

The Aarhus red giants challenge

I. Stellar structures in the red giant branch phase[★]

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ABSTRACT

Context. With the advent of space-based asteroseismology, determining accurate properties of red-giant stars using their observed oscillations has become the focus of many investigations due to their implications in a variety of fields in astrophysics. Stellar models are fundamental in predicting quantities such as stellar age, and their reliability critically depends on the numerical implementation of the physics at play in this evolutionary phase.

Aims. We introduce the Aarhus red giants challenge, a series of detailed comparisons between widely used stellar evolution and oscillation codes that aim to establish the minimum level of uncertainties in properties of red giants arising solely from numerical implementations. We present the first set of results focusing on stellar evolution tracks and structures in the red-giant-branch (RGB) phase.

Methods. Using nine state-of-the-art stellar evolution codes, we defined a set of input physics and physical constants for our calculations and calibrated the convective efficiency to a specific point on the main sequence. We produced evolutionary tracks and stellar structure models at a fixed radius along the red-giant branch for masses of $1.0 M_{\odot}$, $1.5 M_{\odot}$, $2.0 M_{\odot}$, and $2.5 M_{\odot}$, and compared the predicted stellar properties.

Results. Once models have been calibrated on the main sequence, we find a residual spread in the predicted effective temperatures across all codes of ~ 20 K at solar radius and ~ 30 – 40 K in the RGB regardless of the considered stellar mass. The predicted ages show variations of 2–5% (increasing with stellar mass), which we attribute to differences in the numerical implementation of energy generation. The luminosity of the RGB-bump shows a spread of about 10% for the considered codes, which translates into magnitude differences of ~ 0.1 mag in the optical V -band. We also compare the predicted [C/N] abundance ratio and find a spread of 0.1 dex or more for all considered masses.

Conclusions. Our comparisons show that differences at the level of a few percent still remain in evolutionary calculations of red giants branch stars despite the use of the same input physics. These are mostly due to differences in the energy generation routines and interpolation across opacities, and they call for further investigation on these matters in the context of using properties of red giants as benchmarks for astrophysical studies.

Key words. stars: evolution – stars: interiors – asteroseismology

1. Introduction

Red giants of low and intermediate mass are cool luminous stars found in three evolutionary phases: on the red-giant branch (RGB), during core-helium burning (or clump), and on the asymptotic giant branch (AGB). They are of key importance in many fields of astrophysics, for example as benchmarks for testing stellar evolution theory in star clusters. Thanks to their high intrinsic luminosity, red giants are perfectly suited to explore distant regions of the Galaxy where accurate observations of fainter stars become challenging.

Determining precise stellar properties of field giants is extremely difficult when using traditional techniques, such as matching effective temperature, gravity, and composition to stellar tracks or isochrones. The reason is that giant stars in different evolutionary stages and spanning a wide range in mass overlap in the observational plane (e.g. in the Kiel or colour–magnitude diagram) well within the observational errors that are typically obtained with spectroscopy or photometry, for instance. The net result is that the properties of red giants that are determined

in this manner are largely dominated by statistical uncertainties (see e.g. Serenelli et al. 2013; Silva Aguirre & Serenelli 2016).

The study of red-giant stars has gone through a revolution with the advent of asteroseismic data from space missions. The CoRoT (Baglin et al. 2006) and Kepler (Gilliland et al. 2010) satellites have inspired a new paradigm of precisely determined stellar properties. By measuring the brightness variations in a large number of red giants across the Galaxy, these missions have provided new insights into the otherwise inaccessible deep interior of stars. Among the most striking results from asteroseismology are the detection of non-radial pulsation modes in red giant stars (De Ridder et al. 2009). These can help to distinguish between RGB and clump stars (Bedding et al. 2011), they can provide a measurement of the rotation profile from the inner core to the envelope (e.g. Beck et al. 2012; Mosser et al. 2012; Cantiello et al. 2014), of the efficiency of core mixing during the helium-burning phase (e.g. Montalbán et al. 2013; Constantino et al. 2015; Bossini et al. 2017), and the possible prevalence of fossil magnetic fields in their cores (Stello et al. 2016; Mosser et al. 2017).

The availability of asteroseismic data for thousands of red giants also allows the study of ensembles of stars, advancing into the field of Galactic archaeology (e.g. Miglio et al. 2013;

[★] All our evolutionary calculations and models are available at https://github.com/vsilvagui/aarhus_RG_challenge

Silva Aguirre et al. 2018). Properties based on asteroseismic data now include distances (Silva Aguirre et al. 2012; Rodrigues et al. 2014), masses and radii (Casagrande et al. 2014; Pinsonneault et al. 2014; Sharma et al. 2016), and most recently ages for RGB and clump stars (Casagrande et al. 2016; Anders et al. 2017; Pinsonneault et al. 2018). All these properties are determined to an unprecedented level of precision by combining the asteroseismic information with stellar evolution and pulsation calculations. If not only precise but also accurate, asteroseismically derived stellar properties have the potential to serve as a benchmark to improve our understanding of stellar structure and evolution as well as the processes that have been shaping our Milky Way into what it is today.

Inspired by the high-quality asteroseismic data obtained by the CoRoT and *Kepler* missions, and its clear potential for furthering scientific understanding in different fields of astrophysics, there is a fast growing body of literature devoted to validation of masses, radii, distances and ages determined from asteroseismology. This work includes comparing the seismic-inferred properties to those obtained empirically using interferometry (Huber et al. 2012; White et al. 2013), parallaxes (De Ridder et al. 2016; Huber et al. 2017; Sahlholdt et al. 2018), binary stars (e.g. Frandsen et al. 2013; Gaulme et al. 2016; Themeßl et al. 2018), and open clusters (Brogaard et al. 2011, 2018; Basu et al. 2011), to name just a few. Still, our ability to accurately determine asteroseismically-inferred stellar properties ultimately relies on having a realistic theoretical description of the structure and evolution of stars that can reproduce the features given by classical and seismic observations.

Many large compilations of theoretical tracks and isochrones produced by different groups are freely available and widely used by the community to determine stellar properties of red giants (e.g. Pietrinferni et al. 2004; Dotter et al. 2008; Bressan et al. 2012; Choi et al. 2016; Spada et al. 2017; Hidalgo et al. 2018). These sets are computed assuming a certain combination of micro- and macro-physics and by calibrating the convective efficiency to match the properties of the Sun, ensuring that the $1 M_{\odot}$ track has the correct solar temperature, luminosity, and surface composition at the solar age. Beyond this single calibration point, tracks computed by different groups predict different properties for the Sun's subsequent evolution. These differences are inherent to the code's numerical schemes (i.e. equation solvers, interpolations over tables, etc.) and differ from those arising by variations in the input physics. However, when comparing compilations of tracks and isochrones it is challenging to determine which differences belong to the chosen micro- and macro-physics and which would remain if the considered physical description was exactly the same. The latter are of utmost importance, as they define the maximum precision that can be attained when determining stellar properties based on evolutionary calculations, regardless of the nature of the constraints applied (i.e. spectroscopy, interferometry, or asteroseismology).

With this in mind, we started a series of workshops known as the Aarhus red giants challenge. The aim of these meetings was to gather experts working directly in the development of evolutionary and pulsation codes, produce sets of benchmark tracks and models with clearly defined input physics, compare the results from these different implementations, find and understand the origin of any discrepancies, and quantify the intrinsic uncertainties when determining stellar properties of red giants arising solely from the numerical methods applied by each code. Based on this information, the ultimate goal of these workshops is to define the best asteroseismic diagnosis methods for red giant stars and agree on a minimum set of observables necessary

to characterise them to various levels of precision. This is in a sense an exercise focused on red giant stars along the same lines as what was performed in the ESTA framework for main-sequence models (Lebreton et al. 2008).

Here we present the first set of calibration and science cases of red-giant-branch models produced for the Aarhus red giants challenge. Besides a general description of all models produced, in this paper we focus on the structural and evolutionary differences produced by the participating stellar evolution codes with particular emphasis on directly observed features (such as differences in effective temperature, chemical abundance, or the RGB-bump luminosity), parameters that affect derived quantities such as age (convective-core size and energy generation rates), and those that have an impact in asteroseismic observations (such as the interior hydrogen profile). Detailed comparisons of asteroseismic quantities and oscillation frequencies for the science cases presented here are the subject of the accompanying paper (Christensen-Dalsgaard et al. 2020, hereafter Paper II), while the analysis of structures in the clump phase and studies of the impact of changes in the input physics will be the subject of subsequent publications (Miller Bertolami et al., in prep.; Angelou et al., in prep.). A full account of the activities carried out as part of this challenge is available on the website of the workshops and includes a description of the science cases and all models and tracks computed.

2. Input physics and physical constants

We started our comparisons by defining a common set of input physics to be used in all exercises. We considered the original NACRE compilation of nuclear reactions (Angulo et al. 1999) without any updates to the rates, the OPAL opacities and the 2005 version of the equation of state (Iglesias & Rogers 1996; Rogers & Nayfonov 2002), the Potekhin conductive opacities (Cassisi et al. 2007) and the Grevesse et al. (1993) mixture of solar abundances. A simple Eddington relation has been used for the atmospheric stratification and the evolution has been started from the Zero Age Main Sequence (ZAMS). Convection has been treated under the mixing-length theory (MLT), with an efficiency calibrated using the solar radius as defined in Sect. 4. The boundary of convective regions is defined using the Schwarzschild criterion (Schwarzschild & Härm 1958), and we have not included the effects of overshooting, microscopic diffusion, nor mass loss in this set of calculations. The energy lost by neutrinos in nuclear reactions is taken into account as a decrease of the net energy Q released in each reaction. Although some of these ingredients are not completely up-to-date, they provide a common framework that all evolutionary codes participating in the challenge are currently able to include.

When comparing the internal structures we defined a maximum acceptable convergence for a model of α solar masses at β solar radii as follows:

$$\Delta_{\text{convergence}} = \left| 1.0 - \frac{G_{\text{code}} M_{\text{code}} / R_{\text{code}}^3}{G(\alpha \times M_{\odot}) / (\beta \times R_{\odot})^3} \right| \leq 2 \times 10^{-4}, \quad (1)$$

where G_{code} is the gravitational constant assumed by each evolutionary code, and M_{code} , R_{code} are the mass and radius of the calculated model. We emphasise here the role of the gravitational constant G , which is only known to a relative precision of 10^{-5} (Mohr et al. 2016). There are differences in the gravitational constant adopted by each evolutionary code included in this challenge, and to further reduce potential sources of discrepancies we have defined a set of physical constants adopted in our calculations which we summarise in Table 1.

