



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

Viscoelastic model for analysing the behaviour of adhesive-bonded FRP-to-steel joints in civil engineering applications

Citation for published version:

Wang, S, Stratford, T & Reynolds, TPS 2023, 'Viscoelastic model for analysing the behaviour of adhesive-bonded FRP-to-steel joints in civil engineering applications', *International journal of adhesion and adhesives*, vol. 123, 103359. <https://doi.org/10.1016/j.ijadhadh.2023.103359>

Digital Object Identifier (DOI):

[10.1016/j.ijadhadh.2023.103359](https://doi.org/10.1016/j.ijadhadh.2023.103359)

Link:

[Link to publication record in Edinburgh Research Explorer](#)

Document Version:

Peer reviewed version

Published In:

International journal of adhesion and adhesives

General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



1

2 **Viscoelastic model for analysing the behaviour of adhesive-bonded FRP-**
3 **to-steel joints in civil engineering applications**

4 S. Wang^{a,b,*}, T. Stratford^c and T.P.S Reynolds^c

5 ^a School of Civil Engineering, Architecture and Environment, Hubei University of Technology, Wuhan 430068, China

6 ^b Innovation Demonstration Base of Ecological Environment Geotechnical and Ecological Restoration of Rivers and Lakes,
7 Hubei University of Technology, Wuhan 430068, China

8 ^c School of Engineering, Institute for Infrastructure and Environment, The University of Edinburgh, Edinburgh EH9 3FG,
9 UK

10
11 Email: wangsongbo@hbut.edu.cn, tim.stratford@ed.ac.uk, t.reynolds@ed.ac.uk

12 * Corresponding Author
13

14 **Abstract**

15 Adhesively bonding fibre reinforced polymer (FRP) plates have been a mainstream method for
16 strengthening civil engineering structures. The effectiveness of bonding strengthening is
17 dependent on the performance of the adhesive layer. This study examines the time-temperature
18 dependent viscoelasticity of a typical structural epoxy adhesive and develops a linear
19 viscoelastic material model that can be used for numerical analysis. An accelerated test method
20 involving dynamic mechanical analysis (DMA) and time-temperature superposition principle
21 (TTSP) were used to characterise the structural adhesive. The corresponding limitations of this
22 method were discussed, including decomposition effect, nonlinear viscoelasticity, applicability
23 of TTSP, and further curing of the sample. The numerical study of the long-term behaviour of
24 the single lap-shear FRP-to-steel joint found that a slightly warmer temperature (30 °C for this
25 study) is beneficial for the bonded joint as it can reduce the concentrated shear stress with
26 negligible increase in the shear strain. However, a higher temperature (50 °C for this study)
27 that near the adhesive's glass transition temperature (T_g) could be detrimental as it can lead to
28 significant shear strain in the adhesive joint within the first year of service life.
29

30 **Keywords:** Structural epoxy adhesive; Viscoelasticity; Elevated temperature; DMA; FRP-to-
31 steel joint.

32

33 **1 Introduction**

34 Adhesives have been widely used in various industries including automotive, aircraft, and
35 aerospace, since their advent [1–3]. Also for civil engineering, with the rapidly growing need
36 of rehabilitating and strengthening existing structures, adhesively bonding an FRP plate has
37 currently been a mainstream strengthening method [4–6]. Compared to traditional
38 strengthening methods involve welding, bolting, or riveting, the use of adhesively bonding can
39 bring advantages such as lower additional weight, lower time and labour intensity, and more
40 uniformly distributed stresses in the bonding area [7–13].

41 The effectiveness and reliability of bonding strengthening are significantly dependent on
42 the quality, integrity, and durability of the adhesive layer which acts as a load transfer medium
43 between the composite and structure. Especially for FRP-to-steel joints, the adhesive layer
44 inevitably becomes the weakest section due to its relatively lower strength and stiffness [3,14–
45 16]. Commonly used ambient-cured adhesives are typically made of viscoelastic polymers.
46 Thermal exposure can soften the adhesive and induce temperature- and time- dependent
47 viscoelastic creep along bonded joints, which may be detrimental and hence affect the
48 performance of strengthened structures [17–22]. In current design guidelines for strengthening
49 civil engineering metallic structures using FRP, this issue is avoided by simply limiting the
50 maximum operating temperature to a minimum of 15 °C below the peak $\text{Tan } \delta$ glass transition
51 temperature (T_g) of the bonding adhesive and using a multiple combination of large safety
52 factors, which reduces the design efficiency and hampers the extensive use of this advanced
53 strengthening method [7,10,23–25]. A more profound understanding of how the time-

54 temperature related viscoelasticity of adhesives affects the performance of bonded joints is
55 desired.

56

57 **1.1 Literature survey**

58 The existing studies on FRP-to-steel bonded joints in structures have been mainly focusing
59 on their short-term performance [18,20,26,27]. While Heshmati *et al.* [5] examined the
60 performance of FRP-to-steel double lap-shear joints after immersed in distilled water at 20 °C
61 and 45 °C for up to three years and found that there was a noticeable greater strength reduction
62 in those joints immersed at 45 °C. De Zeeuw *et al.* [19] investigated the effects of 40 °C air (or
63 distilled water) and constant load on the behaviour of single lap-shear joints. Within 14 days
64 of sustained loading test, they observed the time-dependent viscoelastic creep behaviour.
65 However, the design service life of civil engineering constructions is more than decades. The
66 results obtained by these conventional experimental methods are usually limited.

67 Another research strategy is to use an accelerated test method to directly characterise the
68 viscoelasticity of adhesives, as it is the major factor responsible for the deterioration of joints'
69 performance. Dynamical mechanical analysis (DMA) is a common technique used to
70 characterise the viscoelasticity of polymers as a function of temperature and frequency (or
71 time). The time-temperature superposition principle (TTSP) is classically applied along with
72 the DMA test, which allows the viscoelastic behaviour at a lower frequency (or over a longer
73 time) to be estimated from the behaviour at a higher frequency (or over a shorter time), but at
74 another higher temperature, thus avoiding the limitations of the measurement instruments
75 [16,28–30]. This method has been used in several studies in other industries [16,21,29,30],
76 however, relevant studies in civil engineering are limited, and the data and conclusions from
77 other studies may not be applicable due to differences in types of adhesives, curing conditions,
78 operating temperatures, and useful service life [3].

79 Houhou *et al.* [25] examined the viscoelasticity of a structural epoxy adhesive using
80 aforementioned accelerated test method (DMA and TTSP), but the further analysis was
81 conducted on the behaviour of FRP-to-concrete joints, in which concrete might be the weakest
82 part. Nevertheless, the study found that the viscoelastic creep can induce a redistribution of
83 interfacial stresses, leading to a reduction in the concentrated peak stress and an increase in
84 effective transfer length, which could be beneficial for the durability of bonded joints. However,
85 this work did not further consider the temperature effect on the joint, which may bring greater
86 creep deformation. The authors [31] previously examined a strengthening adhesive with a
87 relatively low onset T_g (38.0 °C) for investigating the worst case of viscoelastic creep at
88 elevated temperatures. Whilst it was found that the creep reduced the performance of FRP-
89 strengthened metallic beams during the long-term services, the details of stress redistribution
90 and increased strain within the bonded joints were not shown, and the authors were also aware
91 that the characteristic data of the adhesive with low T_g may be less representative. Besides,
92 none of these studies discussed the limitations of using the accelerated test method, leaving it
93 unclear whether the structural adhesive decomposed during the DMA test at high temperatures,
94 and whether applying the TTSP was feasible without introducing substantial errors.

95 Against this background, the objectives of this study are (a) charactering the viscoelasticity
96 of a typical structural adhesive; (b) discussing the limitations of the applied accelerated test
97 method and identifying the need for further research; (c) obtaining a profound understanding
98 of the impact of elevated temperatures on the long-term behaviour of FRP-to-steel joints.

