

# Supplementary Material of "A Multi-Population Evolutionary Algorithm Using New Cooperative Mechanism for Solving Multi-Objective Problems with Multi-Constraint"

Juan Zou <sup>1</sup>, *Member, IEEE*, ✉Ruiqing Sun <sup>1</sup>, Yuan Liu, Yaru Hu, Shengxiang Yang, *Senior Member, IEEE*, Jinhua Zheng, *Member, IEEE*, and Ke Li, *Senior Member, IEEE*,

This is the supplementary of "A Multi-Population Evolutionary Algorithm Using New Cooperative Mechanism for Solving Multi-Objective Problems with Multi-Constraint"

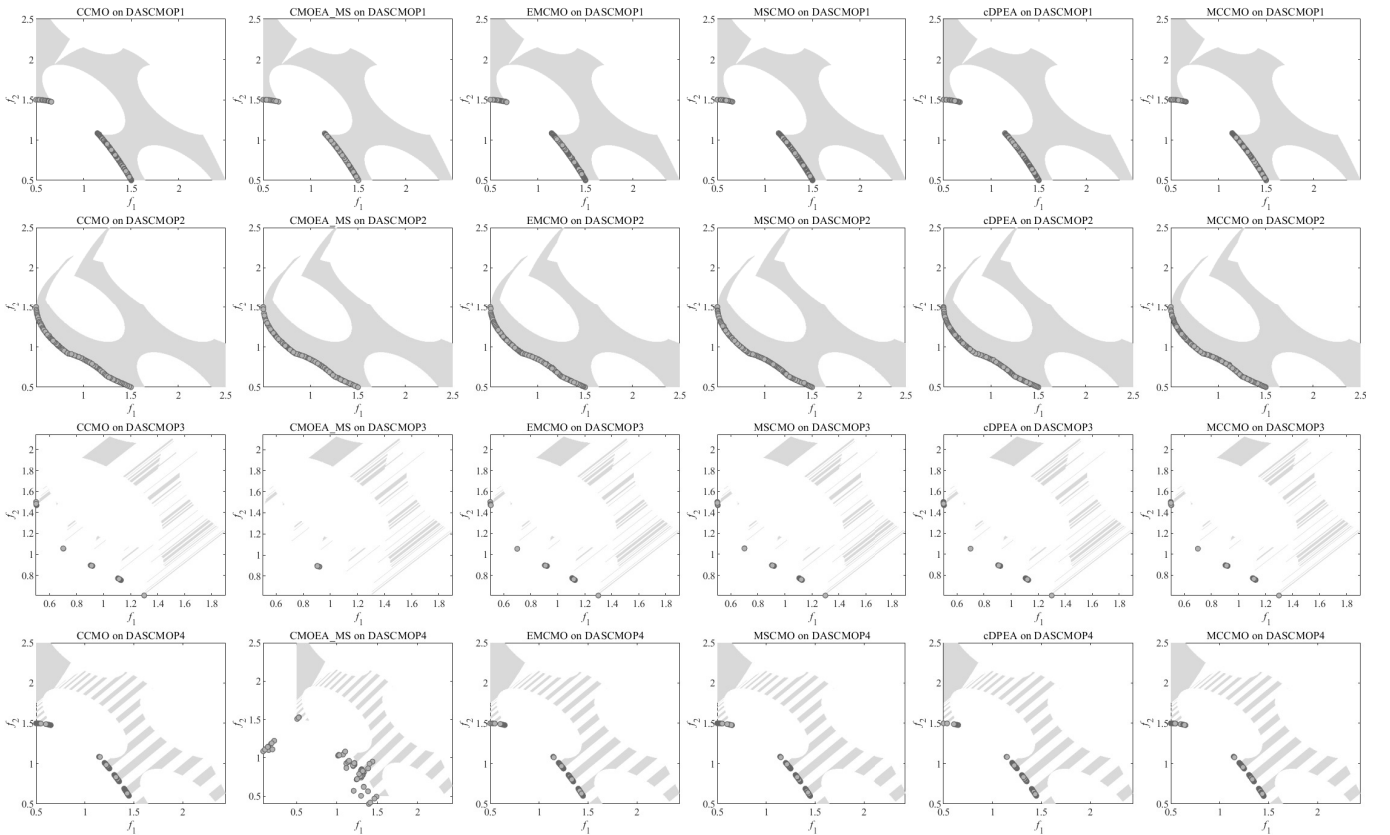


Fig. 1. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DASCMP1-4 respectively.

Ruiqing Sun (Corresponding author, email: sunny0331@foxmail.com), Juan Zou, Yuan Liu, Yaru Hu, Shengxiang Yang and Jinhua Zheng are with Hunan Engineering Research Center of Intelligent System Optimization and Security, Key Laboratory of Intelligent Computing and Information Processing, Ministry of Education of China, and Key Laboratory of Hunan Province for Internet of Things and Information Security, Xiangtan University, Xiangtan, 411105, Hunan Province, China.

Shengxiang Yang is also with the School of Computer Science and Informatics, De Montfort University, Leicester LE1 9BH, U.K.

Ke Li is with the Department of Computer Science, University of Exeter, Exeter EX4 4QF, U.K.

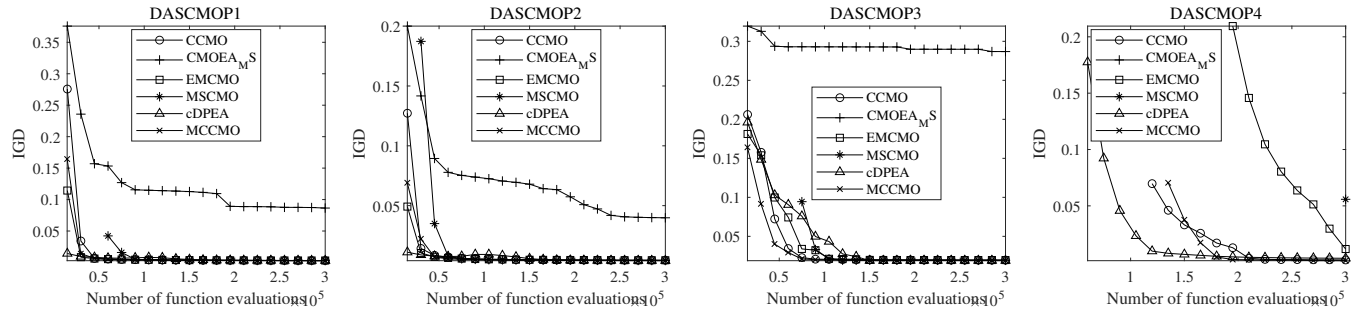


Fig. 2. The profiles of IGD obtained by MCCMO and comparison algorithm on DASCMP1-4, averaged over 30 runs.

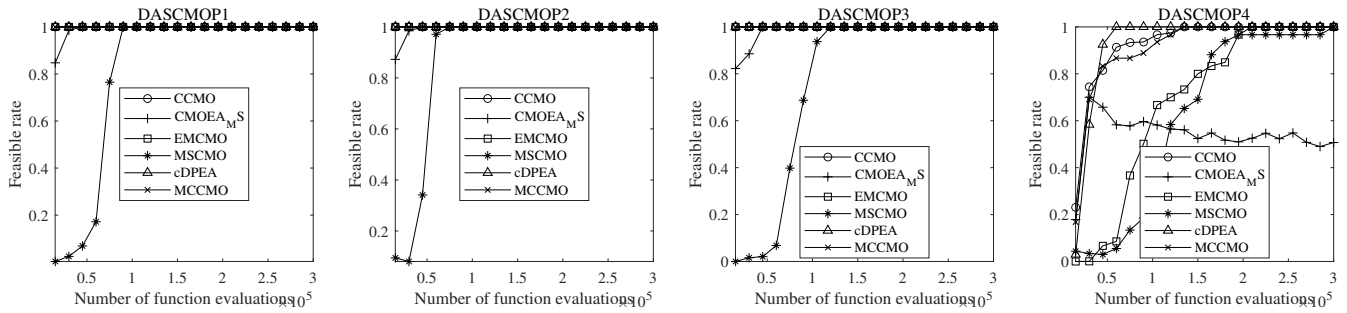


Fig. 3. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DASCMP1-4, averaged over 30 runs.

