OzDES Reverberation Mapping Program: $H\beta$ lags from the 6-yr survey

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ABSTRACT

Reverberation mapping measurements have been used to constrain the relationship between the size of the broad-line region and luminosity of active galactic nuclei (AGN). This *R*–*L* relation is used to estimate single-epoch virial black hole masses, and has been proposed to use to standardize AGN to determine cosmological distances. We present reverberation measurements made with H β from the 6-yr Australian Dark Energy Survey (OzDES) Reverberation Mapping Program. We successfully recover reverberation lags for eight AGN at 0.12 < z < 0.71, probing higher redshifts than the bulk of H β measurements made to date. Our fit to the *R*–*L* relation has a slope of $\alpha = 0.41 \pm 0.03$ and an intrinsic scatter of $\sigma = 0.23 \pm 0.02$ dex. The results from our multi-object spectroscopic survey are consistent with previous measurements made by dedicated source-by-source campaigns, and with the observed dependence on accretion rate. Future surveys, including LSST, TiDES, and SDSS-V, which will be revisiting some of our observed fields, will be able to build on the results of our first-generation multi-object reverberation mapping survey.

Key words: galaxies: active - galaxies: nuclei - quasars: emission lines - quasars: general - quasars: supermassive black holes.

1 INTRODUCTION

Reverberation mapping (RM) has been established as the leading technique for direct determination of black hole masses (M_{BH}) in active galactic nuclei (AGN) outside the local universe. Reverberation measurements anchor the scaling relations used to estimate single-epoch virial black hole (BH) masses (Vestergaard 2002; Vestergaard & Peterson 2006). Over the past decade, RM programs conducted by the Australian Dark Energy Survey (OzDES) and Sloan Digital Sky Survey (SDSS) have leveraged high-multiplexed spectroscopy to perform RM on an 'industrial' scale, aiming to increase the number of measurements available by an order of magnitude (King et al. 2015; Shen et al. 2015). These programs have resulted in over one hundred new lag measurements, while also identifying and addressing the complexities of performing RM on such large scales.

As reverberation mapping resolves the innermost regions of AGN in the time-domain, rather than spatially, it allows the study of these regions out to high redshifts. RM utilizes the difference in the light travel time between the variation of the continuum emission from the accretion disc around the central supermassive black hole (SMBH) and the reprocessed emission from the photoionized broadline region (BLR; Blandford & McKee 1982; Peterson 1993). The time-delay, τ , can be measured using multi-epoch photometry and spectroscopy to probe the continuum and BLR response, respectively, in order to infer the radius of the BLR ($R_{BLR} = c\tau$). Together with the BLR velocity dispersion, ΔV^2 , inferred from the width of the emission line, this can be used to estimate the mass of the SMBH using the virial product:

$$M_{\rm BH} = f \frac{R_{\rm BLR} \Delta V^2}{G}.$$
 (1)

The geometry, orientation, and kinematics of the BLR are encapsulated by the dimensionless scale factor f, which is calibrated using

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sources with independent measurements from RM and the $M_{\rm BH}-\sigma_*$ relation (Ferrarese & Merritt 2000; Gebhardt et al. 2000; Onken et al. 2004; Woo et al. 2015).

Due to the intensity of observational resources required, early programs targeted a small number of local AGN with campaign durations of less than 1 yr. To achieve the fidelity required for RM, they observed bright, highly varying AGN. As a result, the targeted samples are typically biased towards AGN in the local universe (z< 0.3). Lag measurements were made for 63 AGN with the H β line (e.g. Peterson et al. 1998; Kaspi et al. 2000; Peterson & Horne 2004; Bentz et al. 2009). These measurements were used to constrain the relationship between the AGN luminosity and the radius of the BLR (*R*–*L* relation), which exhibited relatively low intrinsic scatter, with a slope consistent with that expected by photoionization physics (Bentz et al. 2009, 2013). This relation calibrates secondary massscaling relations used to estimate single-epoch virial BH masses for samples of thousands of AGN (e.g. SDSS DR7 quasar catalogue, Shen et al. 2011). The R-L relation has also been proposed as a way to standardize AGN for use as luminosity distance indicators for cosmology (Watson et al. 2011; Martínez-Aldama et al. 2019; Khadka et al. 2022).

