Numerical Simulation of Continuous RC Slabs Strengthened using NSM Technique

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ABSTRACT: The effectiveness of the Near Surface Mounted (NSM) technique for the increase of the flexural resistance of reinforced concrete (RC) beams and slabs was already well proved. The NSM technique is especially adapted to increase the negative bending moments of continuous (two or more spans) RC slabs. However, the influence of the NSM strengthening on the moment redistribution capability of RC structures should be investigated. Recently, an exploratory experimental program was conducted to assess the level of moment redistribution that can be obtained in two span RC slabs strengthened with NSM strips for negative bending moments. To help the preparation of an extensive experimental program in this domain, the values of the parameters of a constitutive model, implemented into a FEM-based computer program, were calibrated from the numerical simulation of these tests. The main aspects of the experimental program are presented, the numerical model is briefly described and the numerical simulations are presented and analyzed.

1 INTRODUCTION

When an existing continuous RC structure is strengthened with Fiber Reinforced Polymer (FRP) materials, its ductility and "plastic" rotation capacity may be restricted or even extinct, due to, principally, the linear-elastic stress-strain response of the FRP up to its brittle failure (Arduini et al. 1997, Casadei et al. 2003). As flexural members retrofitted with externally bonded reinforcing (EBR) technique tend to fail by brittle premature plate debonding, well before the FRP tensile strength capacity is reached, the ductility, particularly the plastic rotation capacity, is severely reduced, which decreases the available degree of moment redistribution (Oehlers et al. 2004a). The tests of El-Refaie et al. (2003a, 2003b), Ashour et al. (2004) and Oehlers (2004a) show that, in general, premature debonding of the EBR strengthening systesm is the dominant failure mechanism. However, according to the approach used by these authors to quantify the moment redistribution, significant moment redistribution was obtained in the tests (El-Refaie et al. 2003a, Oehlers et al. 2004a/2004b, Oehlers et al. 2006, Liu et al. 2006a), which contradicts the existing design guidelines (Concrete Societv 2000, fib 2001, ACI 2002) that suggest that moment redistribution should not be allowed for RC members strengthened with EBR technique.

On the other hand, tests on simply supported RC members strengthened with Near Surface Mounted

(NSM) strips (Hassan & Rizkalla 2003, Täljsten et al. 2003, Barros & Fortes 2005, Barros et al. 2006) have shown that NSM strengthening elements debond or fail at much higher relative strain levels than EBR strengthened members are expected to be much more ductile than EBR strengthened members. In addition, NSM strengthening installation procedures are easier and faster to apply than the ones of EBR technique (Täljsten et al. 2003). Therefore, NSM technique is recommended for strengthening negative moment regions, since for this application the NSM technique can be restricted to open slits and fix, with an adhesive, the FRP strips to the concrete substrate.

On the topic of moment redistribution of statically indeterminate RC members strengthened with NSM technique, the first preliminary studies were conducted at the Adelaide University, in Australia (Liu et al. 2006b). A significant amount of moment redistribution was attained with NSM, when compared with EBR technique. With the final purpose of establishing design guidelines for the NSM flexural strengthening of continuous RC structures, an exploratory experimental program was recently conducted (Bonaldo 2008). In this program the level of moment redistribution that can be obtained in two span RC slabs strengthened with NSM strips for negative moments was assessed. To help on the preparation of an extensive experimental program in this domain, the values of the parameters of a constitutive model, implemented into the FEMIX software (Sena-Cruz et al. 2007), a FEM-based computer program, were calibrated from the numerical simulation of these tests. This model is able of simulating the concrete crack initiation and crack propagation, the nonlinear concrete compression behavior, the elastoplastic behavior of steel reinforcements and the elastic-brittle failure behavior of FRP elements. The present work resumes the experimental program (more details can be found in Bonaldo (2008)), and describes and appraises the performance of the numerical model.

