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The role of lubricant feeding conditions on the performance improvement and friction reduction of journal bearings

Influence des conditions d'alimentation sur l'amélioration des performances et la réduction du frottement dans les paliers

Brito FP^{a,b}, Miranda AS^a, Claro JCP^a, Teixeira JC^a, Costa L^c and Fillon M^d

a Centre for Mechanical and Materials Technologies (CT2M), Universidade do Minho, Campus de Azurém, 4800-058 Guimarães, Portugal.

b ISEP IPP, Rua Dr. António Bernardino de Almeida, 431 4200-072 Porto, Portugal.

c Ministry of Energy and Water/DNAAS, Luanda, Angola.

d Institut Pprime, CNRS – Université de Poitiers – ENSMA, UPR 3346, Dept Génie Mécanique et Systèmes Complexes, SP2MI, 11 Bd Marie & Pierre Curie, BP 30179, 86962 Futuroscope Chasseneuil Cedex, France.

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The performance of hydrodynamic journal bearings is significantly affected by the conditions under which the lubricant is fed to the bearing. However, many conventional analyses are not prepared to suitably incorporate these parameters and their effect on bearing performance, due to the over-simplified way they treat them.

A thermohydrodynamic analysis suitable for conveniently deal with lubricant feeding conditions is now presented. It couples the numerical solution of the generalized Reynolds equation, the energy equations within the lubricant film and the heat transfer within the bush body. Special attention has been given to the treatment of the phenomena taking place within the grooves and in their vicinity, as well as to the ruptured film region.

The effect that lubricant feed pressure and temperature, groove length ratio, groove width ratio and groove number (single / twin) have on bearing performance has been analyzed for a broad range of conditions. The results were found to be in good agreement with experimental published results and the robustness of the model to suitably treat these phenomena has been confirmed. It was found that a careful tuning of the feeding conditions may indeed improve bearing performance.

Les performances des paliers lisses hydrodynamiques sont significativement affectées par les conditions dans lesquelles le lubrifiant est introduit dans le palier. Cependant, de nombreuses analyses classiques ne sont pas prêtes à intégrer convenablement ces paramètres et leurs effets sur les performances des paliers, en raison de la façon trop simplifiée avec laquelle ils les traitent.

Une analyse thermohydrodynamique appropriée pour traiter convenablement les conditions d'alimentation de lubrifiant est maintenant présenté. Elle intègre la solution numérique simultanée des équations de Reynolds généralisée, de l'énergie dans le film lubrifiant et de la de chaleur dans le coussinet. Une attention particulière a été portée pour le traitement des phénomènes se produisant dans les rainures et dans leur voisinage, ainsi que dans la région de rupture du film.

L'influence de la pression et de la température d'alimentation en lubrifiant, de la longueur et largeur de la rainure et du nombre de rainures (simple ou double) sur les performances du palier a été analysée pour un large éventail de conditions.

Les résultats numériques obtenus sont en bon accord avec ceux issus de la littérature expérimentale et la robustesse du modèle à traiter convenablement ces phénomènes a pu être confirmée. Il a été constaté qu'un réglage minutieux des conditions d'alimentation peut effectivement améliorer les performances.

1 Introduction

The accurate prediction of hydrodynamic journal bearing behaviour is far more complex than what their simple geometry might initially suggest. In fact, the simultaneous pressure, flow and heat transfer calculations need to include the treatment of phenomena such as film rupture, dual phase flow, film reformation, forced and free heat convection and conduction, viscous dissipation, inner groove lubricant flow mixing and thermo-elastic distortion. The integrated modelling of these phenomena in a single algorithm displaying acceptable computation times does not seem to be a straightforward task.

The complexity of the problem has frequently led to the use of oversimplified models. Particularly, the incorporation of lubricant feeding conditions was normally made in an oversimplified way in most theoretical approaches or inclusively altogether disregarded. In fact, neglecting the effect of lubricant feeding pressure, feeding temperature or the actual geometry of grooves might explain some of the notable discrepancies found between many theoretical predictions and experimental measurements. These discrepancies seem to be especially acute in the case of twin groove journal bearings. The lack of comprehensive experimental data focusing on these issues might have also contributed for the lack of awareness on the important role which lubricant feeding conditions play on bearing performance.

The inclusion of realistic lubricant feeding conditions in journal bearing analyses might raise some theoretical difficulties, depending on the model used. That is why some models neglect the influence of feeding conditions altogether, while others have used simplified approaches such as the consideration of:

- Full film reformation at the maximum film thickness position or the groove position [1];
- Grooves of infinitesimal width (no circumferential extension) [2][3];
- Grooves of finite width but extending them to the full length of the bush body [4][5][6];
- Finite size grooves but imposing flow rate or no feeding pressure (ambient) [5];

- Negligible or oversimplified thermal phenomena occurring at the groove region, such as the effect of recirculated hot oil, feeding temperature, reverse flow (oil that re-enters the groove from downstream) or back flow (fresh oil that flows upstream from the groove).

An analysis of the influence of feeding pressure in the performance of twin groove journal bearings through FEM was performed by [7]. A 1D energy equation was used and the axial pressure profile described through second order polynomials. It was shown that the feeding pressure affects the maximum temperature decreasing it, especially at low Sommerfeld numbers. The increase in feeding pressure was found to increase significantly the flow rate and slightly the power loss.

In [8][9] a series of theoretical and experimental studies on high speed twin groove journal bearings were carried out in order to assess the influence of the position of the two diametrically opposed axial grooves relatively to the load direction. In this last work a more rigorous THD approach was used, in comparison to the former works. Viscosity and temperature were allowed to vary along the thickness and heat conduction through the solid bodies was considered. The shaft temperature was imposed as being equal to the mean film temperature, while at the leading edge of the groove the inlet temperature was calculated through a heat balance. The use of such a groove mixing model proved to be determinant for the improvement of the results. With this new model a much better agreement with experiment was found for the temperature profile. However, huge differences between theory and experiment continued to be detected in flow rate.

Attention to film reformation and the use of mass conserving algorithms for treating feeding conditions was highlighted by [10]. A thorough theoretical and experimental assessment of the influence of lubricant feeding conditions on the performance of circular journal bearings with several groove configurations was made by [11], including twin axial groove journal bearings. Although this analysis was based on an isoviscous approach, a mass conservative algorithm proposed by [12] was used considering the actual dimensions of the grooves. Later [13], this approach was extended to take into account thermal effects, and validated with experimental evidence [14] on the influence of lubricant feeding conditions on the performance of single groove journal bearings. It was shown that often neglected parameters such as the real value of the feeding pressure and the actual groove geometry and location can significantly influence bearing performance.

Ma and Taylor [15] used a theoretical approach based on the separation model [16][17] and also carried out some experimental work in order to study the influence of feeding temperature and feeding pressure on the performance of twin groove elliptical bearings. It was found that the increase of feeding temperature yielded significantly higher values of the maximum temperature and flow rate and significantly lower values of power loss. On the other hand, increasing feeding pressure caused an important increase in flow rate, and moderate decreases in maximum bush temperature and power loss.

[18] analyzed the effect of lubricant feeding starvation on the THD performance of a journal bearing with a single axial groove. A previously developed model [19] was used, leading to the conclusion that a judicious selection of the groove location could reduce substantially the flow rate and the power loss without a deleterious effect in load carrying capacity.

