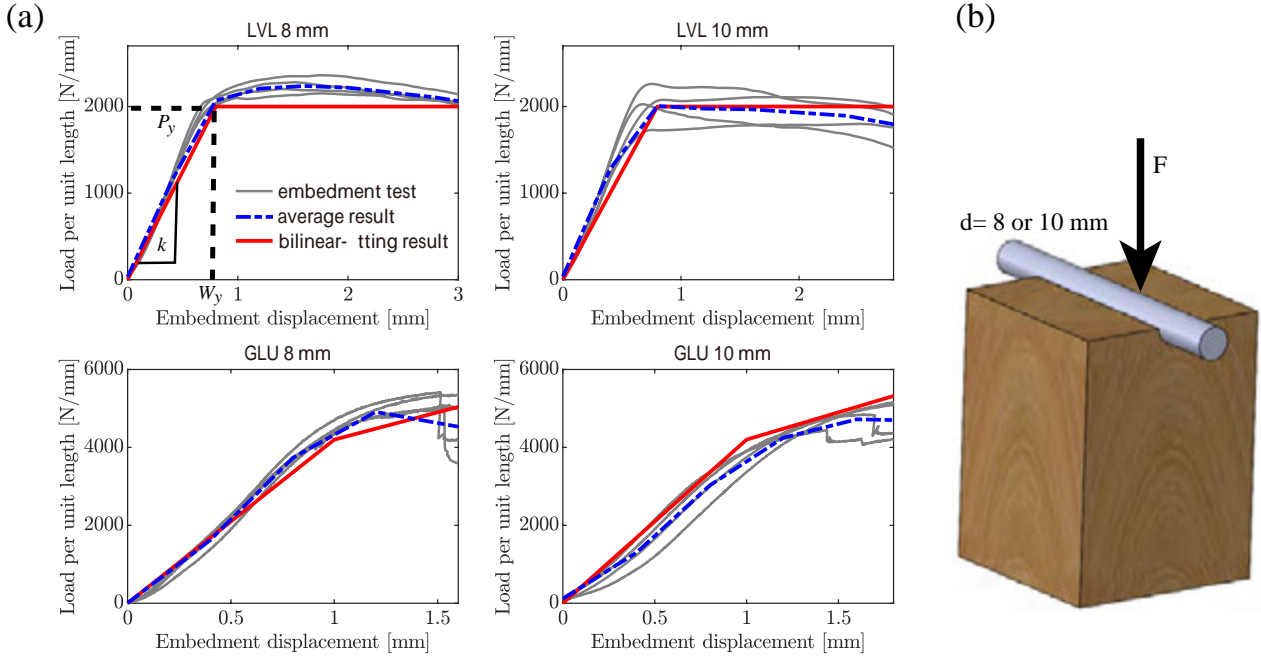


Figure 9: Embedment test: (a) load per unit length (in N/mm) vs. displacement (in mm) curves (gray line) and fitted bilinear constitutive law for wood foundation model (red line). The blue line is the average results of the test; (b) Embedment test method. k is nominal foundation modulus (MPa), P_y is the yield load in the bilinear load/unit length-embedment displacement curve (N/mm), and W_y is the yield deformation in the load/unit length-embedment displacement curve (mm), d is the diameter of bolt (mm).

Table 5: Engineering constants used in the user subroutine of ABAQUS to define wood foundation model for LVL and glulam (GPa).

Wood foundation model	$E_{1,F}$	$E_{2,F}$	$E_{3,F}$	$\mu_{12,F}$	$\mu_{13,F}$	$\mu_{23,F}$	$G_{23,F}$	$G_{13,F}$	$G_{12,F}$
LVL	2.5	0.93	0.18	0.182	0.351	0.364	0.08	0.10	0.11
Glulam	4.20	2.80	1.40	0.282	0.336	0.316	0.20	0.28	0.30

$$\frac{E_{1,F}}{E_1} = \frac{E_{2,F}}{E_2} = \frac{E_{3,F}}{E_3} \quad (8)$$

341 The Poisson's ratios in the wood foundation model ($\mu_{12,F}$, $\mu_{13,F}$, etc.) are the same as that obtained
342 from the prism compression test (see Figure 8 and Table 3). The final parameters for the wood foundation
343 model are listed in Table 5. It can be observed that the elastic constants in the three orthotropic directions
344 are reduced significantly in the wood foundation model compared to the elastic constants reported in Table 3
345 directly obtained from prism compression tests. This is consistent with the approach proposed by Hong and
346 Barrett [32] who adopted effective (reduced) foundation properties (i.e., properties of the material around the
347 bolt) to match the observed stiffness.

3.1.4. Crack modeling

348 It can be seen from Figure C.24 that, the fracture of LVL and glulam, majorly the splitting crack in LVL and
349 shear crack in glulam is the key factor leading to the failure of the connection. Although the softening behavior
350 of LVL and glulam is simulated to some extent by Hill's yield criterion, no crack propagation is considered in
351 this criterion. Herein, An attempt is made to simulate the cracking behavior by removing the damaged elements
352 along the potential cracking zone (red areas in Figure 14) [27, 76]. To do this, a user subroutine, UMAT are
353 integrated in ABAQUS to implement the damage function [34, 33] defined in Eq. 9. The damage variable D in
354 Eq. 9 is utilized in the subroutine such that when its value reaches one, the subroutine passes the zero stress
355 state to the element, and the element is deleted from the mesh. The size of the removed elements is about 0.1
356 mm wide and the total length is extended from the wall of bolt hole to the upper end of the member. The width
357 of the removed elements is closed to the real crack width observed in the test and such a small width can also
358 improve the calculation convergence. The area of the element removal is equal to the area of two shear failure
359 plane and one splitting plane as shown in the red areas in Figure 14. The quantity of the removed elements is
360 equal to the element quantity along these shear failure plane and splitting plane and when the block between
361 two shear plane is totally sheared out (see Figure C.24 L-C-D8) or the block above the bolt is totally split (see
362 Figure C.24 G-C-D10), the calculation will terminate.

$$D = \left(\frac{\bar{\sigma}}{f_{t,90}} \right)^2 + \left(\frac{\bar{\tau}}{f_{v,0}} \right)^2 \quad (9)$$

where $\bar{\sigma}$ and $\bar{\tau}$ are the perpendicular-to-grain tensile stress (σ_{22}) and parallel-to-grain shear stress (σ_{12}) respectively, and $f_{t,90}$ and $f_{v,0}$ are the perpendicular-to-grain tensile strength and parallel-to-grain shear strength respectively which can be obtained from previous material test results (Table 1).

The procedure for the element removal is:

1. Obtain perpendicular-to-grain tensile stress σ_{22} and parallel-to-grain shear stress σ_{12} from state variable in ABAQUS subroutine and check damage variable D .

$$D_e = \left(\frac{\sigma_{22,e}}{f_{t,90}} \right)^2 + \left(\frac{\sigma_{12,e}}{f_{v,0}} \right)^2 = 1 \quad (10)$$

where e is an element number, which links to the elements to be checked.

2. An element is removed if it satisfies the condition in Eq. 10 by setting its material properties to zero. When the ii -th is removed, there will be a redundancy in the Jacobian matrix which will affect the tangential stiffness matrix \mathbf{K}_T :

$$\mathbf{K}_T = \begin{bmatrix} K_{11}^e & \cdot & \cdot & \cdot & K_{1i}^e & \cdot & \cdot & \cdot & K_{1n}^e \\ & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ & & & & & & & & \\ K_{i1}^e & \cdot & \cdot & \cdot & K_{ii}^e = 0 & \cdot & \cdot & \cdot & K_{in}^e \\ & & & & \cdot & \cdot & \cdot & \cdot & \cdot \\ & & & & & & & & \\ K_{n1}^e & \cdot & \cdot & \cdot & K_{ni}^e & \cdot & \cdot & \cdot & K_{nn}^e \end{bmatrix} \quad (11)$$

where n is the total number of elements.

3. Start a new step based on a redundant structural tangential stiffness (i.e., remove the ii -th element associated rows and columns) and repeat steps 1 and 2.

3.1.5. ABAQUS user subroutine and FE material validation

A user subroutine, UMAT, is integrated in ABAQUS to implement the Hill's yielding criteria. This subroutine facilitates the implementation of the element removal criteria introduced in Section 3.1.4. The flowchart for a load increment and the implementation of Hill's yielding criteria and element removal criteria in the ABAQUS subroutine is shown in Figure 10.

To validate the feasibility of the Hill's yielding criterion in the UMAT subroutine, the compression test results of prism specimen are compared to the corresponding simulation results in ABAQUS as shown in Figure 11 and 12. In the modeling of the prism compression test, the material constitutive law of LVL and glubam is programmed in the subroutine according to the flowchart in Figure 10. The materials constants and yielding stress ratio defined in Hill's yielding function are adopted from Table 3 and 4. The update of state variable (equivalent plastic strain $d\bar{\varepsilon}_{pl}$) in each load-increment step is performed according to the flowchart in Figure 10 as well, while the element removal criterion is not exerted herein and only the Hill's yielding behavior is verified. Figure 12 shows the elasto-plastic behavior of LVL and glubam prism specimen under compression. It can be seen that the simulated load-displacement curve is in good agreement with the tested results and the simulated yielding strength keeps good fit with tested values. Therefore, the Hill's yielding criteria is validated in material property issue and the UMAT can accurately describe the LVL and glubam plastic behavior.