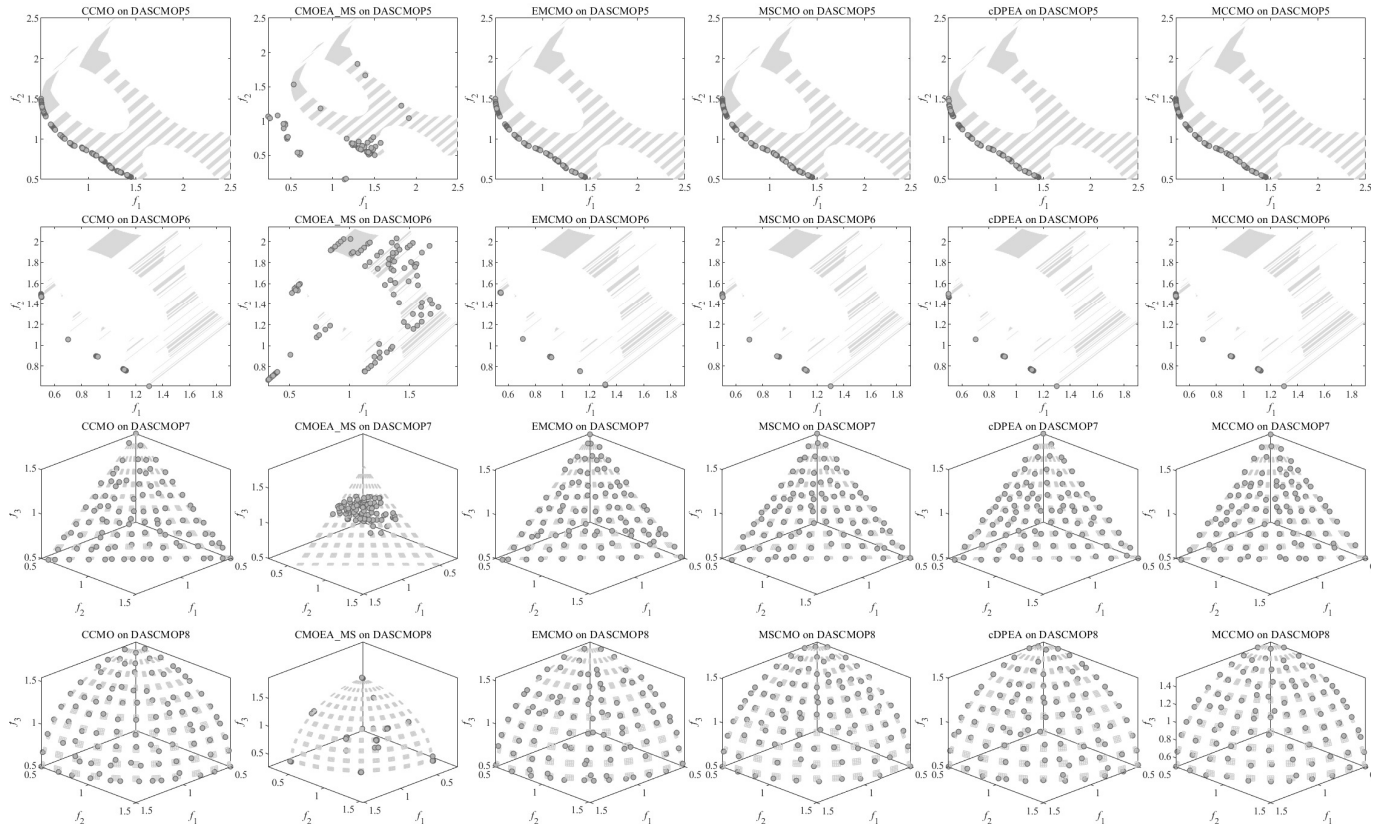


Fig. 4. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DASCMP5-8 respectively.

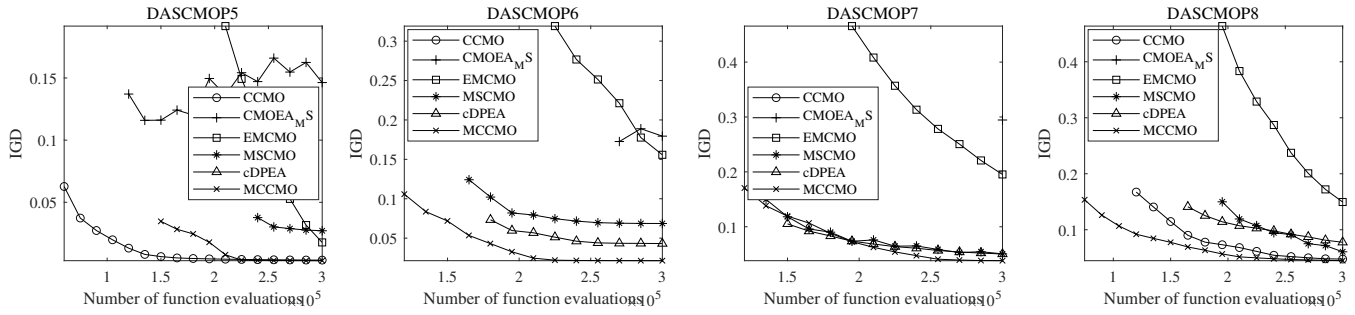


Fig. 5. The profiles of IGD obtained by MCCMO and comparison algorithm on DASCMP5-8, averaged over 30 runs.

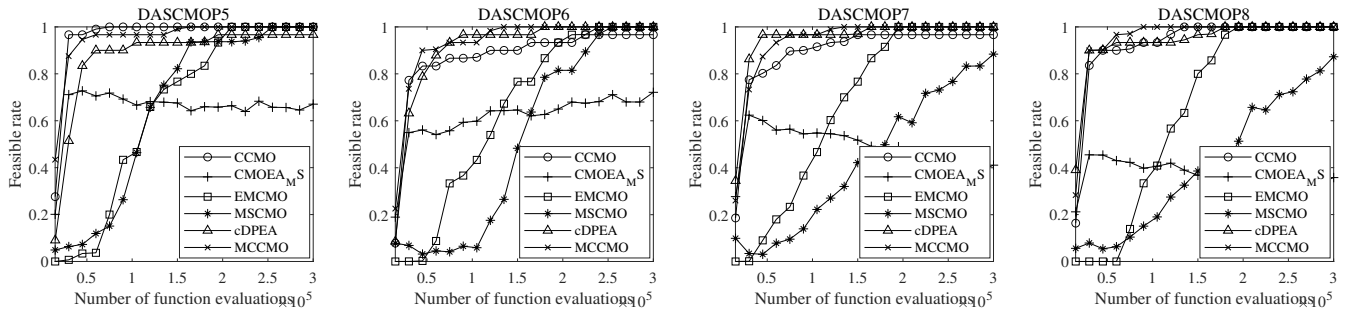


Fig. 6. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DASCMP5-8, averaged over 30 runs.

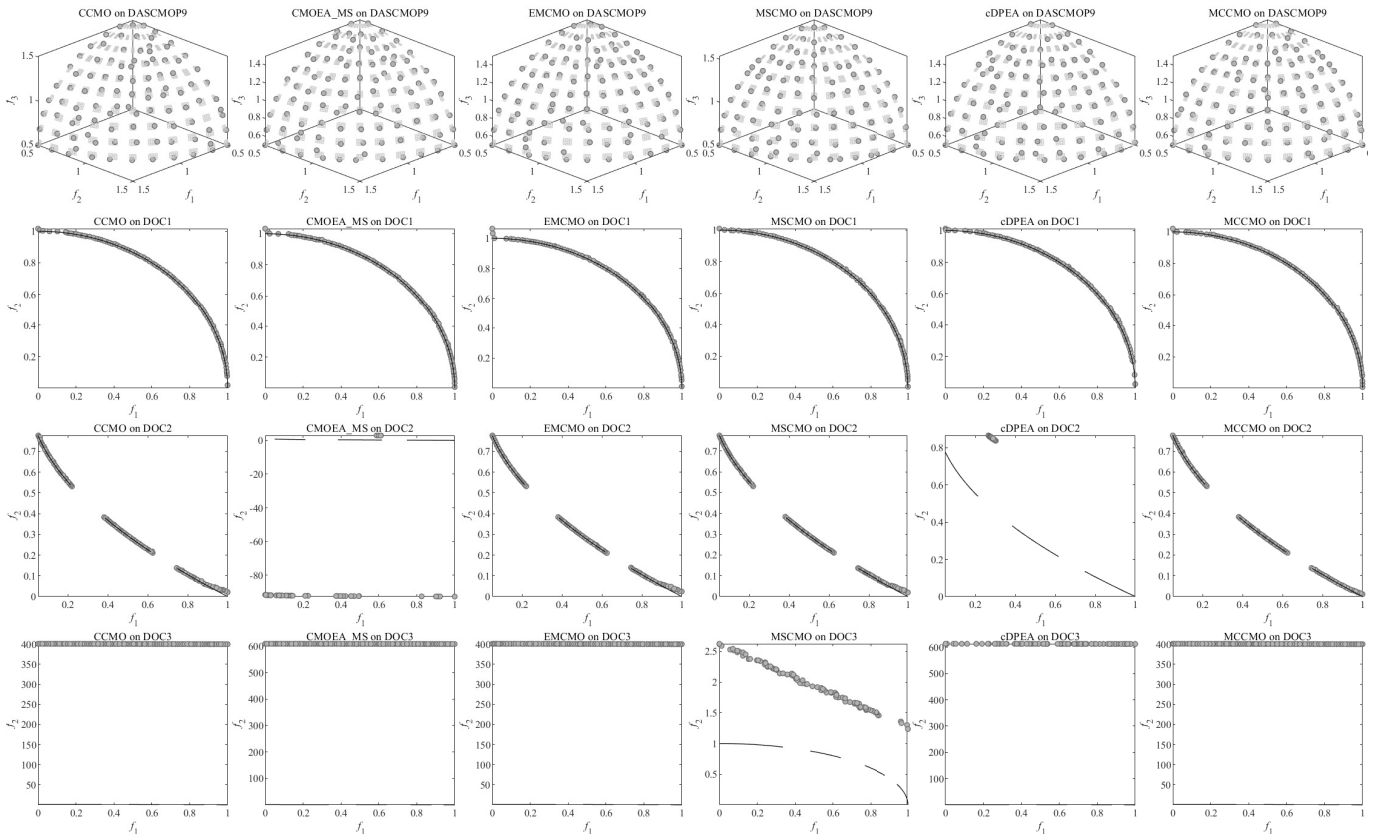


Fig. 7. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DASCMP9 and DOC1-3 respectively.

