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Evidence for a high-energy tail in the gamma-ray spectra of globular clusters

Deheng Song¹, Oscar Macias^{1,2,3}, Shunsaku Horiuchi¹, Roland M. Crocker⁴ and David M. Nataf⁵

¹Center for Neutrino Physics, Department of Physics, Virginia Tech, Blacksburg, VA 24061, USA

²Kavli Institute for the Physics and Mathematics of the Universe (WPI), University of Tokyo, Kashiwa, Chiba 277-8583, Japan

³GRAPPA Institute, Institute of Physics, University of Amsterdam, NL-1098 XH Amsterdam, the Netherlands

⁴Research School of Astronomy and Astrophysics, Australian National University, Canberra, ACT 2611, Australia

⁵Center for Astrophysical Sciences and Department of Physics and Astronomy, The Johns Hopkins University, Baltimore, MD 21218, USA

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ABSTRACT

Millisecond pulsars are very likely the main source of gamma-ray emission from globular clusters. However, the relative contributions of two separate emission processes – curvature radiation from millisecond pulsar magnetospheres versus inverse Compton emission from relativistic pairs launched into the globular cluster environment by millisecond pulsars – have long been unclear. To address this, we search for evidence of inverse Compton emission in 8-yr *Fermi*–LAT data from the directions of 157 Milky Way globular clusters. We find a mildly statistically significant (3.8σ) correlation between the measured globular cluster gamma-ray luminosities and their photon field energy densities. However, this may also be explained by a hidden correlation between the photon field densities and the stellar encounter rates of globular clusters. Analysed in toto, we demonstrate that the gamma-ray emission of globular clusters can be resolved spectrally into two components: (i) an exponentially cut-off power law and (ii) a pure power law. The latter component – which we uncover at a significance of 8.2σ – has a power index of 2.79 ± 0.25 . It is most naturally interpreted as inverse Compton emission by cosmic-ray electrons and positrons injected by millisecond pulsars. We find the luminosity of this power-law component is comparable to, or slightly smaller than, the luminosity of the curved component, suggesting the fraction of millisecond pulsar spin-down luminosity into relativistic leptons is similar to the fraction of the spin-down luminosity into prompt magnetospheric radiation.

Key words: pulsars: general – globular clusters: general – gamma-rays: general.

1 INTRODUCTION

Over two dozen globular clusters (GCs) have been detected in γ rays in *Fermi* Large Area Telescope (LAT) data (Abdo et al. 2009a, 2010; Kong, Hui & Cheng 2010; Tam et al. 2011; Zhou et al. 2015; Zhang et al. 2016). The millisecond pulsar (MSP) populations of those GCs are believed to be the main source of this γ -ray emission. In particular, MSPs have been firmly established as γ -ray sources (Verbunt et al. 1996; Abdo et al. 2009b; Abdo et al. 2013; Espinoza et al. 2013) and a large fraction of them have been discovered in GCs (Camilo & Rasio 2005). Recently, *Fermi*–LAT detected γ -ray pulsations in two GCs (Freire et al. 2011; Johnson et al. 2013), providing further support for this scenario.

The high-energy emission from MSPs emerges from the primary electrons accelerated by them and subsequent radiation by secondary, relativistic electrons and positrons (e^\pm) pair created in their magnetospheres. In particular, Harding, Usov & Muslimov (2005) studied the curvature radiation (CR) of primary electrons within MSP magnetospheres with a focus on GeV-scale emission. Bednarek & Sitarek (2007) then considered a scenario in which e^\pm , injected by

MSPs, gradually diffuse through a GC, upscattering ambient photons, and thus producing inverse Compton (IC) γ -ray emission in the GeV–TeV energy range. Venter, De Jager & Clapson (2009) calculated the CR and IC spectra for an ensemble of MSPs in the GCs 47 Tucanae and Terzan 5. Cheng et al. (2010) found that the spectra of 47 Tucanae and seven other GCs can be explained by IC alone, invoking background photons from the cosmic microwave background (CMB) or Galactic infrared/stellar radiation. For a review of the observations and models about the γ -ray emission from globular clusters, see Tam, Hui & Kong (2016). In general, the GeV emission mechanism of MSPs remains in contention with CR, IC, and synchrotron radiation all proposed (Harding 2021).

Here, motivated by the increasing number of GCs detected in γ -rays, we perform a collective statistical study of their properties in order to gain insight into the nature of their high-energy emission. Our particular aim is to investigate the importance of the contribution of IC emission to the overall γ -ray emission of GCs.

Relations between the detected GC gamma-ray luminosities and properties of GC can be used to probe the origins of γ -ray emission and their underlying sources. For example, correlations with the photon field energy density of GCs could unveil the potential contribution from IC, and correlations with the stellar encounter rate and metallicity could provide insight into the dynamical formation of MPSS in GCs. Previous work here includes a study by Abdo et al.

* E-mail: dhsong@vt.edu (DS); o.a.maciasramirez@uva.nl (OM); horiuchi@vt.edu (SH)

(2010) that reported a correlation between the γ -ray luminosity L_γ and the stellar encounter rate of eight GCs. Hui et al. (2011) studied a group of 15 γ -ray emitting GCs with 2 yr of Fermi data and found a positive correlation between L_γ and, respectively, encounter rate, metallicity, and Galactic photon energy density. Hooper & Linden (2016) studied 25 GCs using 85 months of Fermi data, and found that the γ -ray luminosity function of MSPs in GCs is consistent with that applying to MSPs detected in the field. Lloyd, Chadwick & Brown (2018) studied γ -ray emission from high-latitude GCs and its connection to their X-ray emission. de Menezes, Cafardo & Nemmen (2019) reanalysed 9 yr of Fermi data and found 23 γ -ray emitting GCs; they found that the metallicity only mildly contributes to L_γ while a very high encounter rate seemed to reduce the L_γ from GCs.

In parallel, modelling of GCs' observed broad-band spectral energy distributions provides a handle on their CR and IC emissions. Recently, Kopp et al. (2013) and Ndiyavala et al. (2019) modelled the multiwavelength emission from MSPs considering a potential CR origin for GeV and IC emissions for TeV γ -rays, as well as synchrotron radiation for the radio and X-ray wavebands. These models are successful in explaining the multiwavelength spectra of Terzan 5. However, Terzan 5 is the only GC (perhaps) detected above TeV energies (H. E. S. S. Collaboration 2011). Detailed spectral modelling similar to that presented by Kopp et al. (2013) and Ndiyavala et al. (2019) is difficult for other GCs at present due to a lack of TeV γ -ray data. Although *Fermi*-LAT is sensitive to γ -rays of up to ≈ 1 TeV, the photon count statistics at the highest energies are very low.

In the recently published *Fermi*-LAT fourth source catalogue (Abdollahi et al. 2020) (4FGL),¹ 30 GCs have been detected in GeV γ -rays. With such a number, we can begin to carefully study the nature of the γ -ray emission from GCs through a population study. In this paper, we repeat the bin-by-bin analysis of the 4FGL data for the 157 known Milky Way GCs in the Harris (1996) catalogue.² We search for correlations between the γ -ray luminosity of the GCs and other parameters of the GCs to probe which are good proxies for the γ -ray luminosity and study potential IC contributions; to this end, we consider the photon field energy densities, the stellar encounter rate, and the metallicity of the GCs. Unlike previous studies of correlations of the GC γ -ray emissions, we consider also the upper limits placed by null detections, which we implement via a Kendall τ coefficient test statistic. Furthermore, we also look for evidence of IC from the spectra of GCs. For the first time, we implement a universal two-component model to study the spectra of γ -ray-detected GCs. The two-component model comprises a CR component, which is spectrally curved, plus an IC component modelled as a power law in the energy range of interest.

The remainder of the paper is as follows: In Section 2 we discuss the choice of GC samples and the data analysis procedure. Section 3 presents the methodology and results of our correlation analysis. Section 4 describes the spectral analysis method and reports the e^\pm injection efficiency in the GCs. We discuss the implications of our results in Section 5 and conclude in Section 6.

¹The Fermi collaboration has recently released an incremental update of the fourth source catalogue (Ballet et al. 2020) (4FGL-DR2, for Data Release 2). The new catalogue uses 10 yr of data, a 25 per cent increase with respect to the 4FGL. However, only 1 new GC (NGC 362) has been detected. Given this marginal change, we retain use of the 4FGL catalogue constructed with the 8-yr data set.

²2010 edition: <https://www.physics.mcmaster.ca/~harris/mwgc.dat>

2 γ -RAY EMISSION FROM GLOBULAR CLUSTERS

In this section, we describe our choice of GC sample and the GCs' γ -ray-related parameters. The Fermi data analysis process is reported as well. For GCs with a γ -ray counterpart in the 4FGL, we update their spectral parameters through a maximum-likelihood procedure. For those not detected in the 4FGL, we estimate their 95 per cent C.L. γ -ray upper limits.

2.1 Globular cluster sample

We consider the Harris (1996) catalogue (2010 edition), which contains identifications and basic parameters for 157 GCs in the Milky Way. Here, we reanalyse publicly available *Fermi*-LAT data from the direction of all GCs in the Harris (1996) catalogue. Fig. 1 shows the spatial distribution of the GCs. The top panel shows the projected direction of the GCs on the celestial plane while the bottom two panels display their 3D coordinates. The GCs which are detected in the 4FGL are marked by red stars while null detections are indicated by green circles. Most γ -ray GCs are near the Sun (yellow circle) or located in the Galactic bulge (assumed to be sphere of 3 kpc radius, grey circular area).

The origin of the γ -ray emission from GCs can be studied by comparing its dependence on GC properties. IC emission is sensitive to the ambient photon field on which the e^\pm scatter. Hui et al. (2011) reported a positive correlation between the γ -ray luminosity L_γ and the photon field energy density at the cluster location, indicating an IC contribution. In this work, we improve upon the Galactic radiation field model used by Hui et al. (2011) by extracting the energy density of the interstellar radiation at the locations of the GCs from the 3D interstellar radiation model in GALPROP v56³ (Porter, Jóhannesson & Moskalenko 2017; Jóhannesson, Porter & Moskalenko 2018). This is a fully 3D model that combines the CMB, infrared, and optical photons of the Milky Way, denoted as u_{MW} . In addition, photons from stars in the GCs are expected to make a dominant contribution to the total, ambient radiation field. We estimate this component by

$$u_{\text{GC}} = \frac{L_*}{4\pi cr_h^2}, \quad (1)$$

where L_* and r_h are the stellar luminosity and the half-light radius of the GC. The total photon field energy density is $u_{\text{Total}} = u_{\text{MW}} + u_{\text{GC}}$.

A potential correlation between the γ -ray luminosity L_γ and the stellar encounter rate has been studied as a way to probe the dynamic formation of MSPs in GCs (Abdo et al. 2010; Hui et al. 2011; de Menezes et al. 2019). In this work, we adopt the stellar encounter rate estimated by Bahramian et al. (2013), which is defined as

$$\Gamma_c = \frac{4\pi}{\sigma_c} \int \rho(r)^2 r^2 dr, \quad (2)$$

where σ_c is the velocity dispersion at the core radius, $\rho(r)$ is the stellar density profile of the cluster, and the line-of-sight integration is performed along the half-light radius.