These BH mass estimates have a significant ~ 0.5 dex uncertainty due to our limited understanding of BLR geometry and kinematics, and the small sample of reverberation measurements among other factors (Shen 2013). The former issue is addressed by conducting observationally intensive velocity-resolved RM (e.g. Bentz et al. 2010; Grier et al. 2013; Pancoast et al. 2014b; Du et al. 2018; U et al. 2022), and using dynamical modelling methods (e.g. CARAMEL, Pancoast, Brewer & Treu 2014a), as well as spectroastrometry of the BLR in local AGN (e.g. GRAVITY, Gravity Collaboration et al. 2018). Other programs are targeting a more diverse range of sources. The super-Eddington accreting massive black holes (SEAMBH) program has observed over 40 luminous AGN (Du et al. 2014; Wang et al. 2014; Du et al. 2015, 2016, 2018; Hu et al. 2021). The updated *R*–*L* relation using these H β measurements has increased intrinsic scatter, and an observed dependence on accretion rate. However, these programs are still only targeting AGN at z < 0.4.

The SDSS-RM Project and our OzDES-RM program have pioneered RM on an 'industrial-scale', observing hundreds of AGN probing a wide range of AGN luminosities and redshifts. These programs have added over 100 new lag measurements, and have enabled the Mg II and C IV R-L relations to be constrained with statistically significant samples (Grier et al. 2017; Grier et al. 2019; Hoormann et al. 2019; Homayouni et al. 2020; Yu et al. 2021, 2022, Penton et al. in prep). The first generation of multi-object RM surveys have however highlighted problems with monitoring hundreds of targets. This includes challenges both with data quality (signal to noise, limited temporal coverage; Malik et al. 2022) as well as with reverberation lag recovery techniques and biases such as aliasing (Li et al. 2019; Penton et al. 2022).

OzDES focused mainly on high-redshift AGN; however, about 10 per cent of the sample contains H β emission within the spectroscopic window. This will allow comparison of our OzDES measurements with the large sample of existing H β measurements, in order to examine the consistency of multi-object RM with earlier dedicated source-by-source observations. We present the H β lag results from our 6-yr survey. Section 2 details the observations obtained by OzDES and the data calibration procedures. In Section 3, we describe the techniques we used for lag recovery and the selection criteria we apply to define our final sample. In Section 4, we present our successful lag measurements and black hole masses, as well as an updated *R*–*L* relationship, and discuss these results in Section 5.



Figure 1. Distribution of redshifts and monochromatic luminosities at 5100 Å for the 735 AGN in the OzDES RM sample. The H β sample extends to z = 0.75, with 15 sources overlapping with our Mg II sample.

We summarize our results and then present an outlook for the future work in Section 6. Throughout this work we adopt a flat Λ CDM cosmology with $\Omega_{\Lambda} = 0.7$, $\Omega_{M} = 0.3$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2 DATA

The Australian Dark Energy Survey (OzDES) provided follow-up spectroscopic observations of the 10 supernova fields observed by the DES. The DES supernova fields are located in the ELAIS, XMM-Large-Scale Structure, Chandra deep-field South, and SDSS Stripe 82 regions (Kessler et al. 2015; Morganson et al. 2018). These fields were observed in the griz filters with the Dark Energy Camera (DECam) on the 4-m Blanco telescope at Cerro Tololo Inter-American Observatory (CTIO) (Flaugher et al. 2015). From 2013 to early 2018, the fields were observed with $\sim 6 d$ cadence over a 5-6 month season (August to January), with additional science verification data taken in late 2012 to early 2013, and additional data taken on a monthly cadence in late 2018. OzDES conducted followup multi-object spectroscopic observations with the 2dF multi-object fibre positioning system and the AAOmega spectrograph (3700-8800 Å, Sharp et al. 2006) on the 3.9-m Anglo-Australian Telescope (AAT; Yuan et al. 2015; Childress et al. 2017; Lidman et al. 2020). The OzDES observations were made over the same 5-6 month season with approximately monthly cadence from 2013 to 2019.

