



UvA-DARE (Digital Academic Repository)

Strongly Coupled Anisotropic Gauge Theories and Holography

Giatajanas, D.; Gürsoy, U.; Pedraza, J.F.

DOI

[10.1103/PhysRevLett.121.121601](https://doi.org/10.1103/PhysRevLett.121.121601)

Publication date

2018

Document Version

Final published version

Published in

Physical Review Letters

License

CC BY

[Link to publication](#)

Citation for published version (APA):

Giatajanas, D., Gürsoy, U., & Pedraza, J. F. (2018). Strongly Coupled Anisotropic Gauge Theories and Holography. *Physical Review Letters*, *121*(12), [121601]. <https://doi.org/10.1103/PhysRevLett.121.121601>

General rights

It is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), other than for strictly personal, individual use, unless the work is under an open content license (like Creative Commons).

Disclaimer/Complaints regulations

If you believe that digital publication of certain material infringes any of your rights or (privacy) interests, please let the Library know, stating your reasons. In case of a legitimate complaint, the Library will make the material inaccessible and/or remove it from the website. Please Ask the Library: <https://uba.uva.nl/en/contact>, or a letter to: Library of the University of Amsterdam, Secretariat, Singel 425, 1012 WP Amsterdam, The Netherlands. You will be contacted as soon as possible.

Strongly Coupled Anisotropic Gauge Theories and HolographyDimitrios Giataganas,¹ Umut Gürsoy,² and Juan F. Pedraza³¹*Physics Division, National Center for Theoretical Sciences, National Tsing-Hua University, Hsinchu 30013, Taiwan*²*Institute for Theoretical Physics and Center for Extreme Matter and Emergent Phenomena, Utrecht University, Leuvenlaan 4, 3584 CE Utrecht, Netherlands*³*Institute for Theoretical Physics, University of Amsterdam, Science Park 904, Postbus 94485, 1090 GL Amsterdam, Netherlands*

(Received 9 March 2018; revised manuscript received 30 July 2018; published 20 September 2018)

We initiate a nonperturbative study of anisotropic, nonconformal, and confining gauge theories that are holographically realized in gravity by generic Einstein-axion-dilaton systems. In the vacuum, our solutions describe renormalization group flows from a conformal field theory in the UV to generic scaling solutions in the IR with generic hyperscaling violation and dynamical exponents θ and z . We formulate a generalization of the holographic c theorem to the anisotropic case. At finite temperature, we discover that the anisotropic deformation reduces the confinement-deconfinement phase transition temperature suggesting a possible alternative explanation of inverse magnetic catalysis solely based on anisotropy. We also study transport and diffusion properties in anisotropic theories and observe, in particular, that the butterfly velocity that characterizes both diffusion and growth of chaos transverse to the anisotropic direction saturates a constant value in the IR which can exceed the bound given by the conformal value.

DOI: [10.1103/PhysRevLett.121.121601](https://doi.org/10.1103/PhysRevLett.121.121601)

Introduction.—Quantum many body systems in three spatial dimensions with reduced rotational symmetry have important realizations in nature such as the quark-gluon plasma produced in noncentral heavy ion collisions, or condensed matter systems described by anisotropic spin models, e.g., the anisotropic 3D Ising model. The rotational symmetry in such systems can be broken by application of an external source such as an electric or magnetic field in one direction as in the various condensed matter experiments, by the geometry of the setting as in noncentral heavy ion collisions, or by intrinsic properties of the interaction as in the case of the anisotropic spin models or the Weyl semimetals [1].

Gauge-gravity duality [2] provides a natural avenue to study anisotropic quantum field theories (QFTs) in the presence of strong interactions. Most of the early gauge-gravity literature on anisotropic systems focuses either on scale-invariant systems or nonconformal but charged plasmas. Only the following three special cases have been studied. (i) Initially conformal invariant systems where the isotropy and conformal symmetry is broken by the same mechanism, for example, by a source that depends on a spatial direction as in [3–11]. (ii) Lifshitz invariant

systems with anisotropy as in [12]. (iii) Nonconformal charged plasmas where the anisotropy is introduced by an external magnetic field in one spatial direction as in [13–15].

In this Letter, we initiate a study of uncharged, nonconformal and anisotropic systems with strong interactions by means of the gauge-gravity duality. In particular, we consider a nonconformal, gapped and confining 4D $SU(N)$ gauge theory in the large- N limit, obtained by deforming a strongly interacting fixed point in the UV by means of a scalar operator \mathcal{O} with scaling dimension Δ . We introduce the anisotropy by means of another operator $\tilde{\mathcal{O}}$ that we choose to be marginal, with a coupling that depends on one of the spatial coordinates. Then, we study the influence of anisotropy on the renormalization group (RG) flow at zero temperature and on the thermodynamic observables and transport coefficients at finite temperature. The gauge theory is realized in holography by the Einstein-axion-dilaton theory in five dimensions with a nontrivial potential for the dilaton. This potential can be chosen such that the vacuum state confines color, and there exists a phase transition at finite T_c above which a deconfined plasma state arises. We study this class of nonconformal, confining, anisotropic, and strongly interacting theories holographically for a specific choice of the potentials; however, our qualitative results—which we discuss below—are independent of these choices and hold for the entire class.