Table 1. Adopted physical constants.

Quantity	Value	Unit
Solar mass M_{\odot}	1.9890×10^{30}	kg
Solar radius R_{\odot}	6.95508×10^8	m
Solar luminosity L_{\odot}	3.846×10^{26}	$\text{kg m}^2 \text{s}^{-3}$
Gravitational constant G	6.67232×10^{-11}	$\text{m}^3 \text{kg}^{-1} \text{s}^{-2}$

Notes. Solar mass and gravitational constant are defined based on the measurement of GM_{\odot} (see e.g. Christensen-Dalsgaard et al. 2005, and references therein).

The convergence criterion is chosen to scale with the mean stellar density due to the dependence of the adiabatic oscillation frequencies on this quantity (cf. Aerts et al. 2010). By enforcing this criterion we ensure that differences in the asymptotic large frequency separation are not a consequence of differences in the mass and radius of the models but only on the details of the adiabatic sound speed profile (and therefore in the treatment of opacities, equation of state, etc. see e.g. Belkacem et al. 2013). The tolerance has been set to 2×10^{-4} as a compromise between ease of finding the required model across an evolutionary track and reproducing the acoustic modes of oscillation at a level better than the current uncertainties of the longest seismic observations from the *Kepler* mission (below the $\sim 0.1 \mu\text{Hz}$ level, see e.g. Davies et al. 2016; Lund et al. 2017; Yu et al. 2018). We note that in most cases the comparison points were chosen at specific radii for a given mass value, which defines the quantities α and β in the denominator of Eq. (1). Since the gravitational constant adopted by all codes is the same, once the quantities α and β are defined for each science case the convergence criterion only depends on a ratio between mass and radius (in this case the mean density) of the evolutionary model in question. Because some codes consider the mass change during the evolution produced by the nuclear energy release, M_{model} is not exactly the same as $\alpha \times M_{\odot}$ when the model reaches the radius $\beta \times R_{\odot}$. These differences are compensated with variations in radius to reach the required precision and therefore ensure a consistent mean stellar density across all models compared at a given radius. Our convergence criterion is nevertheless generally applicable to cases in which different physical constants or input physics are used that can vary the quantities entering Eq. (1), and the results of that comparison is the subject of the study by Angelou et al. (in prep.).

3. Stellar evolution codes

Results have been computed with different stellar evolution codes that are widely used for producing sets of tracks and isochrones and have been applied in a broad range of fields of astrophysics. We use the fgong file format as the standard to export and compare interior models, which includes a comprehensive set of global stellar properties and quantities of interest for stellar evolution and asteroseismic comparisons. Tracks in ASCII format including the complete evolution are also compiled and available on the website.

The stellar evolution codes participating in the Aarhus red giants challenge are: ASTEC (Christensen-Dalsgaard 2008), BaSTI (Pietrinferni et al. 2004), CESAM2k (Morel & Lebreton 2008), GARSTEC (Weiss & Schlattl 2008), LPCODE (Althaus et al. 2003), MESA (Paxton et al. 2011), MONSTAR (Constantino et al. 2015), YaPSI (Spada et al. 2017), and YREC (Demarque et al.

2008). For the interested reader, a detailed description of the codes including additional ingredients entering the calculations (such as neutrino losses) is given in Appendix A.

4. Solar radius calibration

Convection has been treated using the mixing-length theory in all calculations. Since the exact implementation of this theory varies across evolutionary codes (see e.g. Salaris & Cassisi 2008, for a discussion), we have initially set up a solar radius calibration to determine the corresponding convective efficiency to be used in all subsequent calculations. The codes were requested to match the solar radius of 6.95508×10^{10} cm at an age of 4.57 Gyr by tuning the mixing-length parameter α_{MLT} ($l_{\text{MLT}} = \alpha_{\text{MLT}} \times H_p$, where H_p is the local pressure scale height) and fixing the initial hydrogen abundance to $X = 0.7$. Given that microscopic diffusion is not included in the standard input physics described in Sect. 2, the solar surface abundances $Z/X = 0.0245$ from the Grevesse et al. (1993) mixture define the initial composition to be $Z = 0.01715$ and $Y = 0.28285$. Consequently, the current solar luminosity and effective temperature were not quantities to be reproduced as part of the calibration.

The choice of this rather unusual procedure to calibrate the convective efficiency was motivated by the constraints from the adopted input physics (i.e. no microscopic diffusion), and the goal of producing stellar structures that have the same mean density as ensured by our convergence criterion in Eq. (1). This is the reason why the solar radius was chosen as the quantity to be reproduced by tuning the mixing-length value instead of the solar luminosity, for instance.

Table C.1 presents the results of this exercise for the participating evolutionary codes. As expected, the obtained luminosity is about 20% higher than solar and the effective temperatures hotter than the Sun by about ~ 250 K. These discrepancies with respect to the solar values are the result of the chosen constraint and input physics, in particular the lower bulk metallicity of the models compared to that of the Sun. It is worth noticing that already at this evolutionary stage the numerical implementation of the evolutionary codes produces variations of up to ~ 40 K and $0.03 L_{\odot}$. How these differences develop at later evolutionary phases is discussed in the following sections.

5. Evolutionary tracks: solar-radius calibrated

Using the standardised input physics, fundamental constants, and the value of the mixing-length parameter α_{MLT} calibrated as described in Sect. 4, we computed our first science cases consisting of evolutionary tracks with masses 1.0, 1.5, 2.0, and $2.5 M_{\odot}$ at a composition of $Y = 0.28$ and $Z = 0.02$. The aim of this exercise was to provide the best-case scenario of model comparisons, namely using the same input physics for all evolutionary codes after calibrating them to a common point in the main-sequence phase. Differences between models reveal the minimum level of systematic uncertainties arising solely from the numerical implementation of each evolutionary code that can be expected when determining stellar properties of red giants using isochrone fitting techniques, for example. We emphasise once again that this is the rationale behind choosing comparison points at fixed mass and radius. In astrophysical applications these quantities are normally not known to a high enough precision to effectively serve as benchmarks for our study.

The overall evolution of these stellar tracks is shown in Fig. 1 where it can be seen that differences in effective temperature

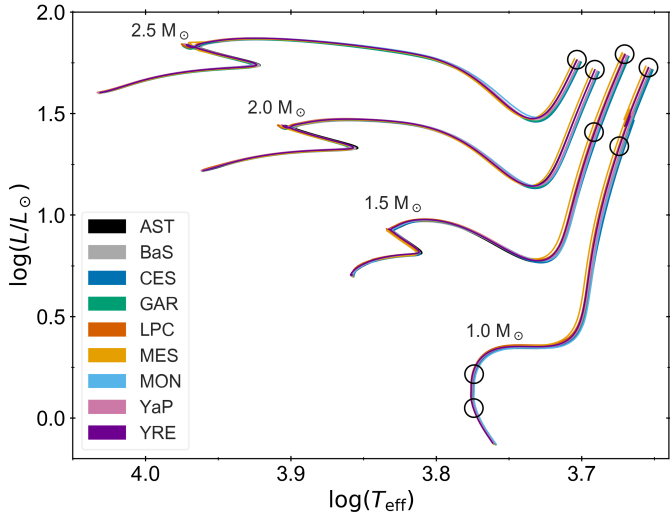


Fig. 1. Hertzsprung–Russell diagram (HRD) of solar-radius calibrated science cases for all participating codes. The position of the stellar models used in our comparisons are shown with open circles. See text for details.

appear on the main sequence and further increase during the red-giant-branch phase. To better understand their origin we compared the interior structure of models at different evolutionary points (see circles in Fig. 1 and Tables C.2, C.3, and C.4), which we analyse in detail in the following sections. We note that the change in composition with respect to the solar radius calibration values was motivated by the existence of original opacity tables at $Z = 0.02$ and thus aiming at minimising differences due to interpolations in the opacity calculations across tables.

5.1. Evolution of $1.0 M_{\odot}$ models

Besides models at a fixed value of stellar radius, we also consider a comparison point at the end of the main-sequence phase (the Terminal Age Main Sequence – TAMS), which we define the stage where the fractional hydrogen abundance in the centre reaches $X_c = 1 \times 10^{-5}$. The tracks are computed from the zero-age main sequence, but some of them include the final phases of the pre-main sequence to produce a properly converged initial model. The net result is that the age across codes is not exactly zero at the ZAMS, and we correct for this effect by defining an age of zero in all calculations at the point where $X_c = 0.69$.

As mentioned in Sect. 4, our resulting solar radius calibration models have the desired solar radius and age but different effective temperatures. In order to quantify the temperature differences in other evolutionary phases after changing the composition, we subtract the T_{eff} difference between the solar radius calibration models of each code and that of ASTEC, which was chosen as the reference. The left panel in Fig. 2 shows effective temperature differences at the considered evolutionary points relative to the ASTEC results with the offset arising from the solar radius calibration already subtracted. The slight change in chemical composition in this exercise ($Y = 0.28$, $Z = 0.02$) compared to the one used in the solar radius calibration ($Y = 0.28285$, $Z = 0.01715$) already induces a divergence in the predicted effective temperature across codes at the level of ~ 20 K for models at $1 R_{\odot}$. These differences are sustained when models reach the TAMS but have increased in the RGB phase to about 40 K. We consider this 20 K and 40 K spread as the minimum level of systematic uncertainty introduced by evolutionary codes in

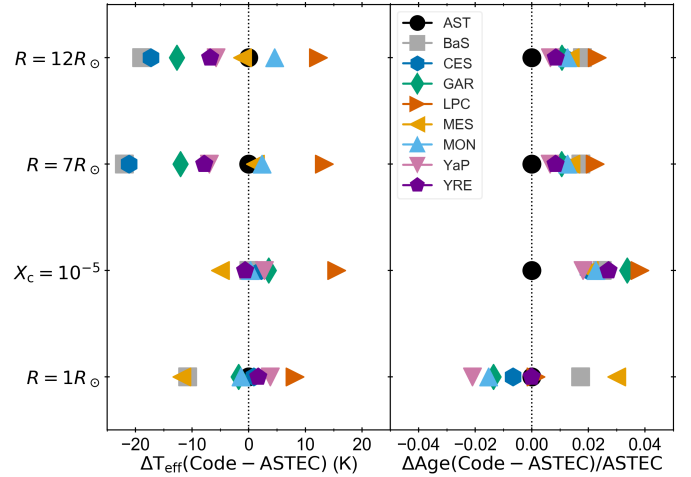


Fig. 2. Differences in $1.0 M_{\odot}$ solar-radius calibrated tracks relative to ASTEC results at different evolutionary points. *Left:* effective temperature differences after correcting for the calibration offset. *Right:* fractional age differences. See text for details.

the effective temperature scale of $1 M_{\odot}$ main-sequence and RGB evolutionary tracks, respectively. This is a remarkable result showing the level of precision in effective temperature that can currently be achieved by stellar models.

