

## Research Article

# A Novel Quantize-and-Forward Cooperative System: Channel Estimation and M-PSK Detection Performance

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A method to improve the reliability of data transmission between two terminals without using multiple antennas is cooperative communication, where spatial diversity is introduced by the presence of a relay terminal. The Quantize and Forward (QF) protocol is suitable to implement in resource constraint relays, because of its low complexity. In prior studies of the QF protocol, all channel parameters are assumed to be perfectly known at the destination, while in reality these need to be estimated. This paper proposes a novel quantization scheme, in which the relay compensates for the rotation caused by the source-relay channel, before quantizing the phase of the received M-PSK data symbols. In doing so, channel estimation at the destination is greatly simplified, without significantly increasing the complexity of the relay terminals. Further, the destination applies the expectation maximization (EM) algorithm to improve the estimates of the source-destination and relay-destination channels. The resulting performance is shown to be close to that of a system with known channel parameters.

## 1. Introduction

As wireless communication networks become more widespread, new methods are being developed to increase the reliability of information transfer. In a multipath propagation environment, the reflected signals can combine both constructively or destructively at the receiving antenna, giving rise to Rayleigh fading. This imposes an upper bound on the reliability of a point-to-point communication system. One way to overcome this problem is by the use of multi-element sending or receiving antennas [1]. However, due to size constraints of mobile terminals, this technique cannot always be applied.

In a cooperative communication system, this problem is overcome by exploiting the broadcast nature of wireless communication. Information broadcast by the source is also received by terminals other than the destination. These terminals relay to the destination the information sent by the source, creating additional independent channels between source and destination. This technique is analyzed from an information theoretic point of view in [2], where upper and lower bounds are obtained for the capacity of the relay

channel. In [3], it is shown that in a fading environment, the spatial diversity introduced by the relay terminals improves the reliability of a communication system, which is now determined by the probability that all channels are simultaneously in fading. By increasing the reliability of the communication system, higher data rates can be achieved without increasing the transmitter power. Alternatively, one can keep the data rate constant and lower the transmission energy, extending the battery life of portable devices.

The diversity gain of various cooperative strategies is discussed in [4]. It is shown that the Amplify and Forward (AF) protocol, in which the relay amplifies the received signal, indeed introduces spatial diversity. However, when using half-duplex terminals that cannot transmit and receive data at the same time, the relay needs to store the received information, in order to forward it later on. This situation is depicted in Figure 1. The AF protocol assumes this data can be stored with an infinite precision. In a more realistic system, this data is quantized before storage, yielding the Quantize and Forward (QF) protocol. In [5], upper and lower bounds on the capacity of the relay channel are obtained for a relay that quantizes the received data using a

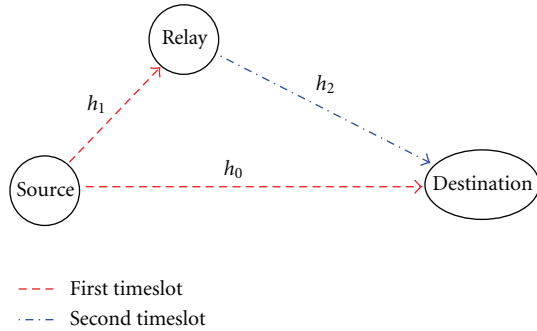


FIGURE 1: A relay channel consisting of half-duplex devices.

Wyner-Ziv coding scheme. Other quantization methods have been analyzed in [6, 7]. The QF protocol described in [6] is attractive for the use in wireless sensor networks, because the complexity of the individual relay terminals is kept low. This is done by moving the more computational intensive tasks to the destination, where typically there is more processing power available.

While cooperative communication has been well investigated from an information theoretic point of view, other aspects also need to be studied in the development of a practical implementation. The issue of channel coding is addressed in [8], where low density parity check (LDPC) codes are designed for the Decode and Forward (DF) protocol. Channel parameter estimation is discussed in [9] for the AF protocol, where pilot-based estimates are calculated for the different channel coefficients involved. Because only the received pilot symbols are used in [9], the obtained estimates could be further refined by also using the information about the channels that is embedded in the received data symbols. This technique is applied for the DF protocol in [10], where a code-aided estimation method is used to obtain very accurate channel estimates. The DF protocol however requires the relay to partially decode the received symbols, significantly increasing the computational complexity and making the system less suitable for sensor networks.

This contribution addresses the issue of channel parameter estimation in QF, keeping in mind the resource constraints at the relay. Because of its low complexity relaying strategy, the QF protocol described in [6] is used as a starting point. In [6], the relay quantizes the phase of the received M-PSK modulated signal without knowing the state of the source-relay channel. The destination is assumed to know all the channel coefficients when decoding the received symbols. It is shown that uniform quantization of the phase with  $\log_2 M + 1$  bits is sufficient to closely approach the performance of a pure AF system. When the channel parameters are considered to be unknown, they need to be estimated at the destination, before the received symbols can be decoded. However, because the destination is not connected to the source-relay channel, obtaining an accurate estimate of this channel is very difficult. This problem is solved by introducing a novel quantization scheme, which greatly facilitates channel parameter estimation, without

introducing a significant increase in computational complexity at the relay.

In the proposed quantization scheme, the relay first makes a coarse estimate of the source-relay channel based on pilot symbols received from the source. This estimate is used to compensate for the channel rotation of this channel, before quantizing the received signal. As will be shown, the proposed protocol requires only  $\log_2 M$  bits for the quantization of each symbol to achieve a performance similar to that of a pure AF system. The issue of channel parameter estimation for the proposed QF protocol has been touched in [11], where estimates are obtained for the source-destination and relay-destination channel coefficients. All noise variances are assumed to be known to the destination. This contribution, besides providing additional results and insights, also deals with the estimation of the different noise variances.

At the destination, initial estimates of the source-destination and relay-destination channel coefficients and noise variances are obtained from the received pilot symbols. These initial estimates are then refined using the expectation maximization (EM) algorithm [12], which is an iterative algorithm that also uses the information embedded in the received data symbols when calculating a new estimate of the channel parameters involved. It is shown that using the proposed algorithms, the performance of the system with estimated channel parameters can be made to be very close to that of a system with known parameters. In an attempt to reduce the computational complexity of the EM algorithm, an approximation is discussed that yields only a minor loss in error performance.

## 2. System Model

At the source, blocks of  $K$  information bits are encoded into blocks of  $N$  coded bits which are then mapped on  $K_d$  M-PSK symbols. In a first timeslot, the source transmits  $K_p$  pilot symbols along with the  $K_d$  coded data symbols, which are received by both the relay and the destination. In a second timeslot, the relay sends to the destination  $K_p$  pilot symbols followed by a quantized version of the noisy  $K_d$  coded symbols received from the source. The relay also sends to the destination an estimate of the instantaneous signal-to-noise ratio (SNR) on the source-relay channel, using  $K_y$  M-PSK coded symbols. The destination combines the signals received during both timeslots in order to detect the information bits sent by the source. The pilot symbols are used for estimating the source-destination and relay-destination channels (at the destination). The instantaneous SNR on the source-relay channel is needed at the destination for properly combining the signals received from the relay and from the source.

**2.1. Communication Channels.** The communication channels involved are modelled as independent flat Rayleigh fading channels with additive white Gaussian noise. The source-destination, source-relay and relay-destination channel coefficients are denoted  $h_0$ ,  $h_1$ , and  $h_2$ , respectively.