The vacuum state of the theory is studied in the section titled “Scaling solutions in the IR” and exhibits interesting qualitative features. In particular, we find that, for marginal \mathcal{O} , that is $\Delta = 4$, we find a nontrivial RG flow from the

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP³.

conformal fixed point in the UV to a Lifshitz-like hyperscaling violating theory in the IR with a range of possible dynamical and hyperscaling violating exponents z and θ whose values are determined by the choice of potentials in the dual gravitational theory [16]. These models, therefore, open new ground for phenomenological applications in strongly interacting plasma physics.

An especially interesting question concerns how the confinement-deconfinement phase transition is affected by anisotropy. We study the phase diagram in the ‘‘Thermodynamics’’ section and discover that the anisotropic deformation decreases the confinement-deconfinement transition temperature. This is in accord with the recent lattice QCD studies [17–20] that show both chiral symmetry restoration and deconfinement occur at lower temperatures in the presence of an external magnetic field, a phenomenon coined ‘‘inverse magnetic catalysis’’ (IMC). Note that magnetic field also breaks isotropy in a similar way as we do in our uncharged plasma. Yet, our finding brings a new twist in this story indicating that IMC may occur even in uncharged plasmas.

Transport properties also exhibit surprising qualitative features. In particular, as we show in the ‘‘Transport and diffusion’’ section, the butterfly velocity violates the ‘‘universal bound’’ conjectured in [21,22].

Holographic setup.—The gravitational theory dual to our anisotropic field theory is defined by the Einstein-axion-dilaton action with generic functions V and Z that determine the potential energy for the dilaton field ϕ and its coupling to the axion field χ

$$S = \frac{1}{2\kappa^2} \int d^5x \sqrt{-g} [R + \mathcal{L}_M], \quad (1)$$

$$\mathcal{L}_M = -\frac{1}{2}(\partial\phi)^2 + V(\phi) - \frac{1}{2}Z(\phi)(\partial\chi)^2, \quad (2)$$

where $\kappa^2 \sim 1/N^2$. Crucially, a linear axion ansatz automatically satisfies the equations of motion and breaks isotropy while preserving translation invariance

$$ds^2 = e^{2A(r)} \left[-f(r)dt^2 + d\vec{x}_\perp^2 + e^{2h(r)}dx_3^2 + \frac{dr^2}{f(r)} \right], \quad (3)$$

$$\phi = \phi(r), \quad \chi = ax_3. \quad (4)$$

The solution is asymptotically anti-de Sitter (AdS) near the boundary $r \rightarrow 0$ where $A \rightarrow -\log r$, $f \rightarrow 1$, $h \rightarrow 0$, and $\phi \rightarrow jr^{4-\Delta}$ [23]. This solution generally corresponds to a nonconformal gauge theory whose IR dynamics is dominated by the stress tensor $T_{\mu\nu}$ dual to the metric and a scalar operator $\mathcal{O} \sim \text{Tr}F^2$, similar to the scalar glueball operator in QCD (when it is marginal), here, dual to the field ϕ . We call the source of this operator j . The theory is, in turn, deformed by a space-dependent theta term

$\tilde{\mathcal{O}} \sim \theta(x_3)\text{Tr}F \wedge F$ dual to the field χ . The 5D Einstein-axion-dilaton theory can be realized in terms of D3/D7-branes in IIB string theory when $V = 12$ and $Z = e^{2\phi}$ [3–5]. In this case, the underlying field theory is conformal. However, we are interested in nonconformal and, in particular, confining gauge theories that follow from a more generic choice of the potentials V and Z [24,25]. A choice of the form [26,27]

$$V(\phi) = 12 \cosh(\sigma\phi) + b\phi^2, \quad Z(\phi) = e^{2r\phi}, \quad (5)$$

with $b \equiv \{[\Delta(4-\Delta)]/2\} - 6\sigma^2$, corresponds to a gauge theory with a scalar operator of scaling dimension Δ that confines color in the vacuum state for $\sigma \geq \sqrt{2/3}$ [25].