Additionally, it has been argued (Hui et al. 2011; de Menezes et al. 2019) that high metallicity [Fe/H] in the GCs could enhance the dynamical formation of MSP. The outer convective zone of metal-rich stars enables magnetic braking, which assists orbital shrinking during binary formation. In this analysis, we use the

³<http://galprop.stanford.edu/>

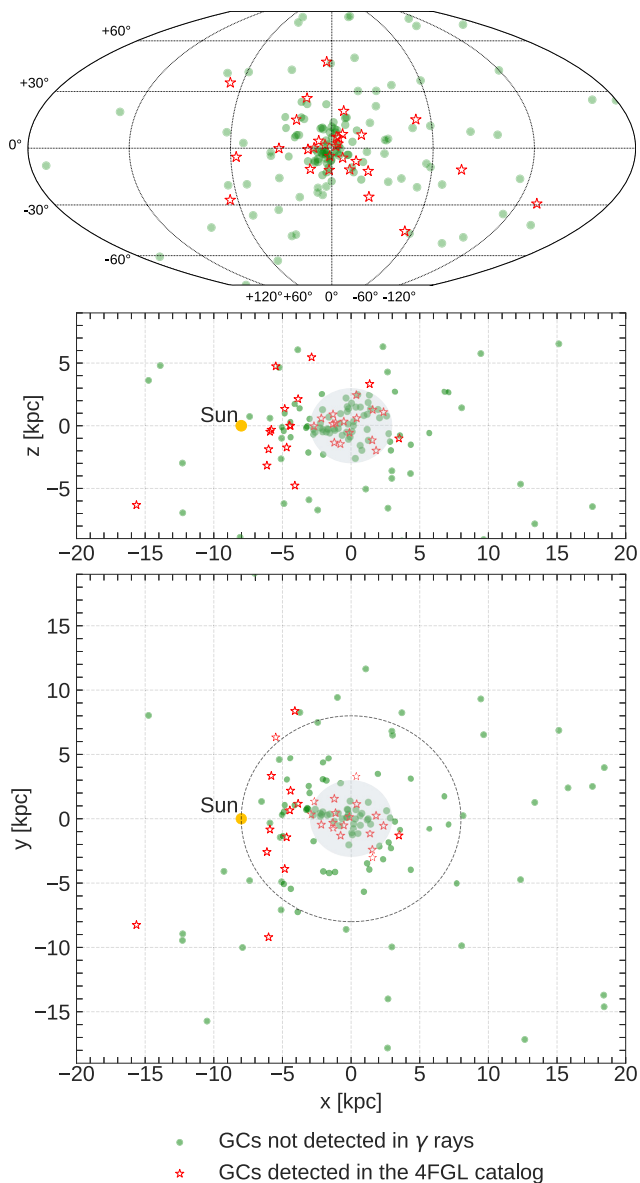


Figure 1. Spatial distribution of the 157 Milky Way GCs in the Harris (1996) catalogue. The top panel shows the all sky spatial distribution in Galactic coordinate. The middle and bottom panel display the 3D Cartesian coordinates of the GCs, in which the Sun (yellow circle) is located in the negative x -axis. The γ -ray-detected GCs in the 4FGL catalogue are shown as red stars, and the GCs not detected in γ -rays are shown as green circles. Most γ -ray-detected GCs are located near the Sun or in the Galactic bulge (grey shaded area in the middle and bottom panel).

GCs metallicities reported in the Harris (1996) catalogue, which summarizes spectroscopic or photometric estimates in the literature.

In summary, we consider the empirical dependence of the inferred γ -ray luminosity of GCs on four parameters, namely, u_{MW} , u_{Total} , Γ_c , and $[Fe/H]$. We summarize the values of these parameters for the 30 γ -ray-detected GCs in Table 1. Also included are the stellar masses M_* of the GCs adopted from Baumgardt (2017), Sollima & Baumgardt (2017), and Baumgardt & Hilker (2018). They are estimated from N -body modelling of the velocity dispersion and surface density profiles. In Section 3, we study the correlations between the γ -ray emission of GCs and these parameters.

2.2 Data analysis

We use 8 yr of *Fermi*–LAT data, from 2008 August 4 to 2016 August 2. This constitutes the same data as the 4FGL. The newest Pass 8 data release is applied. As recommended by the *Fermi*–LAT data analysis documentation,⁴ the event class for the analysis is ‘P8 Source’ class (evclass = 128) and the event type is ‘FRONT+BACK’ (evtype = 3). We use a 90° zenith angle cut to remove Earth limb events and filter the data by (DATA_QUAL>0)&&(LAT_CONFIG==1). The corresponding instrument response function is P8R3_SOURCE_V2. For our analysis, the *Fermipy* software version 0.18.0 is used, together with the *Fermi Science Tools* version 1.2.21.

For 30 GCs detected by the 4FGL, we simply reanalyse the 4FGL γ -ray source. We use a 10° by 10° region-of-interest around the source with a 0.1° by 0.1° bin size. Photons from 300 MeV to 500 GeV are analysed using 9 logarithmic bins. Given that we use a different region-of-interest size and photon class compared to those adopted in the construction of the 4FGL, additional point sources might emerge in our region-of-interest. However, since we use the same observation time as in the 4FGL, the impact of those potential new sources is expected to be minimal. Therefore, we only include known 4FGL sources in our analysis. As recommended by the Fermi team, we rerun a maximum likelihood analysis that starts from the best-fitting parameter values found in the 4FGL and updating accordingly. The most recent Galactic interstellar emission model `gll_iem_v07` and the isotropic component `iso_P8R3_SOURCE_V2_v1` are employed as fore/backgrounds with free-floating normalization. We have followed the *Fermipy* recommended procedure⁵ and fixed the spectral parameters of the sources with $TS < 10$ and $10 < N_{pred} < 100$ to their 4FGL values. However, the spectral parameters of the 4FGL sources lying within 5° of the region-of-interest centre are allowed to float freely. The MINUIT algorithm is used to determine the best-fitting parameters of the sources for each energy bin independently.

For the 127 additional GCs in the Harris (1996) catalogue without 4FGL detections, we estimate the 95 per cent C.L. γ -ray upper limits from their locations. More specifically, we place a point source at the coordinates of those GCs. The point source is assumed to have a power-law spectrum $dN/dE \sim E^{-\Gamma}$ with fixed index $\Gamma = 2$. We applied the same pipeline used on the set of detected GCs and obtained the 95 per cent C.L. flux upper limits on the putative point sources placed at the GCs locations.

Table 1 summarizes the Fermi data analysis results. We report the photon flux and luminosity L_γ for 30 γ -emitting GCs. For each GC, the total photon flux is summed over the bin-by-bin fluxes from the Fermi analysis. The statistical error of the total flux is added quadratically from the bin-by-bin flux errors. The energy flux is estimated similarly, then $L_\gamma = 4\pi R_\odot^2 \times (\text{energy flux})$. We ignore the uncertainties on R_\odot for the GCs since they are either unavailable in the Harris (1996) catalogue or estimated only at percentage level (Baumgardt 2017) and so make a negligible contribution to the overall error of L_γ . For the parameters and flux upper limits of 127 additional GCs, see Appendix A in Supplementary Material (online).

3 CORRELATION ANALYSIS

In this section, we investigate the correlation between L_γ ’s and other GC observables. However, GCs not yet detected in γ -rays and sample

⁴<http://fermi.gsfc.nasa.gov/ssc/data/analysis/>

⁵<http://fermipy.readthedocs.io/en/latest/quickstart.html>

Table 1. Parameters and data analysis results for 30 γ -ray-detected GCs.

Name	Γ_c^a	[Fe/H] ^b	M_* ^c ($10^5 M_\odot$)	u_{MW}^d (eV cm^{-3})	u_{Total}^e (eV cm^{-3})	R_\odot^f (kpc)	Flux ^g ($10^{-8} \text{ ph cm}^{-2} \text{ s}^{-1}$)	L_γ^g ($10^{34} \text{ erg s}^{-1}$)	TS ^h
2MS-GC01	1.79	7.14	3.60	1.96 ± 0.26	3.88 ± 0.81	153.82
GLIMPSE01	1.55	30.23	4.20	2.55 ± 0.28	8.79 ± 0.94	535.61
GLIMPSE02	...	-0.33	...	2.61	>2.61	5.50	2.73 ± 0.25	11.55 ± 1.57	318.41
M 62	2470.00	-1.18	6.76	2.14	293.14	6.80	0.98 ± 0.09	9.16 ± 0.89	1012.19
M 80	937.00	-1.75	2.82	0.92	276.86	10.00	0.17 ± 0.07	4.26 ± 1.39	94.83
NGC 104	1000.00	-0.72	8.13	0.55	31.12	4.50	1.34 ± 0.07	5.61 ± 0.34	4853.63
NGC 1904	126.00	-1.60	1.66	0.29	173.13	12.90	0.11 ± 0.04	2.32 ± 0.98	23.84
NGC 2808	1210.00	-1.14	8.13	0.38	467.35	9.60	0.19 ± 0.06	3.43 ± 1.03	90.30
NGC 5904	120.00	-1.29	3.63	0.55	56.46	7.50	0.11 ± 0.04	1.10 ± 0.47	39.07
NGC 6139	407.00	-1.65	3.47	1.15	161.34	10.10	0.29 ± 0.09	5.82 ± 2.19	59.29
NGC 6218	18.10	-1.37	0.83	0.90	14.94	4.80	0.07 ± 0.05	0.38 ± 0.20	33.92
NGC 6304	150.00	-0.45	1.62	2.33	23.95	5.90	0.10 ± 0.03	1.09 ± 0.42	21.71
NGC 6316	131.00	-0.45	3.63	1.88	270.82	10.40	0.48 ± 0.11	10.91 ± 2.13	207.99
NGC 6341	265.00	-2.31	3.09	0.42	97.31	8.30	0.05 ± 0.04	0.62 ± 0.37	15.84
NGC 6388	1770.00	-0.55	10.47	1.30	1127.11	9.90	0.98 ± 0.09	18.41 ± 1.63	970.86
NGC 6397	146.00	-2.02	0.89	0.92	3.75	2.30	0.11 ± 0.06	0.09 ± 0.05	17.21
NGC 6402	106.00	-1.28	7.41	0.87	136.26	9.30	0.19 ± 0.08	3.13 ± 1.18	51.16
NGC 6440	1750.00	-0.36	5.01	2.50	721.93	8.50	0.76 ± 0.13	10.34 ± 1.97	259.55
NGC 6441	3150.00	-0.46	11.75	1.36	1148.78	11.60	0.74 ± 0.10	18.08 ± 2.62	363.50
NGC 6528	233.00	-0.11	0.59	4.00	158.13	7.90	0.11 ± 0.03	2.06 ± 0.75	31.27
NGC 6541	567.00	-1.81	2.51	1.48	120.84	7.50	0.21 ± 0.06	2.10 ± 0.63	77.12
NGC 6652	805.00	-0.81	0.47	1.22	106.17	10.00	0.22 ± 0.06	4.42 ± 1.03	120.53
NGC 6717	46.10	-1.26	0.36	1.56	22.38	7.10	0.21 ± 0.07	2.04 ± 0.63	70.85
NGC 6752	374.00	-1.54	2.29	0.83	18.59	4.00	0.21 ± 0.05	0.58 ± 0.12	157.19
NGC 6838	2.05	-0.78	0.54	0.85	4.14	4.00	0.20 ± 0.08	0.50 ± 0.18	40.13
NGC 7078	6460.00	-2.37	4.90	0.39	248.98	10.40	0.17 ± 0.05	2.55 ± 0.78	46.55
Omega Cen	144.00	-1.53	33.11	0.71	27.35	5.20	0.59 ± 0.07	3.46 ± 0.42	747.94
Terzan 1	0.63	-1.03	2.95	4.06	4.27	6.70	0.10 ± 0.02	2.93 ± 0.73	62.48
Terzan 2	19.60	-0.69	0.33	4.23	9.33	7.50	0.15 ± 0.05	3.00 ± 1.00	42.65
Terzan 5	1400.00	-0.23	6.17	4.80	98.73	6.90	3.93 ± 0.20	38.65 ± 2.51	3740.32

Notes.^aStellar encounter rate computed using equation (2). The numerical values are normalized by the encounter rate of NGC 104, which is set to 1000.

^bMetallicity.

^cStellar mass.

^dGalactic photon field energy density.

^eTotal photon field energy density, defined as the sum of the Galactic photon field and the photons from stars in the GC.

^fDistance from the Sun.

^g γ -ray flux and luminosity between 300 MeV to 500 GeV.

^hTest statistic.

selection effects must be taken into account to properly determine the significance of any apparent correlations. We use the Kendall τ coefficient as the test statistic for estimating the significance of the correlations, and the expectation–maximization (EM) algorithm for the linear regression of the correlations. Both methods allow us to properly incorporate the luminosity upper limits – implied by GCs not detected in the 4FGL – into our statistical analysis.

3.1 Linear regression with the expectation–maximization algorithm

To study the correlations between the L_γ 's and the other GC observables, we assume a linear relation in logarithmic space of the form:

$$\log(L_\gamma) = a \log(X) + b, \quad (3)$$

where L_γ is the gamma-ray luminosity of the GC, X is the independent observable considered, and a and b are parameters to be determined.