2.1 Target sample

After completing the final data reduction for our survey, the OzDES RM Program sample comprises 735 AGN (reduced from an initial sample of 771 due to a change in the location of the DECam interchip gaps between survey definition and campaign observations), with redshifts ranging up to $z \sim 4$, and with apparent magnitudes $17.2 < r_{AB} < 22.3$ mag. The redshift and luminosity distribution of these AGN is shown in Fig. 1.

Of these 735 AGN, the H β line and nearby continuum falls within the AAOmega spectral range for 78 sources. The expected observer-frame lags for the H β sample (governed by luminosity and time-dilation) range from ~20 d to just over 200 d. In previous analyses, our emission-line flux measurements were made using spectra that were co-added by observing run (Hoormann et al. 2019) (typically 4–7 d during dark time each month). However, some fields were observed over multiple nights within a single observing run. To maximize the cadence of our sampling we treated the spectra



Figure 2. The redshift and luminosity distribution for the OzDES H β sample (open diamonds), final sample (filled diamonds, see Section 4), and existing measurements from Bentz et al. (2013, and references therein); SDSS-RM (Grier et al. 2017, quality 4 and 5); SEAMBH (Du et al. 2014; Wang et al. 2014; Du et al. 2015, 2016, 2018; Hu et al. 2021); Lick AGN Monitoring Project (LAMP, U et al. 2022); and other measurements from Bentz et al. (2009), Barth et al. (2013), Bentz et al. (2014), Pei et al. (2014), Lu et al. (2016), Bentz et al. (2016a), Bentz et al. (2016b), Fausnaugh et al. (2017), Zhang et al. (2019), Rakshit et al. (2019), Li et al. (2021), of which measurements published before 2019 are compiled by Martínez-Aldama et al. (2019).

obtained on different nights as separate epochs for our emission-line light curves. This is particularly valuable for rapidly reverberating sources. The redshift and luminosity range of our H β sample, and H β measurements from the literature are shown in Fig. 2.

We do not measure the continuum luminosity directly from the spectra due to fibre aperture effects from variable atmospheric seeing and fibre placement uncertainties. From the average *r*-band magnitude and redshift of the AGN, we estimated the monochromatic continuum flux at 5100 Å using the DECam *r*-band filter transmission curve and the SDSS quasar template (Vanden Berk et al. 2001). The template is scaled to the magnitude of the source, assuming $L_{bol} = 9 \lambda L_{\lambda}$ (5100 Å) (Kaspi et al. 2000).

2.2 Flux calibration and measurements

The DES photometry is calibrated consistently through to Y6 using the DES data reduction pipeline (Burke et al. 2018; Morganson et al. 2018). We perform a spectrophotometric flux calibration and line flux measurement following Hoormann et al. (2019). The local continuum windows for continuum subtraction are 4760 to 4790 Å and 5100 to 5130 Å. The calibration uncertainties of the line flux were measured using the F-star warping function method as detailed in Yu et al. (2021).

3 LAG RECOVERY AND RELIABILITY

3.1 Time series analysis

To measure the reverberation lags for our sample we use the interpolated cross-correlation function (ICCF; Gaskell & Peterson 1987) and JAVELIN (Zu, Kochanek & Peterson 2011; Zu et al. 2013) methodologies. The JAVELIN method models the AGN continuum variability using a damped random walk (DRW; Kelly, Bechtold & Siemiginowska 2009; Kozłowski et al. 2010; MacLeod



Figure 3. *p*-value versus r_{max} for our 78 AGN. The r_{max} is of the original pair of light curves. The shaded region indicates our selection criteria requiring a *p*-value <0.05 and $r_{\text{max}} > 0.6$.

