



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

## Ballistic response of needlepunched nonwovens

### Citation for published version:

Martinez-Hergueta, F, Ridruejo, A, González, CA & LLorca, J 2022, Ballistic response of needlepunched nonwovens. in VV Silberschmidt (ed.), *Mechanics of Fibrous Networks*. Mechanics of Advanced Materials, Elsevier, pp. 241-261. <https://doi.org/10.1016/B978-0-12-822207-2.00011-8>

### Digital Object Identifier (DOI):

[10.1016/B978-0-12-822207-2.00011-8](https://doi.org/10.1016/B978-0-12-822207-2.00011-8)

### Link:

[Link to publication record in Edinburgh Research Explorer](#)

### Published In:

Mechanics of Fibrous Networks

### General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

### Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact [openaccess@ed.ac.uk](mailto:openaccess@ed.ac.uk) providing details, and we will remove access to the work immediately and investigate your claim.



# Ballistic response of needlepunched nonwovens

F. Martínez-Hergueta<sup>1</sup>, A. Ridruejo<sup>2</sup>, C. González<sup>2,3</sup>, J. LLorca<sup>2,3</sup>

<sup>1</sup> *School of Engineering, Institute for Infrastructure and Environment, The University of Edinburgh, William Rankine Building, EH9 3FG, Edinburgh, UK.*

<sup>2</sup> *Department of Materials Science, Universidad Politécnica de Madrid, E. T. S. de Ingenieros de Caminos. 28040 - Madrid, Spain.*

<sup>3</sup> *IMDEA Materials Institute, C/ Eric Kandel 2, 28906, Getafe, Madrid, Spain.*

---

## Abstract

Needlepunched nonwoven fabrics manufactured with high strength fibres present lower stiffness and strength than their woven counterparts, but possess much higher deformability and energy absorption capacity, leading to excellent ballistic performance against small calibres. Although their potential advantages, very little is known about their deformation and fracture micromechanisms at the microscopic level and how they contribute to macroscopic mechanical properties such as ballistic limit. This lack of knowledge hinders the optimisation of their mechanical performance and also limits their implementation in structural applications. This chapter aims to review the response of needlepunched nonwovens subjected to ballistic impact. The experimental dynamic characterisation is conducted through a combination of Split-Hopkinson bar and impact tests. These procure the wave propagation phenomenon, the dominant deformation micromechanisms at high-strain rates and the residual velocity curves, including the ballistic limit. Additionally, a Finite Element Digital Twin is implemented in the software Abaqus/Explicit to explore the influence of the microstructure in the ballistic performance of the material. The numerical model is validated against previous experimental results and it is employed to analyse the potential of the material to improve the performance of targets such as dry woven fabrics and metal sheets. The addition of the nonwoven layer increases substantially the specific energy absorption capacity of the system, with a negligible increment of the total areal weight of the target.

*Keywords:* Needle punched nonwoven, ballistic, Finite Element Digital Twin

## 1. Introduction

Fibre based dry fabrics are a lightweight solution for ballistic protection conventionally extended in the defence sector in a large variety of applications including soft vehicle and body armour [1, 2]. Depending on their architecture, the fabrics can be classified into two categories: wovens and nonwovens, see Fig. 1. Woven fabrics exhibit a homogeneous distribution where fibres are bundled in yarns weaved into regular patterns, while nonwovens present a random fibre network connected through local bonds consolidated by thermal fusion, chemical binding or mechanical entanglement [3]. These bonds determine the interaction between fibres and have a primary role in the deformation and ductility of the nonwoven. In particular, the needlepunched mechanical consolidation process results in a lower stiffness and strength (as well as processing cost), but much higher strain to failure than their woven counterparts, resulting in outstanding ductility and energy absorption capacity [4, 5, 6], with excellent ballistic performance against shrapnel and small calibres [7, 8], making nonwovens a perfect cushion layer for conventional dry woven fabric soft body armour shields [9, 10, 11, 12, 13].

Although the impact response of dry woven fabrics based on Kevlar and Dyneema fibres is detailed reported in the literature and their application is conventional in the defense sector [14, 15, 16], the technology readiness level of nonwoven fabrics is still immature and their applications are limited. It is possible to find in the literature a handful of examples focused on damage reduction of rear components [17, 18] or sandwich cores [19, 20], nevertheless, the lack of knowledge regarding the ballistic performance of needlepunched nonwovens hinders the development of predictive design tools and delays their wider implementation in the defence and transport sector. The mechanical response of needlepunched nonwovens subjected to quasi-static tensile loads is detailed reported in the literature [21, 22]. The stiffness of the material is directly proportional to the percentage of fibres oriented with the loading direction and the bond density. The manufacturing process can also induce an anisotropic mechanical response by introducing an heterogeneous connectivity between the fibres. Upon uniaxial deformation, the random fibre network evolves exhibiting progressive

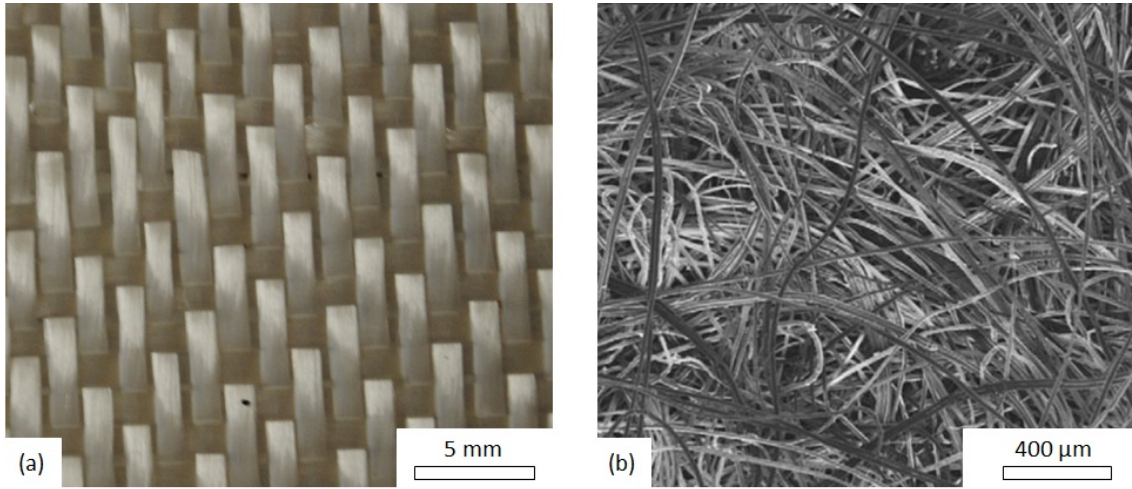


Figure 1: Ultrahigh molecular weight polyethylene fabrics. (a) 3 harness satin dry woven fabric composed of Dyneema SK65 fibre yarns and (b) needlepunched nonwoven fabric composed of Dyneema SK75 fibres.

56 fibre uncurling and rotation. This microstructural evolution leads to a non-linear response of  
57 the material, with increasing tangent stiffness with the deformation. The ductility at large  
58 strains is mainly controlled by frictional deformation micromechanisms such as fibre slid-  
59 ing, slippage and pull-out from the entanglement points (see previous chapter XX). These  
60 physical findings are the basis to develop sound, physically based, constitutive models to  
61 predict the mechanical response of needlepunched nonwovens [23], however, further efforts  
62 are needed to characterise the wave propagation phenomenon and determine the influence  
63 of high strain rates in the mechanical response of the material to extend the constitutive  
64 models to simulate impact events.

65 This chapter aims at reviewing the response of needlepunched nonwovens subjected to  
66 ballistic impact. A detailed experimental dynamic characterisation of the material is accom-  
67 plished through Split-Hopkinson bar and impact tests. These procure the wave propagation  
68 phenomenon, the dominant deformation and failure micromechanisms at high-strain rates  
69 and the residual velocity curves, including the ballistic limit. Additionally, a Finite Element  
70 Digital Twin is developed in the software Abaqus/Explicit to explore potential applications  
71 in the defence and transport sectors. The numerical model is validated against experimental  
72 results and it is employed to analyse the potential of the material to improve the ballistic

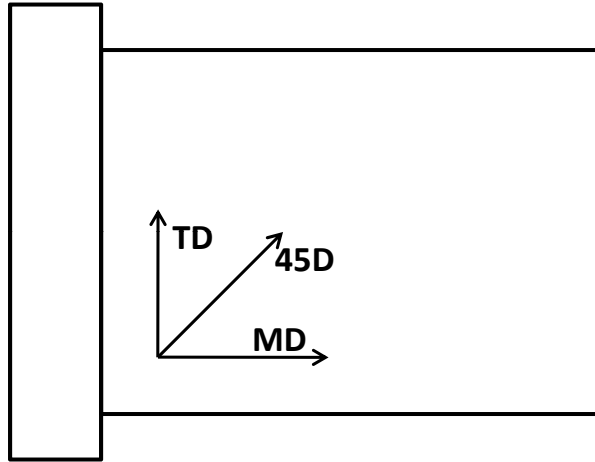


Figure 2: Main material orientations of the fabric. MD stands for machine direction and TD stands for transverse direction.

73 response of conventional targets such as dry woven fabrics and metal sheets. In both cases,  
74 the addition of the nonwoven layer increases substantially the specific energy absorption  
75 capacity of the targets with a minor increment of the total areal weight of the shield.

