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Engineering Structures xx (xxxx) xxx–xxx

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Optimum maintenance strategy for deteriorating bridge structures based on lifetime functions

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Received 19 May 2003; received in revised form 28 May 2004; accepted 14 June 2005

Abstract

The highway networks of most European and North American countries are completed or close to completion. However, many of their bridges are aging, and in the United States alone a very significant part of the about 600,000 existing bridges is considered to be deficient and must be replaced, repaired or upgraded in the short term. The funds available for the maintenance of existing highway bridges are extremely limited when compared with the huge investment necessary, and must, therefore, be spent wisely. In this paper, a model based on lifetime functions for predicting the evolution in time of the reliability of deteriorating bridges under maintenance is presented. This model uses the probability of satisfactory system performance during a specified time interval as a measure of reliability and treats each bridge structure as a system composed of several components. In this manner, it is possible to predict the structural performance of deteriorating structures in a probabilistic framework. In addition, the optimum maintenance strategy is identified using as objective the minimization of the present value of the life-cycle maintenance cost. An existing bridge is analyzed using lifetime functions and its optimum maintenance strategy is found.

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Keywords: Bridges; Maintenance; Lifetime functions; Deteriorating structures; System performance; Optimum maintenance strategy

1. Introduction

The highway networks of most European and North American countries are completed or close to completion. As a result, highway agencies face a decrease in the need for new structures and, on the other hand, a very significant increase in the number of bridges that need to be repaired or replaced in the short term. In the United States a very significant part of the existing bridges is considered to be deficient and must be repaired, upgraded or replaced in the near future. As a result, in the last decade, research has shifted from the design of new bridges to the assessment of existing bridges and prediction of their performance deterioration.

Due to the limited funds available for upgrading and maintaining the performance of existing bridges at acceptable levels, highway agencies, governments and researchers have tried to develop models that predict optimum strategies to be used in the maintenance planning for existing bridges, keeping them safe and serviceable by using the smallest possible investment.

The current bridge management systems use visual inspection results to assess bridge safety [12,16,21]. These systems are based on component level analysis, disregarding overall system effects such as redundancy, ductility, and component reliability importance. It has long been recognized that several reliability measures (e.g., reliability index and probability of survival) are consistent and invariant indicators of structural safety. The reliability index of a structure can be higher or lower than that of its critical component, for parallel and series systems, respectively. Therefore, the evaluation of the overall structural system safety is of paramount importance in assessing the safety of new and existing bridges.

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The deterioration of a bridge depends on several parameters (e.g., environmental conditions, traffic volume, and quality of workmanship) that cannot be accurately predicted. Consequently, bridge deterioration must be modeled in a probabilistic manner, using random variables for the parameters defining the deterioration process. To keep the reliability of a bridge above a minimum target level during a specified period of time, maintenance actions must usually be applied. In general, these actions reduce the rate of increase of the cumulative time system failure probability [5]. Several maintenance strategies satisfying the above requirements are possible. In general, the cost of each feasible maintenance strategy is different from the others. The optimum maintenance strategy, associated with minimum present value of cumulative cost, must be found.

Most decisions in bridge maintenance must to be made with a binary type of information based on visual inspections where defects are found or not found. To be able to correctly assess and predict the performance of existing structures using only this information, the performance must be indicated using the probability of occurrence of a defect rather than a continuous damage model. This approach is less accurate than the continuous damage model approach, but can be implemented using the information currently available on most structures.

In this paper, a model based on lifetime functions for predicting the evolution in time of the reliability of deteriorating bridges under maintenance is presented. This model uses the probability of satisfactory system performance during a specified time interval as a measure of reliability and treats each bridge structure as a system composed of several components. In this manner, it is possible to predict the structural performance of deteriorating structures in a probabilistic framework. In addition, the optimum maintenance strategy is identified using as objective the minimization of the present value of the life-cycle maintenance cost. An existing bridge is analyzed using lifetime functions and its optimum maintenance strategy is found. Probabilistic approaches to deteriorating and/or maintenance of existing structures can also be found in [3,20,4,8].

2. System reliability and reliability importance based on lifetime functions

The safety of a structural system can be analyzed based on the reliability of its components and their role in various failure modes. According to Leemis [17], the state of a component, x_i , is assumed to be binary, as follows:

$$x_i = \begin{cases} 0 & \text{if component } i \text{ has failed} \\ 1 & \text{if component } i \text{ is functioning.} \end{cases} \quad (1)$$

The collection of the states of all components forms the system vector, $\mathbf{x} = (x_1, x_2, \dots, x_n)$. Based on the state of all components of a system, the structure function [17] is

defined as follows:

$$\phi(\mathbf{x}) = \begin{cases} 0 & \text{if the system has failed} \\ 1 & \text{if the system is functioning.} \end{cases} \quad (2)$$

where \mathbf{x} = vector containing the state of each component.

Structures modeled as series and parallel systems are safe when all and at least one of their components are safe, respectively. For these systems, the associated structure functions are, respectively, defined as:

$$\phi(\mathbf{x}) = \min(x_1, x_2, \dots, x_n) = \prod_{i=1}^n x_i \quad (3)$$

$$\phi(\mathbf{x}) = \max(x_1, x_2, \dots, x_n) = 1 - \prod_{i=1}^n (1 - x_i). \quad (4)$$

A coherent system [17] is a system that will not upgrade if a component degrades (i.e., $\phi(\mathbf{x})$ is non-decreasing in \mathbf{x}). For a given structure, modeled as a coherent system, the associated structure function can be obtained by modeling the system as series of parallel components. This system can be successively reduced by using Eqs. (3) and (4) to a single equivalent component whose structure function is defined in terms of all components. However, the state of each component can only be expressed in probabilistic terms by considering components defined by their probabilities of survival.

So far, components and system performance have only been considered at a particular point in time. However, due to material deterioration and/or increase in environmental and/or mechanical loadings the reliability of a structure or component under no maintenance is a non-increasing function of time, called the survivor function $S(t)$. This is a particular type of lifetime distribution function that includes also the hazard function and the mean residual life function, among others. In this study, two survivor functions are considered: Weibull and exponential power. These non-increasing functions are 1 and 0 at $t = 0$ and $t \rightarrow \infty$, respectively. Figs. 1 and 2 show the effects of the number of independent components, each characterized by the same survivor function (i.e., exponential power function with a failure rate λ of 0.005/year), on the survivor function of a series and a parallel system up to 10 components, respectively, considering a lifetime of 75 years.

