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Search for intermediate mass black hole binaries in the first and second observing runs of the Advanced LIGO and Virgo network

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Gravitational-wave astronomy has been firmly established with the detection of gravitational waves from the merger of ten stellar-mass binary black holes and a neutron star binary. This paper reports on the all-sky search for gravitational waves from intermediate mass black hole binaries in the first and second observing runs of the Advanced LIGO and Virgo network. The search uses three independent algorithms: two based on matched filtering of the data with waveform templates of gravitational-wave signals from compact binaries, and a third, model-independent algorithm that employs no signal model for the incoming signal. No intermediate mass black hole binary event is detected in this search. Consequently, we place upper limits on the merger rate density for a family of intermediate mass black hole binaries. In particular, we choose sources with total masses $M = m_1 + m_2 \in [120, 800] M_\odot$ and mass ratios $q = m_2/m_1 \in [0.1, 1.0]$. For the first time, this calculation is done using numerical relativity waveforms (which include higher modes) as models of the real emitted signal. We place a most stringent upper limit of $0.20 \text{ Gpc}^{-3} \text{ yr}^{-1}$ (in comoving units at the 90% confidence level) for equal-mass binaries with individual masses $m_{1,2} = 100 M_\odot$ and dimensionless spins $\chi_{1,2} = 0.8$ aligned with the orbital angular momentum of the binary. This improves by a factor of ~ 5 that reported after Advanced LIGO's first observing run.

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I. INTRODUCTION

The first two observing runs of Advanced LIGO and Virgo (O1 and O2 respectively) have significantly enhanced our understanding of black hole (BH) binaries in the Universe. Gravitational waves (GWs) from ten binary black hole mergers with total mass between $18.6_{-0.7}^{+3.1}$ and $85.1_{-10.9}^{+15.6} M_\odot$ were detected during these two observing runs [1–8]. These observations have revealed a new population of heavy stellar-mass BH components of up to $50 M_\odot$, for which we had no earlier electromagnetic observational evidence [8,9]. This finding limit is consistent with the formation of heavier BHs from core collapse being prevented by a mechanism known as *pulsational pair-instability supernovae* [10–13]. According to this idea, stars with helium core mass in the range $\sim 32\text{--}64 M_\odot$ undergo pulsational pair instability leaving behind remnants of $\lesssim 65 M_\odot$. Stars with helium core mass in the range $\sim 64\text{--}135 M_\odot$ undergo pair instability and leave no remnant, while stars with helium mass $\gtrsim 135 M_\odot$ are thought to directly collapse to intermediate mass black holes.

Intermediate mass black holes (IMBHs) are BHs heavier than stellar-mass BHs but lighter than supermassive black holes (SMBHs), which places them roughly in the range of $10^2\text{--}10^5 M_\odot$ [14,15]. Currently there is only indirect observational evidence. Observations include probing the

mass of the central BH in galaxies as well as massive star clusters with direct kinematical measurements which has led to recent claims for the presence of IMBHs [16–18]. Other observations come from the extrapolation of several scaling relations between the mass of the central SMBH and their host galaxies [19] to the mass range of globular clusters [20,21]. In this way, several clusters have been found to be good candidates for having IMBHs in their centers [22–24]. If present, IMBHs would heat up the cores of these clusters, strongly influencing the distribution of the stars in the cluster and their dynamics, leaving a characteristic imprint in the surface brightness profile, as well as in the mass-to-light ratio [25]. Controversy exists regarding the interpretation of these observations, as some of them can also be explained by a high concentration of stellar-mass BHs or the presence of binaries [22–24,26]. Empirical mass scaling relations of quasiperiodic oscillations [27] in luminous x-ray sources have also provided evidence for IMBHs [28]. Finally, IMBHs have been proposed as candidates to explain ultraluminous x-ray sources in nearby galaxies, which are brighter than the accreting x-ray sources with stellar-mass BHs [29,30]. However, neutron stars or stellar-mass black holes emitting above their Eddington luminosity could also account for such observations. In summary, no definitive evidence of IMBHs has yet been obtained.

The possible astrophysical formation channels of IMBHs remain uncertain. Proposed channels include the direct

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collapse of massive first-generation, low metallicity Population III stars [31–34] and mergers of stellar-mass BHs in globular clusters [35] and multiple collisions of stars in dense young star clusters [18,36–39], among others [40]. Further, some astrophysical scenarios [14] indicate that SMBHs in galactic centers might be formed from hierarchical mergers of IMBHs [15,41]. The direct observation of IMBHs with gravitational waves could strengthen the possible evolutionary link between stellar-mass BHs and SMBHs. Finally, observing an IMBH population would help to understand details of the pulsational pair-instability supernovae mechanism.

The GW observation of a coalescing binary consisting of at least one IMBH component or resulting in an IMBH remnant, which we will term an IMBHB, could provide the first definitive confirmation of the existence of IMBHs. In fact, IMBHBs are the sources that would emit the most gravitational-wave energy in the LIGO-Virgo frequency band, potentially making them detectable to distances (and redshifts) beyond that of any other LIGO-Virgo source [42]. Even in the absence of a detection, a search for IMBHBs provides stringent constraints on their merger rate density, which has implications for potential IMBHB and SMBH formation channels.

IMBHs are not only interesting from an astrophysical point of view, they are also excellent laboratories to test general relativity in the strong field regime [43–46]. Their large masses would lead to strong merger and ringdown signals in the Advanced LIGO-Virgo frequency band. Therefore, higher modes might be visible in IMBHB signals because those modes are especially strong in the merger and ringdown stages. The observation of multimodal merger and ringdown signals is paramount to understanding fundamental properties of general relativity, such as the no-hair theorem [47–50] and BH kick measurements [51–53].

