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DOI
10.1016/j.physletb.2022.137390

Publication date
2022

Document Version
Final published version

Published in
Physics Letters, Section B: Nuclear, Elementary Particle and High-Energy Physics

Physics Letters B 833 (2022) 137390

Contents lists available at ScienceDirect

Physics Letters B

www.elsevier.com/locate/physletb

The soft drop momentum sharing fraction z_g beyond leading-logarithmic accuracy

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ARTICLE INFO

Article history:
Received 15 August 2022
Accepted 16 August 2022
Available online 19 August 2022
Editor: B. Grinstein

ABSTRACT

Grooming techniques, such as soft drop, play a central role in reducing sensitivity of jets to e.g. underlying event and hadronization at current collider experiments. The momentum sharing fraction z_g, of the two branches in a jet that pass the soft drop condition, is one of the most important observables characterizing a collinear splitting inside the jet, and directly probes the QCD splitting functions. In this work, we present a factorization framework that enables a systematic calculation of the corresponding cross section beyond modified leading-logarithmic (MLL) accuracy, showing that this measurement is not only sensitive to the QCD charge but also the spin of the parton that initiates the jet. Our results at next-to-leading logarithmic (NLL′) accuracy include non-global logarithms, and provide a first meaningful assessment of the perturbative uncertainty. We present a comparison to the available experimental data from ALICE, ATLAS, and STAR and find excellent agreement.

1. Introduction

At high-energy collider experiments, jets and their substructure play a central role in probing fundamental aspects of QCD and searching for physics beyond the standard model [1–3]. Jet grooming techniques [4–8] are designed to remove soft radiation inside jets, crucially reducing contamination in the complicated environment of hadron colliders. These techniques will become even more important during the high-luminosity era of the LHC. Grooming algorithms can also lead to significantly reduced nonperturbative (hadronization) corrections, allowing for direct and precise comparisons between theory and data, see e.g. Refs. [9–11].

In this letter, we study the soft drop grooming algorithm [8]. After reclustering a jet with the Cambridge/Aachen (C/A) [12,13] algorithm, it iteratively declusters the jet, at each step removing the softer branch if its momentum fraction z fails the soft drop condition

$$z > z_{\rm cut}\,(\Delta R_{12}/R)^{\beta}\ . \tag{1}$$

Here, ΔR_{12} is the distance between the branches in the y-ϕ plane, R is the radius of the initial ungroomed jet, and $z_{\rm cut}$, β are tuneable grooming parameters. (Soft drop grooming with $\beta = 0$ corresponds to the modified mass drop tagger [6].) Once Eq. (1) is satisfied, the algorithm terminates and $z_g = z$ and $R_g = \Delta R_{12}$, as illustrated in Fig. 1. Both z_g and R_g are central to characterizing the two hard branches of the groomed jet.

The momentum sharing fraction z_g has received a lot of attention by both the theoretical and experimental particle and nuclear physics communities in the past years. The main reason is that it allows for the closest to a direct measurement of the QCD (Altarelli-Parisi) splitting functions [14], providing a glimpse into fundamental splittings at parton level. The cross section differential in z_g was measured by the ALICE [15,16], ATLAS [11], CMS [17,18] collaborations at the LHC and by STAR [19] at RHIC, which we compare to in this work. In addition, the z_g distribution was also extracted from CMS open data [20,21].

This measurement is not only sensitive to the color charge but also the spin of the parton initating the jet. Our precision is essential to have sensitivity to this effect in interpreting experimental results. The momentum sharing fraction is also of great interest for heavy-ion collisions, as it probes modifications of hard-collinear splittings in the quark-gluon plasma. For recent theoretical results, see Refs. [22–29]. We also expect z_g to be of great phenomenological importance at the future Electron-Ion Collider (EIC) [30].