We observe that the holographic version of the c theorem [28] in QFT (or, rather, the ‘‘ a theorem’’ in 4D [29]) has a natural generalization in the anisotropic holographic theories. Introducing the domain-wall coordinate $du = \exp[A(r)]dr$ we find that

$$\frac{d}{du} \left\{ \left(\frac{dA}{du} + \frac{1}{3} \frac{dh}{du} \right) e^{h/3} \right\} \leq 0, \quad (6)$$

which follows from Einstein’s equations. Imposing the bulk null energy condition recovers (6) but, also, leads to an additional monotonicity constraint

$$\frac{d}{du} \left\{ \frac{dh}{du} e^{h+4A} \right\} \leq 0, \quad (7)$$

which can be used to define a second independent central charge for anisotropic theories (see, also, [30–32]). Both expressions inside the brackets of (6) and (7) are monotonically decreasing and, while the first one reduces directly to dA/du in the isotropic limit $h \rightarrow 0$, any linear combination between them may give the holographic analog of the a function [28].

Scaling solutions in the IR.—The RG energy scale of the dual QFT in the ground state is determined by the scale factor A of the metric (3) [33], which exhibits a nontrivial dependence on the holographic coordinate r when the potentials V and Z are not constant. The IR region $r \rightarrow \infty$ corresponds to small values of $\exp(A)$ where the dilaton grows [34] monotonically [24]. In this limit, $V \sim 6e^{\sigma\phi}$ for $\sigma \geq 0$. We can derive the following scaling solutions in the IR limit:

$$ds^2 = \tilde{L}^2(ar)^{2\theta/3z} \left[\frac{-dt^2 + d\vec{x}_\perp^2 + dr^2}{a^2r^2} + \frac{c_1 dx_3^2}{(ar)^{2/z}} \right], \quad (8)$$

$$\phi = c_2 \log(ar) + \phi_0. \quad (9)$$

Here, \tilde{L} , c_1 , and c_2 are constants depending on z and θ , which are given in terms of γ and σ as

$$z = \frac{4\gamma^2 - 3\sigma^2 + 2}{2\gamma(2\gamma - 3\sigma)}, \quad \theta = \frac{3\sigma}{2\gamma}. \quad (10)$$

These constants also depend on the free parameter ϕ_0 which is set by the value of the source j . For $\theta = 0$, the solution exhibits a Lifshitz-like scaling

$$t \rightarrow \lambda t, \quad \vec{x}_\perp \rightarrow \lambda \vec{x}_\perp, \quad r \rightarrow \lambda r, \quad x_3 \rightarrow \lambda^{1/z} x_3. \quad (11)$$

For $\theta \neq 0$, the metric (8) has the hyperscaling violation property and transforms covariantly under (11) as

$$ds \rightarrow \lambda^{\theta/3z} ds. \quad (12)$$

When the IR theory is connected to a heat bath, one obtains the finite temperature version of the scaling metric, which is now a black brane with blackening factor

$$f(r) = 1 - \left(\frac{r}{r_H}\right)^{3+(1-\theta)/z}, \quad (13)$$

where r_H is the location of the horizon. The black brane metric is obtained by multiplying the dt^2 term by f and the dr^2 term by $1/f$ in (8). The entropy density of the plasma in the IR is obtained from the area of the horizon

$$s = c_{\text{IR}} a^{-2-[(1-\theta)/z]} T^{2+[(1-\theta)/z]} / \kappa^2, \quad (14)$$

where c_{IR} is a constant, and T is the Hawking temperature

$$T = \frac{|3 + (1-\theta)/z|}{4\pi r_H}. \quad (15)$$

Notice that the values z and θ are constrained by the bulk null energy condition and the positivity of the specific heat $C_V = d \log s / d \log T$ as follows:

$$(z-1)(1+3z-\theta) \geq 0, \quad (16)$$

$$\theta^2 + 3z(1-\theta) - 3 \geq 0, \quad (17)$$

$$2z + 1 - \theta \geq 0. \quad (18)$$

Combining these inequalities, we observe that, for $z \geq 1$, the value of θ is bounded from above $\theta \leq \theta_{\text{bound}}^{(-)}$, while for $z \leq 0$, it is bounded from below $\theta \geq \theta_{\text{bound}}^{(+)}$, with

$$\theta_{\text{bound}}^{(\pm)} = \frac{1}{2} \left(3z \pm \sqrt{3} \sqrt{4 - 4z + 3z^2} \right). \quad (19)$$

The range $0 < z < 1$ is forbidden altogether. Thus, one derives interesting universal bounds on the IR scaling behavior of strongly interacting anisotropic plasmas from holography.