Figure 13 compares the experimental and simulated results in one representative embedment test (see Figure 1) by using the constitutive model as described above. The material constitutive law of LVL is programmed in the subroutine according to the flowchart in Figure 10. The update of state variables (equivalent plastic strain $d\bar{\varepsilon}_{pl}$ and damage variable D) in each load-increment step is performed according to the flowchart in Figure 10. Both the element removal criterion and Hill's yielding criterion are considered herein. It can be seen that the simulated cracking path is in good agreement with the cracking path observed from test (see Figure 13 b and c). A descending stage due to cracking was observed in the FEM loading-embedment displacement curves (see red line in Figure 13 a). Therefore, the validity of the material constitutive developed in ABAQUS UMAT by integrating the Hill's yielding criterion with the element removal criterion is verified.

3.2. Finite element implementation

The bolted connection with slotted in steel plate is modeled in ABAQUS. The 3D FE model (FEM) consists of one steel plate, bolts and main members (LVL or glubam) as reported in Figure 15 (a). The geometry of the connection components are the same as the geometry of the tested specimens, see Figure 2. In order to simplify the model and reduce the computation burden, the bolted joint with 4 bolts at the bottom end is

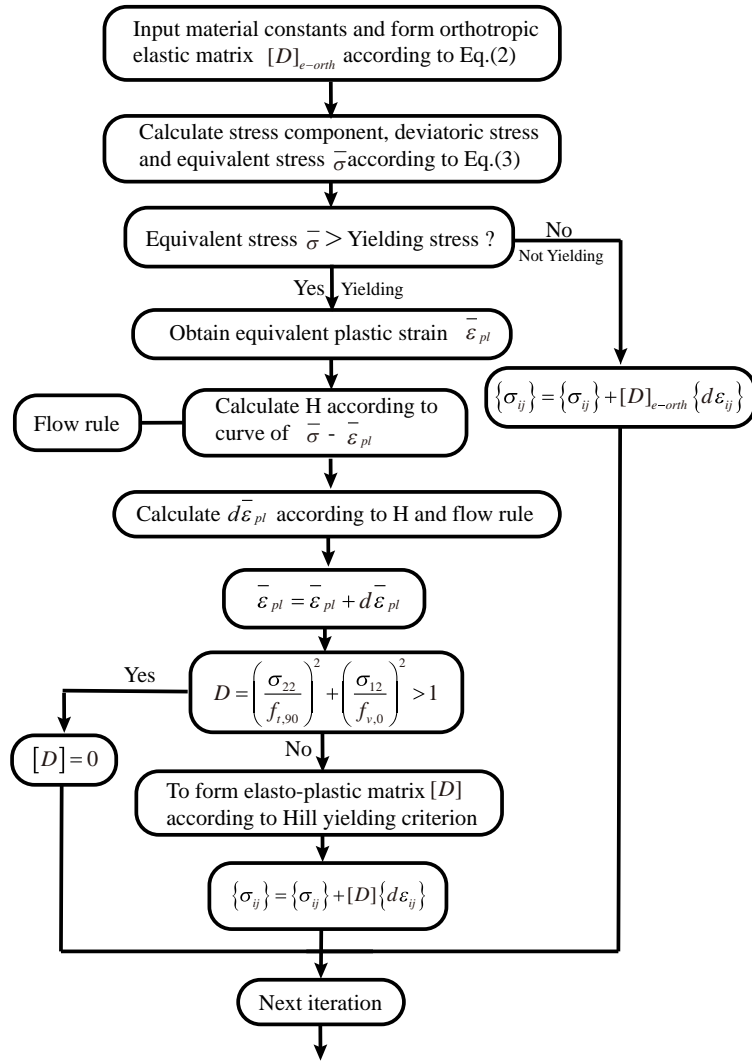


Figure 10: Flowchart for a load increment and implementation of Hill's yielding criterion and element removal criterion in the ABAQUS subroutine.

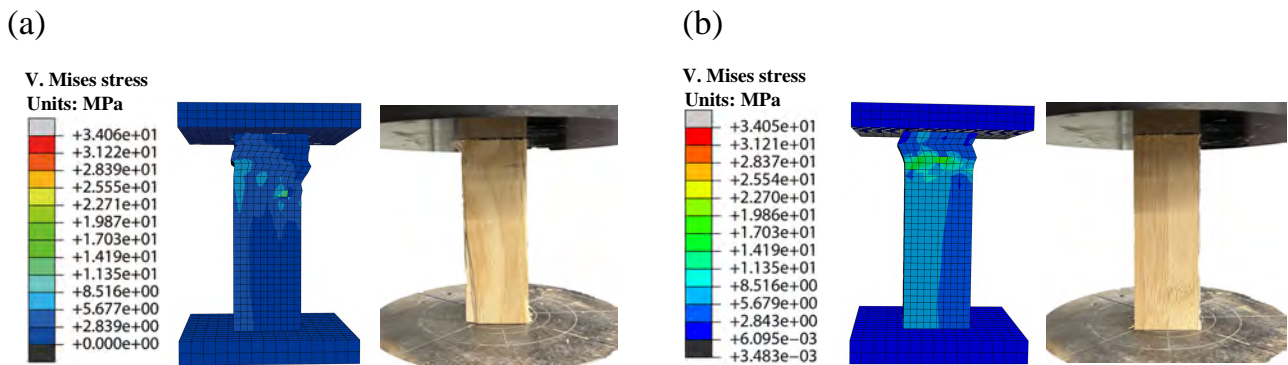


Figure 11: FEM model and simulated strain field in compression test of prism specimen: (a) LVL; (b) glulam.

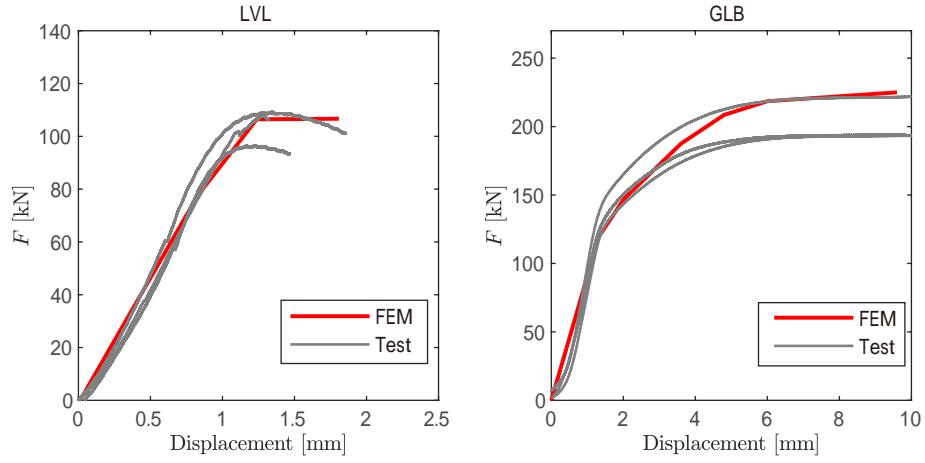


Figure 12: Tested and simulated load (F in kN) vs. displacement (in mm) curves in compression test of prism specimen: LVL (left) and GLB (right). The red line is the FEM result and the gray lines are three repeated test results.

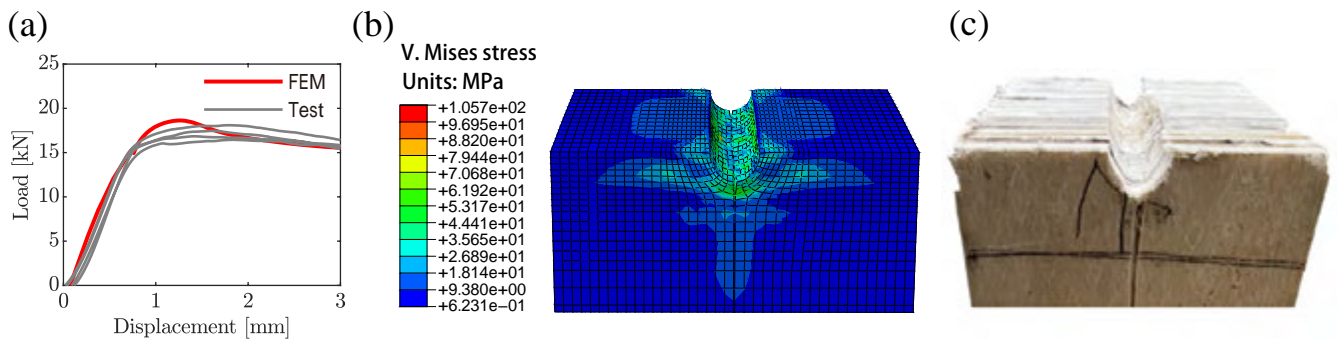


Figure 13: Simulated embedment test for LVL specimen with a 8mm-diameter half hole: (a) load (in kN) vs. embedment displacement (in mm) curve, the red line is the simulated result and the gray lines are four repeated test results; (b) simulated crack pattern and stress field; (c) experimental crack pattern.