The survivor functions of a series-parallel system of four components with different exponential power survivor functions ($\lambda = 0.005/\text{year}$ for components 2, 3, and 4 and λ varying from 0.001/year to 0.01/year for component 1), analyzed over a lifetime period of 75 years, are shown in Fig. 3. As expected, a change in the survivor function of component 1 leads to a significant change in the system survivor function. Additional examples on the effects of the parameters of exponential and Weibull survivor functions are provided in [25,26].

In general, the components of a structural system have different impacts on the overall system reliability. According to Leemis [17], “the component with the largest reliability

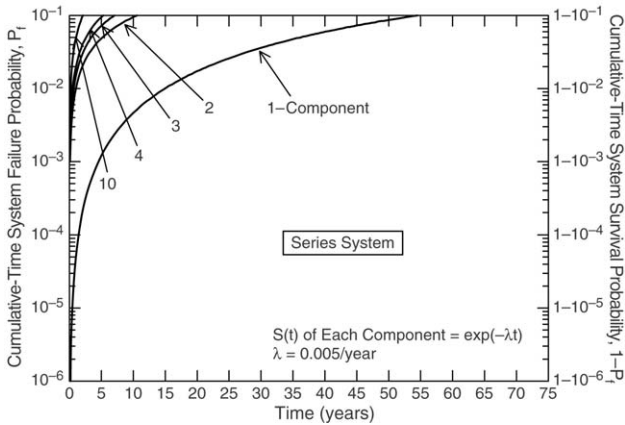


Fig. 1. Effect of number of components on cumulative-time failure probability of series systems.

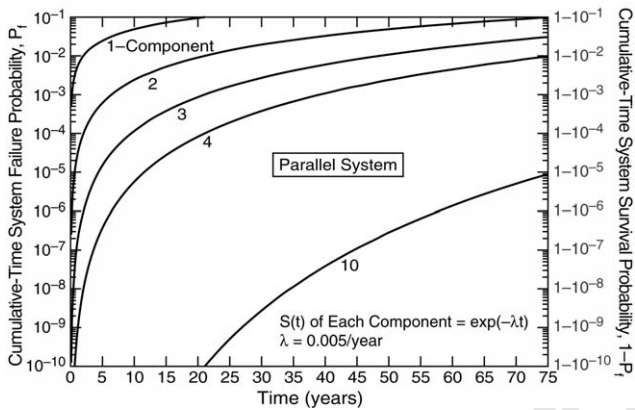


Fig. 2. Effect of number of components on cumulative-time failure probability of parallel systems.

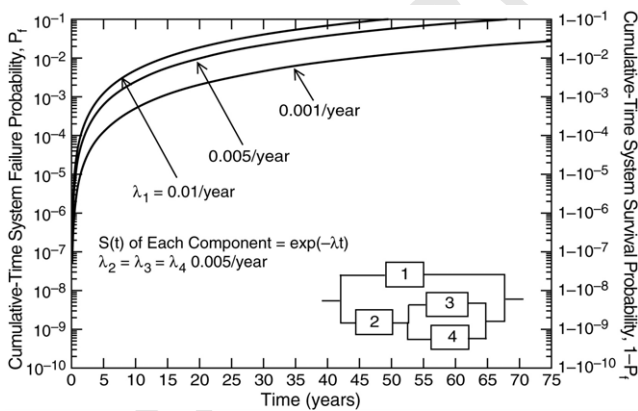


Fig. 3. Effect of failure rate of component 1 on cumulative-time failure probability of a four-component system.

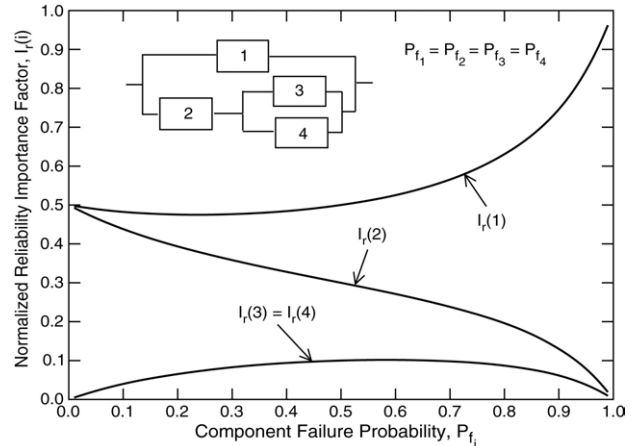


Fig. 4. Normalized reliability importance factors for a four-component system versus component failure probability.

where $r(\mathbf{p})$ = system reliability and p_i = probability of failure of component i .

This factor can be normalized as follows [11]:

$$I_r^0(i) = \frac{I_r(i)}{\sum_{i=1}^n I_r(i)} \quad (6)$$

where $I_r^0(i)$ = normalized reliability importance factor of component i , varying from 0 (not relevant to system reliability) to 1 (only relevant component to system reliability), and n = number of components. Since the system reliability is time dependent so are the reliability importance factors $I_r(i)$ and $I_r^0(i)$.

In Fig. 4 the normalized reliability importance factor $I_r^0(i)$ of each of the four components of the series-parallel system analyzed in Fig. 3 is shown for different probabilities of failure of the iso-reliability components. As expected, component 1, due to its critical function in the system, has the highest reliability importance factor over all the range of component failure probabilities considered.

In most cases, the failure rate of a component is not known a priori and, as a result, it must be treated as a random variable. To illustrate the effect of randomness of the failure rate on the survivor function of a system, Fig. 5 shows the evolution in time of the probability of survival of the four-component system defined in Fig. 3 considering the same random failure rates for all components defined by a uniform distribution varying from 0.00413/year to 0.00586/year. As shown, the range of possible values of the system survival probability depends on the randomness of the failure rate of components.