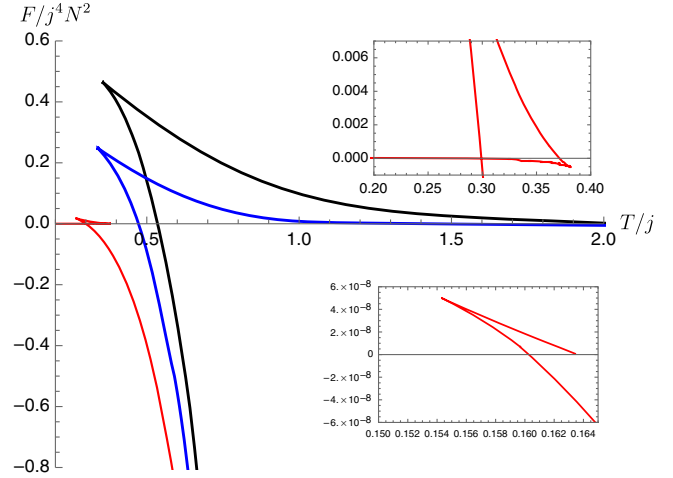


FIG. 1. Free energy as a function of T for different values of the anisotropy parameter $a/j = 0, 1, 3$ (black, blue, and red curves, respectively). The parameters $\sigma = \sqrt{2/3} + 1/10$, $\gamma = 1/5$, $\Delta = 3$ were chosen such that the undeformed theory is confining. The horizontal axis corresponds to the confined state while all other branches correspond to deconfined phases. The insets show details of an additional phase transition for large a , as discussed in the text.

Thermodynamics.—Questions pertaining to thermal equilibrium are answered by working out the free energy in the canonical ensemble, which, in the holographic description equals the Euclidean gravitational action (1) appended by the Gibbons-Hawking and counterterm actions, evaluated on shell. The counterterms in a generic Einstein-axion-dilaton theory were worked out in detail in [36] whose results we use but do not show here. Alternatively, one can calculate the background subtracted free energy directly by integrating the first law of thermodynamics $dF = -s dT$ for j and a held fixed [37].

In Fig. 1, we plot numerical results for the free energy as a function of T for a particular confining theory. We will divide the analysis in two cases, small a/j and large a/j . For small a up to $a/j \approx 2.08$, there are three competing phases. First, there is the confining ground state heated up to temperature T . The corresponding gravitational background is obtained from the black brane solution (3) by sending the mass to zero. This is the so-called thermal gas solution and is our reference background for the free energy computation. More specifically, the free energy of this phase is $\mathcal{O}(N^0)$, therefore, it corresponds to the horizontal axis $F = 0$. Second, we observe two phases of free energy $\mathcal{O}(N^2)$. These are the deconfined, plasma phases corresponding to black brane solutions (3) with a nontrivial blackening factor. One of these solutions, the “small black brane” (upper branches in Fig. 1 for $a/j = 0, 1$) is always subdominant in the ensemble and can be ignored. Moreover, this phase is thermodynamically unstable since $C_V \propto -d^2 F / dT^2 < 0$, as can be read from the figure. The “big black brane” solution (lower branches in Fig. 1 for

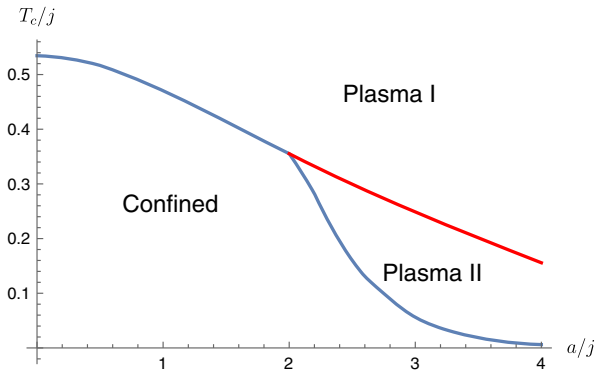


FIG. 2. Phase diagram of the system in the a - T plane. We observe two phases, confined and “plasma I,” for $a/j < 2.08$. For larger a/j , there exist three phases, confined, “plasma I,” and “plasma II.” The blue and red curves indicate lines of first order transitions.

$a/j = 0, 1$) dominates the ensemble for $T > T_c$. Here, T_c is given by the point where the curves cross $F = 0$. Therefore, the system is in the deconfined phase above the critical temperature T_c . This plasma phase is denoted as “plasma I” in Fig. 2. Below T_c the system is in the confined phase. This phase transition is of confinement-deconfinement type, and it is of first order. All of this is in accordance with improved holographic QCD [38,39].