An analysis of the influence of oil inlet conditions on the THD performance of the fully circumferentially grooved journal bearings was performed by [20]. A simplified axial averaging technique was used, that enabled the groove pressure and the entry temperature to the lubricant film to be explicitly incorporated into the lubricant energy equation and highlighted that the mixing effect must be always taken into account.

As a final remark, it may be concluded the experimental works focusing on twin groove journal bearings were found to be scarce or incomplete, namely in what concerns to the influence of feeding conditions and how these conditions may be tuned in order to optimize bearing performance and reduce power loss.

Effectively, [21][22] carried out a good experimental work on these bearings, but with fixed feeding conditions. The same can be said of the work by [23], which also lacks some other important data such as shaft eccentricity conditions. [8][9] presented very interesting experimental results of the behaviour of a twin groove journal bearing under several load angles. Unfortunately the speeds tested were normally too high to consider a laminar regime. Finally, [16] presented experimental results for this bearing type but omitted the main lubricant properties. Furthermore, the test bearing possessed unusually large grooves, spanning 55° each. It seemed that an experimental work testing a wide range of lubricant feeding conditions still needed to be done.

Recently the authors have published some works to address this lack of information. They assessed the influence of feeding temperature and feeding pressure on the performance of a 100mm twin axial groove bearing [24] and it was found that increasing feeding pressure leads to a significant rise in oil flow rate but has little effect on the maximum temperature and power-loss, except for the case of the lightly loaded bearing. Shaft temperature was found to be close to the bearing maximum temperature for low applied loads, being significantly smaller than this value for high loads. The mean shaft temperature was found to be significantly higher than the outlet

Also the role of each groove on the behaviour of a twin axial groove 50mm journal bearing was assessed [25]. As a novelty, they carried out the measurement of the flow rate in each groove and discovered that indeed groove flow rate information is vital to fully understand bearing behaviour. It was found that the cooling effect of the downstream groove is small for low eccentricities, becoming more relevant as eccentricity increases. The opposite phenomenon occurs at the upstream groove. Under high load / low feeding pressure negative flow rate at the upstream groove was detected dramatically affecting the bearing performance. Increasing feeding pressure yielded to a decrease in shaft eccentricity along with a temperature decrease, especially for high loads.

Another work was done with the same rig but focusing on the role of feeding temperature [26]. It was found that the increase of T_f has an effect in bearing performance which is analogous in many ways to the effect of the increase in eccentricity: increase in lubricant flow rate (especially in the low eccentricity range), in outlet temperature (T_{out}) and in maximum bush temperature (T_{max}). Nevertheless, the latter increase was lower than the corresponding increase in T_f .

The authors carried out an original comparison on the performance of a journal bearing with a single $(+90^{\circ})$ to the load line) and a twin $(\pm90^{\circ})$ axial groove configuration [27]. It was found that under heavy loaded operation the twin groove configuration might sometimes deteriorate the bearing performance when compared with the single groove arrangement, namely due to uneven lubricant feed through each groove. It was concluded that the knowledge of the feed flow rates through each groove can be used to improve bearing performance under specific regimes by implementing groove deactivation or flow balancing strategies.

Recently, they assessed the influence of load direction on the behaviour of a twin axial groove bearing [28]. The general trend found was that increasing groove angle tends to decrease the flow rate at the upstream groove and to increase the flow rate at the downstream groove. Hot oil reflux (negative flow rate) may occurs on both grooves (although, naturally, never simultaneously) under some conditions. The flow rate trends were mainly explained by the proximity to the pressure build-up zones and their locations relative to each groove.

Realistic feeding conditions such as the actual groove geometry and location, lubricant feeding pressure and lubricant feeding temperature, have been often neglected or oversimplified in most theoretical models. This has limited the analysis of important related phenomena such as the occurrence of reverse-flow at the inlet region, lubricant back-flow to the region which is located upstream of grooves, the mixing at the grooves, the inlet temperature profile, the occurrence of film rupture and reformation and the feeding flow rate.

The present work tries to address some of these concerns by presenting a model for the analysis of hydrodynamic Journal bearings which is suitable for assessing the aforementioned phenomena. It seems that an effort should be put on the development of an extensively validated model which may enable a better understanding of some of the mechanisms which can significantly affect the performance of common hydrodynamic journal bearings, and are still not thoroughly studied or satisfactorily dominated.

The decision of focusing the present study on twin groove journal bearings was based not only on the fact that this bearing geometry has received much less attention than single groove cases, but also because more acute theoretical performance prediction discrepancies have been observed for this bearing geometry. In fact, most theoretical models do not conveniently represent the temperature field in the ruptured film region and in the vicinity of grooves, and largely overestimate flow rate. Moreover, there are specific issues related to twin groove configuration, such as flow rate partition between the grooves and the occurrence of negative flow rate at one of the grooves, which are still not sufficiently studied and deserve further attention.

A Thermohydrodynamic (THD) approach was implemented. It was based on the simultaneous solution of the Generalized Reynolds Equation and the Energy Equation within the fluid domain and the Laplace equation within the bush body domain. Care was taken in order to realistically incorporate lubricant feeding conditions into the analysis: the real dimensions of the grooves were considered in pressure and flow calculations, mass and energy conserving algorithms were deployed. Models for the ruptured film region and the lubricant mixing at the grooves were derived. A simplified thermo-elastic model was implemented. Suitable boundary conditions were pursued. After describing the model a careful validation of the theoretical model with comparisons between its results and experimental data is presented. Finally, an extensive parametric study to assess the influence of lubricant feeding conditions such as feeding pressure and temperature, groove length and groove width ratio and number of grooves (single/twin) on bearing performance is carried out and discussed.

2 Theoretical Model

The theoretical model for the analysis of the steady state performance of journal bearings and especially adapted for the assessment of lubricant feed conditions is presented in continuation. It is an evolution of previous isoviscous [11] and thermohydrodynamic (THD) [13] models proposed by the group. Many details of the model have already been described in those works, (especially [13]) and so a more condensed description is made here. The model incorporates the full Thermohydrodynamic (THD) analysis and treats realistically the lubricant feeding conditions, namely taking into consideration the lubricant feeding pressure, the feeding temperature and the actual groove dimensions.

Based on input data such as the physical properties of the lubricant and bearing components, the operating conditions, the geometric configuration of the bearing and the lubricant feeding conditions, the model is expected to provide the main performance parameters relevant to bearing design and performance analysis, such as the hydrodynamic pressure and temperature profiles, oil flow rate, minimum film thickness, eccentricity, attitude angle, shaft torque, and power loss.

An outline of the bearing geometry, with all the major geometric characteristics identified, is presented in Fig. 1.



Fig. 1 - Outline of the bearing geometry

The unwrapped bearing gap geometry, with the corresponding axis system can be observed in dimensional and non-dimensional normalized form in Fig. 2, respectively, under the reasonable assumption that bearing curvature and inertial effects may be neglected.



Fig. 2 – Unwrapped dimensional and non-dimensional (normalized) fluid domain

2.1 Pressure and velocity fields

Widely accepted assumptions have been made regarding the pressure and flow field calculation. They include the thin film approximation, where pressure does not vary across the film thickness (not valid within groove regions); flow is in the laminar regime, with fluid inertia and gravity effects being negligible when compared with viscous effects; Steady state regime; The fluid is incompressible and Newtonian, with lubricant viscosity depending solely on temperature; the effect of the bearing curvature is negligible (clearance is much smaller than the bearing radius); there is no contact between surfaces and the effect of surface roughness is negligible (hydraulically smooth surface in the fully hydrodynamic regime); thermal expansion suffered by the components is uniform and based on their average temperature (only their diameter is affected - i.e. a differential thermal expansion approach).