2 EXPERIMENTAL PROGRAM

2.1 Slab specimens and strengthening technique

According to CEB-FIB Model Code (1993), the coefficient of moment redistribution, $\delta = M_{red} / M_{elas}$, is defined as the relationship between the moment in the critical section after redistribution (M_{red}) and the elastic moment (M_{elas}) in the same section, calculated according to the theory of elasticity, while $MR = (1 - \delta) \times 100$ is the moment redistribution percentage. To assess the influence of NSM CFRP strips on the moment redistribution ability of continuous RC slabs, an experimental program composed of nine 120×375×5875 mm³ RC two-way slabs was carried out (Fig. 1), three of them were unstrengthened RC slabs forming a control set (SL15, SL30 and SL45), and six slabs were strengthened with CFRP strips according to the NSM technique (SL15s25, SL15s50, SL30s25, SL30s50, SL45s25 and SL45s50). The notation adopted to identify each slab specimen is SLxsy, where SL is the slab strip base, x is the moment redistribution percentage, MR, (15%, 30% or 45%), s means that the slab is strengthened, and y is the increase of negative moment of the slab cross section at its intermediate support (25% or 50%). Steel bars with nominal diameters of 8 mm and 12 mm were used for the longitudinal reinforcement. The concrete cover thickness is about 26 mm.

Due to space limitation, this paper only deals with the series SL15s25, but the entire experimental program is treated in detail by Bonaldo (2008) and all the simulations can be found in Dalfré & Barros (2008).

2.2 Measuring Devices

To measure the deflection of the slabs, six displacement transducers were applied (see Figure 2).



Figure 1. Cross-section dimensions, see also figure 2 (A'_s - top reinforcement; A_s – bottom reinforcement).

The LVDTs 60541 and 18897, positioned at the slab mid-spans, were also used to control the test. Ten electrical resistance strain gages were installed on the internal steel reinforcement at the central support (SG1 to SG7) and under line loads (SG8 to SG10) to measure the strains in the steel reinforcements at critical regions. Six strain gages (SG11 to SG16) were also bonded on concrete surface to determine the maximum concrete compressive strain. Finally, three strain gages were installed at one CFRP strip (SG17, SG18 and SG19) to evaluate the strain variation along the strip.

3 NUMERICAL SIMULATION

3.1 Constitutive laws

According to the present model, a concrete slab is considered a plane shell formulated under the Reissner-Mindlin theory (Barros 1995). In order to simulate the progressive damage induced by concrete cracking and concrete compression nonlinear behavior, the shell element is discretized in layers. Each layer is considered in a state of plane stress.

The incremental strain vector derived from the incremental nodal displacements obtained under the framework of a nonlinear FEM analysis is decomposed in an incremental crack strain vector, $\Delta \underline{\varepsilon}^{cr}$, and an incremental strain vector of the concrete between cracks, $\Delta \underline{\varepsilon}^{co}$. This last vector is decomposed in an elastic reversible part, $\Delta \underline{\varepsilon}^{e}$, and an irreversible or plastic part, $\Delta \underline{\varepsilon}^{p}$, resulting

$$\Delta \underline{\varepsilon} = \Delta \underline{\varepsilon}^{cr} + \Delta \underline{\varepsilon}^{co} = \Delta \underline{\varepsilon}^{cr} + \Delta \underline{\varepsilon}^{e} + \Delta \underline{\varepsilon}^{p} \tag{1}$$

The incremental stress vector can be computed from the incremental elastic strain vector,

$$\Delta \underline{\sigma} = \underline{D}^{co} \Delta \underline{\varepsilon}^{co} \tag{2}$$



Figure 2. Arrangement of displacement transducers and strain gages.

where \underline{D}^{co} is the concrete tangent constitutive matrix,

$$\underline{D}^{co} = \begin{bmatrix} \underline{D}_{mb}^{co} & \underline{\emptyset} \\ \underline{\emptyset} & \underline{D}_{s}^{co} \end{bmatrix}$$
(3)

with \underline{D}_{mb}^{co} and \underline{D}_{s}^{co} being the in-plane and the out-ofplane shear stiffness matrices, respectively. In the present model, concrete behavior is assumed linear elastic in terms of out-of-plane shear. Therefore, the concrete nonlinear behavior is only considered in the \underline{D}_{mb}^{co} constitutive matrix.