For $a/j > 2.08$ the phase structure becomes more complicated. As shown in Fig. 1 for the choice $a/j = 3$, now, there exist four different black brane branches with free energy $\mathcal{O}(N^2)$, instead of the aforementioned two solutions, the small and the big black branes for $a/j < 2.08$. It is apparent from Fig. 1 that two of them have positive specific heat, analog of the big black brane solution in the small a case. These two solutions are denoted as plasma I and plasma II in Fig. 2. There are two more black brane solutions analog of the small black brane solution in the small a case. However, these are always subdominant and thermodynamically unstable; hence, we can ignore them. As shown in Fig. 2, there are now two phase transitions. There is the confinement-deconfinement type first order transition, analogous to the small a case, and there is a new first order transition between the two plasma phases at a higher critical temperature. Moreover, all of these dominant phases meet at a triple point at $a \approx 2.08$, $T/j \approx 0.36$.

We observe that the confinement-deconfinement transition temperature T_c decreases with increasing anisotropy a as shown in Fig. 2. This is interesting in the context of inverse magnetic catalysis [17–20]. It has been observed that the chiral symmetry breaking temperature decreases with an increasing degree of anisotropy, induced by an external magnetic field B . Our finding suggests an alternative mechanism based only on anisotropy, as explained in the Discussion.

Transport and Diffusion.—Holography is instrumental in the study of dissipative properties of the quark-gluon

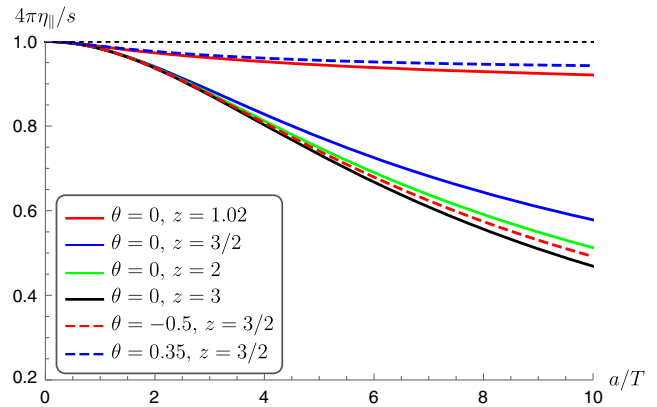


FIG. 3. The viscosity over entropy density ratio for several values of θ and z . Increase of the scaling parameter z leads to lower values of the ratio (solid lines), as well as a decrease of the value of θ (dashed lines).

plasma as exemplified by the agreement between the holographic value of the shear viscosity $\eta/s = 1/4\pi$ [40,41] and experiment [42]. This universal value is violated in anisotropic systems [43–47] for the shear component parallel to the anisotropic direction, $\eta_{||}$, while the component transverse to the anisotropic direction η_{\perp} remains universal. A calculation shows that $\eta_{||}$ can be obtained from the near-horizon form of the metric (3)

$$\frac{\eta_{||}}{s} = \frac{1}{4\pi} \frac{g_{\perp\perp}}{g_{33}} \Big|_{r=r_h}. \quad (20)$$

In Fig. 3, we show the behavior of this quantity for the case $\Delta = 4$ and $j = 0$. The curves are parametrized according to the properties of the IR geometry, i.e., the scaling exponents z and θ . We observe that the shear viscosity in the anisotropic direction is generally below the universal value $\eta/s = 1/4\pi$, which is attained only in the UV. In the IR limit, one obtains

$$\frac{\eta_{||}}{s} = \chi_{\text{IR}} \left(\frac{a}{T} \right)^{\frac{z}{2}-2}. \quad (21)$$

The constant χ_{IR} depends generically on z , θ , and ϕ_0 (or equivalently j). The power of a/T is independent of the hyperscaling violation exponent θ . However, θ determines the allowed range of z through Eqs. (16)–(18); e.g., for $\theta = 0$ the exponent is in the range $(-2, 0]$. More generally, the bounds imply that the power is always negative (for $z \neq 1$) so $\eta_{||}$ typically vanishes in the deep IR.

Another interesting phenomenon is momentum diffusion, which is related to dissipation through shear via an Einstein relation. In holographic theories, diffusion is characterized by the time scale $\tau_L \sim 1/T$ and the butterfly velocity v_B [48], both entering in the diffusion constant as $D \sim \hbar v_B^2/k_B T$. These quantities can be computed

holographically through the near horizon dynamics. They also control the chaotic growth of the commutator $\langle [W(t, x), V(0, 0)]^2 \rangle \sim \exp[(t - x/v_B)/\tau_L]$ for arbitrary hermitian operators W and V , whose properties have been studied extensively recently in [48–53]. Interestingly, the butterfly velocity provides a natural notion of a “light cone” even for nonrelativistic systems; e.g., in [52], it was argued that v_B acts as a low-energy Lieb-Robinson velocity.