The first search for GWs from IMBHBs was carried out in the data from initial LIGO and initial Virgo (2005–2010) [54,55]. Owing to the large masses of IMBHBs, such systems are expected to merge at low frequencies where the initial detectors were less sensitive due to the presence of several noise sources, such as suspension noise, thermal noise, and optical cavity control noise. As a result, those detectors were sensitive to only the merger and ringdown phases of the IMBHB systems. Initial IMBHB analyses applied either the model-independent time-frequency searches [56] or ringdown searches. No IMBHB merger was detected in these searches.

Because of the improved low-frequency sensitivities of the Advanced LIGO and Advanced Virgo detectors [57,58], IMBHB signals are visible in band for a longer period of time, which increases the effectiveness of modeled searches that use more than just the ringdown portion of an IMBHB’s waveform. Reference [42] reports results from a combined search for IMBHBs that used two

independent search algorithms: a matched-filter analysis called `GstLAL` [59–61], which uses the inspiral, merger, and ringdown portions of the IMBHB waveform and the model-independent analysis `coherent WaveBurst` (`cWB`) [56]. No IMBHBs were found by these searches, and upper limits on the merger rate density for 12 targeted IMBHB sources with total mass between 120 and 600 M_{\odot} and mass ratios down to 1/10 were obtained. The most stringent upper limit on the merger rate density from this combined analysis was $0.93 \text{ Gpc}^{-3} \text{ yr}^{-1}$ for binaries consisting of two 100 M_{\odot} BHs with dimensionless spin magnitude 0.8 aligned with the system’s orbital angular momentum.

All upper limits on the IMBHB merger rate reported in past searches [42,54,55] were obtained using models for the GW signal that include only the dominant radiating mode, namely $(\ell, m) = (2, \pm 2)$, of the GW emission [62]. However, it has been shown that higher modes contribute more substantially to signals emitted by heavy binaries. This impact increases as the system becomes more asymmetric in mass [63,64], as the spin of the BHs becomes more negative [65,66], and as the precession in the binary becomes stronger [67]. As a consequence, the omission of higher modes leads in general to more conservative upper limits on the IMBHB merger rate [68]. In this work, we improve on past studies in two distinct ways. We use numerical relativity (NR) simulations with higher modes to model GW signals from IMBHBs for computing upper limit estimates. Additionally, our combined analysis now includes the matched-filter search `PyCBC` [69,70] in addition to `GstLAL` and `cWB`. Because of these novelties, we have, in addition to analyzing the O2 dataset, reanalyzed the O1 dataset and report here combined upper limits for the O1 and O2 observing runs. In this paper, we report upper limits on the merger rate density of 17 targeted (nonprecessing) IMBHB sources. Our most stringent upper limit is $0.20 \text{ Gpc}^{-3} \text{ yr}^{-1}$ for equal-mass binaries with component spins aligned with the orbital angular momentum of the system and dimensionless magnitudes $\chi_{1,2} = 0.8$.

The rest of this paper is organized as follows. In Sec. II we describe the dataset, outline the individual search algorithms that make up the combined search, and report our search’s null detection of IMBHBs. In Sec. III we describe the NR simulations that we use to compute the upper limits on the IMBHB merger rates and report these for the case of 17 IMBHB sources. We draw final conclusions in Sec. IV.

II. IMBHB SEARCH IN O1 AND O2 DATA

A. Data summary

This analysis was carried out using O1 and O2 datasets from the two LIGO (Livingston and Hanford) detectors and Virgo. We have used the final calibration, which was produced after the conclusion of the run, including compensation for frequency-dependent fluctuations in the

calibration [71–73]. Well-identified sources of noise have also been subtracted from the strain data as explained in Refs. [73,74]. The maximum calibration uncertainty across the frequency band of [10–5,000] Hz for the two LIGO detectors is $\sim 10\%$ in amplitude and ~ 5 deg in phase for O1 and $\sim 4\%$ in amplitude and ~ 3 deg in phase for O2 [7,71]. For Virgo we consider an uncertainty of 5.1% in amplitude and 2.3 deg in phase [73]. After removing data with significant instrumental disturbance, we use 48.6 days and 118.0 days of joint Hanford-Livingston data from the O1 and O2 observing runs respectively. The Virgo detector joined the LIGO detectors during the last ~ 15 days of O2, which provided 4.0 days of coincident data (Hanford-Virgo or Livingston-Virgo) in addition to Livingston-Hanford coincident data. The data from O1 and O2 were divided into nine and 21 blocks respectively with coincident time ranging from 4.7–7.0 days. For more details, see Ref. [8].

B. Search algorithms

We combine the two matched-filter searches, namely G_{stLAL} [59–61,75] and P_{yCBC} [69,70], and one model-independent analysis, $c\text{WB}$ [76], into a single IMBHB search. The two model-based matched-filtering analyses use a bank of templates made of precomputed compact binary merger GW waveforms. Matched-filter-based analyses are optimal to extract known signals from stationary, Gaussian noise [77]. However, the templates we use are limited to noneccentric, aligned-spin systems. They contain only the dominant waveform mode of the GW emission and omit higher modes [64,78]. Additionally, Advanced LIGO and Virgo data are known to contain a large number of short noise transients [79], which can mimic short GW signals like those emitted by IMBHBs. While matched-filter searches use several techniques to discriminate between noisy transients and real GW events [61,80,81], they are known to lose significant efficiency when looking for short signals like those from IMBHBs. Therefore, the IMBHB search is carried out jointly with an analysis that can identify short-duration GW signals without a model for the morphology of the GW waveform. In this search, all three analyses use O1 and O2 Advanced LIGO data. However, because of the incomparable sensitivities between the Advanced LIGO detector and Advanced Virgo detector, only the G_{stLAL} analysis uses Virgo data, as is done in Ref. [8].