For linear elastic uncracked concrete, \underline{D}_{mb}^{co} is designated by \underline{D}_{mb}^{eco} , which is defined elsewhere (Barros & Figueiras 2001). For the case of cracked concrete with concrete between cracks exhibiting an elasto-plastic behavior, \underline{D}_{mb}^{co} of (3) is replaced by $\underline{D}_{mb}^{epcrco}$ (Sena-Cruz et al. 2004):

$$\underline{D}_{mb}^{co} \Longrightarrow \underline{D}_{mb}^{epcrco} = \underline{D}_{mb}^{epco} - \underline{D}_{mb}^{epco} \left[\underline{T}^{cr}\right]^{T} \left(\underline{\widehat{D}}^{cr} + TcrDmbepcoTcrT - 1TcrDmbepco$$
(4)

where

$$\underline{\underline{D}}_{mb}^{epco} = \underline{\underline{H}} - \frac{\underline{\underline{H}}\frac{\partial f}{\partial \underline{\sigma}} \left(\frac{\partial f}{\partial \underline{\sigma}}\right)^{T} \underline{\underline{H}}}{h + \left(\frac{\partial f}{\partial \underline{\sigma}}\right)^{T} \underline{\underline{H}} \left(\frac{\partial f}{\partial \underline{\sigma}}\right)}$$
(5)

$$\underline{H} = \left(\left[\underline{D}_{mb}^{eco} \right]^{-1} + h_c \Delta \lambda \frac{\partial^2 f}{\partial \underline{\sigma^2}} \right)^{-1}$$
(6)

where $\partial f / \partial \underline{\sigma}$ is the flow vector, h_c is a scalar function that depends on the hydrostatic pressure, \underline{T}^{cr} is a transformation matrix that depends on the direction of the cracks formed at a sampling point (Sena-Cruz et al. 2004), and $\underline{\hat{D}}^{cr}$ is the constitutive matrix of the set of cracks. In case of one crack per each sampling point,

$$\underline{\widehat{D}}^{cr} = \underline{D}^{cr} = \begin{bmatrix} D_I^{cr} & 0\\ 0 & D_{II}^{cr} \end{bmatrix}$$
(7)

where D_I^{cr} and D_{II}^{cr} are the softening modulus of the fracture modes I and II of the smeared cracks, respectively. D_I^{cr} is characterized by the stress at crack initiation, $\sigma_{n,1}^{cr}$ (see Fig. 3), the fracture energy, G_f , the shape of the softening law and the crack band width, l_b .



Figure 3. Tri-linear tensile-softening diagram.

and

In smeared crack models the fracture zone is distributed over l_b , which must depend on the finite element geometric characteristics in order to assure that the results of the FEM analysis are not dependent on the finite element mesh (Bazant & Oh 1983). The fracture mode II modulus, D_{II}^{cr} , of (7) is obtained from (Barros 1995):

$$D_{II}^{cr} = \frac{\left(1 - \frac{\varepsilon_{II}^{cr}}{\varepsilon_{II,u}^{cr}}\right)^{p_1}}{1 - \left(1 - \frac{\varepsilon_{II}^{cr}}{\varepsilon_{II,u}^{cr}}\right)^{p_1}} G_C$$
(8)

where G_C is the concrete elastic shear modulus and p_1 an integer parameter that can obtain distinct values in order to simulate different levels of concrete shear stiffness degradation (Barros 1995).

In case of cracked concrete with concrete between cracks in linear and elastic state, \underline{D}_{mb}^{co} is still obtained from (4) replacing $\underline{D}_{mb}^{epco}$ by \underline{D}_{mb}^{eco} .