99

100 **2 Experimental characterisation of viscoelasticity**

101 The structural adhesive characterised in the present study was a two-component epoxy resin,
102 Sikadur[®]-330 [32], which has been widely used in FRP strengthening for civil engineering
103 structures. The adhesive samples used in these tests were cured at ambient temperature ($21 \pm$

104 2 °C) and humidity ($50 \pm 10\%$ RH) for 28 days, which could be consistent with the practical
105 strengthening application and ensured that the samples had reasonable T_g values. Prior to
106 characterising the viscoelasticity of the adhesive through DMA tests at high temperatures, the
107 thermogravimetric analysis (TGA) test was conducted to characterise its thermal stability in
108 order to determine the maximum applicable experimental temperature. Combining the DMA
109 test with TTSP, a complete modulus master curve was then constructed. The usage range of
110 applying TTSP was also discussed.

111

112 **2.1 Thermogravimetric analysis (TGA)**

113 In many studies that apply DMA to conduct the accelerated characterisation of adhesives at
114 high temperatures (> 100 °C), the thermal stability of the tested sample was not examined
115 [16,30,31]. However, when the temperature rises above 100 °C, the loss of mass attributed to
116 the evaporation of low molecules from epoxy adhesives may have started, as structural epoxy
117 adhesives typically contain fillers, curing agents, and accelerators [32–35]. This can therefore
118 affect the obtained modulus response data and thus introduce errors.

119 In this study, the TGA experiment was conducted to examine the thermal stability of the
120 studied adhesive according to ISO 11358 [36] through a Mettler Toledo thermogravimetric
121 instrument. The powdery adhesive sample (15.1 mg) was placed in the aluminium oxide
122 crucible which was set in the sample holder of the analyser. The test was run from 25 °C to
123 900 °C in an air atmosphere with a heating rate of 10 °C/min. Figure 1 shows the resultant mass
124 loss curve and mass derivative curve.

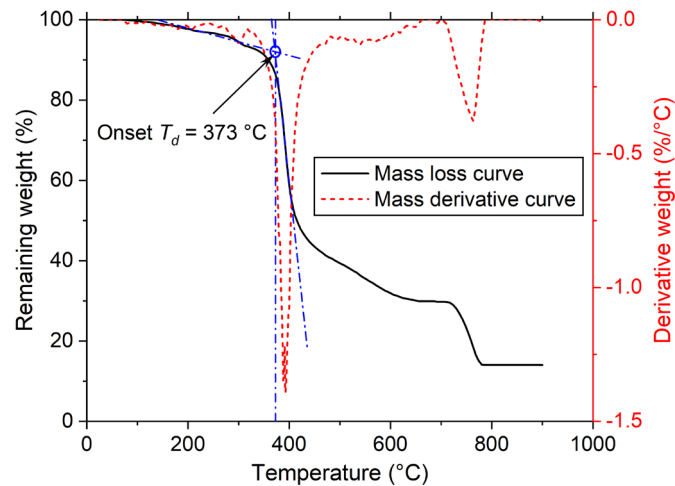


Figure 1: Decomposition temperature (T_d) of the adhesive

125
126

127 Whilst the obtained onset decomposition temperature (T_d) of the structural adhesive was
 128 373 °C [36,37], the thermal decomposition behaviour started to occurs when the temperature
 129 exceeded approximately 100 °C. This suggests a maximum experimental temperature of
 130 100 °C, below which the decomposition behaviour can be ignored.

131

132 2.2 Dynamic mechanical analysis (DMA)

133 The DMA characterising experiments were carried out according to ISO 6721 [38] through
 134 a DMA 8000 instrument. The dimensions of the rectangular adhesive specimen and applied
 135 configuration in each test are illustrated in Table 1.

136

Table 1: Dimensions of specimens and applied configurations in DMA tests

Test	Configuration	Dimension (mm)		
		Length	Width	Thickness
T_g	Single cantilever	35	7.45	1.59
Frequency scan	Single cantilever	35	7.43	1.60
Strain scan	Dual cantilever	45	7.50	1.48

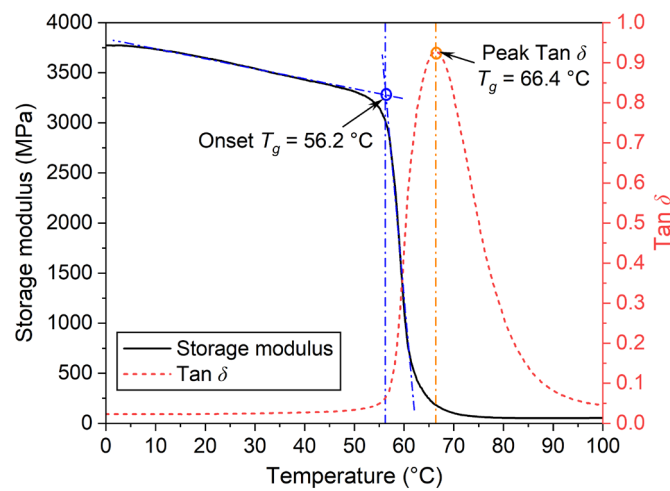
137

138 2.2.1 Glass transition temperature (T_g)

139 As mentioned in Section 1, the maximum working temperature of the structural bonded joint
 140 stipulated in the current design guidelines is based on the T_g of the applied adhesive [7,23]. T_g ,

141 as an important material property, indicates the transition temperature range of a thermoset
142 polymer from a stiff glassy state to a rubbery state [39].

143 The DMA time/temperature scan test was carried out to determine the T_g of the examined
144 adhesive, using a sinusoidal displacement of 0.05 mm at 1.0 Hz, and 2 °C/min temperature
145 ramp [28,38]. The measured temperature-dependent storage modulus and Tan δ were shown in
146 Figure 2.



147
148 Figure 2: Glass transition temperature (T_g) of the adhesive

149 A significant reduction in the storage modulus occurred between the onset T_g (56.2 °C) and
150 the peak Tan δ T_g (66.4 °C) [28,38]. In order to fully characterise the viscoelasticity of the
151 adhesive at elevated temperatures, the average T_g (61.3 °C) was used as the benchmark
152 intermediate temperature so that the applied temperature range of the subsequent viscoelastic
153 characterising tests was set between 25 °C to 100 °C.

154

155 2.2.2 Modulus response in DMA strain scans

156 Strain scans measurements were performed by applying an oscillatory displacement of 1.0
157 Hz with amplitudes ranging from 0.006 mm to 0.100 mm, corresponding to applied strains of
158 between approximately 0.012% and 0.197%, to examine whether the adhesive would exhibit
159 nonlinear viscoelasticity. A dual cantilever configuration was utilised to guarantee that the

160 sample was subjected to a generally uniform strain when large displacements were applied [28].
161 These scans were repeated at 5 °C intervals over a temperature range of 25 °C to 100 °C. Figure
162 3 illustrates the resultant storage modulus responses.