Although the solar radius calibration was performed at a fixed age of 4.57 Gyr, changing the chemical composition in the science cases with respect to the one adopted in the calibration results in models reaching the solar radius after ~ 5.3 Gyr. This is primarily due to their higher metallicity, $Z = 0.02$ compared to $Z = 0.01715$, leading to a higher opacity κ and a lower stellar luminosity, and therefore a slower main-sequence evolution. At $1 R_{\odot}$ age differences of $\sim 5\%$ are already evident, but interestingly enough once the models reach the end of the main sequence all codes show a remarkable agreement in age that is systematically older than the ASTEC results. Once the evolution proceeds towards the red-giant branch the age scatter reaches the 2% level and remains constant in this phase.

The reason for this variation is related to the efficiency in the conversion of hydrogen into helium during the main-sequence phase assigned by each code. The left panel of Fig. 3 shows the derivative of the central hydrogen abundance with respect to age as a function of age, where differences in the evolutionary speeds across codes are already visible after ~ 5 Gyr of evolution. The ASTEC track has a much steeper slope than the rest of the codes, which results in a quicker evolution and younger age when the TAMS is reached. The right panel of Fig. 3 compares the maximum value of nuclear energy generation relative to ASTEC as a function of central temperature. The general trend is that the codes that evolve slowest (BaSTI, GARSTEC, and LPCODE) present the lowest central temperature and value of nuclear energy generation, while conversely the quickest to evolve (ASTEC) has one of the highest. This difference can be tracked down to the energy generation routines used in each code: we have recomputed, using the ASTEC routine, the value of ϵ by adopting the thermal, density and chemical stratification originally provided by each code, and found differences with the original values of similar size as those reported in Fig. 3. Nevertheless, this trend in speed of evolution cannot be solely ascribed to the energy generation routines, as for example the MESA model evolves comparatively slow despite its high central temperature value. The remaining differences may come from e.g., the interpolation schemes used for extracting the opacity values.

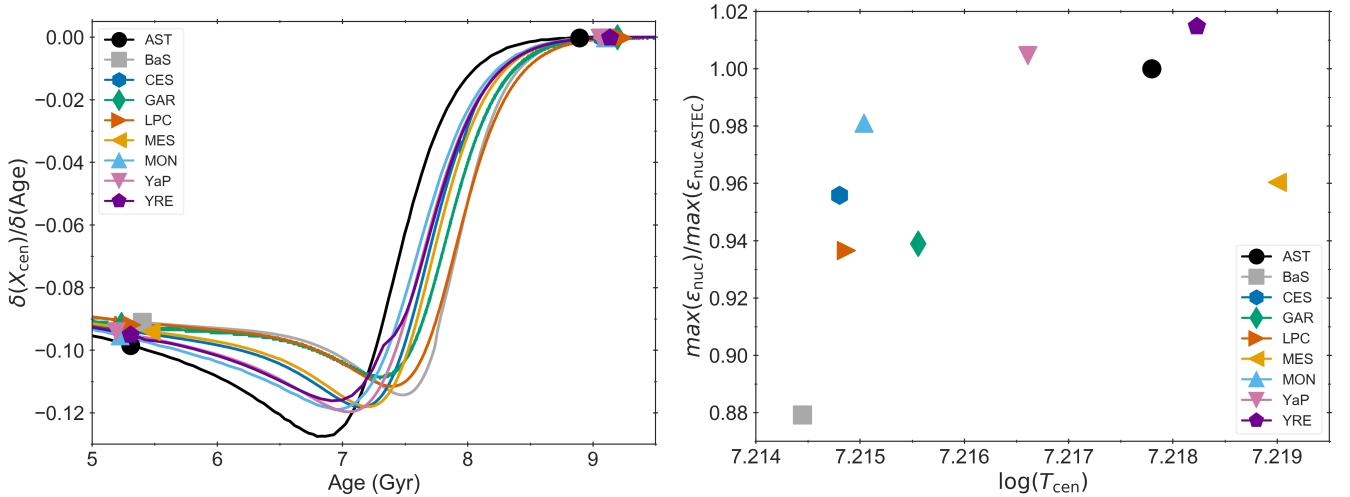


Fig. 3. *Left:* time derivative of the central hydrogen content X_{cen} as a function of age for the $1 M_{\odot}$ solar-radius calibrated tracks. Symbols depict the location of models at $1 R_{\odot}$ and at the end of the main-sequence phase. *Right:* ratio of the maximum nuclear energy generation rate for each code relative to the ASTEC value as a function of the central temperature for the $1 M_{\odot}$ at $1 R_{\odot}$ solar-radius calibrated models.

In order to quantify the efficiency of energy conversion we computed the ratio between the integral of the luminosity with respect to time along the evolution until the analysed model and the amount of hydrogen processed during that period of time:

$$\Lambda = \frac{\int_0^T L dt}{c^2 \left(\int_0^M X_{t=0} dm - \int_0^M X_{t=T} dm \right)} \quad (2)$$

All physical input being the same, the differences in luminosity should be traceable to differences in the amount of hydrogen converted to helium, and therefore the dimensionless ratio Λ in Eq. (2) should be of constant value across codes. The results are given in Table C.2 where differences up to $\sim 5\%$ around the median are seen in the RGB phase across all evolutionary codes in agreement with the differences found in the maximum energy generation rates.

The interior hydrogen profile in the region comprising the edge of the helium core and the point of deepest penetration during the first dredge up are shown in Fig. 4, together with corresponding surface values of $[\text{O}/\text{Fe}]$ and $[\text{C}/\text{N}]$. The latter quantity is of particular importance in the field of Galactic archaeology as it depends on the depth reached by the first dredge up, which is in turn highly sensitive to stellar mass (see e.g. Salaris et al. 2015; Martig et al. 2016). Under these assumptions, masses (and therefore ages) of red giants can be readily extracted from observed $[\text{C}/\text{N}]$ abundances after model-dependent calibrations of the mass- $[\text{C}/\text{N}]$ relation as a function of metallicity (Ness et al. 2016). Our evolutionary codes predict a scatter of about 0.15 dex in the $[\text{C}/\text{N}]$ ratio for the same metallicity and input physics, which comes partly from the different dredge-up depths seen in the hydrogen profiles in Fig. 4. The scatter in the predicted $[\text{O}/\text{Fe}]$ is below 0.02 dex and smaller than the uncertainties reported in alpha-element abundances by large spectroscopic surveys (e.g. APOGEE, Abolfathi et al. 2018).

The discontinuity in composition left behind by the inwards penetration of the convective envelope during the first dredge-up is eventually reached by the advancing H-burning shell, resulting in a decrease in the luminosity known as the RGB-bump (see e.g. Christensen-Dalsgaard 2015, and references therein). The position of the RGB-bump is particularly interesting in studies of stellar clusters because isochrone fitting techniques aim at

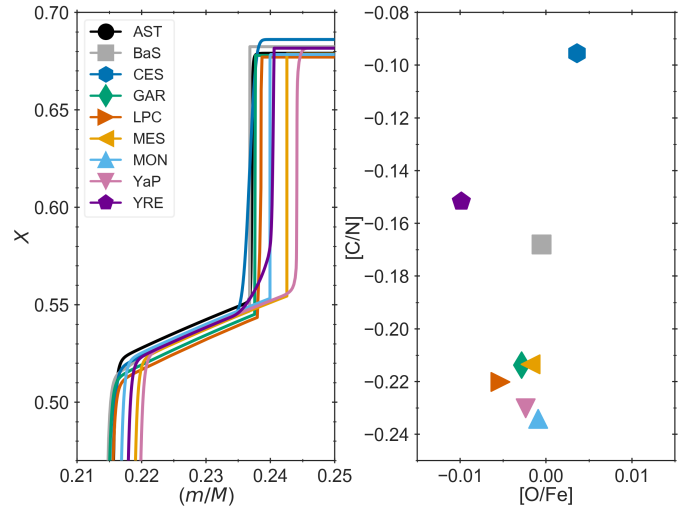


Fig. 4. Composition characteristics of $1 M_{\odot}$ solar-radius calibrated models at $7 R_{\odot}$. *Left:* interior hydrogen profile as a function of mass zoomed in around the point of deepest penetration of the convective envelope during the first dredge-up. *Right:* ratio $[\text{C}/\text{N}]$ as a function of oxygen abundance $[\text{O}/\text{Fe}]$ at the surface.

reproducing its observed luminosity. Current state-of-the-art evolutionary calculations predict bump locations ~ 0.2 mag brighter than observed in clusters (e.g. Cassisi et al. 2011; Angelou et al. 2015). The results of our exercise show differences up to $\sim 4 L_{\odot}$ (or $\sim 13\%$) in the bump luminosity across codes, with the MESA model reporting the highest value and CESAM2k the lowest. We transformed the tracks to the observational plane using the routine of bolometric corrections described in Sect. 4.2 of Hidalgo et al. (2018), and shown in the right panel of Fig. 5. The difference in the bolometric luminosity of the RGB bump as predicted by the various codes translates into a spread of about 0.15 mag in the Johnson V band.

