THE EFFECTS OF VARIATIONS IN NUCLEAR PROCESSES ON TYPE I X-RAY BURST NUCLEOSYNTHESIS

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ABSTRACT

Type I X-ray bursts are violent stellar events that take place in the H/He-rich envelopes of accreting neutron stars. We have investigated the role played by uncertainties in nuclear processes on the nucleosynthesis accompanying these explosive phenomena. Two different approaches have been adopted, in the framework of postprocessing calculations. In the first one, nuclear rates are varied individually within uncertainties. Ten different models, covering the characteristic parameter space for these stellar events, have been considered. The second, somewhat complementary approach involves a Monte Carlo code in which all nuclear rates are randomly varied within uncertainty limits simultaneously. All in all, about 50,000 postprocessing calculations, with a network containing 606 nuclides (H to ¹¹³Xe) and more than 3500 nuclear processes, have been performed in this work. A brief comparison between both procedures is outlined together with an overall account of the key nuclear reactions whose uncertainties have the largest impact in our X-ray burst nucleosynthesis studies.

Subject headings: nuclear reactions, nucleosynthesis, abundances — stars: neutron — X-rays: bursts

Online material: color figures

1. INTRODUCTION

Type I X-ray bursts (XRBs) are cataclysmic stellar events powered by thermonuclear runaways (TNRs) in the H/He-rich envelopes accreted onto neutron stars in close binary systems (see reviews by Bildsten 1998; Lewin et al. 1993, 1995; Psaltis 2006; Schatz & Rehm 2006; Strohmayer & Bildsten 2006). They constitute the most frequent type of thermonuclear stellar explosion in the Galaxy (the third, in terms of total energy output after supernovae and classical novae) because of their short recurrence period (hours to days). More than 80 Galactic low-mass X-ray binaries exhibiting such bursting behavior (with $\tau_{burst} \sim$ 10–100 s) have been found since the discovery of XRBs by Grindlay et al. (1976) and, independently, by Belian et al. (1976).

Modeling of type I XRBs and their associated nucleosynthesis (see pioneering models by Woosley & Taam 1976; Maraschi & Cavaliere 1977; Joss 1977) has been extensively addressed by different groups, reflecting the astrophysical interest in determining the nuclear processes that power the explosion, as well as in providing reliable estimates for the chemical composition of the neutron star surface. Indeed, several thermal (Miralda-Escudé et al. 1990; Schatz et al. 1999), radiative (Paczyński 1983), electrical (Brown & Bildsten 1998; Schatz et al. 1999), and mechanical properties (Bildsten & Cutler 1995; Bildsten & Cumming

1998) of the neutron star depend critically on the specific chemical abundance pattern of its outer layers. The diversity of shapes in XRB light curves ($L_{\text{peak}} \sim 3 \times 10^{38} \text{ ergs s}^{-1}$; see, e.g., Galloway et al. 2007; Lewin et al. 1993; Kuulkers et al. 2003) is also likely due to different nuclear histories (for an account of the interplay between long bursts and the extension of the *rp*-process in XRBs see Heger et al. 2008), suggesting that the final composition is not unique. It is worth noting that, as discussed by Taam (1980) and Woosley et al. (2004), the properties of the bursts recurring in a given stellar source are affected by compositional inertia; that is, they are sensitive to the fact that accretion proceeds onto the ashes of previous bursts. Indeed, this compositional inertia seems to reduce the expected recurrence times between bursts (particularly for scenarios involving accretion of low-metallicity matter). Moreover, these ashes may provide characteristic signatures such as gravitationally redshifted atomic absorption lines from the surface of the neutron star, which could be identified through high-resolution X-ray spectra (see Cottam et al. 2002; Bildsten et al. 2003; Chang et al. 2005, 2006; Weinberg et al. 2006b), providing a valuable tool to constrain XRB models. Furthermore, the mechanism responsible for superbursts, highly energetic (~10⁴² ergs), long-duration ($\tau \sim 10^4$ s) bursts (Cornelisse et al. 2000; Wijnands 2001 and references therein), first reported from the source 4U 1735-44 (Cornelisse et al. 2000), also depends on XRB nucleosynthesis. These phenomena are attributed to ignition in a C-layer accumulated from successive type I XRBs (first proposed by Woosley & Taam 1976; see also Taam &

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Picklum 1978; Brown & Bildsten 1998; Cumming & Bildsten 2001; Schatz et al. 2003; Weinberg et al. 2006a; Weinberg & Bildsten 2007). The potential impact of XRB nucleosynthesis on Galactic abundances is still a matter of debate: although ejection from a neutron star is unlikely because of its large gravitational potential (matter accreted onto a neutron star of mass M and radius R releases $GMm_p/R \sim 200$ MeV nucleon⁻¹, whereas only a few MeV nucleon⁻¹ are released from thermonuclear fusion), radiation-driven winds during photospheric radius expansion may lead to ejection of a tiny fraction of the envelope (containing nuclear processed material; see Weinberg et al. 2006b; MacAlpine et al. 2007). Indeed, XRBs may help to explain the Galactic abundances of the problematic light *p*-nuclei (Schatz et al. 1998).

With a neutron star as the underlying compact object, temperatures and densities in the accreted envelope reach quite high values: $T_{\text{peak}} > 10^9$ K and $\rho \sim 10^6$ g cm⁻³ (note that during superbursts, however, densities may exceed 10^9 g cm⁻³; see Cumming & Bildsten 2001). These values are at least an order of magnitude larger than in a typical classical nova outburst (see, e.g., José & Hernanz 1998). As a result, detailed nucleosynthesis studies require the use of hundreds of isotopes, up to the SnSbTe mass region (Schatz et al. 2001) or beyond (the nuclear activity in the XRB nucleosynthesis studies of Koike et al. [2004] reaches ¹²⁶Xe), and thousands of nuclear interactions. The main nuclear reaction flow is driven by the *rp*-process (rapid proton captures and β^+ -decays), the 3α -reaction, and the αp -process [a sequence of (α , p) and (p, γ) reactions] and is expected to proceed far away from the valley of stability, merging with the proton drip line beyond A = 38 (Schatz et al. 1999).

Until recently, because of computational limitations, studies of XRB nucleosynthesis have been performed using limited nuclear reaction networks, truncated around Ni (Woosley & Weaver 1984; Taam et al. 1993, 1996; all using a 19-isotope network), Kr (Hanawa et al. 1983; 274-isotope network; Koike et al. 1999; 463 nuclides), Cd (Wallace & Woosley 1984; 16-isotope network), or Y (Wallace & Woosley 1981; 250-isotope network). On the other hand, Schatz et al. (1999, 2001) have carried out very detailed nucleosynthesis calculations with a network containing more than 600 isotopes (up to Xe, in Schatz et al. 2001), but using a one-zone approach. Koike et al. (2004) have also performed detailed one-zone nucleosynthesis calculations, with temperature and density profiles obtained from a spherically symmetric evolutionary code, linked to a 1270-isotope network extending up to ¹⁹⁸Bi.

Note, however, that different numerical approaches and approximations (hydrodynamic simulations with limited networks or one-zone calculations with detailed networks) have been adopted in all those works; hence, the predicted nucleosynthesis in each case has to be taken with caution. Indeed, recent attempts to couple hydrodynamic stellar calculations (in one dimension [1D]) and detailed networks include Fisker et al. (2004, 2006, 2007, 2008) and Tan et al. (2007) (using networks of ~300 isotopes, up to ¹⁰⁷Te), José & Moreno (2006) (using a network of 2640 nuclear reactions and 478 isotopes, up to Te), and Woosley et al. (2004) (using up to 1300 isotopes with an adaptive network).

Most of the nuclear reaction rates required for these extensive nucleosynthesis calculations (in particular, those related to heavy species) rely on theoretical estimates from statistical models and therefore may be affected by significant uncertainties. To date, only partial efforts have been made to quantify the impact of such nuclear uncertainties on the overall abundance pattern accompanying XRBs (Wallace & Woosley 1981; Schatz et al. 1998; Iliadis et al. 1999; Koike et al. 1999, 2004; Thielemann et al. 2001; Fisker et al. 2004, 2006, 2008; Amthor et al. 2006), revealing a complex interplay between nuclear activity and the shape of the light curve (Hanawa et al. 1983; Woosley et al. 2004). It has to be stressed, however, that simple, parameterized models cannot adequately address this issue, since nuclear changes in the innermost envelope shell do not show up immediately at the surface of the star.

But in order to provide reliable estimates of the composition of neutron star envelopes, it is of paramount importance to fully identify the key² reactions whose uncertainties have the largest impact on XRB yields (reactions that probably deserve further improvement through nuclear physics experiments at dedicated facilities). To achieve such a goal, we have performed a comprehensive study of the effects of thermonuclear reaction-rate variations on type I XRB nucleosynthesis, sampling the overall parameter space. The scale of this study makes state-of-the-art hydrodynamic models computationally prohibitive. Hence, we rely on postprocessing calculations, coupling a detailed and fully updated nuclear reaction network with temperature and density profiles extracted from literature.

The structure of the paper is as follows. In § 2 we outline the two approaches adopted in this paper, in the framework of postprocessing calculations with temperature and density profiles extracted from the literature. In § 3 we extensively describe the results obtained from the different models, through a sensitivity study in which all reaction rates are varied individually within uncertainty limits. This is compared with Monte Carlo simulations in which all nuclear reactions are simultaneously varied with randomly sampled enhancement factors (§ 4). A summary of the main conclusions reached in this study, including a list of key reactions whose uncertainties deeply influence the final type I XRB yields, is presented in § 5.

2. MODELS AND INPUT PHYSICS

2.1. Rate Uncertainties and Postprocessing Calculations

Nucleosynthesis studies in XRB conditions are computationally challenging because of the characteristic timescales and peak temperatures achieved, the large number of nuclear species involved (several hundred), and the huge networks (with several thousand nuclear processes) required to address the *rp*and αp -processes occurring for H- and He-rich mixtures accreted onto the surface of a neutron star.

Two different, somewhat complementary approaches, based on postprocessing calculations with temperature and density profiles, can be adopted in a comprehensive sensitivity study. In the first one, all rates are varied individually (see § 3) within uncertainty limits so as to check the impact of each nuclear process on the final yields. At least two postprocessing calculations are required per nuclear rate to account for the upper and lower limits posed by its associated uncertainty. For a network containing several thousand interactions the overall number of postprocessing calculations is indeed extraordinarily large. It is worth mentioning that this technique has been previously applied to a large number of astrophysical sites, including nucleosynthesis in the Sun (Bahcall et al. 1982), Type II supernovae (The et al. 1998; Jordan et al. 2003), classical nova explosions (Iliadis et al.

² Throughout this manuscript we refer to "critical" (or key, important. . .) reaction rates as those whose variation within uncertainty limits leads to changes in final abundances by at least a factor of 2 for isotopes with final mass fractions >10⁻⁵ (see § 3). Notice, however, that reaction variations leading to a change in the overall nuclear energy production may also be considered critical. However, this issue cannot be properly addressed in the context of postprocessing calculations (see § 5 for details).



FIG. 1.—Left: Temperature vs. time profiles corresponding to models K04 (Koike et al. 2004), S01 (Schatz et al. 2001), and F08 (Fisker et al. 2008). Right: Same as left panel, but for temperature vs. density. The initial metallicity for each model is listed as well.

2002), primordial (big bang) nucleosynthesis (Coc et al. 2002, 2004), intermediate-mass asymptotic giant branch stars (Izzard et al. 2007), and type I XRBs (Amthor et al. 2006).

A second approach is based on Monte Carlo techniques (see § 4). Here random enhancement factors (often adopted to follow a lognormal distribution) are applied to each nuclear process of the network simultaneously. The impact on the final yields is then tested through a series of postprocessing calculations. This approach requires a large number of trial simulations in order to be statistically sound and has been already applied to big bang nucleosynthesis studies (Krauss & Romanelli 1990; Smith et al. 1993), nova nucleosynthesis (Smith et al. 2002; Hix et al. 2002, 2003), and also to type I XRBs (Roberts et al. 2006).

Both approaches have been adopted in this study (although more emphasis has been placed on the first one). An interesting issue, recently raised by Roberts et al. (2006), is the feasibility of the first method, as compared with the Monte Carlo approach, to properly address the higher order correlations between input rates and XRB model predictions because of the large number of reactions simultaneously involved in the production and destruction of each element. It is also the goal of this manuscript to test this conjecture by comparing the results from an individualvariation sensitivity study with those obtained with a Monte Carlo approach.

2.2. Initial Models: Temperature and Density Profiles

In this work we have used three temperature-density versus time profiles directly extracted from the literature (see Fig. 1). Model K04 (Koike et al. 2004) is based on a spherically symmetric, multizone model of accretion (at a rate $M_{\rm acc} = 2.3 \times 10^4 \text{ g cm}^{-2} \text{ s}^{-1}$) onto a $1.3 M_{\odot}$ neutron star (with $R_{\rm NS} = 8.1 \text{ km}$, $g_{\rm surface} = 3.6 \times 10^{14} \text{ g cm}^{-3}$). This model is characterized by a peak temperature of $1.36 \text{ GK} (L_{\rm peak} \sim 10^{38} \text{ ergs s}^{-1})$, densities ranging between $(0.54-1.44) \times 10^6 \text{ g cm}^{-3}$ (the column density of the burning region reaches $2.2 \times 10^8 \text{ g cm}^{-2}$), and a burst duration of $\sim 100 \text{ s}$. The initial composition is taken directly from Koike et al. (2004), with X = 0.73, Y = 0.25, and Z = 0.02, roughly solar.

Model F08 (Fisker et al. 2008) is based on 1D general relativistic, hydrodynamic, multizone calculations. In this model, the adopted neutron star is $1.4 M_{\odot}$ (with $R_{\rm NS} = 11$ km, $g_{\rm surface} = 1.9 \times 10^{14}$ g cm⁻³), and the mass accretion rate is 0.66×10^4 g cm⁻² s⁻¹. It achieves a peak temperature of only 0.993 GK ($L_{\rm peak} \sim 10^{38}$ ergs s⁻¹), densities ranging between (2.07-5.14) × 10^5 g cm⁻³ (the column density of the burning region reaches 0.79×10^8 g cm⁻²), and a burst duration of ~50 s. The initial composition is taken directly from the hottest burning zone (representative of the depth

at which most of the relevant nucleosynthetic processes take place) of the hydrodynamic models computed by Fisker et al. (2008), with X = 0.40, Y = 0.41, and Z = 0.19 (a metallicity about 10 times solar; see the original manuscript for a detailed account of the distribution of those metals).

Finally, model S01 (based on Schatz et al. 2001) achieves the largest temperature of all models extracted from the literature, with $T_{\text{peak}} = 1.907$ GK. The shape of this temperature profile, based on one-zone model calculations of accretion onto a neutron star (with $g_{\text{surface}} = 1.9 \times 10^{14} \text{ g cm}^{-3}$ and an adopted mass accretion rate $M_{\text{acc}} = 8.8 \times 10^4 \text{ g cm}^{-2} \text{ s}^{-1}$), is quite different from those corresponding to models K04 and F08 (which approximately follow an exponential decay): indeed, it shows a long plateau at about $T \sim 1.4$ GK before the final decline. Since no density profile is directly available for this model, and considering the relatively small variation in density during an XRB. we have scaled K04 to match the values reported in Schatz et al. (2001), resulting in densities ranging between $(0.54-1.73) \times$ 10^6 g cm⁻³. The duration is ~300 s. The initial composition is X = 0.718, Y = 0.281, and Z = 0.001 (a metallicity about 20 times lower than solar). Because of the lack of information on the specific distribution of the metallicity, we assume that all metals correspond to $^{14}\mathrm{N}$ (see also Woosley et al. 2004), following the rapid rearrangement of CNO isotopes that naturally occurs early in the burst (which in this 1D model reaches $L_{\rm peak} \sim 5 \times 10^{38} {\rm ~ergs~s^{-1}}$).

It is worth noting that in realistic hydrodynamic calculations the pressure near the base of the envelope remains almost constant during the entire burst because of the strong gravitational field of the neutron star. We have checked how the temperaturedensity versus time profiles from models K04, F08, and S01 match this condition along the burst: we found that models K04 and F08 deviate from constant pressure at most by just 5% throughout the different epochs of the burst. Model S01, however, shows somewhat larger deviations (about 20%). We have performed a detailed study of the possible implications of these deviations from constant pressure in the S01 model and find them to be negligible given our criteria for identifying critical reactions (see § 3).

The three models mentioned above partially cover the parameter space in XRB nucleosynthesis calculations. However, it is difficult, if not impossible, to disentangle the specific role played by the initial metallicity, the peak temperature achieved, and the duration of the bursts, since all these models are characterized by different values for these physical quantities. Hence, to appropriately address this issue, we have generated additional models through parameterization of the Koike et al. (2004)

TABLE 1

Final Abundance Ratios, $X_i/X_{i,std}$, for Model K04 (Koike et al. 2004), Resulting from Reaction-Rate Variations by a Factor of 10 (Up and Down)

Reaction	Isotope	10	0.1
$^{15}O(\alpha, \gamma)^{19}Ne$	¹⁵ N		8.30
$^{18}Ne(\alpha \ p)^{21}Na$	¹⁵ N	0.43	
1.e(a, p) 1.e	¹⁸ F	0.43	
${}^{31}\text{Cl}(p,\gamma){}^{32}\text{Ar}$	³⁰ Si	0.44	
$^{43}V(p, \gamma)$ ⁴⁴ Cr	⁴⁴ Ti	0.11	0.49
$^{47}Mn(p, \gamma)$ ^{48}Fe	⁴⁶ Ti	0.31	0.15
$^{56}Ni(p, \gamma)$ ⁵⁷ Cu	⁵⁶ Ni	0.51	7 78
${}^{56}Cu(n, x) {}^{57}Zn$	55Co		2 64
$5^{7}Cu(p, \gamma) = 2^{87}Tn$	57Ni		2.04
$^{58}Cu(p, \gamma)$ 21	⁵⁸ Ni		2.75
$^{59}Cu(p, \gamma) \stackrel{60}{\simeq} 7n$	59NI		2.05
61 Zn (p, γ) 62 Ga	⁶¹ Cu		2.02
$^{61}G_{2}(p, \gamma)$ Gamma $^{62}G_{2}$	60Ni	0.16	4 10
$\operatorname{Ga}(p,\gamma)$ Gc	⁶¹ Cu	0.10	4.10
$^{63}G_{2}(n,n)$ $^{64}G_{2}$	⁶³ Cu		4.23
$Ga(p, \gamma)$ Ge	657n		5.29 8.05
$65_{A_2}(r_{-2})$ 66_{B_2}	64 7 n	0.25	0.95 2.50
$As(p, \gamma)$ se	657n	0.35	2.02
	66C-	0.57	2.93
	67 Ge	0.44	2.77
	⁸⁷ Ga	0.40	3.22
	⁸¹ Kb		0.50
	80 Zr		0.49
	⁸⁹ Nb		0.49
	⁹⁰ Mo		0.48
	⁹¹ Nb		0.47
	⁹² Mo		0.47
	⁹⁵ Tc		0.46
	⁹⁴ Mo		0.45
	⁹⁵ Ru		0.44
	⁹⁶ Ru		0.43
	⁹⁷ Ru		0.40
	⁹⁸ Ru		0.39
	⁹⁹ Rh		0.38
	¹⁰⁰ Pd		0.38
	¹⁰¹ Pd		0.38
	102 Pd		0.37
	¹⁰³ Ag		0.38
	¹⁰⁴ Ag		0.40
${}^{66}\text{Ge}(p, \gamma) {}^{67}\text{As}$	⁶⁶ Ge		4.86
${}^{66}\text{As}(p, \gamma) {}^{67}\text{Se}$	⁶⁶ Ge	0.18	
${}^{67}\text{As}(p, \gamma) {}^{68}\text{Se}$	⁶⁷ Ga	0.47	5.71
69 Se(p, γ) 70 Br	⁶⁹ Ge	0.10	8.21
70 Se(<i>p</i> , γ) 71 Br	⁷⁰ Ge		5.18
70 Br(<i>p</i> , γ) 71 Kr	⁷⁰ Ge	0.28	
71 Br(<i>p</i> , γ) 72 Kr	⁷¹ As	0.20	7.11
73 Kr(<i>p</i> , γ) 74 Rb	⁷³ Se	0.10	7.50
74 Kr(<i>p</i> , γ) 75 Rb	⁷⁴ Se	0.30	6.51
74 Rb(p, γ) 75 Sr	⁷⁴ Se	0.40	
$^{75}\text{Rb}(p, \gamma)$ ^{76}Sr	⁷⁵ Br	0.15	6.35
77 Sr(p, γ) 78 Y	⁷⁷ Kr	0.11	5.72
78 Sr(<i>p</i> , γ) 79 Y	⁷⁸ Kr	0.17	5.82
79 Y(p, γ) 80 Zr	⁷⁹ Kr	0.12	5.45
81 Zr(<i>p</i> , γ) 82 Nb	⁸¹ Rb	0.15	3.15
82 Zr(p, γ) 83 Nb	⁸² Sr	0.17	2.92
83 Nb(p, γ) 84 Mo	⁸³ Sr	0.27	
84 Nb(p, γ) 85 Mo	⁸⁴ Sr	0.20	2.44
85 Nb(p, γ) 86 Mo	⁸⁵ V	0.43	
$^{85}Mo(p, \gamma)$ ⁸⁶ Tc	85V	0.48	
$^{86}Mo(p, \gamma)$ ^{87}Tc	86 7 r	0.70	2 42
$^{87}Mo(p, \gamma)$ ⁸⁸ Tc	87 7 r	0.23	2.43
88 To(p, 39) ⁸⁹ Pu	887.	0.32	2.04
$10(p, \gamma) = Ku$	21 89xtl	0.37	2.04
$p_{0}(p, \gamma) = Ku$	90 N Ø	0.24	2.15
$\operatorname{Ku}(p, \gamma)$ Kn	Mo	0.35	

TABLE 1—Continued

Reaction	Isotope	10	0.1
91 Ru(<i>p</i> , γ) 92 Rh	⁹¹ Nb	0.37	
92 Ru(<i>p</i> , γ) 93 Rh	⁹² Mo	0.32	
93 Rh (p, γ) 94 Pd	⁹³ Tc	0.24	2.05
94 Rh (p, γ) 95 Pd	⁹⁴ Mo	0.47	
94 Pd(p, γ) 95 Ag	⁹⁴ Mo	0.45	
95 Pd(p, γ) 96 Ag	⁹⁵ Ru	0.31	
${}^{96}\text{Ag}(p, \gamma) {}^{97}\text{Cd}$	⁹⁶ Ru	0.48	
	⁹⁷ Ru		0.41
	⁹⁸ Ru		0.38
	⁹⁹ Rh		0.43
	¹⁰⁰ Pd		0.48
$^{97}\text{Ag}(p, \gamma) ^{98}\text{Cd}$	⁹⁷ Ru	0.26	2.13
$^{98}Ag(p, \gamma) ^{99}Cd$	⁹⁸ Ru	0.45	
${}^{98}\text{Cd}(p,\gamma) {}^{99}\text{In}$	⁹⁸ Ru	0.43	
99 Cd (p, γ) ¹⁰⁰ In	⁹⁹ Rh	0.32	
$^{100}\text{Cd}(p, \gamma)$ ^{101}In	¹⁰⁰ Pd	0.43	
101 In (p, γ) 102 Sn	¹⁰¹ Pd	0.34	
102 In (p, γ) 103 Sn	¹⁰² Pd	0.36	
	¹⁰³ Ag		0.40
	¹⁰⁴ Ag		0.48
103 In(<i>p</i> , γ) 104 Sn	^{104}Ag	2.80	0.24
	¹⁰⁵ Ag	2.00	
104 In(p, γ) 105 Sn	¹⁰⁵ Ag	4.13	

temperature-density-time profiles. Parameterized models have been used previously to study, for example, nucleosynthesis in novae (Boffin et al. 1993), the α -rich freezeout in Type II supernovae (The et al. 1998; Jordan et al. 2003), and XRBs (Wallace & Woosley 1981, 1984).

To evaluate the role played by the duration of the burst (taken as the characteristic timescale of the temperature and density profiles) in the extension of the nuclear path, we have scaled the K04 profiles in duration by a factor of 0.1 (short burst: model K04-B1) and 10 (long burst: model K04-B2) while preserving T_{peak} and the initial chemical composition.

The role played by the initial metallicity (reflecting that of the stream of infalling material during accretion) has been tested through three models: a low-metallicity model ($Z = 10^{-4}$; model K04-B3) and two high-metallicity ones (with Z = 0.19; models K04-B4 and K04-B5). The initial composition of models K04-B3 and K04-B4 is scaled from the distribution reported in Koike et al. (2004). In contrast, for model K04-B5, we have adopted the distribution given in Fisker et al. (2008). This will also allow us to test if a different distribution of metals has an impact on the final yields.