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https://doi.org/10.1016/j.physletb.2022.137390

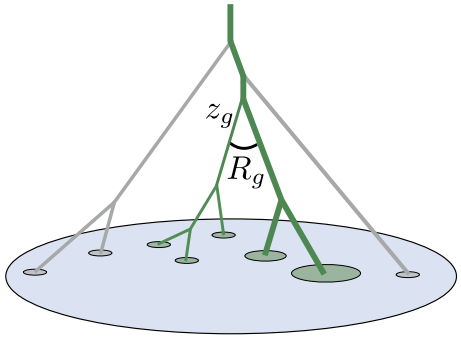

Fig. 1. Illustration of the clustering tree of a jet: Branches are groomed away (grey) until the soft drop condition in Eq. (1) is first satisfied. This splitting sets the observables z_g and R_g, and subsequent splittings (green) are kept.

The observable z_g was first introduced in Ref. [31], where a calculation of the corresponding cross section at leading-logarithmic (LL) accuracy was performed. This result was extended to modified LL (MLL) in Refs. [20,21]. It was found that z_g is Infrared-Collinear (IRC) safe only for $\beta < 0$. For $\beta \geq 0$, z_g is IRC unsafe but calculable: the IRC divergence is tamed by accounting for the Sudakov suppression, making z_g a Sudakov safe observable [32]. The cross section can thus be calculated by performing the joint resummation of the logarithms of z_g and the groomed radius R_g. Alternatively, one can impose a cut on R_g, but this case also requires resummation. Here we extend the work of Ref. [31] by setting up a factorization framework within Soft Collinear Effective Theory (SCET) [33–37], which allows for the systematic extension beyond LL. We obtain results at next-to-leading logarithmic (NLL′) accuracy, accounting for non-global logarithms (NGLs) [38]. Our work also provides the first meaningful assessment of perturbative uncertainties, and opens the door to future calculations at higher perturbative accuracy and for a systematic treatment of nonperturbative effects [39,40]. Theoretical calculations of other groomed observables, such as the groomed jet mass, can be found in Refs. [41–57].

2. Theoretical framework

We now describe how we calculate the cross section differential in the jet's transverse momentum p_T and rapidity η, as well as the groomed jet substructure observables z_g and $\theta_g \equiv R_g/R$. For small jet radii, we can separate the production of the inclusive jet sample from the jet substructure measurement using collinear factorization,

$$\frac{\mathrm{d}\sigma}{\mathrm{d}p_T\,\mathrm{d}\eta\,\mathrm{d}z_g\,\mathrm{d}\theta_g} = \sum_i f_i(p_T,\eta,R,\mu) \times \tilde{\mathcal{G}}_i(z_g,\theta_g,p_T R,z_{\mathrm{cut}},\beta,\mu)\,. \tag{2}$$

The jet production is summarized by quark/gluon fractions $f_{i=q,g}$, which account for parton distribution functions, the hard-scattering, and semi-inclusive jet functions. The jet functions $\tilde{\mathcal{G}}_i$ (using the notation of Ref. [56]) encode the substructure measurement. See Refs. [56,58–64] for more details on this first step of the factorization.

Next, we calculate the jet function $\tilde{\mathcal{G}}_i$, which we will need to describe the region where z_g is order one. We find at leading order (LO) for $z_g, \theta_g > 0$

$$\tilde{\mathcal{G}}_q^{(1)} = \Theta(1/2 > z_g > z_{\mathrm{cut}}\theta_g^\beta)\,\Theta(\theta_g < 1) \frac{\alpha_s}{\pi}\frac{1}{\theta_g}\big[P_{qq}(z_g) + P_{gq}(z_g)\big], \tag{3}$$

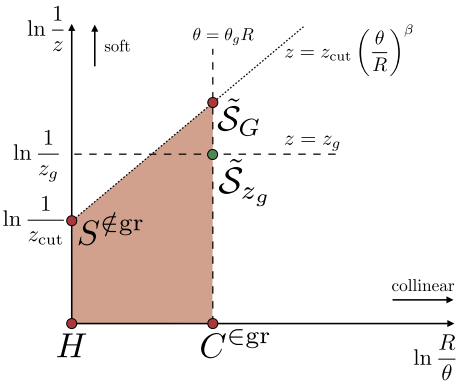

Fig. 2. Lund diagram for the cross section differential in z_g and θ_g. The green dot corresponds to the emission passing the soft drop condition, and emissions in the red area are vetoed. The modes that appear in the corresponding SCET calculation are indicated by green and red dots.