3.2 Steel constitutive law

For modeling the behavior of the steel bars, the stress-strain relationship represented in Figure 4 was adopted (Sena-Cruz 2004). The curve (under compressive or tensile loading) is defined by the points $PT1=(\varepsilon_{sy}, \sigma_{sy})$, $PT2=(\varepsilon_{sh}, \sigma_{sh})$ and $PT3=(\varepsilon_{su}, \sigma_{su})$, and a parameter *p* that defines the shape of the last branch of the curve. Unloading and reloading linear branches with slope E_s ($\sigma_{sy}/\varepsilon_{sy}$) are assumed in the present approach.

3.3 FRP constitutive law

A linear elastic stress-strain relationship was adopted to simulate the behavior of NSM CFRP strips applied in the RC slabs.

4 SIMULATION OF THE TESTS

4.1 Materials properties and finite element mesh

Tables 1 and 2 include the values of the parameters adopted for the characterization of the constitutive models for the concrete and steel, respectively. The CFRP strips, of 10×1.4 mm² cross sectional area, were assumed as an isotropic material with an elasticity modulus of 160 GPa and null value for the Poisson's coefficient, since the consideration of their real anisotropic properties have marginal influence in terms of their contribution for the behavior of NSM strengthened RC slabs.

Due to the structural symmetry, only half of the slab was considered in the numerical simulations. Figure 5 shows the eight node finite element mesh adopted to discretize the half part of the slab. The



Figure 4. Uniaxial constitutive model of the rebars.

support conditions are also represented in this figure. The slab thickness was discretized in 20 layers.

Table 1. Values of the parameters of the concrete constitutive model.

Poisson's ratio	$v_c = 0.15$
Initial Young's modulus	$E_c = 28000 \text{ N/mm}^2$
Compressive strenght	$f_c = 40 \text{ N/mm}^2$
Strain at peak compressive strength	$\varepsilon_{c1} = 2.2 \mathrm{x} 10^{-3}$
Initial yield surface parameter ⁽¹⁾	$\alpha_0 = 0.4$
Tensile softening diagram ⁽²⁾	$f_{ct} = 1.5 \text{ N/mm}^2$
	$G_f = 0.05 \text{ N/mm}$
	$\xi_{l} = 0.015$
	$\alpha_l = 0.6$
	$\xi_2 = 0.2$
	$\alpha_2 = 0.25$
Parameter defining the mode I frac-	n = 2
ture energy available to the new crack $^{(3)}$	
Shear retention factor (Equation 8)	$p_1=2$
Threshold angle ⁽³⁾	$\alpha_{\rm th} = 30^{\circ}$
Maximum number of cracks per inte-	2
gration point	
$\overline{\alpha_0} = \overline{\sigma_0} / \overline{\sigma_n}$, Sena-Cruz (2004)	

 $\begin{aligned} & \alpha_0 = \sigma_0 / \sigma_p, \text{ Sena-Cruz} (2004) \\ & ^{(2)}f_{ct} = \sigma_{n,1}^{cr}; \ \xi_1 = \varepsilon_{n,2}^{cr} / \varepsilon_{n,u}^{cr}; \ \xi_2 = \varepsilon_{n,3}^{cr} / \varepsilon_{n,u}^{cr}; \ \alpha_1 = \sigma_{n,2}^{cr} / \sigma_{n,1}^{cr}; \\ & \alpha_2 = \sigma_{n,3}^{cr} / \sigma_{n,1}^{cr} \text{ (see Figure 3)} \\ \end{aligned}$

Table 2. Values of the parameters of the steel constitutive model (see Figure 4).