1. Modeled analyses

The matched-filter analyses G_{stLAL} and P_{yCBC} use templates that span the parameter space of neutron stars, stellar-mass BHs, and IMBHBs. In this study, we use the same two searches reported in Ref. [8] to calculate upper limits on the merger rate density of IMBHBs.

The matched-filter signal-to-noise ratio (SNR) time series is computed for every template. Triggers are produced when the SNR time series surpasses a predetermined

threshold, where clusters of triggers are trimmed by maximizing the SNR within small time windows. In addition, a signal consistency veto [61,81,82] is calculated for each trigger. A list of GW candidates is constructed from triggers generated by common templates that are coincident in time across more than one detector, where the coincidence window takes into account the travel time between detectors. Next, a ranking statistic is calculated for each candidate that estimates a likelihood ratio that the candidate would be observed in the presence of a GW compared to a pure-noise expectation. Finally, a p -value¹ P is determined by comparing the value of its ranking statistic to that of triggers coming from background noise in the data. A detailed description of the G_{stLAL} and P_{yCBC} pipelines can be found in Refs. [59–61,75] and [69,70], respectively; additionally, details outlining how candidates are ranked across observing runs can be found in Ref. [8].

The G_{stLAL} analysis uses the template bank described in Ref. [83]. The region of this bank that overlaps the IMBHB parameter space, which starts at a total mass of $100 M_{\odot}$, reaches up to a total mass of $400 M_{\odot}$ in the detector frame, and covers mass ratios in the range of $1/98 < q < 1$. The waveforms used are a reduced-order model of the SEOBNRv4 approximant [84]. The spins of these templates are either aligned or antialigned with the orbital angular momentum of the system with dimensionless magnitudes less than 0.999.

The P_{yCBC} analysis uses the template bank described in Ref. [85]. The region of this bank that overlaps the IMBHB parameter space reaches up to a total mass of $500 M_{\odot}$ in the detector frame, excluding templates with duration below 0.15 s, and covers the range of $1/98 < q < 1$. The waveforms used are also a reduced-order model of the SEOBNRv4 approximant, and the aligned or antialigned dimensionless spin magnitudes are less than 0.998.

2. Unmodeled analysis

$c\text{WB}$ is the GW transient detection algorithm designed to look for unmodeled short-duration GW transients in the multidetector data from interferometric GW detector networks. Designed to operate without a specific waveform model, $c\text{WB}$ identifies coincident excess power in the wavelet time-frequency representations of the detector strain data [86], for signal frequencies up to 1 kHz and durations up to a few seconds. The search identifies events that are coherent in multiple detectors and reconstructs the source sky location and signal waveforms by using the constrained maximum likelihood method [76]. The $c\text{WB}$ detection statistic is based on the coherent energy E_c obtained by cross-correlating the signal waveforms reconstructed in multiple detectors. It is proportional to the network SNR and used to rank the events found by $c\text{WB}$.

¹The probability that noise would produce a trigger at least as significant as the observed candidate.

To improve the robustness of the algorithm against nonstationary detector noise, cWB uses signal-independent vetoes, which reduce the high rate of the initial excess power triggers. The primary veto cut is on the network correlation coefficient $c_c = E_c / (E_c + E_n)$, where E_n is the residual noise energy estimated after the reconstructed signal is subtracted from the data. Typically, for a GW signal $c_c \approx 1$ and for instrumental glitches $c_c \ll 1$. Therefore, candidate events with $c_c < 0.7$ are rejected as potential glitches.

To improve the detection efficiency of IMBHs as well as to reduce the false alarm rates (FARs), the cWB analysis employs additional selection cuts based on the nature of IMBH signals. IMBH signals have two distinct features in the time-frequency representation. First, the signal frequencies lie below 250 Hz. We use this to exclude all the non-IMBH events in the search, including noise events. Secondly, the inspiral signal duration in the detector band is relatively short, which leads to relatively low SNR in the inspiral phase as compared to the merger and ringdown phases. In the cWB framework, chirp mass $[\mathcal{M} = (m_1 m_2)^{3/5} M^{-1/5}]$ is estimated using the frequency evolution of a signal's inspiral. However, in the case of low SNRs, we cannot accurately estimate the chirp mass of the binary [87]; still, we use this framework to introduce additional cuts on the estimated chirp mass to reject non-IMBH signals. The simulation studies show that IMBH signals are recovered with $|\mathcal{M}| > 10 M_\odot$ which we use in this search.² We apply this selection cut to reduce the noise background when producing the candidate events.

For estimation of the statistical significance of the candidate event, each event is ranked against a sample of background triggers obtained by repeating the analysis on time-shifted data [1]. To exclude astrophysical events from the background sample, the time shifts are selected to be much longer (1 s or more) than the expected signal time delay between the detectors. By using different time shifts, a sample of background events equivalent to approximately 500 years of background data is accumulated for each of the 30 blocks of data. The cWB candidate events that survived the cWB selection criteria are assigned a FAR given by the rate of the corresponding background events with the coherent network SNR value larger than that of the candidate event.