In anisotropic theories, there are two notions of butterfly velocities, $v_{B\parallel}$ and $v_{B\perp}$ [48], corresponding to the parallel and transverse directions, respectively [54]. These can be obtained by studying the backreaction of an excitation at $\vec{x} = 0$ sent from the asymptotic boundary into the bulk. The excitation solves the Poisson equation on the curved geometry with a delta-function source $\delta(\vec{x})$ and with an effective mass that corresponds to the screening length μ_{\parallel} or μ_{\perp} in the corresponding plasma. On the background (3), one finds

$$\mu_{\perp}^2 = \frac{f'(3A' + h')}{2} \Big|_{r=r_h}, \quad \mu_{\parallel}^2 = \mu_{\perp}^2 e^{2h(r_h)}. \quad (22)$$

The corresponding butterfly velocities $v_{B_i}^2 = (2\pi T)^2/\mu_i^2$ approach the conformal value $v_B^2 = 2/3$ in the UV, while in the IR one obtains

$$v_{B\perp}^2 = \frac{1 - \theta + 3z}{2(1 - \theta + 2z)}, \quad v_{B\parallel}^2 = \zeta_{\text{IR}} \left(\frac{a}{T}\right)^{\frac{z}{2} - 2}, \quad (23)$$

where $\zeta_{\text{IR}} = 4\pi v_{B\perp}^2 \chi_{\text{IR}}$. Remarkably, $v_{B\perp}^2$ saturates to a universal value independent of j . These expressions are to be contrasted with the butterfly velocities for isotropic theories with hyperscaling violation [48,52]. In these works, it was found that they scale generically as $v_B^2 \sim (T_0/T)^{(2/z)-2}$, where T_0 is a UV scale, so $v_B^2 \rightarrow 0$ in the deep IR. In contrast, we find that $v_{B\perp}^2$ saturates to a constant for $a \gg T$. In the allowed range of θ and z , both $v_{B\perp}^2$ and $v_{B\parallel}^2$ are positive and smaller than one, but, surprisingly, the value of $v_{B\perp}^2$ in the IR can exceed the conformal value $v_B^2 = 2/3$. For example, for $\theta = 0$ and $z > 1$, it always exceeds $2/3$ and saturates another bound $v_{B\perp}^2 \rightarrow 3/4$ as $z \rightarrow \infty$. In Fig. 4, we plot $v_{B\perp}^2$ and $v_{B\parallel}^2$ as a function of a/T for some generic examples.

Discussion.—In this Letter, we found several qualitative features of strongly coupled anisotropic systems both in the ground state and at finite temperature. Studying confining plasmas, we found that the confinement-deconfinement phase transition temperature decreases with anisotropy. The decrease in $T_c(a)$ with a resembles the phenomenon of inverse magnetic catalysis where both the confinement-deconfinement and the chiral phase transition temperatures decrease with the magnetic field B . The main difference is that there are no charged fermionic degrees of freedom in our case; our plasma is neutral. This suggests an

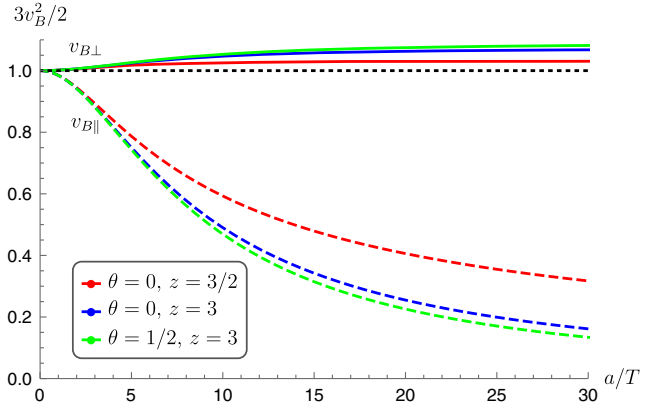


FIG. 4. Butterfly velocities $v_{B\perp}$ (solid lines) and $v_{B\parallel}$ (dashed lines). In the longitudinal direction, the information diffuses slower with increasing anisotropy, with vanishing velocity in the IR. Perturbations in the transverse plane can propagate at a faster rate, with a new upper bound attained in the IR.

explanation for IMC, alternative to, e.g., [57,58]: that, anisotropy—which is caused by B , instead of a in those examples—could be responsible for the phenomenon, instead of charge dynamics. It is tempting to conjecture this as a generic property in a large class of confining anisotropic theories at strong coupling. In fact, studies with different holographic constructions [59] showing a destructive effect of anisotropy on the chiral condensate strongly support our claim. Whether there is a direct field theory argument in support of this conjecture remains to be seen. Nonetheless, it is interesting to note that the fact that anisotropy itself may be responsible for inverse magnetic catalysis could, in principle, be checked by (anisotropic) lattice calculations.