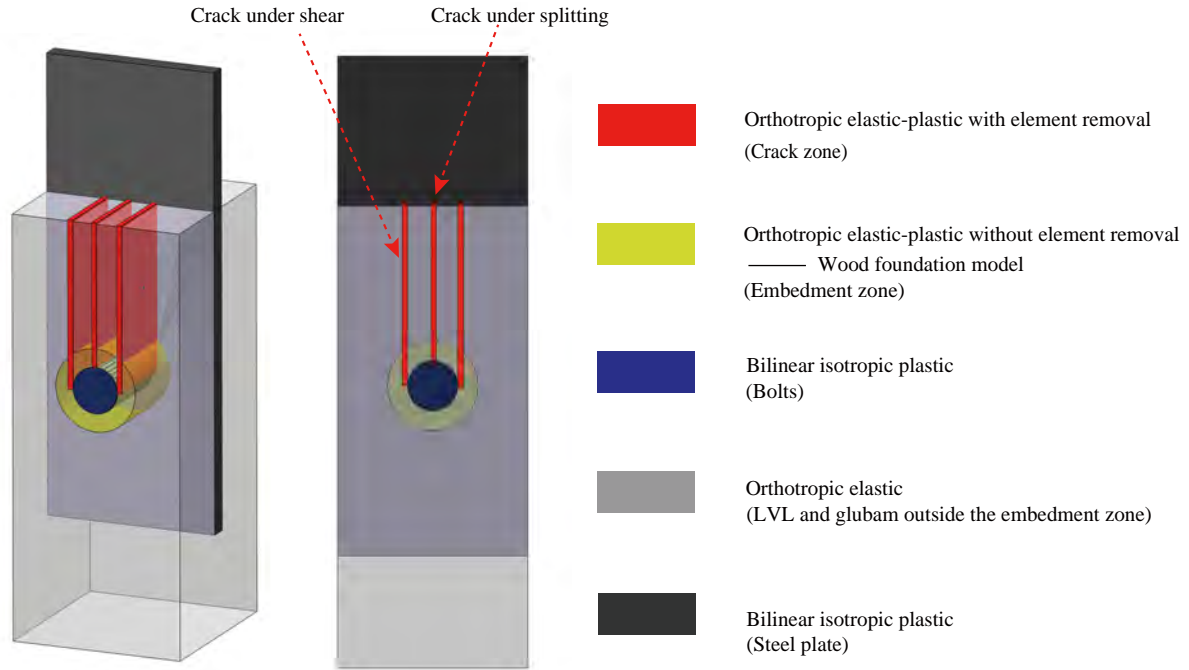


Figure 14: Material constitutive partitioning of the numerical model. The red area (crack zone) uses orthotropic elastic-plastic constitutive law with element removal; The yellow area (embedment zone) uses orthotropic elastic-plastic constitutive law without element removal; The blue area (bolt) uses isotropic plastic constitutive law; The gray area (outside the embedment zone) uses orthotropic elastic constitutive law; The black area (steel plate) uses bilinear isotropic plastic constitutive law.

407 not considered. Their displacement contribution is neglected since the LVDT only measures the displacements
 408 of the bolted joint at the upper end. This configuration of the FEM model can accurately simulate the real
 409 boundary conditions adopted in the tests.

410 All the components were modeled with eight-node brick elements (C3D8) in the ABAQUS software. The
 411 whole finite element model is shown in Figure 15 (a).

412 The bolt and steel plate was modeled as isotropic elastic-perfectly plasticity. For the bolts and steel plate,
 413 the module of elasticity (MOE) is 210 GPa and the Poisson ratio is 0.3 based on C10B21 steel properties [77].
 414 The yield stress is 345 MPa for steel plate. The yield stress is 721.52 and 823.98 MPa respectively for $\Phi 8$ and
 415 $\Phi 10$ bolts, respectively, see Table 1.

416 It has been proved from previous studies [32, 75, 78, 16] that the constitutive of the elements outside the
 417 embedment zone (gray area in Figure 14) is negligible while that in the embedment zone (see red area in
 418 Figure 14) is dominating the response. Therefore, the LVL or glulam block is modeled with different material
 419 properties for elements inside and outside the embedment zone, and crack zone. The material partitioning of the
 420 block is shown in Figure 14. The elements outside the embedment zone (gray area in Figure 14) were assumed
 421 to be orthotropic linear elastic elements, and the Young's modulus was determined by compression tests of
 422 prism specimen (see Table 3). An adaptive mesh is adopted with mean mesh-size equal to around to 3 mm.
 423 The properties of these region are consistent with the description reported in Section 3.1.1. In the embedment
 424 zone, orthotropic elastic-plastic constitutive (Hill's yielding criteria) was used and the Hill's yielding criteria
 425 were implemented by directly inputting the parameter of Hill's yielding function in the ABAQUS user interface
 426 without establishing subroutine. The material properties in the embedment zone are equal to the effective
 427 foundation model properties (Section 3.1.3). As for elements in crack zone (red area in Figure 14), orthotropic
 428 elasto-plastic constitutive (Hill's yielding criteria) with progressive element removal was implemented. In the
 429 crack zone, the Hill's yielding criteria and element removal were both implemented by establishing subroutine.
 430 The thickness in the crack zone was set equal to 0.1mm and the mesh-size equal to around to 3 mm. The
 431 material parameters of the glulam and LVL refer to the experimental results in Section 3.1.

432 The interface property of all the contact surfaces is set as hard contact. The Coulomb friction coefficient of
 433 all the contact surfaces is taken as 0.5. Moreover, to model the initial slip stage caused by the hole clearance
 434 between the bolt and hole wall of timber elements [39], 0.5 mm tolerance between the interface of bolt and
 435 timber elements in ABAQUS model is set.

436 The simulation results of the failure modes obtained by the FEM (G-M-S10) are shown in Figure 15 as
 437 example. A typical shearing-out failure mode can be observed, which is consistent with the test observation (see
 438 Figure C.24). Moreover, a comparison of element status in the predetermined crack plane as fracture propagates
 439 is shown in Figure 16. It can be seen that the vanishing elements on the fracture plane gradually formed the

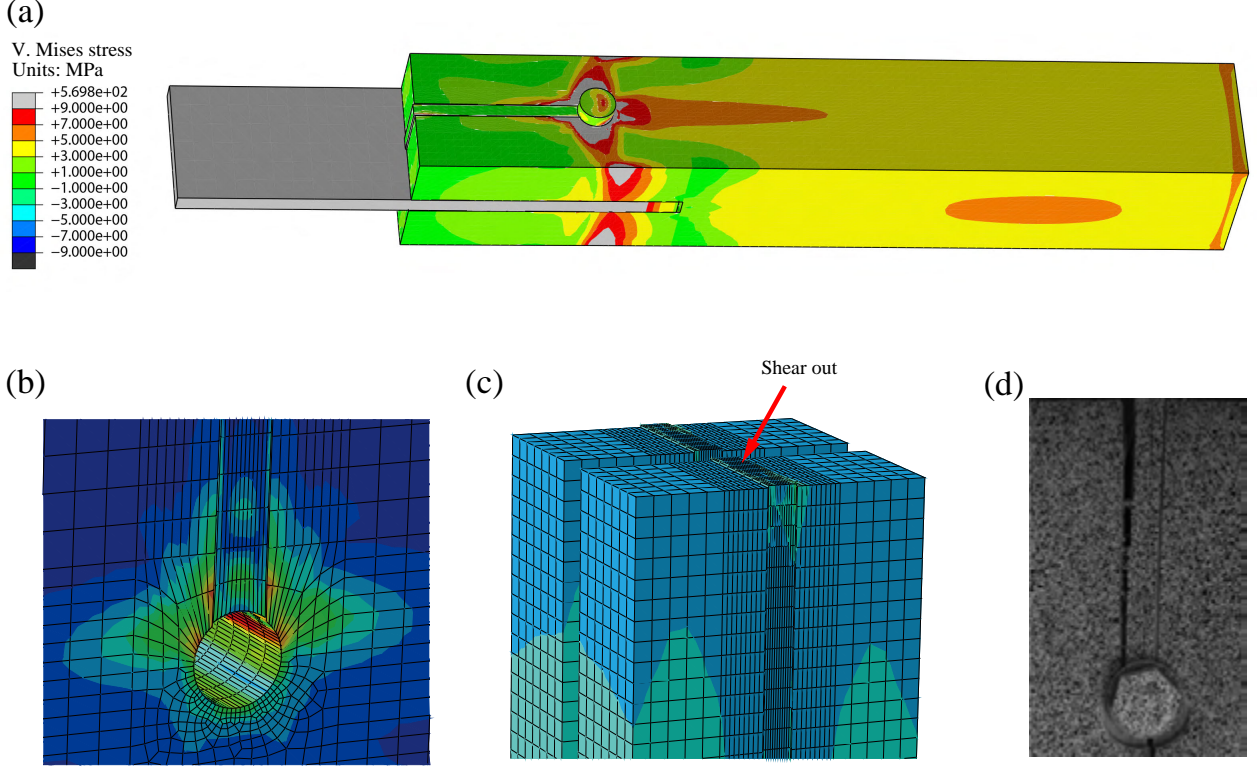


Figure 15: Comparison between simulated failure modes and tested failure modes of G-M-S10: (a) the whole finite element model; (b) strain field around the crack; (c) simulated shear-out failure; (d) shear-out failure from test.

440 final fracture path.

