

Void Creation: Reculer pour mieux sauter

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Reculer pour
mieux sauter!



Montaigne

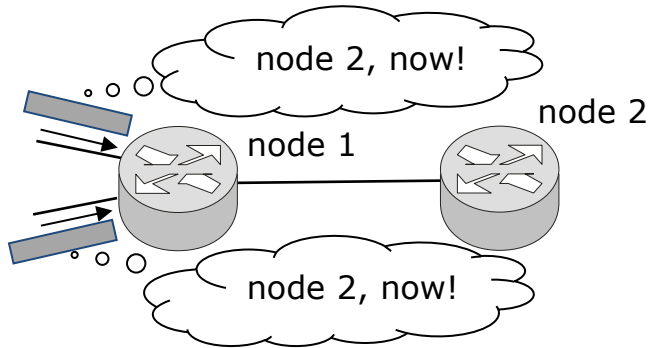
Overview presentation

- Contention resolution & scheduling basics
- Void-creating scheduling algorithm
- Theoretical void values
- Performance results
- Conclusions

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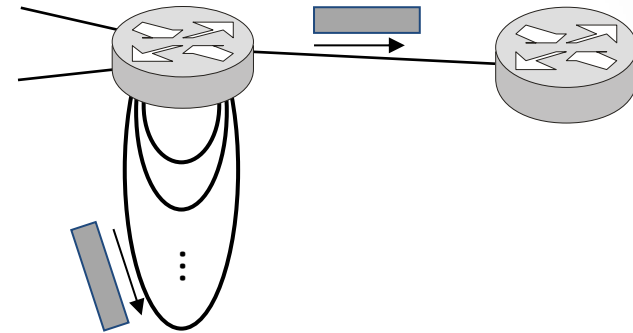
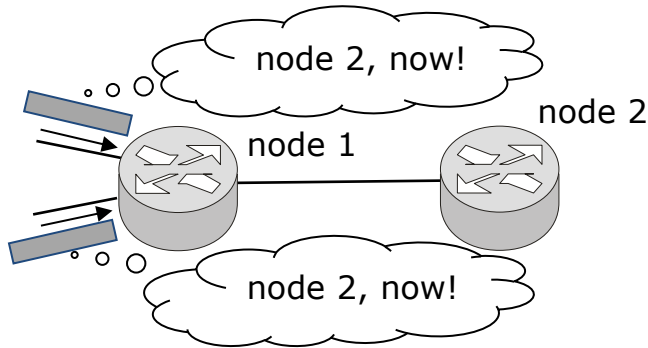
Contention & resolution



Arrival process

- single wavelength
- variable packet lengths B
- exponentially distributed interarrival times (Poisson)

Contention & resolution



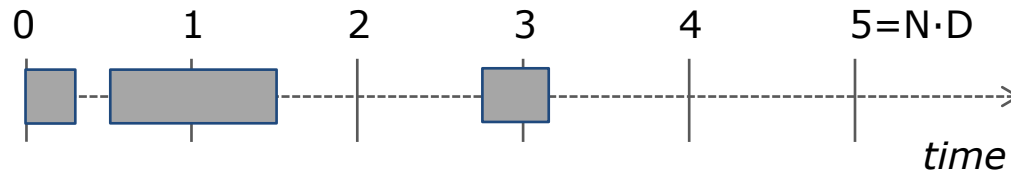
Arrival process

- single wavelength
- variable packet lengths B
- exponentially distributed interarrival times (Poisson)

Fiber Delay Lines (FDLs)

- set of fibers, $\# = N+1$
- lengths $j \cdot D, j=0 \dots N$
- $N =$ buffer size
- $D =$ granularity $= E[B]$

Provisional schedule



- shows already scheduled packets upon arrival of a packet
- horizontal axis: future time
- vertical lines: delays of FDLs ($N=5$, $D=1$)
- updated at every arrival
- choppy but uniform movement of all packets to the left

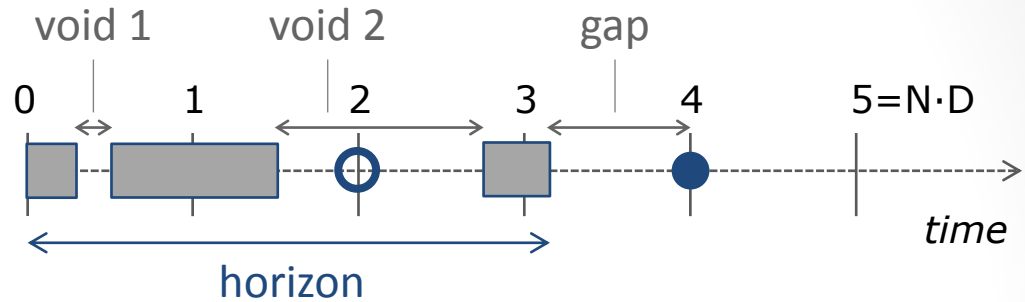
Provisional schedule

choose:

- delay line j ($j=0\dots N$)

constraint:

- no overlap



existing algorithms

non-void-filling: always first FDL after horizon: ●

- only keep track of horizon

void-filling: fill void if possible: ○ else: ●

- keep track of all voids

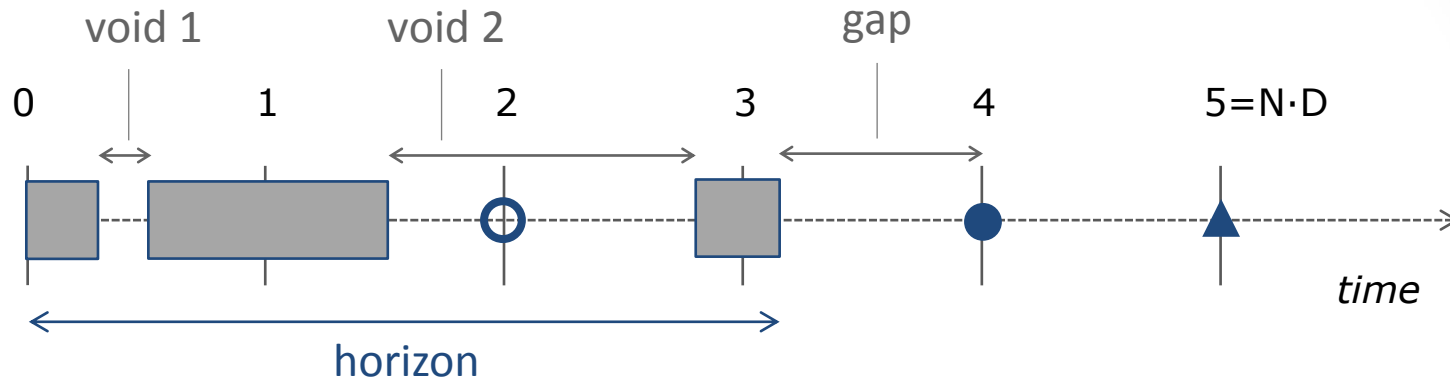
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Void-creating scheduling algorithm