We use an EM algorithm (Feigelson & Nelson 1985; Isobe, Feigelson & Nelson 1986; Lavalley, Isobe & Feigelson 1992) to find the maximum-likelihood estimates of the parameters a and b . In contrast

to the standard maximum-likelihood method, the EM algorithm is designed to be used with censored data, i.e. data consisting of both measurements and limits. Upper limits must be properly incorporated in the correlation analyses so as to obtain statistically robust results. Briefly, the implementation of the EM algorithm is done as follows: first, the expected values of the censored data are estimated based on the regression parameters and the variance of the uncensored data. Secondly, a least-squares fit is performed and the variance is updated. Lastly, the procedure is repeated until convergence is achieved on a , b , and the variance. Using the EM algorithm, we are able to utilize the complete data set (including upper limits) in estimating relations between the L_γ and the other observables.

3.2 Kendall τ coefficient and significance

While the EM algorithm allows us to estimate the linear relations between the L_γ 's and other GC observables, we are also interested in determining the statistical significance of those relations. To that end, we apply the generalized Kendall τ rank correlation test and perform Monte Carlo (MC) simulations to determine the significance of each correlation studied with the EM algorithm.

The Kendall τ rank correlation coefficient (also referred to as the Kendall τ coefficient) is a non-parametric statistical test that has been used to study multiwavelength correlations of star-forming galaxies (Ackermann et al. 2012; Ajello et al. 2020), and misaligned active galactic nuclei (Di Mauro et al. 2014). It has been generalized to include upper limits in the statistical procedure (Ackermann et al. 2012). Therefore, we can calculate the Kendall τ coefficient using all available information concerning GCs (measurements and upper limits).

To estimate the significance of the correlations, we adopt a similar procedure as advanced previously in the literature (Ackermann et al. 2012). Namely, the null hypothesis assumes no correlation between L_γ and X . A set of null hypothesis samples is generated by repeating the following steps: (1) randomly exchange L_γ of two GCs while preserving their locations; (2) if the energy fluxes of the GCs after exchanging the L_γ are above the detection threshold of *Fermi*-LAT, the exchange is kept⁶; and (3) we perform a large number of exchanges, until obtaining a nearly uniform L_γ sample (including corrections from applying the detection threshold) over X , as required by the null hypothesis. In Appendix B in Supplementary Material (online), we discuss the number of exchanges needed to generate the null hypothesis sample.

For each correlation, we generate 10^4 null hypothesis samples and calculate their Kendall τ coefficients. For a large number of samples, the coefficients can be fitted to a normal distribution (Efron & Petrosian 1999),

$$\{\hat{\tau}_i\} \sim N(\nu_0, \sigma_0), \quad (4)$$

where $\{\hat{\tau}_i\}$ represents the distribution of the τ coefficients from the null hypothesis sample, and $N(\nu_0, \sigma_0)$ is a normal distribution with mean ν_0 and standard deviation σ_0 . For each correlation, we can compare the observed value of τ with the corresponding normal distribution from the MC results and compute the significance,

$$\sigma = \frac{\tau - \nu_0}{\sigma_0}. \quad (5)$$

Fig. 2 shows an example of the L_γ - u_{Total} data set. The blue histogram shows the probability density of Kendall τ coefficients of the null hypothesis samples. The dash-dotted line is the best-fitting normal distribution of the probability density, which has $\nu_0 = 0.071$ and $\sigma_0 = 0.0057$. The Kendall τ coefficient of real data is 0.093, shown by the red vertical line. The real data are about 3.8σ away from the centre of the null hypothesis distribution.

3.3 Correlation results

The top (bottom) panel of Fig. 3 shows the correlations between L_γ and u_{MW} (u_{Total}). GCs with measured γ -ray luminosity are shown in red, while GCs with upper limits are shown in blue. We find a very small slope for the L_γ - u_{MW} correlation, with $a = 0.29 \pm 0.26$, which is almost consistent with 0 considering the large statistical error. The significance of the L_γ - u_{MW} correlation is found to be 1.5σ . When the total photon field is considered, we find a L_γ - u_{Total} correlation with

⁶This step guarantees the detectability of the null hypothesis samples. It is crucial to apply realistic estimates of the detection threshold so that the null hypothesis samples are valid. Ackermann et al. (2012) and Ajello et al. (2020) have used the minimum fluxes in their data. Since we are using the same amount of data as the 4FGL, we take advantage of the spatial map of the 8-yr LAT detection threshold published with the 4FGL. We expect this to be a more rigorous way of generating the samples since the map includes the spatial dependence of the LAT threshold.

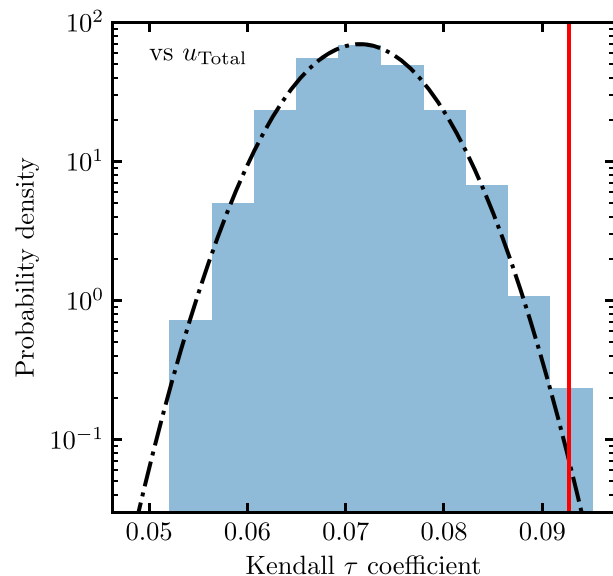


Figure 2. Probability density distribution of the Kendall τ coefficients for the L_γ - u_{Total} data set. The blue histogram corresponds to the density of the Kendall τ coefficients of the null hypothesis samples. The dash-dotted line shows the best-fitting normally distributed probability density function for the null hypothesis. The red vertical line indicates the Kendall τ coefficient for the actual data.

$a = 0.59 \pm 0.09$. In this case, the significance increases to 3.8σ . The L_γ - u_{Total} correlation is mostly driven by u_{GC} , the photon field from the starlight in the GCs (see equation 1). As shown by Table 1, u_{Total} is much greater than u_{MW} due to the dominant contribution from u_{GC} .

We also investigate the correlation of the L_γ 's with the stellar encounter rate (Γ_c) and GC metallicities ([Fe/H]). These observables are argued to be related to the formation of MSPs and may provide a proxy for the total number of MSPs in GCs. Fig. 4 shows the L_γ - Γ_c correlation (top panel) and the L_γ -[Fe/H] correlation (bottom panel) obtained with the EM algorithm. We find a positive correlation between the L_γ and Γ_c , with $a = 0.39 \pm 0.10$, for which the Kendall τ test yields a 6.4σ statistical significance. Similarly, we find a correlation between L_γ and [Fe/H] with the best-fitting value $a = 0.35 \pm 0.14$. However, the statistical significance of the correlation is only 1.8σ .

We summarize the best-fitting correlation results and their respective statistical significance in Table 2.

3.4 Hidden correlation and interpretations

Positive and statistically significant correlations are obtained in both the L_γ - u_{Total} and the L_γ - Γ_c space. The positive L_γ - u_{Total} correlation could indicate a significant contribution from IC emission. If the e^\pm injected by MSPs lose energy through multiple comparable processes, e.g. IC and synchrotron radiation, the L_γ is proportional to the IC energy loss rates, which is linearly proportional to the u_{Total} . In the extreme limit where all the e^\pm injected by MSPs lose their energy through IC, the L_γ is constrained by the energy injection rate of e^\pm by MSPs and the u_{Total} would have less impact. Since we find a preference for a non-linear correlation ($a = 0.59 \pm 0.09$), the γ -rays are unlikely all originated from IC radiation.

However, the positive correlation between L_γ and u_{Total} could alternatively be driven by the L_γ - Γ_c correlation. Here, we investigate a potential hidden correlation between u_{Total} and Γ_c in order to

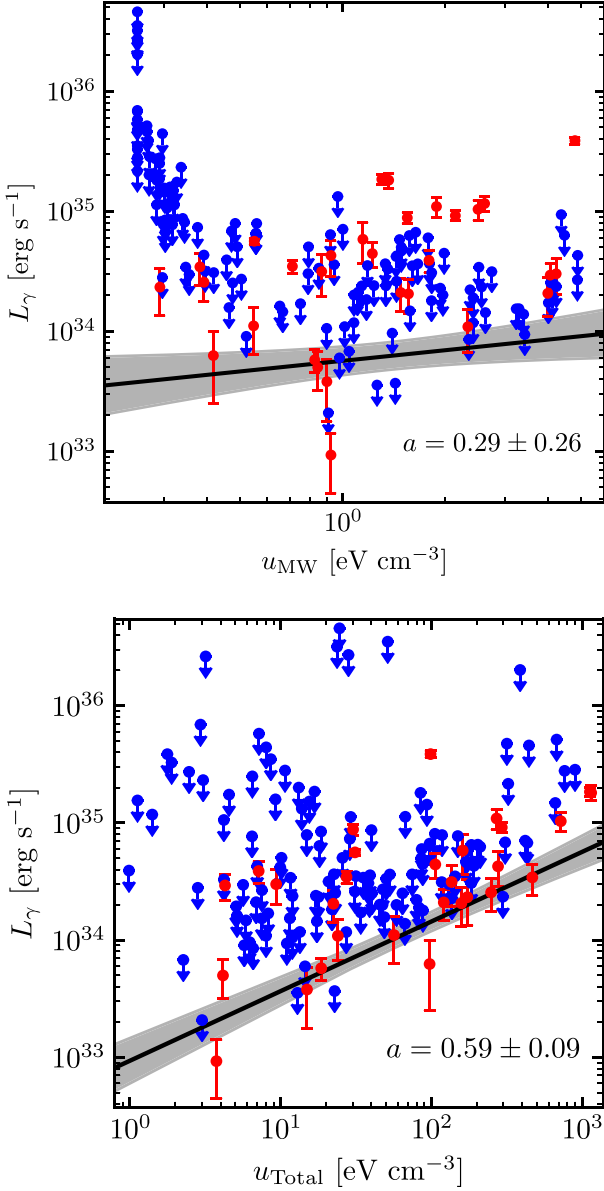


Figure 3. Correlations between L_γ and the photon field energy densities. The top panel shows the L_γ – u_{MW} correlation and the bottom panel shows the L_γ – u_{Total} correlation. GCs with measured γ rays are shown in red, while GCs with upper limits are shown in blue. The best-fitting correlations (black solid lines) are calculated using the EM algorithm discussed in Section 3.1, with 1σ uncertainties included as the grey shaded bands. We find a shallow correlation between L_γ and u_{MW} with $a = 0.29 \pm 0.26$. The correlation between L_γ and u_{Total} is more significant, with $a = 0.59 \pm 0.09$. Numerical values of correlations are summarized in Table 2, along with their significance.

better understand the nature of our detections. Fig. 5 shows the u_{Total} and Γ_c values for our sample of GCs. It is apparent that the u_{Total} tends to be higher for GCs with higher encounter rates. Since these data are uncensored, we simply estimate the correlation using the Spearman coefficient: we find 0.72, confirming a strong correlation. This result is not surprising because a higher photon density implies higher stellar density which implies higher encounter rates (see also equation 2).