Considering the channel model, the output of the different channels can be written as (all vectors are denoted as row vectors.)

$$\begin{aligned} \mathbf{r}_0 &= h_0 \mathbf{c}_s + \mathbf{n}_0, \\ \mathbf{r}_1 &= h_1 \mathbf{c}_s + \mathbf{n}_1, \\ \mathbf{r}_2 &= h_2 \mathbf{c}_r + \mathbf{n}_2, \end{aligned} \quad (1)$$

with  $\mathbf{c}_s$  the symbols sent by the source, and  $\mathbf{c}_r$  the symbols sent by the relay. The channel coefficients  $h_i$  are constant during a timeslot. All channel coefficients have a zero mean circular symmetric complex gaussian (ZMCSCG) distribution with variance  $N_{h_i} = 1/d_i^n$ , with  $d_i$  the distance between the two terminals involved ( $i = 1, 2, 3$ ) and  $n$  the path loss exponent. The elements of the vector  $\mathbf{n}_i$  are also ZMCSCG distributed with variance  $N_i$  ( $i = 1, 2, 3$ ).

Both source and relay use the same amount of energy for the transmission of a frame consisting of  $K$  information bits. This energy equals  $KE_b$ , with  $E_b$  the energy needed to transmit one information bit. The latter is proportional to the energy of the symbols sent by the source and relay, denoted  $E_s$  and  $E_r$ , respectively. Taking into account the transmission of pilot symbols and the instantaneous SNR on the source-relay channel,  $E_s$  and  $E_r$  can be expressed in terms of  $E_b$

$$\begin{aligned} E_s &= \frac{K_d}{(K_d + K_p)} \frac{K \log_2 M}{N} E_b, \\ E_r &= \frac{K_d}{(K_d + K_p + K_y)} \frac{K \log_2 M}{N} E_b. \end{aligned} \quad (2)$$

**2.2. Structure of the Relay Terminal.** We propose a relay that compensates for the channel rotation caused by the source-relay channel  $h_1$ , before quantizing the received signal. This compensation makes use of an estimate  $\hat{h}_1$  of this channel, based on pilot symbols transmitted by the source. The  $i$ th symbol  $c_{r,i}$  is a quantized version of the  $i$ th element  $r_{1,i}$  of  $\mathbf{r}_1$

$$c_{r,i} = e^{jq_i}, \quad (3)$$

where  $q_i$  is defined by the relationship

$$q_i = \frac{2\pi k_i}{2^Q}, \quad (4)$$

if

$$\frac{\pi}{2^Q}(2k_i - 1) < \arg(r_{1,i} \hat{h}_1^*) < \frac{\pi}{2^Q}(2k_i + 1), \quad (5)$$

with  $k \in \{0, 1, \dots, 2^Q - 1\}$  and  $Q$  the number of quantization bits. When using this quantization scheme, the destination will only be required to know the instantaneous SNR on the source-relay channel, given by  $\gamma = |h_1|^2/N_1$ , and not the exact value of  $h_1$ , as will be proven in the next subsection. This instantaneous SNR is estimated by the relay, quantized,

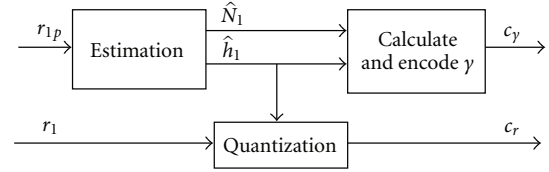


FIGURE 2: Schematic representation of the relay terminal.

encoded, mapped to M-PSK symbols, and forwarded to the destination. The resulting structure of the relay terminal is represented schematically in Figure 2.

Instead of compensating for the channel rotation caused by the source-relay channel, an estimate of this rotation could also be sent to the destination, along with the estimate of the SNR on the source-relay channel. However, the quantization of the channel rotation is more complex than the quantization of the SNR on the source-relay channel. While a coarse quantization is sufficient for the SNR, a much more refined quantization is required for the channel rotation, especially when the phase of  $h_1$  is near the edge of a quantization interval. While this could be achieved by quantizing the channel rotation using a large number of bits or by using a logarithmic quantization scheme, it would significantly increase the complexity of the relay terminal. Therefore, it is beneficial to compensate for the channel rotation caused by the source-relay channel at the relay, instead of forwarding an estimate of this rotation to the destination. Furthermore, when compensating for the source-relay channel rotation at the relay, the received information can be quantized with one bit less as opposed to when no compensation is used. This further lowers the complexity of the relay terminal.

**2.3. Signal Combining at the Destination.** For decoding purposes, the likelihoods of the received symbols must be determined by the destination. Because the source-destination and relay-destination channels are orthogonal, the likelihood of the  $i$ th received source symbol  $c_{s,i}$  equals

$$\begin{aligned} p(\mathbf{r}_{d,i} | c_{s,i}, \mathbf{h}, \mathbf{N}) \\ = p(r_{0,i} | c_{s,i}, h_0, N_0) p(r_{2,i} | c_{s,i}, h_1, h_2, N_1, N_2), \end{aligned} \quad (6)$$

with  $\mathbf{r}_{d,i} = (r_{0,i}, r_{2,i})$ ,  $\mathbf{h} = (h_0, h_1, h_2)$  and  $\mathbf{N} = (N_0, N_1, N_2)$ . The first factor from (6) can be written as

$$p(r_{0,i} | c_{s,i}, h_0, N_0) = \frac{1}{\pi N_0} e^{(-|r_{0,i} - h_0 c_{s,i}|^2)/N_0}. \quad (7)$$

The second factor from (6) can be expressed as the marginal of  $p(r_{2,i}, k_i, \hat{h}_1 | c_{s,i}, h_1, h_2, N_1, N_2)$ , with  $\hat{h}_1$  an estimate of  $h_1$  and  $k_i$  defined by (4). This yields

$$\begin{aligned} p(r_{2,i} | c_{s,i}, h_1, h_2, N_1, N_2) &= \sum_{k=0}^{2^Q-1} \int p(r_{2,i}, k_i, \hat{h}_1 | c_{s,i}, h_1, h_2, N_1, N_2) d\hat{h}_1 \\ &= \sum_{k=0}^{2^Q-1} p(r_{2,i} | k_i = k, h_2, N_2) \\ &\quad \times \int P(k_i = k | c_{s,i}, \hat{h}_1, h_1, N_1) \\ &\quad \times p(\hat{h}_1 | h_1, N_1) d\hat{h}_1. \end{aligned} \quad (8)$$

The evaluation of  $p(r_{2,i} | k_i = k, h_2, N_2)$  proceeds similarly to (7), yielding

$$p(r_{2,i} | k_i = k, h_2, N_2) = \frac{1}{\pi N_2} e^{(-|r_{2,i} - h_2 c_{r,i}|^2)/N_2}, \quad (9)$$

with  $c_{r,i}$  defined by (3). The first factor in the integrand from (8) can be calculated using the phase density function [6]

$$f_{\Theta}(\theta, \gamma) = \frac{1}{2\pi} \left[ e^{-\gamma} + \sqrt{\pi\gamma} \cos(\theta) e^{-\gamma \sin^2(\theta)} \operatorname{erfc}(-\sqrt{\gamma} \cos(\theta)) \right]. \quad (10)$$

This function describes the distribution of the received phase when a symbol with amplitude 1 and phase 0 is sent over an AWGN channel. The variable  $\gamma$  is the SNR ratio at the receiving terminal (the relay in this case). Using this function, one obtains

$$\begin{aligned} P(k_i = k | c_{s,i}, \hat{h}_1, h_1, N_1) &= \int_{\phi_k^l}^{\phi_k^u} f_{\Theta} \left( \theta - \arg(c_{s,i} h_1 \hat{h}_1^*), \frac{|h_1|^2}{N_1} \right) d\theta, \end{aligned} \quad (11)$$

where the integration in (11) is over the quantization interval (5) for  $k_i = k$ .