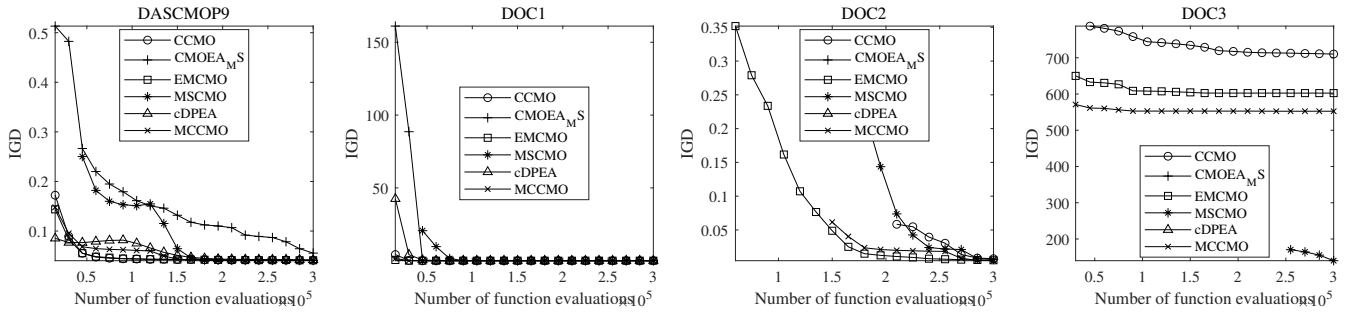


Fig. 8. The profiles of IGD obtained by MCCMO and comparison algorithm on DASCMP9 and DOC1-3, averaged over 30 runs.

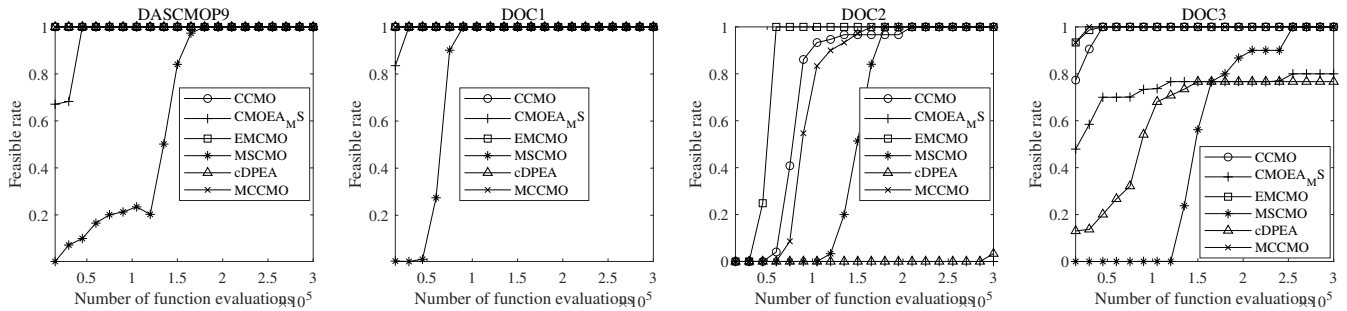


Fig. 9. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DASCMP9 and DOC1-3, averaged over 30 runs.

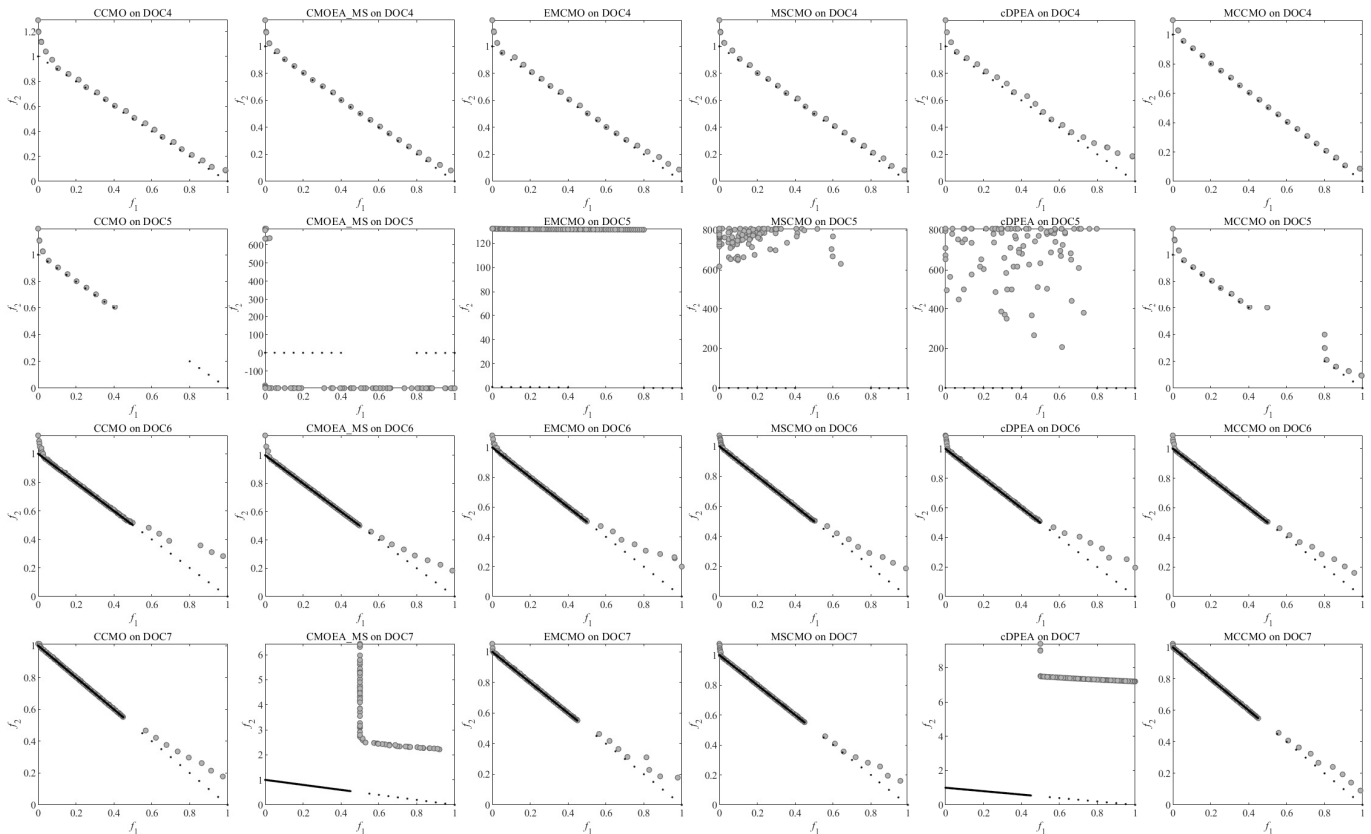


Fig. 10. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DOC4-7 respectively.

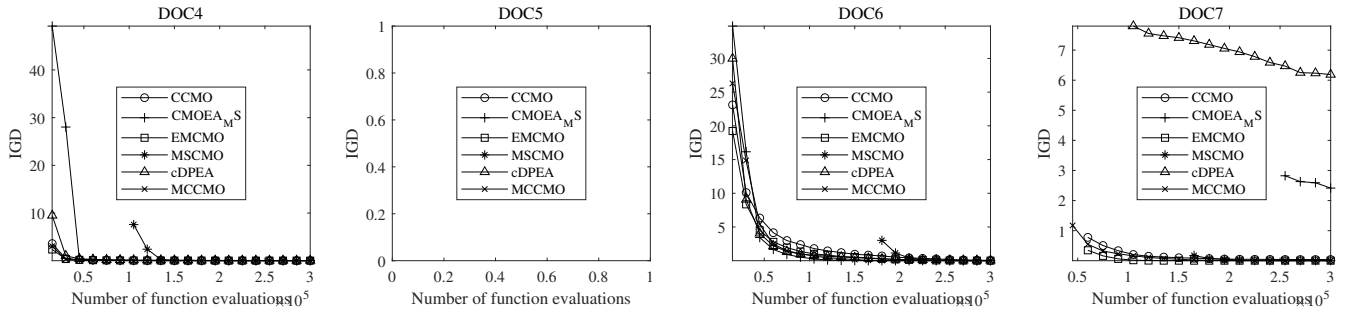


Fig. 11. The profiles of IGD obtained by MCCMO and comparison algorithm on DOC4-7, averaged over 30 runs.

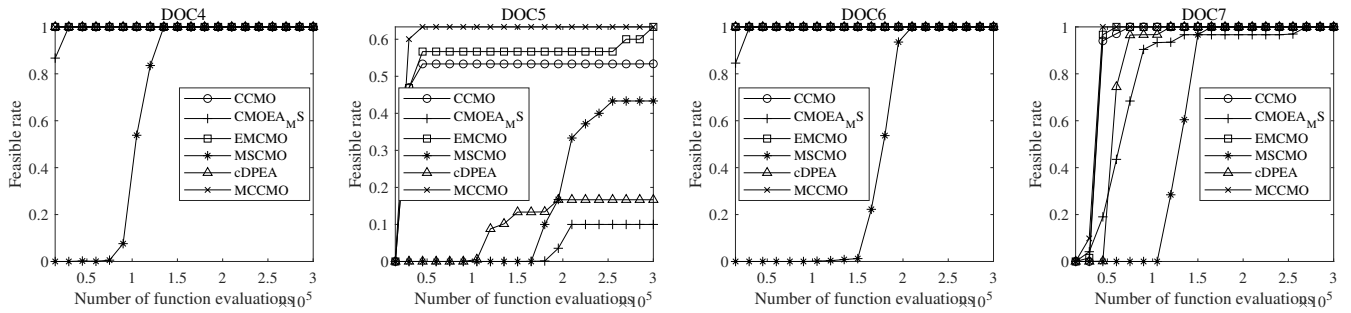


Fig. 12. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DOC4-7, averaged over 30 runs.