C. Combined search

Each of our three algorithms produces its own list of GW candidates characterized by GPS time, FAR, and associated p -value P . These three lists are then combined into a common single list of candidates. To avoid counting candidates more than once, candidates within a time

²Negative \mathcal{M} values correspond to frequencies decreasing with time, which could be due to the pixels corresponding to the ringdown part.

window of 100 ms across different lists are assumed to be the same. To account for the use of three search algorithms, we apply a conservative trials factor of 3 and assign each candidate a new p value given by

$$\bar{P} = 1 - (1 - P_{\min})^3, \quad (1)$$

where P_{\min} denotes the minimum p value reported across the pipelines. This is equivalent to assuming that the three searches produce independent lists of candidates.³ We note that while this choice of trials factor affects the significance of individual triggers, it will not change the numerical value of our upper limits. See Appendix B for a more detailed discussion.

D. Search results

Here we report results from the combined cWB-GstLAL-PyCBC IMBH search on full O1-O2 data. The top 21 most significant events from the combined search include the 11 GW events published in Ref. [8], namely GW150914 [1], GW151012, GW151226 [2], GW170104 [3], GW170608 [4], GW170729, GW170809, GW170814 [6], GW170817 [5], GW170818, and GW170823, and ten events tabulated in Table I. All the events in Table I have a FAR much larger than any of the GWs reported in Ref. [8]; no event in this list was found with enough significance to claim an IMBH detection.

The top-ranked event⁴ from Table I was observed by cWB in O2 data on May 2, 2017 at 04:08:44 UTC with a combined SNR of 11.6 in the two Advanced LIGO detectors and a significance of $P_{\text{cWB}} = P_{\min} = 0.14$. Applying Eq. (1), this event has a combined p value of $\bar{P} = 0.36$, too low to claim it as a gravitational-wave detection.

Despite the low significance of this trigger, its characteristics were consistent with those of an IMBH, and we decided to perform detailed data quality and parameter estimation follow-ups.⁵ In order to check for the presence of environmental or instrumental noise, this event was vetted with the same procedure applied to triggers of marginal significance found in previous searches [8] in O1-O2 data. These checks identified a correlation between the trigger time and the glitching of optical lever lasers at the end of one arm of the Hanford detector. This is a known instrumental artifact previously observed to impact GW searches [88,89]. The time of this trigger was not discarded by the pretuned data quality veto designed to mitigate the effects of these optical lever laser glitches. However, these

³In general, correlations between searches would lead to a trials factor less than 3. However, at the time, we are not able to quantify this, and we choose to adopt the most conservative approach.

⁴We note that the most significant event in the O1 search reported in Ref. [42] is the third event in this table.

⁵See Appendix D for further details regarding the parameter estimation investigations of this candidate.

TABLE I. Details of the ten most significant events (excluding all published lower mass events). We report the date, UTC time, observing pipeline (individual analysis that observed the event with the highest significance), FAR, SNR, and P_{\min} for each event. The combined p -value \bar{P} of each event is calculated using Eq. (1). In the table, the events are tabulated in increasing value of P_{\min} .

No	Date	UTC time	Pipeline	FAR (yr^{-1})	SNR	P_{\min}
1	2017-05-02	04:08:44.9	cWB	0.34	11.6	0.14
2	2017-06-16	19:47:20.8	PyCBC	1.94	9.1	0.59
3	2015-11-26	04:11:02.7	cWB	2.56	7.5	0.68
4	2017-06-08	23:50:52.3	cWB	3.57	10.0	0.79
5	2017-04-05	11:04:52.7	GstLAL	4.55	9.3	0.88
6	2015-11-16	22:41:48.7	PyCBC	4.77	9.0	0.88
7	2016-12-02	03:53:44.9	GstLAL	6.00	10.5	0.94
8	2017-02-19	14:04:09.0	GstLAL	6.26	9.6	0.95
9	2017-04-23	12:10:45.0	GstLAL	6.47	8.9	0.95
10	2017-04-12	15:56:39.0	GstLAL	8.22	9.7	0.98

vetoed are tuned for high efficiency and minimal impact on analyzable time rather than exhaustively removing all non-Gaussian features in the data. Further follow-up indicates that this instrumental artifact is likely contributing power to the gravitational-wave strain channel at the time and frequency of the trigger. Given the SNR of the purported signal in the Hanford detector and the relatively low significance of the reported false alarm rate, we conclude that this trigger is likely explained by detector noise.

III. UPPER LIMITS ON MERGER RATES

Given that no IMBHB signal was detected by our search, we proceed to place upper limits on the coalescence rate of these objects. This is done by estimating the sensitivity of our search to an astrophysically motivated population of simulated IMBHB signals that we inject in our detector data. However, given the absence of well-motivated population estimates of IMBHBs, we opt for sampling the parameter space in a discrete manner (for details, please see Appendix C). As a consequence, in this section we estimate the sensitive distance reach as well as the upper limit on merger rate density for 17 selected fiducial IMBHB sources tabulated in Table II of Appendix C using the loudest event method [90], following the procedure outlined in Ref. [42] and described again in Appendix A. For a given IMBHB source, gravitational waveforms from simulated systems scattered through space are injected into the data and recovered by each of the three analyses. In this section, we describe our simulation set and present our findings.