3. Preventive and essential maintenance models

As previously indicated, the reliability of a structure can be kept above a specified threshold by applying maintenance actions. These actions can be divided in two major groups: (i) preventive actions; and (ii) essential actions. Preventive

importance is that component for which an increase in its reliability corresponds to the largest increase in the system reliability". Consequently, the reliability importance of component i , $I_r(i)$, is as follows [17]:

$$I_r(i) = \frac{\partial r(\mathbf{p})}{\partial p_i} \quad (5)$$

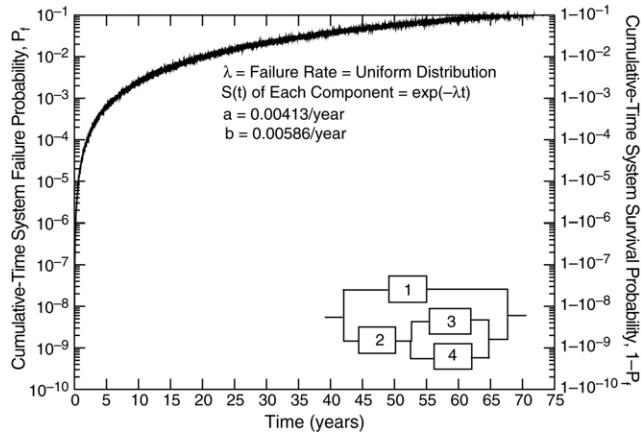


Fig. 5. Cumulative-time failure probability of a four-component series-parallel system considering random failure rates of components.

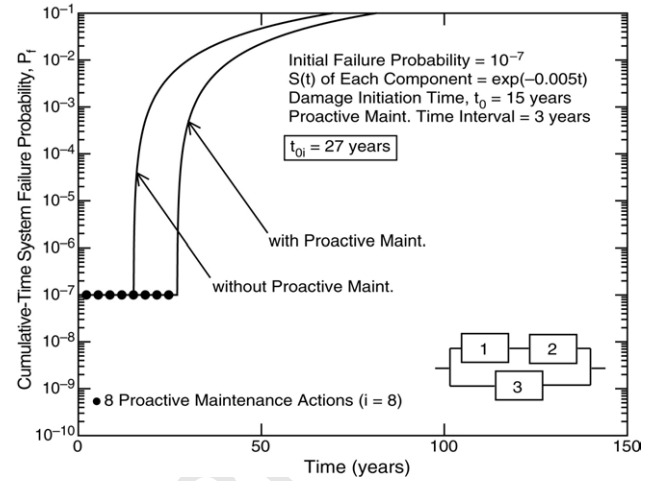


Fig. 6. Effect of proactive maintenance on a three-component series-parallel system.

1 maintenance actions (such as painting, silane treatment, and
 2 cathodic protection) are defined as scheduled maintenance
 3 actions applied to functioning components. The justification
 4 for preventive maintenance action is that if not undertaken
 5 it will require more funds at a later stage to keep the
 6 component from becoming critical [2,9]. Preventive actions
 7 applied to non-deteriorated components are designated as
 8 proactive and their objective is to delay the time of damage
 9 initiation [13]. Preventive maintenance actions applied to
 10 deteriorated components are denoted as reactive, and they
 11 aim at eliminating or reducing the effects of the deterioration
 12 process. Several maintenance models in a probabilistic
 13 context were developed by Frangopol et al. [10], Bris
 14 et al. [1], Kobbacy and Jeon [14], and Lam and Zhang [15],
 15 among others. In this section, both preventive and essential
 16 maintenance models are briefly summarized. Additional
 17 information is provided in [24] and [26].

18 3.1. Proactive preventive maintenance

19 Due to the lack of data on proactive maintenance models,
 20 expert judgment is generally used to define the effect of
 21 applying this type of maintenance. In this study, it is
 22 assumed that each proactive maintenance action (applied
 23 before damage initiation) postpones the initial time of
 24 damage initiation under no maintenance, t_0 , to [26]:

$$25 \quad t_{0i} = t_0 + i \cdot \frac{t_{pi}}{2} \quad (7)$$

26 where t_{0i} = time of damage initiation considering i proactive
 27 maintenance actions, and t_{pi} = time interval between
 28 maintenance actions. In order to compute the number i
 29 of proactive maintenance actions necessary to obtain a
 30 specified value of t_{0i} , the following constraint must be
 31 satisfied:

$$32 \quad i \cdot t_{pi} < t_{0(i-1)} \quad (8)$$

33 where $t_{0(i-1)}$ = time of damage initiation considering $i - 1$
 34 proactive maintenance actions.

35 An example of the effect of proactive maintenance on
 36 cumulative-time system failure probability is shown in
 37 Fig. 6, considering a three-component series-parallel system
 38 with a probability of survival of each component described
 39 by an exponential function. Both proactive maintenance and
 40 no maintenance strategies are considered. In this example,
 41 the damage initiation time of both components and system
 42 is extended from $t_0 = 15$ years (no maintenance) to
 43 $t_{0i} = 27$ years (under eight preventive maintenance actions
 44 applied every three years, $t_{pi} = 3$ years, to all components).

45 3.2. Reactive preventive maintenance

46 In this study, the reactive maintenance model proposed
 47 by Kececioglu [13] is used. This model considers that, if
 48 reactive maintenance is applied at regular time intervals, t_p ,
 49 the survivor function is as follows [13,26]:

$$50 \quad S_{t_p}(t) = [S_t(t_p)]^j S_t(\tau) \quad (9)$$

51 where S_t = survivor function under no maintenance,
 52 $S_{t_p}(t)$ = survivor function under reactive preventive
 53 maintenance at time t , t_p = time interval between
 54 applications of reactive preventive maintenance, j = number
 55 of applications of reactive preventive maintenances before
 56 time t , and τ = time since last application.

57 An example of the effect of reactive preventive
 58 maintenance is presented in Fig. 7. In this figure each
 59 component of the deteriorating two-component parallel
 60 system is subjected to reactive maintenance at different
 61 time intervals, t_p . The survivor function of each independent
 62 component is $\exp(-0.01t)$. As shown in this figure, the
 63 effect of each reactive preventive maintenance action is
 64 to reduce the slope of the cumulative survival function to
 65 its initial value (at $t = 0$). As expected, more frequent
 66 applications lead to higher probabilities of system survival.