## 76 **2. Experimental characterisation**

### 77 *2.1. Material*

78 The two-dimensional needlepunched nonwoven is a DSM product commercialised under  
79 the trademark Fraglight NW201. It is composed of Dyneema SK75 ultrahigh molecular  
80 weight polyethylene fibres (UHMWPE) with an approximate length of  $\approx 60$  mm. The  
81 stochastic nature of the material results in a variable thickness of  $\approx 1.5$  to 2 mm and an areal  
82 weight of  $\rho \approx 190$ -220 g/m<sup>2</sup>. The batt is manufactured on a moving bed by continuous fibre  
83 deposition and mechanically entangled by oscillatory barbed needles [3]. This manufacturing  
84 process induces two principal material directions along the bed or machine direction (MD)  
85 and the transverse direction (TD), see Fig. 2. The difference in mechanical properties  
86 between perpendicular directions was pronounced, with higher stiffness and strength along  
87 the TD. The detailed quasi-static characterisation at different scales is available in previous  
88 chapter XX.

89 *2.2. Experimental techniques*

90 *2.2.1. In-plane dynamic tests*

91 The dynamic testing of the nonwoven fabric was conducted on a Split-Hopkinson Tensile  
92 Bar (SHTB) device with high sensitivity and long pulse duration specially designed for low-  
93 impedance fabrics with complex architectures and large Representative Volume Elements.  
94 The input and output bars comprised of Aluminium 7075-T6 alloy hollow tubes of 50.8  
95 mm outer diameter, 1.651 mm wall thickness and 2.7 m in length. The pulse duration was  
96  $T \approx 1$  ms. The fabric was gripped by conical clamps allowing a maximum specimen  
97 width and gauge length of 35 x 35 mm<sup>2</sup>. The samples were stretched at the orientation  
98 transverse to the roll direction (TD), the stiffest direction of the material, see Fig. 3(b).  
99 This experimental set-up resulted in strain rates of  $\dot{\epsilon} \approx 400$  s<sup>-1</sup>, 4 orders of magnitude  
100 higher than the previously reported quasi-static characterisation [22]. Further details of this  
101 SHB equipment are available in [24, 25].

102 The bars were instrumented with three strain gauges, as in Fig. 3(a). Amplifiers and  
103 high frequency oscilloscopes were used to record the signal on the order of millivolts. The  
104 main outcomes were forces and velocities of the bars. The specimens were speckled with a  
105 random pattern and full-field displacement measurements were carried out via high-speed  
106 photography, employing an ultra-high-speed Kirana camera operated at 50.000 fps. 2D  
107 Digital Image Correlation analysis was performed using the commercial software Vic2D.

108 *2.2.2. Ballistic tests*

109 The ballistic experiments were conducted on specimens of 500 x 500 mm<sup>2</sup> fully clamped  
110 along their four edges on a metallic frame with a free surface of 350 x 350 mm<sup>2</sup>. The  
111 projectiles were steel spheres of 5.5 mm in diameter (caliber 0.22) and 0.706 g of mass.  
112 They were propelled by a SABRE A1 + gas gun at velocities between 270 to 400m/s and  
113 impact energies between 25 and 55 J. The initial and residual velocities were monitored  
114 by a high-speed Phantom V12 camera with a resolution of 512 x 256 and 512 x 512 pixels  
115 and rate acquisition between 20.000 to 40.000 fps depending on the test duration. Further  
116 details of the experimental set-up are available in [26].

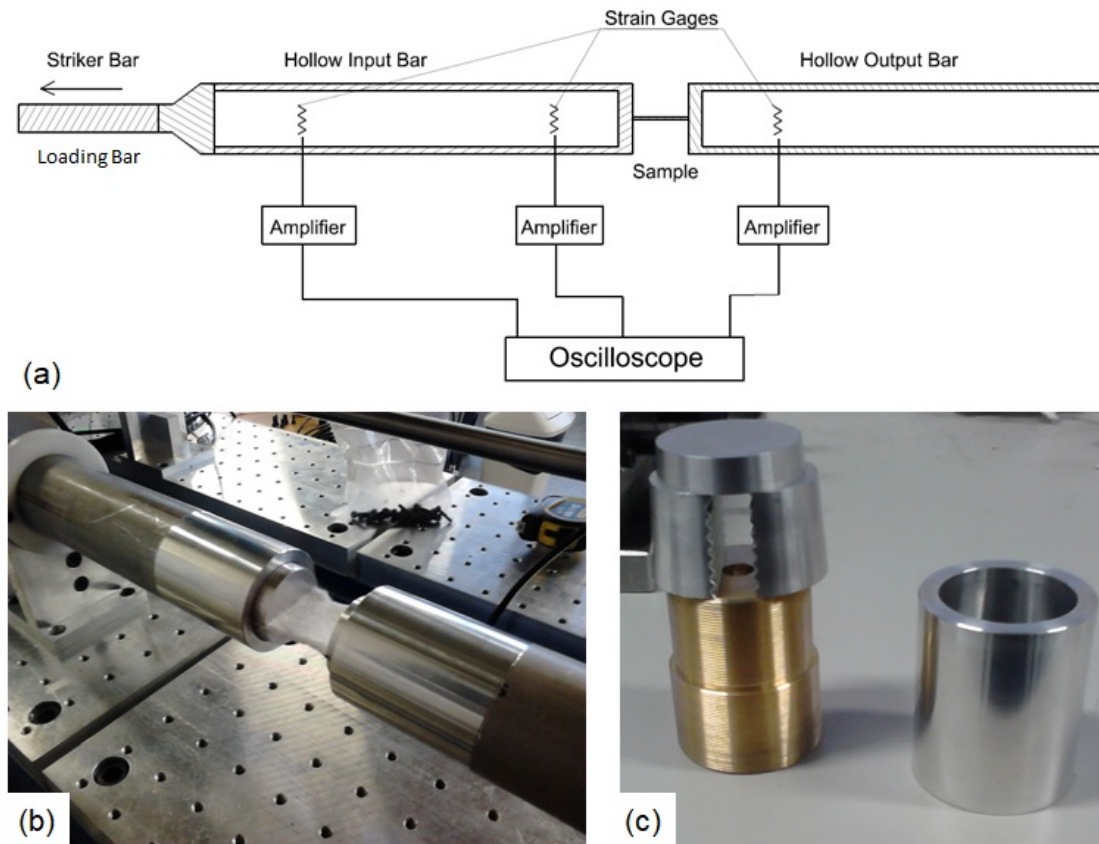


Figure 3: Split-Hopkinson tensile bar experimental set up. (a) Schematic of the different components of the SHTB, (b) gripped specimen between bar ends and (c) aluminium and brass components of the grips [25].

117 *2.3. Experimental results*

118 *2.3.1. High-strain-rate tensile response*

119 The tensile testing at high strain rates was conducted on the SHTB apparatus presented  
 120 in Section 2.2.1. The forces were registered by the strain gauges while the deformation was  
 121 obtained by Digital Image Correlation. The left hand side of Fig. 4 shows the evolution of  
 122 the longitudinal deformation at different stages of the experiment, exhibiting large strain  
 123 gradients across the specimen, in contrast to the characteristic homogeneous strain distri-  
 124 butions obtained at quasi-static loading regimes before the onset of damage in this material  
 125 [22]. At the initial stages of the loading process ( $t = 0.4$  ms), the material acquired an  
 126 oscillating deformation around the 20% as a result of the wave reflection process. After a

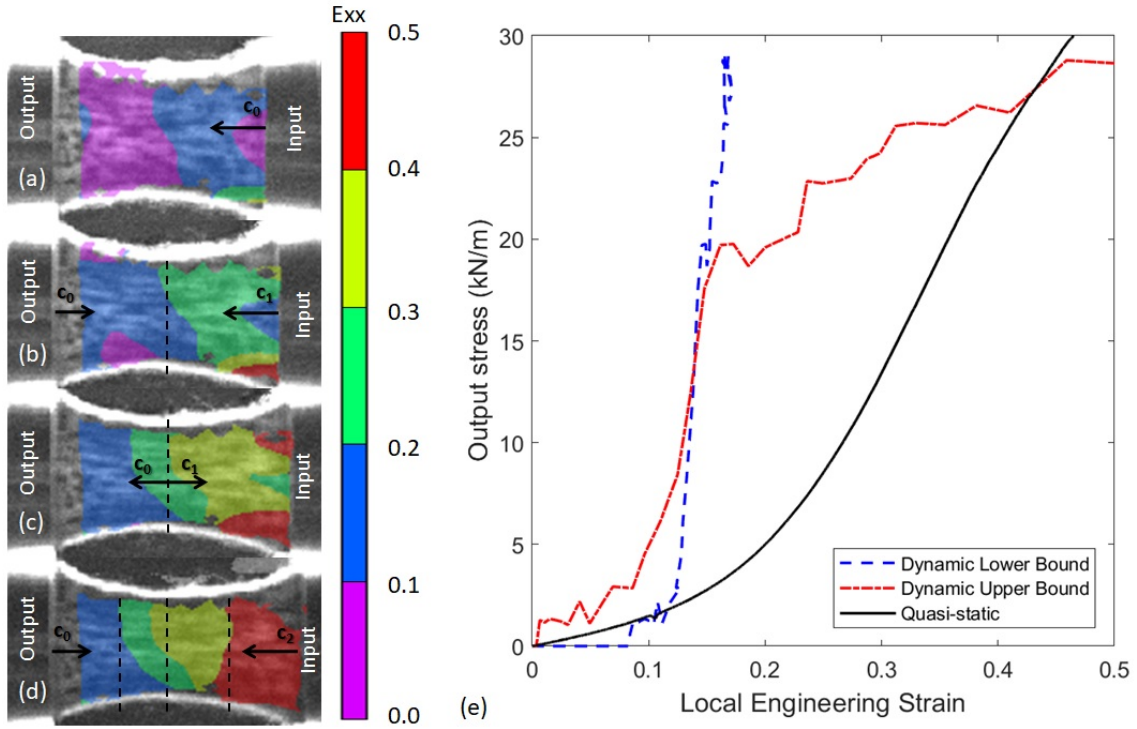


Figure 4: Evolution of the longitudinal strain  $\epsilon_x$  and wave rebound phenomenon. (a)  $t = 0.2$  ms, (b)  $t = 0.4$  ms, (c)  $t = 0.6$  ms, (d)  $t = 0.9$  ms. (e) Output stress *vs.* local engineering strain at the output interface, the lower bound (blue dashed line) and input interface, the upper bound (red dashed line). Quasi-static stress-strain curve has been included for comparison purposes [25].