An important implication of this result is that the L_γ – u_{Total} and the L_γ – Γ_c correlations are not necessarily independent. Using a simple

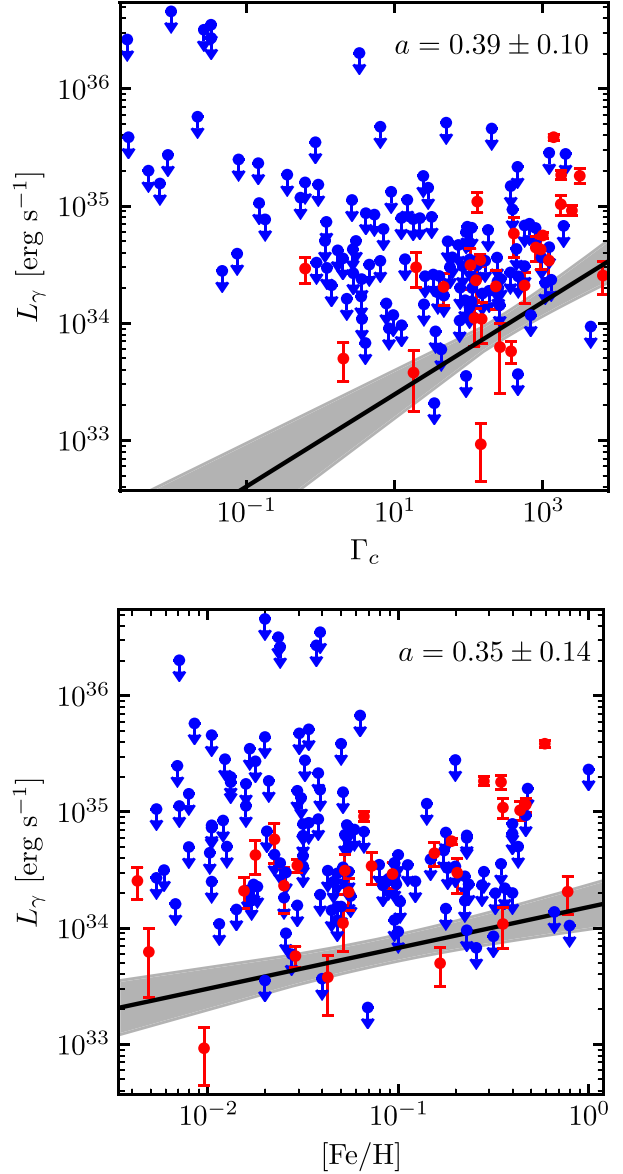


Figure 4. Same as Fig. 3, but correlated with the encounter rate (top panel) and metallicity (bottom panel).

Table 2. Summary of correlations between L_γ and four astrophysical parameters of the GCs. The best-fitting parameters a , b , and the corresponding variance of L_γ are found using the EM algorithm. The significance of the correlations is found by MC simulations with Kendall τ coefficients.

Correlation	a	b	$\sqrt{\text{Variance}}$	Significance
versus Γ_c	0.39 ± 0.10	32.99 ± 0.26	0.59 ± 0.08	6.4σ
versus u_{Total}	0.59 ± 0.09	32.97 ± 0.19	0.47 ± 0.06	3.8σ
versus $[\text{Fe}/\text{H}]$	0.35 ± 0.14	34.18 ± 0.19	0.64 ± 0.08	1.8σ
versus u_{MW}	0.29 ± 0.26	33.75 ± 0.12	0.68 ± 0.09	1.5σ

least-squares method in the logarithmic space, we find the relation between Γ_c and u_{Total} to be

$$\Gamma_c \propto u_{\text{Total}}^{1.44 \pm 0.13}. \quad (6)$$

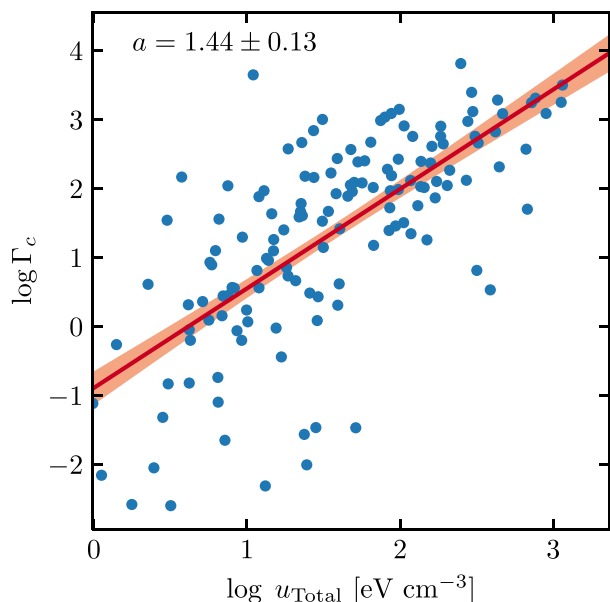


Figure 5. Hidden correlation between u_{Total} and Γ_c . GCs with higher encounter rates tend to have higher total photon field energy densities. The red line shows the relation between u_{Total} and Γ_c based on a least-squares method in logarithmic space.

As reported in Table 2, the correlation between L_γ and Γ_c has a power index $a = 0.39 \pm 0.10$. Based on the hidden relation between Γ_c and u_{Total} , the projected correlation between L_γ and u_{Total} would have an index $a = 0.56 \pm 0.15$. Within the uncertainty, this projected result is consistent with the directly measured correlation between L_γ and u_{Total} found in real data, $a = 0.59 \pm 0.09$. Therefore, the positive correlation between L_γ and u_{Total} could be evidence for IC, or alternatively, an indirect effect of the L_γ – Γ_c correlation which is connected to the dynamic formation of MSPs. The correlation found between L_γ and u_{Total} cannot be considered as concrete evidence for IC due to this ambiguity implicated by the hidden correlation. However, as we discuss next, evidence for IC emission in GCs may still be revealed from the detailed spectral properties of these objects.

4 SPECTRAL ANALYSIS

Motivated by the correlations detected in the previous section, we perform a spectral analysis of the 30 GCs detected in the 4FGL catalogue, with the aim of finding further evidence for IC emission. First, we model the spectra of the GCs individually and compare their spectral parameters with those describing the field MSPs. Secondly, we fit the GCs spectra with universal spectral models which phenomenologically describe possible IC emission. Lastly, we use the detected IC component to constrain the e^\pm injection efficiency in the GCs.

4.1 Individual spectral fits

We consider two possible mechanisms of γ -ray emission, not mutually exclusive: CR, and IC upscattering of starlight.

Detailed theoretical models predict that the maximum energy of the e^\pm accelerated by the MSPs is limited by the CR in the pulsar magnetosphere. The predicted CR spectrum exhibits an energy cut-

off which is related to the e^\pm Lorentz factor (Harding et al. 2005). For this reason, we model the GC γ -ray spectrum – as predicted by CR models – using a power law with an exponential cut-off (PLE) of the form:

$$\left[\frac{dN}{dE}\right]_{\text{CR}} = N_0 \left(\frac{E}{E_0}\right)^{-\Gamma} \exp\left(-\frac{E}{E_{\text{cut}}}\right), \quad (7)$$

where N_0 is the normalization factor, Γ is the spectral index, E_0 is the scaling energy, and E_{cut} is the energy cutoff.

The e^\pm may also leave the MSPs through open magnetic field lines and diffuse into the GC medium. Escaping pairs may upscatter ambient photons and produce IC emission. The spectrum of the IC is determined by the e^\pm spectrum and the ambient photon field. Theoretical studies (Harding & Muslimov 2011) show that the MSPs can inject e^\pm with Lorentz factors $\gamma_{e^\pm} > 10^6$ efficiently. Given ambient photons of $E_0 \sim 1$ eV energy, the upscattered IC photons can reach to above $\gamma_{e^\pm}^2 E_0 = 1$ TeV. Thus, in the Fermi GeV energy range, we assume a power-law (PL) injection distribution for e^\pm . In the Thomson regime, the IC spectrum resulting from the interaction of power-law-like e^\pm with ambient photons following a blackbody radiation distribution (Blumenthal & Gould 1970) is still a power law in γ -ray energy. We consider this spectral form as a phenomenological description of the IC model. Specifically,⁷

$$\left[\frac{dN}{dE}\right]_{\text{IC}} = N_0 \left(\frac{E}{E_0}\right)^{-\Gamma}. \quad (8)$$

We first estimate the GCs' spectral parameters using a maximum-likelihood method. For this, we use the CR model and the IC model separately. We perform a χ^2 test using the bin-by-bin γ -ray fluxes (9 energy bins from 300 MeV to 500 GeV) of each GC and the CR and IC emission models. Therefore, we define

$$\chi^2 = \sum_i \frac{(F_{\text{data}}^i - F_{\text{model}}^i)^2}{(\Delta F_{\text{data}}^i)^2 + (f_{\text{ref}}^i F_{\text{data}}^i)^2}, \quad (9)$$

where F_{data}^i and ΔF_{data}^i are the measured fluxes and flux uncertainties obtained at each independent energy bin, F_{model}^i are the predicted fluxes (either the CR or IC models). We allow all model parameters to be free (i.e. normalization, power-law index, and cut-off energy for CR, and normalization and power-law index for IC). The f_{ref}^i values encapsulate the systematic uncertainties on the effective area of the LAT. We follow the values reported in the 4FGL catalogue (Abdollahi et al. 2020), and set f_{ref} to 0.05 for the first three energy bins, 0.06 for the fourth bin, and 0.1 for the last five bins.

The significance of the spectral curvature is estimated by computing the difference of the best-fitting χ^2 between the IC and the CR models, $\text{TS}_{\text{curve}} = \chi_{\text{IC}}^2 - \chi_{\text{CR}}^2$. We apply a 2σ threshold to determine the type of spectrum: for GCs with $\text{TS}_{\text{curve}} \geq 4$, their PLE spectra are reported. Otherwise, the power-law spectra are reported. Note that this is a lower threshold than the 4FGL, which requires $\text{TS}_{\text{curve}} \geq 9$ before detection of curvature is claimed. We adopt this low threshold because our analysis removes potentially contaminated photons < 300 MeV. Bins encompassing this low energy range usually generate upper limits in the 4FGL analysis and contribute to the detection of curvature. We find, a posteriori, the 2σ threshold adequate in our analysis since our fits generate finite E_{cut} 's within uncertainties for all

⁷For the maximum γ -ray energy (hundreds of GeV) and the photon field (starlight) we considered, the IC is in transition from the Thomson regime to the Klein–Nishina regime with the Thomson regime still an adequate approximation.

Table 3. Spectral parameters for 30 γ -ray-detected GCs from the individual fits, ordered from the least curved to the most curved. For GCs with $\text{TS}_{\text{curve}} < 4$ (2σ), the best-fitting simple power laws (PL) are reported. For the rest GCs, the power laws with an exponential cutoff (PLE) are reported.

Name	Γ	$\log\left(\frac{E_{\text{cut}}}{\text{MeV}}\right)$	$\chi^2/\text{d.o.f.}$	Type ^a	TS_{curve}
2MS-GC01	2.68 ± 0.08	...	1.03	PL	0
NGC 1904	2.89 ± 0.28	...	0.63	PL	0
NGC 6397	2.56 ± 0.20	...	0.36	PL	2
NGC 7078	2.74 ± 0.16	...	0.70	PL	2
NGC 5904	2.53 ± 0.15	...	0.54	PL	2
NGC 6341	0.94 ± 1.12	3.24 ± 0.38	0.74	PLE	4
NGC 6541	1.64 ± 0.57	3.41 ± 0.37	0.25	PLE	4
NGC 6528	1.85 ± 0.54	3.68 ± 0.53	1.24	PLE	4
GLIMPSE02	2.58 ± 0.16	3.94 ± 0.35	2.54	PLE	5
NGC 6717	1.85 ± 0.34	3.71 ± 0.30	0.09	PLE	6
NGC 6218	0.00 ± 1.61	3.42 ± 0.10	0.43	PLE	7
NGC 6402	1.86 ± 0.38	3.73 ± 0.32	0.10	PLE	7
NGC 2808	1.83 ± 0.33	3.75 ± 0.31	0.11	PLE	7
NGC 6139	1.94 ± 0.32	3.77 ± 0.26	0.43	PLE	7
NGC 6838	1.38 ± 0.65	3.27 ± 0.23	0.29	PLE	9
NGC 6304	0.86 ± 0.81	3.10 ± 0.28	0.74	PLE	12
M 80	1.60 ± 0.32	3.71 ± 0.24	0.31	PLE	14
Terzan 2	0.60 ± 0.59	3.40 ± 0.18	1.00	PLE	16
NGC 6440	1.88 ± 0.22	3.63 ± 0.19	1.07	PLE	17
NGC 6441	1.83 ± 0.23	3.59 ± 0.21	0.84	PLE	17
NGC 6652	1.29 ± 0.42	3.29 ± 0.20	0.71	PLE	22
NGC 6316	1.60 ± 0.23	3.54 ± 0.14	1.16	PLE	24
NGC 6752	0.83 ± 0.58	2.99 ± 0.20	0.18	PLE	28
Terzan 1	0.00 ± 0.36	3.28 ± 0.06	0.77	PLE	37
GLIMPSE01	1.67 ± 0.14	3.57 ± 0.10	0.53	PLE	61
M 62	1.48 ± 0.14	3.47 ± 0.08	0.74	PLE	90
Omega Cen	1.05 ± 0.27	3.25 ± 0.12	1.11	PLE	103
NGC 6388	1.33 ± 0.15	3.35 ± 0.07	0.46	PLE	137
Terzan 5	1.58 ± 0.09	3.54 ± 0.06	2.14	PLE	159
NGC 104	1.28 ± 0.11	3.37 ± 0.05	0.54	PLE	207

Note.^a Spectrum type: PL for power law; PLE for power law with an exponential cut-off.