67 If reactive preventive maintenance is applied only to
 68 some components of a system (e.g., two out of four

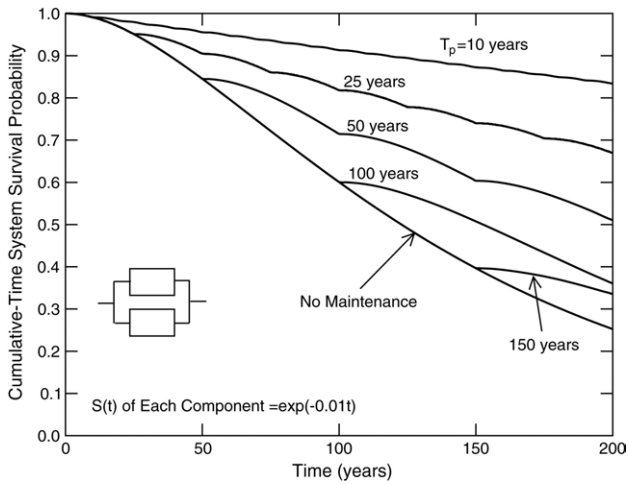


Fig. 7. Cumulative-time system survivor probability of a two-component parallel system under reactive maintenance applied to both components at different time intervals.

girders), Eq. (9) is no longer valid and reliability importance factors must be taken under consideration as indicated by Yang [24]. As an example, Fig. 8 shows the results obtained considering that one, several, or all the three deteriorating components, characterized by the survivor function $S_t = \exp(-0.005t)$, of a series-parallel system are under cyclic reactive preventive maintenance at five years' interval. Component 3, being the most important, has the largest effect on the cumulative-time system failure probability.

3.3. Essential maintenance

Essential maintenance actions are applied to failed or close to failure components. Since it is desirable to repair or replace such components as soon as possible, such maintenance actions cannot be scheduled a priori. In this work the only essential maintenance action considered is replacement of one, several, or all components of a system, resulting in the restoration of the condition of such components to their initial values (at $t = 0$).

The three-component system shown in Fig. 9 is used to explain the essential maintenance model. Each component has an exponential survivor function. It is assumed that all three components are independent and their failure rate is 0.0005/year. The survivor function under no maintenance of the three-component system in Fig. 9 is indicated in [25]. If essential maintenance is performed on one, several, or all components, the survivor function of the system depends on the time since maintenance was last applied to component i ($i = 1, 2, 3$). The three essential maintenance actions considered in Fig. 9 are replacement of component 1, component 2, and all three components at 10, 20, and 40 years, respectively. As indicated in Fig. 9, replacement of components 1 or 2 causes a relatively small reduction in the system failure probability.

Based on an extension of the essential maintenance model presented in this section, using survivor functions for

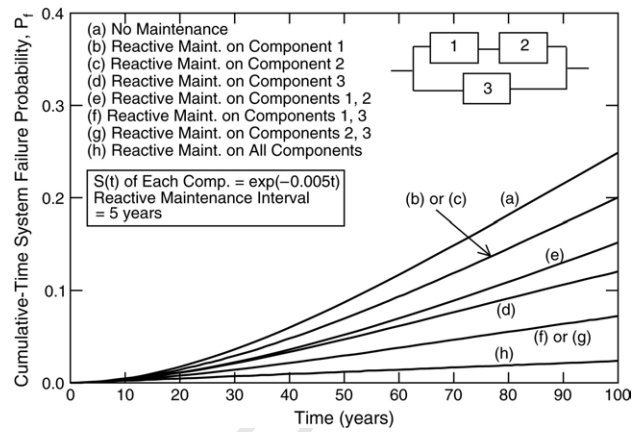


Fig. 8. Cumulative-time system failure probability of a three-component series-parallel system under reactive maintenance applied to one, several, or all components.

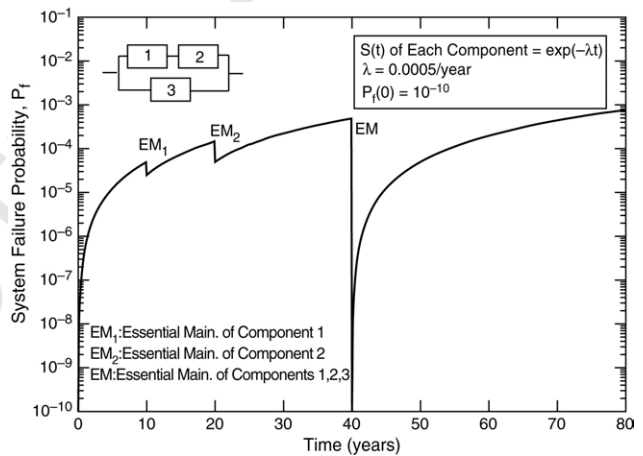


Fig. 9. System failure probability of a three-component series-parallel system under essential maintenance

each component of a series-parallel system, an optimum maintenance strategy is formulated next and applied to an existing bridge.

4. Optimization and data on lifetime functions

The methodology used for optimizing the essential maintenance strategies is adapted from that proposed by Estes and Frangopol [7]. It consists of the following nine steps:

- (a) Construct a system model of the overall structure as a series-parallel combination of individual components and establish a time horizon for the system;
- (b) Define the survivor function to be used for each component;
- (c) Compute the survivor function under no maintenance for the system model considered in step (a);
- (d) Establish a system reliability threshold, at which maintenance must be applied;

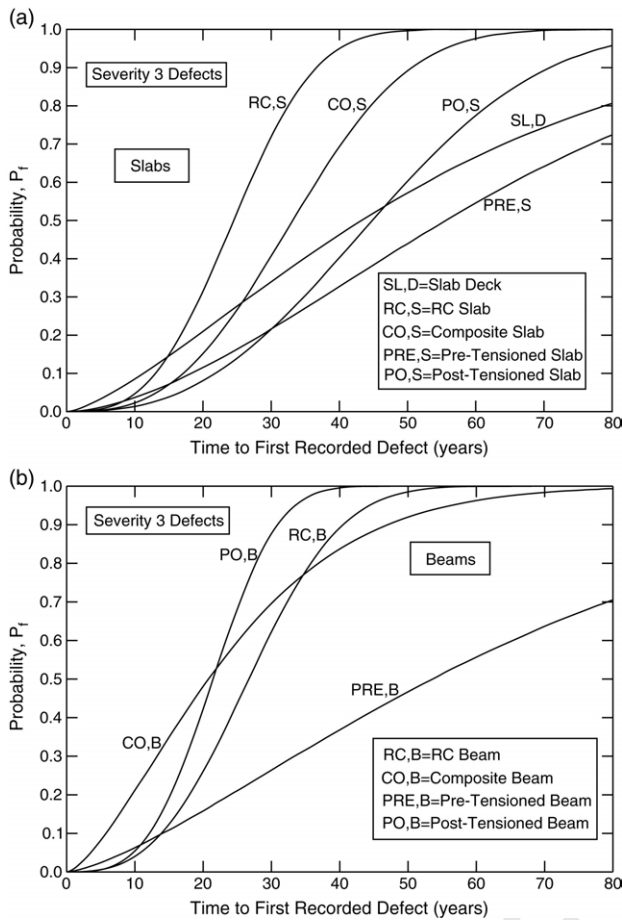


Fig. 10. Cumulative probability of occurrence of severity 3 defect in: (a) slabs, and (b) beams.