A. Injection set

Reference [42] reports upper limits on the merger rate density for 12 IMBHB systems in its Table I. The waveform simulations used to compute upper limits in that study contain only the dominant quadrupolar mode of the GW emission. In this work, we use highly accurate NR simulations computed by the SXS [91], RIT [92], and GeorgiaTech [93] codes, which include higher modes. Since

higher modes are particularly important for large asymmetries in mass and for high total mass binaries, in this study we extend our parameter space to mass ratios as low as $q = 1/10$ and total masses as high as $M = 800 M_{\odot}$ (see Appendix C Table II for a detailed list). In general, NR simulations can include modes of arbitrary (ℓ, m) for a given set of masses in the parameter space. However, weak modes are sometimes dominated by numerical noise and do not agree when compared across different numerical codes. In fact, we disregard numerical modes with $\ell \geq 5$, because these have comparatively small amplitudes. The $\ell \geq 5$ modes with $m = \pm\ell$ have also particularly short wavelengths, which makes it more challenging for numerical relativity codes to resolve the propagation of these modes away from the binary. In order to assess the accuracy of the remaining modes, we only choose IMBHB simulations for which higher modes have been computed by at least two different NR codes. We select only those higher modes that agree to an overlap of at least 0.97 across all available NR codes for each of 17 the selected simulations.⁶

The higher modes that passed this criteria and were included in our analysis were the following: $(\ell, m) = \{(2, \pm 1), (2, \pm 2), (3, \pm 2), (3, \pm 3), (4, \pm 2), (4, \pm 3), (4, \pm 4)\}$. Notably, the (2,2) mode agrees across NR codes to an overlap > 0.995 for every IMBHB source considered in this study; the two modes closest to the 0.97 overlap threshold were the (4,4) and (4,3) modes. We note that, similar to what was described in Ref. [68], omission of $\ell > 4$ modes may lead to an underestimation of the power within the detector band radiated by the largest mass binary BHs.

Of the 17 selected sources, we include three cases with spins aligned or antialigned with the total angular momentum of the binary with dimensionless spin magnitudes $|\chi_{1,2}| = 0.8$. The IMBHB injections are uniformly distributed in the binary orientation parameters $[\varphi, \cos(i)]$

⁶We did allow for overlaps below 0.97 if the mode's contribution to the waveform was negligible.

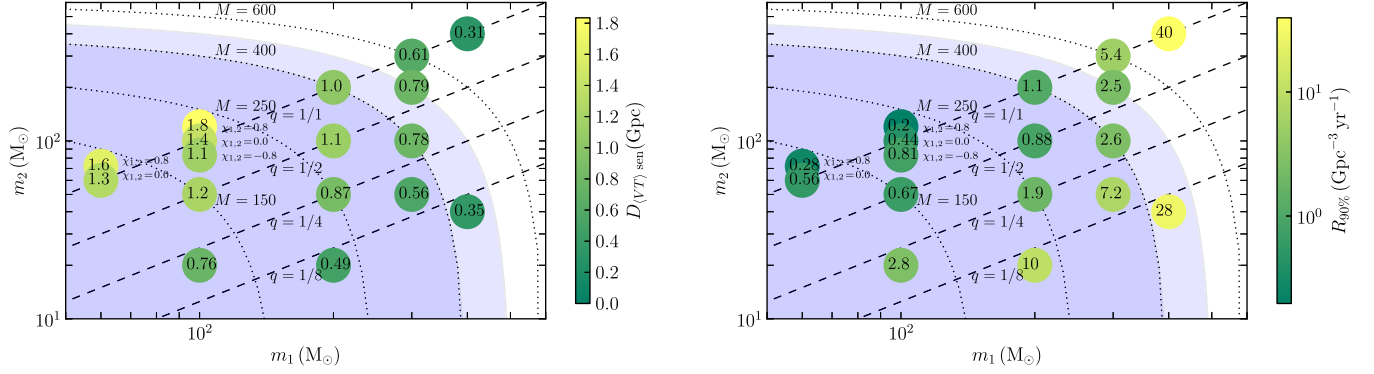


FIG. 1. The sensitive distance reach ($D_{(VT)_{sen}}$) in Gpc (left panel) and 90% upper limit on merger rate density ($R_{90\%}$) in $\text{Gpc}^{-3} \text{yr}^{-1}$ (right panel) for the 17 targeted IMBHB sources in the $m_1 - m_2$ plane. Each circle corresponds to one class of IMBHBs in the source frame with a number in the circle indicating $D_{(VT)_{sen}}$ (left panel) or $R_{90\%}$ (right panel). Spinning injection sets are labeled and shown as displaced circles. The blue and light blue shaded regions mark the template space encompassed by the GstLAL ($M < 400 M_\odot$) and PyCBC ($M < 500 M_\odot$) template banks respectively.

uniformly distributed in comoving volume up to redshift $z \sim 1$ (luminosity distance of 6.7 Gpc) using the TT + lowP + lensing + ext cosmological parameters given in Table IV of Ref. [94], and individually redshifted according to this cosmological model. The overall effect of cosmological redshift is to shift each GW signal to lower frequencies. At a given redshift, the mass of the injection in the detector frame is $(1 + z)$ times larger than the source-frame mass, and the luminosity distance is $(1 + z)$ times the comoving distance. At redshifts of $z = 1$, this results in a decrease in SNR ranging from $\sim 20\%$ for an equal-mass $M = 100 M_\odot$ face-on system to $\sim 50\%$ for an equal-mass $M = 200 M_\odot$ face-on system. The injections are spaced roughly uniformly in time with an interval of at least 80 s over the $T_0 = 413.71$ days of O1-O2 observing time, and each injection set covers a total space-time volume $\langle VT \rangle_{\text{tot}} = 110.68 \text{ Gpc}^3 \text{ yr}$.