GCs with $\text{TS}_{\text{curve}} \geq 4$. For those GCs with $\text{TS}_{\text{curve}} < 4$, the fits only generate lower limits for E_{cut} . Table 3 summarizes the best-fitting parameters of the spectra for 30 γ -ray-detected GCs, sorted by their TS_{curve} . The majority prefer curved spectra, with only 5 preferring simple power-law spectra. Fig. 6 shows the spectra for 2 GCs as examples. The top panel shows the spectrum of NGC 6397, which is best fit by a simple power law, while the lower panel shows the spectrum for NGC 6541, which prefers an exponential cut-off at ~ 350 MeV with $\text{TS}_{\text{curve}} = 4$.

The *Fermi*-LAT has detected more than 200 pulsars. Most of these have been found to have a curved spectrum with best-fitting energy cut offs of the order of a few GeV. Therefore, their γ -ray emission is likely dominated by a CR process. Nevertheless, Hooper & Linden (2018, 2021) find that many MSPs could be surrounded by TeV haloes of IC. The IC emission may also extend to the GeV energy range. Fig. 7 compares the distribution of the spectral parameters of 108 field MSPs in the 4FGL (red dots) with the γ -ray GCs (blue dots), assuming a PLE spectra. The 1σ uncertainties of the best-fitting parameters are also shown. We find that within uncertainties, the spectral distribution of the GCs and the field MSPs are very similar. However, given the starlight in GCs typically contributes a much larger photon field energy density than for field MSPs, IC emission may still provide a sizeable contribution to the overall GC γ -ray emission. The results from individual spectral fit cannot rule

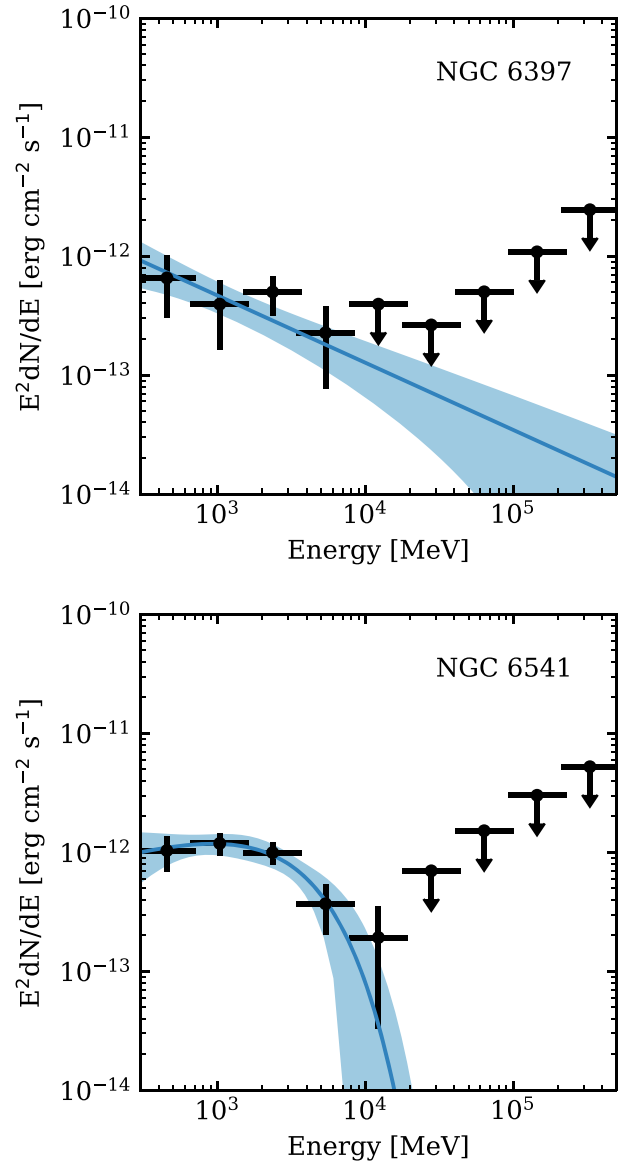


Figure 6. Best-fitting spectra (blue solid line) and the 1σ uncertainties (blue band) for two GCs. The bin-by-bin fluxes from the *Fermi* data analysis are included as black points. The top panel shows the spectrum of NGC 6397 as a simple power law because the PLE model is only slightly favoured ($\text{TS}_{\text{curve}} = 2$). The bottom panel shows the spectrum for NGC 6541, which prefers an exponential cutoff \sim GeV with $\text{TS}_{\text{curve}} = 4$.

out the presence of IC for the following reasons: (1) There are 5 GCs for which the spectra shows no obvious energy cutoffs. This is hard to explain using the CR emission model alone. (2) Many GCs have energy bins above 10 GeV detected even though their spectra have cutoffs of order a GeV (see Appendix C in Supplementary Material). These high-energy measurements may be indicative of an IC component.

4.2 Fit assuming universal spectral components

The curvature of the GCs' spectra at around a few GeV's, as well as their similarity to the field MSPs spectra, support the hypothesis that

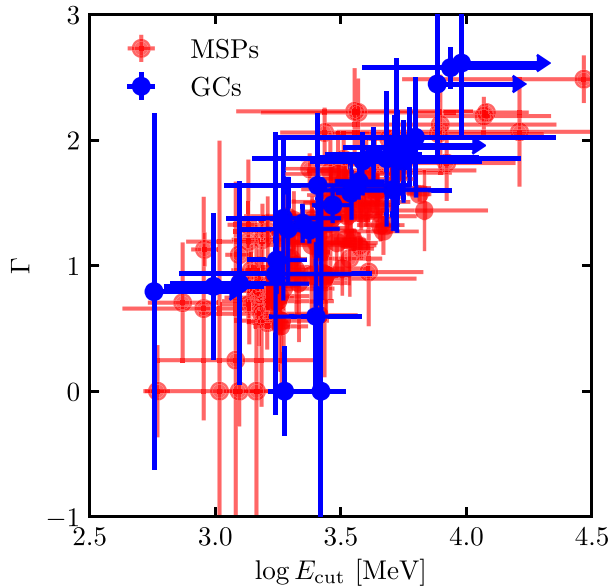


Figure 7. Spectral parameters of the γ -ray emission. The PLE spectrum is assumed, with Γ and E_{cut} as free parameters. Both the GCs (blue dots) and the MSPs (red dots) detected in the 4FGL are included. The error bars represent the 1σ parameter uncertainties. Within uncertainties, the distribution of the GCs’ spectra is very similar to that of the MSPs.

the GeV γ -ray emission from most GCs is due to mainly local CR emission from MSPs within GCs. However, IC may still contribute subdominantly, especially at the high-energy end. To probe this possibility, we perform a reduced χ^2 analysis in which we fit, bin-by-bin, the GCs’ spectra using a linear combination of the spectral components introduced in equations (7) and (8). Specifically;

$$\begin{aligned} \frac{dN}{dE} &= \left[\frac{dN}{dE} \right]_{\text{CR}} + \left[\frac{dN}{dE} \right]_{\text{IC}} \\ &= N_1 \left(\frac{E}{E_0} \right)^{-\Gamma_1} \exp\left(-\frac{E}{E_{\text{cut}}}\right) + N_2 \left(\frac{E}{E_0} \right)^{-\Gamma_2}. \end{aligned} \quad (10)$$

Fitting such a two-component model to each GC’s bin-by-bin data is difficult since the GC spectra only contains nine energy bins, and many high energy bins only provide upper limits. On the other hand, typical GCs can host close to ~ 20 MSPs (Ye et al. 2019) each. So, as a simplifying approximation, we hypothesize that the γ -ray and e^\pm injection from the collection of MSPs in each GC to be similar to one another. Then, we can fit a common or universal spectrum to all the γ -ray detected GCs, i.e. one set of spectral shape parameters in the two component model in equation (10) for all the GCs. More specifically, we tie the Γ_1 , Γ_2 , and E_{cut} across all GCs considered (hereafter referred to as the ‘universal model’). The normalization factors N_1 and N_2 are allowed to float for each GC as these should depend on the number of MSPs and the photon field energy density in the GCs.

We perform the universal fit by minimizing the total χ^2 of 30 γ -ray-detected GCs,

$$\chi_{\text{total}}^2(\Gamma_1, \Gamma_2, E_{\text{cut}}) = \sum_i \chi_i^2(\Gamma_1, \Gamma_2, E_{\text{cut}}, N_1^i, N_2^i). \quad (11)$$

In practice, we assign the same Γ_1 , Γ_2 , and E_{cut} to all γ -ray GCs and perform a minimum χ^2 for each different object. However, during the fit, we free the N_1^i and N_2^i parameters. By scanning the parameter space of Γ_1 , Γ_2 , and E_{cut} , we find the values that minimize the total

χ^2 for the two-component model. These are,

$$\begin{aligned} \Gamma_1 &= 0.88 \pm 0.44, \\ \Gamma_2 &= 2.79 \pm 0.25, \\ \log\left(\frac{E_{\text{cut}}}{\text{MeV}}\right) &= 3.28 \pm 0.16, \end{aligned}$$

for which we find a $\chi_{\text{total}}^2/\text{d.o.f} = 204/206 = 0.99$ (we have 30×9 data points, and the number of free parameters is $60 + 3$ as there are 2 normalization factors for each GC, and 3 global parameters. So, we have $\text{d.o.f} = 30 \times 9 - 60 - 3 - 1 = 206$). In Fig. 8, we show the associated 3σ contours and correlated uncertainties for the parameters Γ_1 , Γ_2 , and E_{cut} as found in this procedure.

In order to compute the statistical significance of the PL component, it is necessary to define the null hypothesis. This corresponds to the universal model containing only the CR component (see equation 7). Again, we tie Γ_1 and E_{cut} across all GCs and allow the normalization factors to individually vary. We find that the best-fitting parameters for the CR-only model are:

$$\begin{aligned} \Gamma_1 &= 1.72 \pm 0.21, \\ \log\left(\frac{E_{\text{cut}}}{\text{MeV}}\right) &= 3.53 \pm 0.19. \end{aligned}$$

In this case, we find a $\chi_{\text{total}}^2/\text{d.o.f} = 349/237 = 1.47$ (the null hypothesis has $30 + 2$ free parameters so the $\text{d.o.f} = 30 \times 9 - 30 - 2 - 1 = 237$). This implies that the two-component model is preferred at the 8.2σ level ($\Delta\chi^2 = 349 - 204$ for 31 d.o.f [1 power-law index plus 30 normalization factors]). It is useful to compare the best-fitting spectral results of the CR component for the universal models with the best-fitting spectral parameters of the MSPs in the 4FGL catalogue. As seen in Fig. 9, although the CR-only model (null hypothesis) has larger Γ and higher E_{cut} than the CR component from the two-component model, our results for both models are compatible with the field MSPs, up to statistical uncertainties.

The universal fitting procedure used in this section is similar to a stacking analysis. This method is usually applied to explore the characteristics of an astrophysical population, especially one that is undetected. Numerous studies have shown that this technique can increase the detection sensitivity to such population characteristics. So, even though there is good statistical evidence for the PL component in the universal fit, this might not be apparent from individual fitting of the two-component model.

We show examples of the spectra obtained in the universal fit of the two-component model for NGC 6397 and NGC 6541 in Fig. 10. As can be seen, the solutions for the CR and PL components look physically plausible. The spectra also include 1σ bow-tie errors, which immediately reveal the level of statistical support for the CR and PL components, respectively. For comparison, the results shown in Fig. 6 presented a single-component (e.g. Abdollahi et al. 2020) spectral curvature analysis applied to NGC 6397 and NGC 6541, individually.