The second factor in the integrand from (8) depends on the optimization criteria used for calculating the estimate of  $h_1$ . In Section 3.1, the maximum likelihood (ML) estimate of  $h_1$  based on  $K_p$  pilot symbols is shown to be equal to

$$\hat{h}_1 = \frac{\mathbf{r}_{1p} \mathbf{c}_{sp}^H}{K_p E_s}, \quad (12)$$

with  $\mathbf{c}_{sp}$  the pilot symbols sent by the source and  $\mathbf{r}_{1p}$  the part of  $\mathbf{r}_1$  corresponding with the received pilot symbols. By using (1), this can be written as

$$\hat{h}_1 = \frac{h_1 \mathbf{c}_{sp} \mathbf{c}_{sp}^H}{K_p E_s} + \frac{\mathbf{n}_1 \mathbf{c}_{sp}^H}{K_p E_s}. \quad (13)$$

In a M-PSK constellation  $\mathbf{c}_{sp} \mathbf{c}_{sp}^H$  equals  $K_p E_s$ , yielding

$$\hat{h}_1 = h_1 + \frac{\mathbf{n}_1 \mathbf{c}_{sp}^H}{K_p E_s}. \quad (14)$$

By taking into account the ZMCSG noise distribution, one obtains the following expression for the distribution of  $\hat{h}_1$  conditioned on  $h_1$  and  $N_1$ :

$$p(\hat{h}_1 | h_1, N_1) = \frac{1}{\pi N_1 / K_p} e^{(-|\hat{h}_1 - h_1|^2)/(N_1 / K_p)}. \quad (15)$$

Using (11) and (15), the integral in (8) can be evaluated numerically, for a given  $h_1$ ,  $N_1$  and  $c_{s,i}$ .

The resulting likelihood (6) of  $c_{s,i}$  contains the channel parameters  $h_0$ ,  $h_1$ ,  $h_2$ ,  $N_0$ ,  $N_1$ , and  $N_2$ . As these parameters are not known at the destination, the likelihood (6) will be computed at the destination with the true channel parameters replaced by estimates. The channel gains  $h_0$  and  $h_2$  and noise variances  $N_0$  and  $N_2$  are estimated at the destination, while estimates of  $h_1$  and  $N_1$ , computed by the relay, could be sent from the relay to the destination. However, in order to avoid the numerical integration in (8), the destination will use the simplifying assumption that the relay makes a perfect estimate of  $h_1$ , so that

$$p(\hat{h}_1 | h_1, N_1) = \delta(\hat{h}_1 - h_1). \quad (16)$$

In this case, (8) reduces to

$$\begin{aligned} p(r_{2,i} | c_{s,i}, h_1, h_2, N_1, N_2) &= \sum_{k=0}^{2^Q-1} p(r_{2,i} | k_i = k, h_2, N_2) \\ &\quad \times P(k_i = k | c_{s,i}, \hat{h}_1 = h_1, h_1, N_1) \\ &= \sum_{k=0}^{2^Q-1} p(r_{2,i} | k_i = k, h_2, N_2) P(k_i = k | c_{s,i}, \gamma), \end{aligned} \quad (17)$$

with  $\gamma = |h_1|^2 / N_1$ ,

$$P(k_i = k | c_{s,i}, \gamma) = \int_{\phi_k^l}^{\phi_k^u} f_{\Theta}(\theta - \arg(c_{s,i}), \gamma) d\theta. \quad (18)$$

As a result, as far as the source-relay channel is concerned, only the value  $\gamma$  now needs to be known by the destination; an estimate of  $\gamma$  is sent from the relay to the destination.

Although the approximation (16) does not hold for small values of  $h_1$ , it does not significantly affect the error performance. As the value of  $h_1$  (and  $\gamma$ ) approaches zero,  $P(k_i = k | c_{s,i}, \gamma)$  approaches a uniform distribution, reducing (17) to

$$p(r_{2,i} | c_{s,i}, h_1, h_2, N_1, N_2) = \frac{1}{2^Q} \sum_{k=0}^{2^Q-1} p(r_{2,i} | k_i = k, h_2, N_2). \quad (19)$$

Because (19) no longer depends on  $c_{s,i}$ , the second factor from (6) can be discarded. The likelihood of the  $i$ th-received source symbol is now calculated using only the source-destination path and is thus not influenced by the invalid approximation (16) regarding the channel gain estimate

of the source-relay channel. This results in a very robust system: with decreasing values of  $h_1$  (and  $\gamma$ ), the error caused by assuming the relay makes a perfect channel estimate increases, but the impact this assumption has on the error performance decreases.

Finally, the impact approximation (16) has on the error performance will also depend on the state of the source-destination channel. When the source-destination channel is in fading (small  $h_0$ ), the calculation of the symbol likelihoods (6) will be more affected by (false) approximations concerning the relay channel, as the direct path cannot provide information on the symbols sent.

### 3. Estimation

When the channel parameters are unknown at the receiver, they need to be estimated. The first step in the estimation process is the calculation of an initial estimate of the different channel coefficients and noise variances, using known pilot symbols sent by the source and the relay. Thereafter, the estimates of the source-destination and relay-destination channel coefficients will be refined using the EM algorithm at the destination. The estimate of the source-relay channel coefficient is not refined using the EM algorithm at the relay, as the increase in complexity would be unacceptable.

*3.1. Pilot-Based Estimation.* Both the relay and the destination must calculate a first estimate of the channel coefficient and the noise variance associated with the channel(s) they are connected to. This is done using pilot symbols sent by the source and the relay. Here we concentrate on the estimation of  $h_0$  and  $N_0$  at the destination. The ML estimates  $\hat{h}_0$  and  $\hat{N}_0$  resulting from the pilot symbols are obtained by solving the following maximization problem

$$(\hat{h}_0, \hat{N}_0) = \arg \max_{h_0, N_0} p(\mathbf{r}_{0p} | h_0, N_0), \quad (20)$$

where  $\mathbf{r}_{0p}$  is the part of  $\mathbf{r}_0$  corresponding to the received pilot symbols. As shown in Appendix A, the values of  $h_0$  and  $N_0$  that maximize (20) are equal to

$$\hat{h}_0 = \frac{\mathbf{r}_{0p} \mathbf{c}_{sp}^H}{K_p E_s}, \quad (21)$$

$$\hat{N}_0 = \frac{|\mathbf{r}_{0p} - h_0 \mathbf{c}_{sp}|^2}{K_p}, \quad (22)$$

where  $\mathbf{c}_{sp}$  denotes the pilot symbols sent by the source and  $K_p$  is the number of pilot symbols sent by both source and relay. Similar equations are obtained for the estimation of  $h_1$  and  $N_1$  at the relay (based on the  $K_p$  pilot symbols sent by the source) and  $h_2$  and  $N_2$  at the destination (based on  $K_p$  pilot symbols sent by the relay).

When using an estimate of  $h_0$  instead of the actual value in (22), the estimate of the noise variance is biased by a factor  $(K_p - 1)/K_p$ , as shown in Appendix B. Especially when using a small number of pilot symbols, it is important to compensate for this bias by multiplying (22) with  $K_p/(K_p - 1)$ . Further,

it can be advantageous to average out the noise variance between consecutive frames, because this variance tends to fluctuate much slower than the channel coefficients. This can be accomplished by using a noise variance  $N_0^{(k)}$  equal to

$$N_0^{(k)} = \alpha N_0^{(k-1)} + (1 - \alpha) \hat{N}_0, \quad (23)$$

when evaluating the symbol likelihoods (6) in the  $k$ th received frame. The notation  $N_0^{(k-1)}$  is employed for the variance used in the previous frame and  $\hat{N}_0$ , given by (22), is an estimate of the noise variance based on the pilot symbols received in the current frame. The weighting factor  $\alpha$  lies between 0 and 1 and depends on the expected speed of fluctuation of the noise variance.