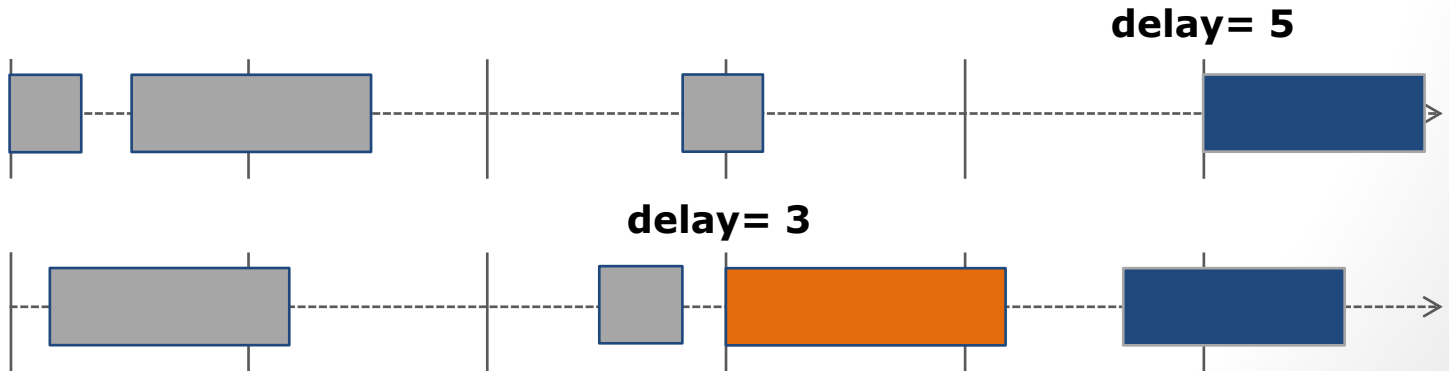
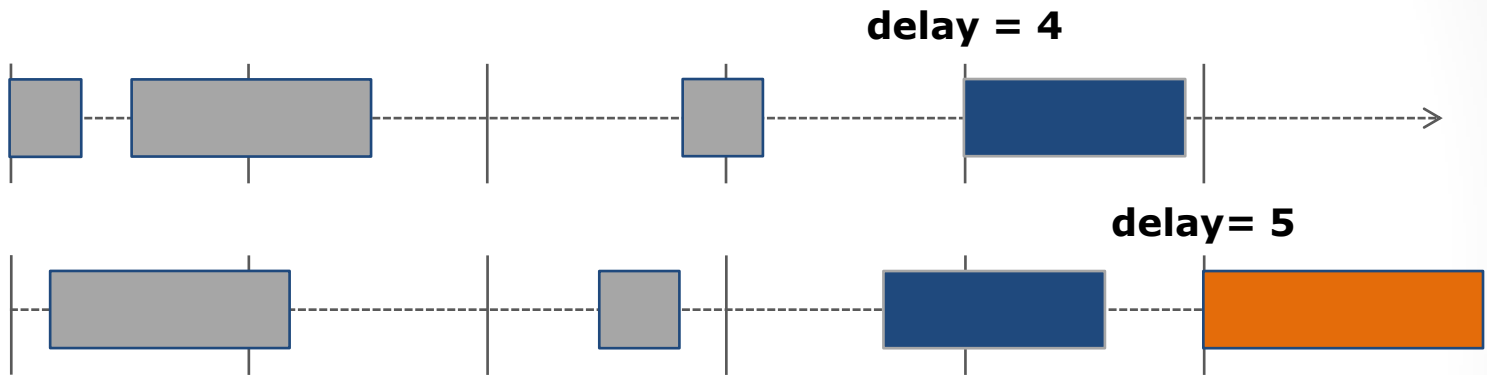
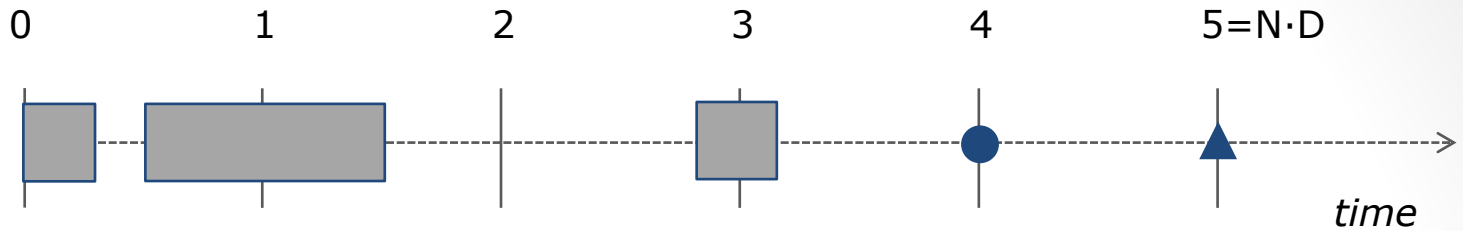


Always fill a void if possible (○ in example) else choose between:

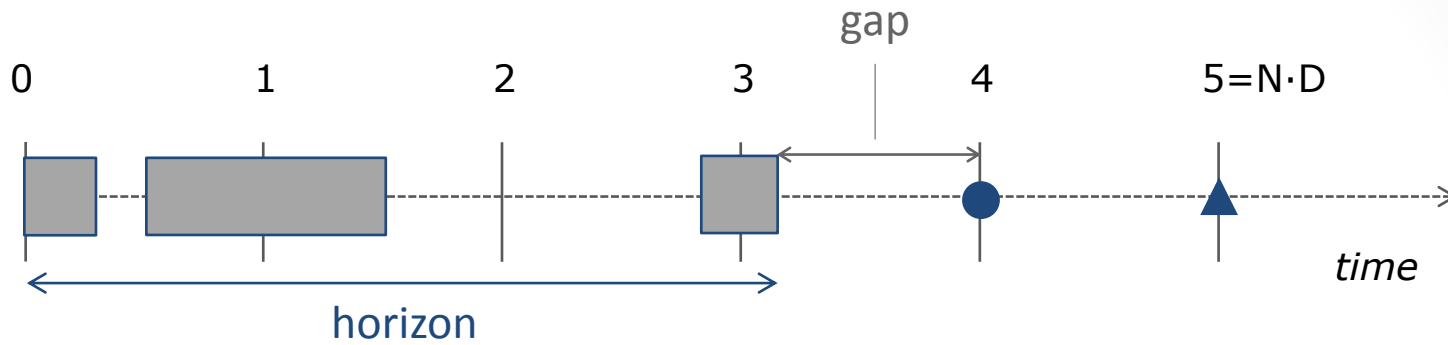
- normal scheduling point
- first FDL after horizon
- creates smaller void

- alternative scheduling point
- second FDL after horizon
- creates larger void

Why ▲ instead of ● ?