We show some additional noteworthy results of the universal fit in Fig. 11. Here, we see that in the case of GC 2MS-GC01, the PL model is sufficient to explain the bin-by-bin spectrum over the full energy range, but we also display the estimated 95 per cent C.L. upper limit for the normalization of the CR model. By contrast, in the case of GC M 80, we find that the data are best described by the CR model alone, and we show the 95 per cent C.L. upper limit for the normalization of the PL component. These examples might indicate special conditions of the environment of the GC.

For 19 GCs (out of the 30 GCs included in the universal fit), we find good statistical support for both the CR and PL models. For

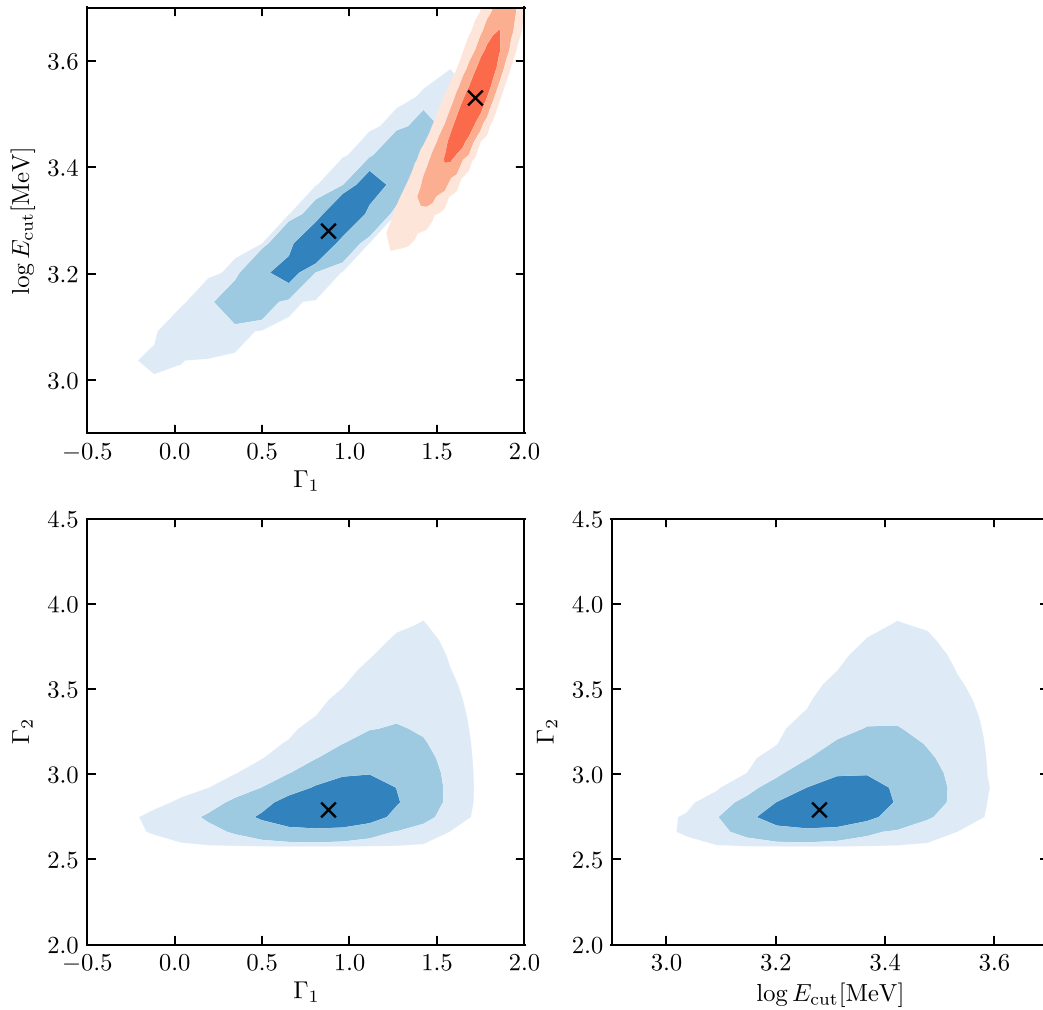


Figure 8. The projected parameter space of the universal model fit, as illustrated in equation (10). The blue shaded contours show the 1σ , 2σ , and 3σ confidence levels for the two-component model. The crosses indicate the best fit values for Γ_1 , Γ_2 , and E_{cut} . On the top-left panel, the red shaded region shows the best-fit value and 3σ confidence levels for the null hypothesis, which includes only the CR model.

the remaining 11 GCs we find that only one component is sufficient to explain the spectrum: 7 GCs require only the CR model and the other 4 GCs require only the PL model. The two-component spectral results for all 30 GCs are shown in Appendix C in Supplementary Material (online).

To explain the best-fitting index of the PL component ($\Gamma_2 = 2.79 \pm 0.25$) as IC emission, the implied emitting e^\pm spectrum would have an index of 4.58 ± 0.50 . The minimum e^\pm energy required to maintain a power-law IC in the energy range of our analysis (300 MeV) is $\lesssim 10$ GeV given that the upscattered photon field has energies ~ 1 eV (Blumenthal & Gould 1970). Interestingly, Harding & Muslimov (2011) has simulated e^\pm pair cascades from pulsar polar caps. For typical MSP parameters, they show that the injected e^\pm flux decreases by $\sim 5 - 10$ orders of magnitude when the e^\pm energy increases from ~ 10 GeV to ~ 1 TeV. The soft e^\pm spectrum we found is in line with their results.

4.3 Leptonic injection efficiency within the globular clusters

The relative normalization of the CR and IC components probes an important property of the MSPs: the γ -ray production and e^\pm

injection efficiencies, respectively. Indeed, the spin-down energy of MSPs can be injected into γ -rays and e^\pm . While prompt γ -rays are mainly produced by CR in the magnetosphere, the e^\pm can propagate into the interstellar environment. We can write down the following empirical relations,

$$L_{\text{CR}} = f_\gamma L_{\text{sd}}, \quad (12)$$

$$L_{e^\pm} = f_{e^\pm} L_{\text{sd}}, \quad (13)$$

where L_{sd} is the spin-down luminosity and the f 's are efficiency parameters.

Assuming that the γ -ray emission is the superposition of CR and IC processes, we have that

$$L_\gamma = L_{\text{CR}} + L_{\text{IC}}. \quad (14)$$

However, e^\pm can also lose energy via synchrotron radiation. We can compare the relative strength of the synchrotron radiation versus the IC emission through

$$\frac{\dot{E}_{\text{SR}}}{\dot{E}_{\text{IC}}} = \frac{u_{\text{B}}^2}{u_{\text{rad}}^2}, \quad (15)$$

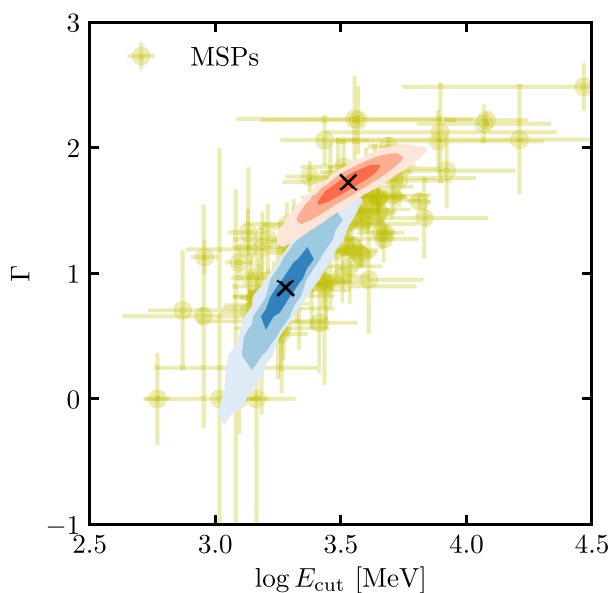


Figure 9. Same as Fig. 7, but with best-fitting parameters of GC replaced by those obtained from the universal models. The 3σ contours are shown for the CR-only model (red) and the CR component from the two-component model (blue), as in Fig. 8. The MSP parameters are included in the background (yellow dots).

where \dot{E}_{SR} and \dot{E}_{IC} are the synchrotron and IC energy loss rates, respectively, u_B is the magnetic energy density, and u_{rad} is the radiation field energy density. We note that this relation assumes that the e^\pm lose all their energy within the GCs. We provide justifications for this assumption in Appendix D in Supplementary Material (online). For a typical GC the magnetic field is estimated to be $B \lesssim 10 \mu\text{G}$ (Bednarek & Sitarek 2007), so we expect to have a $u_B = (10 \mu\text{G})^2 / (2\mu_0) = 2.5 \text{ eV cm}^{-3}$, which is much smaller than the total radiation field of most GCs shown in Table 1. Thus in the usual instance when IC is the leading energy loss process, we have that

$$L_{\text{IC}} \simeq L_{e^\pm}. \quad (16)$$

Since no GC is detected as an extended source by the *Fermi*-LAT, the energy carried away to the interstellar medium by e^\pm propagation is expected to be small. Thus, we can use the following approximate scaling relation,

$$\frac{f_{e^\pm}}{f_\gamma} \simeq \frac{L_{\text{IC}}}{L_{\text{CR}}}. \quad (17)$$

Using this,⁸ we estimate the ratios f_{e^\pm}/f_γ for all γ -ray emitting GCs in Table 4. These are found to be in the range ≈ 0.17 – 1.04 . Note that for some GCs we present only upper or lower limits as only one component is detected. The measurement of pulsars by *Fermi*-LAT estimated the f_γ efficiency from observations of pulsars and found that on average, $f_\gamma \sim 10$ per cent. Furthermore, the e^\pm efficiency f_{e^\pm} was also estimated to be around 10 per cent from TeV observations of nearby pulsars (Hooper et al. 2017; Hooper & Linden 2018, 2021) and the Galactic centre (Bednarek & Sobczak 2013), although MAGIC Collaboration (2019) claims f_{e^\pm} is at the percentage level for one GC they observed (NGC 7078), and Sudoh,

⁸We discuss caveats to the approximation used in equation (17) in Appendix D in Supplementary Material (online).

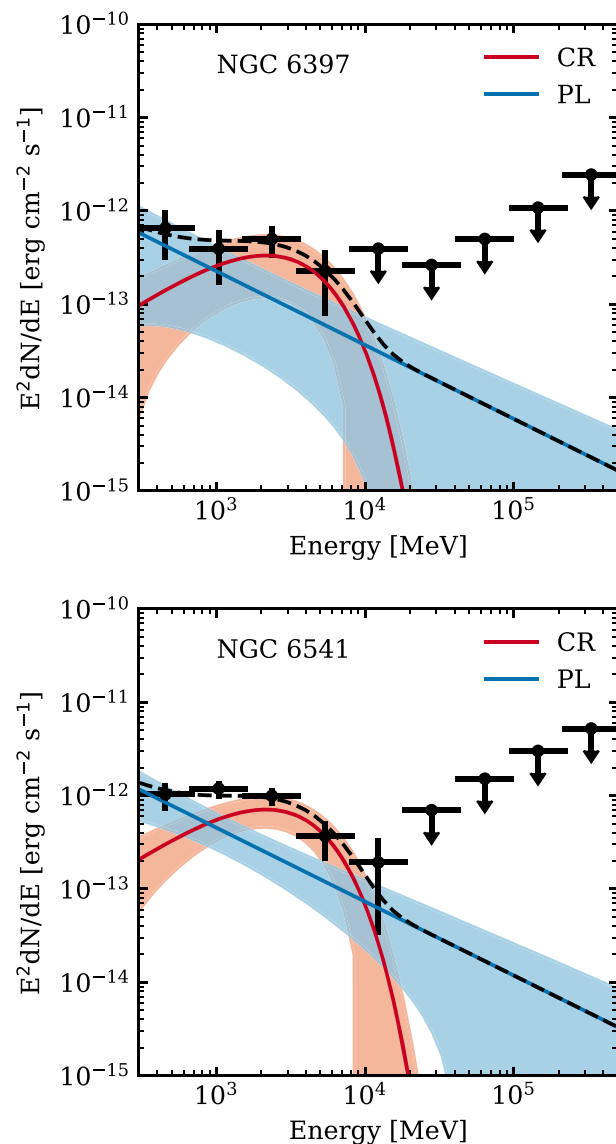


Figure 10. The best-fitting two-component spectra for NGC 6397 (top panel) and NGC 6541 (bottom panel). The spectra are fit to a universal shape with same Γ_1 , Γ_2 , and E_{cut} for all GCs. Only the normalizations of the two components are allowed to vary between GCs. The best-fitting parameters for the CR component (red line with shaded band) is $\Gamma_1 = 0.88 \pm 0.44$ and $\log(E_{\text{cut}}/\text{MeV}) = 3.28 \pm 0.16$. The best-fitting parameter for the PL component (blue line with shaded band) is $\Gamma_2 = 2.79 \pm 0.25$. The black dashed line indicates the total of the two components.