441 3.3. Validation of the FEM model

442 3.3.1. Load-displacement behavior

443 The load-displacement results of the FEA are shown in Figure 17 and 18. The comparison between the
 444 numerical and experimental load-displacement curves shows that the numerical model represents well the exper-
 445 imental curve. The numerical model is in good agreement with experimental observation regarding the main
 446 parameters such as the stiffness and the maximum load (F_u) in the case of monotonic loading (see Table D.8).
 447 The initial stiffness and maximum load capacity obtained from the experimental results and numerical model
 448 are compared further to the current European standards EC5 [79]. According to EC5 [79], the characteristic
 449 load-carrying capacity, $F_{v,Rk}$, of a steel-to-timber connection is formulated as follows:

$$F_{v,Rk} = \min \begin{cases} f_{h,k} t_1 d & (1) \\ f_{h,k} t_1 d \left[\sqrt{2 + \frac{4M_{y,Rk}}{f_{h,k} \cdot d \cdot t_1^2}} - 1 \right] & (2) \\ 2.3 \sqrt{M_{y,Rk} \cdot f_{h,k} \cdot d} & (3) \end{cases} \quad (12)$$

450 where $M_{y,Rk}$ is the characteristic yield moment of the dowel, $f_{h,k}$ is the embedment strength of the timber
 451 member obtained from the material test, t_1 is the thickness of the member, and d is the diameter of the dowel.
 452 However, Eq. 12 specified in Eurocode 5 [79] only applies to single-bolted case. An effective bolts factor n_{ef}
 453 specified in Eurocode 5 [79] needs to be applied to calculate the maximum load for double-bolted cases:

$$F_{v,Rk} = n_{ef} F_{v,Rk} \quad (13)$$

454 For steel to timber joints, Eurocode 5 [79] also provides the following empirical formula to calculate the
 455 initial stiffness k_e per shear plane per fastener:

$$k_e = 2\rho^{1.5}d/23 \quad (14)$$

456 where k_e is the initial stiffness and ρ is the wood or bamboo density in kg/m^3 . Since the investigated members
 457 have two shear planes in total, the initial stiffness of the connections can be predicted as:

$$k_e = n \cdot 4 \cdot \rho^{1.5}d/23 \quad (15)$$

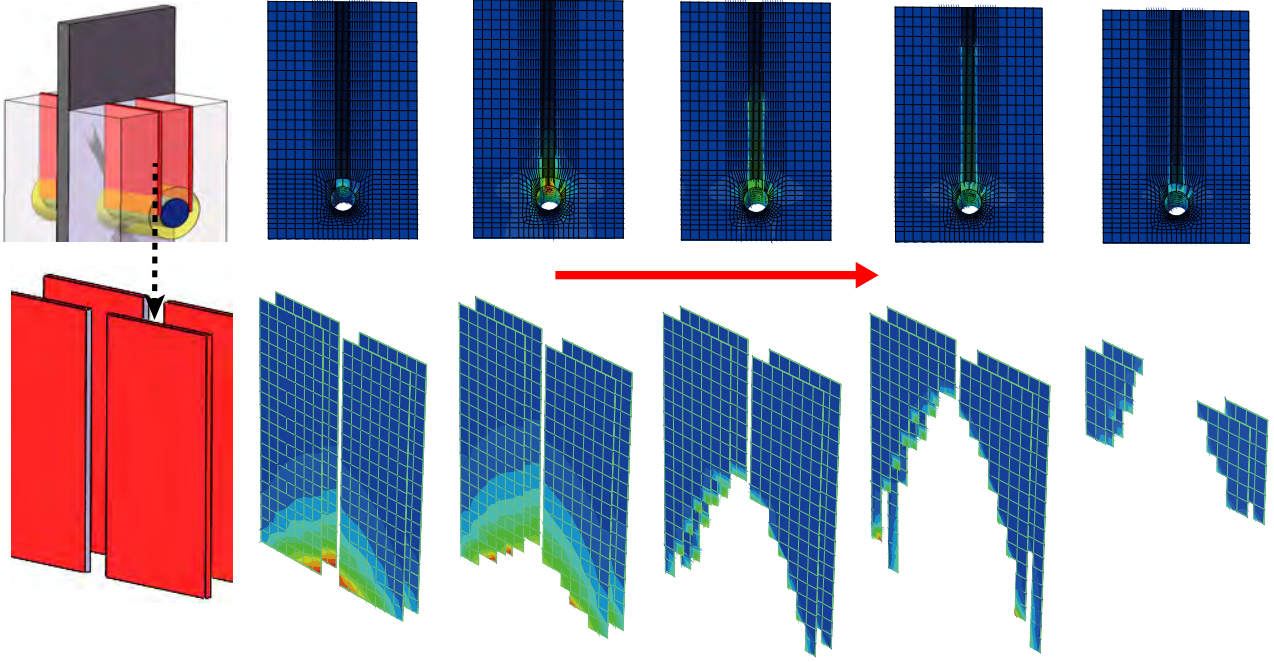


Figure 16: Evolution of element status in the pre-determined crack plane as fracture propagates.

458 The average initial stiffness and maximum load of the tested specimens, FEM results, and predicted results
 459 by EC5 [79] under monotonic loading are summarized in Table D.8. The results indicate that the initial stiffness
 460 of the connection is slightly higher in the FEM compared to the experimental results, which may be due to
 461 the tolerance between hole and fastener diameter. In the case of monotonic loading, the maximum load of the
 462 FE model meets the actual specimen peak load with a margin of error of 4%. As shown in Figure 18, the
 463 cyclic hysteretic loops predicted by the FEM appear to closely follow the shape of the experimental loops. The
 464 numerical initial stiffness and experimental elastic stiffness taken from the unloading-reloading phases are quite
 465 similar. To evaluate the ductility of the tested specimens under monotonic loading, the average ductility was
 466 compared with finite element method (FEM) results, as presented in Table D.8. With the exception of the
 467 L-MD10 and G-MD10 cases, the relative error in the remaining cases was confined within 20%. The observed
 468 discrepancy may be attributed to the larger diameter and number of bolts employed in these two cases, which
 469 resulted in the rapid propagation of cracks. This phenomenon is inconsistent with the progressive process
 470 predicted by the element removal criterion.

471 The formula from EC5 [79] predicts the initial stiffness and maximum load very well for single-bolted cases,
 472 while the prediction to double-bolted cases is not very accurate. A correction factor should be further considered
 473 to make Eqs. 13 and 15 applicable to double-bolted cases of LVL and glulam connections. This will be discussed
 474 in detail in Section 4.

475 3.3.2. Maximum principal strain field

476 Full-field strain data from Digital Image Correlation (DIC) provides rich information for FE analysis vali-
 477 dation. Hybrid FEM-DIC method has been widely adopted in the structural analysis [27, 80] and validation of
 478 numerical model itself [81, 82, 83]. Figure 20 shows the full field strain distribution (maximum principal strain
 479 field) on surfaces of two representative specimens (LVL-D8-3 and GLB-D8-1) obtained from FEM analysis and
 480 DIC analysis at the pre-fracture point. Regarding DIC analysis, the selected surface is the side where the first
 481 crack is occurring. It can be seen that the prediction of the stress concentration area by FEM is in good agree-
 482 ment with measured results by DIC. The peak strain tends to lie in the middle line of surface (see Figure C.24
 483 L-M-D8) or localize between the net and gross shear lines (see Figure C.24 L-M-S10) [84, 85]. This is consistent
 484 with the observed two types of failure mode, shear and splitting failure [86, 87, 88, 62, 89]. Additionally, it can
 485 be reflected by the strain distribution of bolt head that the rope effect can be modeled by the proposed FEM
 486 model.

487 Maximum principal strain of the surface elements obtained from the FEM model was compared with the
 488 DIC measurements mainly at three typical sections (1-1, 2-2 and 3-3), as shown in Figure 20. The validation
 489 is highlighted with 3 stages of the loading application, which are identified by 3 characteristic points A, B and
 490 C representing elastic phase, yield phase and peak load phase respectively as shown in Figure 19. From Figure
 491 20, it can be seen that the evolution pattern of strain at the typical section obtained from the FEM is similar
 492 to DIC results. More specifically, the strain values derived from the FEM model at specific locations have

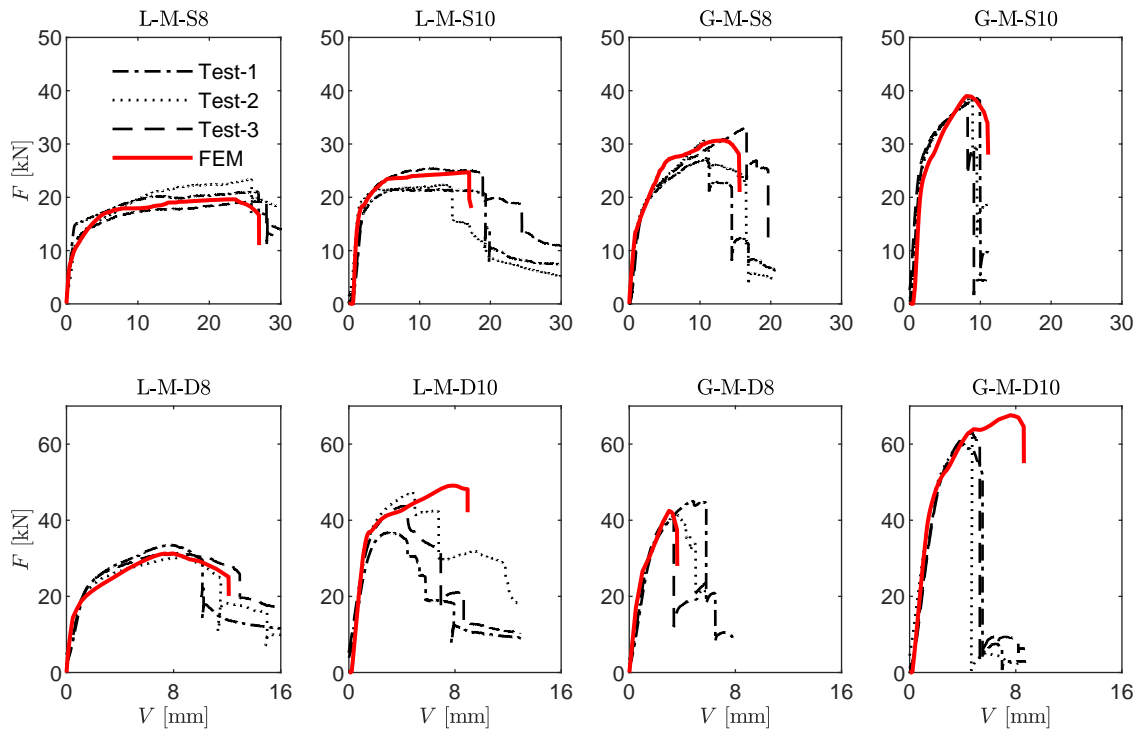


Figure 17: Load (F in kN) vs. displacement (V in mm) results of FEM analyses compared to experimental results under monotonic loading. The red line is the FEM result and gray lines are three repeated test results. The first two columns refers to results of LVL while the last two refers to glulam. The first row refers to single bolt and the second refers to double bolts cases.

allowable error compared to the DIC results. Generally, the strain values obtained by FEM are larger than DIC measurements since the strain obtained by FEM is not pure surface strain but reflects a certain inner strain, given that the studied surface elements in FEM model are hexahedral whose thickness is near 6 mm.