The relay uses the estimates  $\hat{h}_1$  and  $\hat{N}_1$  to compute an estimate  $\hat{\gamma} = |\hat{h}_1|^2 / \hat{N}_1$  of the instantaneous SNR on the source-relay channel, to be forwarded to the destination. The estimates of  $h_0$  and  $h_2$  will be further refined at the destination by means of the EM algorithm. As shown in Section 4.2.1, there is little to gain in refining the pilot based estimates of  $N_0$  and  $N_2$ . Therefore, only the estimates of  $h_0$  and  $h_2$  will be updated using the EM algorithm.

Because the mean-square error (MSE) of (21) satisfies

$$E \left[ |\hat{h}_0 - h_0|^2 \right] = \frac{N_0}{K_p E_s} = \frac{K_p + K_d}{K_p} \frac{1}{K} \frac{N_0}{E_b}, \quad (24)$$

transmitting a fixed number of  $K$  information bits and keeping the ratio  $K_d/K_p$  constant will make the MSE related to the channel coefficient estimation essentially independent of the constellation size  $M$ .

*3.2. EM Algorithm.* The channel coefficient estimates discussed in the previous section are solely based on the pilot symbols which represent only a small part of the received signal energy. In order to improve these estimates, the EM algorithm can be used. The EM algorithm is an iterative algorithm that alternates between an estimation step and a maximization step. It allows calculating a ML estimate of a set of parameters from an observation that is also influenced by other unknown variables, named nuisance parameters. In this specific case, the source-destination channel coefficient ( $h_0$ ) and the relay-destination channel coefficient ( $h_2$ ) are the parameters that need to be estimated, while the symbols sent by the source and relay, denoted  $\mathbf{c}_s$  and  $\mathbf{c}_r$ , respectively, are considered nuisance parameters.

Introducing  $\mathbf{r}_d = (\mathbf{r}_0, \mathbf{r}_2)$ ,  $\mathbf{c}_d = (\mathbf{c}_s, \mathbf{c}_r)$ , and  $\mathbf{h}_d = (h_0, h_2)$ , the estimation step during iteration  $k$  involves calculating the function

$$Q(\mathbf{h}_d, \hat{\mathbf{h}}_d^{(k-1)}) = E_{\mathbf{c}_d} \left[ \ln p(\mathbf{r}_d | \mathbf{c}_d, \mathbf{h}_d) | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)} \right]. \quad (25)$$

In order not to overload the notation, the dependency of the distributions on the noise variance is not noted explicitly. The maximization step involves determining a value for  $h_0$  and  $h_2$  that maximizes the  $Q$  function from (25), so the new estimates calculated at iteration  $k$  are equal to

$$\hat{\mathbf{h}}_d^{(k)} = \arg \max_{\mathbf{h}_d} Q(\mathbf{h}_d, \hat{\mathbf{h}}_d^{(k-1)}), \quad (26)$$

where  $\hat{\mathbf{h}}_d^{(0)}$  contains the estimate of  $(h_0, h_2)$  obtained from the pilot symbols only. As shown in Appendix C, the values of  $h_0$  and  $h_2$  that maximize (26) are equal to

$$\begin{aligned}\hat{h}_0^{(k)} &= \frac{\mathbf{r}_0 \mathbf{u}_s^H}{(K_p + K_d) E_s}, \\ \hat{h}_2^{(k)} &= \frac{\mathbf{r}_2 \mathbf{u}_r^H}{(K_p + K_d) E_r},\end{aligned}\quad (27)$$

with  $\mathbf{u}_s$  and  $\mathbf{u}_r$  denoting the a posteriori expectations (conditioned on  $\mathbf{r}_d$  and  $\hat{\mathbf{h}}_d^{(k-1)}$ ) of the symbol vectors  $\mathbf{c}_s$  and  $\mathbf{c}_r$ , respectively.

The components of  $\mathbf{u}_s$  and  $\mathbf{u}_r$  that correspond to the pilot symbols are equal to these pilot symbols. The computation of the components of  $\mathbf{u}_s$  and  $\mathbf{u}_r$  that correspond to the data symbols is outlined below. The  $i$ th elements of the vectors  $\mathbf{u}_s$  and  $\mathbf{u}_r$  are equal to

$$\begin{aligned}u_{s,i} &= \sum_{c_{s,i}, c_{r,i}} c_{s,i} p(c_{s,i}, c_{r,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}) \\ &= \sum_{c_{s,i}} c_{s,i} p(c_{s,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}),\end{aligned}\quad (28)$$

$$\begin{aligned}u_{r,i} &= \sum_{c_{s,i}, c_{r,i}} c_{r,i} p(c_{s,i}, c_{r,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}) \\ &= \sum_{c_{r,i}} c_{r,i} p(c_{r,i} | c_{s,i}, \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}) p(c_{s,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}).\end{aligned}\quad (29)$$

The summations in (28) and (29) run over all values that  $c_{s,i}$  and/or  $c_{r,i}$  can adopt. Further development of the conditional distribution of  $c_{r,i}$  in (29) yields

$$\begin{aligned}p(c_{r,i} | c_{s,i}, \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}) &= \frac{p(c_{r,i}, r_{d,i} | c_{s,i}, \hat{\mathbf{h}}_d^{(k-1)})}{p(r_{d,i} | c_{s,i}, \hat{\mathbf{h}}_d^{(k-1)})} \\ &= \frac{p(r_{2,i} | c_{r,i}, \hat{h}_2^{(k-1)}) p(c_{r,i} | c_{s,i})}{\sum_{\tilde{c}_{r,i}} p(r_{2,i} | \tilde{c}_{r,i}, \hat{h}_2^{(k-1)}) p(\tilde{c}_{r,i} | c_{s,i})}.\end{aligned}\quad (30)$$

The distribution of  $p(c_{r,i} | c_{s,i})$  follows (18). When evaluating (18), the destination makes use of the estimate  $\hat{y}$ , forwarded by the relay. The marginal a posteriori probabilities of the data symbols  $c_{s,i}$  can be calculated by the decoder at the destination [13]; therefore, this EM approach is referred to as code-aided.

A simple lower bound on the MSE related to the EM estimation of the channel coefficients is obtained by assuming that the data symbols transmitted by the source and the relay are known to the destination (i.e.,  $\mathbf{u}_s = \mathbf{c}_s$ ,  $\mathbf{u}_r = \mathbf{c}_r$ ). A same reasoning as for the pilot-based estimation yields

$$\begin{aligned}E\left[|\hat{h}_0 - h_0|^2\right] &\geq E\left[|\hat{h}_0 - h_0|^2\right]_{\mathbf{u}_s = \mathbf{c}_s} \\ &= \frac{N_0}{(K_p + K_d) E_s} = \frac{1}{K} \frac{N_0}{E_b},\end{aligned}\quad (31)$$

and similarly for  $E[|\hat{h}_2 - h_2|^2]$ .

**3.2.1. EM with Iterative Decoders.** The EM algorithm is used to iteratively refine the channel parameter estimates. For each EM iteration  $k$ , expressions (28) and (29) are evaluated in order to obtain the a posteriori symbol expectations  $\mathbf{u}_s$  and  $\mathbf{u}_r$ . The latter are used in (27) to obtain a new estimate of the channel coefficients  $h_0$  and  $h_2$ , respectively.