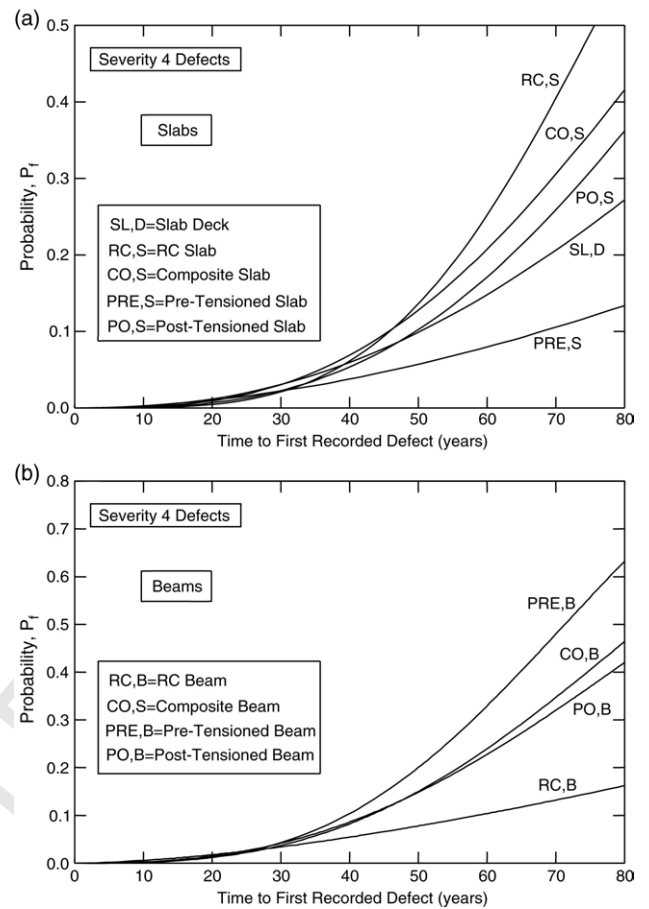


Fig. 11. Cumulative probability of occurrence of severity 4 defect in: (a) slabs, and (b) beams.

- (e) Determine all possible maintenance actions and their associated costs;
- (f) Determine all maintenance strategies (i.e., combination of several maintenance actions during the time horizon);
- (g) Compute the system survivor function for each maintenance strategy;
- (h) Compute the present values of lifetime cost for each maintenance strategy; and
- (i) Determine the optimum solution based on the minimum present value of lifetime cost.

In this study, data compiled by Maunsell [18] for the serviceable life of highway structures and their components is used. The service life is defined as the time taken for a significant defect to be recorded by an inspector. The severity of a defect is classified as follows [18]: Severity 1: no significant defects; Severity 2: minor defects of a non-urgent nature; Severity 3: defects which shall be included for attention within the next annual maintenance program; and Severity 4: the defect is severe and urgent action is needed.

Data on the lifetime functions corresponding to each of these severities is reported in [18] for different components of the most common types of highway bridges. As an example, using the Weibull distribution parameters of

service life for severity 3 and 4 defects provided in [18], Figs. 10 and 11 show the cumulative-time probabilities of the first recorded defect for different types of slabs and beams. The Weibull distribution has been shown to properly model aging and to analytically derive the conditional probability density function of the residual lifetime when the current age is provided [23]. As indicated in Figs. 10 and 11 for severity 3 and 4 defects, respectively, there is significant dispersion of the probabilities of occurrence of the same severity defect among different types of elements and materials.

5. Colorado state highway bridge E-17-AH

As existing bridge located in Colorado, analyzed previously by a system reliability index approach [7], is presented herein as a case study example using the lifetime function approach. Bridge E-17-AH is located on 40th Avenue (State Highway 33) between Madison and Gardfield Streets in Denver, Colorado. The bridge has three simple spans of equal length (13.3 m) and a total length of 42.1 m. The deck consists of a 22.9 cm layer of reinforced concrete and a 7.6 cm surface layer of asphalt. The east–west bridge has two lanes of traffic in each direction with an average

1 daily traffic of 8,500 vehicles. The roadway width is 12.18 m
 2 with 1.51 m pedestrian sidewalks and handrailing on each
 3 side. The bridge offers 6.8 m of clearance for the railroad
 4 spur that runs underneath. There is no skew or curvature.
 5 The slab is supported by nine standard-rolled, compact, and
 6 non-composite steel girders. The girders are stiffed by end
 7 diaphragms and intermediate diaphragms at the third points.
 8 Each girder is supported at one end by a fixed bearing and
 9 an expansion bearing at the other end. The elevation and
 10 cross-section of this nine-girder bridge are indicated in [6],
 11 and [25]. A comprehensive description of this bridge can be
 12 found in [6].

13 In this study, failure of a component is defined as
 14 occurrence of a defect of severity 4 since this type
 15 of defect is relevant enough to justify the application
 16 of essential maintenance actions. No distinction is made
 17 among different sources of structural defects. As a result,
 18 the defects considered include those caused by corrosion,
 19 excessive loading, or fatigue, among other sources. Studies
 20 considering defects due to various causes including fatigue
 21 and corrosion in a probabilistic context can be found in
 22 [27,4], and [19].