The evolution of the strain at the typical sections shows bimodal or unimodal patterns at sections 2-2 and 3-3, corresponding to active splitting planes and two active shear planes, respectively. Regarding section 1-1, the peak strain mainly localizes in the part between two bolts, which is consistent with experimental observations. In the experiment, the region between two bolts always cracked first, leading to the final failure of the specimen.

4. Theoretical analysis of elastic stiffness

This Section presents a theoretical analysis of elastic stiffness based on the FE analyses. Sections 4.1 and 4.2 reports a theoretical analysis of the elastic stiffness of single-bolted and double-bolted connections, respectively. Finally, Section 4.3 reports a validation of the proposed theoretical analysis of elastic stiffness by comparing with experimental, FE, and code-based (Eurocode 5) predictions.

4.1. Elastic stiffness of single-bolted connections

Yingyang and Jiajia [90] derived the initial stiffness model of single-bolted connections referring to the Winkler foundation model [91, 92, 93]. In the model of Yingyang and Jiajia [90], only half part is taken for analysis due to structural symmetry (Figure 21(a)). The axis direction and origin are shown in Figure 21(b). The bolt micro-segment at any x position is taken for analysis and the corresponding free body diagram is shown in Figure 21(c). In Figure 21, x represents the distance between a certain point and the midpoint on the bolt shank, which is positive to the right. w represents the deflection of bolt shank, which is positive upward. M and Q represent the moment and shear force of the bolt shank, respectively. The parameters involved in the derivation include the moment of inertia of bolt section, I , elastic modulus of bolt, E , and dowel-bearing stiffness of timber, k_s .

According to the equilibrium in the ω direction:

$$\frac{dQ}{dx} + k_s \omega(x) = 0 \quad (16)$$

According to the relationship between shear force, bending moment, and curvature of an Euler beam, the following equation can be obtained:

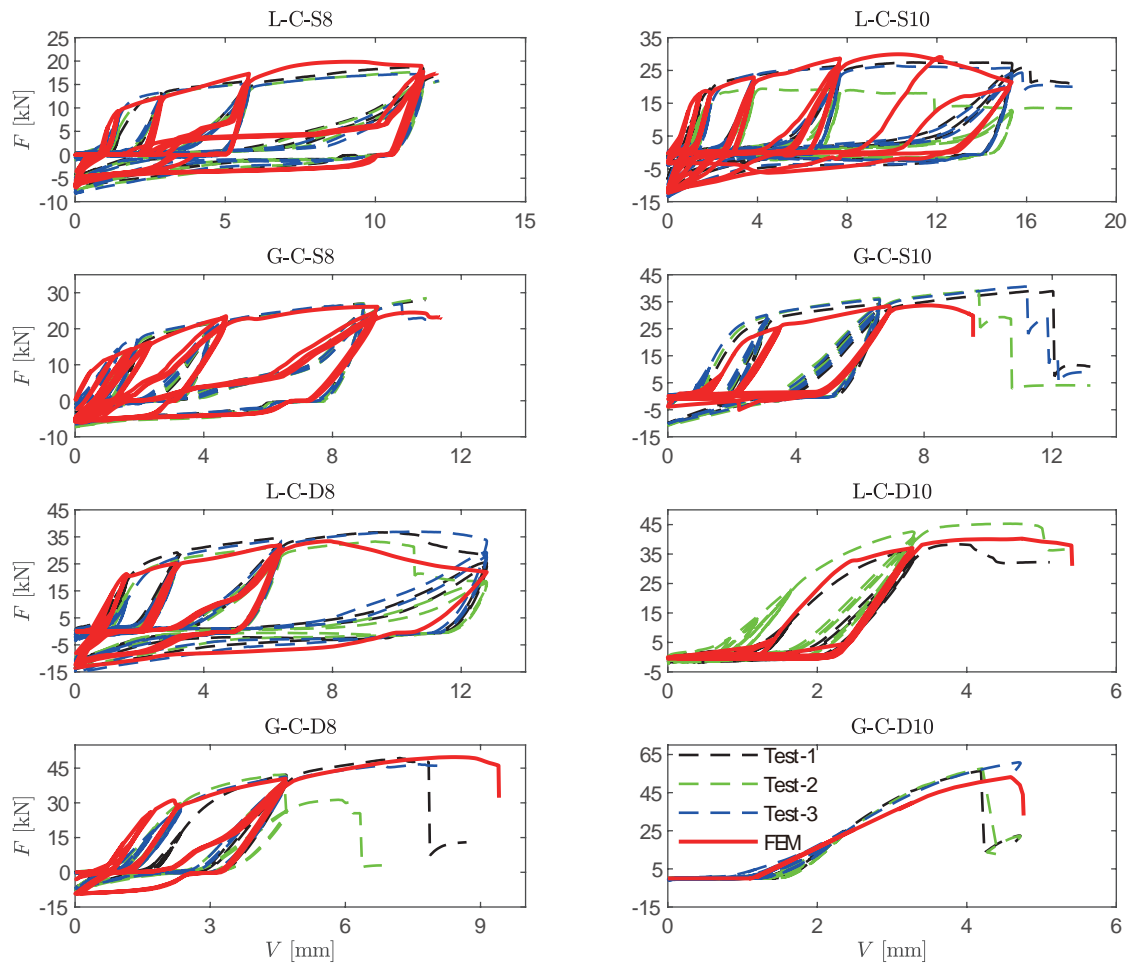


Figure 18: Load (F in kN) vs. displacement (V in mm) results of FEM analyses compared to experimental results under cyclic loading. The red line is the FEM result, and black, green and blue lines are three repeated test results. The first row refers to single-bolted LVL cases; the second row refers to single-bolted glulam cases; the third row refers to double-bolted LVL cases; the fourth row refers to double-bolted glulam cases.

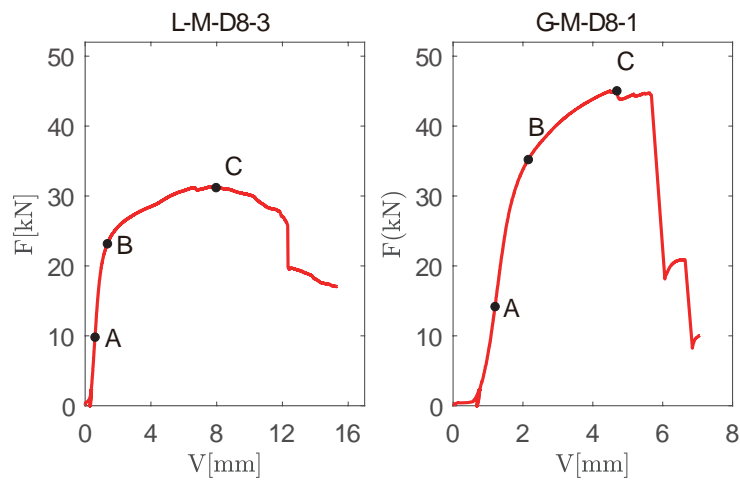


Figure 19: Definition of three characteristic points in the in load-displacement curve: A (limit of elastic phase), B (limit of yielding phase) and C (peak load phase).