The hydrodynamic pressure field, P(x,z) is governed by the Generalized Reynolds Equation (GRE), which is derived from a flow balance [29]:

$$\frac{\partial}{\partial x} \left[\rho_l F_2 \frac{\partial P}{\partial x} \right] + \frac{\partial}{\partial z} \left[\rho_l F_2 \frac{\partial P}{\partial z} \right] = \underbrace{U \frac{\partial}{\partial x} \left[\rho_l h F_3 \right]}_{Due \ to \ axial Poiseulle \ flow} = \underbrace{U \frac{\partial}{\partial x} \left[\rho_l h F_3 \right]}_{Cou et \ o \ circumferential Cou et \ circumferential Cou et \ flow}$$
(1)

With the viscosity integrals, which account for cross-film viscosity variation, being defined as follows:

$$F_0 = \int_0^h \frac{1}{\mu_l} dy \quad ; \quad F_1 = \int_0^h \frac{y}{\mu_l} dy \quad ; \quad F_2 = \int_0^h \frac{y}{\mu_l} \left(y - \frac{F_1}{F_0} \right) dy \quad ; \quad F_3 = 1 - \frac{F_1}{hF_0}$$
(2)

The standard solution of eq. (1) is only suitable within the full film region, where pressure is greater than ambient (P>0). The lubricant is not able to withstand low pressures (e.g. sub-ambient), separating in a series of streamlets separated by gaseous cavities and remaining at uniform pressure (in this work considered as ambient). So, a suitable algorithm must be used in order to locate the ruptured film region borders and then provide a special treatment to this region. The rupture boundary may be obtained with the so-called Reynolds condition, where pressure and pressure gradients in the direction of bearing rotation are considered to be zero. This condition ensures flow continuity and it is widely accepted in bearing modelling.

Concerning the film reformation boundary condition, some authors make the simplifying assumption of considering it to occur at the position of maximum film thickness or at the circumferential coordinate of grooves, which are considered to have negligible thickness and to span the whole bearing length. However, this condition is rather an imposition of the location of film reformation rather than a method for estimating it. This is highly unsuitable when considering realistic feeding conditions as is the aim of the present work.

In reality, film reformation will occur once locally the bearing gap is filled with lubricant (at the circumferential location where the remaining, recirculated, flow volume is enough to fill the gap), and this can be computed based on knowledge over the flow patterns and flow continuity. In fact, the GRE is basically an equation which computes flow continuity accounting for the various flow components existing within the bearing gap. Considering the aforementioned simplifying assumptions, these flows will be reduced to pressure-driven flow (Poiseuille) and the drag-driven flow (Couette). Within the ruptured film region the pressure is normally considered to be ambient and thus the flow will be purely drag-driven. In this way, mass flow continuity may be easily computed and film reformation boundary located. It is therefore possible to change the character of the GRE in the ruptured film region adapting it to a mass conserving equation which is valid throughout the whole bearing domain. Such was accomplished with the algorithm proposed by Elrod [12]. It is based on the mass balance performed to the Couette and Poiseuille flows crossing a finite control volume surrounding each computational node. The computation of Poiseuille and Couette flows will be performed at the full film region while Couette flow and liquid fraction will be accounted for at the ruptured film region. A substitution variable including a switch function which is either 0 or 1 whether the film is ruptured (P=0) or full width (P>0) is used for this. The result is a mass conservative, finite difference version of the Reynolds equation, valid throughout the whole domain and solved iteratively through the Gauss-Seidel method, and with the switch function being updated at each iteration.

The present work uses this algorithm, as adapted to THD by Costa et al. [13]. An advantage of this method is that it automatically provides the mass flow rates of lubricant crossing all faces of each computation cell and the corresponding local liquid fraction at the ruptured film region. This is very suitable for computing flow rates in places such as groove edges (something vital for analyzing feed conditions) and for use in ruptured film region thermal models based on effective length concepts such as those described in [4].

The velocity field must also be computed, as it affects the convective and the dissipative terms of the energy equation. The expressions for the circumferential and axial components of the velocity are the sum of the Poiseuille and Couette components for variable viscosity [29]:

$$\begin{cases} u_x = \frac{\partial p}{\partial x} \left(F_4 - \frac{F_1 F_5}{F_0} \right) + U \frac{F_5}{F_0} \\ u_z = \frac{\partial p}{\partial z} \left(F_4 - \frac{F_1 F_5}{F_0} \right) \end{cases} \quad \text{with} \quad \begin{cases} F_4 = \int_0^y \frac{\lambda}{\mu_l} d\lambda \\ F_5 = \int_0^y \frac{1}{\mu_l} d\lambda \end{cases}$$
(3)

being λ a dummy variable of *y*. The radial velocity u_y is obtained from the solution of the flow continuity equation computed solely for the liquid portion of the flow, which must be affected by the local liquid fraction, θ' :

$$\frac{\partial(\theta' u_x)}{\partial x} + \frac{\partial(\theta' u_y)}{\partial y} + \frac{\partial(\theta' u_z)}{\partial z} = 0$$
(4)

2.2 Thermal Model

The thermal problem is coupled with the flow problem in the sense that viscous dissipation depends on velocity gradients, while the pressure and velocity fields will depend on viscosity, which is temperature dependent.

There are basically three calculation domains, as depicted in Fig. 3: the Fluid Domain, where the Energy equation is solved; the Bush Body domain, where the Laplace equation, which governs conductive heat transfer, is solved. Finally there are the groove regions, where the Reynolds equation is not applicable (thin film condition is not valid). In this latter domain only mass and energy balances are performed. The various domain interfaces are dealt with specific boundary conditions, as depicted in Fig. 3.



Fig. 3 – Outline of the calculation domains and boundary conditions used in the thermal model

Some of the simplifying assumptions include: absence of axial temperature gradients (calculations are performed in the midplane only); the circumferential and axial diffusive terms may be neglected when compared with the corresponding convective terms (high Peclet number), which leads to purely radial conductive heat transfer; Only dissipative terms based on transverse gradients are relevant; The bearing is perfectly aligned – i.e. axial symmetry is assumed.

Fluid domain

The aforementioned assumptions lead to the following simplified form of the energy equation at the midplane of the bearing [29]:



 $(\rho c_p)_{eq}$ and K_{eq} are the properties (density, specific heat and thermal conductivity) of the lubricant or the equivalent properties or the lubricant streamers plus gaseous cavities at the ruptured film region. These will depend on the specific modelling of the ruptured film region. It is common to use the "Effective Length" concept to model the ruptured film region [4]. In fact, if both the lubricant streamers and the gaseous cavities are attached to the bush and shaft surfaces and considering heat transfer to occur radially and in parallel through liquid and gaseous streamers, it may be proved that the equivalent physical properties of the liquid plus gas mixture will be an average of the liquid and gas properties weighted by their corresponding fraction in the mixture, with a particularity found by the authors in which the density and specific heat should be treated as a group, as seen in (1). The effective length of lubricant, \overline{EL} , easily computed by integrating the fluid fraction along the relevant section. The equivalent properties will therefore be the following:

$$\begin{cases} \left(\rho C_{p}\right)_{eq} = \overline{EL} \cdot \rho_{l} c_{p_{l}} + \left(1 - \overline{EL}\right) \cdot \rho_{g} C_{p_{g}} \\ K_{eq} = \overline{EL} \cdot K_{l} + \left(1 - \overline{EL}\right) \cdot K_{g} \\ \mu_{eq} = \overline{EL} \cdot \mu_{l} + \left(1 - \overline{EL}\right) \cdot \mu_{g} \end{cases}$$
(6)

It is important to acknowledge that these equivalent properties (namely the equivalent viscosity) will only be valid for the thermal calculations (they have been derived based on the energy equation). The properties used for the pressure and flow calculations will be solely based on those of the liquid portion of the flow.