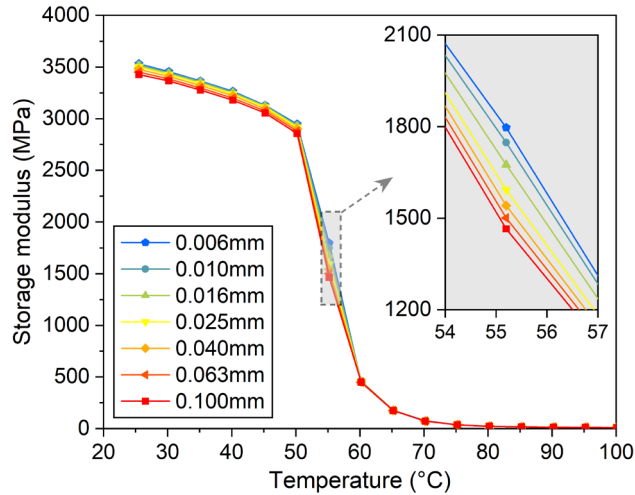


Figure 3: DMA multi-strain scans test

163
164

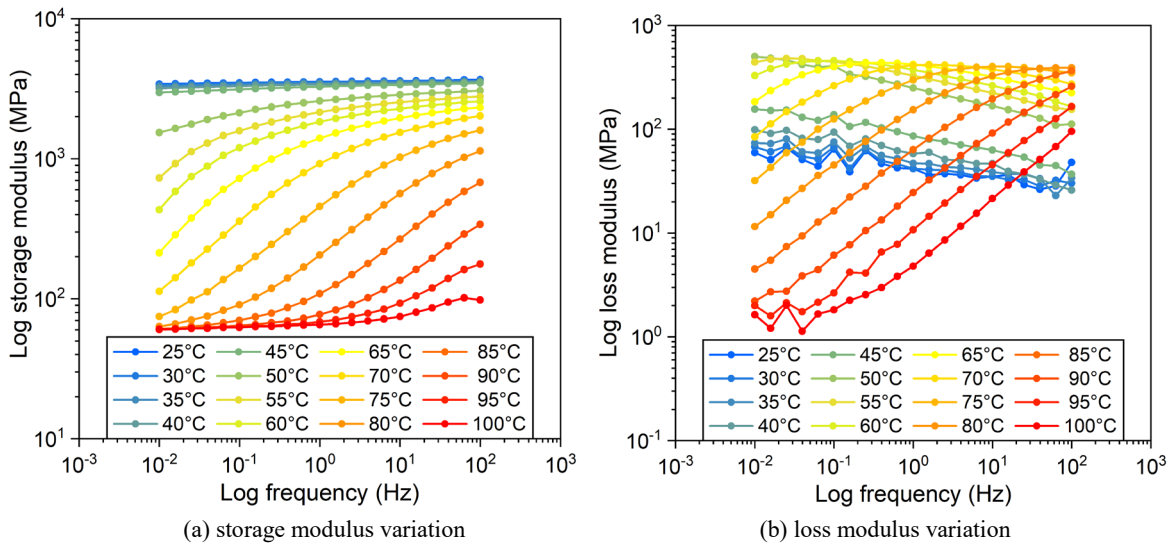
165 The examined adhesive exhibits very limited strain (stress) dependent behaviour. It is only
166 when the temperature rises close to the T_g , resulting in a sharp drop in the storage modulus,
167 that the behaviour of the adhesive shows a relatively noticeable nonlinearity. Consequently, in
168 the current paper, the behaviour of the adhesive was discussed solely in terms of linear
169 viscoelasticity.

170 Note that the strain (stress) applied in the DMA test is relatively minimal to prevent fatigue
171 damage to the sample [28]. The adhesive may exhibit significant nonlinear viscoelastic
172 behaviour when subjected to higher strain (stress). However, the stress redistribution behaviour
173 of bonded joints at elevated temperatures can drastically reduce the stresses carried by the
174 adhesive layer [25,27,40], and thus limit the effect of nonlinear response. Detailed investigation
175 of the nonlinear viscoelasticity of adhesives was not, however, the focus of this paper.

176

177 2.2.3 Modulus response in DMA frequency scans

178 The viscoelastic response of the structural adhesive was examined using DMA multi-
179 frequency scans test [28]. The specimen was exposed to a sinusoidal displacement of 0.01 mm
180 at frequencies ranging from 0.01 Hz to 100 Hz, logarithmically spaced to cover five
181 measurements pre decade. The test was carried out over a temperature range of 25 °C to 100 °C
182 with a temperature step of 5 °C. The obtained storage modulus that increased with frequency
183 but decreased with temperature is shown in Figure 4 (a), and the corresponding loss modulus
184 is shown in Figure 4 (b).



185
186

187 Figure 4: DMA multi-frequency scans test

188

189 2.2.4 Time-temperature superposition principle

190 As mentioned in the literature review, TTSP has been used in a number of studies to build
191 modulus master curves of adhesives based on DMA viscoelastic characterisation results
192 [16,21,25,29–31]. However, most of studies did not consider the applicability of TTSP, which
193 raised concerns about the accuracy of developed master curves.

194 TTSP is applicable to thermorheologically simple materials whose viscoelastic response
195 depend equally on temperature [41,42]. The wicket plot (log Tan δ versus log storage modulus)

196 is one way to identify the thermorheologically simplicity of materials [28,29,41]. Based on the
 197 results of the DMA multi-frequency scans test (Figure 4), the wicket plot for the adhesive
 198 investigated in this study is shown in Figure 5. The near-arch shape (near symmetrical curve)
 199 indicates the thermorheologically simplicity, so as to confirm the applicability of TTSP
 200 [28,29,41].

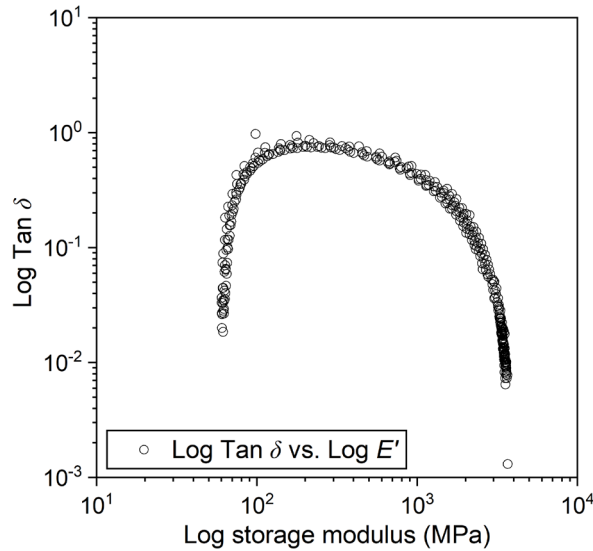
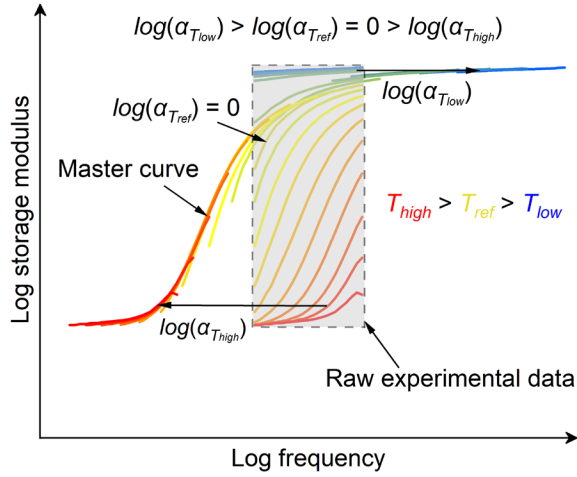


Figure 5: Wicket plot for the examined Sikadur®-330

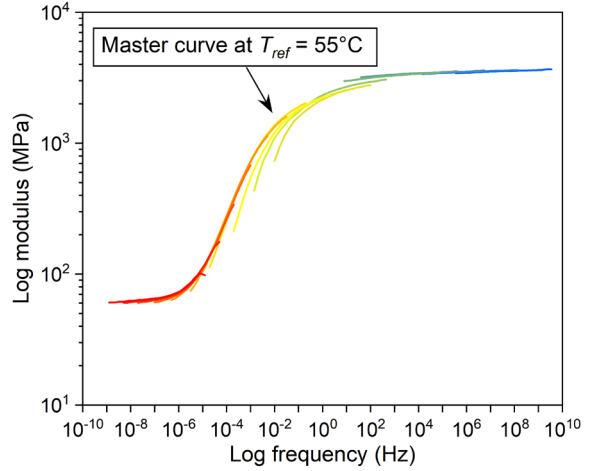
201
 202
 203 According to TTSP, as shown in Figure 6, the horizontal shift was applied to the individual
 204 measurements (Figure 4) to form the master curve at the reference temperature of 55 °C (Figure
 205 6 (b)), which is the closest temperature step to the adhesive's onset T_g , where the modulus
 206 begins to drop significantly. The determined shift factors (α_T) are fitted to the well-known
 207 Williams-Landel-Ferry (WLF) equation (Figure 6 (c)) [28,30]:

$$\log(\alpha_T) = \frac{-C_1(T - T_{ref})}{C_2 + (T - T_{ref})} \quad (1)$$

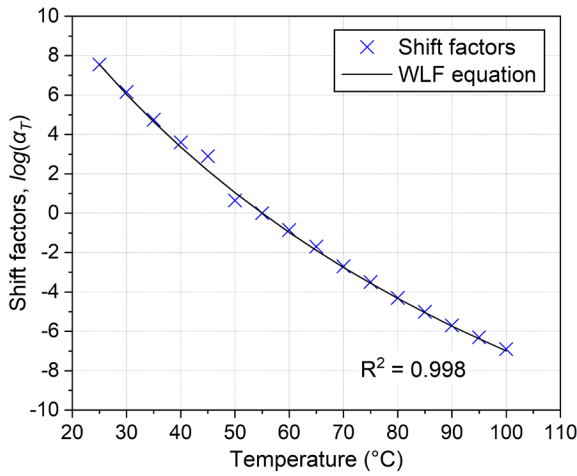
208
 209 where T is the temperature of interest, $C_1 = 30.48$ and $C_2 = 151.14$ (°C) are obtained calibration
 210 constants. The corresponding shifted loss modulus using the same shift factors are illustrated
 211 in Figure 6 (d), showing a good continuity as well.



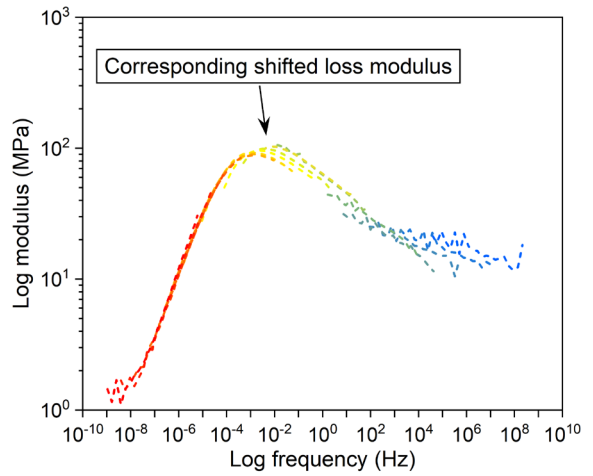
(a) horizontal shift according to TTSP



(b) obtained modulus master curve



(c) shifted factors fitted to WLF equation



(d) corresponding shifted loss modulus

Figure 6: Master curve at $T_{ref} = 55^\circ\text{C}$ obtained using TTSP

212
213

214
215

216

217

218 3 Material modelling

219 3.1 Calibration of the linear viscoelastic material model

220 A Prony series, expressing the generalised Maxwell model, was used for the linear
221 viscoelastic model, which is an in-built material model in the Abaqus analysis software. The
222 shifted storage modulus and loss modulus shown in Figure 6 were fitted to a Prony series in
223 the frequency domain [43,44]:

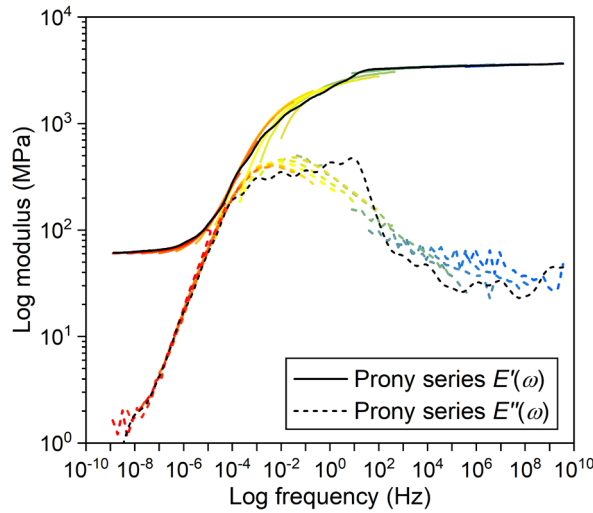
$$224 \quad E'(\omega) = E_0 \left(1 - \sum_{i=1}^n e_i \right) + E_0 \sum_{i=1}^n \frac{\omega^2 \tau_i^2 e_i}{\omega^2 \tau_i^2 + 1} \quad (2)$$

225
$$E''(\omega) = E_0 \sum_{i=1}^n \frac{\omega \tau_i e_i}{\omega^2 \tau_i^2 + 1} \quad (3)$$

226 where E_0 is the instantons elastic modulus, $E'(\omega)$ is the storage modulus, $E''(\omega)$ is the loss
 227 modulus, ω is the angular frequency, and i presents the number of terms in Prony series. τ_i and
 228 e_i are the parameters indicating the relaxation times and relaxation modulus respectively. In
 229 addition, in the Abaqus, a Prony series in time domain using the same parameters can be used
 230 to calculate the time-dependent modulus response [43,44]:

231
$$E(t) = E_0 \left[1 - \sum_{i=1}^n e_i (1 - e^{-t/\tau_i}) \right] \quad (4)$$

232 The fitting results are illustrated in Figure 7 and the obtained parameters are presented in
 233 Table 2. In general, the fitting is satisfactory, and it is typical for the Prony series that the fitting
 234 to the storage modulus is more accurate than the fitting to the loss modulus [16,28,42].
 235 However, in many studies, the fitting to the loss modulus is ignored or not shown [21,25,30,31],
 236 which makes the accuracy of fitting unclear.



237
 238 Figure 7: Comparison of Prony series fitting versus shifted experimental values

239 Table 2: Parameters of the obtained viscoelastic material model

Prony series			
τ_i (s)	e_i	τ_i (s)	e_i
1×10^{-10}	0.0224	1×10^1	0.1295

1×10^{-9}	0.0180	1×10^2	0.1333
1×10^{-8}	0.0057	1×10^3	0.1213
1×10^{-7}	0.0137	1×10^4	0.0724
1×10^{-6}	0.0124	1×10^5	0.0147
1×10^{-5}	0.0084	1×10^6	0.0043
1×10^{-4}	0.0186	1×10^7	0.0008
1×10^{-3}	0.0196	1×10^8	0.0007
1×10^{-2}	0.0136	$\sum e_i = 0.9836$	
1×10^{-1}	0.2141	$E_0 = 3730 \text{ MPa}; \mu_0 = 0.45$	
1×10^0	0.1601	$k_i = 0$	
WLF equation			
$T_{ref} = 55 \text{ }^\circ\text{C}$	$C_1 = 30.48$	$C_2 = 151.14 \text{ (}^\circ\text{C)}$	

240

241 For simplicity, the bulk modulus (k_i) and Poisson's ratio (μ_0) of the adhesive are considered
242 to be independent of time (Table 2), which is usually acceptable for polymers [16,43,44]. In
243 Section 4, the above parameters are applied into the Abaqus FE software to analyse the joint
244 creep behaviour caused by the thermal-viscoelastic response of the adhesive layer. The
245 viscoelasticity of the adhesive is defined by entering each term of the Prony series (τ_i , e_i , and
246 k_i) through the Abaqus *material-viscoelastic* option, while the temperature dependence is
247 defined through the sub-option, *Trs*, using the WLF equation parameters (T_{ref} , C_1 , and C_2).

248

249 3.2 Accuracy investigation of the obtained material model

250 Figure 8 illustrates a comparison between the predicted values of the viscoelastic material
251 model (Prony series) and the original experimental values illustrated in Section 2.2.