Both  $\mathbf{u}_s$  and  $\mathbf{u}_r$  depend on the a posteriori symbol probabilities  $p(c_{s,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)})$ . These probabilities are calculated by the channel decoder, in which the symbol likelihoods (6) are evaluated using a previous estimate  $\hat{\mathbf{h}}_d^{(k-1)}$  of the channel coefficients  $h_0$  and  $h_2$ . As a result, each EM iteration  $k$ , the channel code needs to be fully decoded in order to obtain the a posteriori symbol probabilities, conditioned on the channel coefficient estimates from the previous iteration. When using an iteratively decoded channel code, multiple decoding iterations are needed within each EM iteration, which can be a very intensive computational task.

When decoding is iterative, the computational complexity can greatly be reduced by executing only one decoder iteration for each EM iteration, without resetting the decoder. The a posteriori symbol probabilities obtained this way will only be an approximation of the true a posteriori symbol probabilities. However, with successive EM-code iterations, the channel decoder converges, and the approximated symbol probabilities will approach the real a posteriori probabilities. As shown in [14], this approach does not have a considerable effect on error performance, while it significantly decreases computational complexity.

**3.2.2. Assumption of Uncoded Transmission.** To lower the computational complexity, the calculation of the marginal a posteriori symbol expectations (28) and (29) can be carried out under the (false) assumption that the M-PSK symbols transmitted by the source are uncoded: the symbols contained in  $\mathbf{c}_s$  are considered statistically independent and uniformly distributed over the M-PSK constellation. This approximation involves the following substitution in (28), (29):

$$\begin{aligned}p(c_{s,i}, c_{r,i} | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}) &= C p(r_{0,i} | c_{s,i}, \hat{h}_0^{(k-1)}) \\ &\quad \times p(r_{2,i} | c_{r,i}, \hat{h}_2^{(k-1)}) p(c_{r,i} | c_{s,i}),\end{aligned}\quad (32)$$

where  $C$  is a normalization constant. When using this approximation, no decoding steps are required within the EM algorithm. After the EM algorithm has completed, the resulting estimates are forwarded to the decoder. This approach significantly reduces computational complexity while still achieving an acceptable performance as will be shown in the next section. The proposed approximation is especially useful when using noniterative channel codes, in which case the technique from Section 3.2.1 does not reduce computational complexity.

TABLE 1: Type of data sent during each timeslot.

	First timeslot	Second timeslot
Noncooperative	$\mathbf{i}_1, \mathbf{p}_1$	$\mathbf{p}_2$
Cooperative	$\mathbf{i}_1, \mathbf{p}_1$	$\mathbf{i}'_1, \mathbf{p}'_1$

## 4. Simulations

We consider a source that encodes frames of 1024 information bits by means of a  $(1, 13/15)_8$  RSCC turbo code [15] and maps the encoded bits to M-PSK symbols. The relay is located halfway between source and destination. The path loss exponent equals 4, and the distance between source and destination is considered unity. By means of computer simulations, the Frame Error Rate (FER) performance of the proposed system with the different estimation strategies is determined as function of the  $E_b/N_0$  ratio. Using (2), the energy of the symbols sent by the source and the relay is determined for a given value of  $E_b$ . All noise variances are assumed equal ( $N_0 = N_1 = N_2$ ), but are estimated separately. Unless stated otherwise, the relay uses  $\log_2 M$  bits for the quantization of the received symbols.

**4.1. Known Channel Parameters.** First the FER performance of the novel QF protocol, the pure Amplify and Forward (AF), and a noncooperative system are compared, assuming the relay and the destination are known to all relevant channel parameters. In order to achieve a fair comparison between noncooperative communication and a cooperative system, the turbo code is punctured from rate 1/3 to rate 2/3 when using cooperative communication; this way, the destination receives 1024 information bits and 2048 redundant bits in both scenarios. This is illustrated in Table 1.

When using noncooperative communication, the source uses the first timeslot to send to the destination 1024 information bits, denoted by  $\mathbf{i}_1$ , and 512 parity bits, denoted by  $\mathbf{p}_1$ . In the second timeslot, the source sends to the destination another 1536 parity bits, denoted by  $\mathbf{p}_2$ . At the end of the second timeslot, the destination received 1024 information bits ( $\mathbf{i}_1$ ) and 2048 redundant bits ( $\mathbf{p}_1, \mathbf{p}_2$ ). When using cooperative communication, 1536 parity bits  $\mathbf{p}_2$  are removed by puncturing the output of the channel encoder. In the first timeslot, the source again broadcasts 1024 information bits  $\mathbf{i}_1$  and 512 parity bits  $\mathbf{p}_1$ . In the second timeslot, the relay forwards to the destination the information it received in the first timeslot. The forwarded information bits and parity bits are denoted by  $\mathbf{i}'_1$  and  $\mathbf{p}'_1$ , respectively. At the end of the second timeslot, the destination again received 1024 information bits ( $\mathbf{i}_1$ ) and 2048 redundant bits ( $\mathbf{p}_1, \mathbf{i}'_1, \mathbf{p}'_1$ ).

The FER curve for BPSK mapping is shown in Figure 3. Note that the proposed QF protocol closely approaches the performance of AF when quantizing only with  $\log_2 M$  ( $= 1$ ) bits. Quantizing with more than  $\log_2 M$  bits only marginally improves the error performance. When using QPSK and 8-PSK mapping, we have verified (results not displayed) that quantization with 2 and 3 bits, respectively, is again sufficient

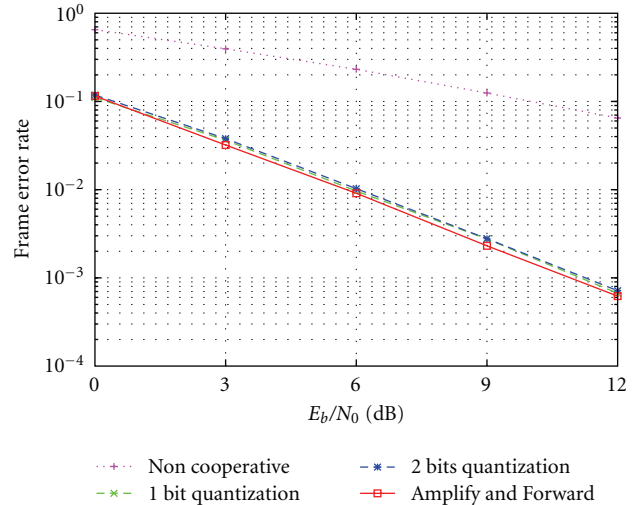


FIGURE 3: Frame Error Rate of a turbo-coded Quantize and Forward system with known channel parameters using BPSK mapping and 12 decoder iterations.

to closely approach the FER performance of a pure AF system using the same constellation. While achieving a similar FER performance, the proposed QF protocol can be used with half-duplex relay terminals, whereas the relay terminals in an AF system need to be able to transmit and receive data at the same time. This makes the QF protocol more suitable for the use in resource-constrained networks. Because of their higher spatial diversity, the cooperative systems considerably outperform the noncooperative system.

**4.2. Estimated Channel Parameters.** We determine the effect of the different estimation methods, discussed in Section 3, on the FER of the proposed QF system. To be able to calculate an initial estimate for the channel coefficients and noise variances,  $K_p$  pilot symbols are sent by both source and relay. To maintain a nearly fixed  $(K_d + K_p)/K_d$  ratio in (2), 9, 5, and 3 pilot symbols are sent when using BPSK, QPSK, and 8PSK mapping, respectively.