and similarly for $\tilde{\mathcal{G}}_g^{(1)}$. Here P_{ij} are the leading-order QCD splitting functions, showing that the measurement of z_g probes these. Since $\tilde{\mathcal{G}}_i^{(1)} \sim 1/\theta_g$, and there is no lower bound on θ_g for $\beta \geq 0$, we cannot integrate out the dependence on θ_g in this case. The integration over θ_g is only possible after taking into account the Sudakov suppression through resummation.

To achieve this, we perform the resummation of large logarithmic corrections of z_g, θ_g and z_{cut}. We start with the result at LL accuracy, which provides physical intuition and helps identify the relevant modes in SCET. It is described by strongly-ordered emission of gluons in the collinear and soft limit. The Lund diagram in Fig. 2 shows the phase space of such emissions in terms of their energy fraction z and angle θ, with dashed lines indicating the soft drop condition in Eq. (1) and the measurement of θ_g and z_g. The emission at the green dot sets z_g and θ_g. Emissions in the red region are not allowed, and the corresponding area enters in the Sudakov exponent:

$$\tilde{\mathcal{G}}_i = \Theta(1/2 > z_g > z_{\mathrm{cut}}\theta_g^\beta)\frac{2\alpha_s C_i}{\pi}\frac{1}{z_g\,\theta_g} \times \exp\left(-\frac{\alpha_s C_i}{\pi}(\beta\ln^2\theta_g + 2\ln z_{\mathrm{cut}}\ln\theta_g)\right), \tag{4}$$

Here $C_{i=F,A}$ denotes the appropriate color factor for quarks and gluons, which is the only dependence on the initial parton at LL. As Eq. (4) indicates, it is now safe to integrate over θ_g due to the Sudakov suppression, and the resulting expression agrees with Eq. (14) of Ref. [31]. We note that θ_g is the natural choice as the auxiliary variable here due to the angular structure of the C/A reclustered jet. We have checked that other auxiliary observables like the jet mass are not sufficient to achieve the correct resummation even at LL.

We can extend this result to NLL′ by identifying the relevant modes within SCET, for which the scaling of the momentum components can be read off from the location of the points in the Lund diagram in Fig. 2. We find

$$\begin{aligned}\tilde{\mathcal{G}}_i = {}& \Theta(1/2 > z_g > z_{\mathrm{cut}}\theta_g^\beta)\,\tilde{H}_i(p_T R,\mu)\,C_i^{\in\mathrm{gr}}(\theta_g p_T R,\mu) \\ & \times S_i^{\notin\mathrm{gr}}(z_{\mathrm{cut}}p_T R,\beta,\mu)\,\tilde{\mathcal{S}}_G(z_{\mathrm{cut}}\theta_g^{1+\beta}p_T R,\beta,\mu) \\ & \times S_i^{\mathrm{NG}}(z_{\mathrm{cut}})\bigg[\frac{\mathrm{d}}{\mathrm{d}z_g}\frac{\mathrm{d}}{\mathrm{d}\theta_g}\tilde{\mathcal{S}}_{z_g}(z_g\theta_g p_T R,\mu) \\ & + \tilde{\mathcal{S}}_{i,1}^{\prime\,\mathrm{NG}}(z_g\theta_g,z_g) + \tilde{\mathcal{S}}_{i,2}^{\prime\,\mathrm{NG}}\Big(z_g\theta_g,\frac{z_g}{z_{\mathrm{cut}}\theta_g^\beta}\Big)\bigg]. \end{aligned} \tag{5}$$