23 Weibull functions are adopted to model the probability
 24 of defect occurrence as they are the best fit of the data
 25 summarized in [18]. The occurrence of the defects in the
 26 reinforced concrete slab deck and steel girders of the bridge
 27 E-17-AH is modeled by a Weibull distribution with the shape
 28 and scale parameters κ and λ as follows [18]: slab deck
 29 ($\kappa = 2.37$ and $\lambda = 0.0077/\text{year}$) and girders ($\kappa = 2.86$
 30 and $\lambda = 0.0106/\text{year}$).

31 Due to redundancy in multi-girder bridge types, single-
 32 girder failure does not cause bridge failure. If one girder
 33 fails, load redistribution takes place and, usually, the overall
 34 bridge is capable of carrying additional loads. Multi-girder
 35 bridges can be modeled, in system reliability analysis, as
 36 a combination of series and parallel components. For the
 37 bridge analyzed, the following failure modes are considered:
 38 (i) failure of any external girder or any two adjacent internal
 39 girders or deck failure cause the bridge failure; (ii) any
 40 two adjacent girder failures or deck failure cause the bridge
 41 failure; (iii) any three adjacent girder failures or deck failure
 42 cause the bridge failure. These system models, denoted by
 43 I, II, and III, respectively, are shown in Fig. 12. In this
 44 figure, the failure function D corresponds to the occurrence
 45 of a severity 4 defect in the deck, and the failure functions
 46 G1, G2, . . . , G9 correspond to the occurrence of a severity
 47 4 defect in girders G1, G2, . . . , G9, respectively. Each of
 48 the proposed models is associated with a different level of
 49 acceptable damage. This level increases from model I to III.
 50 Consequently, models III and I are associated with the least
 51 and most frequent applications of maintenance, respectively.
 52 The choice of the most adequate system model must be,
 53 in each situation, made by the bridge owner, considering
 54 the available funds, and the importance and redundancy of
 55 the structure, among other factors. The maintenance options

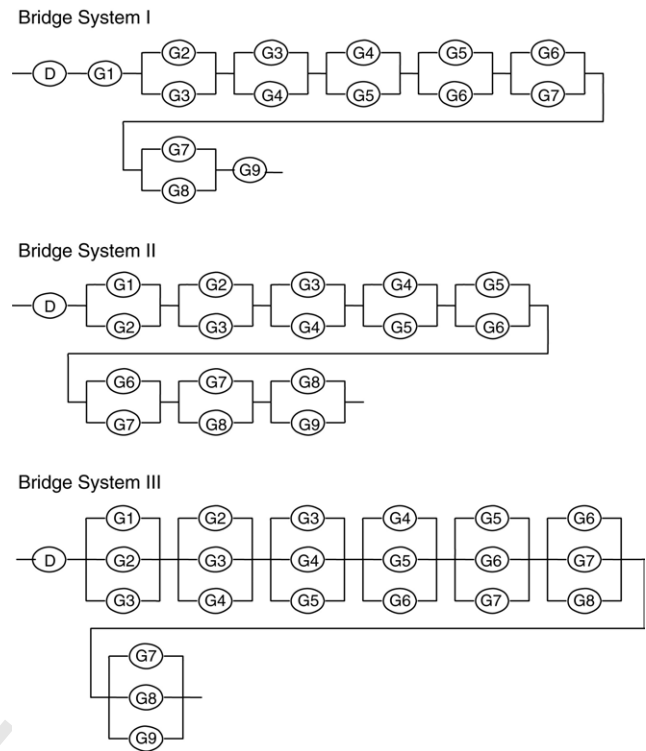


Fig. 12. System models for bridge E-17-AH.

considered for this bridge as well as the associated costs are
 presented in Table 1 [7].

Table 1
 Maintenance actions and their associated costs [7]

Maintenance identification (1)	Maintenance action (2)	Cost (1996 US\$) (3)
1	Replace deck	\$225,600
2	Replace exterior girders	\$229,200
3	Replace deck and exterior girders	\$341,800
4	Replace superstructure	\$487,100

In order to obtain the optimum maintenance strategy, it
 is necessary to establish the minimum acceptable system
 probability of occurrence of a defect of severity 4. In this
 study, this minimum acceptable system probability level
 is assumed to be 10^{-2} and the target service life is 75
 years. All possible combinations of maintenance actions are
 considered in order to increase the service life to 75 years
 with the target system probability of 10^{-2} .

For comparing funds spent at different times the present
 value of cost

$$C_{PV} = \frac{C}{(1 + v)^t} \quad (10)$$

must be used, where C_{PV} = present value of maintenance
 cost, C = cost of maintenance action at time of application,
 v = discount rate of money, and t = time of application of

1 maintenance. Historically, discount rates oscillate between
 2 2% and 8% [22]. In this study discount rates of 0, 2, 4, 6, and
 3 8% are used. The optimization procedure is described next
 4 for a discount rate of 2%. However, results are provided for
 5 all values of discount rate considered.

6 For case I (see Fig. 12), system failure is defined as a
 7 severity 4 defect being found in the deck, or in an external
 8 girder, or in any two adjacent interior girders. As a result,
 9 the deck and the exterior girders have a very significant
 10 reliability importance. From all systems in Fig. 12 system
 11 I is the less redundant and, as a result, the one for which
 12 essential maintenance is necessary sooner ($t = 12$ years). In
 13 Fig. 13, the four possible maintenance actions (1, 2, 3, and
 14 4 in Table 1) at year 12 are compared in terms of lifetime
 15 extension and present value of cost using a discount rate
 16 of money of $\nu = 2\%$. Comparing the present value of
 17 cost of each maintenance option per year of increase of
 18 service life (i.e., the cost effectiveness) the optimum action
 19 at time $t = 12$ years is replacement of deck and exterior
 20 girders (maintenance action 3). After applying maintenance
 21 action 3 at year 12, a second maintenance action must be
 22 applied at year 24. At this time the interior girders are
 23 more deteriorated than the other components and must be
 24 replaced. As a result, at $t = 24$ years, maintenance action 4
 25 (replacement of superstructure) is chosen. The replacement
 26 of all components leads to a repetition of the lifetime
 27 function observed in the first 24 years (Fig. 14). As a result,
 28 cyclic maintenance composed of action 3 followed by action
 29 4 is applied until year 72. At this time a less expensive
 30 maintenance action (action 2 in Table 1) is suitable to
 31 extend the service life beyond the time horizon (75 years).
 32 The resulting system probability of occurrence of defect 4
 33 associated with the optimum maintenance strategy 3@12,
 34 4@24, 3@36, 4@48, 3@60, and 2@72 (where 3@12 means
 35 maintenance action 3 applied at year 12) is shown in Fig. 14.
 36 The present value of the maintenance cost associated with
 37 this strategy, considering 2% discount rate, is \$1,083,174
 38 (1996 US\$).