Finally, two additional models have been constructed to test the effect of varying the peak temperature achieved during the explosion: we have scaled the temperature and density versus time profiles from Koike et al. (2004) to attain peak values of 0.9×10^9 K (lower peak temperature; model K04-B6) and $2.5 \times$ 10^9 K (higher peak temperature; model K04-B7), while preserving the initial composition and the duration of the burst.

It is worth noting that postprocessing calculations are not suited to derive absolute abundances (or, as mentioned above, to provide any insight into light-curve variations and energetics) since they rely only on temperature and density versus time profiles evaluated at a given location of the star (usually, the innermost shells of the envelope). Indeed, it is likely that the evolution at other depths will be characterized by a different set of physical conditions. Furthermore, adjacent shells will eventually mix when convection sets in, altering the chemical abundance pattern

 TABLE 2

 Same as Table 1, but for Model S01 (Schatz et al. 2001)

Reaction	Isotope	10	0.1
$^{15}\text{O}(\alpha, \gamma)^{19}\text{Ne}$	¹⁵ N		8.84
52 Fe(p, γ) 53 Co	⁵² Fe		8.48
52 Co(p, γ) 53 Ni	⁵² Fe		2.03
${}^{56}\text{Ni}(p, \gamma) {}^{57}\text{Cu}$	⁵⁶ Ni		8.33
${}^{56}\text{Ni}(\alpha, p){}^{59}\text{Cu}$	^{1}H	0.36	
	⁵² Fe	2.40	
	⁵⁶ Ni	2.31	
	⁶⁹ Ge	2.27	
	⁷⁰ Ge	2.19	
	⁷¹ As	2.02	
	⁷³ Se	2.25	
	⁷⁴ Se	2.19	
${}^{57}\text{Ni}(p, \gamma) {}^{58}\text{Cu}$	⁵⁷ Ni		2.50
${}^{57}Cu(p, \gamma) {}^{58}Zn$	⁵⁷ Ni		2.09
${}^{58}Cu(p, \gamma) {}^{59}Zn$	⁵⁸ Ni		4.92
${}^{59}Cu(p, \gamma) {}^{60}Zn$	¹ H		0.35
$\operatorname{Cu}(p, \gamma)$ En	⁵² Fe		2 45
	56 _{Ni}		2.45
	59NG		6.60
	⁶⁹ Ca		0.00
	70 C -		2.52
	71 A -		2.24
	73G		2.07
	⁷³ Se	•••	2.29
61- () 62-	/*Se	•••	2.24
61 Zn(<i>p</i> , γ) 62 Ga	⁶¹ Cu		5.59
$^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	⁶⁰ Ni	0.29	
62 Zn (p, γ) 63 Ga	⁶² Zn	•••	3.52
${}^{63}\text{Ga}(p, \gamma) {}^{64}\text{Ge}$	⁶³ Cu	0.31	6.80
${}^{65}\text{Ge}(p, \gamma) {}^{66}\text{As}$	⁶⁵ Zn		7.90
${}^{66}\text{Ge}(p, \gamma) {}^{67}\text{As}$	⁶⁶ Ge	0.22	6.19
${}^{66}\text{As}(p, \gamma) {}^{67}\text{Se}$	⁶⁶ Ge	0.40	
${}^{67}\text{As}(p, \gamma) {}^{68}\text{Se}$	⁶⁷ Ga	0.13	6.71
${}^{69}\text{Se}(p, \gamma) {}^{70}\text{Br}$	⁶⁹ Ge	0.11	6.14
69 Br(<i>p</i> , γ) 70 Kr	⁷² Se		2.06
	⁷⁶ Kr		2.06
70 Se(<i>p</i> , γ) 71 Br	⁷⁰ Ge	0.21	7.01
71 Br(p, γ) 72 Kr	⁷¹ As	0.11	5.53
73 Kr(p, γ) 74 Rb	⁷³ Se	0.11	5.53
74 Kr(p, γ) 75 Rb	⁷⁴ Se	0.14	6.84
75 Rb(<i>p</i> , γ) 76 Sr	⁷⁵ Br	0.12	4.54
77 Sr(p, γ) 78 Y	⁷⁷ Kr	0.16	3.17
78 Sr (p, γ) ⁷⁹ Y	⁷⁸ Kr	0.12	5 42
79 V(p , γ) 80 Zr	⁷⁹ Kr	0.14	3 43
$^{80}V(p, \gamma) ^{81}Zr$	⁸⁰ Sr	0.43	2.84
$(p, \gamma) = 21$ $81_{V}(p, \gamma) = 82_{T}r$	⁸¹ Rb	0.45	2.04
81 <i>Tr</i> (<i>p</i> , <i>q</i>) 82 Nb	⁸¹ Ph	0.27	2.15
$\frac{82}{r(p, \gamma)}$ Nb	82 Sr	0.27	2 25
$\frac{83}{2r(r,r)} \frac{84}{84} \frac{84}{16}$	83 51	0.20	2.23
$^{84}Zr(p, \gamma)$ NO	84C	0.57	•••
84 Zr(p, γ) 85 ND	84G	0.46	
$^{\circ}$ ND(p, γ) $^{\circ}$ MO	* Sr 85 r	0.42	
$^{86}Nb(p, \gamma) ^{87}mb$	867	0.29	
$MO(p, \gamma)$ of 1c	⁸⁰ Zr	0.40	
$^{67}Mo(p, \gamma)$ ^{66}Ic	⁸⁷ Zr	0.36	•••
$^{80}Mo(p, \gamma)$ ^{89}Ic	⁸⁰ Zr	0.27	•••
89 Ic(<i>p</i> , γ) 90 Ru	⁸⁹ Nb	0.32	
20 Mo(p, γ) 21 Tc	⁹⁰ Mo	0.45	
21 Ic(p, γ) 22 Ru	⁹¹ Nb	0.30	
92 Ru (p, γ) 93 Rh	⁹² Mo	0.23	
93 Ru (p, γ) 94 Rh	⁹³ Te	0.47	
93 Rh (p, γ) 94 Pd	⁹³ Te	0.30	2.29
94 Rh (p, γ) 95 Pd	⁹⁴ Mo	0.28	
94 Pd (p, γ) 95 Ag	⁹⁴ Mo	0.49	
95 Rh(p, γ) 96 Pd	⁹⁵ Ru	0.46	
95 Pd (p, γ) 96 Ag	⁹⁵ Ru	0.32	
${}^{96}\text{Ag}(p, \gamma) {}^{97}\text{Cd}$	⁹⁶ Ru	0.46	2.29

TABLE 2—Continued

Reaction	Isotope	10	0.1
$^{97}\text{Ag}(p, \gamma)$ ^{98}Cd	⁹⁷ Ru	0.22	
${}^{97}\text{Cd}(p, \gamma) {}^{98}\text{In}$	⁹⁷ Ru	0.43	
$^{98}Ag(p, \gamma) ^{99}Cd$	⁹⁸ Ru	0.42	
${}^{98}\text{Cd}(p, \gamma) {}^{99}\text{In}$	⁹⁸ Ru	0.40	2.30
99 Cd (p, γ) 100 In	⁹⁹ Rh	0.28	
100 Cd(p, γ) 101 In	¹⁰⁰ Pd	0.49	
100 In(p, γ) 101 Sn	¹⁰⁰ Pd	0.44	
101 In(p, γ) 102 Sn	¹⁰¹ Pd	0.30	
102 In(p, γ) 103 Sn	¹⁰² Pd	0.36	
103 In(p, γ) 104 Sn	¹⁰³ Ag	0.46	
103 Sn $(\alpha, p)^{106}$ Sb	¹⁰⁶ Cd	0.34	
2-((-, -, -) - 2	¹⁰⁷ Cd	0.24	
	¹⁰⁸ Cd	0.21	
	¹⁰⁹ In	0.21	
$105 \text{Sp}(n, \infty)$ 106 Sh	105 A g	0.33	
$107 \text{Sn}(p, \gamma)$ 108 Sh	¹⁰⁸ Cd	2 32	
108 Sb(p, γ) 109 Te	¹⁰⁹ In	3 33	
109Sh(p, r) 110Ta	1091.0	0.46	
$\operatorname{SD}(p, \gamma)$ Te	in	0.46	2.32

in those layers. However, this approach is reliable to identify the key processes governing the main nuclear activity at the specific temperature and density regimes that characterize such bursting episodes. Hence, the goal of this paper is to provide the reader with a list of key nuclear processes whose uncertainties have the largest influence on the final yields, covering as much as possible the proper range of temperatures, densities, and timescales that characterize XRBs. Any attempt to properly quantify the extent of this impact (for instance, in terms of absolute abundances), however, must rely on state-of-the-art hydrodynamic codes coupled to detailed nuclear networks.

2.3. Nuclear Reaction Network

The temperatures and densities achieved in XRB nucleosynthesis are sufficiently high so that many nuclear reactions, especially those with relatively small Q-values, achieve an equilibrium between the forward and reverse process. For example, if the reaction $A(p, \gamma)B$ has a small Q-value, then the strong $B(\gamma, p)A$ photodisintegration will give rise to a small equilibrium abundance of nuclei B that may then capture another proton. Such cases, which are called (sequential) two-proton captures, must be considered carefully since they represent waiting points (and may even be candidates for termination points) for a continuous abundance flow toward heavier mass nuclei. Among the most important of these waiting points are ⁶⁴Ge, ⁶⁸Se, and ⁷²Kr (Schatz et al. 1998). When a reaction rate equilibrium has been established, the most important nuclear physics information needed is the reaction Q-value (which enters exponentially in the effective decay constant of A) of the link $A(p, \gamma)B$ and the reaction rate of the second-step reaction $B(p, \gamma)C$, but the *rate* of the reaction $A(p, \gamma)B$ is irrelevant. Note that for the three nuclei mentioned above, the (p, γ) Q-values have not been measured directly yet. According to Audi et al. (2003b), their predicted values amount to $Q = -80 \pm 300, -450 \pm 100, \text{ and } -600 \pm 100$ 150 keV, respectively. Some encouraging progress has been made through mass measurements of ⁶⁴Ge (Clark et al. 2007; Schury et al. 2007), ⁶⁸Se (Clark et al. 2004; Wohr et al. 2004; Chartier et al. 2005), and ⁷²Kr (Rodríguez et al. 2004).

In order to set up the reaction library for our study, we started by adopting the proton drip line from Audi et al. (2003a, 2003b). For reactions $A(p, \gamma)B$ with Q-values below 1 MeV the rates (below the element Pd) are calculated using the Hauser-Feshbach

 TABLE 3

 Same as Table 1, but for Model F08 (Fisker et al. 2008)

Reaction	Isotope	10	0.1
$^{12}C(n, \gamma)^{13}N$	¹² C	0.41	
$^{12}C(\alpha, \alpha)^{16}O$	^{12}C	0.42	
$C(\alpha, \gamma)$ O	160	0.42	
	200 1	3.27	0.50
	²⁰ Ne	3.03	0.42
14 20	²⁴ Mg	2.40	
$^{16}O(\alpha, \gamma)^{20}Ne$	¹⁶ O	0.11	8.36
20 Ne(α, γ) ²⁴ Mg	²⁰ Ne	0.10	9.84
$^{22}Mg(\alpha, p)^{25}A1$	²⁵ Mg		8.81
	²⁷ A1		2.23
$^{24}Mg(p, \gamma)$ ^{25}Al	²⁵ Mg	3.02	0.43
$^{24}Mg(\alpha, \gamma)^{28}Si$	²⁴ Mg	0.18	4.16
	²⁵ Mg	0.24	4.10
$^{25}\text{Al}(\alpha, p)^{28}\text{Si}$	²⁵ Mg	0.22	2.36
$^{26g}Al(p,\gamma)^{27}Si$	²⁷ A1	2.71	0.40
$^{26g}Al(\alpha, p)^{29}Si$	²⁶ Mg		2.34
$\Pi(\alpha, p)$ similar	26g A 1	0.08	2 38
	²⁷ A1	0.00	2.50
$^{26}Si(\alpha, p)^{29}P$	26g A 1	0.08	
$\mathfrak{SI}(\alpha, p)$ 1	27 1	0.03	•••
27 A1(a) = 308;	27 • 1	0.23	
$27 \text{ Gr}(\alpha, p)$ SI	27 A 1	0.32	•••
28 SI(α , p) 32 G	27 AI 28 G :	0.30	
²⁸ Si(α , γ) ³² S	²⁰ S1	0.43	
20	³² S	3.73	0.37
$^{29}\mathrm{Si}(\alpha, \gamma)^{33}\mathrm{S}$	33S	2.15	
$^{30}P(p, \gamma)$ ^{31}S	³¹ P	2.38	0.29
30 P(α , p) 33 S	³³ S	2.29	
$^{34}Cl(p, \gamma) ^{35}Ar$	³⁵ Cl	2.07	
$^{36}\text{Ar}(p, \gamma) ^{37}\text{K}$	³⁷ Ar	0.40	2.76
39 K(p, γ) 40 Ca	⁴⁰ Ca	2.15	
$^{44}\text{Ti}(p,\gamma)$ ^{45}V	⁴⁵ Ti	0.18	2.32
$^{44}V(p, \gamma)^{45}Cr$	⁴⁵ Ti		0.47
$^{45}V(p, \gamma)^{46}Cr$	⁴⁵ Ti		2.25
$^{46}V(p,\gamma)$ ^{47}Cr	⁴⁷ Ti	2.22	
${}^{47}Cr(n, \gamma){}^{48}Mn$	⁴⁷ Ti	0.42	2 78
$^{49}Mn(n, \gamma)^{50}Fe$	49V	0.12	2.10
$^{52}\text{Fe}(n, 2)$ ^{53}Co	52 _{Ee}	0.31	3.06
$re(p, \gamma)$ community	53Mm	0.51	0.49
$53C_{2}(n-1)$ 54NI;	53N 4m	0.19	0.40
$54C_{2}(r, r)$ 55N:	545-	0.18	4.00
57 N^2	57NT		2.01
5^{7} Ni(p, γ) 5^{8} Zu	57 N1		/./1
57 Cu(p, γ) 58 Zn	⁵⁰ N1		2.07
	57N1	0.46	2.31
	⁵⁸ Ni	3.31	0.37
	⁵⁹ Ni	2.20	0.47
58 Cu(<i>p</i> , γ) 59 Zn	⁵⁸ Ni	0.44	5.57
59 Cu(<i>p</i> , γ) 60 Zn	⁵⁹ Ni		2.88
61 Zn (p, γ) 62 Ga	⁶¹ Cu	0.21	3.59
	⁶² Zn		0.49
${}^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	⁶⁴ Zn	3.11	
	⁶⁵ Zn	3.06	
	⁶⁶ Ge	3.06	
	⁶⁷ Ga	3.13	
${}^{62}\text{Ga}(n, \gamma) {}^{63}\text{Ge}$	⁶² Zn	0.23	2 39
$^{63}Ga(n, \gamma)$ ⁶⁴ Ge	63Cu	0.49	2.37
$^{65}Ge(p, \gamma) \stackrel{66}{\sim} As$	657n	0.49	3 74
${}^{66}Ge(p, q) {}^{67}As$	66Ge	0.49	5.74
$67 \text{ As}(p, \gamma) = 68 \text{ Sp}$	67 C o	0.79	2 20
$ro(p, \gamma)$ or	69C -	0.38	3.20
$\mathfrak{Sc}(p,\gamma)$ Br	²⁰ Ge	0.24	5.57
700 () 715	70 Ge	•••	0.44
$^{70}\text{Se}(p, \gamma)$ ^{71}Br	/°Ge	0.41	2.66
$^{\prime \circ}$ Br(p, γ) $^{\prime 1}$ Kr	/ºGe	0.33	
$^{\prime 1}$ Br (p, γ) $^{\prime 2}$ Kr	^{/1} As	0.24	3.89
$^{/3}$ Kr(<i>p</i> , γ) 74 Rb	⁷³ Se	0.20	3.64
	⁷⁴ Se		0.47
74 Kr(<i>p</i> , γ) 75 Rb	⁷⁴ Se	0.32	2.91

TABLE 3—Continued

Reaction	Isotope	10	0.1
74 Rb(p, γ) 75 Sr	⁷⁴ Se	0.41	
75 Rb(p, γ) 76 Sr	⁷⁵ Br	0.21	4.13
76 Rb(p, γ) 77 Sr	⁷⁷ Kr		0.48
77 Sr(<i>p</i> , γ) 78 Y	⁷⁷ Kr	0.19	3.57
78 Sr(<i>p</i> , γ) 79 Y	⁷⁸ Kr	0.24	3.18
78 Y(p, γ) 79 Zr	⁷⁸ Kr	0.48	
79 Y(p, γ) 80 Zr	⁷⁹ Kr		4.99
${}^{80}Y(p, \gamma) {}^{81}Zr$	⁸¹ Rb		0.43
81 Zr(p, γ) 82 Nb	⁸¹ Rb	0.19	3.35
82 Zr(p, γ) 83 Nb	⁸² Sr	0.21	3.21
	⁸³ Sr		0.46
83 Nb(p, γ) 84 Mo	⁸³ Sr		3.62
84 Nb(p, γ) 85 Mo	⁸⁴ Sr		4.18
85 Mo(p, γ) 86 Tc	⁸⁵ Y	0.19	2.83
	⁹⁰ Mo		0.50
	⁹¹ Nb		0.46
86 Mo(p, γ) 87 Tc	⁸⁶ Zr	0.17	2.97
	⁸⁷ Zr		0.44
	⁸⁸ Zr		0.40
	⁸⁹ Nb		0.44
	⁹⁰ Mo		0.42
87 Tc(p, γ) 88 Ru	⁸⁷ Zr	0.21	
	⁸⁸ Zr		0.43
⁸⁸ Tc(p, γ) ⁸⁹ Ru	⁸⁹ Nb		0.47
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code MOST (Goriely 1998; Arnould & Goriely 2006) and the corresponding reverse photodisintegrations are computed with the *extrapolated* proton separation energies from Audi et al. (2003b). Notice that nuclear masses enter twice: first in the calculation of the forward Hauser-Feshbach rate, and second in the calculation of the reverse photodisintegration rate. The second-step reactions, $B(p, \gamma)C$, are also computed with the code MOST. We had to include many nuclides beyond the proton drip line in order to properly account for sequential two-proton captures. For all other reactions for which experimental rates are not available, we used the results from the Hauser-Feshbach code NON-SMOKER (Rauscher & Thielemann 2000).

Our entire nuclear network consists of 606 nuclides ranging from ¹H to ¹¹³Xe. All charged-particle induced reactions between these isotopes, as well as their corresponding reverse processes, have been included. Experimental information was only available for the rates of a small subset of reactions. These rates are adopted from Angulo et al. (1999), Iliadis et al. (2001), and some recent updates for selected reactions. Neutron captures are disregarded since our early test calculations have revealed that they play a minor role in XRB nucleosynthesis. All reaction rates incorporate the effects of thermal excitations in the target nuclei (Rauscher & Thielemann 2000).

For the weak interactions, we use laboratory decay rates (Audi et al. 2003a); the impact of β -delayed nucleon emission has also been considered. For a discussion of employing *stellar* versus *laboratory* decay rates, see Woosley et al. (2004). Also, note that many computed stellar decay rates (Fuller et al. 1982a, 1982b) do not converge to their laboratory values at lower temperatures and densities, calling into question the model used for these calculations. In order to avoid this problem, we decided against using available stellar decay rates (Fuller et al. [1982a, 1982b] and Langanke & Martinez-Pinedo [2000] provide stellar decay rates for A = 21-60 and 45–65, respectively). Although the use of properly converging stellar decay rates for all isotopes in an XRB network (including A > 65; see § 3 for the extent of the

TABLE 4 SAME AS TABLE 1, BUT FOR MODEL K04-B1

Reaction	Isotope	10	0.1
$^{15}O(\alpha, \gamma)^{19}Ne$	¹⁵ N	0.11	6.14
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$	¹⁵ N	0.28	
	¹⁸ F	0.29	
	²¹ Ne	0.26	2.03
$^{22}Mg(p, \gamma)^{23}Al$	²² Na	0.49	6.21
$^{23}Al(p, \gamma)^{24}Si$	²² Na		4.45
$^{27}P(n, \gamma)^{28}S$	²⁷ A1	0.25	6 34
${}^{31}Cl(p,\gamma) \stackrel{32}{\to} Ar$	³⁰ Si	0.16	2.57
	³¹ P	0.16	2 72
	³² S	0.10	0.29
${}^{34}Ar(p, \gamma){}^{35}K$	³⁴ S	0.44	2 25
$\operatorname{rn}(p, \gamma)$ is a second sec	36 Ar	0.44	0.30
$^{39}C_{2}(n, \gamma)^{40}S_{2}$	³⁹ K		0.50
$42 \text{Ti}(p, q) \frac{43 \text{V}}{43}$	42Ca	•••	2.11
$^{43}V(p, \gamma) ^{44}Cr$	4^2C_2	0.22	7 20
47Mn(n, x) $48Ee$	46Ti	0.22	7.20
$\operatorname{Will}(p, \gamma)$ re	48Cr	0.17	2.30
$51E_{2}(r_{1},r_{2})$	51Cm	•••	6.10
$5^{2}E_{2}(r, r)$ $5^{3}C_{2}$	52Ea	0.25	0.19
$5^{2}C_{2}(p, \gamma) = 5^{3}N^{2}$	52E-	0.55	2.24
$55 v'(p, \gamma) = 0.56 c$	55C		2.24
$50 \text{ Ni}(p, \gamma)$ 50 Cu	56 U		2.83
$560 (p, \gamma) 577$	50 N1	0.33	/./4
$\operatorname{Cu}(p,\gamma)$ ^{sy} Zn	55Co	0.34	4.09
57 0 () 58 7	⁵⁰ N1		2.16
5^{7} Cu(p, γ) 5^{8} Zn	⁵⁷ N1		2.33
61 Ga(<i>p</i> , γ) 62 Ge	⁶⁰ N1	0.17	2.93
	⁶¹ Cu	0.16	3.01
	⁶² Zn		0.35
	⁰⁴ Zn		0.39
	⁶³ Zn		0.37
	°°Ge		0.37
	⁶⁷ Ga		0.38
	⁶⁸ Ge		0.33
	⁶⁹ Ge		0.31
	⁷⁰ Ge		0.31
	⁷¹ As		0.32
	⁷² Se		0.30
	⁷⁶ Kr		0.29
${}^{63}\text{Ga}(p, \gamma) {}^{64}\text{Ge}$	⁶³ Cu		2.13
${}^{65}\text{Ge}(p, \gamma) {}^{66}\text{As}$	⁶⁵ Zn	0.25	7.08
65 As(p, γ) 66 Se	⁶⁸ Ge	3.85	
	⁶⁹ Ge	3.92	
	⁷⁰ Ge	3.94	
	⁷¹ As	4.04	
	⁷² Se	4.73	0.40
	⁷⁶ Kr	5.05	0.32
${}^{66}\text{Ge}(p, \gamma) {}^{67}\text{As}$	⁶⁶ Ge		2.68
${}^{66}\text{As}(p, \gamma) {}^{67}\text{Se}$	⁶⁶ Ge	0.19	2.66
${}^{67}\text{As}(p, \gamma) {}^{68}\text{Se}$	⁶⁷ Ga		3.15
69 Se(<i>p</i> , γ) 70 Br	⁶⁹ Ge		5.91
70 Se (p, γ) 71 Br	⁷⁰ Ge		2.96
71 Br(<i>p</i> , γ) 72 Kr	⁷¹ As	0.42	4.16

nucleosynthesis in our models) is in principle preferred, we doubt that the results of our work here would be significantly affected by their inclusion (see \S 3).