Why ▲ instead of ● ?



IF void is filled:

- average delay / packet: ↘

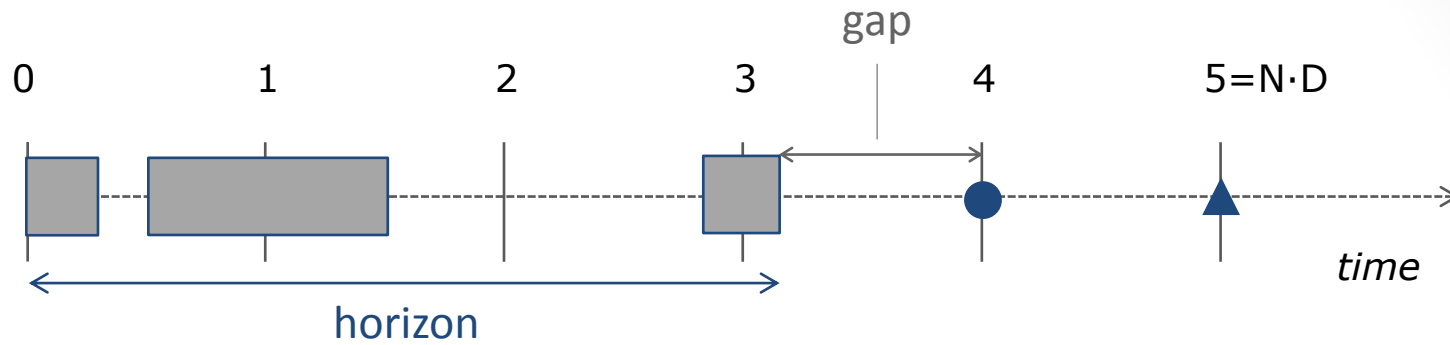


stacking becomes more dense



loss probability ↘

Why ▲ instead of ● ?



Ⓜ void is filled:

- average delay / packet: ↘



stacking becomes more dense



loss probability ↘

- position with respect to FDL has to be favorable
- depends on size arriving packet
- depends on arrival instances future packets (stochastic arrival process)
- larger voids: chance of filling ↗

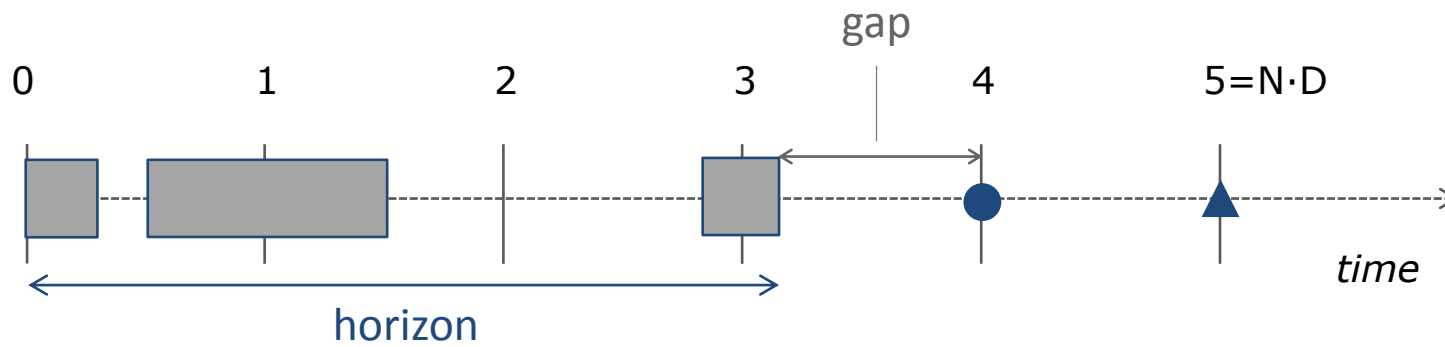
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Choosing between ▲ and ●