127 certain instant in time ( $t = 0.6$  ms) the evolution of the strain nearby the output bar froze  
 128 at a maximum value of 18% strain leading to a heterogeneous strain field across the specimen  
 129 with an steep increment of deformation and damage localisation nearby the input bar, see  
 130 Fig. 4(d). This strain gradients indicated a lack of dynamic force equilibrium between the  
 131 bars during the whole duration of the experiment, usually observed during the first stages  
 132 of the dynamic experiment before the input and output forces overlap [27].

133 The dynamic deformation induced progressive fibre straightening, rotation and sliding  
 134 with the loading direction at microstructural level, as previously registered for quasi-static  
 135 uniaxial deformation [22]. This evolution resulted in a non-linear pseudo-plastic mechani-  
 136 cal response of the material with an inherent increment of the tangent stiffness. The fibre  
 137 orientation distribution function was also proportional to the wave speed of the material



138 that increased with the applied deformation. The initial fibre curvature and the random  
139 fibre orientation decreased the effective longitudinal propagation velocity, and the progres-  
140 sive fibre alignment increased the apparent wave speed of the fabric. Additionally, the  
141 magnitude of the tensile waves decreased with the distance with the input interface due to  
142 two different sources of mechanical dissipation: (i) the frictional nature of the deformation  
143 micromechanisms and (ii) the partial wave reflection at the entanglement points.

144 As a result of the variable stiffness and wave propagation velocity with the applied defor-  
145 mation, heterogeneous strain gradients appeared on the specimen during dynamic testing.  
146 The tensile pulse first propagated into the specimen with velocity  $c_0$ , see left hand side of  
147 Fig. 4. After a certain amount of time, the tensile pulse reached the output interface, mean-  
148 while faster waves with a higher stress magnitude appeared at the input interface due to the  
149 non-linear increment of stiffness with fibre realignment ( $c_1 > c_0$ ). Once the transmitted and  
150 reflected waves arrived at the same material point, they created a macromechanical interface  
151 with an impedance mismatch at both sides due to the differences in microstructural evolu-  
152 tion, preventing the propagation of larger strain waves into the left side of the specimen.  
153 The reflections were repeated with waves of higher stress magnitude and velocity over the  
154 test duration ( $c_2 > c_1$ ), generating additional mismatch fronts.

155 The output forces were analysed to determine the influence of the high strain rates in  
156 the mechanical response of the fabric. The Fig. 4(e) plots the output stress monitored by  
157 the strain gauge *vs.* the local longitudinal strains registered by DIC at the input and output  
158 interfaces. The lack of a constant strain over the specimen hindered the acquisition of a  
159 conventional stress-strain curve. These curves are compared against the quasi-static stress-  
160 strain constitutive relationship. A sudden increase in stiffness was registered, reaching a  
161 stress value of 30 kN/m within the range 15-17% deformation, which indicated a significant  
162 strain rate sensitivity of the frictional deformation micromechanisms. Further information  
163 is available in [25].

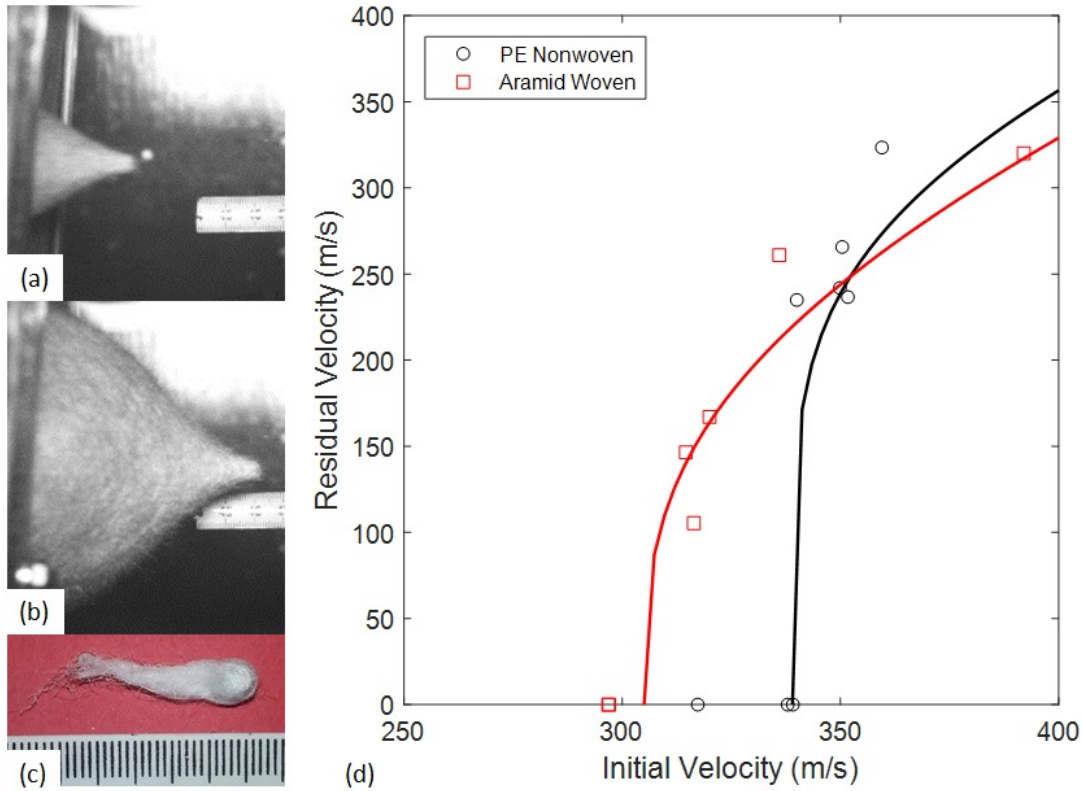


Figure 5: Deformation of the polyethylene nonwoven fabric during impact at the ballistic limit  $v = 338 \text{ m/s}$ . (a)  $t = 175 \mu\text{s}$ . (b)  $t = 1025 \mu\text{s}$ . (c) Extracted fibres around the projectile after impact. (d) Residual velocity curves of the nonwoven fabric (1 layer with equivalent areal weight  $200 \text{ g/m}^2$ ) and comparison with a conventional woven aramid laminate (4 layers with equivalent areal weight  $922 \text{ g/m}^2$ ). The symbols stand for experimental results and the lines for eq. (1) [26].

### 164 2.3.2. Ballistic performance

165 The ballistic experimental campaign was conducted to evaluate the ballistic response of  
 166 the material, obtain the residual velocity curve and identify the ballistic limit,  $v_{50}$ . Fig. 5  
 167 shows an example of the deformation of the fabric subjected to an impact velocity around  
 168 the ballistic limit ( $v = 338 \text{ m/s}$ ). The differences in wave propagation velocities across per-  
 169 pendicular directions (MD and TD) resulted in an elliptical cross-section and the transverse  
 170 wave that followed the deflection of the layer exhibited a cone profile. The needlepunched  
 171 nonwoven absorbed the kinetic energy of the projectile by in-plane deformation. The load

172 was transferred through the mechanical entanglements inducing fibre uncurling, rotation  
 173 and sliding towards the impact point, as previously appreciated during quasi-static and dy-  
 174 namic uniaxial tensile testing. For impact velocities above the ballistic limit, large fibre  
 175 pull-out and final tearing of the layer was registered, see Fig. 5(c). In all the cases, the  
 176 damage was localised at the impact point and large strain gradients were exhibited, similar  
 177 to the ones observed during the Split Hopkinson bar experiments. The thermal softening of  
 178 the directly impacted fibres was also registered and validated through Differential Scanning  
 179 Calorimetry. This resulted in a lower energy absorption capacity at velocities above the  $v_{50}$ .  
 180 Further information is available in [26].

181 The residual velocity curve of the material is shown in Fig. 5(d). The experimental  
 182 results were post-processed to obtain the least squares fitting with the Lambert equation,

$$V_{res} = (V_{ini}^n - V_{50}^n)^{1/n} \quad (1)$$

183 where  $V_{res}$  and  $V_{ini}$  are the residual and initial impact velocities, respectively. The ballistic  
 184 response of the material was compared against the response of a conventional dry woven  
 185 aramid target composed of 4 layers of Kevlar KM2 fibres with an equivalent areal weight  
 186 of 920 g/m<sup>2</sup>. The nonwoven exhibited a ballistic limit of 339 m/s and an energy absorp-  
 187 tion capacity of 40 J, 10 J higher than the maximum energy absorption capacity of the  
 188 aramid protection, even if the nonwoven protection was four times lighter. This experimen-  
 189 tal campaign probes the advantage of nonwovens over woven against ballistic impact for  
 190 small calibres and shrapnel.