One could note that this value is of the same order of magnitude of the (typical) observed discrepancy between observations and standard model predictions of the bump luminosity. For instance, BaSTI models appear about 0.2 mag brighter than observational data for the RGB-bump in Galactic

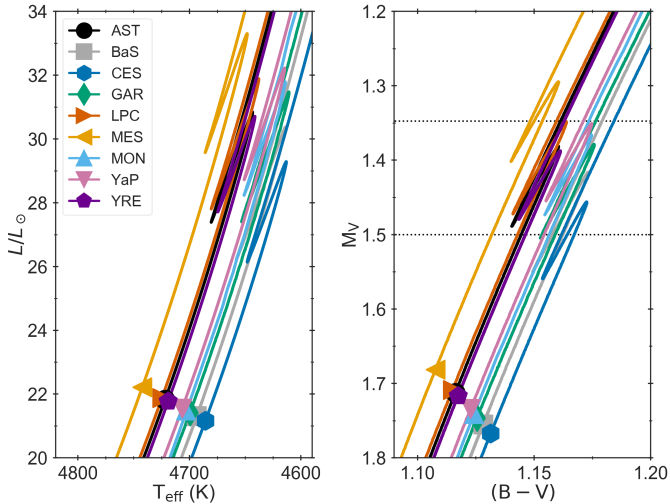


Fig. 5. *Left:* HRD depicting the $1 M_{\odot}$ solar-radius calibrated tracks and the position of models at $7 R_{\odot}$. *Right:* optical band colour–magnitude diagram of the $1 M_{\odot}$ solar-radius calibrated tracks and corresponding models at $7 R_{\odot}$. Horizontal dashed lines mark the position of the brightest and faintest predicted bump absolute magnitudes across the codes to guide the eye.

Globular Clusters (see detailed discussion in [Cassisi et al. 2011](#); [Cassisi & Salaris 2013](#)). Our results show that the BaSTI models predict one of the faintest luminosity for this feature among those shown in Fig. 5, suggesting that the difference between the observed and predicted bump luminosity cannot be ascribed to discrepancies on how evolutionary codes manage the location of the canonical convective envelope boundary, but is the direct result of a first dredge-up event that does not penetrate deep enough in all evolutionary codes for the considered input physics. Similar results were found by [Khan et al. \(2018\)](#) who analysed a sample of red giants observed with *Kepler* and found that overshoot from the convective envelope was required to reproduce the brightness of the RGB bump.

The next comparison point was beyond the RGB luminosity bump at a radii of $12 R_{\odot}$. In this case the interior hydrogen profiles present only one near-discontinuity corresponding to the position of the hydrogen-burning shell that is slowly moving outwards in mass as the helium core continues to grow. The surface chemical composition is the same as obtained at $7 R_{\odot}$ since, in the absence of any additional mixing process, there is no change in the surface composition after the RGB-bump (see Table C.2). Age differences remain at the same level as they were at $7 R_{\odot}$ (cf., Fig. 2) and are sustained in the subsequent evolution towards the RGB tip.

5.2. Evolution of $1.5 M_{\odot}$, $2.0 M_{\odot}$, and $2.5 M_{\odot}$ models

Using the same initial composition as in the $1 M_{\odot}$ case, we calculated and compared tracks and stellar structures at higher masses: $1.5 M_{\odot}$, $2.0 M_{\odot}$, and $2.5 M_{\odot}$. The first and most evident difference with respect to the lower-mass case is the existence of a convective core during the main-sequence evolution, whose extent as a function of age is depicted in Fig. 6. Although all codes rely on the Schwarzschild criterion for defining the core convective boundary there are differences in the predicted core size of the order of 10% across codes.

In many cases a saw-tooth profile is visible at the edge of the core as a consequence of changes in its chemical composition throughout the evolution. Nuclear burning produces changes

across the chemically homogeneous central region of the model. In the case of growing convective cores ($1.5 M_{\odot}$), the sharp increase in density at the edge of the core increases the opacity, which consequently increases the radiative temperature gradient in that position. As evolution proceeds and the discontinuity becomes larger, the radiative gradient outside the core surpasses the value of the adiabatic gradient turning that additional layer convectively unstable. The core suddenly increases in size as is revealed by the sharp spikes in the core profiles (see left panel in Fig. 6), and the subsequent fast decrease in the core extent occurs once the composition of the layer is homogenised to the core value. The radiative temperature gradient then decreases as a result of the opacity decrease and the layer becomes convectively stable again (see e.g. [Silva Aguirre et al. 2011](#); [Gabriel et al. 2014](#)). The existence of these “peaks” in the core size as a function of time are the result of the numerical implementation of the Schwarzschild criterion in evolutionary codes, and the behaviour of the core boundary is expected to be smooth as a function of time in real stars. For the higher-mass cases ($2 M_{\odot}$ and $2.5 M_{\odot}$) the evolution of the convective-core size is indeed smoother as it reaches its maximum extension at the beginning of the main sequence and contracts throughout the core hydrogen-burning phase.

One of the expected consequences of the different convective-core sizes is variations in the time spent in the main-sequence phase due to the amount of hydrogen available for nuclear burning. Models with the largest main-sequence convective cores are the oldest at the point of central hydrogen exhaustion TAMS (e.g. MONSTAR and ASTEC for the $1.5 M_{\odot}$ case), while BaSTI (and CESAM2k for the $1.5 M_{\odot}$ track) has the smallest core and is the youngest at the TAMS (see Fig. 6). Age differences at the point of central hydrogen exhaustion are of the order of 4–5% for these masses across codes.

Effective temperatures and ages at the comparison points (selected radii in the RGB phase) are shown in Fig. 7. The variations in T_{eff} are at the ~ 30 K level after subtracting the difference arising from the solar radius calibration model (cf., Sect. 5.1), which is similar to the results found for the $1.0 M_{\odot}$ cases (see Fig. 2). This reinforces the notion that differences in temperature at the RGB phase due to the numerical implementations in each code contribute to only ~ 30 – 40 K regardless of the mass.

In terms of age differences, in the $1.0 M_{\odot}$ results we found a decrease in the age scatter between the TAMS and the RGB (from $\sim 3.5\%$ to $\sim 2\%$, see Fig. 2). For the $1.5 M_{\odot}$ models the decrease in age scatter goes from $\sim 5\%$ at the end of the main sequence (not shown in the figure) to $\sim 3\%$ on the RGB due to the size of the convective core: a larger mixed core in the hydrogen-burning phase translates into a longer main-sequence lifetime, which is compensated by faster evolution in the subgiant phase as the resulting helium core is closer to the Schönberg–Chandrasekhar limit (see [Miglio et al. 2015](#), and references therein). This effect is still partly evident in the $2.0 M_{\odot}$ models where the age scatter decreases from $\sim 5.3\%$ to $\sim 5\%$ between the TAMS and the RGB, and it is negligible at the higher mass end as seen by the constant age scatter of $\sim 5\%$ in the $2.5 M_{\odot}$ models throughout the main-sequence and red-giant-branch evolution.

An interesting feature from the asteroseismology point of view is seen in Fig. 8, where the interior profiles of hydrogen are shown for the following models: $1.5 M_{\odot}$ at $7 R_{\odot}$, $2.0 M_{\odot}$ at $10 R_{\odot}$, and $2.5 M_{\odot}$ at $10 R_{\odot}$. The differences in hydrogen profiles correspond to different density distributions, which in turn translate into differences in the Brunt–Väisälä frequency and therefore in the asteroseismic properties of the models. The point of deepest

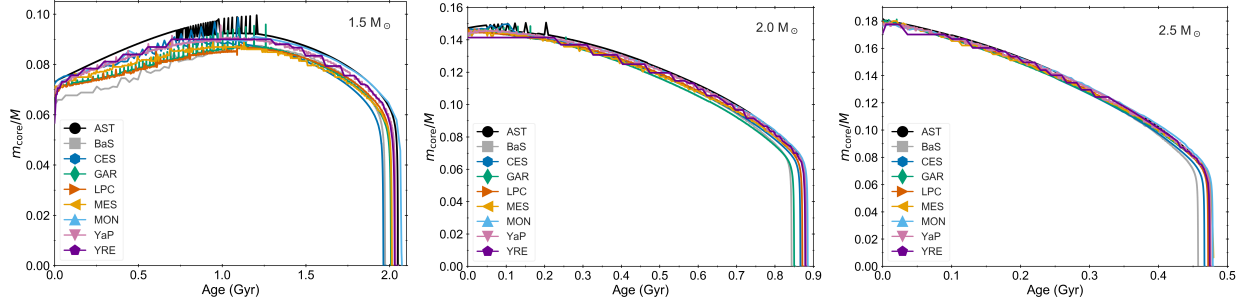


Fig. 6. Evolution of the convective-core size during the main-sequence phase as a function of age for the $1.5 M_{\odot}$ (left), $2.0 M_{\odot}$ (centre), and $2.5 M_{\odot}$ (right) solar-radius calibrated models.

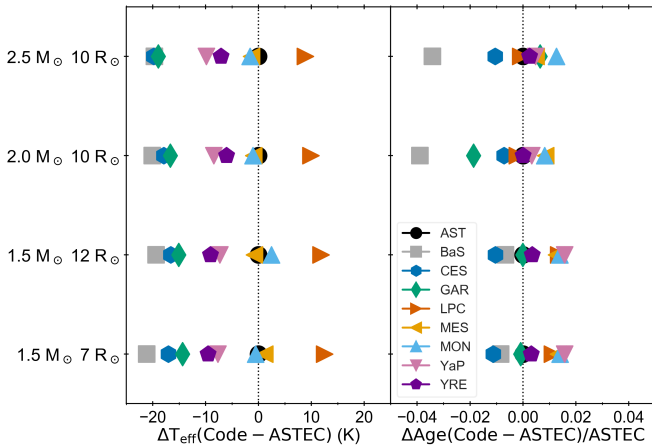


Fig. 7. Same as Fig. 2, but for $1.5 M_{\odot}$, $2.0 M_{\odot}$, and $2.5 M_{\odot}$ solar-radius calibrated models. *Left*: effective temperature differences. *Right*: fractional age differences. See text for details.

penetration of the convective envelope during the first dredge-up and the location of the H-burning shell produce a structural glitch in the Brunt–Väisälä frequency that could be detectable from asteroseismic inference (Cunha et al. 2015). The impact of these differences in hydrogen profiles on the predicted frequencies of oscillation is investigated in Paper II.