3. INDIVIDUAL REACTION-RATE VARIATIONS

Some general procedures must be outlined before a detailed analysis of the main results is presented. For all 10 models considered in this section, a first calculation, with *standard* rates (as described in § 2.3), has been performed. This is used to scale the level of changes (indicated in Tables 1–10, 13, and 14 as

TABLE 5 SAME AS TABLE 1, BUT FOR MODEL K04-B2

Reaction	Isotope	10	0.1
$^{12}C(\alpha, \gamma)^{16}O$	¹² C	0.19	2.37
	²⁴ Mg		0.26
	²⁸ Si		0.29
20 Ne(α , γ) ²⁴ Mg	²⁰ Ne		8.28
24 Mg(α , γ) ²⁸ Si	²⁴ Mg	0.16	3.77
a	³⁴ S	0.48	4.30
24 Mg(α , p) ²⁷ Al	³⁴ S	3.99	0.49
$^{28}\mathrm{Si}(\alpha, \gamma)^{32}\mathrm{S}$	²⁸ Si	0.31	2.63
320 36	34S		2.56
$^{52}S(\alpha, \gamma)^{50}Ar$	32S	0.31	
	35S	0.48	
	³⁶ A n	0.24	0.25
	39V	2.45	0.55
$^{32}S(n, n)$ $^{35}C1$	35C1	2.20	0.30
$^{33}S(n, 2)$ $^{34}C1$	37 A r	0.43	0.50
$^{33}S(\alpha, \alpha)^{37}Ar$	335	0.40	
5(<i>a</i> , <i>j</i>) A	³⁷ Ar	4 12	
$^{34}S(n, \gamma)^{35}C1$	³⁴ S	0.35	2.02
${}^{34}S(\alpha \ \gamma)^{38}Ar$	³⁴ S	0.33	2.02
S(a,)) II	³⁸ Ar	2.18	
$^{35}Cl(p, \gamma) ^{36}Ar$	³⁵ Cl	0.34	
${}^{35}Cl(\alpha, p)^{38}Ar$	³⁸ Ar	4.47	0.45
$^{36}\text{Ar}(\alpha, p)^{39}\text{K}$	³⁹ K	5.47	0.23
39 K(p, γ) 40 Ca	³⁹ K	0.45	2.07
${}^{40}\text{Ca}(\alpha, p){}^{43}\text{Sc}$	⁴⁴ Ti		2.78
41 Sc(<i>p</i> , γ) 42 Ti	⁴⁴ Ti		0.50
43 Sc(<i>p</i> , γ) 44 Ti	⁴⁴ Ti	2.78	
51 Mn(<i>p</i> , γ) 52 Fe	⁵¹ Cr		3.66
55 Co(p, γ) 56 Ni	⁵⁵ Co		2.89
60 Cu(p, γ) 61 Zn	⁶¹ Cu	4.92	0.15
${}^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	⁶⁰ Ni		2.54
	⁶¹ Cu		2.12
()	⁶³ Cu		2.56
$^{63}\text{Ga}(p, \gamma) ^{64}\text{Ge}$	⁶³ Cu		2.73
64 Ga(p, γ) 65 Ge	⁰⁵ Zn	5.48	0.26
65 As (p, γ) 66 Se	³⁰ Ar	•••	0.49
	⁵⁵ K		0.38
	647.		0.22
	65 7	0.31	0.10
	66Ca	0.38	2.20
	67Ga	0.34	4.24
	71 A s	•••	0.33
	⁷³ As	•••	0.33
	⁷³ Se		0.42
	⁸⁴ Sr		0.28
${}^{67}\text{Ge}(p, \gamma) {}^{68}\text{As}$	⁶⁷ Ga	3.47	
${}^{67}\text{As}(p, \gamma) {}^{68}\text{Se}$	⁶⁶ Ge		2.09
	⁶⁷ Ga		2.49
68 As(p, γ) 69 Se	⁶⁹ Ge	2.46	0.42
$^{69}\text{As}(p, \gamma)$ ⁷⁰ Se	⁷⁰ Ge	2.36	
71 Se (p, γ) 72 Br	⁷¹ As	8.13	0.13
71 Br(<i>p</i> , γ) 72 Kr	⁷⁰ Ge	0.44	3.95
72 Br(<i>p</i> , γ) 73 Kr	⁷³ As	2.75	0.37
	⁷³ Se	2.71	0.37
74 Kr(p , γ) 75 Rb	⁷⁵ Br	0.28	
75 Rb (p, γ) 76 Sr	⁷⁴ Se		2.77
	⁷⁵ Se		3.79
76	⁷⁵ Br	0.24	3.77
$^{\prime o}$ Rb (p, γ) $^{\prime \prime}$ Sr	//Br	2.52	0.46
790 () 7077	//Kr	2.49	0.46
$^{\prime \circ}$ Sr(p , γ) $^{\prime 9}$ Y	^{/8} Kr		3.16
$^{\prime 5}Y(p, \gamma)^{\circ 0}Zr$	/ ² Kr	0.12	5.75
$^{\circ 2}$ Zr(p, γ) $^{\circ 5}$ Nb	°2Sr		3.49

TABLE 5—Continued

Reaction	Isotope	10	0.1
83 Nb(<i>p</i> , γ) 84 Mo	⁸³ Sr		2.50
84 Zr(p, γ) 85 Nb	⁸⁴ Sr	2.35	0.17
	⁸⁵ Sr	0.16	
	⁸⁵ Y	0.15	
84 Nb(<i>p</i> , γ) 85 Mo	⁸³ Sr		3.33
86 Mo(p, γ) 87 Tc	⁸⁶ Y		2.73
CA · 77	⁸⁶ Zr		2.70
87 Mo(p, γ) 88 Tc	⁸⁷ Y	2.13	
	⁸⁷ Zr	2.08	
88 Mo(p, γ) 89 Tc	⁸⁹ Zr	0.19	
	⁸⁹ Nb	0.19	
92 Ru(<i>p</i> , γ) 93 Rh	⁹² Mo	2.46	
	⁹³ Mo	0.27	
	⁹³ Tc	0.26	
92 Rh(p, γ) 93 Pd	⁹¹ Nb	2.14	
93 Rh (p, γ) 94 Pd	⁹² Mo		2.45
	⁹³ Mo		2.66
	⁹³ Tc		2.62
${}^{96}\text{Ag}(p, \gamma) {}^{97}\text{Cd}$	⁹⁵ Tc		2.06
	⁹⁵ Ru		2.03
	⁹⁶ Ru	0.31	4.80
99 Cd(p, γ) 100 In	⁹⁹ Rh		3.19
100 In(<i>p</i> , γ) 101 Sn	¹⁰⁰ Rh		3.12
	¹⁰⁰ Pd	0.31	3.10
101 Cd(p, γ) 102 In	¹⁰² Pd	0.45	

 $X_i/X_{i,std}$, that is, the ratio of mass fractions obtained with a modified network [resulting from our exploration of uncertainties] to those obtained with our *standard* network). Following this, a whole series of postprocessing calculations have been computed, in which each nuclear rate is varied individually by a factor of 10 up and down, for each of the 10 models.

Several important remarks have to be made at this stage: First, we have chosen a factor of 10 for the level of uncertainty affecting theoretical reaction rate estimates, in general. Other authors (see Schatz 2006; Amthor et al. 2006) claim, instead, that excitation energies of theoretically calculated levels for XRB conditions may suffer uncertainties of ~ 100 keV, which translates into an overall uncertainty in some rates that may reach several orders of magnitude. It is also worth noting that efforts to ascertain systematic uncertainties through a direct comparison between different theoretical models (see § 5.1) often report variations smaller than a factor of 10. In any event, if uncertainties turn out to be larger than a factor of 10 (in general, or for particular rates), this study would have to be extended in the future. Second, some nuclear rates, such as the triple-alpha reaction, some (p, γ) reaction rates on low-mass targets, or most of the β -decay rates (note again that we used *ground-state* or *laboratory* β -decay rates), are known with much better precision. This has been addressed when necessary and is discussed in the following sections of this manuscript. Third, it is important to stress that forward and reverse reactions have been varied simultaneously with the same uncertainty factor, to preserve the principle of detailed balance. Fourth, a particular strategy has been adopted to evaluate the impact of β -decay rate uncertainties: they have initially been varied by a factor of 10 up and down as a way to discriminate the key β -decay rates from the rest (see Table 11). Then, additional postprocessing calculations focused on these key rates have been performed assuming more realistic uncertainties (around 30%, according to ground-state β -decay rate uncertainties; see Audi et al. 2003a). This approach also helps to test the impact of using stellar versus laboratory decay rates

TABLE 6 SAME AS TABLE 1, BUT FOR MODEL K04-B3

Reaction	Isotope	10	0.1
$\frac{15}{15}\Omega(\alpha, \gamma)^{19}$ Ne	¹⁵ N		8 17
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$	¹⁵ N	0.43	0117
1. c (<i>a</i> , <i>p</i>) 1. a	¹⁸ F	0.44	
31 Cl(p, γ) 32 Ar	³⁰ Si	0.45	
$^{43}V(p, \gamma)^{44}Cr$	⁴² Ca		4.68
(A) (7)	⁴⁴ Ti		0.48
47 Mn(<i>p</i> , γ) 48 Fe	⁴⁶ Ti	0.32	
${}^{56}\text{Ni}(p, \gamma) {}^{57}\text{Cu}$	⁵⁶ Ni		7.93
56 Cu(<i>p</i> , γ) 57 Zn	⁵⁵ Co		2.63
57 Cu(<i>p</i> , γ) 58 Zn	⁵⁷ Ni		2.79
58 Cu(<i>p</i> , γ) 59 Zn	⁵⁸ Ni		2.08
59 Cu(p, γ) 60 Zn	⁵⁹ Ni		2.05
61 Zn (p, γ) 62 Ga	⁶¹ Cu		2.39
${}^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	⁶⁰ Ni	0.17	4.17
	⁶¹ Cu		4.33
$^{63}\text{Ga}(p, \gamma)$ ^{64}Ge	63Cu		3.31
$^{\text{os}}\text{Ge}(p, \gamma) ^{\text{oo}}\text{As}$	⁶³ Zn		8.88
65 As (p, γ) 66 Se	⁶⁴ Zn	0.34	3.41
	⁶⁵ Zn	0.36	2.81
	⁶⁰ Ge	0.43	2.66
	⁶⁷ Ga	0.40	3.12
	⁸¹ Rb		0.48
	867.		0.49
	87 Z r		0.50
	⁸⁸ Zr		0.49
	⁸⁹ Nib		0.40
	90Mo		0.48
	⁹¹ Nb		0.47
	⁹² Mo		0.46
	⁹³ Tc		0.40
	⁹⁴ Mo		0.44
	⁹⁵ Ru		0.44
	⁹⁶ Ru		0.43
	⁹⁷ Ru		0.41
	⁹⁸ Ru		0.39
	⁹⁹ Rh		0.39
	¹⁰⁰ Pd		0.39
	¹⁰¹ Pd		0.38
	¹⁰² Pd		0.38
	¹⁰³ Ag		0.39
	¹⁰⁴ Ag		0.42
${}^{66}\text{Ge}(p, \gamma) {}^{67}\text{As}$	⁶⁶ Ge		4.81
${}^{66}\text{As}(p, \gamma) {}^{67}\text{Se}$	⁶⁶ Ge	0.18	
67 As (p, γ) 68 Se	⁶⁷ Ga	0.45	5.73
69 Se(p, γ) 70 Br	⁶⁹ Ge	0.10	8.19
70 Se(p, γ) 71 Br	⁷⁰ Ge	•••	5.24
70 Br (p, γ) 71 Kr	⁷⁰ Ge	0.28	
$^{71}\text{Br}(p, \gamma)$ ^{72}Kr	⁷¹ As	0.20	7.01
75 Kr(p, γ) 77 Rb	⁷⁵ Se	0.10	7.53
7^{4} Kf (p, γ) 7^{5} Rb	74Se	0.30	6.30
$75 \text{Pb}(p, \gamma)$ 76Sr	⁷⁵ D#	0.40	 6 15
77 Sr(p , γ) ⁷⁸ V	77 _K	0.15	0.45 5 59
$78 Sr(p, \gamma)$ ⁷⁹ V	78Kr	0.11	6.15
$^{79}V(n,\gamma) = \frac{80}{7}r$	⁷⁹ K r	0.17	5 73
$^{81}Zr(p, \gamma) \overset{82}{\sim} Nh$	⁸¹ Rh	0.12	3 20
$^{82}Zr(p, \gamma)$ ⁸³ Nb	⁸² Sr	0.15	2 94
$^{83}Nb(p, \gamma)$ ⁸⁴ Mo	⁸³ Sr	0.29	2.74
$^{84}\text{Nb}(p,\gamma)$ ⁸⁵ Mo	⁸⁴ Sr	0.20	2.51
$^{85}\text{Nb}(p,\gamma)$ ^{86}Mo	⁸⁵ Y	0.44	2.01
85 Mo(p, γ) 86 Tc	⁸⁵ Y	0.48	
86 Mo(p , γ) 87 Tc	⁸⁶ Zr	0.23	2.56
87 Mo(p, γ) 88 Tc	⁸⁷ Zr	0.32	
88 Tc(<i>p</i> , γ) 89 Ru	⁸⁸ Zr	0.39	

TABLE 6—Continued

Reaction	Isotope	10	0.1
$\frac{1}{^{89}}$ Tc(p, γ) 90 Ru	⁸⁹ Nb	0.25	2.16
90 Ru(p, γ) 91 Rh	⁹⁰ Mo	0.33	
${}^{91}\text{Ru}(p, \gamma) {}^{92}\text{Rh}$	⁹¹ Nb	0.36	
92 Ru(<i>p</i> , γ) 93 Rh	⁹² Mo	0.32	
93 Rh (p, γ) 94 Pd	⁹³ Tc	0.24	
94 Rh (p, γ) 95 Pd	⁹⁴ Mo	0.45	
94 Pd(p, γ) 95 Ag	⁹⁴ Mo	0.43	
95 Pd(<i>p</i> , γ) 96 Ag	⁹⁵ Ru	0.30	
${}^{96}\text{Ag}(p, \gamma) {}^{97}\text{Cd}$	⁹⁶ Ru	0.45	
	⁹⁷ Ru		0.41
	⁹⁸ Ru		0.38
	⁹⁹ Rh		0.43
	¹⁰⁰ Pd		0.48
${}^{97}\text{Ag}(p, \gamma) {}^{98}\text{Cd}$	⁹⁷ Ru	0.26	2.04
${}^{98}\text{Ag}(p, \gamma) {}^{99}\text{Cd}$	⁹⁸ Ru	0.45	
${}^{98}\text{Cd}(p, \gamma) {}^{99}\text{In}$	⁹⁸ Ru	0.44	
99 Cd (p, γ) ¹⁰⁰ In	⁹⁹ Rh	0.33	
100 Cd(p, γ) 101 In	¹⁰⁰ Pd	0.44	
101 In (p, γ) 102 Sn	¹⁰¹ Pd	0.34	
102 In (p, γ) 103 Sn	¹⁰² Pd	0.38	
	¹⁰³ Ag	2.05	0.39
	¹⁰⁴ Ag		0.46
103 In (p, γ) 104 Sn	¹⁰³ Ag	0.50	
	¹⁰⁴ Ag	2.81	0.25
	¹⁰⁵ Ag	2.08	
104 In (p, γ) 105 Sn	¹⁰⁵ Ag	4.13	

for XRB conditions: we found differences between our (laboratory) decay rates and the available Fuller et al. (1982a, 1982b) stellar decay rates (over A = 21-60) of as large as a factor of 10, but usually more like $\sim 20\%$ -60%; over A = 50-60, the stellar decay rates of Langanke & Martinez-Pinedo (2000) differ from the Fuller et al. (1982a, 1982b) rates by up to 3 orders of magnitude, but usually more like a factor of ~ 10 . Fifth, some additional tests aimed at identifying the influence of *O*-value variations have been performed using the uncertainties estimated by Audi et al. (2003b) (see Tables 12–14). This part of our study has been restricted to models K04 and F08, to proton-capture reactions on A < 80 nuclei, and to reactions with |Q| < 1 MeV, for which the estimated uncertainty exceeds 50 keV (see Table 12). Sixth, since the main goal of this paper is to identify the key nuclear processes whose uncertainties have the largest impact on XRB nucleosynthesis, we have restricted the analysis (in the tables and forthcoming discussion) to nuclear species that achieve a mass fraction of at least 10^{-5} at the end of the burst and deviate from the abundances computed with standard rates by at least a factor of 2. Seventh, for the sake of clarity and conciseness, the isotopes displayed and discussed throughout this manuscript correspond to species that are either stable or have a half-life longer than 1 hr (the rest are assumed to fully decay at the end of the burst and consequently are added to the corresponding stable or long-lived daughter nuclei).

3.1. Results

In this section we report results from a series of \sim 40,000 postprocessing calculations (requiring 14 CPU-months) performed for this study of XRB nucleosynthesis.

3.1.1. Model K04

Here we describe in detail the results obtained from our postprocessing calculations using temperature and density versus time profiles extracted from Koike et al. (2004) (model K04). A general discussion of the main nuclear path achieved for these profiles

TABLE 7 SAME AS TABLE 1, BUT FOR MODEL K04-B4

Reaction	Isotope	10	0.1
$^{12}C(\alpha, \gamma)^{16}O$	¹² C	0.24	2.53
	¹⁶ O	2.38	
	²⁰ Ne	2.30	0.26
	²⁴ Mg		0.29
	²⁸ Si		0.41
$^{16}O(\alpha, \gamma)^{20}Ne$	¹⁶ O		7.65
20 Ne(α, γ) ²⁴ Mg	²⁰ Ne		7.87
$^{24}Mg(\alpha, \gamma)^{28}Si$	²⁴ Mg	0.20	3.48
	³⁰ Si	0.44	5.51
$^{24}Mg(\alpha, p)^{27}A1$	³⁰ Si	5.84	0.44
$^{28}\text{Si}(\alpha, p)^{31}\text{P}$	³¹ P	3.39	0.44
28 Si $(\alpha, \gamma)^{32}$ S	²⁸ Si	0.30	3.04
5.(a, ,) 5	³¹ P	0.20	4 07
30 Si $(\alpha \ \gamma)^{34}$ S	³⁰ Si	0.39	5 84
$^{30}P(p, \gamma)^{31}S$	³³ S	0.50	0.01
(<i>p</i> , <i>j</i>) 5	³⁶ C1	0.56	
$^{30}P(\alpha, n)$ ^{33}S	³⁰ Si	0.40	23 47
$\Gamma(\alpha, p)$ 5	31p	•••	23.47
	36C1	•••	0.27
30 S(c) n) 33 C1	30		5.94
$S(\alpha, p)$	310	•••	5.84
	33C		2.88
	35S	0.04	6.20
	³⁰ Cl		4.19
21- () 24~	³⁷ Ar	0.42	2.56
$^{31}P(\alpha, p) {}^{34}S$	⁵¹ P		4.63
$^{32}S(\alpha, \gamma)^{36}Ar$	³² S	0.36	
	³⁶ Ar	2.35	0.48
$^{33}S(\alpha, p) ^{36}Cl$	36Cl	5.59	
$^{33}S(\alpha, \gamma)^{37}Ar$	³³ S	0.05	
$^{34}S(\alpha, \gamma)^{38}Ar$	³⁴ S	0.23	
$^{34}Cl(p, \gamma)^{35}Ar$	^{34}S	0.39	
$^{34}\text{Cl}(\alpha, p)^{37}\text{Ar}$	³⁴ S	0.26	
	³⁷ Ar	2.72	0.44
34 Ar(α , p) ³⁷ K	³⁴ S	0.42	
$^{35}Cl(\alpha, p)^{38}Ar$	³⁵ C1	0.36	
37 Ar(α , γ) ⁴¹ Ca	⁴¹ Ca	3.93	
38 K(α , <i>p</i>) 41 Ca	⁴¹ Ca	6.45	0.43
39 K(<i>p</i> , γ) 40 Ca	⁴⁰ Ca	2.28	
40 Ca(α , p) 43 Sc	⁴³ Ca	0.40	
	⁴³ Sc	0.40	
$^{42}Ca(p, \gamma) {}^{43}Sc$	⁴² Ca	0.29	
43 Sc(<i>p</i> , γ) 44 Ti	⁴⁴ Ti	2.99	
$^{46}\text{Ti}(\alpha, p)^{49}\text{V}$	⁴⁹ V	2.12	
$^{48}Cr(p,\gamma)$ ^{49}Mn	⁴⁹ V		3.27
49 Mn(<i>p</i> , γ) 50 Fe	⁴⁹ V		2.12
${}^{58}\text{Cu}(n, \gamma) {}^{59}\text{Zn}$	⁵⁸ Ni	6.90	0.38
${}^{60}Cu(p, \gamma) {}^{61}Zn$	⁶¹ Cu	3 59	0.39
${}^{61}Zn(p, \gamma) {}^{62}Ga$	⁶¹ Cu	0107	2.41
$^{62}Zn(p, \gamma)$ 63Ga	⁶² Zn	4 80	0.32
$\operatorname{En}(p, \gamma)$ Gumma	⁶³ Cu	0.33	0.52
$^{64}G_{2}(n, \gamma) ^{65}G_{2}$	657n	2 52	
$Ga(p, \gamma) = Gc$	657n	2.32	3.12
$65 \Lambda_{S}(p, \gamma) = 143$	64 7 n	0.43	5.12
$\operatorname{As}(p,\gamma)$ se	66Ca	0.43	•••
	67Ce	0.48	
660-() 67 A -	66C-	0.48	
$\operatorname{Ge}(p,\gamma)$ As	67 Ge		0.24
700 () 710	⁵⁷ Ga 71		5.62
$r_{1} \operatorname{Se}(p, \gamma)$ $r_{2} \operatorname{Br}$	71 AS		2.65
$^{73}\text{Se}(p, \gamma)$ ^{74}Br	''As	8.95	
$^{\prime 3}$ Kr(p, γ) $^{\prime *}$ Rb	⁷³ Se		2.16
$^{\prime}$ Kr(p, γ) $^{\prime}$ Rb	/4Se		0.33
94 95	^{/5} Br		4.28
$^{84}Zr(p, \gamma) {}^{85}Nb$	85Y	0.44	
$^{8/}$ Mo(p, γ) 88 Tc	⁸⁸ Zr	0.47	

TABLE 8 SAME AS TABLE 1, BUT FOR MODEL K04-B5

TABLE 8—Continued

Reaction	Isotope	10	0.1	300 (
$\frac{12}{12}C(\alpha, \gamma)^{16}O$	¹² C	0.26		$^{50}S(\alpha,$
	¹⁶ O	2.54		
	²⁰ Ne	2.44	0.18	
	²⁴ Mg	2.13	0.21	
	²⁸ Si		0.46	
$^{16}\text{O}(\alpha, \gamma)^{20}\text{Ne}$	¹⁶ O		7.66	
$^{20}\text{Ne}(\alpha, \gamma)^{24}\text{Mg.}$	²⁰ Ne		7.87	
$^{24}\text{Mg}(\alpha, \gamma)^{28}\text{Si}$	²⁴ Mg	0.20	3.38	
²³ Si(α , p) ² °P	³⁰ Si	2.12	0.39	
	36 A	0.39		
	³⁰ Ar 37 A r	0.40		
	47 T i	0.15	2.34	
	55Co		2.10	
	⁵⁶ Ni	0.37	2.00	
	⁵⁹ Ni	0.36	2.10	
	⁶⁵ Zn	2.21	2.15	
	⁶⁶ Ge	2.21		31 P(α ,
	⁶⁸ Ge	2.03		$^{32}S(\alpha,$
	⁶⁹ Ge	2.30		$^{33}S(\alpha,$
	⁷⁰ Ge	3.48		$^{34}Cl(\alpha$
	⁷¹ As	3.35	0.35	38 K(p
	⁷² Se	2.88	0.48	40Ca(a
	⁷³ Se	4.12		⁴² Ca(1
	⁷⁶ Kr	4.02	0.36	43 Sc(p
	⁸⁰ Sr	5.57		⁴⁶ Ti(<i>p</i>
${}^{28}\text{Si}(p, \gamma) {}^{29}\text{P}$	²⁹ Si	2.88		⁴⁶ V(<i>p</i>
28 Si(α , γ) 32 S	²⁸ Si	0.30	2.33	⁴⁸ Cr(<i>p</i>
	^{32}S		0.34	⁴⁹ Mn(
29 Si (p, γ) ³⁰ P	²⁹ Si	0.46		⁵² Fe(<i>p</i>
29 Si $(\alpha, \gamma)^{33}$ S	²⁹ Si		3.62	53Fe(p
29 P(α , p) 32 S	²⁹ Si		4.17	⁵⁵ Co(
$^{29}S(\alpha, p)$ $^{32}C1$	³² S	0.42		36Ni(0
	³⁶ Ar	0.41		
	³⁷ Ar	0.18		
	⁵⁰ Ni	0.38		
	⁵⁵ N1	0.34		
	⁶⁰ Ge	2.02		
	⁰⁹ Ge	2.02		
	71 • 0	2.64		
	72 S a	2.61		
	73 S e	2.45		
	⁷⁶ Kr	3.39	•••	
	⁸⁰ Sr	4 51		
$^{30}P(p, \gamma)^{31}S$	³⁰ Si	0.32		
(p,)) ~	³¹ P	2.11	0.35	
${}^{30}\mathrm{P}(\alpha, p) {}^{33}\mathrm{S}$	³⁰ Si	0.03	2.87	
	³³ S		0.28	
30 S(α , p) 33 Cl	^{32}S	0.09		57Cu()
	³³ S	0.20		
	³⁴ S	0.39		⁵⁹ Cu(1
	³⁵ Cl	0.26		
	³⁶ Ar	0.17	2.20	
	³⁷ Ar	0.05	3.72	
	³⁸ Ar	0.36	2.05	
	³⁹ K	0.36		
	⁴⁰ Ca	0.35		
	⁴² Ca	0.44	2.18	
	⁴³ Sc	0.41		
	⁴⁴ Ti	0.33		
	40Ti	0.38	2.65	
	4/Ti	0.37	2.63	
	4°Ti	0.37	2.65	
	⁵⁰ 1i	0.35	2.65	

Reaction	Isotope	10	0.1
30 S(α , <i>p</i>) 33 Cl	⁵¹ Ti	0.36	2.48
	⁵⁴ Fe	0.34	2.67
	⁵⁵ Co	0.33	2.63
	⁵⁶ Ni	0.23	
	⁵⁹ Ni	0.25	3.66
	⁶¹ Cu	2.15	
	⁶² Zn	2.43	
	⁶⁵ Zn	4.98	
	⁶⁶ Ge	5.83	
	⁶⁷ Ga	2.58	
	⁶⁸ Ge	3.01	
	⁶⁹ Ge	5.59	
	⁷⁰ Ge	11.80	
	71As	8.17	
	⁷² Se	5.36	
	⁷³ Se	14.32	
	^{/6} Kr	9.40	0.49
21- () 24-	⁸⁰ Sr	15.91	
$^{31}P(\alpha, p)$ ^{34}S	³¹ P	0.17	
$^{32}S(\alpha, \gamma)^{30}Ar$	³⁶ Ar	3.60	
$^{33}S(\alpha, \gamma)^{37}Ar$	³⁷ Ar	5.33	0.36
$^{34}Cl(\alpha, p)^{37}Ar$	³⁷ Ar	3.19	
$^{30}K(p, \gamma)$ ^{39}Ca	³⁸ Ar	0.44	
40 Ca(α , p) 43 Sc	42 G	0.48	
$^{42}Ca(p, \gamma)$ ^{43}Sc	⁴² Ca	0.35	
$^{45}Sc(p, \gamma) + 11$	47m;	4.48	0.29
$46 \chi(p, \gamma)^{47} V$	47T	2.65	
48 V(p, γ) (Cr	4957	2.41	
$49N_{rr}(p, \gamma) > 50 \Sigma_{rr}$	49 x 7	0.28	2.20
$52F_{2}(r_{1}, r_{2})$ $53C_{2}$	52E-		2.30
$53F_{2}(p, \gamma) = 0$	53N (2.52
$5^{3}C_{2}(p, \gamma) = 0$	53Mm		2.23
$56N_{1}(p, \gamma) = N_{1}$	3501	2.08	5.00
$\operatorname{NI}(\alpha, p)$	³⁶ A r	2.08	
	37 A r	2.74	
	46Ti	5.74 2.18	
	47 T i	2.18	
	48Cr	2.70	
	50Cr	2.30	
	51Cr	2.24	
	54 _{Ee}	2.18	
	55Co	2.29	
	⁵⁶ Ni	2.51	
	⁵⁹ Ni	4 43	
	⁶⁵ Zn	0.49	
	⁶⁹ Ge	0.45	
	⁷¹ As	0.32	
	⁷² Se	0.32	
	⁷⁶ Kr	0.31	
57 Cu(<i>p</i> , γ) 58 Zn	⁵⁶ Ni		2.85
	⁵⁹ Ni	2.04	
59 Cu(<i>p</i> , γ) 60 Zn	³⁵ Cl	2.0.	2.10
	³⁶ Ar		2.79
	³⁷ Ar		3.83
	⁴⁶ Ti		2.20
	⁴⁷ Ti		2.77
	⁴⁸ Cr		2.35
	⁵⁰ Cr		2.29
	⁵¹ Cr		2.21
	⁵⁴ Fe		2.32
	⁵⁵ Co		2.35
	⁵⁶ Ni		2.53
	⁵⁹ Ni		8.36
	⁶⁵ Zn		0.48
	⁶⁹ Ge		0.45

TABLE 8—Continued

Reaction	Isotope	10	0.1
59 Cu(<i>p</i> , γ) 60 Zn	⁷¹ As		0.30
	⁷² Se		0.42
	⁷⁶ Kr		0.30
61 Zn(<i>p</i> , γ) 62 Ga	⁶¹ Cu	0.25	3.37
	⁶² Zn		0.44
${}^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	⁶⁴ Zn		0.47
	⁶⁷ Ga		0.49
	⁶⁸ Ge		0.46
	⁶⁹ Ge		0.47
62 Ga(p, γ) 63 Ge	⁶² Zn	0.20	2.75
$^{63}\text{Ga}(p, \gamma)$ ^{64}Ge	⁶³ Cu		2.36
64 Ga(<i>p</i> , γ) 65 Ge	⁶⁵ Zn		0.50
$^{65}\text{Ge}(p, \gamma) ^{66}\text{As}$	⁶⁵ Zn	0.21	3.68
$^{65}\text{As}(p, \gamma) ^{66}\text{Se}$	⁶⁸ Ge	2.11	
	⁶⁹ Ge	2.10	
	⁷⁰ Ge	2.14	
	⁷¹ As	2.15	
	⁷² Se	2.69	
	⁷³ Se	2.63	
	⁷⁶ Kr	2.89	0.47
	⁸⁰ Sr	2.97	
${}^{66}As(p, \gamma) {}^{67}Se$	⁶⁶ Ge	0.29	2.13
${}^{67}\text{As}(p, \gamma) {}^{68}\text{Se}$	⁶⁷ Ga	0.48	2.78
69 Se (p, γ) 70 Br	⁶⁹ Ge		2.27
70 Se (p, γ) 71 Br	⁷⁰ Ge	2.91	,
	⁷¹ As	0.38	
71 Br(<i>p</i> , γ) 72 Kr	⁷⁰ Ge		2.36
	⁷¹ As	0.30	3.81
73 Kr(<i>p</i> , γ) 74 Rb	⁷³ Se		3.23

can be found in Iliadis (2007). Our main results, from individually varying each reaction rate by a factor of 10 (up and down), are summarized in Table 1.

Because of the moderate peak temperature achieved, the extent of the nuclear activity (defined as the heaviest isotope with $X_i > 10^{-2}$, in the final yields) reaches ⁹⁶Ru. The most abundant species (stable or with a half-life >1 hr) at the end of the burst are H (0.20, by mass), ⁴He (0.021), ⁶⁸Ge (0.20), ⁷²Se (0.13), 64 Zn (0.071), and 76 Kr (0.074). Qualitatively, this is in agreement with the results reported from Koike et al. (2004) (model 2, Table 8), in which the most abundant species, at the end of the burst, are also ⁶⁸Ge (0.17), ⁷²Se (0.14), ⁶⁴Zn (0.27), and ⁷⁶Kr (0.078). Note that the final mass fraction of 4 He reported by Koike et al. (2004), 0.011, is also comparable to the value reported in this paper. However, Koike's model is fully depleted of H (9.76 $\times 10^{-17}$, by mass), whereas some H remains at the end of our simulations. This could result from differences in the adopted nuclear reaction networks, as well as the hybrid use of evolutionary and postprocessing calculations in Koike et al. (2004). This discrepancy is of some importance as the presence of H in the ashes may induce marginal nuclear activity driving a second burst if the set of necessary conditions for a TNR are satisfied (for details see Woosley & Weaver 1984).

Our study reveals that the most influential reaction, by far, is the 3α , which affects a large number of species (⁴He, ¹⁸F, ²¹Ne, ^{24,25}Mg, ^{28–30}Si, ^{33,34}S, ^{36–38}Ar, ⁴¹Ca, ^{44,46,47}Ti, ⁴⁹V, ⁵⁰Cr, ⁵³Mn, ⁵⁴Fe, ^{57–59}Ni, ^{61,63}Cu, ⁶²Zn, ¹⁰²Pd, and ^{103,104}Ag), when its nominal rate is varied by a factor of 10, up and down. A similar result on the importance of the 3α reaction has been previously reported by Roberts et al. (2006), using a Monte Carlo approach. But, as discussed above, this uncertainty factor is far too large and, accordingly, this reaction has been removed from Tables 1–10.

TABLE 9 SAME AS TABLE 1, BUT FOR MODEL K04-B6

Reaction	Isotope	10	0.1
$^{15}O(\alpha, \gamma)^{19}Ne$	¹⁵ N		9.47
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$	¹⁵ N	0.42	
	¹⁸ F	0.41	
$^{22}Mg(p, \gamma)^{23}Al$	²² Na		3.14
23 Al (p, γ) ²⁴ Si	²² Na		5.61
$^{27}P(p, \gamma)$ ²⁸ S	²⁷ A1		4.73
20~ () 10~	²⁸ Si		0.48
$^{32}Ca(p, \gamma) + ^{40}Sc$	³³ K	•••	8.52
$^{5}V(p, \gamma)$	^{*2} Ca		2.65
5^{2} Fe (p, γ) 5^{3} Co	52Fe		8.62
$53C_{2}(p, \gamma) = N_{1}$	⁵³ Mp	•••	2.20
$56N_{1}(p, \gamma) = 1N_{1}$	56NI:	0.25	2.07
$N(p, \gamma) \subset U$	⁵⁵ Co	0.23	0.40
$Cu(p, \gamma)$ Zin	⁵⁷ Ni	0.30	2.86
$S^{58}Cu(p, \gamma) = 2n$	⁵⁸ Ni	0.57	2.00
59 Cu(<i>p</i> , γ) 60 Zn	⁵⁹ Ni		2.57
$^{61}Zn(p, \gamma)$ ^{62}Ga	⁶¹ Cu		3.74
$^{61}\text{Ga}(p, \gamma)$ ^{62}Ge	⁶⁰ Ni	0.16	5.05
	⁶¹ Cu	0.15	5.71
	⁶³ Cu		3.22
	⁶⁹ Ge		0.49
	⁷³ Se		0.43
	⁷⁴ Se		0.43
	⁷⁵ Br		0.43
	⁷⁶ Kr		0.47
	⁷⁷ Kr		0.40
	⁷⁸ Kr	•••	0.40
	⁷⁹ Kr		0.40
	⁸⁰ Sr		0.44
	°'Rb		0.39
	⁸² Sr	•••	0.40
	⁸³ Sr		0.40
	85V		0.41
	86 7 .	•••	0.41
	87 7 r		0.41
	$\frac{21}{88}$ Zr		0.40
	⁸⁹ Nb	•••	0.39
	⁹⁰ Mo		0.39
	⁹¹ Nb		0.39
	⁹² Mo		0.39
	⁹³ Tc		0.40
	⁹⁴ Mo		0.41
63 Ga(p, γ) 64 Ge	⁶³ Cu		4.97
$^{65}\text{Ge}(p, \gamma) ^{66}\text{As}$	⁶⁵ Zn	0.11	9.19
65 As (p, γ) 66 Se	⁸⁸ Zr	2.01	
	⁸⁹ Nb	2.06	
	⁹⁰ Mo	2.12	
	⁹¹ Nb	2.19	
	⁹² Mo	2.25	
	⁹³ Tc	2.27	
66 ~ () 67 .	⁹⁴ Mo	2.30	
$^{60}\text{Ge}(p, \gamma)$ ^{67}As	⁶⁶ Ge	0.39	6.27
$^{67}As(p, \gamma)$ ^{67}Se	⁶⁰ Ge	0.23	
$^{69}S_2(p, \gamma) \sim 5e$	69C a	0.28	7.20
$70S_2(p, q)$ $71P_r$	⁷⁰ Ce	0.10	/.08
$\operatorname{Sc}(p, \gamma) \stackrel{\text{DI}}{\longrightarrow} \operatorname{DI}$	⁷⁰ Go	0.39	0.29
$\operatorname{Br}(p, \gamma)$ KI	71 A c	0.39	6.88
73 Kr(p , γ) 74 Rb	⁷³ Se	0.10	6.83
74 Kr(<i>p</i> , γ) 75 Rb	⁷⁴ Se	0.22	6.80
75 Rb(p, γ) 76 Sr	⁷⁵ Br	0.13	5.73
77 Sr(<i>p</i> , γ) 78 Y	⁷⁷ Kr	0.13	4.46
78 Sr(<i>p</i> , γ) ⁷⁹ Y	⁷⁸ Kr	0.14	5.35
·* / //			

TABLE 9—Continued

Reaction	Isotope	10	0.1
79 Y(p, γ) 80 Zr	⁷⁹ Kr	0.12	4.53
80 Y(p, γ) 81 Zr	⁸¹ Rb		0.48
81 Zr(p, γ) 82 Nb	⁸¹ Rb	0.19	2.26
${}^{82}Zr(p, \gamma) {}^{83}Nb$	⁸² Sr	0.21	2.12
	⁸⁷ Zr		0.49
	⁸⁸ Zr		0.48
	⁸⁹ Nb		0.48
	⁹⁰ Mo		0.47
	⁹¹ Nb		0.47
	⁹² Mo		0.46
	⁹³ Tc		0.46
	⁹⁴ Mo		0.10
83 Zr(<i>n</i> \sim) 84 Nb	⁸³ Sr	0.49	0.15
$^{83}Nb(n \ \gamma) \ ^{84}Mo$	⁸³ Sr	0.45	
$^{84}Nb(p, \gamma) ^{85}Mo$	⁸⁴ Sr	0.20	
$\operatorname{NO}(p, \gamma)$ we	⁹² Mo	0.29	0.48
	⁹³ Te	•••	0.40
	94Mo		0.44
85 Nb(p, c) 86 Mo	85V	0.26	0.41
$NO(p, \gamma)$ MO	1 867.	0.30	
$\operatorname{MO}(p, \gamma)$ ic	91 NIL	0.57	0.47
	92N (-		0.47
	93T-	•••	0.43
	94 N (0.40
87. () 88.	87 -7		0.37
$^{\circ,}$ Mo(p, γ) $^{\circ\circ}$ Ic	^o ,Zr	0.34	
	92 ND		0.48
	⁹² Mo		0.45
	95 IC		0.43
89. r () 80m	^{>•} Mo		0.40
$^{\circ\circ}Mo(p, \gamma)$ $^{\circ\circ}Ic$	⁸⁸ Zr	0.37	
80	⁸⁹ Nb		0.50
89 Tc(p, γ) 90 Ru	⁸⁹ Nb	0.31	
91 Tc(<i>p</i> , γ) 92 Ru	⁹¹ Nb	0.42	
	⁹² Mo		0.46
91 Ru (p, γ) 92 Rh	⁹⁴ Mo		0.49
92 Ru(p, γ) 93 Rh	⁹² Mo	0.30	
	⁹³ Tc		0.27
	⁹⁴ Mo		0.32
93 Rh(<i>p</i> , γ) 94 Pd	⁹³ Tc	0.38	
94 Rh (p, γ) 95 Pd	⁹⁴ Mo	0.46	

Hereafter we drop from the discussion of the different models any additional comment on the importance of the 3α reaction, which, when arbitrarily varied by a factor of 10, systematically becomes the single most influential reaction of the whole network, for all 10 models. Indeed, additional tests performed with a more realistic uncertainty³ of $\pm 40\%$ (see Angulo et al. 1999) show no effect on any individual isotope, for any of the 10 models (the impact of nuclear uncertainties affecting the 3α rate on the total energy output will be specifically addressed in § 5).

From the several thousand nuclear processes, we find that only 56 reactions, as well as the corresponding reverse reactions, have an impact on the final yields when their rates are varied by a factor of 10 up and down for this model (see Table 1).⁴ Furthermore,

³ Note that, according to Tur et al. (2006), the 3α rate is known to ±12%. ⁴ It is worth noting that final yields depend somewhat on the specific choice of time (or, equivalently, temperature) at which calculations are stopped. This may be relevant for absolute determinations of yields, but certainly not for the identification of key nuclear reactions. As discussed previously, this manuscript focuses chiefly on reaction-rate variations that lead to relative abundance changes of (at least) a factor of 2. As we found differences in the final relative yields caused by different stopping times (corresponding to postburst temperatures down to 0.1 GK) to be typically 5%–10%, this issue has no significant effect on the conclusions of our studies here.

 TABLE 10

 Same as Table 1, but for Model K04-B7

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Reaction	Isotope	10	0.1
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{15}O(\alpha, \gamma)^{19}Ne$	¹⁵ N		7.89
	$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$	¹⁸ F	0.48	
	$^{31}\text{Cl}(p, \gamma)$ ^{32}Ar	³⁰ Si		2.17
	34 Ar(<i>p</i> , γ) 35 K	³⁴ S	0.37	2.14
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{47}Mn(p, \gamma)$ ⁴⁸ Fe	⁴⁶ Ti	•••	3.23
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{57}Cu(p, \gamma)$ ^{58}Zn	⁵⁷ Ni		2.12
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{61}\text{Ga}(p, \gamma)$ ^{62}Ge	⁶⁰ Ni	0.13	5.21
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	63 As (p, γ) 68 Se	⁶⁷ C	0.38	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{69}S_{2}(p, \gamma)$ $^{70}B_{p}$	⁶⁹ Ca		3.13
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	69 Br(p, γ) ⁷⁰ Kr	68Ge	0.10	9.00
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\operatorname{Di}(p,\gamma)$ Ki	⁶⁹ Ge	0.18	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		⁷⁰ Ge	0.19	
		⁷¹ As	0.18	
	70 Se(p, γ) 71 Br	⁷⁰ Ge		3.39
	70 Br(p, γ) 71 Kr	⁷⁰ Ge	0.17	2.06
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{71}\text{Br}(p,\gamma)$ ^{72}Kr	⁷¹ As	0.48	5.63
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	73 Kr(<i>p</i> , γ) 74 Rb	⁷³ Se	0.10	8.80
	74 Kr(<i>p</i> , γ) 75 Rb	⁷⁴ Se		5.35
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	74 Rb(p, γ) 75 Sr	⁷⁴ Se	0.25	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	75 Rb(p, γ) 76 Sr	⁷⁵ Br	0.31	6.68
$ \begin{split} & \begin{tabular}{lllllllllllllllllllllllllllllllllll$	77 Sr (p, γ) 78 Y	⁷⁷ Kr	0.11	7.48
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	78 Sr (p, γ) 79 Y	⁷⁸ Kr	0.27	6.46
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	78 Y(p, γ) 79 Zr	⁷⁸ Kr	0.46	
	$^{\prime9}$ Y(p, γ) 80 Zr	^{/9} Kr	0.13	7.26
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$^{81}Zr(p, \gamma)$ ^{82}Nb	⁸¹ Rb	0.12	4.97
	$^{62}Zr(p, \gamma) ^{63}Nb$	⁶² Sr 83Sr	0.14	4.15
	84 Nb(p, γ) 85 Mo	⁸³ Sr	0.17	2.70
	$^{85}Mo(p, \gamma) = ^{86}Tc$	85V	0.14	3.32
	$^{86}Mo(p, \gamma)$ ⁸⁷ Tc	⁸⁶ 7r	0.27	3.01
	$^{87}Mo(p, \gamma)$ ⁸⁸ Tc	⁸⁷ Zr	0.17	5.01
	87 Tc(<i>p</i> , γ) ⁸⁸ Ru	⁸⁷ Zr	0.42	
	${}^{88}\text{Tc}(p, \gamma) {}^{89}\text{Ru}$	⁸⁸ Zr	0.30	2.44
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$^{89}\text{Tc}(p, \gamma)^{90}\text{Ru}$	⁸⁹ Nb	0.28	2.34
	90 Ru(<i>p</i> , γ) 91 Rh	⁹⁰ Mo	0.25	2.46
	91 Ru(<i>p</i> , γ) 92 Rh	⁹¹ Nb	0.32	
	92 Ru(<i>p</i> , γ) 93 Rh	⁹² Mo	0.40	
	92 Rh (p, γ) 93 Pd	⁹² Mo	0.45	
	93 Rh (p, γ) 94 Pd	⁹³ Tc	0.21	2.41
	94 Pd(p, γ) 95 Ag	⁹⁴ Mo	0.35	
	95 Pd(p, γ) 90 Ag	⁹⁵ Ru	0.26	2.11
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\operatorname{Ag}(p, \gamma)$ Cd	⁹⁰ Ru 97D	0.39	2.41
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		⁹⁸ Ru	•••	0.46
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$97 \text{ Ag}(p, q) \frac{98}{2} \text{ Cd}$	97 R 1	0.25	0.47
$ \begin{array}{c} \operatorname{Rd}(p,\gamma) \stackrel{\text{minimum}}{\operatorname{minimum}} & \operatorname{Rd} & 0.47 & \dots \\ \operatorname{Rd}(p,\gamma) \stackrel{\text{97}}{\operatorname{SR}}(q,\gamma) \stackrel{\text{97}}{\operatorname{Cd}} \dots & \stackrel{\text{98}}{\operatorname{Ru}} & 0.49 & \dots \\ \operatorname{98}\operatorname{Rd}(p,\gamma) \stackrel{\text{99}}{\operatorname{In}} \dots & \stackrel{\text{98}}{\operatorname{Ru}} & 0.32 & \dots \\ \operatorname{99}\operatorname{Cd}(p,\gamma) \stackrel{\text{101}}{\operatorname{In}} \dots & \stackrel{\text{99}}{\operatorname{Rh}} & 0.27 & 2.10 \\ \operatorname{100}\operatorname{Cd}(p,\gamma) \stackrel{\text{101}}{\operatorname{In}} \dots & \stackrel{\text{100}}{\operatorname{Pd}} & 0.43 & \dots \\ \operatorname{100}\operatorname{In}(p,\gamma) \stackrel{\text{101}}{\operatorname{Sn}} \dots & \stackrel{\text{100}}{\operatorname{Pd}} & 0.41 & \dots \\ \operatorname{101}\operatorname{In}(p,\gamma) \stackrel{\text{102}}{\operatorname{Sn}} \dots & \stackrel{\text{101}}{\operatorname{Pd}} & 0.27 & \dots \\ \operatorname{102}\operatorname{In}(p,\gamma) \stackrel{\text{103}}{\operatorname{Sn}} \dots & \stackrel{\text{102}}{\operatorname{Pd}} & 0.32 & \dots \\ \operatorname{103}\operatorname{Ag} & \dots & 0.45 \\ \operatorname{103}\operatorname{In}(p,\gamma) \stackrel{\text{104}}{\operatorname{Sn}} \dots & \stackrel{\text{103}}{\operatorname{Rg}} & 0.45 & \dots \\ \operatorname{104}\operatorname{Ag} & 2.01 & 0.28 \\ \operatorname{105}\operatorname{Ag} & \dots & 0.43 \\ \operatorname{106}\operatorname{Cd} & \dots & 0.24 \\ \operatorname{105}\operatorname{Sn}(p,\gamma) \stackrel{\text{106}}{\operatorname{Sb}} \dots & \stackrel{\text{105}}{\operatorname{Ag}} & 0.43 & \dots \\ \operatorname{106}\operatorname{Cd} & 2.16 & 0.31 \\ \end{array} $	$^{97}Cd(n, \gamma)$ Cd	⁹⁷ Ru	0.23	2.30
	${}^{98}Ag(p, \gamma) {}^{99}Cd$	⁹⁸ Ru	0.49	
	${}^{98}Cd(p, \gamma) {}^{99}In$	⁹⁸ Ru	0.42	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	99 Cd (p, γ) ¹⁰⁰ In	⁹⁹ Rh	0.27	2.10
	$^{100}Cd(p, \gamma)$ ^{101}In	¹⁰⁰ Pd	0.43	
	100 In (p, γ) 101 Sn	¹⁰⁰ Pd	0.41	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	101 In (p, γ) 102 Sn	¹⁰¹ Pd	0.27	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	102 In(p, γ) 103 Sn	¹⁰² Pd	0.32	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		¹⁰³ Ag		0.45
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	103 In (p, γ) 104 Sn	¹⁰³ Ag	0.45	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		¹⁰⁴ Ag	2.01	0.28
$\stackrel{105}{=} \text{In}(p, \gamma) \stackrel{105}{=} \text{Sn} \dots \stackrel{105}{=} \text{Ag} \qquad 3.03 \qquad 0.20 \\ \stackrel{106}{=} \text{Cd} \qquad \dots \qquad 0.24 \\ \stackrel{105}{=} \text{Sn}(p, \gamma) \stackrel{106}{=} \text{Sb} \dots \stackrel{105}{=} \text{Ag} \qquad 0.43 \qquad \dots \\ \stackrel{106}{=} \text{Cd} \qquad 2.16 \qquad 0.31 \\ \stackrel{106}{=} \text{Cd} \qquad 2.16 \qquad 0.31 \\ \stackrel{106}{=} \text{Cd} \qquad 0.43 \qquad \dots \\ \stackrel{106}{=} \text{Cd} \qquad 0.44 \qquad \dots \\ \stackrel{106}{=} $	1047	¹⁰⁵ Ag		0.43
$ \begin{array}{cccc} & & & & & & & & & & & & & & & & & $	$\ln(p, \gamma) \sin n$	¹⁰⁵ Ag	3.03	0.20
^{105}Ag 0.43 ^{106}Cd 2.16 0.31	1059(100Cd		0.24
Ca 2.16 0.31	$\operatorname{sn}(p, \gamma) \longrightarrow \operatorname{sb}(p)$	106 Ag	0.43	
		Cu	2.10	0.31