There is experimental evidence that in the ruptured film region not all the lubricant flows along streamers that are attached to both the shaft and bush surfaces. In reality, a portion of it is attached solely to the shaft surface forming an adhered layer to this surface [31]. This will affect heat transfer since no velocity gradients (and therefore no heat dissipation) will be present for that portion of the lubricant. Some authors have taken this phenomenon into account [4], although within the scope of a simplified model.



Fig. 4 - Outline comparison between the Effective Length and the modified Effective Length thermal models of the ruptured film region proposed in the present work.

The following expressions for the equivalent properties for thermal calculations, which will vary according to the radial position in the film (whether in the layer region or the streamer-only region) have been derived:

Streamer-only region
$$(0 \le \eta < 1 - \overline{e}_s(\alpha))$$

$$\begin{cases} \left(\rho C_p\right)_{eq} = \overline{EL}_m \cdot \rho_l c_{p_l} + \left(1 - \overline{EL}_m\right) \cdot \rho_g C_{p_g} \\ K_{eq} = \overline{EL}_m \cdot K_l + \left(1 - \overline{EL}_m\right) \cdot K_g \\ \mu_{eq} = \overline{EL}_m \cdot \mu_l + \left(1 - \overline{EL}_m\right) \cdot \mu_g \end{cases}$$

$$\begin{cases} \left(\rho C_p\right)_{eq} = \rho_l c_{p_l} \\ K_{eq} = K_l \\ \mu_{eq} = \overline{EL}_m \cdot \mu_l \end{cases}$$

$$(7)$$

With \overline{EL}_m being the corrected Effective Length of lubricant, which corrects \overline{EL} in order to reflect the portion of lubricant which has been taken out of streamer flow (Couette flow) and allocated to the shaft adhered layer (uniform flow). $\overline{e}_s(\alpha)$ is the fraction of the bearing gap occupied by the lubricant layer at a given circumferential position α , calculated by continuity from its initial value at the rupture front, \overline{e}_{s0} , and the variation of the local film height, $\overline{h}(\alpha)$:

$$\overline{EL}_m = \frac{\overline{EL} - 2\overline{e}_s(\alpha)}{1 - 2\overline{e}_s(\alpha)} \qquad \overline{e}_s(\alpha) = \overline{e}_{s0} \cdot \frac{\overline{h}(\alpha_{rupt})}{\overline{h}(\alpha)}$$
(8)

It may be easily deduced that if all the lubricant will flow adhered to the shaft with no streamers present ($_{EL_m=0}$), the fraction of the bearing gap occupied by the lubricant layer will be at the best 0.5 (the linear profile of the Couette flow of the streamers will be converted into a uniform velocity profile possessing the speed of the shaft) and no heat dissipation will occur. Again, the existence of this shaft-adhered layer has been considered only for the thermal model. The computation of cell flow rates which is the basis for the pressure field calculation relies on the assumption that in the ruptured film region the lubricant flows solely along streamers attached both to the bush and the shaft surfaces. The energy equation is solved through a method proposed by Boncompain et al [3], which consists in solving the energy equation as an initial value problem in the circumferential direction. This may be done as long as the circumferential velocity component is positive. However, if a region with negative speed exists, then this solution scheme may still be applied using the domain separation iterative approach, where calculations are performed successively in the two separate speed domains (positive and negative) as an initial value problem and in the direction of the flow. The results of one domain will be used as a boundary/initial conditions for the other one.

Bush body domain

The conductive heat transfer across the bush body is solved through the Laplace Equation for cylindrical coordinates [29]:

$$\frac{\partial^2 T_b}{\partial r^2} + \frac{1}{r} \frac{\partial T_b}{\partial r} + \frac{1}{r^2} \frac{\partial^2 T_b}{\partial \alpha^2} = 0$$
(9)

This equation is elliptical and may be solved iteratively through the successive over-relaxation method. Once again, no axial flux is considered to occur, so the terms in the *z* direction have vanished.

Groove regions

A suitable thermal modelling of the phenomena taking place within groove regions and their surroundings is vital when analyzing the role of feeding conditions. However, within groove regions (recall Fig. 3) the thin film assumption ($c_r \ll r$) which is the basis for the Reynolds equation, is no longer valid. A CFD approach could be used, but since this calculation would have to be repeated in each iteration at the expense of massive computation time, a detailed mass and energy balance becomes more appropriate in the scope of the present work.

The aim of this balance is to estimate the temperature of the inlet section of the bearing land located downstream of this groove (also called the leading edge of the groove). This temperature will be the initial condition to be supplied for the resolution of the energy equation at the fluid domain located downstream of that grove. In the present work this balance takes into account: all major inbound and outbound heat fluxes due to lubricant flow across the boundaries of the groove region; the heat fluxes due to forced convection between the bush body and the inner groove lubricant; the influence of the actual groove dimensions, namely the groove length ratio, *a/b*; the occurrence of fresh oil backflow (upstream of the groove) and reverse flow (downstream of the groove); the influence of the occurrence of negative feeding flow rate (hot oil reflux) in one of the groove). An outline of the heat fluxes crossing the boundaries of the groove region is presented in Fig. 5(a).

But the thermal balance is not sufficient, by itself, to determine the several average temperatures corresponding to the various outward lubricant flows and the inner groove temperature, \overline{T}_{gr} . Regardless of the mixing efficiency, it seemed reasonable to assume that the backflow temperature, \overline{T}_{bkf} and the axial flow temperature \overline{T}_{axial} will be similar to \overline{T}_{gr} . However, the average leading edge temperature will depend on the degree of mixing between the hot oil coming from upstream and reaching the trailing edge of the groove at an average temperature \overline{T}_{te} and the inner groove oil at temperature \overline{T}_{gr} . An outline of the mixing process is sketched in Fig. 5 (b).



Fig. 5 – (a) Heat fluxes across the boundaries of the groove region in the presence of back flow upstream and reverse flow downstream of the groove; (b) Outline of the thermal mixing model within the groove region.

A mixing coefficient, *c_{mix}* was introduced:

$$\overline{T}_{gr} = c_{mix}\overline{T}_{le} + (1 - c_{mix})\overline{T}_{f}$$
(10)

where c_{mix} may vary between two theoretical limits:

- Perfect mix (c_{mix} =1), with the oil reaching the groove from upstream perfectly mixing with the inner groove oil, in which case all four outward temperatures will be virtually identical, that is, $\overline{T}_{er} = \overline{T}_{le}$.