Figure 9 shows the position of the luminosity bump in the HRD, revealing once again differences of $\sim 6 L_{\odot}$ (or $\sim 10\%$) across codes that translate into ~ 0.12 mag in the V -band. This spread is of the same magnitude as found in the $1 M_{\odot}$ case and reinforces the notion that part of the discrepancy between observed and modelled RGB-bump luminosities is an effect of the treatment of convective boundaries in evolutionary calculations.

Variations in the luminosity integral (cf., Eq. (2)) are of the order of 3–5% around the median for the $1.5 M_{\odot}$, $2.0 M_{\odot}$, and $2.5 M_{\odot}$ solar-radius calibrated models on the RGB. These values are at a similar level as those found in the $1 M_{\odot}$ case, and suggest that differences are related to the implementation of the CNO-cycle during the central hydrogen-burning phase. The ratios of carbon to nitrogen as a function of oxygen for the high mass models are depicted in Fig. 10. The scatter in $[O/Fe]$ is below 0.03 dex, while the abundances of $[C/N]$ show a spread of about 0.1 dex. This level of variation is similar to that found in the $1 M_{\odot}$ science case and suggests that observations of the $[C/N]$ ratio to determine masses should be treated with caution, as the calibrators needed to correlate abundances with stellar properties can suffer from systematics as those shown in these calculations.

6. Summary and conclusions

We have presented the first sets of science cases for the Aarhus red giants challenge, a series of workshops focused on in-depth comparison of stellar evolution and pulsation codes. We produced evolutionary tracks and structure models in the RGB phase after calibrating the mixing length parameter to the solar radius at solar age, while keeping the input physics and fundamental constants the same for all participating codes. Thus, our results can be regarded as the minimum level of systematic uncertainty in evolutionary models of red-giant-branch stars arising solely due to the numerical implementation and underlying assumptions adopted in stellar evolution codes. Our main findings can be summarised as follows:

- Changing the chemical composition of our models after the solar-radius calibration produces differences in effective temperature in the main-sequence phase at the 20 K level. This result suggests that theoretical temperatures are not accurate below this threshold.
- Evolutionary tracks of different masses on the RGB present effective temperature differences of the order of 30–40 K, and age differences increasing from 2% at $1 M_{\odot}$ to 5% at $2.5 M_{\odot}$. The age scatter can be partly traced back to the energy generation routines used by each code, as also revealed by the differences in the energy produced per gram of burned hydrogen (cf., Eq. (2)).
- For the $1.0 M_{\odot}$ and $1.5 M_{\odot}$ cases where evolution proceeds through the RGB-bump we obtain differences of the order of 10% in the bump mean luminosity, which translates into a spread of ~ 0.1 mag in absolute visual magnitude. However, since the bumps for the BaSTI models, which are already brighter by about 0.2 mag than empirical measurements, are among the faintest ones, this result indicates that the first dredge-up event is not deep enough in all considered stellar evolution codes when using the input physics we adopted.
- We find good agreement in the predicted abundance of oxygen on the RGB, but a significant spread of 0.1 dex in the $[C/N]$ ratio. Care must be taken when using this ratio as a tracer of mass after calibration to evolutionary calculations, since there is no unique correlation between the model masses, their metallicities, and their predicted carbon and nitrogen abundances after the first dredge-up.

We would like to close this paper with a short summary about the learning process resulting from the Aarhus red giants challenge. During 9 one-week workshops over the past 7 years we have been sitting together as code developers and openly compared our evolutionary codes, digging deep into routines that in some cases have been written decades ago. We have found bugs and inconsistencies in every single one of the participating codes that

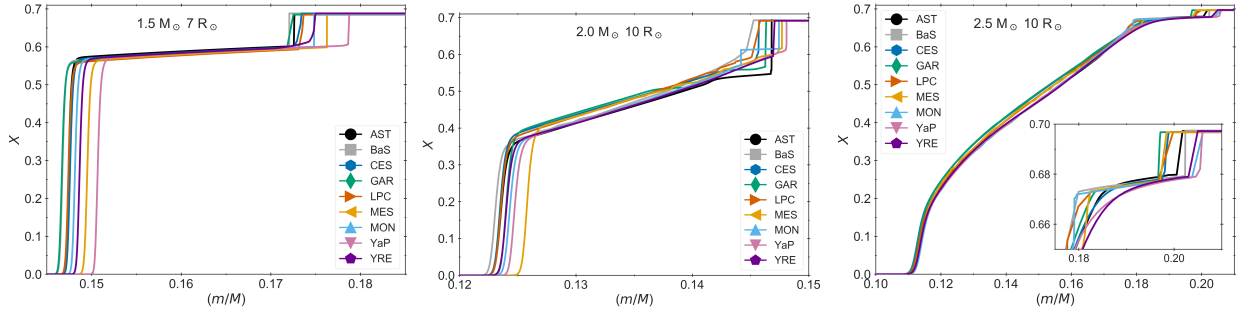


Fig. 8. Hydrogen profiles for models before the RGB bump of $1.5 M_{\odot}$ ($7 R_{\odot}$, left), $2.0 M_{\odot}$ ($10 R_{\odot}$, centre), and $2.5 M_{\odot}$ ($10 R_{\odot}$, right) solar-radius calibrated models.

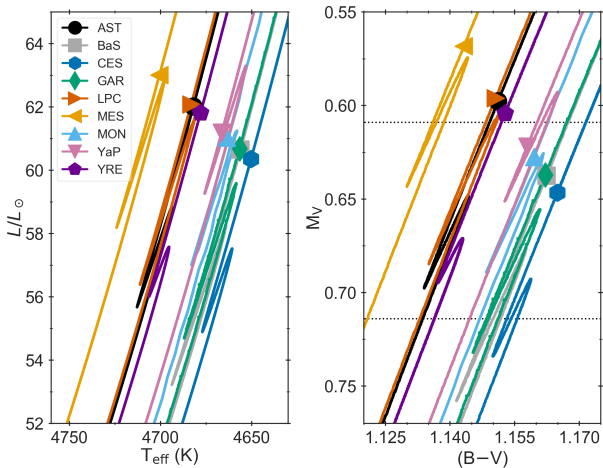


Fig. 9. Same as Fig. 5, but for $1.5 M_{\odot}$ tracks of solar-radius calibrated models.

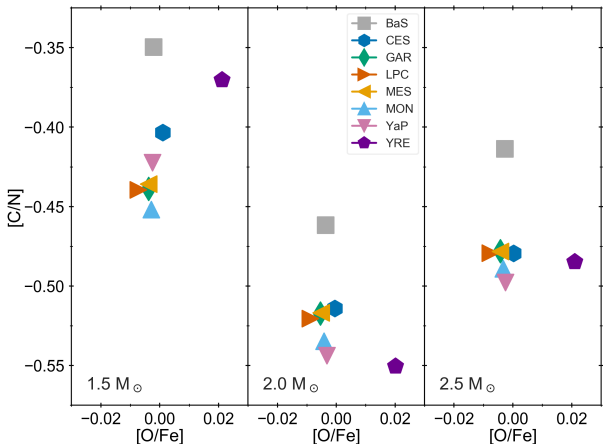


Fig. 10. Abundance of $[C/N]$ as a function of oxygen abundance for solar-radius calibrated models in the RGB. From left to right: $1.5 M_{\odot}$ at $7 R_{\odot}$, $2.0 M_{\odot}$ at $10 R_{\odot}$, $2.5 M_{\odot}$ at $10 R_{\odot}$.

have helped improve our numerical and physical prescriptions as well as understanding the underlying source of differences in our results. We are certain that our codes have become more robust in this process, and we are sure that such tests and comparisons are necessary for every stellar evolution code in order to guarantee a certain level of precision. The comparisons are being extended to the helium-burning phase and will include additional input physics as part of this series, always keeping the goal in mind of providing a better representation than before of the changing properties of stars as they evolve from the main sequence to the red-giant phase.

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References

- Abolfathi, B., Aguado, D. S., Aguilar, G., et al. 2018, *ApJS*, **235**, 42
- Aerts, C., Christensen-Dalsgaard, J., & Kurtz, D. W. 2010, *Asteroseismology* (Berlin: Springer Science & Business Media)
- Akima, H. 1991, *ACM Trans. Math. Softw.*, **17**, 341
- Alastuey, A., & Jancovici, B. 1978, *ApJ*, **226**, 1034
- Althaus, L. G., Serenelli, A. M., Córscico, A. H., & Montgomery, M. H. 2003, *A&A*, **404**, 593
- Anders, F., Chiappini, C., Rodrigues, T. S., et al. 2017, *A&A*, **597**, A30
- Angelou, G. C., D'Orazi, V., Constantino, T. N., et al. 2015, *MNRAS*, **450**, 2423
- Angulo, C., Arnould, M., Rayet, M., et al. 1999, *Nucl. Phys. A*, **656**, 3
- Baglin, A., Michel, E., Auvergne, M., & Team, T. C. 2006, *Proceedings of SOHO 18/GONG 2006/HELAS I*, 624, 34
- Bahcall, J. N. 1989, *Neutrino Astrophysics* (Cambridge: Cambridge University Press)
- Basu, S., Grundahl, F., Stello, D., et al. 2011, *ApJ*, **729**, L10
- Beaudet, G., Petrosian, V., & Salpeter, E. E. 1967, *ApJ*, **150**, 979
- Beck, P. G., Montalbán, J., Kallinger, T., et al. 2012, *Nature*, **481**, 55
- Bedding, T. R., Mosser, B., Huber, D., et al. 2011, *Nature*, **471**, 608
- Belkacem, K., Samadi, R., Mosser, B., Goupil, M. J., & Ludwig, H. G. 2013, *Progress in Physics of the Sun and Stars: A New Era in Helio- and Asteroseismology, Proceedings of a Fujihara Seminar held 25–29 November*, 61
- Bossini, D., Miglio, A., Salaris, M., et al. 2017, *MNRAS*, **469**, 4718
- Bressan, A., Marigo, P., Girardi, L., et al. 2012, *MNRAS*, **427**, 127
- Brogaard, K., Bruntt, H., Grundahl, F., et al. 2011, *A&A*, **525**, A2
- Brogaard, K., Hansen, C. J., Miglio, A., et al. 2018, *MNRAS*, **476**, 3729
- Cantiello, M., Mankovich, C., Bildsten, L., Christensen-Dalsgaard, J., & Paxton, B. 2014, *ApJ*, **788**, 93
- Casagrande, L., Silva Aguirre, V., Stello, D., et al. 2014, *ApJ*, **787**, 110
- Casagrande, L., Silva Aguirre, V., Schlesinger, K. J., et al. 2016, *MNRAS*, **455**, 987
- Cassisi, S., & Salaris, M. 2013, *Old Stellar Populations: How to Study the Fossil Record of Galaxy Formation* (New York: Wiley)
- Cassisi, S., Potekhin, A. Y., Pietrinferni, A., Catelan, M., & Salaris, M. 2007, *ApJ*, **661**, 1094