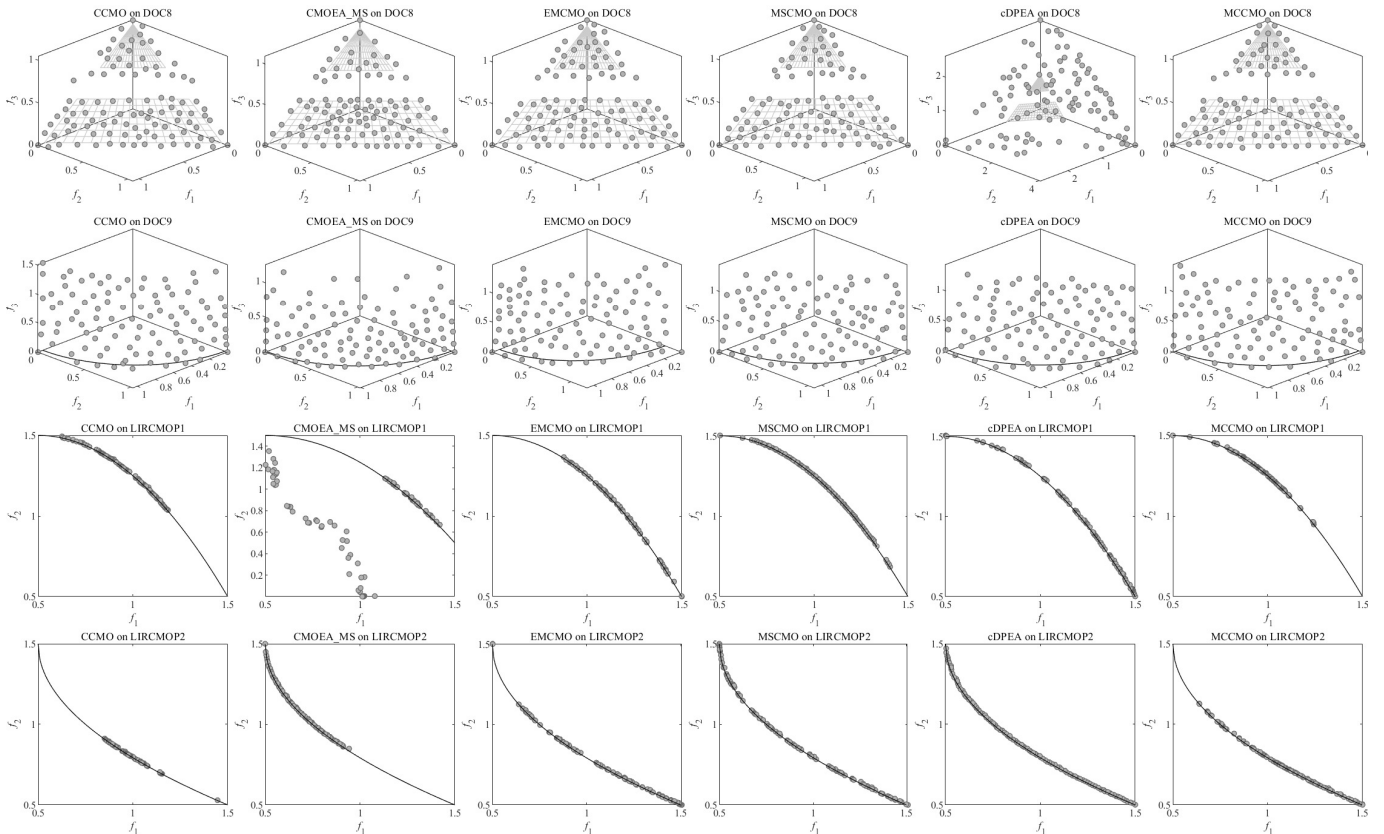


Fig. 13. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DOC8-9 and LIRCMOP1-2 respectively.

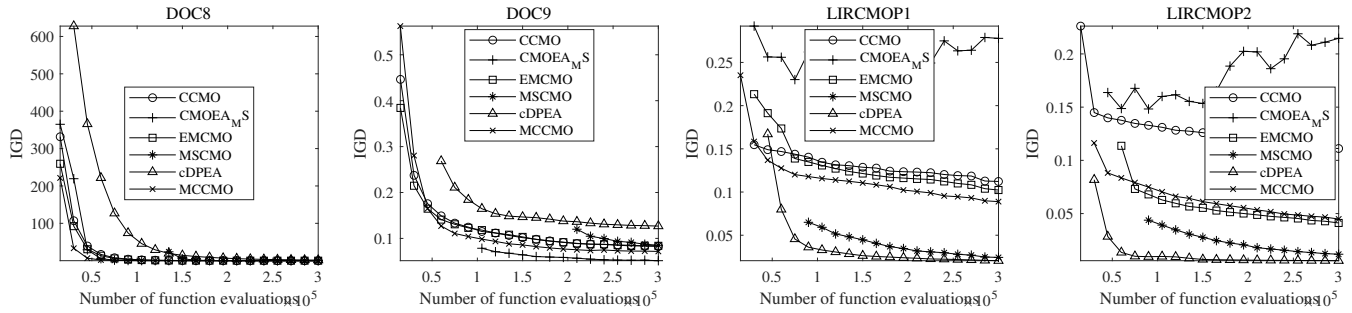


Fig. 14. The profiles of IGD obtained by MCCMO and comparison algorithm on DOC8-9 and LIRC MOP1-2, averaged over 30 runs.

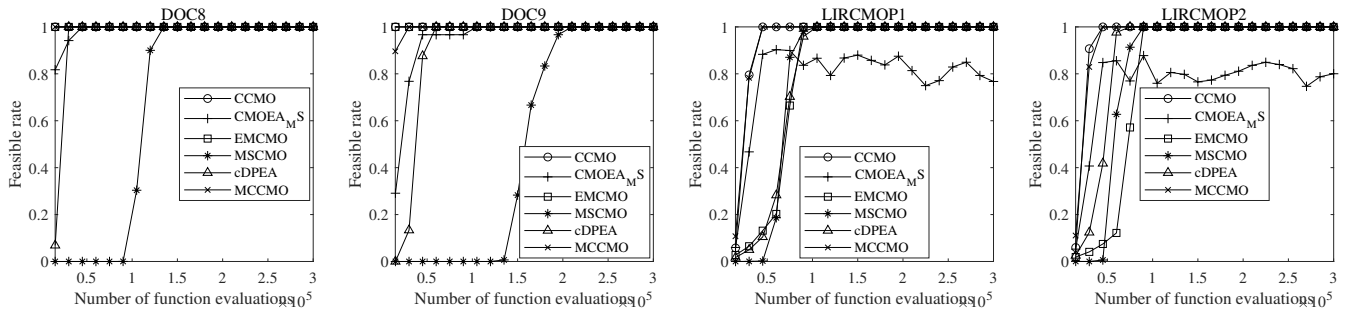


Fig. 15. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DOC8-9 and LIRC MOP1-2, averaged over 30 runs.

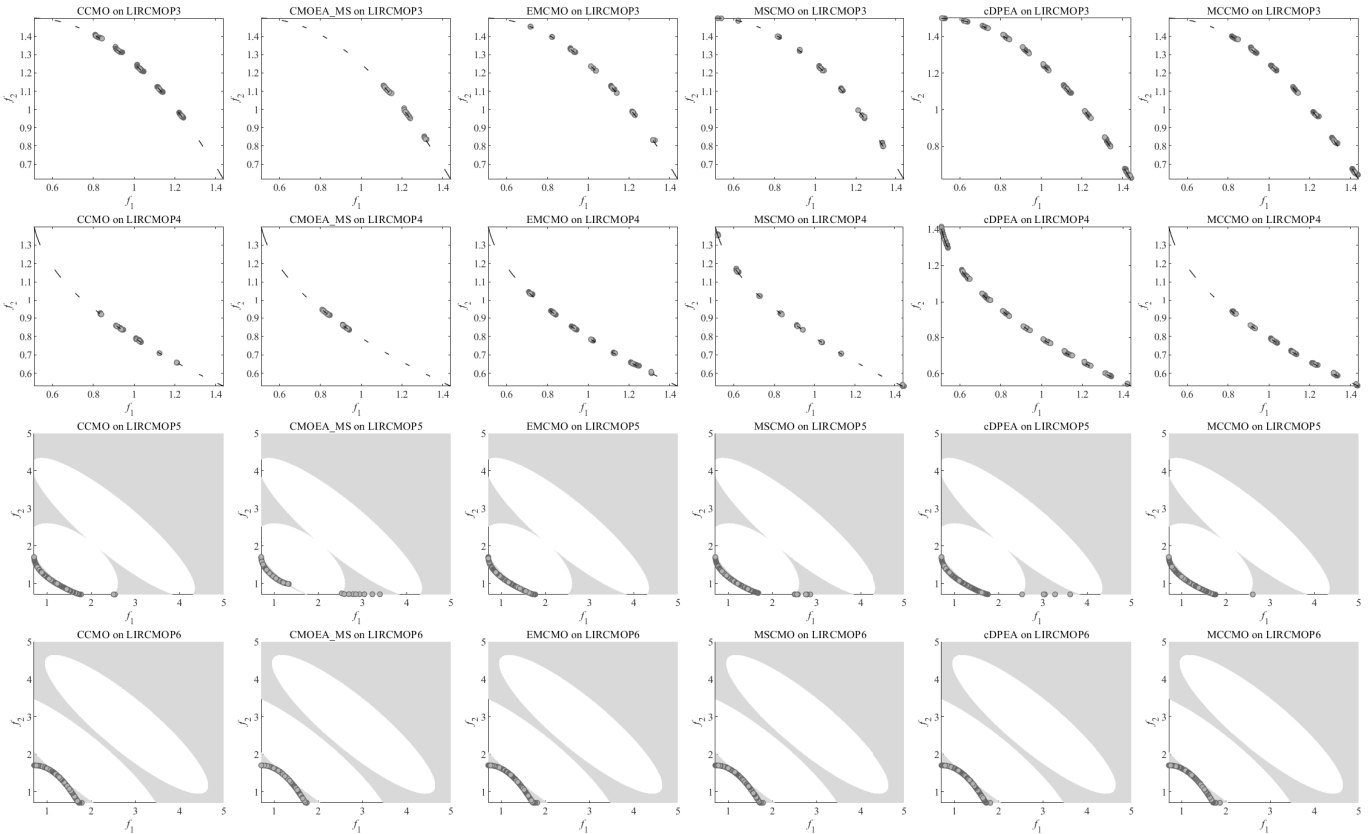


Fig. 16. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on LIRC MOP3-6 respectively.