- No mixing at all (c_{mix} =0), where all recirculated hot oil is re-fed to the next bearing land without the occurrence of any heat exchange with the groove oil, that is, the groove oil will be solely affected by the lubricant feeding temperature and thus, $\overline{T}_{gr} = \overline{T}_{f}$.

The mixing efficiency within a groove is likely to depend on several factors and is out of the scope of this work. A fixed value of 0.1 has been selected after a brief parametric study. This small mixing coefficient is in agreement with the CFD study of Kosasih and Tieu [32], which concluded that although the flows occurring within the groove interior are highly recirculating, they have almost negligible effects on thermal mixing.

It is now possible to derive the leading edge temperature, \bar{T}_{le} , from the thermal balance expressed in Fig. 5:

$$\overline{T}_{le} = \frac{\overline{q}_{te}^{+} + \overline{q}_{H} + \overline{Q}_{f}\overline{T}_{f} + \left|\overline{q}_{rvf}\right| - \left(\left|\overline{Q}_{axial}\right| + \left|\overline{Q}_{bkf}\right|\right)(1 - c_{mix})\overline{T}_{f}}{c_{mix}\left|\overline{Q}_{axial}\right| + c_{mix}\left|\overline{Q}_{bkf}\right| + \overline{Q}_{le}^{+}}$$
(11)

The present thermal approach is 2D, made in the midplane of the bearing, and in fact several studies [23][33] have confirmed that in most cases the axial temperature gradients along the bearing length are indeed negligible and what happens at the midplane is representative of the whole bearing length. However, if the grooves have a small length, the midplane thermal analysis made above should be corrected in order to reflect, on average, the whole bearing length, and not just the grooved length. With the knowledge of the velocity field it is possible to determine the average inlet section temperature, \bar{T}_{is} , which reflects more accurately the effective temperature of the whole bearing length. This temperature will be calculated from a balance that includes not just the flow rate and the temperature of the lubricant leaving the groove, \bar{T}_{le} , but also the flow rate and temperature of the oil flowing at the portion of the bearing length which is not covered by the groove, \bar{T}_{le_side} , as depicted in Fig. 6.



Fig. 6 - Outline of the thermal balance carried out to determine the average inlet section temperature, \overline{T}_{is} , which incorporates the influence of the groove length ratio, a/b

Thus, the energy and mass balances performed to the groove and the dotted control volume depicted in Fig. 6 yields the following expressions:

$$\overline{T}_{is} = \frac{\overline{Q}_{le}^{+}\overline{T}_{le}^{+} + \overline{Q}_{le_side}\overline{T}_{le_side}}{\overline{Q}_{le}^{+} + \overline{Q}_{le_side}} \qquad \text{with} \qquad \overline{T}_{le_side} = \frac{\overline{Q}_{te_side}\overline{T}_{te} + \overline{Q}_{axial}\overline{T}_{axial}}{\overline{Q}_{te_side} + \overline{Q}_{axial}}$$
(12)

Conditions at the interfaces

The conditions set at the various interfaces, as already outlined in Fig. 3, are presented in continuation.

At the shaft-film interface a condition of no net heat flux was imposed. This may be considered as a midterm between situations where the shaft acts a heat sink or a heart source. Also, the shaft surface temperature is considered to be constant, following experimental evidence [33]. These two assumptions are widely accepted and used in the literature [34][35][36].

At the bush-film interface, the temperature and heat flux continuity are applied, while natural and forced convection conditions are used at the bush-ambient interface and at the inner groove walls, respectively. It is worth noting that the accounting for convective heat transfer at the groove walls must be done both in the bush body conduction calculation and in the groove thermal balance. Otherwise, a virtual heat source/sink will exist due to this. A higher than usual value of 750W/m²K was chosen for H_{gr} . Such value appears to be in better agreement with the highly recirculating flow found within groove regions [32][37] and indeed this allowed to replicate the strong temperature fade found experimentally in the vicinity of grooves [24].

2.3 Numerical procedure

The theoretical model was implemented using the FORTRAN 90/95 programming language. The global algorithm implements the following sequence: Imposition/update of eccentricity and attitude angle, and calculation of the pressure field until attitude angle convergence is achieved; solution of the

thermal problem within the fluid domain, followed by the groove energy balance (and repeated for each bearing land); solving of the Laplace equation; updating of the bush-film interface temperature and, if it has not converged, going back to the beginning of the thermal algorithm; calculation of the shaft temperature based on the no net heat flux condition and, if this temperature and T_{is} have not converged, going back to the beginning of the thermal algorithm; calculation of the load capacity and, if load has not converged, going back to the beginning of the algorithm, otherwise, conclusion of the calculation.

The selection of the mesh parameters and convergence criteria was based on a comprehensive parametric study in order to obtain a good compromise between accuracy and processing time. The approach relied on the use of refined meshes in order to detect more subtle phenomena such as reverse flow. The two cells in the vicinity of the groove edges were refined by a factor of six after the first few iterations. Taking into account the small randomness found in the results (even at very high eccentricities), along with the small differences found between the results obtained with the final mesh and the finest meshes tested, the present algorithm seems to be particularly robust.

2.4 Model validation

There is a lack of models presenting a thorough validation with experimental data, something which compromises the reliability of the results obtained. Such was tried with the present model. A comparison against the results of Ferron et al [38], which are extensively used in model validation, can be seen in Fig. 7.



Fig. 7 – Comparison between the present analysis and experimental data [38] under two different conditions, for (a) inner bush surface temperature profile (b) pressure profile at the midplane of the bearing and (c) eccentricity ratio and flow rate.

A very good theoretical-experimental correlation is obtained for maximum temperature (T_{max} .Fig. 7a) with differences of around 1°C, within the error of temperature measurements. The temperature trend is fairly well predicted for both cases except in the region immediately downstream of the groove, as seen in Fig. 7a. This may have happened due to the fact that, while the experimental values were measured at the midplane of the bearing, the theoretical approach performs averaged thermal calculations over the whole section. The hydrodynamic pressure profiles displayed in Fig. 7b are within the experimental error margin, the same happening with the estimation of eccentricity ratio. Flow rate (Fig. 7c) has been slightly overestimated.

Fig. 8 presents the predicted temperature profiles against experimental results obtained by the authors [39]. Again, it should be highlighted that the temperature correlation in the region immediately downstream of grooves is not satisfactory since the predicted values are representative of the whole section and not just of the midplane, as measured experimentally.

The suitability of the predictions may be better acknowledged by observing the peak temperatures occurring in each one of the bearing lands and also on the shaft surface (see Fig. 9). In fact, seldom has the temperature trend in the ruptured film region of twin groove journal bearings been accurately predicted. The present model seems to accomplish this rather satisfactorily for the generality of the tests, as seen in Fig. 9.



Fig. 8 - Comparison between the present analysis and experimental temperature profiles at the midplane of the inner bush surface of the bearing for four different shaft speeds and an applied load of (a) 2kN, (b) 6kN and (c) 10kN; (d) Total flow rate (Pf=140kPa) [39].

Fig. 10 depicts the comparison of the predictions of the present analysis against experimental results from another paper by the group [24], where the feeding pressure varied threefold from 70 to 210kPa. The same good correlation may be observed (something positive for the present analysis, in the scope of the assessment of feeding conditions), except for the flow rate, which was substantially underestimated.