The ground states in our theories are generically characterized in the IR, by the dynamical and hyperscaling violating exponents z and θ . Theories are thermodynamically stable for a wide range of these exponents. We also obtained a generalization of the holographic c theorem valid for anisotropic theories in Eq. (6). It would be interesting to work out the implications of this for RG flows, and to provide a proof directly in quantum field theory.

Finally, as expected from previous works, we found η_{\parallel}/s to be generically smaller than the so-called universal result $1/4\pi$. We also found that $v_{B\perp}^2$ can exceed the bound conjectured in [21,22]. There is no contradiction, since these papers assumed isotropy. However, this result is surprising: it implies a new upper bound for the transfer of quantum information, enhanced, here, by the effects of anisotropy. It will be interesting to figure out the field theoretic reason behind these observations. It will also be interesting to find realization of our findings in physical systems. In connection to this, we refer to [60,61] as a way to measure the anisotropic shear viscosity of a strongly interacting, ultracold, unitary Fermi gas confined in a harmonic trap.

The authors acknowledge useful conversations with Mariano Chernicoff, Chong-Sun Chu, Viktor Jahnke, David Mateos, and Phil Szepletowski. This work is partially supported by the Ministry of Science and Technology of Taiwan under Grants No. 101-2112-M-007-021-MY3 and No. 104-2112-M-007-001-MY3, the Netherlands Organisation for Scientific Research (NWO) under the VIDI Grant No. 680-47-518 and the VENI Grant No. 680-47-456/1486, and the Delta-Institute for Theoretical Physics (Δ -ITP), which is funded by the Dutch Ministry of Education, Culture and Science (OCW).