### 191 **3. Numerical simulation**

#### 192 *3.1. Numerical implementation*

193 A finite element model of the needlepunched nonwoven was implemented in the software  
 194 Abaqus/Explicit to create a Digital Twin to predict the ballistic response of the material.  
 195 The multiscale constitutive model presented in previous Chapter XXX was implemented  
 196 as a VUMAT subroutine within the framework of large deformations taking as reference  
 197 the unstressed state of the material. The detailed description of the model is available in

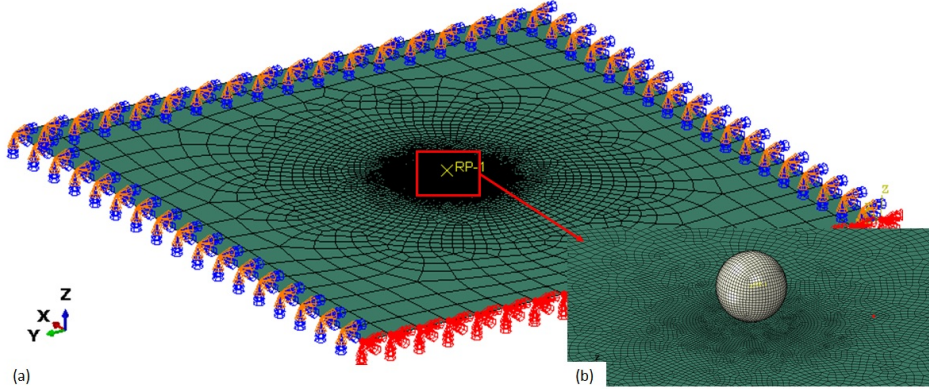


Figure 6: (a) Mesh strategy and boundary conditions and (b) mesh refinement at the impact point.

208 [23, 28]. The implementation for dynamic analysis incorporated one modification at Gauss  
 209 point level, such that each mesodomain of the fibre network was described by 65 sets of fibres  
 210 with different orientation instead of 33 to reduce the numerical instabilities. The strain rate  
 211 dependency previously observed during the dynamic characterisation was accounted by two  
 212 different material parameters; (i) the fibre pull-out length,  $L_{po}$ , that increased up to the  
 213 total length of the fibre of 60 mm, in agreement with the full fibre pull-out registered  
 214 experimentally, see Fig. 5(c), and (ii) the pull-out strength,  $\sigma_{po}$ , randomly defined withing  
 215 the range [0.3 - 1.7] GPa, to fit the ballistic limit of the fabric. See Table XX in Chapter XX  
 216 for reference. The same deletion criteria (average damage variable  $D > 0.99$ ) as in previous  
 217 quasi-static simulations was applied to replicate the penetration by fibre disentanglement of  
 218 the target.

209 The clamped free area of the fabric of 350 x 350 mm<sup>2</sup> was discretised with reduced  
 210 integration M3D4R membrane elements, with enhanced hourglass control and second order  
 211 accuracy, see Fig. 6. The target was fully clamped along the four edges. The impact point  
 212 was discretised with a fine mesh composed of elements of 1 mm<sup>2</sup>, and a coarser mesh was  
 213 implemented with the distance from the impact zone to decrease the number of degrees of  
 214 freedom. The projectile was modelled as a solid rigid steel sphere of 5.5 mm in diameter  
 215 and 7.85 g/cm<sup>3</sup>. The tangential friction coefficient between the sphere and the fabric was  
 216 set as 0.1.

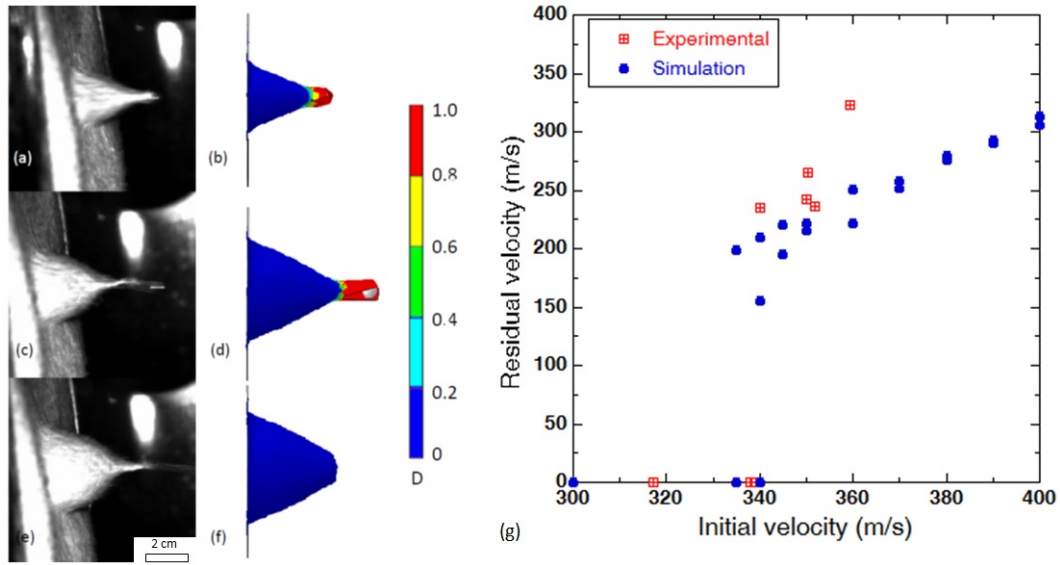


Figure 7: Correlation between the experimental deflection and the damage contour plot of the needlepunched nonwoven during an impact at 360 m/s. (a) and (b)  $t = 100 \mu\text{s}$ . (c) and (d)  $t = 175 \mu\text{s}$  and (e) and (f)  $t = 250 \mu\text{s}$ . The red color stands for the disentangled fabric. (g) Experimental and numerical residual velocity curves. Reproduced with permission from [28].

### 217 3.2. Validation

218 The performance of the Digital Twin was analysed to determine if it captured accurately  
 219 the energy absorption mechanisms of the nonwoven material. The left hand side of Fig. 7  
 220 shows the numerical comparison of the experimental and numerical deflection of the layer  
 221 during an impact above the ballistic limit, showing very good agreement in terms of damage  
 222 prediction. An in-plane tensile wave stretched the layer towards the impact point, while  
 223 the transverse wave captured the deflection with elliptical cross-section previously observed  
 224 during the experimental campaign. The region of the material within the bounds of the  
 225 in-plane longitudinal tensile wave dissipated the impact energy through the deformation  
 226 mechanisms aforementioned; fibre uncurling, rotation and sliding. The model also predicted  
 227 the strain gradients localised at the impact point and the fibre disentanglement resulting in  
 228 tearing and penetration of the ply.

229 The Digital Twin also captured the energy absorption capacity of the material and the  
 230 ballistic limit. Fig. 7(g) shows the residual velocity curves and compares the experimental

231 and numerical residual velocities,  $V_{res}$ , as a function of the initial impact velocities,  $V_{ini}$ . The  
232 experimental scattering was reproduced by the stochastic definition of the pull-out strength  
233 as mentioned in Section 3.1. Although the model was able to capture the ballistic limit, it  
234 overestimated the energy absorption capacity above that threshold, as it did not considered  
235 the thermal softening of the Dyneema fibres registered during ballistic impact. Further  
236 information regarding the validation of the Digital Twin might be consulted in [28].

#### 237 4. Case Study 1. Ballistic response of hybrid nonwoven/woven targets

238 Dry woven and nonwoven fabrics can be combined to create soft body armour protections  
239 with improved ballistic performance to arrest a large range of caliber sizes. The nonwoven is  
240 usually placed in the frontal face to act as cushion layer and enhance the load transmission  
241 into the woven fabric [18, 17, 29]. In this section we aim to investigate the synergistic  
242 contribution between the nonwoven and woven layers against impact, from an experimental  
243 and numerical point of view. A ballistic experimental campaign has been conducted to  
244 determine the ballistic limit and the energy absorption capacity of the hybrid target. The  
245 role of each layer at different stages of the impact process was ascertained using a Digital  
246 Twin, that provided separately information on kinetic and strain energy absorbed as function  
247 of time.

##### 248 4.1. Materials

249 The Dyneema hybrid target was composed by a nonwoven (NW) layer and 4 rear harness  
250 satin woven fabrics (W) with stacking sequence [NW/0<sub>W</sub>/90<sub>W</sub>/0<sub>W</sub>/90<sub>W</sub>]. The areal density  
251 of the shield was 920 g/m<sup>2</sup>, where each individual layer of the woven Dyneema fabric had an  
252 areal density of  $\approx 180$  g/m<sup>2</sup> and thickness of  $\approx 0.5$  mm. The full description of the experi-  
253 mental set-up which comprised a gas gun and high-speed camera is available in section 2.2.2.  
254 The size of the projectile (5.5 mm diameter) was approximately 4 times the width of the  
255 woven Dyneema yarns, easily promoting yarn sliding during ballistic impact due to the low  
256 friction coefficient of the Dyneema fibres. Further details of this experiment are available in  
257 [30].