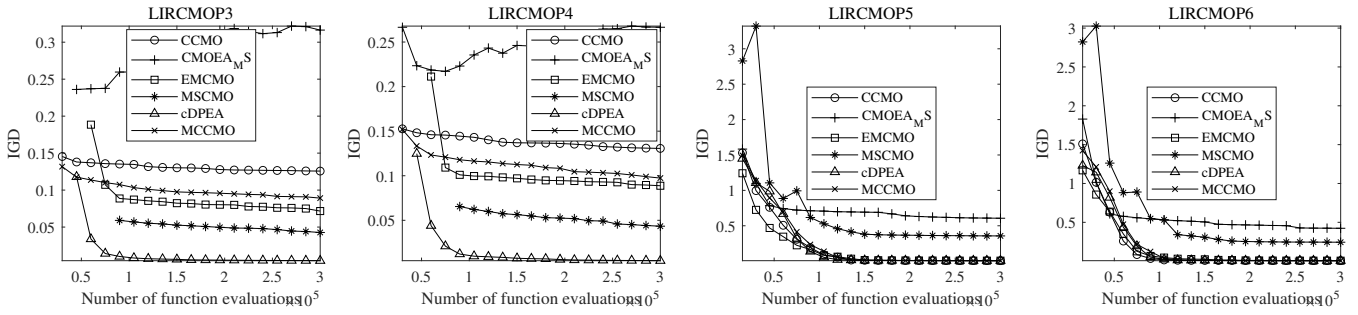


Fig. 17. The profiles of IGD obtained by MCCMO and comparison algorithm on LIRC MOP3-6, averaged over 30 runs.

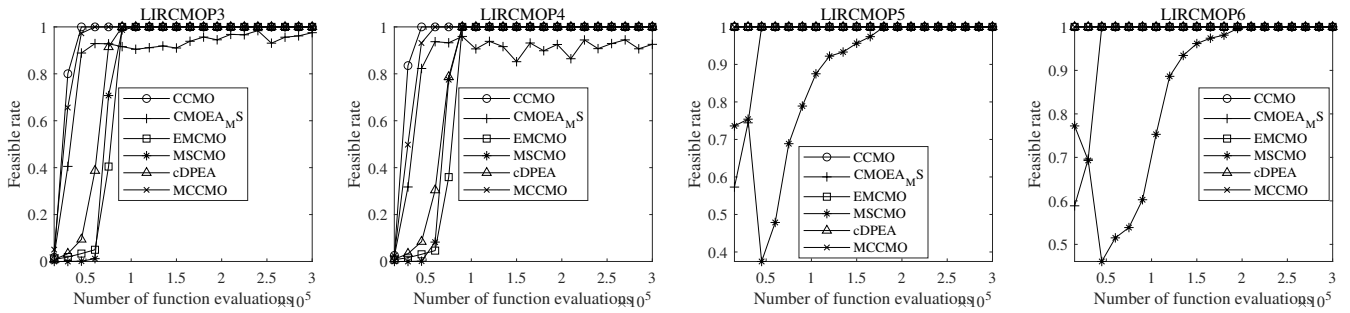


Fig. 18. The profiles of feasible rates obtained by MCCMO and comparison algorithm on LIRC MOP3-6, averaged over 30 runs.

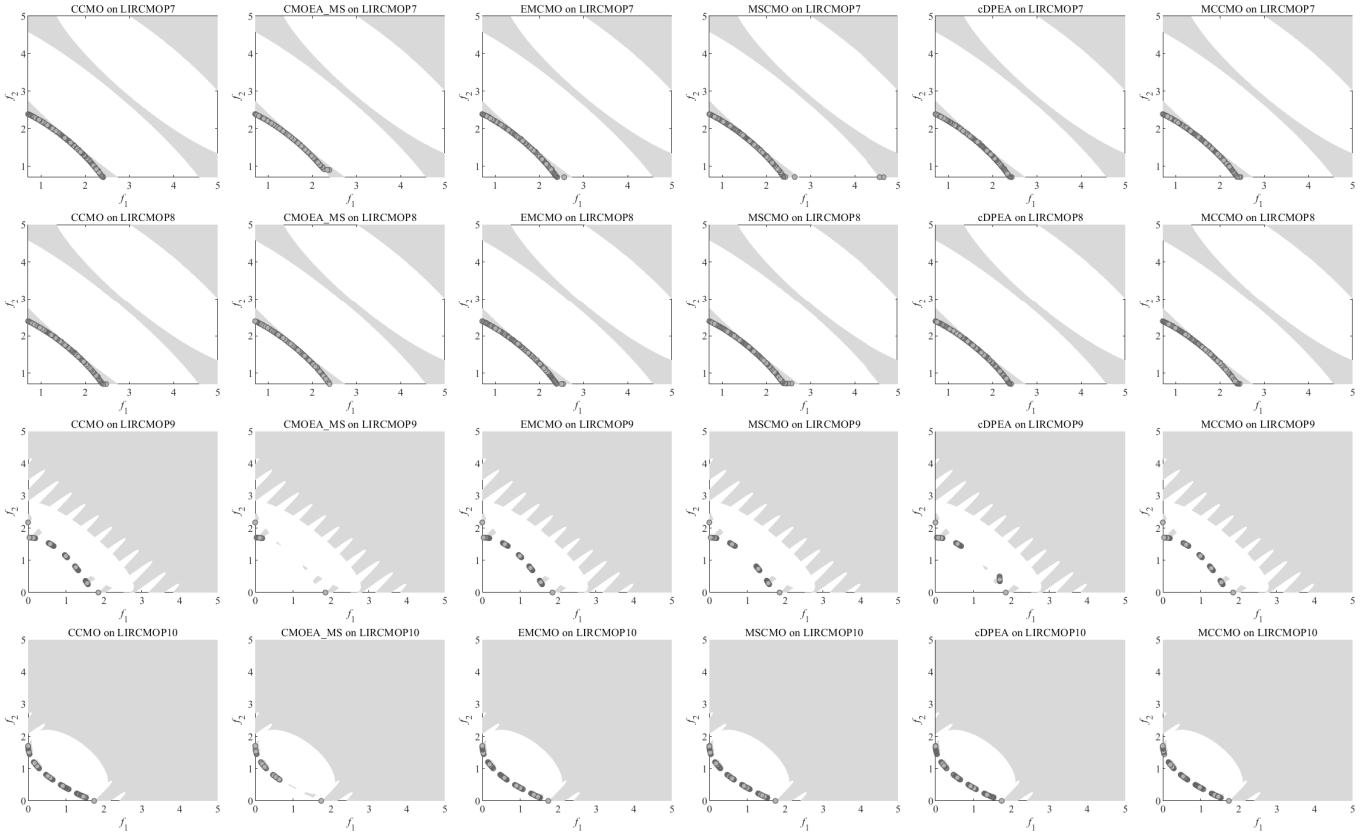


Fig. 19. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on LIRC MOP7-10 respectively.

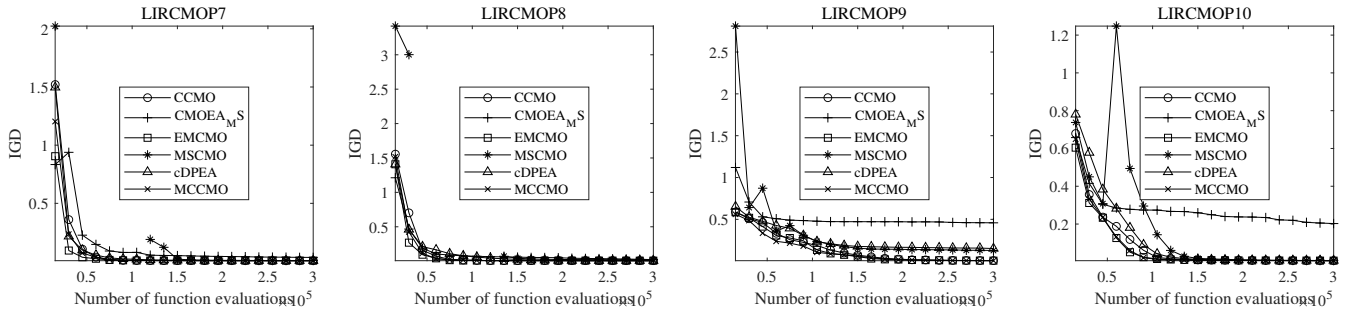


Fig. 20. The profiles of IGD obtained by MCCMO and comparison algorithm on DASC MOP1-6, averaged over 30 runs.