- Cassisi, S., Marin-Franch, A., Salaris, M., et al. 2011, *A&A*, **527**, A59
- Choi, J., Dotter, A., Conroy, C., et al. 2016, *ApJ*, **823**, 102
- Christensen-Dalsgaard, J. 2008, *Ap&SS*, **316**, 13
- Christensen-Dalsgaard, J. 2015, *MNRAS*, **453**, 666
- Christensen-Dalsgaard, J., Di Mauro, M. P., Schlattl, H., & Weiss, A. 2005, *MNRAS*, **356**, 587
- Christensen-Dalsgaard, J., Silva Aguirre, V., Cassisi, S., et al. 2020, *A&A*, **635**, A165
- Constantino, T., Campbell, S. W., Christensen-Dalsgaard, J., Lattanzio, J. C., & Stello, D. 2015, *MNRAS*, **452**, 123
- Cunha, M. S., Stello, D., Avelino, P. P., Christensen-Dalsgaard, J., & Townsend, R. H. D. 2015, *ApJ*, **805**, 1
- Davies, G. R., Aguirre, V. S., Bedding, T. R., et al. 2016, *MNRAS*, **456**, 2183
- De Ridder, J., Barban, C., Baudin, F., et al. 2009, *Nature*, **459**, 398
- De Ridder, J., Molenberghs, G., Eyer, L., & Aerts, C. 2016, *A&A*, **595**, L3
- Demarque, P., Guenther, D. B., Li, L. H., Mazumdar, A., & Straka, C. W. 2008, *Ap&SS*, **316**, 31
- Dewitt, H. E., Graboske, H. C., & Cooper, M. S. 1973, *ApJ*, **181**, 439
- Dicus, D. A., Kolb, E. W., Schramm, D. N., & Tubbs, D. L. 1976, *ApJ*, **210**, 481
- Dotter, A., Chaboyer, B., Jevremović, D., et al. 2008, *ApJS*, **178**, 89
- Ferguson, J. W., Alexander, D. R., Allard, F., et al. 2005, *ApJ*, **623**, 585
- Festa, G. G., & Ruderman, M. A. 1969, *Phys. Rev.*, **180**, 1227
- Frandsen, S., Lehmann, H., Hekker, S., et al. 2013, *A&A*, **556**, A138
- Gabriel, M., Noels, A., Montalbán, J., & Miglio, A. 2014, *A&A*, **569**, A63
- Gaulme, P., McKeever, J., Jackiewicz, J., et al. 2016, *ApJ*, **832**, 121
- Gilliland, R. L., Brown, T. M., Christensen-Dalsgaard, J., et al. 2010, *PASP*, **122**, 131
- Graboske, H. C., Dewitt, H. E., Grossman, A. S., & Cooper, M. S. 1973, *ApJ*, **181**, 457
- Grevesse, N., & Noels, A. 1993, in *35ème cours de perfectionnement de l'Association Vandoise des Chercheurs en Physique*, eds. B. Hauck, S. Paltani, & D. Raboud (Lausanne: AVCP), 205
- Haft, M., Raffelt, G., & Weiss, A. 1994, *ApJ*, **425**, 222
- Hidalgo, S. L., Pietrinferni, A., Cassisi, S., et al. 2018, *ApJ*, **856**
- Huber, D., Ireland, M. J., Bedding, T. R., et al. 2012, *ApJ*, **760**, 32
- Huber, D., Zinn, J., Bojsen-Hansen, M., et al. 2017, *ApJ*, **844**
- Iglesias, C. A., & Rogers, F. J. 1996, *ApJ*, **464**, 943
- Itoh, N., Totsuji, H., Ichimaru, S., & Dewitt, H. E. 1979, *ApJ*, **234**, 1079
- Itoh, N., Adachi, T., Nakagawa, M., Kohyama, Y., & Munakata, H. 1989, *ApJ*, **339**, 354
- Itoh, N., Hayashi, H., Nishikawa, A., & Kohyama, Y. 1996, *ApJS*, **102**, 411
- Khan, S., Hall, O. J., Miglio, A., et al. 2018, *ApJ*, **859**, 156
- Lebreton, Y., Monteiro, M. J. P. F. G., Montalbán, J., et al. 2008, *Astrophys. Space Sci.*, **316**, 1
- Lund, M. N., Silva Aguirre, V., Davies, G. R., et al. 2017, *ApJ*, **835**, 1
- Marigo, P., & Aringer, B. 2009, *A&A*, **508**, 1539
- Marques, J. P., Goupil, M. J., Lebreton, Y., et al. 2013, *A&A*, **549**, A74
- Martig, M., Fouesneau, M., Rix, H.-W., et al. 2016, *MNRAS*, **456**, 3655
- Miglio, A., Chiappini, C., Morel, T., et al. 2013, *MNRAS*, **429**, 423
- Miglio, A., Girardi, L., Rodrigues, T. S., Stello, D., & Chaplin, W. J. 2015, in *Asteroseismology of Stellar Populations in the Milky Way*, eds. A. Miglio, P. Eggenberger, L. Girardi, & J. Montalbán, *Astrophys. Space Sci. Proc.*, **39**, 11
- Miller Bertolami, M. M. 2016, *A&A*, **588**, A25
- Mohr, P. J., Newell, D. B., & Taylor, B. N. 2016, *Rev. Mod. Phys.*, **88**, 035009
- Montalbán, J., Miglio, A., Noels, A., et al. 2013, *ApJ*, **766**, 118
- Morel, P. 1997, *A&AS*, **124**, 597
- Morel, P., & Lebreton, Y. 2008, *Ap&SS*, **316**, 61
- Mosser, B., Goupil, M. J., Belkacem, K., et al. 2012, *A&A*, **548**, A10
- Mosser, B., Belkacem, K., Pinçon, C., et al. 2017, *A&A*, **598**, A62
- Ness, M., Hogg, D. W., Rix, H. W., et al. 2016, *ApJ*, **823**, 114
- Paxton, B., Bildsten, L., Dotter, A., et al. 2011, *ApJS*, **192**, 3
- Paxton, B., Cantiello, M., Arras, P., et al. 2013, *ApJS*, **208**, 4
- Pietrinferni, A., Cassisi, S., Salaris, M., & Castelli, F. 2004, *ApJ*, **612**, 168
- Pietrinferni, A., Cassisi, S., Salaris, M., & Castelli, F. 2006, *ApJ*, **642**, 797
- Pietrinferni, A., Cassisi, S., Salaris, M., Percival, S., & Ferguson, J. W. 2009, *ApJ*, **697**, 275
- Pietrinferni, A., Cassisi, S., Salaris, M., & Hidalgo, S. 2013, *A&A*, **558**, A46
- Pinsonneault, M. H., Elsworth, Y., Epstein, C., et al. 2014, *ApJS*, **215**, 19
- Pinsonneault, M. H., Elsworth, Y. P., Tayar, J., et al. 2018, *ApJS*, **239**, 32
- Ramadurai, S. 1976, *MNRAS*, **176**, 9
- Rodrigues, T. S., Girardi, L., Miglio, A., et al. 2014, *MNRAS*, **445**, 2758
- Rogers, F. J., & Nayfonov, A. 2002, *ApJ*, **576**, 1064
- Sahlholdt, C. L., Silva Aguirre, V., Casagrande, L., Mosumgaard, J. R., & Bojsen-Hansen, M. 2018, *MNRAS*, **476**, 1931
- Salaris, M., & Cassisi, S. 2008, *A&A*, **487**, 1075
- Salaris, M., Pietrinferni, A., Piersimoni, A. M., & Cassisi, S. 2015, *A&A*, **583**, A87
- Salpeter, E. E. 1954, *Aust. J. Phys.*, **7**, 373
- Salpeter, E. E. 1961, *ApJ*, **134**, 669
- Schwarzschild, M., & Härm, R. 1958, *ApJ*, **128**, 348
- Serenelli, A. M., Bergemann, M., Ruchti, G., & Casagrande, L. 2013, *MNRAS*, **429**, 3645
- Sharma, S., Stello, D., Bland-Hawthorn, J., Huber, D., & Bedding, T. R. 2016, *ApJ*, **822**, 15
- Silva Aguirre, V., & Serenelli, A. M. 2016, *Astron. Nachr.*, **337**, 823
- Silva Aguirre, V., Ballot, J., Serenelli, A. M., & Weiss, A. 2011, *A&A*, **529**, A63
- Silva Aguirre, V., Casagrande, L., Basu, S., et al. 2012, *ApJ*, **757**, 99
- Silva Aguirre, V., Bojsen-Hansen, M., Slumstrup, D., et al. 2018, *MNRAS*, **475**, 5487
- Spada, F., Demarque, P., Kim, Y.-C., Boyajian, T. S., & Brewer, J. M. 2017, *ApJ*, **838**, 161
- Späth, H. 1991, *Zweidimensionale Spline-Interpolations-Algorithmen*
- Stello, D., Cantiello, M., Fuller, J., et al. 2016, *Nature*, **529**, 364
- Themeßl, N., Hekker, S., Southworth, J., et al. 2018, *MNRAS*, **478**, 4669
- Wallace, R. K., Woosley, S. E., & Weaver, T. A. 1982, *ApJ*, **258**, 696
- Weigert, A. 1966, *Z. Astrophys.*, **64**, 395
- Weiss, A., & Schlattl, H. 2008, *Ap&SS*, **316**, 99
- White, T. R., Huber, D., Maestro, V., et al. 2013, *MNRAS*, **433**, 1262
- Yu, J., Huber, D., Bedding, T. R., et al. 2018, *ApJS*, **236**, 42

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Appendix A: Description of evolutionary codes

A.1. ASTEC

The “Aarhus STellar Evolution Code” (Christensen-Dalsgaard 2008) uses an integrated treatment of the solution of the structure and chemical evolution, with time-centred differences for the dominant evolution of the hydrogen abundance, allowing fairly large time steps at adequate numerical precision. Low-temperature opacities are obtained from the Ferguson et al. (2005) tables, with a gradual transition to the interior opacities around 10^4 K. Opacity interpolation in density and temperature uses bi-rational splines (Späth 1991), while interpolation in X and Z uses the uni-variate scheme of Akima (1991). Electron screening is treated using the Salpeter (1954) formulation. Apart from the obvious inclusion in hydrogen burning, neutrino energy losses are not taken into account. In the calculation of nuclear reactions ^3He is taken to be always in nuclear equilibrium. All initial ^{12}C is assumed to be converted into ^{14}N in the pre-main-sequence phase, while the gradual conversion of ^{16}O into ^{14}N is taken into account. The effects of nuclear burning on the overall heavy element abundance (as used in the equation of state and opacity) are not taken into account.