The relay converts the estimated value  $\hat{\gamma}$  of the instantaneous SNR to dB and uniformly quantizes it between  $\gamma_{\min, \text{dB}}$  and  $\gamma_{\max, \text{dB}}$  using 5 bits. Using computer simulations, we have selected the values of  $\gamma_{\min, \text{dB}}$  and  $\gamma_{\max, \text{dB}}$  such that they minimize, at  $E_b/N_0 = 6$  dB, the FER of the system with known channel parameters as described in Section 4.1, but with the value of  $\gamma$  unknown to the destination. For all values of  $E_b/N_0$  in (0 dB, 12 dB), we used the  $\gamma_{\min, \text{dB}}$  and  $\gamma_{\max, \text{dB}}$  that are optimum at  $E_b/N_0 = 6$  dB. The quantized bits are encoded with a simple  $(1, 3)_8$  convolutional code, mapped on M-PSK symbols and sent to the destination.

A factor  $\alpha$ , equal to 0.95 which is used in (23) for averaging out the noise variances. The EM iterations and turbo decoding iterations are carried out as explained in Section 3.2.1. For each frame, 12 EM-code iterations are used. When using the approximation of uncoded symbols discussed in Section 3.2.2, the EM algorithm is allowed 5

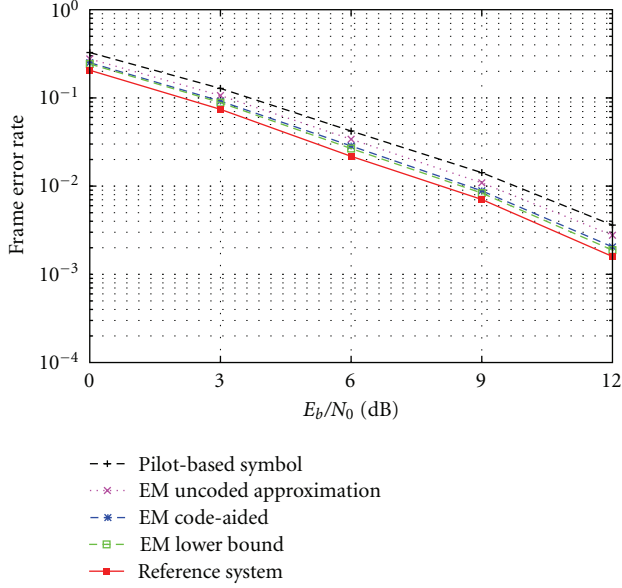


FIGURE 4: Frame Error Rate of the different proposed estimation techniques using 8-PSK mapping.

iterations, after which the turbo code is decoded using 12 iterations.

The FER performance resulting from the considered estimation technique is compared to an EM lower bound. This EM lower bound on the FER corresponds to the best performance the EM algorithm can achieve and is calculated by assuming that the data symbols sent by the source and relay are known at the destination when calculating the estimates of  $h_0$  and  $h_2$ . As compared to the reference system with known channel parameters and no pilot symbols transmitted, this EM lower bound has the worse FER performance due to channel estimation errors (especially the estimation of the source-relay channel coefficient, where only pilot symbols are used) and the smaller  $E_s$  and  $E_r$  from (2), because of the pilot symbols (assuming a constant total transmit energy per frame).

Three different estimation methods are being considered: pilot based only, code-aided EM, and uncoded EM. The pilot-based approach uses only the received pilot symbols for calculating an estimate of the different channel parameters, without running the EM algorithm. In the code-aided EM method, the a posteriori symbol probabilities needed to calculate (28) and (29) are provided by the channel decoder, while in the uncoded EM approach, these probabilities are approximated as explained in Section 3.2.2.

The effect of the different estimation methods on the error performance for BPSK, QPSK, and 8-PSK mapping is summarized in Table 2 for FER = 0.01 while Figure 4 shows the FER versus  $E_b/N_0$  in the case of 8-PSK. The results indicate that the effect of channel estimation errors on the FER becomes more severe as the number of bits per symbol increases (and the minimum distance between 2 constellation points decreases). The simulation results also show that the assumption of uncoded symbols works

TABLE 2:  $E_b/N_0$  ratio needed to achieve an FER of 0.01.

BPSK	$E_b/N_0$ (dB)	Difference (dB)
Reference system	5.94	0
EM lower bound	6.04	+0.10
EM code-aided	6.04	+0.10
EM uncoded approx.	6.05	+0.11
Pilot based only	6.52	+0.58
QPSK	$E_b/N_0$ (dB)	Difference (dB)
Reference system	6.06	0
EM lower bound	6.29	+0.23
EM code-aided	6.32	+0.26
EM uncoded approx.	6.42	+0.36
Pilot based only	6.91	+0.85
8-PSK	$E_b/N_0$ (dB)	Difference (dB)
Reference system	8.10	0
EM lower bound	8.52	+0.42
EM code-aided	8.67	+0.57
EM uncoded approx.	9.18	+1.08
Pilot based only	9.78	+1.68

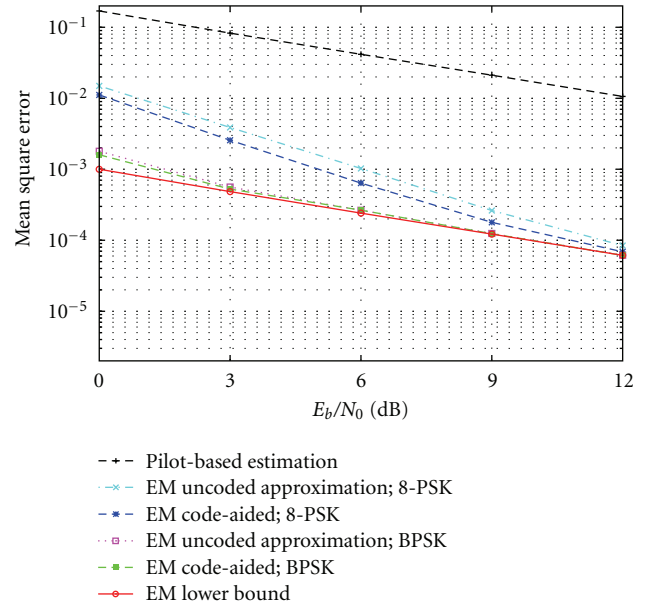


FIGURE 5: Mean Square Error values for the estimate of  $h_0$ .

very well for BPSK, but the performance deteriorates as the number of bits per symbol increases.