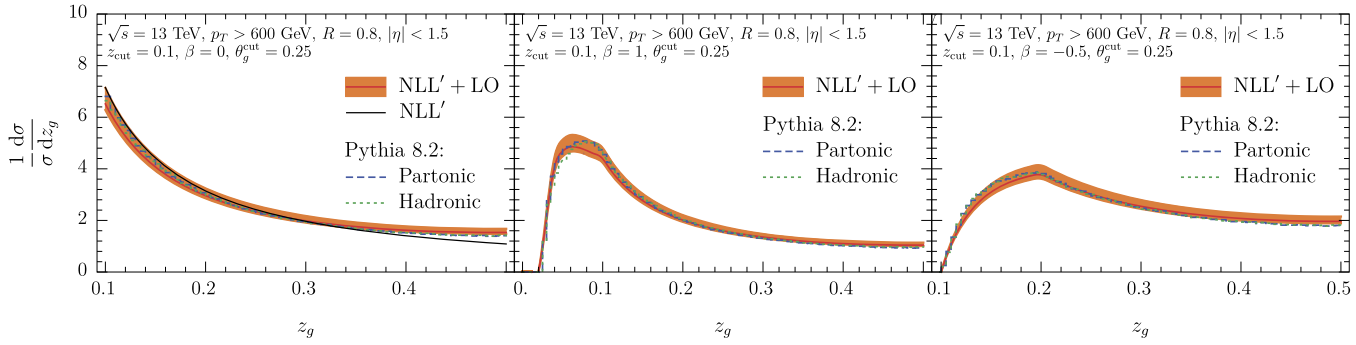

Fig. 3. Comparison of our numerical results for the momentum sharing fraction z_g at NLL′+LO to Pythia 8 simulations [65] at parton and hadron level, for representative jet kinematics and three choices of soft drop grooming parameters.

The function $\tilde{\mathcal{S}}_{z_g}$ is special, as it describes the *single* emission that sets z_g and θ_g. The collinear function $C_i^{\in \rm gr}$ describes energetic radiation at angular scales $\theta_g R$. This radiation is never groomed away, so it is constrained by the θ_g measurement. The collinear-soft radiation at the same angular scale, described by $\tilde{\mathcal{S}}_G$, is furthermore subjected to the soft-drop condition in Eq. (1). Wide-angle soft radiation is always groomed away and accounted for by $S_i^{\notin \rm gr}$. Finally, the hard function $\tilde{H}_i$ describes energetic radiation at angular scale R, and corrects for the fact that in the calculation of jet production (f_i in Eq. (2)), such radiation was unconstrained inside the jet. Except for $\tilde{\mathcal{S}}_{z_g}$, these functions also appeared in the factorization of the groomed jet radius [66], and the corresponding expressions can be found there.

The resummation of logarithms of z_g, θ_g, and $z_{\rm cut}$ is achieved by evaluating each ingredient (except those describing NGLs) at its natural scale, which can be read off from their first argument, and using the renormalization group equations (RGEs) to evolve them to a common scale μ. We set the μ scales for the cross section differential in θ_g and cumulative in z_g, and therefore present the order α_s expression and RGE for the new ingredient $\tilde{\mathcal{S}}_{z_g}$ differential in θ_g:

$$\frac{\mathrm{d}}{\mathrm{d}\theta_g}\tilde{\mathcal{S}}_{z_g}(z_g\theta_g p_T R,\mu) = -\frac{2\alpha_s C_i}{\pi}\frac{1}{\theta_g}\ln\frac{\mu}{z_g\theta_g p_T R}\,,$$
$$\frac{\mathrm{d}}{\mathrm{d}\ln\mu}\frac{\mathrm{d}}{\mathrm{d}\theta_g}\tilde{\mathcal{S}}_{z_g} = -\frac{2\alpha_s C_i}{\pi}\frac{1}{\theta_g}\,. \tag{6}$$

A similarly unusual RGE was encountered in Refs. [55,56], to which we refer the reader for details.