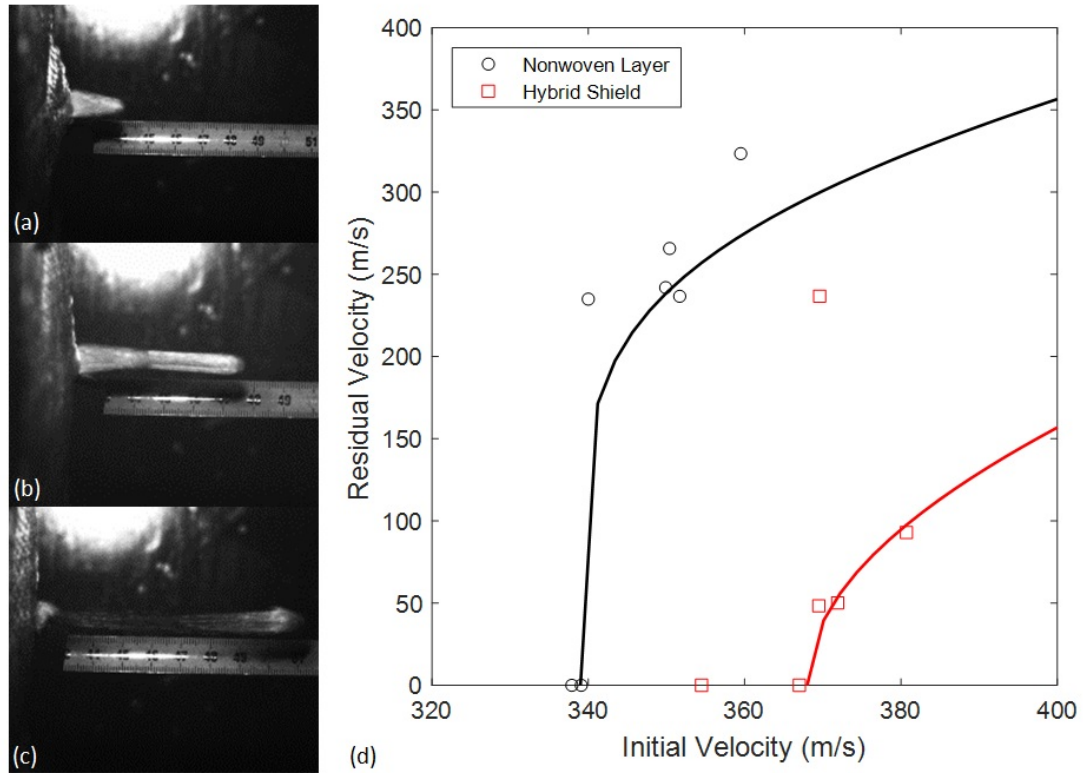


Figure 8: Deflection of the hybrid shield for an impact velocity of 370 m/s. (a)  $t = 150 \mu\text{s}$ . (b)  $t = 600 \mu\text{s}$ . (c)  $t = 1350 \mu\text{s}$ . (d) Residual velocity curves of the hybrid shield ( $920 \text{ g/m}^2$ ) and comparison with the nonwoven layer ( $200 \text{ g/m}^2$ ) [30].

#### 258 4.2. Experimental results

259 The impact response of the hybrid target is shown in Fig. 8 during an impact at 370 m/s.  
 260 Initially, all layers deflected together until the yarns of the rear woven layers slid and the  
 261 nonwoven got confined into the resulting gap. The confinement led to a high level of fibre  
 262 alignment with the loading direction followed by a large percentage of extracted fibres.  
 263 This resulted in a ductile response of the nonwoven layer with large deformation before  
 264 final disentanglement, inducing a very high energy dissipation. The hybrid configuration  
 265 presented superior energy absorption capacity when compared against the single nonwoven  
 266 fabric. The residual velocity curves are shown in Fig. 8(d). The additional four layers of  
 267 woven Dyneema increased the ballistic limit of the nonwoven by  $\approx 30 \text{ m/s}$  with an increment

Table 1: Elastic constants of the polyethylene SK65 yarns [32].

Density ( $\rho_f$ )	970 kg/m <sup>3</sup>
Longitudinal elastic modulus ( $E_1$ )	95 GPa
Transverse elastic modulus ( $E_2$ )	9.5 GPa
Poisson's ratio ( $\nu_{12}$ )	0
Shear modulus ( $G_{12}$ )	0.95 GPa

268 of 7 J of energy. It should be noted that the specific energy absorption capacity was higher  
 269 for the single nonwoven considering the reduced weight, however, the areal weight of the  
 270 hybrid shield was comparable to the previous dry woven aramid shield, see Fig. 5, and still  
 271 exhibited a higher energy absorption capacity and ballistic limit than the previous [16, 1].  
 272 Furthermore, the addition of the nonwoven layer to the woven shield permitted the load  
 273 transfer into the woven yarns and avoided the slippage failure mode previously observed  
 274 during the ballistic impact of the single woven layers [30].

#### 275 4.3. Numerical implementation

276 The analysis of the previous ballistic response was conducted by means of a Digital Twin  
 277 based on a Finite Element Model. The nonwoven ply was implemented following the method-  
 278 ology exposed in previous Section 3.1, meanwhile, the woven fabric layers were modelled at  
 279 mesoscale level, discretising the weaved yarns with C3D8 solid elements [31, 32], see Fig. 9.  
 280 The elastic constants of the transversely isotropic yarn model are available in Table 1.

281 The nonwoven and the woven layers were combined to replicate the shield with stacking  
 282 sequence [NW/0<sub>W</sub>/90<sub>W</sub>/0<sub>W</sub>/90<sub>W</sub>]. The dimensions of the nonwoven were set to 350 x 350 mm<sup>2</sup>,  
 283 meanwhile, the woven fabrics were limited to 100 x 100 mm<sup>2</sup> to reduce the computational  
 284 cost. All fabrics were separated by a gap of 0.025 mm to avoid initial contact between layers  
 285 and were constraint along the edges. The contact interaction between all the elements (the  
 286 projectile, the yarns and the nonwoven) was modelled by a Coulomb friction algorithm with  
 287 a friction coefficient of 0.0075. Further details are available in [30].



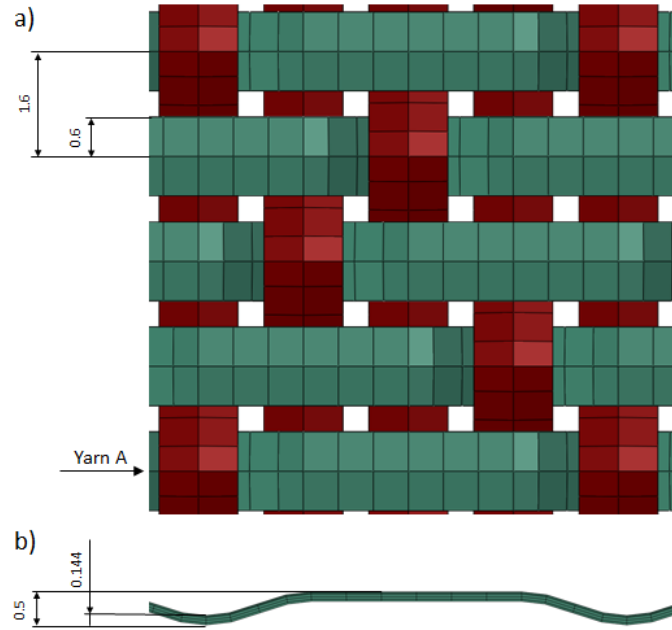


Figure 9: 3 harness satin pattern and mesoscale implementation of the woven layers. (a) Plan view. (b) Lateral view of yarn A. Measurements in mm [30].

288 *4.4. Simulation results*

289 The correlation between experimental and numerical results is shown in Fig. 10. A  
 290 good agreement was found in terms of residual velocities and ballistic limit, such that the  
 291 experimental results were obtained within the numerical scattering. Furthermore, the Digital  
 292 Twin reproduced the improved behaviour of the hybrid shield with respect to the nonwoven  
 293 and woven layers individually, and the complex interaction between the nonwoven and the  
 294 weaved yarns. The left-hand side of Fig. 10 shows a comparison between the predicted and  
 295 the experimental response at an impact velocity of 380 m/s. At the early stages of deflection  
 296 ( $t < 20 \mu s$ ) all the plies deflected together. The main energy absorption mechanisms at this  
 297 stage were the kinetic and elastic energies transmitted to the rear woven layers. After yarn  
 298 sliding and during the confinement stage, elastic deformation and kinetic energy transmitted  
 299 to the nonwoven layer became the predominant dissipation mechanism. Final penetration  
 300 of the shield occurred by extensive fiber disentanglement. The major contribution to the  
 301 energy dissipation happened at the very early stages of the impact, where a reduction of the

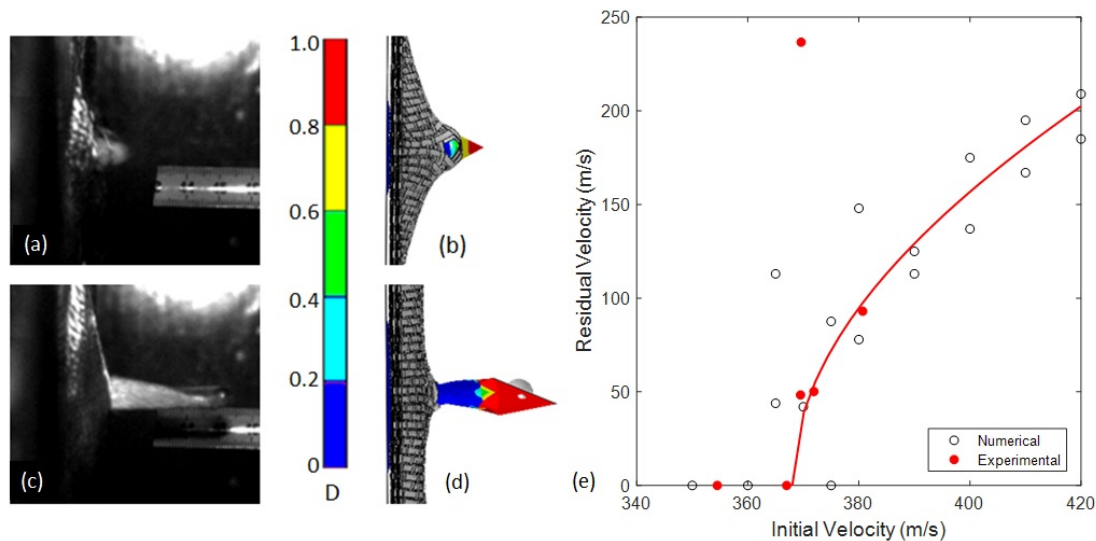


Figure 10: Correlation between the experimental deflection and the damage contour plot of the hybrid shield for an impact at 380 m/s. (a) and (b)  $t = 25 \mu\text{s}$  and (c) and (d)  $t = 150 \mu\text{s}$ . The red colour stands for the disentangled fibre network. (e) Comparison between experimental and predicted residual velocities as function of the impact velocity [30].