Steel	bar diameter (mm)	Ø 8mm	Ø 10mm	Ø 12mm
$\overline{P_1}$	$\varepsilon_{sy}(-)$	2.30×10^{-3}	2.70×10^{-3}	2.40x10 ⁻³
	$\sigma_{sy}(MPa)$	421.00	446.00	445.00
P_2	$\varepsilon_{\rm sh}(-)$	4.42×10^{-2}	3.07×10^{-2}	3.05×10^{-2}
	$\sigma_{\rm sh}({\rm MPa})$	526.25	446.00	445.00
P ₃	$\varepsilon_{su}(-)$	8.85x10 ⁻²	1.31×10^{-1}	1.02×10^{-1}
	$\sigma_{su}(MPa)$	555.72	557.50	547.35
Es	s (GPa)	200.8	178.24	198.36

4.2 Results and discussion

Figures 6 to 9 represent relevant results of the simulations corresponding to the slabs of the SL15 series. The analysis of the simulations of the other series can be found elsewhere (Dalfré & Barros 2008).

	3	6	9	12	15	18	21	24	27	30	33	36	39	42	45	48	51	54	57	60	63	66	69	72	75	78	81	84
20	1 2 1	5	8	11	14	17	20	23	26	29	32	35	38	41	44	47	50	53	56	59	62	65	68	71	74	77	80	83 🖂
5∠ ▲		4	7	10	13	16	19	22	25	28	31	34	37	40	43	46	49	52	55	58	61	64	67	70	73	76	79	82

►S1





Figure 6. Force-loaded section deflection relationship.





 \bowtie u3=0 \bowtie u2= θ 1=0 \blacksquare u1=u3= θ 2=0



Figure 8. Force – Concrete strain relationships at (a) slab symmetry cross section and (b) loaded section.





The figures show that the numerical model is able to capture with good accuracy the behavior of the constituent materials of this structural system during the loading process of the tested slabs. Crucial experimental results registered in the monitoring system installed in the constituent materials at the zones of the intermediate support and at the loaded sections (IS and LS, respectively) are included in Table 3.

Table 3.	Main	results	of	series	SL	15.
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		Hinge at intermediate support									
	F_y^{IS} (kN)	u ^{IS} (mm)	$arepsilon_c^{IS}$ (‰)	\mathcal{E}_{c}^{LS} (‰)	\mathcal{E}_{s}^{LS} (‰)	Е _{f,max} (‰)					
Reference SL15s25 SL15s50	85.29 88.00 96.15	15.85 15.82 16.28	-1.22 -1.48 -1.43	-1.53 -1.17 -1.08	2.20 2.00 2.03	2.81 2.87					
		Hing	ge at loa	ded secti	ons						
	F_y^{LS} (kN)	u ^{IS} (mm)	$arepsilon_{c}^{IS}$ (‰)	$arepsilon_c^{LS}$ (‰)	$arepsilon_{s}^{IS}$ (‰)	E _{f,max} (‰)					
Reference SL15s25 SL15s50	98.00 100.00 100.45	21.50 19.09 18.43	-3.77 -1.77 -1.58	-1.91 -1.40 -1.19	2.45 2.49 2.08	3.29 3.16					
	F _{max} (kN)	$\mathcal{E}_{f,max}^{F_{max}}$ (%)									
Reference SL15s25 SL15s50	98.00 106.49 118.60	7.86 7.83	-								

In this Table, F_y^{IS} and F_y^{LS} are the total load at the formation of the plastic hinge at IS and LS, ε_c^{IS} , ε_c^{LS} are the average concrete strains at IC and LS, ε_s^{IS} and ε_s^{LS} are the maximum and the average steel bars strains at IS and LS, respectively, $\varepsilon_{f,max}$ is the maximum strain in the CFRP strips, F_{max} is the maximum total load up to a concrete compressive strain of 3.5% in the IS ($\varepsilon_c^{IS} = 3.5\%_0$), and $\varepsilon_{f,max}^{F_{max}}$ is the maximum strain in the CFRP strips at F_{max} . It was assumed that a plastic hinge was formed when yield strain was attained at the steel bars.