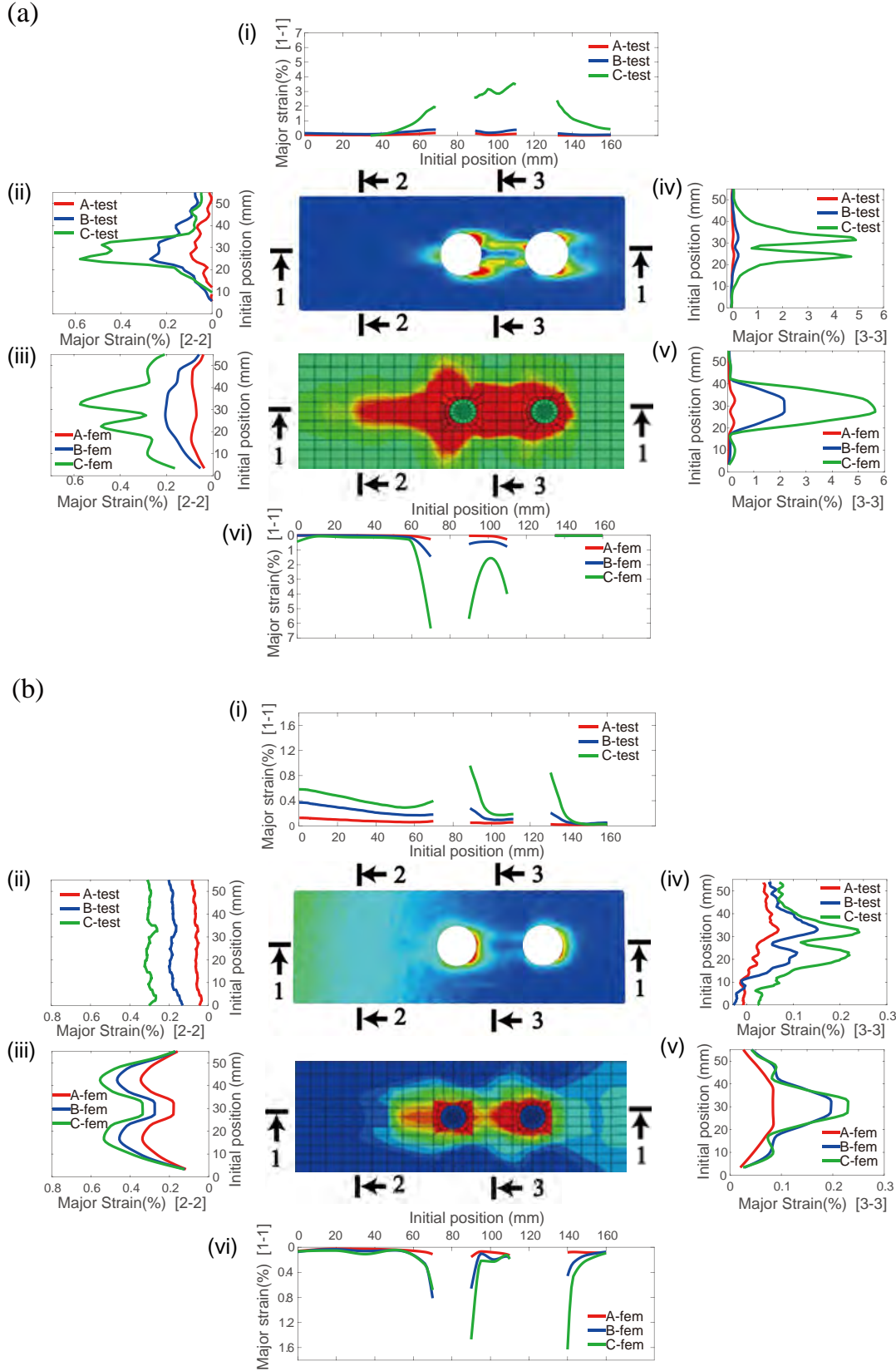


Figure 20: Comparison of sectional strain distribution between numerical and measured results by DIC: (a) LVL-D8-3; (b) GLB-D8-1. The red line shows the tested strain and simulated strain corresponding to A stage of Figure 19, blue line corresponds to B stage of Figure 19, and green line corresponds to C stage of Figure 19. The strain diagram (i) and (vi) show the strain evolution along Section 1-1 in the test and simulation results, respectively. The strain diagram (ii) and (iii) show the strain evolution along Section 2-2 in the test and simulation results, respectively. The strain diagram (iv) and (v) show the strain evolution along Section 3-3 in the test and simulation results, respectively.

$$\frac{d^4\omega(x)}{dx^4} + \frac{k_s}{EI}\omega(x) = 0 \quad (17)$$

518 Assuming $l_c = \sqrt[4]{4EI/k_s}$ and $\xi = x/l_c$, the following equation can be obtained:

$$\frac{d^4\omega(\xi)}{d\xi^4} + 4\omega(\xi) = 0 \quad (18)$$

519 The solution to the above homogeneous differential equation can be written as:

$$\omega(\xi) = A_1e^\xi(\cos\xi + i\sin\xi) + A_2e^\xi(\cos\xi - i\sin\xi) + A_3e^{-\xi}(\cos\xi + i\sin\xi) + A_4e^{-\xi}(\cos\xi - i\sin\xi) \quad (19)$$

520 where A_1, A_2, A_3, A_4 are constants. Assuming $B_1 = A_1 + A_2, B_2 = A_1i - A_2i, B_3 = A_3 + A_4, B_4 = A_3i - A_4i$,
521 the following equation can be obtained:

$$\omega(\xi) = B_1e^\xi\cos\xi + B_2e^\xi\sin\xi + B_3e^{-\xi}\cos\xi + B_4e^{-\xi}\sin\xi \quad (20)$$

522 As x (that is, ξ) increases, the deflection ω gradually approach to 0 and the terms containing $e^\xi\cos\xi$ and
523 $e^\xi\sin\xi$ in Eq. 20 diverge, thus $B_1 = B_2 = 0$.

524 Assuming $g_1 = e^{-\xi}\cos\xi, g_2 = e^{-\xi}\sin\xi, g_3 = g_1 + g_2, g_4 = g_1 - g_2$, thus $\frac{dg_1}{d\xi} = -g_3, \frac{dg_2}{d\xi} = g_4, \frac{dg_3}{d\xi} = -2g_2$,
525 $\frac{dg_4}{d\xi} = -2g_1$. The deflection ω , rotation angle θ , moment M , shear force Q at certain x position can be obtained
526 as:

$$\omega(\xi) = B_3g_1 + B_4g_2, \theta(\xi) = \frac{d\omega(x)}{dx} = \frac{1}{l_c}(-B_3g_3 + B_4g_4) \quad (21)$$

$$M(\xi) = EI\frac{d^2\omega(x)}{dx^2} = \frac{2EI}{l_c^2}(B_3g_2 - B_4g_1), Q(\xi) = \frac{dM(x)}{dx} = \frac{2EI}{l_c^3}(B_3g_4 + B_4g_3) \quad (22)$$

527 At $x = 0$ ($\xi = 0$), there is shear force Q_0 , moment M_0 , and when substituted into Eq.22, one can solve as:

$$B_3 = \frac{l_c}{2EI}(l_cQ_0 + M_0), B_4 = \frac{-l_c}{2EI}M_0 \quad (23)$$

528 Thus Eqs. 21-22 can be expressed as:

$$\omega = \frac{l_c^2}{2EI}(l_cQ_0g_1 + M_0g_4), \theta = \frac{-l_c}{2EI}(l_cQ_0g_3 + 2M_0g_1) \quad (24)$$

$$M = l_cQ_0g_2 + M_0g_3, Q = Q_0g_4 - \frac{2}{l_c}M_0g_2 \quad (25)$$

529 The elastic stiffness k_e of the bolt joint can be described as the ratio of the external force F to the displace-
530 ment V of bolt shank at the midpoint. It could be approximately considered that $V \approx \omega_0$.

531 At $x = 0$ ($\xi = 0$), the shear force is $Q_0 = 0.5F$ and when substituted into Eq. 24, the following equation
532 can be obtained:

$$V = \omega_0 = \frac{l_c^2}{2EI}\left(l_c\frac{F}{2} + M_0\right) \quad (26)$$

533 Assuming

$$\beta_1 = \frac{1}{\left(1 + 2\frac{M_0}{l_cF}\right)} \quad (27)$$

534 The elastic stiffness k_e of the bolt joint can be calculated as follows when substituting $l_c = \sqrt[4]{4EI/k_s}$ into Eq.
535 26.

$$k_e = \frac{F}{V} = \beta_1\left(k_s\sqrt[4]{\frac{4EI}{k_s}}\right) \quad (28)$$

536 where $k_s = k_{h,0}d$ and EI are determined adopting material properties (see Table 1) and geometric dimensions.

537 The determination of β_1 is discussed as follows:

538 1. When the rotation of the mid-point of bolt shank ($x = 0$) is fully constrained ($\theta_0 = 0$), substituting
539 ($\theta_0 = 0$) into Eqs. 24 and 27, one can solve that $\beta_1 = 2$;

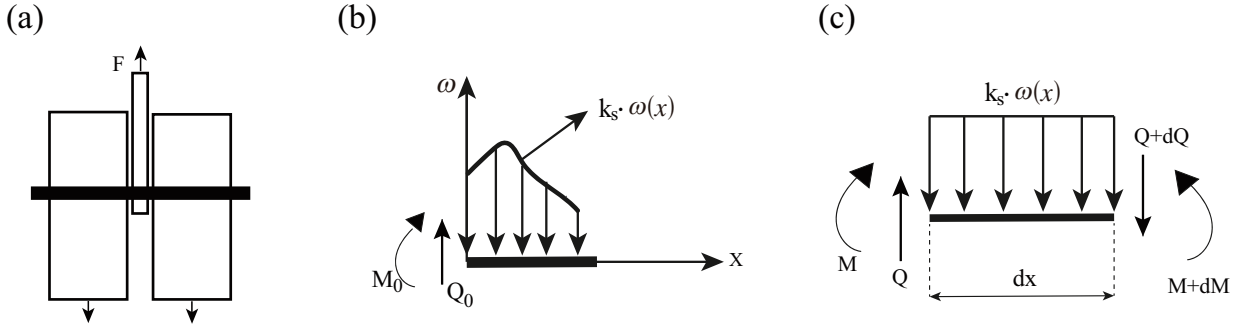


Figure 21: Force analysis of bolt shank: (a) diagram of bolt joint; (b) free body diagram of half bolt shank; (c) free body diagram of micro unit of bolt shank. M and Q represent the moment and shear force of the bolt shank, respectively. k_s represents the dowel-bearing stiffness of LVL or glulam block.