TABLE 11 Important β -Decay (and β -delayed Proton Decay) Rates, as Found in Our 10 Models

Model	Reaction
Model K04	
Model F08	$ \begin{array}{c} {}^{26}{\rm Si}(\beta^+){}^{26m}{\rm Al} \\ {}^{29}{\rm S}(\beta^+){}^{29}{\rm P} \\ {}^{29}{\rm S}(\beta^+,p){}^{28}{\rm Si} \\ {}^{30}{\rm S}(\beta^+){}^{30}{\rm p} \\ {}^{33}{\rm Ar}(\beta^+){}^{32}{\rm Si} \\ {}^{33}{\rm Ar}(\beta^+,p){}^{32}{\rm Si} \\ {}^{34}{\rm Ar}(\beta^+){}^{34}{\rm Cl} \\ {}^{37}{\rm Ca}(\beta^+){}^{37}{\rm K} \\ {}^{37}{\rm Ca}(\beta^+,p){}^{36}{\rm Ar} \\ {}^{38}{\rm Ca}(\beta^+){}^{38}{\rm K} \\ {}^{60}{\rm Zn}(\beta^+){}^{60}{\rm Cu} \\ {}^{68}{\rm Se}(\beta^+){}^{68}{\rm As} \\ {}^{72}{\rm Kr}(\beta^+){}^{76}{\rm Rb} \\ {}^{80}{\rm Zr}(\beta^+){}^{80}{\rm Y} \end{array} $
Model S01	
Model K04-B1	$\begin{array}{c} {}^{25}\mathrm{Si}(\beta^+)^{25}\mathrm{Al} \\ {}^{25}\mathrm{Si}(\beta^+,p)^{24}\mathrm{Mg} \\ {}^{33}\mathrm{Ar}(\beta^+)^{33}\mathrm{Cl} \\ {}^{33}\mathrm{Ar}(\beta^+,p)^{32}\mathrm{S} \\ {}^{36}\mathrm{Ca}(\beta^+,p)^{35}\mathrm{Ar} \\ {}^{36}\mathrm{Ca}(\beta^+,p)^{36}\mathrm{K} \\ {}^{37}\mathrm{Ca}(\beta^+,p)^{36}\mathrm{K} \\ {}^{37}\mathrm{Ca}(\beta^+,p)^{36}\mathrm{Ar} \\ {}^{38}\mathrm{Ca}(\beta^+)^{38}\mathrm{K} \\ {}^{41}\mathrm{Ti}(\beta^+)^{41}\mathrm{Sc} \\ {}^{41}\mathrm{Ti}(\beta^+,p)^{40}\mathrm{Ca} \\ {}^{59}\mathrm{Zn}(\beta^+)^{59}\mathrm{Cu} \\ {}^{62}\mathrm{Ge}(\beta^+)^{62}\mathrm{Ga} \\ {}^{63}\mathrm{Ge}(\beta^+)^{63}\mathrm{Ga} \\ {}^{64}\mathrm{Ge}(\beta^+)^{64}\mathrm{Ga} \\ {}^{68}\mathrm{Se}(\beta^+)^{68}\mathrm{As} \end{array}$
Model K04-B2	$\begin{array}{c} {}^{25}{\rm Si}(\beta^+)^{25}{\rm Al}\\ {}^{25}{\rm Si}(\beta^+,p)^{24}{\rm Mg}\\ {}^{68}{\rm Se}(\beta^+)^{68}{\rm As}\\ {}^{72}{\rm Kr}(\beta^+)^{76}{\rm Bt}\\ {}^{80}{\rm Zr}(\beta^+)^{76}{\rm Rb}\\ {}^{80}{\rm Zr}(\beta^+)^{80}{\rm Y}\\ {}^{92}{\rm Pd}(\beta^+)^{92}{\rm Rh}\\ {}^{94}{\rm Pd}(\beta^+)^{94}{\rm Rh}\\ {}^{101}{\rm Sn}(\beta^+)^{101}{\rm In}\\ {}^{102}{\rm Sn}(\beta^+)^{102}{\rm In}\\ {}^{103}{\rm Sn}(\beta^+)^{104}{\rm In}\\ \end{array}$

TABLE 11—Continued

Model	Reaction
Model K04-B3	${}^{68}Se(\beta^+){}^{68}As$ ${}^{72}Kr(\beta^+){}^{72}Br$ ${}^{76}Sr(\beta^+){}^{76}Rb$ ${}^{80}Zr(\beta^+){}^{80}Y$ ${}^{88}Ru(\beta^+){}^{88}Tc$ ${}^{92}Pd(\beta^+){}^{92}Rh$ ${}^{99}In(\beta^+){}^{99}Cd$
Model K04-B4	
Model K04-B5	
Model K04-B6	${}^{18}\text{Ne}(\beta^+){}^{18}\text{F} \\ {}^{64}\text{Ge}(\beta^+){}^{64}\text{Ga} \\ {}^{68}\text{Se}(\beta^+){}^{68}\text{As} \\ {}^{72}\text{Kr}(\beta^+){}^{72}\text{Br} \\ {}^{76}\text{Sr}(\beta^+){}^{76}\text{Rb} \\ {}^{80}\text{Zr}(\beta^+){}^{80}\text{Y} $
Model K04-B7	

TABLE 12

List of Reactions Selected for the Q-Value Variation Study, Restricted to Proton-Capture Reactions on A < 80 Nuclei, with |Q| < 1 MeV, and a Q-Value Uncertainty >50 keV (See Audi et al. 2003b and \S 3)

	Q-Value ^a	Uncertainty
Reaction	(keV)	(keV)
$\frac{1}{2^{1}}$ Mg(<i>p</i> , γ) ²² Al	17	95
$^{24}\text{Si}(p, \gamma)^{25}\text{P}$	-828	197
$^{25}\text{Si}(p, \gamma)^{26}\text{P}$	140	196
$^{25}P(p, \gamma)^{26}S$	191	357
$^{26}P(p, \gamma)^{27}S$	719	281
$^{29}S(p, \gamma)^{30}Cl$	-314	202
${}^{30}S(p, \gamma){}^{31}Cl^{b}$	294	50
${}^{30}\text{Cl}(p, \gamma){}^{31}\text{Ar}$	439	284
$^{33}\text{Ar}(p, \gamma)^{34}\text{K}$	-614	298
$^{41}\text{Ti}(p, \gamma)^{42}\text{V}$	-242	220
$^{42}\text{Ti}(p,\gamma)^{43}\text{V}$	192	233
$^{45}Cr(p, \gamma)^{46}Mn$	694	515
${}^{46}{ m Cr}(p, \gamma){}^{47}{ m Mn}$	78	160
49 Fe(<i>p</i> , γ) ⁵⁰ Co	-98	224
50 Fe(<i>p</i> , γ) 51 Co	88	161
${}^{51}\text{Fe}(p, \gamma){}^{52}\text{Co}$	982	67
54 Ni $(p, \gamma)^{55}$ Cu	-298	302
$^{55}Ni(p, \gamma)^{56}Cu$	555	140
58 Zn (p, γ) 59 Ga	-888	175
59 Zn $(p, \gamma)^{60}$ Ga	27	118
${}^{59}\text{Ga}(p, \gamma){}^{60}\text{Ge}$	936	287
60 Zn $(p, \gamma){}^{61}$ Ga ^b	192	54
${}^{63}\text{Ge}(p, \gamma){}^{64}\text{As}$	-100	300
${}^{64}\text{Ge}(p, \gamma){}^{65}\text{As}$	-80	300
67 Se $(p, \gamma)^{68}$ Br	-560	300
68 Se(<i>p</i> , γ) 69 Br	-450	100
72 Kr(<i>p</i> , γ) ⁷³ Rb	-600	150
75 Sr(<i>p</i> , γ) ⁷⁶ Y	-629	549
76 Sr(<i>p</i> , γ) ⁷⁷ Y	-50	50
76 Y(<i>p</i> , γ) ⁷⁷ Zr ^c	802	400
80 Zr(<i>p</i> , γ) ⁸¹ Nb	-750	150

^a All *Q*-values and errors are from Audi et al. (2003b), except where indicated. They have been estimated in that work from systematic trends. ^b Reactions with experimental *Q*-values and errors in Audi et al. (2003b).

 $^{\rm c}$ *Q*-value as used in the Hauser-Feshbach calculation for this rate in our network. No *Q*-value was estimated in Audi et al. (2003b) for this reaction. The associated uncertainty was assumed to be 400 keV.

our study reveals that the impact of most of these reactions is restricted to the vicinity of the target nuclei. A clear example is ¹⁵O(α , γ): when its nominal rate is multiplied by a factor of 0.1, only one isotope, ¹⁵N, is modified by more than a factor of 2 (as compared with the mass fraction obtained with the recommended rate; but see also § 5). Indeed, the most influential reaction is by far ⁶⁵As(p, γ), perhaps expected due to its bridging effect on the ⁶⁴Ge waiting point. To a lesser extent, ⁹⁶Ag(p, γ) and ¹⁰²In(p, γ) also show an impact on a number of nuclear species.

The most important β -decay rates identified in this model are those of ⁶⁴Ge, ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, ⁸⁰Zr, ⁸⁸Ru, ⁹²Pd, and ⁹⁹In (see Table 11). But it is important to stress that additional calculations, in which these (laboratory) β -decay rates were varied within realistic uncertainties (half-lives varied by roughly ±30%), have revealed no effect on any single isotope (see Woosley et al. [2004] for a sensitivity study based on variations of groups of weak rates, including all positron emission rates for nuclei heavier than ⁵⁶Ni, by an order of magnitude).

From the list of nuclear reactions selected for the Q-value variation study (see Table 12 and the discussion in § 3), only

TABLE 13 FINAL ABUNDANCE RATIOS, $X_i/X_{i,std}$, for Model K04 (Koike et al. 2004), Resulting from Variations on *Q*-Values (See Table 12 and Text)

Reaction	Isotope	High- $Q (Q + \Delta Q)$	Low- $Q(Q - \Delta Q)$
26 P(<i>p</i> , γ) 27 S	²⁵ Mg	0.35	
${}^{46}Cr(p, \gamma) {}^{47}Mn$	⁴⁶ Ti	0.23	
${}^{55}\text{Ni}(p, \gamma) {}^{56}\text{Cu}$	⁵⁵ Co		3.95
60 Zn(<i>p</i> , γ) 61 Ga	⁶⁰ Ni	0.47	
${}^{64}\text{Ge}(p, \gamma) {}^{65}\text{As}$	⁶⁴ Zn	0.08	4.13
	⁶⁵ Zn		3.04
	⁶⁶ Ge		3.05
	⁶⁷ Ga		3.65
	⁷³ Se		0.49
	⁷⁴ Se		0.50
	⁷⁷ Kr		0.42
	⁷⁸ Kr		0.42
	⁷⁹ Kr		0.42
	⁸⁰ Sr		0.47
	⁸¹ Rb		0.40
	⁸² Sr		0.41
	⁸³ Sr		0.42
	⁸⁴ Sr		0.42
	⁸⁵ Y		0.42
	⁸⁶ Zr		0.40
	⁸⁷ Zr		0.39
	⁸⁸ Zr		0.38
	⁸⁹ Nb		0.38
	⁹⁰ Mo		0.37
	⁹¹ Nb		0.36
	⁹² Mo		0.36
	⁹³ Tc		0.36
	⁹⁴ Mo		0.35
	⁹⁵ Ru		0.34
	⁹⁶ Ru		0.33
	⁹⁷ Ru		0.31
	⁹⁸ Ru		0.30
	99Rh		0.29
	¹⁰⁰ Pd		0.30
	¹⁰¹ Pd		0.29
	¹⁰² Pd		0.29
	¹⁰³ Ag		0.30
	¹⁰⁴ Ag		0.32
	8		

²⁶P(p, γ)²⁷S, ⁴⁶Cr(p, γ)⁴⁷Mn, ⁵⁵Ni(p, γ)⁵⁶Cu, ⁶⁰Zn(p, γ)⁶¹Ga, and ⁶⁴Ge(p, γ)⁶⁵As show some impact on the final yields when their *Q*-values are varied between 1 σ uncertainty bounds. However, as summarized in Table 13, the effects are restricted to single isotopes, except for the last reaction, ⁶⁴Ge(p, γ), whose influence ranges between ⁶⁴Zn and ¹⁰⁴Ag. Indeed, the significance of this reaction on the ⁶⁴Ge waiting point is well known (see, e.g., Woosley et al. 2004; Thielemann et al. 2001; Schatz 2006; Fisker et al. 2008 and references therein). Mass measurements on ⁶⁴Ge have indeed been performed (Clark et al. 2007; Schury et al. 2007). When combining these measurements with the ⁶⁵As mass value given by Audi et al. (2003b), the corresponding 1 σ uncertainty limits in the ⁶⁴Ge(p, γ)⁶⁵As *Q*-value ($-74 \pm$ 303 and -46 ± 302 keV, respectively) are well covered by the range used in our study ($Q = -80 \pm 300$ keV; Audi et al. 2003b).

TABLE 14 Same as Table 13, but for Model F08

Reaction	Isotope	High- $Q (Q + \Delta Q)$	Low- $Q(Q - \Delta Q)$
45 Cr(p , γ) 46 Mn	⁴⁵ Ti	0.50	

Clearly, mass measurements on 65 As are still required to better determine this *Q*-value. These are challenging experiments because of the difficulty of producing 65 As (J. A. Clark 2007, private communication).

3.1.2. Model S01

Here we summarize the main results obtained from our postprocessing calculations with the temperature versus time profile extracted from the one-zone model of Schatz et al. (2001) (model S01).

Because of the larger peak temperature achieved in this model, the main nuclear activity extends to heavier nuclei (¹⁰⁷Cd, for $X > 10^{-2}$) than in model K04. The most abundant species (stable or with a half-life >1 hr) at the end of the burst are now H (0.071, by mass), ⁴He (0.013), and the heavy isotopes 104 Ag (0.328), ¹⁰⁶Cd (0.244), ¹⁰³Ag (0.078), and ¹⁰⁵Ag (0.085). This chemical pattern bears some resemblance to that reported by Schatz et al. (2001) and also to a similar model (zM) computed by Woosley et al. (2004) with a 1D hydrodynamic code. For example, a large overproduction of the *p*-nucleus ¹⁰⁶Cd is explicitly mentioned in Schatz et al. (2001, Fig. 4); as well, Woosley et al. (2004, Fig. 7) find a large mass fraction of ¹⁰⁶Sn (which will decay into ¹⁰⁶Cd), followed by 64Ge, 68Se, 104In (which will decay into 104Ag), 4He, and H. It is worth noting that the final amount of H is much smaller than in model K04: here H and He are almost depleted and hence the next burst will necessarily require the piling up of fresh H/He-rich fuel on top of this H/He-depleted shell.

Only 64 reactions (and the corresponding reverse processes) from the overall nuclear network turn out to have an impact on the final yields when their rates are varied by a factor of 10 up and down (Table 2). As reported for model K04, the influence of these reactions is often limited to the vicinity of the target nuclei. Remarkable exceptions are ⁵⁶Ni(α , p), ⁵⁹Cu(p, γ), and to a lesser extent ¹⁰³Sn(α , p). Notice also that, among the most important reactions, only three α -captures [¹⁵O(α , γ), ⁵⁶Ni(α , p), and ¹⁰³Sn(α , p)] are found. The role played by ¹⁵O(α , γ) is as marginal as for model K04, however (but see discussion in § 5).

Concerning the most influential β -decay rates, we found similarities with the results reported for model K04. Hence, the β -decay rates of ⁶⁸Se, ⁷²Kr, ⁸⁰Zr, ⁸⁸Ru, and ⁹²Pd are important, but due to the higher peak temperatures reached in this model, the list also extends to heavier species, including ^{101–106}Sn and ¹⁰⁶Sb (see Table 11). Additional studies of the specific impact of these decays with realistic uncertainty bounds (Audi et al. 2003a) have also been performed for this case, revealing no effect on any particular isotope.

3.1.3. Model F08

Since this model achieves the lowest peak temperature of the three models extracted from the literature, its main nuclear path is somewhat more limited, reaching only $(X > 10^{-2})^{72}$ Se: the most abundant species (stable or with a half-life >1 hr) at the end of the burst are now ⁴He (0.085), ⁵⁶Ni (0.13), ⁶⁰Ni (0.38), ¹²C (0.040), ²⁸Si (0.041), and ⁶⁴Zn (0.034). Moreover, H has been depleted down to 10^{-11} by mass. Qualitatively, there is good agreement with the relevant chemical pattern reported in Fisker et al. (2008, Fig. 20). It is worth noting that the large amount of ¹²C obtained at the end of the burst may have implications for the energy source that powers superbursts (see § 1).

Again, only a few reactions (62 and the corresponding reverse reactions) have an impact on the final yields when their rates are varied by a factor of 10 up and down (Table 3). The most influential reactions are ${}^{12}C(\alpha, \gamma)$, ${}^{26g}Al(\alpha, p)$, ${}^{57}Cu(p, \gamma)$, ${}^{61}Ga(p, \gamma)$,

and ^{85,86}Mo(p, γ). Additional discussion and tests on the impact of the ¹²C(α, γ) rate are presented in § 5. Thirteen *alpha*-capture reactions show some impact on the yields, a larger number than in K04 and S01. Indeed, all key reactions affecting A < 30 species are mainly (α, γ) or (α, p) reactions. It is worth mentioning, however, that ¹⁵O(α, γ) is absent from this list (see § 5).

The most influential β -decay rates are now shifted toward lighter unstable isotopes because of the lower T_{peak} value achieved. These include decays of 26,29 Si, 29,30 S, 33,34 Ar, 37,38 Ca, 60 Zn, 68 Se, 72 Kr, 76 Sr, and 80 Zr (Table 11). As in K04 and S01, however, no effect is seen on any isotope when realistic uncertainties are adopted for these decay rates.

Finally, the only nuclear reaction from Table 12 that has a significant impact on the final yields when its *Q*-value is varied between 1 σ uncertainty bounds is ⁴⁵Cr(*p*, γ) (see Table 14).

3.1.4. Effect of the Duration of the Burst: Model K04-B1 versus K04-B2

Because of the shorter duration of model K04-B1, as compared with model K04, the main nuclear path extends up to 68 Ge. In contrast, the longer burst of model K04-B2 drives the main path up to 106 Cd.

The most abundant species at the end of the bursts are H (0.42, by mass), ⁴He (0.061), ⁶⁰Ni (0.10), ⁶⁴Zn (0.31), and ⁶⁸Ge (0.023), for the shorter burst of model K04-B1; and ⁴He (0.0051), ⁶⁸Ge (0.159), ⁷²Se (0.121), ⁷⁶Kr (0.077), ⁸⁰Sr (0.040), ⁹⁰Mo (0.042), ⁹⁴Mo (0.055), ⁹⁸Ru (0.040), ¹⁰²Pd (0.034), ¹⁰³Ag (0.060), ¹⁰⁴Ag (0.097), and ¹⁰⁵Ag (0.042), for model K04-B2. The final amount of H in the latter model has decreased down to 10^{-15} . The larger extension of the main nuclear activity reported for model K04-B2 is a direct consequence of the longer exposure times to higher temperatures. However, the depletion of H results from the complex interplay between exposure time to high temperatures, which decreases the overall H content, and the effects of photodisintegrations, which raise the H abundance.

Concerning nuclear uncertainties, model K04-B1 is characterized by 28 critical reactions, the most important ones being ${}^{61}\text{Ga}(p, \gamma)$ and ${}^{65}\text{As}(p, \gamma)$, with a marginal role played by ${}^{18}\text{Ne}(\alpha, p)$ and ${}^{31}\text{Cl}(p, \gamma)$ (Table 4). For model K04-B2, with 51 critical reactions, the most important are ${}^{65}\text{As}(p, \gamma)$ and ${}^{32}\text{S}(\alpha, \gamma)$, followed, to some extent, by ${}^{12}\text{C}(\alpha, \gamma)$, ${}^{61}\text{Ga}(p, \gamma)$, ${}^{75}\text{Rb}(p, \gamma)$, ${}^{84}\text{Zr}(p, \gamma)$, ${}^{92}\text{Ru}(p, \gamma)$, ${}^{93}\text{Rh}(p, \gamma)$, and ${}^{96}\text{Ag}(p, \gamma)$ (Table 5). Only two α -capture reactions appear to be influential in model K04-B1 [one being ${}^{15}\text{O}(\alpha, \gamma)$; see Table 4], whereas uncertainties affecting 12 α -capture reactions turn out to be critical for model K04-B2 (see Table 5).

Table 11 lists the most important β -decay rates for these models, when these rates are varied by a factor of 10 up and down. In summary, β -decay rates of ²⁵Si, ³³Ar, ^{36–38}Ca, ⁴¹Ti, ⁵⁹Zn, ^{62–64}Ge, and ⁶⁸Se become critical in model K04-B1, whereas those of ²⁵Si, ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, ⁸⁰Zr, ^{92,94}Pd, and ^{101–104}Sn play a major role in model K04-B2. As before, no noticeable effect remains when realistic uncertainties are adopted for these rates.

3.1.5. Effect of the Initial Metallicity: Models K04-B3, K04-B4, and K04-B5

In the low-metallicity model K04-B3, the main nuclear path $(X > 10^{-2})$ stops at ⁹⁶Ru. In contrast, the higher metallicity models K04-B4 and K04-B5 reach ⁶⁸Ge and ⁷²Se, respectively. The most abundant species at the end of the bursts are H (0.194), ⁴He (0.021), ⁶⁸Ge (0.205), ⁷²Se (0.132), ⁶⁴Zn (0.075), ⁷⁶Kr (0.073), ⁸⁰Sr (0.041), and ⁸²Sr (0.023), for model K04-B3; ⁴He (0.018), ⁶⁰Ni (0.696), ⁶⁴Zn (0.161), ⁵⁶Ni (0.051), ³²S (0.014), and ⁶⁸Ge (0.016), for model K04-B4; and finally, ⁴He (0.018),





FIG. 2.— Time evolution of the hydrogen mass fraction in models K04-B6 (low *T*) and K04-B7 (high *T*). Models are based on Koike et al. (2004) (see text for details). Value t = 0 corresponds to the time at which T_{peak} is reached.

⁵⁶Ni (0.273), ⁶⁰Ni (0.256), ³⁹K (0.057), ⁶⁴Zn (0.062), and ⁶⁸Ge (0.041), for model K04-B5. Note that H has been seriously depleted in both high-metallicity models, achieving mass fractions of 4×10^{-14} and 10^{-15} , respectively.

Concerning nuclear uncertainties, model K04-B3 is characterized by 56 critical reactions, while models K04-B4 and K04-B5 have 43 and 45, respectively. The most important ones for model K04-B3 (Table 6) are ⁶⁵As(p, γ) and ⁹⁶Ag(p, γ), with a marginal role played by ^{102,103}In(p, γ). For model K04-B4 (Table 7), the most influential reactions are ¹²C(α , γ), ³⁰S(α , p), and to some extent, ³⁰P(α , p) and ⁶⁵As(p, γ). Finally, for model K04-B5 (Table 8), the key reactions are ³⁰S(α , p), ²⁵Si(α , p), ⁵⁹Cu(p, γ), ⁵⁶Ni(α , p), ²⁹S(α , p), ⁶⁵As(p, γ), ¹²C(α , γ), and to some extent, ⁶¹Ga(p, γ). Note that ¹⁵O(α , γ) is only important for model K04-B3. The number of influential α -induced reactions seems to increase with metallicity: only two reactions of this type are important for models K04 and K04-B3, whereas 22 and 17 are important for models K04-B4 and K04-B5, respectively.

Finally, the most influential β -decays from model K04-B3 are ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, ⁸⁰Zr, ⁸⁸Ru, ⁹²Pd, and ⁹⁹In. Model K04-B4 is characterized by the importance of the β -decays of ^{33,34}Ar, ³⁷⁻³⁹Ca, ⁴²Ti, ⁴⁶Cr, ⁴⁹Fe, ⁵⁵Ni, ⁵⁸Zn, ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, and ⁸⁰Zr, whereas for model K04-B5, the β -decay rates of ²¹Mg, ^{24,25}Si, ²⁸⁻³⁰S, ^{33,34}Ar, ^{37,38}Ca, ⁶⁴Ge, and ⁶⁸Se are the most important (see Table 11). Again, no effect shows up when realistic (ground state) uncertainties are adopted for these rates.