et al. 2010). It assumes the emission-line light curve is a scaled, smoothed, and shifted version of the continuum light curve that can be described by the convolution of the continuum with a top-hat transfer function. Using Markov Chain Monte Carlo (MCMC), it constrains the characteristic variability amplitude and damping time-scale of the continuum light curve. Applying this DRW fit as a prior, it simultaneously fits both the continuum and emission-line light curves, to derive the posterior distributions of the transfer function parameters: lag, top-hat width, and scale factor, as well as an updated DRW amplitude and time-scale. We allow these parameters to vary freely, while setting a lag prior of $[-3\tau_{exp}, 3\tau_{exp}]$, where τ_{exp} is the expected H β lag for the source using the Bentz et al. (2013) *R*–*L* relation.

We use the PYCCF code to perform the ICCF method (Sun, Grier & Peterson 2018). This linearly interpolates the continuum and emission-line light curves over a user defined grid spacing, and cross-correlates the interpolated light curves as a function of time-lag. The centroid of the cross-correlation function (CCF) is computed as the median of the CCF values >0.8 r_{max} counted out from the peak of the CCF, r_{max} . A cross-correlation centroid distribution (CCCD) is obtained from 10 000 Monte Carlo realizations of the flux randomization and random subset sampling (FR/RSS) process (Peterson et al. 1998), which accounts for the flux measurement uncertainties and potentially spurious correlations between light-curve points. Following Hoormann et al. (2019), we set the interpolation grid spacing to 3 d, and the r_{max} threshold to 0.5. We use the same lag prior as for JAVELIN from $[-3\tau_{exp}, 3\tau_{exp}]$.

The recovered lag, τ , with lower and upper uncertainties, σ_{τ} , are taken to be median and 16th and 84th percentiles of the lag probability distribution functions (PDF) from JAVELIN and PYCCF.

3.2 Null hypothesis test

Our survey window function for the (expected) short H β lags is less than ideal and the signal to noise of the spectroscopy is only modest. We wish to test the null hypothesis that our lag recovery



Figure 4. For each source, the upper-left-hand panel shows the DECam *g*-band continuum light curve, and lower-left-hand panel the H β emission-line light curve, with the continuum light curve phase-shifted by the JAVELIN lag. The fluxes have been re-scaled. The upper-right-hand panel shows the cross-correlation function computed using PYCCF. The lower-right-hand panel shows the cross-correlation centroid distribution (CCCD) from PYCCF in blue, and the lag posterior from JAVELIN in orange, with the vertical solid and dashed lines indicating the recovered lag and upper and lower uncertainties from each method.

is not simply a product of the interaction of the window function with underlying red-noise correlation in the photometric light curves (an underlying assumption of any RM technique). Therefore, we do not report extensive light-curve simulations of the H β sample (as per U et al. 2022), as this would simply reuse the same window function properties with the added uncertainty of the appropriateness of the variability model for our sources. Instead we randomized the spectroscopic light curves (with flux values shuffled while retaining the dates of observation), and cross correlated this with the original photometric light curve. We find the r_{max} value of the cross-correlation coefficient *r* at the peak of the CCF, and compare it to that found from the CCF of the original light curves. After 1000 iterations, the *p*-value was calculated as the fraction of r_{max} values which exceeded the original r_{max} .

By randomizing the emission-line light curves, we generate uncorrelated light curves that do not posses a reverberation signature. We chose to randomize the observed spectroscopic light curve, rather than using simulated light-curve realizations, as done by U et al. (2022). Simulated light-curve realizations have the same variability time-scale and underlying lag as the source, and therefore may result in significant spurious correlations at random lag values.

Fig. 3 shows the results of this test applied to each of the H β sources. We see that below a r_{max} of 0.6, there are always a significant number of uncorrelated signals which exceed this r_{max} , resulting in high *p*-values. Therefore, we can not trust a result which has a r_{max} below 0.6.