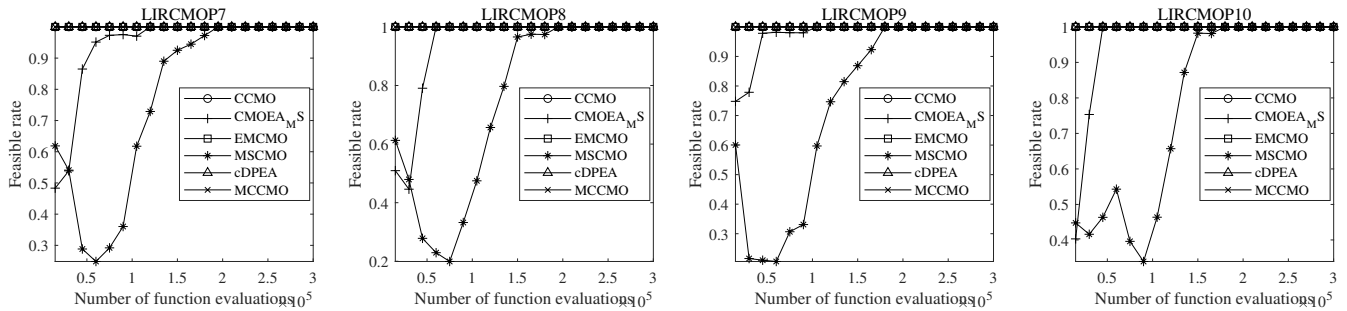


Fig. 21. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DASC MOP1-6, averaged over 30 runs.

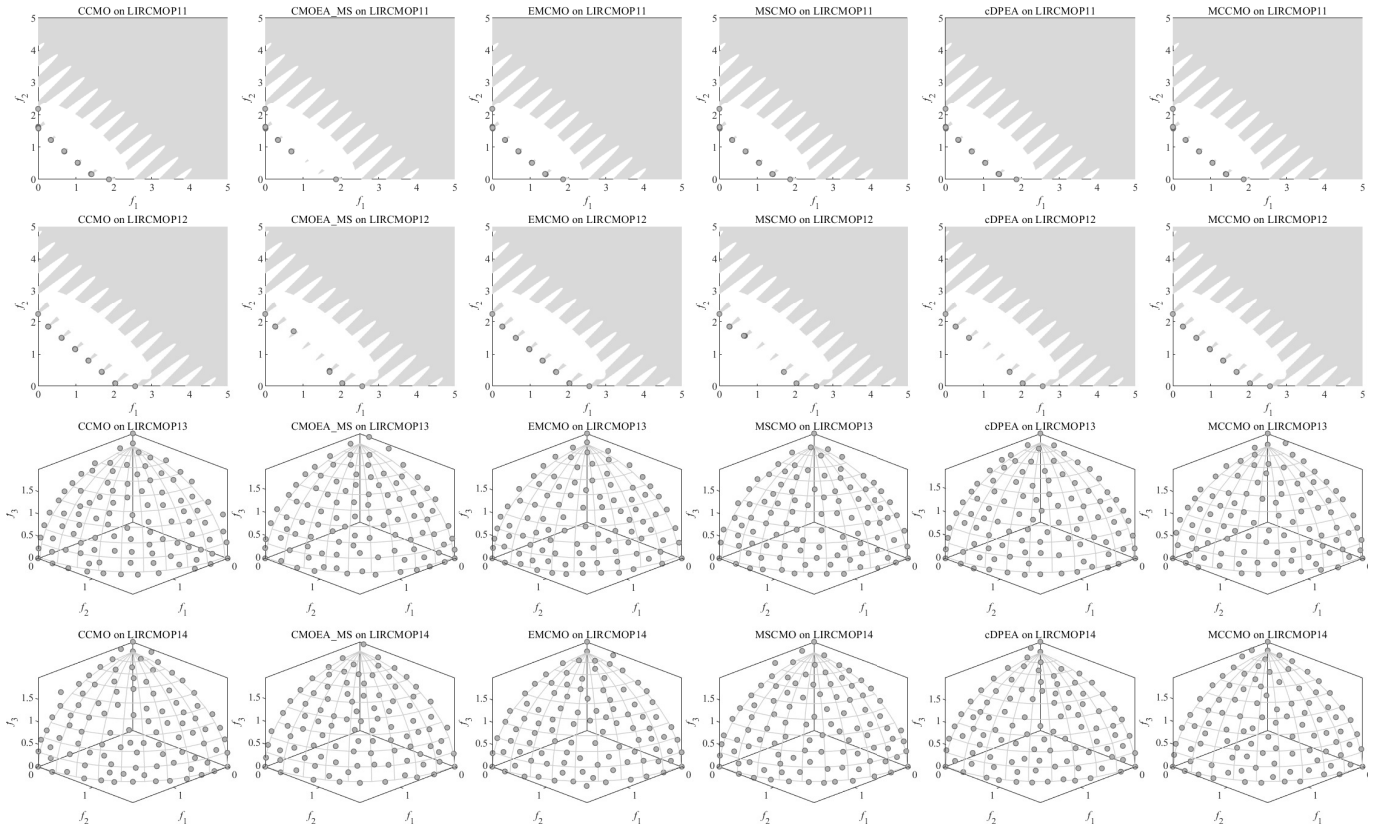


Fig. 22. Solutions with median IGD value among 30 runs obtained by MCCMO and comparison algorithm on DASC MOP1-6 respectively.



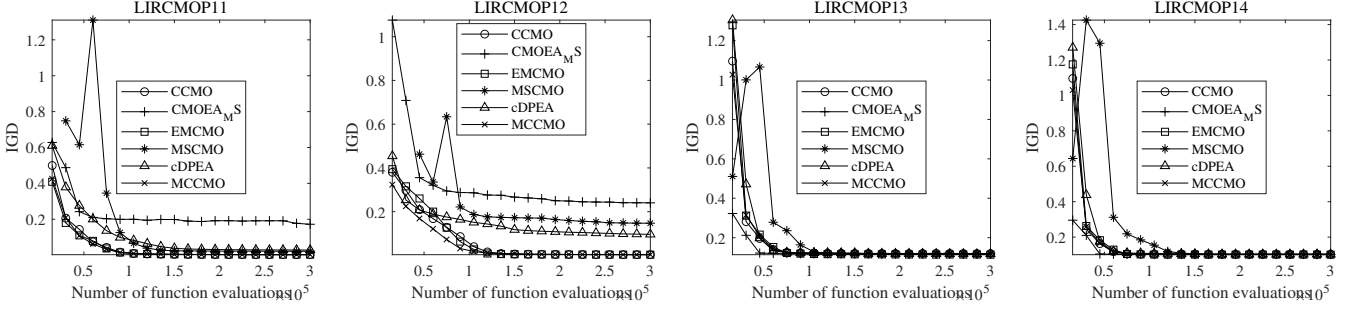


Fig. 23. The profiles of IGD obtained by MCCMO and comparison algorithm on DASC MOP1-6, averaged over 30 runs.

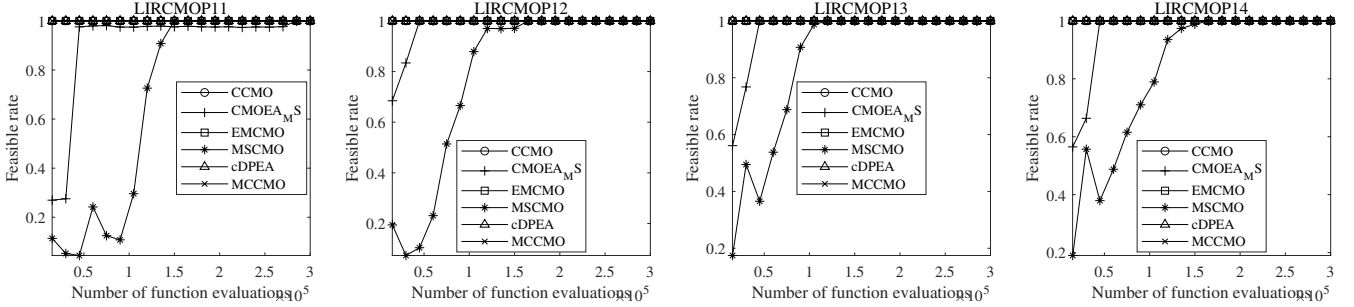


Fig. 24. The profiles of feasible rates obtained by MCCMO and comparison algorithm on DASC MOP1-6, averaged over 30 runs.

TABLE I

MEAN AND STANDARD DEVIATION OF RUNTIME. '+', '-', AND '≈' INDICATE THAT THE RESULT IS SIGNIFICANTLY BETTER, SIGNIFICANTLY WORSE, AND STATISTICALLY SIMILAR TO THAT OBTAINED BY MCCMO, RESPECTIVELY.

| Problem    | $M$ | $D$ | CCMO                  | CMOEA <sub>MS</sub>   | EMCMO                 | MSCMO                 | cDPEA                 | MCCMO               |
|------------|-----|-----|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|---------------------|
| DASC MOP1  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP2  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP3  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP4  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 5.0700e-1 (2.18e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP5  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 6.7067e-1 (2.43e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 9.6667e-1 (1.83e-1) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP6  | 2   | 30  | 9.6667e-1 (1.83e-1) ≈ | 7.2133e-1 (2.22e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP7  | 3   | 30  | 9.6667e-1 (1.83e-1) ≈ | 4.1100e-1 (2.61e-1) - | 1.0000e+0 (0.00e+0) ≈ | 8.8400e-1 (2.65e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP8  | 3   | 30  | 1.0000e+0 (0.00e+0) ≈ | 3.5767e-1 (2.45e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DASC MOP9  | 3   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC1       | 2   | 6   | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC2       | 2   | 16  | 1.0000e+0 (0.00e+0) ≈ | 0.0000e+0 (0.00e+0) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 3.3333e-2 (1.83e-1) - | 1.0000e+0 (0.00e+0) |
| DOC3       | 2   | 10  | 1.0000e+0 (0.00e+0) ≈ | 8.0000e-1 (4.07e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 7.6667e-1 (4.30e-1) - | 1.0000e+0 (0.00e+0) |
| DOC4       | 2   | 8   | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC5       | 2   | 8   | 5.3367e-1 (5.07e-1) ≈ | 1.0000e-1 (3.05e-1) - | 6.3333e-1 (4.90e-1) ≈ | 4.3333e-1 (5.04e-1) ≈ | 1.6667e-1 (3.79e-1) - | 6.3333e-1 (4.90e-1) |
| DOC6       | 2   | 11  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC7       | 2   | 11  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC8       | 3   | 10  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| DOC9       | 3   | 11  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP1  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 7.6733e-1 (2.78e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP2  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 8.0033e-1 (1.63e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP3  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 9.7533e-1 (6.34e-2) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP4  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 9.2567e-1 (1.20e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP5  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP6  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP7  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP8  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP9  | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP10 | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP11 | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP12 | 2   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP13 | 3   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| LIRC MOP14 | 3   | 30  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
|            |     |     | + / - / ≈             | 0/0/32                | 0/12/20               | 0/0/32                | 0/2/30                | 0/3/29              |