39 For case II in Fig. 12, system failure is defined as finding
 40 a severity 4 defect in the deck or in any two adjacent girders.
 41 In this system model no distinction between interior girders
 42 and exterior girders is made. This system is more redundant
 43 than system I and, as a result, the first maintenance action
 44 is applied later and the time interval between maintenance
 45 actions is larger (Fig. 15). As indicated in Fig. 16, the
 46 threshold system probability of 10^{-2} is achieved after 18
 47 years (instead of 12 years for system I). At this time, due
 48 to the higher reliability importance of the deck, maintenance
 49 option 1 (replacement of the deck) is optimum. At year
 50 28 a second essential maintenance action must be applied.
 51 As for case I, the girders are now more deteriorated and
 52 must be replaced. Since there is no distinction between
 53 interior and exterior girders for the reliability of this system,
 54 maintenance option 4 (replace superstructure) is optimum
 55 at this time. As all components are repaired (Fig. 16), a
 56 repetition of the lifetime function observed in the first 28

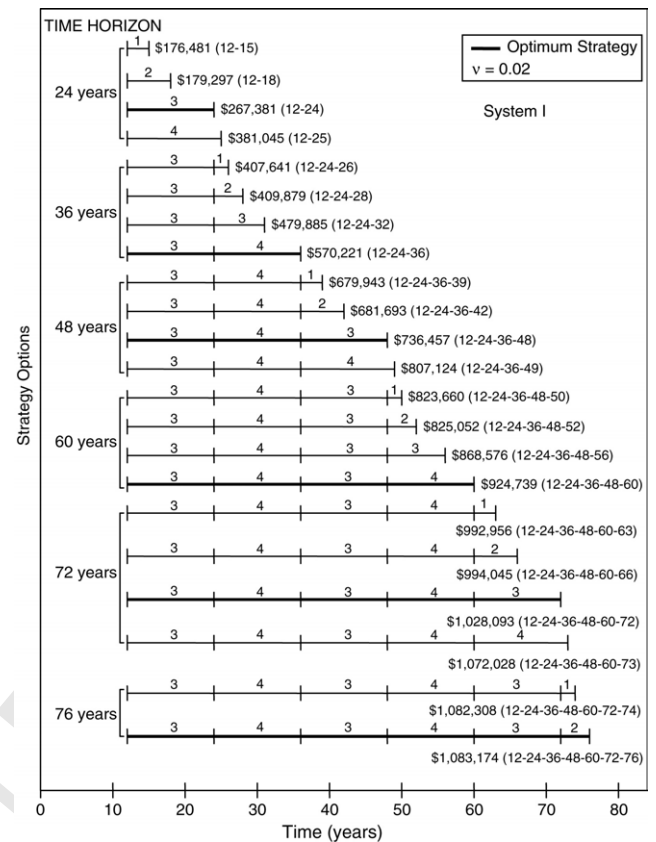


Fig. 13. Optimization of maintenance strategy for bridge system I.

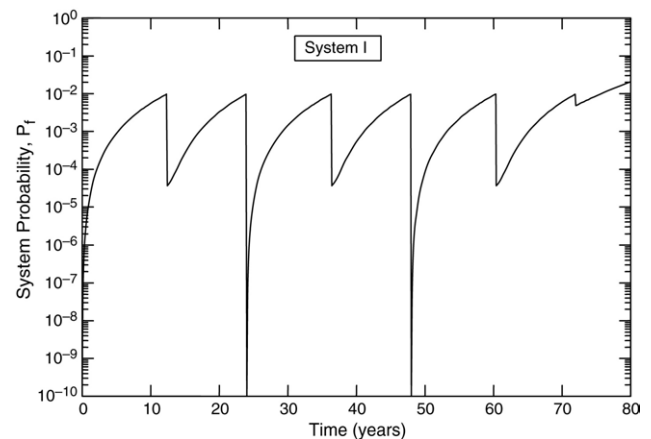


Fig. 14. System probability of occurrence of severity defect 4 under optimum maintenance strategy for bridge system I.

years occurs. As a result, a cycle composed by maintenance
 action 1 followed by action 4 is repeated until the service
 life is greater or equal to the time horizon of 75 years (see
 Fig. 15).

Finally, for case III, system failure is defined as finding
 a severity 4 defect in the deck or in any three adjacent
 girders. For this system model, analyzed in [25], the results
 are presented in Figs. 17 and 18.

In Table 2, the present values of optimum lifetime cost of
 the three system models in Fig. 12 are presented considering

Table 2
Comparison of optimum costs for different bridge system models and discount rates

Bridge system model (1)	Optimum lifetime maintenance cost (1996 US\$)				
	$\nu = 0\%$ (2)	$\nu = 2\%$ (3)	$\nu = 4\%$ (4)	$\nu = 6\%$ (5)	$\nu = 8\%$ (6)
I	2,228,800	1,083,174 ^a	601,910	370,528	245,476
II	1,651,000	739,098 ^b	375,560	209,997	125,682
III	1,163,900	526,453 ^c	268,039	149,320	88,949

^a See Figs. 13 and 14.
^b See Figs. 15 and 16.
^c See Figs. 17 and 18.

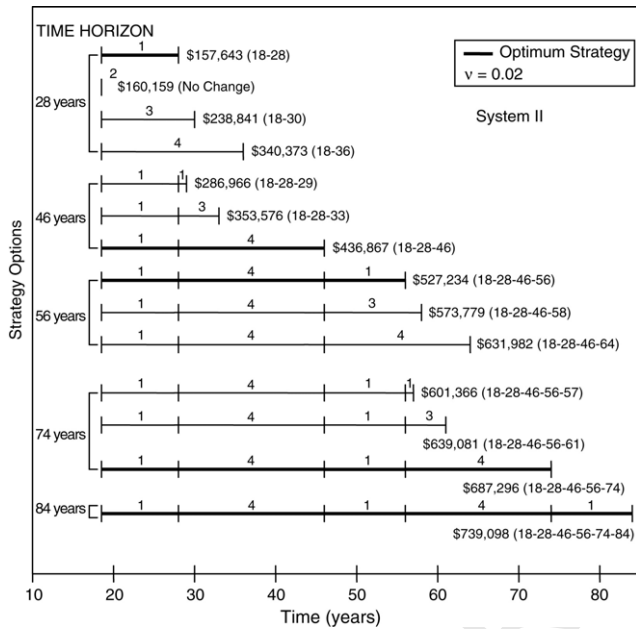


Fig. 15. Optimization of maintenance strategy for bridge system II.