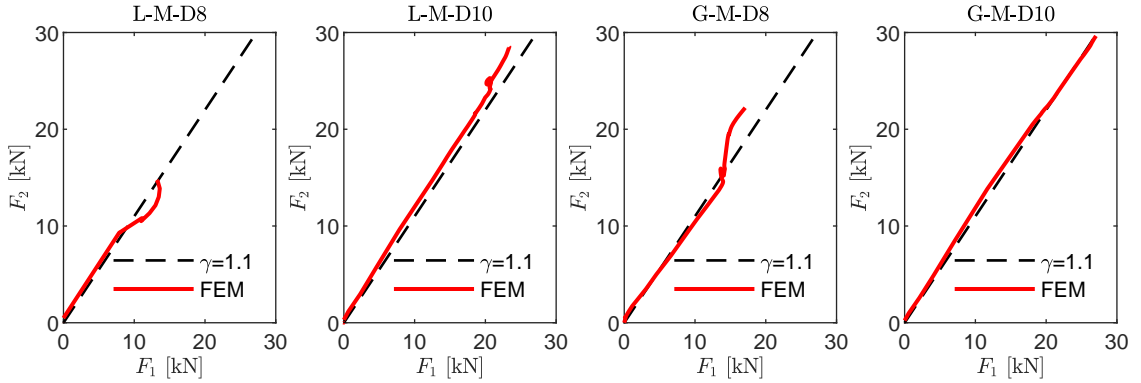


Figure 22: Comparison of the load born by the first bolt and the second bolt derived from the FE model. The red line is the relationship between F_1 and F_2 obtained from FEM analysis, and the black dashed line is the reference line with a slope of 1.1.

540 2. When the rotation of the mid-point of bolt shank ($x = 0$) is not fully constrained ($M_0 = 0$), substituting
 541 ($M_0 = 0$) into Eq. 27, one can solve that $\beta_1 = 1$.

542 Therefore, β_1 is ranging between 1 and 2. During the elastic stage, β_1 can be approximately taken as 2, since
 543 the rotation of the mid-point of the bolt shank is small.

544 4.2. Elastic stiffness of double-bolted connections

545 In double-bolted connections, the applied total load F on the bolted connections can be considered as the
 546 sum of the load applied on the first bolt F_1 and the load applied on the second bolt F_2 . From the numerical
 547 analysis, the load distributions on each bolt were obtained by summing the force of elements in contact with
 548 the bolt along the length of the bolt, and the contact force on the wood-to-bolt interface in the parallel to grain
 549 direction could be output from FE model developed in ABAQUS. The values of F_1 and F_2 obtained from the
 550 FE analyses for different configurations are listed in Figure 22. According to Figure 22, the ratio of the forces
 551 on the two bolts is $\gamma = F_2/F_1 \approx 1.1$.

552 At $x = 0$ ($\xi = 0$), the shear force is $Q_0 = 0.5F_1 = F/[2(1 + \gamma)] = F/4.2$ and when substituted into Eq. 24,
 553 the following equation can be obtained:

$$V - \phi_v = \omega_0 = \frac{l_c^2}{2EI} \left(l_c \frac{F}{4.2} + M_0 \right) \quad (29)$$

554 It is noteworthy that the deflection ω_0 of the first bolt hole at $x = 0$ in double bolted connections is no
 555 longer equal to the total displacement V as in the single bolted case (see Eq. 26). A corrected deflection term
 556 ϕ_v has to be subtracted from V to get the final deflection of the first bolt hole at $x = 0$, since the force from
 557 the second bolt F_2 has caused certain movement of the cross-section aligning with the first bolt hole. ϕ_v can
 558 be obtained as:

$$\phi_v = \frac{F_2}{E_0 A} L = \frac{F}{1.9E_0 A} L \quad (30)$$

559 where E_0 is the parallel-to-grain elastic modulus of glulam and LVL, A is the cross-sectional area of the member
 560 ($60 \times 60 \text{ mm}^2$), and L is the distance between the fixed end and the cross-section aligning with the first bolt

Table 6: Comparison of the elastic stiffness from experimental tests, FEM analyses, and proposed theoretical model. The error is calculated as the difference between the considered variable and $k_{e.Test}$ normalized by $k_{e.Test}$. $k_{e.Test}$ is the average elastic stiffness measured from the tests (see Table B.7). $k_{e.FEM}$ is the elastic stiffness determined from the FE analyses. $k_{e.Theo}$ is the elastic stiffness calculated using proposed theoretical model.

	Units	L-MS8		L-MS10		G-MS8		G-MS10		L-MD8		L-MD10		G-MD8		G-MD10	
		value	error	value	error	value	error	value	error	value	error	value	error	value	error	value	error
$k_{e.Test}$	kN/mm	20.29	—	24.61	—	24.48	—	37.48	—	30.28	—	46.22	—	33.33	—	49.70	—
$k_{e.FEM}$	kN/mm	17.76	-12%	26.52	8%	26.24	7%	36.33	-3%	28.89	-5%	51.36	11%	32.53	-2%	47.54	-4%
$k_{e.Theo}$	kN/mm	17.89	-12%	27.85	13%	28.74	17%	34.98	-7%	32.99	9%	48.10	4%	46.46	39%	53.86	8%

561 hole, equal to 290 mm (see Figure 2(b)).

562 Assuming

$$\beta_2 = \frac{1}{1 + 4.2 \frac{M_0}{l_c F}} \quad (31)$$

563 The elastic stiffness, k_e , of the bolt joint can be calculated as follows when substituting $l_c = \sqrt[4]{4EI/k_s}$ and Eq.
564 30 into Eq. 29.

$$k_e = \frac{F}{V} = \beta_2 \left(\frac{2.1 \cdot 1.9E_0 A k_s \sqrt[4]{\frac{4EI}{k_s}}}{1.9E_0 A + 2.1\beta_2 L k_s \sqrt[4]{\frac{4EI}{k_s}}} \right) \quad (32)$$

565 The determination of β_2 is similar to β_1 (see Section 4.1). Therefore, for small displacements, β_2 can also be
566 approximately taken as 2.

567 4.3. Validation

568 Table 6 shows the theoretical elastic stiffness values of the bolted connections studied here, obtained by
569 substituting the material property parameters from Table 6 into Eqs. 28 and 32. Moreover, Table 6 summarizes
570 the experimental value, simulated value from FEM and theoretical value of elastic stiffness. The theoretical
571 values and the simulated value from FEM show a better fit to the test results. It is found that the theoretical
572 values of elastic stiffness are in good agreement with the test results. Comparing Tables 6 and D.8, it can be
573 observed that the prediction of the proposed model over-perform the predictions of Eurocode 5. These findings
574 suggest that the theoretical formula proposed in this study is effective in predicting initial stiffness.

575 5. Conclusions

576 The present study investigates the mechanical performance of bolted steel connections to laminated timber
577 and bamboo composite members with slotted-in steel plates. The study compares the mechanical response of
578 two different laminated composite bio-based materials for the first time, and characterizes their cracking modes
579 and hysteretic responses. The study also implements a user-defined constitutive subroutine into a ABAQUS FE
580 code to simulate the 3-dimensional structural behavior of the connections, and proposes a material constitutive
581 integrating Hill's yielding criteria with element removal criteria for predicting brittle fracture.

582 The results show that the response of the bolted steel connections strongly depends on the number and
583 diameter of bolts and the material employed (LVL and glulam). LVL connections exhibit greater ductility
584 and energy dissipation capacity compared to glulam connections, which generally exhibit brittle behavior and
585 higher peak strength. The FE simulations are found to be in good agreement with the experimental results,
586 and the proposed material constitutive with element removal is shown to effectively simulate crack growth and
587 predict brittle fracture. The study also provides theoretical formulas for bolt joint stiffness that can be used as
588 a reference for the development of design guidelines for such connections.

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594 CRediT

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598 Declaration of Competing Interest

599 The authors declare that they have no known competing financial interests or personal relationships that
600 could have appeared to influence the work reported in this paper.

601 Data availability

602 The data that support the findings of this study are available from the corresponding author, S.D., upon
603 reasonable request.

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784 **Appendix A. Loading protocol and definition of performance indices**

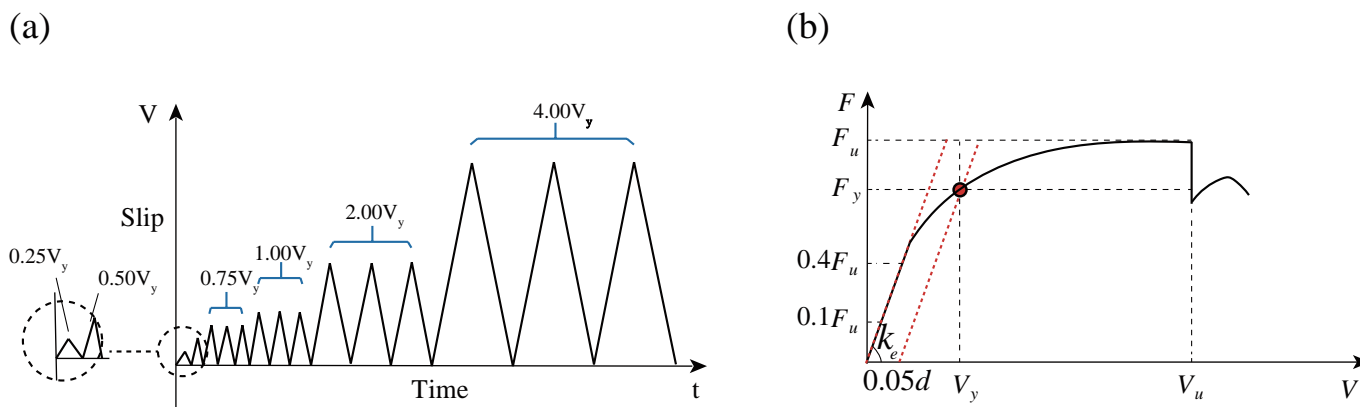


Figure A.23: Loading regime for cyclic testing (a) and definition of k_e , F_y , F_u , and V_u and V_y according to ASTM D5764-97a [42] (b).