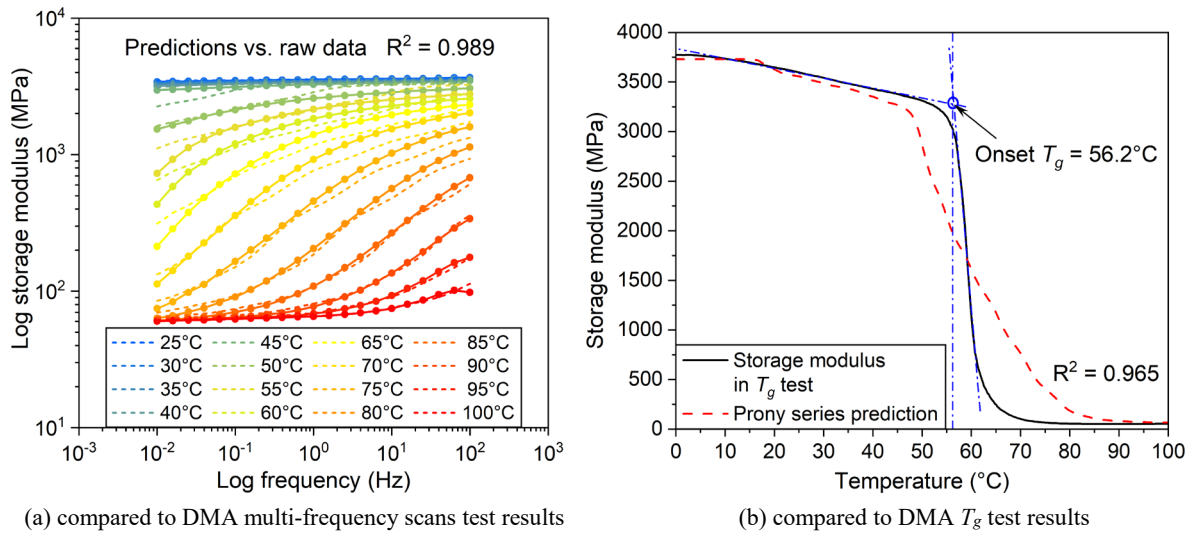


Figure 8: Comparison of viscoelastic model predictions versus raw experimental values

As shown in Figure 8 (a), the material model developed through the TTSP shifting and curve fitting processes has a high accuracy in expressing the raw viscoelastic modulus response of the adhesive.

However, as shown in Figure 8 (b), compared to the modulus response in the DMA T_g test (Section 2.2.1), the predicted modulus decreases more slowly around the T_g . This could be due to the further curing of the examined adhesive sample during DMA multi-frequency scans test at high temperatures, which has received little attention in literatures. In real life applications, the adhesive may also have further curing at elevated ambient temperatures during the long-term service, which to some extent counteracts the effect of further curing of the sample in the accelerated chacterising test. Further investigation of this issue was not possible within the current study, but nevertheless the comparison shown in here identifying the need for further research.

4 Numerical study of the behaviour of the FRP-to-steel joint

This section presents an FE analysis of an adhesive-bonded single lap-shear joint to investigate the effect of elevated temperatures on the behaviour of bonded joints in civil

271 engineering applications. The constitutive material model developed in Section 3 was used to
272 determine the time-temperature dependent viscoelasticity of the adhesive layer.

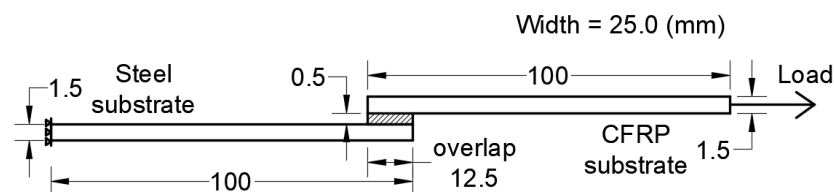
273 Three temperature levels were applied:

- 274 • 30 °C, being a slightly warmer temperature compared to the ambient condition;
- 275 • 40 °C, which is a potential elevated temperature in civil engineering conditions;
- 276 • 50 °C, which is consistent with the maximum operating temperature stipulated in current
277 design guidelines, which should be a minimum of 15 °C below the peak $\text{Tan } \delta T_g$, giving
278 a 51.4 °C (66.4 °C - 15 °C) for the studied adhesive [7,23,24].

279

280 4.1 FE model for the adhesive-bonded single lap-shear joint

281 Figure 9 shows the geometry of the studied lap-shear joint, which was developed according
282 to BS 5350-C5 [45].



283 Figure 9: Geometry of the adhesive-bonded single lap-shear joint (dimensions in mm)
284

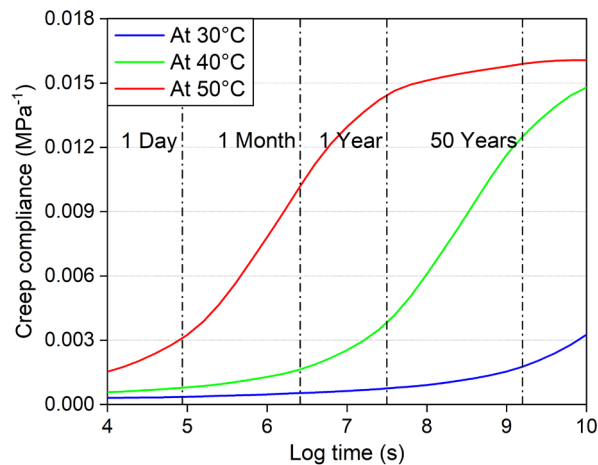
285 The joint was modelled in Abaqus using CPS4R planar stress elements with reduced
286 integration and hourglass control to limit the stress singularity effect [44,46]. Finer meshes
287 (0.1 mm) were applied to the area close to the overlap. The CFRP substrate was modelled as
288 elastic with a Yong's modulus of 170 GPa and a Poisson's ratio of 0.3, while the steel substrate
289 was modelled as elasto-plastic with a Young's modulus of 205 GPa, a yield strength of 355
290 MPa and a Poisson's ratio of 0.3. The adhesive layer was defined as viscoelastic material. The
291 temperature was uniformly applied to all parts of the model. The load of 1 kN was applied to
292 the CFRP substrate, which can result in a high instantaneous stress in the adhesive joint (but
293 below the strength of the adhesive [32]) to investigate the behaviour of stress redistribution.

294 Note that this study focuses on the impact of viscoelastic creep of the structural adhesive on
295 the response of the FRP-to-steel bonded joint. The joint damage related to the strength of the
296 joint is not within the scope of this study, as a result, perfect bond was assumed between
297 different sections.

298

299 4.2 The effect of viscoelasticity of the adhesive on the bonded joint

300 Figure 10 illustrates the creep compliances of the studied adhesive at elevated temperatures,
301 which were obtained from a single cube element (C3D8) model, whilst it can also be calculated
302 from equation (1) and (4).



303
304

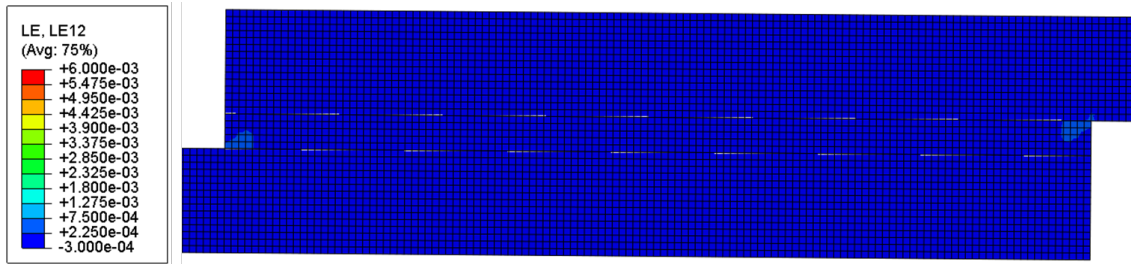
Figure 10: Creep compliances of the viscoelastic adhesive at various temperatures

305 The constitutive material model is sufficient to predict creep over the temperature range
306 examined up to 50 years. After 50 years at 30 °C, the creep compliance of the adhesive
307 increases almost as much as that after only 1 month at 40 °C, and even less than that after 1
308 day at 50 °C. Temperature has a great influence on the viscoelastic creep response of the
309 adhesive, which will therefore affect the long-term behaviour of the adhesive bonded joint.