3.3 Selection criteria

Based on the results of simulations from Li et al. (2019), Yu et al. (2020), and Penton et al. (2022), we adopt the lag and uncertainties from JAVELIN as the final lag. We define a successful lag recovery as meeting the following criteria:

(i) The upper and lower lag uncertainties $\sigma_{\tau, \text{ JAV}}$ are less than $|\tau_{\text{JAV}}|$, or 30 d, whichever is greater

- (ii) τ_{PyCCF} lies within the $2\sigma_{\tau, JAV}$ uncertainties
- (iii) *p*-value <0.05 and $r_{\text{max}} > 0.6$

As the expected lags of our sources range from ~ 20 to 200 d, we use a relative rather than absolute cut on the lag uncertainties. We require the lags recovered from JAVELIN and PYCCF to agree in an attempt to exclude cases where PDF's are flat or have significant aliasing peaks. Our *p*-test and r_{max} criteria ensure there is significant correlation between the light curves that is unlikely to be spurious.

4 RESULTS

We successfully measure lags for five H β sources with the criteria listed in Section 3.3. The recovered lags are given in Table 1. We present the light curves and the lag distributions for each of the five sources in Figs 4 and 5. The re-scaled and phase-shifted light curves for each of the sources display visually discernible reverberation. For each source, there is overlap between the phase-shifted light curves. In most cases, the lag PDF's from PYCCF and JAVELIN agree, although there is significant scatter in the PYCCF CCCD's for some sources. However, even for these cases, the JAVELIN lag is well defined, which is consistent with the finding that JAVELIN is better able to recover short lags than PYCCF (Li et al. 2019).

4.1 Additional sources

After visually inspecting the lag recoveries from our full H β sample, we identified eight sources with lag PDF's of comparable quality to the sample that passed our selection criteria, but with JAVELIN aliasing peaks. This signal is produced as an artefact of the survey window function; predominantly the seasonal gaps. These aliasing peaks do not coincide with a peak in the PYCCF CCCD or CCF, and always occur at negative lags coincident with the seasonal gaps in the observational campaign (~ -150 to -250 d). We show the light curves and lag PDF's of these sources in Figs 6, A1, and A2. For most sources, there is good agreement in the light curves phaseshifted by the positive recovered lag. For three of the eight sources (Fig. 6), there is a overlap between the photometric and spectroscopic observations, while the light curves for the other five (Figs A1 and A2) shift such that the spectroscopic observations fall wholly within gaps in the photometric observations. For comparison, we phaseshifted the continuum light curve by the lag at which the negative JAVELIN peak occurs. We show the light curves phase-shifted by both the positive lag and the negative lag in Figs A3 and A4. In some cases, the light curves show smooth multiyear variations, for which the negatively phase-shifted light curves do seem to reasonably interpolate between the seasonal gaps; however, there is no coincident peak in the PYCCF CCCD.

If we omit the negative peaks in the JAVELIN PDF's, five of the eight sources pass our selection criteria, and therefore illustrate comparable quality to the sample recovered originally. Given there is no physical motivation for a negative reverberation lag, and the negative aliasing peaks seem to be an artefact of the JAVELIN method alone, we choose to include the three sources that demonstrate overlap between their light curves when shifted by the positive lag in our final sample. We provide the lags for these three sources in Table 1. At this stage, we choose not to include the other two sources, DES J024533.65-000744.91 and DES J004009.06-431255.29, which have positive lags that cause the phase-shifted light curves to land completely within the seasonal gaps. The three sources that do not pass all our selection criteria only fail the r_{max} criterion, although we note that their r_{max} are above 0.5. The phase-shifted light curves for these three sources also fall within the seasonal gaps. High cadence monitoring to resolve shorter term variations, and observing over longer seasons will be required to reliably recover these lags.

Fig. 2 shows the redshift and luminosity distribution of our final recovered sample of eight AGN, compared with existing measurements. Our sample probes higher redshifts, and spans 1 dex in luminosity.

4.2 Black hole masses and the *R*-*L* relation

We measured the H β line-width using the line dispersion of the mean spectra. Although H β line-width measurements are commonly made using the root mean squared (rms) spectra, the signal to noise of our spectra are insufficient to support this approach. We measure $M_{\rm BH}$ for our final sample of eight AGN using equation (1) and a virial factor f = 4.47 (Woo et al. 2015), and give these in Table 1, along with the line dispersion measurements.