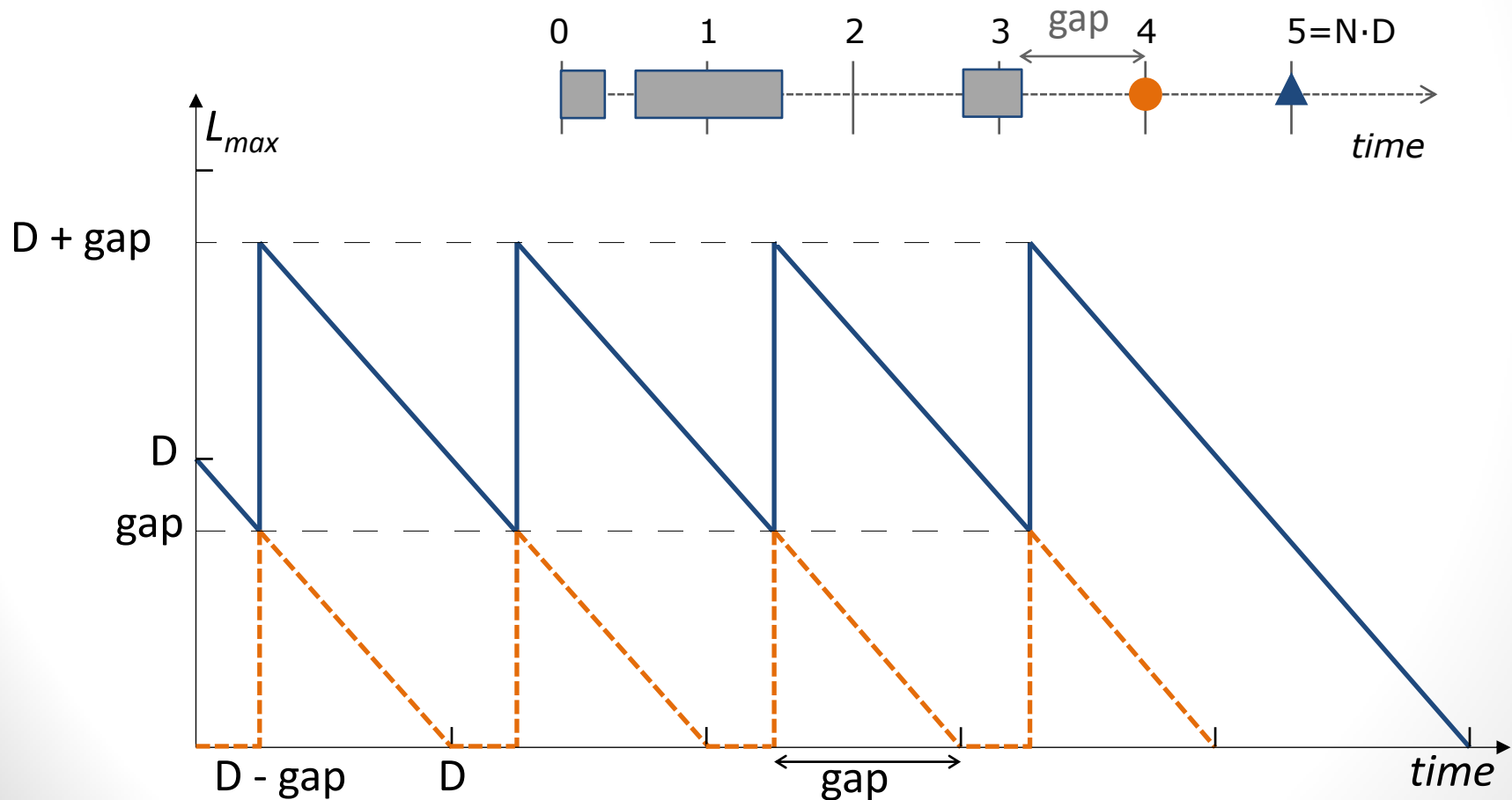
The value (=negative cost) of a void should be related to its future fillability

- Depends on:
- size of void
 - time until expiration
 - packet size distribution

Added value of ▲ over ● depends on same variables

Lifecycle of a void

shows the maximum packet size $L_{max}(t)$ that fits in the void (assuming no prior arrival already filled it)



Theoretical void values

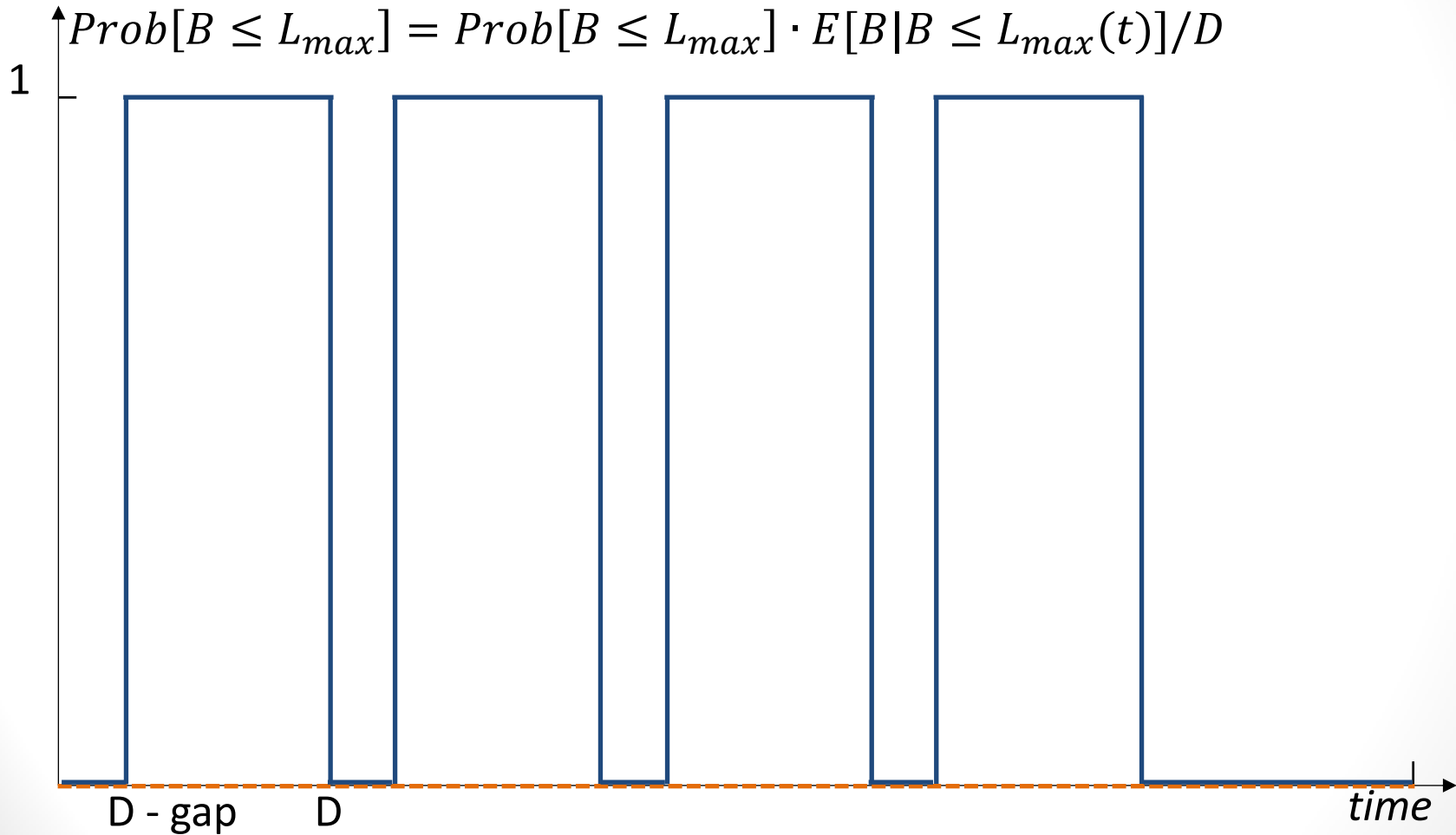
- different packet size distributions possible ($E[B]=D$)
- exponentially distributed interarrival times (Poisson process $E[T]=1/\lambda$)
- load $\rho=E[B]/E[T]$
- arrivals that fit into void are inhomogeneous Poisson process
with arrival rate $\lambda(t) = \lambda \cdot \text{Prob}[B \leq L_{\max}(t)]$
- overall expected number of packets that could fill the void during its life cycle = integrating $\lambda(t)$ over the life cycle

$$\Lambda = \int \lambda(t) dt = \frac{\rho}{D} \cdot \int_0^{\infty} \text{Prob}[B \leq L_{\max}(t)] dt$$