310 Figure 11 shows the effect of adhesive creep at 50 °C on the distribution of shear strain
311 (LE12) and shear stress (S12) of the single lap-shear bonded joint. After 50 years (Figure 11
312 (b) and (d)), compared to the instantaneous behaviour of the joint (Figure 11 (a) and (c)), creep

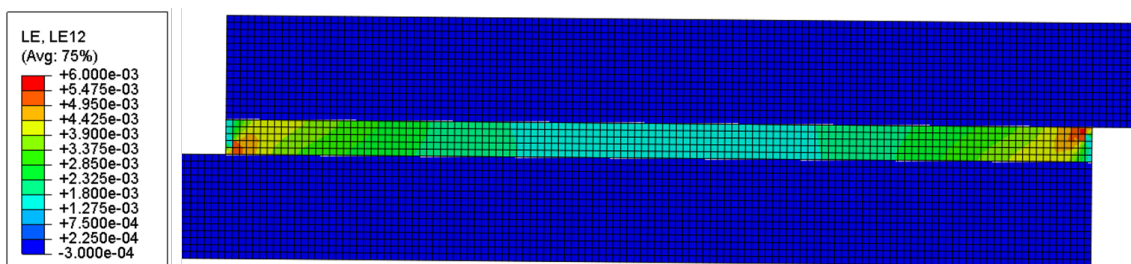
313 of the adhesive leads to a significant increase in the shear strain, however, it is accompanied
 314 by a redistribution behaviour of the shear stress, which reduces the concentrated shear stress at
 315 the edges of the joint and increases the effective stress transfer length.

316



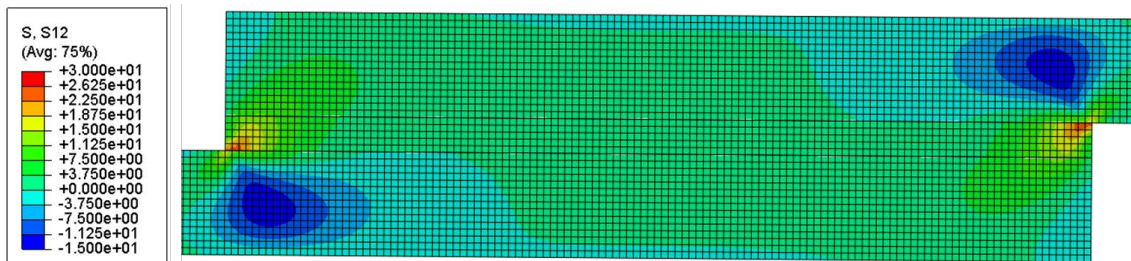
(a) instantaneous shear strain distribution after deformation

318



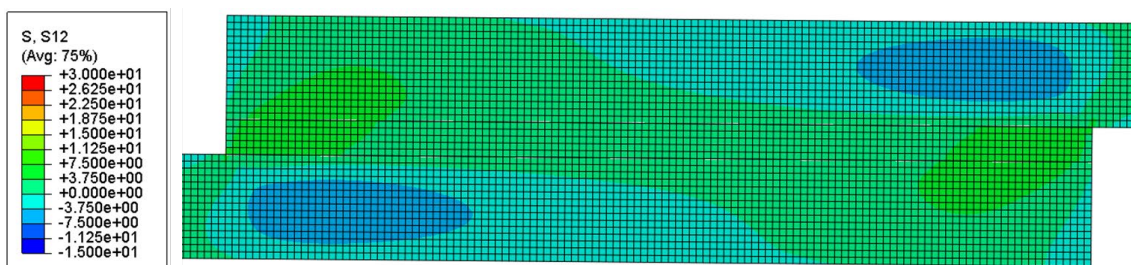
(b) shear strain redistribution after 50 years

320



(c) instantaneous shear stress distribution after deformation

322



(d) shear stress redistribution after 50 years

324

Figure 11: Distribution of the shear strain and shear stress of the bonded joint at 50 °C

325

Figure 12 depicts the detailed changes in the maximum (concentrated) shear strain and shear stress at the edge of the joint over a period of 50 years at 30 °C, 40 °C, and 50 °C, respectively.

326

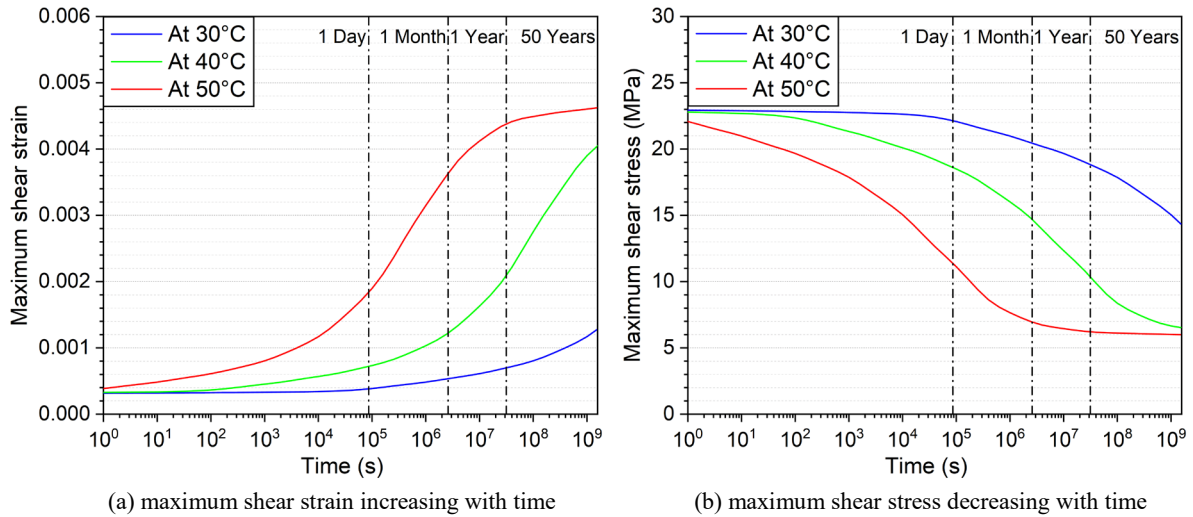


Figure 12: The shear strain and shear stress at the edge of the adhesive joint varying with time at different temperatures

At 30 °C, the maximum shear stress starts to decrease significantly after about 1 day due to the redistribution of stresses resulting from the viscoelastic behaviour of the adhesive layer. After 50 years, the maximum shear stress decreases by almost 37 % from about 23 MPa to 14.5 MPa, and the shear strain only increases by less than 0.001. This could be beneficial for the long-term performance of the bonded joint.

At 40 °C, the maximum shear stress begins to decrease within a few minutes, however, it is accompanied by a sharp rise in the rate of shear strain increase. Whilst the maximum shear stress decreases to about 6.5 MPa after 50 years, the maximum shear strain increased by more than three times compared to the results at 30 °C.

At 50 °C, the maximum shear stress and shear strain change significantly within the first year of use. This may indicate that the first year of service life of the bonded structure is critical under high operating temperature conditions, as creep in the joint may introduce significant shear strain, resulting in limited effectiveness of the bonded strengthening and the potential of early debonding failure.

5 Conclusions

346 In this study, a viscoelastic material model was developed for a typical structural epoxy
347 adhesive (Sikadur[®]-330 [32]) by applying an accelerated test method involving dynamic
348 mechanical analysis (DMA) and time-temperature superposition principle (TTSP), which was
349 utilised to investigate the effects of elevated temperatures on the response of the adhesive-
350 bonded FRP-to-steel joint.