3.1.6. Effect of the Peak Temperature: Model K04-B6 versus K04-B7

In model K04, the main nuclear path $(X > 10^{-2})$ reached ⁹⁶Ru. Because of the lower peak temperature achieved in model K04-B6, the main nuclear path reaches ⁸²Sr. In contrast, the higher temperatures achieved in model K04-B7 drive the main path up to ¹⁰³Ag.

The most abundant species at the end of the burst are now H (0.151), ⁴He (0.034), ⁶⁴Zn (0.375), ⁶⁸Ge (0.193), ⁶⁰Ni (0.051), ⁷²Se (0.074), ⁷⁶Kr (0.031), ⁸⁰Sr (0.015), and ⁸²Sr (0.011), for the lower peak temperature model K04-B6 (Table 9); and H (0.460), ⁴He (0.013), ⁶⁸Ge (0.058), ⁷²Se (0.069), ⁷⁶Kr (0.048), ⁸⁰Sr (0.031), and ⁹⁶Ru (0.026), for model K04-B7 (Table 10). It is worth noting that model K04-B7 ends with a larger amount of hydrogen than K04-B6 as a result of the major role played by photodisintegration reactions when the temperature exceeds ~2 GK. This is illustrated in Figure 2, where the time evolution of the hydrogen mass fraction is plotted for the two models K04-B6 (low *T*) and K04-B7 (high *T*). Indeed, the *bump* exhibited by model K04-B7 during the 20 s after *T*_{peak} (that is, when the temperature ranges between 1.5 and 2.5 GK) is caused by the protons released through

 (γ, p) reactions on a number of nuclear species. Hence, the final hydrogen mass fraction may provide a diagnostic of the peak temperature achieved during the explosion (for bursts of similar duration).

Concerning nuclear uncertainties, model K04-B6 is characterized by 49 critical reactions, the most important ones being ${}^{61}\text{Ga}(p,\gamma)$, ${}^{82}\text{Zr}(p,\gamma)$, ${}^{65}\text{As}(p,\gamma)$, ${}^{86,87}\text{Mo}(p,\gamma)$, and ${}^{84}\text{Nb}(p,\gamma)$, with a minor role played by ${}^{92}\text{Ru}(p,\gamma)$ (Table 9). For model K04-B7, we find 53 critical reactions, with the largest roles played by ${}^{69}\text{Br}(p,\gamma)$, followed by ${}^{96}\text{Ag}(p,\gamma)$ and ${}^{103}\text{In}(p,\gamma)$ (Table 10). It is also worth mentioning that in both models only two α -induced reactions appear to be influential [one being ${}^{15}\text{O}(\alpha,\gamma)$].

As expected, the most important β -decay rates involve heavier species in model K04-B7 than in K04-B6, as a result of the former's larger peak temperature (see Table 11). Hence, the β -decay rates of ¹⁸Ne, ⁶⁴Ge, ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, and ⁸⁰Zr are influential in model K04-B6, whereas those of ⁶⁸Se, ⁷²Kr, ⁷⁶Sr, ⁸⁰Zr, ⁸⁸Ru, ⁹²Pd, and ^{101,102}Sn are important in model K04-B7 (again only for uncertainty factors of 10 up and down).

4. MONTE CARLO SIMULATIONS

As discussed earlier, realistic simulations of type I XRBs have revealed a dramatic extension of the nuclear path, reaching the proton drip line at many points, and extending typically up to A = 50-60 (Fisker et al. 2008), or eventually up to the SnSbTe mass region (Schatz et al. 2001) or beyond (Koike et al. 2004). The overall number of nuclear processes is huge, since many different reactions are involved in the synthesis and/or destruction of any particular isotope during the explosion.

Recently, it has been claimed (Roberts et al. 2006) that, because of the coupling of so many different channels in XRBs, *traditional* sensitivity studies (like the one presented in § 3), in which only one reaction is varied while the others are held constant, cannot properly address all the important correlations between rate uncertainties and nucleosynthetic predictions, leading to wrong (or at least biased) conclusions.

Here we examine the impact of simultaneously varying all reaction rates in the highly coupled environment characteristic of an XRB through Monte Carlo simulations and discuss the feasibility of traditional sensitivity studies through a direct comparison.

4.1. The Monte Carlo Code

The simultaneous variation of reaction rates relies on the generation of a set of pseudorandom numbers that follow a given probability density function.

Since nuclear reaction rates are positive quantities, we assume that the random *enhancement factors* that are applied to each individual reaction follow a lognormal probability function (note that other distributions, such as Gaussian, may give negative values). The lognormal probability function adopted has the form

$$f(x; \mu, \sigma) = \frac{1}{\sqrt{2\pi\sigma}x} \exp\left[\frac{-(\ln x - \mu)^2}{2\sigma^2}\right], \quad x > 0, \quad (1)$$

where μ and σ are the mean and the standard deviation of $\ln x$, respectively.⁵

This lognormal distribution is implemented in such a way that the geometric mean of all enhancement factors is $\mu^* = 1$,

⁵ By definition, if x is lognormally distributed, ln x is normally distributed. Note that $\mu^* \equiv e^{\mu}$ is the geometric mean (as well as the median) of the lognormal distribution, whereas $\sigma^* \equiv e^{\sigma}$ is the geometric standard deviation.



FIG. 3.— Uncertainties in the final distribution of abundances resulting from the simultaneous variation of all nuclear processes in bulk by factors ranging roughly between 0.1 and 10, for model K04 (see § 4.2 for details). [See the electronic edition of the Supplement for a color version of this figure.]

and the probability to generate a random number between 0.1 and 10 (that is, in the range $[\mu^*/(\sigma^*)^2, \mu^*(\sigma^*)^2]$), to match the factors adopted for our sensitivity study in § 3, is chosen to be 95.5%. This is accomplished by setting $\sigma^* = \sqrt{10}$. From the many algorithms available in the literature for generating pseudorandom numbers, we have used that from Guardiola et al. (1995).

The set of enhancement factors is applied to all nuclear reactions included in the network; the same enhancement factor was applied to a forward-reverse reaction pair.⁶ This is coupled to a postprocessing nucleosynthesis code that allows us to compute the final yields for a particular temperature and density versus time profile, in a similar way as described in §§ 2 and 3. The process is then iterated for a preselected number of trials, in order to achieve statistically sound results. The series of computations performed in this work rely on 1000 trials. Although previous Monte Carlo simulations have been based on a larger number of trials (10,000, Smith et al. 2002; Hix et al. 2003; 50,000, Roberts et al. 2006), we feel that our choice is sufficient for the goals of this manuscript (see §§ 4.2 and 5).

4.2. Results

We have applied the Monte Carlo technique to our set of models discussed in § 3. However, since results are qualitatively similar in all cases, we restrict our discussion here to model K04 (Koike et al. 2004).

Before a thorough analysis of the results is made, several aspects must be considered in detail. First, the use of realistic uncertainties affecting all the rates is critical in Monte Carlo simulations, since the simultaneous variation of all reactions may otherwise result in inflated uncertainties in the final yields (Smith et al. 2002). Because of this, studies based on individual



Fig. 4.—Same as Fig. 3, but when all nuclear processes, except the 3α and all the β -decay rates, are allowed to vary simultaneously by factors ranging roughly between 0.1 and 10, for model K04 (see § 4.2 for details). [See the electronic edition of the Supplement for a color version of this figure.]

reaction-rate variations are more easily interpreted. This is illustrated in Figures 3 and 4, where *relative abundances* and their *normalized geometric standard deviations* (see Limpert et al. 2001; Carobbi et al. 2003) are plotted as a function of the mass number, for model K04. The *relative abundances* correspond to the geometric mean abundances obtained from the set of Monte Carlo trials normalized to abundances found with standard rates.



FIG. 5.—Same as Fig. 3, but for model F08. [See the electronic edition of the Supplement for a color version of this figure.]

⁶ A rigorous Monte Carlo procedure would require a random sampling of the reaction *Q*-value for the calculation of the reverse reaction rate. We did not address this extra complication, which we leave to future investigations.



FIG. 6.—Same as Fig. 4, but for model F08. [See the electronic edition of the Supplement for a color version of this figure.]

In turn, the *normalized geometric standard deviations* define the interval for which the probability to enclose any possible geometric mean abundance for a given species matches a certain value (95.5% in this study).

The simultaneous variation of all nuclear processes in bulk between 0.1 and 10, according to our lognormal distribution, results in large uncertainty bars for many isotopes (Fig. 3). Notice, however, that these final abundance uncertainties are overestimated since all β^+ -decays, as well as some important, relatively well-known reactions, such as the triple- α , were allowed to vary in this way. As discussed in § 3, more realistic uncertainties must be used instead, since these rates are known with better precision (usually better than ~30%, for β -decay rates). Indeed, when all nuclear processes, except the 3α and all the β -decay rates, are allowed to vary between roughly 0.1 and 10 in the Monte Carlo study, the overall uncertainties in the final yields decrease dramatically (Fig. 4). Similar results have been achieved for model F08 (see Figs. 5 and 6).

A second warning associated with Monte Carlo simulations involves the reduced subset of reactions whose variation affects the overall energy production (see § 5). In individual reactionrate variation studies, these reactions can be appropriately flagged for separate, detailed analysis with better numerical tools (semianalytical or hydrodynamic codes that can properly address changes in the temperature and density profiles driven by variations in the total energy output). In Monte Carlo studies, however, one cannot simply remove those trials in which the overall energy production is modified as this would affect the input distribution of enhancement factors (which are assumed to be random). Therefore, while results from individual reaction-rate variations are not corrupted by these effects, Monte Carlo simulations cannot disentangle this from the overall analysis and hence the interpretation of the results has to be taken with caution.

Figure 4 shows the impact of the simultaneous variation of all rates (except for the 3α and all the β -decay rates) on the final yields, for the temperature and density versus time profiles of



FIG. 7.—Correlation between the random enhancement factors applied to the 56 Ni(α , p) rate and the final 69 Ge normalized abundance, for model K04. [See the electronic edition of the Supplement for a color version of this figure.]

model K04 (Koike et al. 2004). It illustrates the interplay of multiple nuclear processes in the highly coupled environment of an XRB. The identification of the key reactions, whose uncertainties have the largest impact on the final yields, is more complicated than in *traditional* sensitivity studies. Figure 4 shows indeed which isotopes are mostly affected by the uncertainties associated with the rates. However, the identification of those specific reactions that are perhaps most responsible for those changes is by no means straightforward. Following Smith et al. (2002), Hix et al. (2003), and Roberts et al. (2006), we have searched for possible correlations between variations in the final abundance of a specific nucleus and each nuclear reaction rate that was varied in the Monte Carlo routine.

In many cases, correlations are small, as illustrated in Figure 7: although the relative abundance of ⁶⁹Ge shows a significant variability, it cannot be attributed to the uncertainty affecting the ⁵⁶Ni(α , p)⁵⁹Cu [and ⁵⁹Cu(p, α)⁵⁶Ni] rate, since the fit has a correlation coefficient of only r = 0.101. In sharp contrast, Figures 8 and 9 show a large correlation between the ⁶⁹Ge abundance and ⁶⁹Se(p, γ)⁷⁰Br, as well as between ⁷²Se and ⁶⁵As(p, γ)⁶⁶Se. However, despite the large correlation, varying the ⁶⁵As(p, γ) rate by a factor of 10 has no dramatic impact on the final ⁷²Se yield (Fig. 9). Hence, a key reaction in the Monte Carlo approach must have a significant correlation with the yield of an isotope (as indicated by the correlation coefficient), as well as a pronounced impact on the final abundance of an isotope as its rate is varied.

The most important correlations from the Monte Carlo study applied to model K04, as characterized by fits with correlation coefficients r > 0.5, are listed in Table 15. From the 50 reactions listed in the table, all but 5 [namely, ${}^{34}\text{Ar}(p, \gamma)$, ${}^{53}\text{Co}(p, \gamma)$, ${}^{62}\text{Ga}(p, \gamma)$, ${}^{69}\text{Br}(p, \gamma)$, and ${}^{80}\text{Y}(p, \gamma)$] were previously identified in the study based on individual reaction-rate variations (Table 1).



FIG. 8.—Same as Fig. 7, but for the strong correlation between the ${}^{69}Se(p, \gamma)$ rate and the final ${}^{69}Ge$ abundance. [See the electronic edition of the Supplement for a color version of this figure.]

Table 16 displays reactions that have the largest effects on the final yields for model K04, according to the individual reactionrate variation study (second column) and Monte Carlo simulations (third column). Reactions included in Table 16 were restricted to those that, in either the individual reaction-rate variation study or the Monte Carlo simulations, affected the final abundances of the isotopes by at least a factor of 2 (for the



FIG. 9.— Same as Fig. 7, but for the strong correlation between the 65 As(p, γ) rate and the final 72 Se abundance. [See the electronic edition of the Supplement for a color version of this figure.]

 TABLE 15

 Correlations between Final Yields and Enhancement Factors Applied to Reaction Rates in the Monte Carlo Approach, for Model K04

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Isotope	Reaction	Correlation Coefficient, r	Slope
¹⁵ N	$^{15}\mathrm{O}(\alpha, \gamma)^{19}\mathrm{Ne}$	-0.778	-0.927
³⁰ Si	$^{31}Cl(p, \gamma)^{32}Ar$	-0.751	[-0.205]
³³ S	18 Ne(α , p) ²¹ Na	-0.601	[-0.063]
³⁴ S	34 Ar(<i>p</i> , γ) ³⁵ K	-0.603	[-0.148]
³⁷ Ar	$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}$	-0.649	[-0.061]
³⁸ Ar	18 Ne(α , p) ²¹ Na	-0.571	[-0.062]
⁴⁴ Ti	$^{43}V(p, \gamma)^{44}Cr$	0.648	[0.134]
⁴⁶ Ti	47 Mn(<i>p</i> , γ) ⁴⁸ Fe	-0.822	-0.292
⁵⁰ Cr	$^{18}\text{Ne}(\alpha, n)^{21}\text{Na}$	-0.582	[-0.061]
⁵³ Mn	${}^{53}Co(p, \gamma){}^{54}Ni$	-0.628	[-0.121]
⁵⁴ Fe	${}^{18}\text{Ne}(\alpha, p){}^{21}\text{Na}$	-0.507	[-0.055]
⁵⁵ Co	${}^{56}Cu(p, \gamma){}^{57}Zn$	-0.777	-0.484
⁵⁶ Ni	${}^{56}\text{Ni}(p, \gamma){}^{57}\text{Cu}$	-0.840	-0.703
⁵⁷ Ni	${}^{57}Cu(p, \gamma){}^{58}Zn$	-0.807	-0.376
⁵⁸ Ni	${}^{58}Cu(p, \gamma){}^{59}Zn$	-0.593	[-0.176]
⁵⁹ Ni	${}^{59}Cu(p, \gamma){}^{60}Zn$	-0.658	[-0.172]
⁶⁰ Ni	${}^{61}\text{Ga}(p,\gamma){}^{62}\text{Ge}$	-0.910	-0.688
⁶¹ Cu	${}^{61}\text{Ga}(n, \gamma){}^{62}\text{Ge}$	-0.893	-0.701
⁶² Zn	${}^{62}\text{Ga}(p, \gamma){}^{63}\text{Ge}$	-0.645	[-0.185]
£11	$^{61}\text{Ga}(p, \gamma)^{62}\text{Ge}$	0.620	[0.178]
⁶³ Cu	$^{63}\text{Ga}(p, \gamma)^{64}\text{Ge}$	-0.779	[-0.327]
⁶⁴ Zn	$^{65}As(p, \gamma)^{66}Se$	-0.960	-0.517
⁶⁵ 7n	$^{65}Ge(n, \gamma)^{66}As$	-0.848	-0.886
⁶⁶ Ge	${}^{66}As(p, \gamma){}^{67}Se$	-0.585	-0.547
G c	${}^{66}\text{Ge}(n, \gamma){}^{67}\text{As}$	-0.566	-0.528
⁶⁷ Ga	67 As $(p, \gamma)^{68}$ Se	-0.699	-0.520
04	$^{65}As(p, \gamma)^{66}Se$	-0.553	-0.440
⁶⁸ Ge	69 Br $(p, \gamma)^{70}$ Kr	-0.697	[-0.063]
⁶⁹ Ge	${}^{69}\text{Se}(p, \gamma){}^{70}\text{Br}$	-0.972	-0.961
⁷⁰ Ge	70 Se $(p, \gamma)^{71}$ Br	-0.754	-0.492
⁷¹ As	71 Br $(p, \gamma)^{72}$ Kr	-0.963	-0.795
⁷² Se	${}^{65}As(p, \gamma){}^{66}Se$	0.748	[0.079]
⁷³ Se	73 Kr(p, γ) ⁷⁴ Rh	-0.969	-0.943
⁷⁴ Se	74 Kr(p, γ) ⁷⁵ Rb	-0.895	-0.699
⁷⁵ Br	75 Rb(p, γ) ⁷⁶ Sr	-0.964	-0.817
⁷⁶ Kr	$^{65}As(p, \gamma)^{66}Se$	0.711	[0 112]
⁷⁷ Kr	77 Sr(p, γ) ⁷⁸ Y	-0.962	-0.845
⁷⁸ Kr	78 Sr(p, γ) ⁷⁹ Y	-0.953	-0.794
⁷⁹ Kr	79 Y $(p, \gamma)^{80}$ Zr	-0.956	-0.845
⁸⁰ Sr	80 Y $(p, \gamma)^{81}$ Zr	-0.672	[-0.194]
⁸¹ Rb	81 Zr($p \ \gamma$) 82 Nb	-0.907	-0.663
⁸² Sr	$^{82}Zr(p, \gamma)^{83}Nb$	-0.918	-0.645
⁸³ Sr	$^{83}Nb(p, \gamma)^{84}Mo$	-0.730	-0.428
⁸⁴ Sr	$^{84}Nb(p, \gamma)^{85}Mo$	-0.832	-0.555
⁸⁵ Y	$^{85}Nb(p, \gamma)^{86}Mo$	-0.656	-0.371
⁸⁶ Zr	${}^{86}Mo(p, \gamma){}^{87}Tc$	-0.818	-0.519
⁸⁷ Zr	87 Mo(<i>p</i> , γ) ⁸⁸ Tc	-0.752	-0.412
⁸⁸ Zr	88 Tc(<i>p</i> . γ) ⁸⁹ Ru	-0.611	-0.360
⁸⁹ Nb	89 Tc(<i>p</i> , γ) ⁹⁰ Ru	-0.755	-0.467
⁹⁰ Mo	90 Ru(<i>p</i> , γ) ⁹¹ Rh	-0.680	-0.391
⁹¹ Nb	91 Ru(<i>p</i> , γ) 92 Rh	-0.583	-0.329
⁹² Mo	92 Ru(<i>p</i> , γ) ⁹³ Rh	-0.699	-0.429
⁹³ Tc	93 Rh(p, γ) ⁹⁴ Pd	-0.716	-0.460
⁹⁴ Mo	94 Rh(<i>p</i> , γ) 95 Pd	-0.585	-0.358
⁹⁵ Ru	$^{95}Pd(p, \gamma)^{96}Ag$	-0.648	-0.388
⁹⁶ Ru	$^{96}Ag(p, \gamma)^{97}Cd$	-0.591	-0.331
⁹⁷ Ru	${}^{97}\text{Ag}(p, \gamma)^{98}\text{Cd}$	-0.549	-0.420
¹⁰⁴ Ag	103 In $(p, \gamma)^{104}$ Sn	0.597	0.589
¹⁰⁵ Ag	104 In $(p, \gamma)^{105}$ Sn	0.550	0.623

Notes.—All correlations with r > 0.5 (see text) are included. Reactions that have an impact of less than a factor of 2 on the final yields of correlated isotopes (for enhancement factors ranging between roughly 0.1 and 10) are indicated by brackets in the last column, in which slopes of the different linear fits (final isotopic yield vs. rate enhancement factor; see, e.g., Figs. 8 and 9) are given. The error associated with the slopes is typically ~1%–10%.

 TABLE 16

 Isotopes Most Affected by Nuclear Uncertainties,

 According to Our Sensitivity Studies for Model K04

Isotope	Reaction (Individual Variations)	Reaction (Monte Carlo)
¹⁵ N	$^{15}\mathrm{O}(\alpha, \gamma)^{19}\mathrm{Ne}$	$^{15}\mathrm{O}(\alpha, \gamma)^{19}\mathrm{Ne}$
	18 Ne(α , p) ²¹ Na	
¹⁸ F	¹⁸ Ne $(\alpha, p)^{21}$ Na	
³⁰ Si	$^{31}\text{Cl}(p, \gamma)^{32}\text{Ar}$	
³³ S		
⁴⁴ Ti	$^{43}V(p, \gamma)^{44}Cr$	
⁴⁶ Ti	47 Mn(<i>p</i> , γ) ⁴⁸ Fe	47 Mn(<i>p</i> , γ) 48 Fe
⁵⁵ Co	56 Cu $(p, \gamma){}^{57}$ Zn	56 Cu $(p, \gamma){}^{57}$ Zn
⁵⁶ Ni	56 Ni $(p, \gamma)^{57}$ Cu	56 Ni (p, γ) 57 Cu
⁵⁷ Ni	57 Cu $(p, \gamma)^{58}$ Zn	${}^{57}\mathrm{Cu}(p, \gamma){}^{58}\mathrm{Zn}$
⁵⁸ Ni	${}^{58}{ m Cu}(p,\gamma){}^{59}{ m Zn}$	
⁵⁹ Ni	59 Cu $(p, \gamma)^{60}$ Zn	
⁶⁰ Ni	61 Ga $(p, \gamma){}^{62}$ Ge	61 Ga $(p, \gamma){}^{62}$ Ge
⁶¹ Cu	61 Ga $(p, \gamma){}^{62}$ Ge	61 Ga $(p, \gamma){}^{62}$ Ge
	61 Zn $(p, \gamma)^{62}$ Ga	
⁶³ Cu	63 Ga $(p, \gamma){}^{64}$ Ge	
⁶⁴ Zn	65 As $(p, \gamma)^{66}$ Se	65 As (p, γ) 66 Se
⁶⁵ Zn	65 Ge $(p, \gamma)^{66}$ As	${}^{65}\text{Ge}(p, \gamma){}^{66}\text{As}$
	65 As $(p, \gamma)^{66}$ Se	
⁶⁶ Ge	66 Ge $(p, \gamma)^{67}$ As	${}^{66}\text{Ge}(p, \gamma){}^{67}\text{As}$
	65 As $(p, \gamma)^{66}$ Se	
	66 As $(p, \gamma)^{67}$ Se	66 As $(p, \gamma)^{67}$ Se
⁶⁷ Ga	67 As $(p, \gamma)^{68}$ Se	6 As $(p, \gamma)^{68}$ Se
60 -	63 As $(p, \gamma)^{66}$ Se	65 As $(p, \gamma)^{66}$ Se
⁶⁹ Ge	69 Se $(p, \gamma)^{70}$ Br	69 Se $(p, \gamma)^{70}$ Br
^{/0} Ge	70 Se $(p, \gamma)^{71}$ Br	$^{/0}$ Se $(p, \gamma)^{/1}$ Br
71 .	70 Br $(p, \gamma)^{71}$ Kr	715 ()7277
⁷¹ As	71 Br(p, γ) 72 Kr	71 Br(p, γ) ⁷² Kr
⁷³ Se	75 Kr (p, γ) Rb	75 Kr(p, γ) ⁷⁵ Rb
⁻ Se	74 Kr(p, γ)/ ⁵ Rb	4 Kr $(p, \gamma)^{5}$ Rb
75 D #	$75 \text{Ph}(p, \gamma)^{76} \text{Sr}$	75Dh()76Ca
77 V -	$77Sr(p, \gamma)$ SI	$77Sr(p, \gamma)$ Sr
78Kr	$78Sr(p, \gamma)$ 1 $78Sr(p, \alpha)$ ⁷⁹ V	78 Sr(p, γ) ⁷⁹ V
⁷⁹ Kr	$79 \mathbf{V} (\mathbf{p}, \gamma)^{80} \mathbf{7r}$	$79V(n, \alpha)^{80}$ 7r
⁸¹ Rb	81 Zr(p, γ) ⁸² Nh	81 Zr $(p, \gamma)^{82}$ Nh
100	$^{65}As(n \ \gamma)^{66}Se$	$\Sigma(p, \gamma)$ ito
⁸² Sr	82 Zr(p , γ) 83 Nh	82 Zr($p \ \gamma$) ⁸³ Nb
⁸³ Sr	83 Nb(p, γ) ⁸⁴ Mo	$^{83}Nb(n, \gamma)^{84}Mo$
⁸⁴ Sr	$^{84}Nb(p, \gamma)^{85}Mo$	84 Nb(<i>p</i> , γ) ⁸⁵ Mo
⁸⁵ Y	85 Mo(p, γ) ⁸⁶ Tc	
	85 Nb(<i>p</i> , γ) ⁸⁶ Mo	85 Nb(p, γ) 86 Mo
⁸⁶ Zr	86 Mo(p, γ) ⁸⁷ Tc	86 Mo(<i>p</i> , γ) 87 Tc
⁸⁷ Zr	87 Mo(<i>p</i> , γ) ⁸⁸ Tc	87 Mo(<i>p</i> , γ) ⁸⁸ Tc
⁸⁸ Zr	88 Tc (p, γ) 89 Ru	${}^{88}\text{Tc}(p, \gamma){}^{89}\text{Ru}$
	65 As $(p, \gamma)^{66}$ Se	
⁸⁹ Nb	89 Tc $(p, \gamma)^{90}$ Ru	⁸⁹ Tc(p, γ) ⁹⁰ Ru
	65 As $(p, \gamma)^{66}$ Se	
⁹⁰ Mo	90 Ru(p, γ) 91 Rh	90 Ru(p, γ) 91 Rh
	65 As $(p, \gamma)^{66}$ Se	
⁹¹ Nb	91 Ru $(p, \gamma)^{92}$ Rh	91 Ru $(p, \gamma)^{92}$ Rh
	65 As $(p, \gamma)^{66}$ Se	
⁹² Mo	92 Ru $(p, \gamma)^{93}$ Rh	92 Ru(p, γ) 93 Rh
	65 As $(p, \gamma)^{66}$ Se	
⁹³ Tc	93 Rh $(p, \gamma)^{94}$ Pd	93 Rh $(p, \gamma)^{94}$ Pd
04	65 As (p, γ) 66 Se	
⁹⁴ Mo	65 As $(p, \gamma)^{66}$ Se	
	94 Pd $(p, \gamma)^{95}$ Ag	
05-	94 Rh $(p, \gamma)^{95}$ Pd	94 Rh $(p, \gamma)^{95}$ Pd
⁹³ Ru	95 Pd (p, γ) ⁹⁶ Ag	95 Pd $(p, \gamma)^{96}$ Ag
06-	65 As $(p, \gamma)^{66}$ Se	
⁹⁰ Ru	65 As $(p, \gamma)^{66}$ Se	
	96 Ag(p, γ) 97 Cd	90 Ag(p, γ) 97 Cd