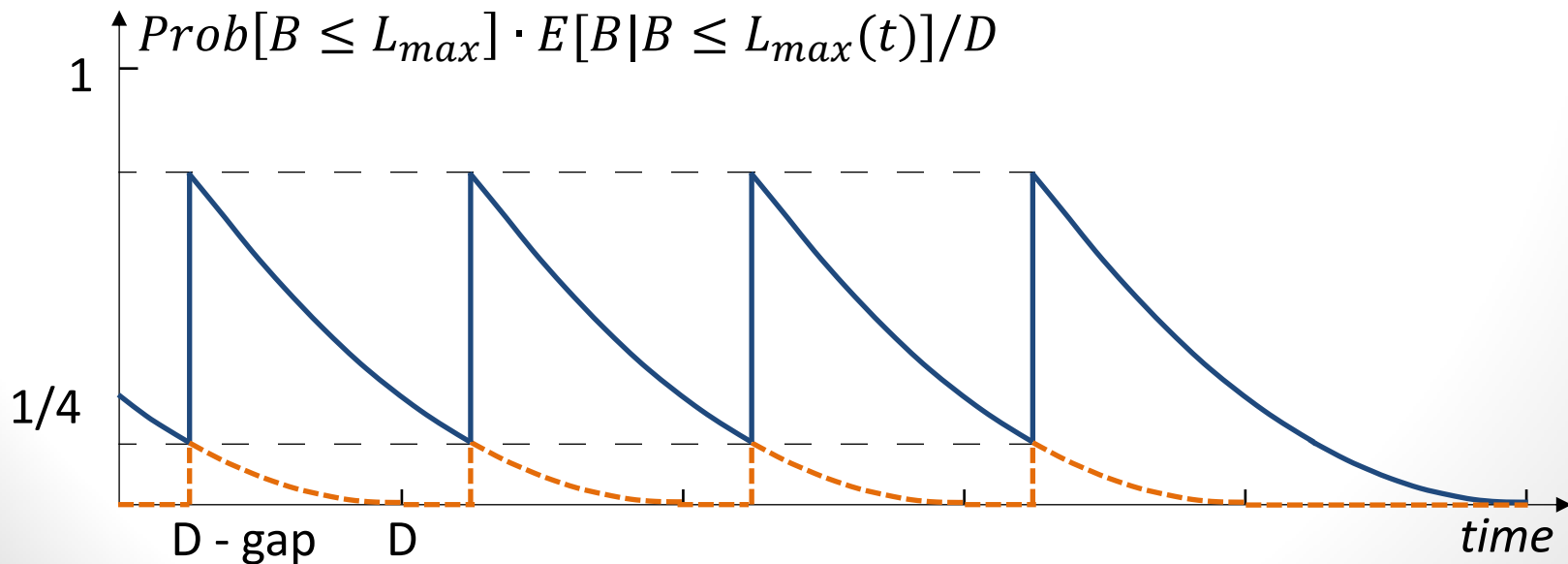
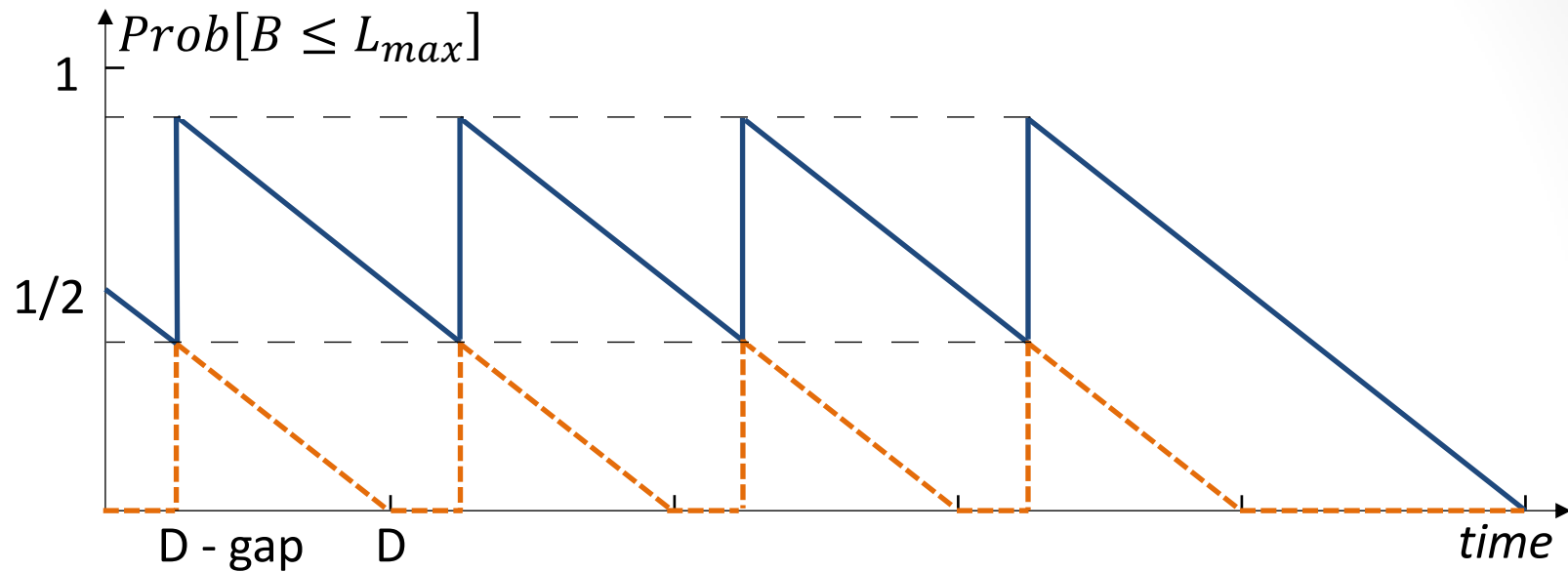
- overall normalized expected packet size of those arrivals:

$$\bar{\Lambda} = \int \bar{\lambda}(t) dt = \frac{\rho}{D} \cdot \int_0^{\infty} \text{Prob}[B \leq L_{\max}(t)] \cdot \frac{E[B|B \leq L_{\max}(t)]}{D} dt$$