302 60% of the kinetic energy of the projectile was registered, 3 times higher than the energy  
 303 absorbed by the baseline woven target. After the woven yarns slippage, an additional 20%  
 304 of kinetic energy was dissipated due to the localised fibre pull-out. The hybrid configuration  
 305 outperformed the capacity of each individual ply due to the synergistic interaction between  
 306 layers. In particular, the nonwoven layer resulted in an optimal material to transfer the load  
 307 to the adjacent woven layers, drastically increasing the energy absorption capacity of the  
 308 woven target for these small calibers.

## 309 5. Case Study 2. Ballistic response of multi-layered metal/nonwoven shields

310 Dry fabrics can be also included in conventional hollow metallic components to improve  
 311 the ballistic performance with a minimum increase of structural weight. The concept has  
 312 been proven valid for turbine barriers, where the addition of Kevlar woven fabrics increased  
 313 the ballistic performance against projectiles [33, 34]. This section aims to investigate the  
 314 performance of a multilayered shield based on steel sheets, nonwovens and air gaps.

315 *5.1. Materials*

316 The nonwoven fabric was combined with a commercial bake hardening steel 260BH man-  
317 ufactured by Arcelor-Mittal [35]. The alloy is conventionally used in the automotive industry  
318 to manufacture components such as vehicle doors. It is designed specifically for structural  
319 applications and exhibits a high ductility, with high dent and impact resistance. The vehi-  
320 cle door was modelled as a hollow target with a total width of 80 mm constituted by two  
321 thin steel plates with 0.7 mm thickness with and equivalent areal weight of 11 kg/m<sup>2</sup>. This  
322 configuration allow the incorporation of additional internal nonwoven fabrics in between the  
323 steel plates to increase the energy absorption capacity of the baseline structure. A maximum  
324 of 3 nonwoven layers was evaluated, regularly spaced with gaps of 10 mm and a distance of  
325 30 mm with the steel plates, see Fig. 11. This resulted in an increment of 5.5% of the areal  
326 weight of the component, up to 11.6 kg/m<sup>2</sup>.

327 *5.2. Numerical implementation*

328 A Digital Twin of the previous multilayered shield was implemented in the software  
329 Abaqus/Explicit to study the ballistic response of the target. The mechanical response of  
330 the nonwoven layers was implemented as described in previous section 3.1. The constitutive  
331 behaviour of the bake hardening steel was modelled as a standard isotropic elasto-plastic ma-  
332 terial available in the Abaqus/Explicit library based on the ductile failure criterion proposed  
333 in [36, 37, 38]. The model incorporated a linear hardening with a Von Mises yield surface  
334 which evolved as function of the applied plastic deformation,  $\varepsilon^{pl}$ , following the expression:

$$\sigma_y = \sigma_y^0 + H\varepsilon^{pl} \quad (2)$$

335 where  $\sigma_y^0$  stood for the initial value of the yield strength and  $H$  for the hardening modulus.  
336 The onset of damage was determined by the ultimate strength of the material,  $\sigma_0$ . This value  
337 was combined with the hardening modulus to obtain the equivalent plastic strain to failure.  
338 Once the failure enveloped was overtaken, the material degradation was implemented by a  
339 phenomenological softening of the undamaged stress tensor,  $\bar{\sigma}$ , such as:

$$\sigma = (1 - d)\bar{\sigma} \quad (3)$$

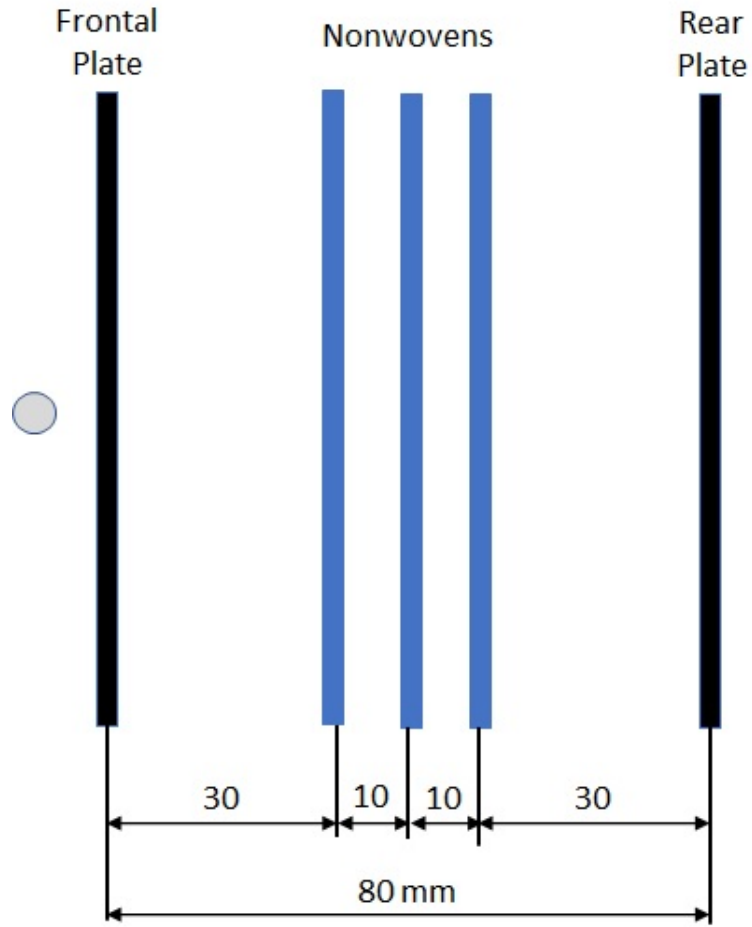


Figure 11: Multilayered configuration composed by 2 steel plates and 3 nonwoven plies. Measurements in millimeters.

340 where the damage variable,  $d$ , followed a conventional Lemaitre continuum damage model  
 341 to ensure the dissipated energy was equal to the fracture toughness of the material,  $\Gamma$ , and  
 342 avoid any size mesh dependency [39, 40]. Further information about the material model is  
 343 available in [38] and material properties are summarized in Table 2. More details of the  
 344 implementation are available in [41].

345 The door vehicle with the internal nonwoven layers was simplified as a  $350 \times 350 \text{ mm}^2$   
 346 target to reduce the computational cost. A higher mesh density was also defined around  
 347 the impact point, with finite elements of  $1 \text{ mm}^2$  area. All the layers were fully clamped  
 348 on the edges during the impact simulation. The nonwoven layers were modelled using the

Table 2: Material parameters for Steel 260BH [41]

Density, $\rho$	7850 kg/m <sup>3</sup>
Young's Modulus, E	200 GPa
Poisson's ratio, $\nu$	0.27
Hardening Modulus, H	2.5 GPa
Ultimate Strength, $\sigma_0$	400 MPa
Yield Strength, $\sigma_y^0$	280 MPa
Strain to failure, $\varepsilon_D^{pl}$	0.3
Strain rate, $\dot{\varepsilon}^{pl}$	10 <sup>6</sup>
Triaxiality, $\xi$	0.8
Fracture toughness $\Gamma$	0.072 J/mm <sup>2</sup>

349 approach in previous section 3.1, meanwhile, the thin steel plates were modelled with S4R  
 350 shell elements, reduced integration, hourglass control and finite membrane strain. A rigid  
 351 steel sphere of 5.5 mm in diameter as in previous ballistic studies was implemented to  
 352 simulate the projectile. The penetration of the layers was reproduced by the deletion of the  
 353 fully damaged elements, once the damage variable achieved the threshold  $D > 0.99$ . The  
 354 contact between steel plates and nonwoven layers was implemented by a softened tangential  
 355 contact behaviour with an sticking friction slope of  $\kappa=0.001$  and a friction coefficient  $\mu=0.1$ .

### 356 5.3. Simulation results

357 The Digital Twin was able to reproduce the ballistic response of the multilayered shield,  
 358 and the interaction between the layers. The right hand side of Fig. 12 shows the penetration  
 359 sequence. Initially, the projectile pierced the frontal steel plate causing a minimum plas-  
 360 tic deformation located at the impact point and hit the rest of the layers and rear metal  
 361 plate, increasing the strain and kinetic energy absorbed by the system and decreasing the  
 362 kinetic energy of the projectile. The progressive deformation induced damage on the non-  
 363 woven layers, nevertheless, final disentanglement was inhibited by the rear metal plate, that  
 364 contributed structurally delaying the penetration of the layers and increasing the energy

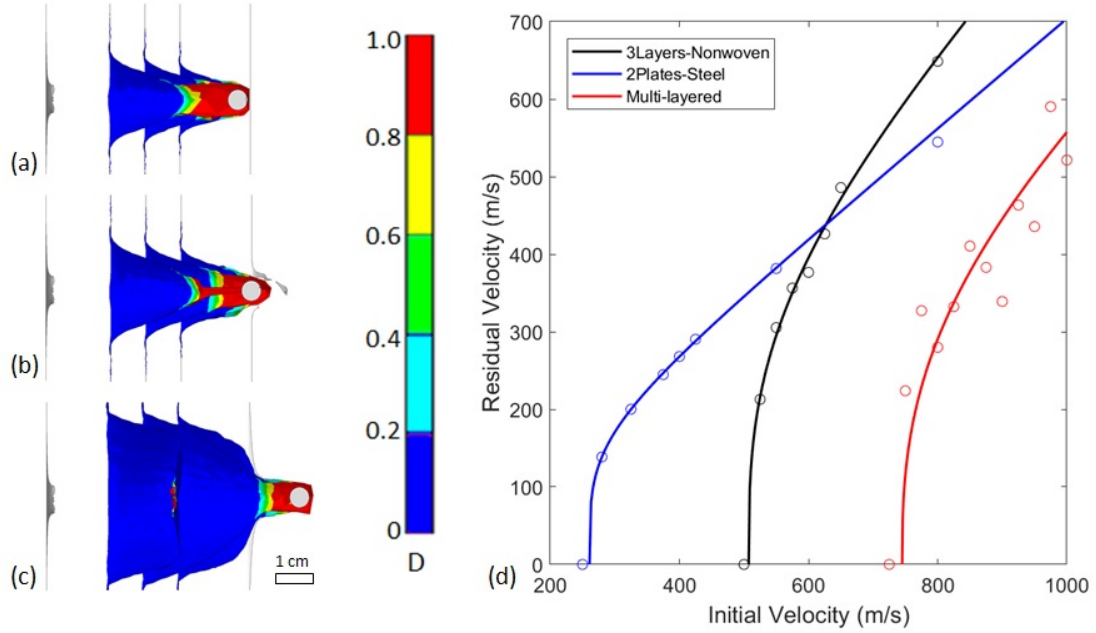


Figure 12: Ballistic response of the multi-layered shield impacted at 725 m/s. (a)  $t = 90 \mu\text{s}$  (b)  $t = 135 \mu\text{s}$  and (c)  $t = 225 \mu\text{s}$ . Contour plots of the damage variable. (d) Residual velocity curves for the multi-layered shield and comparison against the baseline configuration (2 plates of steel) and the 3 layers of nonwoven reinforcement [41].