We constrain the R-L relation as shown in Fig. 7. Our best fit to the existing data and our final sample is

$$\log(R_{\rm BLR}/{\rm lt} - {\rm day}) = K + \alpha \log(\lambda L_{\lambda})/10^{44} [{\rm erg \, s^{-1}}]$$
⁽²⁾

with slope $\alpha = 0.41 \pm 0.03$, $K = 1.33 \pm 0.02$, and an intrinsic scatter of $\sigma = 0.23 \pm 0.02$ dex.

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Table 1. Results for our final sample of eight AGN. Columns left to right: DES name (J2000), redshift, observer-frame JAVELIN lag, observer-frame PYCCF lag, *p*-value, monochromatic luminosity at 5100Å, line dispersion measured from mean spectrum, virial black hole mass, and dimensionless accretion rate.

Source	Z	$\tau_{\rm JAV}$ (d)	τ_{PyCCF} (d)	<i>p</i> -value	$\frac{\log{(\lambda L_{5100})}}{(\mathrm{erg}\mathrm{s}^{-1})}$	$\sigma_{\rm mean}$ (km s ⁻¹)	$M_{ m BH}$ (× 10 ⁷ M _☉)	Ŵ
DES J002802.42-424913.52	0.127	18^{+3}_{-3}	16^{+10}_{-18}	0.000	43.67	1393 ± 3	$2.64^{+0.85}_{-0.87}$	1.43
DES J024347.34-005354.84	0.237	34^{+1}_{-2}	32^{+19}_{-13}	0.000	43.74	$1658~\pm~6$	$6.62^{+1.87}_{-1.89}$	0.28
DES J022330.16-054758.06	0.354	22^{+27}_{-20}	21^{+34}_{-47}	0.002	43.85	$1846~\pm~11$	$4.86_{-4.62}^{+6.12}$	0.79
DES J002904.43-425243.04	0.644	98^{+27}_{-57}	87^{+31}_{-177}	0.002	44.61	$1851~\pm~4$	$17.8^{+7.0}_{-11.4}$	0.80
DES J022617.85-043108.99	0.707	67^{+49}_{-18}	33_{-80}^{+73}	0.006	44.70	1691 ± 8	$9.78^{+7.60}_{-3.76}$	3.63
DES J034028.46-292902.41	0.310	51^{+9}_{-6}	54^{+24}_{-22}	0.002	44.43	$1732~\pm~5$	$10.3^{+3.3}_{-3.1}$	1.30
DES J022249.67-051453.01	0.314	25^{+7}_{-5}	29^{+45}_{-55}	0.005	44.07	$1883~\pm~5$	$5.99^{+2.28}_{-2.00}$	1.08
DES J003954.13-440509.97	0.332	48^{+12}_{-7}	56^{+17}_{-37}	0.001	43.92	1856 ± 11	$10.9^{+4.1}_{-3.4}$	0.20



The SEAMBH program targeted highly accreting AGN at z < 0.4 (Du et al. 2014; Wang et al. 2014; Du et al. 2015, 2016, 2018; Hu et al. 2021). SEAMBH found that highly accreting AGN have systematically shorter reverberation lags. They proposed that

accretion rate explains the observed deviation from the steeper R-L relation from the Bentz et al. (2013) compilation of earlier results. Following Du et al. (2018), we measure the dimensionless accretion rate of our sample using the estimator derived from the standard thin



Figure 6. Same as for Fig. 4, for sources with JAVELIN aliasing signals. The orange vertical dotted lines indicate the negative aliasing peak in the JAVELIN PDF, for which we show the phase-shifted light curves in Appendix A. These three sources are included in the final sample.