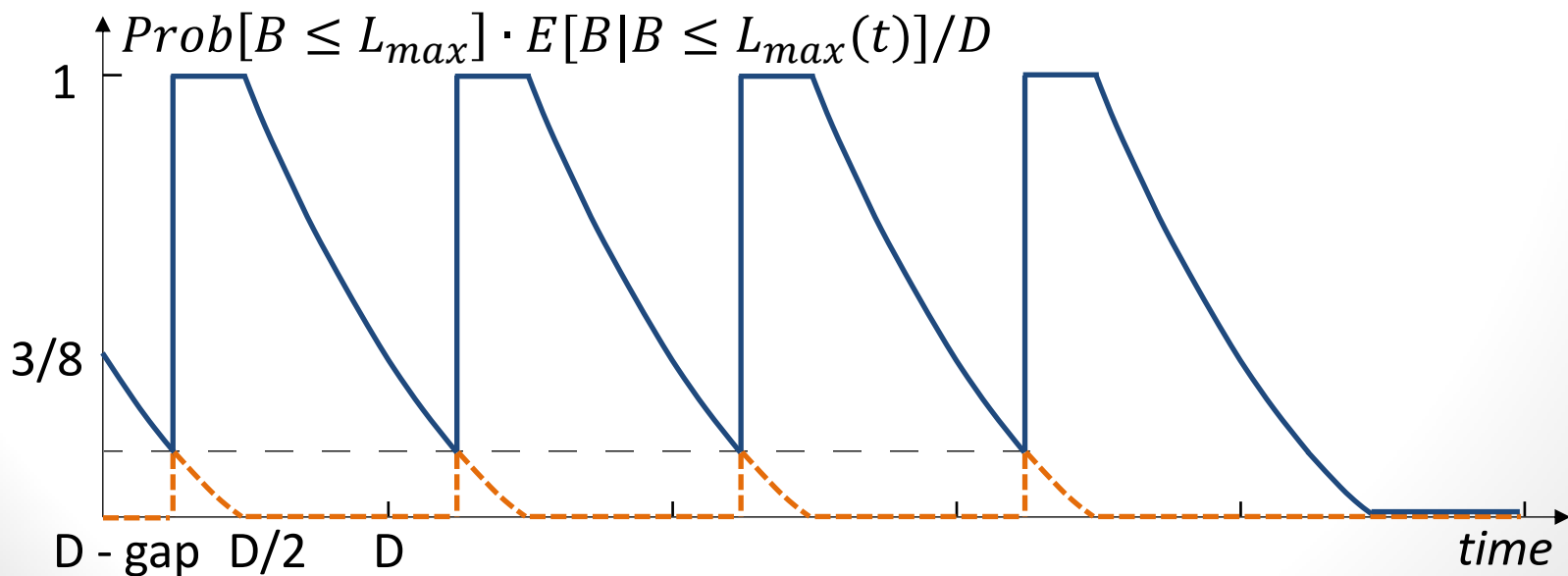
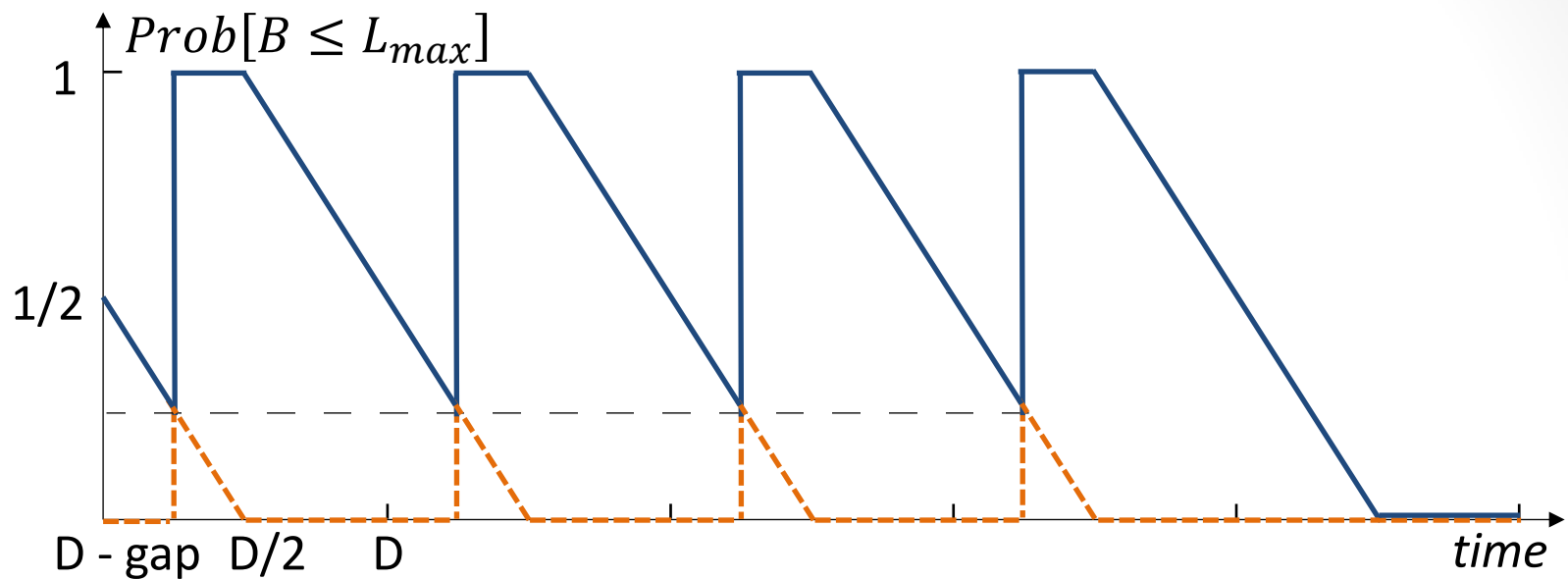
Example: fixed packet size $B=E[B]=D$