TABLE 1	6—Continued
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Isotope	Reaction (Individual Variations)	Reaction (Monte Carlo)
⁹⁷ Ru	${}^{97}\text{Ag}(p, \gamma){}^{98}\text{Cd}$	${}^{97}\text{Ag}(p, \gamma){}^{98}\text{Cd}$
	65 As $(p, \gamma)^{66}$ Se	
	96 Ag(p, γ) 97 Cd	
⁹⁸ Ru	96 Ag(p, γ) 97 Cd	
	65 As $(p, \gamma)^{66}$ Se	
	${}^{98}\text{Cd}(p, \gamma){}^{99}\text{In}$	
	98 Ag $(p, \gamma)^{99}$ Cd	
⁹⁹ Rh	99 Cd $(p, \gamma)^{100}$ In	
	65 As $(p, \gamma)^{66}$ Se	
	96 Ag $(p, \gamma)^{97}$ Cd	
¹⁰⁰ Pd	65 As $(p, \gamma)^{66}$ Se	
	100 Cd(p, γ) 101 In	
	96 Ag $(p, \gamma)^{97}$ Cd	
¹⁰¹ Pd	101 In $(p, \gamma)^{102}$ Sn	
	65 As $(p, \gamma)^{66}$ Se	
¹⁰² Pd	102 In $(p, \gamma)^{103}$ Sn	
	65 As $(p, \gamma)^{66}$ Se	
¹⁰³ Ag	65 As $(p, \gamma)^{66}$ Se	
	102 In $(p, \gamma)^{103}$ Sn	
¹⁰⁴ Ag	103 In $(p, \gamma)^{104}$ Sn	103 In $(p, \gamma)^{104}$ Sn
	65 As $(p, \gamma)^{66}$ Se	
	102 In $(p, \gamma)^{103}$ Sn	
¹⁰⁵ Ag	104 In $(p, \gamma)^{105}$ Sn	104 In(p, γ) 105 Sn
	103 In $(p, \gamma)^{104}$ Sn	

Note.—Results from the individual reaction-rate approach (Table 1) are compared with those from Monte Carlo simulations (Table 15) (see text for details).

former, see Table 1; for the latter, reactions from Table 15 without brackets in the slope column). Qualitatively, results are in excellent agreement, except at the very end of the network (nuclei with A > 97). Indeed, most of the discrepancies correspond to reactions that were indeed identified in Table 15 but that affect the final abundances by less than a factor of 2 when enhancement factors ranging between 0.1 and 10 are considered. These discrepancies might be related to the correlations that the individual reaction-rate variation study is not capable of dealing with.

Similar agreement is reported on the comparison of both techniques when applied to model F08 (Fisker et al. 2008), as illustrated in Tables 17 and 18.

Finally, we would like to stress that our preliminary Monte Carlo studies rely on 1000 trials, a limited number that calls for a justification. To this end, we have extended the study of models K04 and F08 to 10,000 trials. Indeed, no significant differences, neither in the list of key reactions nor in the correlation coefficients and slopes, have been found.

5. DISCUSSION AND CONCLUSIONS

Table 19 summarizes the most important reactions collected from Tables 1–10. For the sake of brevity we have restricted Table 19 and the discussion here to those reactions that affect the yield of three species or more in any of our 10 models, in the individual-variation studies. We have also carefully identified reactions that were seen to modify the XRB energy output when their rates were varied by a factor of 10, up or down. This is explicitly indicated in Table 20, which lists the subset of reactions with any impact on XRB yields (reactions identified in Tables 1– 10 that affect, at least, one isotope) that simultaneously modify the overall energy output by more than 5% at some point during the burst, when their nominal rates are varied by a factor of 10, up or down. This table has to be taken as a warning of the limitations

TABLE 17 Same as Table 15, but for Model F08

Isotope	Reaction	Correlation Coefficient, r	Slope
⁴ He	$^{12}\mathrm{C}(\alpha, \gamma)^{16}\mathrm{O}$	-0.679	[-0.030]
¹² C	$^{12}C(\alpha, \gamma)^{16}O$	-0.585	[-0.203]
	$^{12}C(p, \gamma)^{13}N$	-0.581	[-0.203]
¹⁶ O	$^{16}O(\alpha, \gamma)^{20}Ne$	-0.878	-0.945
²⁰ Ne	20 Ne(α , γ) ²⁴ Mg	-0.894	-1.01
²⁴ Mg	24 Mg(α , γ) 28 Si	-0.829	-0.667
²⁰ Mg	$^{26g}\text{Al}(\alpha, p)^{29}\text{Si}$	-0.686	-0.631
269 + 1	$^{26}Si(\alpha, p)^{29}P$	-0.550	-0.493
²⁰⁹ Al	$^{269}Al(\alpha, p)^{29}Bl$	-0.709	-0.788
29 c ;	$26q \Lambda 1(\alpha, p)$ P	-0.340	-0.384
³⁰ Si	$^{30}P(n \sim)^{31}S$	-0.687	[0.221]
³¹ P	$^{30}P(p, \gamma)^{31}S$	0.856	0 466
³² S	${}^{28}\text{Si}(\alpha, \gamma){}^{32}\text{S}$	0.822	0.467
³³ S	${}^{30}P(\alpha, p)^{33}S$	0.587	[0.204]
³⁴ S	$^{34}Cl(p, \gamma)^{35}Ar$	-0.590	[-0.108]
³⁵ Cl	$^{34}Cl(p, \gamma)^{35}Ar$	0.661	[0.283]
³⁷ Ar	${}^{36}\text{Ar}(p, \gamma){}^{37}\text{K}$	-0.915	-0.482
³⁸ Ar	38 K(<i>p</i> , γ) ³⁹ Ca	-0.606	[-0.084]
³⁹ K	${}^{40}\text{Sc}(p, \gamma){}^{41}\text{Ti}$	-0.704	[-0.142]
⁴⁰ Ca	39 K(<i>p</i> , γ) ⁴⁰ Ca	0.594	[0.191]
⁴³ Sc	44 V(p, γ) 45 Cr	-0.838	[-0.249]
⁴⁴ Ti	$^{44}V(p, \gamma)^{45}Cr$	0.540	[0.190]
⁴⁵ Ti	$^{44}\text{Ti}(p, \gamma)^{45}\text{V}$	-0.782	-0.593
⁴ /Ti	47 Cr(p, γ) 46 Mn	-0.745	-0.417
⁴⁰ Cr	$^{49}Cr(p, \gamma)^{49}Mn$	-0.646	[-0.173]
50Cm	49 Mn(p, γ) ⁵⁰ Fe	-0.859	-0.295
⁵¹ Cr	5^{50} Nin $(p, \gamma)^{51}$ Fe	-0.554	[-0.082]
⁵² Fe	$52 \text{Fe}(p, \gamma)^{53} \text{Co}$	-0.709	0.513
⁵³ Mn	$^{53}C_0(n, \alpha)^{54}N_i$	-0.934	-0.513 -0.675
⁵⁴ Fe	$^{54}Co(p, \gamma)^{55}Ni$	-0.721	[-0.253]
⁵⁵ Co	${}^{55}Co(p, \gamma){}^{56}Ni$	-0.761	[-0.183]
⁵⁶ Ni	${}^{57}Cu(p, \gamma){}^{58}Zn$	-0.805	[-0.265]
⁵⁷ Ni	${}^{57}\text{Ni}(p, \gamma){}^{58}\text{Cu}$	-0.900	-0.858
⁵⁸ Ni	${}^{58}Cu(p, \gamma){}^{59}Zn$	-0.754	-0.584
	${}^{57}\mathrm{Cu}(p, \gamma){}^{58}\mathrm{Zn}$	0.624	0.478
⁵⁹ Ni	${}^{57}\mathrm{Cu}(p, \gamma){}^{58}\mathrm{Zn}$	0.670	0.328
	59 Cu $(p, \gamma){}^{60}$ Zn	-0.668	-0.327
⁶⁰ Ni	57 Cu $(p, \gamma)^{58}$ Zn	0.614	[0.096]
⁶¹ Cu	$^{61}Zn(p, \gamma)^{62}Ga$	-0.902	-0.621
⁶² Zn	62 Ga(<i>p</i> , γ) 63 Ge	-0.777	-0.498
647	63 Ga $(p, \gamma)^{64}$ Ge	-0.865	-0.406
⁶⁵ Zn	$^{65}Ga(p, \gamma)^{66}Aa$	0.938	0.545
66Ge	$66 \Lambda s(p, \gamma)^{67} Se$	-0.831	-0.002
⁶⁷ Ga	$^{67}As(p, \gamma)^{68}Se$	-0.021 -0.747	-0.402 -0.495
Guiini	${}^{61}\text{Ga}(p, \gamma){}^{62}\text{Ge}$	0.528	[0 349]
⁶⁸ Ge	${}^{61}\text{Ga}(p, \gamma){}^{62}\text{Ge}$	0.851	[0.031]
⁶⁹ Ge	${}^{69}\text{Se}(p, \gamma){}^{70}\text{Br}$	-0.945	-0.599
⁷⁰ Ge	70 Se $(p, \gamma)^{71}$ Br	-0.676	-0.427
	70 Br $(p, \gamma)^{71}$ Kr	-0.518	-0.330
⁷¹ As	$^{71}\mathrm{Br}(p,\gamma)^{72}\mathrm{Kr}$	-0.935	-0.627
⁷² Se	72 Br $(p, \gamma)^{73}$ Kr	-0.514	[-0.005]
⁷³ Se	73 Kr $(p, \gamma)^{74}$ Rb	-0.936	-0.654
⁷⁴ Se	74 Kr $(p, \gamma)^{75}$ Rb	-0.797	-0.514
⁷⁵ Br	75 Rb $(p, \gamma)^{76}$ Sr	-0.938	-0.660
^{/°} Kr	$^{73}\text{Rb}(p, \gamma)^{76}\text{Sr}$	0.571	[0.020]
′′Kr	$^{\prime\prime}$ Sr $(p, \gamma)^{\prime 8}$ Y	-0.926	-0.653
⁷⁹ Kr	$^{\prime \circ}$ Sr $(p, \gamma)^{\prime 9}$ Y	-0.862	-0.573
⁶⁶ Kr 81 p L	$(p, \gamma)^{30}$ Zr	-0.932	-0.771
KD 82 S r	$\frac{1}{82}$ Zr(p, γ) ²² ND	-0.903	-0.639
⁸³ Sr	83 Nb(p, γ) ⁸⁴ Mo	-0.912	-0.390

TABLE 17—Continued

Isotope	Reaction	Correlation Coefficient, r	Slope
⁸⁴ Sr	${}^{84}\text{Nb}(p, \gamma)^{85}\text{Mo} \\ {}^{85}\text{Mo}(p, \gamma)^{86}\text{Tc} \\ {}^{86}\text{Mo}(p, \gamma)^{87}\text{Tc} \\ {}^{87}\text{Tc}(p, \gamma)^{88}\text{Ru} \\ {}^{87}\text{Tc}(p, \gamma)^{88}\text{Ru} $	-0.935	-0.750
⁸⁵ Y		-0.901	-0.569
⁸⁶ Zr		-0.916	-0.617
⁸⁷ Zr		-0.752	-0.451
⁸⁸ Zr		0.526	[0.289]

of postprocessing techniques (for both individual-variation and Monte Carlo studies). Furthermore, we have identified some additional reactions in our studies that affect the energy output but remarkably did not affect any yields in any of our models [for instance, ${}^{14}O(\alpha, p)$, ${}^{27}Si(p, \gamma)$, ${}^{31}S(p, \gamma)$, or ${}^{35}S(p, \gamma)$]. Several aspects are worth noting here. First, the total number of reactions affecting the energy output, for any model, is small. Second, as indicated in Table 20, some of those reactions are known with better precision than a factor of 10. Third, there is no way to overcome this problem in the context of postprocessing calculations. Indeed, a self-consistent analysis with a hydrodynamic code capable of self-adjusting both the temperature and the density of the stellar envelope seems mandatory to address this issue, for the few reactions of concern. And fourth, the presence of reactions affecting the energy output is particularly dangerous within a Monte Carlo context, as results rely on the simultaneous variation of all rates, whereas most of the results obtained from an individual reactionrate variation approach remain unaffected. Note, however, that Tables 19 and 20 reveal a very limited number of reactions that were seen to affect the energy output for models K04 and F08, giving support to the results obtained in our Monte Carlo studies.

It is also worth mentioning that no discussion involving the triple- α reaction or any β -decay rate has been made here, since these reactions, when varied within realistic uncertainty limits, have no effect, neither on yields nor on the nuclear energy output. We do, however, encourage the development of improved, consistent treatments for calculating stellar weak rates for all isotopes in our network, especially the important rates identified in Table 11. Finally, except for the exceptional case of ⁶⁴Ge(p, γ), the results of our Q-value variations (Tables 13 and 14) are not affected by variations of the energy output.

5.1. Overview of the Most Influential Reactions

The main purpose of this section is to elaborate on the reactions listed in Tables 19 and 20, namely, the most influential reactions found in this study.

First, we focus on those rates that were drawn from theoretical estimates, due to insufficient or unavailable experimental information. Their main characteristics are summarized in Table 21. To help illustrate systematic uncertainties associated with these important reactions, we have compared the theoretical rates adopted in our network with those found in the recent REACLIBv0 compilation⁷ over the temperature range covered in our studies. Overall, the agreement is quite good; however, we note that even when using the same basic Hauser-Feshbach code (NON-SMOKER) along with similar *Q*-values, a difference in the rates as large as a factor of ~3 is obtained. Differences as large as a factor of ~4 are seen between rates from different statistical model codes, but using similar *Q*-values. Moreover, the factor of 10 disagreement for the ⁶¹Ga(*p*, γ) rate arises from

⁷ See http://www.nscl.msu.edu/~nero/db/.

TABLE 18 Same as Table 16, but for Model F08

Isotope	Reaction (Individual Variations)	Reaction (Monte Carlo)
12C	$\frac{12C(n-2)^{13}N}{12}$	· · · · ·
C	$C(p, \gamma) = N$ $^{12}C(\alpha, \alpha)^{16}O$	
¹⁶ O	$^{16}\Omega(\alpha, \gamma)^{20}$ Ne	$^{16}O(\alpha \ \gamma)^{20}Ne$
0	$^{12}C(\alpha, \gamma)^{16}O$	0(a, /) ite
²⁰ Ne	20 Ne(α, γ) ²⁴ Mg	20 Ne(α , γ) ²⁴ Mg
1.0	$^{12}C(\alpha, \gamma)^{16}O$	
²⁴ Mg	24 Mg $(\alpha, \gamma)^{28}$ Si	$^{24}Mg(\alpha, \gamma)^{28}Si$
e	$^{12}C(\alpha, \gamma)^{16}O$	
²⁵ Mg	22 Mg(α , p) ²⁵ Al	
	24 Mg $(\alpha, \gamma)^{28}$ Si	
	25 Al $(\alpha, p)^{28}$ Si	
	24 Mg $(p, \gamma)^{25}$ Al	
²⁶ Mg	26g Al $(\alpha, p)^{29}$ Si	26g Al(α , p) 29 Si
24	20	$^{26}\mathrm{Si}(\alpha, p)^{29}\mathrm{P}$
²⁶ <i>g</i> Al	$^{26g}\text{Al}(\alpha, p)^{29}\text{Si}$	$^{26g}\text{Al}(\alpha, p)^{29}\text{Si}$
27	$^{26}Si(\alpha, p)^{29}P$	$^{26}\mathrm{Si}(\alpha, p)^{29}\mathrm{P}$
²⁷ Al	20 Si $(\alpha, p)^{25}$ P	
	$^{27}S1(\alpha, p)^{30}P$	••••
	$^{27}\text{Al}(\alpha, p)^{50}\text{S1}$	
	$^{269}Al(p, \gamma)^{-1}Sl$	
	$^{22}Mg(\alpha, p)$ SI	
²⁸ Si	28 Si($\alpha \propto \gamma$) ³² S	•••
³¹ P	${}^{30}P(n \ \gamma)^{31}S$	$^{30}P(n, \gamma)^{31}S$
³² S	28 Si(α, γ) ³² S	$^{28}\text{Si}(\alpha, \gamma)^{32}\text{S}$
³³ S	$^{30}P(\alpha, p)^{33}S$	
	29 Si $(\alpha, \gamma)^{33}$ S	
³⁵ C1	$^{34}Cl(p, \gamma)^{35}Ar$	
³⁷ Ar	${}^{36}{ m Ar}(p,\gamma){}^{37}{ m K}$	${}^{36}\text{Ar}(p, \gamma){}^{37}\text{K}$
⁴⁰ Ca	39 K(<i>p</i> , γ) ⁴⁰ Ca	
⁴⁵ Ti	44 Ti $(p, \gamma)^{45}$ V	$^{44}{ m Ti}(p,\gamma)^{45}{ m V}$
	44 V $(p, \gamma)^{45}$ Cr	
15	45 V $(p, \gamma)^{46}$ Cr	
⁴ /Ti	$4/\mathrm{Cr}(p, \gamma)^{48}\mathrm{Mn}$	47 Cr(p, γ) 48 Mn
40	$^{46}V(p, \gamma)^{4}/Cr$	
⁴⁹ V	$^{49}Mn(p, \gamma)^{50}Fe$	49 Mn(<i>p</i> , γ) ⁵⁰ Fe
53N 4-	$5^{2}Fe(p, \gamma)^{55}Co$	$52 \operatorname{Fe}(p, \gamma)^{55} \operatorname{Co}(p, \gamma)^{54} \operatorname{Vi}$
¹¹ Mn	$^{52}\text{Eq}(p, \gamma)^{53}\text{Cq}$	$Co(p, \gamma)^{-1}Ni$
⁵⁴ Fe	$^{54}Co(p, q)^{55}Ni$	•••
⁵⁶ Ni	57 Cu(p, γ) ⁵⁸ Zn	
⁵⁷ Ni	5^{7} Ni $(p, \gamma)^{58}$ Cu	${}^{57}\text{Ni}(p_{-}\gamma){}^{58}\text{Cu}$
1 1111111111	${}^{57}Cu(p, \gamma){}^{58}Zn$, Cu
⁵⁸ Ni	${}^{58}Cu(p, \gamma){}^{59}Zn$	${}^{58}Cu(p, \gamma){}^{59}Zn$
	${}^{57}Cu(p, \gamma){}^{58}Zn$	${}^{57}Cu(p, \gamma){}^{58}Zn$
⁵⁹ Ni	${}^{59}Cu(p, \gamma){}^{60}Zn$	${}^{59}Cu(p, \gamma){}^{60}Zn$
	${}^{57}\mathrm{Cu}(p,\gamma){}^{58}\mathrm{Zn}$	${}^{57}\mathrm{Cu}(p, \gamma){}^{58}\mathrm{Zn}$
⁶¹ Cu	61 Zn $(p, \gamma)^{62}$ Ga	61 Zn (p, γ) 62 Ga
⁶² Zn	62 Ga $(p, \gamma){}^{63}$ Ge	62 Ga $(p, \gamma){}^{63}$ Ge
	61 Zn $(p, \gamma)^{62}$ Ga	
⁶³ Cu	63 Ga $(p, \gamma)^{64}$ Ge	63 Ga (p, γ) ⁶⁴ Ge
⁶⁴ Zn	61 Ga $(p, \gamma){}^{62}$ Ge	61 Ga $(p, \gamma){}^{62}$ Ge
⁶⁵ Zn	$^{65}\text{Ge}(p, \gamma)^{66}\text{As}$	${}^{65}\text{Ge}(p, \gamma){}^{66}\text{As}$
66 ~	61 Ga $(p, \gamma)^{62}$ Ge	
⁶⁶ Ge	${}^{61}\text{Ga}(p, \gamma){}^{62}\text{Ge}$	
	00 Ge(p, γ) 07 As	66 A a(a) 67 C -
67 C o	67 A of m = > 1685 o	67 As $(p, \gamma)^{68}$ Se
Ja	$As(p, \gamma)^{-5}Se^{61}Ga(p, \gamma)^{62}Ge^{61}Ga(p, \gamma)^{62}Ge^{61}Ga(p, \gamma)^{62}Ge^{61}Ga(p, \gamma)^{62}Ga(p, \gamma)^{62}G$	$\operatorname{As}(p, \gamma)^{-se}$
⁶⁹ Ge	69 Se(p, γ) UC	69 Se(n $\sim)^{70}$ Br
⁷⁰ Ge	70 Br $(n \sim)^{71}$ Kr	70 Br(p, γ) ⁷¹ Kr
	70 Se $(p, \gamma)^{71}$ Br	70 Se $(p, \gamma)^{71}$ Br
	69 Se $(p, \gamma)^{70}$ Br	$\mathcal{S}(p, j)$ Di
⁷¹ As	71 Br(p, γ) ⁷² Kr	71 Br(p. γ) ⁷² Kr
⁷³ Se	73 Kr(p, γ) ⁷⁴ Rb	73 Kr(<i>p</i> , γ) ⁷⁴ Rb

TABLE 1	8-Con	tinued
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Isotope	Reaction (Individual Variations)	Reaction (Monte Carlo)
⁷⁴ Se	74 Kr(<i>p</i> , γ) ⁷⁵ Rb	74 Kr $(p, \gamma)^{75}$ Rb
	74 Rb $(p, \gamma)^{75}$ Sr	
	73 Kr(<i>p</i> , γ) ⁷⁴ Rb	
⁷⁵ Br	75 Rb $(p, \gamma)^{76}$ Sr	75 Rb(p, γ) 76 Sr
⁷⁷ Kr	77 Sr $(p, \gamma)^{78}$ Y	77 Sr(p, γ) ⁷⁸ Y
	76 Rb $(p, \gamma)^{77}$ Sr	
⁷⁸ Kr	78 Sr(p, γ) ⁷⁹ Y	78 Sr(p, γ) ⁷⁹ Y
	78 Y(p, $\gamma)^{79}$ Zr	
⁷⁹ Kr	$^{79}Y(p, \gamma)^{80}Zr$	79 Y(p, $\gamma)^{80}$ Zr
⁸¹ Rb	81 Zr(<i>p</i> , γ) 82 Nb	81 Zr (p, γ) 82 Nb
	80 Y(<i>p</i> , γ) ⁸¹ Zr	
⁸² Sr	82 Zr(<i>p</i> , γ) 83 Nb	82 Zr(<i>p</i> , γ) 83 Nb
⁸³ Sr	83 Nb(<i>p</i> , γ) ⁸⁴ Mo	83 Nb(<i>p</i> , γ) ⁸⁴ Mo
	82 Zr(<i>p</i> , γ) 83 Nb	
⁸⁴ Sr	84 Nb(<i>p</i> , γ) ⁸⁵ Mo	84 Nb($p, \gamma)^{85}$ Mo
⁸⁵ Y	85 Mo(p, γ) ⁸⁶ Tc	85 Mo(p, γ) ⁸⁶ Tc
⁸⁶ Zr	86 Mo(<i>p</i> , γ) ⁸⁷ Tc	86 Mo(<i>p</i> , γ) ⁸⁷ Tc
⁸⁷ Zr	87 Tc(p, γ) 88 Ru	87 Tc(p, γ) 88 Ru
	86 Mo(p, γ) ⁸⁷ Tc	
⁸⁸ Zr	86 Mo(<i>p</i> , γ) ⁸⁷ Tc	
	87 Tc(p, γ) 88 Ru	
⁸⁹ Nb	86 Mo(<i>p</i> , γ) ⁸⁷ Tc	
	88 Tc(p, γ) 89 Ru	
⁹⁰ Mo	86 Mo(p, γ) ⁸⁷ Tc	
	85 Mo(<i>p</i> , γ) ⁸⁶ Tc	
⁹¹ Nb	85 Mo(<i>p</i> , γ) ⁸⁶ Tc	

the comparison between a NON-SMOKER result and a shell model calculation. The magnitude of these discrepancies lends support to our choice of varying rates by a factor of 10 rather than by a significantly larger factor.