There are three types of non-global logarithms [38,67–76] in Eq. (5): First, the NGLs described by $S_i^{\rm NG}$ are similar to the usual hemisphere case, and arise due to correlations between the unconstrained emissions in the region outside the jet and the radiation inside the jet that fails the grooming condition. Second, the NGLs $\mathcal{S}'^{\rm NG}_{i,1,2}$ arise from correlated emissions, where one sets z_g and θ_g (green dot) and the other is either outside the groomed radius and fails the grooming condition or inside the groomed radius and is unconstrained (corresponding to one of the two red dots on the vertical dashed line $\theta = \theta_g R$ in Fig. 2). These NGLs are sensitive to C/A clustering effects [77–79]. We include their leading contribution at order α_s^2,

$$\tilde{\mathcal{S}}'^{\rm NG,(2)}_{i,1}(z_g\theta_g, z_g) = 2.58 C_i C_A \left(\frac{\alpha_s}{2\pi}\right)^2 \frac{1}{z_g\theta_g}\ln z_g\,, \tag{7}$$

and the form of $\tilde{\mathcal{S}}'^{\rm NG,(2)}_{i,2}$ is the same at this order. In our numerical implementation these NGLs are multiplied by the global Sudakov suppression factor, see Eq. (5), making their numerical size small (percent level).

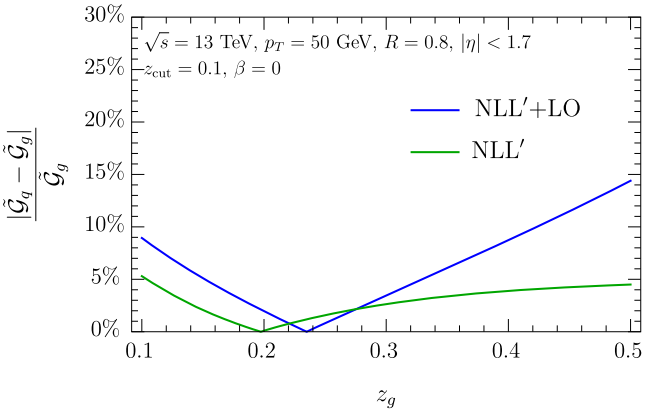

Fig. 4. Relative difference between the z_g distribution for quark and gluon-initiated jets. The difference between the green and blue curve indicates the size of the non-singular part of the QCD splitting function, encoding the spin-dependence.

3. Numerical results and comparison to data

Throughout this section we consider (ungroomed) jets which are reconstructed with the anti-k_T algorithm [80], as in the measurement of the experimental collaborations. We use the parton distribution functions of Ref. [81].

We start by comparing our numerical results at NLL′+LO accuracy to Pythia 8 simulations [65]. The comparison for exemplary jet kinematics is shown in Fig. 3. We choose three representative values of the grooming parameter β and impose a cutoff on the groomed jet radius of $\theta_g^{\rm cut} > 0.25$ to reduce the sensitivity to nonperturbative physics. The QCD scale uncertainty bands in the figures shown here are obtained by independently varying all relevant scales in Eqs. (2) and (5) by a factor of 2 around the central scale choice. In addition, we smoothly freeze all scales at $\mathcal{O}(1\ \text{GeV})$ [82]. The hadronization corrections for the chosen kinematics are very small which can be seen by comparing Pythia results at parton and hadron level.

Overall, we observe very good agreement of our results with Pythia. In addition to the improved precision, there are notable qualitative differences with the earlier results of Ref. [31]: The shape of our distribution for $\beta < 0$ is rather different, and we find a smooth transition to $\beta = 0$ for $z_g > z_{\rm cut}$, whether we approach from negative or positive β. This qualitative difference stems from our inclusion of additional logarithms[1] and the matching to LO given in Eq. (3). We also find that the cut imposed on θ_g gives our calculation greater perturbative stability, while qualitatively chang-

[1] We count logarithms L in the exponent. Schematically, $\ln\sigma \sim \alpha_s^n L^m$ with $m \leq n+1$.