accretion disc model (Shakura & Sunyaev 1973):

$$\dot{M} = 20.1 \left(\frac{l_{44}}{\cos\left(i\right)}\right)^{3/2} m_7^{-2},\tag{3}$$

where $l_{44} = L_{5100}/10^{44}$ erg s⁻¹, $m_7 = M_{BH}/10^7$ M_☉, and the inclination angle of the disc to the line of sight is taken to be cos (*i*) = 0.75. All but one of our sources have low accretion rates, which is consistent



Figure 7. Radius–luminosity relation for H β using our final sample of eight new AGN together with existing measurements from Bentz et al. (2013, and references therein); SDSS-RM (Grier et al. 2017, quality 4 and 5); SEAMBH (Du et al. 2014; Wang et al. 2014; Du et al. 2015, 2016, 2018; Hu et al. 2021); Lick AGN Monitoring Project (LAMP, U et al. 2022); and other measurements from Bentz et al. (2009), Barth et al. (2013), Bentz et al. (2014), Pei et al. (2014), Lu et al. (2016), Bentz et al. (2016a), Bentz et al. (2016b), Fausnaugh et al. (2017), Zhang et al. (2019), Rakshit et al. (2019), Li et al. (2021), of which measurements published before 2019 are compiled by Martínez-Aldama et al. (2019). The slope of the relation is given in the legend, along with the slopes constrained previously by Bentz et al. (2013) and Du et al. (2018). All sources in the OzDES sample have low accretion rates, apart from our highest luminosity measurement (right-most black point), which has a moderately high accretion rate (Table 1).

with the observed agreement between our results and the Bentz et al. (2013) relation, which was constrained using mainly lowaccretion sources. One of our sources is on the lower boundary of what SEAMBH define to be highly accreting, and is consistent with both the low-accretion and high-accretion samples.

5 DISCUSSION

The primary goal of the OzDES RM program was to make RM measurements at high redshifts, with the Mg II and C IV lines. Our monthly cadence was sufficient for this, due to the intrinsically longer reverberation lags for these high ionization lines, and the increased time dilation for such sources that are typically at higher redshifts than our H β sample. Simulations showed the OzDES observational cadence was likely insufficient to provide a full sample of H β RM measurements (King et al. 2015; Malik et al. 2022). Since our survey is not as sensitive to these shorter lags, some of our selection criteria are not as strict as other analyses. Some of the uncertainties on the lags we have recovered are considerably larger than previous works, as we lack the temporal resolution to recover lags precisely.

Our new measurements are more consistent with the Bentz et al. (2013) slope than the SDSS-RM H β sample (Grier et al. 2017),

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although our sample has a similar redshift-luminosity distribution to SDSS-RM. As discussed by Grier et al. (2017), the SDSS-RM lags may underestimate $M_{\rm BH}$ due to selection effects from having only a single campaign season of observation, which limits the lag search window to 100 d. Our OzDES analysis is based on a 7 yr of photometry and 6 yr of spectroscopy but with lower observational cadence. However, simulations by Fonseca Alvarez et al. (2020) suggest this deviation is not due to observational biases. They attribute the deviation of their sample to changes in the UV/optical spectral energy distribution (SED), although this was not measured directly. The only significant difference between the OzDES and SDSS-RM samples and lag analyses is the baseline and cadence of the light-curve data.

Simulations presented by Malik et al. (2022) modelled survey window functions for OzDES and upcoming surveys, and investigated lag recovery efficacy with degraded or increased sampling. They find that with low sampling the scatter in the recovered R–L relation is increased, however there is no systematic offset from the input slope (see Fig. 13 in Malik et al. 2022). For sources with shorter expected lags and with a less-than-ideal cadence, they did not systematically recover longer lags. In the case that these idealized simulations are not representative of the data, it is possible that

with our cadence we may not be as sensitive to shorter lags if they were present. Upcoming surveys, including the Time-Domain Extragalactic Survey (TiDES; Swann et al. 2019) and SDSS-V Black Hole Mapper (Kollmeier et al. 2017), which will be spectroscopically following up the Legacy Survey of Space and Time (LSST) deepdrilling fields, will be revisiting most of the OzDES fields with shorter spectroscopic cadence. These programs can investigate any potential discrepancies with our results due to the longer cadence of OzDES.