These figures show that, after crack initiation, which occurred at the top surface of the intermediate support for a total load of about 13 kN, the slab stiffness decreased significantly, but the elasto-cracked stiffness was almost maintained up to the formation of the plastic hinge at the intermediate support, at a load level of about 85 kN, 88 kN and 96 kN for the reference, SL15s25 and SL15s50 slabs, respectively.

At these load levels, the maximum concrete compressive strains of the bottom surface at the intermediate support, ε_c^{IS} , and of the top surface at the applied load section, ε_c^{LS} , are in the ranges -1.22 ‰ to -1.48 ‰ and -1.08 ‰ to 1.53 ‰, respectively. At F_y^{LS} , the maximum strain of the steel bars of the bottom layer at the applied load section, ε_s^{LS} , and the maximum strain at the CFRP strips, $\varepsilon_{f,max}$, are in the ranges 2.0 ‰ to 2.2 ‰ and 2.81 ‰ to 2.87 ‰, respectively, which indicates that tensile stresses in the laminates are far below its tensile strength at the moment of the formation of the plastic hinge at intermediate support.

In fact, the force-deflection relationship (Figure 6) evinces that, up to the formation of the plastic hinge at the intermediate support, CFRP strips did not contribute significantly for the slabs' load carrying capacity. The deflection at F_{v}^{LS} , u_{v}^{IS} , was not significantly affected by the presence of the CFRP laminates. Since at the moment of the formation of the plastic hinge at the intermediate support the strains in the steel bars of the loaded sections, ε_s^{LS} , are near the steel yield strain (see Table 2), the load increment between the formation of the plastic hinges at intermediate and loaded sections decreased with the increase of the percentage of CFRP laminates. As expected, F_v^{LS} was almost equal for the three slabs of SL15 series (98 to 100 kN), since the deflection at F_{y}^{LS} , u_{ν}^{IS} , decreased with the increase of the CFRP percentage (from 21.5 mm in the reference slab up to 18.43 mm in the SL15s50). In the reference slab, at F_{y}^{LS} , ε_c^{IS} was higher than the strain at concrete compressive strength (ε_{c1} , see Table 1) and ε_c^{LS} was almost attaining ε_{c1} , which justifies the formation of the structural mechanism. At F_y^{LS} , $\varepsilon_{f,max}$ was around 3.22 ‰, which is far below the CFRP ultimate strain. However, since ε_c^{IS} and ε_c^{LS} are both lower than ε_{c1} , the laminates contributed to increase the slab's load carrying capacity. At concrete crushing strain (3.5 ‰ was assumed on the design of the CFRP percentage), the F_{max} of SL15s25 and SL15s50 slabs was 106.49 and 118.60 kN, respectively, being the corresponding CFRP strains 7.86 ‰ and 7.83 ‰. The contribution of the CFRP laminates for the slab's maximum load carrying capacity was limited due to the occurrence of concrete crushing. In terms of moment redistributing capacity, NSM laminates did not introduce any restriction, and no debond or concrete detachment premature failure modes occurred up to the interruption of the tests.

5 CONCLUSIONS

This work presented and discussed the results obtained in a preliminary experimental program dealing with the thematic of moment redistribution capability of two-way RC slabs strengthened according to the NSM technique. The main focus was put on the numerical simulation of the tested slabs, in order to calibrate the constitutive model for its future use on parametric studies, for the evaluation of the influence of relevant parameters on the NSM flexural strength and moment redistribution capability of continuous RC slabs. Since the numerical model was able to capture, with good accuracy, the behavior of the tested slabs, it will be also used to define an extensive experimental work aiming to support the results to be provided by the parametric studies. The comparison between the strains registered experimentally in the CFRP laminates and the strains determined by the numerical model shows that it can be assumed a perfect bond between NSM laminates and surrounding concrete.

The contribution of the NSM laminates for the slab's load carrying capacity was limited by the concrete crushing. The NSM strengthened slabs had moment redistribution capability similar of the reference slab. No premature CFRP failure modes were detected up the end of the tests, which occurred at a deflection more than 40 mm.

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