B. Sensitive distance reach and merger rate density estimate

We use the loudest event method [90] to calculate the sensitive distance reach of our search and to place upper limits on the merger rate density of IMBHBs (see Appendix C for a detailed description of our procedure). The results of our combined search are reported using a combined p value of $\bar{P} = 0.36$ given by that of our loudest event in Table I.

The left panel of Fig. 1 shows the sensitive distance reach of our combined search toward our 17 targeted IMBHB sources represented in the $m_1 - m_2$ plane (see Table II in Appendix C for a more detailed description). We find an across-the-board improvement in the sensitive distance of our combined search compared to the 12 targeted sources reported in Ref. [42]. In particular, we find that the combined search is most sensitive to the $(100 + 100) M_\odot$ aligned-spin source, which can be observed up

to 1.8 Gpc and is an increase of more than 10% compared to the 1.6 Gpc obtained in Ref. [42]. These improvements are the result of better detector sensitivity, the inclusion of higher modes in our injections, and significant improvements to the cWB search algorithm. As a general trend, our reach decreases for increasing mass ratio and for increasing total mass once this surpasses $\sim 200 M_\odot$. There are several reasons for this behavior. First, the intrinsic amplitude of the IMBHB signal decreases as the mass ratio decreases for a fixed total mass. Second, sources with small q have a significant fraction of their power contained in their higher modes. Consequently, they are not well matched by our search templates, which only include the dominant quadrupole mode. Last, although the intrinsic luminosity of IMBHBs rises with total mass, the merger frequency decreases, and so signals persist in the detector sensitive frequency band for a very short duration. This makes it difficult to distinguish them from noise transients. This effect is evident from the roughly equivalent sensitive distances obtained for the $(60 + 60)$ and $(100 + 100) M_\odot$ sources despite the significantly larger total mass of the latter.

The right panel of Fig. 1 shows the upper limits on the merger rate density of our 17 targeted IMBHB sources, which improve on those reported after O1 in Ref. [42]. We set our most stringent upper limit at $0.20 \text{ Gpc}^{-3} \text{ yr}^{-1}$ for equal-mass spin-aligned IMBHBs with component masses of $100 M_\odot$ and aligned dimensionless spins of 0.8. By assuming a redshift-independent globular cluster (GC) density of 3 GC Mpc^{-3} [95], we find that this upper limit is equivalent to $0.07 \text{ GC}^{-1} \text{ Gyr}^{-1}$, an improvement of a factor of ~ 5 over the $0.31 \text{ GC}^{-1} \text{ Gyr}^{-1}$ that was reported in Ref. [42]. We also observe that for all equal-mass ratio IMBHB sources, the merger rate density upper limits are also improved. The sources with unequal masses show larger improvement in the merger rate density as compared to the previous result.

IV. CONCLUSIONS

We conducted a search for IMBHs in the data collected in the two observing runs of the Advanced LIGO and Virgo detectors. This search combined three analysis pipelines: two matched-filter algorithms `GstLAL` and `PyCBC` and the model-independent algorithm `cWB`. The `PyCBC` and `cWB` analyses used data from the Advanced LIGO detectors, and `GstLAL` used data from the Advanced LIGO and Advanced Virgo detectors. No IMBH detections were made in this search. The loudest candidate event was found with a marginal p -value $\bar{P} = 0.36$ in our combined search. A detailed detector characterization study of this event suggested that it is likely explained by the detector noise.

Given the null detection, we placed upper limits on the merger rate density for 17 IMBH systems. For estimation of the rate upper limits, we used NR waveforms provided by the SXS, RIT, and `Georgiatech` groups that include higher modes in the gravitational-wave emission. The reported rate limits are significantly more stringent than the previous result reported in Ref. [42]. In particular, the most stringent rate limit of $0.20 \text{ Gpc}^{-3} \text{ yr}^{-1}$ placed on $(100 + 100) M_{\odot}$ aligned-spin IMBH systems is an improvement of a factor of ~ 5 . This improvement is due to the combination of three factors: the increased sensitivity of our detector network, the improvements in the `cWB` search algorithm, and the incorporation of higher modes into our models for IMBH signals.

Anticipated increases of the network sensitivity in future runs, particularly at low frequency, and further improvement of the search algorithms will place more stringent upper limits on the merger rate density of IMBHs and may even result in the first definitive detection of an IMBH.

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APPENDIX A: SENSITIVE DISTANCE REACH AND MERGER RATE

In this appendix we provide further details on our method to compute the averaged space-time volume observed by a search and its corresponding sensitive distance at a given significance threshold. In general, the averaged space-time volume to which our searches are sensitive is given by [96,97]

$$\langle VT \rangle_{\text{sen}} = T_0 \int dz d\theta \frac{dV_c}{dz} \frac{1}{1+z} s(\theta) f(z, \theta). \quad (\text{A1})$$

Here, T_0 is the length of the observation in the detector frame, and $V_c(z)$ is the comoving volume spanned by a sphere of redshift z . The function $s(\theta)$ is the distribution of binary parameters θ , and $0 \leq f(z, \theta) \leq 1$, where $f(z, \theta)$ denotes the fraction of injections with parameters θ detected at a redshift z .