351 The process of the accelerated tests has been illustrated and the limitations of applying this
352 method have been discussed:

- 353 • The thermal stability of studied samples should be examined prior to performing DMA
354 characterisation tests at high temperatures (> 100 °C).
- 355 • Materials that obey TTSP should be thermorheologically simple, which can be
356 confirmed using the wicket plot.
- 357 • DMA tests may be challenging to characterise the nonlinear viscoelasticity of the
358 sample, and the sample can be further cured in high temperature tests.

359 Whilst the accelerated test method has some limitations and requires further research, it
360 remains a viable option for estimating the long-term behaviour of bonded joints, as it is
361 impractical to carry out the conventional sustained load creep tests for decades to fully cover
362 the design life of civil engineering structures.

363 The numerical study results of the single lap-shear FRP-to-steel joint indicate that:

- 364 • Elevated temperatures have a great influence on the creep response of the adhesive layer.
365 The creep can lead to a significant increase in the shear strain of the adhesive joint
366 accompanied by a redistribution behaviour of the shear stress, which reduces the
367 concentrated shear stress at the edges of the joint and increases the effective stress
368 transfer length.

369 • A slightly warmer temperature (30 °C for this study) than ambient environments is
370 considered to be beneficial for the bonded joint as it can reduce the concentrated shear
371 stress (by 37 % after 50 years) with negligible increase in the shear strain (by 0.001
372 after 50).

373 • However, higher temperatures (≥ 40 ° C in this study) significantly increase the creep
374 rate of the adhesive, resulting in a multifold increase in shear strain of the joint with
375 limited reduction in the shear stress, which can be detrimental.

376 For cyclic (oscillating) temperature conditions, when the maximum temperature exceeds
377 40 °C, attention should also be paid to the detrimental effects of viscoelastic creep on bonded
378 joints [47].

379 The available characterisation data and material models for adhesives used in civil
380 engineering are limited. The developed viscoelastic model can be used for further numerical
381 analysis as long as the applied adhesive is the same and has a similar T_g . For other structural
382 adhesives, it will be necessary to carry out similar tests and modelling work (described in
383 Section 2 and 3) to develop the corresponding material models.

384 The long-term creep failure of the joints tends to lead to interface fracture in FRP-
385 strengthened structures, which has so far lacked satisfactory explanations and predictions. The
386 constitutive material model developed in this paper focuses on analysing the viscoelasticity of
387 the structural adhesive, whereas for the future study, the plasticity and the damage of the FRP-
388 to-steel bonded joint will also be significant to investigate.

389

390 **CRedit authorship contribution statement**

391 **S. Wang:** Methodology, Formal analysis, Investigation, Writing - original draft,
392 Visualization. **T. Stratford:** Conceptualization, Resources, Writing - review & editing. **T.P.S.**
393 **Reynolds:** Writing - review & editing.

394

395 **Declaration of competing interest**

396 The authors declare that they have no known competing financial interests or personal
397 relationships that could have appeared to influence the work reported in this paper.

398

399 **Acknowledgments**

400 The authors are grateful for the support from the International Collaborative Research Fund
401 for Young Scholars in the Innovation Demonstration Base of Ecological Environment
402 Geotechnical and Ecological Restoration of Rivers and Lakes. This work was funded by the
403 Doctoral Research Starting Foundation of Hubei University of Technology under Grant
404 [XJ2022001301].

405

406 **References**

- 407 [1] Karbhari VM, Shulley SB. Use of Composites for Rehabilitation of Steel Structures—Determination of Bond
408 Durability. *J Mater Civ Eng* 1995;7:239–45. [https://doi.org/10.1061/\(asce\)0899-1561\(1995\)7:4\(239\)](https://doi.org/10.1061/(asce)0899-1561(1995)7:4(239)).
- 409 [2] Higgins A. Adhesive bonding of aircraft structures. *Int J Adhes Adhes* 2000;20:367–76.
410 [https://doi.org/10.1016/S0143-7496\(00\)00006-3](https://doi.org/10.1016/S0143-7496(00)00006-3).
- 411 [3] Heshmati M, Haghani R, Al-Emrani M. Environmental durability of adhesively bonded FRP/steel joints in civil
412 engineering applications: State of the art. *Compos Part B Eng* 2015;81:259–75.
413 <https://doi.org/10.1016/j.compositesb.2015.07.014>.
- 414 [4] Hollaway LC, Teng JG. *Strengthening and Rehabilitation of Civil Infrastructures Using Fibre-Reinforced Polymer*
415 *(FRP) Composites*. Woodhead Publishing Ltd, UK; 2008.
- 416 [5] Heshmati M, Haghani R, Al-Emrani M. Durability of CFRP/steel joints under cyclic wet-dry and freeze-thaw
417 conditions. *Compos Part B Eng* 2017;126:211–26. <https://doi.org/10.1016/j.compositesb.2017.06.011>.

- 418 [6] Ascione F, Granata L, Guadagno L, Naddeo C. Hygrothermal durability of epoxy adhesives used in civil structural
419 applications. *Compos Struct* 2021;265:113591. <https://doi.org/10.1016/j.compstruct.2021.113591>.
- 420 [7] Cadei JMC, Stratford TJ, Hollaway LC, Dcukett WG. Strengthening metallic structures using externally bonded fibre-
421 reinforced polymers. Construction Industry Research and Information Association (CIRIA), London, UK; 2004.
- 422 [8] Zhao XL, Zhang L. State-of-the-art review on FRP strengthened steel structures. *Eng Struct* 2007;29:1808–23.
423 <https://doi.org/10.1016/j.engstruct.2006.10.006>.
- 424 [9] Zhao X-L. FRP-strengthened metallic structures. Taylor and Francis, Boca Rotan, FL; 2013.
- 425 [10] Heshmati M, Haghani R, Al-Emrani M. Durability of bonded FRP-to-steel joints Effects of moisture, de-icing salt
426 solution, temperature and FRP type. *Compos Part B Eng* 2017;119:153–67.
427 <https://doi.org/10.1016/j.compositesb.2017.03.049>.
- 428 [11] He J, Xian G, Zhang YX. Numerical modelling of bond behaviour between steel and CFRP laminates with a ductile
429 adhesive. *Int J Adhes Adhes* 2021;104:102753. <https://doi.org/10.1016/j.ijadhadh.2020.102753>.
- 430 [12] Ascione F, Granata L, Lombardi A. The influence of the hygrothermal aging on the strength and stiffness of adhesives
431 used for civil engineering applications with pultruded profiles: an experimental and numerical investigation. *J Adhes*
432 2022;98:1733–1771. <https://doi.org/10.1080/00218464.2021.1936507>.
- 433 [13] Ascione F, Granata L, Carozzi G. Flexural and shear behaviour of adhesive connections for large scale GFRP frames:
434 Influence of the bonded area and hygro-thermal aging. *Compos Struct* 2022;283:115122.
435 <https://doi.org/10.1016/j.compstruct.2021.115122>.
- 436 [14] Teng JG, Yu T, Fernando D. Strengthening of steel structures with fiber-reinforced polymer composites. *J Constr*
437 *Steel Res* 2012;78:131–43. <https://doi.org/10.1016/j.jcsr.2012.06.011>.
- 438 [15] Shishesaz M, Hosseini M. Effects of joint geometry and material on stress distribution, strength and failure of bonded
439 composite joints: an overview. *J Adhes* 2020;96:1053–121. <https://doi.org/10.1080/00218464.2018.1554483>.
- 440 [16] Agha A, Abu-Farha F. Viscoelastic model to capture residual stresses in heat cured dissimilar adhesive bonded joints.
441 *Int J Adhes Adhes* 2021;107:102844. <https://doi.org/10.1016/j.ijadhadh.2021.102844>.
- 442 [17] Feng CW, Keong CW, Hsueh YP, Wang YY, Sue HJ. Modeling of long-term creep behavior of structural epoxy
443 adhesives. *Int J Adhes Adhes* 2005;25:427–36. <https://doi.org/10.1016/j.ijadhadh.2004.11.009>.
- 444 [18] Cree D, Gamaniouk T, Loong ML, Green MF. Tensile and Lap-Splice Shear Strength Properties of CFRP Composites
445 at High Temperatures. *J Compos Constr* 2015;19:04014043. [https://doi.org/10.1061/\(asce\)cc.1943-5614.0000508](https://doi.org/10.1061/(asce)cc.1943-5614.0000508).
- 446 [19] de Zeeuw C, Teixeira de Freitas S, Zarouchas D, Schilling M, Lopes Fernandes R, Dolabella Portella P, et al. Creep
447 behaviour of steel bonded joints under hygrothermal conditions. *Int J Adhes Adhes* 2019;91:54–63.
448 <https://doi.org/10.1016/j.ijadhadh.2019.03.002>.
- 449 [20] Ke L, Li C, He J, Dong S, Chen C, Jiao Y. Effects of elevated temperatures on mechanical behavior of epoxy
450 adhesives and CFRP-steel hybrid joints. *Compos Struct* 2020;235. <https://doi.org/10.1016/j.compstruct.2019.111789>.