TABLE II

MEAN AND STANDARD DEVIATION OF IGD VALUES OF VARIANTS OF MCCMO. '+' , '-' , AND '≈' INDICATE THAT THE RESULT IS SIGNIFICANTLY BETTER, SIGNIFICANTLY WORSE, AND STATISTICALLY SIMILAR TO THAT OBTAINED BY MCCMO, RESPECTIVELY.

| Problem   | $M$ | $D$ | MCCMO1                | MCCMO2                | MCCMO3                | MCCMO               |
|-----------|-----|-----|-----------------------|-----------------------|-----------------------|---------------------|
| DASCMOP1  | 2   | 30  | 3.1886e-3 (6.65e-4) – | 2.8558e-3 (2.21e-4) ≈ | 2.9329e-3 (4.27e-4) ≈ | 2.8410e-3 (2.29e-4) |
| DASCMOP2  | 2   | 30  | 4.1161e-3 (1.32e-4) ≈ | 4.2011e-3 (1.08e-4) – | 4.1148e-3 (9.50e-5) ≈ | 4.1368e-3 (9.31e-5) |
| DASCMOP3  | 2   | 30  | 1.8488e-2 (2.41e-3) ≈ | 1.9446e-2 (2.21e-4) ≈ | 3.1279e-2 (4.96e-2) ≈ | 1.9180e-2 (1.25e-3) |
| DASCMOP4  | 2   | 30  | 1.3943e-3 (5.58e-4) ≈ | 1.4791e-3 (3.12e-4) – | 1.7282e-2 (7.19e-2) ≈ | 1.3517e-3 (2.73e-4) |
| DASCMOP5  | 2   | 30  | 3.0789e-3 (1.84e-4) ≈ | 4.0282e-3 (3.87e-3) – | 5.5662e-2 (2.03e-1) ≈ | 3.0396e-3 (1.55e-4) |
| DASCMOP6  | 2   | 30  | 4.0979e-2 (9.75e-2) ≈ | 1.0109e-1 (2.05e-1) ≈ | 3.6965e-2 (4.13e-2) ≈ | 2.1414e-2 (6.55e-3) |
| DASCMOP7  | 3   | 30  | 6.0847e-2 (8.96e-2) ≈ | 1.5295e-1 (2.51e-1) – | 1.0279e-1 (1.78e-1) ≈ | 3.8207e-2 (3.51e-3) |
| DASCMOP8  | 3   | 30  | 1.0651e-1 (1.77e-1) ≈ | 1.5608e-1 (2.45e-1) – | 9.8616e-2 (1.48e-1) – | 4.4730e-2 (4.72e-3) |
| DASCMOP9  | 3   | 30  | 4.0612e-2 (1.31e-3) ≈ | 4.1095e-2 (1.10e-3) – | 4.0863e-2 (1.05e-3) ≈ | 4.0501e-2 (1.02e-3) |
| DOC1      | 2   | 6   | 5.1269e-3 (3.35e-4) ≈ | 5.3624e-3 (3.41e-4) – | 5.1773e-3 (3.29e-4) ≈ | 5.1229e-3 (3.01e-4) |
| DOC2      | 2   | 16  | 3.4635e-3 (5.58e-4) ≈ | 2.1395e-2 (9.45e-2) – | 4.0878e-3 (1.55e-3) + | 4.4874e-3 (6.65e-3) |
| DOC3      | 2   | 10  | 5.0951e+2 (3.79e+2) ≈ | 4.6282e+2 (3.01e+2) ≈ | 4.8315e+2 (3.43e+2) ≈ | 5.5249e+2 (3.92e+2) |
| DOC4      | 2   | 8   | 1.6729e-2 (3.09e-3) ≈ | 1.6941e-2 (1.54e-3) – | 1.5946e-2 (3.05e-3) ≈ | 1.5915e-2 (1.82e-3) |
| DOC5      | 2   | 8   | 2.3066e+1 (5.13e+1) – | 6.2510e+0 (2.85e+1) – | 1.0083e+1 (3.55e+1) ≈ | 4.2398e-2 (7.12e-2) |
| DOC6      | 2   | 11  | 2.8723e-3 (2.32e-4) – | 3.2332e-3 (5.80e-4) – | 2.6524e-3 (1.37e-4) ≈ | 2.6411e-3 (1.37e-4) |
| DOC7      | 2   | 11  | 2.2819e-3 (1.00e-4) ≈ | 1.1597e-2 (5.05e-2) – | 2.2458e-3 (1.27e-4) ≈ | 2.2736e-3 (1.12e-4) |
| DOC8      | 3   | 10  | 5.8969e-2 (2.21e-3) ≈ | 6.3490e-2 (3.20e-3) – | 5.9405e-2 (3.04e-3) ≈ | 5.8864e-2 (2.53e-3) |
| DOC9      | 3   | 11  | 7.2490e-2 (9.08e-3) ≈ | 7.9326e-2 (1.21e-2) – | 6.9112e-2 (9.58e-3) ≈ | 7.1673e-2 (9.23e-3) |
| LIRCMOP1  | 2   | 30  | 4.2300e-2 (2.21e-2) + | 7.8463e-2 (5.09e-2) ≈ | 8.6139e-2 (6.40e-2) ≈ | 8.8916e-2 (5.98e-2) |
| LIRCMOP2  | 2   | 30  | 2.2462e-2 (1.39e-2) ≈ | 4.5704e-2 (3.52e-2) ≈ | 7.2274e-2 (5.97e-2) ≈ | 4.4883e-2 (4.84e-2) |
| LIRCMOP3  | 2   | 30  | 9.2622e-2 (5.61e-2) ≈ | 8.2305e-2 (5.52e-2) ≈ | 9.2043e-2 (5.39e-2) ≈ | 8.9156e-2 (6.67e-2) |
| LIRCMOP4  | 2   | 30  | 1.1647e-1 (8.01e-2) ≈ | 1.1012e-1 (5.24e-2) ≈ | 9.3681e-2 (5.83e-2) ≈ | 9.7371e-2 (6.35e-2) |
| LIRCMOP5  | 2   | 30  | 1.0416e-2 (7.57e-3) – | 7.3403e-3 (5.85e-4) – | 6.8721e-3 (7.57e-4) ≈ | 6.8219e-3 (3.84e-4) |
| LIRCMOP6  | 2   | 30  | 3.0549e-2 (9.16e-2) ≈ | 6.7984e-3 (4.16e-4) – | 6.5489e-3 (4.63e-4) – | 6.3725e-3 (3.74e-4) |
| LIRCMOP7  | 2   | 30  | 7.4043e-3 (6.18e-4) – | 7.2953e-3 (4.43e-4) ≈ | 7.2112e-3 (3.91e-4) ≈ | 7.1702e-3 (1.85e-4) |
| LIRCMOP8  | 2   | 30  | 7.2798e-3 (2.41e-4) ≈ | 7.1962e-3 (2.00e-4) ≈ | 7.3239e-3 (2.71e-4) ≈ | 7.2100e-3 (2.23e-4) |
| LIRCMOP9  | 2   | 30  | 2.4233e-1 (9.44e-2) – | 7.4890e-3 (2.93e-3) – | 6.1834e-3 (1.37e-3) ≈ | 5.9192e-3 (1.85e-3) |
| LIRCMOP10 | 2   | 30  | 1.0443e-1 (1.17e-1) – | 6.7643e-3 (4.45e-4) – | 6.0783e-3 (2.62e-4) ≈ | 6.1305e-3 (2.98e-4) |
| LIRCMOP11 | 2   | 30  | 1.1509e-1 (7.53e-2) – | 2.7453e-3 (1.13e-4) – | 2.7116e-3 (1.22e-4) ≈ | 2.6624e-3 (1.01e-4) |
| LIRCMOP12 | 2   | 30  | 1.2916e-1 (7.04e-2) – | 4.0361e-3 (6.49e-4) – | 3.7872e-3 (4.33e-4) ≈ | 3.7508e-3 (4.13e-4) |
| LIRCMOP13 | 3   | 30  | 1.7781e-1 (2.41e-1) ≈ | 1.1858e-1 (2.38e-3) ≈ | 1.1780e-1 (2.40e-3) ≈ | 1.1818e-1 (2.21e-3) |
| LIRCMOP14 | 3   | 30  | 1.0250e-1 (1.41e-3) ≈ | 1.0321e-1 (1.48e-3) ≈ | 1.0319e-1 (1.58e-3) ≈ | 1.0304e-1 (1.15e-3) |
|           |     |     | + / - / ≈             | 1/9/22                | 0/20/12               | 1/2/29              |

