# Do preferences and beliefs in dilemma games exhibit complementarity? 

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QI15

## Introduction

- Start from "Preferences and beliefs in a sequential social dilemma: a within-subjects analysis." (Blanco, et.al., 2014)
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- Results seemed promising for a quantum model
- Work in progress. Some problems, advice needed!
(1) Introduction
(2) The experiment
- The game
- The experiment
(3) Three effects
- FM and SM correlation
- Consensus effect
- Reasoned player
(4) QP\&B model
- The measurements
- Three effects revisited
- Dimension of the belief basis?
- QP\&B model
(5) Discussion and future plans


## The game

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- Prisoner Dilemma variant, 2 players
- Sequential: first FM, then SM
- 'No unconditional cooperation'

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| Treatment | Baseline | Elicit_Beliefs | True_Distribution |
| ---: | :--- | :--- | :--- |
| Task 1 | 2nd move | 2nd move | 2nd move |
| Feedback $\left(a_{-i}^{S M}\right)$ | No | No | Yes |
| Task 2 | 1st move | beliefs $\left(a_{-i}^{S M}\right)$ | 1st move |
| Task 3 | beliefs $\left(a_{-i}^{F M}\right)$ | 1st move | beliefs $\left(a_{-i}^{F M}\right)$ |
| N. Participants | 40 | 60 | 60 |

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FM and SM correlation
Consensus effect
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## FM and SM correlation

## FMCR and SMCR

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## FMCR and SMCR

- Positive correlation
- Significant in all conditions
- Discussed in original paper


## Consensus effect

SMCR and beliefs

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## SMCR and beliefs

- Beliefs are biased towards actions (driven by preferences)
- Focus of original paper
- Seen as social projection by Busemeyer \& Pothos (2012), suitable for a quantum model


## Reasoned player

## Beliefs and FMCR

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- Equivalent to full information
- Measurement influences the system


## The measurements

- FM measurement $\rightarrow\left\{\left|a_{C}^{F M}\right\rangle,\left|a_{D}^{F M}\right\rangle\right\}$
- SM measurement $\rightarrow\left\{\left|a_{C}^{F M}\right\rangle,\left|a_{D}^{F M}\right\rangle\right\}$


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- Build the Hilbert Space by modeling the three effects

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## Three effects revisited

FM \& SM correlation:

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FM \& SM correlation:

- Classical correlation, can be measured at the same time
- In $\mathbb{H}^{4}$ spanned $\left\{\left|a_{i}^{F M}\right\rangle \otimes\left|a_{j}^{S M}\right\rangle\right\}$
- Not unlike Pothos and Busemeyer (2009)

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This tensoring also defines the belief base of $\mathbb{H}^{C E} \otimes \mathbb{H}^{R P}$.

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$\rightarrow$ Beliefbasis (and $\mathbb{H}^{C E}$ and $\mathbb{H}^{R P}$ ) 2 dimensional
- EX: Player thinks 7 opponents cooperate:



## QP\&B model

- Player is represented by a state vector in $\mathbb{H}^{4}=\mathbb{H}^{2} \otimes \mathbb{H}^{2}$, spanned by $\left\{\left|a_{i}^{F M}\right\rangle \otimes\left|a_{j}^{S M}\right\rangle\right\}$.


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- In $\mathbb{H}^{4}$ we have 2 orthogonal planes $B_{C}$ en $B_{D}$.
- Bundle of planes spanned by $B_{C}$ and $B_{D}$, contains the planes associated with belief measurement.


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- Relation between beliefs and actions are modeled by the angles between the beliefplanes and actionplanes.
- Fit is promising:


