

Evaluation of bootstrap procedures for fMRI data

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Problem

- ◇ Bootstrap procedures for fMRI time series have become popular: e.g. thresholding, ...
- ◇ Friman and Westin (2005)[1]: in *blocked* designs GLM-based **pre-whitening** better than Fourier or Wavelet decomposition
- ◇ fMRI data is both spatially and temporally complex
- ◇ **whitening**: **parametric** noise model ↔ **blocked**: **model-free** noise model [2]
- ◇ Smoothing heavily affects the data: should it occur before or after bootstrapping?

Goals

- ◇ Account for data complexity while bootstrapping
- ◇ Focus on spatial and temporal **reconstructability** of the original volume
- ◇ **Comparison** of blocked bootstrap (BR), pre-whitening bootstrap (W) and combination of both [3] (BW) as bootstrap procedures for the resampling of GLM-residuals

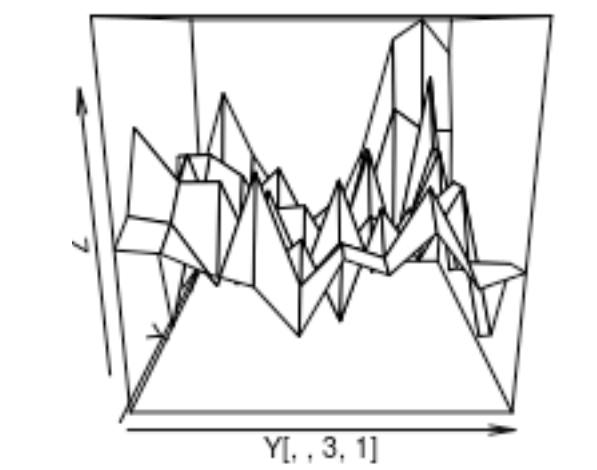
Resampling GLM-residuals

- ◇ fMRI data analysed typically using $Y_{it} = X_{it}\beta + \epsilon_{it}$ with $\epsilon_i \sim N(0, \mathbf{V}\sigma^2)$ for each voxel i and time point t
- ◇ In SPM8: $\mathbf{W}\mathbf{W}' = \mathbf{I}$ with \mathbf{W} is estimated as *quasiAR*(1) structure
- ◇ $e_{white} = \mathbf{W}e_{raw} = \mathbf{W}\mathbf{y}_i - \mathbf{W}\mathbf{x}_i\hat{\beta}$ assumed to be uncorrelated BUT $E(e_{white}) \neq 0$
- ◇ *Whitening* bootstrap uses e_{white} and *blocked* bootstrap uses e_{raw}
- ◇ we use **centered studentized**[3] residuals for e_{white} and for e_{raw} : scaled by $(\sqrt{1 - h_{ii}})^{-1}$: h_{ii} diagonal element of $\mathbf{W}\mathbf{X}(\mathbf{W}\mathbf{X}'\mathbf{W}\mathbf{X})^{-1}\mathbf{W}\mathbf{X}'$
- ◇ 3 scenarios: Independent resampling e_{white} (IW), blocked resampling e_{raw} (BR) and blocked resampling e_{white} (BW) with spatial composition retained over bootstrap sequence by individual resampling over all voxels

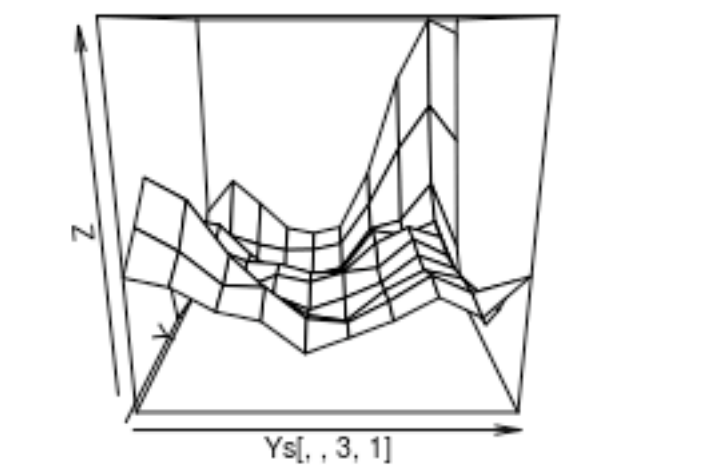
Smoothing

- ◇ Typical isotropic Gaussian 6mm kernel
- ◇ Impact on signal *itself* and noise model
- ◇ 3 scenarios: (B) Before bootstrap, (A) after bootstrap or (BA) both?