365 absorbed by the target, see Fig.12(a). For impact velocities just below the ballistic limit,  
 366 the penetration of the rear steel plate was predicted before the full nonwoven disentangle-  
 367 ment took place, resulting in a similar confinement to the one appreciated in the hybrid  
 368 woven/nonwoven shield, see Section 4.2. This confinement resulted in a high volume of fibre  
 369 alignment, increasing the energy absorbed locally due to fibre pull-out.

370 The ballistic performance of the multi-layered component was compared in terms of en-  
 371 ergy absorption capacity against the predictions for its individual components; the steel  
 372 plates and the nonwoven layers. Fig.12(d) compares the residual velocity curves. The steel  
 373 plates with an equivalent weight of  $11 \text{ kg/m}^2$  presented the lowest ballistic limit with a  
 374 maximum energy absorption capacity of 19.5 J, characteristic of thin metallic plates. A  
 375 large increment of energy absorption capacity was found for the 3 nonwoven layers, with  
 376 an equivalent energy absorption capacity of 94.5 J. The multi-layered shield surpassed the

377 ballistic performance of their individual components, with a maximum energy absorption  
378 capacity of 195.9 J, almost doubling the capacity of the sum of the previous. This repre-  
379 sented a massive improvement of specific energy absorption capacity over a factor of 8 when  
380 compared against the conventional door vehicle with a minor increment of total areal weight  
381 of 5.5%. The large deformation of the nonwoven layers and their synergistic interaction with  
382 the rear metal sheet led to this outstanding improvement of ballistic performance.

## 383 **6. Conclusions**

384 The ballistic response of a Dyneema needlepunched nonwoven fabric composed by a  
385 random network of long fibres entangled through a mechanical process has been reviewed,  
386 with special focus on the main deformation and failure mechanisms, and their contribution  
387 to the overall energy absorption capacity of the material. The ballistic performance of the  
388 material was analysed in terms of residual velocity curves and ballistic limit. Additionally, a  
389 Digital Twin by means of a high fidelity Multiscale Finite Element Model was developed to  
390 provide further insight into physical events at microscale level that could not be revealed by  
391 high-speed imaging. The model was able to capture the main deformation micromechanisms  
392 such as fibre re-orientation and localisation of damage and was validated and calibrated  
393 against experimental data to ensure the robustness of the approach.

394 The in-plane dynamic response under high strain rates of the material was determined  
395 using a Split-Hopkinson tensile bar, specially designed for this purpose. The apparatus in-  
396 cluded a high-sensitivity output bar and had a long pulse duration to register the response of  
397 the low-impedance fibre network under large deformations. A high-speed camera registered  
398 the deformation micromechanisms under high strain rates, which comprised fibre straight-  
399 ening, rotation and sliding with the loading direction. These mechanisms were previously  
400 observed during the in-plane tensile quasi-static characterisation of the material. The main  
401 differences between the dynamic and the quasi-static loading regimes was the heterogeneous  
402 strain gradient developed at high-strain rates across the gauge length, not registered pre-  
403 viously during the quasi-static analysis before the onset of damage. This heterogeneous  
404 strain field was a direct consequence of the dissipative nature of the frictional deformation

405 processes and the internal impedance fronts originated in the material due the differences  
406 in microstructural evolution. As a result, the wave propagation phenomenon prevented the  
407 propagation of larger strain waves away from the loading point, resulting in large strain  
408 gradients located nearby the input edge. The frictional mechanisms between the entangled  
409 fibres presented a strong strain rate dependency with a significant increment of strain for  
410 low applied strains.

411 The ballistic response of the nonwoven layer was characterised by a combination of ex-  
412 perimental and numerical analyses. The nonwoven layer was subjected to ballistic impact  
413 by a small steel sphere (5.5 mm in diameter) and presented outstanding energy absorp-  
414 tion capacity compared to a conventional aramid woven target four times heavier than the  
415 novel nonwoven solution. During impact, the energy of the projectile was accommodated  
416 by the formation of a cone of deformed material with an elliptical cross-section due to the  
417 different wave propagation speed along material directions. The deformation was accommo-  
418 dated by the same micromechanisms observed during dynamic in-plane deformation, with  
419 a pronounced fibre rotation and re-alignment towards the impact point, and a sharp strain  
420 gradient with localised damage. The high ductility of the material resulted in its outstand-  
421 ing energy absorption capacity. The energy was dissipated by the tensile deformation of the  
422 fabric within the elliptical region defined by the wave speed of the material. The penetration  
423 of the ply occurred due to fibre disentanglement, with a large volume of fibres extracted from  
424 the layer at very large strain values.

425 The potential of the material to improve the ballistic response of conventional barriers  
426 was analysed with two additional case studies. In the first one, the nonwoven layer was used  
427 to improve the ballistic performance of a conventional Dyneema woven target, with a small  
428 ratio between projectile diameter and yarn width easily promoting yarn sliding and a poor  
429 ballistic performance. The nonwoven was positioned as a frontal layer to redistribute the  
430 load over the adjacent woven plies. As a result, a drastic increment of the ballistic limit  
431 and the energy absorption with respect to the original woven configuration was observed.  
432 During the first stages of the impact the energy was transmitted to the woven yarns through  
433 the nonwoven fabric, increasing by a factor of 3 the kinetic and strain energy absorbed by



434 the woven shield. At a second stage, the projectile slipped through the yarns of the woven  
435 fabrics, however, the large ductility of the nonwoven resulted in a large fibre confinement  
436 with an additional energy absorption due to the large volume of extracted fibres.

437 The second case study focused on the improvement of the mechanical performance of  
438 conventional metal components in the transport sector such as a vehicle door. Three addi-  
439 tional nonwoven layers were incorporated, separated by gaps of 10 mm. The hybrid system  
440 outperformed the performance of the steel plates and nonwoven layers, resulting in an out-  
441 standing energy absorption capacity about twice the sum of the energies dissipated by its  
442 individual components. Furthermore, the hybrid shield increased the energy absorption ca-  
443 pacity of the baseline steel plates over a factor of 8, with a negligible increment of areal  
444 weight of a 5.5%.

445 The Digital Twin provided high-fidelity predictions of the different configurations in  
446 terms of ballistic limit and deformation mechanisms, with valuable insight regarding the  
447 evolution of energy absorption for each component of the shields. It has been proven a  
448 useful numerical tool that could be used in future design and optimisation tasks, however,  
449 the current approach to simulate the ballistic response of needlepunched nonwoven fabrics  
450 presents certain limitations and challenges that still need to be addressed. In particular,  
451 (i) the implementation of the strain rate dependency of the material is phenomenological  
452 and has been fitted against experimental results due to the lack of a high-strain-rate stress-  
453 strain relationship; (ii) the wave propagation phenomenon of the fibre network could not be  
454 accurately represented by the continuous mesodomain, so the simulations could not replicate  
455 the scattering and dissipation observed during the Slip Hopkinson bar experiments and (iii)  
456 a thermo-mechanical constitutive model needs to be implemented to capture the thermal  
457 softening of the fibres during ballistic impact.

458 This chapter demonstrates that the Dyneema needlepunched nonwoven fabric presents  
459 a lightweight solution to arrest small fragments, providing a low-cost alternative to improve  
460 the ballistic performance of conventional shields. As a result, it is possible to improve the  
461 ballistic performance of conventional civil automotive and aerospace components without  
462 penalising the fuel consumption to protect passengers against shrapnel. The nonwoven

463 layer can be also incorporated into soft-body armour protections without reducing the users  
464 comfort, at a minimal increment of areal weight.

## 465 7. Acknowledgement

466 This research was supported by The Royal Society through the grant [RGS/R2/180091]  
467 and the Start-up funding for recently appointed lectures of The University of Edinburgh.  
468 The collaboration of Mr J. Vila-Ortega, Mr S. Carter, Dr F. Gálvez, Dr A. Pellegrino and  
469 Prof Nik Petrinic, are gratefully acknowledged.