Fig. 9 - Comparison between theory and experiment, for several loads and shaft speeds, of (a) Shaft surface temperature, (b) maximum bush temperature, (c) maximum bush temperature at the loaded (lower) land and (d) maximum bush temperature at the unloaded (upper) land of the bearing (Pf=140kPa);[39]

Unfortunately, the crude underestimation of the flow rate in twin groove journal bearings analyses is a commonly known issue, still unresolved and found in numerous reference works [8][9][11][34] and even popular bearing design tools [40]. This might be linked with the intrinsic limitations in the modelling of flow in grooves located in the midst of the ruptured film region [41] and requires further investigation. Nonetheless, this general underestimation does not seem to decisively affect the maximum temperature of the bush, which has been fairly well predicted in most cases.



Fig. 10 - Comparison between theory and experiment, for several loads and feeding pressures, of (a) Shaft surface temperature, (b) maximum bush temperature, (c) maximum bush temperature at the loaded (lower) land, (d) maximum bush temperature at the unloaded (upper) land of the bearing and (e) flow rate. [24]

Therefore, the current model seems apt to be used in the analysis of the performance of single and twin groove hydrodynamic journal bearings with realistic feeding conditions.

3 Analysis of lubricant feeding conditions

In continuation, the lubricant feed conditions such as the lubricant feeding pressure and temperature, the groove length ratio (a/b), the groove width ratio (w/d) and the number of grooves (single/twin) are analyzed for a bearing geometry which is roughly the one used in [24] and [39]. This analysis aims to assess how these parameters may affect bearing performance and how they can be optimized to achieve a reduction in friction without sacrificing the integrity of the system. The input parameters used in the analysis are presented in Table 1 and Table 2.

Table 1 – Geometric characteristics, Operating a	and
feeding conditions used in the analysis.	

Geometric characteristics		Units	Default Value / Range
 Inner bush diameter (nominal) 	d	mm	100
 Outer Bush diameter 	D	mm	200
- Bush width / diameter ratio	b/d		0.8
- Groove number			1 ; 2
- Groove angle with load line			+90° ; ±90°
- Groove lenght / bush length ratio	a/b		0.30; 0.6; 0.875
- Groove width / diam. ratio	w/d		0.18 ; 0.16
 Bearing radial clearance (at 20°C) 	Cr	μm	75
Operating and feeding conditions			
- Rotational speed	N	krpm	1; 3 ; 5
 Specific load range (approx). 	Ws	MPa	0.1 - 10
- Oil feeding pressure	P_f	kPa	0; 50; 100 ; 200; 300
- Oil feeding temperature	T _f	°C	30; 40 ; 50; 60

Table 2 – Lubricant properties used in the analysis

Lubricant properties			Value
- T1		ы	40
- T2		°C	70
 Dynamic viscosity @ T1 	μ_{T1}	Pa.s	0.0293
- Dynamic viscosity @ T2	μ_{T2}	Pa.s	0.0111
- Specific Heat	C_p	J/kgK	2000
- Density	ρ	kg/m ³	870
 Thermal conductivity 	k	W/mK	0.13

3.1 Feeding Pressure (P_f)

Feeding pressure (P_f) is one of the feeding parameters which is frequently neglected in modelling as its analysis requires a realistic treatment of groove geometry and a mass conserving algorithm with film rupture and regeneration front estimation. Nonetheless, it affects deeply the thermal behaviour of the bearing due to its cooling effect. Also, if the bearing is too starved, contact might occur, while if there is lubricant excess there will be increased power loss.

Fig. 11 shows the effect of P_f on the total flow rate and on the flow rate through each groove, for a broad range of specific loads.

While total flow rate follows a well known trend with load, the flow rates through each groove show rather dissimilar or even opposite trends. This phenomenon has already been observed experimentally and explained in several of the authors' publications [25][26][28][42][27], including the curious phenomenon of negative flow rate occurring at high loads in the +90° groove, the groove which serves the loaded land of the bearing (also called the upstream groove). This means that this groove starts acting as a lubricant sink instead of a lubricant source for the bearing. This behaviour is caused by the excessive closeness between the groove and the strong hydrodynamic pressures, which eventually exceed feeding pressure, reversing pressure gradients and thus the direction of the lubricant flow. This phenomenon occurs under heavily loaded conditions and thus raises the seizure risk. In fact, the lubricant is being retrieved just upstream of the active bearing region, where it would

be most needed. And this lubricant starvation might happen inadvertently since the total flow rate (the parameter which is measured in industrial applications, at best) will indicate a seemingly normal feeding flow rate value. Here it can be seen that the increase of P_f plays an important role in preventing this phenomenon as seen in Fig. 11b.



Fig. 11- Influence of specific load and lubricant feeding pressure on (a) total flow rate, (b)+90° groove flow rate and (c) -90° groove flow rate (N=3000rpm).

The effect which P_f has on power loss, minimum film thickness (h_{min}) and maximum bush temperature (T_{max}) may be observed in Fig. 12a, b and c, respectively. Indeed, when increasing P_f h_{min} increases, something which is generally positive. However, this is obtained at the expense of an increase in power loss from 9% to 30% for a threefold increase in P_f . This is due to the fact that a higher flow rate of oil will reduce the average oil temperature and thus increase viscosity and viscous drag. Also the full film region will be somewhat broader, and so the viscous drag will further increase.

By looking at Fig. 12c it can be seen that T_{max} is not minimized in the presence of the lowest loads but rather slightly higher values of this parameter. This is due to the fact that lightly loaded bearings typically display a low rate of lubricant leakage/renewal, as observed experimentally [24]. However, it can be observed that an increase in P_{f} might indeed reduce T_{max} significantly for light load conditions.



Fig. 12 - Temperature profiles at the midplane of the inner bush surface for several feeding pressures and (a) Ws=0.1MPa, (b) Ws=1MPa and (c) Ws=8MPa. (N=3000rpm).

Fig. 13 displays the effect which P_f has on the inner bush surface temperature profile for a light, a medium and a heavy load. It can be seen that T_{max} is higher for Ws=0.1 than for Ws=1MPa under low P_f (100kPa). Not so when increasing P_f to 300kPa.



Fig. 13 – Influence of feeding pressure on (a) minimum film thickness and (b) power loss.

The effect which P_f has on eliminating negative flow rate can be observed in Fig. 13c in the unloaded land of the bearing. Indeed, when P_f =100kPa it can be seen that the +90° (upstream) groove provides no cooling to the system, that is, no fresh oil is fed to the bearing gap since flow rate through this groove is negative (recall flow rate plot in Fig. 11b). Once increasing P_f from 100kPa to 200 kPa the groove temperature drops abruptly from 64°C to 42°C, a value close to the feeding temperature (40°C). This indicates that the flow rate has started to be positive.

3.2 Feeding Temperature (T_f)

Lubricant viscosity, which strongly depends on temperature, is the parameter responsible for hydrodynamic pressure generation within the fluid. Therefore, the variation of T_f is likely to exert a strong influence not only on the temperature field, the power loss and the flow patterns, but also on minimum film thickness and ultimately on the load carrying capacity of the bearing.



Fig. 14 - Influence of specific load / eccentricity and lubricant feeding pressure on (a)/(d) total flow rate, (b)/(e)+90° groove flow rate and (c)/(f) -90° groove flow rate.