A.2. BaSTI

The stellar evolution code considered for the present analysis is a slightly updated version of the one used for constructing the BaSTI stellar models database (Pietrinferni et al. 2004, 2006, 2009, 2013), which is now capable of storing stellar structure models in the fgong file format at any requested point during the evolution and computes the asymptotic period spacing on the fly during calculations. Concerning the input physics, the BaSTI code treats electron screening according to the prescriptions given by Graboske et al. (1973) and uses the Ferguson et al. (2005) radiative opacities for temperatures below 10^4 K. The energy losses driven by neutrinos are accounted for using the prescriptions by Haft et al. (1994) for the case of plasma-neutrino processes that are the dominant mechanism for neutrino emission in the cores of RGB stars; for the other mechanisms we rely on the recipes provided by Itoh et al. (1996). This code explicitly follows the evolution with time of the abundance of the following isotopes involved in the H-burning process: ^1H , ^2H , ^3He , ^4He , ^7Li , ^7Be , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{17}O .

A.3. CESAM2k

The Cesam2k stellar evolution code (standing for “Code d’Evolution Stellaire Adaptatif et Modulaire”, 2000 version) has been described in Morel & Lebreton (2008), but see also Morel (1997) for the first version and Marques et al. (2013) for the recent version including the effects of rotation. The quasi-static equilibrium of a star is solved by means of a collocation method based on piece-wise polynomial approximations projected on a B-spline basis. This allows the production of the solution everywhere, not only at grid points, and also for the discontinuous variables. For the present models, the nuclear reaction network includes the reactions from the p–p chain and CNO cycle for H-burning where the abundances of ^1H , ^3He , ^4He , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{17}O are followed in detail. In the convection zones mixing and evolution of chemicals are simultaneous. Energy loss due to neutrinos is accounted for following Haft et al. (1994) for plasma neutrinos and Weigert (1966) for photon neutrinos. Weak

screening in nuclear reactions rates is accounted for following Salpeter (1961).

A.4. GARSTEC

The “GARChing STellar Evolution Code” was used for this project in a version very close to that described in Weiss & Schlattl (2008). The main significant difference is the update of electron screening of nuclear reactions now covering the intermediate regime as well, following Dewitt et al. (1973) and Graboske et al. (1973). Of the different physics options described in Weiss & Schlattl (2008) we treat convective mixing as an instantaneous process. The low-temperature opacities are from Ferguson et al. (2005), while the transition and inclusion of conductive opacities is again as described in Weiss & Schlattl (2008). The nuclear network contains for H-burning the following isotopes: ^1H , ^3He , ^4He , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{17}O .

A.5. LPCODE

The “La Plata stellar evolution Code” used for this work is an updated version of the one reported in Althaus et al. (2003) and Miller Bertolami (2016) that stores complete models including the stellar atmosphere. Radiative opacities at low temperatures are from Ferguson et al. (2005) and a smooth transition to the atomic OPAL opacities is carried out between 10^4 and 1.25×10^4 K. Plasma-neutrino processes are taken from Haft et al. (1994) and other processes are from Itoh et al. (1996). Electron screening of nuclear reactions covers both the weak intermediate and strong regimes, following Graboske et al. (1973) and Wallace et al. (1982). Convective mixing is always treated as a diffusive process, with the diffusion coefficient $D_c = v_c l / 3$, where v_c and l are the local convective velocity and mixing length respectively, obtained from the MLT. In convective regions, mixing and nuclear burning are always treated simultaneously, as described in Althaus et al. (2003). The version of LPCODE used in the present work includes a detailed nuclear reaction network involving 32 species (including neutrons n and the aluminium isomer $^{26\text{m}}\text{Al}$) and 96 reactions for the pp chains, the CNO tri-cycle, the hot CNO cycle, the 3α and advanced α capture reactions, together with the most relevant neutron capture reactions. The included species are n , ^1H , ^2H , ^3He , ^4He , ^7Li , ^7Be , ^{12}C , ^{13}C , ^{14}C , ^{13}N , ^{14}N , ^{15}N , ^{16}O , ^{17}O , ^{18}O , ^{19}F , ^{20}Ne , ^{21}Ne , ^{22}Ne , ^{23}Na , ^{24}Mg , ^{25}Mg , ^{26}Mg , ^{26}Al , $^{26\text{m}}\text{Al}$, ^{27}Al , ^{28}Si , ^{29}Si , ^{30}Si , ^{31}P , and ^{32}P .

A.6. MESA

We used version 6950 of “Modules for Experiments in Stellar Astrophysics” (Paxton et al. 2011, 2013). In addition to the physics described in Sect. 2, we used the ‘extended’ option for electron screening, which combines Graboske et al. (1973) in the weak regime and Alastuey & Jancovici (1978) with plasma parameters from Itoh et al. (1979) in the strong regime. We used the low-temperature opacities from Ferguson et al. (2005), and calculations of energy loss from neutrinos are following the prescription of Itoh et al. (1996). The included species are ^1H , ^2H , ^3He , ^4He , ^7Li , ^7Be , ^8B , ^{12}C , ^{13}C , ^{13}N , ^{14}N , ^{15}N , ^{14}O , ^{15}O , ^{16}O , ^{17}O , ^{18}O , ^{18}F , ^{19}F , ^{18}Ne , ^{19}Ne , ^{20}Ne , ^{22}Ne , ^{22}Mg , and ^{24}Mg . The `inlists` used for this project are available at the workshop website.

A.7. MONSTAR

We have implemented minor modifications to the Monash version of the Mt. Stromlo evolution code as reported in [Constantino et al. \(2015\)](#). Supplementary to the agreed upon input physics, stellar model calculations include the effects of weak screening ([Dewitt et al. 1973](#)). We consider the usual neutrino losses through nuclear reactions, as well as those by pair-neutrino processes, photo-neutrino processes and plasma neutrino processes ([Beaudet et al. 1967](#)), whilst bremsstrahlung rates are from [Festa & Ruderman \(1969\)](#). Corrections due to neutral currents are applied according to [Ramadurai \(1976, for pair, plasma, and photo-neutrino processes\)](#) and [Dicus et al. \(1976, for bremsstrahlung\)](#) which impact the location of the off-centre core flash. The Aesopus low-temperature opacities ([Marigo & Aringer 2009](#)) are utilised below temperatures of 10 000 K. When computing EOS quantities and opacities near table boundaries we perform linear interpolation across datasets to ensure a smooth transition. If required, values are linearly extrapolated beyond table boundaries. For the models calculated during this workshop we instantaneously mix convective regions with mixing and burning decoupled. For the current exercise we employed a hydrogen-burning network that explicitly follows ^1H , ^3He , ^4He , ^{12}C , ^{15}N , and ^{16}O .

A.8. YaPSI

These models were constructed with the same version of the ‘‘Yale Rotational stellar Evolution Code’’ (YREC) used in the Yale–Potsdam Stellar Isochrones (YaPSI; see Sect. 2 of [Spada et al. 2017](#)). The basic choices of input physics coincide with those of the YaPSI project, except for the following in order to comply with the decided choices of common physics in Sect. 2: (a) the NACRE nuclear reaction rates are adopted here; (b) convective-core overshooting and microscopic diffusion are ignored; (c) the Potekhin conductive opacities have been implemented; (d) the [Grevesse et al. \(1993\)](#) solar abundance mixture is adopted. The nuclear reaction network for hydrogen burning contains the following isotopes: ^1H , ^3He , ^4He , ^7Be , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{18}O (cf. [Demarque et al. 2008](#)).

A.9. YREC

The ‘‘Yale Rotating stellar Evolution Code’’ used to generate the models is described in [Demarque et al. \(2008\)](#). In addition to the agree input physics, the YREC version used (YREC7) uses the low-temperature opacities from [Ferguson et al. \(2005\)](#) and includes the following species in the nuclear network: ^1H , ^3He , ^4He , ^7Be , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , and ^{18}O . Neutrino loss rates are taken from the monograph by [Bahcall \(1989\)](#). For advanced stages of stellar evolution, the neutrino rates from photo, pair and plasma sources reported in [Itoh et al. \(1989\)](#) are included.

Appendix B: Evolutionary tracks: effective-temperature calibrated

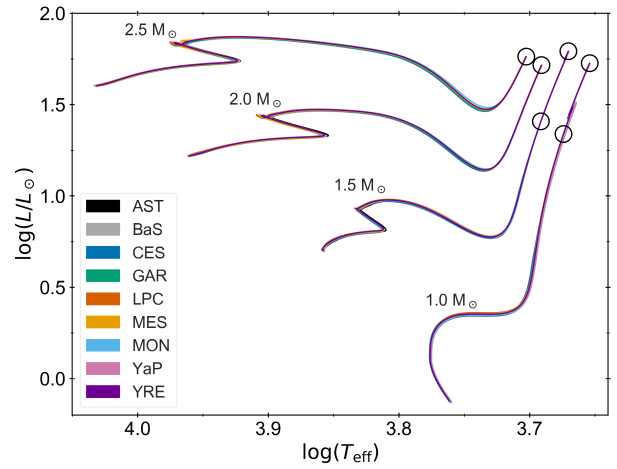


Fig. B.1. Hertzsprung–Russell diagram of effective-temperature calibrated science cases of 1.0, 1.5, 2.0 and 2.5 M_{\odot} for all participating codes. Open circles depict the position of models selected for detailed comparisons.