- 451 [21] Shim W, Jang J, Choi JH, Cho JM, Yoon SJ, Choi CH, et al. Simulating rate- and temperature-dependent behaviors
452 of adhesives using a nonlinear viscoelastic model. *Mech Mater* 2020;147:103446.
453 <https://doi.org/10.1016/j.mechmat.2020.103446>.
- 454 [22] Zhang Y, Li W, Rui Y, Wang S, Zhu H, Yan Z. A modified cellular automaton model of pedestrian evacuation in a
455 tunnel fire. *Tunn Undergr Sp Technol* 2022;130:104673. <https://doi.org/10.1016/j.tust.2022.104673>.
- 456 [23] National Research Council Advisory Committee. Guidelines for the design and construction of externally bonded
457 FRP systems for strengthening existing structures - metallic structures. Rome, Italy: National Research Council; 2007.
- 458 [24] American Concrete Institute (ACI), Aci 440.2R-08: Guide for the design and construction of externally bonded FRP
459 systems for strengthening concrete structures. USA; 2008.
- 460 [25] Houhou N, Benzarti K, Quiertant M, Chataigner S, Fléty A, Marty C. Analysis of the nonlinear creep behavior of
461 concrete/FRP-bonded assemblies. *J Adhes Sci Technol* 2014;28:1345–66.
462 <https://doi.org/10.1080/01694243.2012.697387>.
- 463 [26] Nguyen TC, Bai Y, Zhao XL, Al-Mahaidi R. Mechanical characterization of steel/CFRP double strap joints at
464 elevated temperatures. *Compos Struct* 2011;93:1604–12. <https://doi.org/10.1016/j.compstruct.2011.01.010>.
- 465 [27] Sahin MU, Dawood M. Experimental Investigation of Bond between High-Modulus CFRP and Steel at Moderately
466 Elevated Temperatures. *J Compos Constr* 2016;20:04016049. [https://doi.org/10.1061/\(asce\)cc.1943-5614.0000702](https://doi.org/10.1061/(asce)cc.1943-5614.0000702).
- 467 [28] Menard K, Menard N. *Dynamic Mechanical Analysis*, 3rd ed. CRC Press, Boca Rotan, FL, USK; 2020.
- 468 [29] Rouleau L, Deü JF, Legay A, Le Lay F. Application of Kramers-Kronig relations to time-temperature superposition
469 for viscoelastic materials. *Mech Mater* 2013;65:66–75. <https://doi.org/10.1016/j.mechmat.2013.06.001>.
- 470 [30] Abouhamzeh M, Sinke J, Jansen KMB, Benedictus R. Kinetic and thermo-viscoelastic characterisation of the epoxy
471 adhesive in GLARE. *Compos Struct* 2015;124:19–28. <https://doi.org/10.1016/j.compstruct.2014.12.069>.
- 472 [31] Wang S, Stratford T, Reynolds TPS. Linear creep of bonded FRP-strengthened metallic structures at warm service
473 temperatures. *Constr Build Mater* 2021;283:122699. <https://doi.org/10.1016/j.conbuildmat.2021.122699>.
- 474 [32] SIKA. Sikadur®-330 Data Sheet. Sika Construction Chemicals; 2017.
- 475 [33] Chin J, Forster A, Clerici C, Hunston D. Characterization of ambient temperature cure epoxies used in adhesive
476 anchor applications. *J Adhes* 2010;86:1041–67. <https://doi.org/10.1080/00218464.2010.515494>.
- 477 [34] Qin G, Na J, Mu W, Tan W, Yang J, Ren J. Effect of continuous high temperature exposure on the adhesive strength
478 of epoxy adhesive, CFRP and adhesively bonded CFRP-aluminum alloy joints. *Compos Part B Eng* 2018;154:43–55.
479 <https://doi.org/10.1016/j.compositesb.2018.07.059>.
- 480 [35] Hidalgo-Salazar MA, Correa JP. Mechanical and thermal properties of biocomposites from nonwoven industrial
481 Fique fiber mats with Epoxy Resin and Linear Low Density Polyethylene. *Results Phys* 2018;8:461–7.
482 <https://doi.org/10.1016/j.rinp.2017.12.025>.
- 483 [36] ISO E. 11358-1: 2014—Plastics—Thermogravimetry (TG) of Polymers—Part 1: General Principles. International

- 484 Organization of Standardization: Geneva, Switzerland; 2014.
- 485 [37] Del Prete I, Bilotta A, Bisby L, Nigro E. Elevated temperature response of RC beams strengthened with NSM FRP
486 bars bonded with cementitious grout. *Compos Struct* 2021;258:113182.
487 <https://doi.org/10.1016/j.compstruct.2020.113182>.
- 488 [38] British Standards Institutions. BSI Standards Publication Plastics — Determination of dynamic mechanical properties.
489 BS ISO 6721:2019; 2019. <https://doi.org/https://doi.org/10.3403/BSISO6721>.
- 490 [39] Adams RD. Adhesive bonding : science, technology and applications. Boca Raton, FL : Cambridge: CRC Press ; 2005.
- 491 [40] Wang S, Stratford T, Reynolds TPS. A comparison of the influence of nonlinear and linear creep on the behaviour of
492 FRP-bonded metallic beams at warm temperatures. *Compos Struct* 2022;281:115117.
493 <https://doi.org/10.1016/j.compstruct.2021.115117>.
- 494 [41] Knapp G, Oreski G, Pinter G. Method to characterize the damping behavior of thin passively constrained layer
495 laminates using dynamic mechanical analysis (DMA) in shear mode. *Polym Test* 2015;42:215–24.
496 <https://doi.org/10.1016/j.polymertesting.2015.01.011>.
- 497 [42] Springer M, Bosco N. Linear viscoelastic characterization of electrically conductive adhesives used as interconnect
498 in photovoltaic modules. *Prog Photovoltaics Res Appl* 2020;28:659–81. <https://doi.org/10.1002/pip.3257>.
- 499 [43] Barbero EJ. Finite element analysis of composite materials using AbaqusTM. CRC press; 2013.
- 500 [44] Abaqus. ABAQUS user’s manual 6.14. ABAQUS Inc; 2014.
- 501 [45] British Standards Institutions. BSI. BS 5350-C5:2002 Methods of Test for Adhesives. Determination of Bond
502 Strength in Longitudinal Shear for Rigid Adherends. 2002.
- 503 [46] Teng JG, Zhang JW, Smith ST. Interfacial stresses in reinforced concrete beams bonded with a soffit plate: A finite
504 element study. *Constr Build Mater* 2002;16:1–14. [https://doi.org/10.1016/S0950-0618\(01\)00029-0](https://doi.org/10.1016/S0950-0618(01)00029-0).
- 505 [47] Wang S, Stratford T, Reynolds TPS. Creep of an FRP-strengthened metallic beam under cyclic temperature and cyclic
506 load. *J Constr Steel Res* 2022;196:107417. <https://doi.org/10.1016/j.jcsr.2022.107417>.
- 507