6 SUMMARY

We successfully recover reverberation lags with H β for eight AGN from the 6-yr observations from DES and OzDES. These results from our multi-object survey are consistent with previous H β analyses done with source-by-source observations, including the early results compiled in Bentz et al. (2013). Our observations seem inconsistent with the large scatter observed in the SDSS-RM H β sample (Grier et al. 2017), although the only significant difference between our analyses is the baseline and cadence of the survey data. Our sample includes only one moderately high accretion rate source, and the location of our final sample on the R-L relation is consistent with earlier measurements with similar source accretion rates. This work compliments the higher redshift results for the rest of the OzDES RM sample of 735 AGN, made with the Mg II (Yu et al. 2021, 2022) and C IV lines (Hoormann et al. 2019; Penton et al. 2022, Penton et al. in prep), which will be used to recalibrate black hole mass-scaling relations for those emission lines.

The H β sample is highly sensitive to the observational window function. Additional campaign seasons seem to help, but higher cadence and observing over longer seasons is necessary to reliably recover these lags. Future surveys, including TiDES (Swann et al. 2019) and SDSS-V BHM (Kollmeier et al. 2017), which will be following up LSST, will observe some of the same fields as OzDES. These surveys can follow up with a more suitable window function (Malik et al. 2022). In order to anchor the ends of the H β *R*-*L* relation, future programs will need to target lower luminosity sources at $10^{41} < \lambda L_{\lambda} (5100 \text{ Å}) < 10^{43} \text{ ergs s}^{-1}$, and higher luminosity sources at λL_{λ} (5100 Å) > 10⁴⁵ ergs s⁻¹. The challenge is to have a survey area large enough to observe local sources at low luminosity, and the rare local high-luminosity sources. This is especially difficult for multi-object RM surveys, but by extending spectral coverage into the red-optical and infra-red range, such surveys can access the greater volume for such sources at higher redshifts with $H\beta$.

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This analysis used NUMPY (Harris et al. 2020), ASTROPY (Astropy Collaboration et al. 2013, 2018), and SCIPY (Virtanen et al. 2020). Plots were made using MATPLOTLIB (Hunter 2007). This work has made use of the SAO/NASA Astrophysics Data System Bibliographic Services.

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DATA AVAILABILITY

Machine-readable light curves for the eight AGN in the final sample are available in the online supplementary material. The underlying DES and OzDES data are available in Abbott et al. (2021) and Lidman et al. (2020).

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SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

Hbeta_lightcurves.zip

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APPENDIX A: SOURCES WITH JAVELIN ALIASING

Here we include additional figures referenced in Section 4.1. Figs A1 and A2 show the light curves and lag PDF's for the five of the eight sources with JAVELIN aliasing signals that we do not include on our final sample. Although two of these sources do pass our selection criteria after omitting the negative JAVELIN aliasing peak, we choose to not include them in our final sample as the positive lag is not constrained by overlap between the photometric and spectroscopic data. We show the light curves phase-shifted by both the positive lag and the negative lag in Fig. A3 for the three sources which are included in our final sample, and in Fig. A4 for the other five sources.



Figure A1. Same as for Fig. 6. These sources are not included in the final sample.



Figure A2. Same as for Fig. 6. These sources are not included in the final sample.



Figure A3. The emission-line light curve (black) and phase-shifted continuum light curve (orange) for the additional three sources we include in our final sample. The top and bottom panels show the continuum shifted by the positive and negative lag, respectively. For each source there is overlap between the light curves phase-shifted by the positive lag, while the negative lag shifts the continuum light curves wholly within the seasonal gaps of the emission-line light curve.



Figure A4. The emission-line light curve (black) and phase-shifted continuum light curve (orange) for the five sources in Fig. A1 and Fig. A2, which we do not include in our final sample. The top and bottom panels show the continuum shifted by the positive and negative lag, respectively. For each source, in both cases there is no overlap between the photometric and spectroscopic observations.

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