On one hand, if T_f is too low, the viscosity of the lubricant will be high and an excessive power loss will exist. On the other hand, if T_f is too high there will be no sufficient load carrying capacity, with risk of

contact. Besides, the thermal crowning of surfaces due to thermal distortion will further raise the risk of seizure.

Fig. 14 displays the same flow rate data but now as a function of two different variables, specific load and eccentricity ratio. Within the lower range of specific loads (below 2MPa) the flow rate at the +90° groove increases when T_f rises, indicating the fall on viscosity suffered by the hotter lubricant. However, the opposite occurs for higher specific load values. The reason for this lies in the rise in eccentricity ratio which is much more pronounced for higher loads. In fact, when analyzing this same data, but seen as a function of eccentricity ratio (see Fig. 14d,e and f) it is apparent that this latter parameter plays a decisive role in flow rates. For instance, negative flow rate seems to start occurring for an eccentricity ratio around 0.9 irrespective of the value of T_f . This corresponds to between 8 and 10MPa specific loads, depending on T_f .

The increase of eccentricity (or the decrease in minimum film thickness) with increasing T_f may be observed in Fig. 15a, while the effect of T_f on the maximum temperature and shaft surface temperature as well as power loss is displayed in Fig. 15b and c, respectively. As expected, the viscosity reduction caused by the increase in T_f with temperature yielded a decrease of the viscous dissipation and, therefore, of the power loss. For instance, a 30% reduction in power loss may be obtained when increasing T_f from 30°C to 60°C, for a specific load around 1MPa.



Fig. 15 – (a) Influence of feeding temperature on (a) minimum film thickness, (b) maximum bush temperature and shaft surface temperature and (c) power loss as a function of specific load (N=3000rpm).

A comparison between the temperature profiles for T_f of 30°C and 60°C is presented in Fig. 16 for a wide range of specific loads.



Fig. 16 - Temperature profile at the midplane of the inner bush surface for several specific loads and (a) Tf=30° and (b) Tf=60°C

In accordance with the experimental observations [24] [26], the increase in T_{max} is always much less than the corresponding increase in T_f . In this case, a 30°C increase in T_f yielded increases of 7°C for the lowest load case ($W_s = 0.1$ MPa) and 15°C for the highest ($W_s = 10$ MPa). Another interesting fact is that the increase of T_f triggered the appearance of the hot oil reflux phenomenon in the test with $W_s = 8$ MPa, as seen in Fig. 16b..

3.3 Groove Length Ratio (*a/b*)

Despite the present thermal model being 2D (performed in the bearing midplane only), the pressure and flow calculations are performed in the whole 3D fluid domain and the thermal balances of the groove regions (the places where axial temperature differences might be significant) have incorporated the influence of a/b, as noted when describing the model.

The hydrodynamic pressure fields obtained for two bearings with dissimilar a/b ratios (0.3 and 0.875), along with the delimitation of the regions of full and ruptured film are presented in Fig. 17a and b, respectively. The two different groove geometries can be distinguished by observing their constant pressure plateaus (P= P_t) in groove regions. In the vicinity of the +90° groove and in the region downstream of it, it can be seen that there are some differences between the pressure fields obtained for the two cases: In the case of the large grooved bearing, there is hydrodynamic pressure generation immediately downstream of this groove extending to the whole axial length of the bearing. On the contrary, in the case of the small grooved bearing, the pressure build-up zone only extends to the whole bearing length further downstream.



Fig. 17 - Influence of groove length ratio on (a) the hydrodynamic pressure field and (b) extension of full film and ruptured film regions (Ws=1.1MPa)

The lower extension of the full film region caused by decreasing groove length is translated into a lower carrying capacity, that is, a higher eccentricity for a given applied load, as confirmed by inspecting the eccentricity ratio plot in Fig. 18a. The effect of a/b upon the flow rates can be observed in Fig. 18b. As expected, the total flow rate increases with the increase of a/b since the edges of the groove are farther from the exterior and so there is increased resistance to oil leakage. In this case, total flow rate more than doubled when increasing a/b from 0.3 to 0.875. If lower a/b values tend to decrease flow rate, then it is natural that T_{max} and T_{shaft} should increase due to the lower cooling power provided by the lubricant flux, as confirmed in Fig. 18c.



Fig. 18 - Influence of the groove length ratio on (a) the global and partial flow rates in each groove, (b) shaft temperature and maximum bush temperature and (c) power loss, for varying Specific load

Fig. 18d shows a positive effect of decreasing groove length, which is the substantial cut in the power loss obtained (around 35% in the whole load range) when decreasing *a/b* from the highest to the lowest value tested. It should be noted, however, that localized lubricant feed might originate dry regions in the bearing gap (namely close to edges) and promote uneven thermal distortion. If these phenomena are combined with some misalignment, localized contact might occur. So, reducing groove length in order to obtain reduced power loss is a solution which should be carefully assessed.

3.4 Groove Width Ratio (*w/d*)

The increase of the circumferential extension of groove, also called the groove width, *w*, will affect bearing performance in various ways as it reduces the extension of the bush lands and therefore, there will be a loss of load supporting area and load capacity, especially if the grooves are close to the pressure buildup region.

The total and partial flow rates in each groove are presented in Fig. 19a for the two w/d values tested. Curiously, the total flow rate was not significantly affected by the changes in w/d. However, when increasing w/d, the flow rate at the +90° groove suffered a strong decrease, especially for specific loads higher than 0.3MPa, while the opposite happened in the -90° groove. As a consequence, the critical W_s for the occurrence of hot oil reflux was lowered from around 8MPa to about 4MPa when increasing w/d.



Fig. 19 - Influence of groove width ratio on the temperature profiles at the midplane of the inner bush surface for (a) Ws=0.5MPa, (b) Ws=1.1MPa and (c) Ws=6MPa.

Fig. 19b,c,d shows the influence of *w* in the inner bush surface temperature profiles of lightly to heavily loaded bearings. On one hand, the general lowering of the temperature level is apparent in these plots and also in Fig. 20a, which depicts T_{max} and T_{shaft} . Curiously, and unlike what happens with other feeding conditions, this temperature decrease happens simultaneously with a reduction in power loss despite the increase of the average lubricant viscosity due to temperature lowering. This means that the reduction in power loss should be mainly associated to the reduction of the circumferential extension of the bush lands. Under those conditions, viscous drag will occur in a smaller angular extension, thus reducing the overall drag.



Fig. 20 - Influence of groove width ratio on (a) maximum bush and shaft surface temperature and (b) on power loss.

The reduction of the global temperature level should also be due to a stronger cooling effect of the groove oil by convective heat transfer over a broader groove surface (recall that convective heat transfer inside the groove has been included in the modelling).

Of course, there should be limits to the beneficial effect of increasing w, namely because the area for load support will be reduced when w is increased. Also, the oil reflux phenomenon will be amplified with the pressure build-up zone getting closer to grooves.

3.5 Number of Grooves

The comparison of the performance of single (at $+90^{\circ}$ to the load line) and twin groove ($\pm90^{\circ}$) hydrodynamic journal bearings for the same operating conditions has seldom been made either theoretically or experimentally. The common sense perception that a twin groove bearing will operate at a lower temperature and with a more efficient lubrication than the single groove one still needs to be confirmed. Recently the authors published an experimental work focusing on this issue [27].