The effect of the constellation size on the FER performance degradation can be explained by investigating the MSE values resulting from the different estimations, shown in Figure 5 (for  $h_0$ ) and Figure 6 (for  $h_2$ ). The curves related to pilot-based estimation and to the EM lower bound coincide with (24) and with the lower bound in (31), respectively. The deterioration in FER performance for higher constellations when using the assumption of uncoded symbols is also reflected in the increasing MSE of the



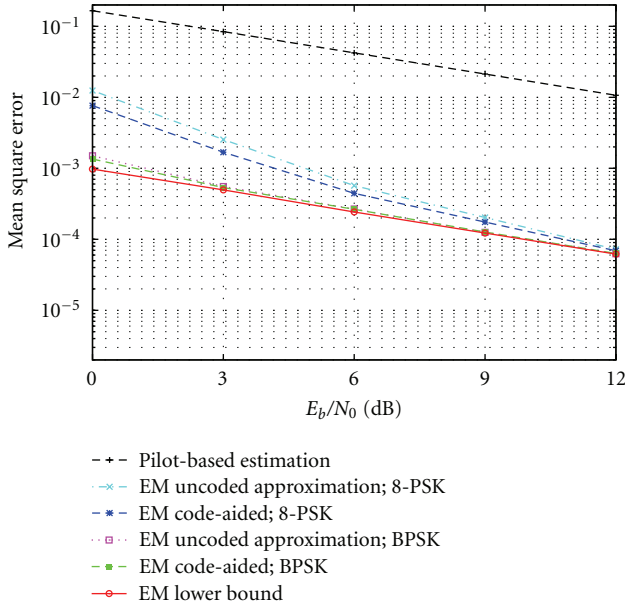


FIGURE 6: Mean Square Error values for the estimate of  $h_2$ .

estimates of  $h_0$  and  $h_2$ . The difference between the likelihoods of the different symbols in (32) will become less pronounced when there are more constellation points, making it harder to determine which symbol has been sent, and thus making an accurate estimation difficult. The MSE of the code-aided approach is closer to the EM lower bound compared to the uncoded approximation for the same constellation, but also rises with the increasing number of bits per symbol due to the higher symbol error rate (QPSK) and more decoding errors (8-PSK) than in the case of BPSK. From (28) and (29), one notices that the a posteriori expectation of the symbol vectors sent by both source and relay is conditioned on the observation of both communication channels (direct link and relay path). This cooperative nature accounts for the very accurate estimate of the source-destination and relay-destination channel.

**4.2.1. Noise Estimation Performance.** In this section, the performance loss resulting from the noise variance estimation is analyzed. This is done by comparing a system with estimated noise variances to a system where the noise variances are assumed to be known to the destination. The noise variance estimates are computed as described in Section 3.1 while the other channel parameters are estimated using a code-aided EM approach. The FER performance of both systems is displayed in Figure 7 in the case of BPSK and 8-PSK mapping. As shown in the aforementioned figure, the FER performance of the system with estimated noise variances is very close to that of the system in which the noise variances are assumed to be known. This shows that there is little to be gained in refining the noise variance estimates, as the potential improvement in FER performance is very small.

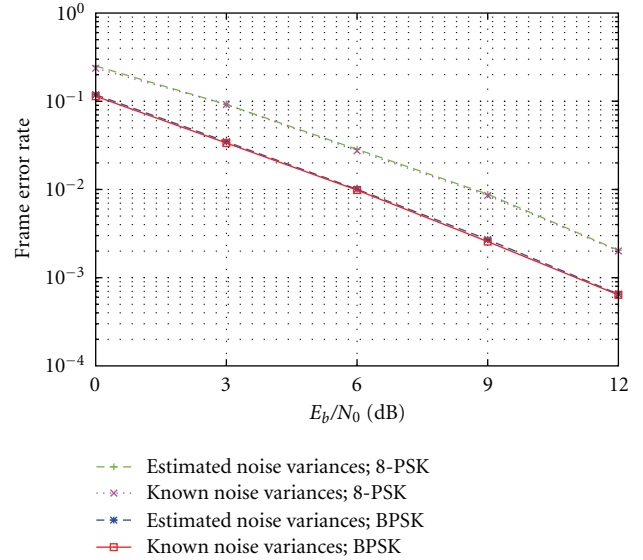


FIGURE 7: Frame Error Rate of a system with estimated noise variances, compared to a system with known noise variances, for both BPSK and 8-PSK mapping.

### 5. Conclusions

In this paper, a novel Quantize and Forward protocol has been introduced, which involves the relay making a coarse estimate of the source-relay channel, using only the received pilot symbols. Doing so, it is shown that quantization with only  $\log_2 M$  bits is sufficient to approach the performance of an AF system, while respecting the half-duplex constraint at the relay terminals. Furthermore, one aspect of the relay terminal becomes less complicated, in comparison to [6], because no overhead is needed in order to allow the destination to make an estimate of the source-relay channel. This makes the proposed QF protocol suitable for the use in sensor networks where a low complexity at the relay terminals is mandatory.

At the destination, the EM algorithm allows improving the pilot-based estimates of the source-destination and relay-destination channel coefficients. The EM algorithm yields a very good FER performance, but it also increases the computational complexity, as each EM iteration in principle requires the decoder to fully decode. This complexity can partly be reduced when using iterative decoding by changing the way the EM iterations and the decoder iterations are executed. When using noniterative decoding, the number of calculations can be reduced by using an approximation that assumes that the received signal consists of uncoded M-PSK symbols. This way, no decoding steps are required within the EM algorithm. The aforementioned approximation performs very well when used with BPSK mapping, but deteriorates with increasing number of bits per symbol. When using high-density constellations like 8-PSK, the code-aided EM algorithm should be used to achieve a Frame Error Rate that is very close to that of a system with known channel parameters.

## Appendices

### A. Pilot-Based ML Estimation

By definition, the ML estimates of a channel coefficient  $h$  and noise variance  $N$ , given the channel observation  $\mathbf{r}$ , are equal to

$$(\hat{h}, \hat{N}) = \arg \max_{(h, N)} p(\mathbf{r} | h, N) = \arg \max_{(h, N)} \ln p(\mathbf{r} | h, N). \quad (\text{A.1})$$

In a Rayleigh fading environment, the probability distribution of  $\mathbf{r}$  is given by

$$p(\mathbf{r} | h, N, \mathbf{c}_{\text{sp}}) = \frac{1}{(\pi N)^{K_p}} e^{(-|\mathbf{r} - h\mathbf{c}_{\text{sp}}|^2)/N}, \quad (\text{A.2})$$

with  $\mathbf{c}_{\text{sp}}$  being a vector consisting of  $K_p$ -known pilot symbols with a symbol energy that is equal to  $E_s$ . By substituting (A.2) in (A.1), the latter can be written as

$$(\hat{h}, \hat{N}) = \arg \max_{(h, N)} \left( -K_p \ln(N) - \frac{|\mathbf{r} - h\mathbf{c}_{\text{sp}}|^2}{N} \right). \quad (\text{A.3})$$

Maximizing (A.3) with respect to  $h$  yields

$$\begin{aligned} \hat{h} &= \arg \max_h -|\mathbf{r} - h\mathbf{c}_{\text{sp}}|^2 \\ &= \arg \min_h (h\mathbf{c}_{\text{sp}}^H \mathbf{r} - h\mathbf{r}^H \mathbf{c}_{\text{sp}} - h\mathbf{c}_{\text{sp}}^H \mathbf{r}) \\ &= \arg \min_h \left( K_p E_s \left| h - \frac{\mathbf{r}^H \mathbf{c}_{\text{sp}}}{K_p E_s} \right|^2 \right) \\ &= \frac{\mathbf{r}^H \mathbf{c}_{\text{sp}}}{K_p E_s}. \end{aligned} \quad (\text{A.4})$$

The value of  $N$  that maximizes (A.3) can be found by searching the root of the derivative with respect to  $N$  of (A.3), yielding the following equation:

$$0 = -\frac{K_p}{N} + \frac{|\mathbf{r} - h\mathbf{c}_{\text{sp}}|^2}{N^2}. \quad (\text{A.5})$$

Solving this equation yields

$$\hat{N} = \frac{|\mathbf{r} - h\mathbf{c}_{\text{sp}}|^2}{K_p}. \quad (\text{A.6})$$

### B. Noise Variance Estimation Bias

The ML estimate of the noise variance of a direct Rayleigh fading channel is given by (22). When the channel coefficient  $h$  is not known, an estimate  $\hat{h}$  can be used instead, yielding

$$\hat{N} = \frac{|\mathbf{r} - \hat{h}\mathbf{c}_{\text{sp}}|^2}{K_p}. \quad (\text{B.1})$$