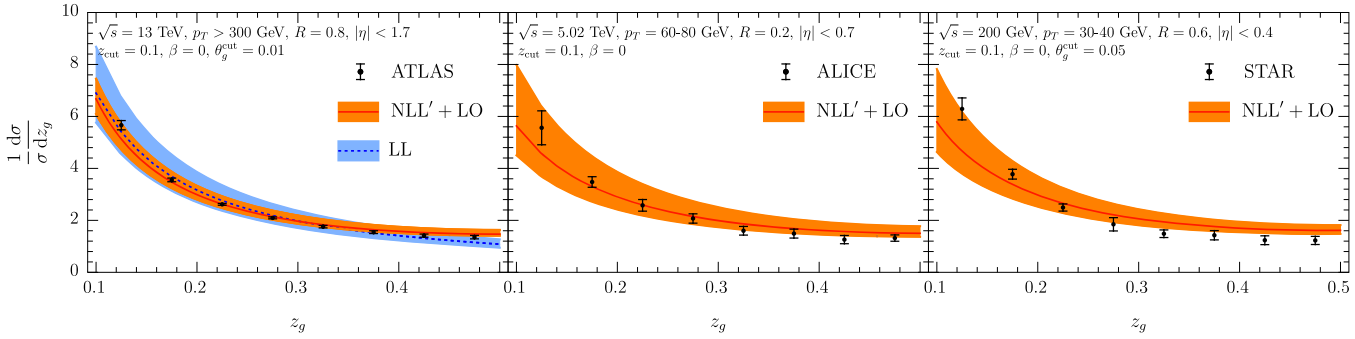

Fig. 5. Comparison of our results to ATLAS [11], ALICE [16] and STAR [19] data for $\beta = 0$.

ing the result as well. Although Ref. [31] did include the full QCD splitting function, the improved theoretical uncertainties and accuracy achieved here allow us to assess the size of the spin dependent contribution. For large z_g the matching to the LO in Eq. (3) is essential, which is done multiplicatively because of the common singularity in θ_g. Indeed, the non-singular terms added by the matching are important to achieve good agreement with Pythia, as illustrated in the left panel of Fig. 3 by the black NLL′ curve (that does not include the matching). This demonstrates the sensitivity of z_g distribution to the full splitting function beyond the leading $1/z_g$ behavior in the singular limit. The size of these corrections, which encode the spin-dependence of the splitting function, are visualized in Fig. 4. Since their size can be up to order 10%, we expect that this can be probed experimentally by for example comparing inclusive vs. photon-tagged jets or jets with different rapidities.

Next, we compare to the experimental results from ATLAS [11], ALICE [16] and STAR [19] for $\beta = 0$ in Fig. 5. We normalize our results to the data[2] and impose the same cut on θ_g. The hadronization effects in Pythia for ALICE and STAR kinematics (not shown) are much more sizable than in Fig. 3, in accord with the larger perturbative uncertainties. Nevertheless, we find very good agreement even for these relatively low jet transverse momenta. We note that the CMS result of Ref. [17] is not unfolded, prohibiting a direct comparison. As a representative example, we show the LL QCD scale uncertainty band in the left panel of Fig. 5 which is significantly larger than at NLL′. This implies that the NLL′ accuracy achieved in this work is needed to match the current experimental precision.

Next, we compare in Fig. 6 our results to ATLAS measurement [11] for $\beta = 1$, as an example. We normalize our results to the data in the region to the right of the dotted line, as our prediction for the left most data point is very sensitive to nonperturbative effects. Note that this was not needed for $\beta = 0$, where $z_{\rm cut}$ provides a lower bound on z_g. We observe excellent agreement! In this case our NLL′+LO prediction is substantially better than the LL result.

Lastly, we present predictions for jet kinematics at the future EIC in Fig. 7. We consider jets reconstructed in the laboratory frame $ep \to e + \text{jet} + X$ for typical EIC kinematics [83,84] with cuts on the photon virtuality Q^2 and the inelasticity y as indicated in the figure. The clean environment at the EIC will allow studies of hadronization effects, and z_g measurements in single- and di-jet events can help improve our understanding of quark/gluon differences (see also Fig. 4).