Next, we have collected in Table 22 the principal end products in all 10 models, as well as those rates that change these particular yields by at least a factor of 2 (when varied by a factor of 10 up and/or down). These rates may have a direct impact on the properties of the neutron star crust (see, e.g., Brown & Bildsten 1998) as our studies show that they modify the main postburst constituents of the crust. The majority of the reactions listed in Table 22 are also found in Tables 19 and 20. We now focus on the rates listed in Tables 19 and 20 that have been determined experimentally, and we assess whether a factor of 10 variation is reasonable for these rates. For those cases where a smaller uncertainty is justified, we have performed additional postprocessing calculations to supplement results from Tables 1-10 and 20 (namely, to determine the impact of individual rate variations by smaller factors on yields and on the overall nuclear energy output). For reference, we continue to compare the rate adopted in this work with that used in the REACLIBv0 compilation. Although we do not discuss experimental information (if available) for other reactions listed in Tables 1-10 (namely, those that affected less than three isotopes in any model), this must of course be considered by anyone examining reactions beyond the most influential ones listed in Table 19:

1. ¹²C(α , γ)¹⁶O: We have used the Kunz et al. (2002) experimental rate, which, over the range of temperatures used in our models, agrees to better than 20% with the recommended NACRE (Angulo et al. 1999) rate, and to better than a factor of ~2 with the recommended Buchmann (1996) rate adopted in REACLIBv0. A factor of ~3 variation in our rate would cover the limits given in both NACRE and Buchmann (1996). Hence, we have varied this rate individually by a factor of 3, up and

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				TABI	LE 19					
IMARY	OF THE	Most	INFLUENTIAL	NUCLEAR	PROCESSES,	AS	Collected	FROM	TABLES	1 - 10

Reaction	Models Affected
$^{12}C(\alpha, \gamma)^{16}O^a$	F08, K04-B2, K04-B4, K04-B5
18 Ne(α , p) ²¹ Na ^a	K04-B1 ^b
$^{25}{\rm Si}(\alpha, p)^{28}{\rm P}$	K04-B5
26g Al $(\alpha, p)^{29}$ Si	F08
$^{29}S(\alpha, p)^{32}Cl$	K04-B5
$^{30}P(\alpha, p)^{33}S$	K04-B4
$^{30}S(\alpha, p)^{33}C1$	K04-B4, ^b K04-B5 ^b
$^{31}\mathrm{Cl}(p,\gamma)^{32}\mathrm{Ar}$	K04-B1
$^{32}S(\alpha, \gamma)^{36}Ar$	K04-B2
${}^{56}\text{Ni}(\alpha, p){}^{59}\text{Cu}$	S01, ^b K04-B5
5^{7} Cu $(p, \gamma)^{58}$ Zn	F08
59 Cu(<i>p</i> , γ) ⁶⁰ Zn	S01, ^b K04-B5
51 Ga $(p, \gamma)^{62}$ Ge	F08, K04-B1, K04-B2, K04-B5, K04-B6
55 As $(p, \gamma)^{66}$ Se	K04, ^b K04-B1, K04-B2, ^b K04-B3, ^b K04-B4, K04-B5, K04-B6
59 Br(<i>p</i> , γ) ⁷⁰ Kr	K04-B7
75 Rb $(p, \gamma)^{76}$ Sr	K04-B2
32 Zr(<i>p</i> , γ) ⁸³ Nb	K04-B6
34 Zr(<i>p</i> , γ) ⁸⁵ Nb	K04-B2
34 Nb(<i>p</i> , γ) ⁸⁵ Mo	K04-B6
35 Mo(p, γ) ⁸⁶ Tc	F08
36 Mo(p, γ) ⁸⁷ Tc	F08, K04-B6
37 Mo(p, γ) ⁸⁸ Tc	K04-B6
92 Ru(<i>p</i> , γ) ⁹³ Rh	K04-B2, K04-B6
93 Rh $(p, \gamma)^{94}$ Pd	K04-B2
$^{96}\text{Ag}(p, \gamma)^{97}\text{Cd}$	K04, K04-B2, K04-B3, K04-B7
102 In $(p, \gamma)^{103}$ Sn	K04, K04-B3
103 In $(p, \gamma)^{104}$ Sn	K04-B3, K04-B7
103 Sn(α , p) 106 Sb	S01 ^b

NOTES.—These reactions affect the yields of at least three isotopes when their nominal rates are varied by a factor of 10 up and/or down. See text for details.

^a Reaction experimentally constrained to better than a factor of ~ 10 at XRB temperatures. See § 5.

^b Reaction that affects the total energy generation rate by more than 5% at some time interval in this

model, when its rate is varied by a factor of 10 up and/or down. See text and Table 20 for details.

TABLE 20 Nuclear Processes Affecting the Total Energy Output by More than 5% and at Least One Isotope

SUM

Reaction	Models Affected
$^{15}O(\alpha, \gamma)^{19}Ne^{a}$	K04, K04-B1, K04-B6
$^{18}\text{Ne}(\alpha, p)^{21}\text{Na}^{a}$	K04-B1, K04-B6
$^{22}Mg(\alpha, p)^{25}A1$	F08
$^{23}\text{Al}(p, \gamma)^{24}\text{Si}$	K04-B1
$^{24}Mg(\alpha, p)^{27}Al^{a}$	K04-B2
$^{26g}Al(p, \gamma)^{27}Si^{a}$	F08
${}^{28}\mathrm{Si}(\alpha, p){}^{31}\mathrm{P}^{\mathrm{a}}$	K04-B4
$^{30}S(\alpha, p)^{33}Cl$	K04-B4, K04-B5
$^{31}Cl(p, \gamma)^{32}Ar$	K04-B3
$^{32}S(\alpha, p)^{35}Cl$	K04-B2
$^{35}Cl(p, \gamma)^{36}Ar^{a}$	K04-B2
${}^{56}\text{Ni}(\alpha, p){}^{59}\text{Cu}$	S01
59 Cu(<i>p</i> , γ) 60 Zn	S01
65 As $(p, \gamma)^{66}$ Se	K04, K04-B2, K04-B3
${}^{69}\text{Br}(p, \gamma){}^{70}\text{Kr}$	S01
71 Br(p, γ) ⁷² Kr	K04-B7
103 Sn(α , p) 106 Sb	S01

Notes.—Nuclear processes affecting the total energy output by more than 5%, as well as the yield of at least one isotope, when their nominal rates are individually varied by a factor of 10 up and/or down, for the given model. See text for details.

^a Reaction experimentally constrained to better than a factor of ~ 10 at XRB temperatures. See § 5.

down, and tested its effect for those models in which a factor of 10 variation, as discussed in § 3, had an impact (models F08, K04-B2, K04-B4, and K04-B5). Indeed, only model K04-B2 (where the ¹²C yield is affected by a factor of 0.47 when this rate is multiplied by 3) and K04-B5 (where ²⁰Ne and ²⁴Mg are affected by factors of 0.44 and 0.47, respectively, when the rate is reduced by a factor of 3) reveal changes in the final yields (note that variation of this reaction by a factor of 10 did not affect the overall nuclear energy output in any of our models).

2. ¹⁸Ne(α , p)²¹Na: We use the Chen et al. (2001) experimental rate, which agrees to a factor of \sim 3 with the Görres et al. (1995) Hauser-Feshbach (SMOKER) calculation adopted in REACLIBv0. There are, however, additional data from Groombridge et al. (2002). Indeed, using the information from Chen et al. (2001), for $E_r < 1.7$ MeV, and that from Groombridge et al. (2002), for $E_r > 1.98$ MeV, we find a rate that deviates from the Chen et al. (2001) rate by 30%, a factor of \sim 3, and a factor of \sim 7 at 1.0, 1.4, and 2 GK, respectively. Since we found this reaction to affect yields and/or the total nuclear energy in models K04-B1 and K04-B6, neither of which reach temperatures above 1.36 GK, we have restricted our analysis to a variation of the Chen et al. (2001) rate by a factor of 3, up and down. No impact on the yields is found when varying the rate as such; however, model K04-B1 shows some variation of the total energy output when the rate is multiplied by 3.

3. ¹⁵O(α , γ)¹⁹Ne: We use the Davids et al. (2003) rate, which agrees to a factor of ~3 with the Hahn et al. (1996) rate used in REACLIBv0, over the temperatures spanned by our models. If

	TABLE 21	
COMPARISON BETWEEN THEORETICAL	L RATES FROM TABLES 19 AND 20, A	ACCORDING TO DIFFERENT RATE COMPILATIONS

	Q-VALUE (keV)			
REACTION	Audi et al. (2003b)	This Work ^a	REACLIBv0 ^a	Maximum Disagreement
$^{22}Mg(\alpha, p)^{25}A1$	3655(1)	3655 [NS]	3655 [NS]	20%
$^{25}{\rm Si}(\alpha, p)^{28}{\rm P}$	6119(11)	6122 [NS]	6119 [NS]	20%
$^{26g}Al(\alpha, p)^{29}Si$	4820.68(6)	4823 [NS]	4820 [NS]	40%
$^{29}S(\alpha, p)$ ^{32}Cl	5306(50)	5307 [NS]	5306 [NS]	×2
$^{30}S(\alpha, p)$ ^{33}Cl	2077(3)	2076 [NS]	2076 [NS]	×2
$^{30}P(\alpha, p)$ ^{33}S	1521.36(34)	1522 [NS]	1521 [NS]	20%
$^{31}\text{Cl}(p, \gamma)^{32}\text{Ar}$	2422(50)	2404 [Her95]	2404 [Her95]	0
$^{32}S(\alpha, \gamma)^{36}Ar$	6640.76(14)	6639 [NS]	6641 [NS]	×2
${}^{56}\text{Ni}(\alpha, p){}^{59}\text{Cu}$	-2411(11)	-2413 [NS]	-2411 [NS]	×3
${}^{57}Cu(p,\gamma) {}^{58}Zn$	2277(52)	2277 [For01]	2277 [For01]	0
${}^{59}Cu(p, \gamma) {}^{60}Zn$	5120(11)	5121 [NS]	5120 [NS]	10%
${}^{61}\text{Ga}(p, \gamma) {}^{62}\text{Ge}$	$2442(149)^{b}$	2427 [NS]	2576 [Fis04]	$\times 10$
65 As (p, γ) 66 Se	2030(424) ^b	2587 [NS]	2433 [NS]	10%
69 Br(<i>p</i> , γ) 70 Kr	2489(399) ^b	2434 [NS]	2579 [NS]	10%
$^{71}\text{Br}(p, \gamma)$ ^{72}Kr	4167(568)	4525 [NS]	4167 [NS]	30%
75 Rb(<i>p</i> , γ) 76 Sr	4311 (38)	4467 [NS]	4311 [NS]	10%
82 Zr(<i>p</i> , γ) 83 Nb	2055(387) ^b	2060 [NS]	2056 [NS]	20%
84 Nb(p, γ) 85 Mo	4513(409) ^b	4510 [M]	4513 [NS]	40%
84 Zr(p, γ) 85 Nb	2946(297) ^b	2109 [NS]	2946 [NS]	40%
85 Mo(p, γ) 86 Tc	1393(409) ^b	1390 [M]	1393 [NS]	$\times 4$
86 Mo(p, γ) 87 Tc	1855(530) ^b	1860 [M]	1855 [NS]	×3
${}^{87}\text{Mo}(p, \gamma) {}^{88}\text{Tc}$	2304(300) ^b	2300 [M]	2304 [NS]	50%
92 Ru(<i>p</i> , γ) 93 Rh	2054(499) ^b	2002 [NS]	2054 [NS]	20%
${}^{93}\text{Rh}(p, \gamma) {}^{94}\text{Pd}$	4467(566) ^b	4365 [NS]	4466 [NS]	40%
${}^{96}\text{Ag}(p, \gamma) {}^{97}\text{Cd}$	3321(566) ^b	3258 [NS]	3321 [NS]	×2
102 In (p, γ) 103 Sn	3554(318) ^b	4095 [NS]	3554 [NS]	$\times 2$
103 In (p, γ) 104 Sn	4281(107)	4241 [NS]	4281 [NS]	40%
103 Sn(α , p) 106 Sb	$-5508(432)^{b}$	-5508 [NS]	-5508 [NS]	10%

Note.—The table shows, for a particular reaction, the maximum disagreement between our rate and the REACLIBv0 rate over the temperature range covered in all our studies (\sim 0.4–2.5 GK).

^a Sources of the theoretical estimates: M = MOST Hauser-Feschbach code; NS = NON-SMOKER Hauser-Feschbach code; For01 = Forstner et al. (2001); Fis04 = Fisker's shell model calculation (see REACLIBv0 database); Her95 = Herndl et al. (1995), shell model calculation.

^b Q-value estimated from systematics. See Audi et al. (2003b).

we combine the new information reported by Tan et al. (2007), for $E_x < 4.55$ MeV, with the information in Davids et al. (2003), for the states at $E_x = 4.600$, 4.712, and 5.092 MeV, we calculate a new rate that agrees to a factor of ~ 2 with the original Davids et al. (2003) rate, over the relevant temperatures. Varying our rate within a factor of \sim 3 would cover the uncertainty limits in the Tan-Davids rate calculation. We have tested the impact of varying our ¹⁵O(α , γ) rate by a factor of 3 up and down, for models K04, K04-B1, and K04-B6. We find that the total nuclear energy is affected only in the early stages of model K04, when the rate is multiplied by 3. Concerning the yields, only ¹⁵N is affected (consistent with Tables 1, 4, and 9): when the rate is reduced by a factor of 3, the ¹⁵N normalized yields in models K04, K04-B1, and K04-B6 are 3.13, 2.75, and 3.17, respectively; when the rate is increased by a factor of 3, no effect is seen except in model K04-B1, where the normalized yield of ¹⁵N decreases to 0.35.

4. ²³Al(p, γ)²⁴Si: We use the Schatz et al. (1997) rate, as does REACLIBv0. This rate is based on both theoretical estimates and measurements of excited states in ²⁴Si. Its uncertainty spans up to 3 orders of magnitude, for typical XRB temperatures. For this reason, we deem our results from varying this rate by a factor of 10 to be adequate.

5. ${}^{24}Mg(\alpha, p){}^{27}Al$: Both REACLIBv0 and our network rely on the experimental rate reported in Iliadis et al. (2001). Above

0.3 GK, this rate is reported to be uncertain by only $\pm 20\%$. No effect on the yields is found when the rate is varied by 20% in our postprocessing calculations (model K04-B2; see Table 20). The total nuclear energy is, however, affected when this rate is increased by 20%, in that particular model.

6. ${}^{26g}\text{Al}(p, \gamma){}^{27}\text{Si}$: We use the (unpublished) rate from the Ph.D. thesis of Vogelaar (1989), as does REACLIBv0 (the new TRIUMF measurement [Ruiz et al. 2006] on the 184 keV resonance does not affect the rate at typical XRB temperatures). According to NACRE, the experimental information is only sufficient to determine the rate for T < 0.9 GK (they use Hauser-Feshbach calculations to extend this rate to higher temperatures). Our rate agrees with the NACRE recommended rate to 30% over the temperature range covered by our models; varying our rate by a factor of 2 up and down would cover the uncertainties reported in NACRE. Assuming such a degree of uncertainty in our rate for model F08 (see Table 20) leads to no effect on any yield, nor on the total nuclear energy.

7. ²⁸Si(α , p)³¹P: The rate used in our network and that of REACLIBv0 is from the compilation of Iliadis et al. (2001). An uncertainty of $\pm 20\%$ is assigned to this rate above 0.2 GK. Actually, varying this rate by $\pm 20\%$ in model K04-B4 (see Table 20) has no effect on any yields, nor on the total nuclear energy.

8. ${}^{32}S(\alpha, p){}^{35}Cl$: We use the Iliadis et al. (2001) experimental rate, as does REACLIBv0. The uncertainty of this rate, over

Model	Principal End Products	Most Influential Reactions
K04	Н	
	⁴ He	
	⁶⁴ Zn	65 As (p, γ)
	⁶⁸ Ge	
	⁷² Se	
	⁷⁶ Kr	
S01	Н	56 Ni(α , p), 59 Cu(p , γ)
	⁴ He	
	¹⁰³ Ag	103 In (p, γ)
	¹⁰⁴ Ag	
	¹⁰⁵ Ag	105 Sn(p, γ)
	¹⁰⁶ Cd	103 Sn(α , p)
F08	⁴ He	
	^{12}C	$^{12}\mathrm{C}(\alpha, g),^{a} {}^{12}\mathrm{C}(p, \gamma)^{a}$
	²⁸ Si	$^{28}\mathrm{Si}(lpha,\ g)^{\mathrm{a}}$
	⁵⁶ Ni	57 Cu(p, γ)
	⁶⁰ Ni	
	⁶⁴ Zn	61 Ga (p, γ)
K04-B1	⁴ He	
	⁶⁰ Ni	61 Ga (p, γ)
	⁶⁴ Zn	61 Ga (p, γ)
	⁶⁸ Ge	61 Ga(p, γ), 65 As(p, γ)
K04-B2	⁶⁸ Ge	
	⁷² Se	
	⁷⁶ Kr	
	⁹⁴ Mo	
	¹⁰³ Ag	
	¹⁰⁴ Ag	
K04-B3	Н	
	⁶⁴ Zn	65 As (p, γ)
	⁶⁸ Ge	
	⁷² Se	
	⁷⁶ Kr	
	⁸⁰ Sr	
K04-B4	⁵⁶ Ni	
	⁶⁰ Ni	
	⁶⁴ Zn	65 As (p, γ)
K04-B5	³⁹ K	30 S (α, p)
	⁵⁶ Ni	²⁵ Si(α , p), ²⁹ S(α , p), ³⁰ S(α , p), ⁵⁶ Ni(α , p), ⁵⁹ Cu(p , γ)
	⁶⁰ Ni	
	⁶⁴ Zn	61 Ga (p, γ)
	⁶⁸ Ge	²⁵ Si(α , p), ³⁰ S(α , p), ⁶¹ Ga(p , γ), ⁶⁵ As(p , γ)
K04-B6	Н	
	⁶⁰ Ni	61 Ga (p, γ)
	⁶⁴ Zn	
	⁶⁸ Ge	
	⁷² Se	
	⁷⁶ Kr	61 Ga (p, γ)
K04-B7	H	
	⁶⁸ Ge	⁶⁹ Br (p, γ)
	⁷² Se	
	⁷⁶ Kr	
	⁸⁰ Sr	····
	⁹⁶ Ru	⁹⁶ Ag (p, γ)

 TABLE 22

 Reaction Rates that Affect the Principal XRB End Products in Our 10 Models

^a Rate is experimentally constrained to better than a factor of 10. See text for details.

XRB typical temperatures, spans up to 3 orders of magnitude (Iliadis et al. 2001). Consequently, we feel that our results, based on a variation of this rate by a factor of 10 (see Table 20), are reliable.

9. 35 Cl(p, γ) 36 Ar: Again, we adopt the Iliadis et al. (2001) experimental rate, as does REACLIBv0. The uncertainty in this rate is ~20% above 0.2 GK (Iliadis et al. 2001). We find no effect on any yield when varying this rate by $\pm 20\%$ in our post-

processing calculations for model K04-B2 (see Table 20). However, we remarkably find that increasing this rate by 20% does indeed affect the total nuclear energy at the early stages of the TNR in this model.

Finally, because of past interest in the literature, we discuss some specific reactions that we found to affect the total nuclear energy when their rates were varied individually by a factor of 10, but affected no yields whatsoever (see § 5.1): ${}^{31}S(p, \gamma)$, ${}^{35}Ar(p, \gamma)$, ${}^{27}Si(p, \gamma)$, and ${}^{14}O(\alpha, p)$:

1. ${}^{31}S(p, \gamma){}^{32}Cl, {}^{35}Ar(p, \gamma){}^{36}K, and {}^{27}Si(p, \gamma){}^{28}P$: For these three reactions, we have used the rates reported in Iliadis et al. (1999), determined through the use of experimental information when available (e.g., excitation energies), along with calculations and information from the respective mirror nuclei. Judging from the uncertainties presented in that work, we conclude that uncertainty factors of 2, 3, and 2 (up and down) are more reasonable for the ${}^{31}S(p, \gamma)$, ${}^{35}Ar(p, \gamma)$, and ${}^{27}Si(p, \gamma)$ rates over XRB temperatures, respectively. Accordingly, we individually varied each of these reactions within those limits for the models affected [i.e., models K04-B1 and K04-B7 for ³¹S(p, γ); models K04-B2 and K04-B7 for 35 Ar(p, γ); and models K04-B4 and K04-B7 for ²⁷Si(p, γ)] to determine the resulting impact on the total nuclear energy, as no yields were affected by varying any of these by a factor of 10. Increasing the ${}^{31}S(p, \gamma)$ rate by a factor of 2 changed the total nuclear energy (by at least 5% at some point of the burst) in model K04-B1, increasing the 35 Ar(p, γ) rate by a factor of 3 changed the nuclear energy in model K04-B2, and increasing the ²⁷Si(p, γ) rate by a factor of 2 changed the nuclear energy in model K04-B7. The impact of these reactions on XRB light curves has been examined in Iliadis et al. (1999) and Thielemann et al. (2001).

2. ¹⁴O(α , p)¹⁷F: This reaction is of critical importance for breakout from the hot CNO cycle. We use the rate from Blackmon et al. (2003), which is larger than the Hahn et al. (1996) rate, adopted by REACLIBv0, by a factor of ~ 10 at typical XRB temperatures. This increased rate is due to the inclusion of some of the contributions from the ${}^{17}F^*$ exit channel by Blackmon et al. (2003); however, branches for states of $E_x > 7$ MeV in ¹⁸Ne were not measured. Actually, Notani et al. (2004a, 2004b) observed what could be the population of ${}^{17}F^*$ through a state

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at $E_x(^{18}\text{Ne}) \sim 7.1$ MeV, but the interpretation of their results has been questioned by Fu et al. (2007). As the studies of Blackmon et al. (2003) and Notani et al. (2004a, 2004b) are both published in only preliminary forms, and taking into account the argument of Fu et al. (2007), we find it difficult to evaluate the uncertainty in this rate. Variations by a factor of 10 affected nuclear energy in 5 of our 10 models: K04, F08, K04-B1, K04-B3, and K04-B4. Further efforts to constrain this rate, based on analyses of previous measurements and/or new measurements, would certainly be desirable.

In summary, we have identified a very limited number of reactions (see Tables 19-21 and this section) that play a significant role in our XRB nucleosynthesis studies. Indeed, our results can help to guide and motivate future measurements by experimental nuclear physicists. Stellar modelers, as well, may tackle the challenge to properly address the role played by the few reactions flagged as affecting the overall energy output, an aspect that lies beyond the possibilities offered by postprocessing calculations.

Finally, we have compared the two general approaches to the sensitivity study: individual reaction-rate variations, and simultaneous variation of all rates through Monte Carlo techniques. The highly coupled environment characteristic of an XRB provides the opportunity to test for the effects of correlations in the uncertainties of reaction rates. We find similar results from both approaches, with minor differences attributed to such correlation effects.

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