ORIGINAL



SMOOTHED

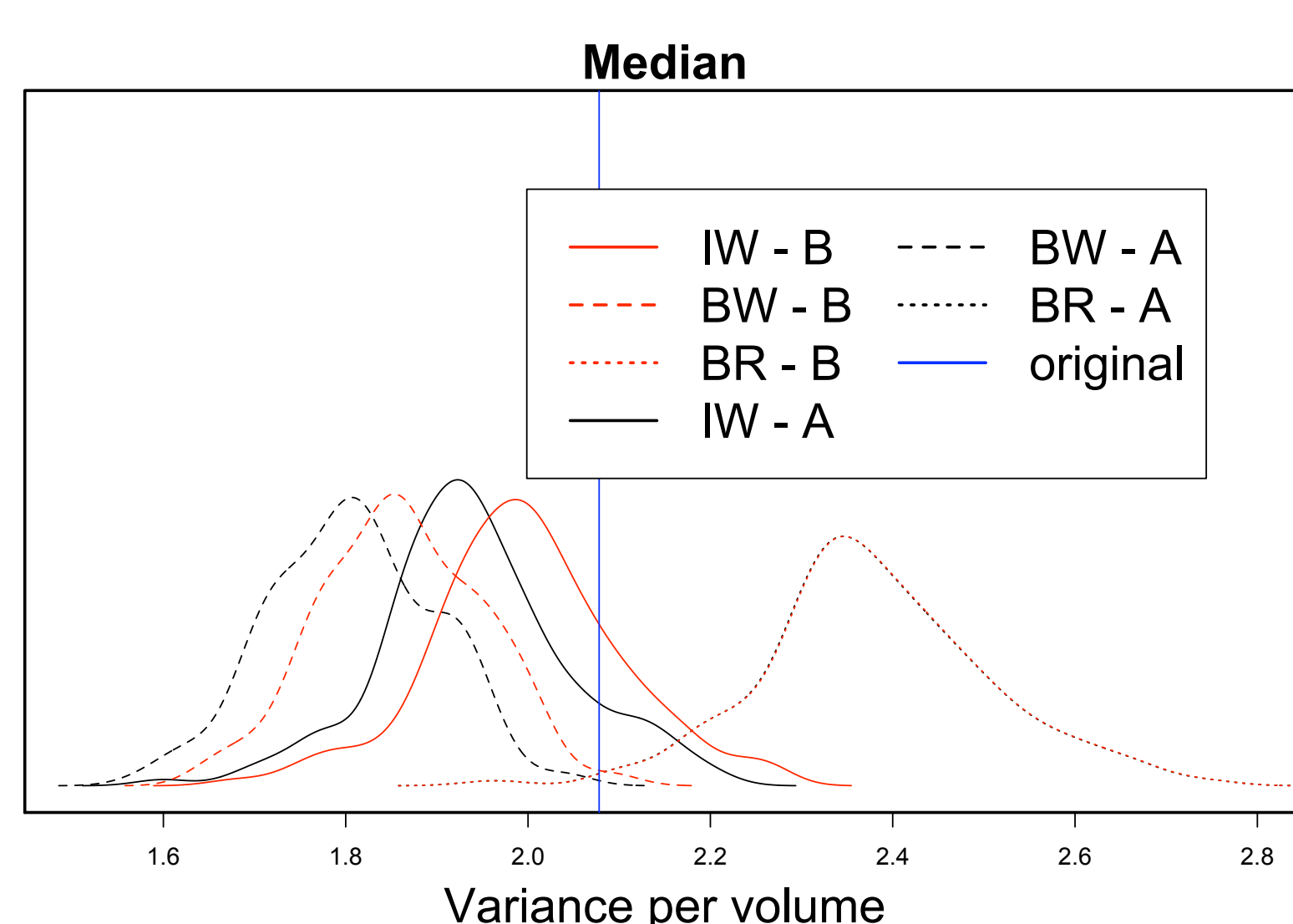


Exploration on the SPM auditory dataset[4]

- ◇ Comparison of spatial and temporal properties of the 150 bootstrap samples versus properties of the original data
- ◇ We evaluate raw residuals: $e_{raw} = \mathbf{K}\mathbf{y}_i - \mathbf{K}\mathbf{x}_i\hat{\beta}$, with \mathbf{K} = standard 128 s cut-off high-pass filter to compare the bootstrapped volumes with the original volume
- ◇ For both BW and BR bootstrap scheme blocks of 7 observation were used ("optimal" block length)