In this determination of sensitivity we have two main limitations. First, the true population of IMBHs in the Universe is unknown, so it prevents us from choosing a particular function $s(\theta)$. Second, numerical relativity

waveforms cover a discrete parameter space in θ . For this reason, our study is focused on probing a discrete set of IMBHB classes with parameters $\{\theta_i\}$ described in Table II. Then the averaged space-time volume sensitivity of Eq. (A1) can be approximated using a Monte Carlo technique via

$$\langle VT \rangle_{\text{sen}} \sim \frac{N_{\text{rec}}}{N_{\text{tot}}} \langle VT \rangle_{\text{tot}}. \quad (\text{A2})$$

Here, N_{tot} is the total number of injections in a given set, which are distributed in redshift and source orientations as indicated in Sec. III A. $\langle VT \rangle_{\text{tot}}$ is the total space-time volume into which injections were distributed. N_{rec} is the number of recovered injections by the search, i.e., the number of injections assigned a value $\bar{P} \leq \bar{P}_0$, where \bar{P}_0 is in general some arbitrary threshold. In our case, we set $\bar{P}_0 = 0.36$, which is the \bar{P} of our most significant event in our combined search.

The corresponding sensitive distance reach is computed as

$$D_{\langle VT \rangle_{\text{sen}}} = \left(\frac{3 \langle VT \rangle_{\text{sen}}}{4\pi T_a} \right)^{1/3}, \quad (\text{A3})$$

where T_a is the amount of time analyzed by the search. We estimated the 90% confidence upper limit in the merger rate density for selected simulated signal classes as given by

$$R_{90\%} = - \frac{\ln(0.1)}{\langle VT \rangle_{\text{sen}}}, \quad (\text{A4})$$

where $\langle VT \rangle_{\text{sen}}$ is estimated using the loudest event method and Eq. (A2).

APPENDIX B: DETERMINING THE p VALUE OF THE COMBINED SEARCH

In general, the p value of the triggers of our combined search is given by

$$\bar{P} = 1 - (1 - P_{\text{min}})^m, \quad (\text{B1})$$

where P_{min} is the minimum p value reported by any of our three searches, and $m \in [1, 3]$ is the trials factor. The trials factor is $m = 1$ if the three searches are fully correlated (for instance, if they are the same search) and 3 if they are fully independent. In this work we adopt a conservative approach and choose $m = 3$, omitting possible correlations between the three analysis pipelines. Indeed, excluding the 11 detected GWs mentioned in Sec. II D, none of the 123 events with $\text{FAR} < 100/\text{yr}$ was common across the three pipelines.

We note that while the significance of individual triggers depends on our particular choice for the trials factor m applied in Eq. (B1) (which we set to $m = 3$), N_{rec} is

independent of this choice. This is because every GW candidate output by the three analyses, including our loudest event, will have the same trials factor applied when combined into a single list, so that their relative ranking will remain unchanged (see Sec. II C). Therefore, the numerical value of our upper limit is unaffected by our conservative choice of $m = 3$, since any choice would yield the same N_{rec} and $\langle VT \rangle_{\text{sen}}$.

As pointed out, since our choice of the trials factor affects the significance of individual triggers, our conservative approach may overly diminish the significance of prospective louder IMBHB triggers, and it may become important to make more accurate estimates of m in the future. Since the lowest p value reported by any of our individual analyses was $P = 0.14$, we conclude that our choice of m does not impact our conclusion that no IMBHBs have been observed.

APPENDIX C: SENSITIVE DISTANCE REACH FOR INDIVIDUAL SEARCH ALGORITHMS

In this appendix, we report and compare the sensitive distance reach of the three individual searches and the combined search at their respective loudest event thresholds (see Table II). For the case of the individual searches, this threshold is set to $\bar{P}_0 = 0.14$, equal to the loudest (most significant) event found by cWB; for the combined search, this is set to $\bar{P}_0 = 0.36$. We control for differences in the amount of analyzed time by only considering common observing times in Table II, which allows for a more direct comparison between the searches.

Table II shows that cWB reports the largest sensitive distance reach to every IMBHB source considered. This is expected for sources with $M_{\text{tot}} > 500 M_{\odot}$, since the GstLAL and PyCBC template banks are bounded by a total mass 40 and 500 M_{\odot} , respectively. Additionally, since cWB is not limited by constraints on waveform morphology, it significantly outperforms matched-filter analyses in the large mass and small mass ratio regions of the parameter space that are covered by our analyses' template banks. This finding is consistent with Ref. [68], since in that region of parameter space, signals are shorter and higher modes are more important. Reference [68] also found that matched-filter searches outperform cWB in the low mass end of our parameter space. Since then, however, cWB has undergone major improvements that have led to a sensitivity comparable to that of matched-filter searches even for the lightest equal-mass systems considered in this analysis.

GstLAL reports sensitive distance reaches that are lower than those found in Ref. [42]. This is the result of using a large bank here that was not specifically tuned and targeted for IMBHBs. Future searches will benefit from investigations into optimal template placement and binning as well as a return to a dedicated IMBH bank.

TABLE II. The sensitive distance reach and the merger rate density calculated for the 17 targeted IMBHB sources considered in this study, whose intrinsic parameters are indicated in the first four columns. The fifth column indicates the numerical simulations used for each case, following the naming conventions of the corresponding NR groups. The next three columns report the sensitive distance reach for each of the individual analyses (cWB, GstLAL, and PyCBC), where we use the loudest event threshold of $P = 0.14$ for each analysis for comparison purposes. The last column gives the sensitive distance reach from the combined search. To control for differences in the amount of analyzed time between individual analyses, we consider only common observed time across the three pipelines time, which yields $T_a = 0.428$ yr.