TABLE III

MEAN AND STANDARD DEVIATION OF RUNTIME OF MCCMO VARIANTS '+', '-', AND '≈' INDICATE THAT THE RESULT IS SIGNIFICANTLY BETTER, SIGNIFICANTLY WORSE, AND STATISTICALLY SIMILAR TO THAT OBTAINED BY MCCMO, RESPECTIVELY.

| Problem   | M | D  | MCCMO1                | MCCMO2                | MCCMO3                | MCCMO               |
|-----------|---|----|-----------------------|-----------------------|-----------------------|---------------------|
| DASCMP1   | 2 | 30 | 5.3892e+1 (2.42e+1) + | 1.5167e+2 (2.69e+1) - | 7.8661e+1 (2.65e+1) + | 9.1918e+1 (2.93e+1) |
| DASCMP2   | 2 | 30 | 5.2224e+1 (2.31e+1) + | 1.6153e+2 (2.14e+1) - | 7.7244e+1 (2.26e+1) ≈ | 8.6311e+1 (3.36e+1) |
| DASCMP3   | 2 | 30 | 1.2382e+2 (3.84e+1) + | 2.3784e+2 (6.73e+1) - | 1.2853e+2 (3.75e+1) + | 1.6804e+2 (7.14e+1) |
| DASCMP4   | 2 | 30 | 1.1540e+2 (6.36e+1) + | 2.5901e+2 (9.25e+1) - | 1.7399e+2 (1.42e+2) ≈ | 1.5812e+2 (7.79e+1) |
| DASCMP5   | 2 | 30 | 1.1488e+2 (6.28e+1) ≈ | 2.8178e+2 (1.31e+2) - | 1.9627e+2 (1.50e+2) ≈ | 1.2500e+2 (5.88e+1) |
| DASCMP6   | 2 | 30 | 2.0209e+2 (7.40e+1) + | 4.0542e+2 (1.33e+2) - | 2.5174e+2 (1.43e+2) ≈ | 2.4825e+2 (9.13e+1) |
| DASCMP7   | 3 | 30 | 4.4078e+1 (1.23e+1) + | 1.0086e+2 (2.10e+1) - | 6.6448e+1 (1.34e+1) + | 7.5134e+1 (1.52e+1) |
| DASCMP8   | 3 | 30 | 4.5867e+1 (1.07e+1) + | 1.0004e+2 (1.60e+1) - | 7.0146e+1 (1.68e+1) ≈ | 7.2605e+1 (9.76e+0) |
| DASCMP9   | 3 | 30 | 2.8102e+1 (1.84e+0) + | 6.3488e+1 (7.15e+0) - | 5.1953e+1 (3.06e+0) ≈ | 5.1848e+1 (1.72e+0) |
| DOC1      | 2 | 6  | 3.9718e+1 (2.61e+0) + | 6.0093e+1 (3.60e+0) + | 5.0558e+1 (2.72e+0) + | 6.6185e+1 (3.75e+0) |
| DOC2      | 2 | 16 | 4.9297e+1 (4.53e+0) + | 8.2070e+1 (5.05e+0) - | 6.4802e+1 (7.33e+0) + | 7.6189e+1 (5.11e+0) |
| DOC3      | 2 | 10 | 1.1137e+2 (2.39e+1) + | 1.3850e+2 (4.13e+1) ≈ | 1.2122e+2 (2.89e+1) ≈ | 1.2856e+2 (2.69e+1) |
| DOC4      | 2 | 8  | 4.7259e+1 (2.57e+0) + | 6.1694e+1 (1.43e+0) - | 5.1139e+1 (1.63e+0) + | 5.7523e+1 (2.16e+0) |
| DOC5      | 2 | 8  | 3.9203e+1 (8.27e+0) + | 5.2305e+1 (6.90e+0) ≈ | 4.2300e+1 (3.18e+0) + | 5.1632e+1 (7.78e+0) |
| DOC6      | 2 | 11 | 7.8429e+1 (8.69e+0) - | 7.5839e+1 (3.79e+0) - | 6.3292e+1 (2.65e+0) ≈ | 6.3804e+1 (4.19e+0) |
| DOC7      | 2 | 11 | 4.0023e+1 (4.18e+0) + | 5.8790e+1 (4.95e+0) - | 4.8143e+1 (2.61e+0) + | 5.1742e+1 (4.55e+0) |
| DOC8      | 3 | 10 | 5.2519e+1 (1.01e+1) + | 8.0987e+1 (1.41e+1) - | 6.0613e+1 (4.23e+0) + | 6.6044e+1 (9.42e+0) |
| DOC9      | 3 | 11 | 7.8637e+1 (2.43e+1) ≈ | 1.7066e+2 (4.30e+1) - | 6.8814e+1 (1.44e+1) + | 8.7616e+1 (2.64e+1) |
| LIRCMOP1  | 2 | 30 | 2.7359e+1 (2.93e+0) + | 4.6455e+1 (1.16e+0) + | 4.4542e+1 (1.14e+0) + | 4.7617e+1 (1.38e+0) |
| LIRCMOP2  | 2 | 30 | 2.8063e+1 (4.08e+0) + | 4.7144e+1 (1.09e+0) + | 4.5922e+1 (1.01e+0) + | 5.1714e+1 (5.81e+0) |
| LIRCMOP3  | 2 | 30 | 3.2225e+1 (3.03e+0) + | 5.3635e+1 (3.44e+0) ≈ | 4.6400e+1 (1.14e+0) + | 5.3968e+1 (4.54e+0) |
| LIRCMOP4  | 2 | 30 | 3.3285e+1 (2.87e+0) + | 5.5956e+1 (3.26e+0) ≈ | 4.7395e+1 (1.14e+0) + | 5.5212e+1 (3.31e+0) |
| LIRCMOP5  | 2 | 30 | 4.5504e+1 (4.76e+0) + | 7.5566e+1 (3.81e+0) - | 6.2673e+1 (3.04e+0) + | 7.1950e+1 (3.97e+0) |
| LIRCMOP6  | 2 | 30 | 3.9385e+1 (3.13e+0) + | 7.2844e+1 (3.37e+0) - | 5.9857e+1 (3.12e+0) + | 6.9633e+1 (4.78e+0) |
| LIRCMOP7  | 2 | 30 | 3.8882e+1 (5.17e+0) + | 7.3097e+1 (1.24e+1) ≈ | 5.7681e+1 (7.06e+0) + | 6.8124e+1 (7.74e+0) |
| LIRCMOP8  | 2 | 30 | 3.8750e+1 (4.46e+0) + | 7.0470e+1 (6.52e+0) - | 6.5739e+1 (4.81e+0) - | 6.2715e+1 (7.48e+0) |
| LIRCMOP9  | 2 | 30 | 5.1843e+1 (3.20e+0) + | 8.8042e+1 (4.73e+0) ≈ | 6.6811e+1 (3.46e+0) + | 8.5448e+1 (7.05e+0) |
| LIRCMOP10 | 2 | 30 | 5.4052e+1 (3.67e+0) + | 9.6843e+1 (6.53e+0) - | 8.0292e+1 (4.50e+0) + | 9.1888e+1 (8.20e+0) |
| LIRCMOP11 | 2 | 30 | 4.2997e+1 (4.49e+0) + | 7.7221e+1 (3.17e+0) - | 5.9662e+1 (2.66e+0) + | 7.0142e+1 (4.54e+0) |
| LIRCMOP12 | 2 | 30 | 3.1377e+1 (3.94e+0) + | 6.8117e+1 (3.67e+0) - | 5.1351e+1 (3.02e+0) + | 6.0423e+1 (5.97e+0) |
| LIRCMOP13 | 3 | 30 | 5.9844e+1 (1.45e+1) + | 1.6809e+2 (3.64e+1) ≈ | 1.2799e+2 (2.28e+0) + | 1.5202e+2 (1.72e+1) |
| LIRCMOP14 | 3 | 30 | 6.1336e+1 (1.54e+1) + | 1.7471e+2 (4.02e+1) - | 1.2253e+2 (2.26e+0) + | 1.5538e+2 (2.34e+1) |
| + / - / ≈ |   |    | 29/1/2                | 3/2/7                 | 23/1/8                |                     |

TABLE IV

MEAN AND STANDARD DEVIATION OF FEASIBLE RATE OF MCCMO VARIANTS '+', '-', AND '≈' INDICATE THAT THE RESULT IS SIGNIFICANTLY BETTER, SIGNIFICANTLY WORSE, AND STATISTICALLY SIMILAR TO THAT OBTAINED BY MCCMO, RESPECTIVELY.

| Problem   | M | D  | CCMO                  | CMOEA_MS              | EMCCMO                | MSCMO                 | cDPEA                 | MCCMO               |
|-----------|---|----|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|---------------------|
| RWMOP29   | 2 | 7  | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) ≈ | 5.0000e-1 (5.09e-1) - | 1.0000e+0 (0.00e+0) ≈ | 1.0000e+0 (0.00e+0) |
| RWMOP31   | 2 | 25 | 1.3333e-1 (3.46e-1) ≈ | 1.0000e-1 (3.05e-1) ≈ | 1.6667e-1 (3.79e-1) ≈ | 0.0000e+0 (0.00e+0) - | 2.0000e-1 (4.07e-1) ≈ | 1.6667e-1 (3.79e-1) |
| RWMOP35   | 2 | 30 | 4.0000e-1 (4.98e-1) ≈ | 0.0000e+0 (0.00e+0) - | 4.0000e-1 (4.98e-1) ≈ | 0.0000e+0 (0.00e+0) - | 1.0000e-1 (3.05e-1) - | 3.3333e-1 (4.79e-1) |
| + / - / ≈ |   |    | 0/0/3                 | 0/1/2                 | 0/0/3                 | 0/3/0                 | 0/1/2                 |                     |