Spatial reconstructability

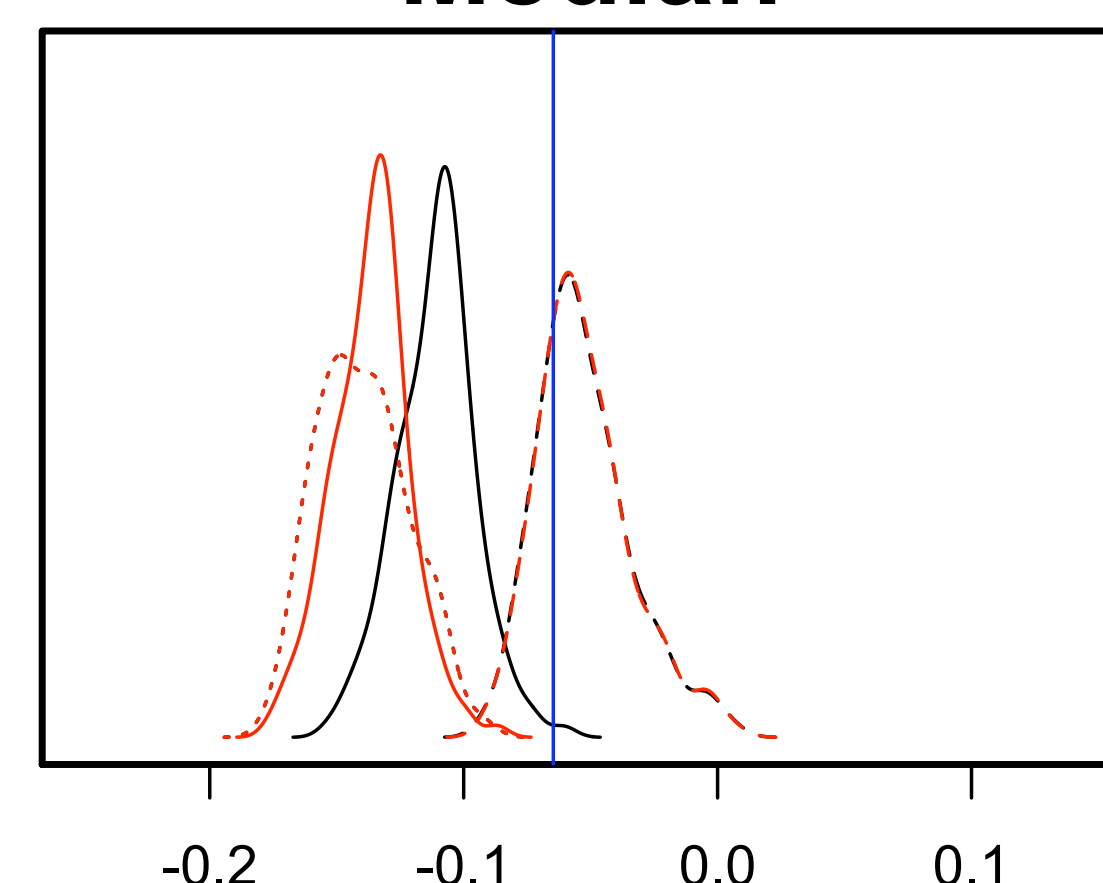
- ◇ BA smoothing, bootstrap samples are too smooth (up to twice as smooth) Smoothness is preserved well in both B and A
- ◇ Spatial variability has no clear pattern