[2] The ALICE normalization is not normalized by a few percent, because of their treatment of jets that never pass the soft drop condition.

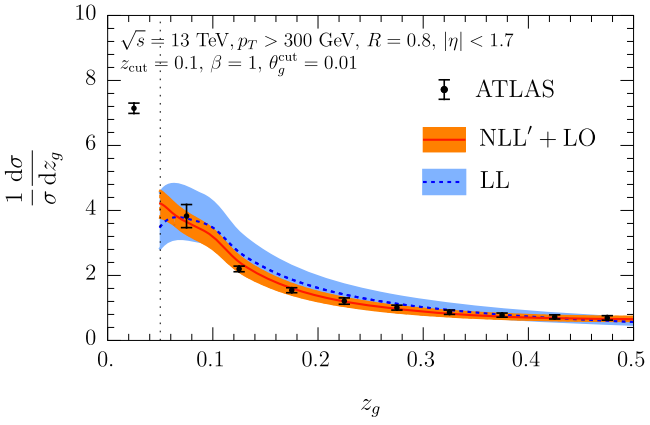

Fig. 6. Comparison to ATLAS results [11] for $\beta = 1$.

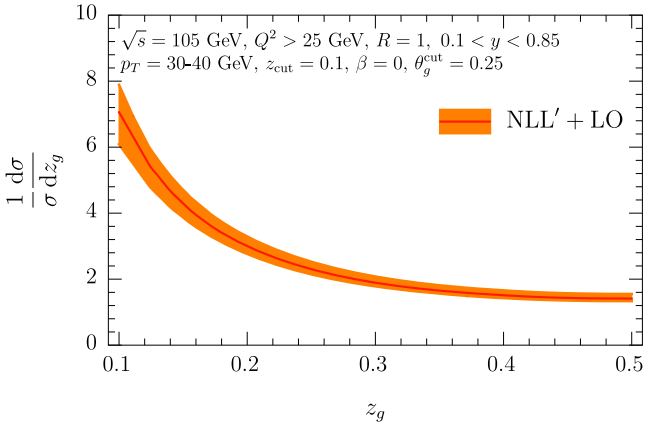

Fig. 7. Prediction for the Electron-Ion Collider.

4. Conclusions

In this work we have presented a calculation of the soft drop groomed momentum sharing fraction z_g at NLL′+LO accuracy. This Sudakov-safe jet substructure observable, which probes the hard branching process inside the jet, constitutes the closest to a direct measurement of the QCD splitting function. Our framework allows for a systematic extension beyond the previously achieved MLL accuracy, yielding qualitatively different results for $\beta < 0$ than in an earlier study, and provides the first meaningful assessment of theoretical uncertainties. Because z_g probes the full QCD splitting function, it is sensitive to the spin of the particle that initiates the jet. This effect is sufficiently large, and our calculations are sufficiently precise, to resolve it experimentally. The momentum sharing fraction z_g is one of the hallmark observables in the field

of jet substructure and has been measured by several experimental collaborations at the LHC and RHIC. We compared to the available experimental data and found very good agreement with our purely perturbative calculation. In addition, we provided predictions for the future Electron-Ion Collider. Our precise calculations with reliable uncertainty estimates are in excellent agreement with the data.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

Acknowledgements

We thank Yi Chen, Raghav Elayavalli, Matt LeBlanc, Yen-Jie Lee, Ezra Lesser, James Mulligan, Ben Nachman, Mateusz Ploskon, Jennifer Roloff, and Marta Verweij for helpful discussions. We also thank Andrew Larkoski and Jesse Thaler for feedback on our manuscript. PC and WW are supported by the ERC grant ERC-STG-2015-677323, the NWO projectruimte 680-91-122 and the D-ITP consortium, a program of NWO that is funded by the Dutch Ministry of Education, Culture and Science (OCW). KL is supported by the US Department of Energy, Office of Nuclear Physics. FR is supported by the US Department of Energy under Contract No. DE-AC02-05CH11231 and the LDRD Program of LBNL.

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