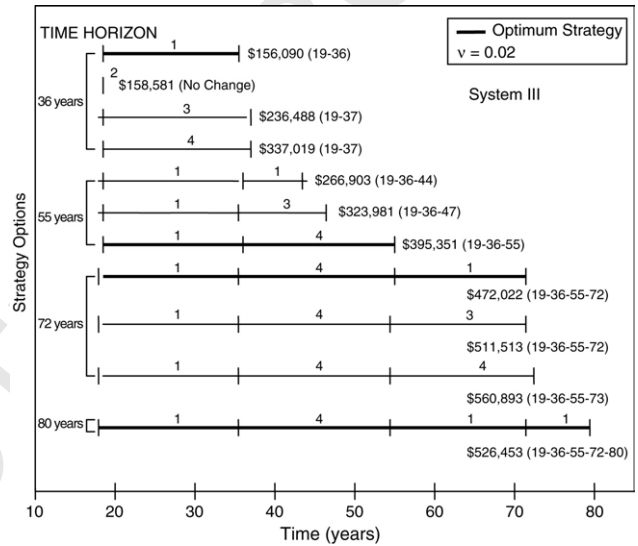


Fig. 17. Optimization of maintenance strategy for bridge system III.

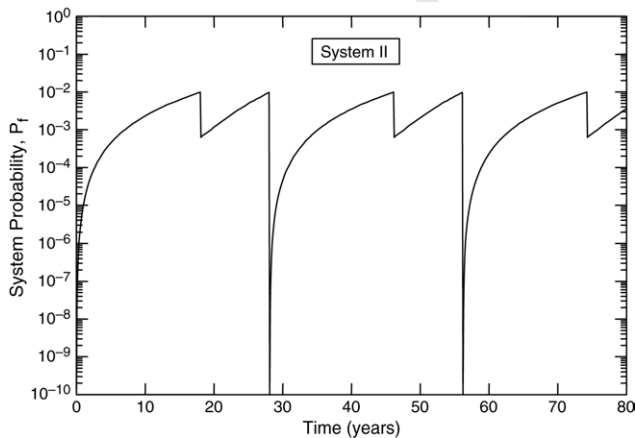


Fig. 16. System probability of occurrence of severity defect 4 under optimum maintenance strategy for bridge system II.

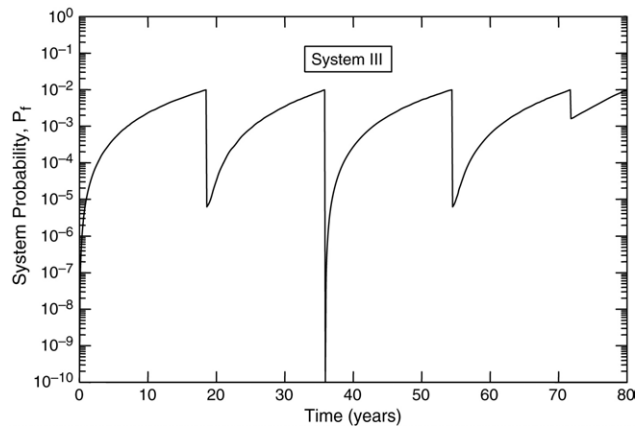


Fig. 18. System probability of occurrence of severity defect 4 under optimum maintenance strategy for bridge system III.

1 discount rates of 0, 2, 4, 6, and 8%. As expected, the increase
2 in redundancy from system I to III is accompanied by a
3 significant decrease in cost. It is also noted that there is a

significant change in the present values of optimum lifetime
cost due to the discount rate.

6. Conclusions

In this study, a model for predicting the evolution in time of the reliability of deteriorating structures based on lifetime functions is presented. The approach discussed in this paper complements that presented in [25,26]. The effects of proactive, reactive, and essential maintenance on components and systems are studied and models for incorporating these effects in the analysis of deteriorating structures using lifetime functions are discussed.

In this paper, a binary performance indicator is used to decide on the best maintenance strategy for deteriorating structures. This approach is less accurate than the continuous damage model approach, but can be implemented using the information currently available on most structures. Lifetime functions proved to be adequate to model the evolution in time of the performance of deteriorating structures under the effect of maintenance actions. The uncertainty in the lifetime of deteriorating components is captured through Weibull and exponential distributions.

The optimization process based on lifetime functions produces an optimum lifetime maintenance strategy for initial planning purposes. It is therefore important for the optimized plan to be updated based on inspection results [7].

The proposed model is applied to an existing bridge in Denver, Colorado. Several system models, each corresponding to different damage-tolerant policies, are considered for the bridge superstructure and the optimum maintenance strategy for each of these models is computed. The results obtained show significant changes in the optimum strategy and the associated present value of cumulative cost among different system models. Therefore, a correct definition of the system model is crucial in the design, assessment and optimum maintenance planning for deteriorating structures. The present value of cumulative cost of optimum maintenance scenarios, for all system models, is very sensitive to the discount rate.

The use of an analytical model alone is not, however, sufficient to provide an accurate prediction of the future performance of a structure. The optimization of bridge maintenance actions must combine both analytical models and the results obtained from non-destructive tests and visual inspections. In this study, only historical records from visual inspections on similar bridges are used. However, more accurate assessment and prediction of performance will be possible if the results provided by this model are updated using health monitoring information.

Acknowledgements

The partial financial support of the U.S. National Science Foundation through grants CMS-9912525 and CMS-0217290 is gratefully acknowledged. The support provided by the Colorado Department of Transportation and by the Dutch Ministry of Transportation, Public Works, and

Water Management is also gratefully acknowledged. The opinions and conclusions presented in this paper are those of the writers and do not necessarily reflect the views of the sponsoring agencies.

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