When using an ML channel coefficient estimate (21), and taking into account the channel model defined by (1), (B.1) can be written as

$$\begin{aligned} \hat{N} &= \frac{|\mathbf{h}\mathbf{c}_{\text{sp}} + \mathbf{n} - h\mathbf{c}_{\text{sp}} - (\mathbf{n}\mathbf{c}_{\text{sp}}^H \mathbf{c}_{\text{sp}} / K_p E_s)|^2}{K_p} \\ &= \frac{1}{K_p} \left( \mathbf{n}\mathbf{n}^H - \frac{\mathbf{n}\mathbf{c}_{\text{sp}}^H \mathbf{c}_{\text{sp}} \mathbf{n}^H}{K_p E_s} \right). \end{aligned} \quad (\text{B.2})$$

Calculating the expected value of (B.2) yields

$$\mathbb{E}[\hat{N}] = \frac{1}{K_p} \left( \mathbb{E}[\mathbf{n}\mathbf{n}^H] - \mathbb{E} \left[ \frac{\mathbf{n}\mathbf{c}_{\text{sp}}^H \mathbf{c}_{\text{sp}} \mathbf{n}^H}{K_p E_s} \right] \right). \quad (\text{B.3})$$

The statistical independence of the noise samples can be expressed as

$$\mathbb{E}[n_i n_j^*] = \begin{cases} 0, & \text{if } i \neq j, \\ N, & \text{if } i = j. \end{cases} \quad (\text{B.4})$$

Taking (B.4) into consideration, (B.2) can be rewritten as

$$\hat{N} = N - \frac{N}{K_p} = N \left( \frac{K_p - 1}{K_p} \right). \quad (\text{B.5})$$

The expression above shows that when an ML estimate of  $h$  is used in (22), the estimate of the noise variance is biased by a factor that is equal to  $(K_p - 1)/K_p$ . This estimate can be made true by multiplying it with  $K_p/(K_p - 1)$ .

### C. Maximization of $Q(\mathbf{h}_d, \hat{\mathbf{h}}_d^{(k-1)})$

For each EM iteration  $k$ , new estimates of the channel coefficients  $h_0$  and  $h_2$  are calculated by selecting the value of those parameters that maximizes the function  $Q(\mathbf{h}_d, \hat{\mathbf{h}}_d^{(k-1)})$ . Using factorization (6), this function can be written as

$$\begin{aligned} Q(\mathbf{h}_d, \hat{\mathbf{h}}_d^{(k-1)}) &= \mathbb{E}_{\mathbf{c}_d} [\ln p(\mathbf{r}_0 | \mathbf{c}_s, h_0) | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}] \\ &\quad + \mathbb{E}_{\mathbf{c}_d} [\ln p(\mathbf{r}_2 | \mathbf{c}_r, h_2) | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}]. \end{aligned} \quad (\text{C.1})$$

The new estimate of  $h_0$  should maximize the first term in (C.1) while the new estimates of  $h_2$  should maximize the second term in (C.1)

$$\begin{aligned} \hat{h}_0^{(k)} &= \arg \max_{h_0} \mathbb{E}_{\mathbf{c}_d} [\ln p(\mathbf{r}_0 | \mathbf{c}_s, h_0) | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}], \\ \hat{h}_2^{(k)} &= \arg \max_{h_2} \mathbb{E}_{\mathbf{c}_d} [\ln p(\mathbf{r}_2 | \mathbf{c}_r, h_2) | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}]. \end{aligned} \quad (\text{C.2})$$

Taking into consideration the Rayleigh fading channel model defined in Section 2.1, the first line of (C.2) can be written as

$$\begin{aligned} \hat{h}_0^{(k)} &= \arg \min_{h_0} \mathbb{E}_{\mathbf{c}_d} [|\mathbf{r}_0 - h_0 \mathbf{c}_s|^2 | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}] \\ &= \arg \min_{h_0} \mathbb{E}_{\mathbf{c}_d} [h_0 h_0^* \mathbf{c}_s^H - \mathbf{r}_0 h_0^* \mathbf{c}_s^H - h_0 \mathbf{c}_s \mathbf{r}_0^H | \mathbf{r}_d, \hat{\mathbf{h}}_d^{(k-1)}]. \end{aligned} \quad (\text{C.3})$$

By introducing the notation  $\mathbf{u}_s$  for  $\sum_{c_d} \mathbf{c}_s p(\mathbf{c}_d | \mathbf{r}_d, \hat{\mathbf{h}}^{(k-1)})$ , (C.3) can be written as

$$\hat{h}_0^{(k)} = \arg \min_{h_0} (h_0 h_0^* (K_p + K_d) E_s - \mathbf{r}_0 h_0^* \mathbf{u}_s^H - h_0 \mathbf{u}_s \mathbf{r}_0^H). \quad (\text{C.4})$$

This minimization problem is very similar to (A.4), yielding the following solution for  $\hat{h}_0^{(k)}$ :

$$\hat{h}_0^{(k)} = \frac{\mathbf{r}_0 \mathbf{u}_s^H}{(K_p + K_d) E_s}. \quad (\text{C.5})$$

A similar method can be used in the second line of (C.2), in order to obtain an estimate  $\hat{h}_2^{(k)}$  of the relay-destination channel coefficient, yielding

$$\hat{h}_2^{(k)} = \frac{\mathbf{r}_2 \mathbf{u}_r^H}{(K_p + K_d) E_r}, \quad (\text{C.6})$$

with

$$\mathbf{u}_r = \sum_{c_d} \mathbf{c}_r p(\mathbf{c}_d | \mathbf{r}_d, \hat{\mathbf{h}}^{(k-1)}). \quad (\text{C.7})$$

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## Preliminary call for papers

The 2011 European Signal Processing Conference (EUSIPCO-2011) is the nineteenth in a series of conferences promoted by the European Association for Signal Processing (EURASIP, [www.urasip.org](http://www.urasip.org)). This year edition will take place in Barcelona, capital city of Catalonia (Spain), and will be jointly organized by the Centre Tecnològic de Telecomunicacions de Catalunya (CTTC) and the Universitat Politècnica de Catalunya (UPC).

EUSIPCO-2011 will focus on key aspects of signal processing theory and applications as listed below. Acceptance of submissions will be based on quality, relevance and originality. Accepted papers will be published in the EUSIPCO proceedings and presented during the conference. Paper submissions, proposals for tutorials and proposals for special sessions are invited in, but not limited to, the following areas of interest.

## Areas of Interest

- Audio and electro-acoustics.
- Design, implementation, and applications of signal processing systems.
- Multimedia signal processing and coding.
- Image and multidimensional signal processing.
- Signal detection and estimation.
- Sensor array and multi-channel signal processing.
- Sensor fusion in networked systems.
- Signal processing for communications.
- Medical imaging and image analysis.
- Non-stationary, non-linear and non-Gaussian signal processing.

## Submissions

Procedures to submit a paper and proposals for special sessions and tutorials will be detailed at [www.eusipco2011.org](http://www.eusipco2011.org). Submitted papers must be camera-ready, no more than 5 pages long, and conforming to the standard specified on the EUSIPCO 2011 web site. First authors who are registered students can participate in the best student paper competition.

## Important Deadlines:



Proposals for special sessions	15 Dec 2010
Proposals for tutorials	18 Feb 2011
<b>Electronic submission of full papers</b>	<b>21 Feb 2011</b>
Notification of acceptance	23 May 2011
Submission of camera-ready papers	6 Jun 2011

Webpage: [www.eusipco2011.org](http://www.eusipco2011.org)

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