Temporal reconstructability

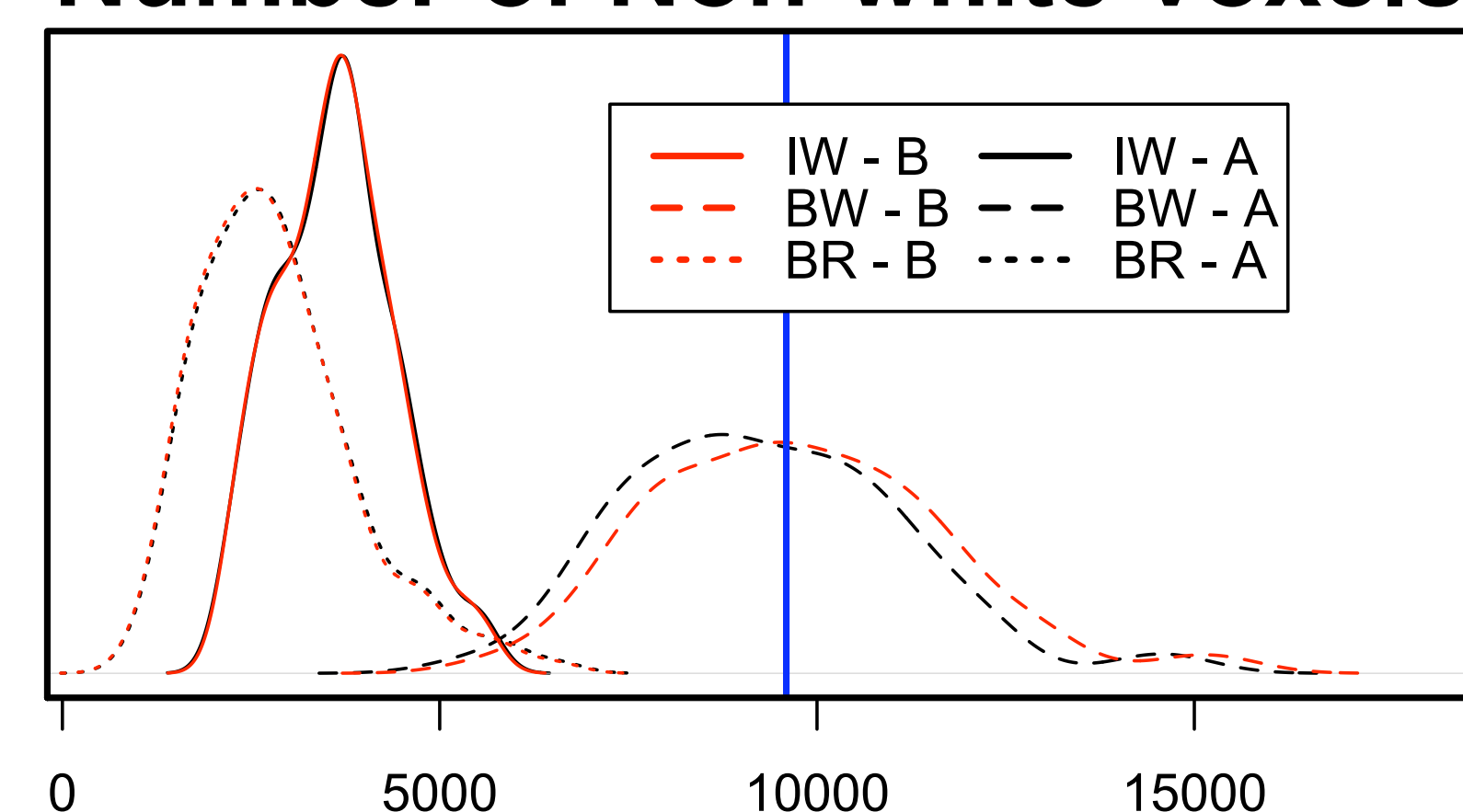
- ◇ Result of BA smoothing are omitted due to too little variation
- ◇ Durbin Watson test statistic is based on the whitened residuals of the bootstrapped volumes

Median



Correlation Residuals

Number of Non-white voxels



Durbin Watson test

- ◇ The BR bootstrap induced a higher degree of variability in the raw residuals compared to the other bootstrap schemes

Conclusions

- ◇ **Smoothing locus** Small differences B or A, but BA is too smooth
- ◇ **Bootstrap scheme** BW preserves the temporal correlation in the residuals
- ◇ Spatial variability needs further exploration
- ◇ **Confirmation needed** from other datasets and from simulation studies

Remarks

- ◇ Auditory dataset is an old dataset with long TR
- ◇ Limited amount of smoothing (6 mm)
- ◇ No impact of block length investigated yet

References

- [1] Friman, O., & Westin, C-F (2005). *Resampling fMRI time serie*, NeuroImage, 25, 859-867.
- [2] Lahiri, S.N. (2003). *Resampling methods for dependent data*, Springer.
- [3] Davison, A.C & Hinkley, D.V. (1997). *Bootstrap Methods and their Applications*, Cambridge University Press.
- [4] Friston, Karl et al. (2007). *Statistical Parametric Mapping: The Analysis of Functional Brain Images*, Elsevier Ltd./Academic Press