-
- [1] In this latter case, isotropy is broken by separating the left-handed and right-handed Dirac cones along an axis in the momentum space.
- [2] J. M. Maldacena, *Adv. Theor. Math. Phys.* **2**, 231 (1998).
- [3] T. Azeyanagi, W. Li, and T. Takayanagi, *J. High Energy Phys.* **06** (2009) 084.
- [4] D. Mateos and D. Trancanelli, *J. High Energy Phys.* **07** (2011) 054.
- [5] D. Mateos and D. Trancanelli, *Phys. Rev. Lett.* **107**, 101601 (2011).
- [6] D. Giataganas, *J. High Energy Phys.* **07** (2012) 031.
- [7] M. Chemicoff, D. Fernandez, D. Mateos, and D. Trancanelli, *J. High Energy Phys.* **08** (2012) 100.
- [8] D. Giataganas and H. Soltanpanahi, *Phys. Rev. D* **89**, 026011 (2014).
- [9] R. Rougemont, R. Critelli, and J. Noronha, *Phys. Rev. D* **91**, 066001 (2015).
- [10] J. F. Fuini and L. G. Yaffe, *J. High Energy Phys.* **07** (2015) 116.
- [11] I. Ya. Aref'eva, A. A. Golubtsova, and E. Gourgoulhon, *J. High Energy Phys.* **09** (2016) 142.
- [12] U. Gursoy, A. Jansen, W. Sybesma, and S. Vandoren, *Phys. Rev. Lett.* **117**, 051601 (2016).
- [13] R. Rougemont, R. Critelli, and J. Noronha, *Phys. Rev. D* **93**, 045013 (2016).
- [14] T. Drwenski, U. Gursoy, and I. Iatrakis, *J. High Energy Phys.* **12** (2016) 049.
- [15] U. Gursoy, I. Iatrakis, M. Jrvinen, and G. Nijs, *J. High Energy Phys.* **03** (2017) 053.
- [16] Generalizing examples in IIB supergravity [3,4] which only allows a fixed dynamical exponent $z = 3/2$.
- [17] G. S. Bali, F. Bruckmann, G. Endrodi, Z. Fodor, S. D. Katz, S. Krieg, A. Schafer, and K. K. Szabo, *J. High Energy Phys.* **02** (2012) 044.
- [18] G. S. Bali, F. Bruckmann, G. Endrodi, Z. Fodor, S. D. Katz, S. Krieg, A. Schafer, and K. K. Szabo, *Proc. Sci., LATTICE2011* (2011) 192.
- [19] G. S. Bali, F. Bruckmann, G. Endrodi, Z. Fodor, S. D. Katz, and A. Schafer, *Phys. Rev. D* **86**, 071502 (2012).
- [20] M. D'Elia, *Lect. Notes Phys.* **871**, 181 (2013).
- [21] M. Mezei and D. Stanford, *J. High Energy Phys.* **05** (2017) 065.
- [22] M. Mezei, *J. High Energy Phys.* **05** (2017) 064.
- [23] The asymptotic expansions for $\Delta = 4$ are more subtle. For $\Delta = 4$, we impose $\phi \rightarrow 0$ in order to have an asymptotically AdS background.
- [24] U. Gursoy and E. Kiritsis, *J. High Energy Phys.* **02** (2008) 032.
- [25] U. Gursoy, E. Kiritsis, and F. Nitti, *J. High Energy Phys.* **02** (2008) 019.
- [26] S. S. Gubser and A. Nellore, *Phys. Rev. D* **78**, 086007 (2008).
- [27] S. S. Gubser, A. Nellore, S. S. Pufu, and F. D. Rocha, *Phys. Rev. Lett.* **101**, 131601 (2008).
- [28] D. Z. Freedman, S. S. Gubser, K. Pilch, and N. P. Warner, *Adv. Theor. Math. Phys.* **3**, 363 (1999).
- [29] Z. Komargodski and A. Schwimmer, *J. High Energy Phys.* **12** (2011) 099.
- [30] C. Hoyos and P. Koroteev, *Phys. Rev. D* **82**, 084002 (2010); **82**, 109905(E) (2010).
- [31] J. T. Liu and Z. Zhao, [arXiv:1206.1047](https://arxiv.org/abs/1206.1047).
- [32] S. Cremonini and X. Dong, *Phys. Rev. D* **89**, 065041 (2014).
- [33] A. W. Peet and J. Polchinski, *Phys. Rev. D* **59**, 065011 (1999).
- [34] The monotonicity is subject to a certain upper bound on σ [35] which we assume throughout the Letter.
- [35] U. Gursoy, A. Jansen, and W. van der Schee, *Phys. Rev. D* **94**, 061901 (2016).
- [36] I. Papadimitriou, *J. High Energy Phys.* **08** (2011) 119.
- [37] The physical coupling on the boundary ax_3 is kept fixed.
- [38] U. Gursoy, E. Kiritsis, L. Mazzanti, and F. Nitti, *Phys. Rev. Lett.* **101**, 181601 (2008).
- [39] U. Gursoy, E. Kiritsis, L. Mazzanti, and F. Nitti, *J. High Energy Phys.* **05** (2009) 033.
- [40] G. Policastro, D. T. Son, and A. O. Starinets, *Phys. Rev. Lett.* **87**, 081601 (2001).
- [41] P. Kovtun, D. T. Son, and A. O. Starinets, *J. High Energy Phys.* **10** (2003) 064.
- [42] J. Casalderrey-Solana, H. Liu, D. Mateos, K. Rajagopal, and U. A. Wiedemann, [arXiv:1101.0618](https://arxiv.org/abs/1101.0618), DOI: 10.1017/CBO9781139136747.
- [43] A. Rebhan and D. Steineder, *Phys. Rev. Lett.* **108**, 021601 (2012).
- [44] K. A. Mamo, *J. High Energy Phys.* **10** (2012) 070.
- [45] S. Jain, R. Samanta, and S. P. Trivedi, *J. High Energy Phys.* **10** (2015) 028.
- [46] S. Jain, N. Kundu, K. Sen, A. Sinha, and S. P. Trivedi, *J. High Energy Phys.* **01** (2015) 005.
- [47] J. Erdmenger, P. Kerner, and H. Zeller, *Phys. Lett. B* **699**, 301 (2011).
- [48] M. Blake, *Phys. Rev. Lett.* **117**, 091601 (2016).
- [49] S. A. Hartnoll, *Nat. Phys.* **11**, 54 (2015).
- [50] D. A. Roberts, D. Stanford, and L. Susskind, *J. High Energy Phys.* **03** (2015) 051.
- [51] S. H. Shenker and D. Stanford, *J. High Energy Phys.* **05** (2015) 132.
- [52] D. A. Roberts and B. Swingle, *Phys. Rev. Lett.* **117**, 091602 (2016).
- [53] T. Hartman, S. A. Hartnoll, and R. Mahajan, *Phys. Rev. Lett.* **119**, 141601 (2017).
- [54] See [55,56] for related works.
- [55] S.-F. Wu, B. Wang, X.-H. Ge, and Y. Tian, *Phys. Rev. D* **97**, 066029 (2018).
- [56] V. Jahnke, *J. High Energy Phys.* **01** (2018) 102.
- [57] F. Bruckmann, G. Endrodi, and T. G. Kovacs, *J. High Energy Phys.* **04** (2013) 112.

- [58] V. A. Miransky and I. A. Shovkovy, *Phys. Rep.* **576**, 1 (2015).
- [59] U. Gursoy, M. Jarvinen, G. Nijs, and J. Pedraza (to be published).
- [60] R. Samanta, R. Sharma, and S. P. Trivedi, *Phys. Rev. A* **96**, 053601 (2017).
- [61] R. Samanta, R. Sharma, and S. P. Trivedi, [arXiv:1611.02720](https://arxiv.org/abs/1611.02720).