Table B.7: Summary of mechanical indicators (k_e , F_y , F_u , V_y , V_u and D) for all the tests. (Over-bar: average across the tests; CV: Coefficient of variation). After Shi et al. [39].

ID	k_e [kN/mm]	k_e [kN/mm]	CV [%]	F_y [kN]	F_y [kN]	CV [%]	F_u [kN]	F_u [kN]	CV [%]	V_y [mm]	V_y [mm]	CV [%]	V_u [mm]	V_u [mm]	CV [%]	D	D	CV [%]
LMS8-1	20.95			15.06			21.03			1.31			26.56			26.53		
LMS8-2	16.22	20.29	20.63	12.39	13.19	12.27	23.34	21.19	9.77	0.89	1.09	19.27	27.46	27.21	2.09	18.13	22.05	20.82
LMS8-3	23.73			12.13			19.20			1.08			27.61			21.49		
LMS10-1	30.81			20.10			24.32			1.27			12.05			8.74		
LMS10-2	22.77	24.61	13.84	17.99	19.33	5.40	21.55	22.76	8.38	1.15	1.23	5.69	17.92	15.86	20.81	11.96	9.30	24.23
LMS10-3	20.24			19.91			22.41			1.26			17.60			7.20		
LMD8-1	26.10			23.69			33.48			1.74			9.68			5.53		
LMD8-2	29.76	30.28	14.36	21.73	22.95	4.76	30.38	31.74	4.98	1.12	1.31	28.24	11.03	10.91	10.82	7.80	7.40	32.99
LMD8-3	34.99			23.42			31.38			1.08			12.03			8.88		
LMD10-1	40.70			35.31			36.69			1.45			4.56			2.94		
LMD10-2	44.84	46.22	15.40	36.17	36.97	6.52	43.75	42.54	12.56	1.31	1.36	5.88	6.04	5.00	18.00	2.84	2.98	21.29
LMD10-3	53.13			39.43			47.16			1.31			4.40			3.14		
GMS8-1	28.77			17.06			27.30			1.04			10.43			6.58		
GMS8-2	23.95	24.48	16.48	17.01	17.25	1.98	30.60	30.40	9.87	1.19	1.15	9.57	14.45	13.45	19.78	6.35	7.22	11.32
GMS8-3	20.73			17.68			33.30			1.24			15.46			8.74		
GMS10-1	34.99			27.20			38.59			1.30			9.09			4.80		
GMS10-2	44.54	37.48	16.60	26.50	26.97	1.41	38.46	38.27	1.18	1.10	1.25	11.20	7.75	8.15	10.06	6.14	5.19	13.00
GMS10-3	32.92			27.20			37.76			1.37			7.61			4.64		
GMD8-1	31.71			36.19			45.07			1.61			5.14			2.10		
GMD8-2	39.34	33.33	18.78	34.52	36.47	3.38	42.12	43.21	3.75	1.36	1.41	12.06	3.87	3.89	31.88	2.39	1.93	21.03
GMD8-3	28.92			38.70			42.43			1.28			2.66			1.31		
GMD10-1	58.86			53.30			60.25			1.48			4.50			3.04		
GMD10-2	43.92	49.70	15.89	53.97	54.03	1.22	62.98	62.15	2.65	1.80	1.69	10.65	3.99	4.23	6.15	2.22	1.98	17.79
GMD10-3	46.33			54.83			63.21			1.80			4.20			2.34		

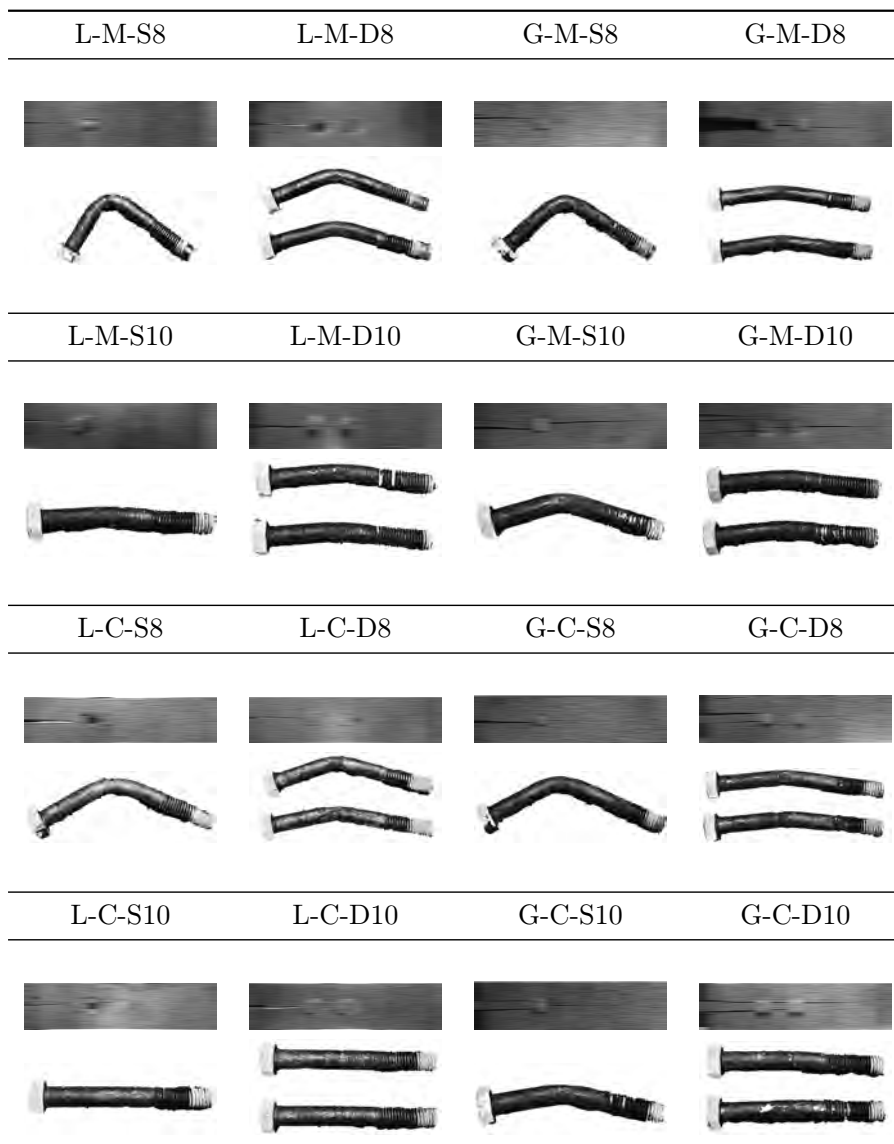


Figure C.24: Failure pattern and bolt deformation after the test. The first two columns show the crack pattern for LVL specimen and the last two columns show glulam specimen. The first two rows show the monotonic cases and the last two rows show the cyclic cases.

789

790 Appendix D. Comparison of the tested results, FEM results, and predicted results by EC5 under
 791 monotonic loading

Table D.8: Comparison of initial stiffness and maximum load between test and predicted value by FEM and EC5 [79]. The error is calculated as the difference between the considered variable and $k_{e,Test} (F_{u,Test}, D_{Test})$ normalized by $k_{e,Test} (F_{u,Test}, D_{Test})$. $k_{e,Test}$ is the average elastic stiffness measured from the tests (see Table B.7). $k_{e,FEM}$ is the elastic stiffness determined from the FE analyses. $k_{e,EC5}$ is the elastic stiffness calculated according to EC5. $F_{u,Test}$ is the average maximum load measured from the tests (see Table B.7). $F_{u,FEM}$ is the maximum load determined from the FE analyses. $F_{u,EC5}$ is the maximum load calculated according to EC5. D_{Test} is the average ductility obtained from the tests (see Table B.7). D_{FEM} is the ductility determined from the FE analyses.

Conf.	Units	L-MS8		L-MS10		G-MS8		G-MS10		L-MD8		L-MD10		G-MD8		G-MD10	
		value	error	value	error	value	error	value	error	value	error	value	error	value	error	value	error
$k_{e,Test}$	kN/mm	20.29	—	24.61	—	24.48	—	37.48	—	30.28	—	46.22	—	33.33	—	49.70	—
$k_{e,FEM}$	kN/mm	17.76	-12%	26.52	8%	26.24	7%	36.33	-3%	28.89	-5%	51.36	11%	32.53	-2%	47.54	-4%
$k_{e,EC5}$	kN/mm	21.16	4%	26.44	7%	28.52	17%	35.64	-5%	42.32	40%	52.88	14%	57.04	71%	71.28	43%
$F_{u,Test}$	kN	21.19	4%	22.76	-8%	30.40	24%	38.27	2%	31.74	5%	42.54	-8%	43.21	30%	62.15	25%
$F_{u,FEM}$	kN	20.33	0.2%	24.38	-1%	30.62	25%	38.71	3%	30.82	2%	49.31	7%	42.51	28%	67.6	36%
$F_{u,EC5}$	kN	16.77	-17%	22.36	-9%	23.31	-5%	35.98	-4%	24.82	-18%	31.08	33%	33.10	-1%	50.00	1%
D_{Test}	—	22.05	—	9.30	—	7.22	—	5.19	—	7.40	—	2.98	—	1.93	—	1.98	—
D_{FEM}	—	21.79	-1%	11.49	24%	11.07	53%	7.10	37%	7.31	-1%	5.24	76%	2.12	9.8%	5.48	177%