Linden & Beacom (2021) suggest $f_{e^\pm} \sim 90$ per cent on the basis of the radio continuum emission detected from galaxies with low specific star formation rates.

For the CR and IC luminosities, we integrate the best-fitting two-component spectra from 300 MeV to 500 GeV, the same energy range used in the *Fermi* data analysis. For the IC emission, the minimum e^\pm injection energy probed by this energy range is $\lesssim 10$ GeV assuming the ambient photon field is starlight. We note that Harding & Muslimov (2011) investigated the e^\pm pair cascades from MSPs and proposed several theoretical models. Their fig. 10 shows that their predicted pair spectra peak at $\sim \text{GeV}$ and extend to $\gtrsim \text{TeV}$. This roughly corresponds to the *Fermi* energy range we assume. If the

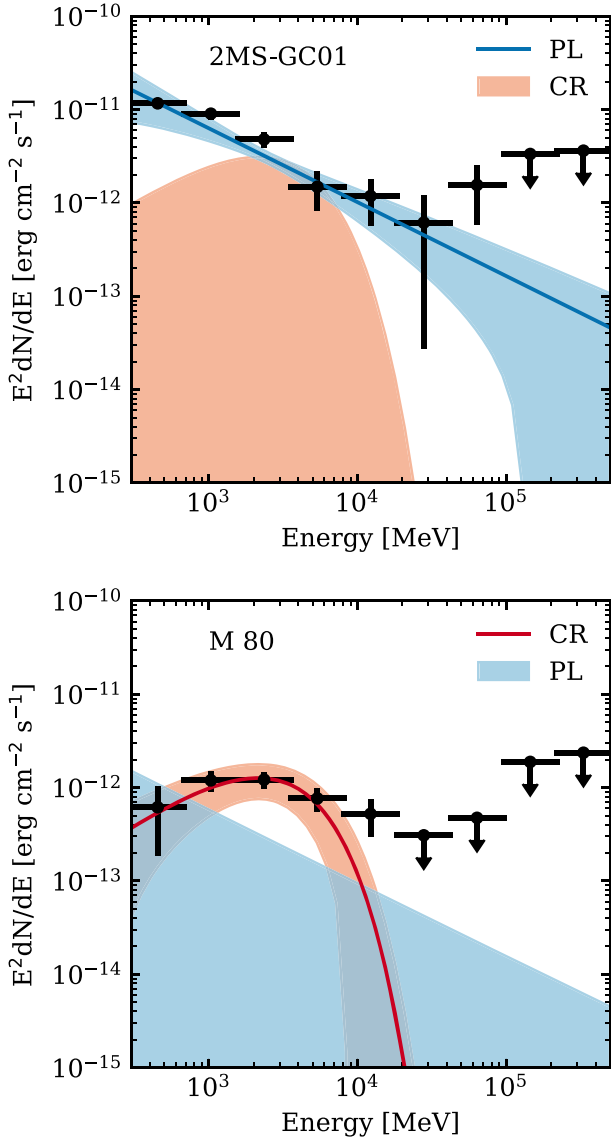


Figure 11. Spectra of 2MS-GC01 (top panel) and M 80 (bottom panel) from the two-component fit. The 2MS-GC01 prefers only the PL model (blue solid line). The 95 per cent upper limit on the normalization of the CR model is shown by the red shaded region. In contrast, only the CR model is detected for M 80 (red solid curve). The 95 per cent upper limit on the normalization of the PL model is shown by the blue shaded region.

e^\pm injection spectra extend to lower energy, they will lead to higher L_{IC} . Therefore, the choice of γ -ray energy range will contribute as systematic uncertainties on the estimated f_{e^\pm}/f_γ . For example, we verify that the f_{e^\pm}/f_γ would be ~ 5 times larger if the minimum γ -ray energy is assumed to be 30 MeV.

5 DISCUSSION

5.1 Implications of the correlation analysis

We have found strong positive correlations between L_γ , the stellar encounter rate Γ_c , and the total photon field energy density u_{Total} of GCs. The latter correlation may indicate a significant contribution of IC upscattering of ambient starlight to the total γ -ray emission

Table 4. γ -ray luminosity for the IC and CR components and the ratios between f_{e^\pm} and f_γ . For GCs with only one component detected, the 95 per cent C.L. upper limits are reported for another component.

Name	L_{IC} (10^{34} erg s $^{-1}$)	L_{CR} (10^{34} erg s $^{-1}$)	f_{e^\pm}/f_γ
GLIMPSE02	10.90 ± 1.06	< 1.70	> 6.40
2MS-GC01	3.20 ± 0.44	< 1.08	> 2.95
NGC 7078	2.38 ± 0.62	< 1.14	> 2.08
NGC 1904	1.75 ± 0.75	< 1.62	> 1.08
NGC 5904	0.54 ± 0.31	0.52 ± 0.24	1.04 ± 0.77
NGC 6397	0.05 ± 0.04	0.05 ± 0.03	0.97 ± 1.00
NGC 6440	4.83 ± 1.20	5.12 ± 0.97	0.94 ± 0.29
NGC 6541	0.99 ± 0.42	1.09 ± 0.35	0.92 ± 0.48
NGC 6139	2.33 ± 1.14	2.64 ± 0.90	0.88 ± 0.52
NGC 6441	8.36 ± 1.80	9.57 ± 1.57	0.87 ± 0.24
NGC 6752	0.25 ± 0.09	0.33 ± 0.08	0.76 ± 0.33
NGC 6717	0.80 ± 0.42	1.19 ± 0.35	0.67 ± 0.40
NGC 6402	1.18 ± 0.79	1.83 ± 0.62	0.65 ± 0.48
NGC 2808	1.18 ± 0.63	2.09 ± 0.56	0.56 ± 0.34
NGC 6838	0.16 ± 0.14	0.28 ± 0.11	0.55 ± 0.54
GLIMPSE01	2.77 ± 0.65	5.89 ± 0.62	0.47 ± 0.12
NGC 6316	2.99 ± 1.44	7.71 ± 1.26	0.39 ± 0.20
Terzan 5	10.02 ± 1.68	27.46 ± 1.83	0.37 ± 0.07
NGC 6652	1.16 ± 0.77	3.35 ± 0.68	0.35 ± 0.24
M 62	2.20 ± 0.60	6.92 ± 0.63	0.32 ± 0.09
NGC 6388	4.37 ± 1.18	14.22 ± 1.27	0.31 ± 0.09
NGC 104	0.96 ± 0.22	4.67 ± 0.30	0.21 ± 0.05
Omega Cen	0.50 ± 0.24	2.90 ± 0.27	0.17 ± 0.08
NGC 6528	< 2.41	1.38 ± 0.58	< 1.74
NGC 6218	< 0.39	0.23 ± 0.12	< 1.67
NGC 6341	< 0.71	0.49 ± 0.23	< 1.45
NGC 6304	< 0.79	0.89 ± 0.30	< 0.88
M 80	< 2.31	3.45 ± 0.74	< 0.67
Terzan 2	< 0.49	2.66 ± 0.52	< 0.18
Terzan 1	< 0.16	2.42 ± 0.49	< 0.07

of GCs. However, we showed in Fig. 5 that the u_{Total} also increases with Γ_c . So, the detection of the L_γ - u_{Total} correlation alone does not unambiguously demonstrate the presence of IC emission in GCs.⁹ On the other hand, corroborating evidence for IC emission was found from the universal two-component fit, wherein we were able to estimate, separately, the luminosities of the CR and IC components of most GCs. The ratios of the luminosities between the CR and IC components were found to be comparable. This implies that MSPs in GCs can potentially inject e^\pm as efficiently as they inject prompt magnetospheric γ -rays.

Overall, our correlation results in the L_γ - Γ_c plane are consistent with those in Hui et al. (2011) and de Menezes et al. (2019), though it is important to note that our method is more statistically robust since we include GCs with detection limits which were previously neglected. In particular, our high significance (6.4σ) detection of a L_γ - Γ_c correlation naively supports a dynamic formation scenario for MSPs in GCs. However, as pointed out earlier, this correlation may not be independent due to the hidden correlation of u_{Total} and Γ_c . On the other hand, we have not found an obvious correlation between f_{e^\pm}/f_γ and u_{Total} (see Appendix D in Supplementary Material). The lack of this latter correlation may indicate that IC

⁹We also analysed other potential hidden correlations, but no obvious correlations with other parameters such as the interstellar radiation field and the distance from the Sun were found (see Appendix D in Supplementary Material).

is, in fact, the leading energy loss process for e^\pm in GCs: in the limit of IC dominance, the IC luminosity of GCs already saturates the power going into freshly injected e^\pm pairs, so ‘dialling-up’ the light field energy density has no effect on the IC luminosity. Thus, in this situation of IC dominance, we expect, at most, only a weak correlation between L_γ and u_{Total} and we would anticipate that the L_γ – Γ_c correlation is the fundamental one (while the L_γ – u_{Total} correlation is caused by the fact that GCs with higher stellar encounter rate naturally have higher stellar density which leads to higher photon field density). With the uncertainties of the data and the number of variables involved, it is challenging to statistically confirm this scenario. Overall, however, our results are consistent with there being both a significant role for dynamical formation of MSPs in GCs and for the presence of a significant contribution of IC to the overall γ -ray emission of GCs.

Previous studies (Hui et al. 2011) found a positive correlation between L_γ and u_{MW} , and L_γ and $[\text{Fe}/\text{H}]$. However, our study does not confirm these results. The former discrepancy is possibly due to the different interstellar radiation field models assumed in these works, or it could be due to the more limited sample data used in Hui et al. (2011). Specifically, while we have used the most up-to-date interstellar radiation field for the Milky Way – which is the 3D radiation field model in GALPROP v56 (Porter et al. 2017) – Hui et al. (2011) used the 2D radiation field model in GALPROP v54. Also, as explained above, our correlation study includes 30 γ -ray-detected GCs, as well as the luminosity upper limits from the 127 non-detected ones, thus covering the entire GC Harris (1996) catalogue. As for the latter discrepancy, similar results for the L_γ – $[\text{Fe}/\text{H}]$ correlation were obtained by de Menezes et al. (2019), which also found low statistical evidence for this correlation.

5.2 Implications for the Fermi GeV excess

The emission from a putative population of about 40 000 (Ploeg et al. 2020) unresolved MSPs in the Galactic Centre region is currently the preferred explanation for the Fermi GeV excess (Bartels et al. 2018; Macias et al. 2018; Macias et al. 2019; Abazajian et al. 2020). Since GCs also contain large numbers of unresolved MSPs, it is useful to compare the light-to-mass ratios for these two systems so as to obtain additional clues for the physical processes causing the observed high-energy γ -ray emissions in their directions. In Fig. 12, we show the relation between L_γ and the stellar mass for several different systems. The blue dots show the sample of the γ -ray detected GCs in this work. The nuclear bulge (orange dot) has a stellar mass around $1.4 \times 10^9 M_\odot$ and a γ -ray luminosity of $(3.9 \pm 0.5) \times 10^{36} \text{ erg s}^{-1}$ and the boxy bulge (green dot) has $1.5 \times 10^{10} M_\odot$ and $(2.2 \pm 0.4) \times 10^{37} \text{ erg s}^{-1}$ (Macias et al. 2019). The combination of the nuclear bulge and the boxy bulge is responsible for the Galactic centre GeV excess. Also included are the Galactic disc (red dot) luminosity predicted by Bartels et al. (2018) and the M31 galaxy (purple star) (Ackermann et al. 2017). The dot-dashed line shows the γ -ray luminosity-to-stellar-mass relation implied for the nuclear bulge and the boxy bulge, which is $2 \times 10^{27} \text{ erg s}^{-1} M_\odot^{-1}$.

As can be seen in Fig. 12, the luminosities of the detected sample of GCs exceed the luminosities expected based on the correlations. In total, the GC samples have a stellar mass of $\sim 1.4 \times 10^7 M_\odot$ and a γ -ray luminosity of $\sim 1.5 \times 10^{36} \text{ erg s}^{-1}$. This means that GCs systematically emit ~ 50 times more γ -rays per stellar mass than other objects such as the nuclear bulge and the Galactic bulge. The GCs have long been known for producing MSPs efficiently (Camilo & Rasio 2005). On average GCs make up ~ 0.05 per cent of the total number of stars in the Milky Way (Ye

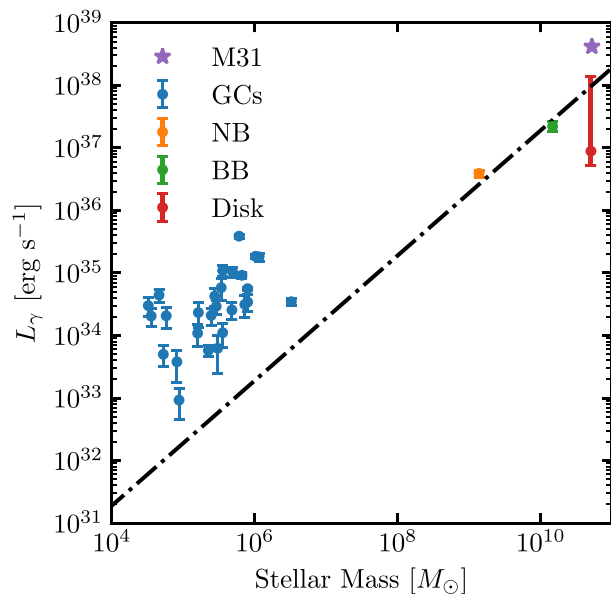


Figure 12. Relations between L_γ and the stellar mass for several systems. The results for the nuclear bulge (orange dot) and boxy bulge (green dot) are adopted from Macias et al. (2019). The Galactic disc (red dot) luminosity is predicted by Bartels et al. (2018), and the M31 (purple star) are adopted from Ackermann et al. (2017). The blue dots show the data for 30 γ -ray detected GCs. The dash-dotted line is the relation implied by the nuclear bulge and boxy bulge.

et al. 2019), but more than one-third of the known MSPs are found in these systems (Manchester et al. 2005). Our observations support this scenario. This is also consistent with the larger stellar densities and larger stellar encounter rates in GCs than in the Galactic bulge. We also note in passing that a large fraction of γ -ray-detected GCs are located in the Galactic bulge region (see Fig. 1), which means that it is possible that at least some of the unresolved MSPs contributing to the Fermi GeV excess are hosted by GCs in the Galactic bulge region.

5.3 TeV observations of globular clusters

Using the universal two-component fit, we identified a power-law component with a slope of 2.79 ± 0.25 from the spectra of γ -ray-detected GCs. The power-law component can be plausibly explained by IC emission from GCs. The fact that this power-law component is rather soft may explain why most GCs are not detected in the TeV energy range. In order to explore this more closely, we extrapolate the high energy tail of the GCs spectra to TeV energies in Fig. 13. In this figure, the black line shows the extrapolated fluxes for Terzan 5, and the grey band shows the range of extrapolated fluxes for the other 23 GCs with a detected IC component. Above 100 GeV, *Fermi*–LAT only find upper limits (blue arrows) for Terzan 5. The red dots are the H.E.S.S. measurements from the direction of Terzan 5. It is interesting to note that the extrapolated spectrum for Terzan 5 is about one order of magnitude lower than the H.E.S.S. measurements from the same object. This discrepancy might be explained by the fact that the γ -ray source reported by H.E.S.S. is misaligned with the centre of Terzan 5 so that this association could be a chance coincidence. However, such a coincidence with known objects has been estimated to be improbable ($\sim 10^{-4}$) (H. E. S. S. Collaboration 2011). If the

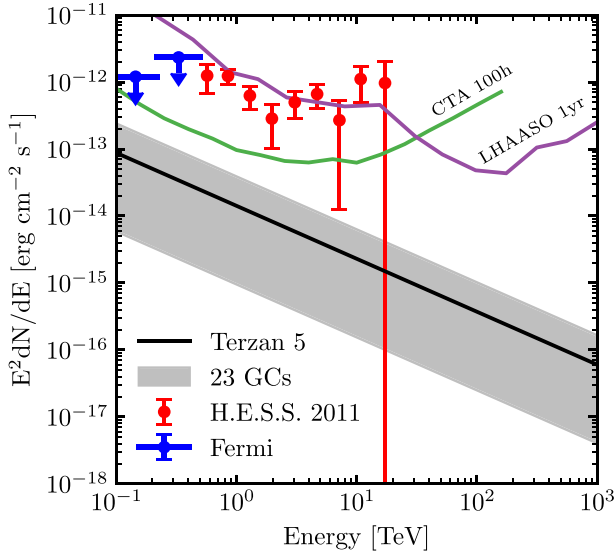


Figure 13. Extrapolated spectra for Terzan 5 (black line) and 23 GCs with the IC component detected (grey region). The H.E.S.S. measurement of Terzan 5 is shown by red dots with error bars. The *Fermi*-LAT only find upper limits (blue arrows) for Terzan 5 in this energy range. Also included are the sensitivities for 100-h CTA South (green line) and 1-yr LHAASO (purple line).

H.E.S.S. source is indeed associated to Terzan 5, it could be that e^\pm injection spectrum from MSPs has a spectral break at approximately 1 TeV. Note that a substantial fraction of stars in Terzan 5 have been identified as young and centrally concentrated (Ferraro et al. 2016; Gotta et al. 2020), which could lead to a larger number of younger pulsars. The H.E.S.S. measurements could be explained if these young pulsars have higher energy e^\pm cutoffs. Therefore, Terzan 5 may not be representative compared to other GCs which are dominated by old stellar systems. However, Nataf et al. (2019) also find that the abundance variations among Terzan 5 is indeed consistent with a regular globular cluster. Alternatively, the TeV γ -rays could originate from sources other than MSPs (e.g. hadronic emission from supernova remnants). Further investigation of those scenarios, though very interesting, is beyond the scope of this work.

We also include in Fig. 13 the sensitivities to point-like sources for the next-generation γ -ray observatories. The green line shows the sensitivity for the Cherenkov Telescope Array (CTA)–South assuming 100 h of observation time. The purple line shows the 1-yr sensitivity of the Large High Altitude Air Shower Observatory (LHAASO). The extrapolated IC fluxes are close to the 100-h CTA sensitivity. It is clear that it will be difficult for the next-generation TeV γ -ray telescopes to actually detect each individual GC considered in our study. This might require a much more ambitious observation strategy that increases the sensitivity by factor of a few at the TeV energy range. Efforts to measure the diffuse IC emission from the putative MSP population responsible for the Fermi GeV excess have been made and are very encouraging; see Song, Macias & Horiuchi (2019) and Macias et al. (2021). Alternatively, Bednarek, Sitarek & Sobczak (2016) studied TeV γ -ray emission from MSPs taking into account the advection of e^\pm with the wind from the GC. They showed that CTA can constrain models incorporating such effects.

6 SUMMARY AND CONCLUSIONS

We have reanalysed *Fermi*-LAT data in the energy range between 300 MeV and 500 GeV from the direction of 157 GCs in the Harris (1996) catalogue. Using the same data cuts adopted in the construction of the 4FGL catalogue, we confirmed the detection of 30 GCs in γ -rays, and updated the γ -ray spectral parameters for the sample of detected objects. We also estimated the 95 per cent C.L. luminosity upper limits for the sample of 127 undetected GCs in the 4FGL catalogue. The main objective of our reanalysis was to find evidence for IC emission from e^\pm injected by MSPs in GCs. This was done using two different methodologies. First, we searched for correlations of the γ -ray luminosities with other GCs properties. Secondly, we performed a spectral analysis of the GCs with a universal fit method that enhances the sensitivity to the high energy tail of the spectra. Specifically:

(1) Using an expectation–maximization algorithm that properly incorporates null detections (L_γ upper limits) in the pipeline, we found a correlation between L_γ and the GCs’ total photon field energy density u_{Total} of the form,

$$\log\left(\frac{L_\gamma}{\text{erg s}^{-1}}\right) = (0.59 \pm 0.09) \log\left(\frac{u_{\text{Total}}}{\text{eV cm}^{-3}}\right) + (32.97 \pm 0.19). \quad (18)$$

Using the Kendall τ coefficient as the test statistic we determined this correlation to have a 3.8σ significance. The total photon field is dominated by the stellar light of the GCs (u_{GC}), and we find a much weaker correlation (below the 2σ level) when only the photon field at the location of the GC (u_{MW}) is used. In addition, we obtained a strong correlation (at 6.4σ significance) between L_γ and the stellar encounter rate Γ_c , which is given by

$$\log\left(\frac{L_\gamma}{\text{erg s}^{-1}}\right) = (0.39 \pm 0.10) \log(\Gamma_c) + (32.99 \pm 0.26). \quad (19)$$

Finally, we found only weak evidence (below the 2σ level) for a correlations between L_γ and the stellar metallicity [Fe/H].

(2) We revealed a hidden correlation between u_{Total} and Γ_c , which implies that the L_γ – u_{Total} and L_γ – Γ_c correlations are not entirely independent. However, as described below, we find spectral evidence for IC emission. The correlation results are consistent with there being both a significant role for dynamical formation of MSPs in GCs and for the presence of a significant contribution of IC to the observed γ -ray luminosity.

(3) We applied a universal spectral fit to the sample of 30 GCs in the 4FGL catalogue and searched for evidence of an IC component on top of a curvature radiation model—accounting for the MSPs prompt emission in the GCs. We found that the extra power-law IC component is preferred at the 8.2σ significance over the curvature radiation model only. The best-fitting power-law index of the IC component was found to be 2.79 ± 0.25 . This implies a power-law e^\pm spectrum with an index of 4.58 ± 0.50 and a minimum energy as low as ~ 10 GeV.

(4) We estimated the e^\pm injection efficiency f_{e^\pm} for MSPs residing in GCs. We determined the IC γ -ray luminosities over 300 MeV to 500 GeV, which roughly corresponds to e^\pm energies from 10 GeV to 1 TeV. We found the fraction of MSP spin-down energy injected to e^\pm is comparable to or slightly smaller than that injected to γ rays, $f_{e^\pm} \lesssim f_\gamma$ and is at $\lesssim 10$ per cent level. This parameter has been estimated in different environments, such as nearby pulsars (Hooper et al. 2017; Hooper & Linden 2018, 2021), the Galactic centre (Bednarek & Sobczak 2013), individual GCs (MAGIC Collaboration 2019), and galaxies with low specific star formation rate (Sudoh et al.

2021). Our results provide new insights into the f_{e^\pm} parameter based on the universal properties of γ -ray-detected GCs in the Milky Way.

In summary, our analysis reveals strong evidence for soft IC emission in *Fermi*–LAT GCs. This is indicative of e^\pm injected by MSPs hosted by such systems. Although the *Fermi*–LAT sensitivity for energies larger than 10 GeV is not sufficiently high to claim a detection in each individual GC, we employed a universal fit method with the bin-by-bin spectra of the sample of detected objects and were able to increase the sensitivity to the IC component. Our results also explain why it is difficult to detect GCs with TeV γ -ray telescopes: we have obtained a very soft spectra for the high energy tail of the GC population. It is possible that with a more aggressive observation campaign such objects could be detected by forthcoming TeV telescopes (see Ndiyavala, Krüger & Venter 2018 for a recent sensitivity analysis) such as CTA (Cherenkov Telescope Array Consortium et al. 2019) and LHAASO (Bai et al. 2019). Globular clusters remain some of the most important systems within which to search for and study millisecond pulsars. We have shown the potential of extracting critical knowledge from γ -ray data of globular clusters with advanced statistical tools and intensive modelling.

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DATA AVAILABILITY

The *Fermi*–LAT data analysed in this article were accessed from <https://heasarc.gsfc.nasa.gov/FTP/fermi/data/lat/weekly/>. The derived data generated in this research are available in the article.

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SUPPORTING INFORMATION

Supplementary data are available at [MNRAS](https://academic.oup.com/mnras/article/507/4/5161/6356581) online.

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