The comparisons presented in Sect. 4 were made at a given mass and radius using the solar-calibrated mixing-length efficiency α_{MLT} . As discussed in the main text, this leads to different T_{eff} values and luminosities at a given R , and thus to different helium core sizes due to the core mass–luminosity relation. To uncouple the differences in the models from the details of the solar calibration, we produced an additional set of models where we calibrated α_{MLT} to reproduce a certain T_{eff} value on the RGB. We chose as reference an earlier set of ASTEC models, as they generally lie in the centre of the T_{eff} range covered by all codes as shown in Sect. 5. The resulting HRD for the masses considered is shown in Fig. B.1, where we have marked the position of the selected models: 1.0 M_{\odot} and 1.5 M_{\odot} at 7 and 12 R_{\odot} , and 2.0 M_{\odot} and 2.5 M_{\odot} at 10 R_{\odot} .

The overall evolutionary properties in this science case are very similar to those obtained in the solar radius calibration models. However, their oscillation frequencies show interesting differences, which are investigated in Paper II. All models are available for the community on the website of the workshops.

Appendix C: Main properties of calibration and science cases models

The following tables contain the main properties of our models obtained from the modified solar calibration procedure (Table C.1, see Sect. 4) and the solar-calibrated set of models (Tables C.2, C.3, C.4, see Sect. 5).

Table C.1. Results of the modified solar calibration

Code	ASTEC	BaSTI	CESAM	GARSTEC	LPCODE	MESA	MONSTAR	YaPSI	YREC
α_{MLT}	2.0437	1.9982	1.9496	1.9958	2.0431	2.0736	2.0489	2.0118	2.0388
L/L_{\odot}	1.2032	1.1981	1.1913	1.1950	1.1947	1.2187	1.1864	1.1966	1.2073
T_{eff}	6053	6046	6038	6042	6042	6072	6032	6044	6058
X_c	0.2804	0.2874	0.2900	0.2903	0.2947	0.2880	0.2880	0.2909	0.2853

Table C.2. Main stellar properties of $1.0 M_{\odot}$ solar-radius calibrated models.

$1.0 M_{\odot}, 1 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_S	Y_S	Λ (10^{-3})
ASTEC	1.1192	5944	5.3077	–	0.7000	0.2800	8.5756
BaSTI	1.1062	5927	5.4013	–	0.7000	0.2800	8.6649
CESAM2k	1.1085	5930	5.2714	–	0.7000	0.2800	8.5574
GARSTEC	1.1101	5932	5.2340	–	0.7000	0.2800	8.5609
LPCODE	1.1173	5942	5.3157	–	0.7000	0.2800	8.5891
MESA	1.1249	5952	5.4707	–	0.7000	0.2800	8.4755
MONSTAR	1.1023	5922	5.2244	–	0.7000	0.2800	8.4826
YaPSI	1.1158	5940	5.1936	–	0.7000	0.2800	8.6041
YREC	1.1243	5951	5.3071	–	0.7000	0.2800	8.5394
$1.0 M_{\odot}, X_c = 10^{-5}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_S	Y_S	Λ (10^{-3})
ASTEC	1.6446	5942	8.8919	0.0380	0.7000	0.2800	7.5816
BaSTI	1.6783	5935	9.1164	0.0350	0.7000	0.2800	7.6482
CESAM2k	1.6715	5929	9.0703	0.0376	0.7000	0.2800	7.6158
GARSTEC	1.7313	5935	9.1960	0.0394	0.7000	0.2800	7.6123
LPCODE	1.7375	5947	9.2361	0.0398	0.7000	0.2800	7.6360
MESA	1.6733	5956	9.0750	0.0371	0.7000	0.2800	7.6272
MONSTAR	1.6694	5921	9.0962	0.0405	0.7000	0.2800	7.5707
YaPSI	1.7054	5936	9.0551	0.0416	0.7000	0.2800	7.6403
YREC	1.7128	5946	9.1357	0.0419	0.7000	0.2800	7.6604
$1.0 M_{\odot}, 7 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_S	Y_S	Λ (10^{-3})
ASTEC	21.829	4721	11.490	0.2149	0.6790	0.3010	7.2193
BaSTI	21.309	4693	11.692	0.2140	0.6824	0.2975	7.4837
CESAM2k	21.167	4685	11.619	0.2148	0.6861	0.2939	7.5385
GARSTEC	21.417	4699	11.613	0.2142	0.6779	0.3020	7.3139
LPCODE	21.877	4724	11.750	0.2148	0.6771	0.3029	7.4480
MESA	22.211	4742	11.651	0.2183	0.6786	0.3013	7.2222
MONSTAR	21.482	4703	11.637	0.2161	0.6965	0.2835	7.2142
YaPSI	21.548	4706	11.565	0.2191	0.6817	0.2983	7.3300
YREC	21.778	4719	11.587	0.2172	0.6816	0.2984	7.3741
$1.0 M_{\odot}, 12 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_S	Y_S	Λ (10^{-3})
ASTEC	53.315	4508	11.567	0.2564	0.6790	0.3010	7.1441
BaSTI	52.126	4482	11.776	0.2560	0.6824	0.2975	7.4326
CESAM2k	51.804	4476	11.702	0.2571	0.6861	0.2939	7.4255
GARSTEC	52.232	4485	11.692	0.2554	0.6779	0.3020	7.2736
LPCODE	53.392	4510	11.837	0.2568	0.6771	0.3029	7.4815
MESA	54.186	4526	11.725	0.2600	0.6786	0.3013	7.1583
MONSTAR	52.534	4491	11.714	0.2578	0.6799	0.3000	7.1481
YaPSI	52.651	4494	11.644	0.2620	0.6817	0.2983	7.2467
YREC	53.232	4506	11.666	0.2595	0.6816	0.2984	7.2853

Notes. The quantity $m(\text{He})$ is the mass coordinate of the helium core, defined as the point of maximum energy release in the burning shell.

Table C.3. Main stellar properties of $1.5 M_{\odot}$ solar-radius calibrated models.

$1.5 M_{\odot}, 7 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_{S}	Y_{S}	Λ (10^{-3})
ASTEC	25.618	4914	2.5925	0.1473	0.6863	0.2937	7.2613
BaSTI	25.049	4886	2.5702	0.1467	0.6882	0.2916	7.3903
CESAM2k	24.953	4882	2.5628	0.1475	0.6882	0.2917	7.2976
GARSTEC	25.106	4889	2.5903	0.1466	0.6851	0.2948	7.2978
LPCODE	25.655	4916	2.6217	0.1473	0.6848	0.2950	7.4134
MESA	26.049	4935	2.6277	0.1494	0.6856	0.2942	7.2853
MONSTAR	25.165	4893	2.6295	0.1481	0.7000	0.2800	7.2351
YaPSI	25.289	4898	2.6341	0.1506	0.6880	0.2920	7.4037
YREC	25.526	4910	2.6007	0.1486	0.6883	0.2916	7.4358
$1.5 M_{\odot}, 12 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_{S}	Y_{S}	Λ (10^{-3})
ASTEC	62.015	4681	2.6493	0.1746	0.6863	0.2937	7.1827
BaSTI	60.657	4656	2.6315	0.1741	0.6882	0.2917	7.3531
CESAM2k	60.351	4650	2.6212	0.1748	0.6882	0.2917	7.2264
GARSTEC	60.678	4656	2.6492	0.1738	0.6851	0.2948	7.2601
LPCODE	62.075	4683	2.6856	0.1749	0.6848	0.2950	7.4457
MESA	63.006	4700	2.6833	0.1770	0.6855	0.2943	7.2136
MONSTAR	61.029	4663	2.6867	0.1754	0.6925	0.2874	7.1635
YaPSI	61.188	4666	2.6918	0.1785	0.6879	0.2921	7.3127
YREC	61.807	4677	2.6585	0.1761	0.6883	0.2916	7.3455

Table C.4. Main stellar properties of $2.0 M_{\odot}$ and $2.5 M_{\odot}$ solar-radius calibrated models.

$2.0 M_{\odot}, 10 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_{S}	Y_{S}	Λ (10^{-3})
ASTEC	52.003	4907	0.9657	0.1234	0.6920	0.2880	7.2913
BaSTI	50.884	4881	0.9273	0.1230	0.6929	0.2870	7.1103
CESAM2k	50.627	4875	0.9587	0.1234	0.6921	0.2877	7.2875
GARSTEC	50.866	4880	0.9472	0.1239	0.6914	0.2884	7.1968
LPCODE	51.971	4907	0.9636	0.1234	0.6912	0.2886	7.3594
MESA	52.792	4926	0.9742	0.1257	0.6917	0.2881	7.3120
MONSTAR	51.066	4886	0.9738	0.1242	0.7000	0.2800	7.3598
YaPSI	51.295	4891	0.9690	0.1246	0.6919	0.2881	7.3454
YREC	51.965	4907	0.9658	0.1239	0.6916	0.2884	7.2701
$2.5 M_{\odot}, 10 R_{\odot}$	L/L_{\odot}	T_{eff} (K)	Age (Gyr)	$m(\text{He})$	X_{S}	Y_{S}	Λ (10^{-3})
ASTEC	58.256	5049	0.5001	0.1130	0.6972	0.2828	7.2159
BaSTI	57.061	5023	0.4826	0.1121	0.6974	0.2824	6.9519
CESAM2k	56.670	5014	0.4947	0.1122	0.6969	0.2829	7.1819
GARSTEC	56.915	5020	0.5034	0.1124	0.6968	0.2831	7.3280
LPCODE	58.174	5047	0.4996	0.1126	0.6967	0.2831	7.2982
MESA	59.095	5067	0.5026	0.1135	0.6968	0.2830	7.2484
MONSTAR	57.214	5026	0.5066	0.1135	0.7000	0.2800	7.3196
YaPSI	57.425	5031	0.5025	0.1131	0.6971	0.2829	7.2790
YREC	58.164	5047	0.5014	0.1131	0.6972	0.2828	7.2087