$m_1 M_\odot$	$m_2 M_\odot$	Spin $\chi_{1,2}$	$M M_\odot$	NR simulation	$D_{(VT)_{\text{sen}}} \text{ (Gpc)}$			
					cWB	GstLAL	PyCBC	Combined
60	60	0	120	SXS:BBH:0180, RIT:BBH:0198:n140, GT:0905	1.2	1.2	1.2	1.3
60	60	0.8	120	SXS:BBH:0230, RIT:BBH:0063:n100, GT:0424	1.6	1.0	1.5	1.6
100	20	0	120	SXS:BBH:0056, RIT:BBH0120:n140, GT:0906	0.72	0.69	0.70	0.76
100	50	0	150	SXS:BBH:0169, RIT:BBH:0117:n140, GT:0446	1.2	0.79	1.1	1.2
100	100	-0.8	200	SXS:BBH:0154, RIT:BBH:0068:n100	1.1	1.0	0.99	1.2
100	100	0	200	SXS:BBH:0180, RIT:BBH:0198:n140,GT:0905	1.4	0.90	1.3	1.4
100	100	0.8	200	SXS:BBH:0230, RIT:BBH:0063:n100, GT:0424	1.8	1.2	1.7	1.8
200	20	0	220	RIT:BBH:Q10:n173, GT:0568	0.48	0.30	0.36	0.49
200	50	0	250	SXS:BBH:0182, RIT:BBH:0119:n140, GT:0454	0.85	0.48	0.67	0.87
200	100	0	300	SXS:BBH:0169, RIT:BBH:0117:n140, GT:0446	1.1	0.59	0.86	1.1
300	50	0	350	SXS:BBH:0181, RIT:BBH:0121:n140, GT:0604	0.55	0.18	0.27	0.56
200	200	0	400	SXS:BBH:0180, RIT:BBH:0198:n140, GT:0905	1.0	0.47	0.72	1.0
300	100	0	400	SXS:BBH:0030, RIT:BBH:0102:n140, GT:0453	0.78	0.23	0.34	0.78
400	40	0	440	RIT:BBH:Q10:n173, GT:0568	0.35	0.10	0.16	0.35
300	200	0	500	RIT:BBH:0115:n140, GT:0477	0.79	0.16	0.14	0.79
300	300	0	600	SXS:BBH:0180, RIT:BBH:0198:n140, GT:0905	0.61	0.09	0.18	0.61
400	400	0	800	SXS:BBH:0180, RIT:BBH:0198:n140, GT:0905	0.31	0.10	0.23	0.31

APPENDIX D: LOUDEST EVENT PARAMETER ESTIMATION

Despite the low significance of our loudest event, two characteristics motivated a detailed follow-up analysis. On the one hand, initial parameter estimation put this trigger in the IMBHB region of the parameter space. On the other, this trigger was observed by our matched-filter analyses with a SNR of only ~ 6 , much lower than that recovered by cWB. If this were a real GW, this difference might be indicative that the signal contained physics that our search templates omit (such as precession and higher modes), which would lead to a reduction of its SNR and significance.

To explore this possibility, we ran standard parameter estimation on this event using the same approximants used in Ref. [8], namely SEOBNRv4 [84] and IMRPhenomPv2 [98]. Note that the latter approximant includes the effects of precession that our search templates omit. For the precessing IMRPhenomP run, we assumed a spin magnitude prior uniform between 0 and 0.99, and spin orientations were isotropically distributed on the sphere; for the spin-aligned SEOBNR waveforms, we used a spin prior such that the components of the spin aligned with the orbital angular momentum matched the prior used for the IMRPhenomP analysis. Remarkably, the two analyses not only report broadly consistent parameter posterior distributions but they also report consistent SNRs of ~ 6 , in agreement with

that reported by our matched-filter searches. The latter indicates that the low SNR obtained by our matched-filter searches is not likely due to lack of precession in our templates. Assuming this event is a compact binary, we recover a source-frame chirp mass of $70_{-20}^{+24} M_\odot$, a source-frame total mass of $171_{-48}^{+68} M_\odot$, an effective inspiral spin of $0.19_{-0.46}^{+0.44}$, and a luminosity distance of $7.0_{-4.2}^{+8.0}$ Gpc. We also note that, given the lack of information about the spins, spin results are sensitive to the choice of prior. Further parameter estimation was performed using the new SEOBNRv4HM [99] approximant, which includes the impact of higher order modes. This analysis reported parameter posterior distributions and SNR consistent with the previous ones, suggesting that the low SNR obtained by our matched-filter searches is not due to the lack of higher modes in the search templates.

We further conducted parameter estimation of this trigger by directly using numerical relativity waveforms of generic spin configurations and higher modes with the RIFT algorithm [100,101], which reported results consistent with those obtained by our waveform approximants. In addition, the event was also reconstructed using the model agnostic algorithm BayesWave [102,103], which reported a SNR consistent with those obtained by our templates.

In summary, detailed follow-up of this event suggests that, in the most optimistic scenario, this trigger would be the combination of a weak IMBHB signal plus a noise

transient with power detected by cWB (see Sec. II D), raising the significance of the underlying IMBHB signal. Since the resulting event has a marginal significance, the

underlying IMBHB trigger would be even less significant. Hence, we conclude that this event is best explained by detector noise.

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