## 470 References

- 471 [1] Mulat Alubel Abteu, Francois Boussu, Pascal Bruniaux, Carmen Loghin, and Irina Cristian. Ballistic  
472 impact mechanisms-a review on textiles and fibre-reinforced composites impact responses. *Composite*  
473 *Structures*, page 110966, 2019.
- 474 [2] Unsanhame Mawkhlieng, Abhijit Majumdar, and Animesh Laha. A review of fibrous materials for soft  
475 body armour applications. *RSC Advances*, 10(2):1066–1086, 2020.
- 476 [3] S. J. Russell. *Handbook of nonwovens*. The Textile Institute. Woodhead Publishing, 2007.
- 477 [4] Roy C. Laible and Malcolm C. Henry. A review of the development of ballistic needle-punched felts.  
478 Technical report, No. C/PSEL-TS-167. Clothing and Personal Life Support Equipment Laboratory.  
479 U.S. Army Natick Laboratories, 1969.
- 480 [5] S.J. Russell, A. Pourmohammadi, I. Ezra, and M. Jacobs. Formation and properties of fluid jet  
481 entangled HMPE impact resistant fabrics. *Composites Science and Technology*, 65(6):899–907, 2005.
- 482 [6] G. A. Thomas. Non-woven fabrics for military applications. In *Military Textiles*, pages 44–47. The  
483 Textile Institute. Woodhead Publishing, 2008.
- 484 [7] Thomas W. Ipson and Edward P. Wittrock. Response of non-woven synthetic fiber textiles to ballistic  
485 impact. Technical report, No. TR-67-8-CM. Denver Research Institute, 1966.
- 486 [8] Howard L Thomas, Ashok Bhatnagar, and Lori L. Wagner. Needle-Punched Non-Woven for High  
487 Fragment Protection. In *14th International Conference of Composite Materials*, San Diego, California,  
488 2003.
- 489 [9] S. H. Lee and T. J. Kang. Mechanical and Impact Properties of Needle Punched Nonwoven Composites.  
490 *Journal of Composite Materials*, 34(10):816–840, May 2000.
- 491 [10] Jia-Horng Lin, Chan-Hung Hsu, and Hsien-Hui Meng. Process of preparing a  
492 nonwoven/filament/woven-fabric sandwich structure with cushioning effect of ballistic resistance.  
493 *Fibres & Textiles in Eastern Europe*, 13:43–47, 2005.

- 494 [11] P Rama Subba Reddy, T Sreekantha Reddy, I Srikanth, Juhi Kushwaha, and V Madhu. Development  
495 of cost effective personnel armour through structural hybridization. *Defence Technology*, 2019.
- 496 [12] Ruosi Yan, Qianyu Zhang, Bao Shi, Zhigang Qin, Sainan Wei, and Lixia Jia. Investigating the integral-  
497 structure of hr/bp/chp/cf consisting of non-woven flexible inter/intra-ply hybrid composites: compres-  
498 sion, puncture-resistance, electromagnetic interference shielding effectiveness. *Composite Structures*,  
499 page 112501, 2020.
- 500 [13] GA Thomas. Non-woven fabrics for military applications. *Military textiles*, pages 17–48, 2008.
- 501 [14] D Naik, S Sankaran, B Mobasher, S Rajan, and J Pereira. Development of reliable modeling method-  
502 ologies for fan blade out containment analysis. Part I: Experimental studies. *International Journal of*  
503 *Impact Engineering*, 36(1):1–11, 2009.
- 504 [15] Philip M. Cunniff. An Analysis of the System Effects in Woven Fabrics Under Ballistic Impact. *Textile*  
505 *Research Journal*, 62(9):495–509, 1992.
- 506 [16] Ala Tabiei and Gaurav Nilakantan. Ballistic Impact of Dry Woven Fabric Composites: A Review.  
507 *Applied Mechanics Reviews*, 61(1):010801–1–13, 2008.
- 508 [17] Chia Chang Lin, Chao Chiung Huang, You Liang Chen, Ching Wen Lou, Chin Mei Lin, Chan Hung  
509 Hsu, and Jia Horng Lin. Ballistic-resistant stainless steel mesh compound nonwoven fabric. *Fibers and*  
510 *Polymers*, 9(6):761–767, 2009.
- 511 [18] C. C. Lin, C. M. Lin, C. C. Huang, C. W. Lou, H. H. Meng, C. H. Hsu, and J. H. Lin. Elucidating the  
512 Design and Impact Properties of Composite Nonwoven Fabrics with Various Filaments in Bulletproof  
513 Vest Cushion Layer. *Textile Research Journal*, 79(3):268–274, 2009.
- 514 [19] Jia Horng Lin, Chan Hung Hsu, and Hsien Hui Meng. Process of Preparing a Nonwoven / Filament  
515 / Woven-Fabric Sandwich Structure with Cushioning Effect of Ballistic Resistance. *Fibres & Textiles*,  
516 13(4(52)):43–47, 2005.
- 517 [20] Amir Shahdin, Laurent Mezeix, Christophe Bouvet, Joseph Morlier, and Yves Gourinat. Fabrication  
518 and mechanical testing of glass fiber entangled sandwich beams: A comparison with honeycomb and  
519 foam sandwich beams. *Composite Structures*, 90(4):404–412, 2009.
- 520 [21] S. Chocron, A. Pintor, D. Cendón, C. Roselló, and V. Sanchez-Galvez. Characterization of Fraglight  
521 non-woven Felt and Simulation of FSP’s Impact in it. Technical report, Technical University of Madrid,  
522 2002.
- 523 [22] F. Martínez-Hergueta, A. Ridruejo, C. González, and J. LLorca. Deformation and energy dissipation  
524 mechanisms of needle-punched nonwoven fabrics: A multiscale experimental analysis. *International*  
525 *Journal of Solids and Structures*, 64:120–131, 2015.
- 526 [23] F. Martínez-Hergueta, A. Ridruejo, C. González, and J. LLorca. A multiscale micromechanical model  
527 of needlepunched nonwoven fabrics. *International Journal of Solids and Structures*, 96:81–91, 2016.

- 528 [24] R. Gerlach, C. Kettenbeil, and N. Petrinic. A new split Hopkinson tensile bar design. *International*  
529 *Journal of Impact Engineering*, 50:63–67, 2012.
- 530 [25] F. Martínez-Hergueta, A. Pellegrino, A. Ridruejo, N. Petrinic, C. Gonzalez, and J. LLorca. Dynamic  
531 tensile testing of needlepunched nonwoven fabrics. *Applied Sciences*, 10(15):5081, 2020.
- 532 [26] F. Martínez-Hergueta, A. Ridruejo, F. Gálvez, C. González, and J. LLorca. Influence of fiber orientation  
533 on the ballistic performance of needlepunched nonwoven fabrics. *Mechanics of Materials*, 94:106–116,  
534 2016.
- 535 [27] F. Martínez-Hergueta, D. Ares, A. Ridruejo, J. Wiegand, and N. Petrinic. Modelling the in-plane strain  
536 rate dependent behaviour of woven composites with special emphasis on the non-linear shear response.  
537 *Composite Structures*, 210:840–857, 2019.
- 538 [28] F. Martínez-Hergueta, A. Ridruejo, C. González, and J. Llorca. Numerical simulation of the ballistic  
539 response of needle-punched nonwoven fabrics. *International Journal of Solids and Structures*, 106:56–67,  
540 2017.
- 541 [29] Hasam Basri Kocer. *Laminated and hybrid soft armor systems for ballistic applications*. PhD thesis,  
542 Auburn University, 2007.
- 543 [30] F. Martínez-Hergueta, A. Ridruejo, C. González, and J. LLorca. Ballistic performance of hybrid  
544 nonwoven/woven polyethylene fabric shields. *International Journal of Impact Engineering*, 111:55–  
545 65, 2018.
- 546 [31] Sidney Chocron, Eleonora Figueroa, Nikki King, Trenton Kirchdoerfer, Arthur E. Nicholls, Erick Sage-  
547 biel, Carl Weiss, and Christopher J. Freitas. Modeling and validation of full fabric targets under ballistic  
548 impact. *Composites Science and Technology*, 70(13):2012–2022, 2010.
- 549 [32] Sidney Chocron, Trenton Kirchdoerfer, Nikki King, and Christopher J. Freitas. Modeling of Fabric Im-  
550 pact With High Speed Imaging and Nickel-Chromium Wires Validation. *Journal of Applied Mechanics*,  
551 78(5):051007, 2011.
- 552 [33] Donald A Shockey, David C Erlich, and Jeffrey W Simons. Lightweight Fragment Barriers for Com-  
553 mercial Aircraft. *18Th International Symposium on Ballistics*, pages 15–19, 1999.
- 554 [34] Z. Stahlecker, B. Mobasher, S. D. Rajan, and J. M. Pereira. Development of reliable modeling method-  
555 ologies for engine fan blade out containment analysis. Part II: Finite element analysis. *International*  
556 *Journal of Impact Engineering*, 36(3):447–459, 2009.
- 557 [35] ArcelorMittal. Bake hardening steels, 2018.
- 558 [36] H Hooputra, H Gese, H Dell, and H Werner. A comprehensive failure model for crashworthiness  
559 simulation of aluminium extrusions. *International Journal of Crashworthiness*, 9(5):449–464, 2004.
- 560 [37] Ravi Kiran and Kapil Khandelwal. A triaxiality and lode parameter dependent ductile fracture criterion.  
561 *Engineering Fracture Mechanics*, 128:121–138, 2014.

- 562 [38] Dassault Systemes. *Abaqus 6.12 User's manual*. 2012.
- 563 [39] Jean Lemaitre. *A course on damage mechanics*. Springer Science & Business Media, 2012.
- 564 [40] Zdenek P Bazant and Jaime Planas. *Fracture and size effect in concrete and other quasibrittle materials*,  
565 volume 16. CRC press, 1997.
- 566 [41] J. Vila-Ortega, A. Ridruejo, and F. Martínez-Hergueta. Multiscale numerical optimisation of hy-  
567 brid metal/nonwoven shields for ballistic protection. *International Journal of Impact Engineering*,  
568 138:103478, 2020.