Fig. 21a displays the flow rates corresponding to both cases. It is interesting to acknowledge that the total flow rate is nearly the same for the two bearings along the whole load range, something which was already observed in the experimental work. This means that a redistribution of the same flow rate towards two grooves happens instead of an increase of total flow rate.

The effect of groove number on shaft locus may be seen in Fig. 21b, with the attitude angle of the single groove case being higher than that of the twin groove one, especially for low eccentricities. This is a well known characteristic of single groove bearings: the resulting force caused by the hydrostatic pressure in the groove region (the feeding pressure), is not being cancelled by a symmetrical force on the opposite side of the bearing, as it would happen with the twin groove case. Therefore, in the presence of a single groove bearing, the shaft centreline tends to move away from the +90° groove towards the opposite side, thus increasing the attitude angle. Differences in eccentricity for a given load are more easily apprehended in a separate chart as a function of specific load, as seen in Fig. 21c. According to this plot it seems that twin groove bearings operate at a lower eccentricity, thus farther from contact than single groove ones. The reason for this seems to be that the temperature level of twin groove bearings is lower than that of single groove bearings, thus operating with higher oil viscosities, as seen further ahead.



Fig. 21 - Influence of the number of grooves on (a) the lubricant flow rates and (b) on shaft locus and (c) on eccentricity ratio.

Fig. 23 displays the temperature field in the midplane of the bearing for both groove configurations and a specific load of 3.9MPa. Fig. 23a shows the inner bush surface temperature only, while Fig. 23b pertains the whole fluid (lubricant) and solid (bush) domains. The differences (namely, 12°C in T_{max}) are quite significant. This can be better understood by taking into account the following chain of effects: the less efficient cooling of the single groove configuration causes a higher fluid temperature, which in turn causes a loss in lubricant viscosity, which originates higher eccentricity, thus aggravating the temperature excess.

This dramatic difference of the temperature levels of the two groove configurations with increasing load can be further observed in Fig. 23a, which displays the evolution of T_{max} and T_{shaft} with W_s . Here it can be seen that the number of grooves also affects significantly T_{shaft} , with differences in T_{max} and T_{shaft} being as high as 25°C and 30°C, respectively.



Fig. 22 - Influence of the number of grooves on (a) the temperature profile at the midplane of the inner bush surface and (b) the midplane temperature field of the fluid domain and of the bush body domain (Ws=3.9MPa).

These factors also deserve to be analyzed as a function of eccentricity ratio (b). This can help isolating the temperature effects of the two factors which were pointed out as being responsible for the temperature rising (ineffective cooling and eccentricity increase). In fact, if eccentricity is kept constant, the differences in T_{max} and T_{shaft} are exclusively linked with the cooling efficiency. It can be seen that even cancelling the effect of eccentricity variation on temperature there are still significant differences between the two cases (as much as 15 and 20°C for T_{max} and T_{shaft} , respectively).



Fig. 23 - Influence of the number of grooves on the maximum bush temperature and the shaft surface temperature as a function of (a) specific load and (b) eccentricity ratio. (c) Influence of the number of grooves in power loss.

The number of grooves also seems to significantly affect the power loss, as seen in Fig. 23c. The reduction in this parameter, as high as 25% when eliminating the -90° groove, seems to be associated to the loss of viscosity (and therefore, of heat generation by viscous dissipation) suffered by the hotter oil.

As a concluding remark, it is worth noting that the results just presented seem to indicate that the addition of the -90° groove causes the decrease of temperature level and eccentricity especially for high loads, at the expense of a higher power loss. However, some caution should be taken with the generalization of these results. In fact, it has been observed before that the present model tends to over-predict the +90° groove flow rate in the high eccentricity range for the case of the twin groove bearing. This over-estimation might be affecting significantly the predictions in some cases: if in reality

the +90° groove flow rate is much smaller than predicted, starvation problems might start appearing and become dominant.

The overestimation of the +90° groove flow rate is also the reason why the model also tends to overpredict the critical load at which hot oil reflux problems start occurring. In the case studied, this phenomenon was predicted to occur for specific loads above 8MPa (Fig. 21a). This problem, which is deleterious for bearing performance, namely for eccentricity, appears only in multi groove bearings and has been barely detected in the analysis for these conditions.

Therefore, it is possible that in some situations the oil starvation caused by the splitting of the flow by two grooves instead of one might become a critical effect, making the twin groove bearing a poorer choice than the single groove bearing. In fact, this seems to be the case with the experimental results presented by the authors in [25]and [26]. The incorporation of a 3D thermal analysis, along with a more realistic estimation of the thermal and mechanical deformations of the bodies might enable a better prediction of bearing performance in such cases.

4 Conclusions

A Thermohydrodynamic (THD) model for the analysis of hydrodynamic journal bearings with realistic lubricant feed conditions has been proposed and used to assess the role of lubricant feeding conditions on the performance improvement and friction reduction of hydrodynamic journal bearings.

The model is based on the simultaneous solution of the Generalized Reynolds Equation through a mass conserving algorithm and the Energy Equation within the fluid domain, as well as the Laplace equation within the bush body domain.

Care was taken in order to realistically incorporate lubricant feeding conditions into the analysis: the real dimensions of the grooves were considered in pressure and flow calculations. Models for the ruptured film region and the lubricant mixing at the grooves were derived, while a simplified thermoelastic model was deployed. A thorough validation of the theoretical model was successfully performed and the robustness of the model for a wide range of input conditions was confirmed.

The main factors which can affect the lubricant feeding - feeding pressure and temperature, groove length ratio, groove width ratio and number of grooves (single/twin) were analyzed for a broad range of specific loads, extended well beyond the range of practical applications. It was found that:

- In general, the same trends and tendencies which are experimentally observed were predicted by the model. Despite the limitations pointed out in the validation, the results obtained appear to be globally coherent, physically plausible, and with small randomness.
- The feeding pressure proved to be a critical factor in reducing the temperature level of the bearing and in preventing the occurrence of hot oil reflux, even if it was at the expense of a higher power loss;
- The increase of the lubricant feeding temperature proved to be beneficial under low loads (it decreased power loss) but especially dangerous under high loads as it strongly increases the eccentricity, *T_{max}*, *P_{max}*, and the thermal and mechanical distortions, while lowering the critical load for which hot oil reflux starts occurring.
- The use of smaller length grooves (lower *a/b*) yielded decreases in power loss around 35%, but at the expense of a less efficient bearing cooling, a smaller extension of complete lubricant film and thus a lower load carrying capacity. If excessive, the narrower range of the lubricant film, combined with the stronger thermal crowning of surfaces due to cooling asymmetries might inclusively cause local contact.
- The increase of *w/d* induced a decrease in power loss and maximum bush temperature without a significant decrease in load carrying capacity. However, the critical load for which hot oil reflux starts occurring was lowered.
- When comparing single groove (+90° to the load line) and twin groove (±90° to the load line) it was found that the addition of the -90° groove caused a decrease in the temperature level and in eccentricity, especially in the higher load range. There are also negative effects of adding an extra groove, which are the increase in power loss and the appearance of hot oil reflux for high eccentricities.

It may be stated with confidence that the lubricant feeding conditions play a vital role in the performance of hydrodynamic journal bearings and therefore should not be neglected in bearing analyses. Their optimization can result in substantial energy savings and reduced environmental impact. Truly, in some cases the feeding conditions might even dictate the occurrence or the avoidance of bearing seizure in ways that conventional bearing design tools are not able to anticipate.

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