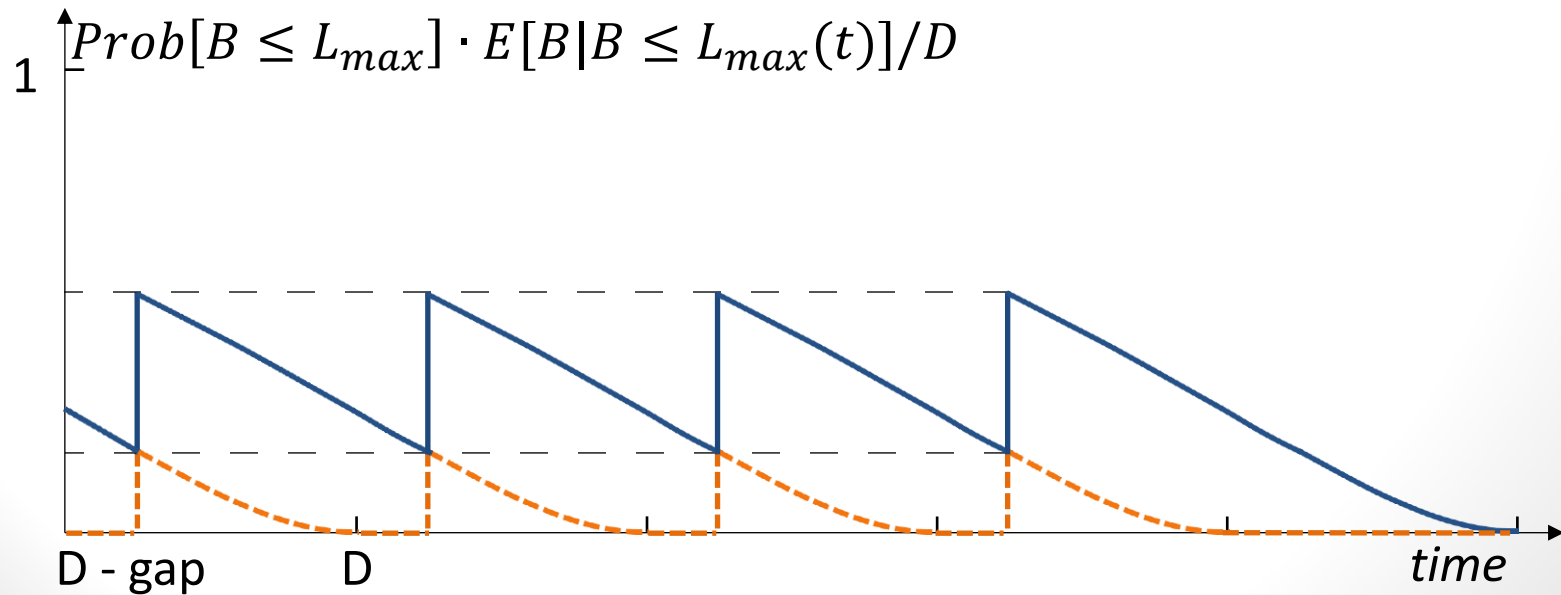
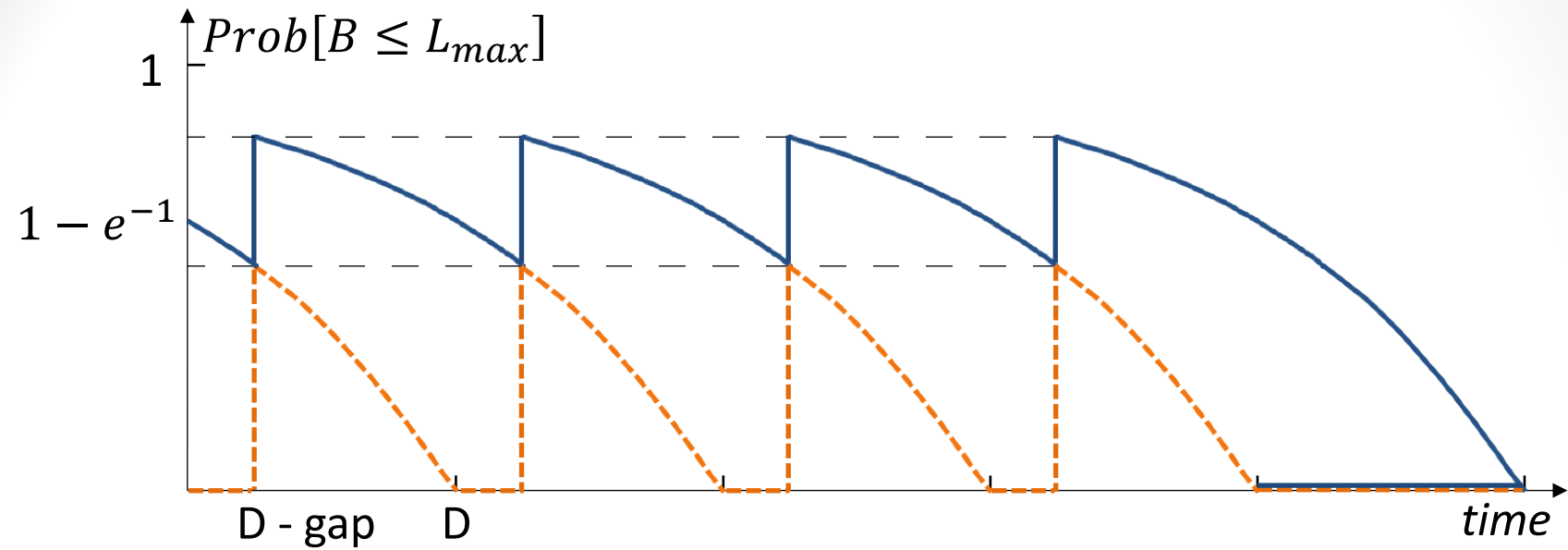
Example: uniform on $[0, 2 \cdot D]$



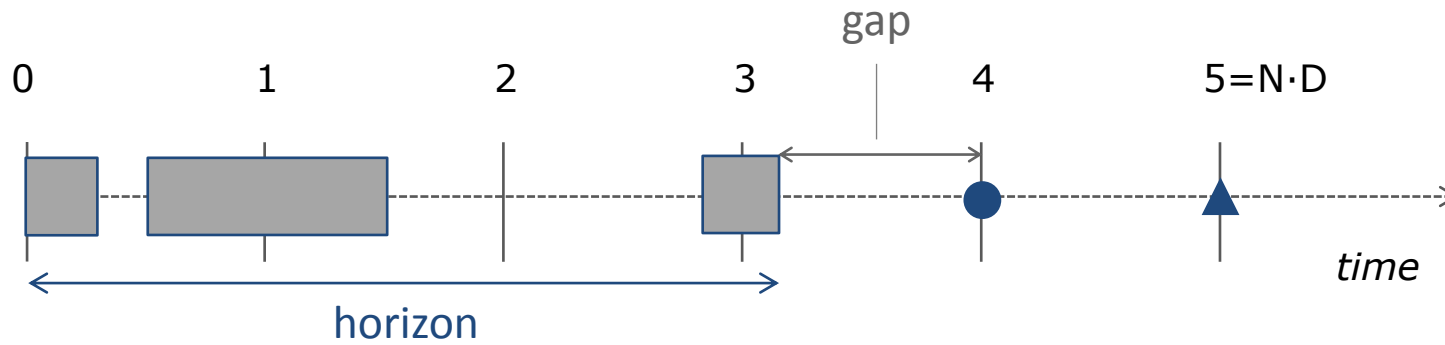
Example: uniform on $[0.5 \cdot D, 1.5 \cdot D]$



Example: exp. dist. with $E[B]=D$



Choosing between ▲ and ●



Added value of ▲ over ● = $\bar{\Lambda}(\blacktriangle) - \bar{\Lambda}(\bullet)$

The added value is related to the difference in future fillability

- Depends on:
- size of void
 - time until expiration
 - packet size distribution

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Assumptions

- **inter-arrival time packets** = exponentially distributed, $E[T]$
- **packet size distributions**: fixed, uniform $[0, 2D]$ and $[0.5D, 1.5D]$, exp. dist.
all $E[B]=D$
- **D** = granularity = 100
- **N+1** = # Fiber Delay Lines = 10
- **load** = $\rho = \frac{E[B]}{E[T]} = 80\% \text{ AND } 60\%$
- **reference algorithm**: schedule on lowest FDL possible (with void filling)
- **void-creating algorithm**:
 - fill void if possible
 - else: schedule on \blacktriangle if $\bar{\Lambda}(\blacktriangle) - \bar{\Lambda}(\bullet) \geq \text{threshold}$
 - optimize threshold

Performance improvements

maximum gain	<i>fixed</i> <i>B=D</i>		<i>uniform</i> <i>[0, 2D]</i>		<i>uniform</i> <i>[0.5D, 1.5D]</i>		<i>exp. dist.</i> <i>E[B]=D</i>	
	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$
LP	-54,1 %	-36,1 %	-5,7 %	-6,9 %	-28,7 %	-19,4 %	-4,5 %	-6,4 %
LPlength	-54,1 %	-36,1 %	-0,6 %	-1,9 %	-25,0 %	-16,5 %	-0,24 %	-0,14 %
delay	-16,3 %	-16,2 %	-1,7 %	-3,9 %	-8,2 %	-8,8 %	-0,8 %	-3,4 %

optimal threshold	<i>fixed</i> <i>B=D</i>		<i>uniform</i> <i>[0, 2D]</i>		<i>uniform</i> <i>[0.5D, 1.5D]</i>		<i>exp. dist.</i> <i>E[B]=D</i>	
	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$	$\rho=0,6$	$\rho=0,8$
LP	1,0	1,2	1,4	1,6	1,2	1,5	1,1	1,4
LPlength	1,0	1,2	1,9	2,0	1,3	1,6	2,3	3,0
delay	1,0	1,2	1,1	1,0	1,2	1,1	0,9	0,9

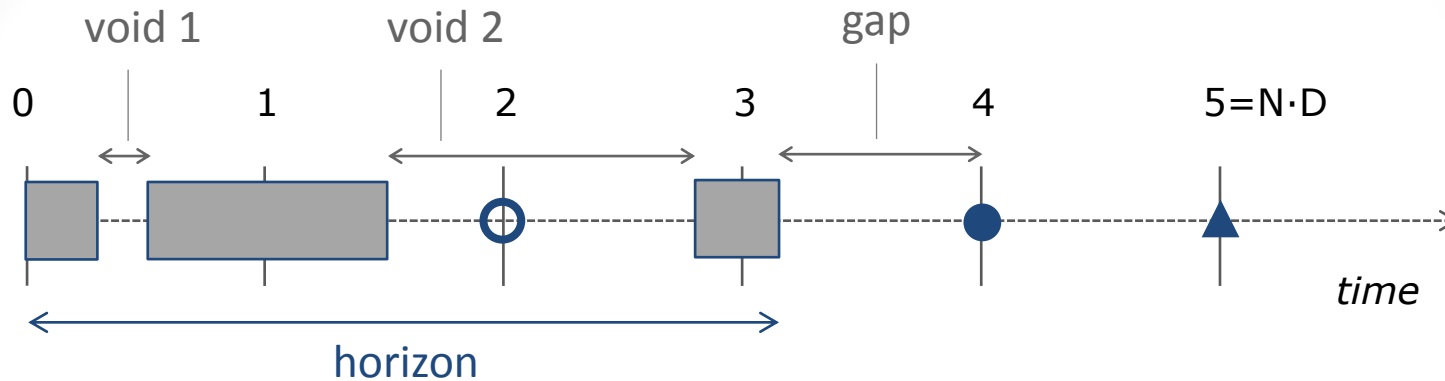
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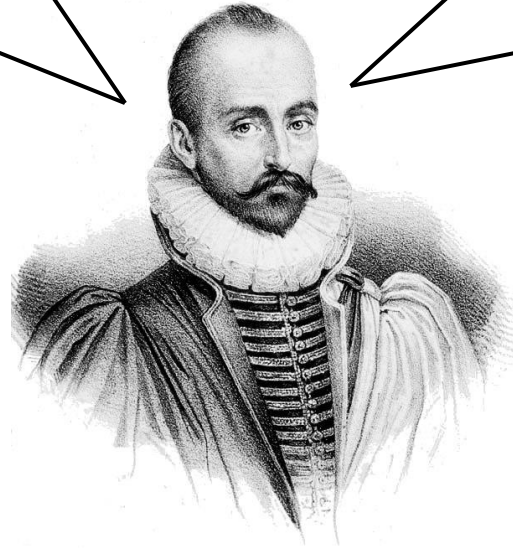
Conclusions



- current algorithms: fill void if possible (○), else ●
- **void creating** algorithms: fill void if possible (○) else ● or ▲
- ▲ : creates larger void
- speculating on **more dense stacking** ⇒ loss probability and delay ↘
- choose between ● and ▲ based on added value $\bar{\Lambda}(\blacktriangle) - \bar{\Lambda}(\bullet) \geq \text{threshold}$
- **performance improvements** up to 54 % LP reduction
- **optimal threshold** depends on packet size distribution, load and performance measure

Reculer pour
mieux sauter!

I quote others only
to better express myself!



Montaigne

Questions

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